

# Top signals at the LHC

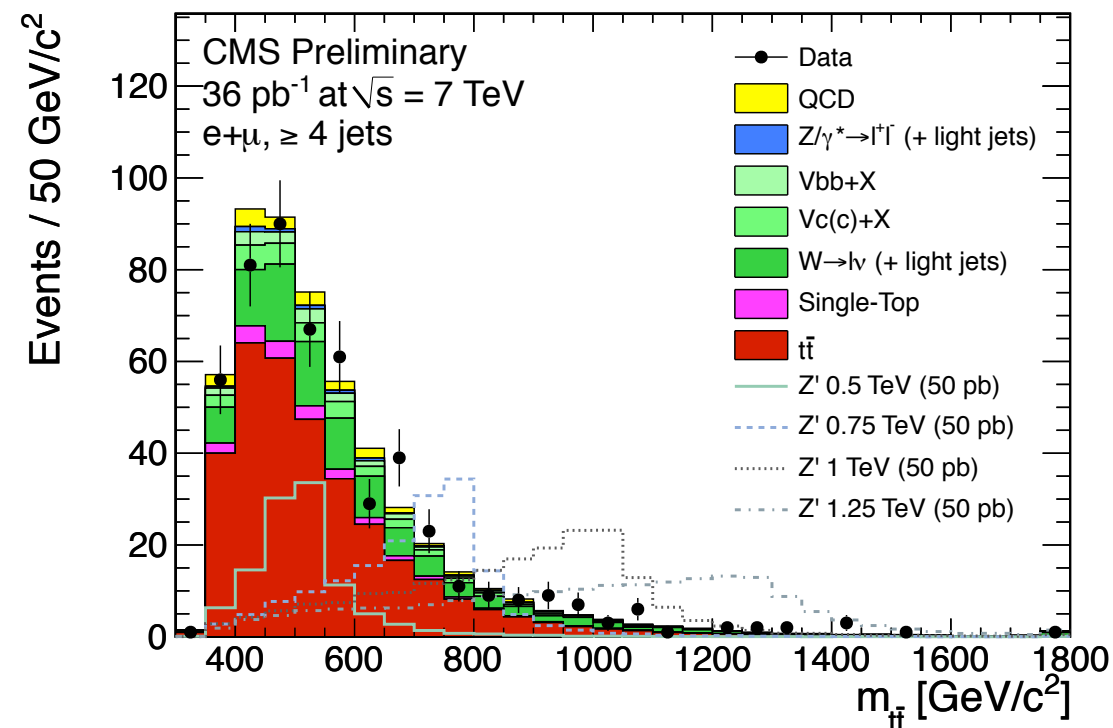
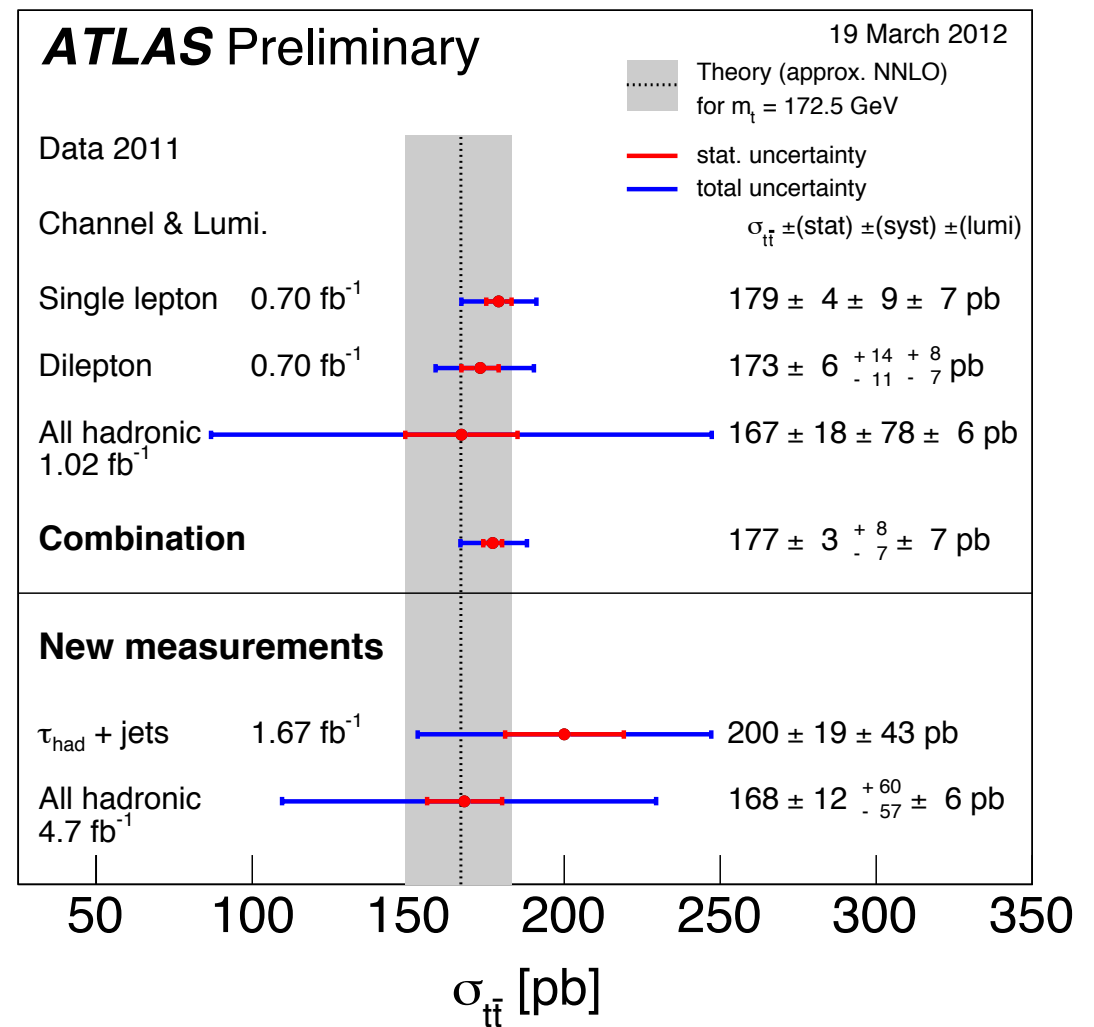
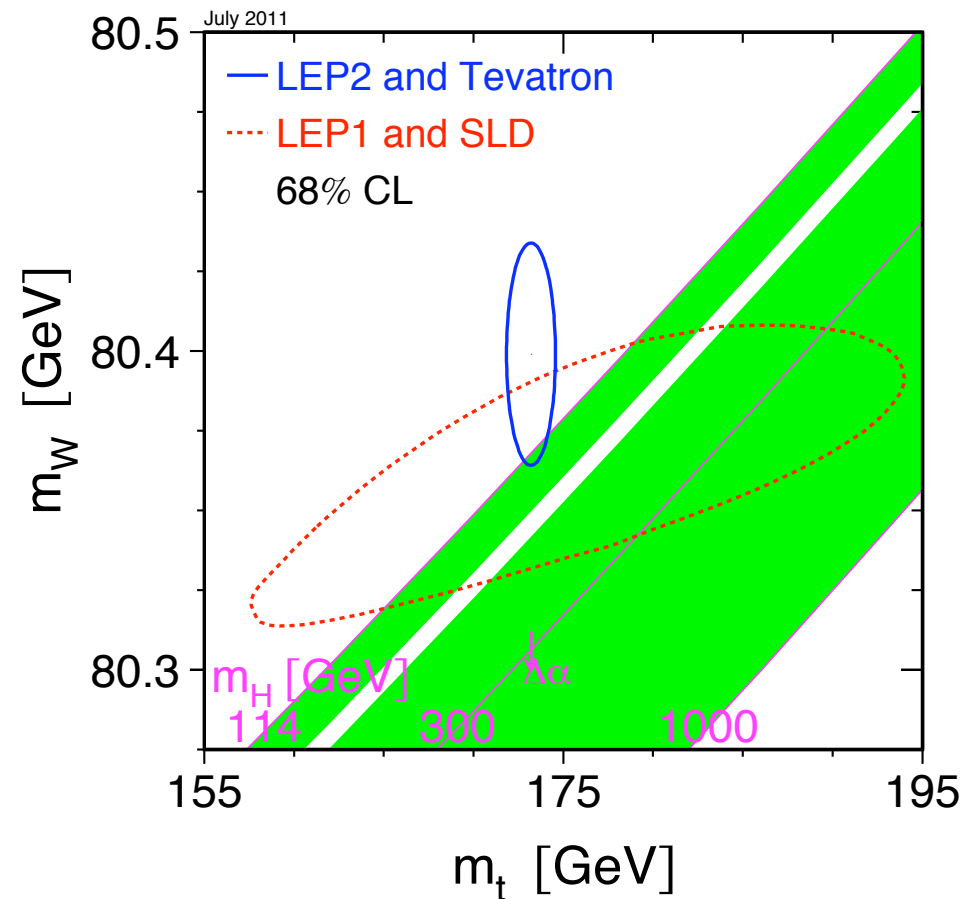
Lian-Tao Wang  
University of Chicago

Chicago 2012 workshop on LHC physics  
May 2, 2011

# Main message

- Top (bottom) rich channels are the most likely places for new physics to show up.
- It is definitely worth while to exhaust every possibilities.
- I will remind you the main motivations and give a (very partial and sketchy) list of possibilities.
  - ▶ Highlights a few new developments.

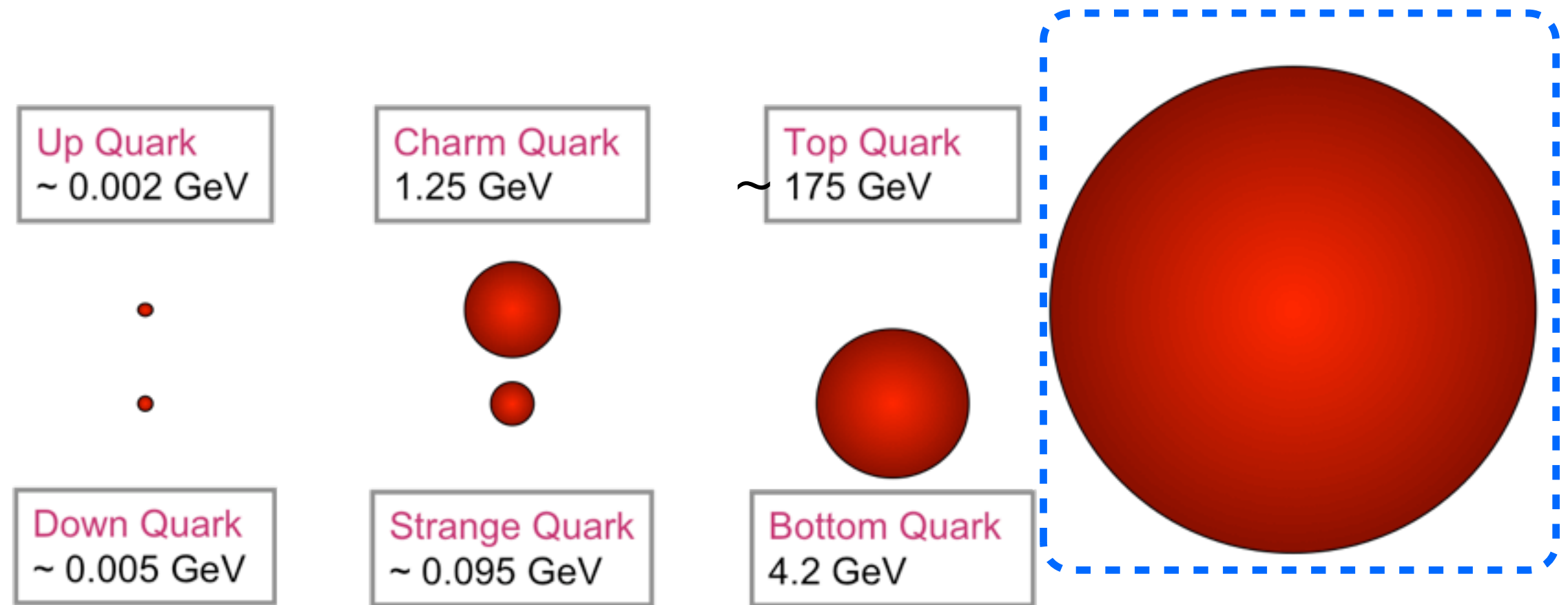
# Measuring the top



— Rare decay, spin correlation,  
 W helicity...

Top is special

# Top is special



—  $m_{\text{top}} \gg m_{\text{u,d,c,s,b}}$  .

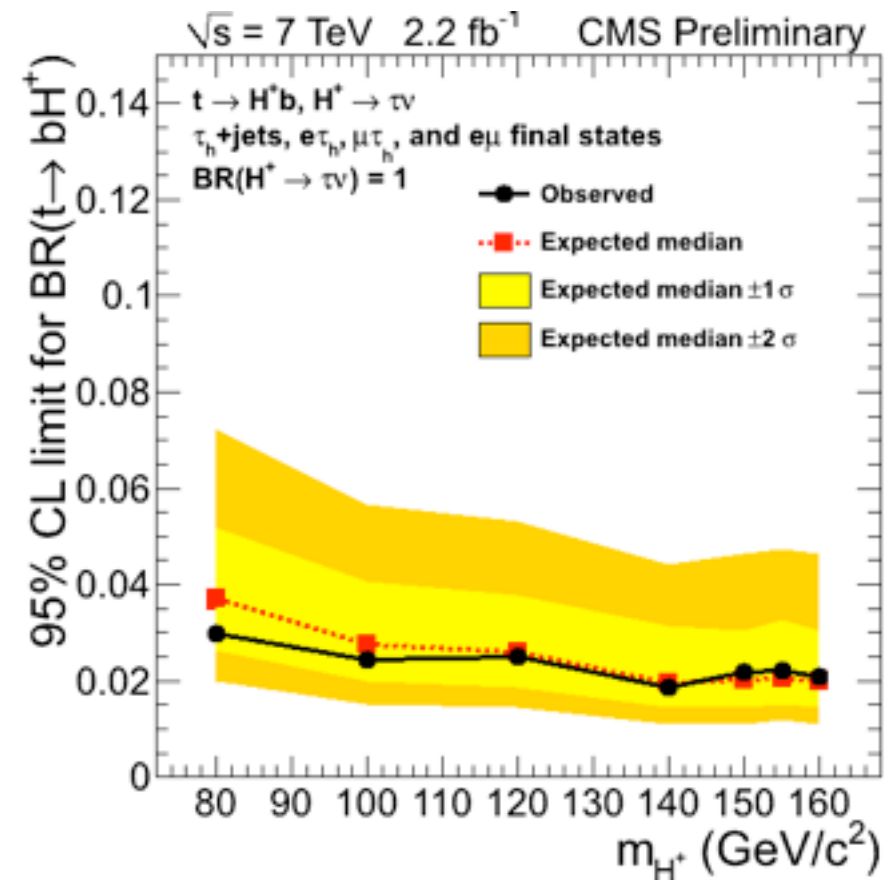
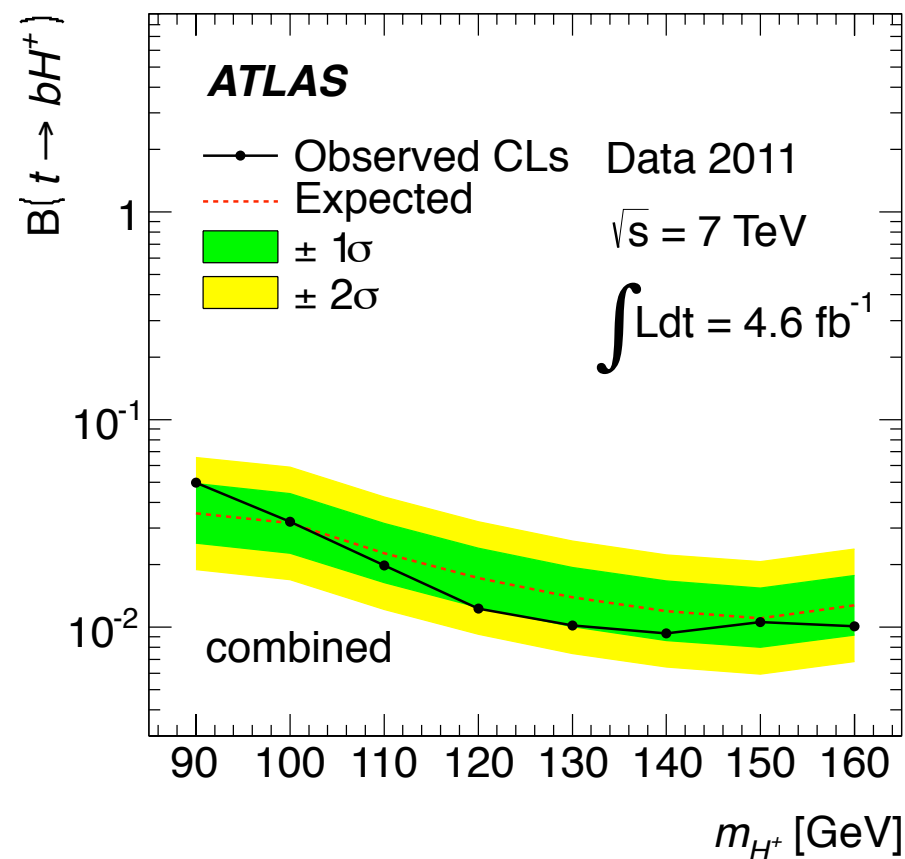
# Tight connection with EWSB.

- SM is chiral. Fermions only get mass after Electroweak symmetry breaking.
- (very) Heavy top  $\rightarrow$  top couples strongly to the mechanism of electroweak symmetry breaking.
  - ▶ e.g. large Yukawa coupling  $y_t h t_L t_R$  to the Higgs

# Top knows more about the Higgs sector.

- Is there an extended Higgs sector? (likely!)

$$t \rightarrow H^+ b$$



For heavier  $H^+$ ,  $H^+ \rightarrow t b$

# $t\bar{t}$ resonances.

- Special dynamics (new force)  $\rightarrow$  heavy top.
  - ▶ New dynamics will create new resonances.
  - ▶ Such new resonances couples strongly to the tops.
- Perhaps there is new strong dynamics responsible to EWSB.
  - ▶ Heavy top  $\rightarrow$  strongly couples to EWSB  $\rightarrow$  strongly couples to new dynamics.



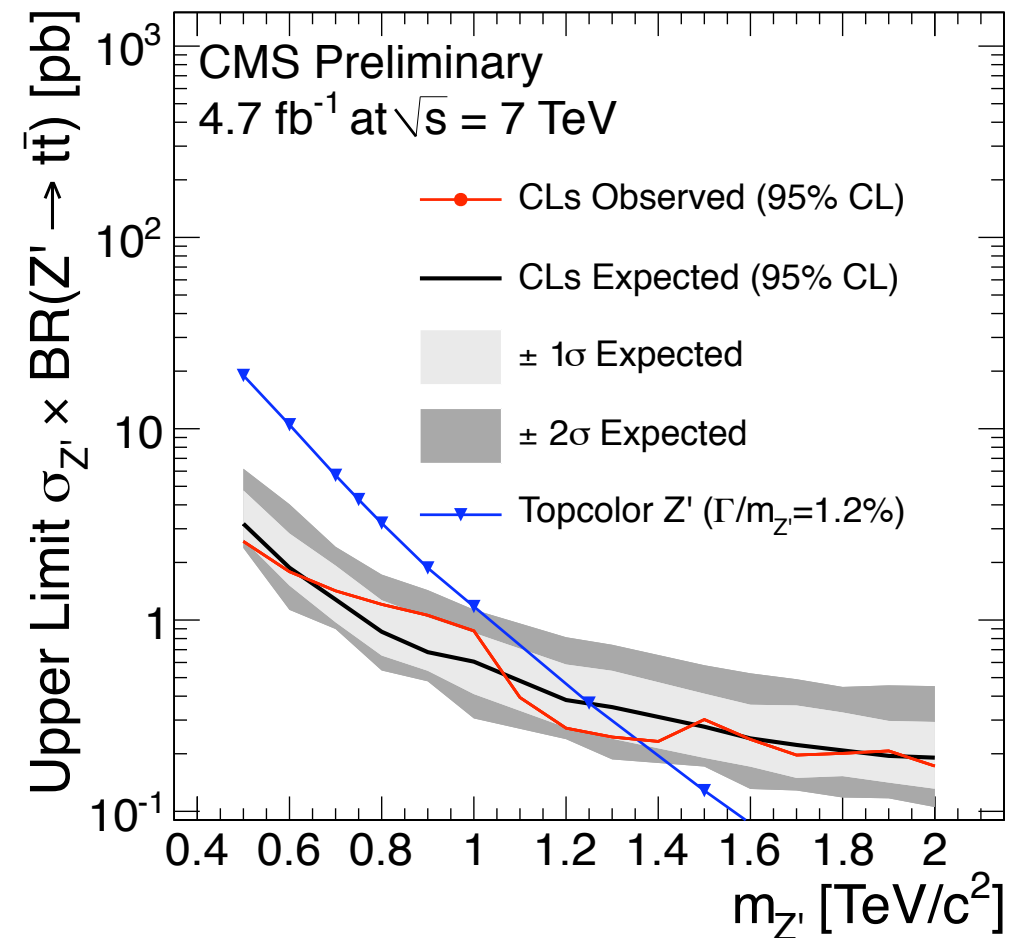
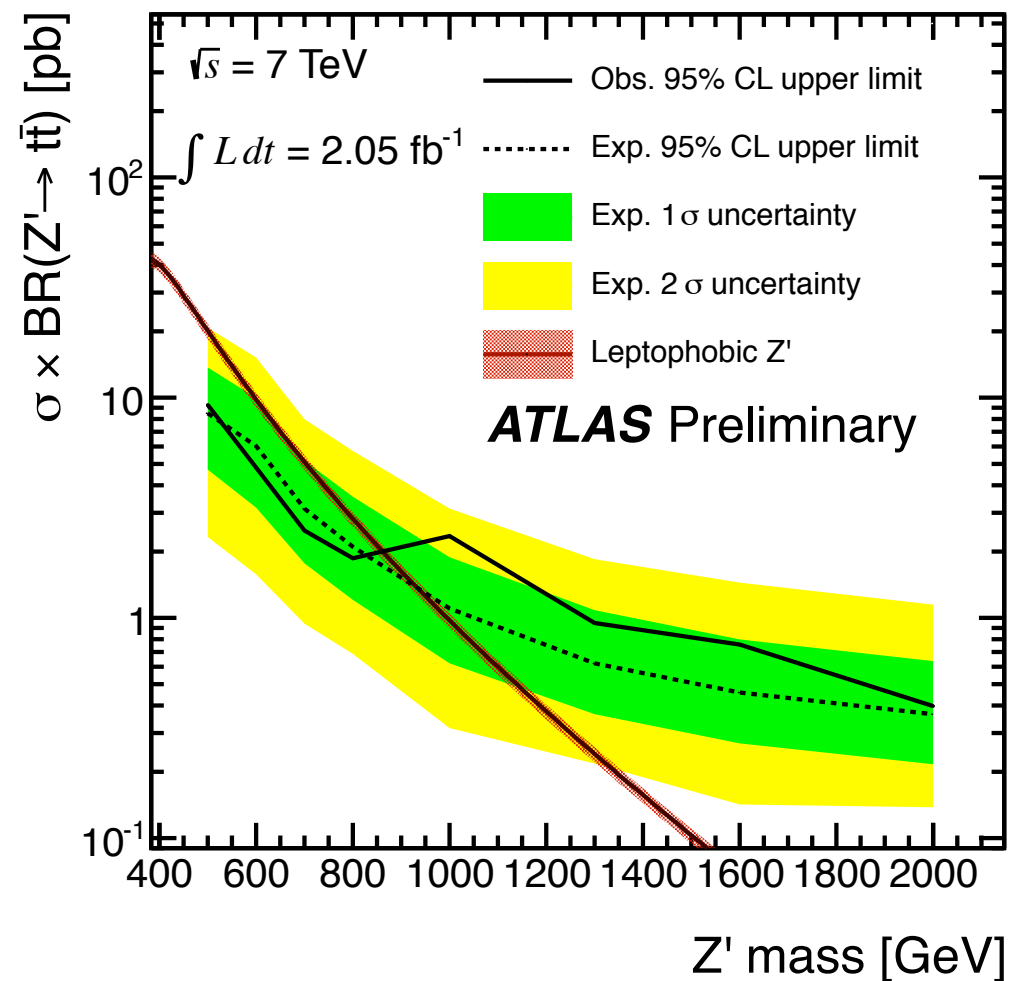
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- Models in this category.
  - Technicolor, deconstruction, composite Higgs, little Higgs, ....
  - extra-dimension, Randall-Sundrum...

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  - extra-dimension, Randall-Sundrum... a.k.a, anything other than SUSY.

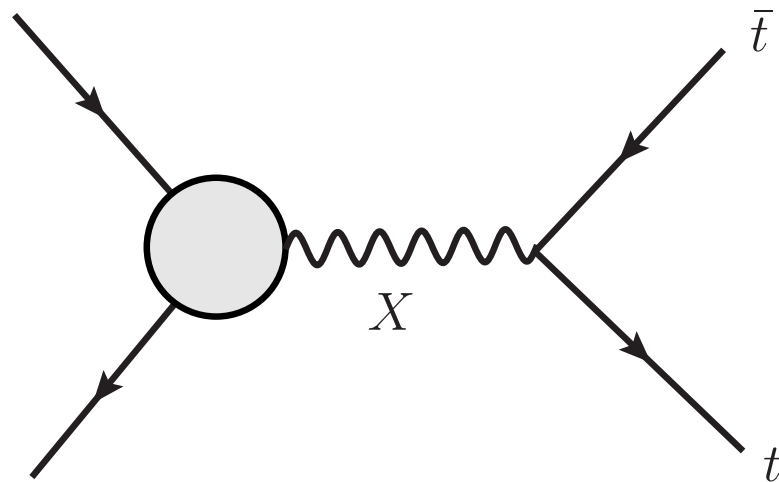
# Search for $t\bar{t}$ resonance.



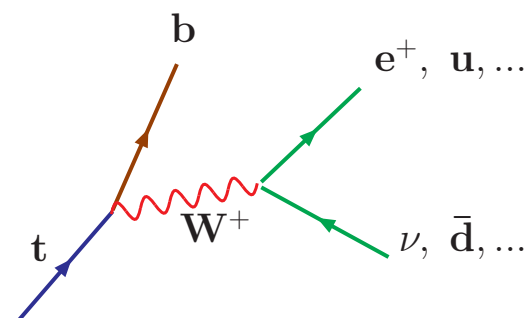
- Generic resonance could also be spin-0, or spin-2.
- Can be broad. Need careful modeling.

# Boosted top is also hard to identify.

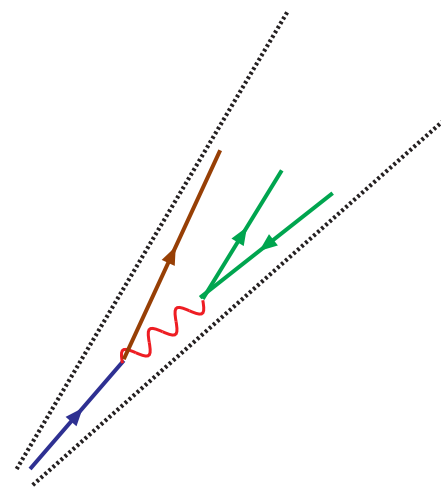
- Heavy resonance decay.



$$E_{\text{top}} \simeq \frac{M_X}{2}$$



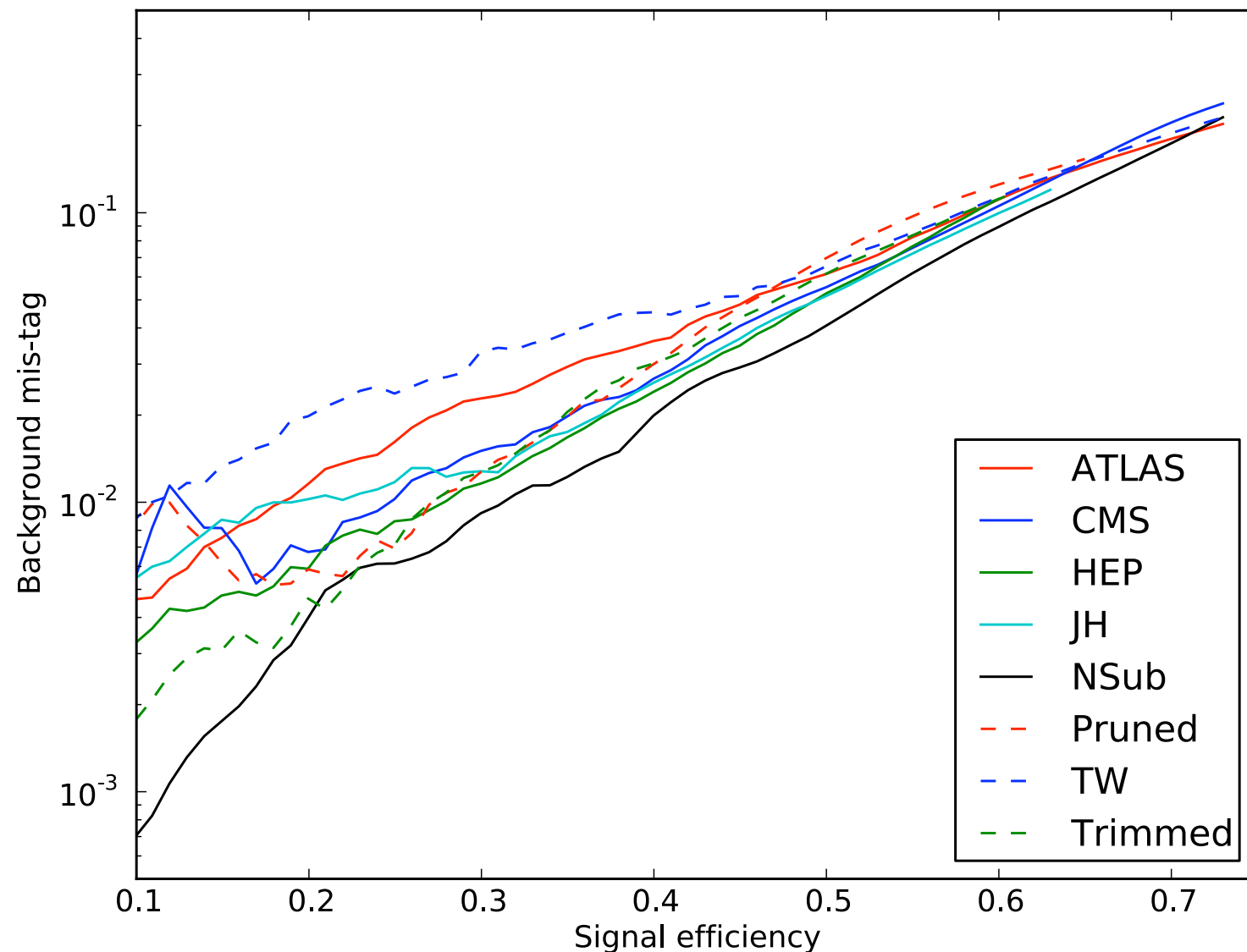
boost



← No isolated objects

B. Lillie, L. Randall, and LTW, hep-ph/0701166

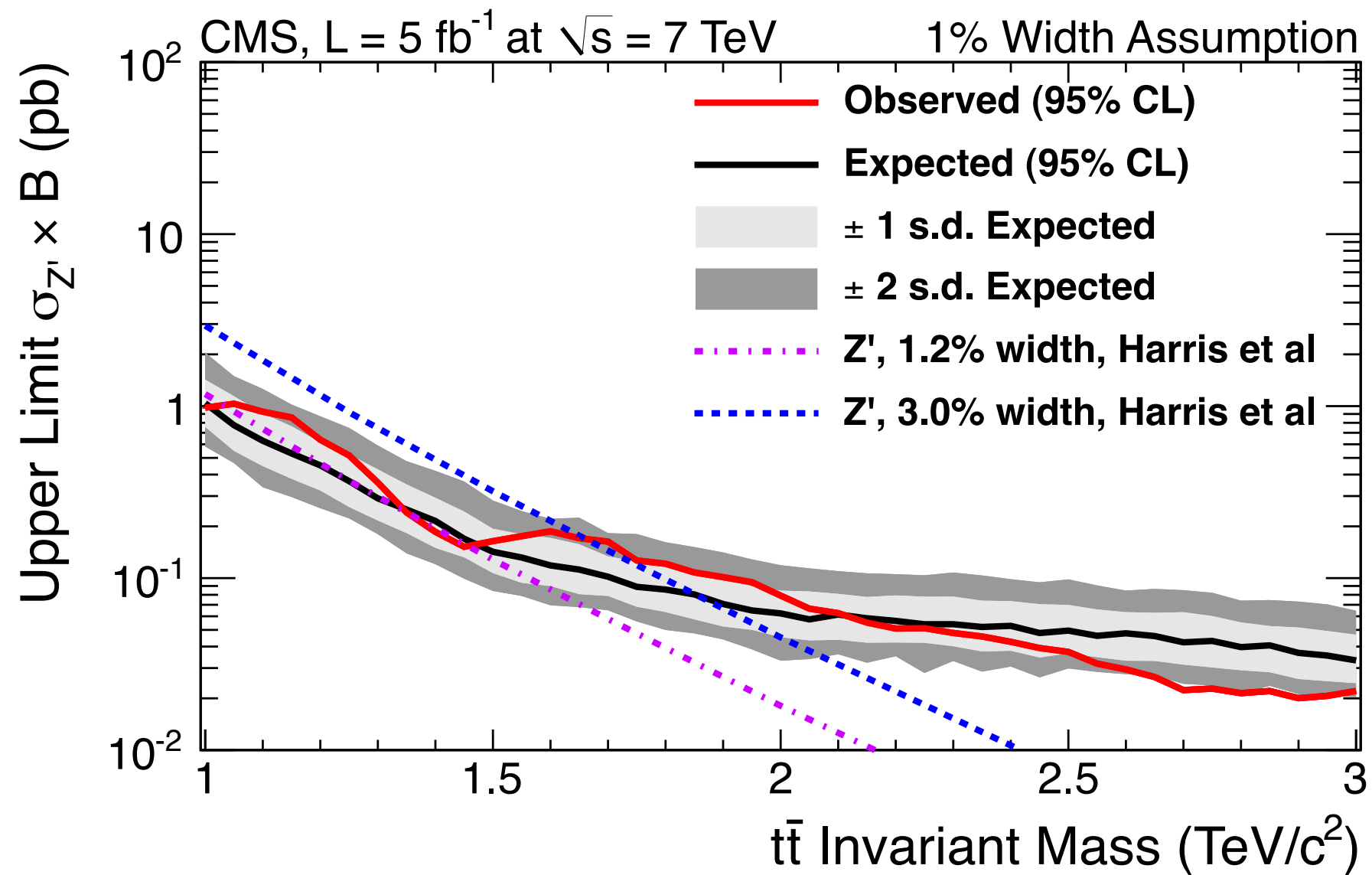
# boosted top taggers



1201.0008

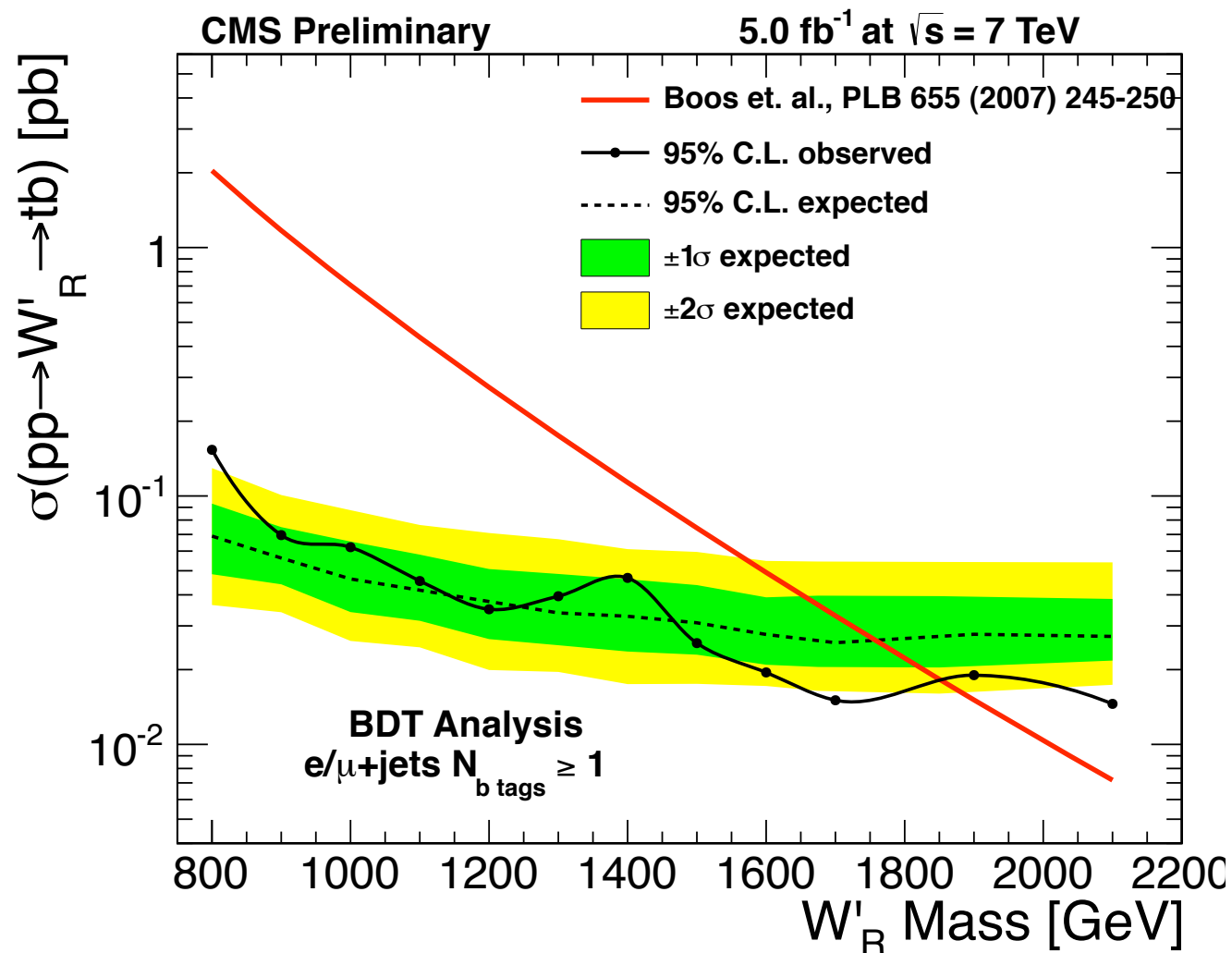
- Jet substructure.
- “Grooming techniques”

Talks by Miller, Rappoccio and Krohn



— Expectation: resonance mass  $\sim \text{TeV}$ s.

$$W' \rightarrow tb$$



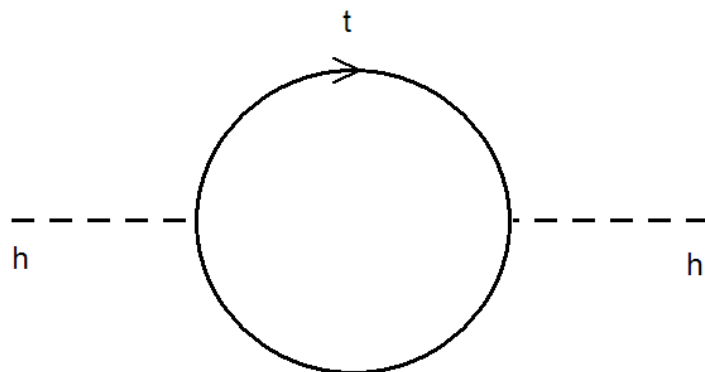
- Almost as generic as the  $X \rightarrow t\bar{t}$  channel.
- New physics typically comes in with non-trivial SU(2) representation.

Top partner



# Top partner

- Heavy top  $\rightarrow$  largest coupling to the Higgs.
  - Biggest contribution to its mass.



$$\delta m_h^2 = -\frac{3}{8\pi^2} y_t^2 \Lambda^2$$

- This is the essential piece of the so-called naturalness or hierarchy problem.
- Any natural theory must introduce top partner.
  - Most anticipated new physics particle.

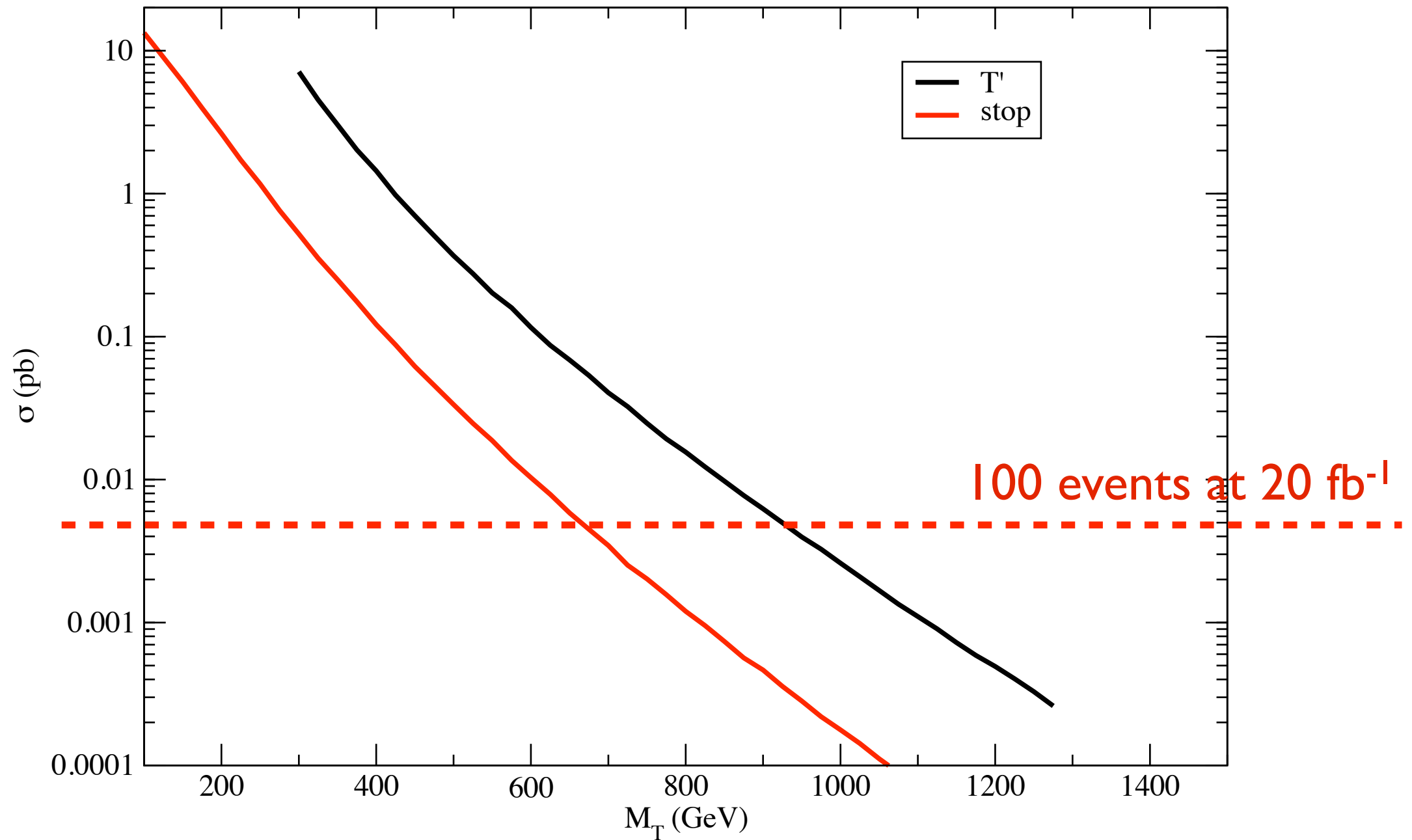
# Top partners.

- Introducing top partners.
  - ▶ stop in SUSY,  $T'$  in little Higgs, etc.
  - ▶ top like states in extra-dim models.
- Another “standard” feature: a discrete parity ( $Z_2$ )
  - ▶ Good for precision test, flavor, CP.
    - R-parity, KK parity, T parity...
  - ▶ Dark matter candidate, lightest stable neutral NP state.

# Top partner production at 8 TeV

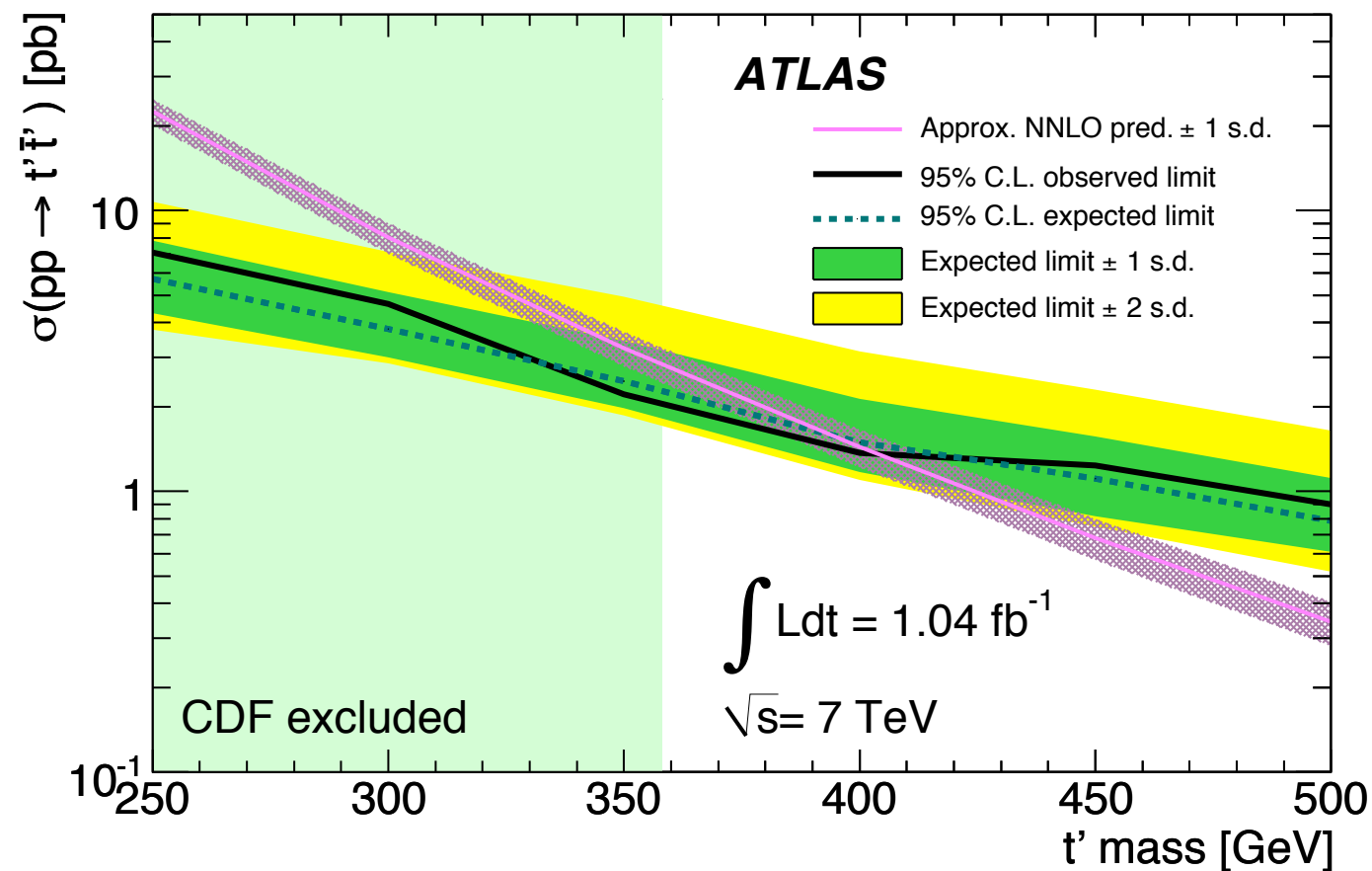
$pp \rightarrow t't'$

Production rate at 8 TeV



PYTHIA parton level

# Signal of top partner (without parity).

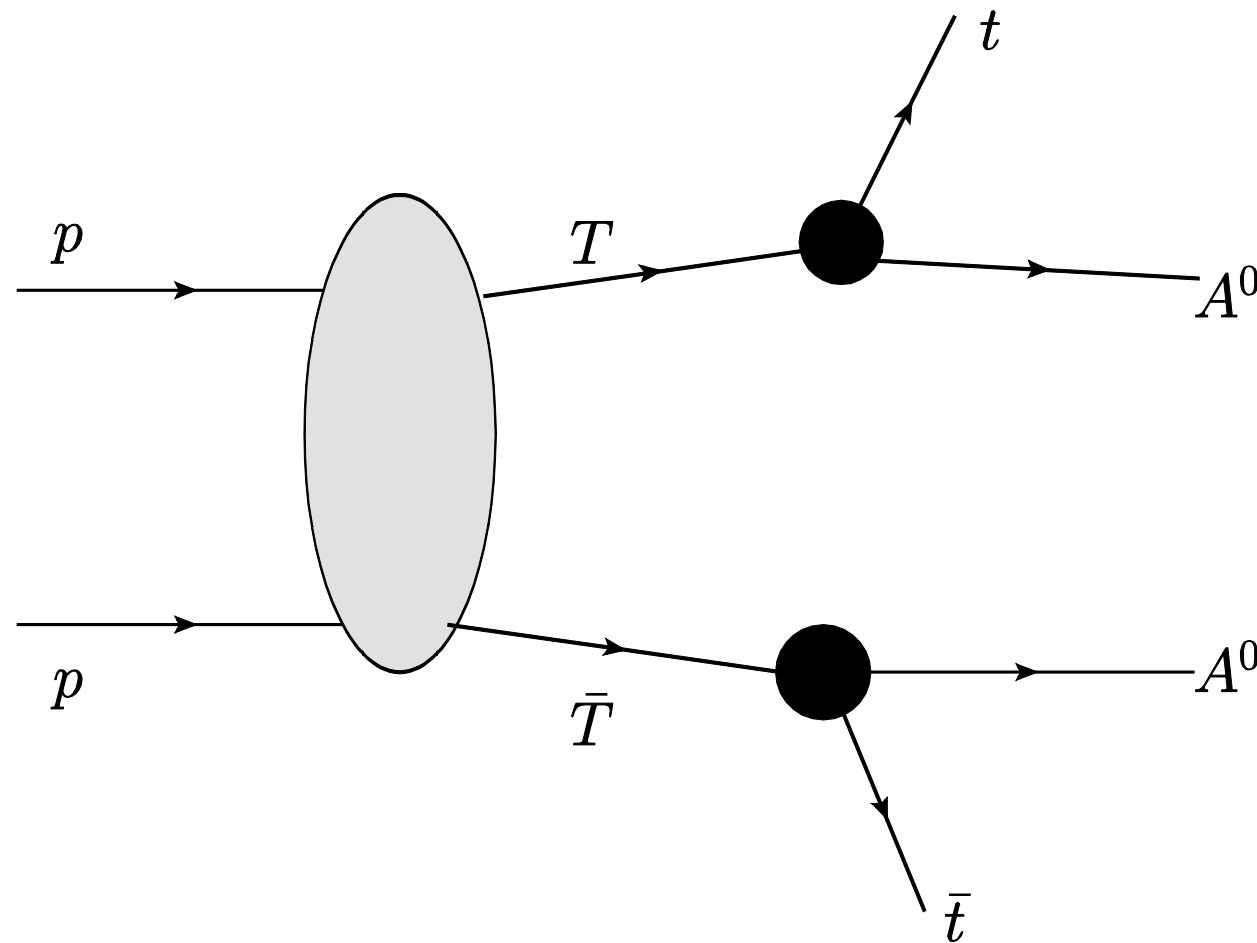


- Pair production of  $t'$  followed by
- $t' \rightarrow Wb$ , “heavy top”

# Signal of top partner (without parity).

- What about the  $tZ$  and  $th_0$  channels?
- Expected to be there.
  - ▶  $t' \rightarrow Wb : tZ : th_0 \approx 2:1:1$  (Goldstone equivalence theorem)  
Perelstein, Peskin, Pierce, 0310039
  - ▶ top-like or b-rich signal.

# Signal of top partner, with $Z_2$ parity.



$$t \bar{t} + \cancel{E}_T$$

$T(\bar{T})$  top partner :  $\tilde{t}$ ,  $t^{\text{KK}}$ ,  $t^{\text{T}}$ , ...

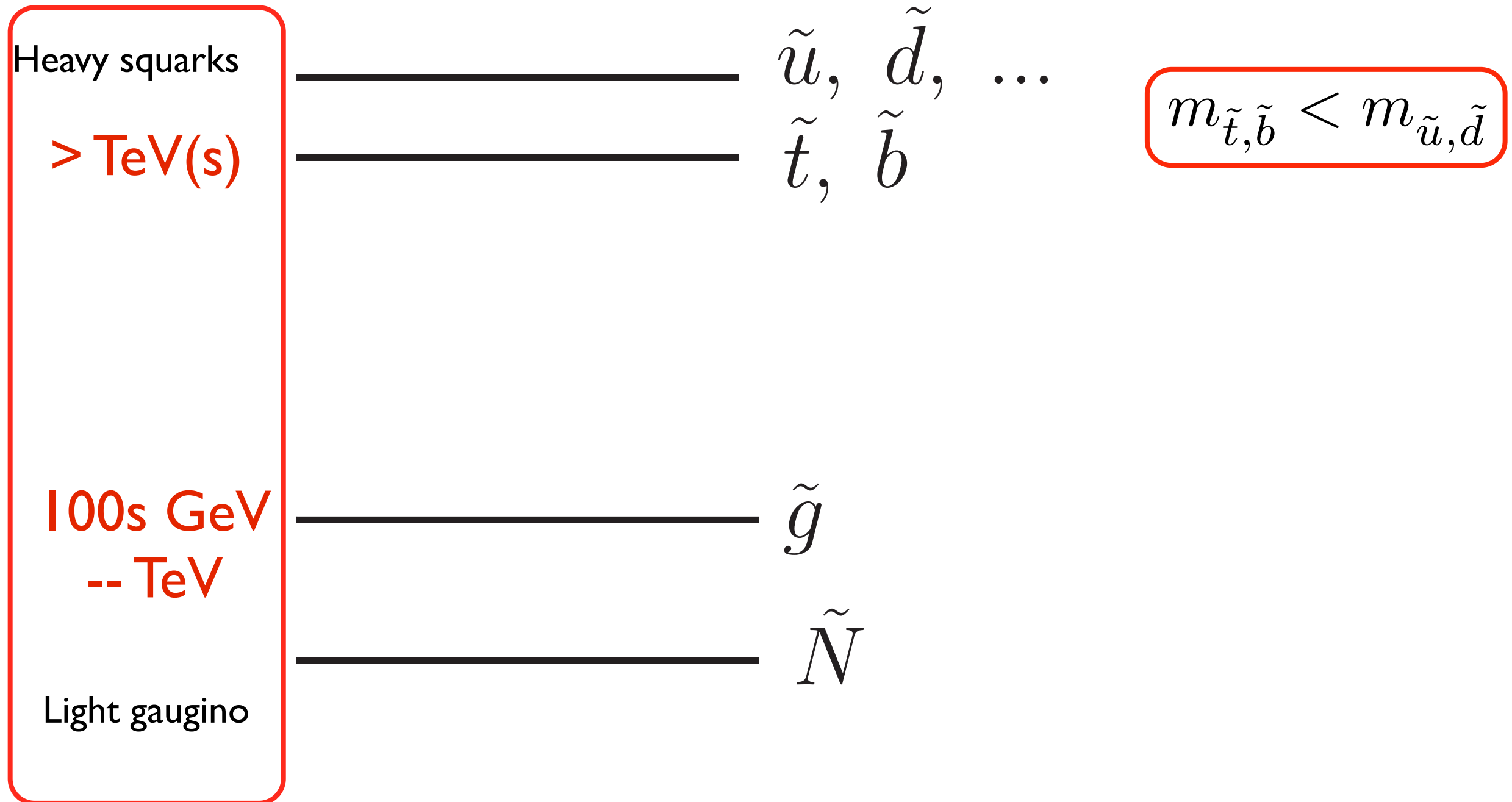
$A^0$  missing neutral particle : LSP, LKP, LTP, ...

Top partner can have spin 0, 1/2, 1

Difficult due to: limited rate, similar to SM  $t\bar{t}$

Many recent studies. Talk by Reece

# A promising scenario.



# Why considering heavy scalars?



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- On general round, scalar tends to be heavier.
  - ▶ From Kahler potential, hard to suppress its couplings to SUSY breaking.
  - ▶ R-symmetry tends to protect gaugino mass terms.

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  - ▶ R-symmetry tends to protect gaugino mass terms.
- Examples: F-term SUSY breaking.
  - ▶ With R-symmetry broken. But gauginos are sequestered (geometry, etc.) at tree level.
  - ▶ Gaugino mass from AMSB.

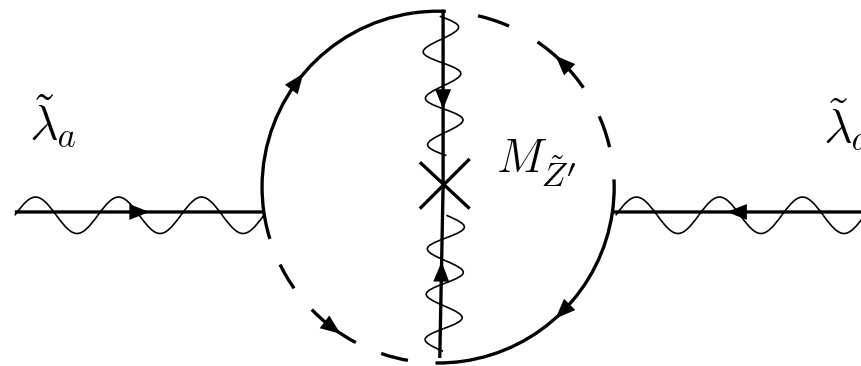
$$m_{\tilde{q},\tilde{\ell}} \sim m_{2/3}, \quad m_{1/2} \sim \frac{1}{16\pi^2} m_{2/3}$$

# Zprime-ino mediation.

- Gaugino mediation through an extra  $U(1)'$

$$\int d^2\theta \frac{X}{M} W_{Z'} W_{Z'} \rightarrow m_{\tilde{Z}'} = \frac{F_X}{M}$$

$$m_{\tilde{q}, \tilde{\ell}}^2 \sim \frac{g_{Z'}^2}{16\pi^2} \frac{F_X^2}{M^2}, \quad m_{1/2}^{\text{MSSM}} \sim \frac{g^2 g_{Z'}'^2}{(16\pi^2)^2} \frac{F_X}{M}$$



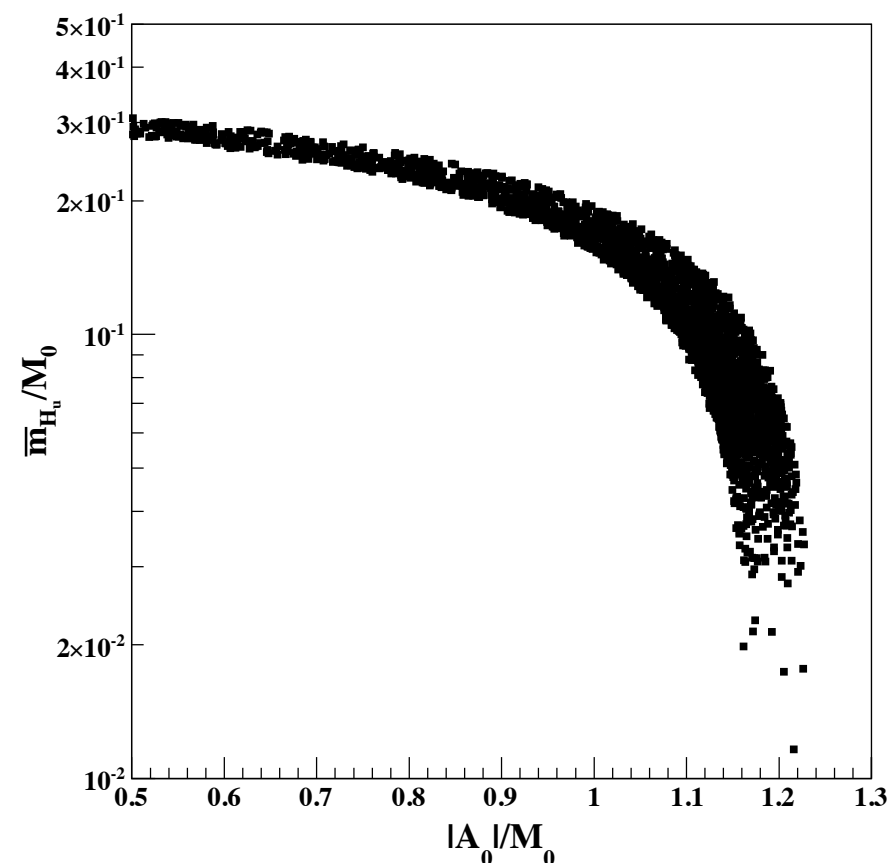
$$\frac{m_{\text{scalar}}}{m_{\text{MSSM gaugino}}} \sim (4\pi)^3$$

Langacker, Paz, LTW, Yavin, 0710.1632,  
Verlinde, LTW, Wijnholt, Yavin, 0711.3214

# Heavy scalar benefits.

- Better consistency with constraints:
  - ▶ flavor, CP:  $\propto 1/(16\pi^2 m_{\text{squark}}^2)$
  - ▶ Higgs mass (125? ) in MSSM:  
 $\approx m_Z^2 + 3/(2\pi^2) |y_t m_t|^2 \log[(m_{\text{stop}})/m_t]$
- Fine with EWSB.

Feldman, Kane, Kuflik, Lu, 1105.3765



# 3rd vs first two generations

\_\_\_\_\_  $\tilde{u}, \tilde{d}, \dots$   
\_\_\_\_\_  $\tilde{t}, \tilde{b}$

– RGE.

$$\frac{dm_{\tilde{t},\tilde{b}}^2}{dt} = \frac{1}{16\pi^2} |y_{t,b}|^2 (m_{H_{u,d}}^2 + m_{Q_3}^2 + m_{\tilde{t}_R,\tilde{b}_R}^2) + \dots$$

\_\_\_\_\_  $\tilde{g}$   
\_\_\_\_\_  $\tilde{N}$

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same as 1, 2 gen.

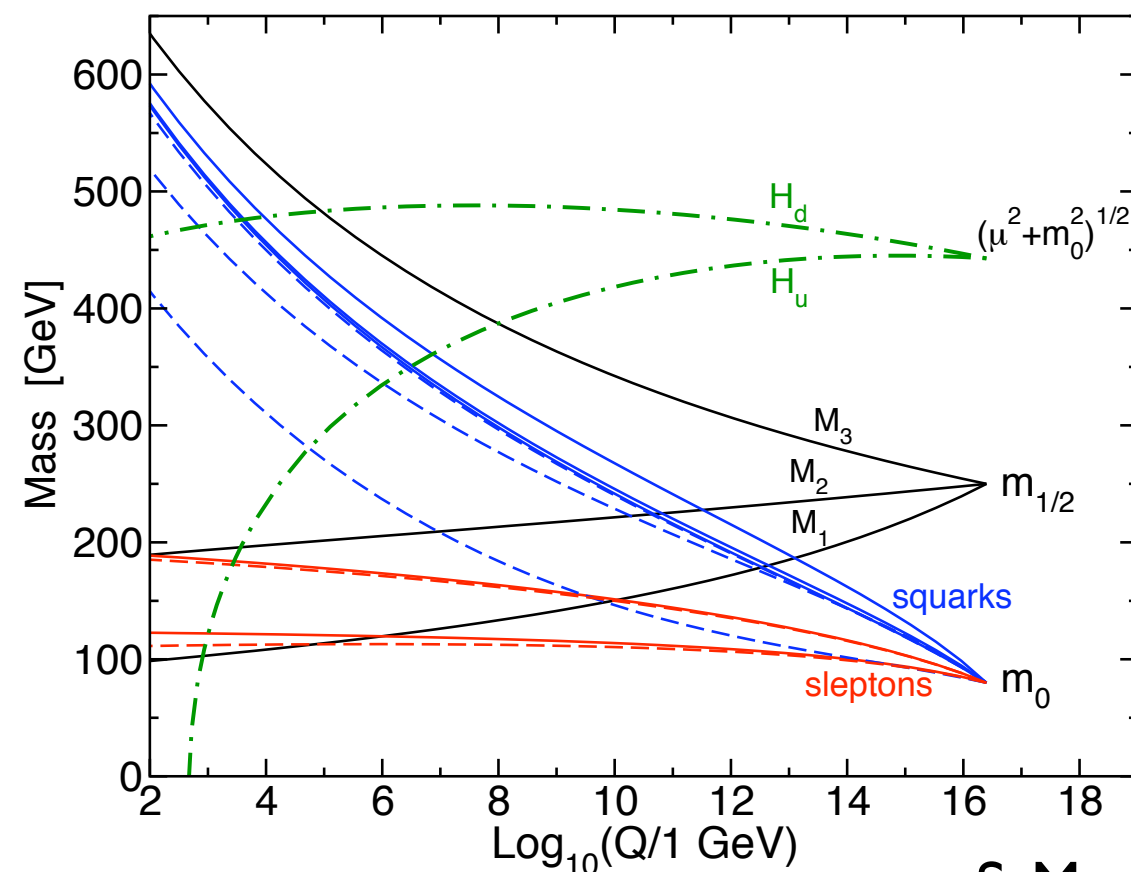
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S. Martin

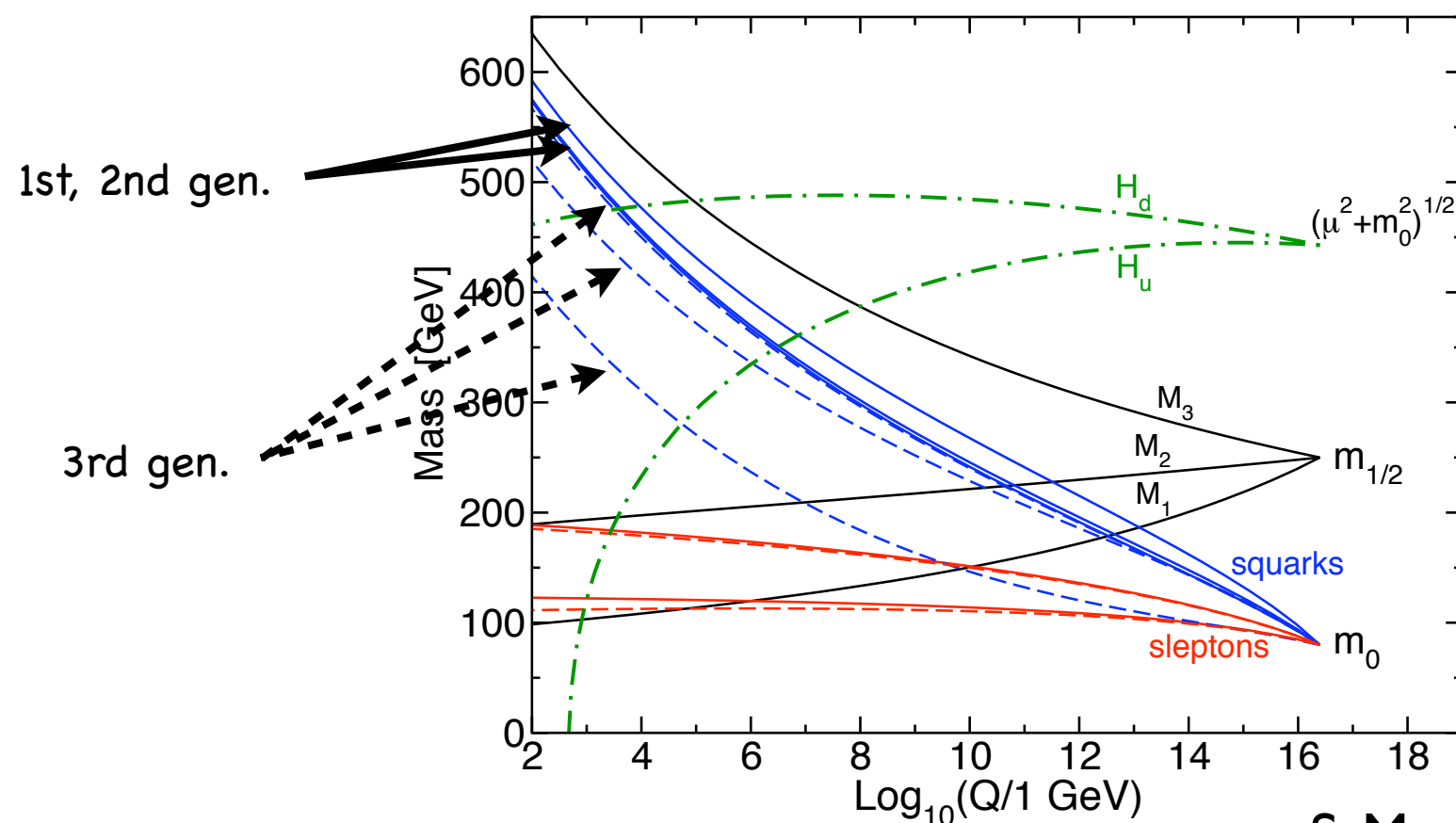
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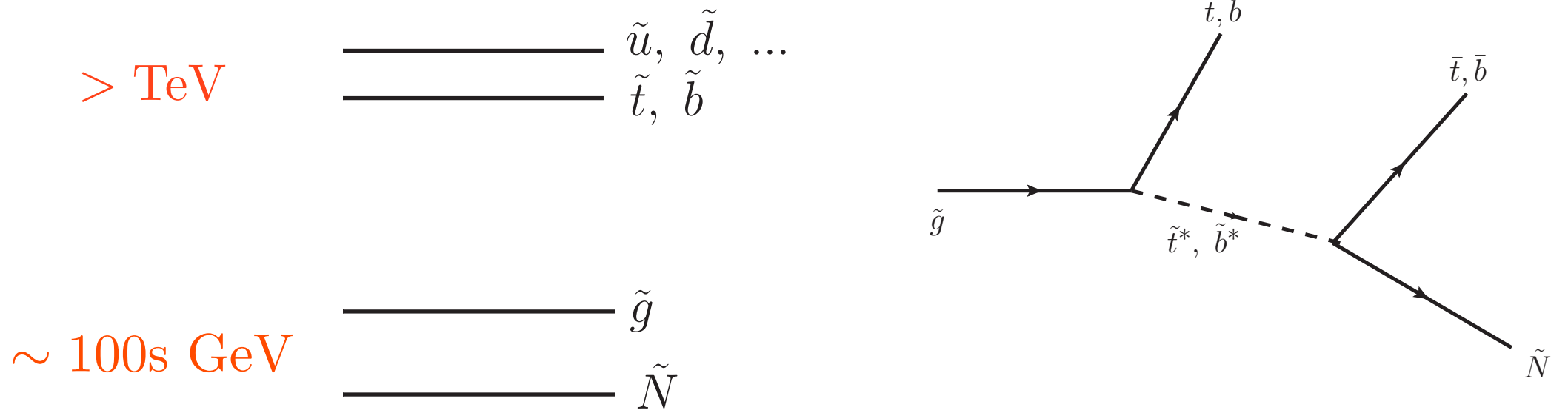


# Recent Models (partial list)

- Langacker, Paz, LTW, Yavin, 0710.1632
- Verlinde, LTW, Wijnholt, Yavin, 0711.3214
- Acharya, Bobkov, Kane, Kumar, 0801.0478
- Nakamura, Okumura, Yamaguchi, 0803.3725
- Everett, Kim, Ouyang, Zurek, 0806.2330
- Hackman, Vafa, 0809.3452
- Sundrum, 0909.5430
- Barbieri, Bertuzzo, Farina, Lodone, Rappadopulo, 1004.2256

# A promising, and complicated, scenario.

Kane, Kuflik, Lu and LTW, 1101.1963



## The Dominant channel

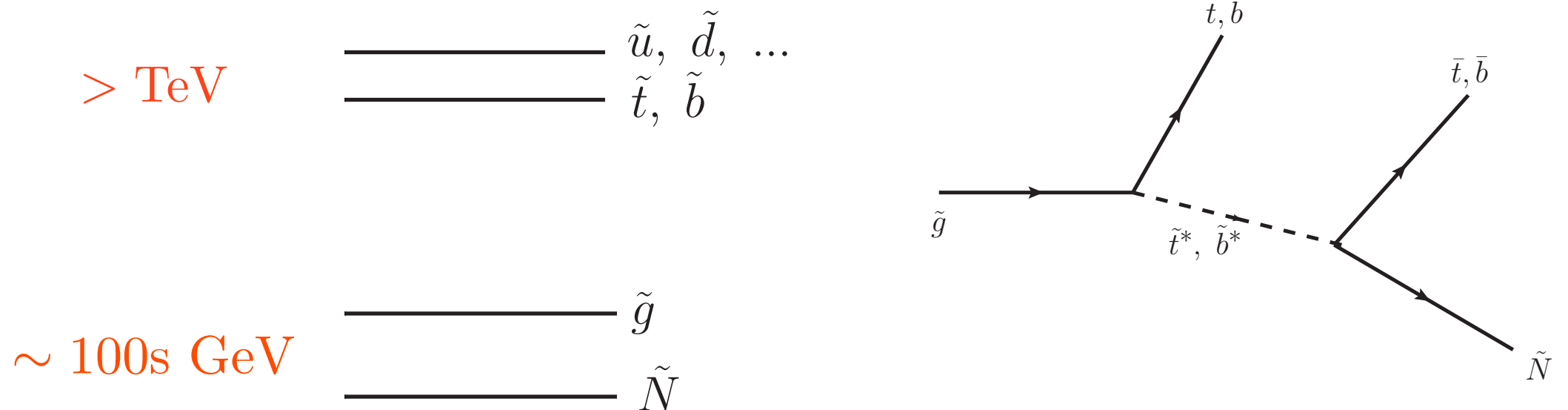
$$p\,p \rightarrow \tilde{g}\tilde{g} \rightarrow t\bar{t}t\bar{t}(\text{or } t\bar{t}b\bar{b},\, t\bar{t}t\bar{b} \dots)$$

$$\tilde{g} \rightarrow t\bar{t}(b\bar{b}) + \tilde{N}, \text{ or } t\bar{b} + \tilde{C}^- \quad t \rightarrow b\ell^+\nu$$

- Multiple b, multiple lepton final state.
- Good early discovery potential.
- Challenging to interpret: top reconstruction difficult.

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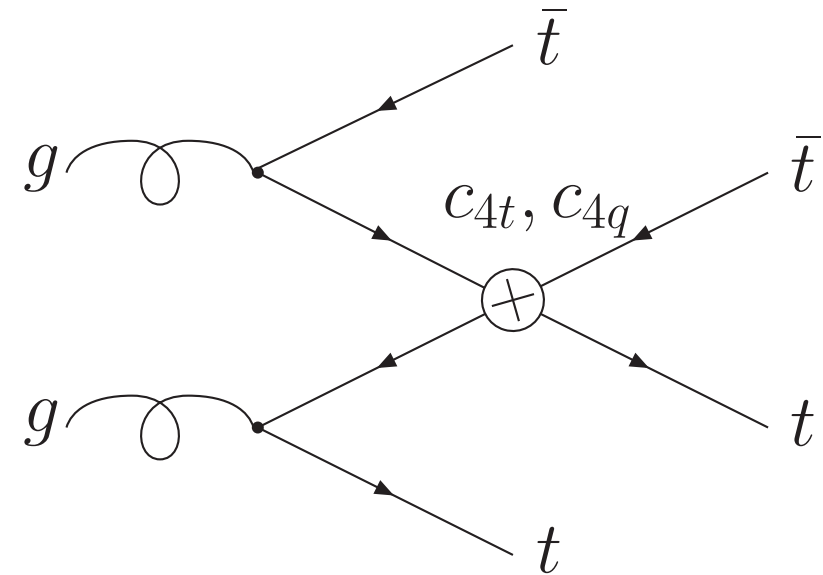
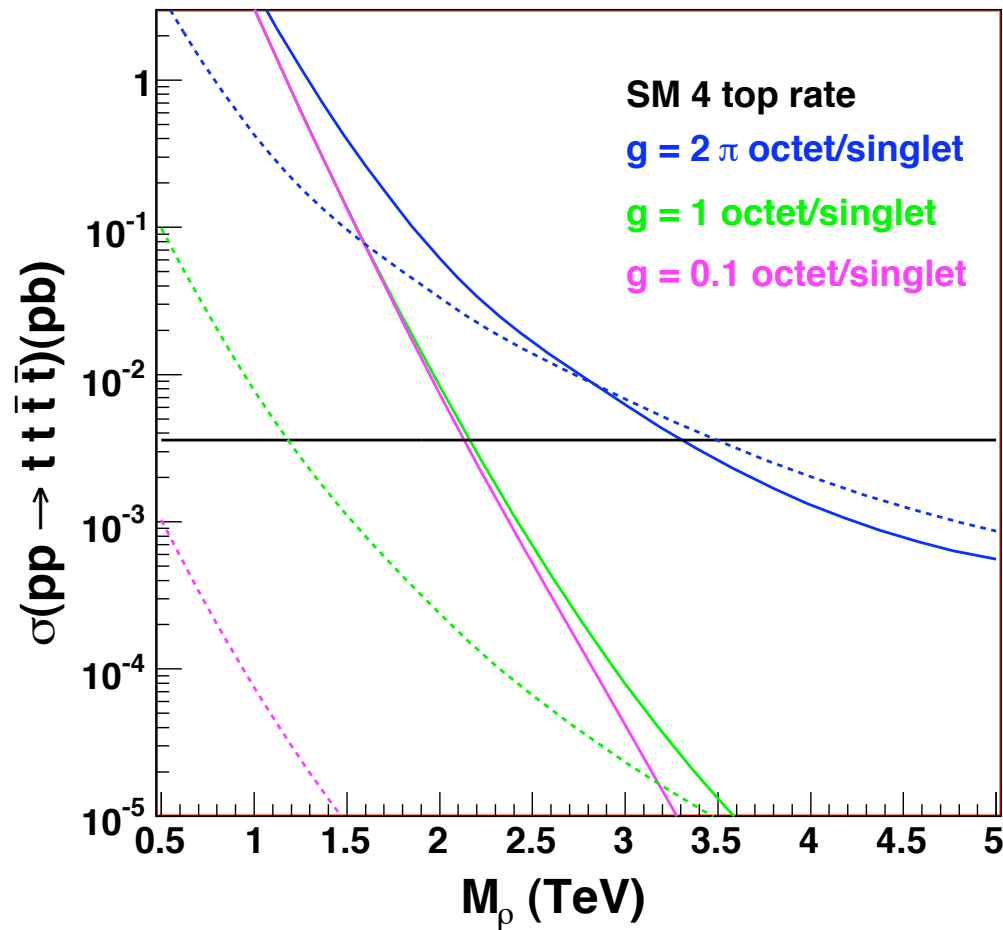
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Quite a few recent searches

Signal similar to [gluino  $\rightarrow$  on-shell stop], talk by Reece

# Another multi-top signal: top compositeness



Lillie, Shu, Tait, 0712.3057

Pomarol, Serra, 0806.3247

# Top partner related.

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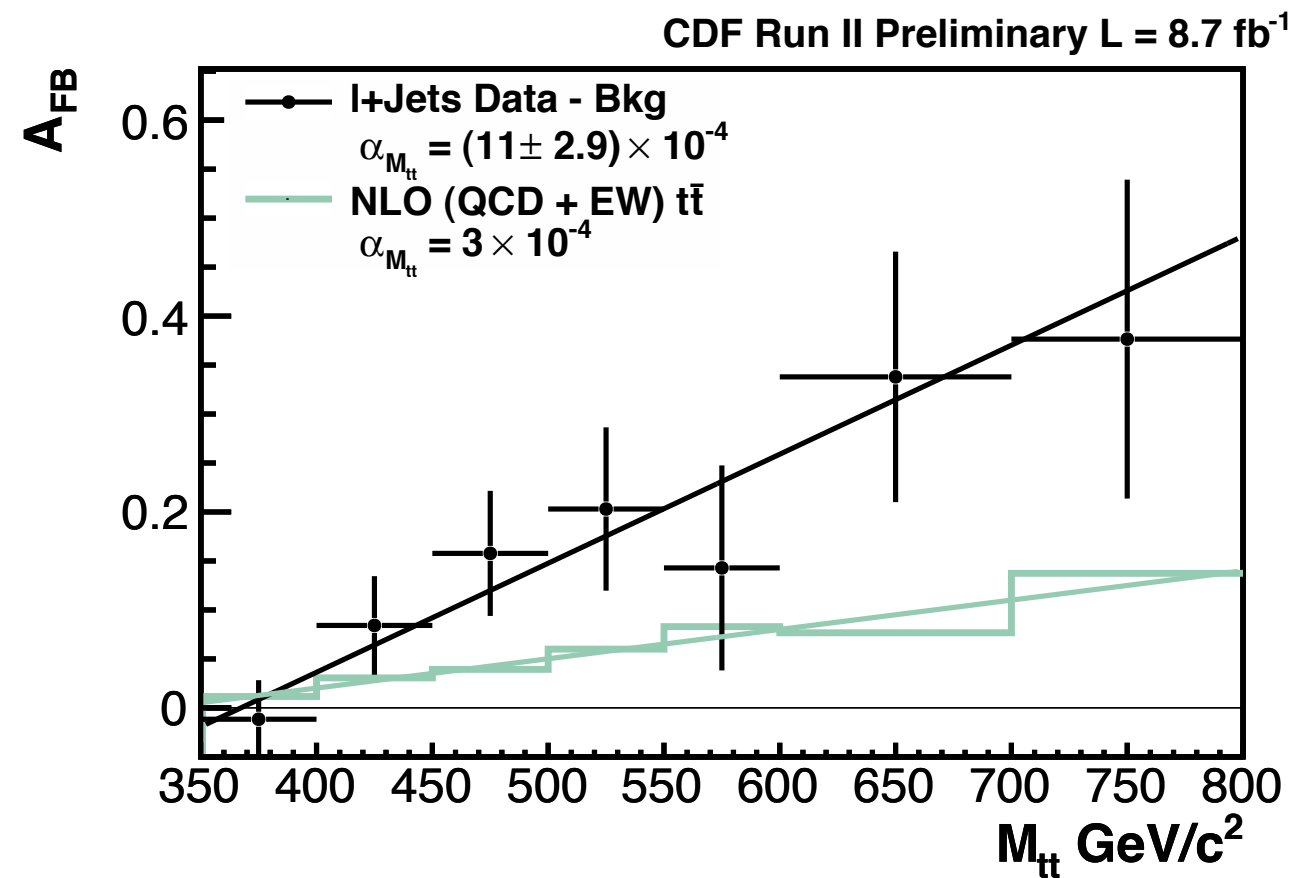
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- 3rd generation related FCNC.  $V_{tb} \dots$
- 4th generation (motivated by the first 3).

Top can give us surprises.

It is the least tested sector

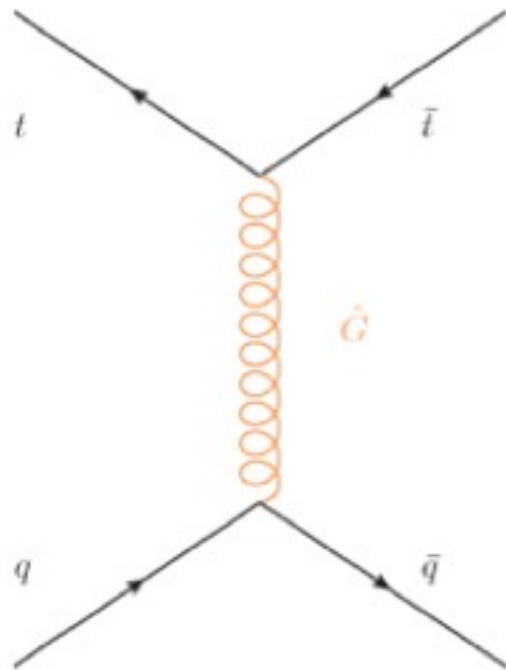
# For example: Top AFB

- Motivated by potential experimental evidence.

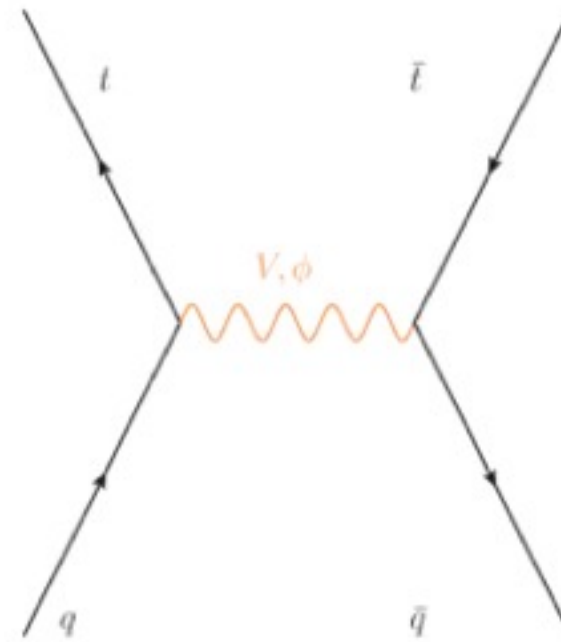


- Many studies and models.

# Two classes of Models.



- S-channel. Large couplings. “work”s.
- $G$ : 1–2 TeV or 400 GeV.
- $t\bar{t}$  resonance search.



- t-channel. Large couplings. “work”s. Flavor “structure”.
- $O(10^2)$ s GeV mediator.
- $tq$  resonances.

# At the LHC.

- AFB measurement less direct, but possible.
- However,
  - ▶ All models are designed to give large AFB and barely consistent with other Tevatron  $t\bar{t}$  data.
    - Surprising if nature works this way.
  - ▶ At the LHC, with the large increase of  $E_{\text{cm}}$ , can not stay hidden anymore.
  - ▶ Current LHC data should already give strong constraints.

# Various tests of models

- ☒ New resonance searches (Kim, Gresham, Zurek (2011); Hewett, Shelton et al (2011))
- ☒ Same sign top pair production: t-channel  $Z'$  model (Berger et. al. (2011))
- ☒ Excesses in  $t\bar{t}$  and single  $t$  production (Aguilar-Saavedra, Perez-Victoria (2011); Gedalia et al (2011); Degrande et al (2011))
- ☒ Top polarization: measure chiral structure (D. Krohn, Tao Liu, J. Shelton, LTW (2011); Godbole et. al.; Choudhury et. al. (2010); V. Barger et. al (2011))
- ☒ Non-SM spin-correlation of top pair: distinguish s- and t-channel models (D. Krohn, Tao Liu, J. Shelton, LTW (2011))

Will be covered later in the workshop: talk by Zupan



# Top polarization as a probe of NP.

- New physics typically gives different top polarizations.
  - ▶ e.g. some AFB model prefers right-handed couplings.
- Direct measurement of polarization after accurate reconstruction.
  - ▶ Powerful, probably need larger statistics.

# (semi)Lepton asymmetry

$$\mathcal{A}_{FB}^{\ell} = \frac{N(q_{\ell}y_{\ell} > 0) - N(q_{\ell}y_{\ell} < 0)}{N(q_{\ell}y_{\ell} > 0) + N(q_{\ell}y_{\ell} < 0)}$$

frame and mass range	$t\bar{t}$ asymmetry	Lepton asymmetry	stat. sig. (5.3 fb <sup>-1</sup> )
$G_A$ lab, sel. cuts	9 %	4 %	1.1
lab, $m_{t\bar{t}} > 450$ GeV	17 %	9 %	1.9
CM, sel. cuts	12 %	6 %	1.7
CM, $m_{t\bar{t}} > 450$ GeV	19 %	12 %	2.4
$G_L$ lab, sel. cuts	7 %	-3 %	0.9
lab, $m_{t\bar{t}} > 450$ GeV	14 %	-1 %	0.2
CM, sel. cuts	13 %	-4 %	1.4
CM, $m_{t\bar{t}} > 450$ GeV	20 %	-3 %	0.6
$G_R$ lab, sel. cuts	9 %	12 %	3.9
lab, $m_{t\bar{t}} > 450$ GeV	14 %	18 %	5.0
CM, sel. cuts	9 %	16 %	3.5
CM, $m_{t\bar{t}} > 450$ GeV	15 %	22 %	4.4
$W'$ lab, sel. cuts	15 %	13 %	3.9
lab, $m_{t\bar{t}} > 450$ GeV	26 %	22 %	4.9
CM, sel. cuts	20 %	16 %	4.4
CM, $m_{t\bar{t}} > 450$ GeV	31 %	26 %	5.3

- Nice performance on  $G_R$  and  $W'$  .
- CM frame asym. better, but lab frame asym. already useful.
- $G_L$ ,  $G_A$  models are more difficult. But can improve with full data set.

□ D. Krohn, Tao Liu, J. Shelton, LTW (2011)

# Conclusions.

- Top rich final states are well motivated in search for BSM NP.
  - ▶ I would argue it is **the** place to look for NP.
- In this talk
  - ▶ Top – Higgs connection
  - ▶  $t\bar{t}$  resonances.
  - ▶ Top partner.
  - ▶  $t\bar{t}$  AFB.
- More possibilities. Can have surprises.

extras

# Benchmark models

- Reference models.

Model	$M$ [TeV]	$\Gamma$ [TeV]	$g_1^A$	$g_1^V$	$g_3^A$	$g_3^V$	$g^A$	$g^V$
$G_A$	2.0	1.40	-2.3	0.0	3.35	0.0	/	/
$G_L$	2.0	1.40	-2.3	0.0	3.35	3.35	/	/
$G_R$	2.0	1.40	-2.3	0.0	3.35	-3.35	/	/
$W'$	0.40	0.04	/	/	/	/	-0.90	0.90

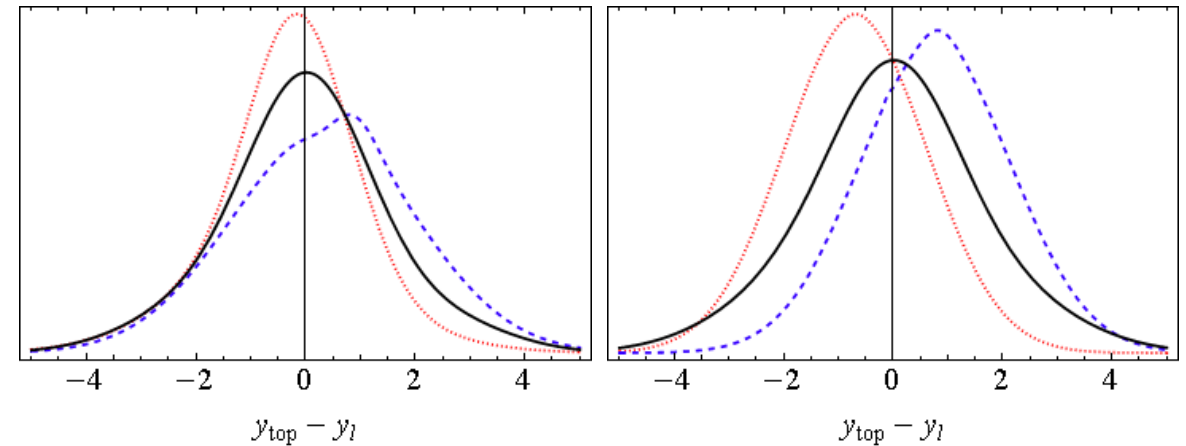
Model	$\sigma_{tt}^{\text{Tevatron}}$ [pb]	$\sigma_{tt}^{\text{LHC}}$ [pb]	$A_{fb}^{\text{Tevatron}}$
SM	5.6	89	0%
$G_A$	5.8	91	14%
$G_L$	6.1	95	13%
$G_R$	6.1	95	13%
$W'$	7.3	123	24%

- Our simulation
  - Madgraph + Pythia + PGS.

# Using leptons

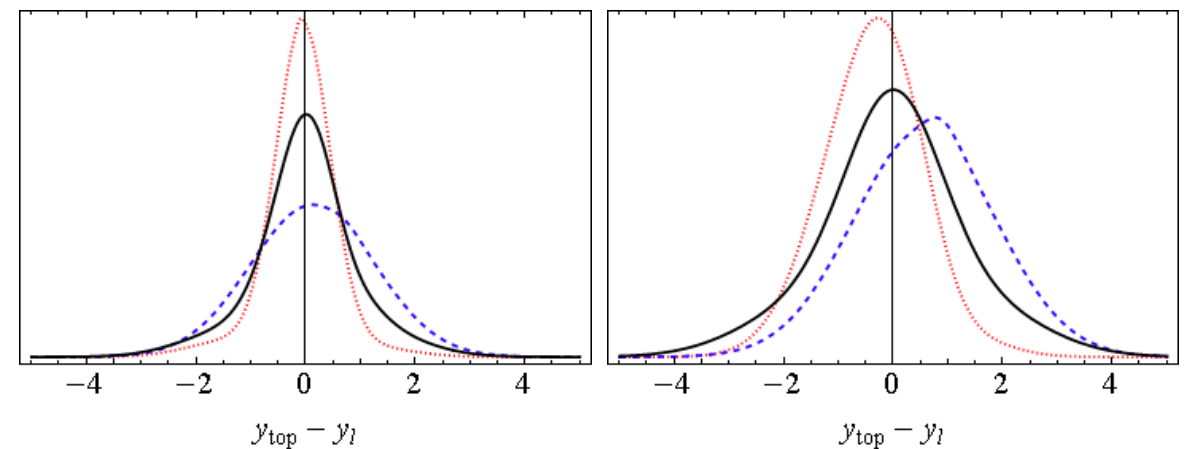
- Charge leptons “follows” the direction of top. Probes AFB.
- (left) right-polarized top leads to (anti)boosted leptons. Probes chiral coupling.

red: RH, blue: LH, black: SM



(a)  $\beta_t = 0.5, \cos \theta_t = 0.4$

(b)  $\beta_t = 0.5, \cos \theta_t = 0.9$



(c)  $\beta_t = 0.9, \cos \theta_t = 0.4$

(d)  $\beta_t = 0.9, \cos \theta_t = 0.9$

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{i,n}} = \frac{1}{2} (1 + \mathcal{P}_n \kappa_i \cos \theta_{i,n})$$

$$\kappa_{\text{lepton}} = 1$$

$$\mathcal{P}_n = 1(-1), \text{ right(left)-handed}$$

# (di)leptonic asymmetry

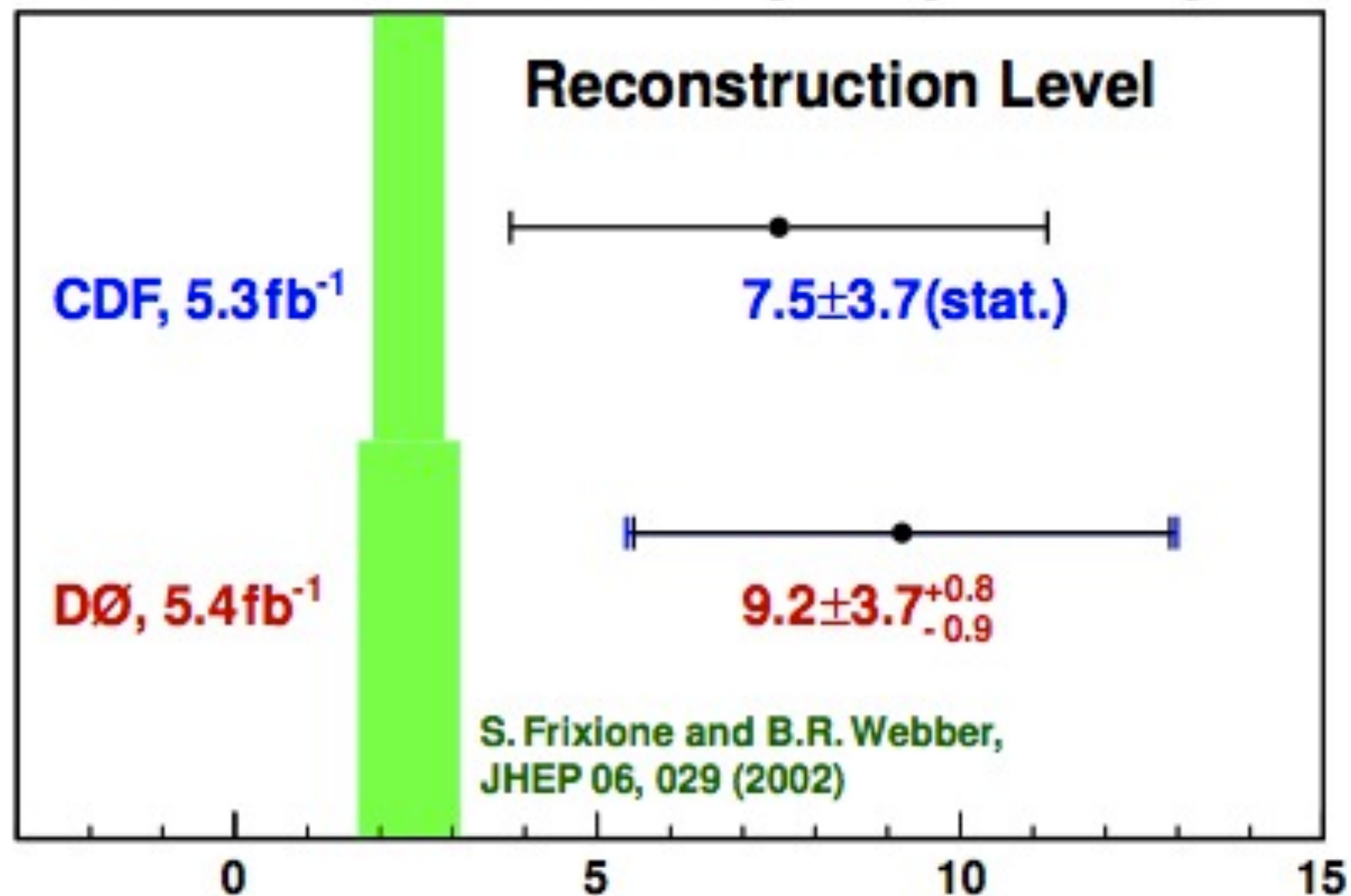
$$\mathcal{A}_{FB}^{\Delta\ell} = \frac{N((y_{\ell+} - y_{\ell-}) > 0) - N((y_{\ell+} - y_{\ell-}) < 0)}{N((y_{\ell+} - y_{\ell-}) > 0) + N((y_{\ell+} - y_{\ell-}) < 0)}$$

mass range	asymmetry (5.1 fb <sup>-1</sup> )	stat. sig.
$G_A$ sel. cuts	8 %	1.2
$m_{t\bar{t}} > 450$ GeV	14 %	1.4
$G_L$ sel. cuts	-4 %	0.5
$m_{t\bar{t}} > 450$ GeV	1 %	0
$G_R$ sel. cuts	15 %	2.4
$m_{t\bar{t}} > 450$ GeV	20 %	2.1
$W'$ sel. cuts	15 %	2.3
$m_{t\bar{t}} > 450$ GeV	24 %	2.6

- Useful and complementary to the semileptonic mode, especially with the full data set.

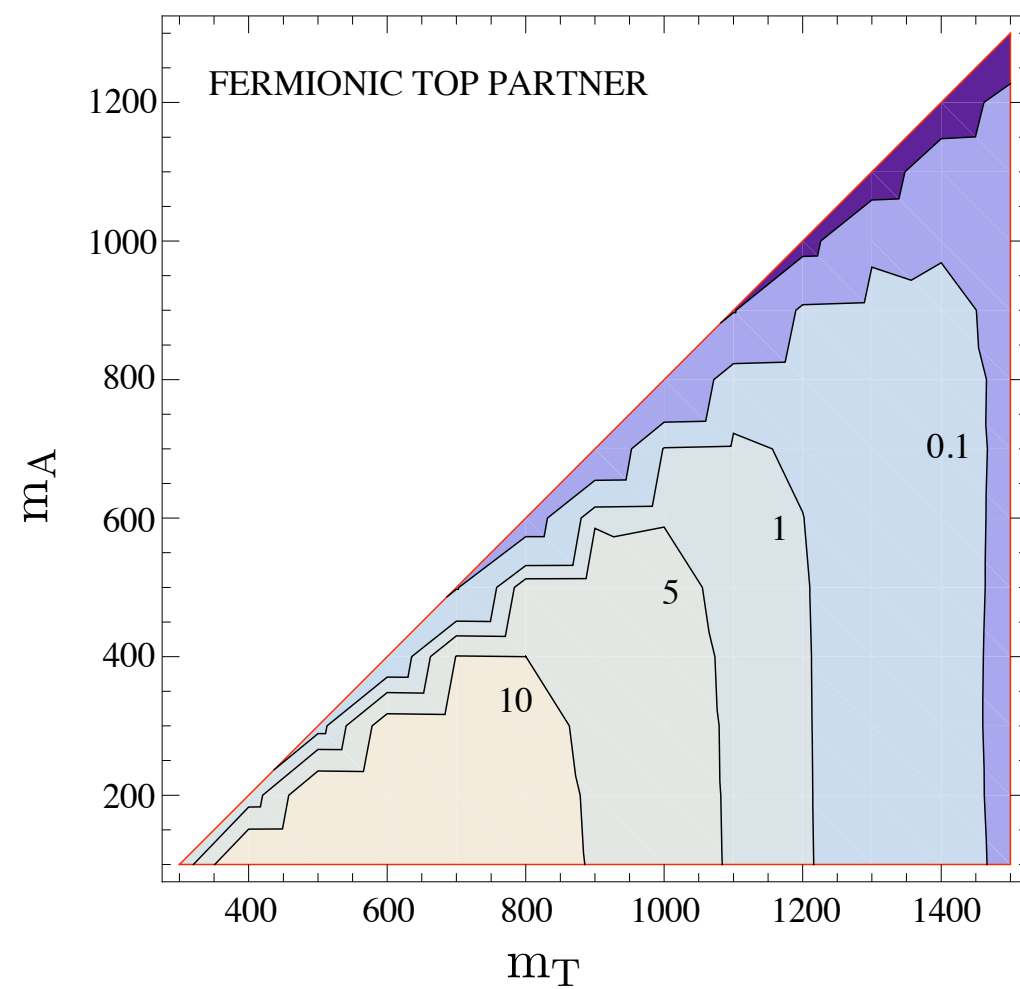
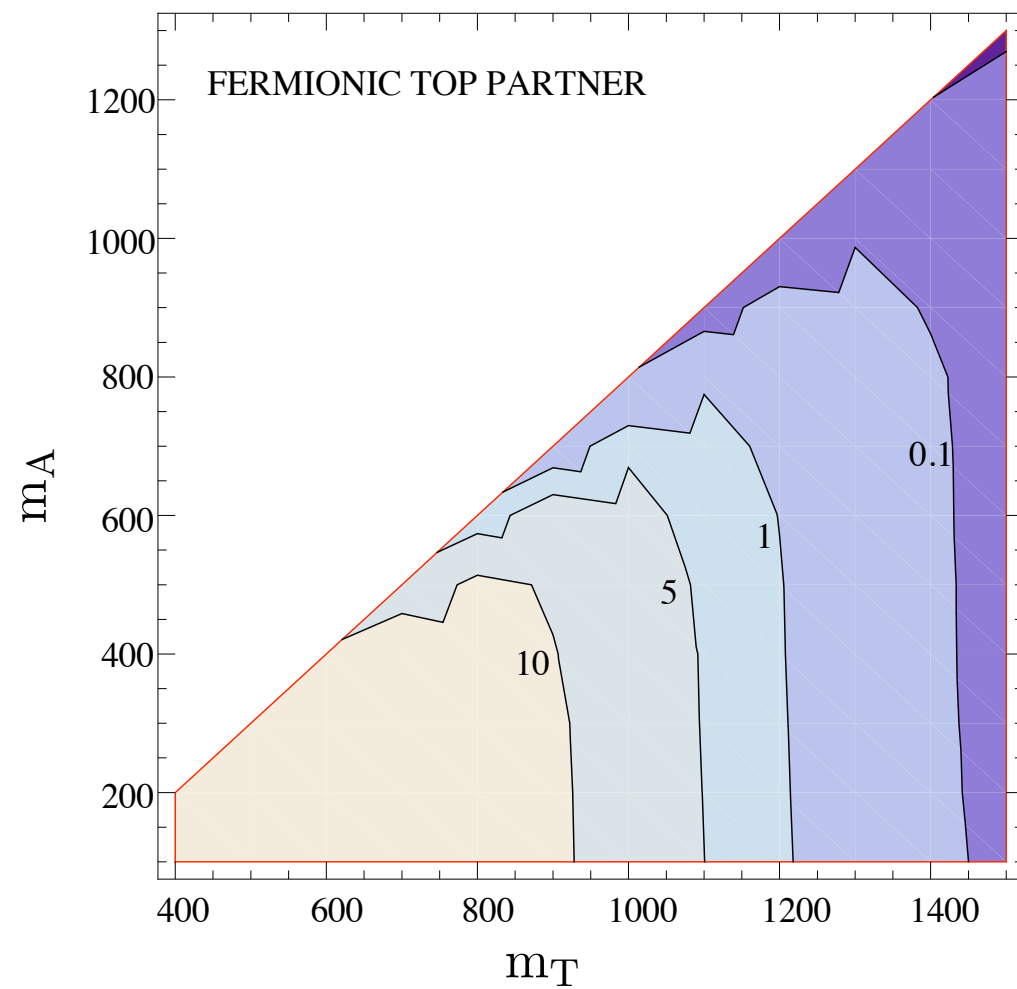


## Forward-Backward Top Asymmetry, %





# Top partner reach, 14 TeV, 100 fb<sup>-1</sup>



# Polarization: LHC

$$\mathcal{P}_n = \frac{N(\cos \theta_{\ell,n} > 0) - N(\cos \theta_{\ell,n} < 0)}{N(\cos \theta_{\ell,n} > 0) + N(\cos \theta_{\ell,n} < 0)}$$

- Select helicity basis as the polarization axis

	$G_A(\%)$	$G_L(\%)$	$G_R(\%)$	$W'(\%)$	SM(%)
Selection cuts	1	-1	4	18	1 ( $\pm 1.2$ )
$m_{t\bar{t}} > 450 \text{ GeV}$	2	-2	6	26	0 ( $\pm 1.7$ )
$ y(t) + y(\bar{t})  > 2$	0	-4	3	19	-2 ( $\pm 3.2$ )

- Select beam basis as the polarization axis

	$G_A(\%)$	$G_L(\%)$	$G_R(\%)$	$W'(\%)$	SM(%)
Selection cuts	4	-1	5	9	2 ( $\pm 1.2$ )
$m_{t\bar{t}} > 450 \text{ GeV}$	1	-4	4	11	0 ( $\pm 1.7$ )
$ y(t) + y(\bar{t})  > 2$	2	-5	7	15	1 ( $\pm 3.2$ )

- The GR and W' models can be distinguished from the SM at a C.L. > 3 sigma in the helicity basis
- The left- chiral, right-chiral models and the SM can be distinguished from each other at a C.L. > 2 sigma in the beam basis

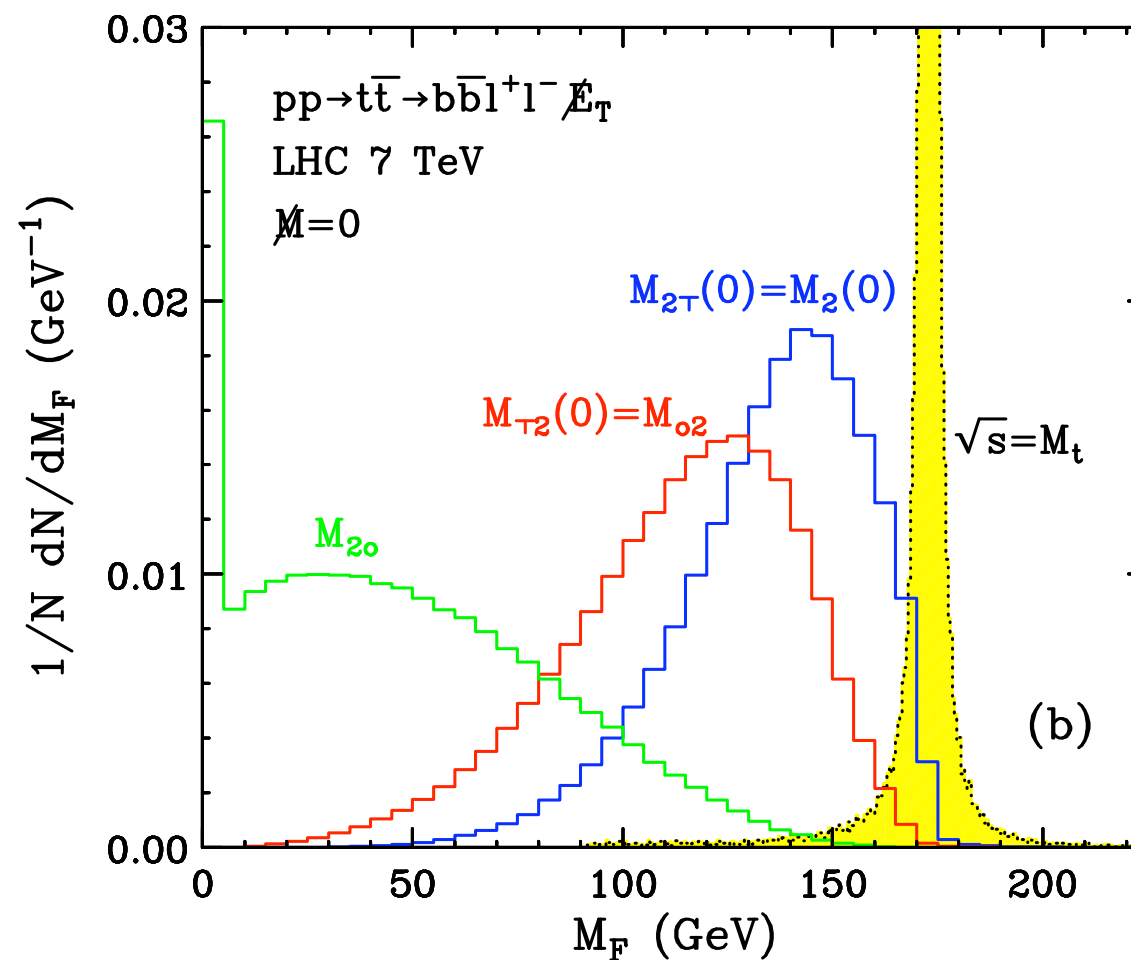
See our paper for more details

# Top as testing ground.

- Top is heavy, gives new physics-like signals.
  - ▶ With high multiplicity final state.
  - ▶ With jets, lepton and MET.
- Headache for new physics discovery.
  - ▶ Important to understand it very well.
- Good testing ground for many kinematical variables, reconstruction techniques.
  - ▶  $M_{T2}$  and its descendants

# A recent example

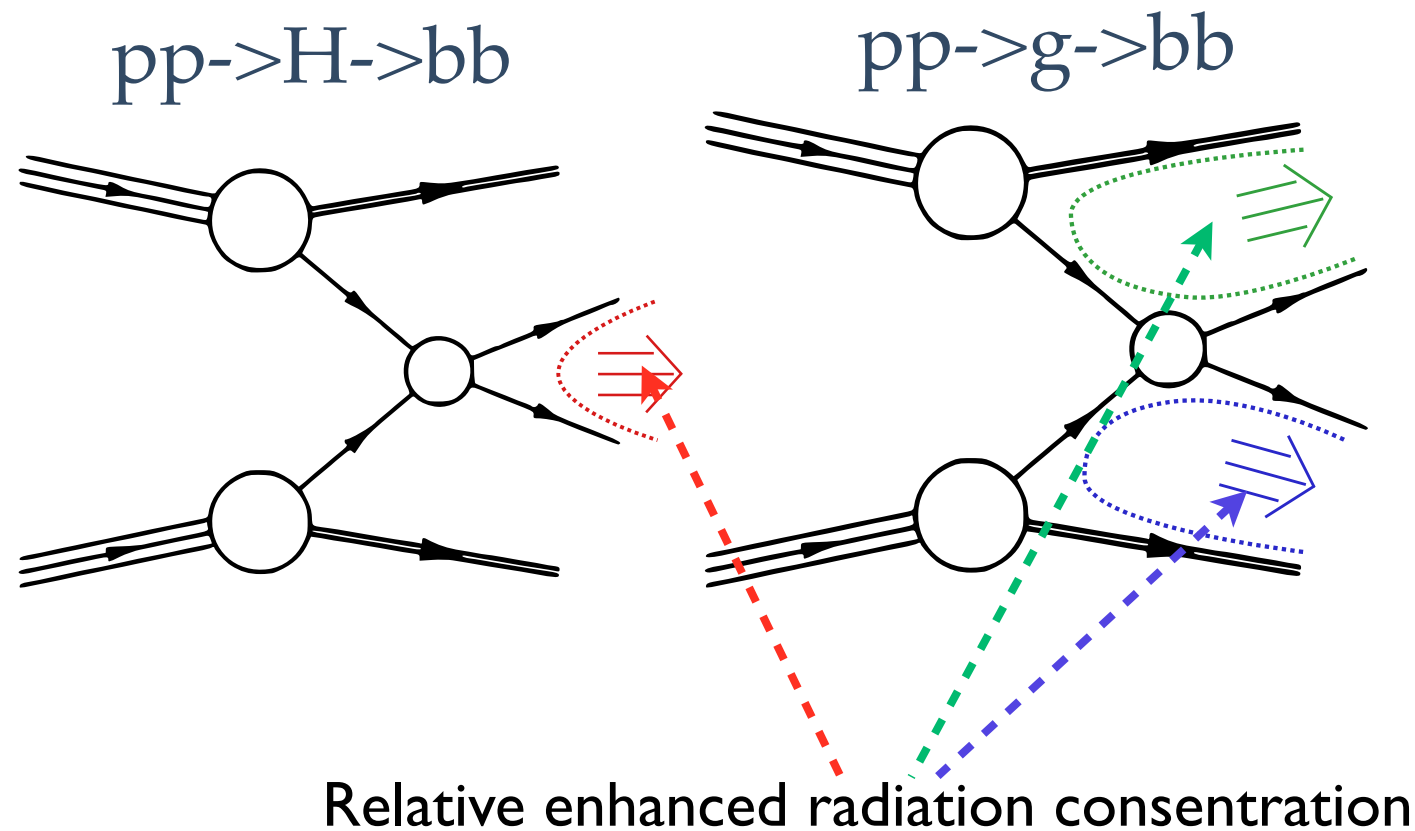
Barr, Konar, Kong, Lester, Matchev, Park | 08.5182



- Such variables are crucial in discovery and reconstruction of NP.
- They can be affected by additional radiation, etc.
  - More tests.

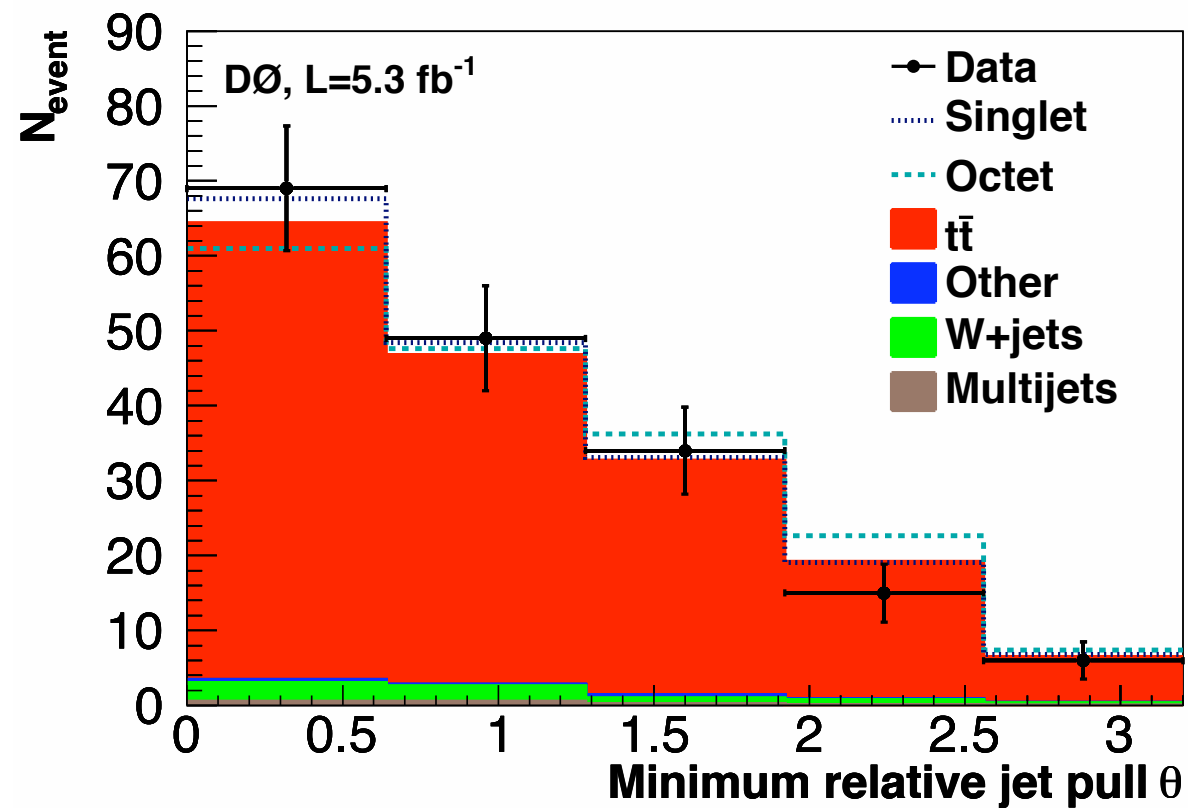
# Superstructure

Gallicchio, Schwartz, 1001.5027



- Using more global information.
- Applications to other channels as well.
- Not very well modeled by MC, exp. test crucial.

# $W \rightarrow$ jets in $t\bar{t}b\bar{a}$



- part of  $t\bar{t}b\bar{a}$  events
  - Good (statistics) sample of singlet  $\rightarrow$  dijet.
- Sensitive to higher level of pile-up.

# Examples.

- F-term breaking, with R-symmetry preserved.

$$W = \mu^2 X + \dots, \quad K = XX^\dagger + \frac{(XX^\dagger)^2}{M^2} + \dots$$

$$R[X] = 2, \quad F_X = \mu^2, \quad \langle X \rangle = 0$$

$$\int d^4\theta \frac{XX^\dagger}{M^2} Q^\dagger Q \rightarrow m_{\tilde{Q}}^2 = \frac{\mu^4}{M^2}$$

$$\int d^4\theta \frac{XX^\dagger}{M^3} W_\alpha W^\alpha r \rightarrow m_{1/2} = \frac{\mu^4}{M^3} r \quad \text{r: additional R-symm breaking spurion}$$

- Similar story for D-term breaking.