

# Anisotropic Flow at RHIC and at the LHC

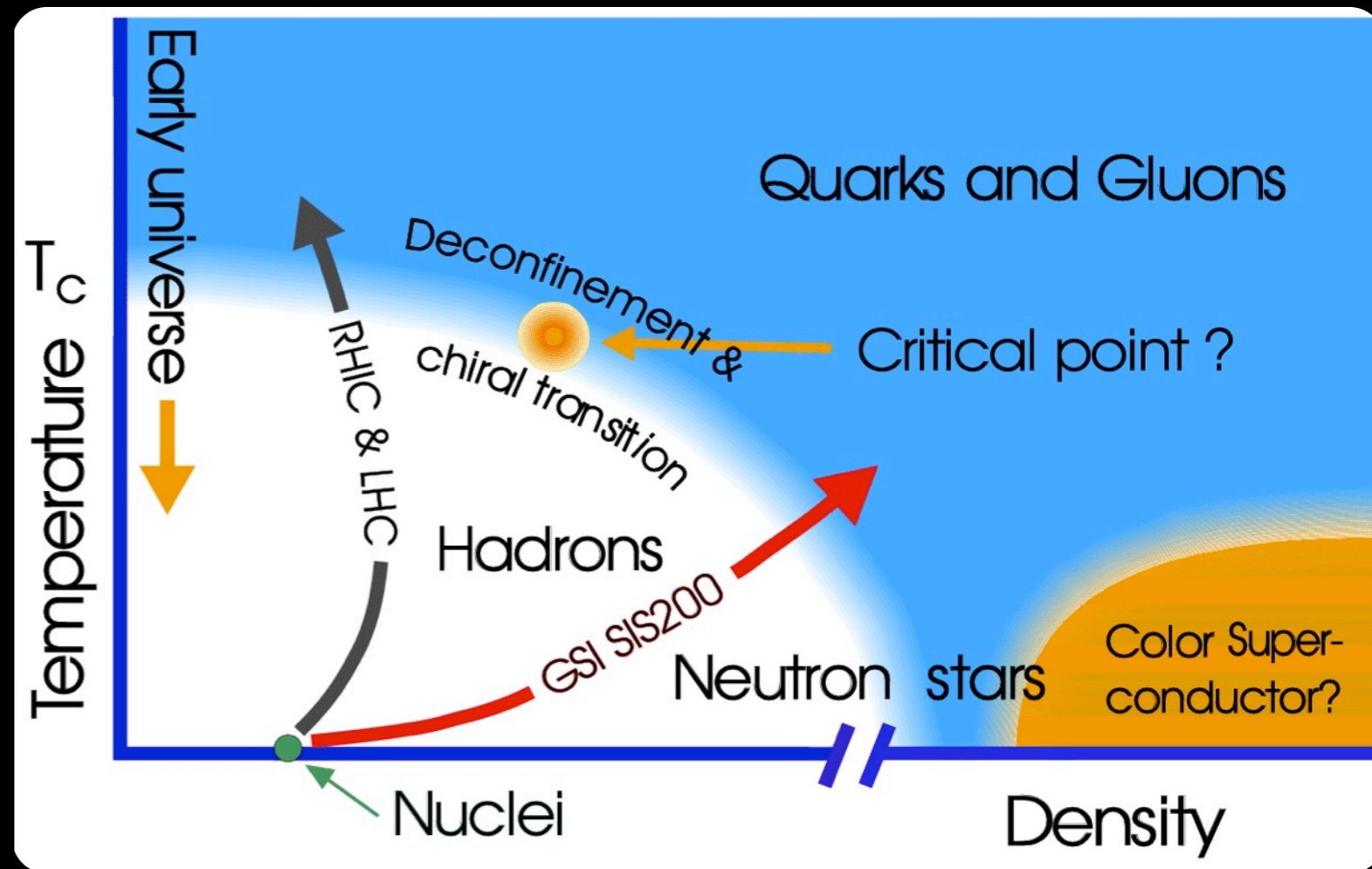
ICFP Kolymbari, Crete 2012

Raimond Snellings  
Utrecht University



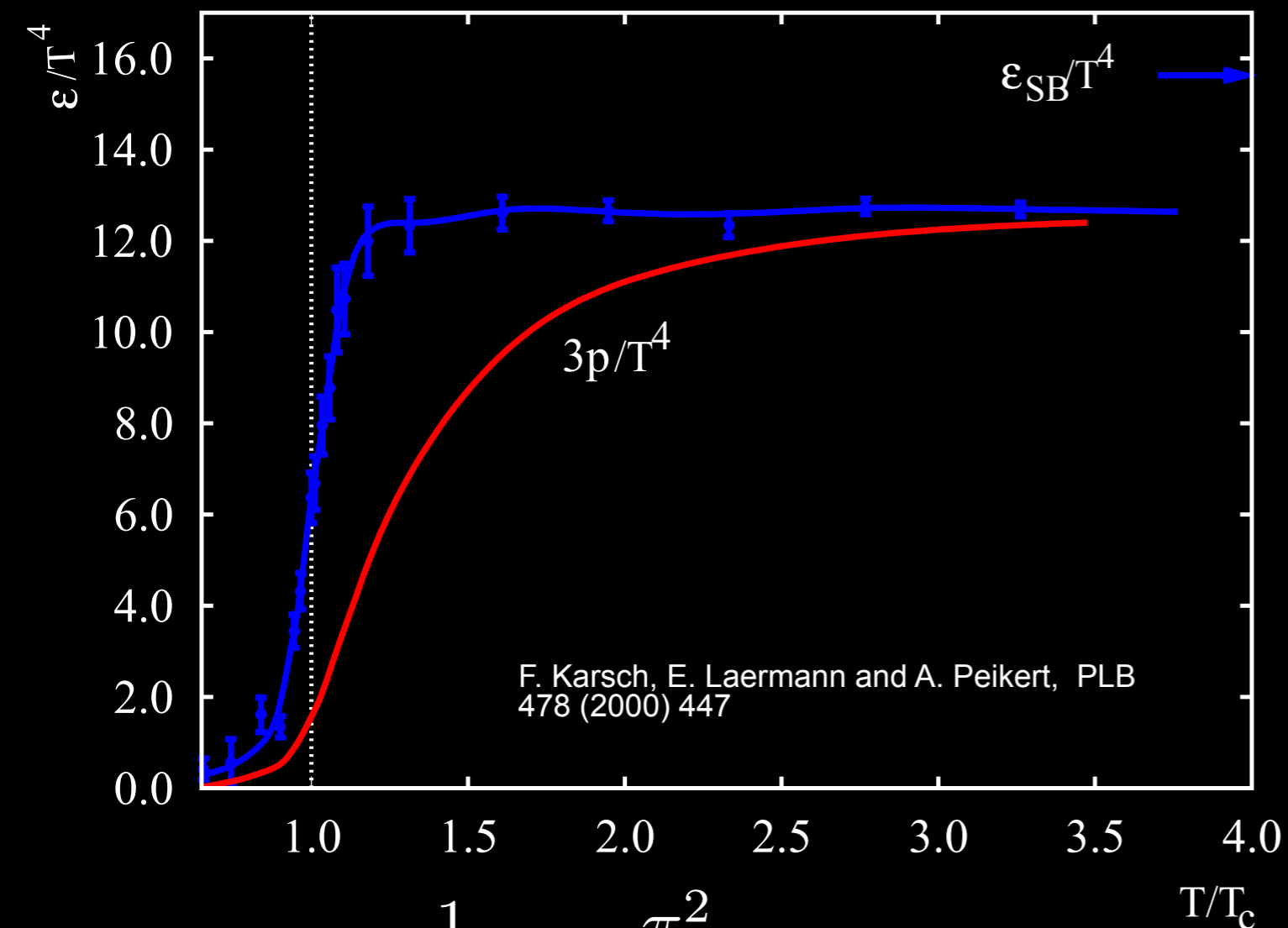
# What happens when you heat and compress matter to very high temperatures and densities?

This talk focusses on what we learned at RHIC and the LHC from anisotropic flow



high- $p_t$  physics in the next talk of B. Wyslouch

# QCD on the Lattice



$$T_c \sim 170 \pm 20 \text{ MeV}, \quad \epsilon_c \sim 0.6 \text{ GeV/fm}^3$$

at the critical temperature a strong increase in the degrees of freedom

✓ gluons, quarks & color!

at the phase transition  $dp/d\epsilon$  decreases rapidly

not an ideal massless gas!

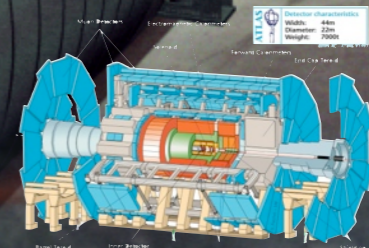
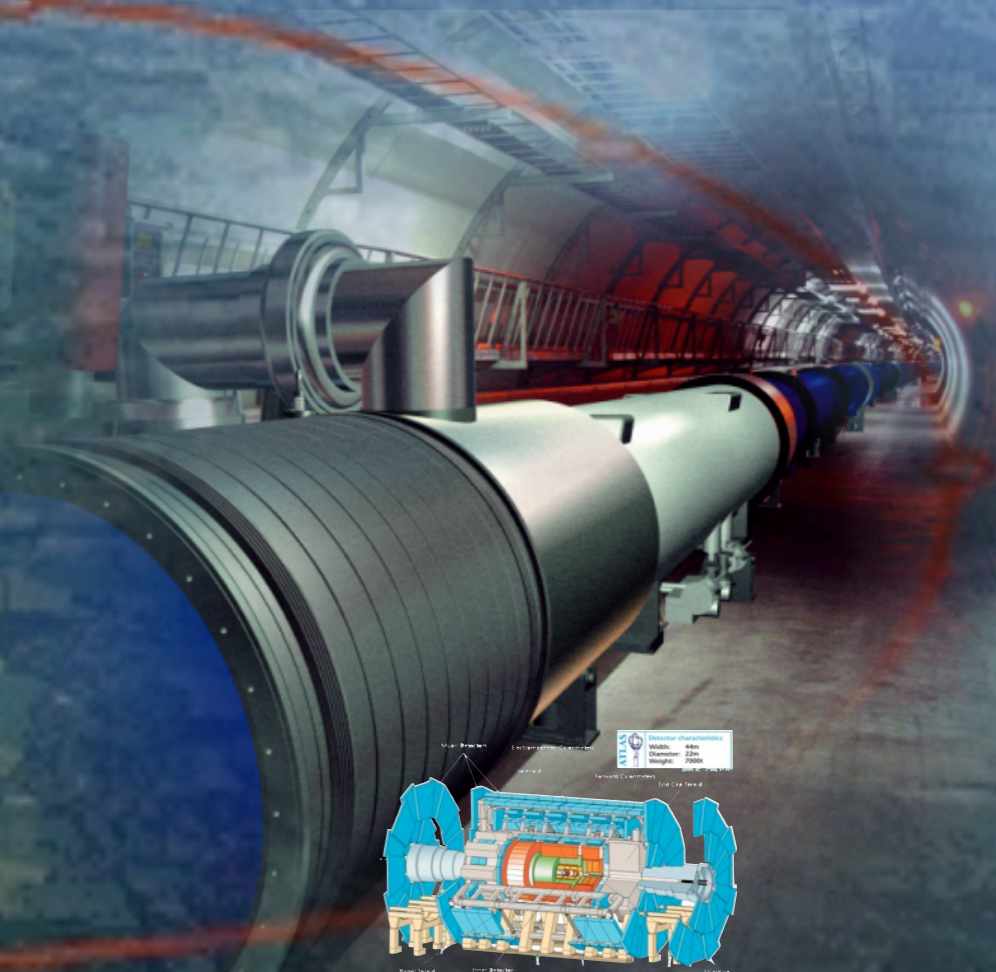
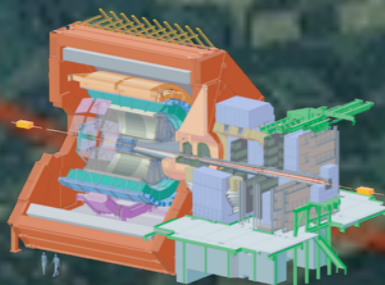
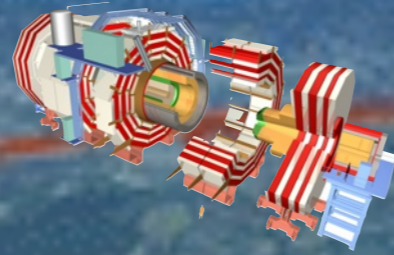
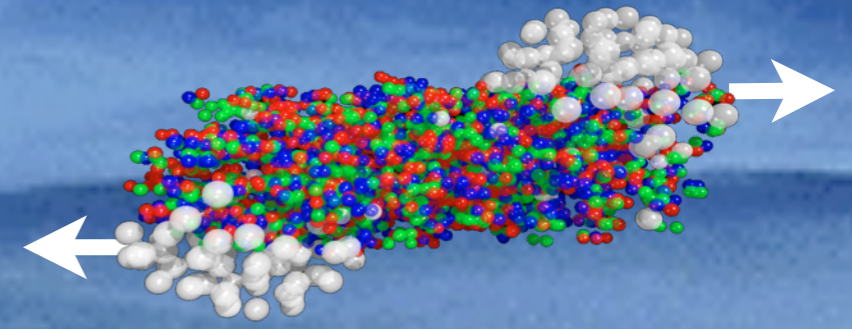
what are the transport properties?

$$p = \frac{1}{3}\epsilon = g \frac{\pi^2}{90} T^4$$

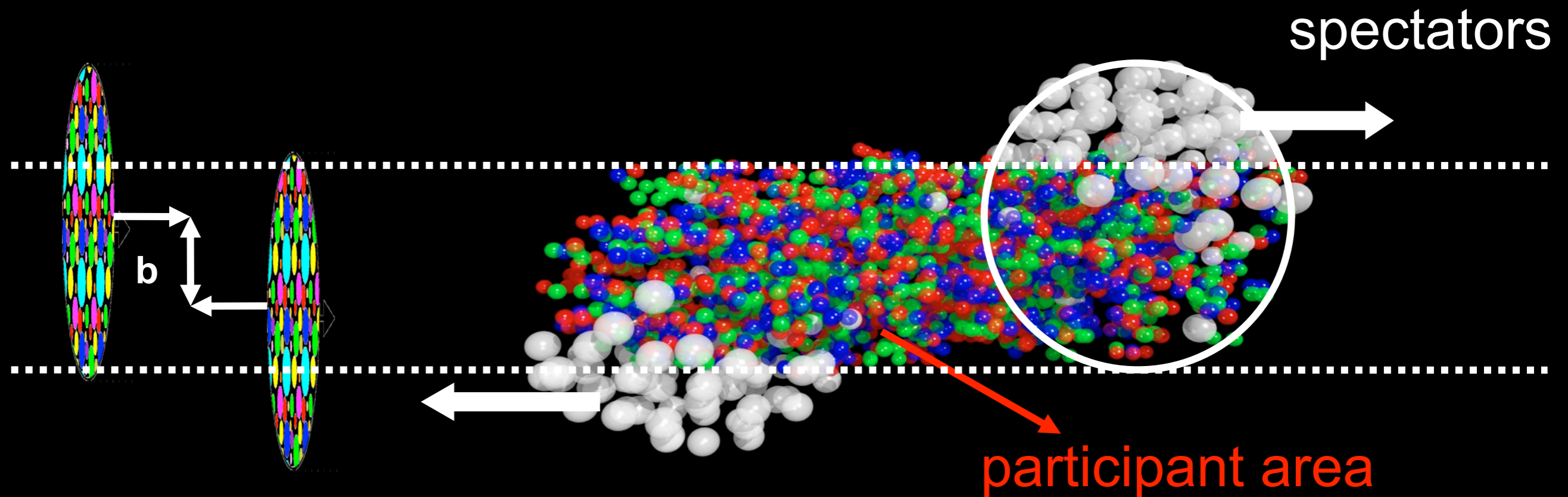
$$g_H \approx 3 \quad g_{\text{QGP}} \approx 37$$

$$g = 2_{\text{spin}} \times 8_{\text{gluons}} + \frac{7}{8} \times 2_{\text{flavors}} \times 2_{q\bar{q}} \times 2_{\text{spin}} \times 3_{\text{color}}$$

# study phase transition in controlled lab conditions by colliding heavy-ions

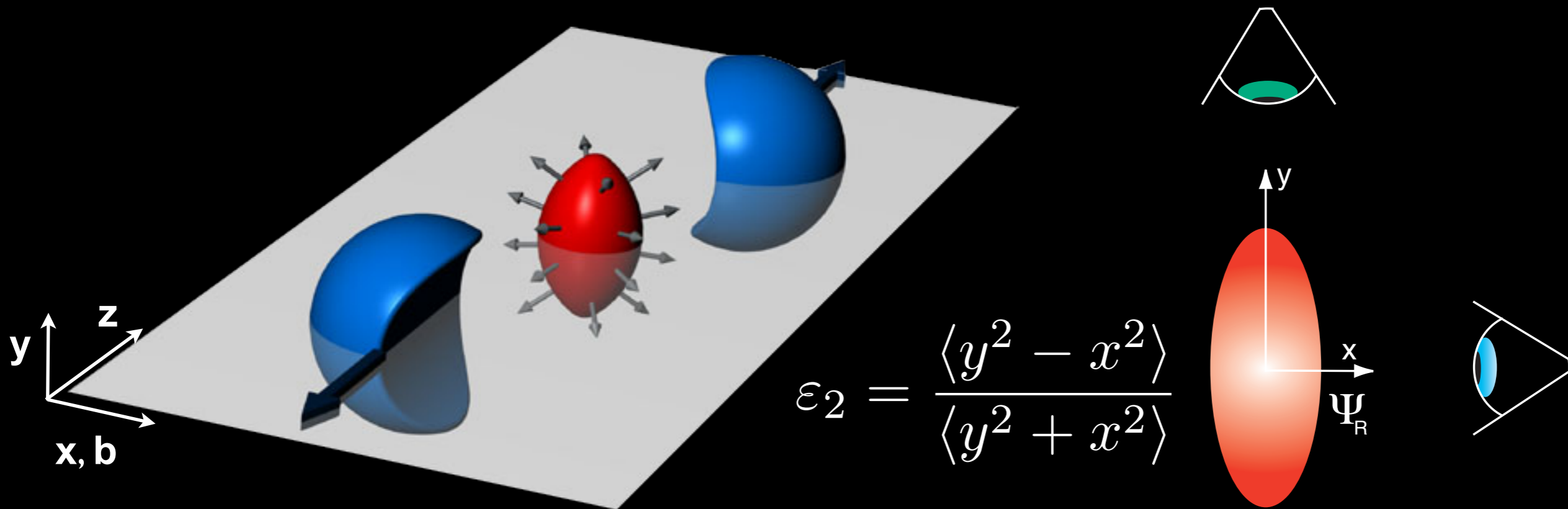


# Collision Centrality



very hot and dense nuclear matter in more central collisions while we approach “simple” nucleon-nucleon collisions in very peripheral collisions

# The Reaction Plane



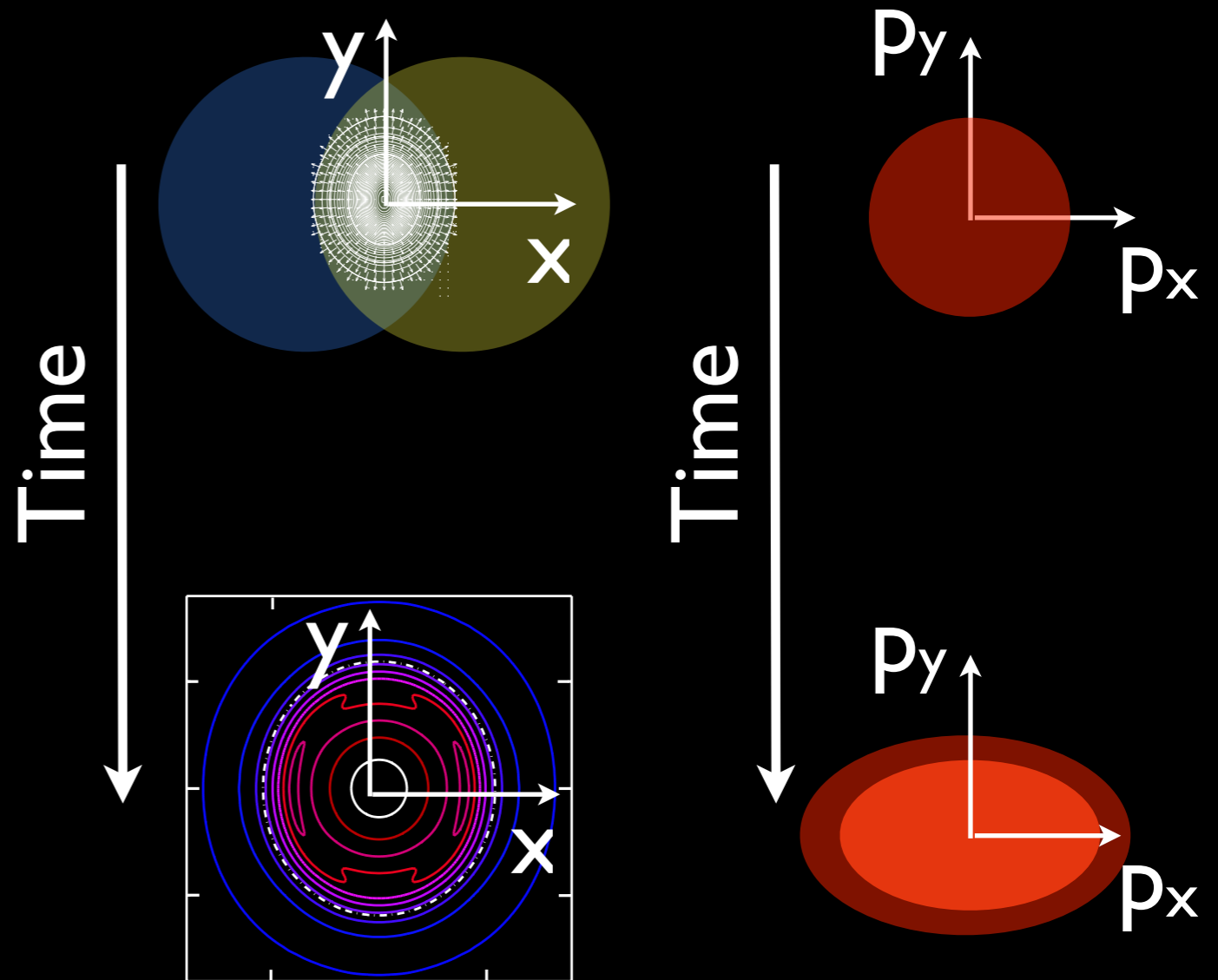
in non-central collisions the participant area is not azimuthally symmetric

# Elliptic Flow

$$\varepsilon = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$

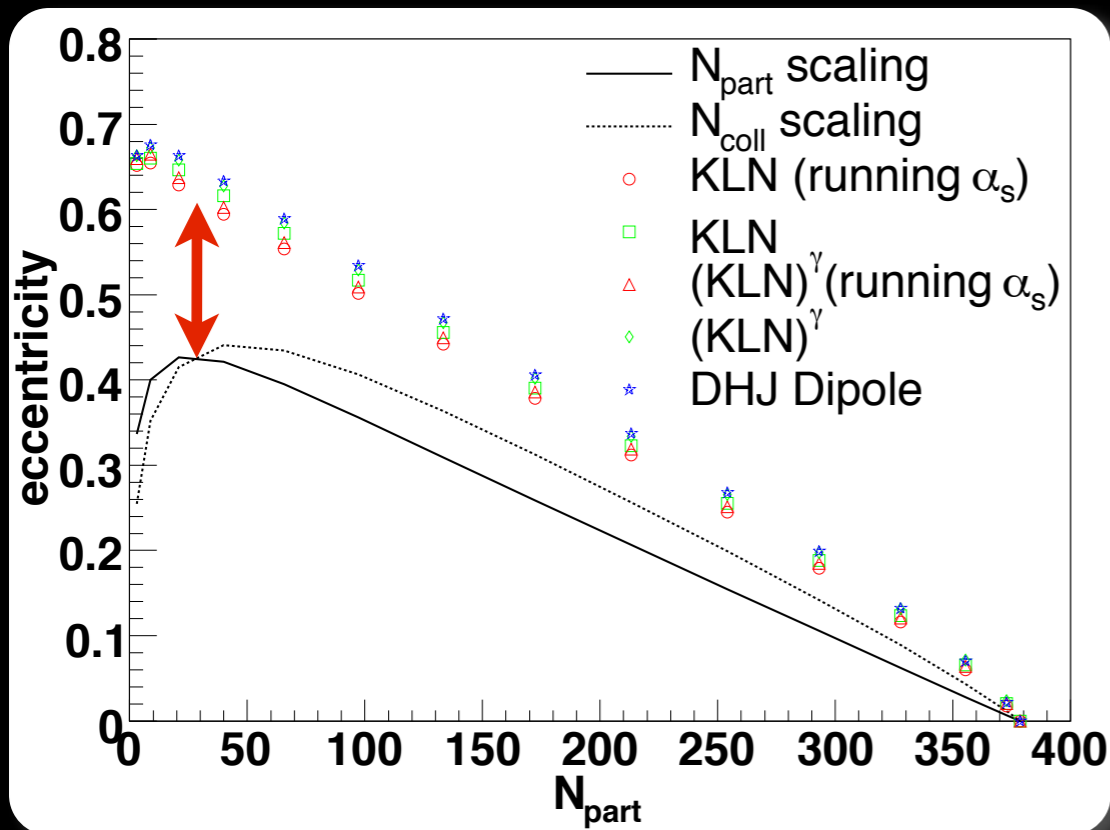
$$v_2 = \langle \cos 2\phi \rangle$$

- in non central collisions coordinate space configuration is anisotropic (almond shape). However, initial momentum distribution isotropic (spherically symmetric)
- interactions among constituents generate a pressure gradient which transforms the initial coordinate space anisotropy into the observed momentum space anisotropy  $\rightarrow$  anisotropic flow
- self-quenching  $\rightarrow$  sensitive to early stage

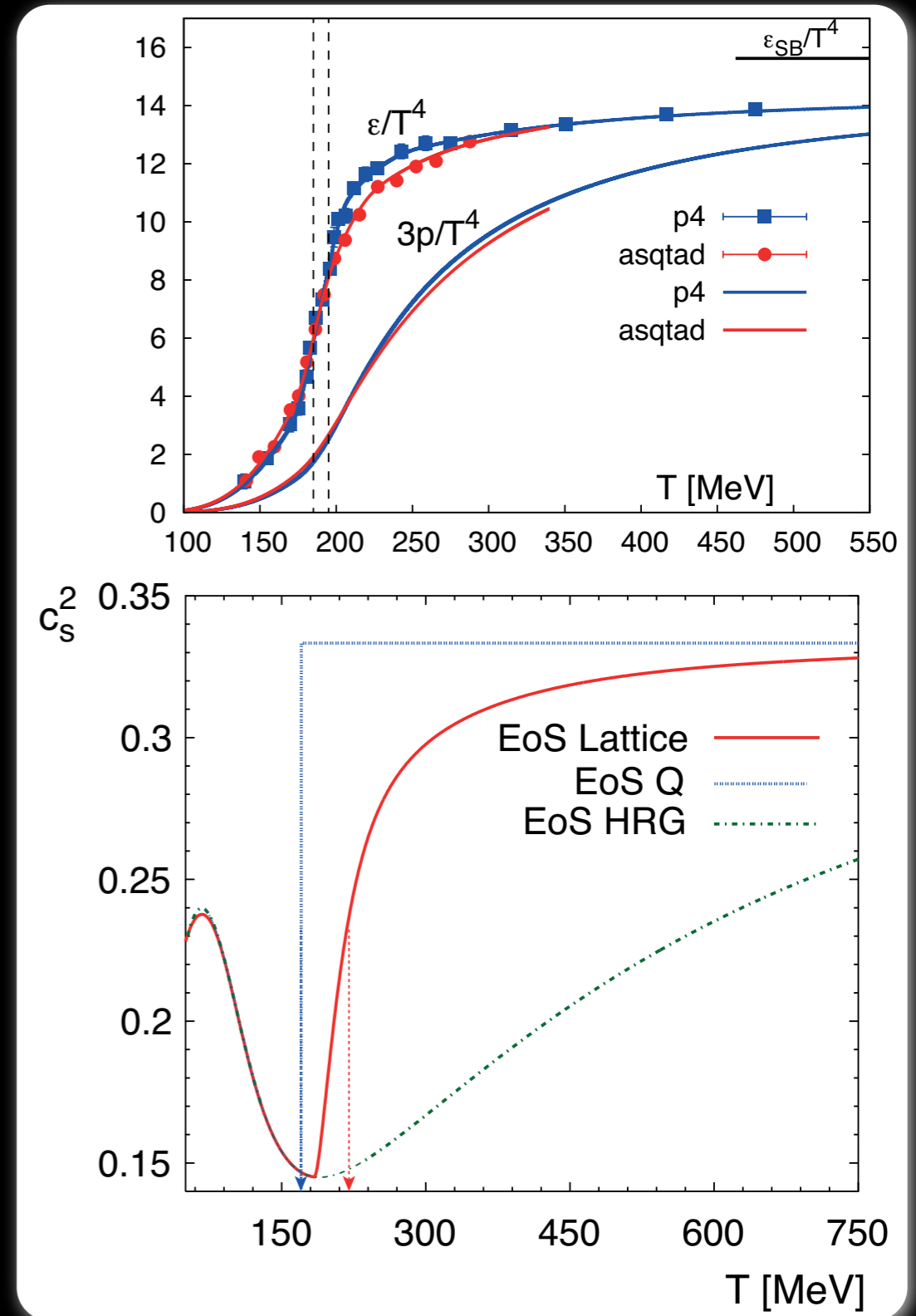


# Elliptic Flow

Elliptic flow  $v_2$  depends on fluid properties: the EoS via  $c_s^2 = \frac{\partial p}{\partial \epsilon}$ , shear viscosity over entropy ratio  $\eta/s$  but also on: initial conditions: particular initial spatial eccentricity  $\epsilon_2$

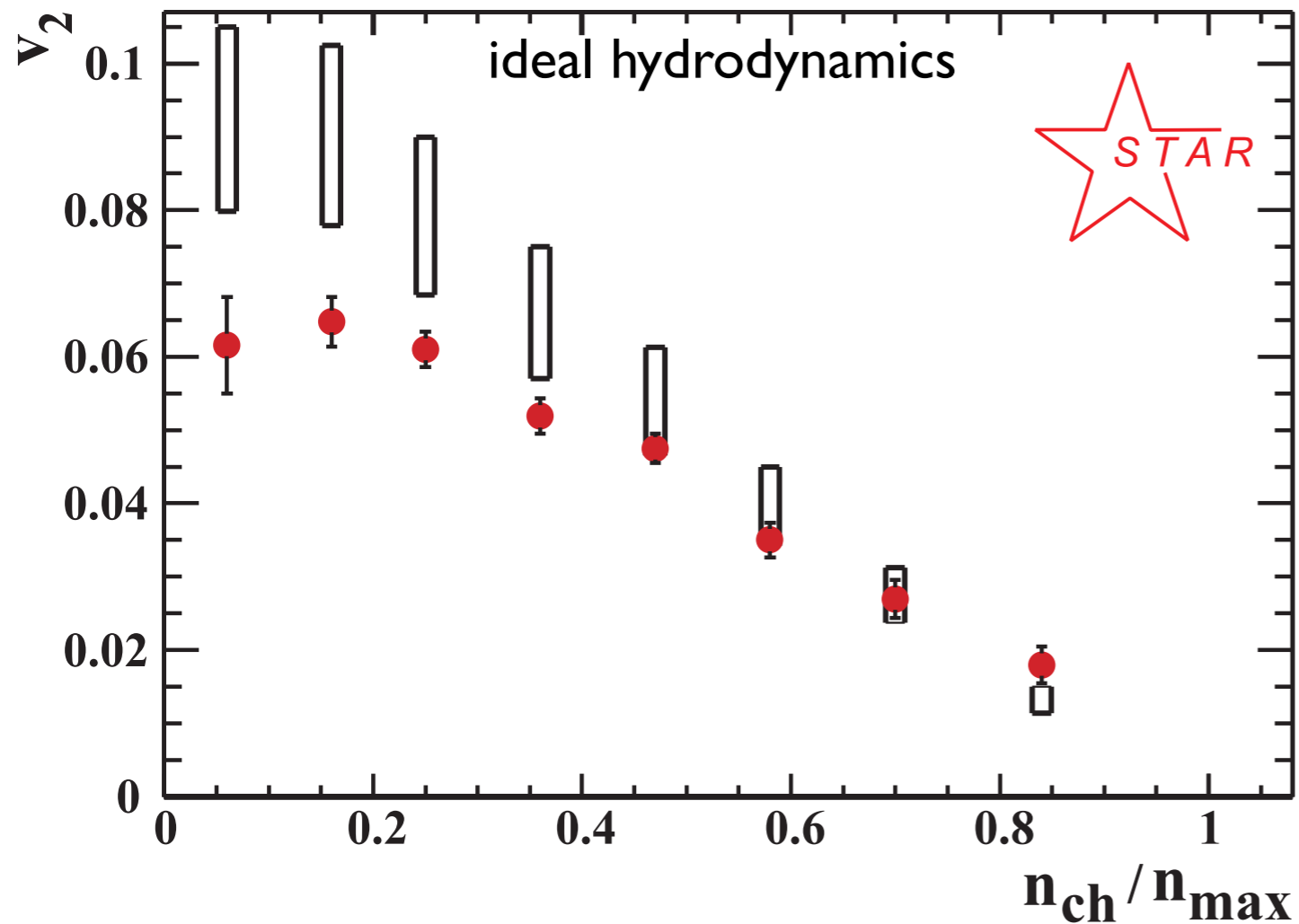


H.-J. Drescher et al.,  
Phys.Rev.C74:044905,2006





# Elliptic Flow at RHIC



STAR Phys. Rev. Lett. 86, 402–407 (2001)

for an ideal gas the elliptic flow would be almost zero while the observed elliptic flow is large

ideal hydro ( $\eta/s=0$ ) predicts the  $v_2$  magnitude for more central collisions

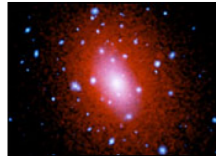
system behaves like an almost ideal liquid, not an ideal gas!

# RHIC Scientists Serve Up "Perfect" Liquid

## New state of matter more remarkable than predicted -- raising many new questions

April 18, 2005

### Early Universe Went With the Flow



Posted April 18, 2005 5:57PM

Between 2000 and 2003 the lab's Relativistic Heavy Ion Collider repeatedly smashed the nuclei of gold atoms together with such force that their energy briefly generated trillion-degree temperatures. Physicists think of the collider as a time machine, because those extreme temperature conditions last prevailed in the universe less than 100 millionths of a second after the big bang.

### Early Universe was a liquid

Quark-gluon blob surprises particle physicists.

Mark Peplow

**nature**

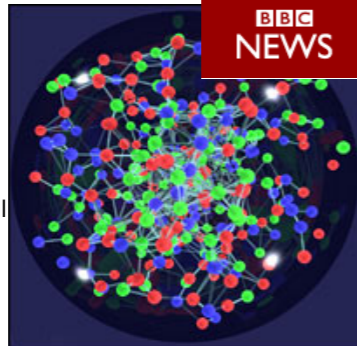
The Universe consisted of a perfect liquid in its first moments, according to results from an atom-smashing experiment.

### Early Universe was 'liquid-like'

Physicists say they have created a new state of hot, dense matter by crashing together the nuclei of gold atoms.

The high-energy collisions prised open the nuclei to reveal their most basic particles, known as quarks and gluons.

The researchers, at the US Brookhaven National Laboratory, say these particles were seen to behave as an almost perfect "liquid".



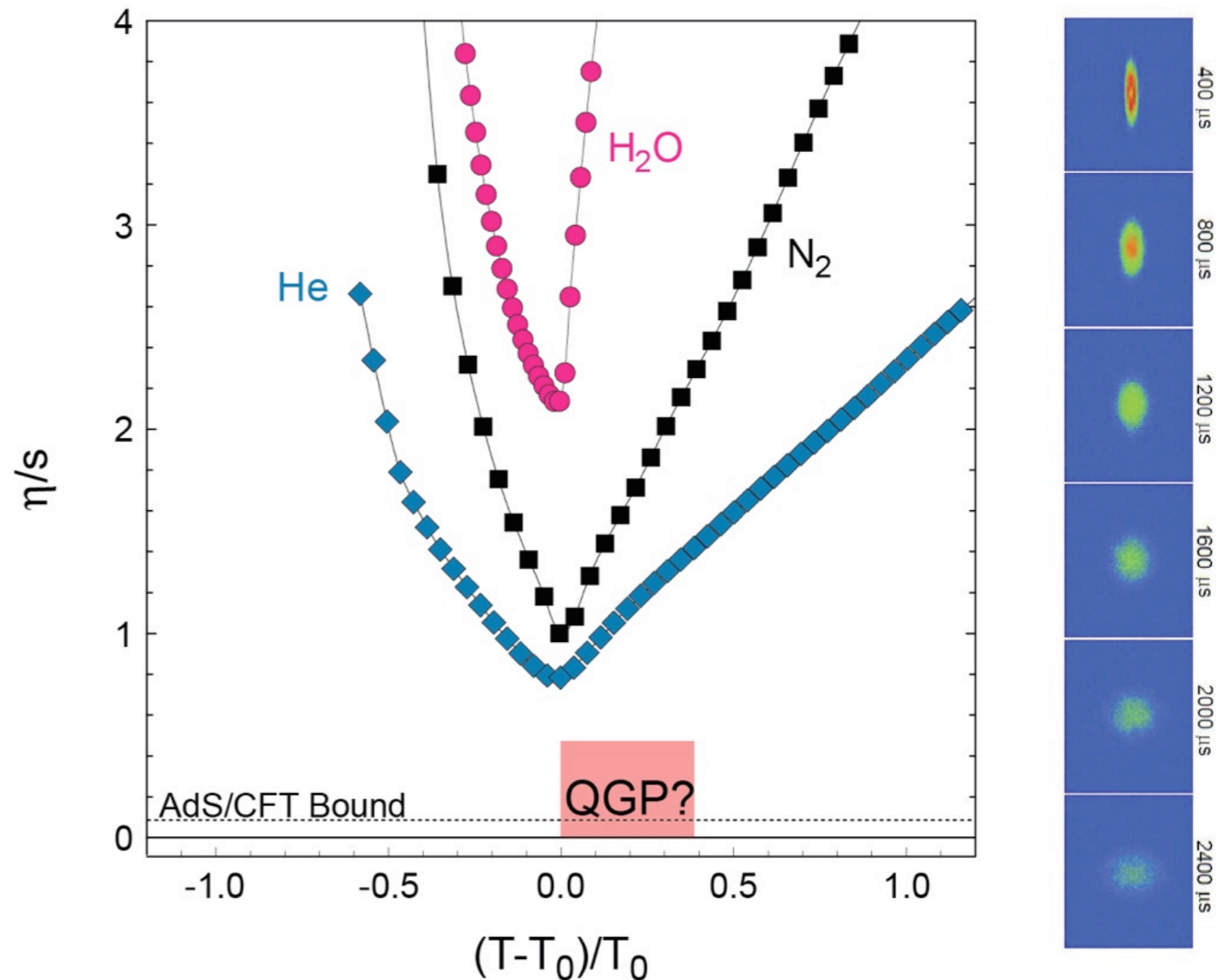
The impression is of matter that is more strongly interacting than predicted

### Universe May Have Begun as Liquid, Not Gas

Associated Press  
Tuesday, April 19, 2005; Page A05

**The Washington Post**

New results from a particle collider suggest that the universe behaved like a liquid in its earliest moments, not the fiery gas that was thought to have pervaded the first microseconds of existence.

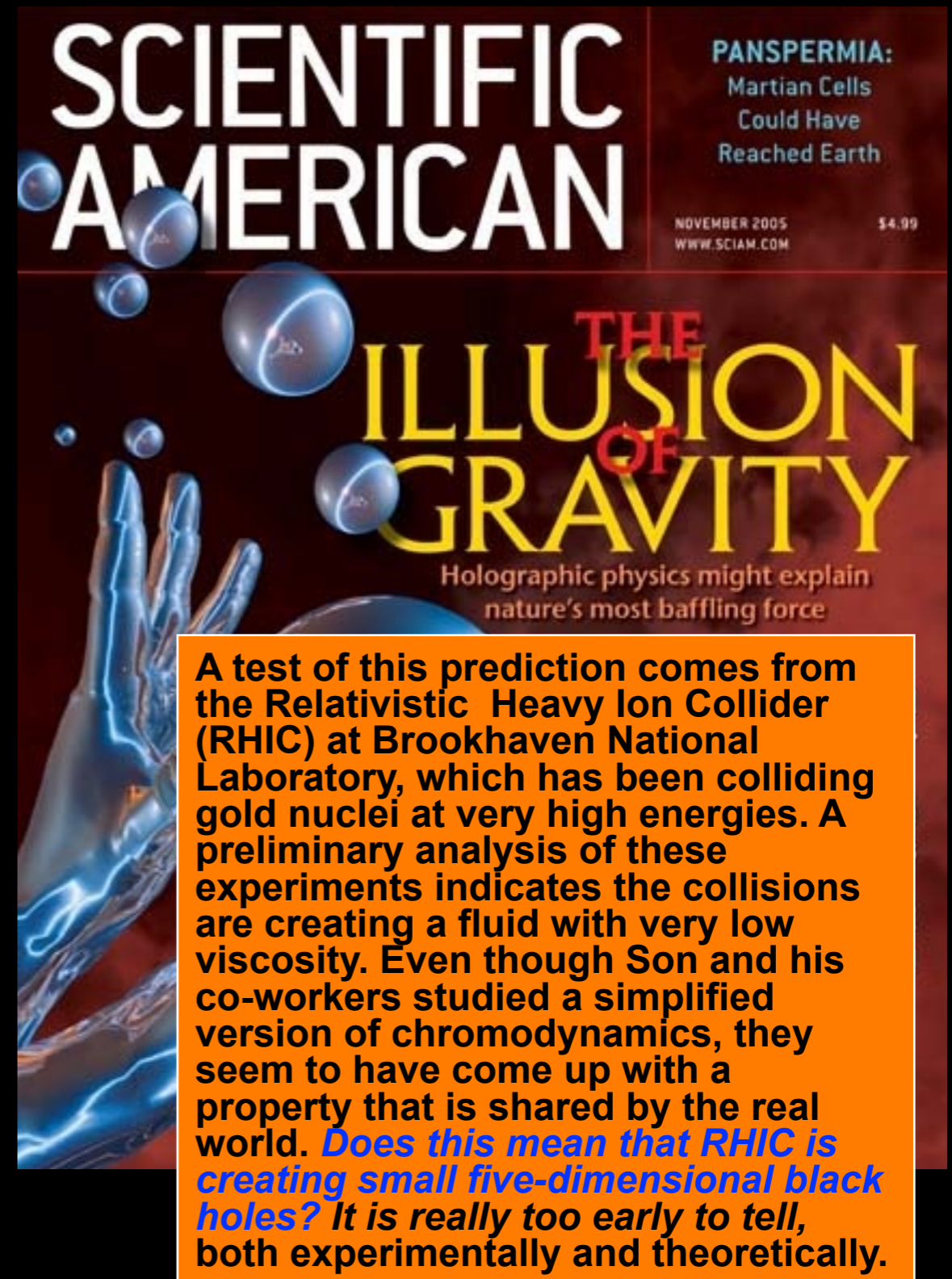


from AdS/CFT to cold atoms

# $\eta/s?$

- good fluids in nature have a kinematic viscosity  $\eta/s$  of order  $\hbar/k_B$
- calculable in perturbative QCD:  $\eta/s \sim 1/g^4 \ln(1/g)$
- calculable in a N=4 Super Yang Mills theory with large number of colors using a gauge gravity duality
- $\eta/s = \hbar/4\pi k$

“The Illusion of Gravity” J. Maldacena

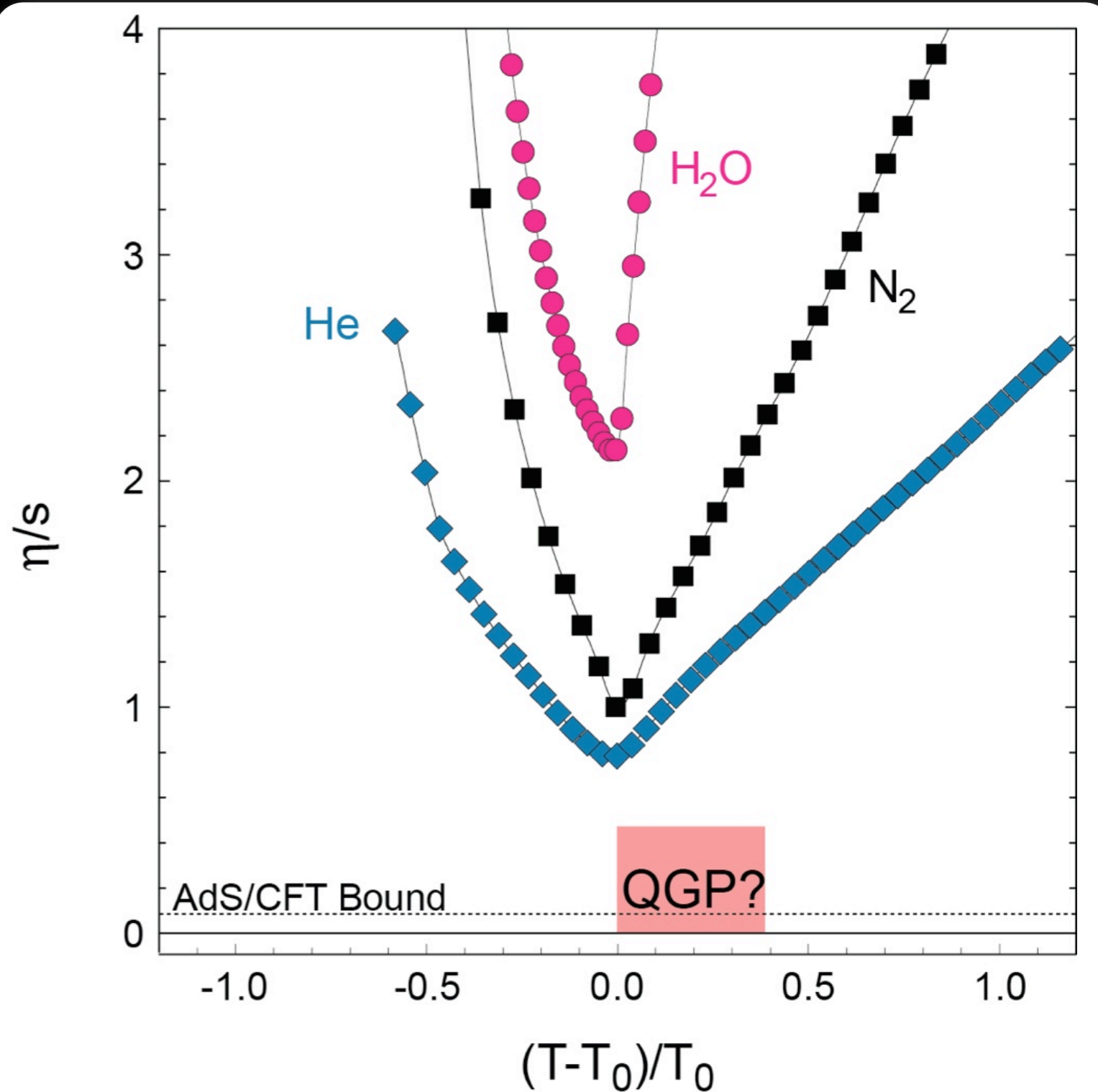


# The Perfect Liquid?

model calculations suggest that the RHIC  $v_2$  results are close to the ideal hydrodynamical limit.

these calculations place an upper limit on  $\eta/s$  which is smaller than  $\sim 4 \times \text{AdS/CFT bound}$

main uncertainties on  $\eta/s$  due to uncertainties in the initial conditions and the unknown dependence of  $\eta/s$  versus temperature

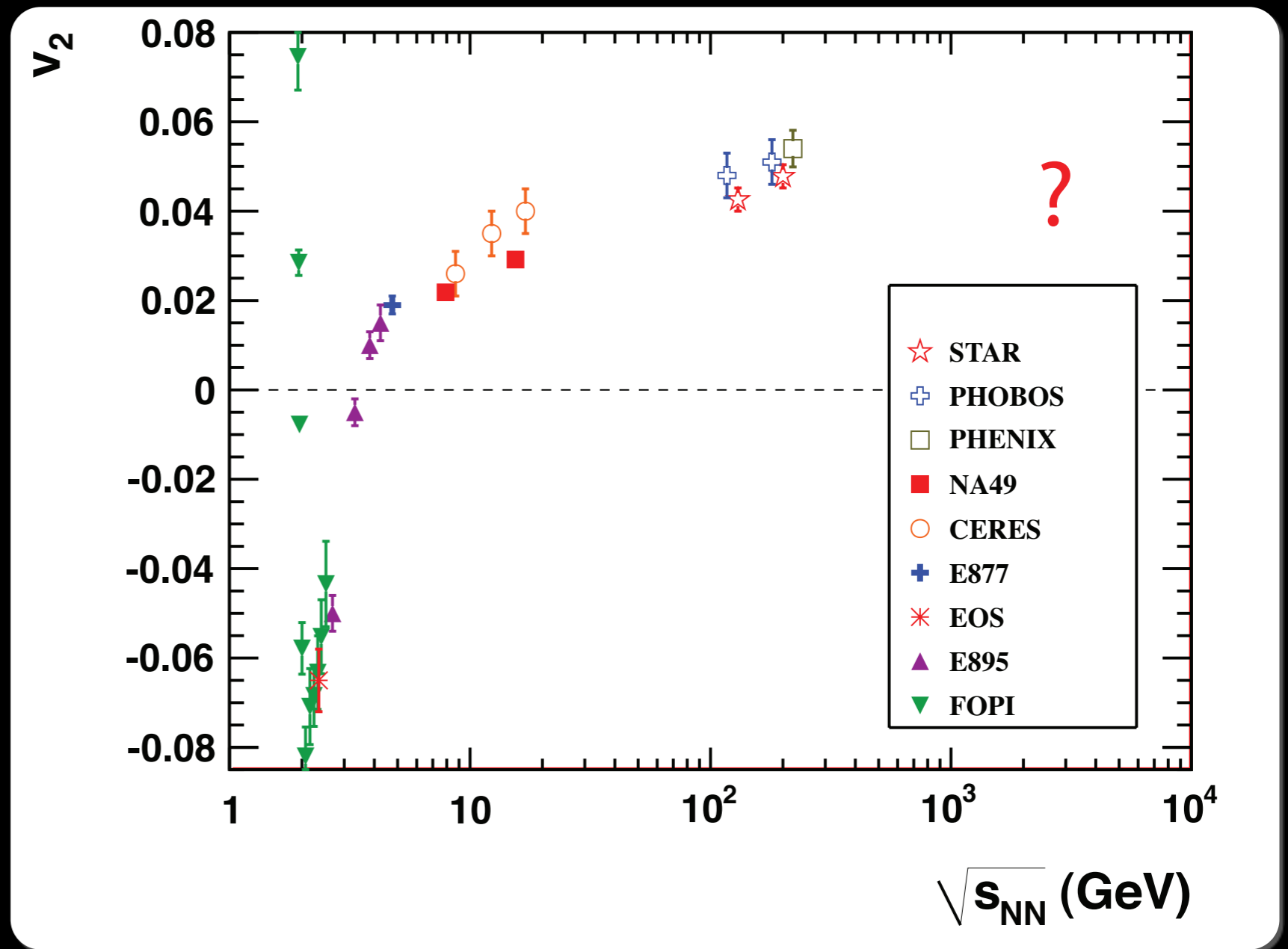


Based on R. Lacey et al., Phys.Rev.Lett.98:092301,2007.

# The Perfect Liquid?

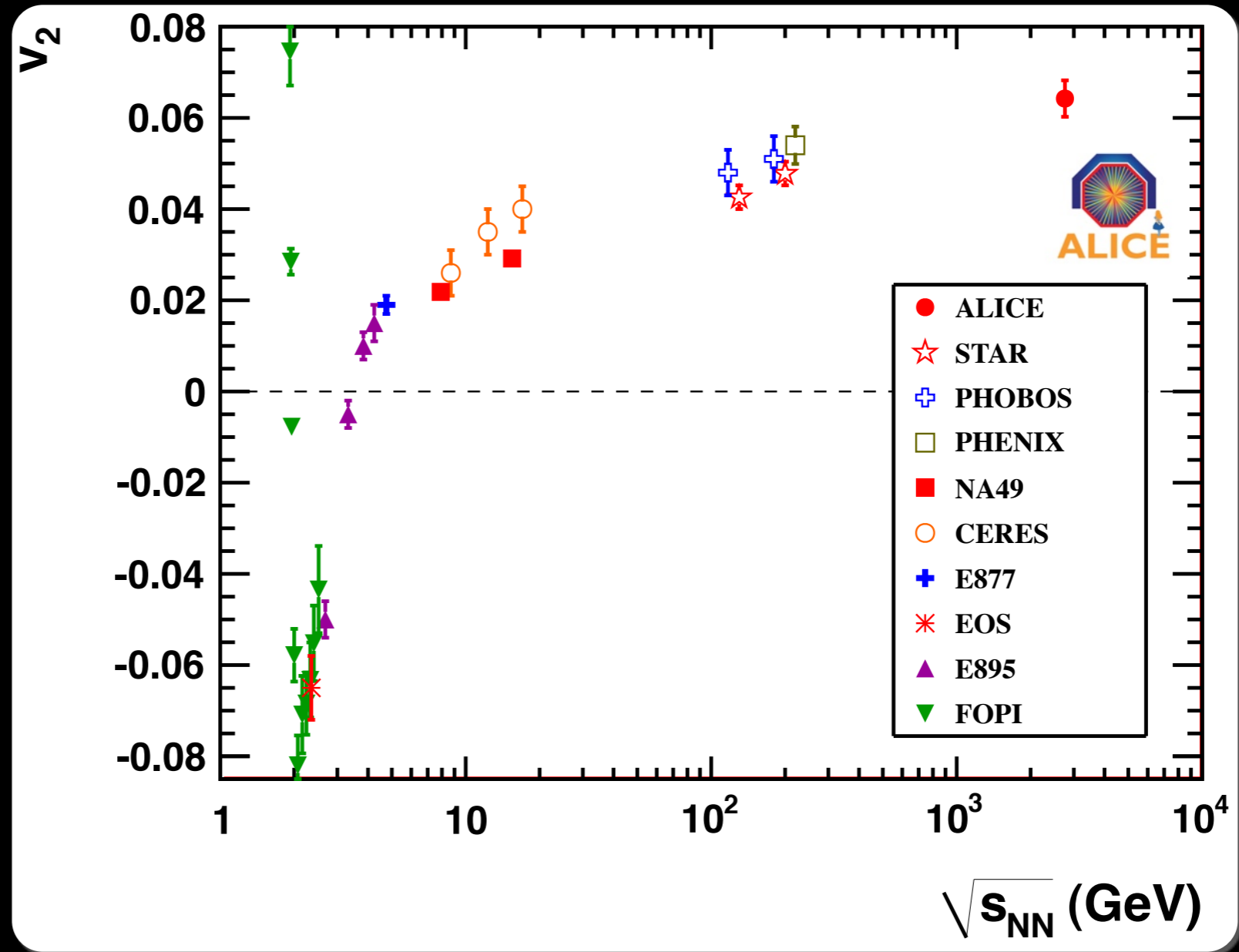
What to expect at the LHC: still the perfect liquid or are we approaching the viscous ideal gas?

Can we get better constraints on  $\eta/s$  (constrain initial conditions and temperature dependence of  $\eta/s$ )?



# The Perfect Liquid

K. Aamodt et al. (ALICE Collaboration)  
PRL 105, 252302 (2010)

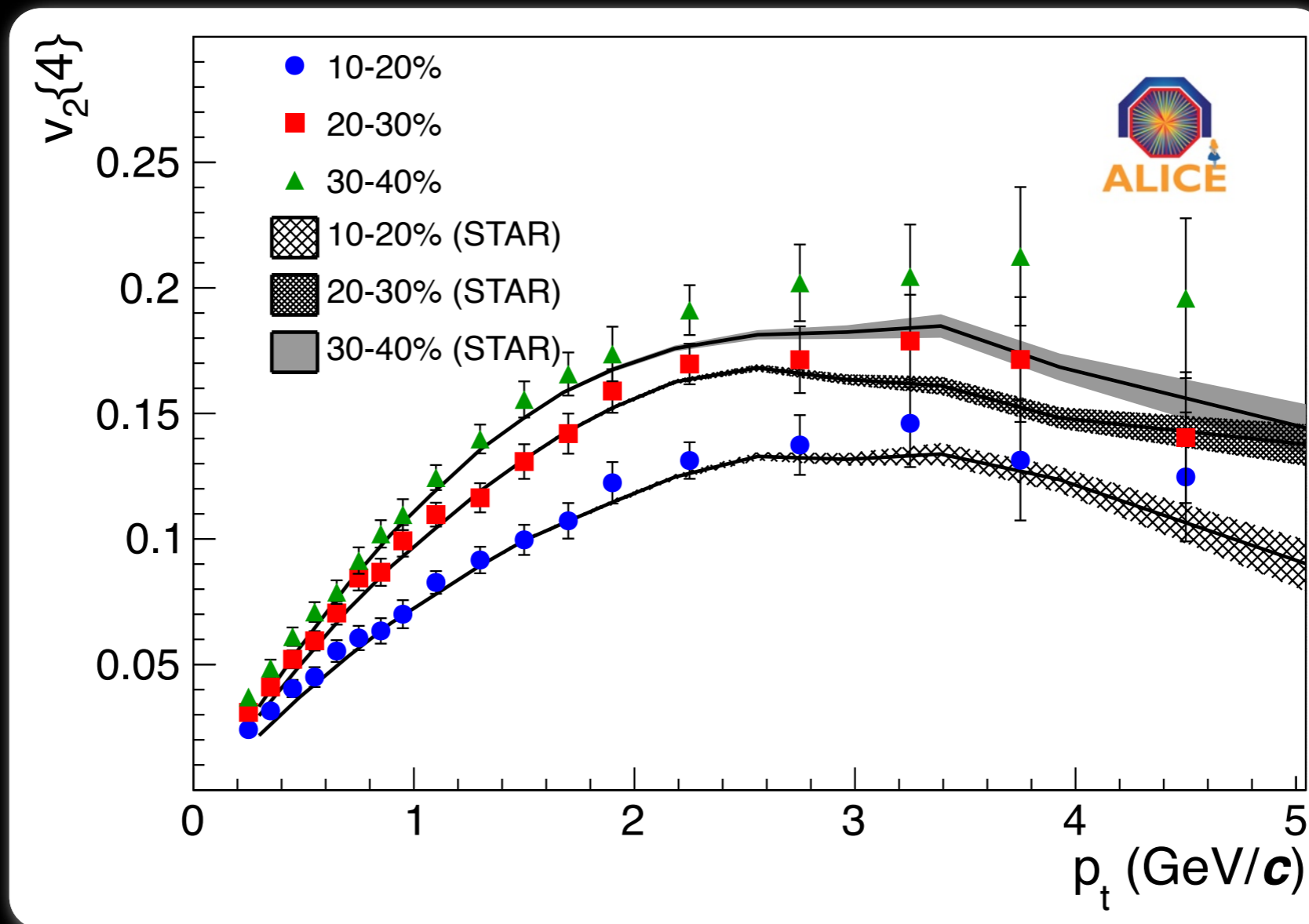


The system produced at the LHC behaves as a very low viscosity fluid (a perfect fluid), constraints dependence of  $\eta/s$  versus temperature

# $v_2$ as function of $p_t$

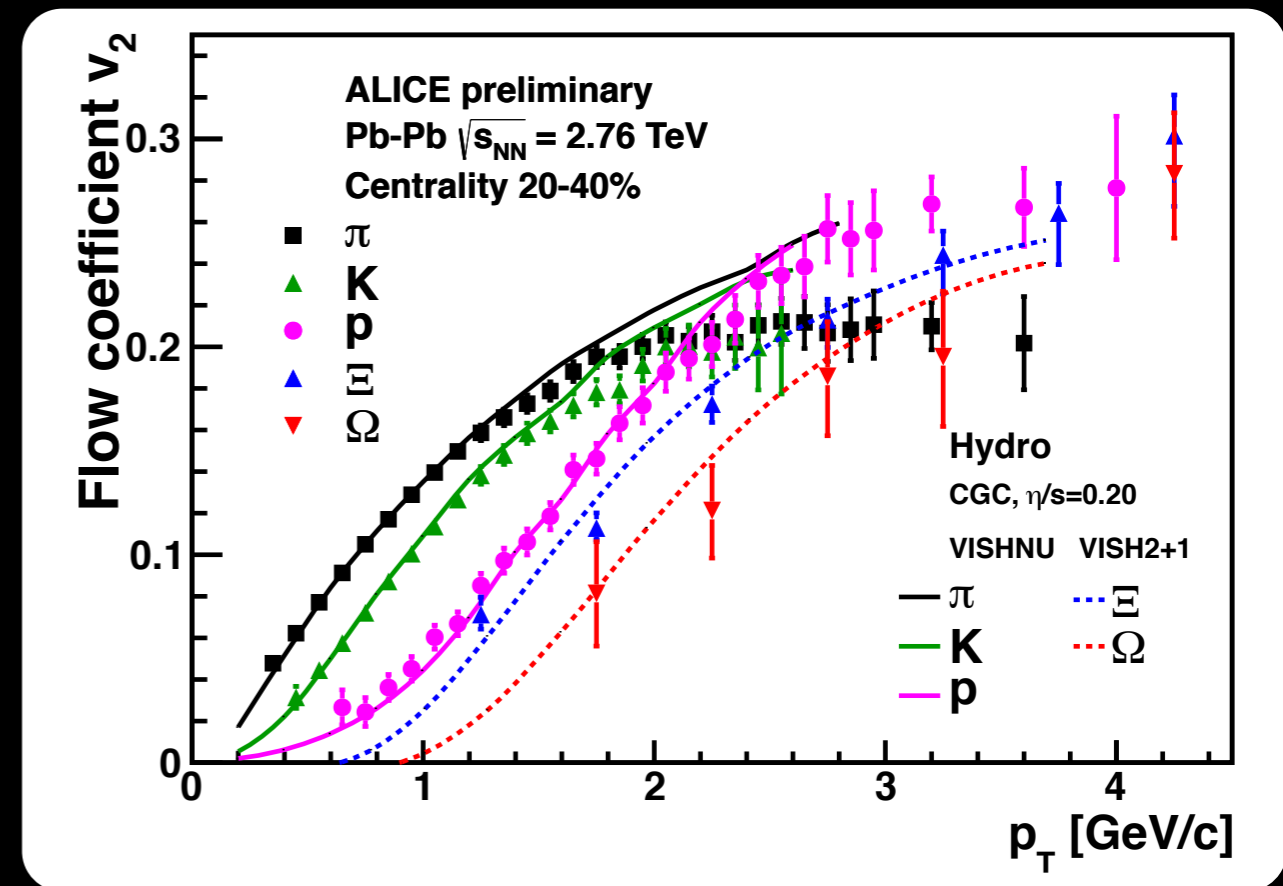
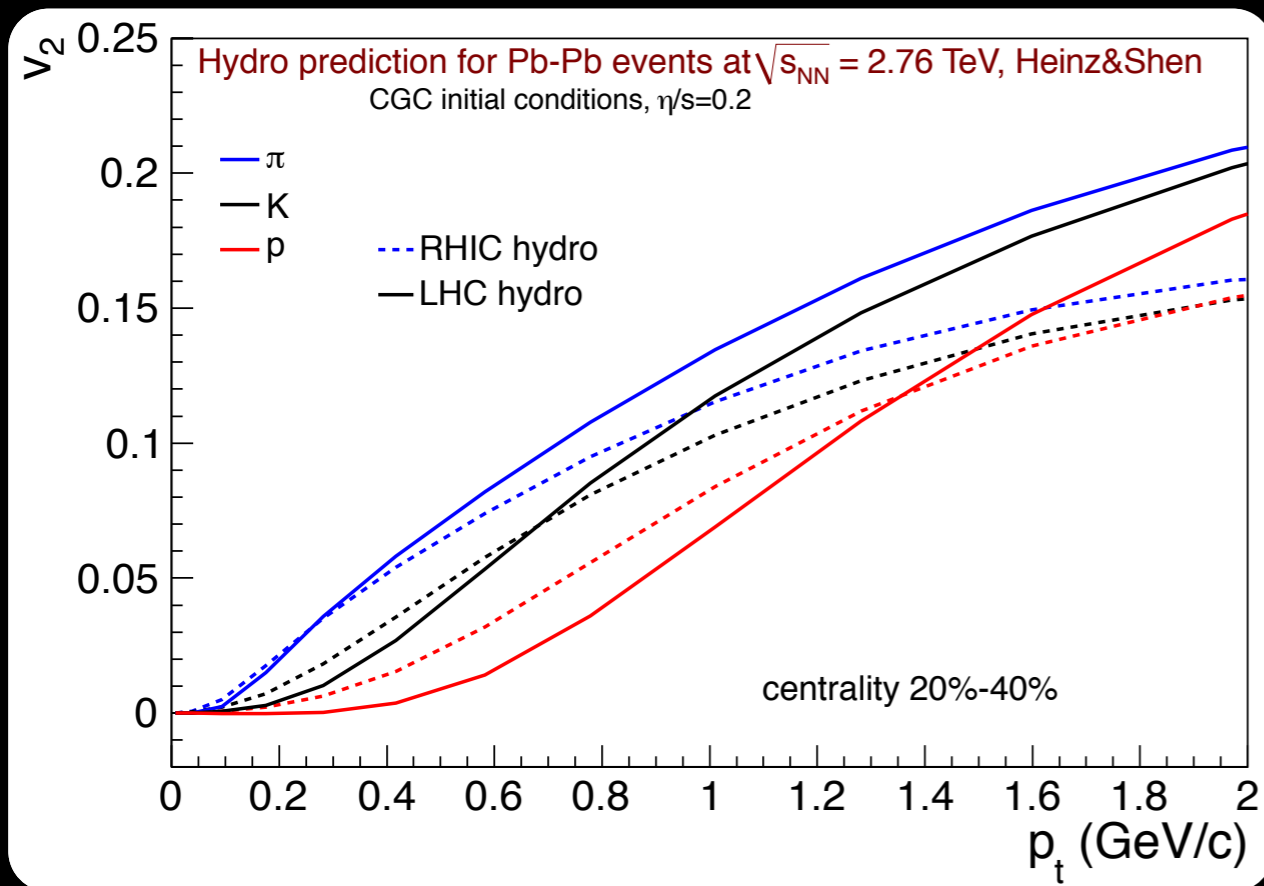
K. Aamodt et al. (ALICE Collaboration)

PRL 105, 252302 (2010)



Elliptic flow as function of transverse momentum does not change much from RHIC to LHC energies, can we understand that from hydro?

# $v_2$ for identified particles

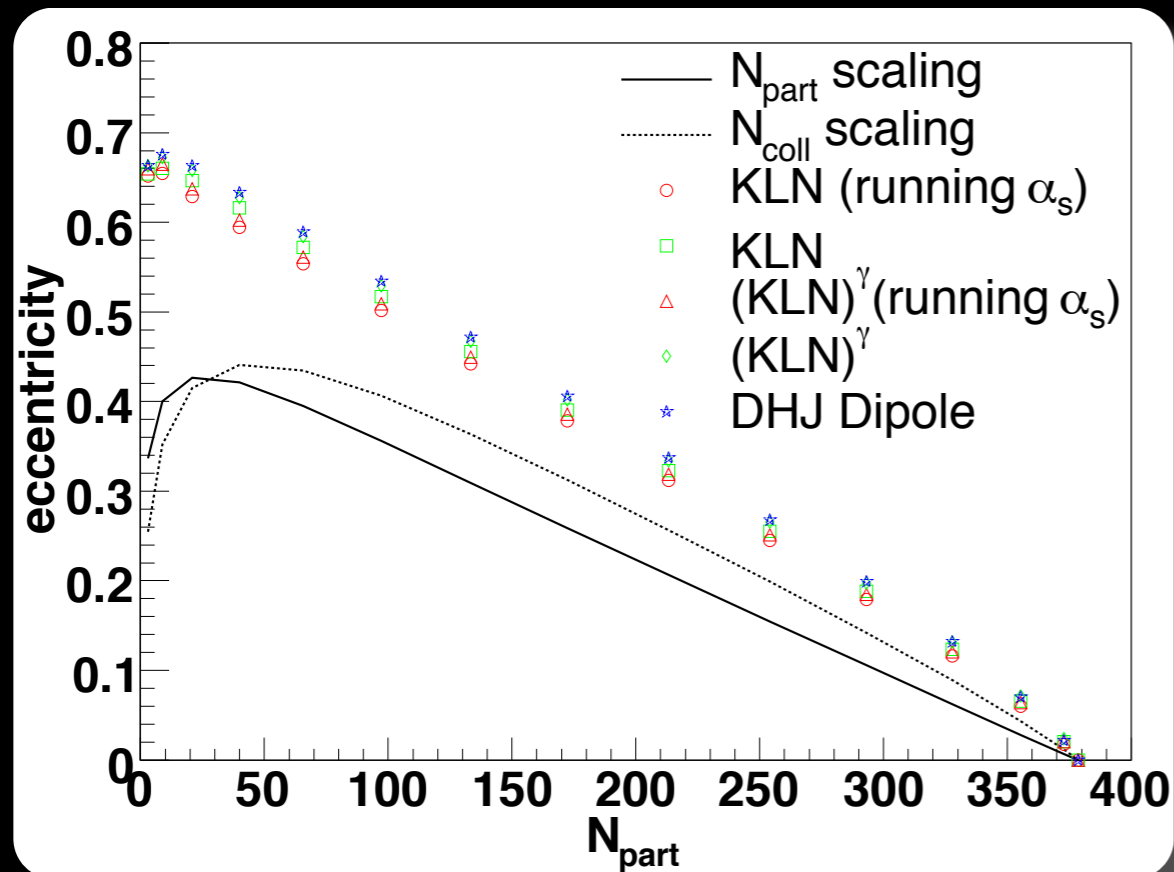


Hydro: Shen, Heinz, Huovinen & Song, arXiv:1105.3226

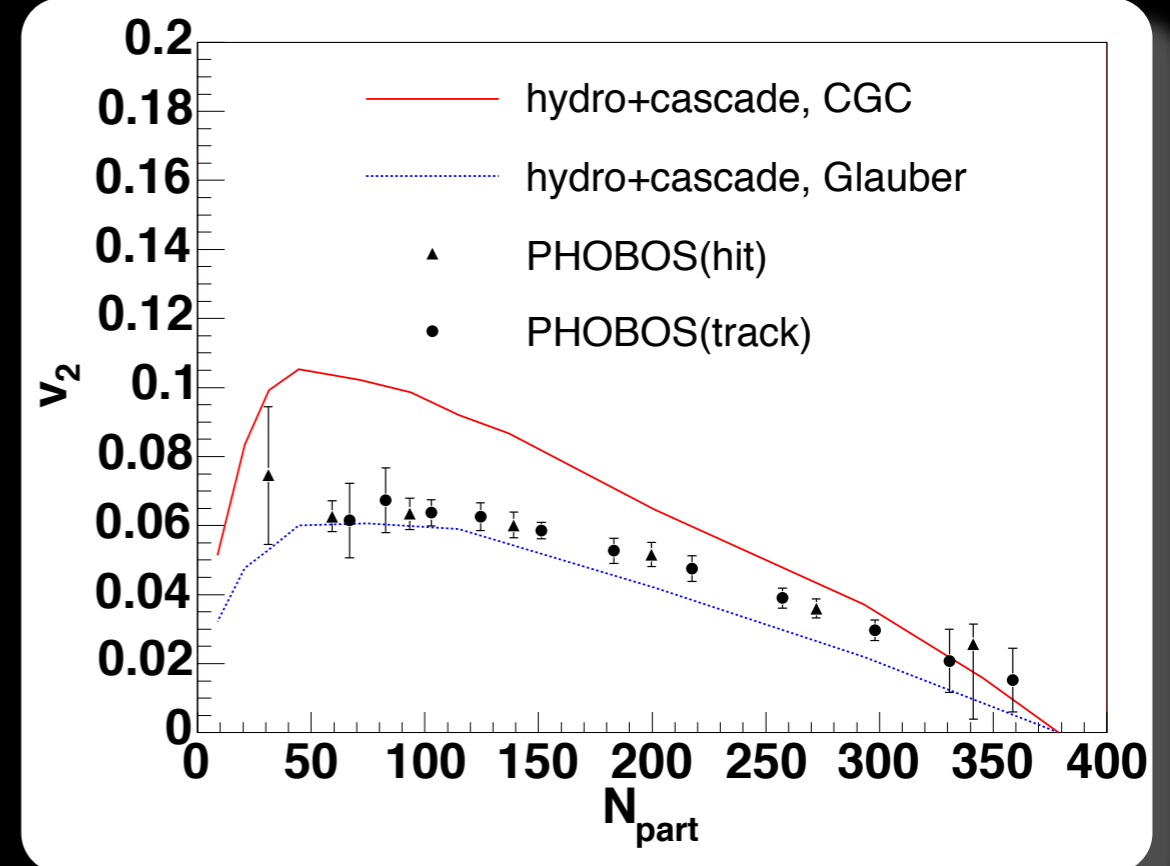
hydro models predict larger mass splitting  
data follows this mass splitting and agrees well with  
hydro predictions for mid-central collisions



# Better constraints on $\eta/s$ (understanding the initial conditions)



H-J. Drescher et al., Phys.Rev.C74:044905,2006



T. Hirano et al., Phys. Lett. B 636 299 (2006)  
T. Hirano et al., J.Phys.G34:S879-882,2007

$$v_2 \propto \epsilon$$

- Estimates of the eccentricity vary significantly  $\sim 30\%$ !
- Leads to large uncertainty in estimate of  $\eta/s$

# Flow Fluctuations

in limit of small (not necessarily Gaussian) fluctuations

$$v_n^2\{2\} = \bar{v}_n^2 + \sigma_v^2$$

$$v_n^2\{4\} = \bar{v}_n^2 - \sigma_v^2$$

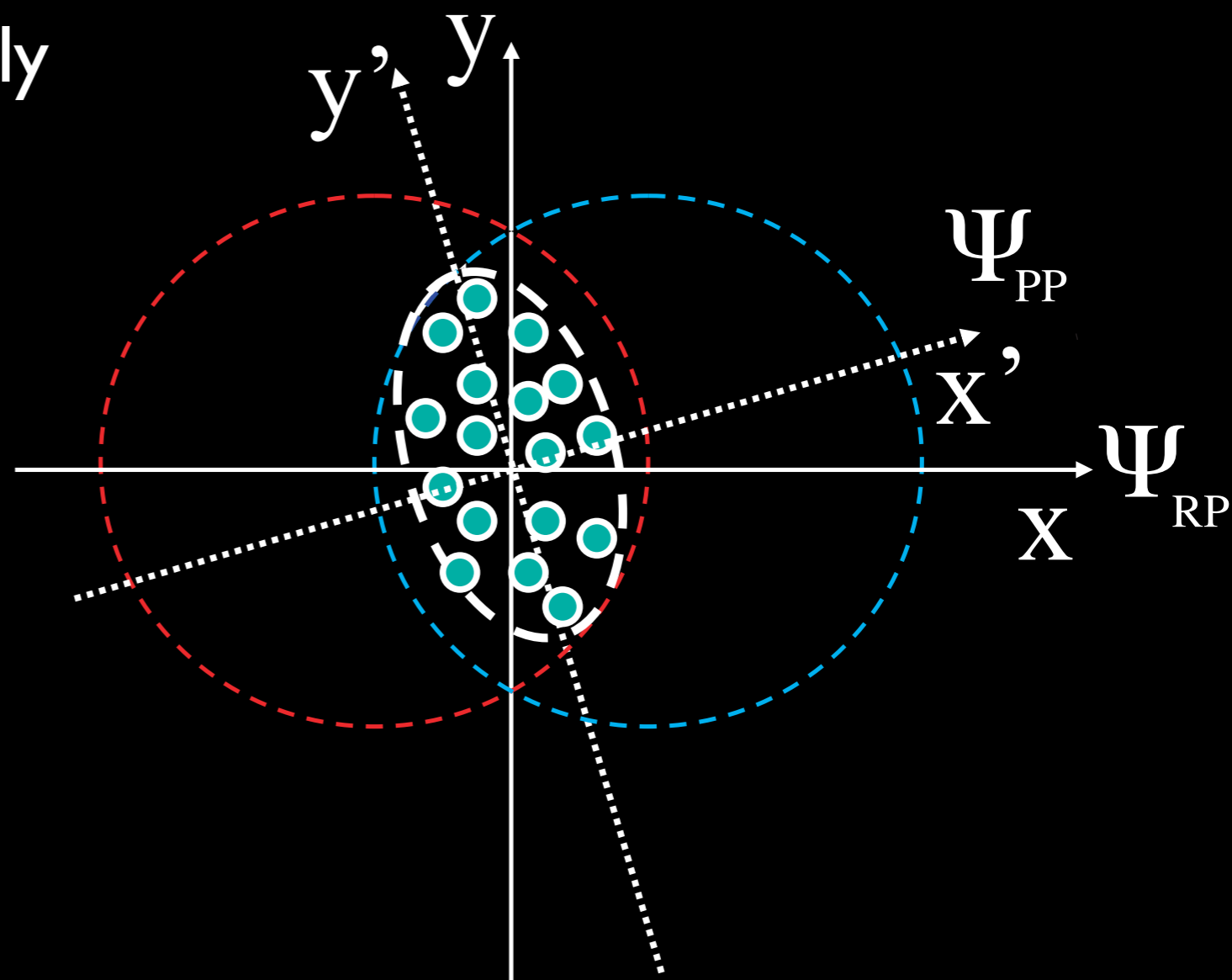
$$v_n^2\{2\} + v_n^2\{4\} = 2\bar{v}_n^2$$

$$v_n^2\{2\} - v_n^2\{4\} = 2\sigma_v^2$$

in limit of only (Gaussian) fluctuations

$$v_n\{4\} = 0$$

$$v_n\{2\} = \frac{2}{\sqrt{\pi}} \bar{v}_n$$



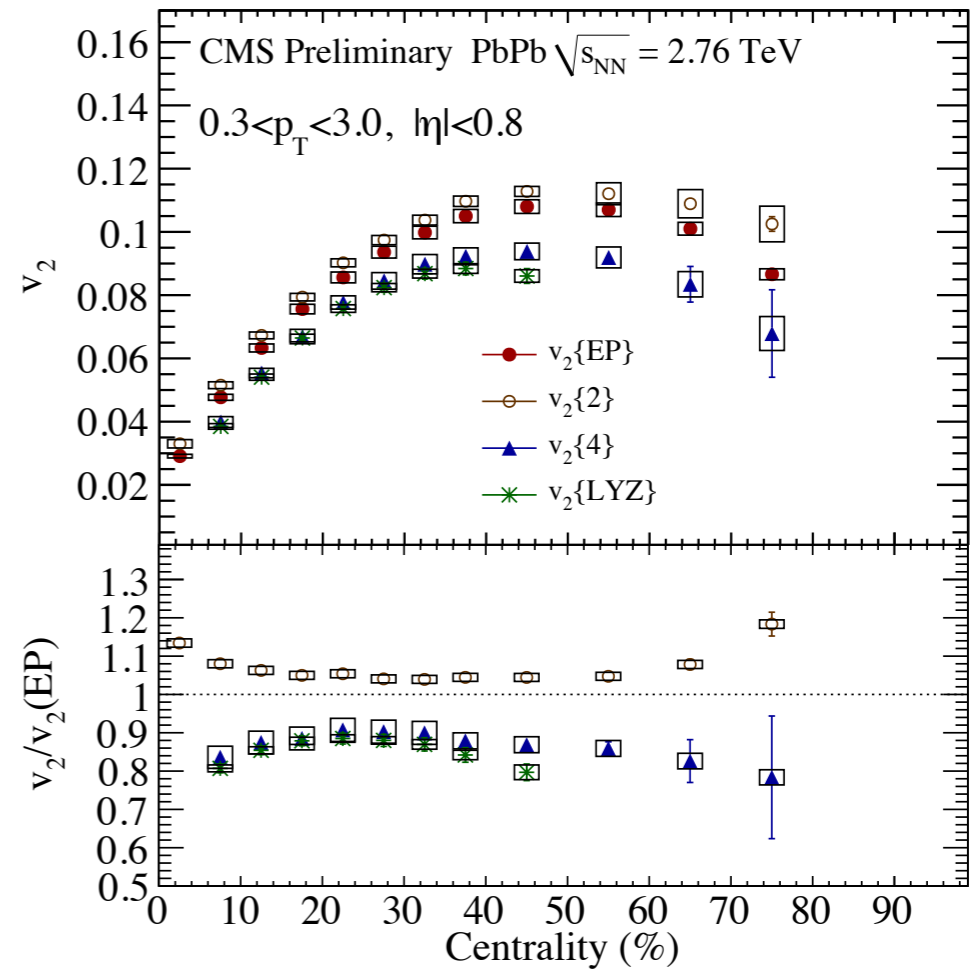
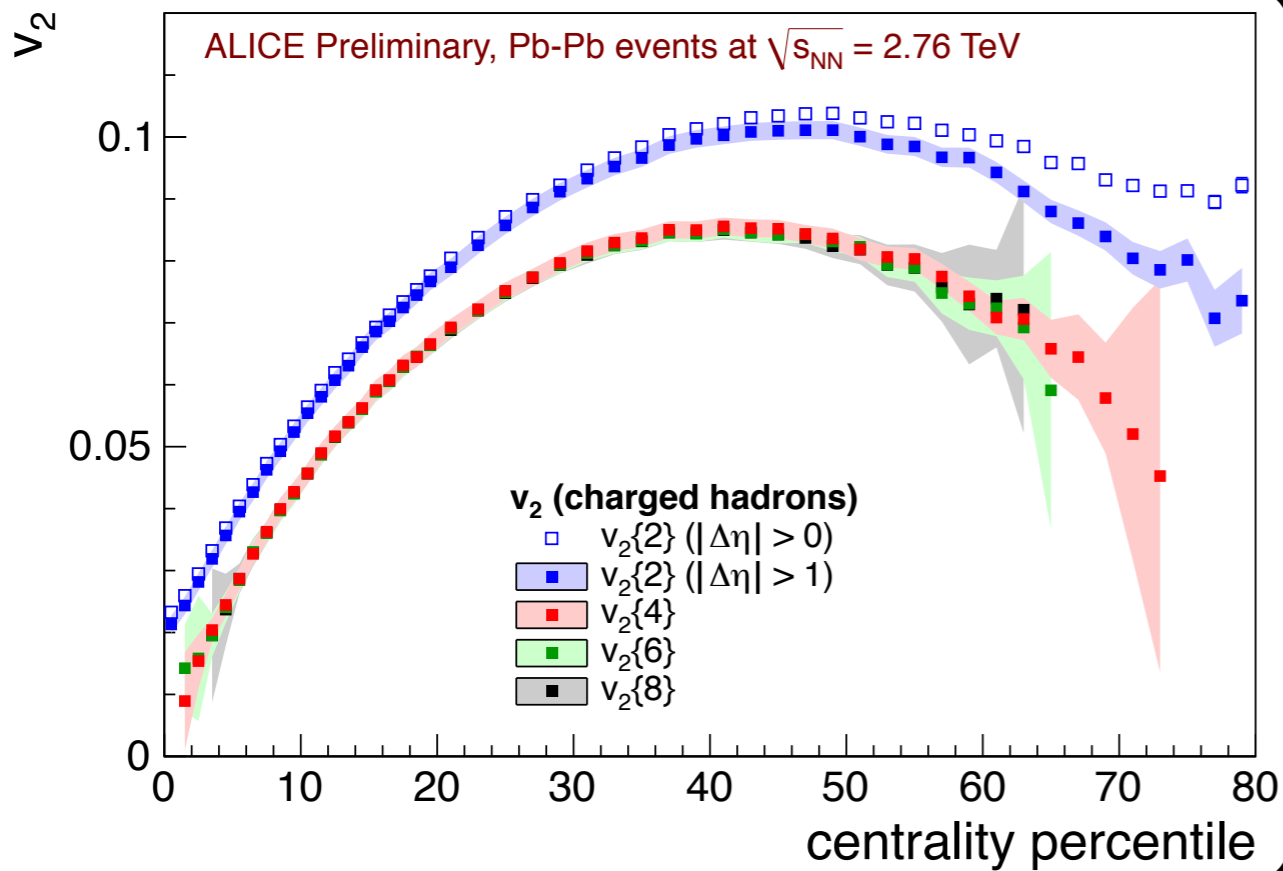
eccentricity fluctuations:

M. Miller and RS, arXiv:nucl-ex/0312008 (2003)

participant eccentricity

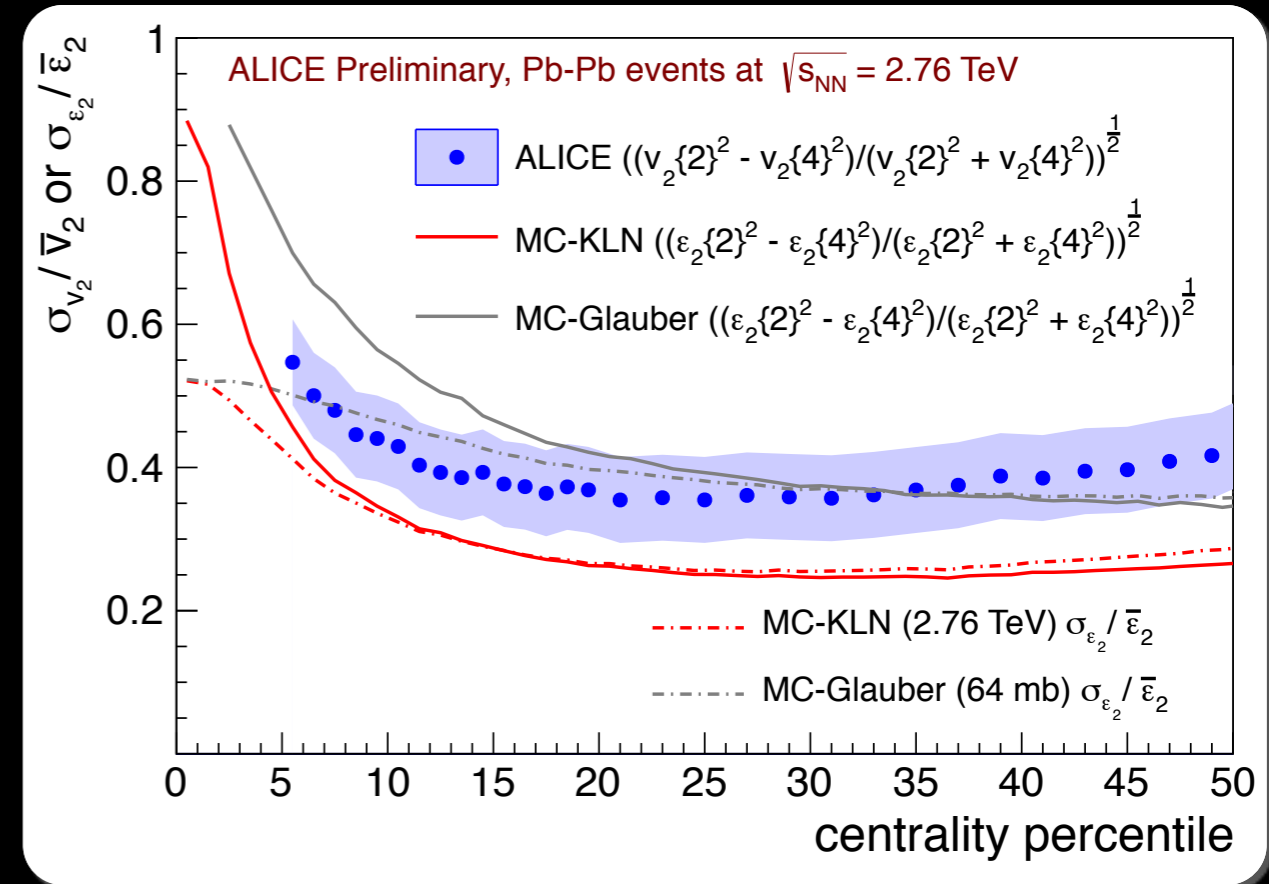
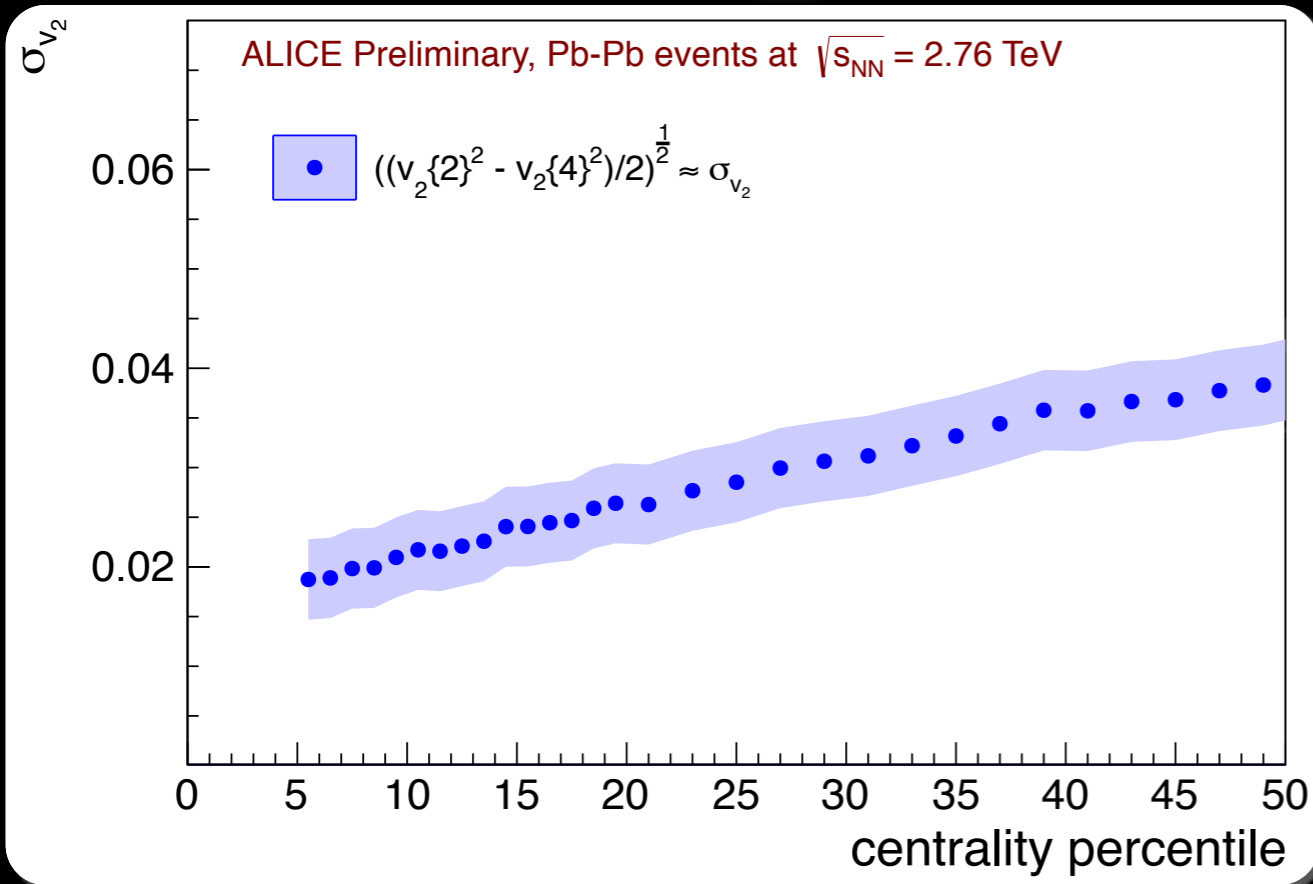
PHOBOS QM2005: Nucl. Phys. A774: 523 (2006)

# $v_2$ Fluctuations



behavior as expected when correlations are dominated by collective flow (difference between two- and multi-particle estimates mainly due to e-by-e fluctuations in the flow)

# $v_2$ Fluctuations



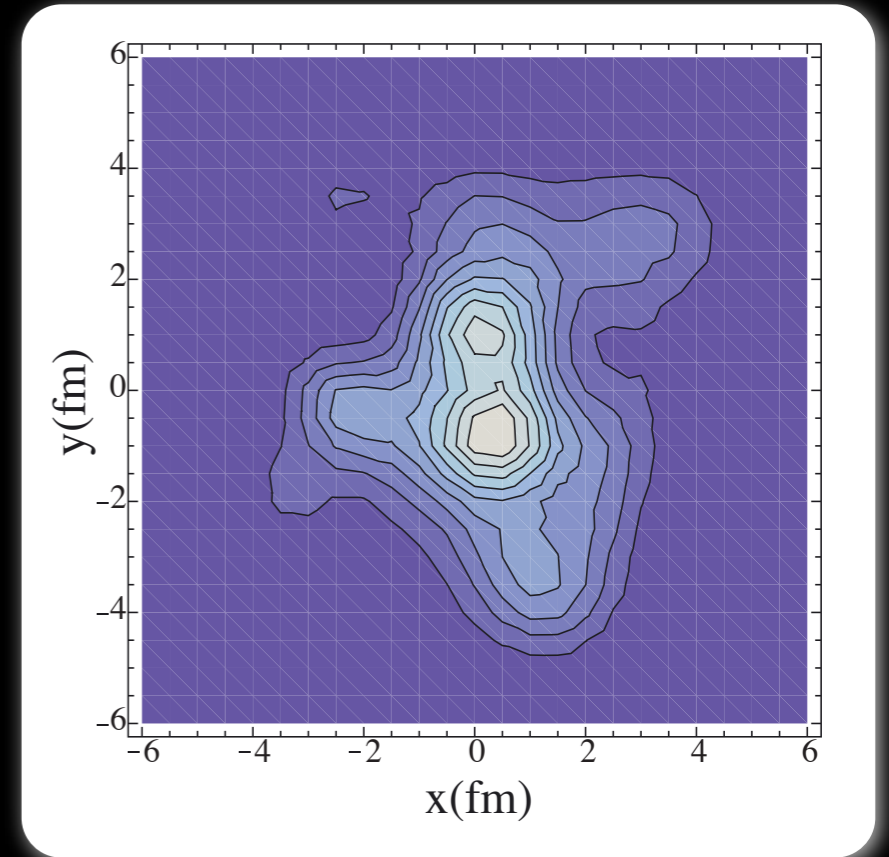
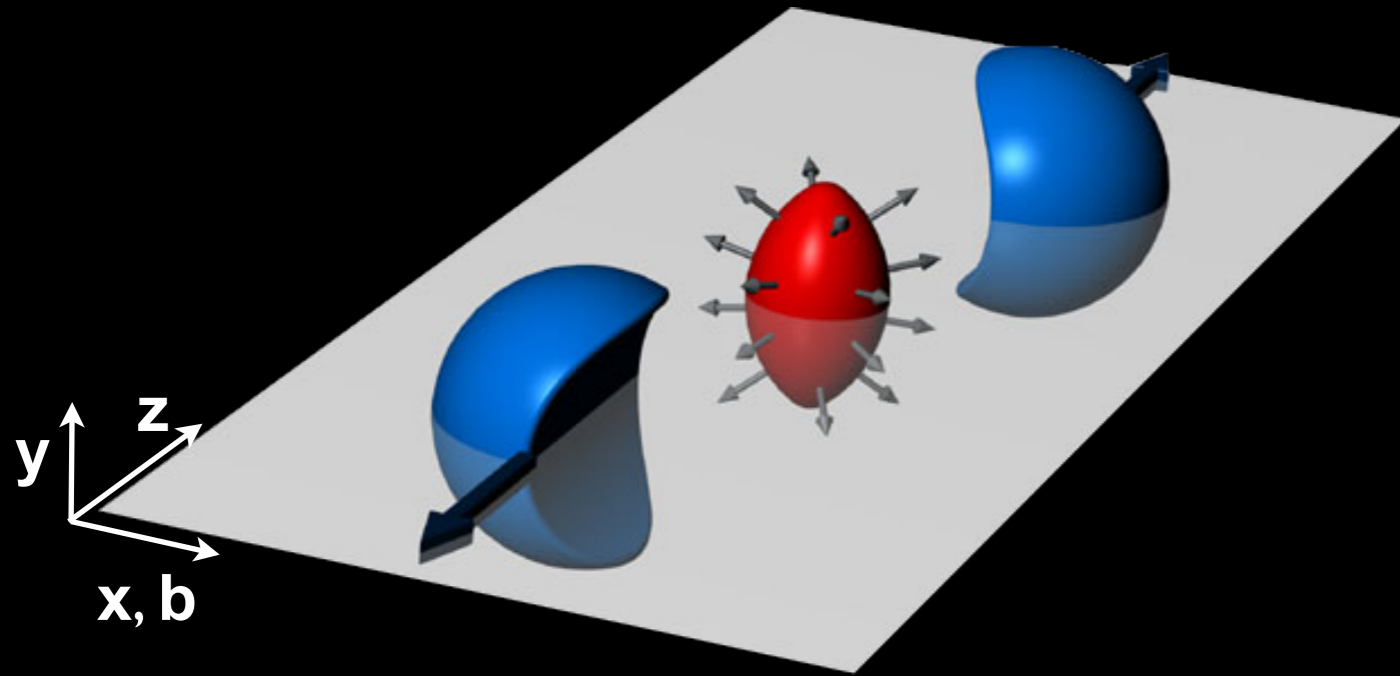
$$\sigma_{v_n} \simeq \left[ \frac{1}{2} (v_n^2\{2\} - v_n^2\{4\}) \right]^{\frac{1}{2}}$$

$$\frac{\sigma_{v_n}}{\bar{v}_n} \simeq \left( \frac{v_n^2\{2\} - v_n^2\{4\}}{v_n^2\{2\} + v_n^2\{4\}} \right)^{\frac{1}{2}}$$

Fluctuations are significant and are for more central collisions not in agreement with the eccentricity fluctuations in MC-Glauber and MC-KLN CGC

# Anisotropic Flow $v_n$

G. Qin, H. Petersen, S. Bass, and B. Muller



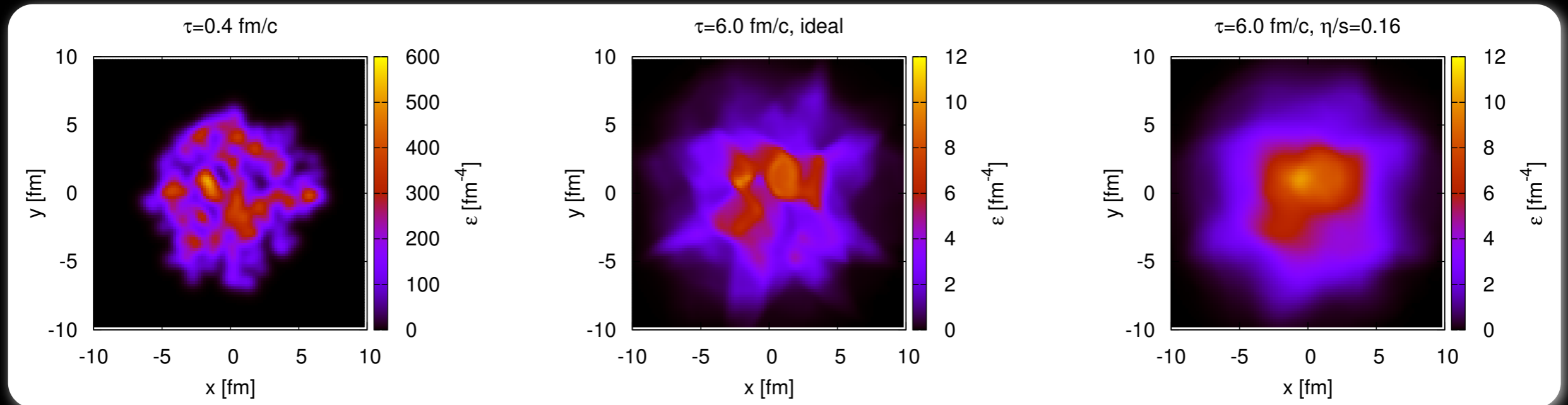
$$\frac{2\pi}{N} \frac{dN}{d\phi} = 1 + \sum_{n=2,4,6,\dots}^{\infty} 2v_n \cos n(\phi - \Psi_R)$$

$$\frac{2\pi}{N} \frac{dN}{d\phi} = 1 + \sum_{n=1}^{\infty} 2v_n \cos n(\phi - \Psi_n)$$

initial spatial geometry not a smooth almond event-by-event (for which all odd harmonics and  $\sin n(\Phi - \Psi_R)$  are zero due to symmetry) may give rise to higher odd harmonics and symmetry planes in momentum space (**detailed probes of initial conditions**)

# Shear Viscosity

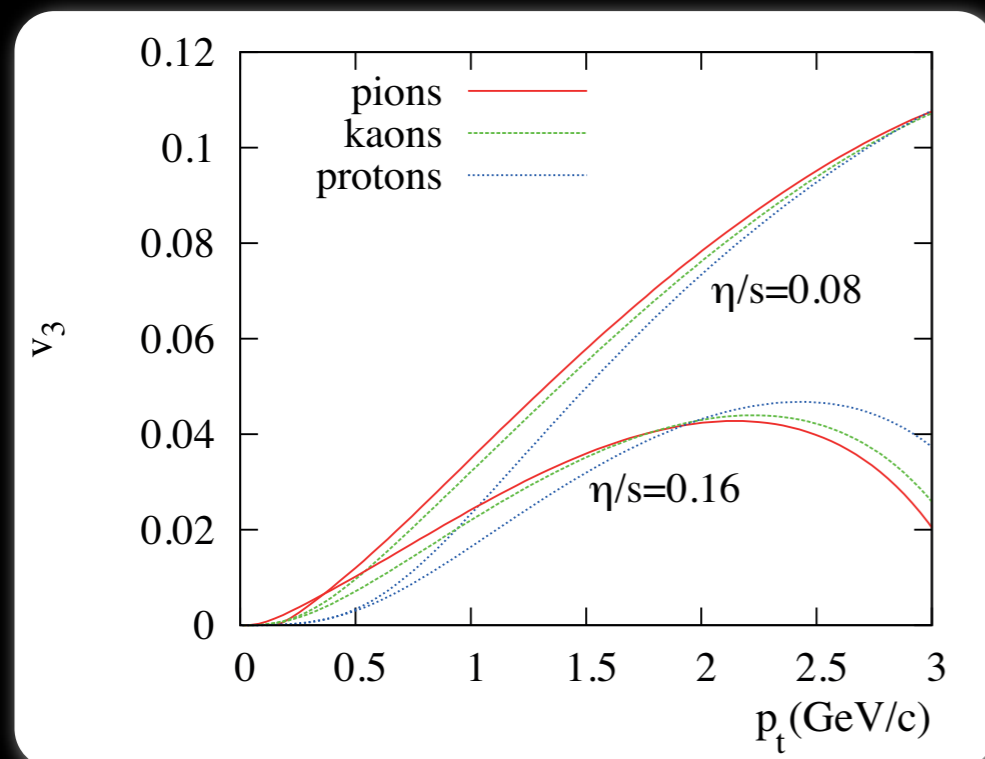
Music, Sangyong Jeon



initial conditions

ideal hydro  $\eta/s=0$

viscous hydro  $\eta/s=0.16$

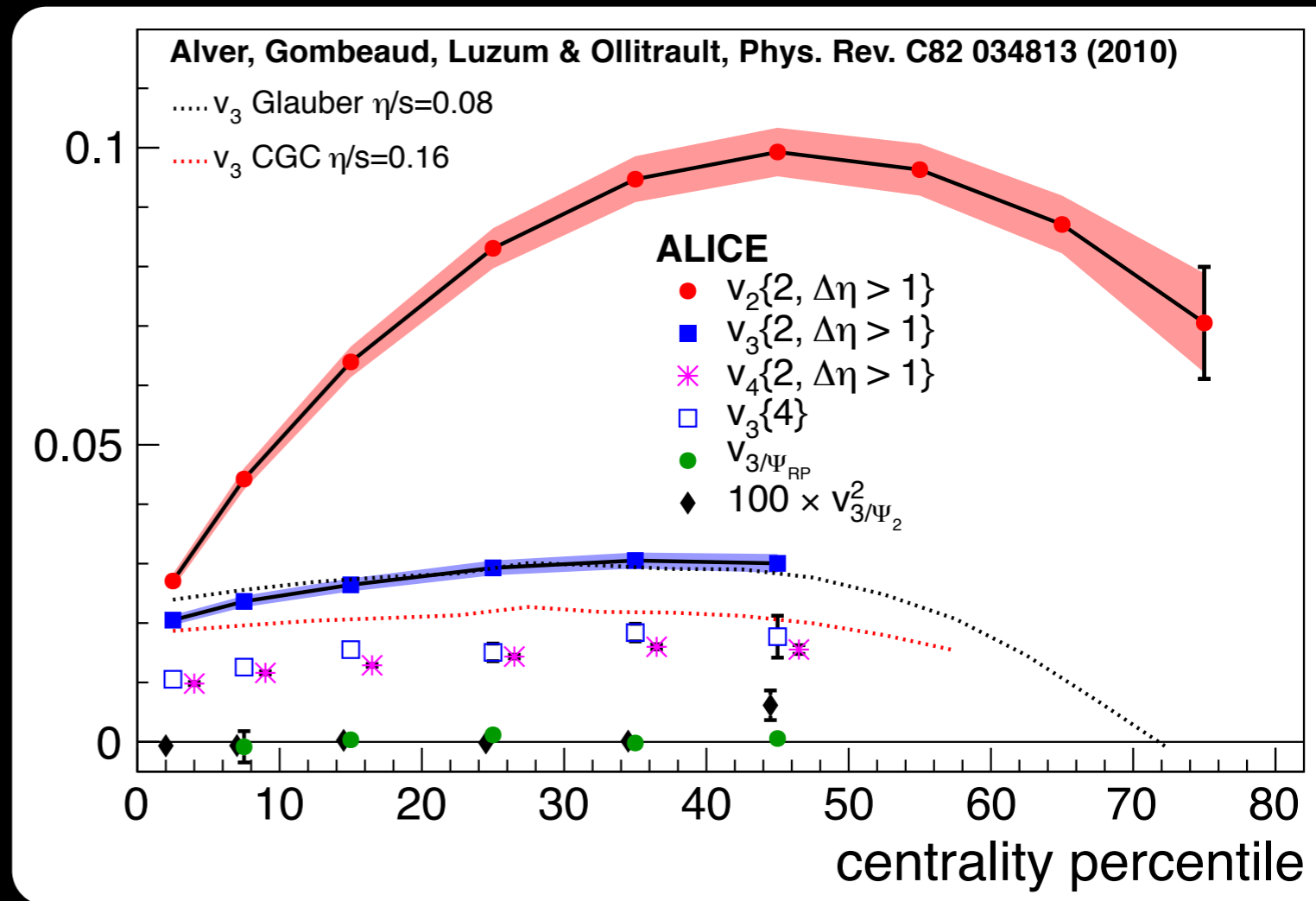


Larger  $\eta/s$  clearly smoothes the distributions and suppresses the higher harmonics (e.g.  $v_3$ )

# the $v_n$ 's

The  $v_3$  with respect to the reaction plane determined in the ZDC and with the  $v_2$  participant plane is consistent with zero as expected if  $v_3$  is due to fluctuations of the initial eccentricity

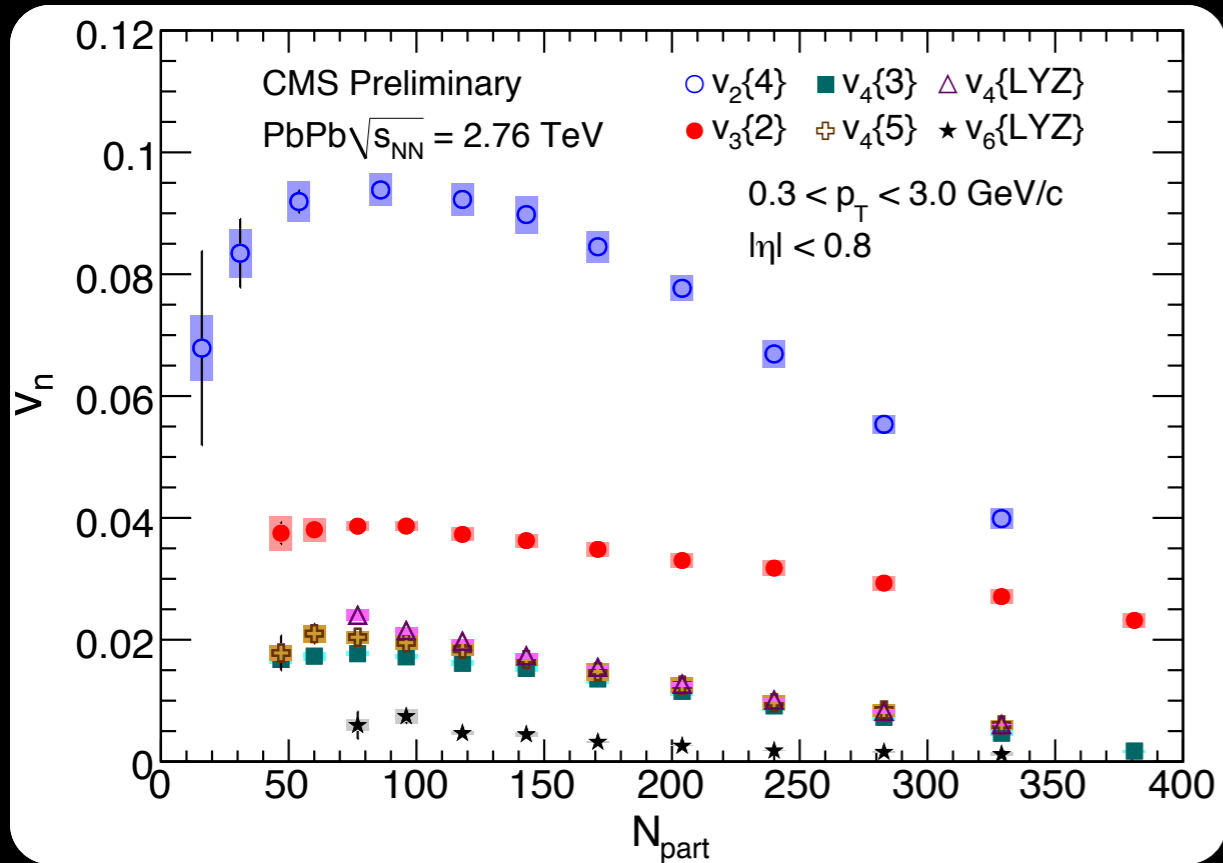
The  $v_3\{2\}$  is about two times larger than  $v_3\{4\}$  which is also consistent with expectations based on initial eccentricity fluctuations



ALICE Collaboration, arXiv:1105.3865  
PRL 107 (2011) 032301

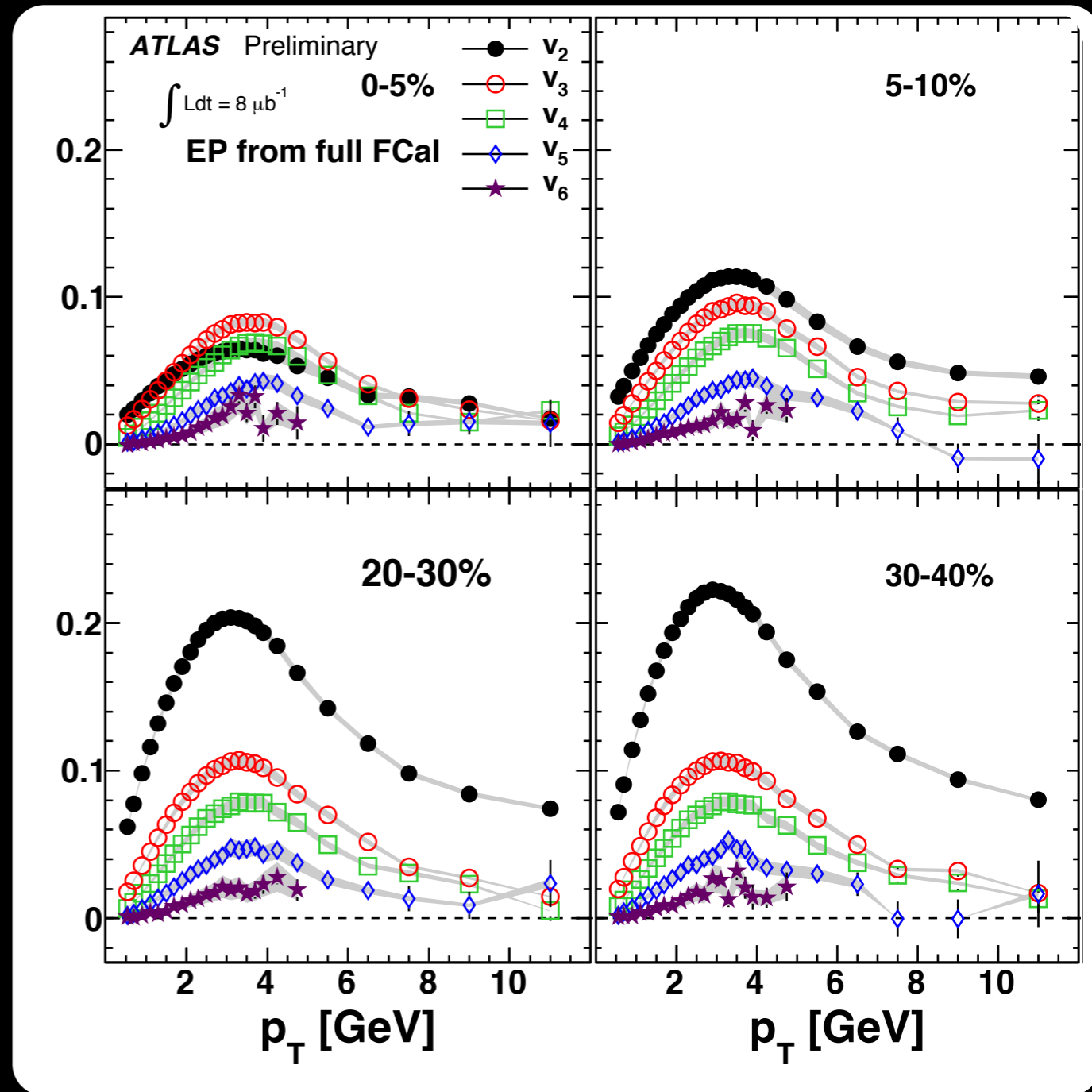
We observe significant  $v_3$  and  $v_4$  which compared to  $v_2$  has a different centrality dependence (already strong constrain for  $\eta/s$ )

# the $v_n$ 's



CMS PAS HIN-11-005

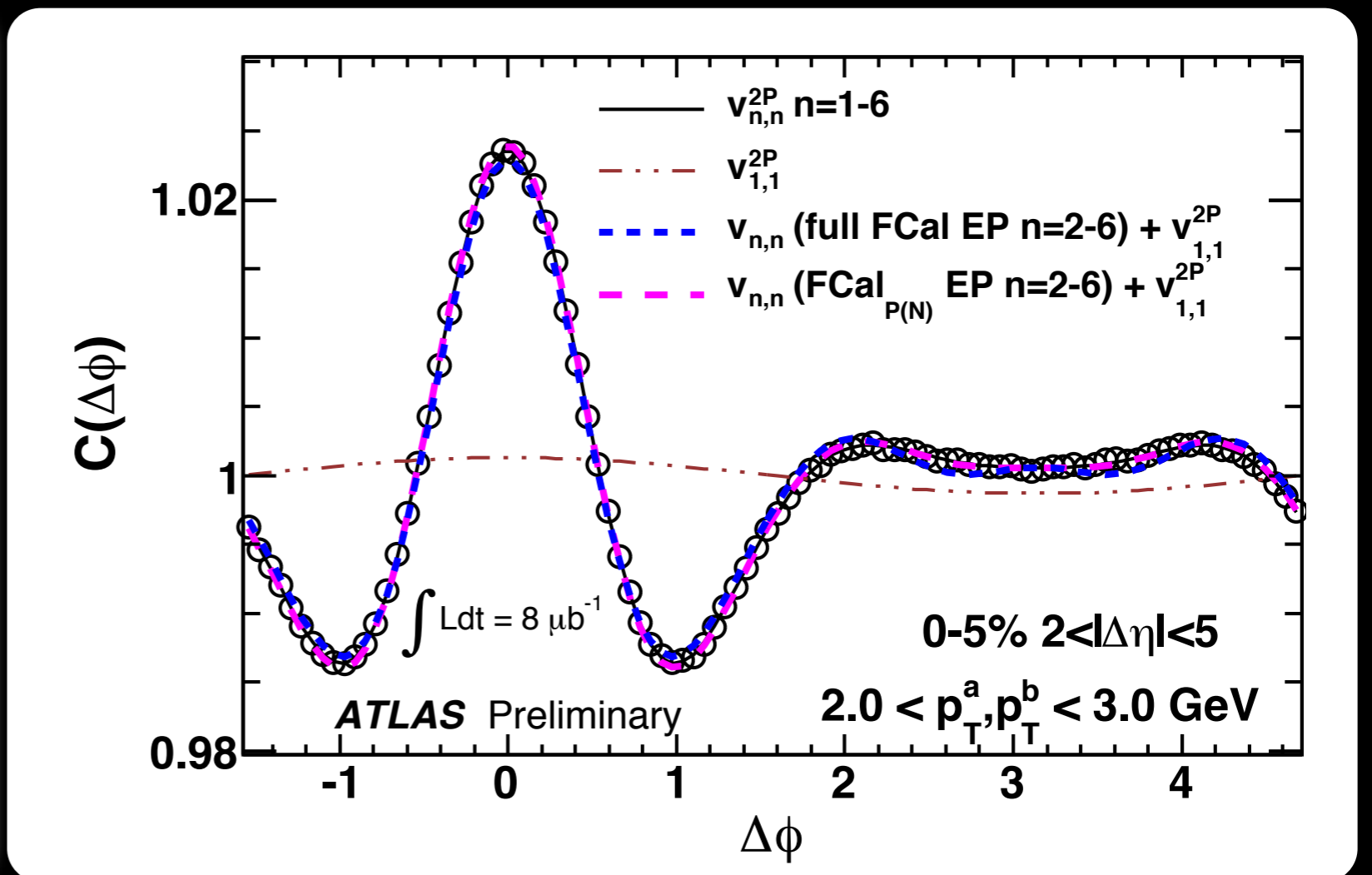
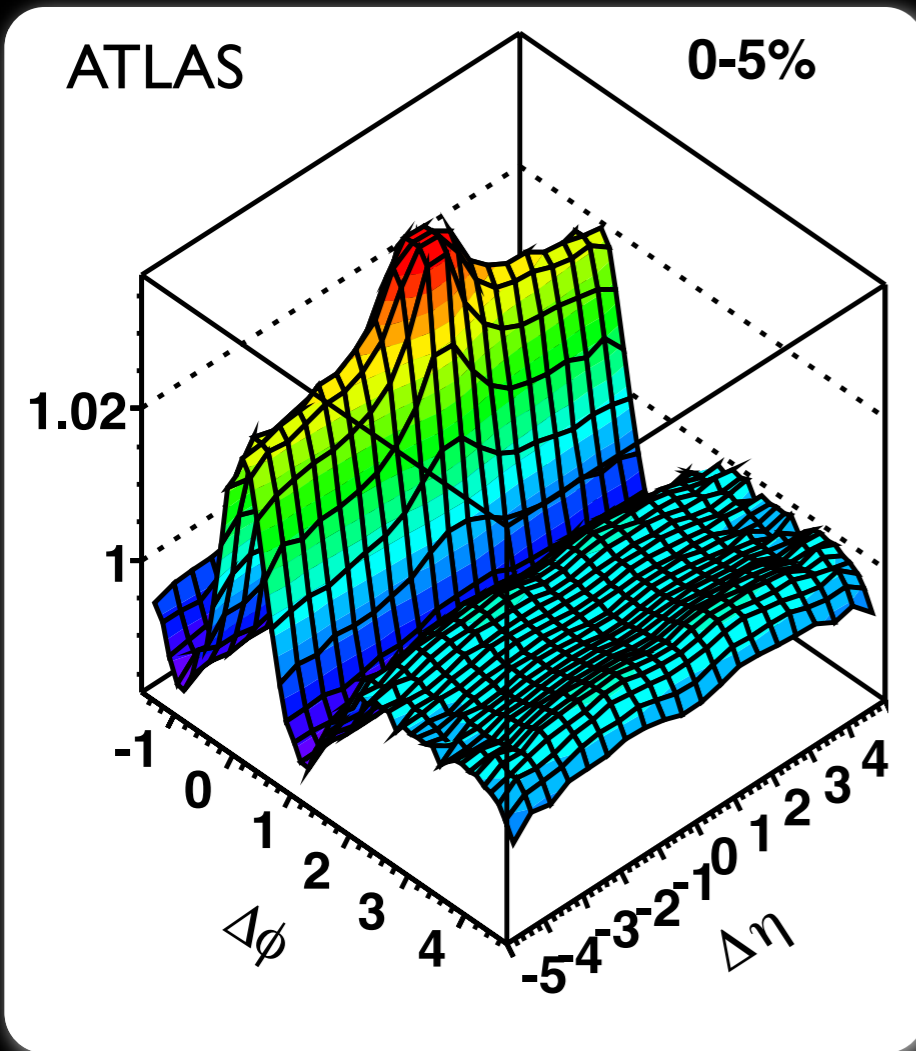
For most central collisions  $v_3$  and  $v_4$  become at intermediate  $p_T$  larger than  $v_2$



ATLAS-CONF-2011-074



# Angular Correlations



ATLAS-CONF-2011-074

Two particle azimuthal correlations can be described efficiently with the first 6  $v_n$  coefficients and naturally explain the so called ridge and mach cone structure first observed at RHIC which were thought to be due to jet induced medium modifications

# Conclusions

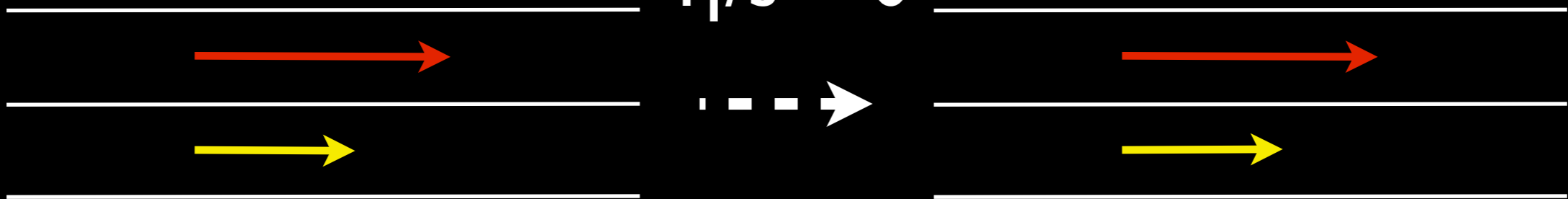
- Anisotropic flow measurements provide strong constraints on the bulk properties of hot and dense matter produced at RHIC and LHC energies and have led to the new paradigm of the QGP as the so called perfect liquid
  - At the LHC we observe even stronger flow than at RHIC which is expected for almost perfect fluid behavior
- The first measurements of  $v_3$  and higher  $v_n$ 's have recently been made at RHIC and at the LHC and indicate that these flow coefficients behave as expected from fluctuations of the initial spatial eccentricity (geometry!) and a created system which has a small  $\eta/s$ 
  - provide new strong experimental constraints on  $\eta/s$  and initial conditions

Thanks

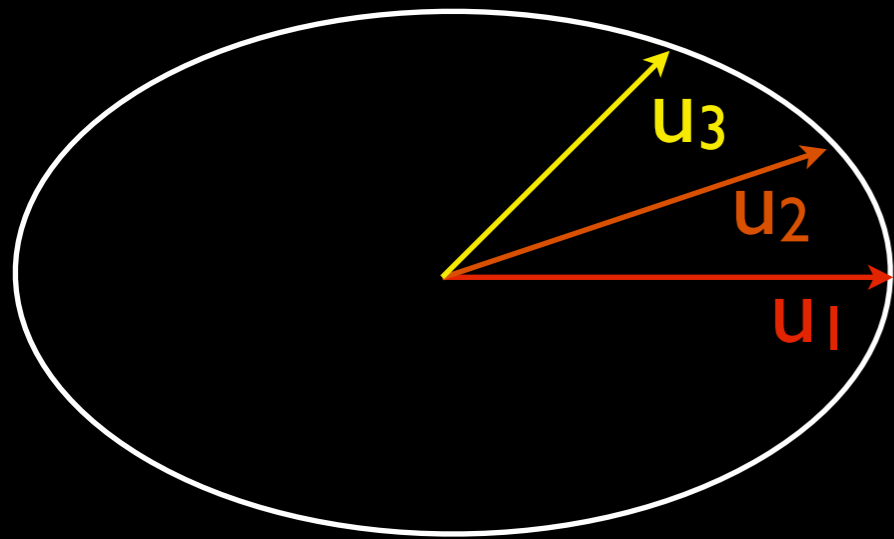
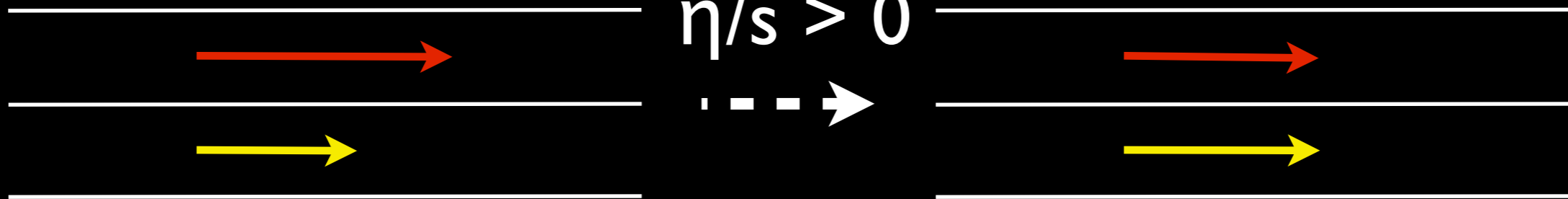
# Backup

# Shear Viscosity

$$\eta/s = 0$$

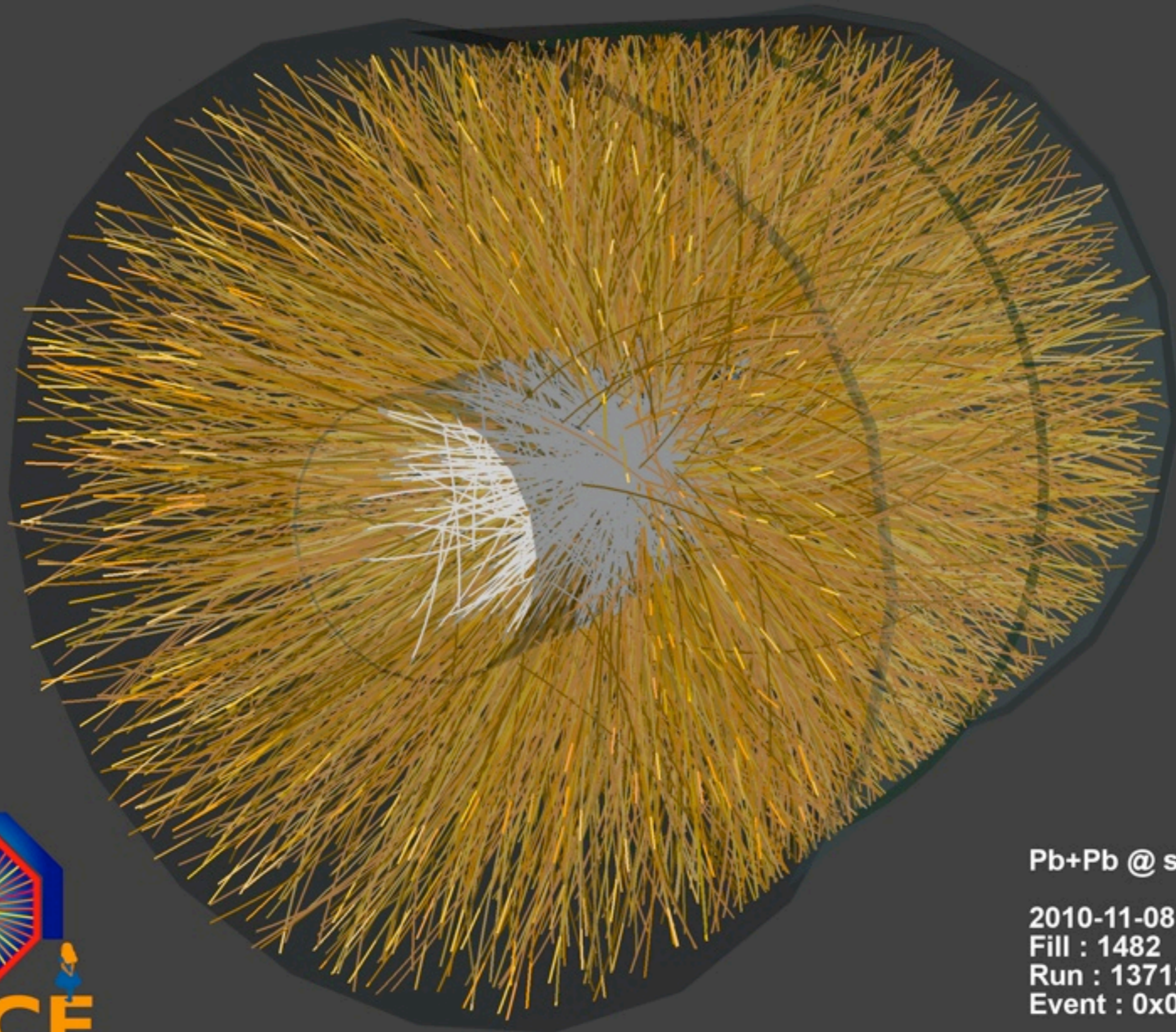


$$\eta/s > 0$$



$u_1 > u_2 > u_3$  shear viscosity will make them equal and destroy the elliptic flow  $v_2$  higher harmonics represent smaller differences which get destroyed more easily, and which, if measurable, makes them more sensitive probes to  $\eta/s$

# First Pb-Pb collisions!



Pb+Pb @  $\sqrt{s} = 2.76$  ATeV

2010-11-08 11:30:46

Fill : 1482

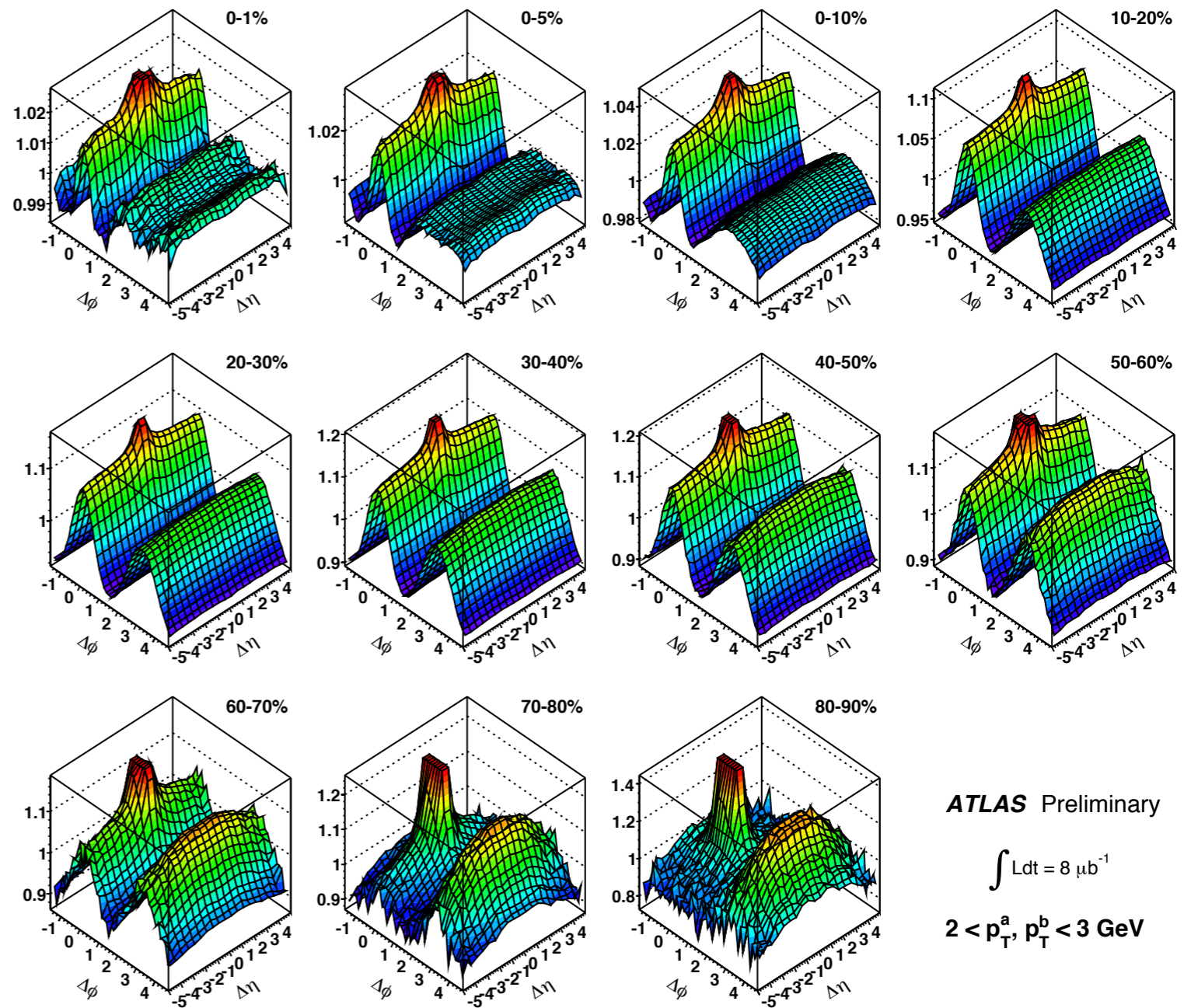
Run : 137124

Event : 0x00000000D3BBE693

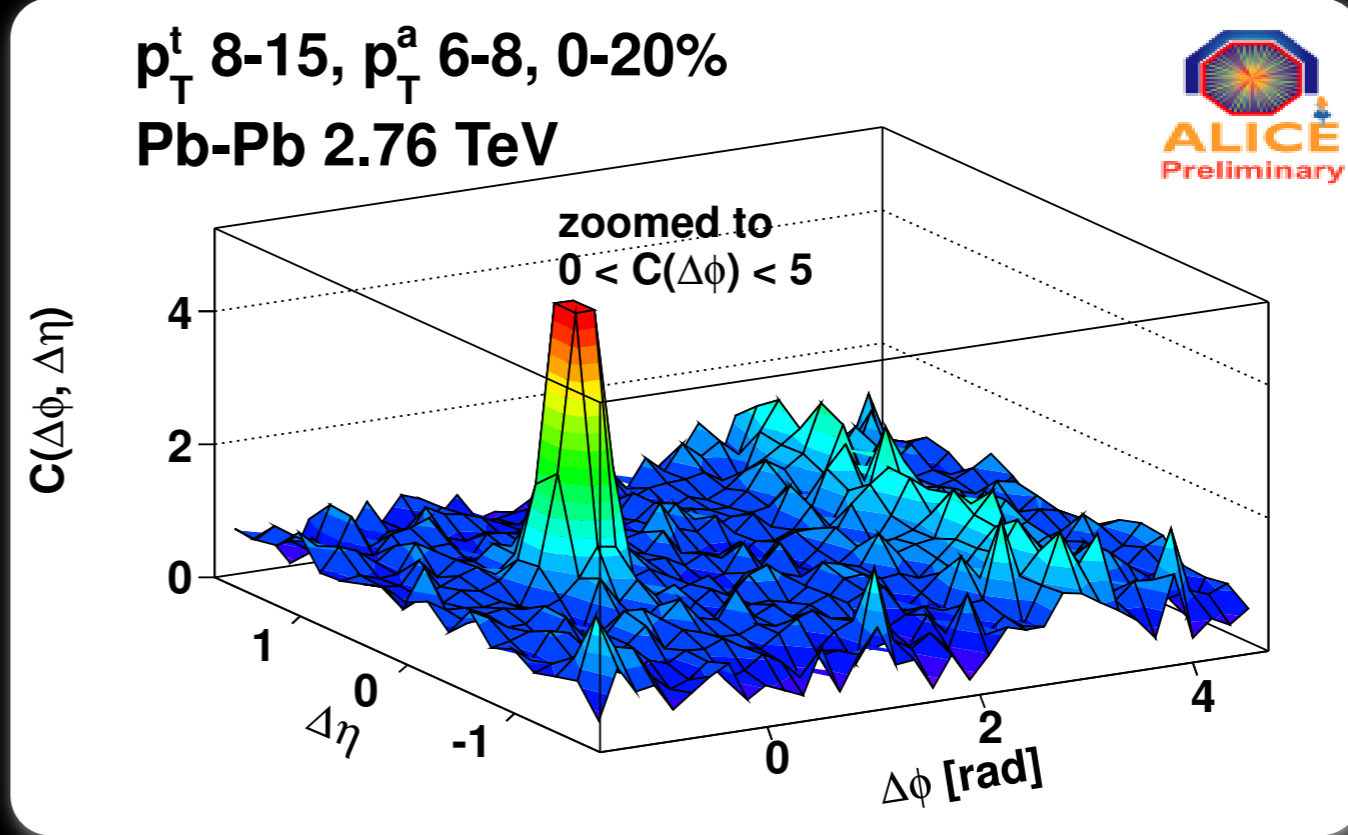
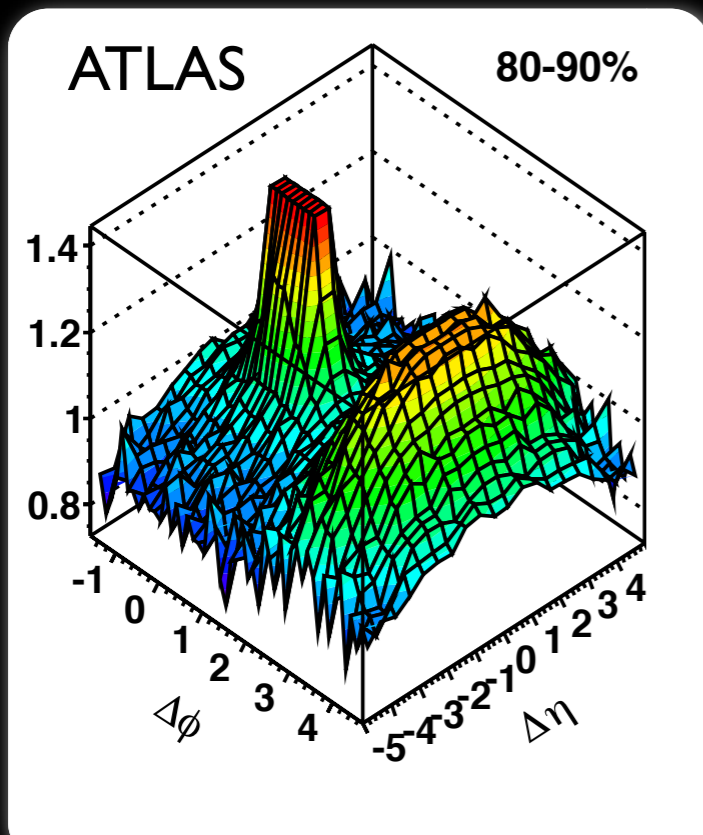
# Angular Correlations at the LHC

$$C(\Delta\phi\Delta\eta) \equiv \frac{N_{\text{mixed}}}{N_{\text{same}}} \frac{d^2 N_{\text{same}}/d\Delta\phi d\Delta\eta}{d^2 N_{\text{mixed}}/d\Delta\phi d\Delta\eta}$$

Contributions to the  
two-particle  $\Delta\phi, \Delta\eta$   
angular correlation  
come from  
anisotropic flow;  $v_1$ ,  
 $v_2, v_3, \dots$ , Jets,  
resonances, HBT, etc

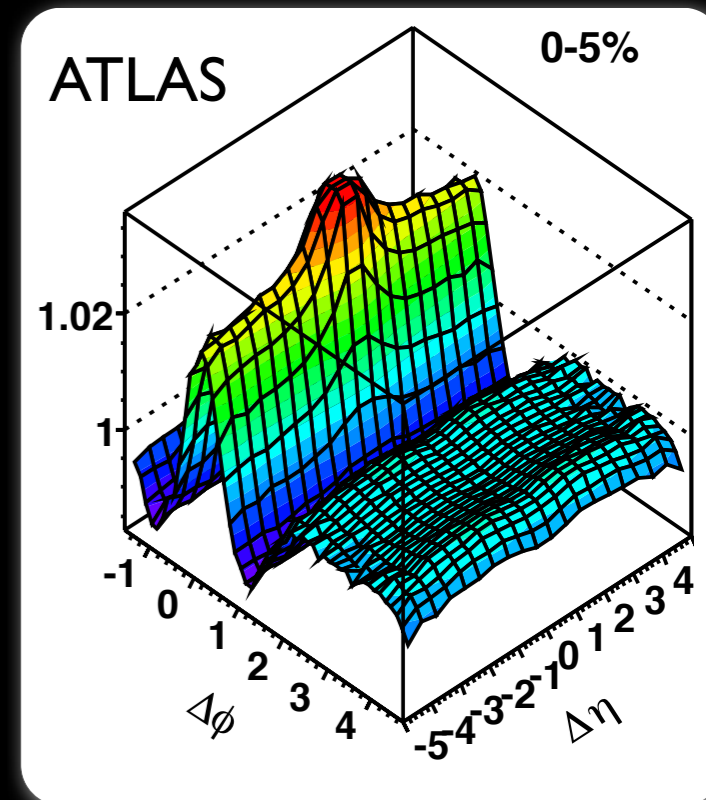
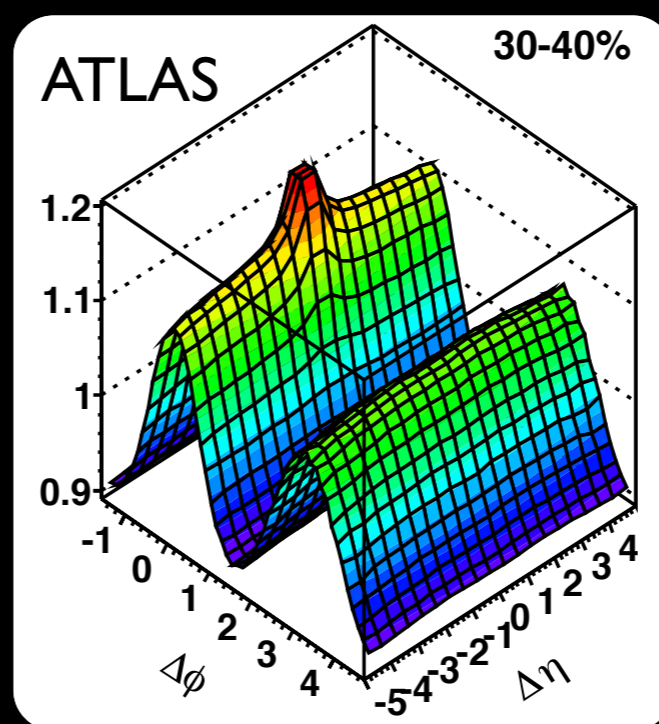


# Angular Correlations



For very peripheral collisions or when triggered with a high- $p_T$  charged particle the dominant contribution to two particle angular correlations is due to jet-correlations

More central heavy ion collisions look very very different!

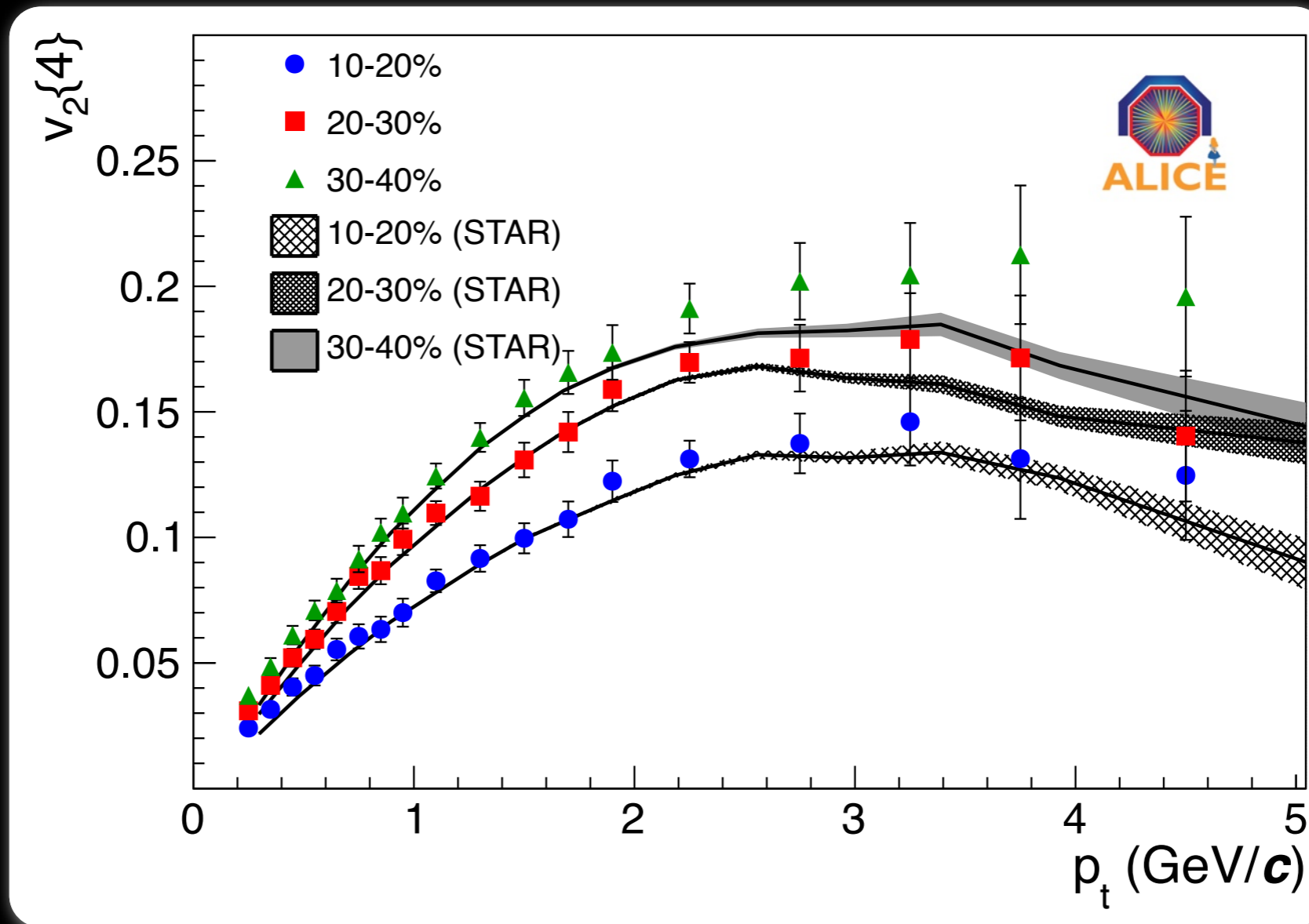




# $v_2$ as function of $p_t$

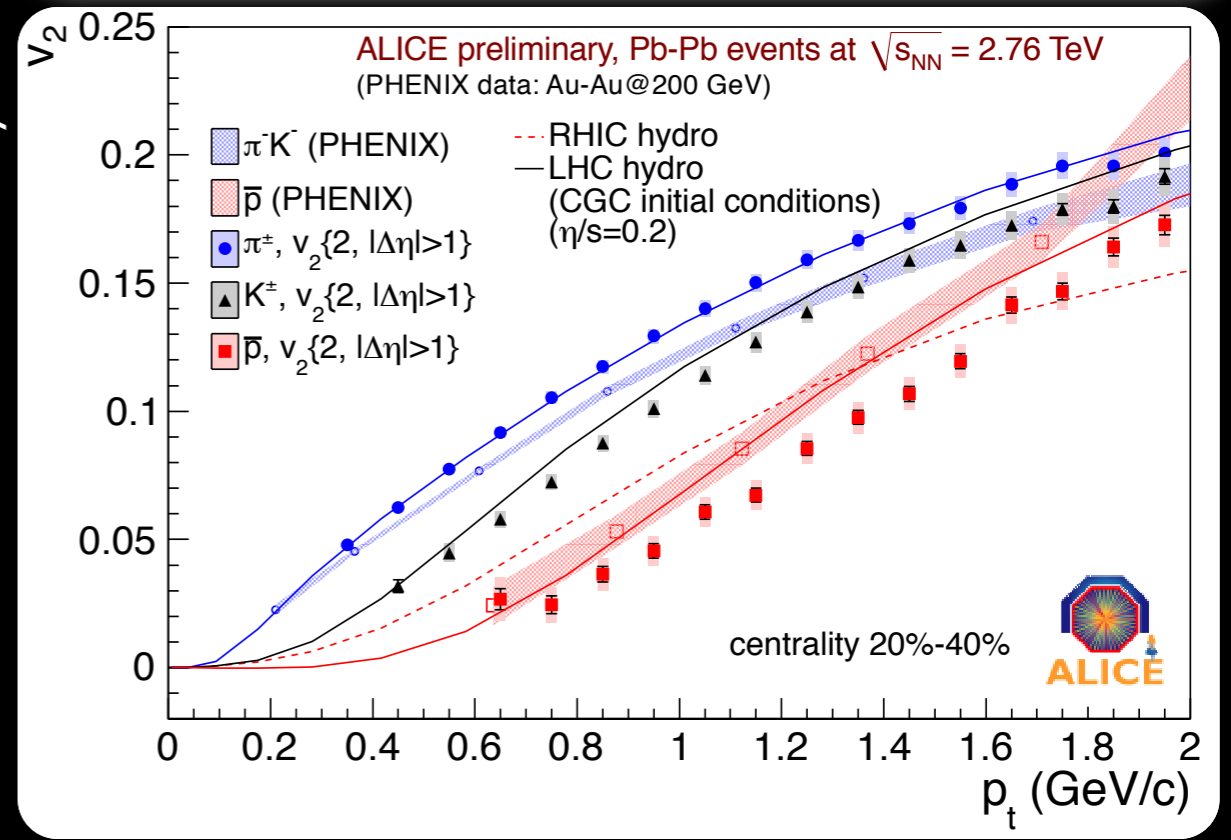
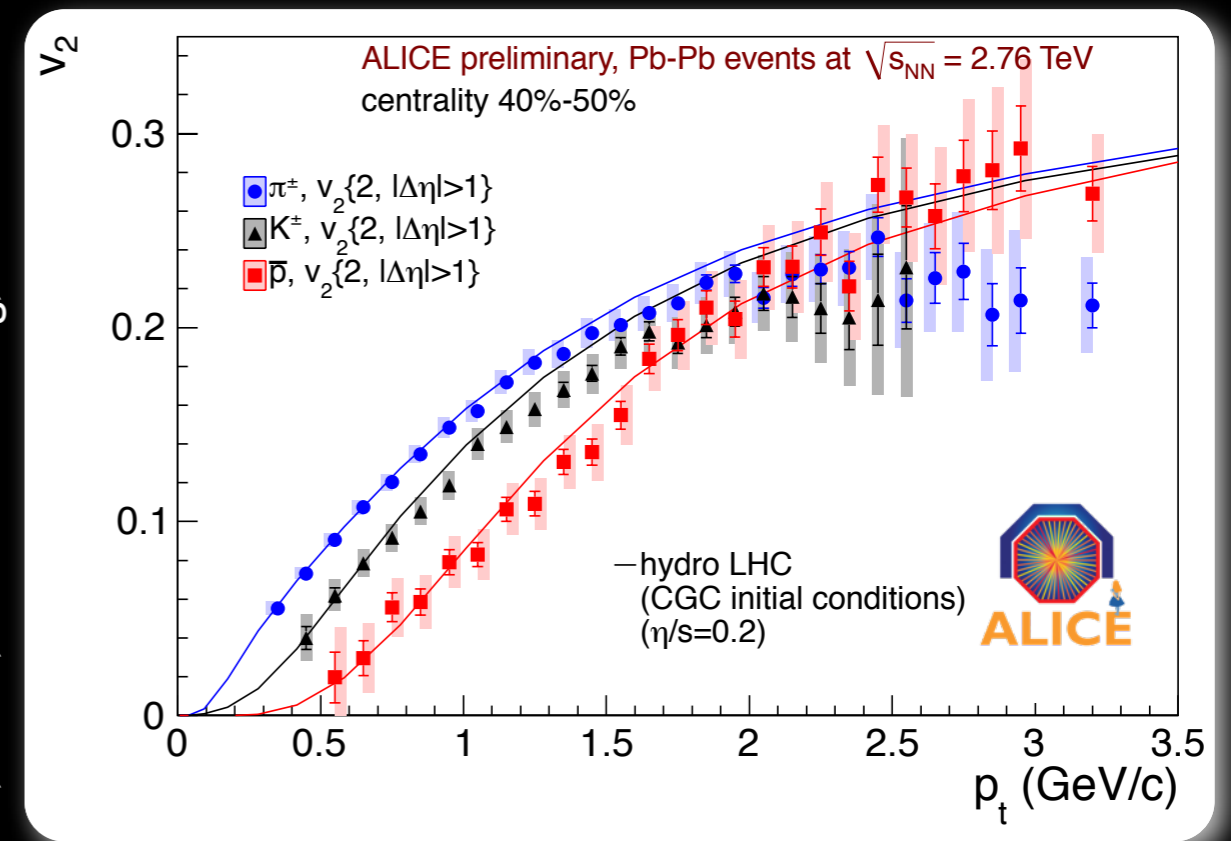
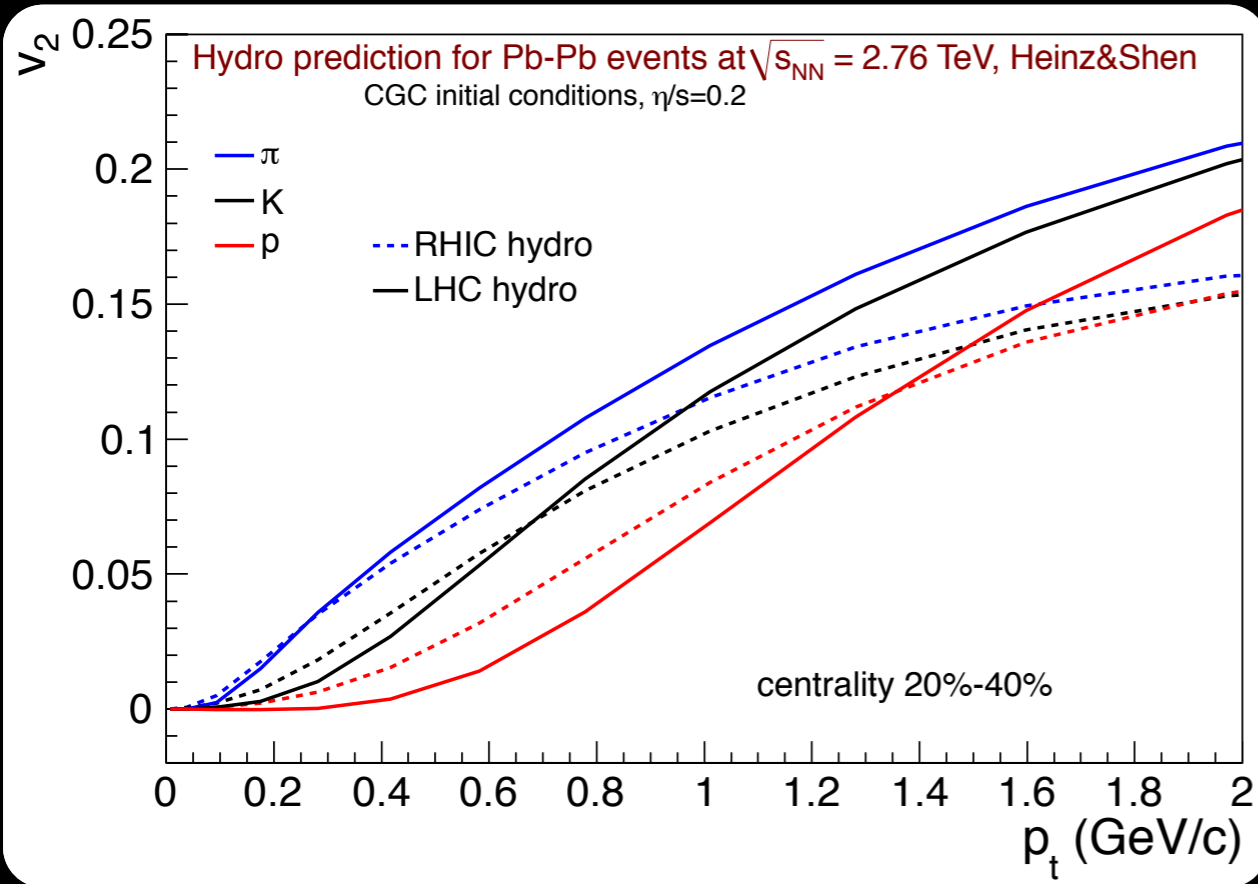
K. Aamodt et al. (ALICE Collaboration)

PRL 105, 252302 (2010)



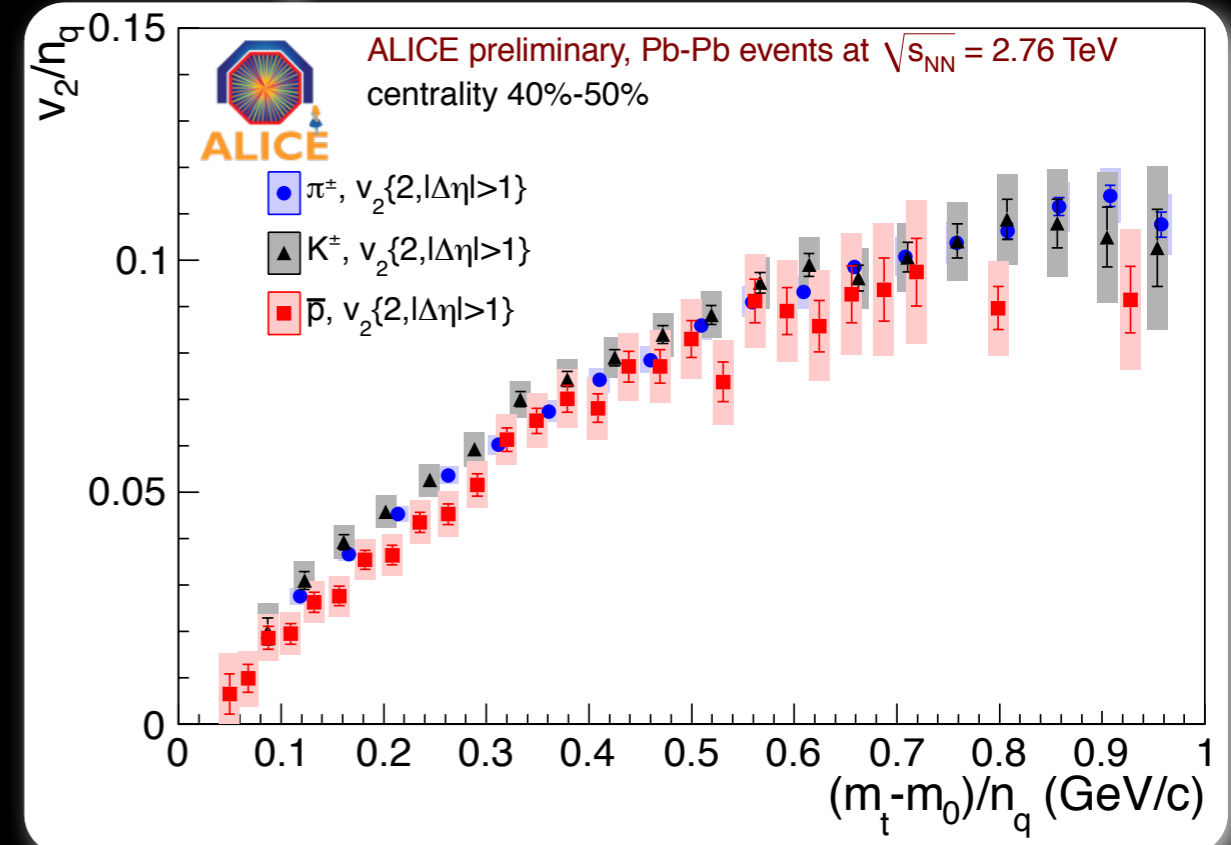
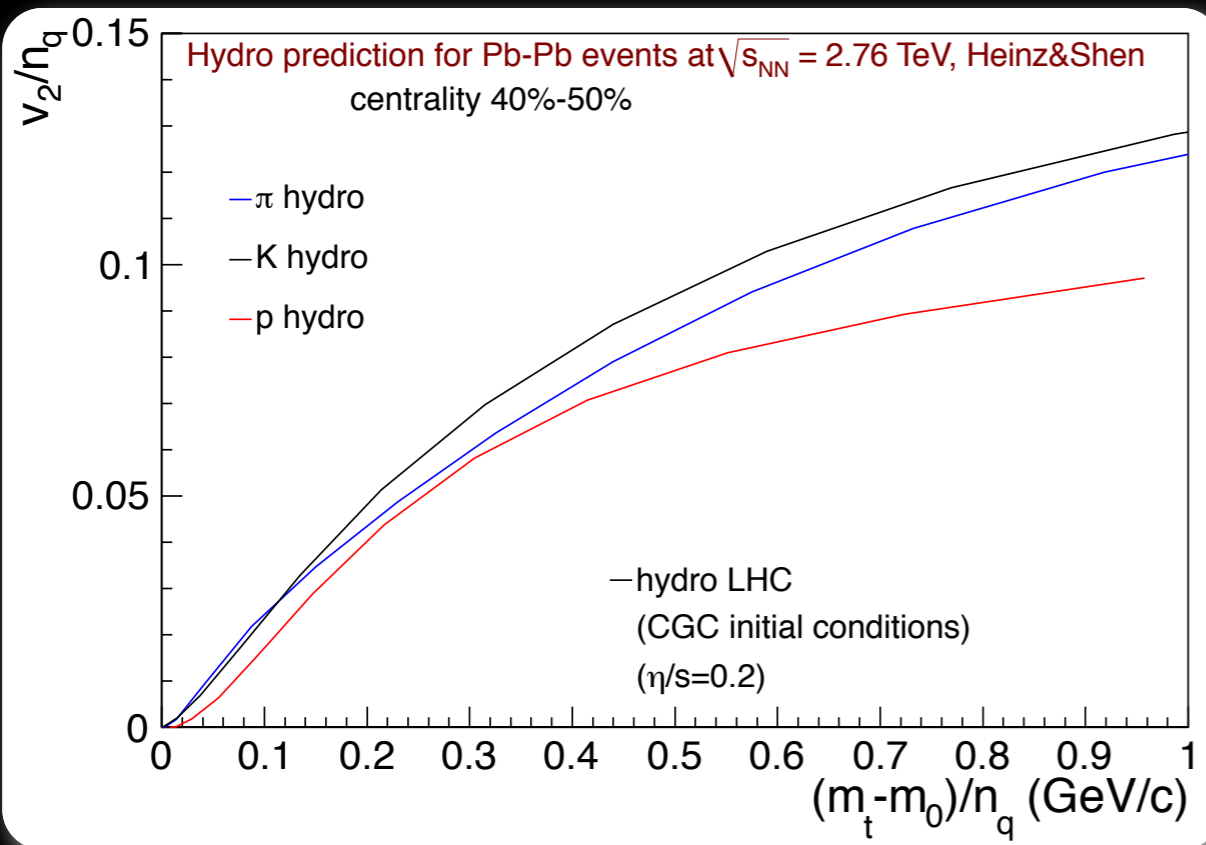
Elliptic flow as function of transverse momentum does not change much from RHIC to LHC energies, can we understand that?

# $v_2$ for identified particles



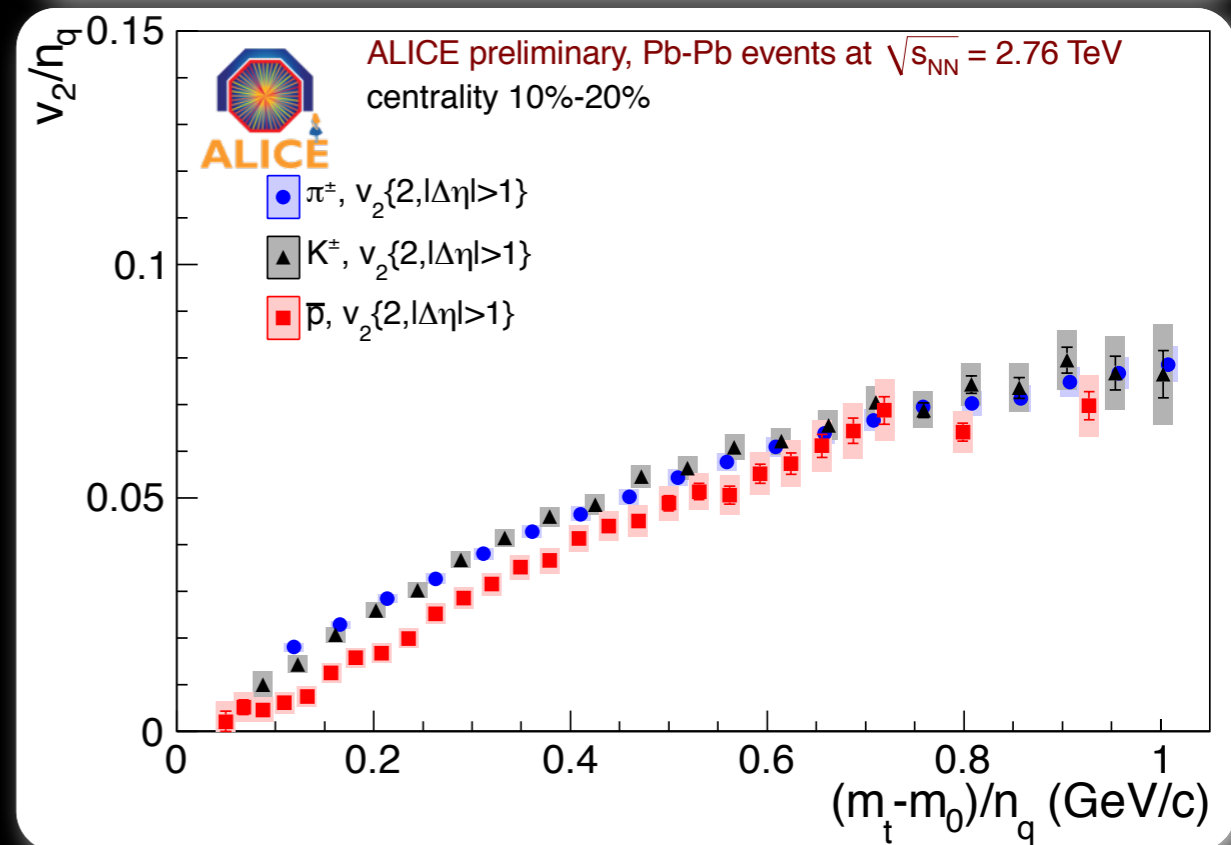
hydro models predict larger mass splitting  
data shows mass splitting and agrees well with hydro predictions for mid-central collisions

# $v_2$ for identified particles



at small  $(m_t - m_0)/n_q$  the scaling in the data resemble the scaling as observed in hydrodynamics

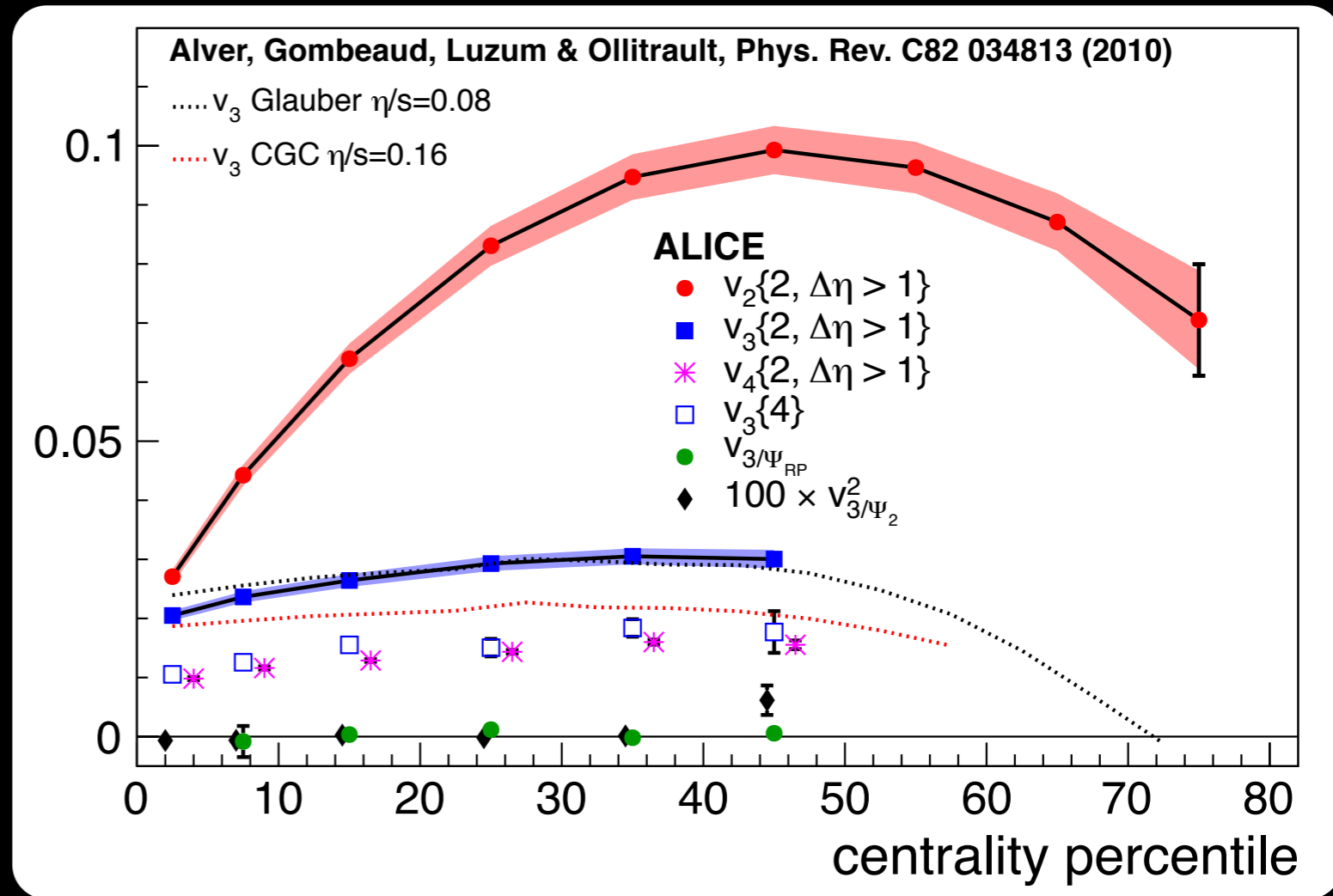
at large  $(m_t - m_0)/n_q$  the quark scaling seems to work better



# $v_2$ , $v_3$ and $v_4$ at the LHC

We observe significant  $v_3$  which compared to  $v_2$  has a much weaker centrality dependence

The centrality dependence and magnitude are similar to predictions for MC Glauber with  $\eta/s=0.08$  but above MC-KLN CGC with  $\eta/s=0.16$

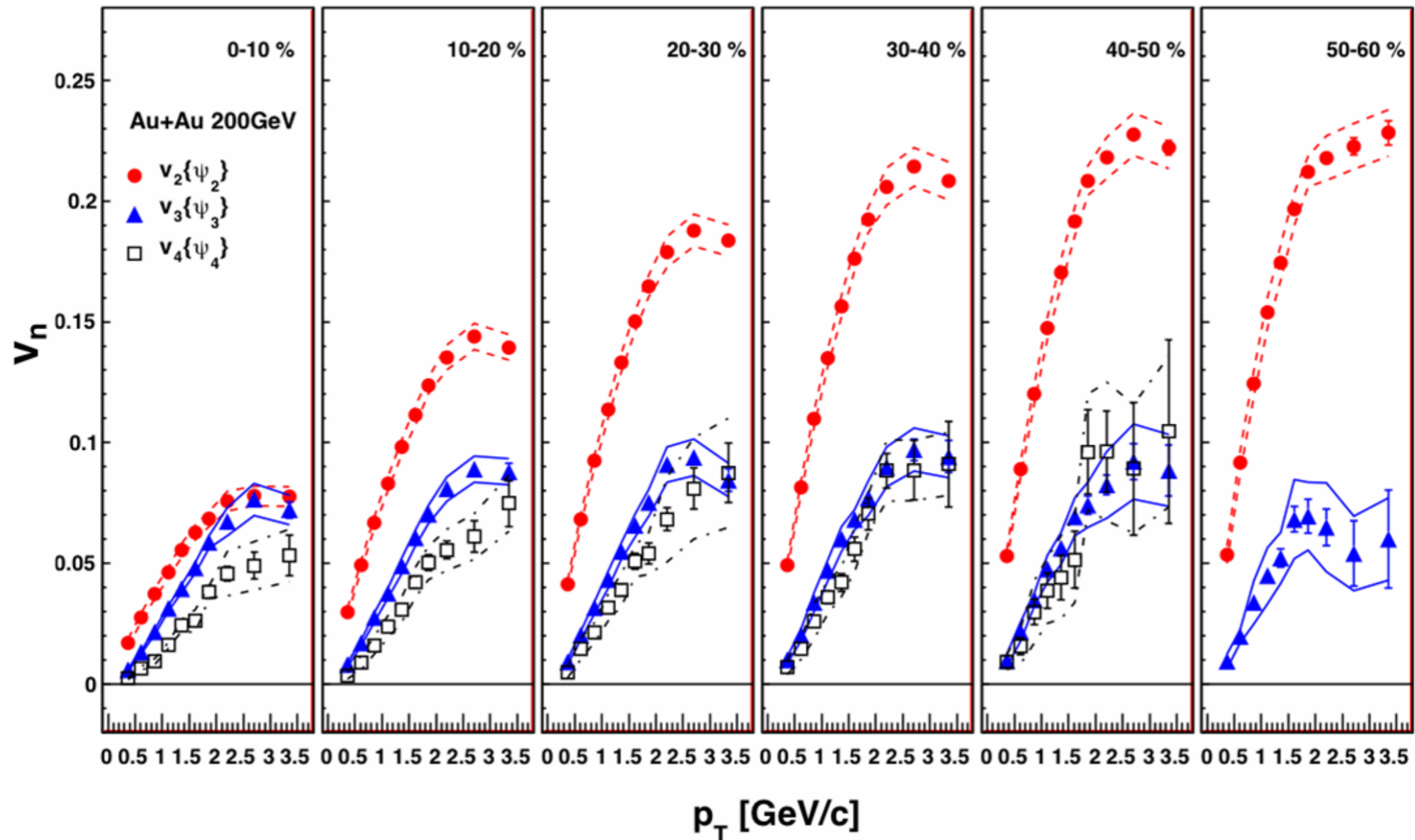


ALICE Collaboration, arXiv:1105.3865, PRL 107, 032301 (2011)

The  $v_3$  with respect to the reaction plane determined in the ZDC and with the  $v_2$  participant plane is consistent with zero as expected if  $v_3$  is due to fluctuations of the initial eccentricity

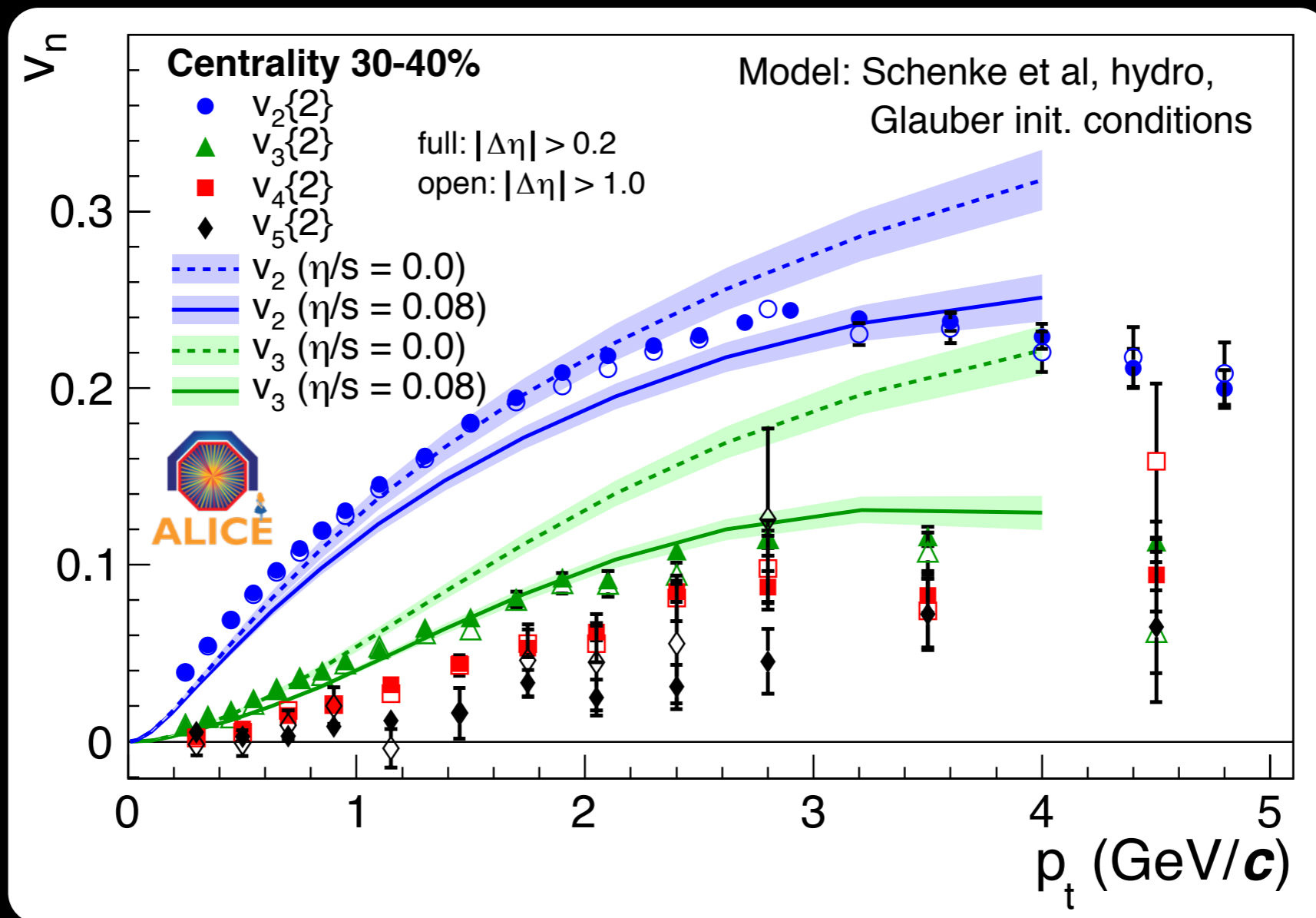
# $v_2$ , $v_3$ and $v_4$ at RHIC

PHENIX, arXiv:1105.3928



As at the LHC we observe at RHIC a significant  $v_3$  and  $v_4$  which compared to  $v_2$  have a much weaker centrality dependence

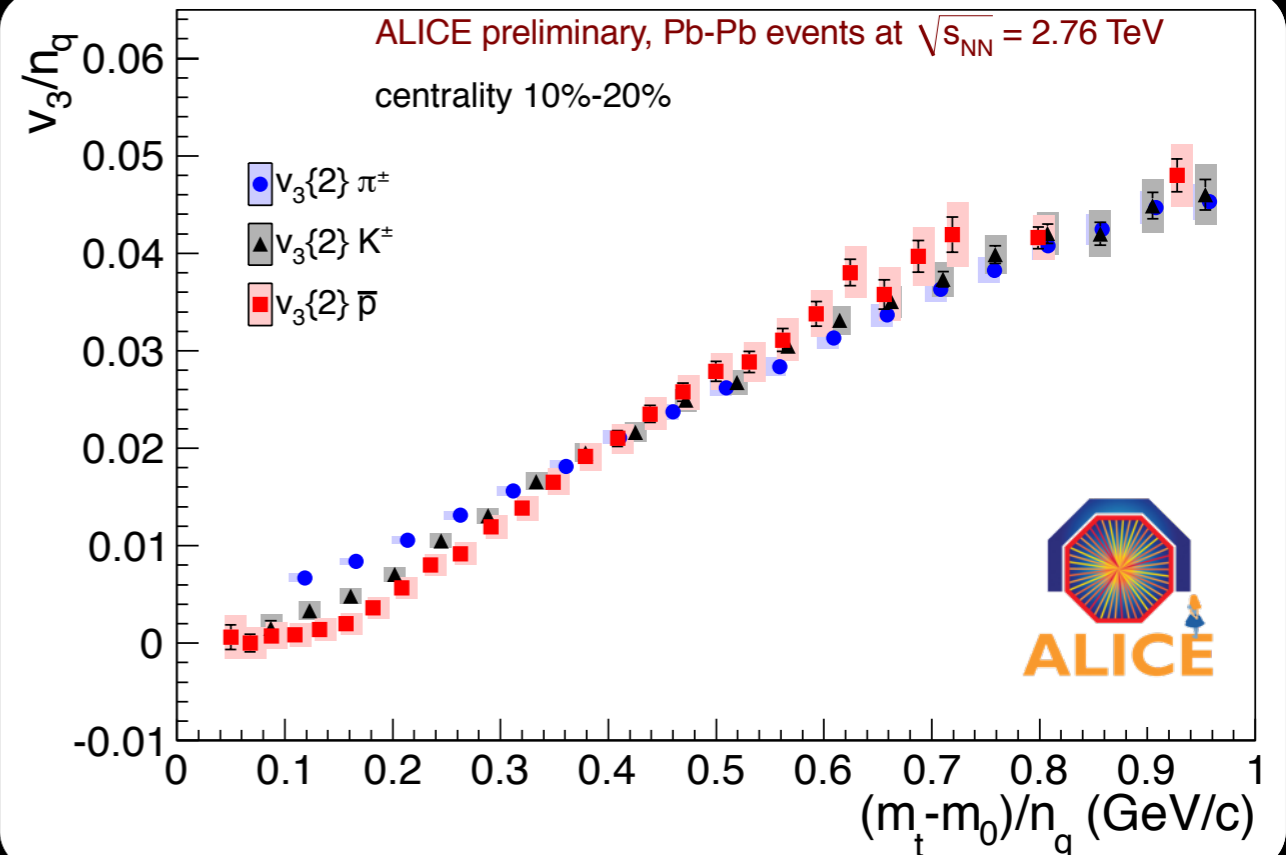
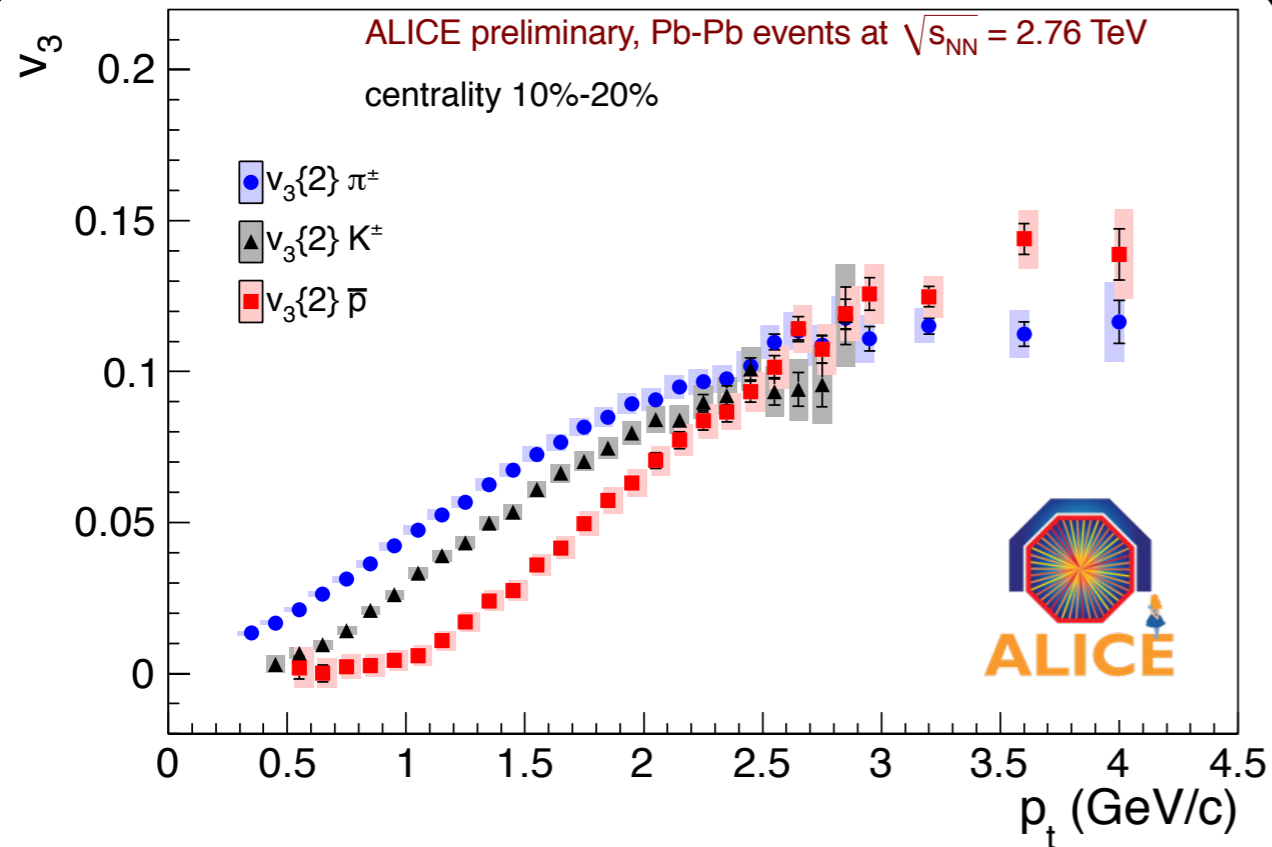
# $v_2, v_3, v_4$ and $v_5$ at the LHC



ALICE Collaboration, arXiv:1105.3865, PRL 107, 032301 (2011)

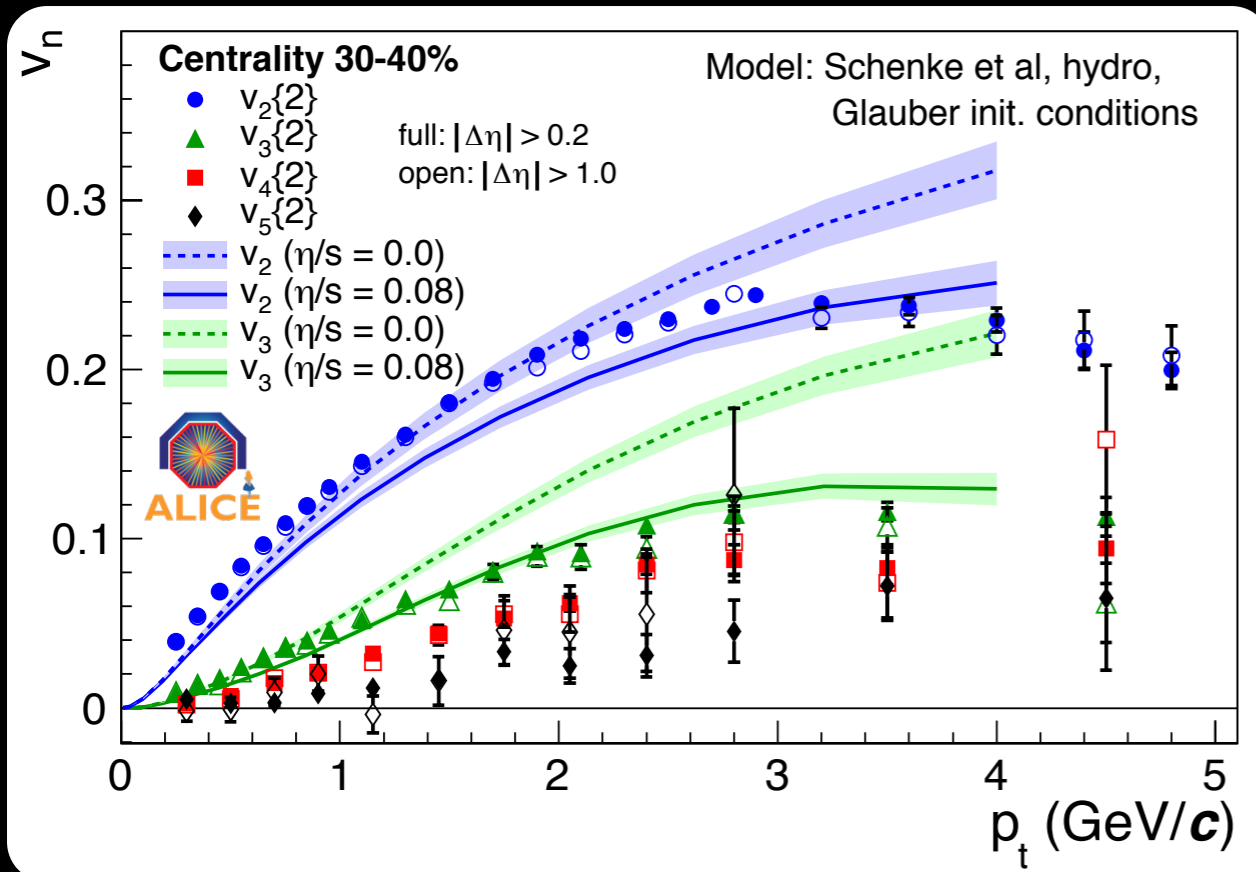
The overall dependence of  $v_2$  and  $v_3$  is described  
However there is no simultaneous description with a  
single  $\eta/s$  of  $v_2$  and  $v_3$  for Glauber initial conditions

# Triangular Flow



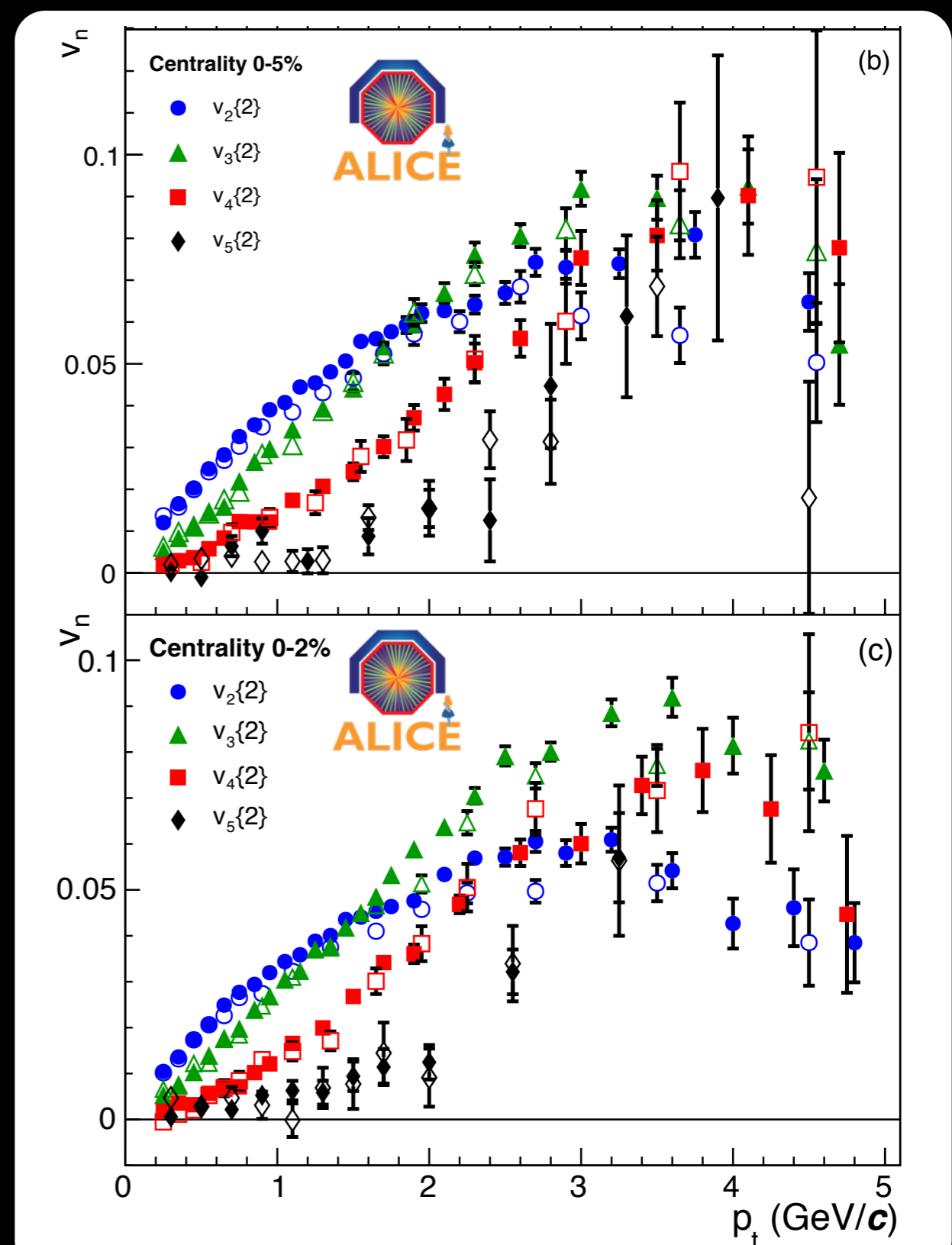
The behavior of  $v_3$  as function of  $p_t$  for pions, Kaons and protons shows the same features as we already observed for  $v_2$   
(we observe the mass splitting and, in addition, the crossing of the pions with protons at intermediate  $p_t$ , which for  $v_2$  was considered as a signature for coalescence/recombination)

# Other Harmonics



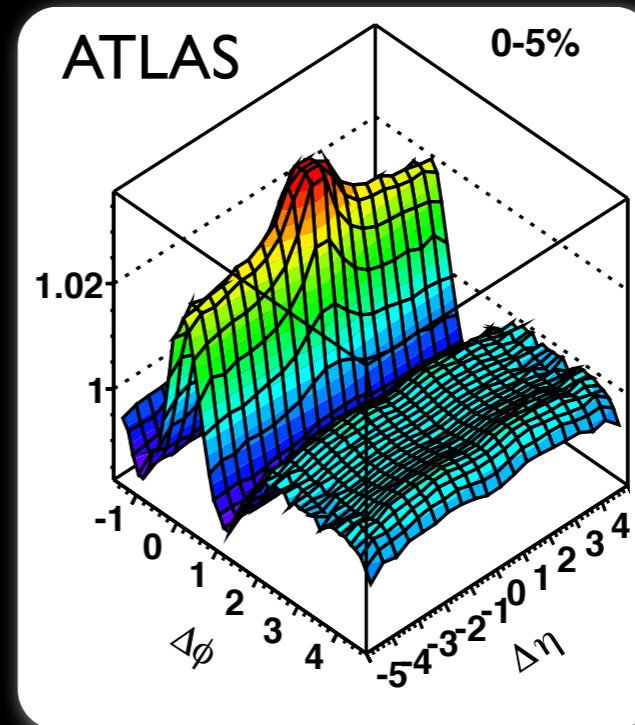
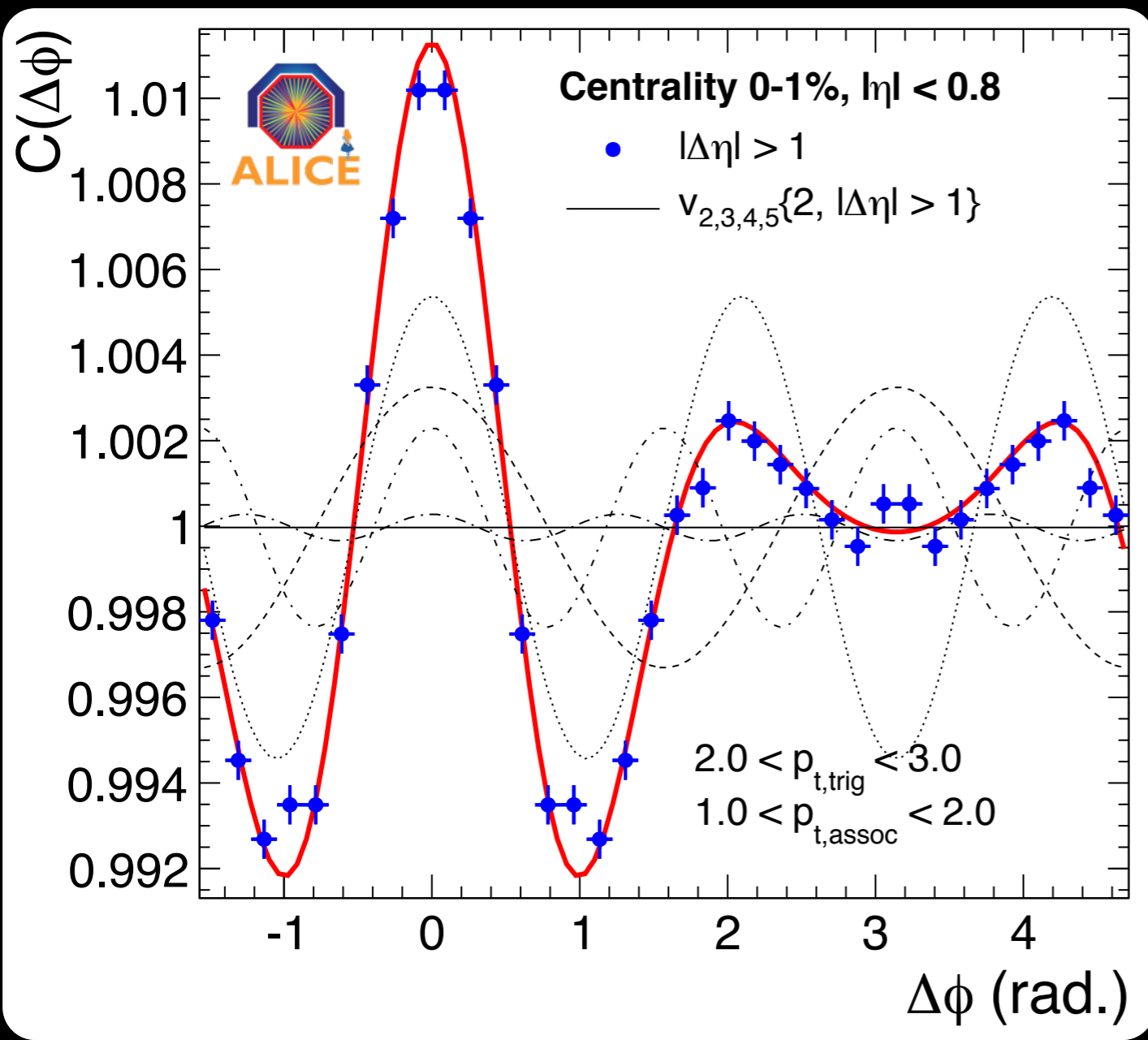
For central collisions at intermediate  $p_t$  the higher harmonics  $v_3$  and  $v_4$  cross  $v_2$  and become the dominant harmonics

For more central collisions this occurs already at lower  $p_t$





# Other Harmonics



We observe a doubly-peaked structure in the azimuthal correlation function opposite to the trigger particle

The red line shows the sum of the measured anisotropic flow Fourier coefficients. Those flow coefficients give a natural description of the observed correlation structure (no need for Mach cones)

$$C(\Delta\phi) \equiv \frac{N_{\text{mixed}}}{N_{\text{same}}} \frac{dN_{\text{same}}/d\Delta\phi}{dN_{\text{mixed}}/d\Delta\phi}$$