

## Problem 2. Pulsestacker in the visible range

A 3.8ps long gaussian pulse of the second harmonic wave from a Nd:YVO4 laser needs to be stacked to produce a quasy flat-top shape.

- Find central wavelength for second harmonic using web resources
- Calculate delay between consecutive pulses when using a 10 mm and a 20 mm long z-cut YVO4 crystal for stacking (Sellmeier equations can be found on CASIX website).
- Draw the arrangement showing input polarization and crystal axes  
optional) Calculate total intensity profile not taking into account interference

### I.) The original pulse profile

$$\begin{aligned}
 c &:= 0.299792 \text{ mm/ps} && \text{speed of light} \\
 \tau_0 &:= 3.8 \text{ ps} && \text{pulse length} \\
 \lambda_0 &:= 0.532 \cdot 10^{-3} \text{ mm} && \text{central wavelength} \\
 \Delta\lambda &:= 0.000004 \text{ mm} && \text{spectral range included in calculation} \\
 \Pi &:= 2 \cdot \pi \cdot c && \omega_0 := \frac{\Pi}{\lambda_0} \\
 \omega_0 &= 3.541 \times 10^3 && \text{central frequency}
 \end{aligned}$$

### Complex field spectrum of the Gaussian pulse

$$\begin{aligned}
 \Delta &:= \frac{4 \cdot \ln(2)}{\tau_0} && \text{spectral width} \\
 K2 &:= \frac{\sqrt{2 \cdot \ln(2)}}{\Delta} && \epsilon_0(\Delta\omega) := \exp[-(K2 \cdot \Delta\omega)]^2
 \end{aligned}$$

### The temporal shape

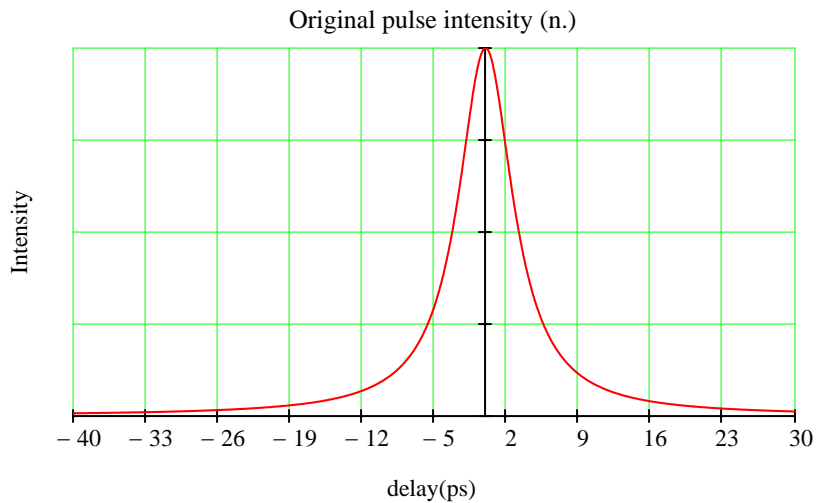
(in the case of broadband pulses full spectral domain can be calculated, not necessary for this case)

$$\begin{aligned}
 \Omega_1 &:= \frac{\Pi}{\lambda_0 - \frac{\Delta\lambda}{2}} - \omega_0 && \Omega_2 := \frac{\Pi}{\lambda_0 + \frac{\Delta\lambda}{2}} - \omega_0 \\
 N &:= 1000 && d\omega := \frac{\Omega_1 - \Omega_2}{N} \\
 p &:= 0 \dots N - 1 && d\omega = 0.027 \\
 \omega_p &:= \Omega_2 + p \cdot d\omega
 \end{aligned}$$

$$E(t) := \frac{1}{2\pi} \cdot \sum_{p=0}^{N-1} \left[ \epsilon_0(\omega_p) \cdot \exp[i \cdot (\omega_p \cdot t - \omega_0 \cdot t)] \cdot d\omega \right]$$

time window

$$tt_1 := -40 \quad tt_2 := 30 \quad ddt := 0.1 \quad tt := tt_1, tt_1 + ddt .. tt_2$$



### III.) The stacking

#### Delay generated by the YVO4

Sellmeier equations from CASIX website

$$o(\lambda_s) := 3.77834 + \left[ \frac{0.069736}{(\lambda_s^2 - 0.04724)} \right] - 0.0108133 \cdot \lambda_s^2$$

$$e(\lambda_s) := 4.59905 + \left[ \frac{0.110534}{(\lambda_s^2 - 0.04813)} \right] - 0.0122676 \cdot \lambda_s^2$$

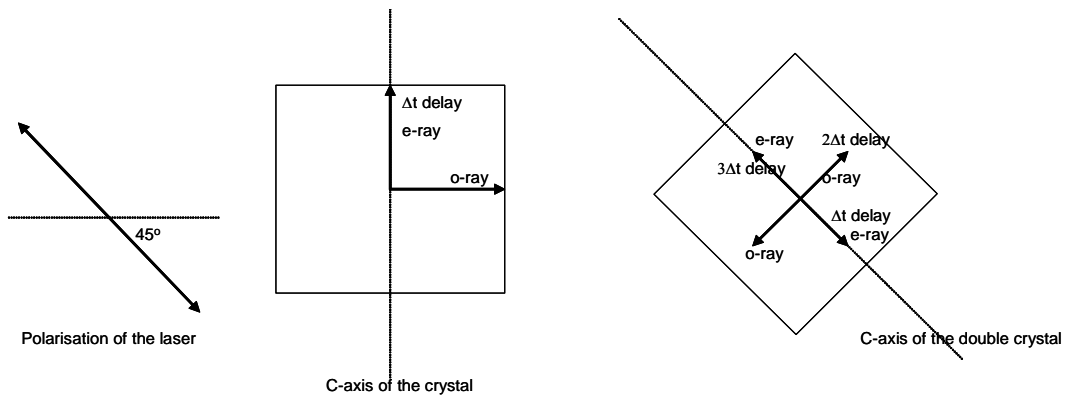
$$\lambda := 10 \quad \text{mm}$$

$$n_e := \left( \sqrt{e(\lambda_0 \cdot 10^3)} \right)$$

$$n_o := \left( \sqrt{o(\lambda_0 \cdot 10^3)} \right)$$

$$\text{deltat} := |n_e - n_o| \cdot \frac{1}{c} \quad \text{deltat} = 7.776 \quad \text{ps}$$

#### Polarization setup



Following allows to calculate pulse shape error resulting from inaccurate alignment of the crystals

$\alpha := 45\text{deg}$  crystal axis to input polarisation

$\beta := 90\text{deg}$  2nd crystal axis to input polarisation

$E_e(t) := [\cos(\alpha) \cdot (E(t) \cdot \cos(\beta - \alpha) + E(t + 2 \cdot \text{deltat}) \cdot \sin(\beta - \alpha))]$  extraordinary fields

$E_o(t) := [\sin(\alpha) \cdot (E(t - \text{deltat}) \cdot \cos(\beta - \alpha) + E(t + \text{deltat}) \cdot \sin(\beta - \alpha))]$  ordinary fields

$\text{Sum}(t) := [(|E_e(t)|)^2 + (|E_o(t)|)^2]$  total temporal intensity distribution

