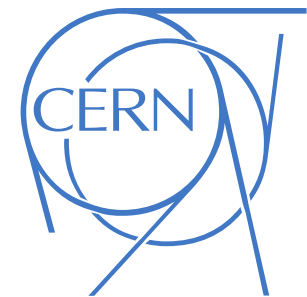


Electroweak symmetry breaking

Search for the missing piece of the Standard Model III

Pedro Ferreira da Silva – psilva@cern.ch

(CERN/LIP)

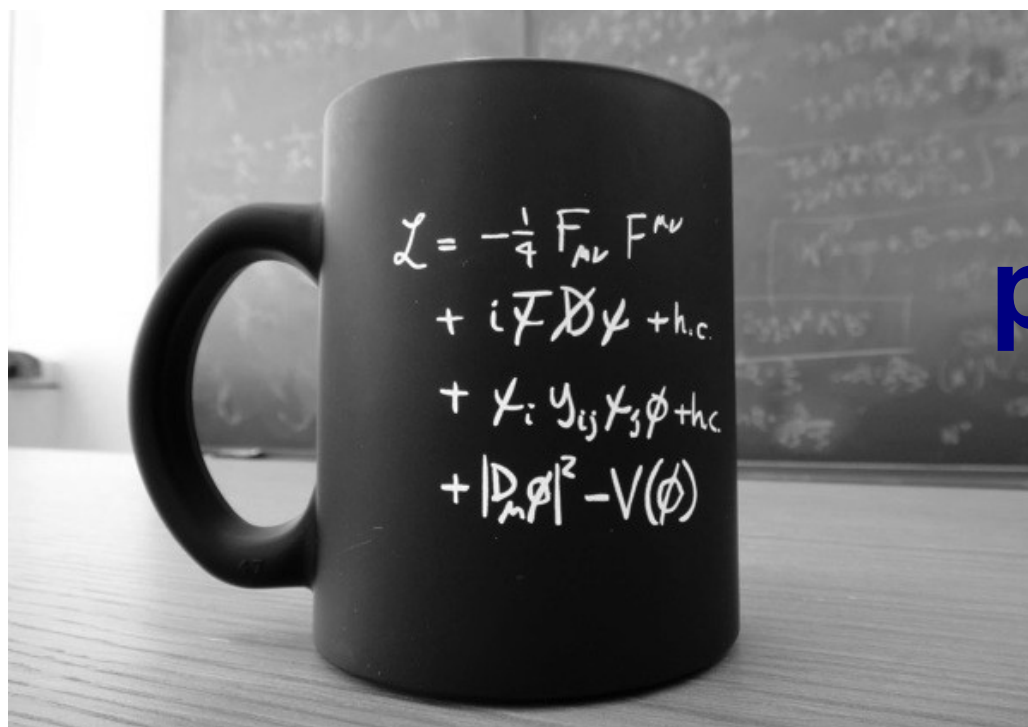


Plan for today

Summary of previous lectures

VV scattering

Searching for deviations in VV scattering



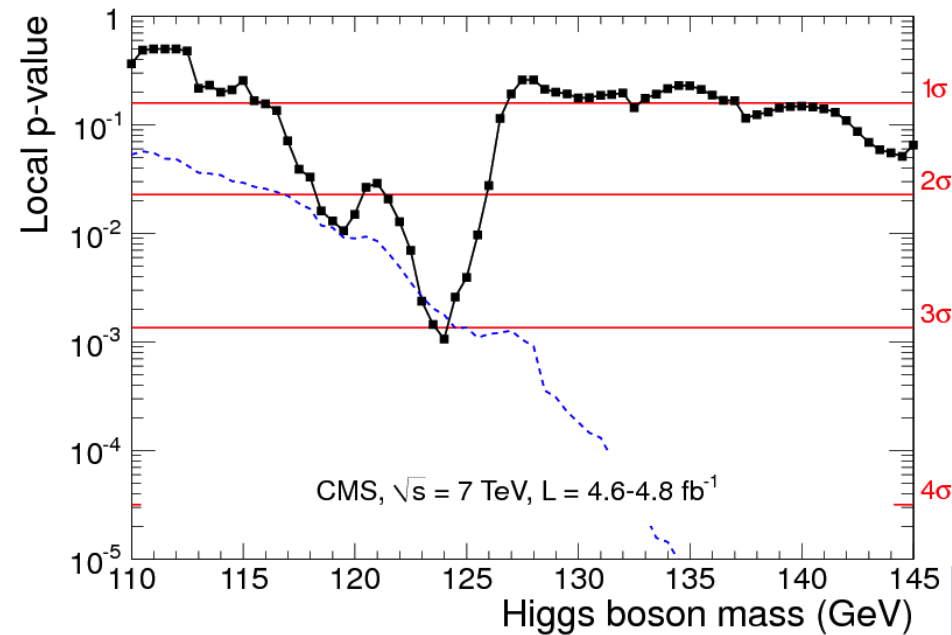
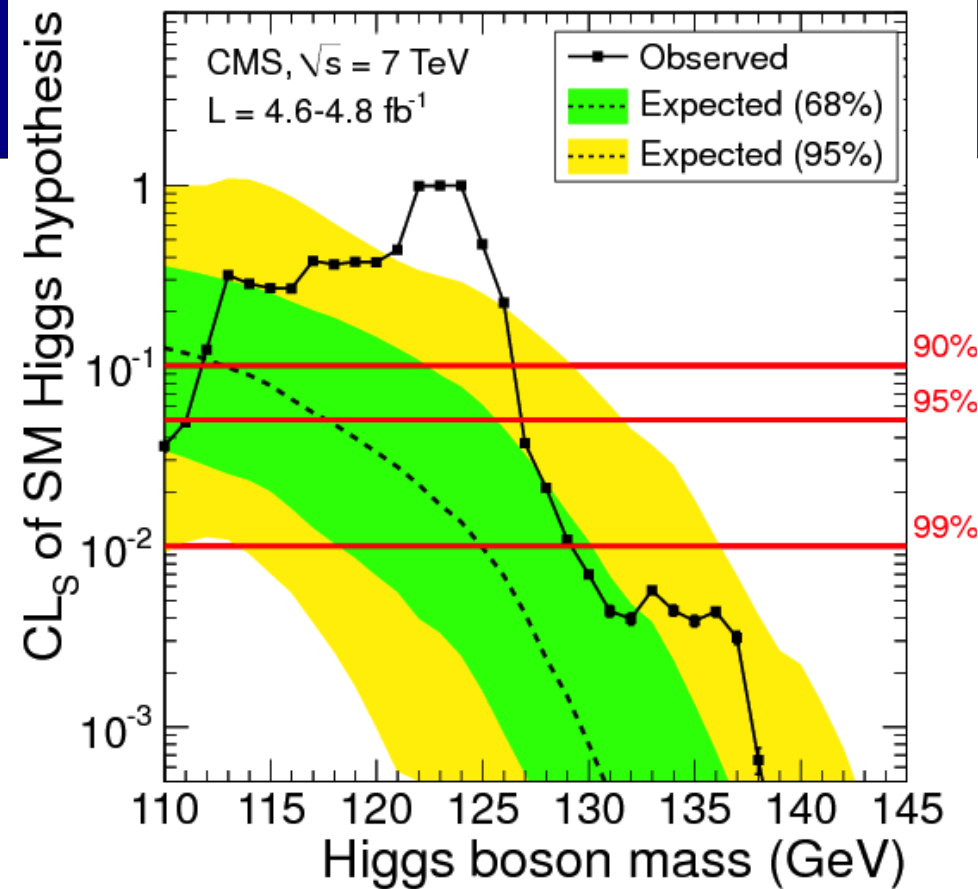
Summary of the previous lectures

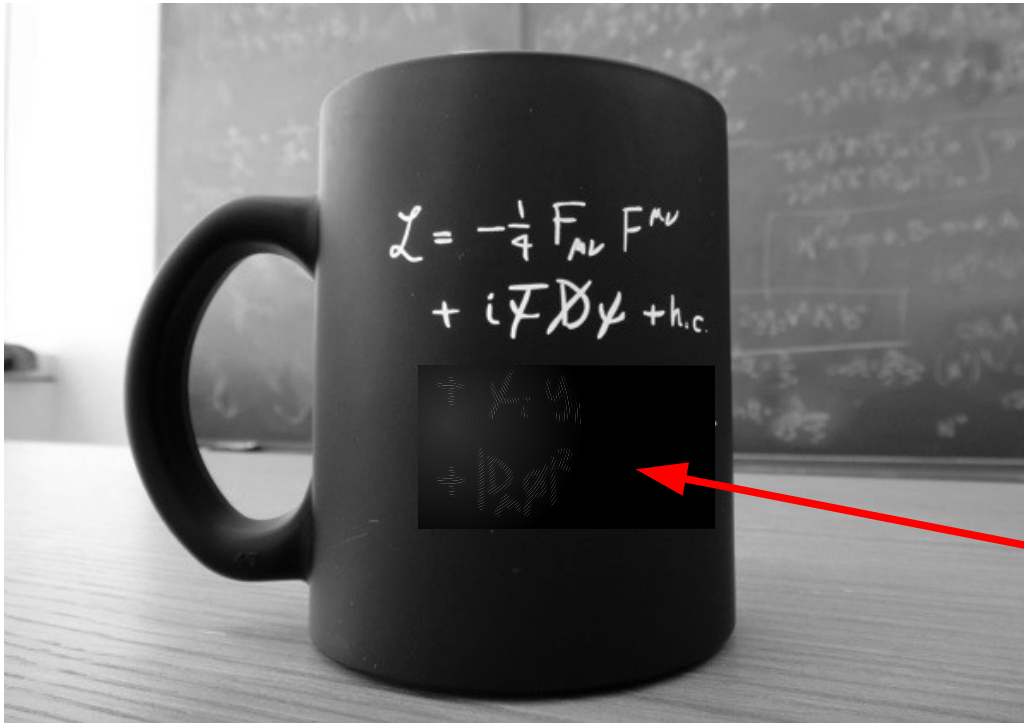
Close to conclusion?

- With 2011 data we have excluded most of the Higgs mass range
- Except where it is most favored to be found: $m_H < 127 \text{ GeV}/c^2$
- No combined limit between ATLAS and CMS until individual discovery or exclusion
- Observe an excess in the full mass range which as been searched:

ATLAS 10% probability (in 110-146 GeV)

CMS 2.1 σ local significance (in 110-145 GeV)





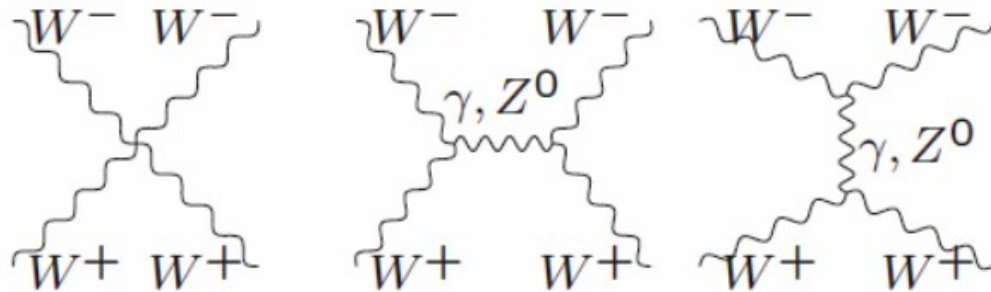
VV scattering

let's take one step back

What's special about vector boson scattering

6/46

- It's the key process to understand the EWK symmetry breaking mechanism

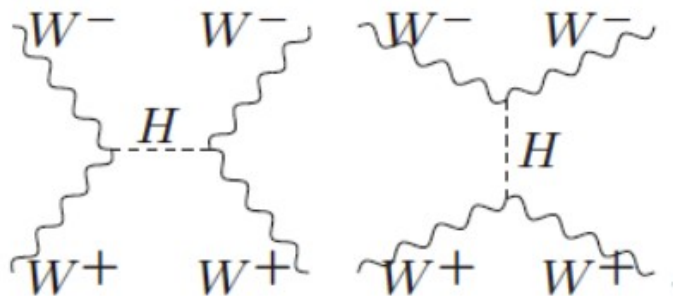


$$M_{gauge} = -\frac{g^2}{4M_W^2} \left(4 - \frac{3}{\rho}\right) u + \dots$$

$$\text{with, } u = -\frac{s}{2}(1 + \cos \theta)$$

$$\rho = (M_W^2/M_Z^2) \cos^2 \theta_W$$

- Unitarity is restored by introducing a new scalar field:



$$M_{Higgs} = \frac{g^2}{4M_W^2} u + \dots$$

What's special about vector boson scattering - 2

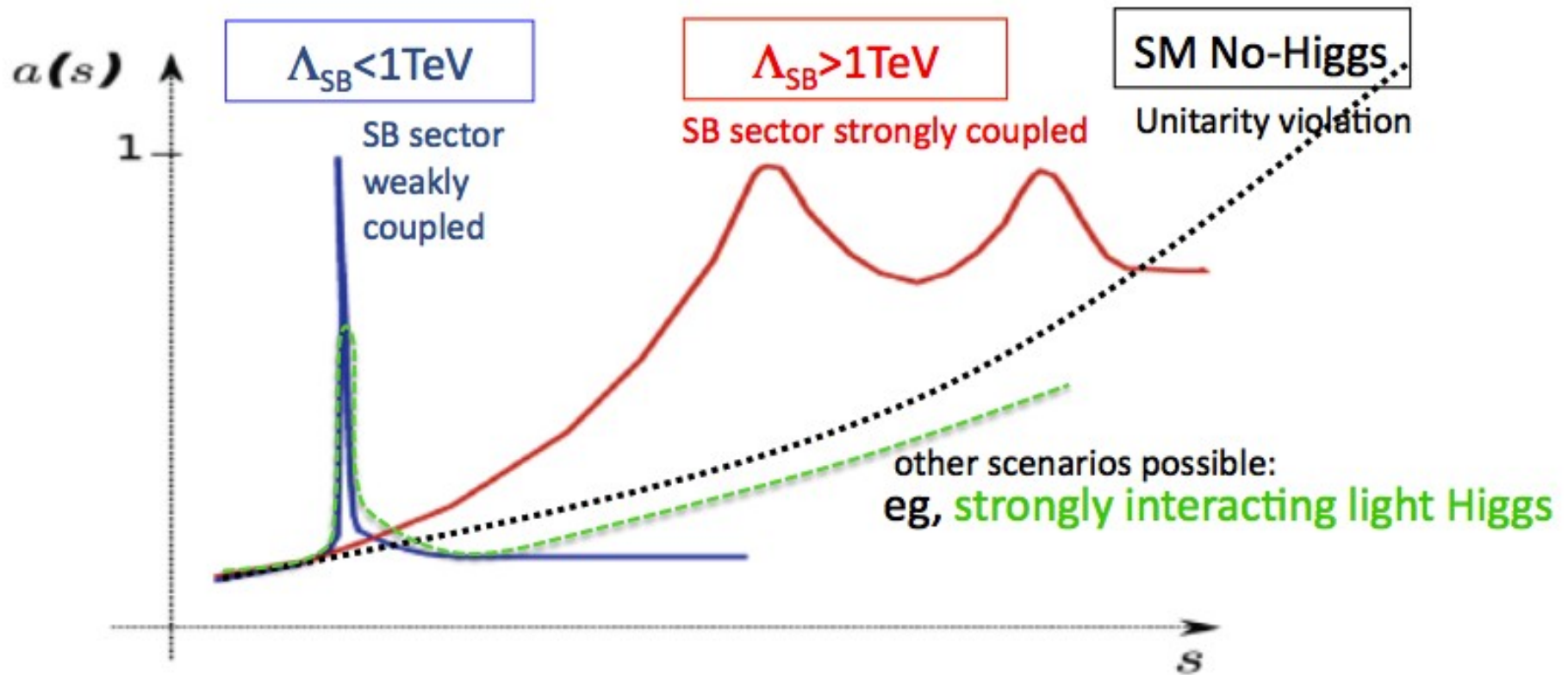
7/46

- If the SM Higgs is there

- the VV spectrum will be resonant
- probe effectively the full mass range

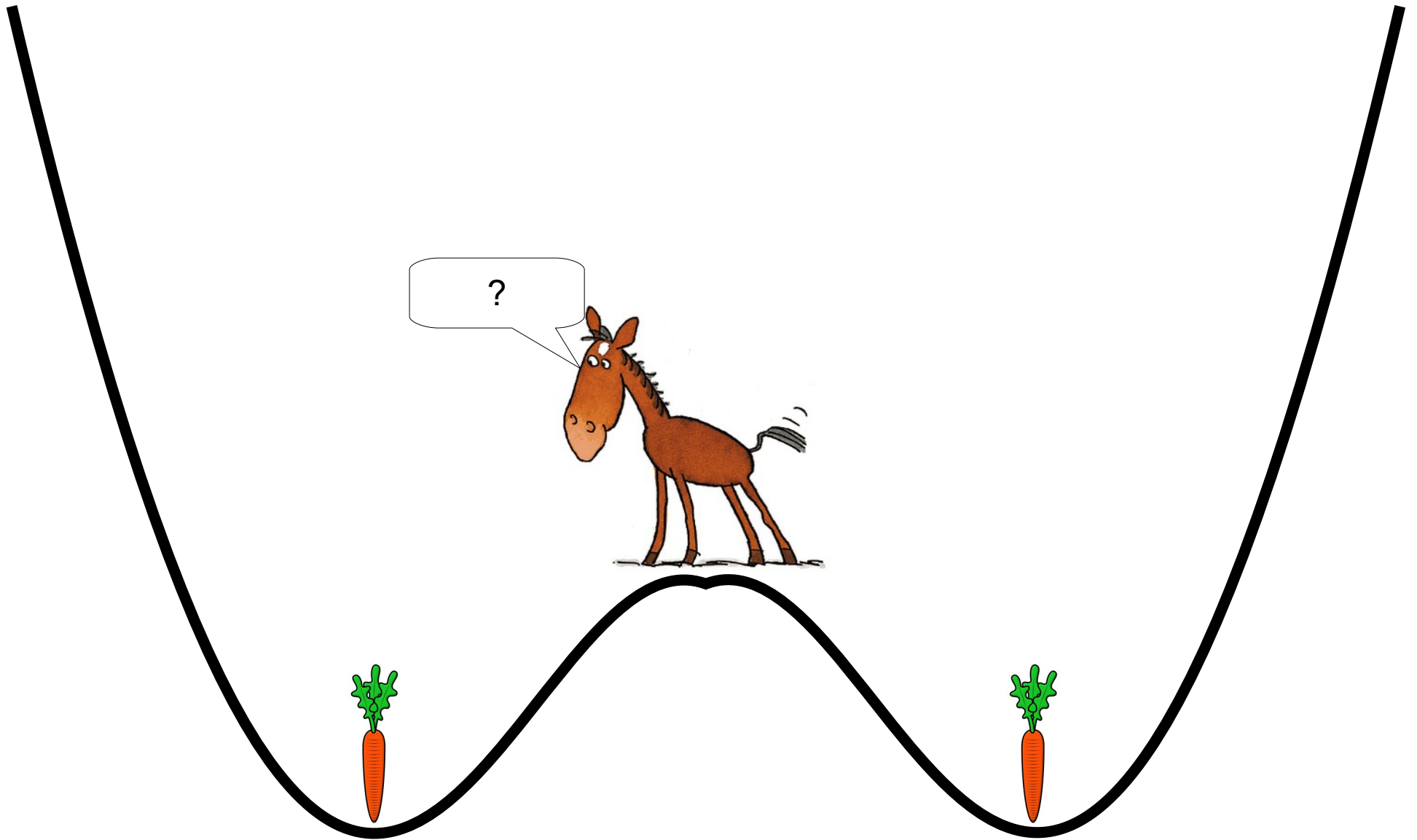
- If no Higgs is found:

- will interact strongly at $\Lambda \approx 1$ TeV
- observe deviation from SM prediction



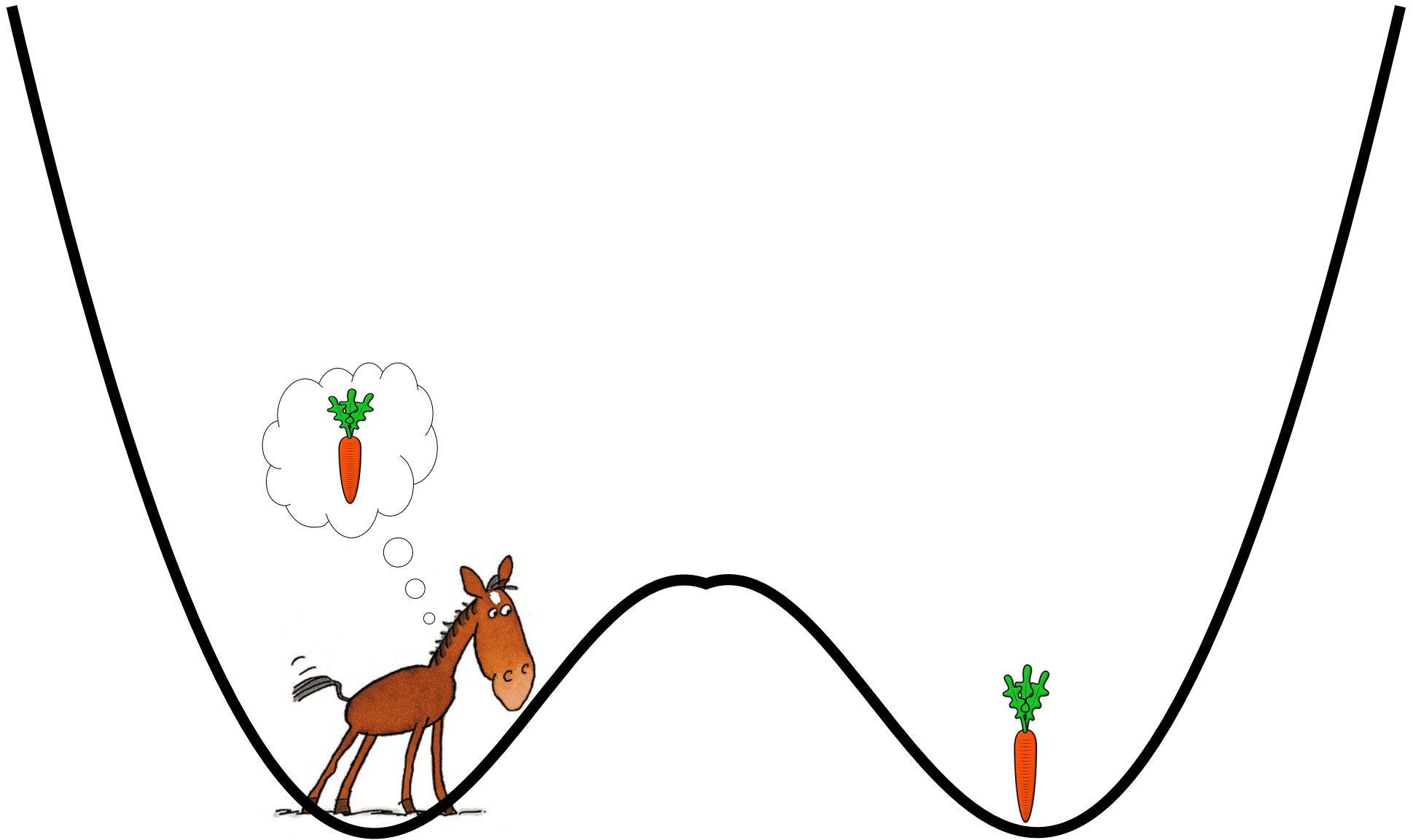
Whether the Higgs exists or not, VV scattering deserves dedicated study

Introducing the Higgs mechanism

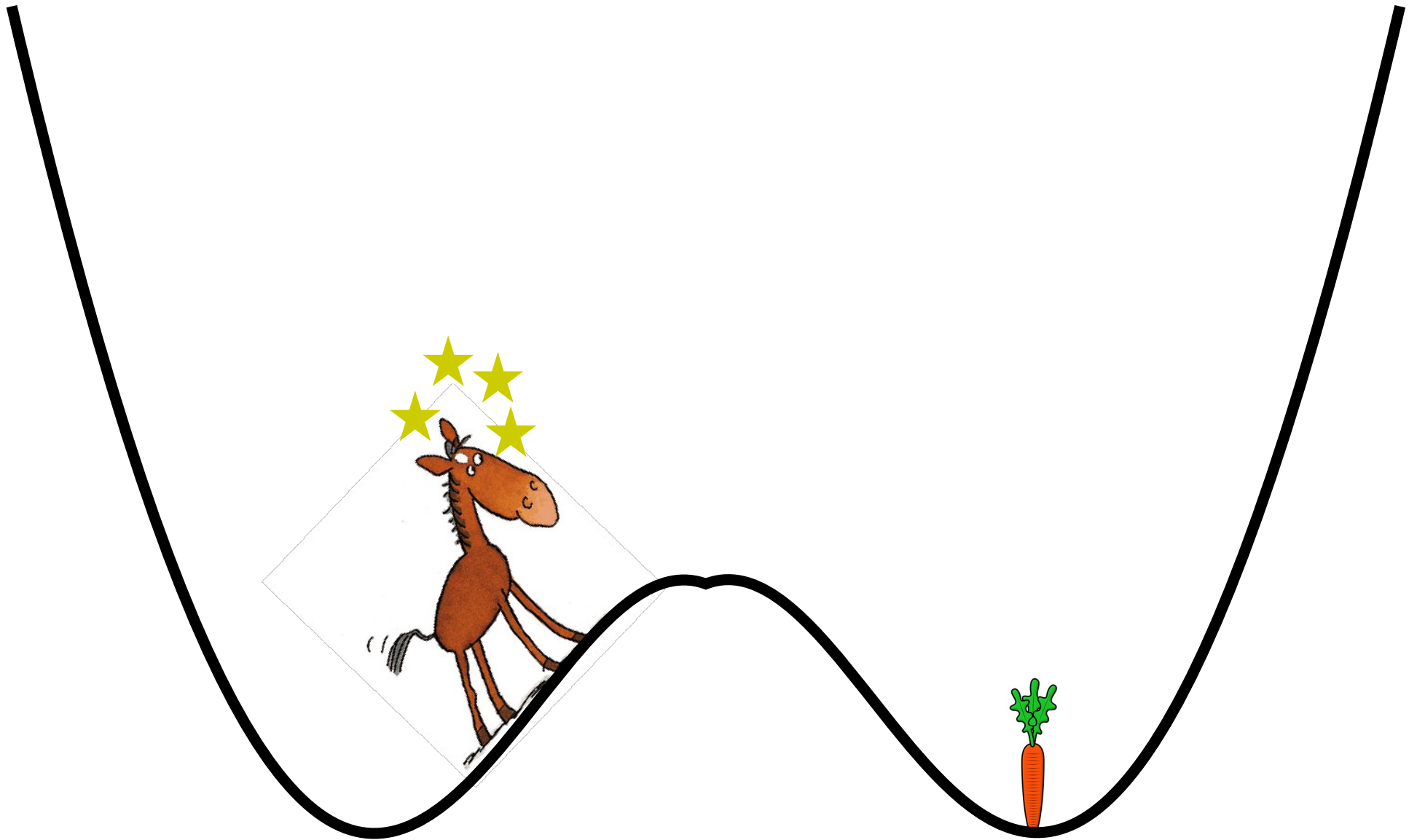


Introducing the Higgs mechanism

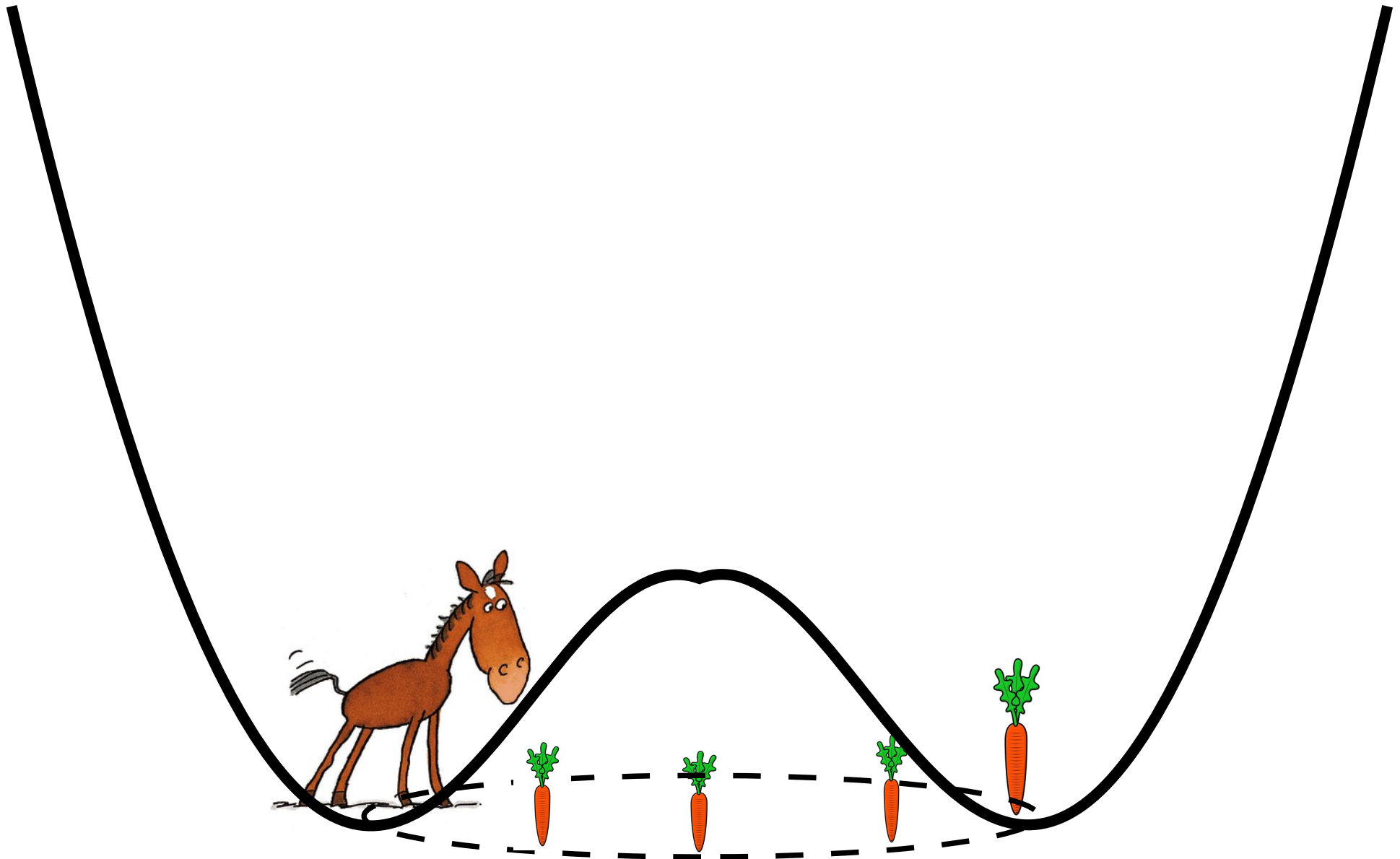
9/46



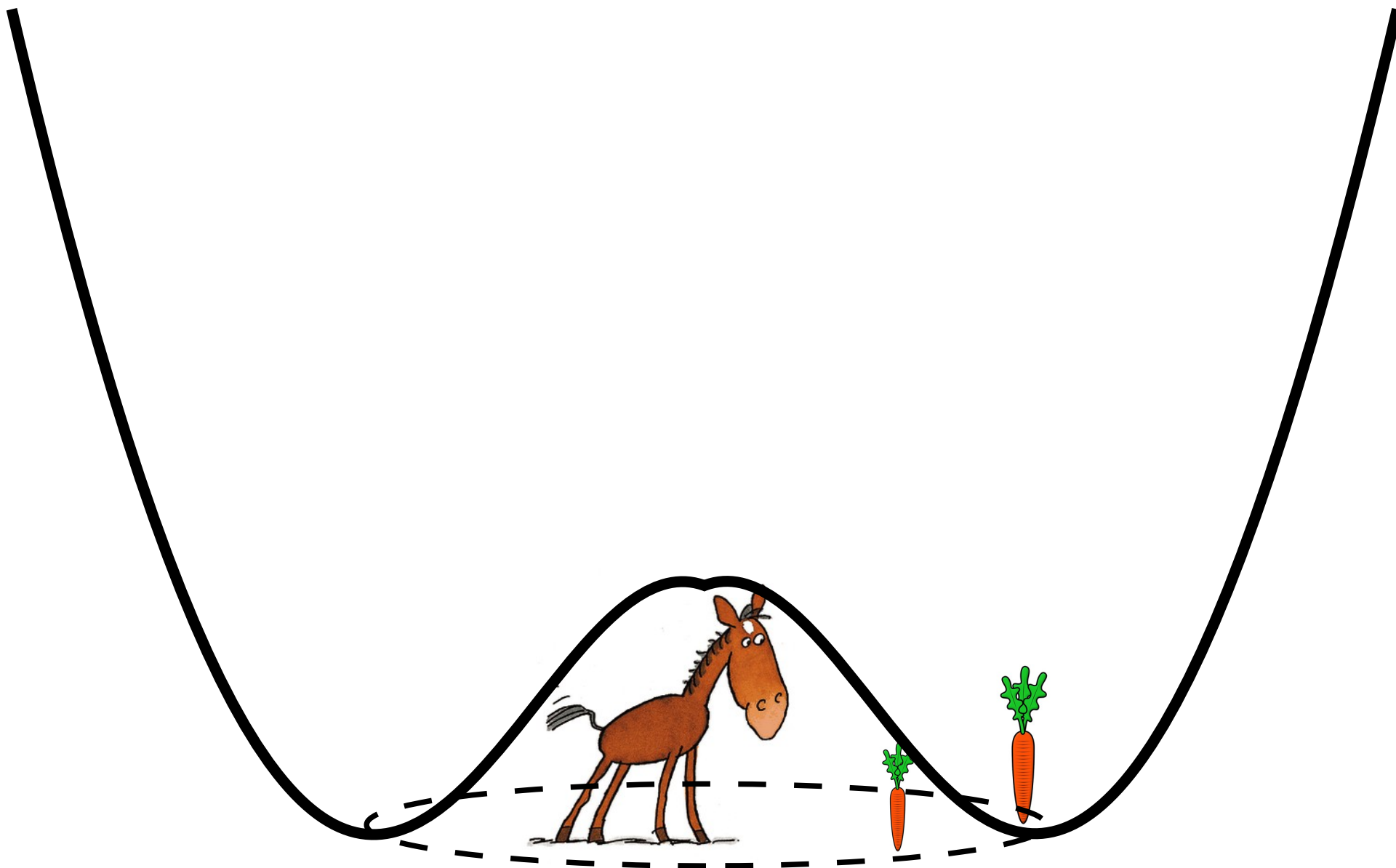
Introducing the Higgs mechanism



Introducing the Higgs mechanism



Introducing the Higgs mechanism



Goldstone bosons

- **Picture an infinite straight rope** (it has translation invariance)

- break its translational invariance in directions perpendicular to it



- the transverse waves are the Goldstone modes

$$\frac{1}{c^2} \frac{\partial^2 \phi}{\partial t^2} = \frac{\partial^2 \phi}{\partial x^2} \quad \rightarrow \omega^2 = c^2 k^2$$

- Waves can propagate with arbitrary frequency

→ after quantization will generate massless particles

- **EWK ground state / the vacuum is said to be “spontaneously broken”**

- A spontaneously broken symmetry always produces a massless scalar particle.

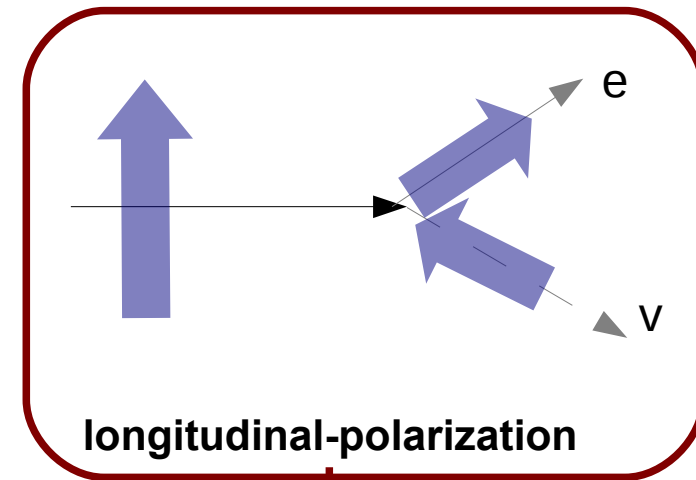
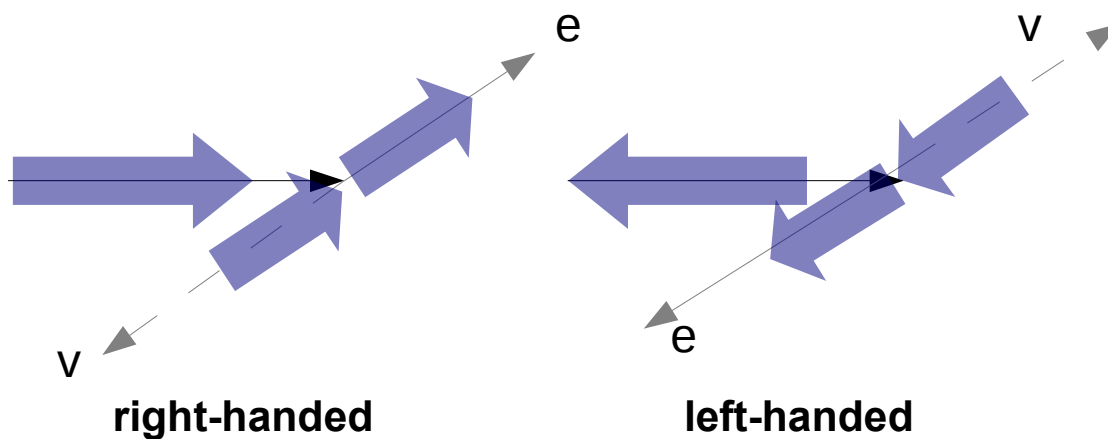
- If the symmetry is approximate, the particle won't be massless, but can be very light.

Vector bosons at high energy

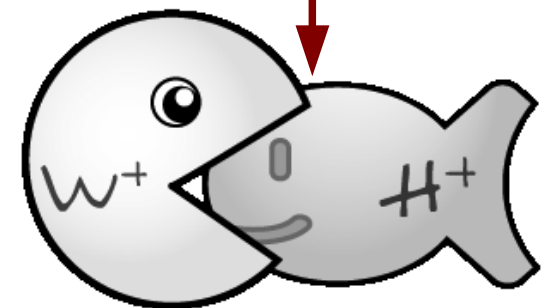
14/46

- In the limit $m_W/s^{1/2} \rightarrow 0$ and $m_Z/s^{1/2} \rightarrow 0$
 - the mass can be neglected, vector bosons acquire large boost
 - W/Z become effectively goldstone bosons because longitudinal polarization dominates

- Pictorially:

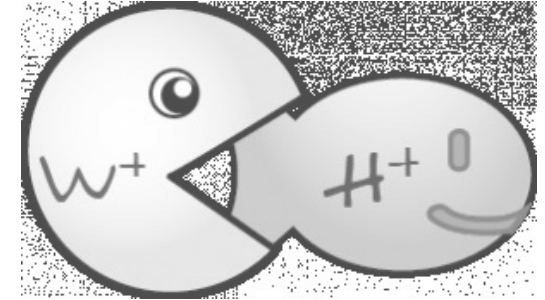


- The longitudinal component corresponds in practice to a “swallowed” goldstone bosons ▶



Vector bosons at high energy

- At high $s^{1/2}$ the longitudinal component becomes dominant
- Vector bosons are in practice goldstone bosons



- The fields can be generically written as: $U = \exp\left(i \frac{\omega^\alpha \tau^\alpha}{u_v}\right)$
- Behavior is purely chiral
- The Lagrangian of interactions is given by:

$$\mathcal{L}_{EWChL} = \mathcal{L}^{(2)} + \mathcal{L}^{(4)} + \dots = \frac{u^2}{4} \text{Tr}\{D_\mu U D^\mu U^\dagger\} + \alpha_4 (\text{Tr}\{D_\mu U D^\mu U^\dagger\})^2 + \alpha_5 (\text{Tr}\{D_\mu U D^\nu U^\dagger\})^2$$

Kinematic term

Terms that do not introduce anomalous triple gauge couplings

- Different choices of α_4 and α_5 correspond to different models of the strongly interacting electroweak breaking sector

Electroweak Chiral Formalism

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- In this approximation the global symmetry is now $SU(2)_{L+R}$
- The scattering amplitude is generically written as:

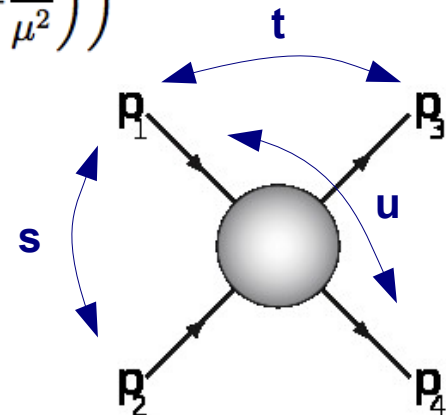
$$\mathcal{M}(V_L^a V_L^b \rightarrow V_L^c V_L^d) \equiv A(s, t, u) \delta^{ab} \delta^{cd} + A(t, s, u) \delta^{ac} \delta^{bd} + A(u, t, s) \delta^{ad} \delta^{bc}$$

with the amplitude given generically by:

$$\begin{aligned} A(s, t, u) = & \frac{s}{u^2} + \frac{1}{4\pi u^4} (2\alpha_4(\mu)s^2 + \alpha_5(\mu)(t^2 + u^2)) + \\ & + \frac{1}{16\pi^2 u^4} \left(-\frac{t}{6}(s + 2t) \log\left(-\frac{t}{\mu^2}\right) \right) - \\ & - \frac{1}{16\pi^2 u^4} \left(\frac{u}{6}(s + 2u) \log\left(-\frac{u}{\mu^2}\right) - \frac{s^2}{2} \log\left(-\frac{s}{\mu^2}\right) \right) \end{aligned}$$

- Note: s,t,u are the classic Mandelstam variables ►

→ for WW scattering $s+t+u=4M_W^2$



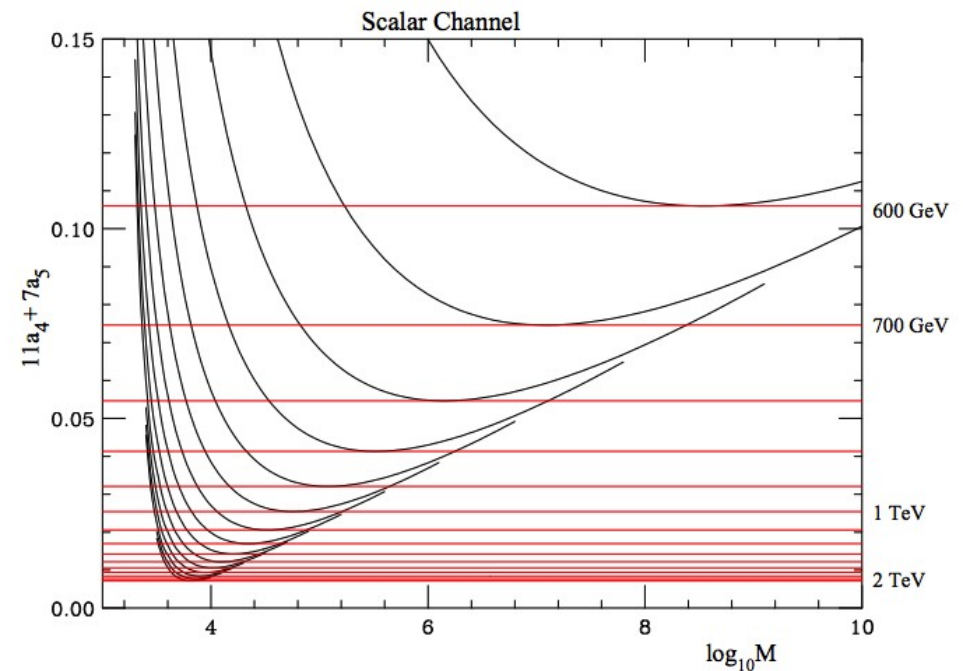
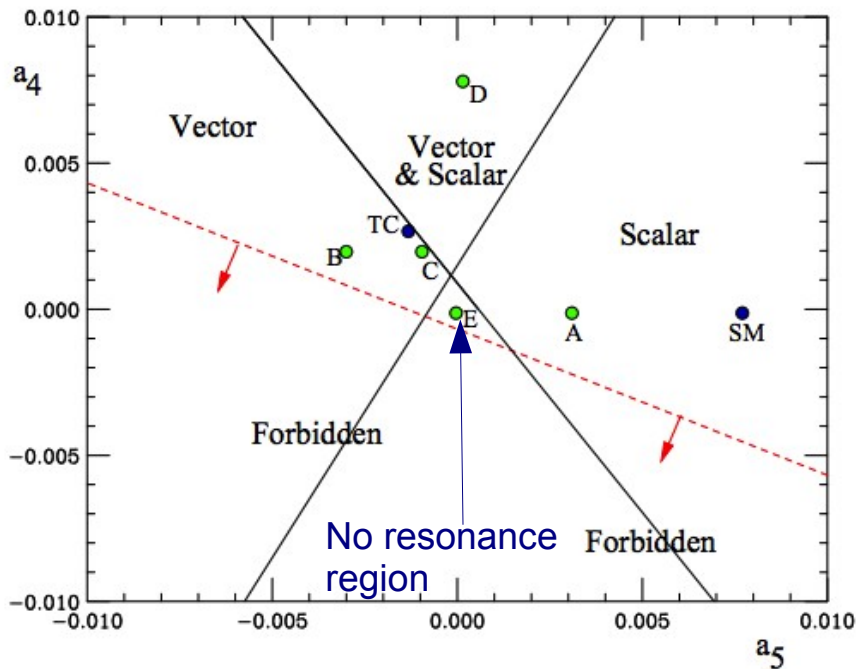
WW scattering in EWKchL formalism

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- The amplitude is now given by: $\mathcal{M}(W_L^\pm W_L^\pm \rightarrow W_L^\pm W_L^\pm) = A(t, s, u) + A(u, t, s)$
- A unitarization procedure has to be performed otherwise it will diverge
- Two approaches followed (see details in Butterworth et al aXiv:hep-ph/0201098)

Pade protocol: $\text{Im } A = |A|^2$ is implied by elastic unitarisation for $s > 0$.

N/D protocol: besides ensuring partial wave unitarity and matching 1-loop EWKchL computation. Constraints are imposed in the Numerator/Denominator of the partial waves



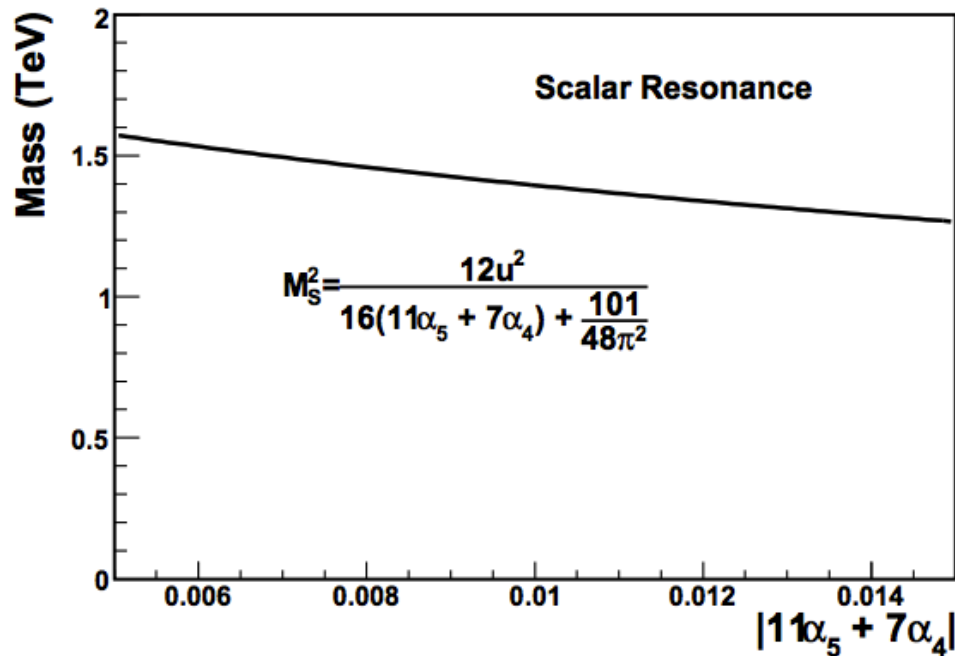
Partial waves may lead to resonances (scalar, vectorial, tensorial) → play similar role to Higgs

Examples in the Padé protocol

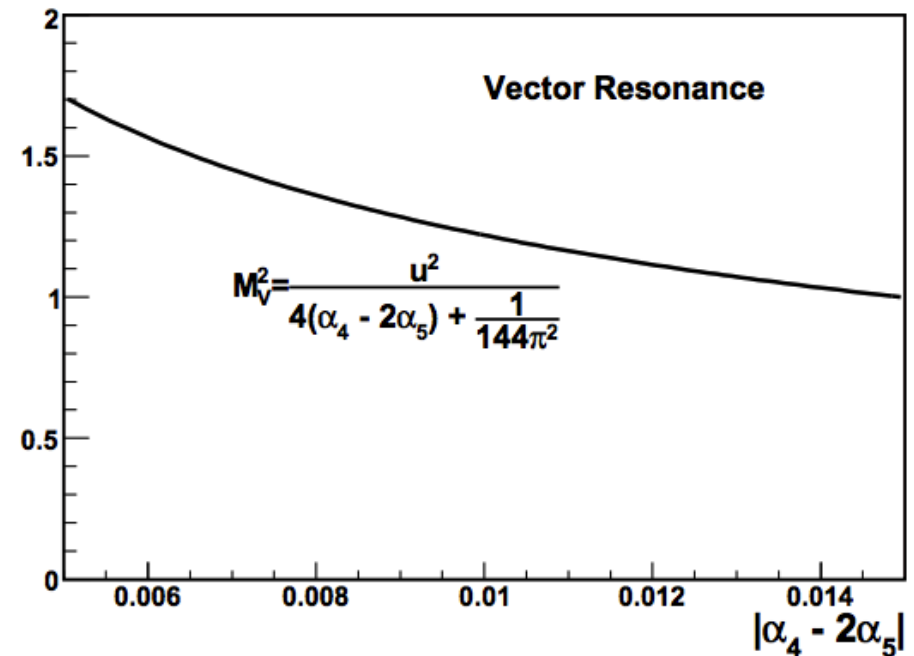
- Parameterize the scalar and vectorial resonances in terms of simple combinations of α_5 and α_4 parameters.

- Examples for $\mu=1$ TeV

$$M_S^2 = \frac{12u_v^2}{16[11\alpha_5(\mu) + 7\alpha_4(\mu)] + \frac{101-50 \log(M_S^2/\mu^2)}{48\pi^2}}, \quad \Gamma_S = \frac{M_S^3}{16\pi u_v^2}$$



$$M_V^2 = \frac{u_v^2}{4[\alpha_4(\mu) - 2\alpha_5(\mu)] + \frac{1}{144\pi^2}}, \quad \Gamma_V = \frac{M_V^3}{96\pi u_v^2}$$



Examples in the Padé protocol

- Parameterize the scalar and vectorial resonances in terms of simple combinations of α_5 and α_4 parameters.

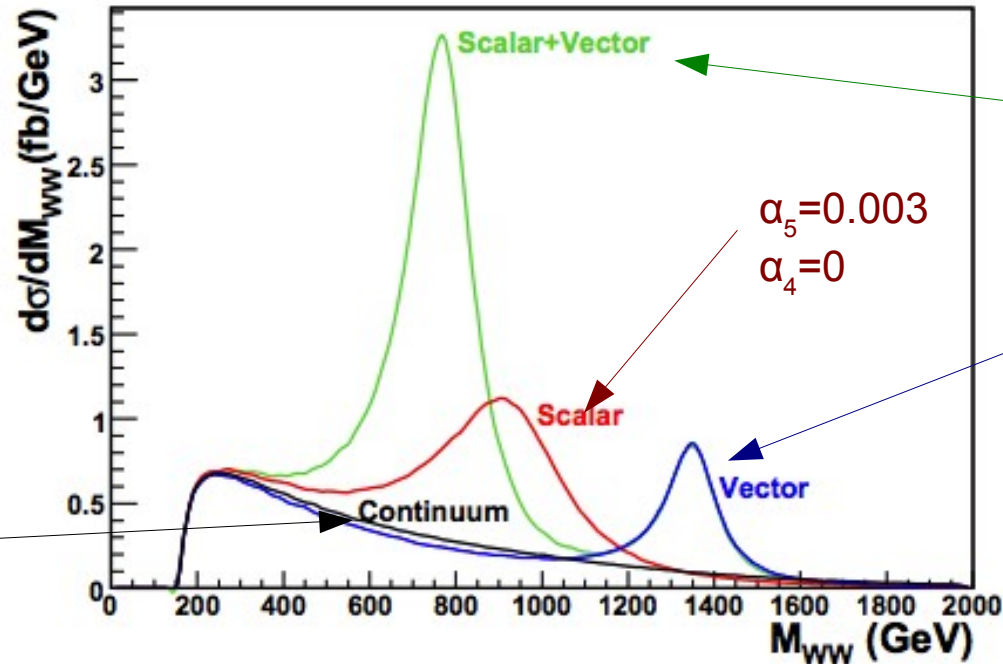
- Examples for $\mu=1$ TeV

$$M_S^2 = \frac{12u_v^2}{16[11\alpha_5(\mu) + 7\alpha_4(\mu)] + \frac{101-50 \log(M_S^2/\mu^2)}{48\pi^2}},$$

$$\Gamma_S = \frac{M_S^3}{16\pi u_v^2}$$

$$M_V^2 = \frac{u_v^2}{4[\alpha_4(\mu) - 2\alpha_5(\mu)] + \frac{1}{144\pi^2}},$$

$$\Gamma_V = \frac{M_V^3}{96\pi u_v^2}$$



$$\alpha_5=0$$

$$\alpha_4=0$$

$$\alpha_5=0$$

$$\alpha_4=0.008$$

$$\alpha_5=0.003$$

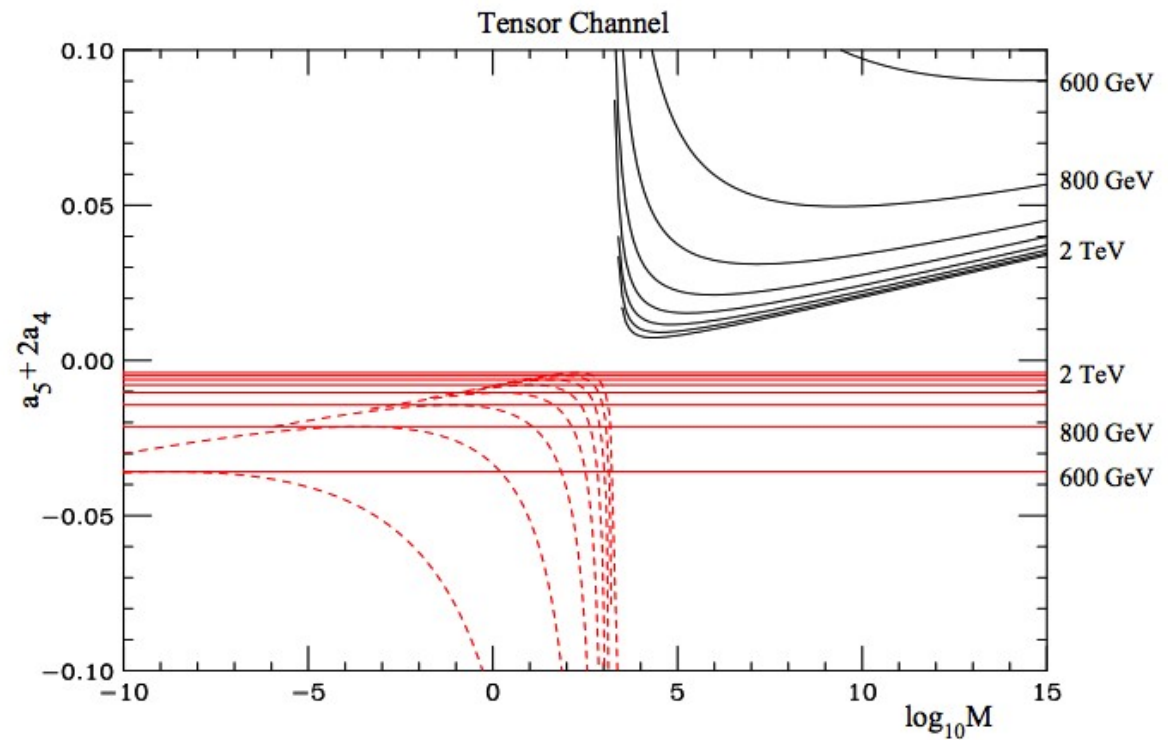
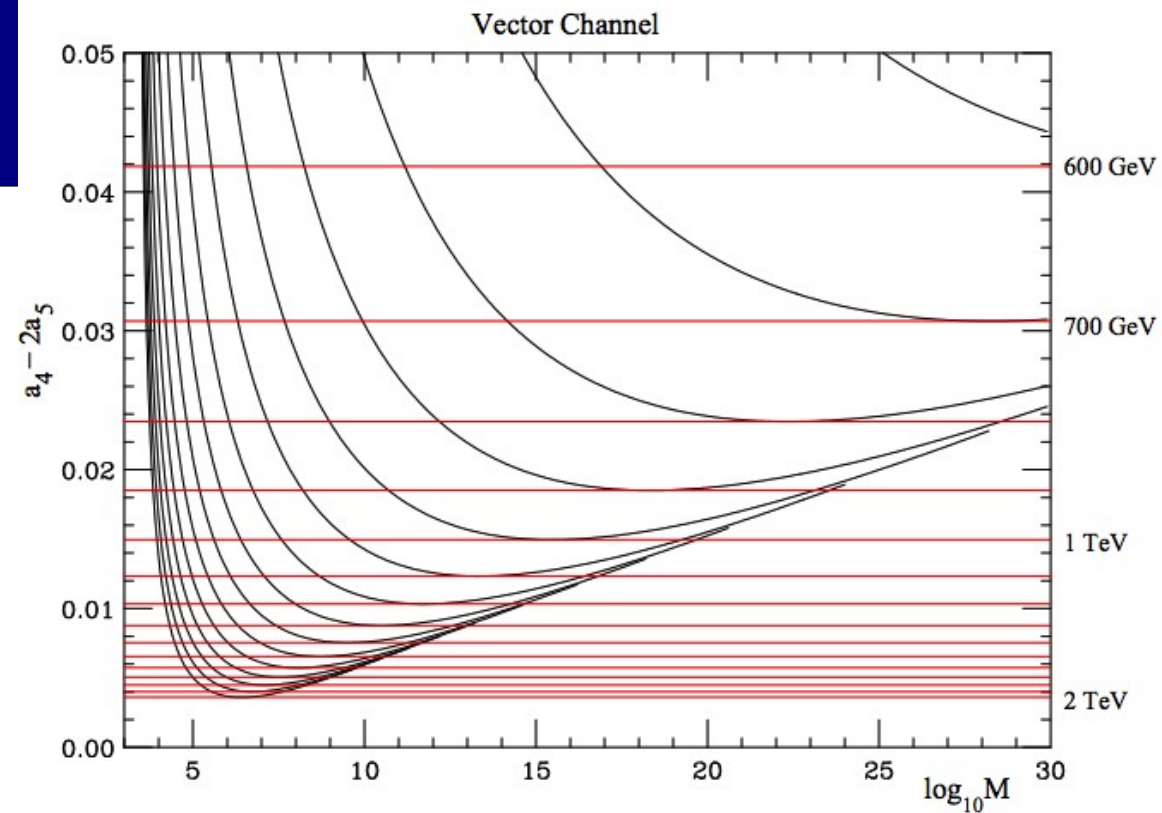
$$\alpha_4=0$$

$$\alpha_5=-0.003$$

$$\alpha_4=0.002$$

Examples for N/D

- The mass of the resonance in the N/D protocol depends as well on α_4 , α_5 and in the $\mu=M$ (cut-off parameter)
- Contours for physical solutions are given for different resonance (predictions for scalars are in slide 12)

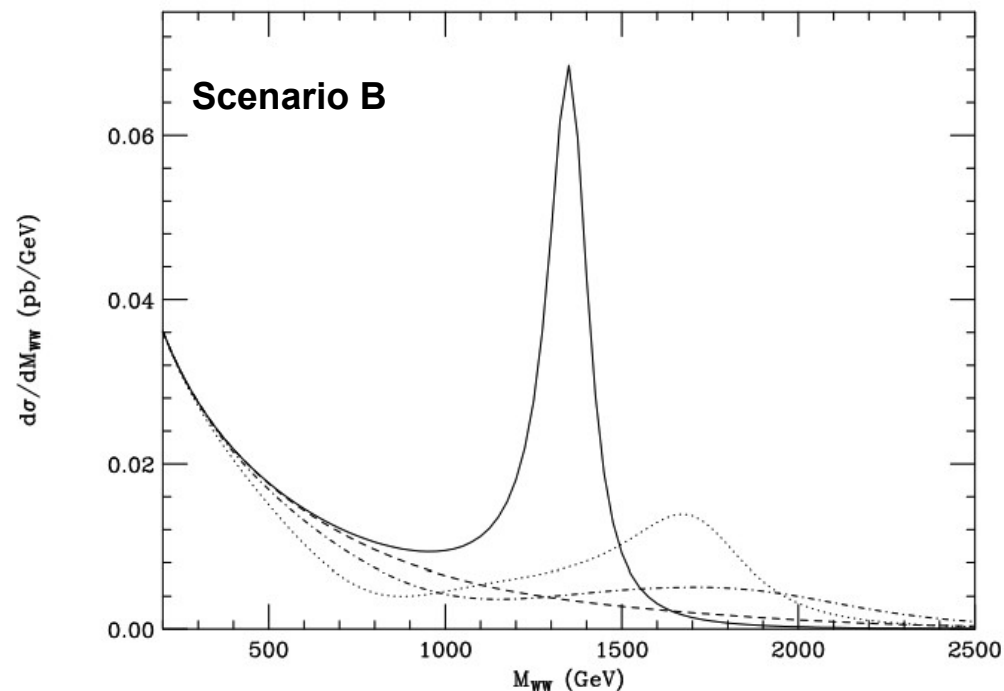
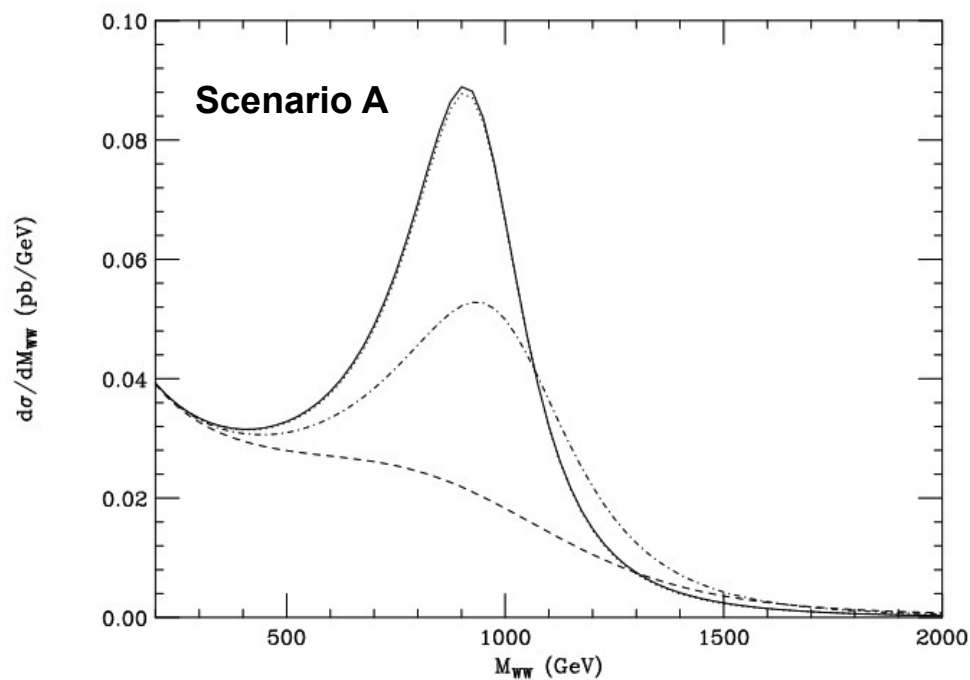


M_{WW} spectrum

- Prediction can be compared for both models in different scenarios and lead to broad/narrow resonance or a continuum spectrum

Scenario	$a_4(1 \text{ TeV})$	$a_5(1 \text{ TeV})$
A	0.0	0.003
B	0.002	-0.003
C	0.002	-0.001
D	0.008	0
E	0	0

Shown: Padé – solid N/D – dashed (shown for different μ)

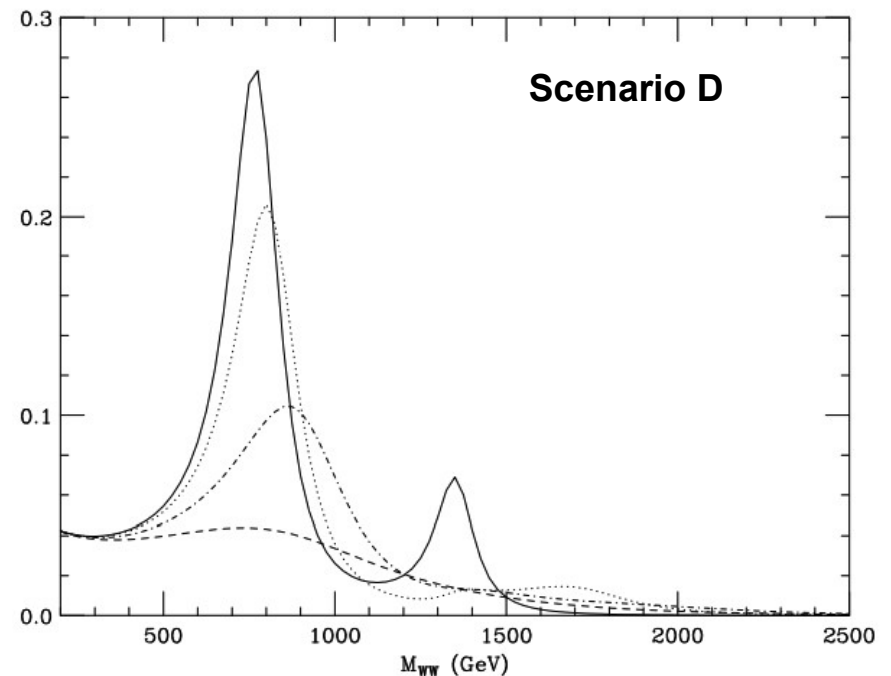
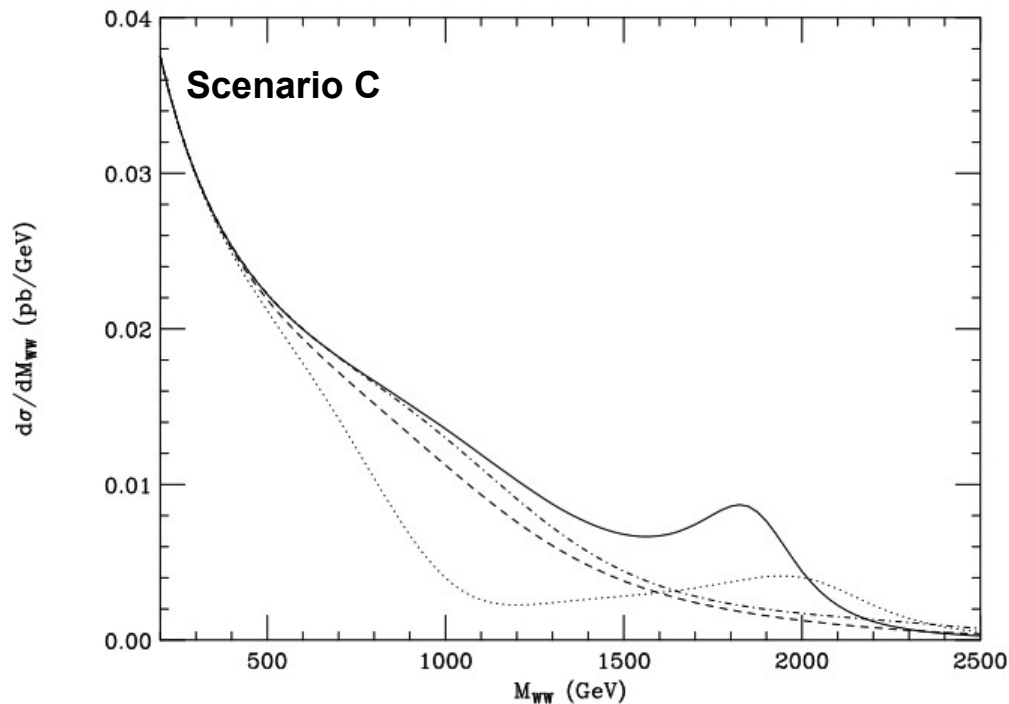


M_{WW} spectrum – cont.

- Prediction can be compared for both models in different scenarios and lead to broad/narrow resonance or a continuum spectrum

Scenario	$a_4(1 \text{ TeV})$	$a_5(1 \text{ TeV})$
A	0.0	0.003
B	0.002	-0.003
C	0.002	-0.001
D	0.008	0
E	0	0

Shown: Padé – solid N/D – dashed (shown for different μ)



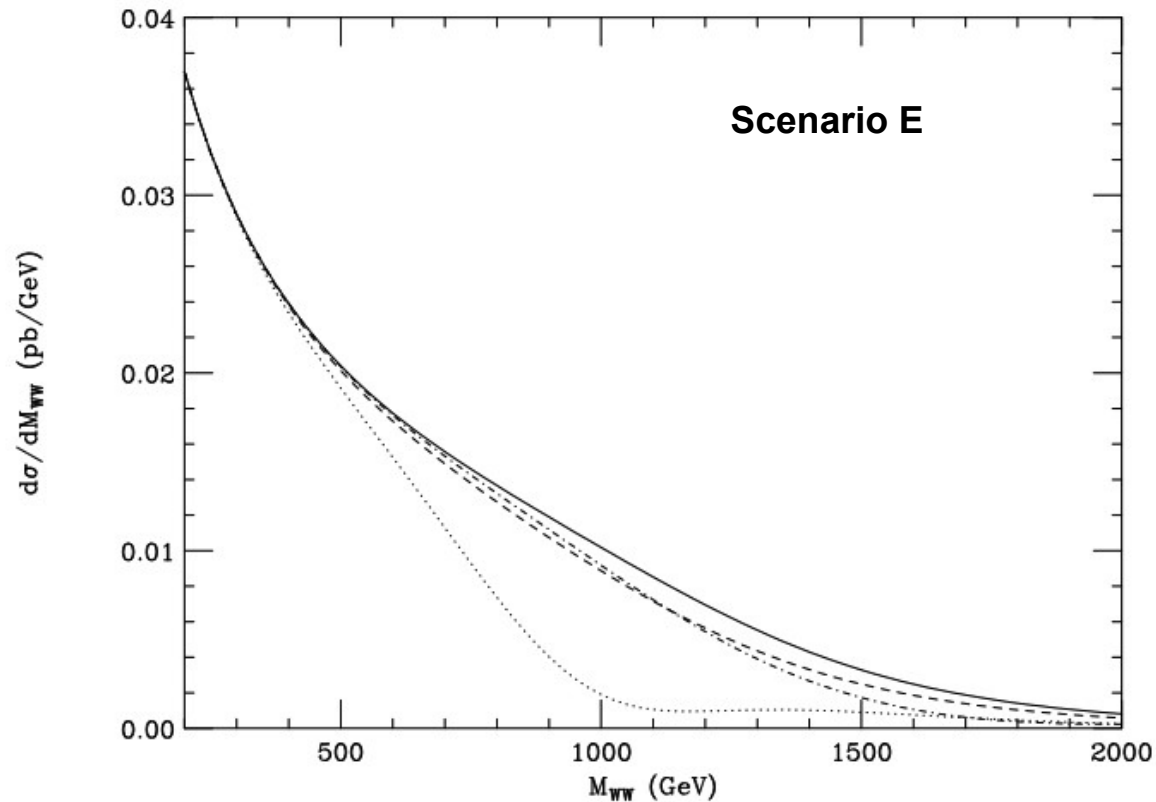
M_{WW} spectrum – cont.

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- Prediction can be compared for both models in different scenarios and lead to broad/narrow resonance or a continuum spectrum

Scenario	$a_4(1 \text{ TeV})$	$a_5(1 \text{ TeV})$
A	0.0	0.003
B	0.002	-0.003
C	0.002	-0.001
D	0.008	0
E	0	0

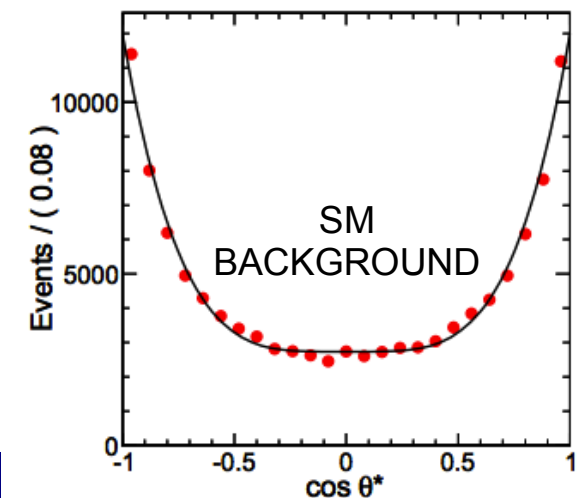
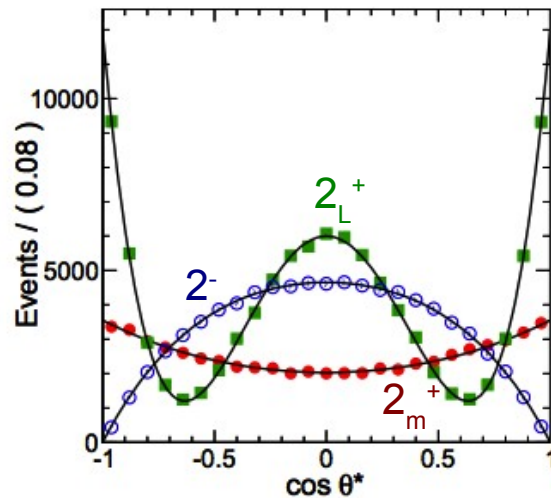
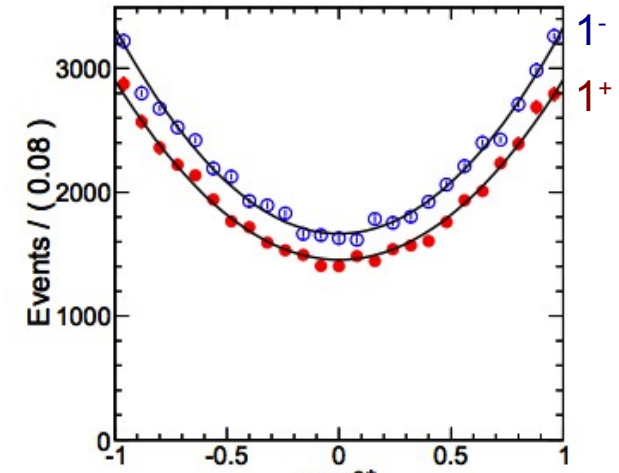
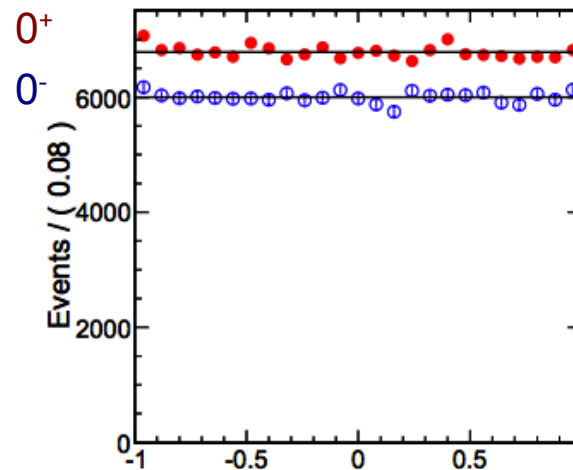
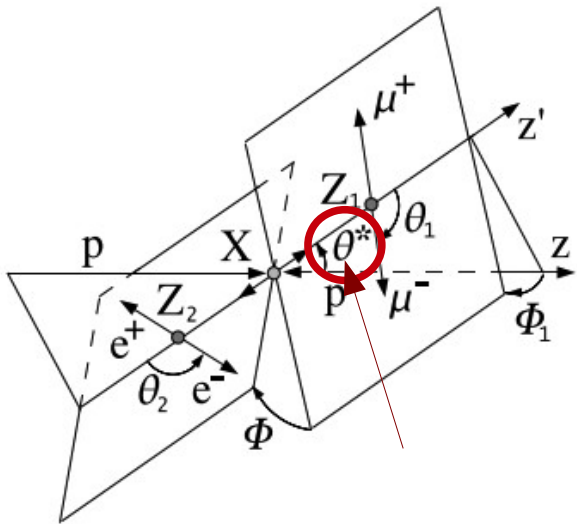
Shown: Padé – solid N/D – dashed (shown for different μ)



Example: how to discriminate nature of resonance

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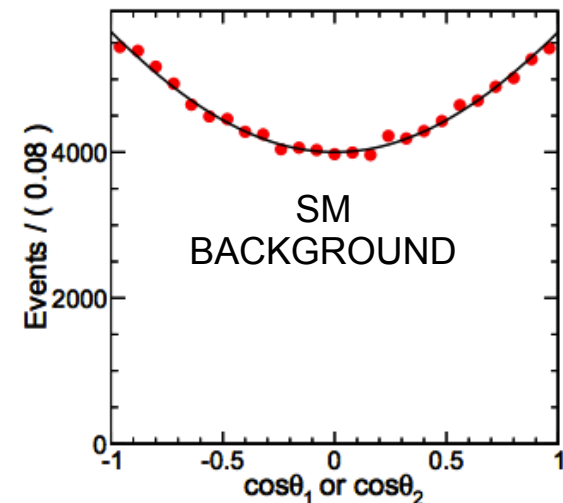
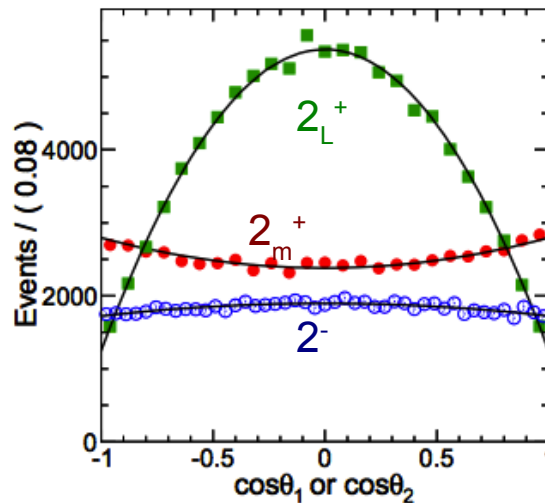
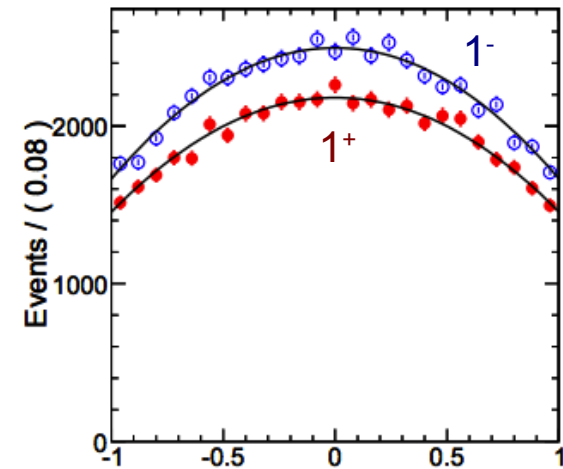
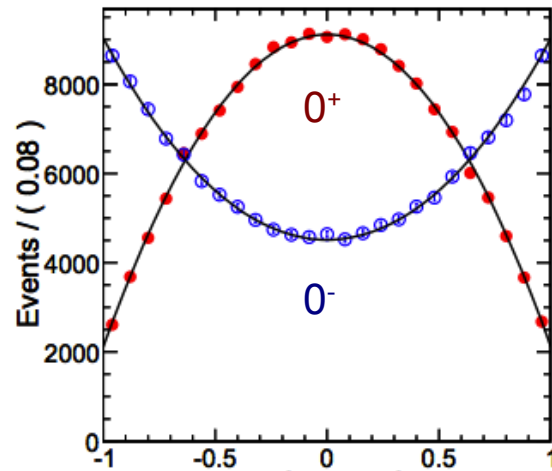
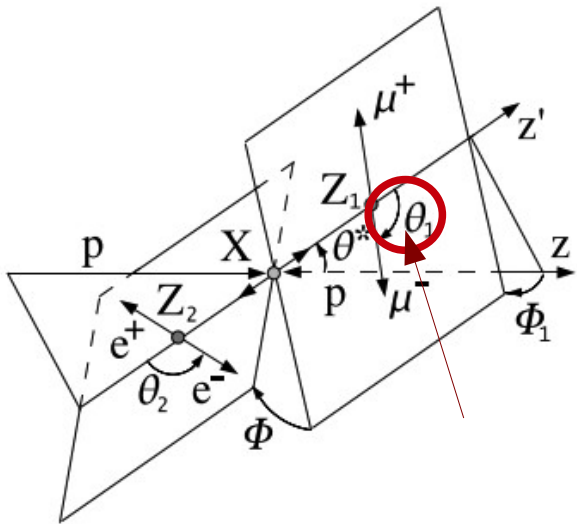
- As an example consider ZZ production after one of these generic resonances
- For θ^* (Z angle with respect to beam-line) in the ZZ rest-frame:
 - Distribution depends on spin and parity of the resonance



Example: how to discriminate nature of resonance

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- As an example consider ZZ production after one of these generic resonances
- For θ_i (lepton angle with respect to Z direction) in the ZZ rest-frame:
 - Distribution depends on spin and parity of the resonance

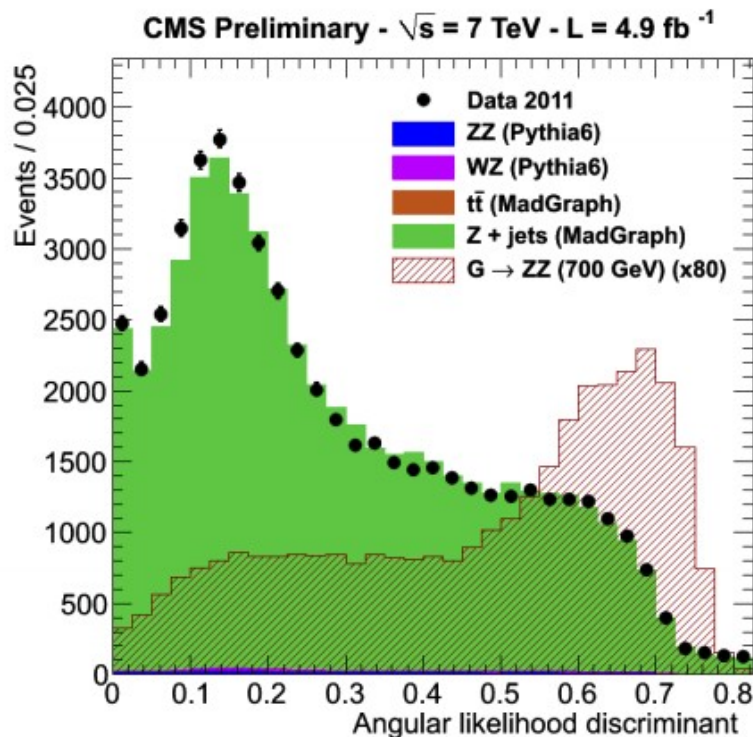


Example in practice: $G \rightarrow ZZ \rightarrow 2l2q$

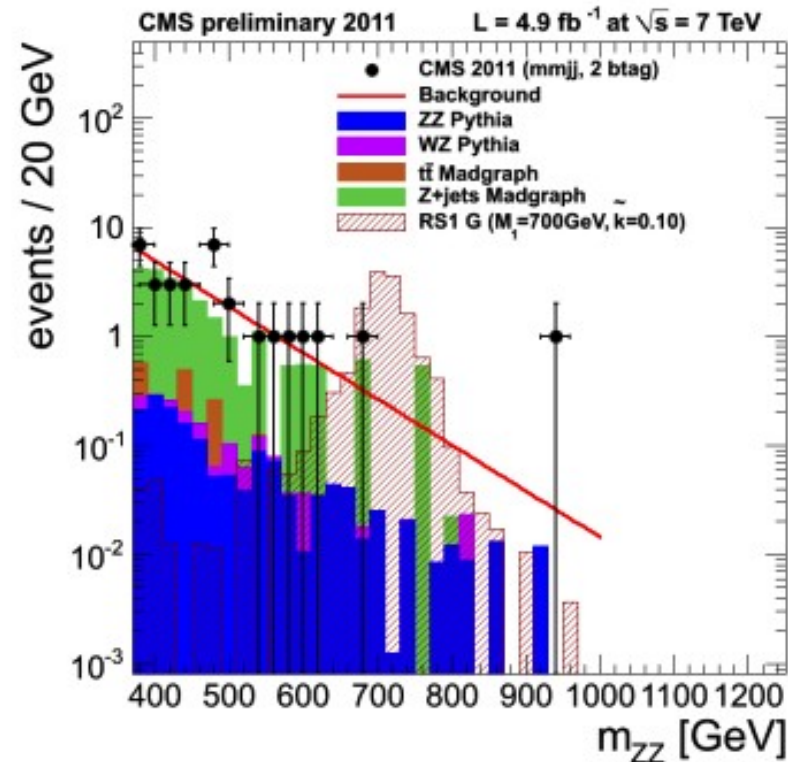
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- A graviton can be an example of a spin 2 particle
- Couplings to bosons suppressed in Randall-Sundrum original model but enhanced if SM fields propagate in the extra-dimension

Use likelihood ratio discriminator to select signal-like events



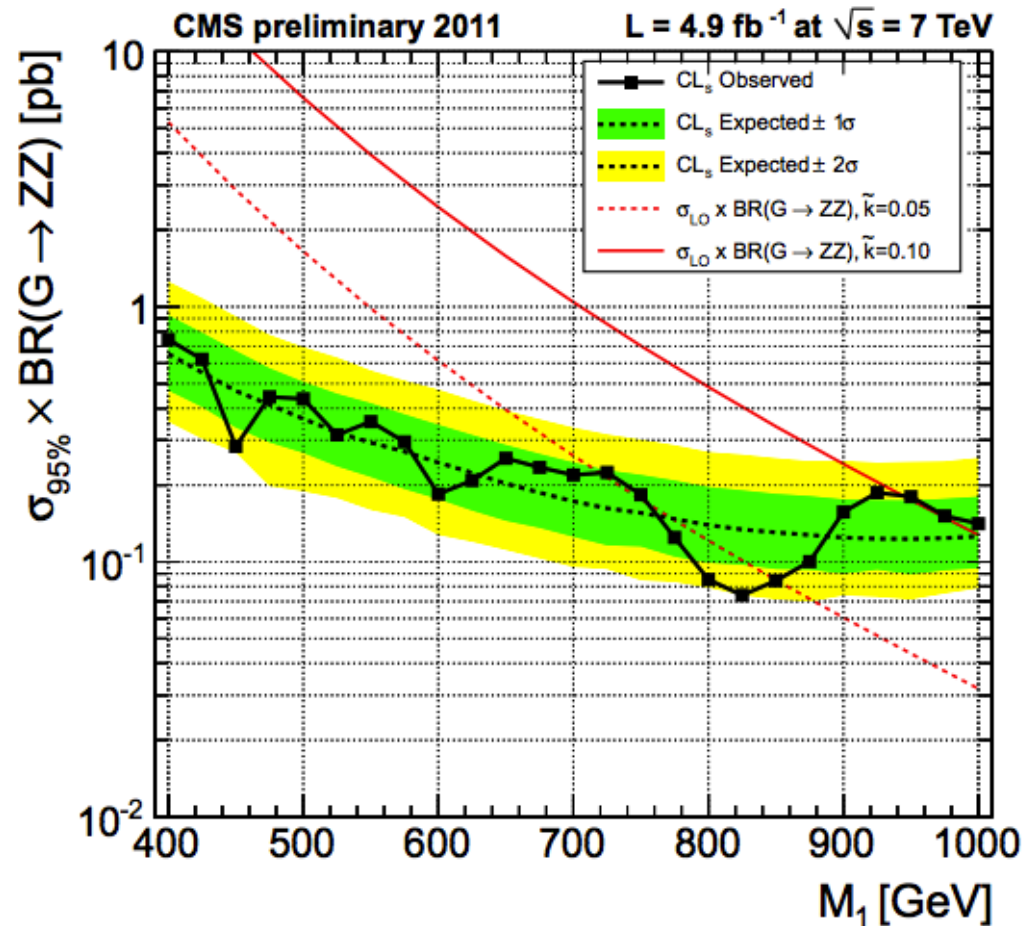
Search for resonance in the ZZ spectrum (background taken from sidebands)



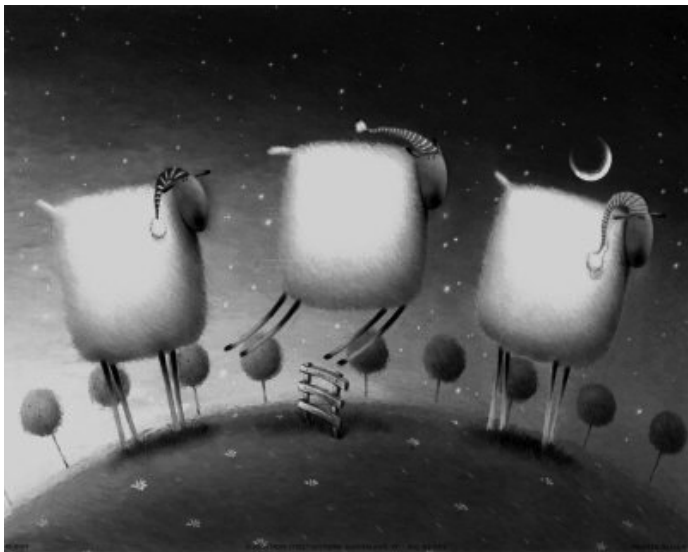
Limits on G mass

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- The model is specified by the curvature of the extra dimension – k
- Usually measured in units of Planck mass (2.435×10^{18} GeV/ c^2): $\tilde{k} = \bar{k} / \bar{M}_{Pl}$
- Excluded up to 1 TeV (Note: RS1 searches excluded up to)



Searching for deviations in VV scattering



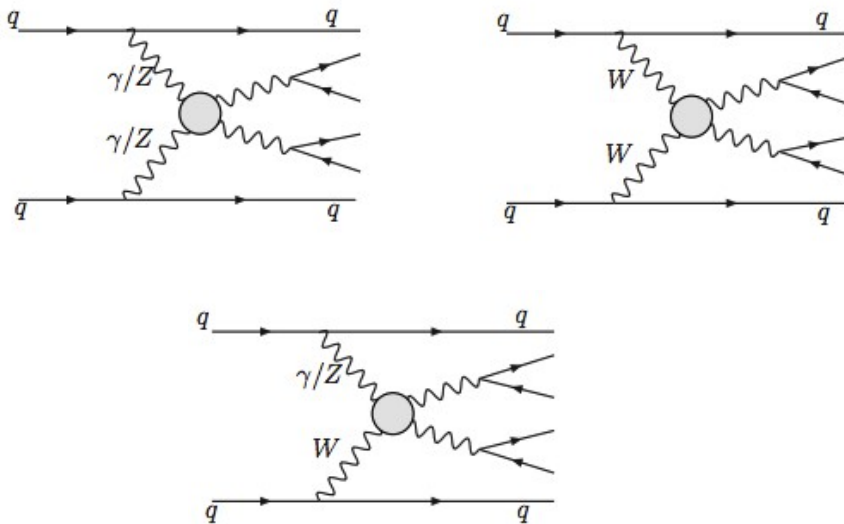
First step: scatter di-bosons

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We don't have (yet) the technology to collide WW bosons. But we can collide protons

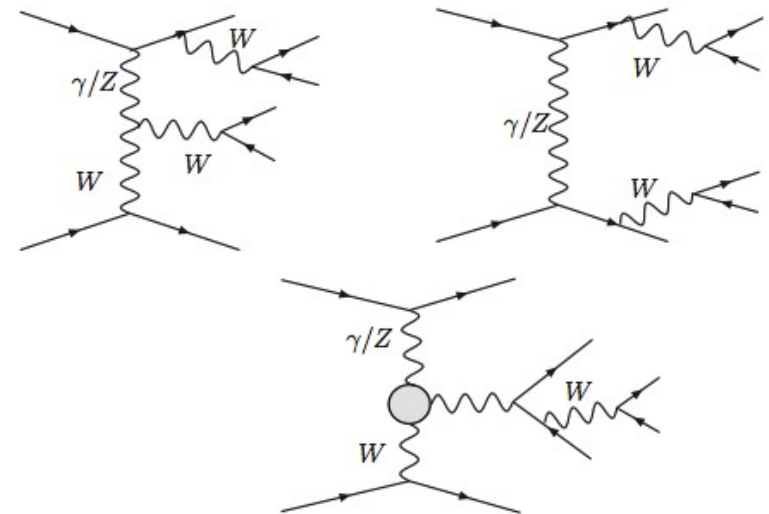
• Pros

- $s^{1/2}$ is not fixed – depends on the partons colliding → can probe the full spectrum
- VV fusion has distinctive signature



• Cons

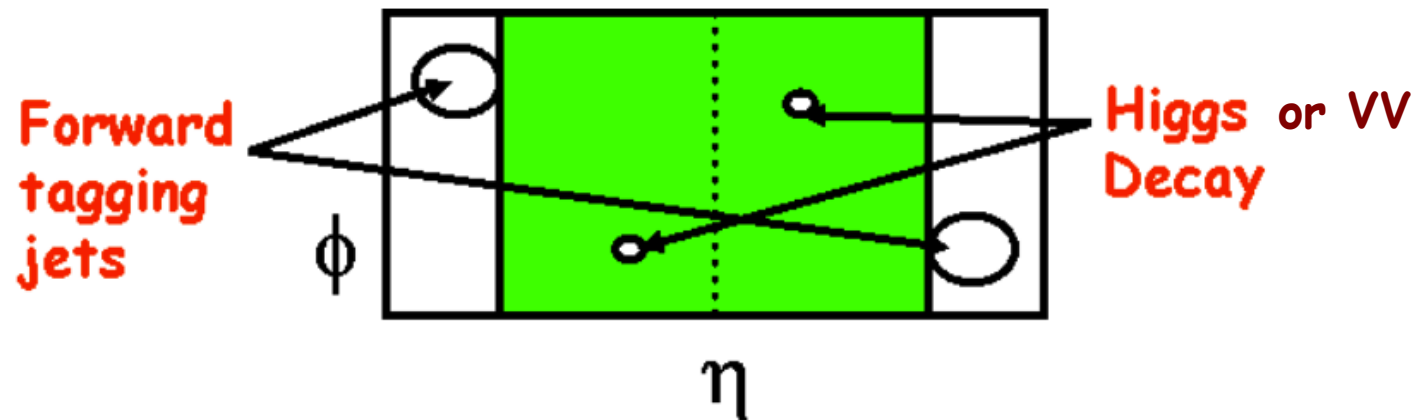
- It's a rare process: will take large luminosity acquired (typically $>50\text{fb}^{-1}$ at 14 TeV)
- Competes with non-VBF production



Signature for vector boson fusion

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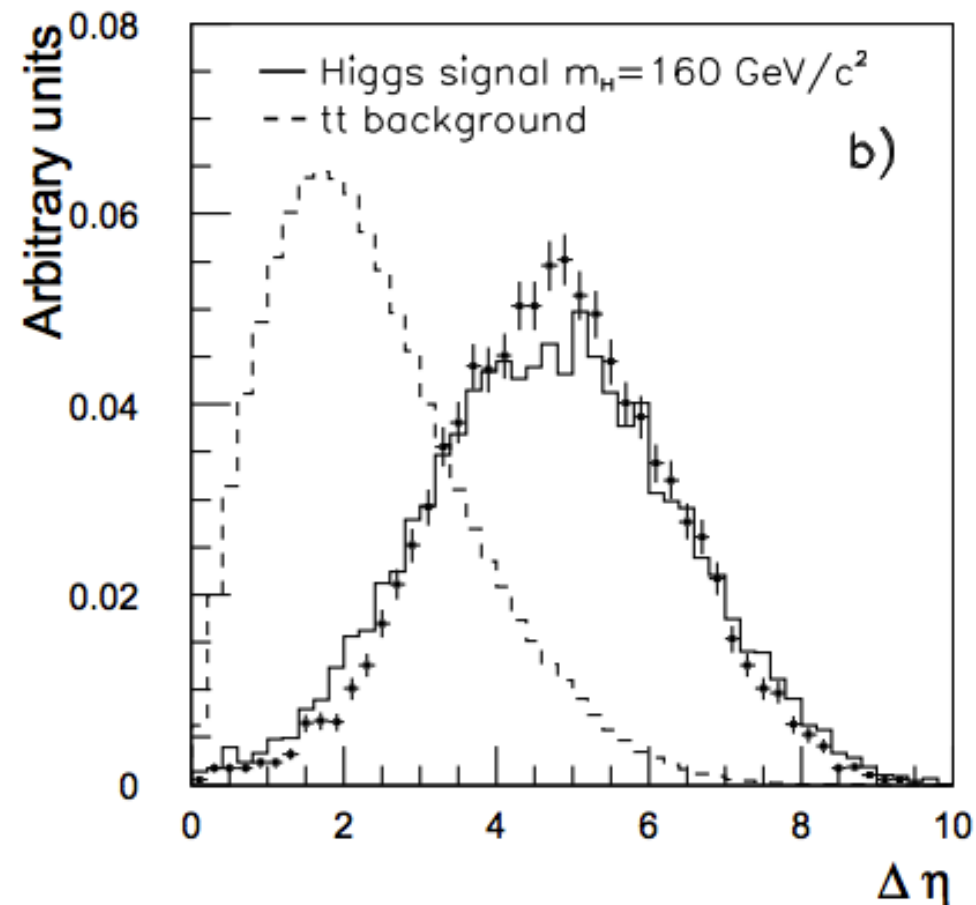
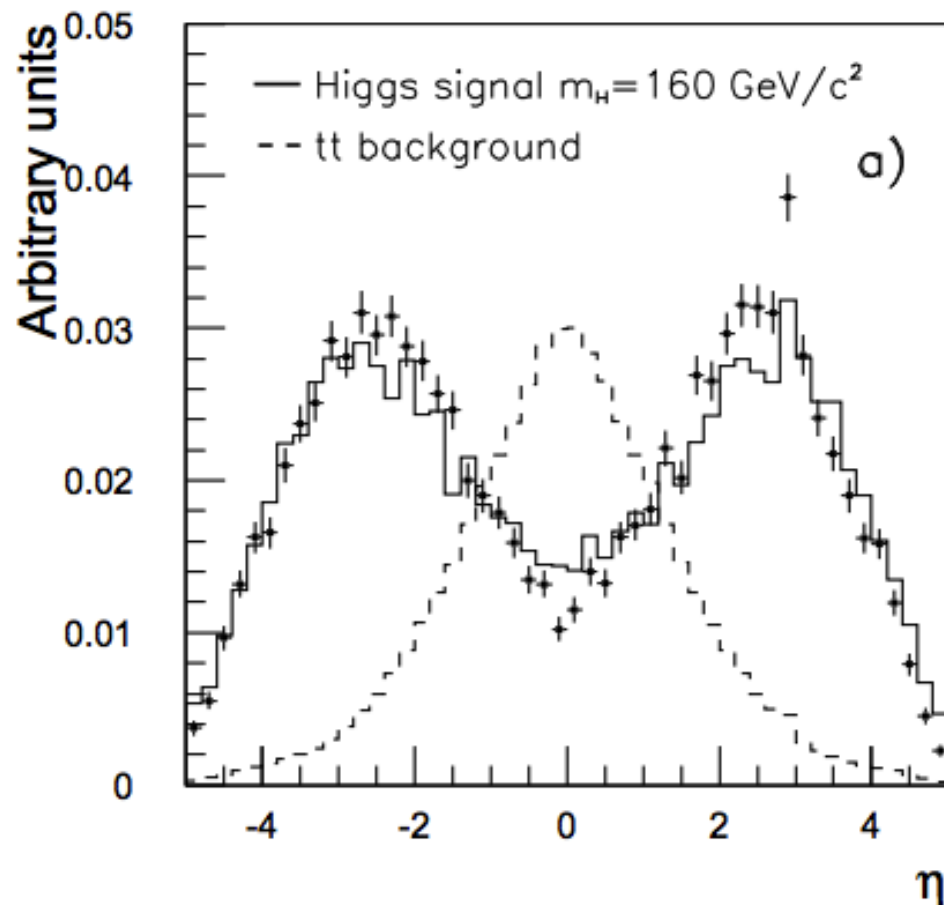
- We expect two high p_T jets with a large rapidity gap \rightarrow large M_{jj}
- These are called the VBF - tag jets



VBF tag jets

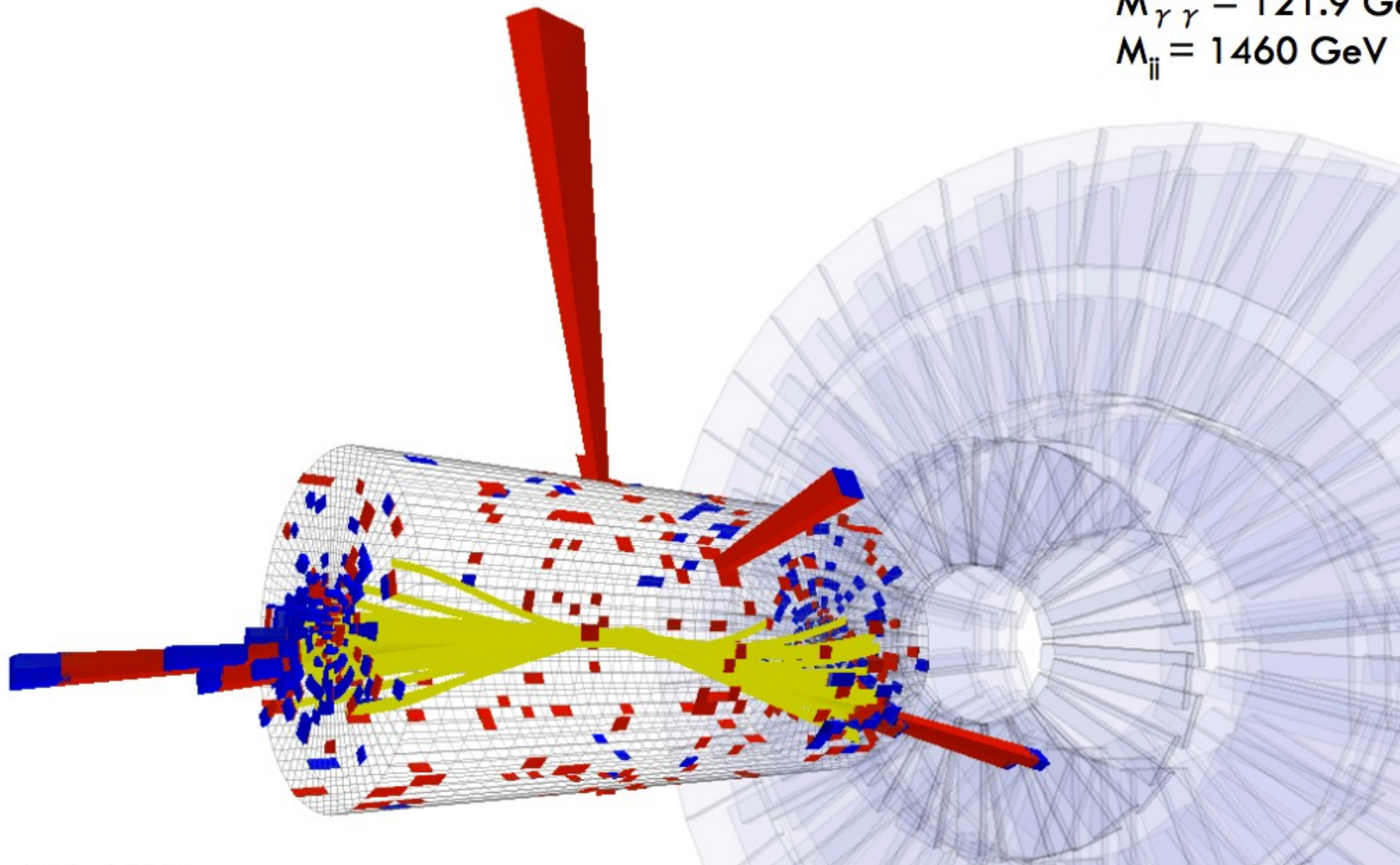
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- Found mostly at large η : region instrumented only by calorimeters, poorer resolution, prone to pileup contamination
- Rapidity gap is totally distinct from QCD production



Example in real data: $H \rightarrow \gamma\gamma$

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$M_{\gamma\gamma} = 121.9 \text{ GeV}$
 $M_{jj} = 1460 \text{ GeV}$

More on rapidity gap

- In the t-channel $Q^2=(p_f-p_i)^2$ is always negative
- Consequences on the vector boson propagator

$$\frac{-i}{k^2 - M^2} \left\{ g^{\mu\nu} - \frac{k^\mu k^\nu}{M^2} \right\}$$

→ is highly suppressed, except if $Q^2 \sim 0$

- In this limit:

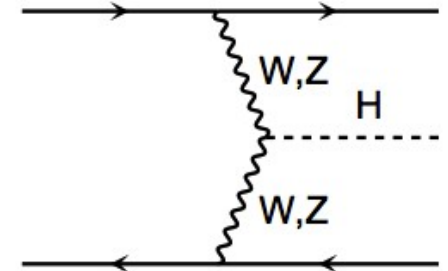
$$Q^2 = (p_f - p_i)^2 = E_q^2 \cdot (1 - x) \cdot \theta$$

Energy of
the quark

Fraction
taken by the
V boson

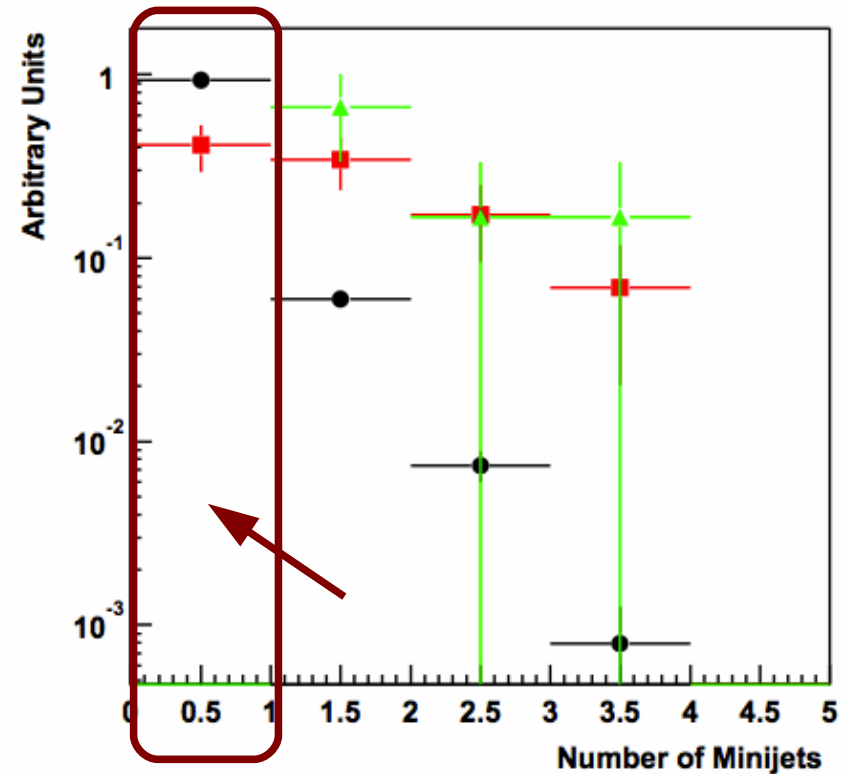
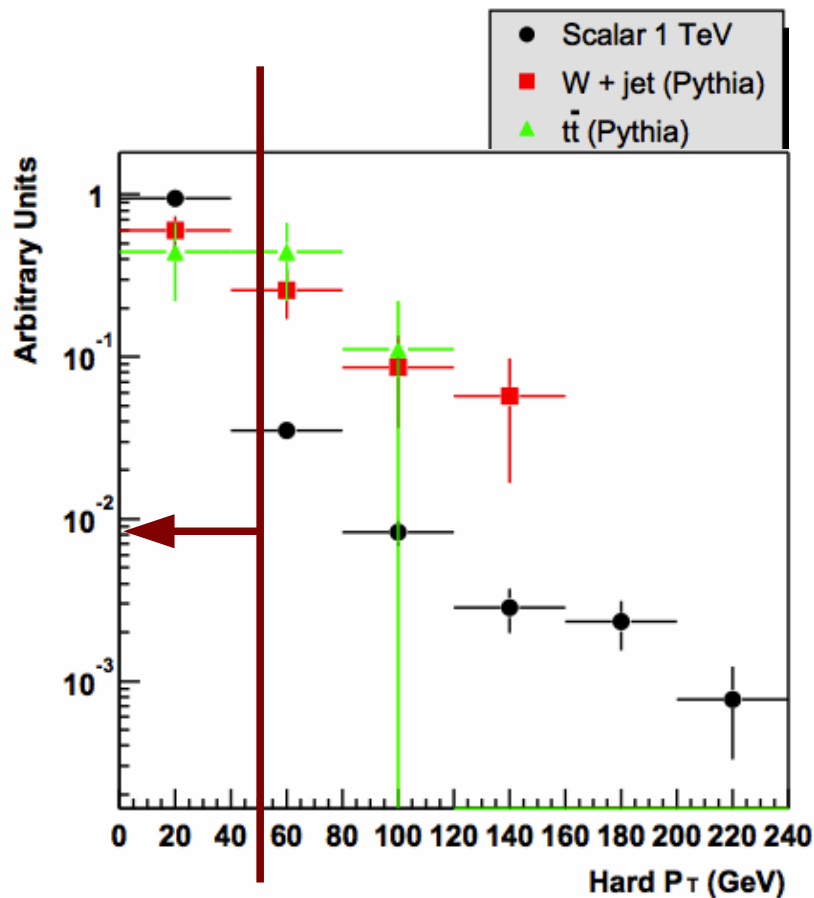
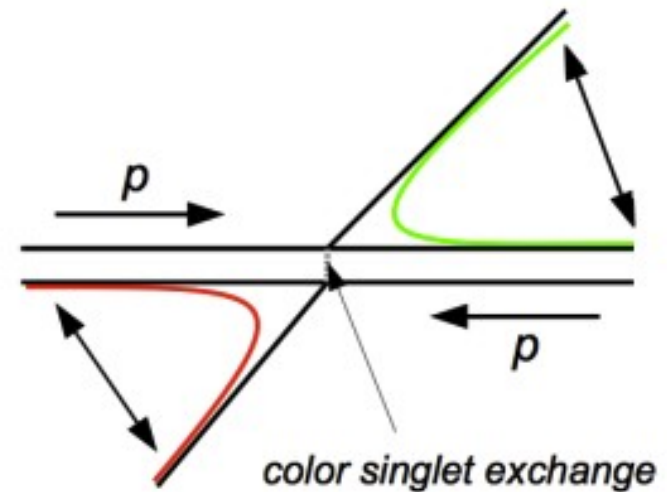
Scattering
angle

θ is necessarily small leading to large rapidities of the tag jets



More on rapidity gap

- Scattering of approx. collinear partons leads to **well balanced event**
- Due to EWK nature of the interaction **no hadronic activity is expected in the central region**



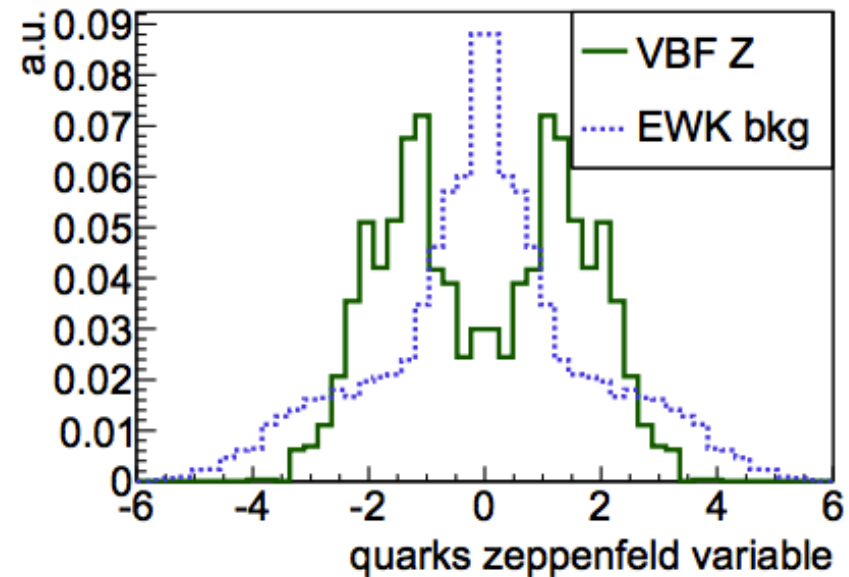
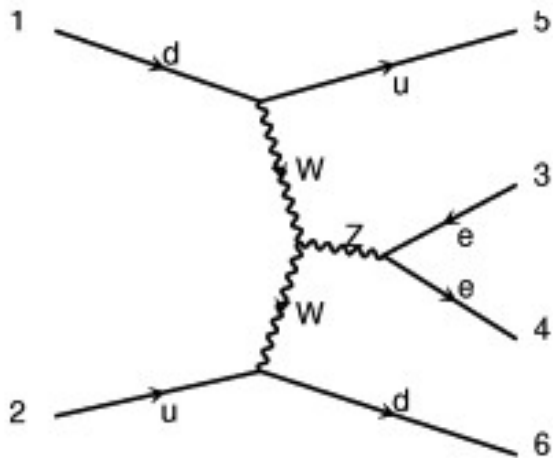
The Zeppenfeld variable

- Another distinctive variable is defined as:

$$z_i^* = \frac{z_i}{\Delta\eta} = \frac{\eta_i - \langle\eta\rangle}{\Delta\eta}$$

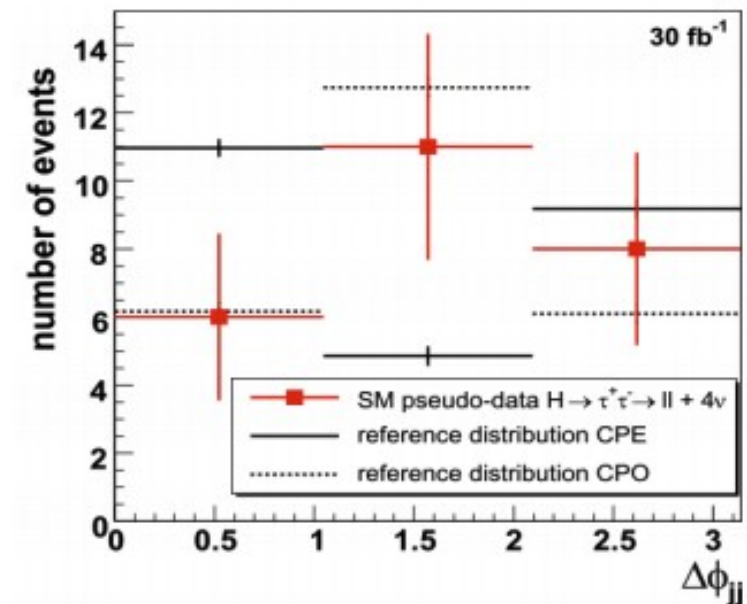
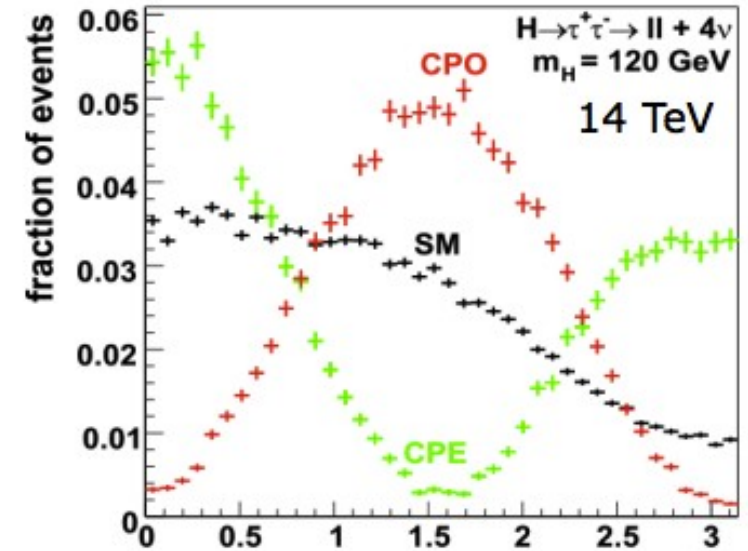
it translates and measures the rapidity relatively

to the reference defined by the two tag jets



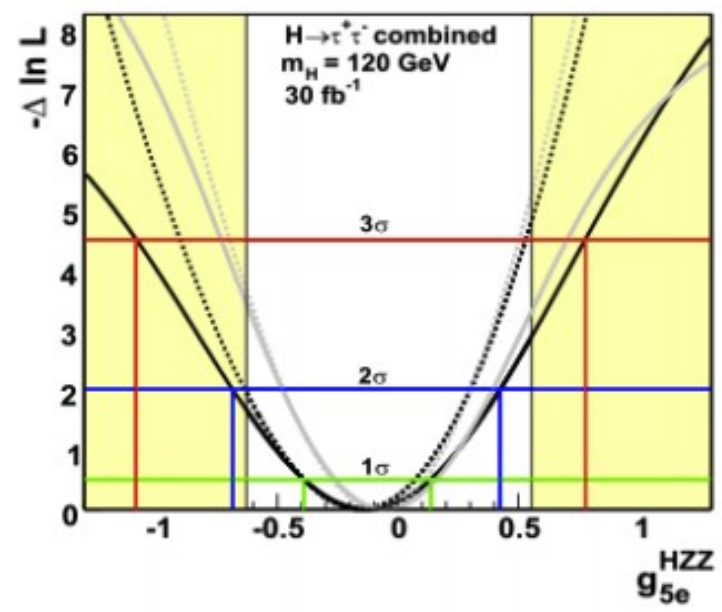
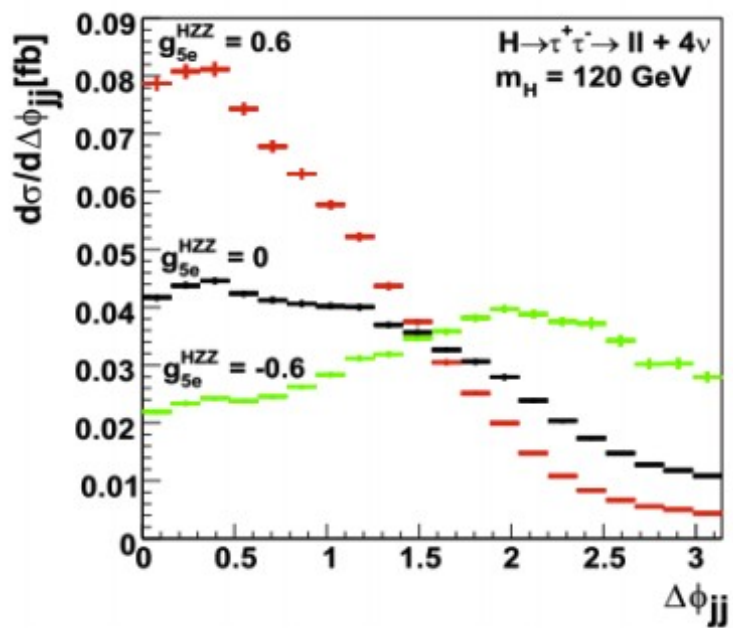
Resonance properties from VBF tags

- The azimuthal angle between the tag jets carries a distinctive hallmark
 - Can be used to probe anomalous couplings
- (Notice the integrated luminosity, and E_{cm} considered)



integrated luminosity, hypothesis tested		probability for		median	
		$> 5\sigma$	$< 5\%$	χ^2 -prob.	dev. in σ
$H \rightarrow W^+W^- \rightarrow ll\nu\nu$					
10 fb^{-1}	CPE	59%	100%	1.3×10^{-7}	5.3σ
	CPO	35%	98%	6.0×10^{-6}	4.5σ
30 fb^{-1}	CPE	100%	100%	-	-
	CPO	100%	100%	-	-
$H \rightarrow \tau^+\tau^-$ combined					
30 fb^{-1}	CPE	2%	68%	1.2×10^{-2}	2.5σ
	CPO	0%	52%	4.3×10^{-2}	2.0σ

Resonance properties from VBF tags – cont.



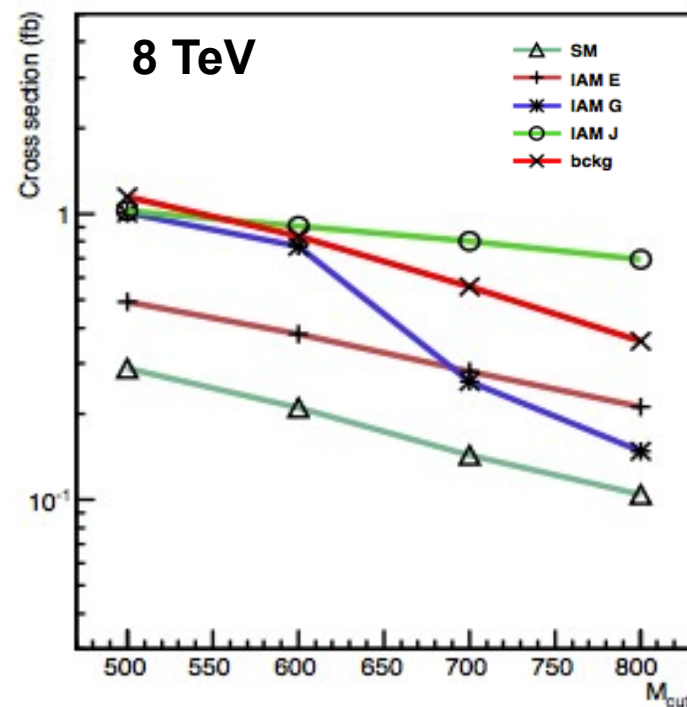
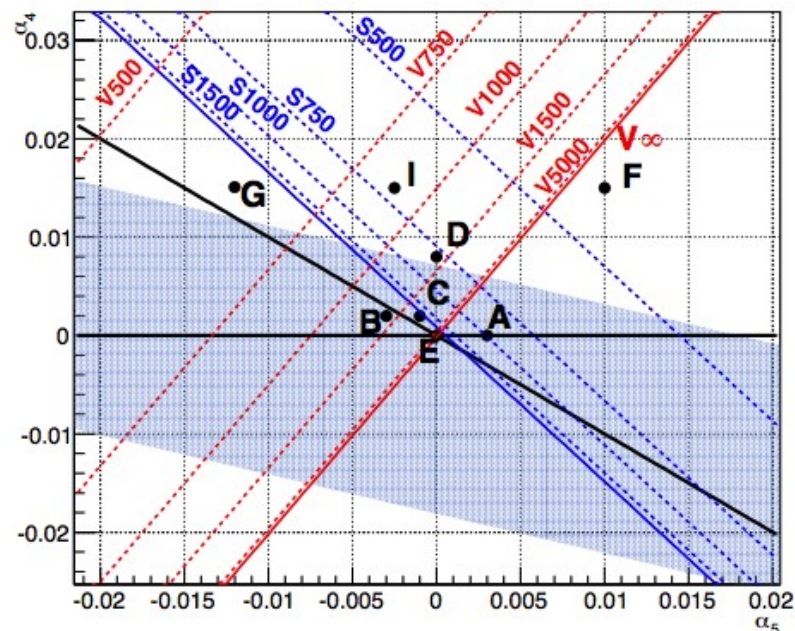
background included:

		minimum $-\Delta \ln L$	1σ interval	2σ interval	3σ interval	σ estimate
$H \rightarrow W^+W^- \rightarrow ll\nu\nu$	10 fb^{-1} non-extended	-0.09	[-0.30, 0.11]	[-0.50, 0.31]	[-0.73, 0.54]	0.20
	extended	-0.07	[-0.26, 0.12]	[-0.44, 0.31]	[-0.64, 0.51]	0.19
30 fb^{-1}	non-extended	-0.11	[-0.22, 0.00]	[-0.34, 0.12]	[-0.45, 0.23]	0.11
	extended	-0.10	[-0.21, 0.01]	[-0.31, 0.12]	[-0.42, 0.23]	0.11
$H \rightarrow \tau^+\tau^- \rightarrow ll + 4\nu$	30 fb^{-1} non-extended	-0.25	[-0.64, 0.12]	[-1.23, 0.53]	-	0.38
	extended	-0.25	[-0.59, 0.07]	[-0.97, 0.40]	[-1.38, 0.74]	0.33
$H \rightarrow \tau^+\tau^-$ combined	30 fb^{-1} non-extended	-0.13	[-0.40, 0.13]	[-0.69, 0.42]	[-1.08, 0.78]	0.27
	extended	-0.16	[-0.40, 0.06]	[-0.64, 0.40]	[-0.90, 0.53]	0.23

Looking forward for high $s^{1/2}$

- Search for VV scattering at high $s^{1/2}$ has to combine different channels to gain in sensitivity
- Example from Ballestrero et al (arXiv:1203.2771) (in the following IAM – Inverse Amplitude Method is equivalent to the Padé protocol)
- Cuts for: $lv+4j$ / $2l2v+2j$ / $3lv+2j$ final states

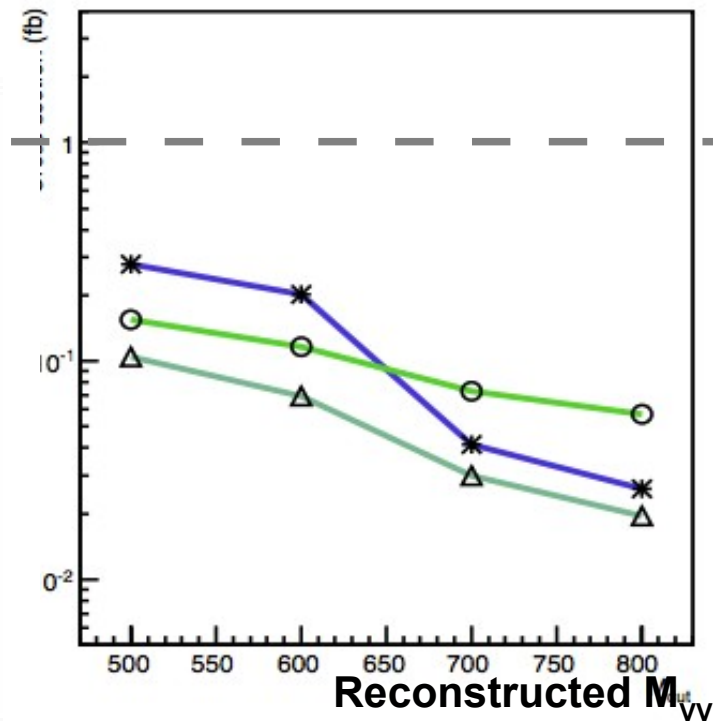
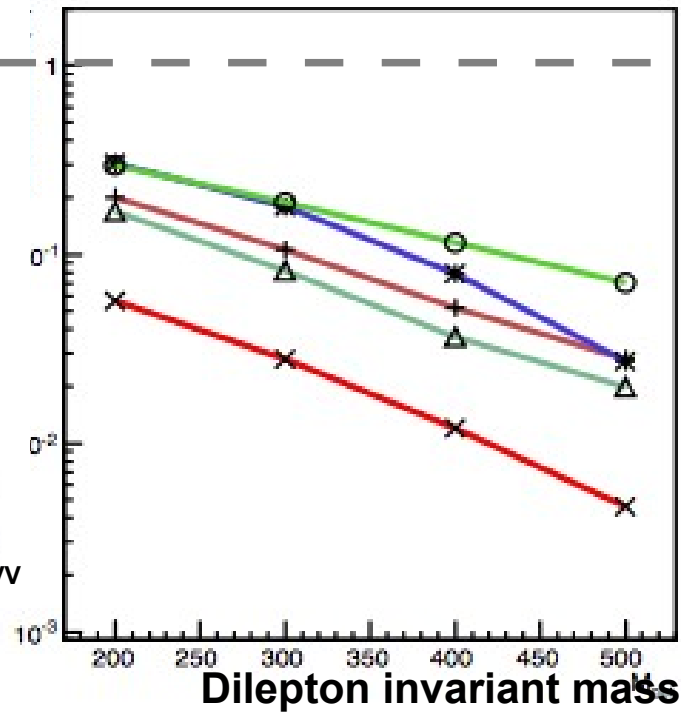
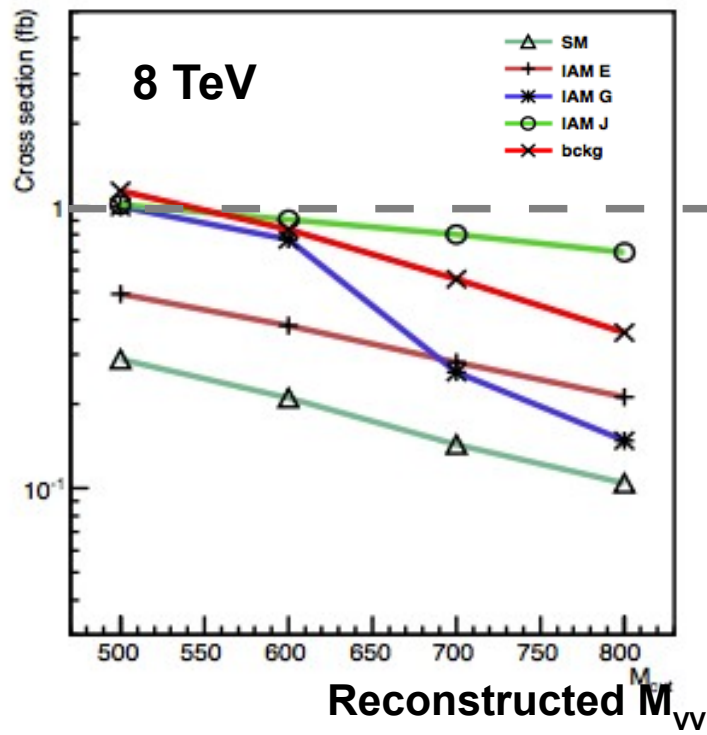
$p_T(j) > 30$ GeV	$p_T(\ell) > 70/70/20$ GeV
$p_T^{miss} > 70/20/20$ GeV	$p_T(j_c) > 70$ GeV
$\eta(j) < 6.5$	$\eta(\ell) < 2/2/3$
$\Delta\eta(j_f j_b) > 4/4/3$	$\Delta\eta(V_{rec} j) > 0.6$
$\Delta R(jj) > 0.3$	$M(\ell\ell) > 20$ GeV
$M(jj) > 60$ GeV	$M(j_f j_b) > 700/600/100$ GeV
$p_T(V_{rec}) > 70/100$ GeV	$ M(V_{rec} j) - M_{TOP} > 15$ GeV
$M(j\ell) > 180$ GeV	$ p_T(\ell^+) - p_T(\ell^-) > 100$ GeV



... and for high luminosity

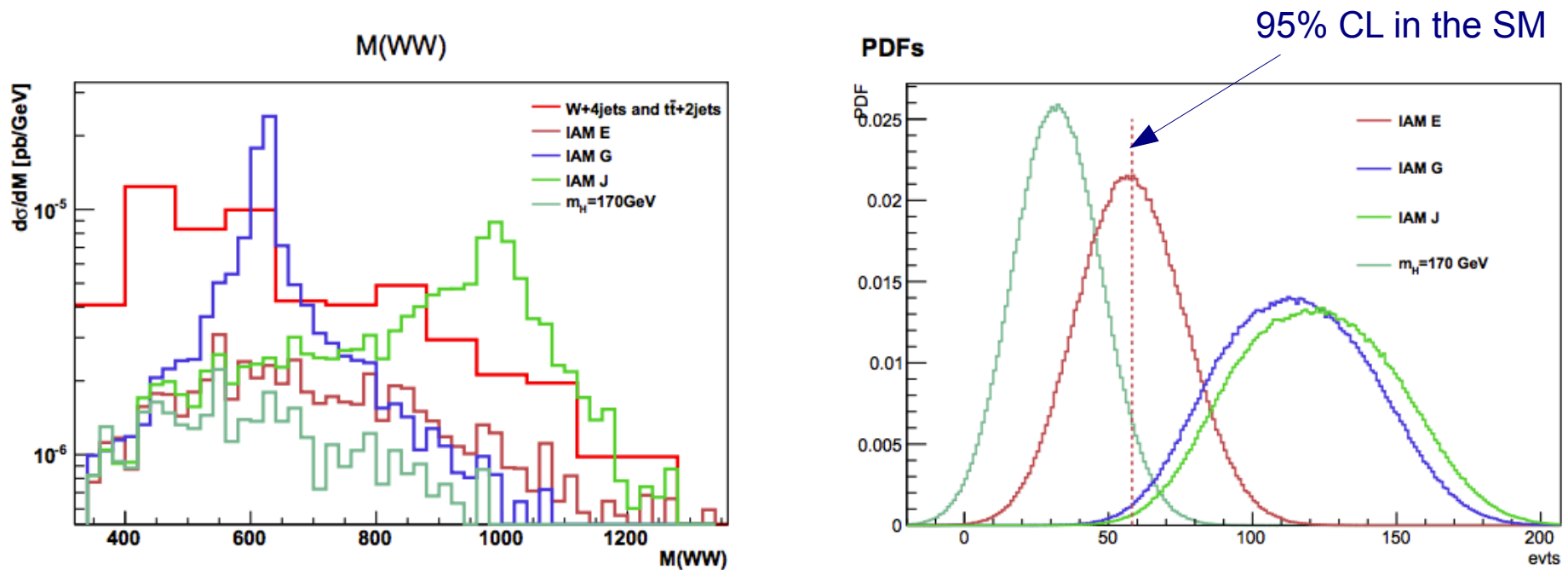
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- After the selection cuts we're expecting to select ~ 5 event / 10 fb^{-1}



Expected mass distributions

- The expected spectrum (right) and the probability to observe a given number of events with $M_{VV} > 500 \text{ GeV}/c^2$ for $L = 50 \text{ fb}^{-1}$



- Within the reach of the LHC experiments after the upgrade: with this year's data we can at most exercise these searches

Probability BSM @ 95% CL

	IAM E			IAM G			IAM J		
L\E	7	8	10	7	8	10	7	8	10
25	16.06 ^a	19.03 ^a	35.37 ^b	71.10 ^a	75.48 ^a	93.80 ^a	73.32 ^d	81.77 ^d	99.32 ^d
50	22.70 ^a	27.88 ^a	51.56 ^b	89.14 ^a	91.68 ^a	99.12 ^a	91.55 ^d	95.62 ^d	99.99 ^d
100	33.51 ^a	41.08 ^a	69.28 ^c	97.85 ^a	98.54 ^a	99.97 ^a	98.89 ^d	99.66 ^e	100 ^d
200	48.25 ^b	57.08 ^a	83.44 ^c	99.87 ^a	99.93 ^a	100 ^a	99.97 ^d	100 ^d	100 ^d

Table 2. PBSM@95%CL in the $l\nu + 4$ jets channel with 25, 50, 100 and 200 fb^{-1} of integrated luminosity, L. For each luminosity and model we have used the mass cut which gives the best probability. They are specified by the superscript according to the following scheme: ^a, ^b, ^c, ^d, ^e for 500, 600, 700, 800, 900 GeV respectively

	IAM E			IAM G			IAM J		
L\E	7	8	10	7	8	10	7	8	10
25	8.47 ^a	10.44 ^b	14.23 ^a	24.41 ^a	36.49 ^a	51.83 ^a	27.17 ^b	42.69 ^b	65.68 ^a
50	10.02 ^a	13.06 ^b	18.94 ^a	35.83 ^a	53.23 ^a	70.07 ^a	37.90 ^b	61.95 ^b	84.73 ^b
100	12.63 ^a	17.34 ^b	26.37 ^b	52.81 ^a	72.07 ^a	84.59 ^a	56.76 ^b	81.94 ^b	95.97 ^b
200	16.49 ^a	24.08 ^b	36.35 ^b	71.87 ^a	86.74 ^a	93.23 ^a	76.92 ^b	94.91 ^b	99.50 ^b

Table 3. PBSM@95%CL in the $(WW)l\nu l\nu + 2j$ channel with 25, 50, 100 and 200 fb^{-1} of integrated luminosity, L. For each luminosity and model we have used the mass cut which gives the best probability. They are specified by the superscript according to the following scheme: ^a, ^b for 300, 400 GeV respectively.

Probability BSM @ 95% CL – cont.

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	IAM G			IAM J		
L\E	7	8	10	7	8	10
25	50.53 ^a	63.18 ^a	82.05 ^a	21.74 ^d	29.28 ^d	48.50 ^e
50	71.93 ^a	82.12 ^a	93.99 ^a	31.02 ^d	43.24 ^e	68.63 ^e
100	88.13 ^a	94.08 ^a	98.97 ^b	43.83 ^e	63.71 ^e	86.42 ^e
200	97.09 ^b	98.94 ^b	99.95 ^b	63.63 ^e	82.62 ^e	96.56 ^e

Table 4. PBSM@95%CL in the $3l\nu + 2$ jets channel with 25, 50, 100 and 200 fb^{-1} of integrated luminosity, L. For each luminosity and model we have used the mass cut which gives the best probability. They are specified by the superscript according to the following scheme: ^a, ^b, ^c, ^d, ^e for 500, 600, 700, 800, 900 GeV respectively

Same sign WW scattering

- Process has good separation for different scenarios

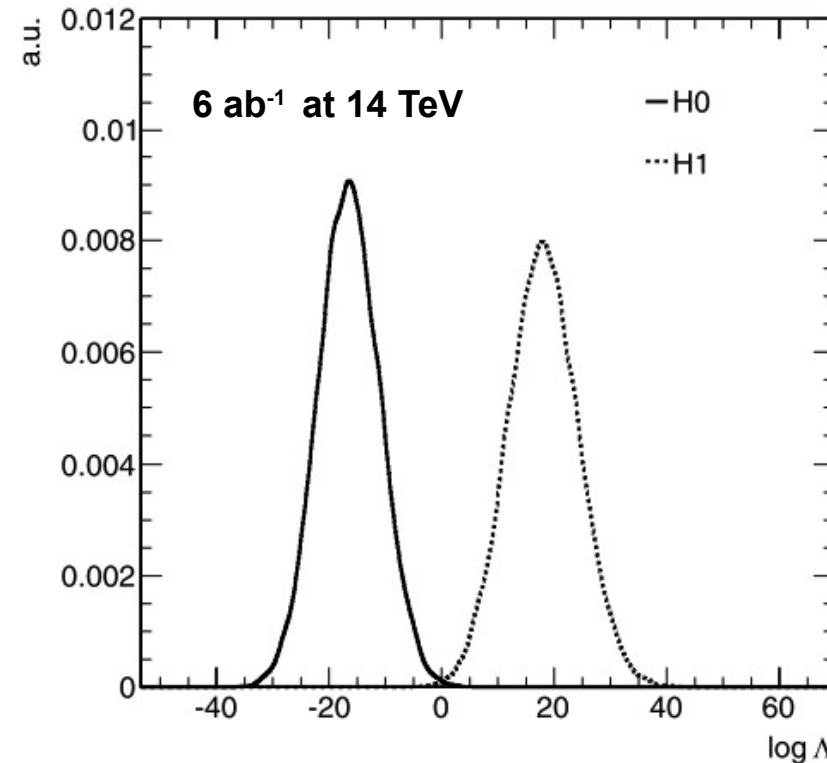
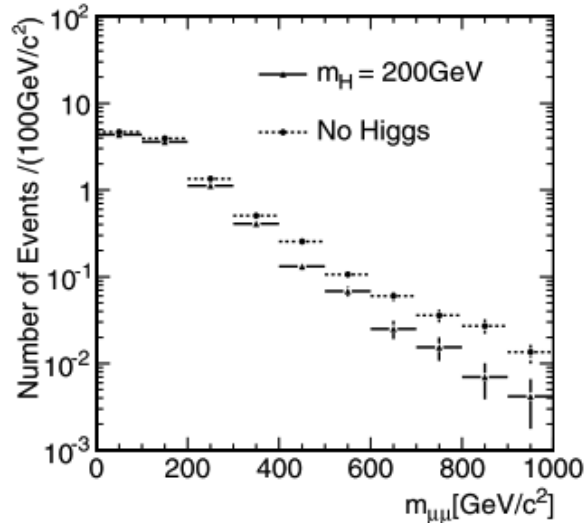
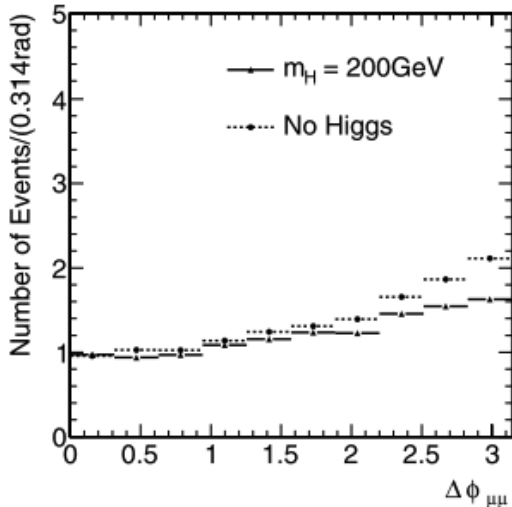
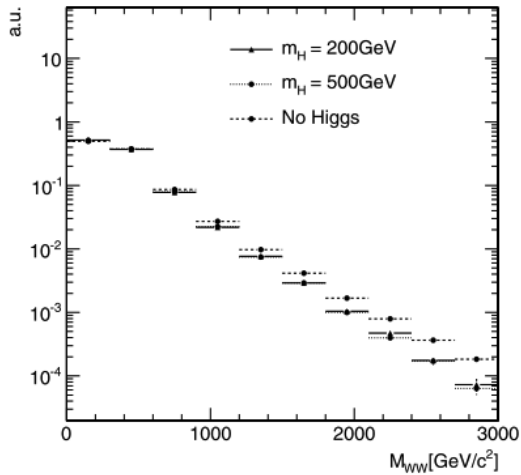
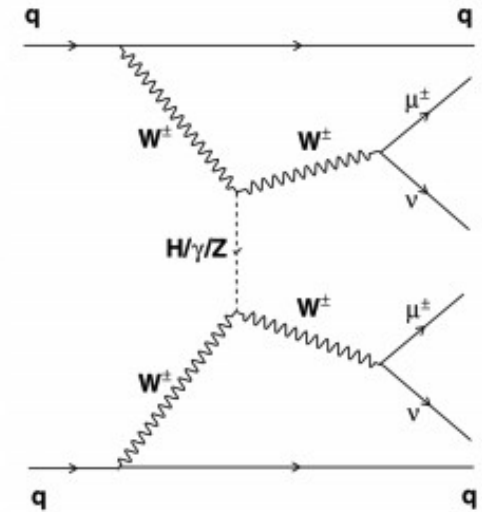
- Optimize selection from ratios:

$$\alpha = \frac{N_{\text{NoH}} - N_{m_H(200)}}{\sqrt{N_{m_H(200)} + N_{\text{Bkg}}}}$$

Discriminator	NoH	$m_H(200)$	NoH/ $m_H(200)$
$m_{\mu\mu}$	2.4 ± 0.1	1.8 ± 0.1	1.3 ± 0.1
$\Delta\phi_{\mu\mu}$	6.5 ± 0.1	5.4 ± 0.1	1.2 ± 0.1

Expect 1 (3.5) background

events after $m_{\mu\mu}$ ($\Delta\phi_{\mu\mu}$)



Conclusions

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- **VV scattering at high $s^{1/2}$ is a territory with many unknowns**
 - Unique probe of the EWSB mechanism
 - Requires both high energy beams and high luminosity
 - many possibilities to explore
- **Can start to exercise (rule out some models) already this year**
 - EWKchL unitarized via two protocols: Padé or N/D
 - lead to **resonance or continuum predictions for the VV invariant mass spectrum**
 - combine different channels: expect sensitivity to part of phase space with $\sim 20\text{fb}^{-1}$ and 8 TeV
- Not covered today (but can be looked up in Michele's presentation)
 - Usage of boosted topologies (jet substructure) to reconstruct boosted W/Z \rightarrow qq

End of Lecture III on Higgs Physics

References

- Stefanidis, E., *Study of the WW scattering in the absence of light Higgs boson using the ATLAS Detector at LHC*, PhD Thesis 2007
- Rainwater, D. “*Searching for the Higgs boson*”, arXiv:hep-ph/0702124
- Gao, Y et al, “Spin determination of single-produced resonances at hadron colliders”, arXiv:1001.3396
- CMS Collaboration, “*Search for a narrow spin-2 resonance decaying to Z vector bosons in the semileptonic final state*”, CMS PAS EXO-11-102
- **Ballestrero, A., “*Exploring alternative symmetry breaking mechanisms at the LHC with 7, 8 and 10 TeV total energy*” , ,arXiv:1203.2771**