# Impact of the main linac couplers on the beam

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# **Objectives of this work**

- 1. Study the impact of the baseline main linac couplers on the beam dynamics, TD26\_CC
- 2. Compare the baseline design with an alternative design
  - baseline TD26\_CC : "double-feed" coupler
  - alternative TD26\_CCSF : "single-feed" coupler

Tools developed:

- Set of programs to extract the multipole coefficients from a 3-dimensional complex field-map
- Introduced rf-multipolar kicks in Placet

## **Overview of this talk**

- Introduction
- Multipole expansion of a field map
- RF-Multipoles
- Simulation setup and case studies
- Results
- Conclusions

## TD26\_CC: double-feed compact coupler

(pictures courtesy of W. Wuensch and G. Riddone, CLIC ACE Meeting, Feb 2011)



# Introduction

- Baseline main linac cavities, TD26, foresee double-feed compact couplers (TD26\_CC)
- An alternative design exists, implementing single-feed couplers (TD26\_CCSF)
- Each carries pros and cons:
  - complexity, cost, impact on the beam-dynamics, ...

- Couplers, as they break the cylindrical symmetry of the beam pipe, give (undesired) transverse RF-kicks to the beam
- > By design:
  - TD26\_CC introduces quadrupolar and octupolar fields
  - TD26\_CCSF introduces, also, a dipole and a sextupole component

## **Extracting the Multipolar Components**

Given a 3d field map,  $E_{xyz}(x,y,z)$ :

- the field is sliced along the z axis :  $E_{xyz,i}(x,y)=E_{xyz}(x,y,z_i)$
- the multipolar components are calculated over each slice :  $E_{xyz,i}(x,y)$

The multipole expansion can be carried out either in the xy plane, or along the z axis:

(1) Using E <sub>x</sub> and E <sub>y</sub>	(2) Using E <sub>z</sub>
$E_{y} + iE_{x} = \sum_{n=1}^{N} C_{n} (x + iy)^{n-1}$	$E_z = \sum_{n=0}^{N} D_n \left( x + iy \right)^n$

The coefficients can be computed through a disk integral within the aperture, or along a circle  $1 - f(r \mid R) = \frac{1}{2}$ 

$$C_n = \frac{1}{A_{\Omega}} \iint_{\Omega} \left[ \frac{B_r(r,\varphi)}{r^n e^{in\varphi}} r \right] \, \mathrm{d}\Omega$$

Whether (1) or (2) are considered, the transverse kick on the particles can be computed:

- (1) applying the Lorentz force
- (2) using the Panofsky-Wenzel theorem

# Qadrupole and Octupole Components in TD26 CC

The multipole coefficients have been converted in the equivalent magnetic gradients



Quadrupole

The integrated strengths have been calculated (and applied) in:

- 2 locations: Input Coupler, Output Coupler for the *quadrupole* component
- 1 location: Average (middle of the cavity) for the octupole component

# **Rf-Multipolar Expansion**

- Given the symmetries of the problem, the RF-field can be expanded in multipoles
- As it's a phasor, i.e. a "rotating field" : its components depend on the longitudinal position of the particles within the accelerating structure
- A rotating multipolar field can be represented using a modified multipole: an **rfmultipole**, where the coefficients are the real part (cosine) of the *phasor* associated with the standard multipolar coefficient.
- Multipole expansion of a (magnetic) field

$$B_y + iB_x = \sum_{n=1}^{N} \left( B_n(r_0) + i A_n(r_0) \right) \cdot \frac{z^{n-1}}{r_0^{n-1}}$$

• Dependence of the coefficients on z and on the RF parameters

$$C_{n}(z) = B_{n}(z) + i A_{n}(z), \qquad k_{\rm RF} = \frac{\omega_{\rm RF}}{c} = \frac{2\pi}{\lambda_{\rm RF}} \quad \text{RF wave number},$$

$$B_{n}(z) = B_{n} \cos\left(k_{\rm RF}z + \vartheta_{n}\right) \qquad \qquad B_{n} \text{ absolute value of the phasor } \vec{B}_{n}, \text{ absolute value of the phasor } \vec{A}_{n},$$

$$A_{n}(z) = A_{n} \cos\left(k_{\rm RF}z + \varphi_{n}\right) \qquad \qquad \vartheta_{n} \text{ phase of the phasor } \vec{B}_{n}; \text{ phase of the phasor } \vec{A}_{n}.$$

### Strengths of the Multipolar-Kicks Summary Table

### TD26\_CC: on crest

	Symbol	Input C	Acc Structure	Output C	Units
Quadrupole	S <sub>2</sub>	0.002	-	-0.001	GeV/m
Octupole	S <sub>4</sub>	-	59.7	-	GeV/m <sup>3</sup>

### TD26\_CCSF: TD26\_CC +

Horizontal dipole kick

	$S_{1,\mathrm{input}}$ [GeV]	$S_{1, \text{output}} \left[ \text{GeV} \right]$
$\phi=8^\circ$	$-1.38\cdot10^{-5}$	$-4.02\cdot10^{-6}$
$\phi=30^\circ$	$-1.156\cdot 10^{-5}$	$-3.77\cdot10^{-6}$

• Sextupole kick

	$S_{3,\rm input}[{\rm GeV/m^2}]$	$S_{\rm 3,output}[{\rm GeV/m^2}]$
$\phi=8^\circ$	-0.25	0.068
$\phi=30^\circ$	-0.21	0.059

Comment: we expect TD26\_CCSF to perform worse than TD26\_CC

# Phase dependence of the strength

The EM field depends on the phase and so do the transverse kicks.

In the CLIC main linac, the beam is accelerated off-crest, at two phases:

• 8 and 30 degrees.

The bunch length, 44 microm, accounts for 0.63 degrees phase difference.



At phi=30 degrees the octupolar component is magnified by a factor ~70 w.r.t. the on-crest particle.

## Transverse kick strength in TD26\_CC

Compare the integrated strength of the main linac quads vs the couplers' kicks

Couplers strength / Main linac quads strengths



Preliminary conclusion: The coupler kicks are very small.

## 1<sup>st</sup> order compensation of the dipole kick in TD26\_CCSF

To compensate the dipole kick, an alternate pattern has been considered

- Left plot: uncompensated case
- Right plot: 1<sup>st</sup> order cancellation of the dipole kick



Uncompensated configuration

1st order compensation of the kick: TD26\_CCSF2

In the following, only the compensated case is considered (sometimes it's called TD26\_CCSF2)

### Case studies and simulation results

- Impact on a perfect main linac
- Statically misaligned cavities
- Tolerances:
  - Coupler misalignments
  - Cavity RF-gradient
  - Cavity RF-phase
  - Cavity roll
  - Cavity tilt (uncorrected, 1:1 corrected)
  - Cavity tilt bookshelf (uncorrected, 1:1 corrected)

# Impact of TD26\_CC couplers on a perfect main linac

Emittance growth in a perfect 3 TeV CLIC main linac

• Single-bunch wakefield effects are taken into account



The impact is negligible even if magnified by a factor 100

### Impact of TD26\_CC couplers on a main linac with misaligned cavities

Cavity misalignment

• The RMS transverse misalignment of the accelerating cavities is assumed to be ~10 microm



# Impact of TD26\_CCSF couplers on a perfect main linac

Emittance growth in a perfect 3 TeV CLIC main linac

• Single-bunch wakefield effects are taken into account



The impact on the horizontal axis is somehow significant The impact in the vertical axis is negligible even if magnified by a factor 2

## Impact of TD26\_CCSF couplers on a perfect main linac: 1:1 correction

Emittance growth in a perfect 3 TeV CLIC main linac

• Single-bunch wakefield effects are taken into account



The impact on the horizontal axis is now negligible

# Impact of TD26\_CCSF couplers on a main linac with misaligned cavities: 1:1 corrected

Impact of 10 um RMS cavity misalignment. Horizontal axis.



Corrected, the impact is negligible even if magnified by a factor 2

# Impact of TD26\_CCSF couplers on a main linac with misaligned cavities

Impact of 10 um RMS cavity misalignment. Vertical axis.



The impact is negligible

### **Tolerances:** misalignment

Random offset misalignment of the couplers



### **Tolerances: cavity gradient**

#### Random gradient changes, the coupler kicks scale with the gradient



### **Tolerances: cavity phase**

Random offsets in the RF-phase, the coupler kicks change accordingly



### **Tolerances: cavity roll**

#### 25 0.1 1 4 TD26\_CC TD26 CC TD26 CCSF2 TD26\_CCSF2 3.5 0.0995 0.995 no couplers no couplers -20 3 0.099 0.99 2.5 0.0985 0.985 15 $\Delta \epsilon_{\chi}$ [nm] Δε<sub>y</sub> [nm] $\Delta \epsilon_{\chi}$ [%] 2 0.98 0.098 10 1.5 0.0975 0.975 0.097 0.97 1 5 0.5 0.0965 0.965 0.096 0.96 0 0 500 1000 1500 2000 500 1000 1500 2000 0 0 $\sigma_{CC,roll}$ [µrad ] $\sigma_{CC.roll}$ [µrad ]

 $\Delta \epsilon_{y}$  [%]

### Random roll angles of each accelerating structure

The results are the average of 100 random seeds

### Tolerances: cavity tilt

#### Random offsets in h- and v- angles of the accelerating structures



### Tolerances: cavity tilt, 1:1



Random offsets in the h- and v- angles of the accelerating structures

The results are the average of 100 random seeds

### Tolerances: cavity tilt, bookshelf

#### Random offsets in the h- and v- angles of the accelerating structures



### Tolerances: cavity tilt, bookshelf, 1:1

Random offsets in h- and v- angles of the accelerating structures



### Tolerances: quadrupole tilt

Random offsets in h- and v- angles of the quadrupoles



### Tolerances: quadrupole tilt, 1:1

Random offsets in h- and v- angle of the quadrupoles, 1:1 corrected



### Conclusions

The impact of the couplers TD26\_CC and TD26\_CCSF has been studied.

New tools have been created, and PLACET has been modified to implement Rf-Multipoles

The impact of both designs on the beam dynamic seems modest and there seem not to be significant difference between the two designs