

Introduction to Lasers I

October 14th-19th 2012, GANIL, Caen, France
1st LA³NET School Laser Applications at Accelerators

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CLPU CENTRO DE LASERES PULSADOS ULTRACORTOS ULTRAINTENSOS

Centro de Laseres Pulsados

Salamanca

www.clpu.es



MINISTERIO DE ECONOMÍA Y COMPETITIVIDAD



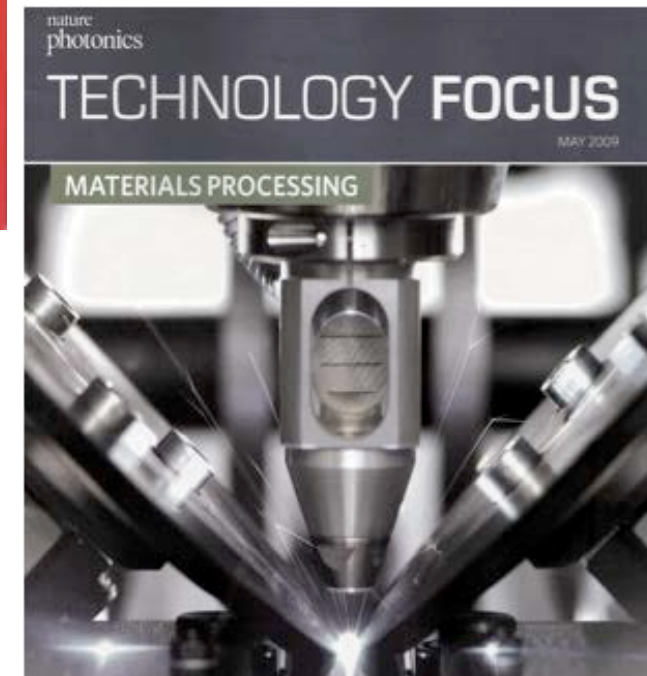
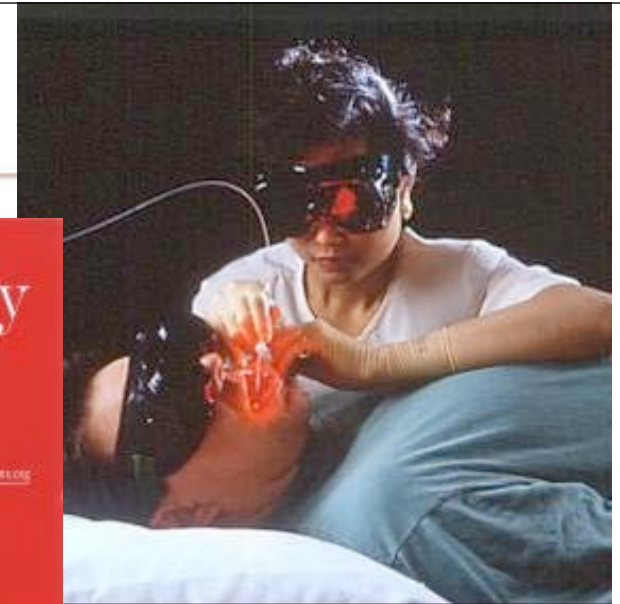
Junta de Castilla y León



UNIVERSIDAD DE SALAMANCA



Lasers are very popular



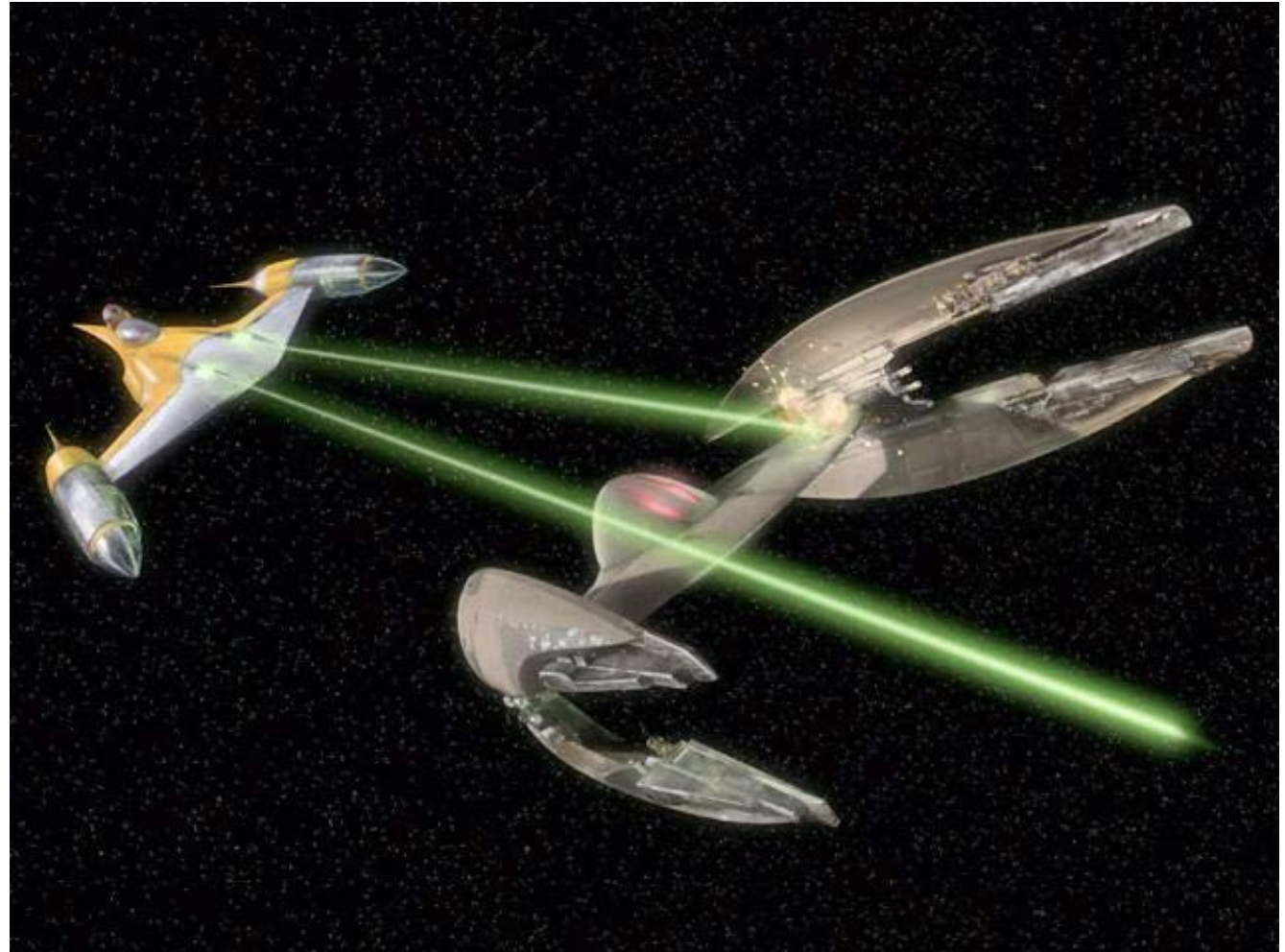
Lasers have many applications

- laser spectroscopy
- optical communications
- holography
- laser cut and industrial applications
- medical applications: surgery, oftalmology, ...
- laser hair removal
- ...
- laser acceleration

New sciences as Photonics have appeared

And very fantastic applications !

light in vacuum





Introduction to Lasers I

- Laser fundamentals
- Optical resonators
- Gaussian Beams
- Laser Pumping
- Multimode lasing



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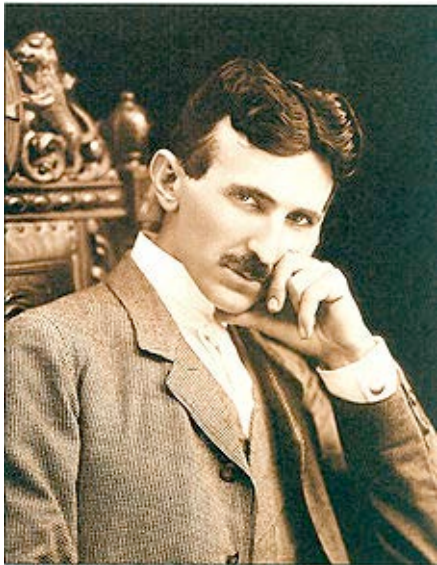
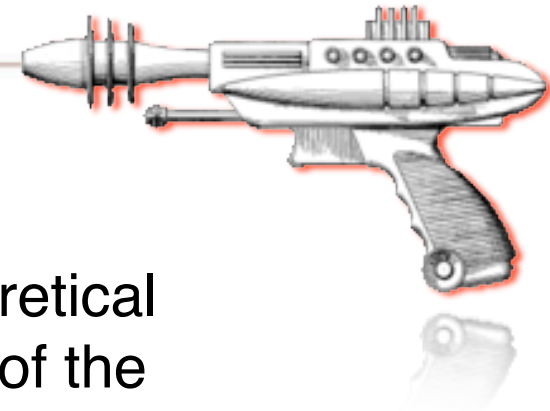
Introduction to Lasers I

- **Laser fundamentals**
- Optical resonators
- Gaussian Beams
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- Multimode lasing

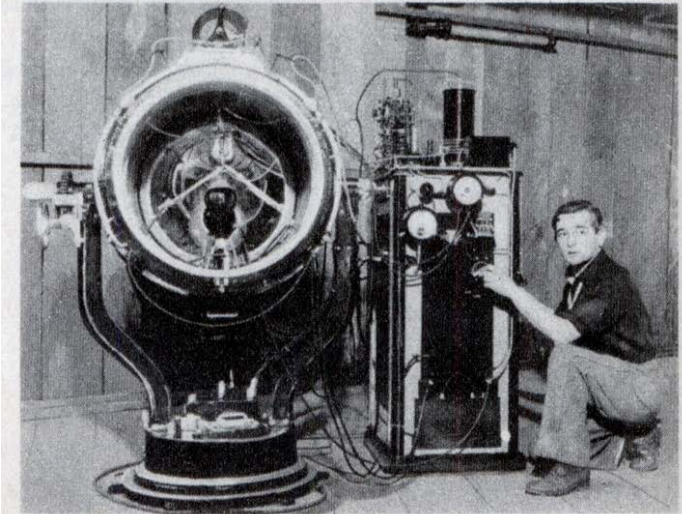
C First is Imagination

Death ray From Wikipedia

The **death ray** or **death beam** was a theoretical particle beam or electromagnetic weapon of the 1920s through the 1930s that was claimed to have been invented independently by Nikola Tesla, ..., as well as others.



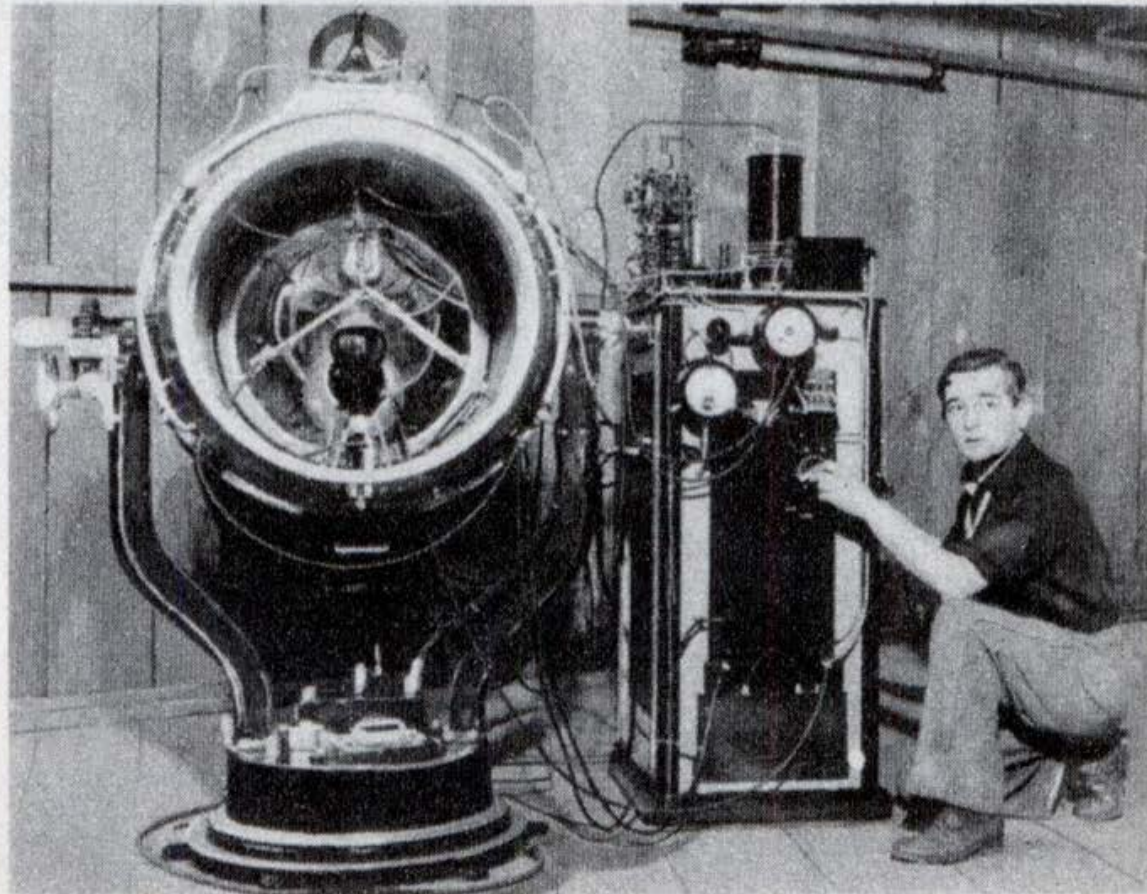
Death Ray Effective On Snakes



Posing before his infra-red death ray, Henry Fleur prepares to turn the control that will place the ray into operation. In tests



Death Ray Effective On Snakes



1936

Posing before his infra-red death ray, Henry Fleur prepares to turn the control that will place the ray into operation. In tests made before a jury the instrument proved effective on snakes.

Then comes Science



LEIPZIG, 1905.

ANNALEN DER PHYSIK.



6. *Über einen
die Erzeugung und Verwandlung des Lichtes
betreffenden heuristischen Gesichtspunkt;
von A. Einstein.*

Zwischen den theoretischen Vorstellungen, welche sich die Physiker über die Gase und andere ponderable Körper gebildet haben, und der Maxwell'schen Theorie der elektromagnetischen Prozesse im sogenannten leeren Raume besteht ein tiefgreifender formaler Unterschied. Während wir uns

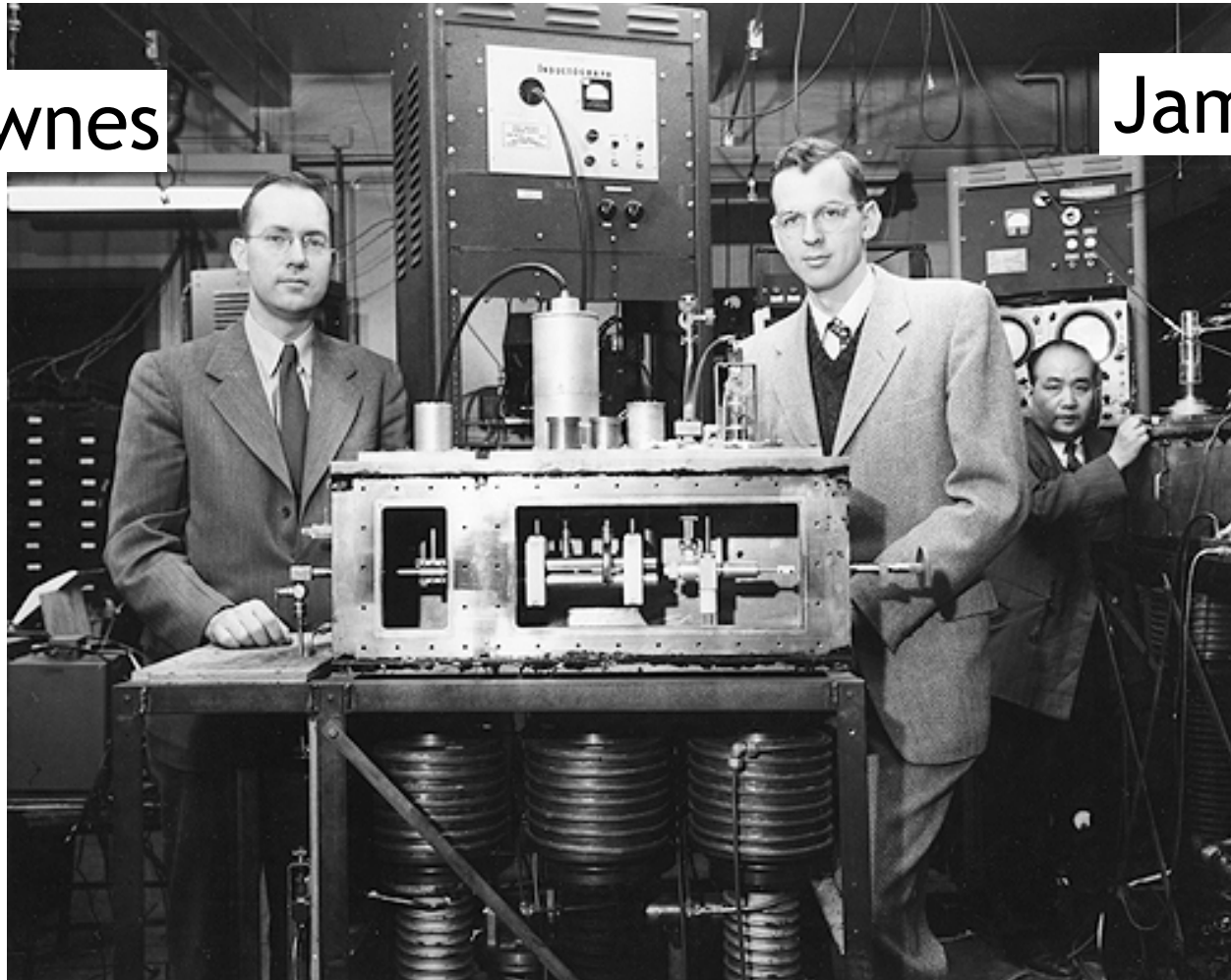
1905

Maser came first

Microwave Amplification by Stimulated Emission of Radiation

Charles Townes

James Gordon



1955

Credit: Bettmann/Corbis

Laser Fundamentals



Charles Townes



Physics
1964



Nicolay Basov
"for fundamental work in the field of quantum electronics, which has led to the construction of oscillators and amplifiers based on the maser-laser principle"

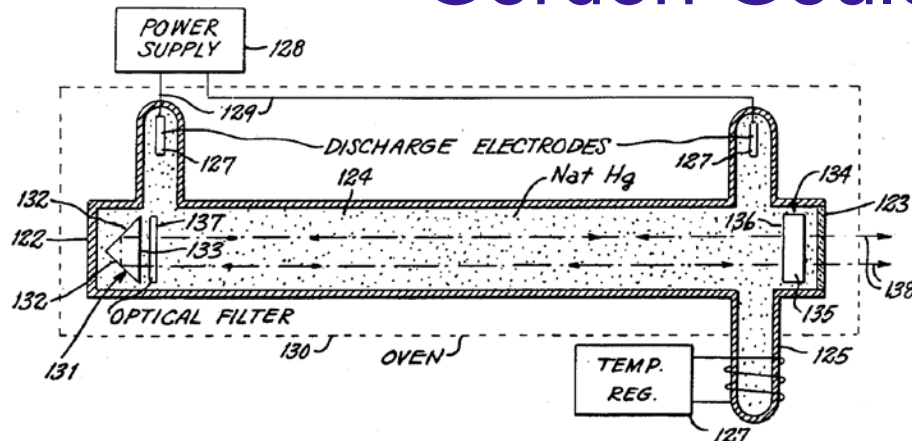


Aleksandr Prokhorov

To publish or to patent?



Gordon Gould



United States Patent [19]

Gould

[54] **LIGHT AMPLIFIERS EMPLOYING COLLISIONS TO PRODUCE A POPULATION INVERSION**

[76] Inventor: **Gordon Gould**, 1200 N. Nash Ave., Arlington, Va. 22209

[21] Appl. No.: **823,611**

[22] Filed: **Aug. 11, 1977**

Related U.S. Application Data

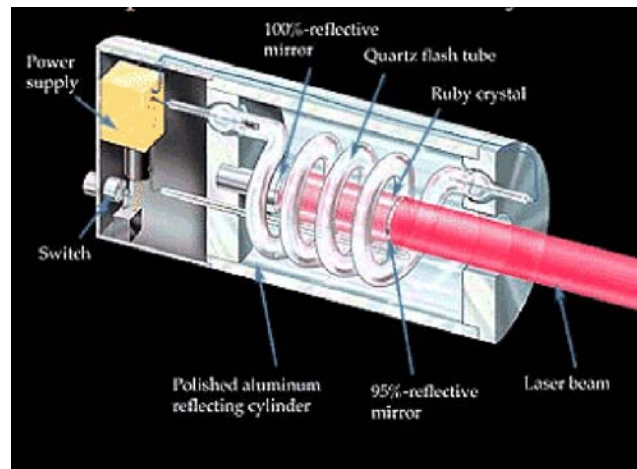
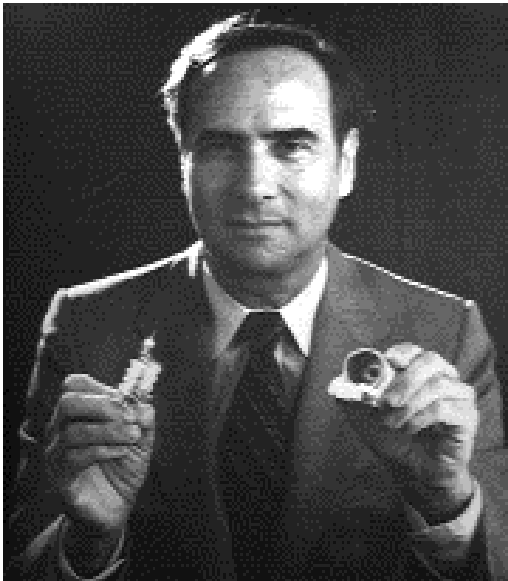
[60] Division of Ser. No. 498,065, Aug. 16, 1974, Pat. No. 4,053,845, which is a continuation of Ser. No. 644,035, Mar. 6, 1967, abandoned, and Ser. No. 804,540, Apr. 6, 1959, abandoned, said Ser. No. 644,035, is a division of Ser. No. 804,540, Apr. 6, 1959, abandoned, and a continuation-in-part of Ser. No. 804,539, Apr. 6, 1959, abandoned.

... and finally the first laser ... 1960

Light Amplification by Stimulated Emission of Radiation

T H Maiman

Rubi laser @ 694 nanometers



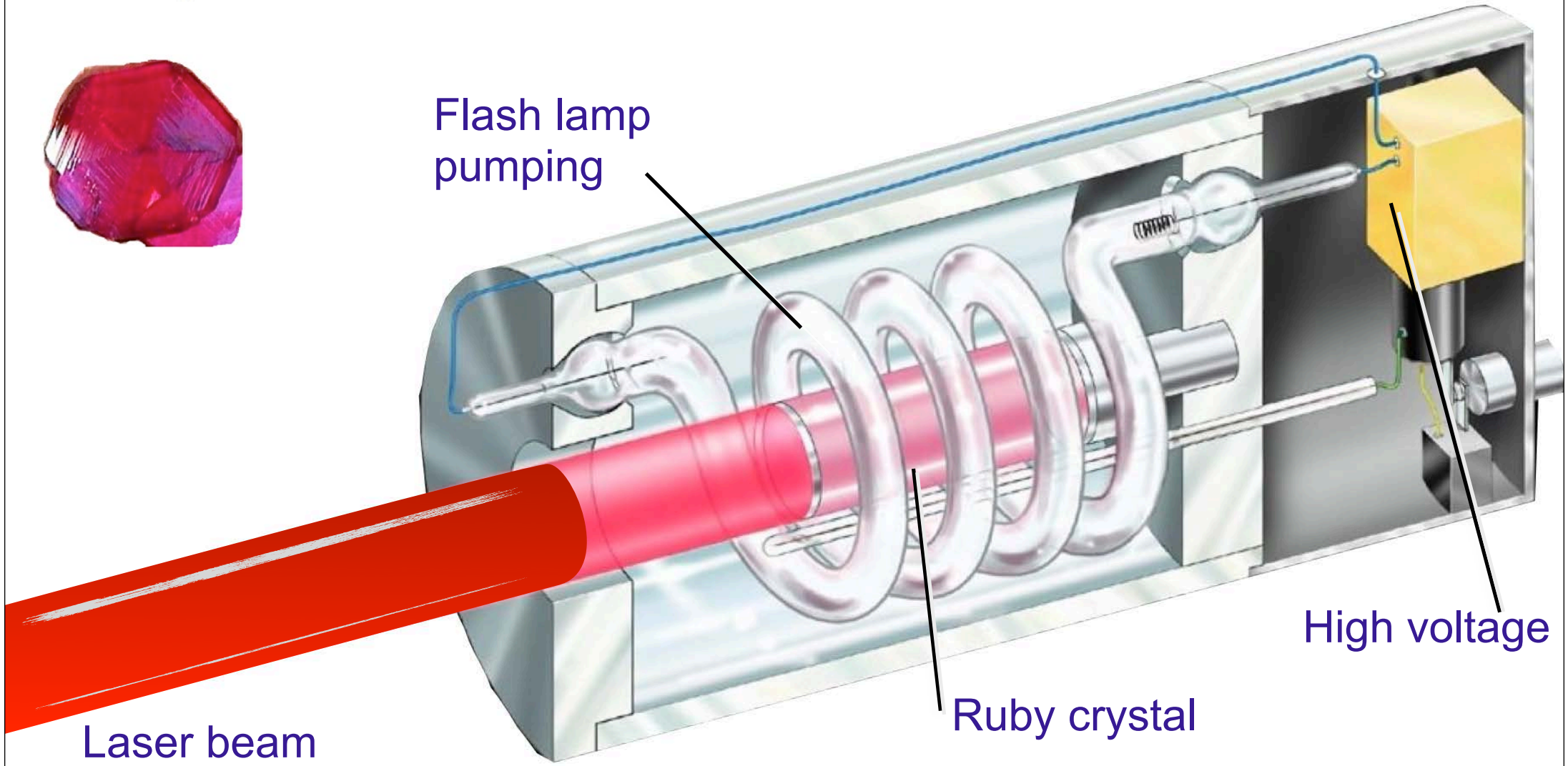
First laser was named
as first optical maser



Ruby Laser ... 1960



Flash lamp
pumping



High voltage

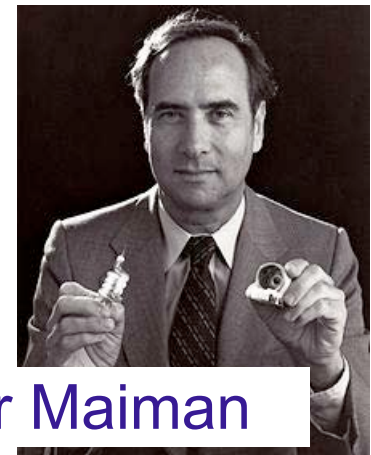
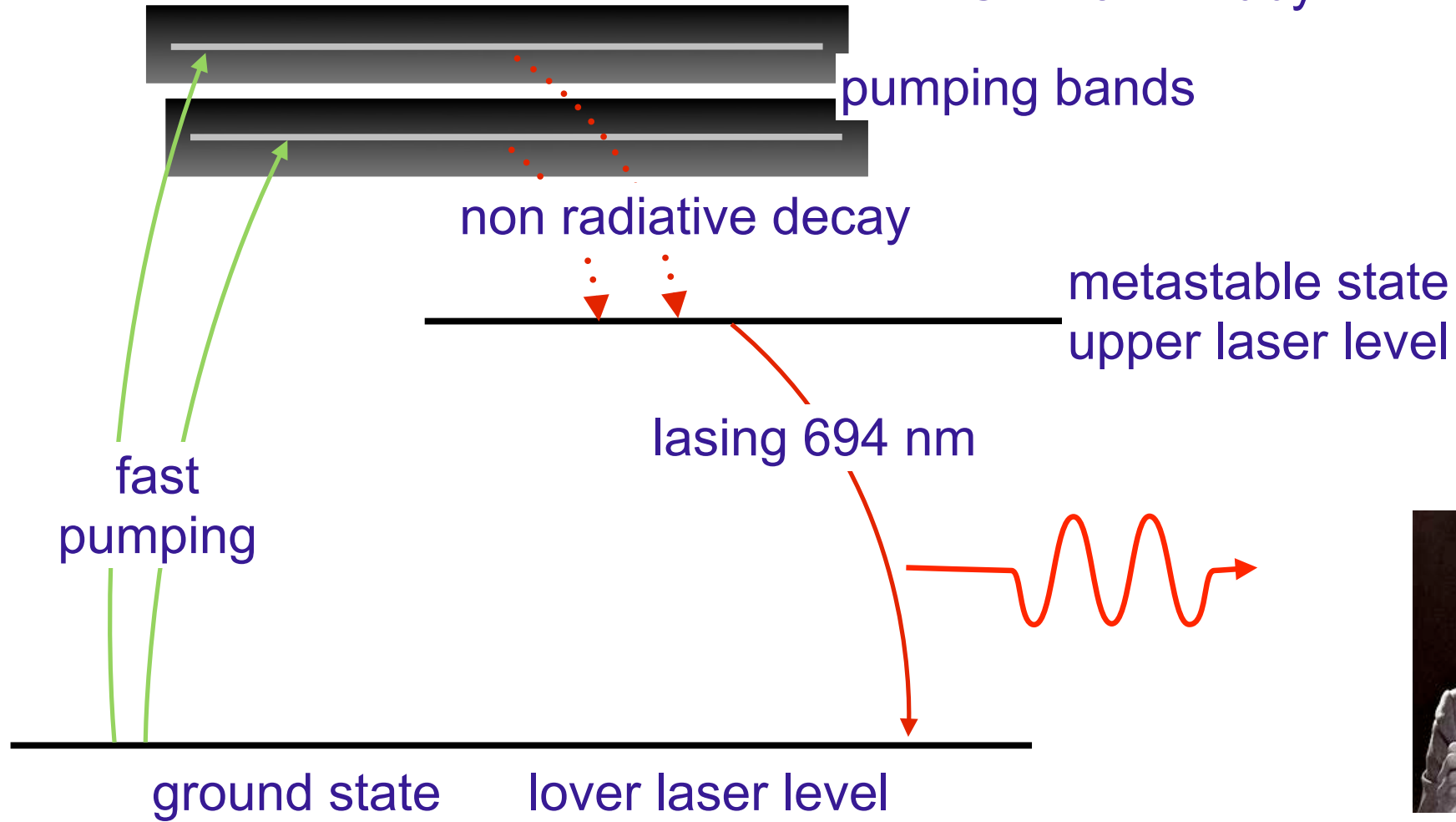
Ruby crystal

Laser beam



Chromium-ion laser (ruby laser)

Cr^{+++} ion in ruby



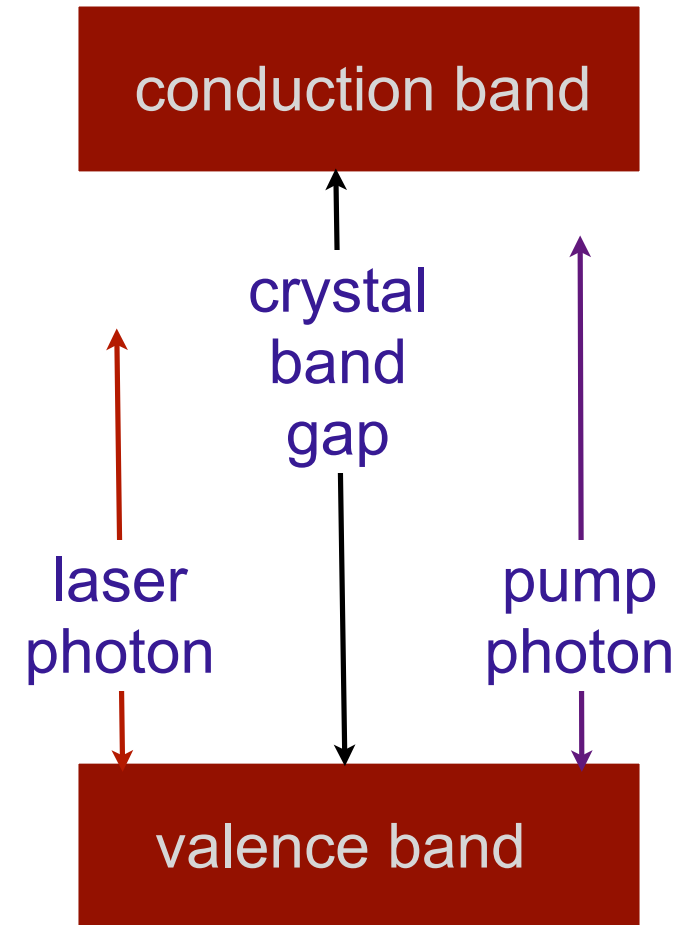
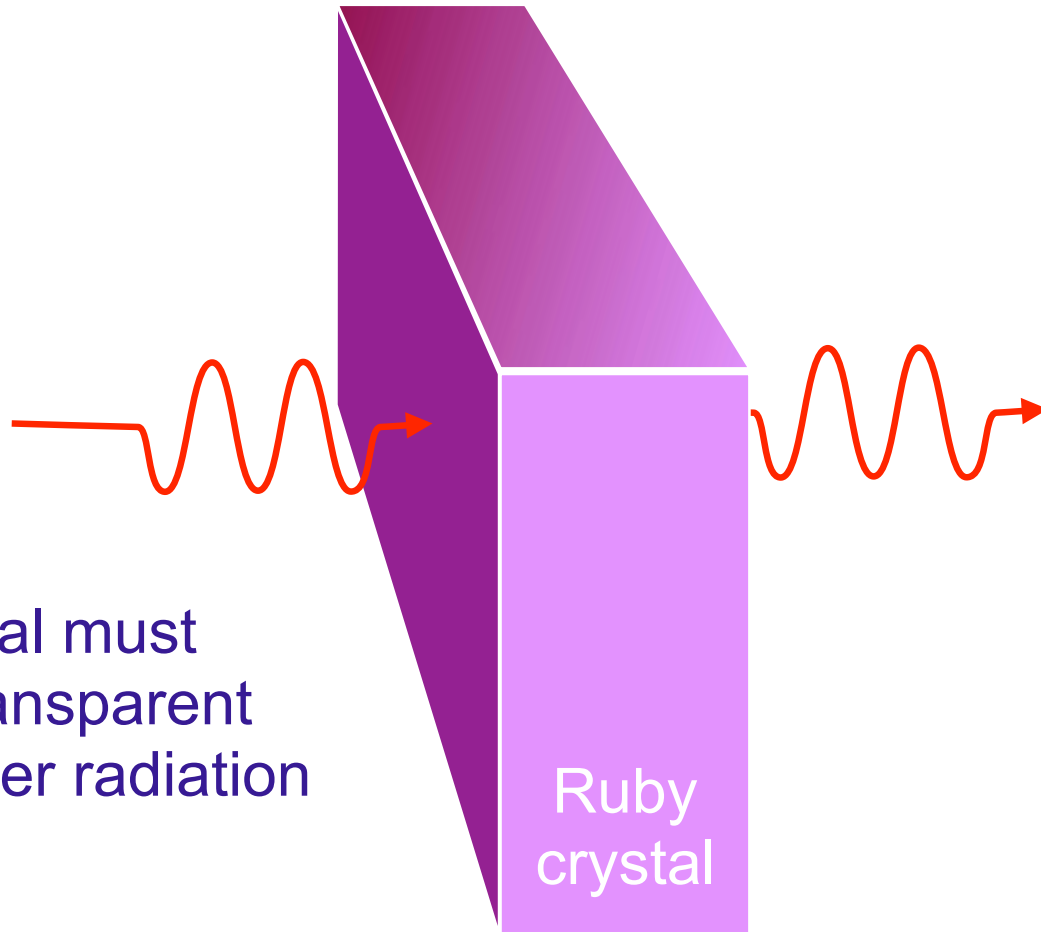
Theodor Maiman



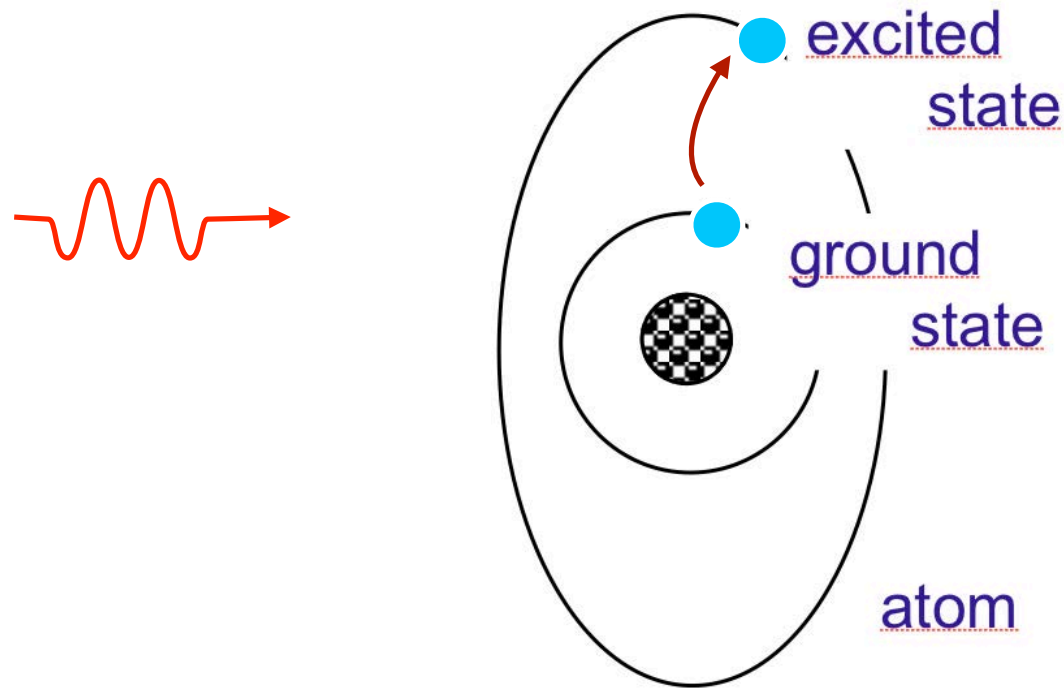
Role of the crystal matrix (ruby)

Just do not disturb!

Crystal must be transparent to laser radiation

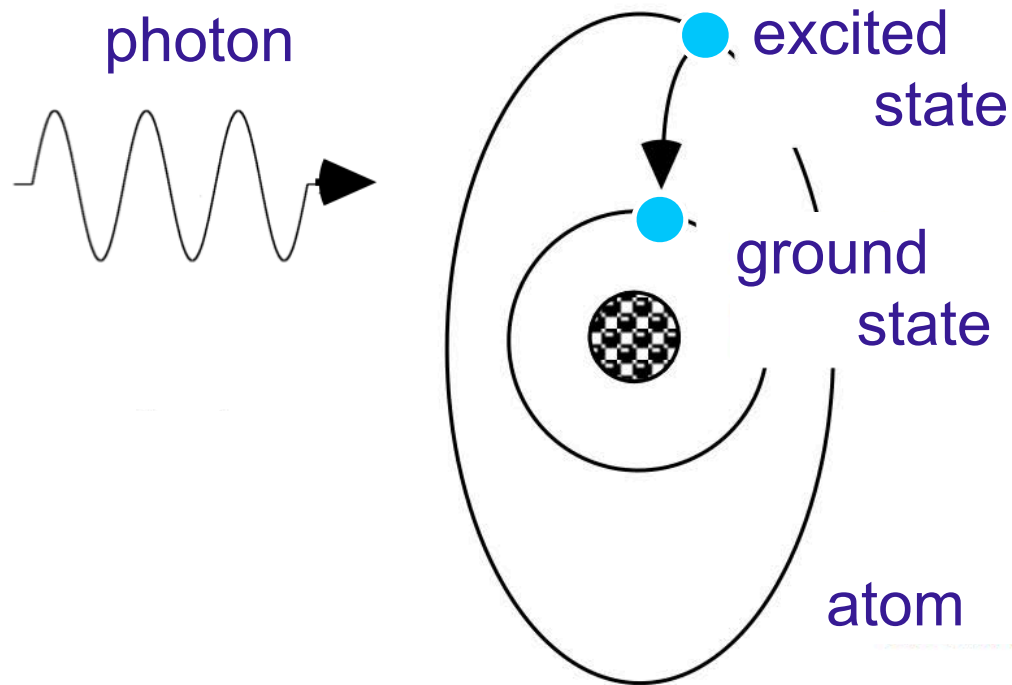


Photon absorption



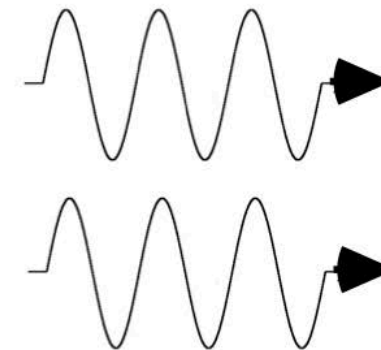
All that in dipole approx

Stimulated emission



laSer

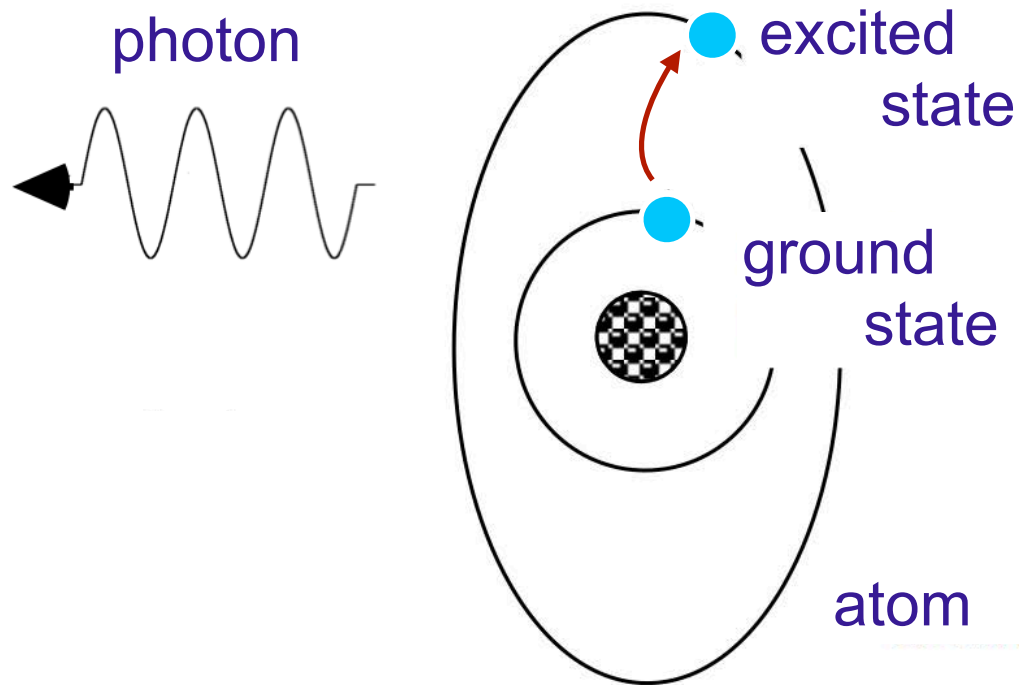
two identical copies
of the initial photon



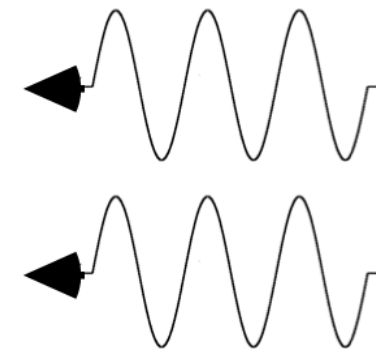
Similar to cloning the photon !!!

Photon absorption

Change arrow of time

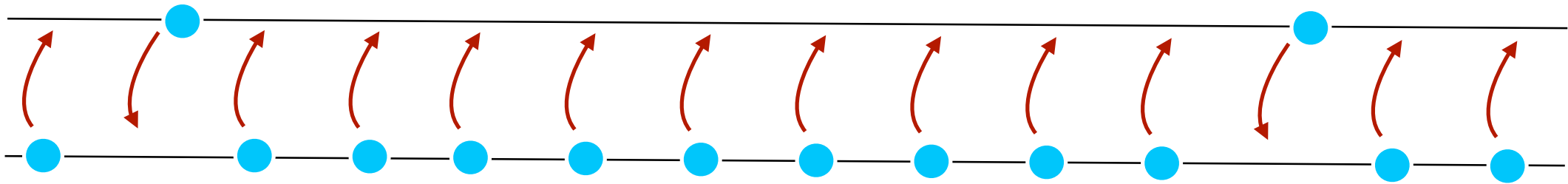


two photons



stimulated emission and absorption
are inverse processes ...
... so they compete

Photon absorption

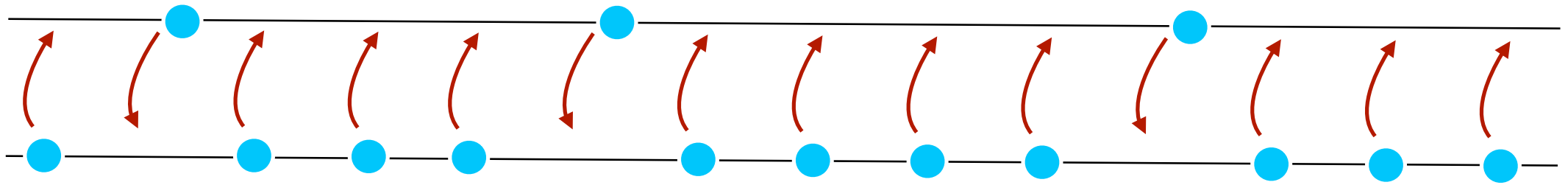


Normally, more electrons in the ground state than in the excited state

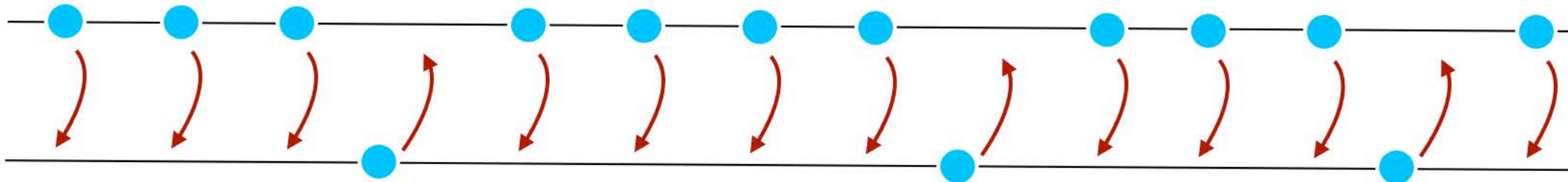
Absorption dominates over stimulated emission ...

... no lasing

Absorption vs stimulated emission



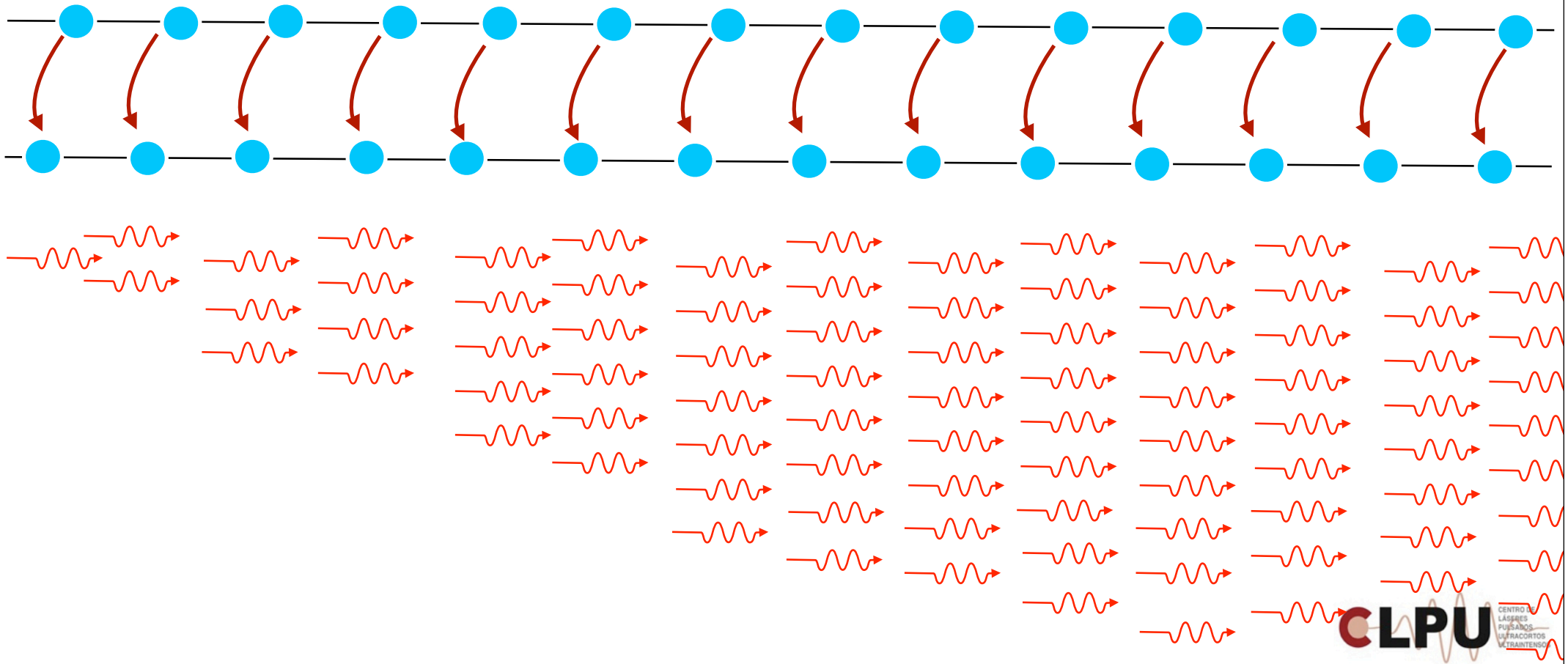
Normally, more electrons in the ground state than in the excited state
Absorption dominates over stimulated emission ... no lasing



If, more electrons in the excited state than in the ground state
then stimulated emission dominates over absorption ...

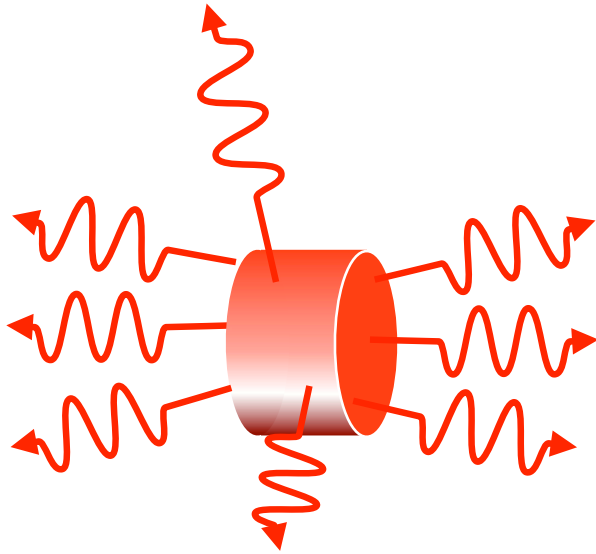
lasing !!!

Chain reaction



Anisotropy

Why a preferred direction for stimulated emission?



A preferred direction is given by a very long active material

Very long active material

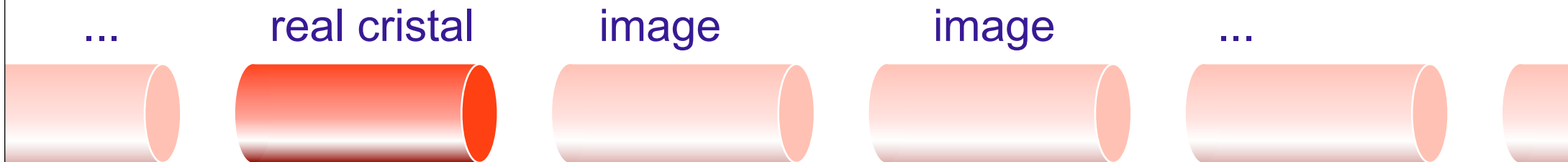
A preferred direction is given by a very long active material

Two options:

A real very long material: an optical fiber (with guiding)



A virtual very long material: a laser cavity

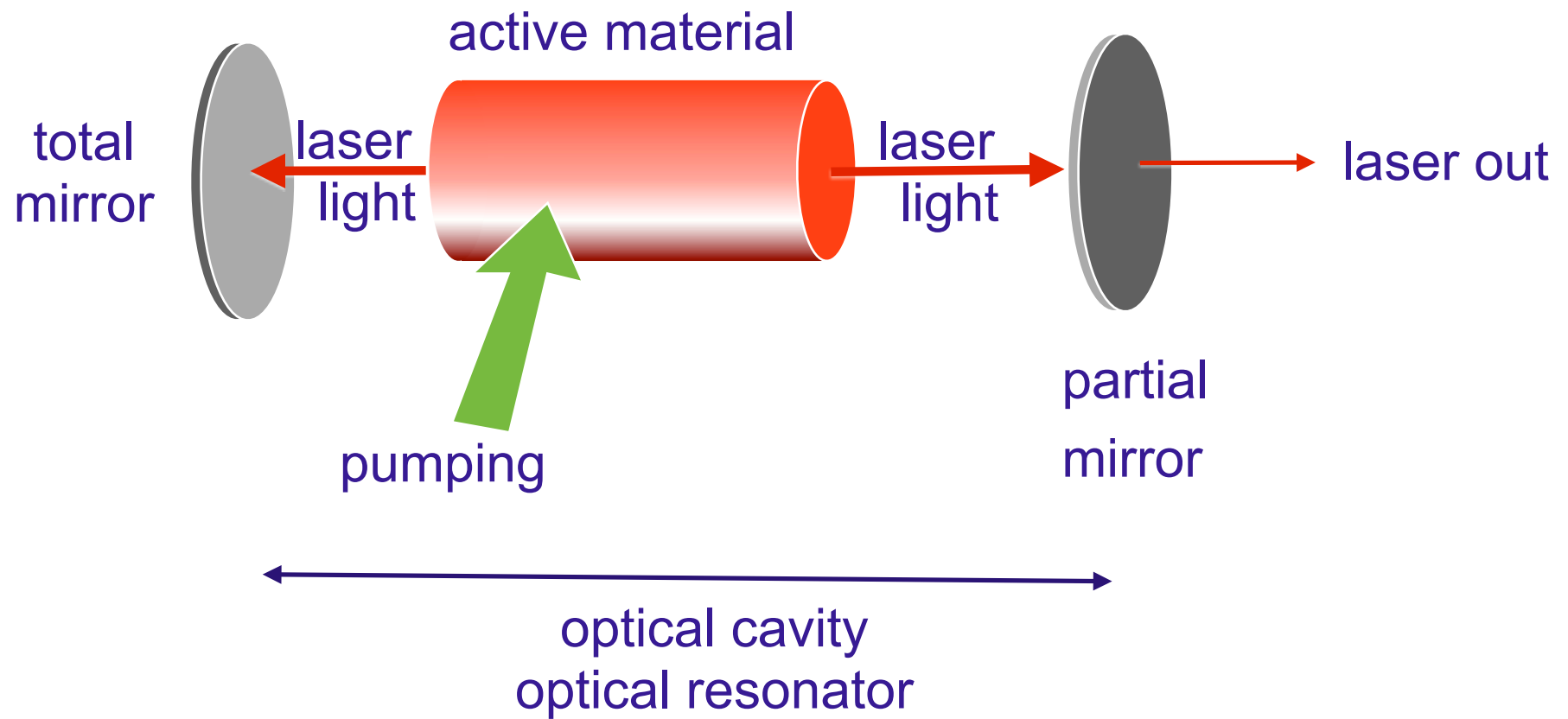




Introduction to Lasers I

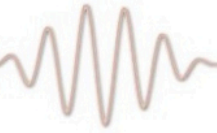
- Laser fundamentals
- **Optical resonators**
- Gaussian Beams
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Optical cavity

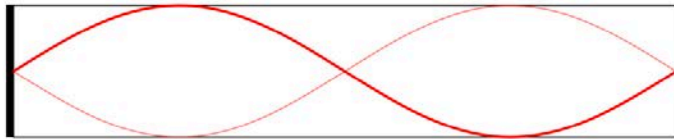




Cavity modes



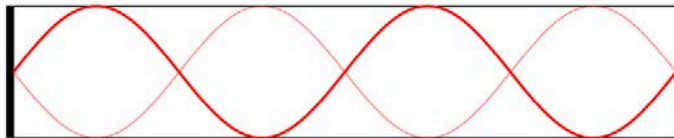
Fundamental mode $n=1$



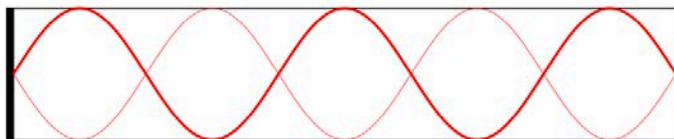
$n=2$



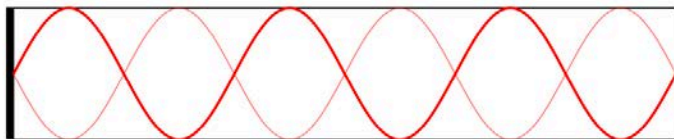
$n=3$



$n=4$



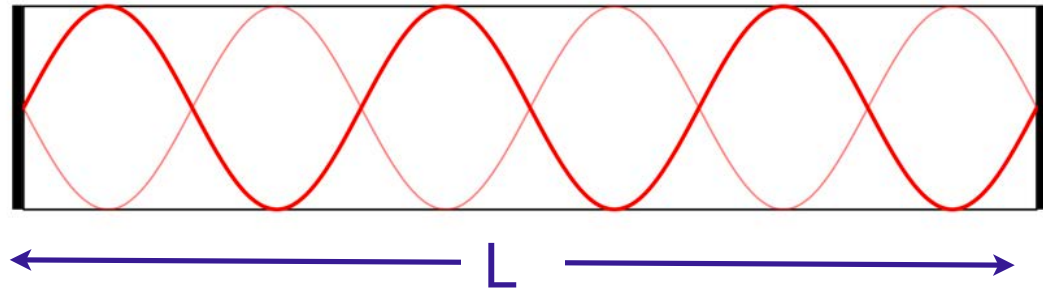
$n=5$



$n=6$



Cavity modes



Electric field inside the cavity

$$E(z,t) = E_0 \cos(kz) \cos(\omega_L t)$$

Boundary conditions

$$E(L,t) = E(-L,t) = 0$$

Allowed wavelengths

$$n\lambda = 2L \quad n = 1, 2, 3, \dots$$

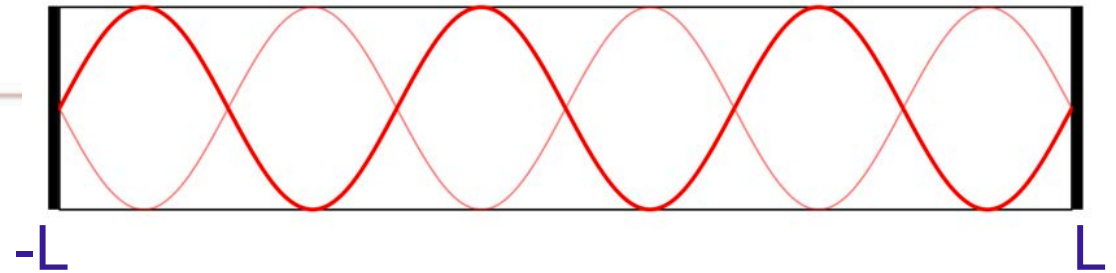
Cavity modes

$$k = \frac{2\pi}{\lambda} = \frac{n\pi}{L}$$

Resonant frequencies

$$\omega = kc = \frac{2\pi c}{\lambda} = n \frac{\pi c}{L}$$

Cavity modes



Example, $L = 25 \text{ cm}$ and 500 nm wavelength (green) corresponds to $n = 1\,000\,000$

Consecutive frequencies

$$\Delta\omega = \omega_{n+1} - \omega_n = \frac{\pi c}{L}$$

$$\lambda = \frac{2L}{n} = \frac{50 \text{ cm}}{1\,000\,000} = \frac{1000.}{1.} \text{ nm} = 500 \text{ nm}$$

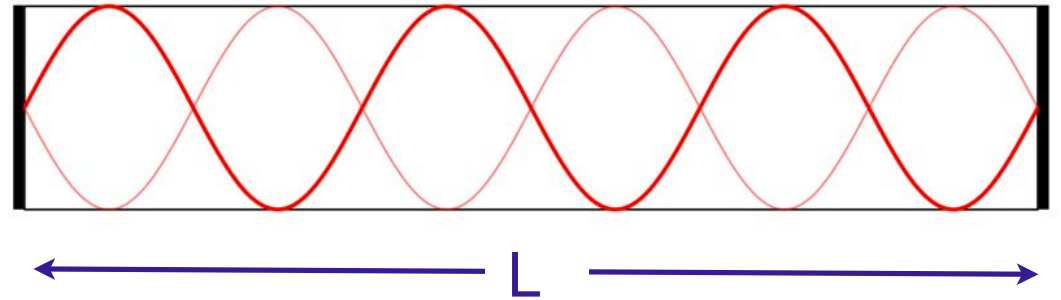
$$\nu_n = n \frac{c}{2L}$$

$$\lambda = \frac{2L}{n+1} = \frac{50 \text{ cm}}{1\,000\,001} = \frac{500.}{1.000001} \text{ nm} = 499.995 \text{ nm}$$

$$\nu_{n+1} = (n+1) \frac{c}{2L}$$

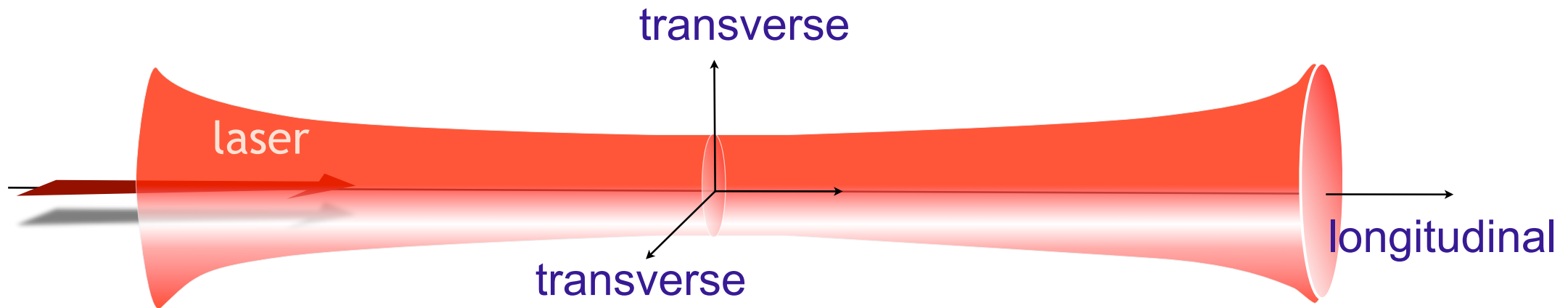
$$\Delta\nu = \frac{c}{2L} = \frac{300\,000\,000 \text{ m/s}}{0.5 \text{ m}} = 600 \text{ MHz} = 0.6 \text{ GHz}$$

Cavity longitudinal modes



Just longitudinal ... plane waves

Real waves have a transverse profile!



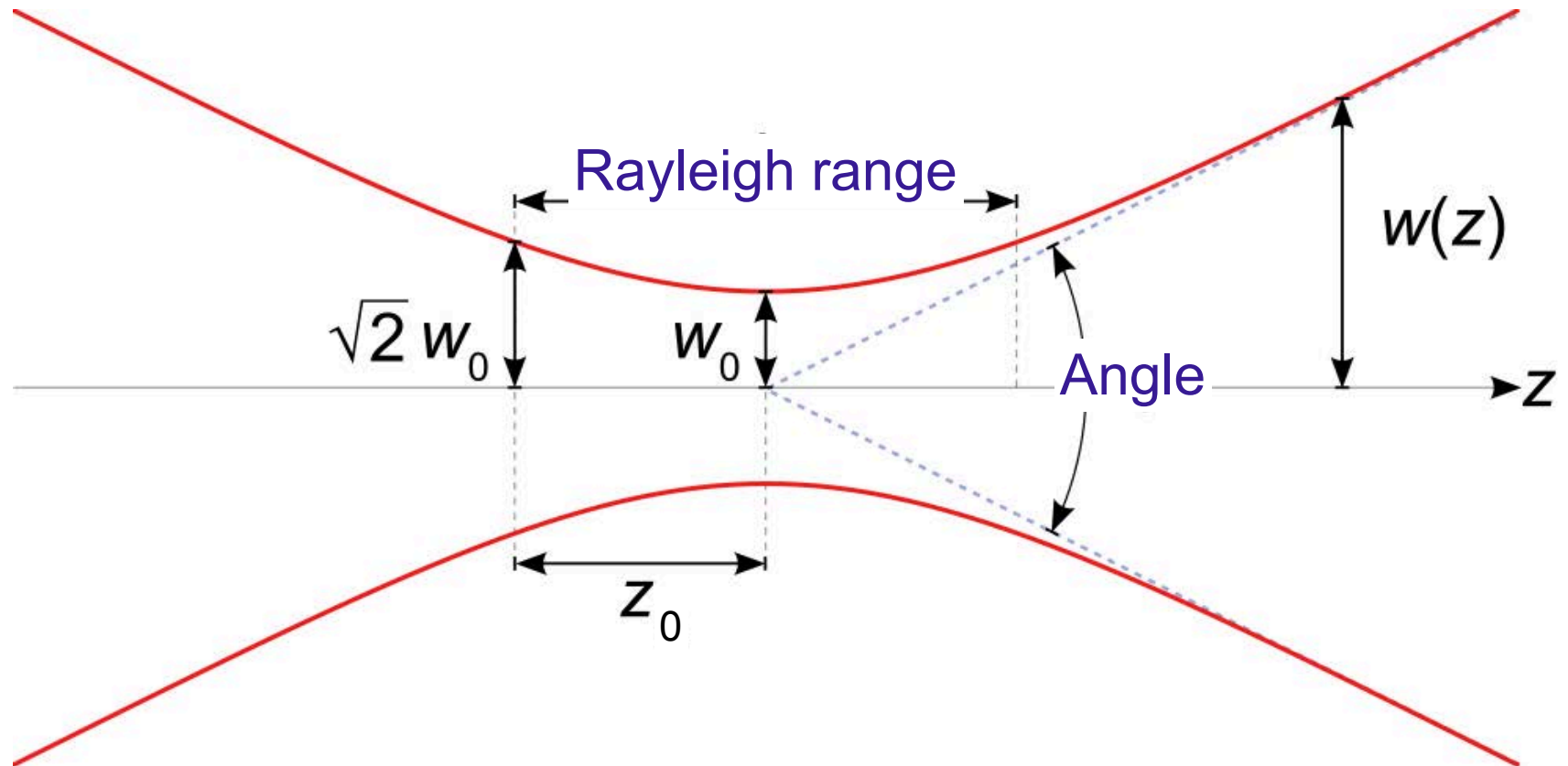


Introduction to Lasers I

- Laser fundamentals
- Optical resonators
- **Gaussian Beams**
- Laser Pumping
- Multimode lasing

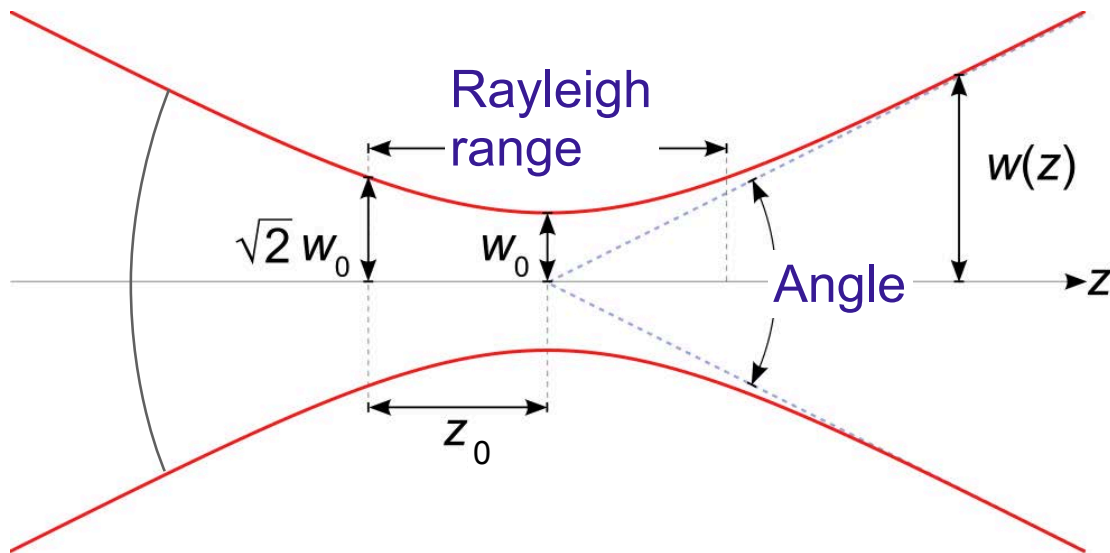


Gaussian beam





Gaussian beam (monochromatic) k



Radius

$$R(z) = z + \frac{z_0^2}{z}$$

Waist (spot size)

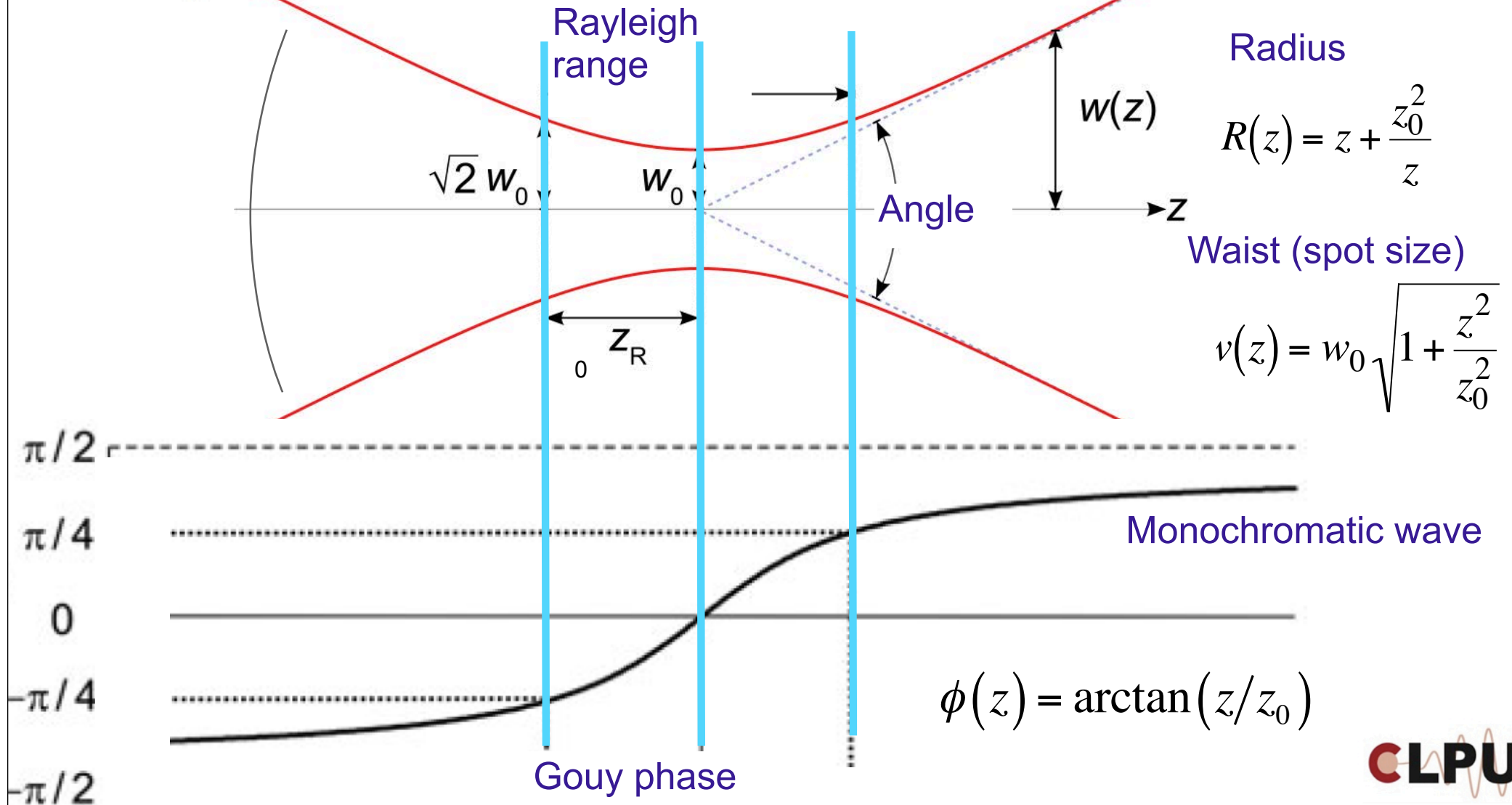
$$w(z) = w_0 \sqrt{1 + \frac{z^2}{z_0^2}}$$

$$E(x, y, z) = A \frac{w_0}{w(z)} \exp[i(kz - \phi(z))] \exp\left[ik \frac{x^2 + y^2}{2R(z)}\right] \exp\left[-\frac{x^2 + y^2}{w^2(z)}\right]$$

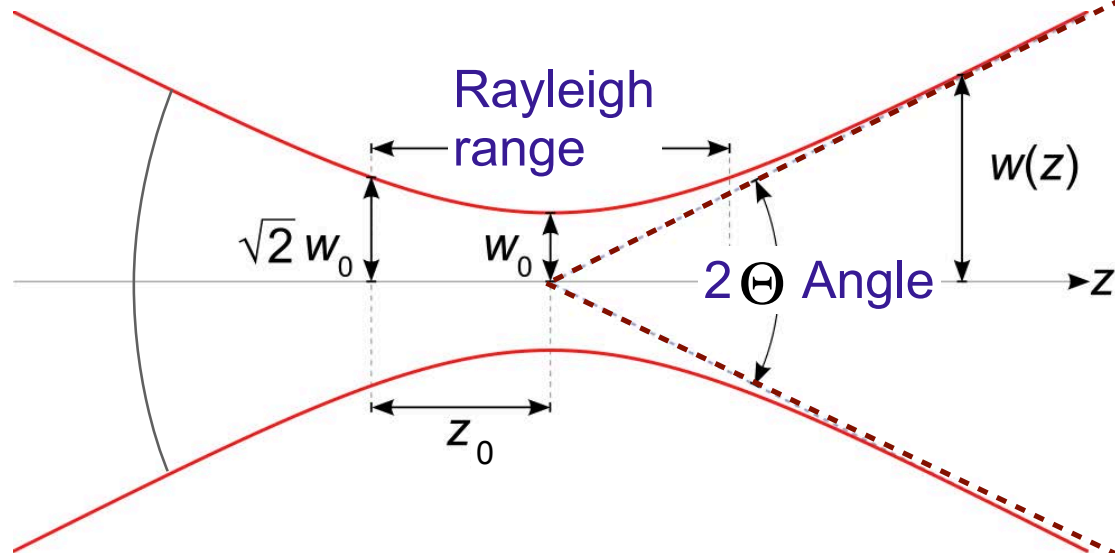
Monochromatic wave

$$\phi(z) = \arctan(z/z_0) \quad \text{Gouy phase}$$

Gouy phase



Divergence



Radius

$$R(z) = z + \frac{z_0^2}{z}$$

Waist (spot size)

$$w(z) = w_0 \sqrt{1 + \frac{z^2}{z_0^2}}$$

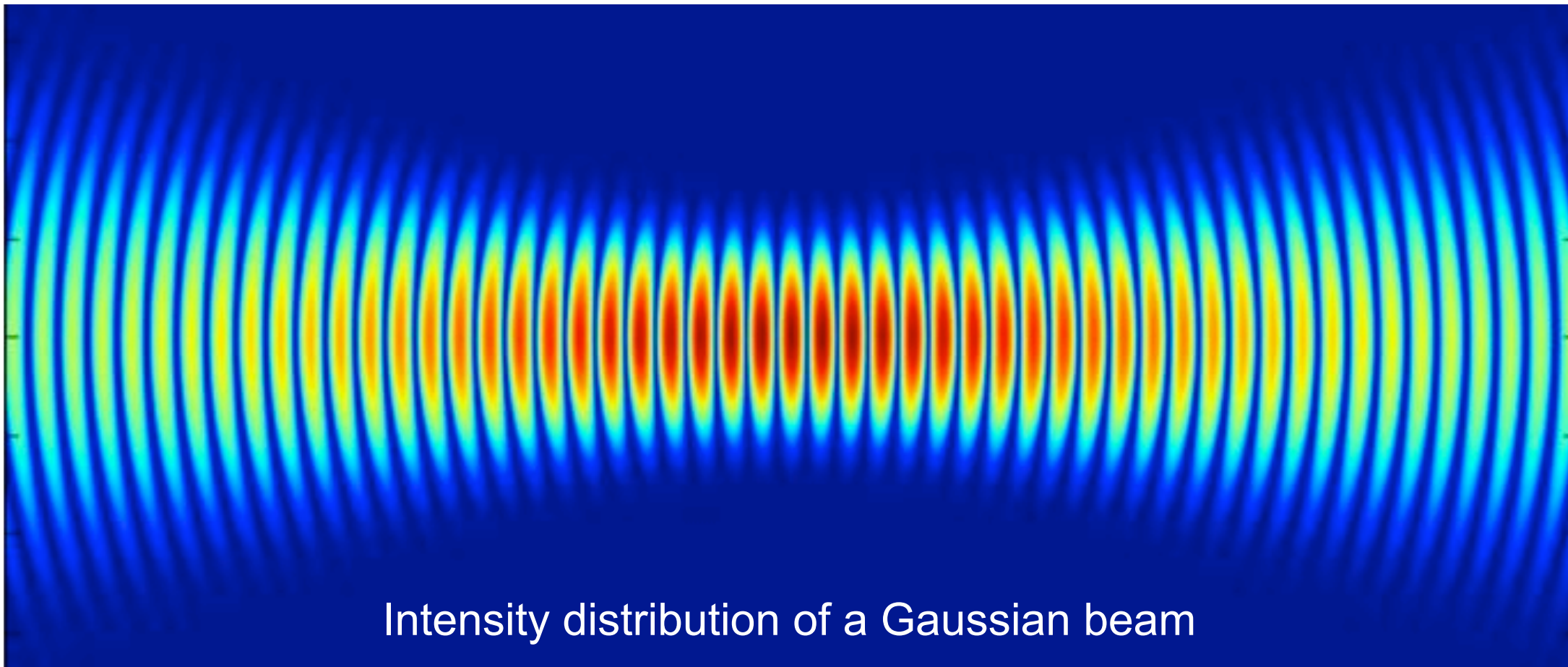
$$E(x, y, z) = A \frac{w_0}{w(z)} \exp[i(kz - \phi(z))] \exp\left[ik \frac{x^2 + y^2}{2R(z)}\right] \exp\left[-\frac{x^2 + y^2}{w^2(z)}\right]$$

Monochromatic wave

Divergence angle

$$\Theta = \frac{w_0}{z_0} = \frac{\lambda}{\pi w_0}$$

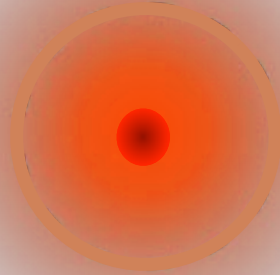
Gaussian beam





Gaussian field vs Gaussian intensity

$$E(x, y, z) = A \frac{w_0}{w(z)} \exp[i(kz - \phi(z))] \exp\left[ik \frac{x^2 + y^2}{2R(z)}\right] \exp\left[-\frac{x^2 + y^2}{w^2(z)}\right]$$



$$I(x, y, z) = A^2 \left(\frac{w_0}{w(z)}\right)^2 \exp\left[-2 \frac{x^2 + y^2}{w^2(z)}\right]$$

Electric field

Intensity

Distance to center

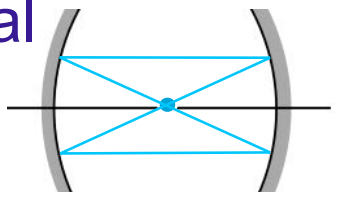
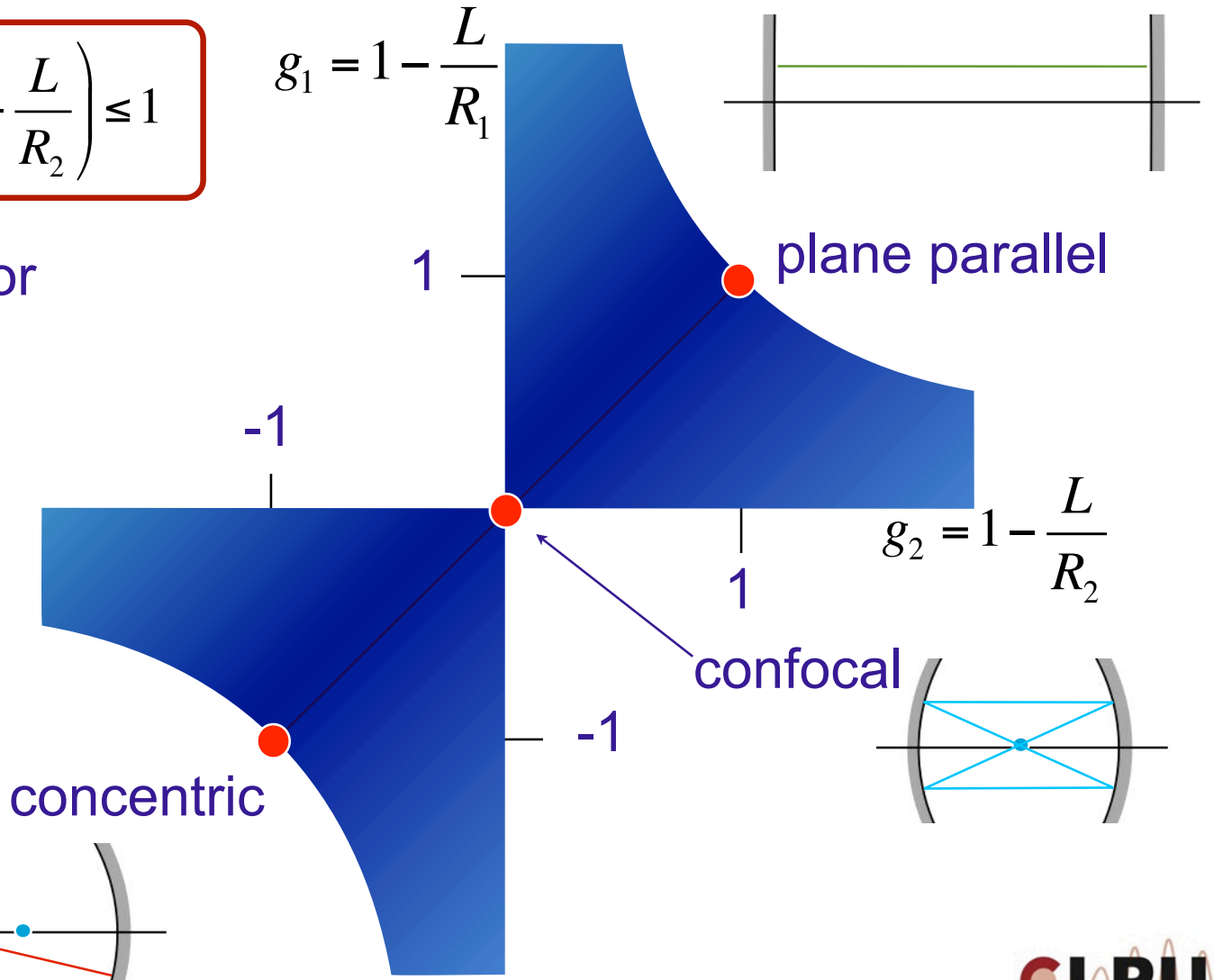
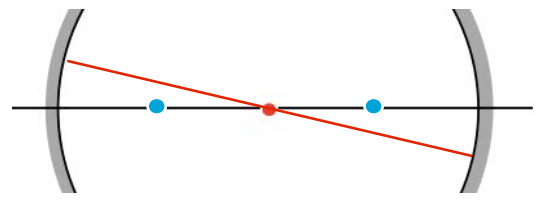
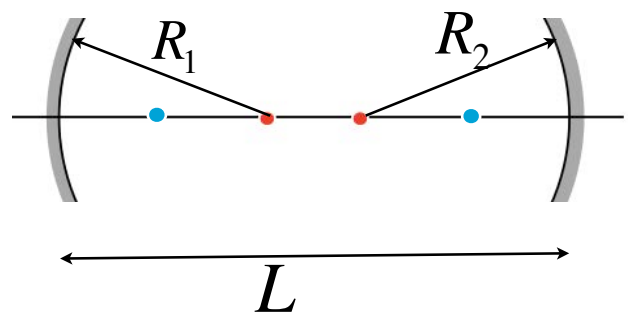
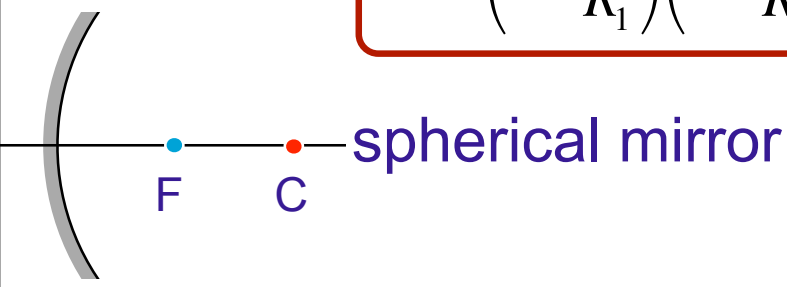
Stable cavities ...



$$0 \leq \left(1 - \frac{L}{R_1}\right) \left(1 - \frac{L}{R_2}\right) \leq 1$$

$$g_1 = 1 - \frac{L}{R_1}$$

$$g_2 = 1 - \frac{L}{R_2}$$

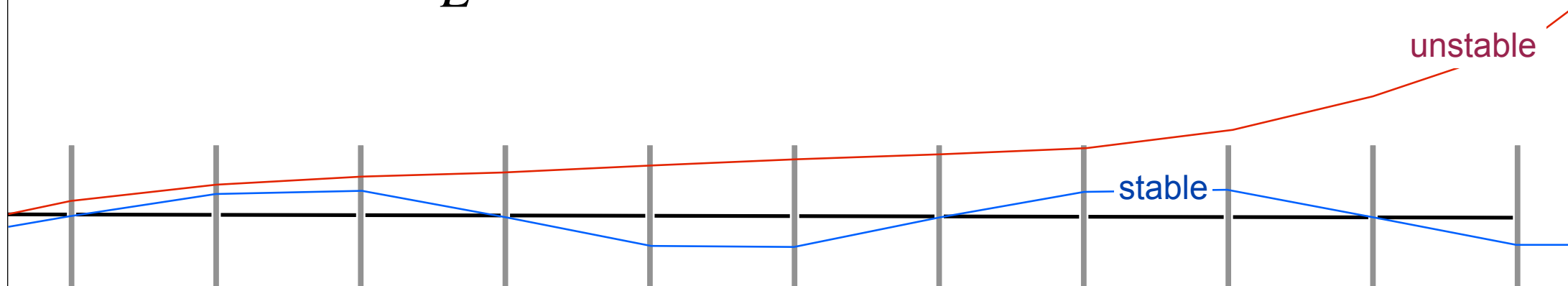
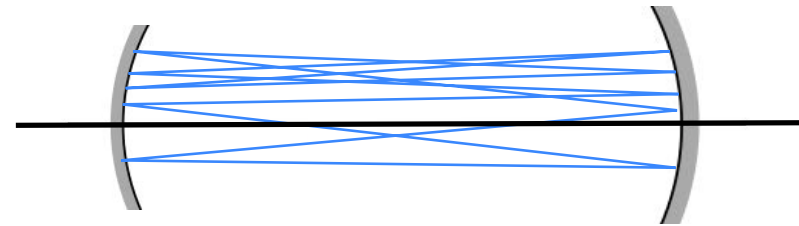
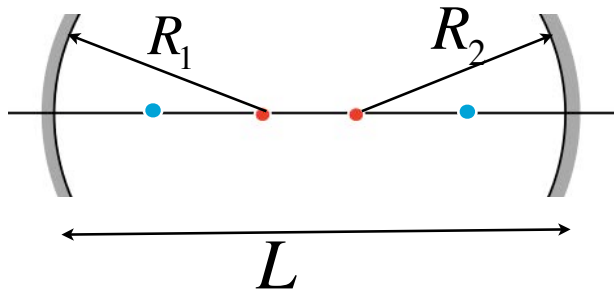




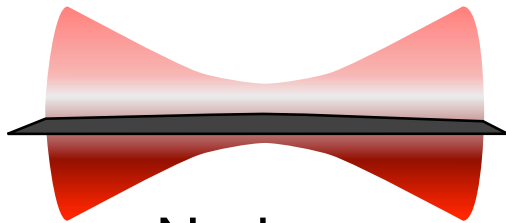
Stable cavities ...

$$0 \leq \left(1 - \frac{L}{R_1}\right) \left(1 - \frac{L}{R_2}\right) \leq 1$$

stability condition

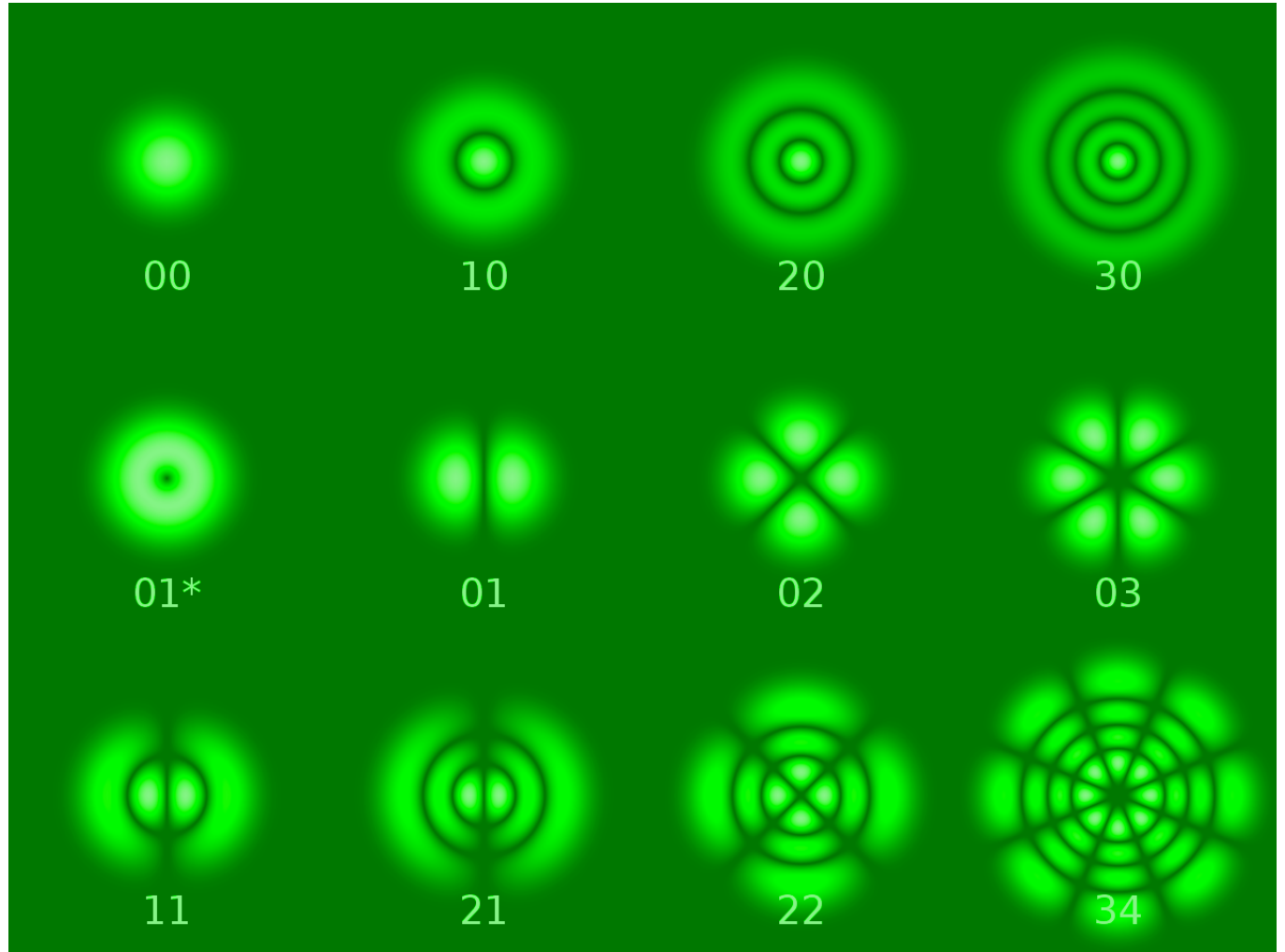


Transverse modes

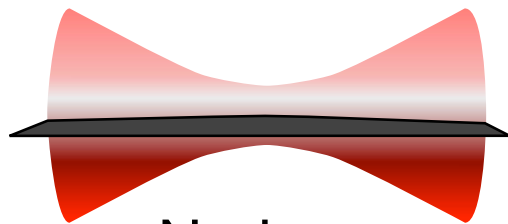


Node

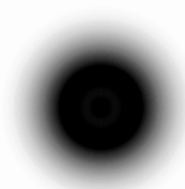
Laguerre-Gauss
modes
for cylindrical
boundary conditions



Transverse modes

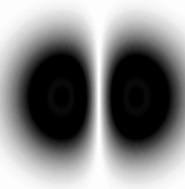


Node

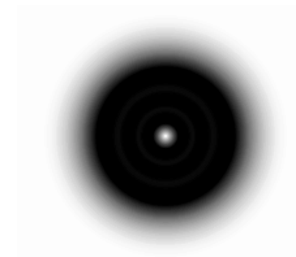
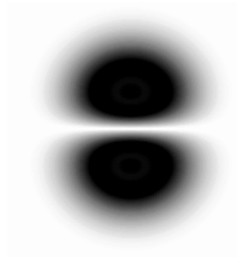


00 mode

00



01



donut mode

Laguerre-Gauss modes
for cylindrical boundary conditions

... all this is scalar,
with vectors, polarization modes



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Pumping

Is the way the active material gets the inversion.

Many kinds of pumping ...

Collisions with electrons, plasmas.

Conventional light ... flash lamp

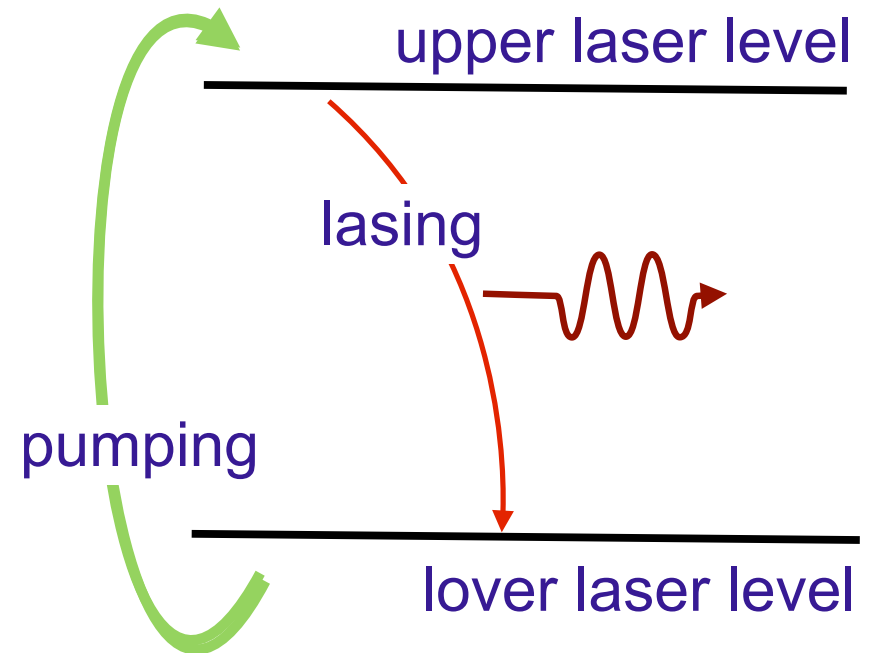
Chemical reactions

Voltage in a semiconductor

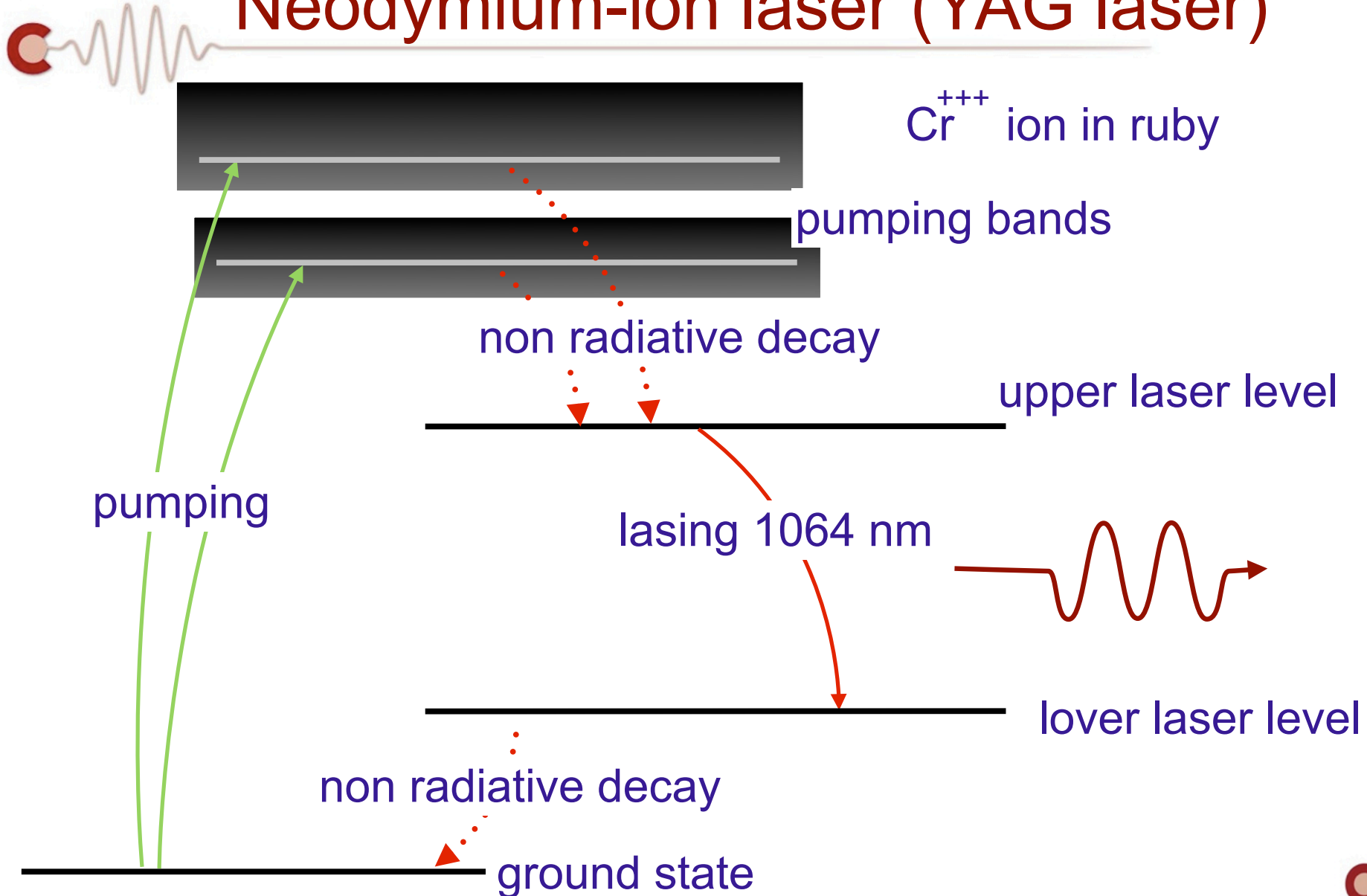
A wiggling relativistic electron

... and many many many more,

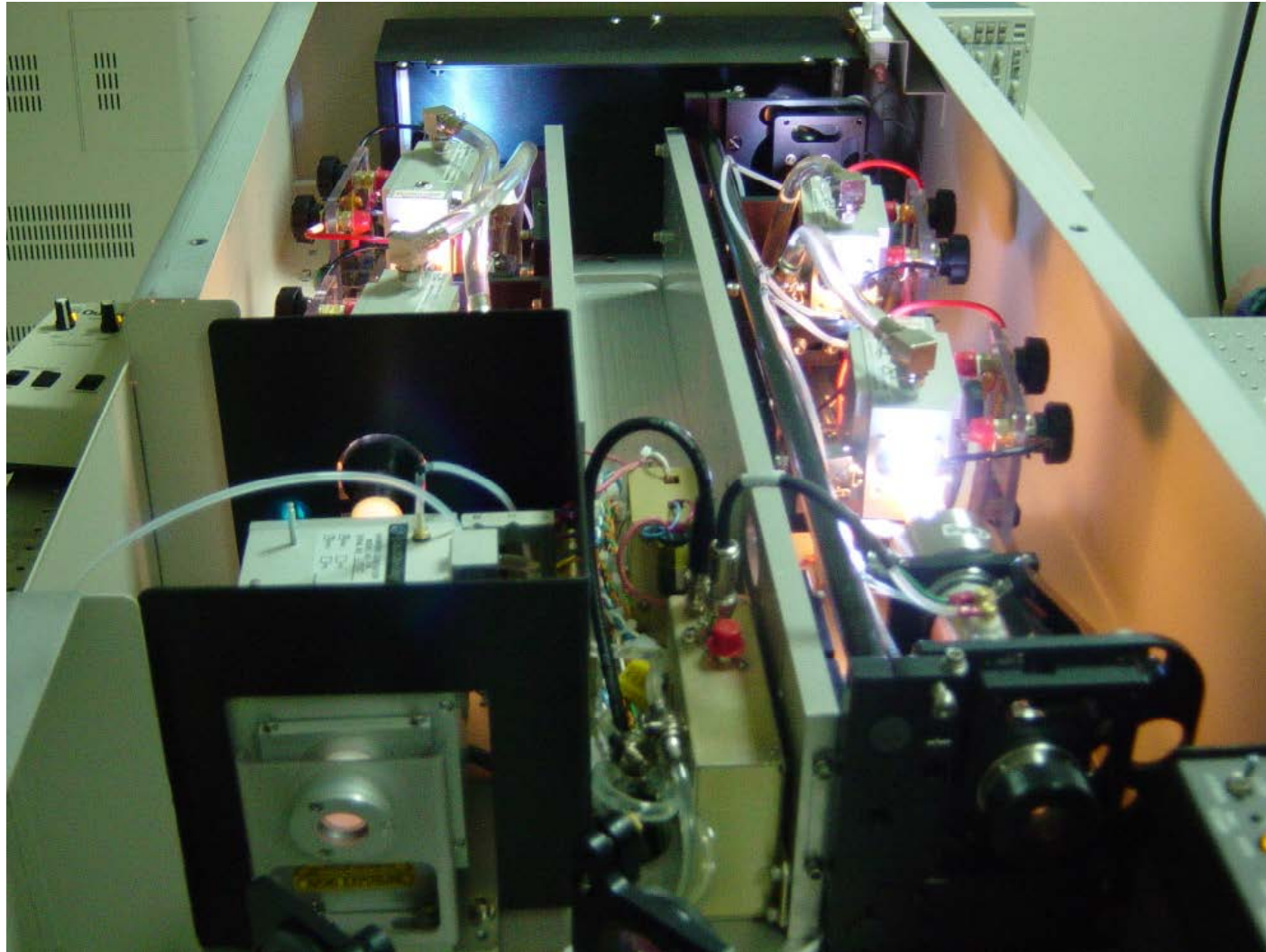
also pumped by another laser



Neodymium-ion laser (YAG laser)

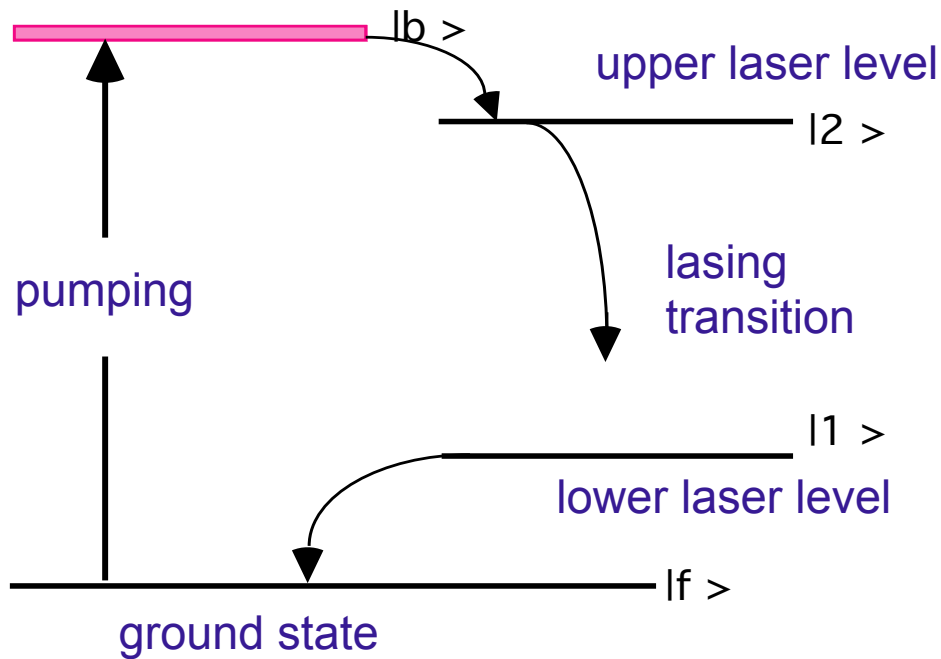


Nd ion laser



Nd:YAG laser
1064 nm

Four-level laser



population inversion

$$P_1 < P_2 \text{ if } \gamma_1 > \gamma_2$$

$$\frac{dP_b}{dt} = -\gamma_b P_b + b P_f$$

$$\frac{dP_2}{dt} = -\gamma_2 P_2 + \gamma_b P_b$$

$$\frac{dP_1}{dt} = -\gamma_1 P_1 + \gamma_2 P_2$$

$$\frac{dP_f}{dt} = -b P_f + \gamma_1 P_1$$

steady state solution

$$0 = -\gamma_b P_b + b P_f$$

$$0 = -\gamma_2 P_2 + \gamma_b P_b$$

$$0 = -\gamma_1 P_1 + \gamma_2 P_2$$

$$0 = -b P_f + \gamma_1 P_1$$



Rate equations model

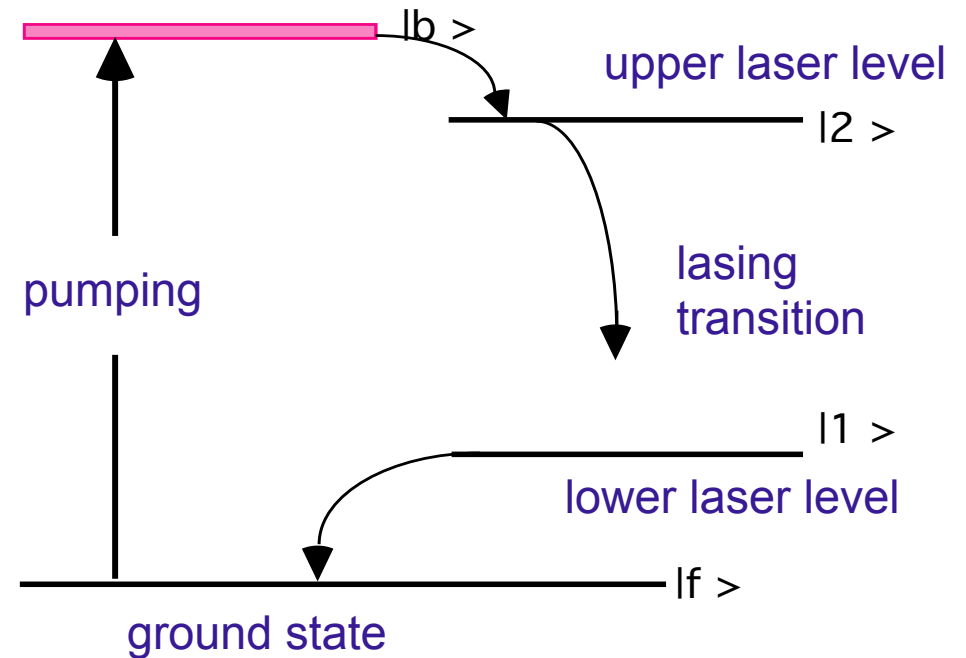
$$\frac{d}{dt} P_b = -\gamma_b P_b + b P_f$$

$$\frac{d}{dt} P_2 = -C(P_2 - P_1) I - \gamma_2 P_2 + \gamma_b P_b$$

$$\frac{d}{dt} P_1 = C(P_2 - P_1) I - \gamma_1 P_1 + \gamma_2 P_2$$

$$\frac{d}{dt} P_f = -b P_f + \gamma_1 P_1$$

$$\frac{d}{dt} I = -\gamma_c I + G(P_2 - P_1) I$$



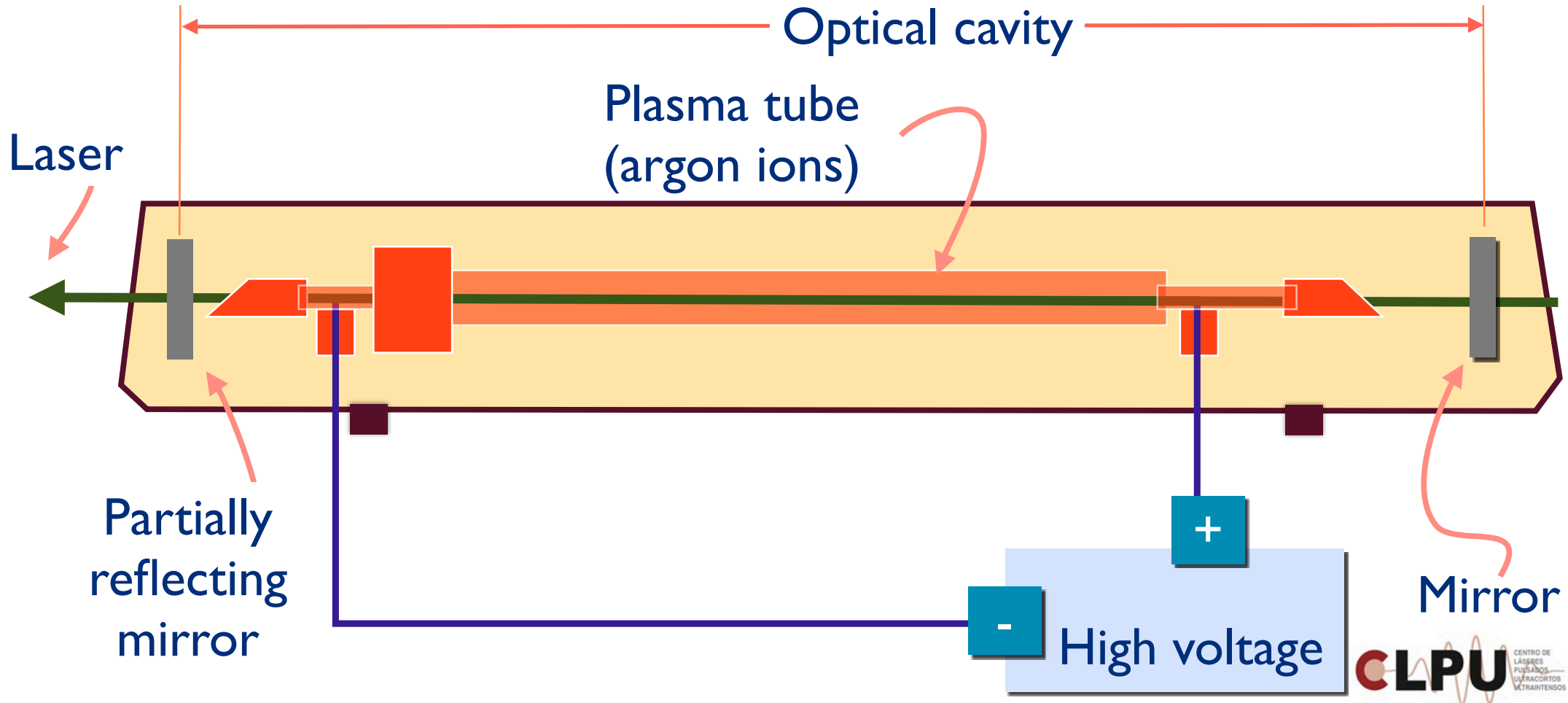
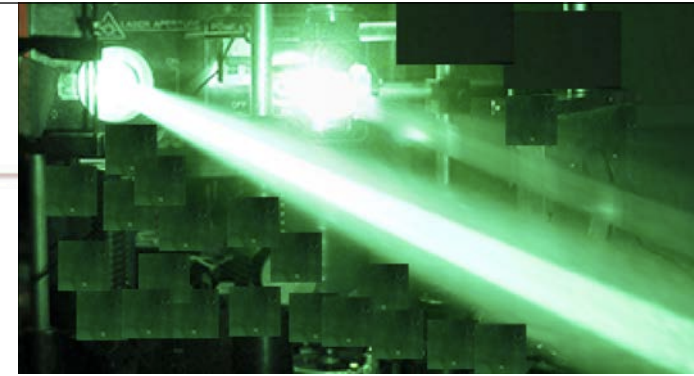
$$G(P_2 - P_1) > \gamma_c$$

threshold for lasing

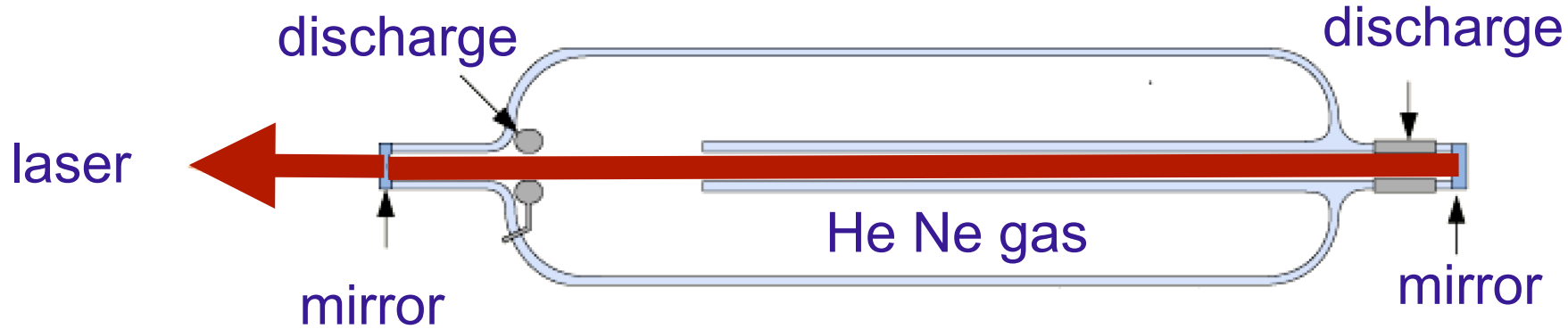
gain loss loss



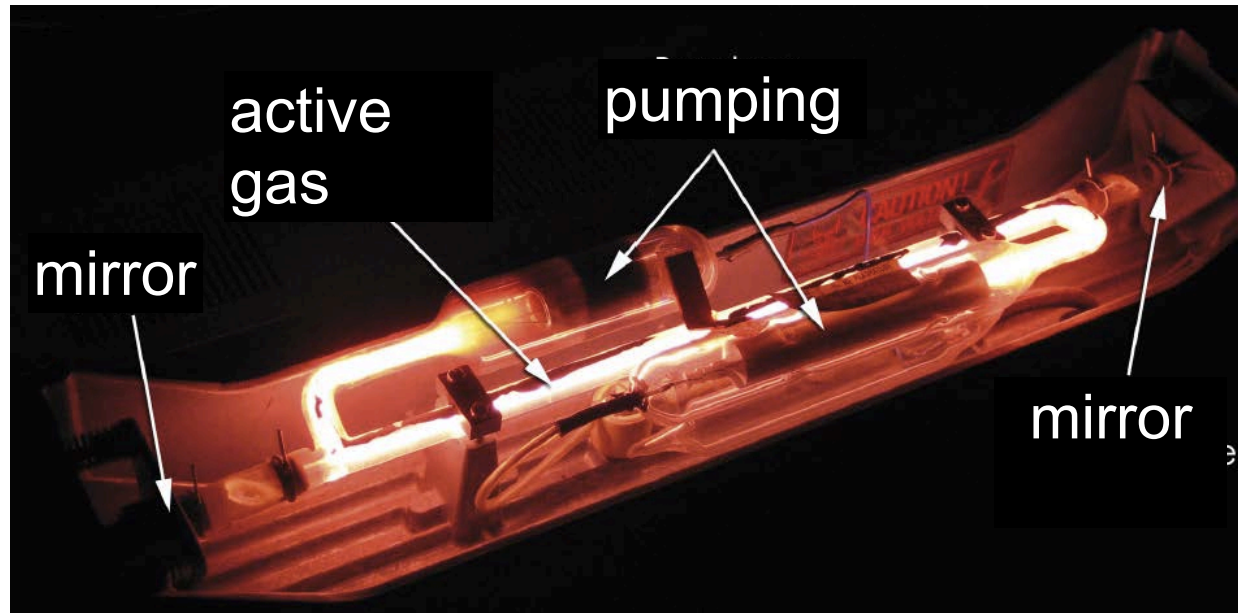
Argon ion laser 514 nm



Helium neon laser 632 nm

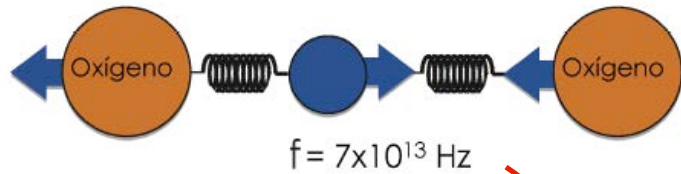


Pumping: electric discharge

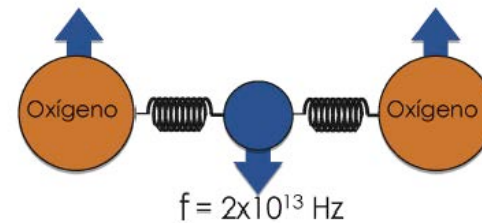
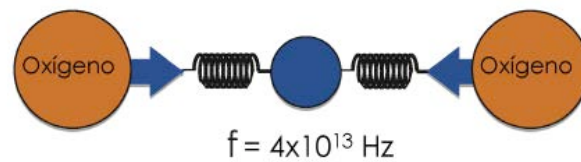


CO2 laser 10.6 microns FIR

Molecular laser vibrations of the CO2 molecule

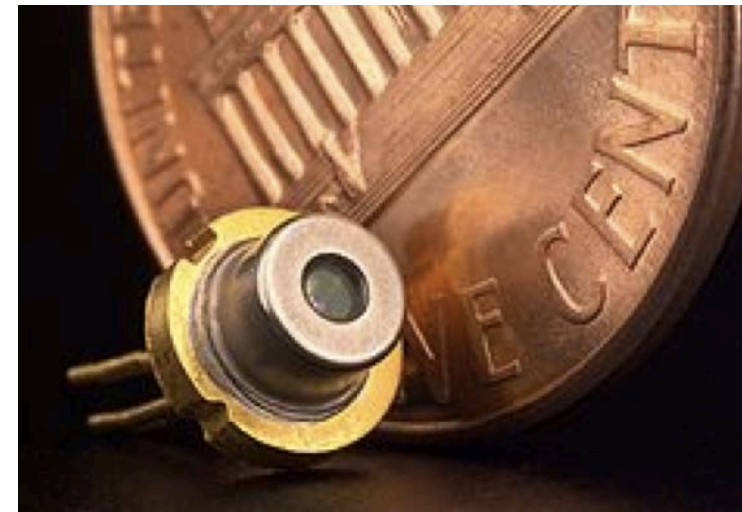
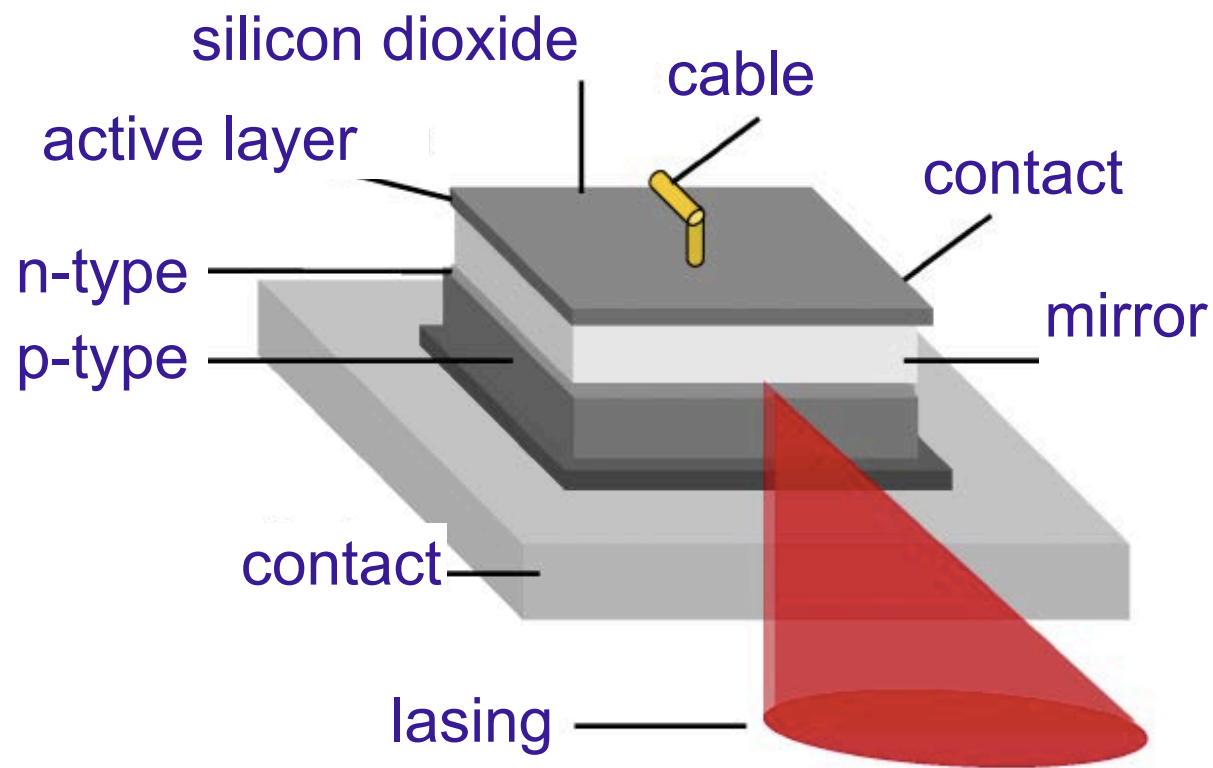


lasing



Semiconductor lasers

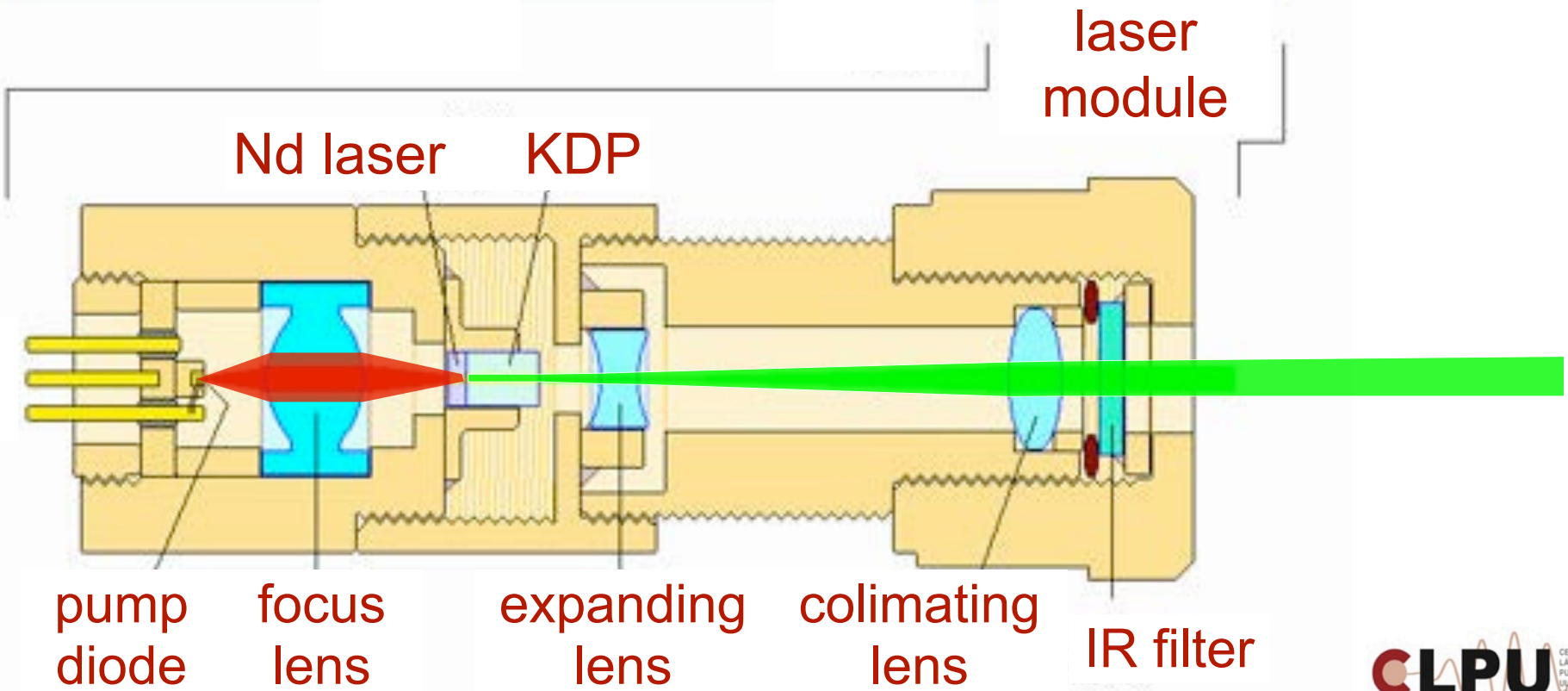
The laser of the XXI Century !!!



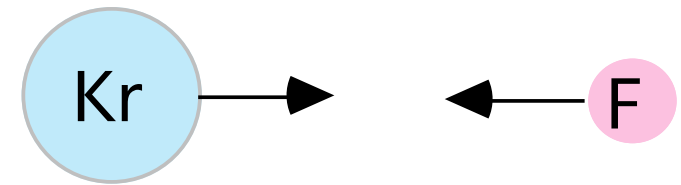
Laser pointer



Text

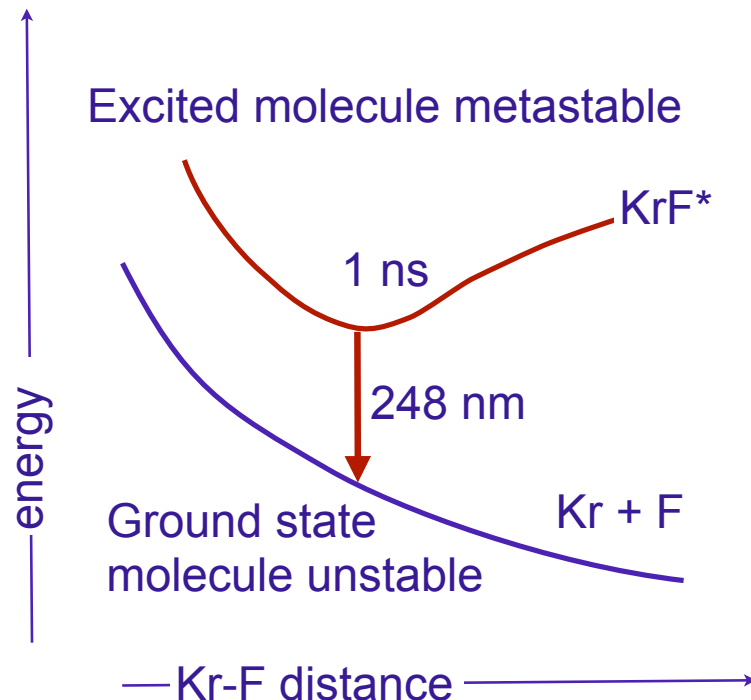


Excimers



Excimer: Excited dimer (two equal atoms) e.g.

Exciplet: Excited molecular complex (different atoms) e.g. KrF

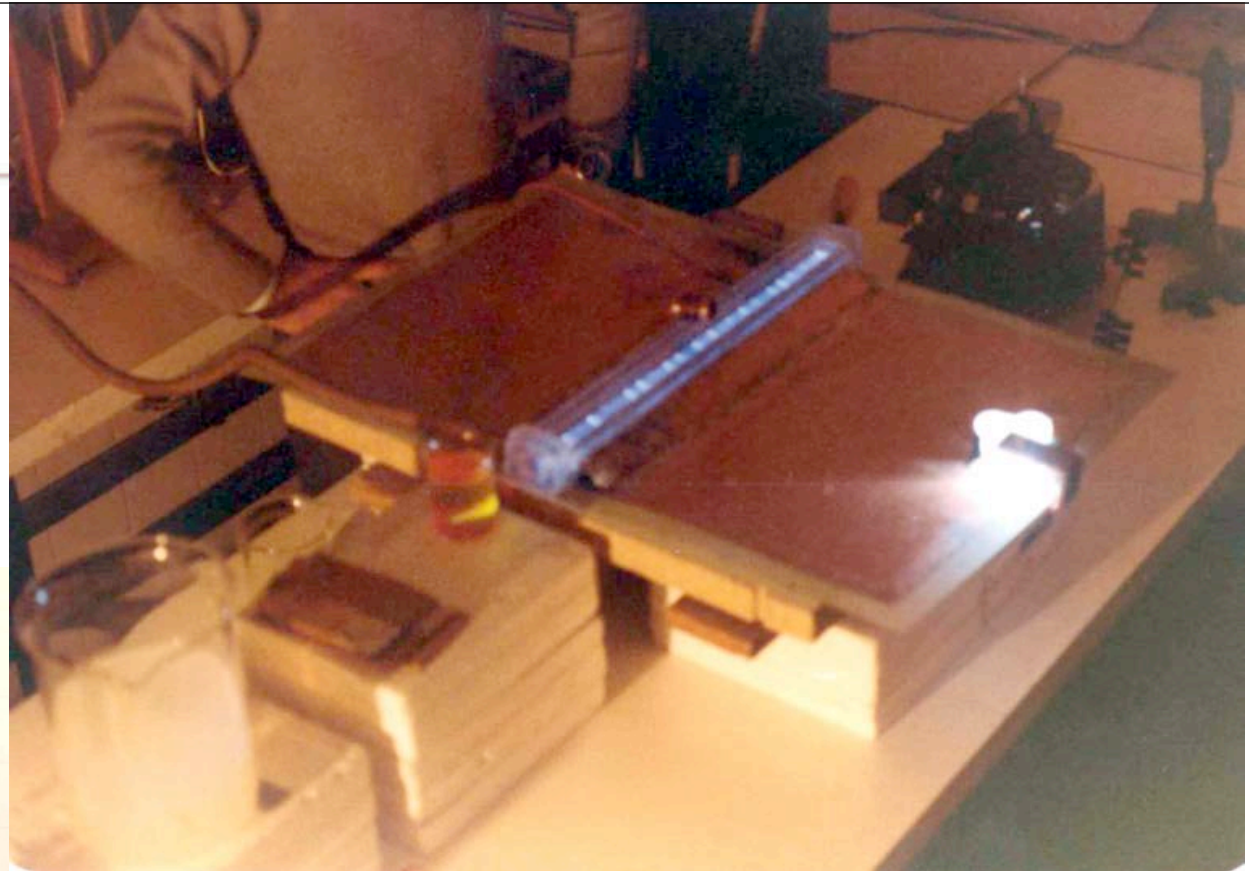


Ar-Ar dimer	126 nm
Kr-Kr dimer	146 nm
Xe-Xe dimer	172 nm
Ar-F molec	193 nm
Kr-F molec	248 nm
Xe-Cl molec	351 nm
Kr-Br molec	206 nm
Ar-Br molec	161 nm
Ne-F molec	108 nm



Air laser !!!

Home made air laser
N₂ laser
near UV 337 nm



Barcelona 1980
Ramon Vilaseca

All you need is
two cooper plates
(capacitor)
a high voltage source

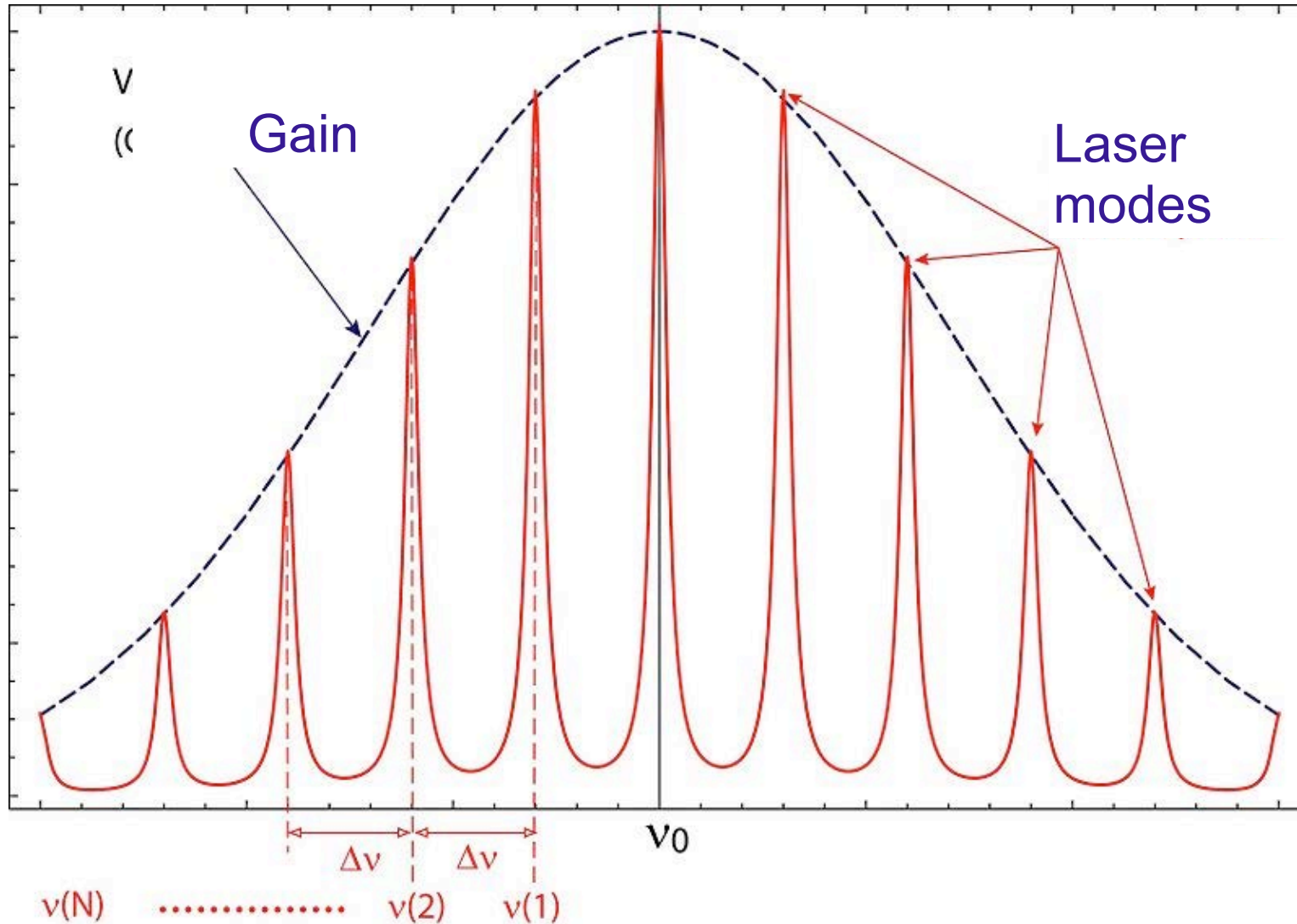


Introduction to Lasers I

- Laser fundamentals
- Optical resonators
- Gaussian Beams
- Laser Pumping
- **Multimode lasing**

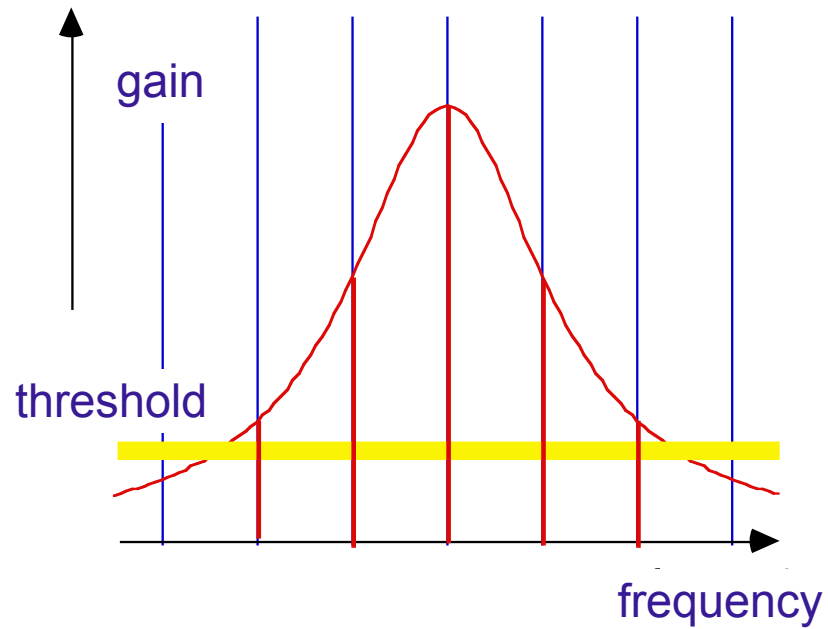


Longitudinal modes



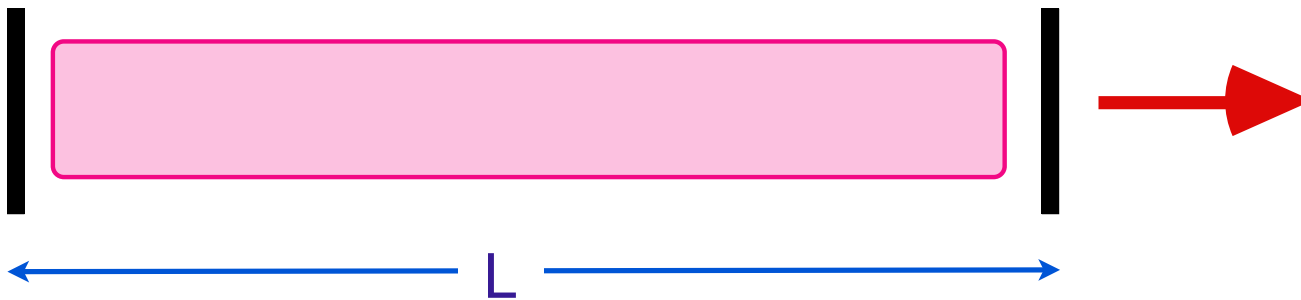


Multimode laser



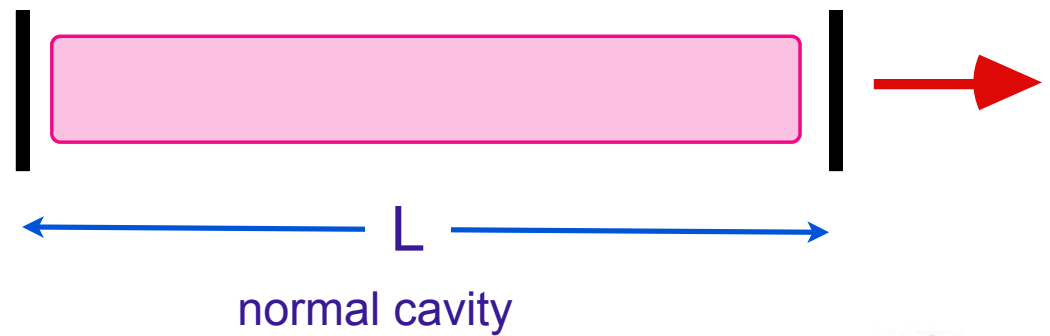
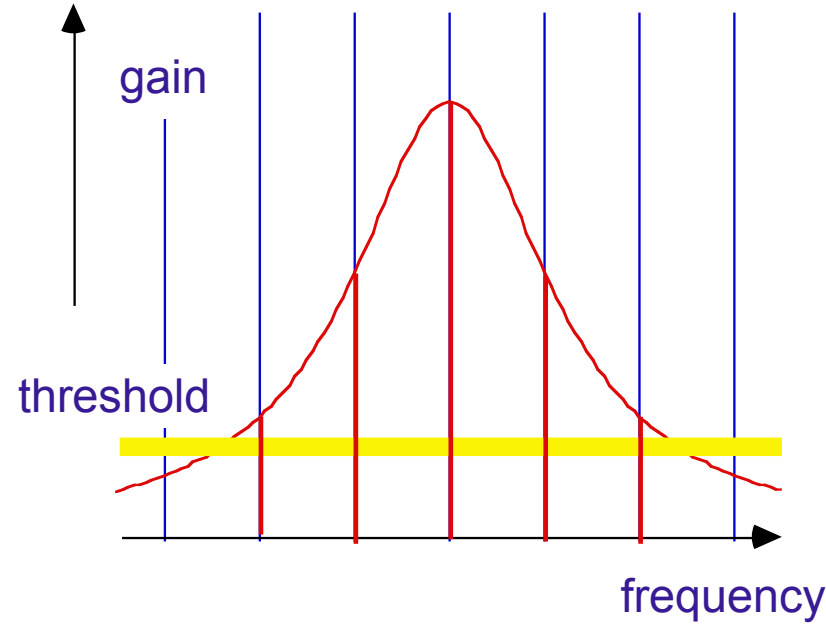
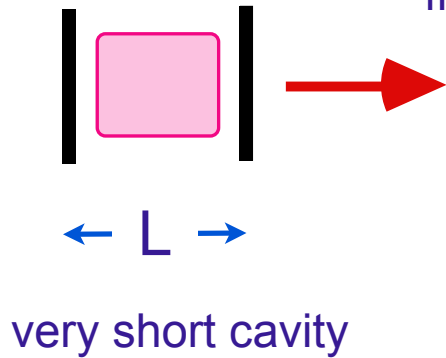
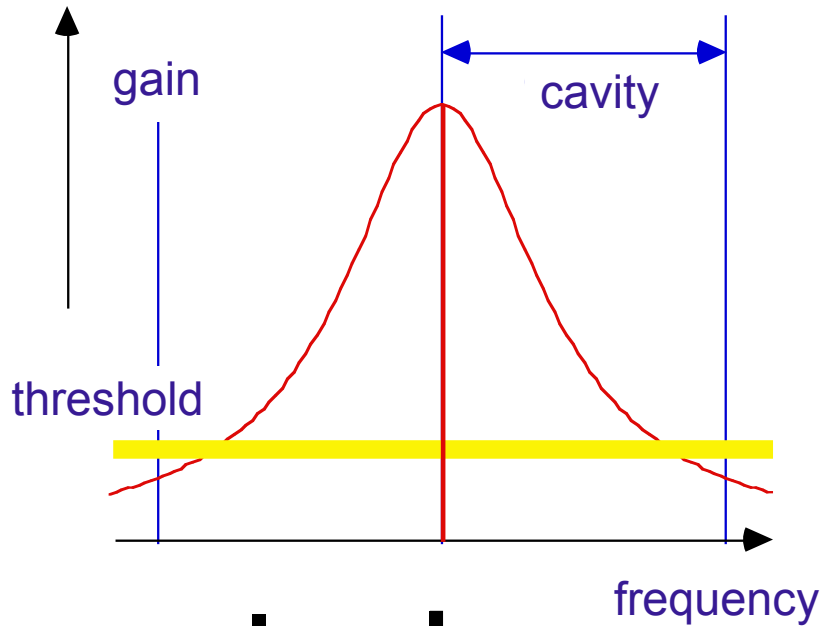
Consecutive frequencies

$$\Delta\omega = \omega_{n+1} - \omega_n = \frac{\pi c}{L}$$

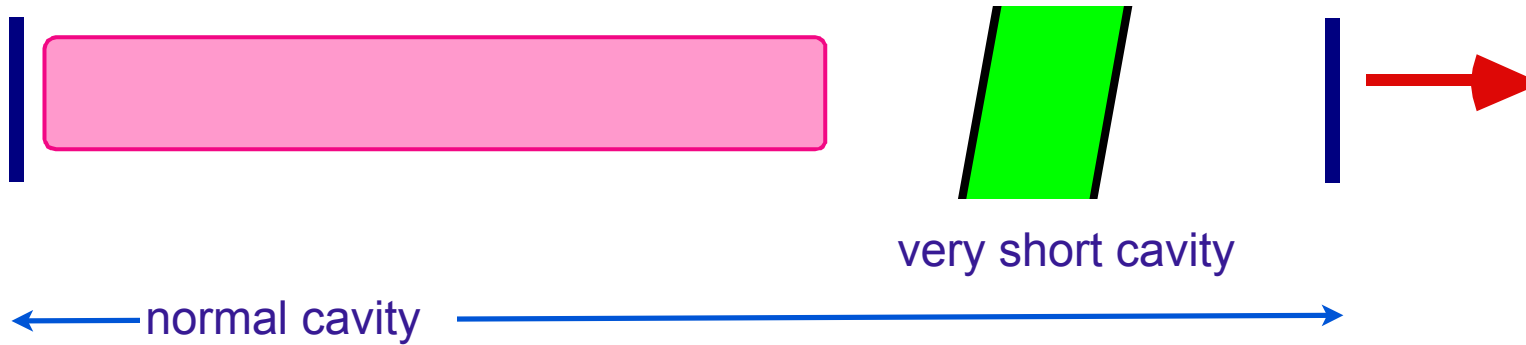
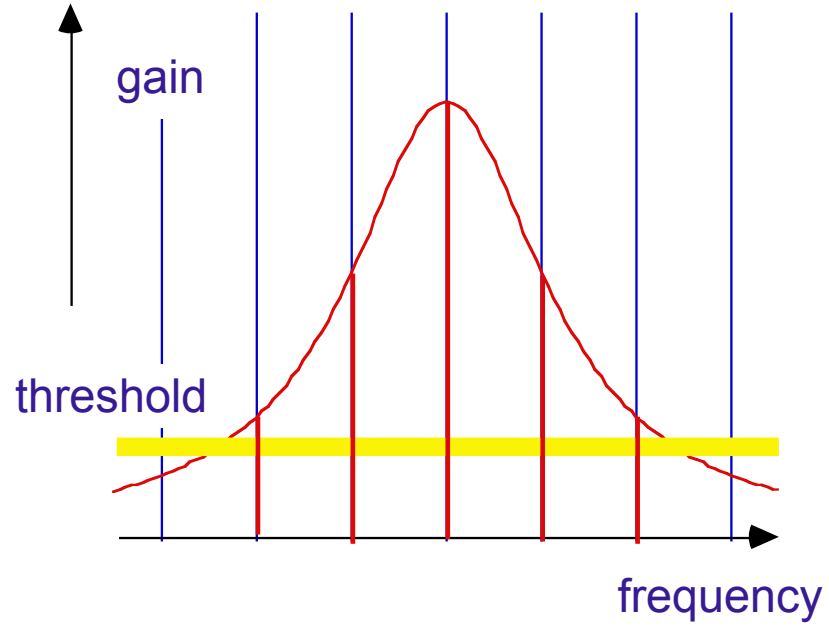
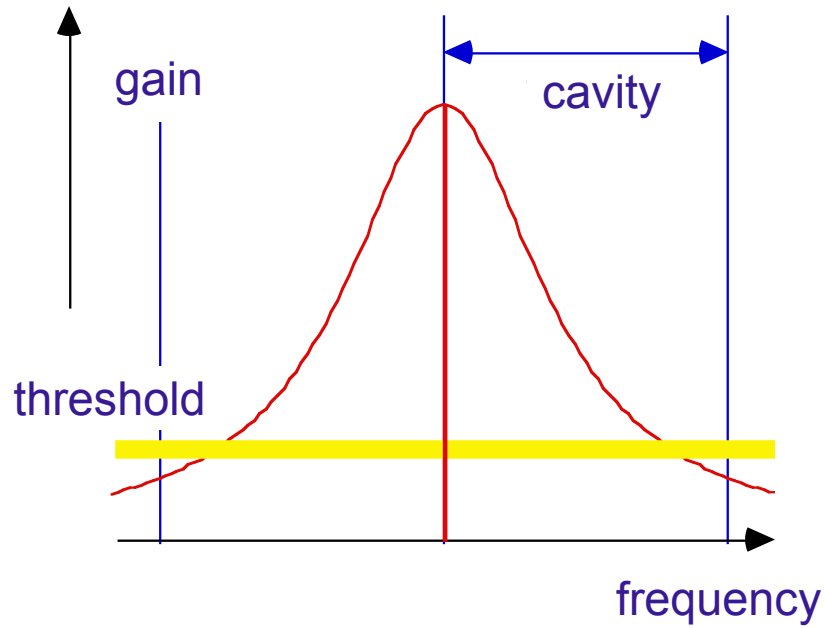




Monomode laser

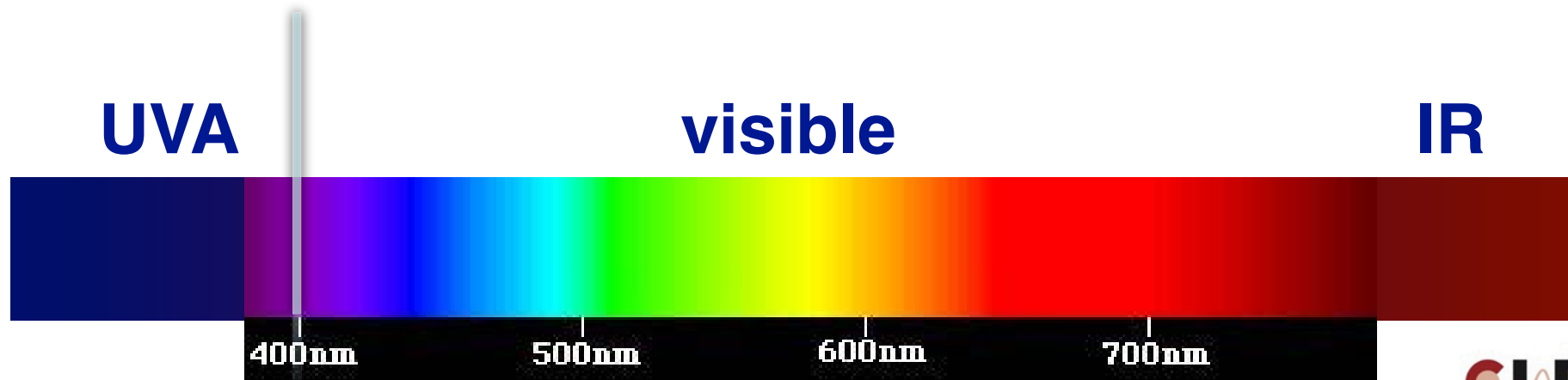


Etalon



Broad band lasers

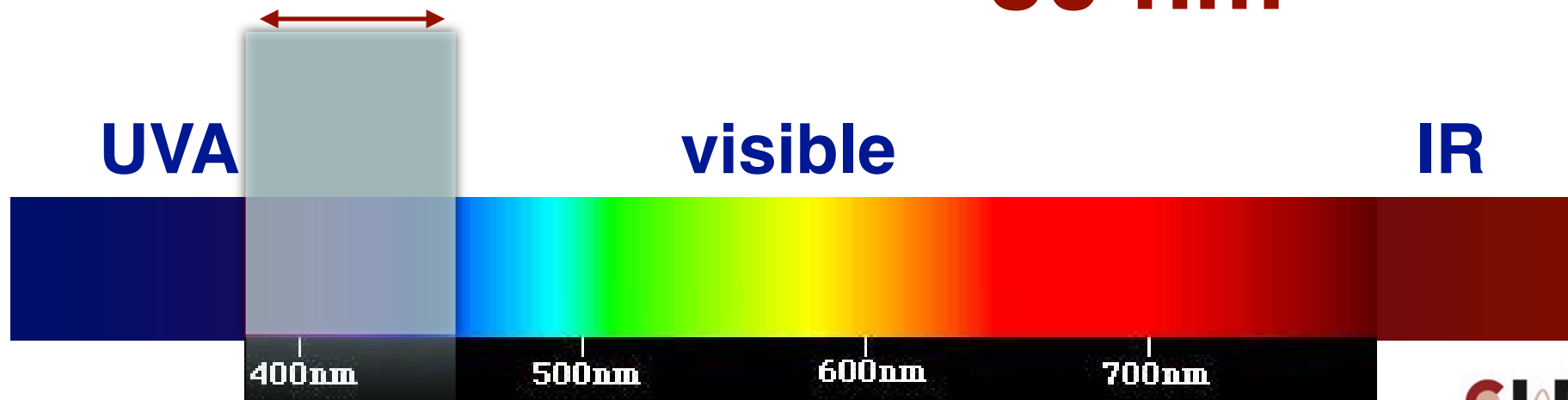
**long pulse ... quasi
monochromatic**



Broad band lasers

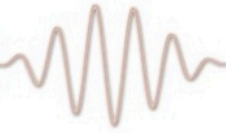
short pulse ... broadband

30 fs
30 nm



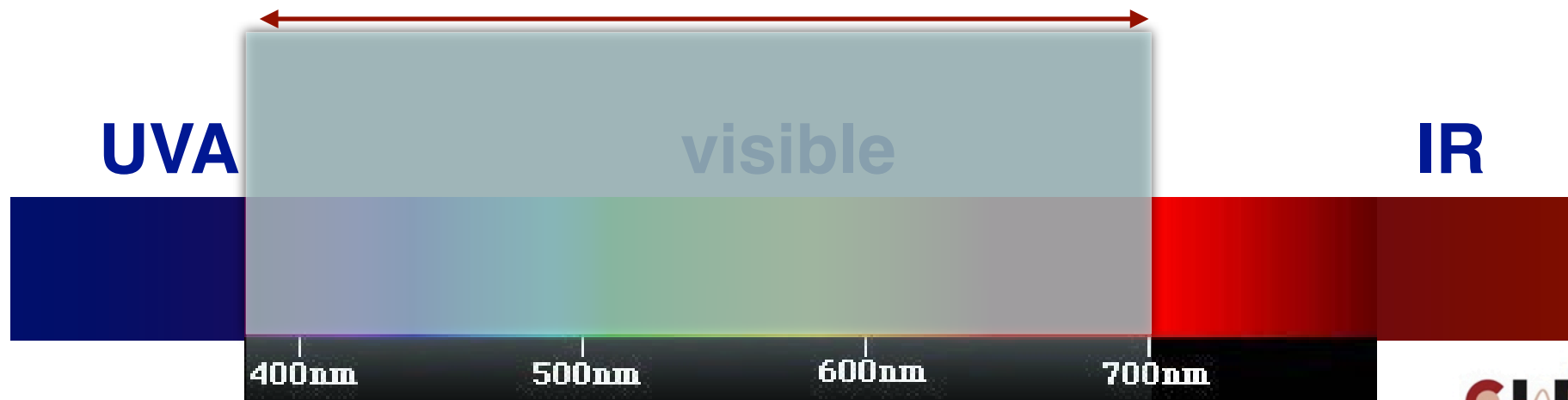


Broad band lasers



**ultra short pulse ... very
broad band**

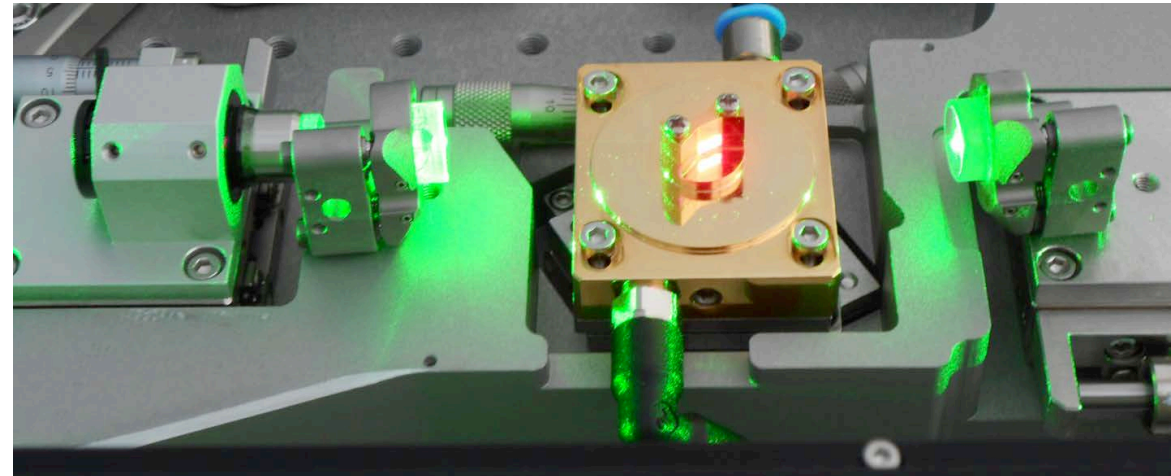
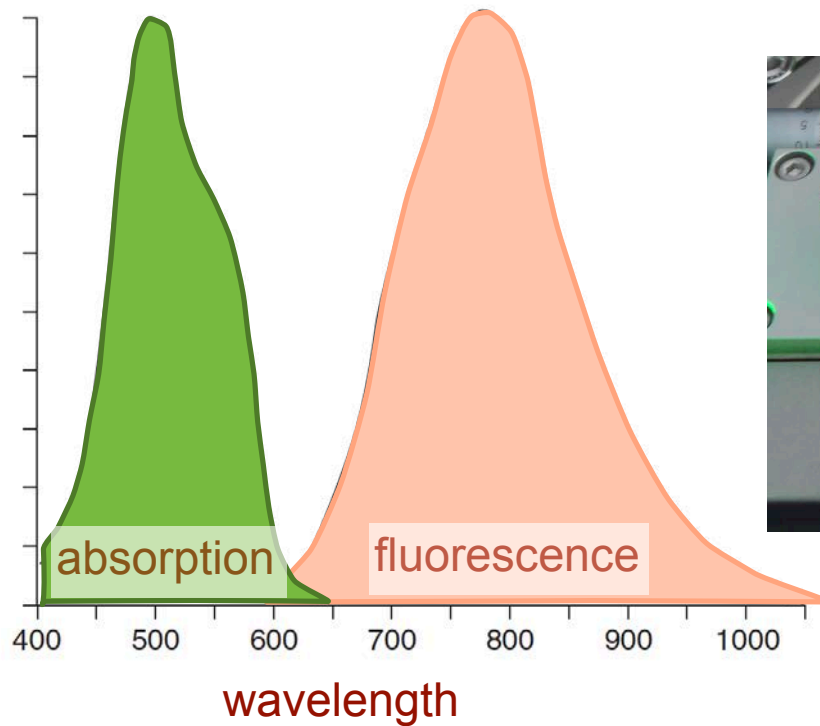
**few fs
all visible**



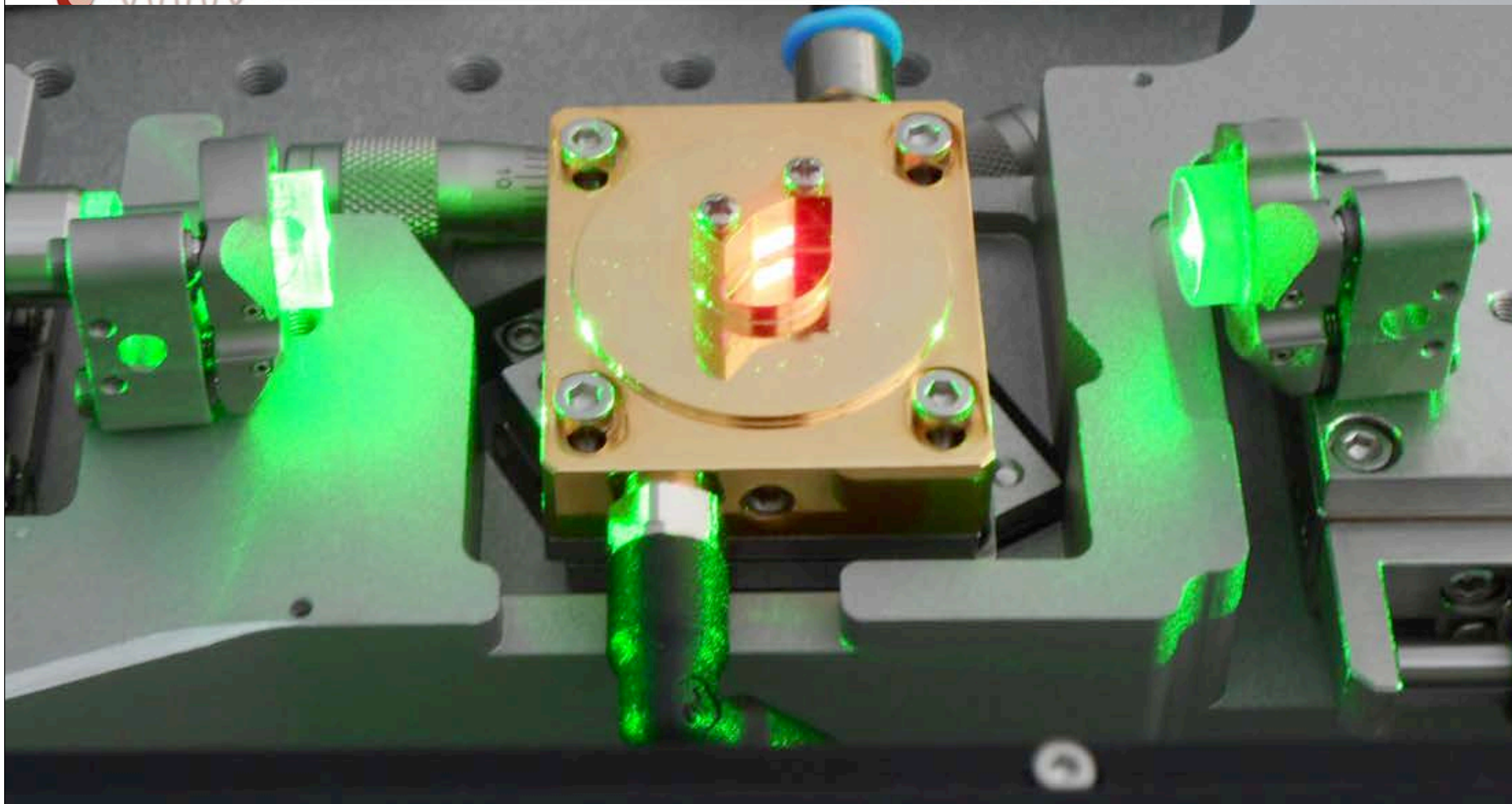


Ti:sapphire laser

short pulses \longleftrightarrow broad band



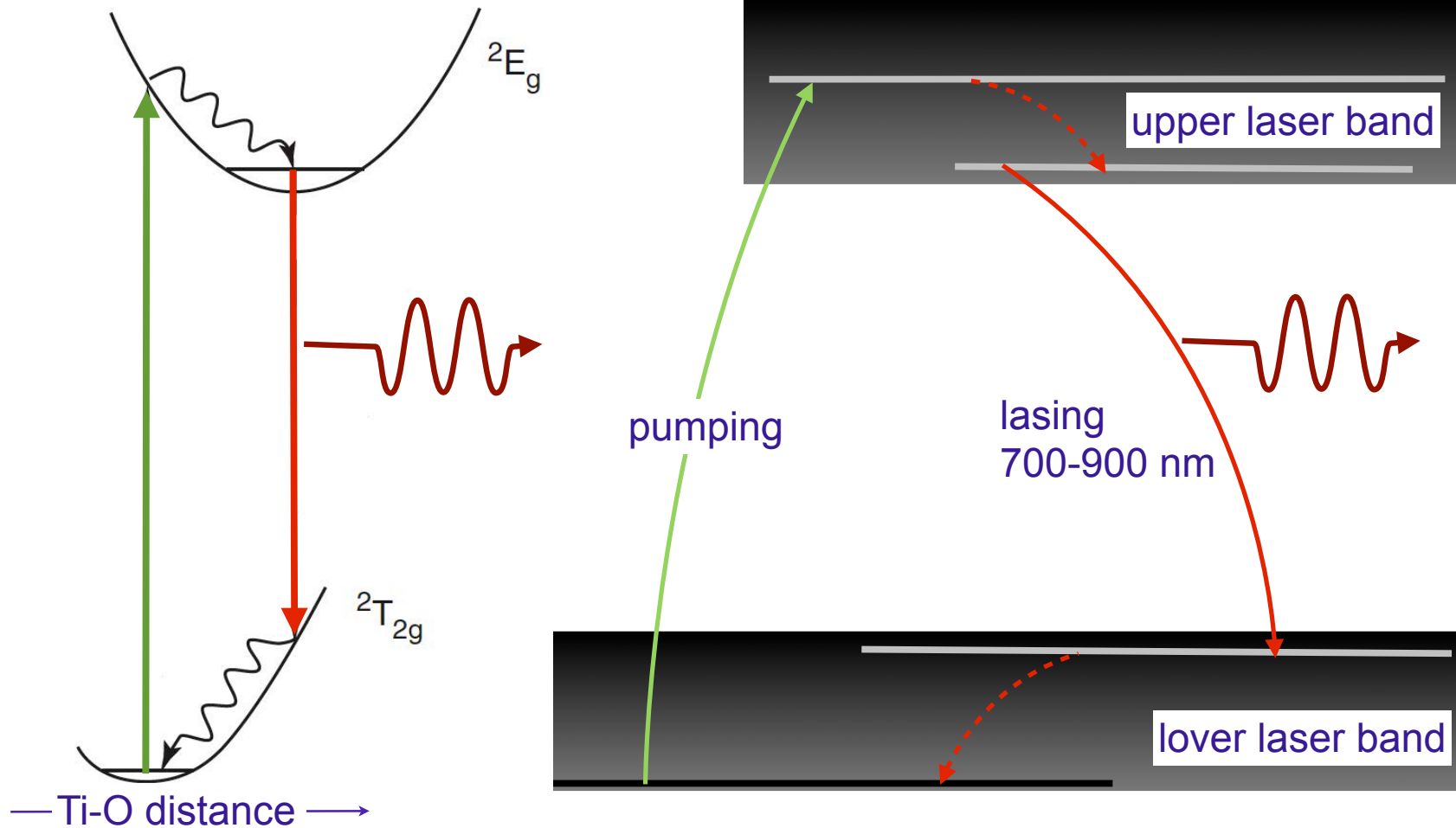
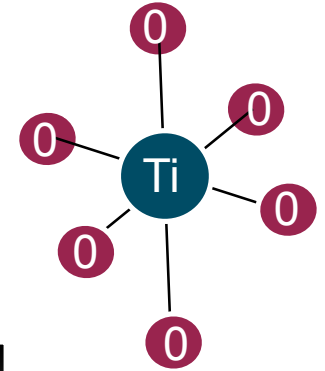
Ti:sapphire laser



Vibronic laser, Ti:sapphire



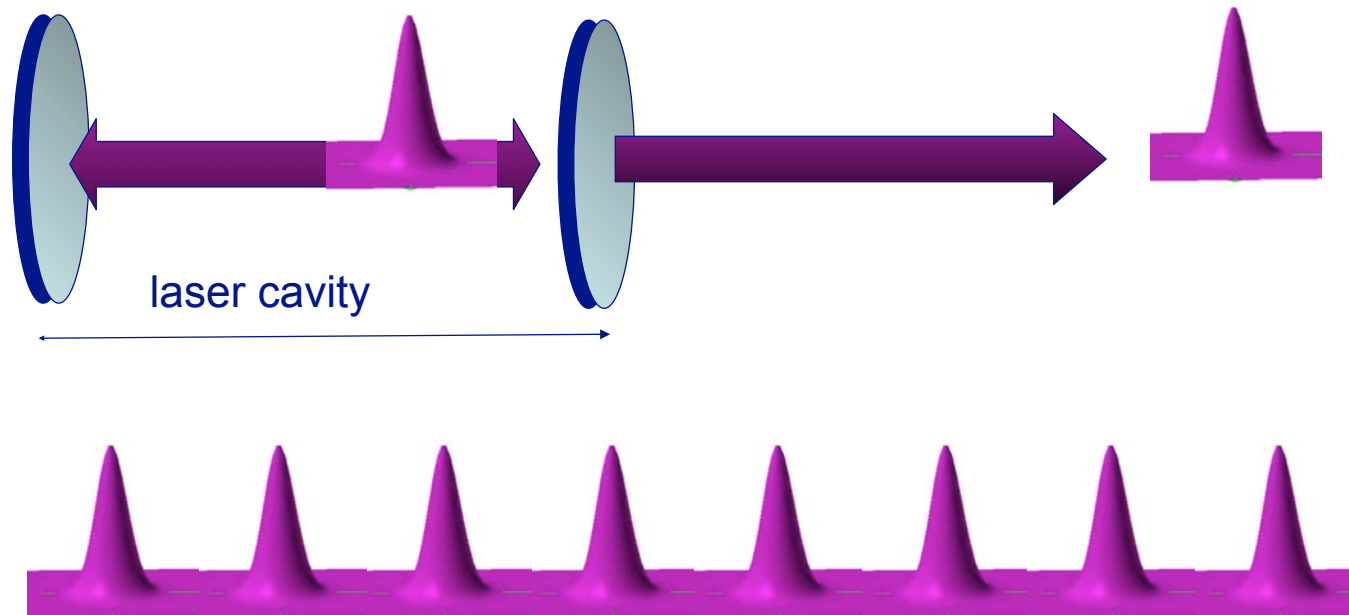
Ti⁺⁺⁺ ion in sapphire



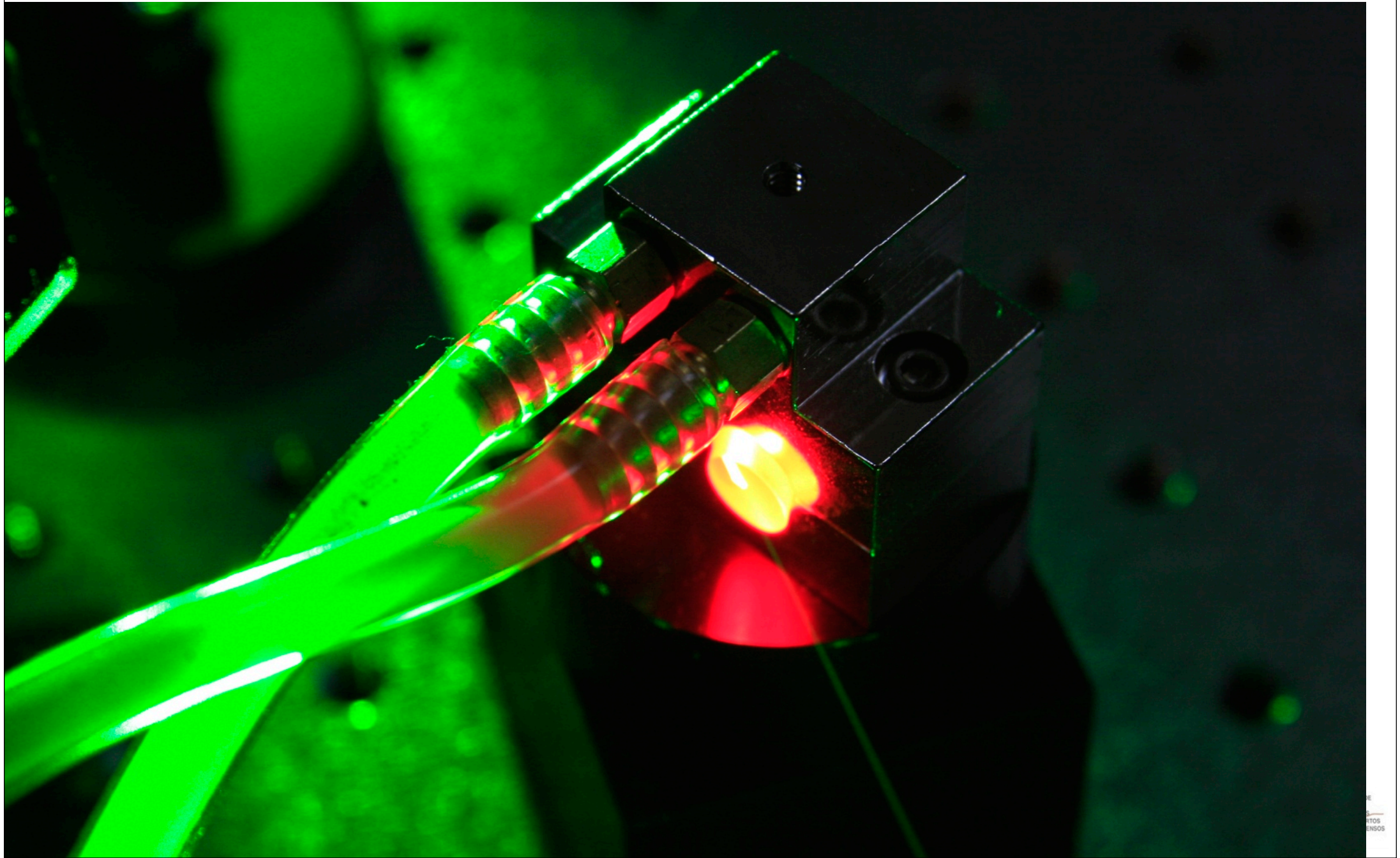


Mode-locking lasers

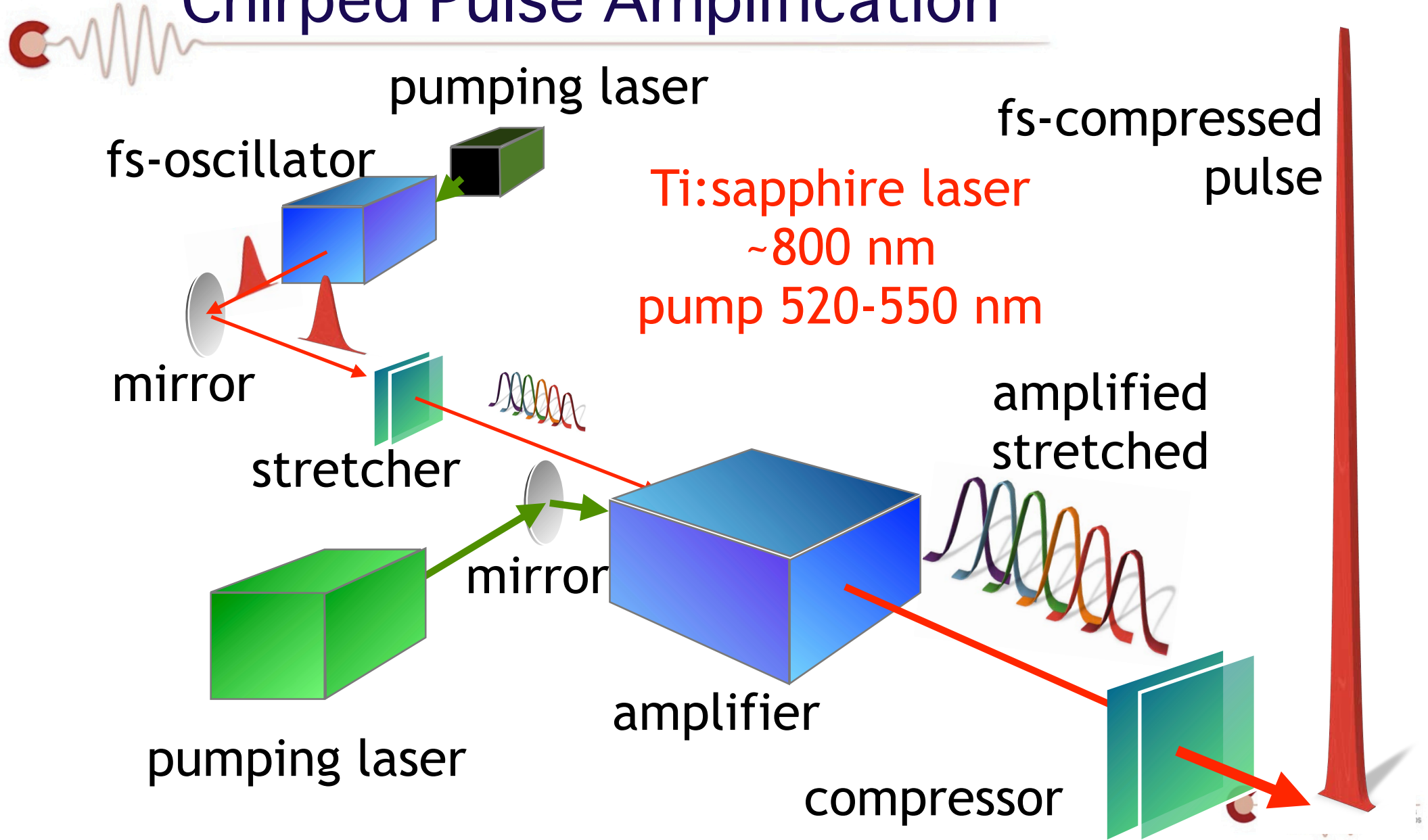
A pulse is generated each round trip of



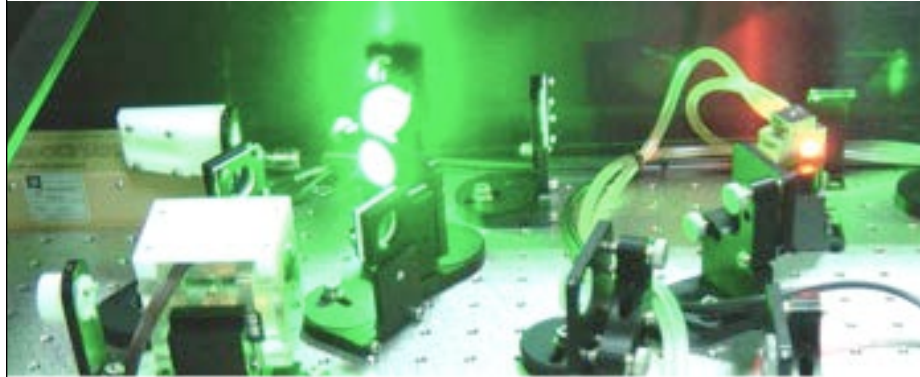
- Ultrashort pulses imply many many modes in phase: for example,
- one picoseg implies a 1 nm bandwidth
 - 10 femtosecons imply 100 nanómetros (almost all the visible)



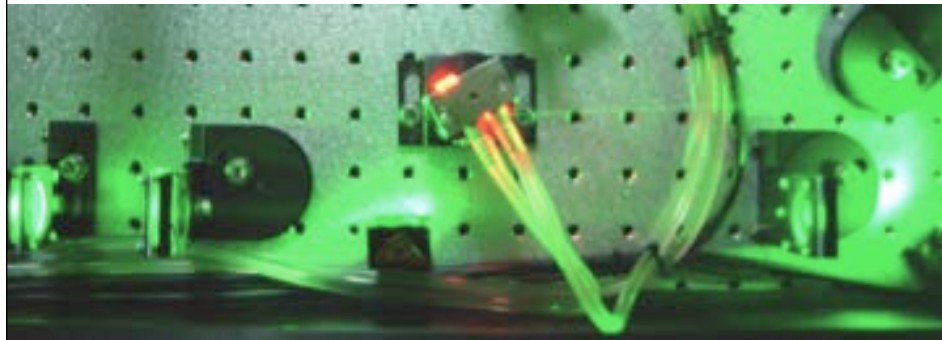
Chirped Pulse Amplification



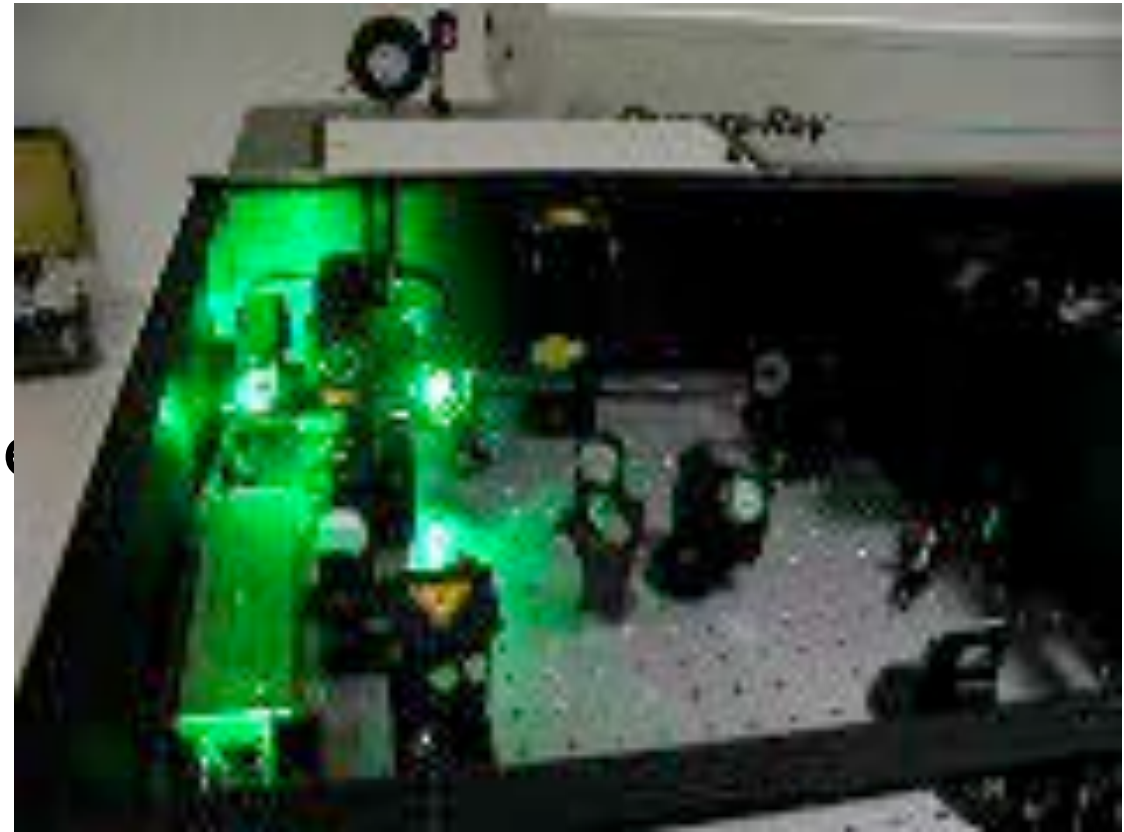
Titanium:Sapphire amplifier



Regenerative amplifier (side view)



Regenerative amplifier (top view)



Ti:Sapphire
amplifiers allow today

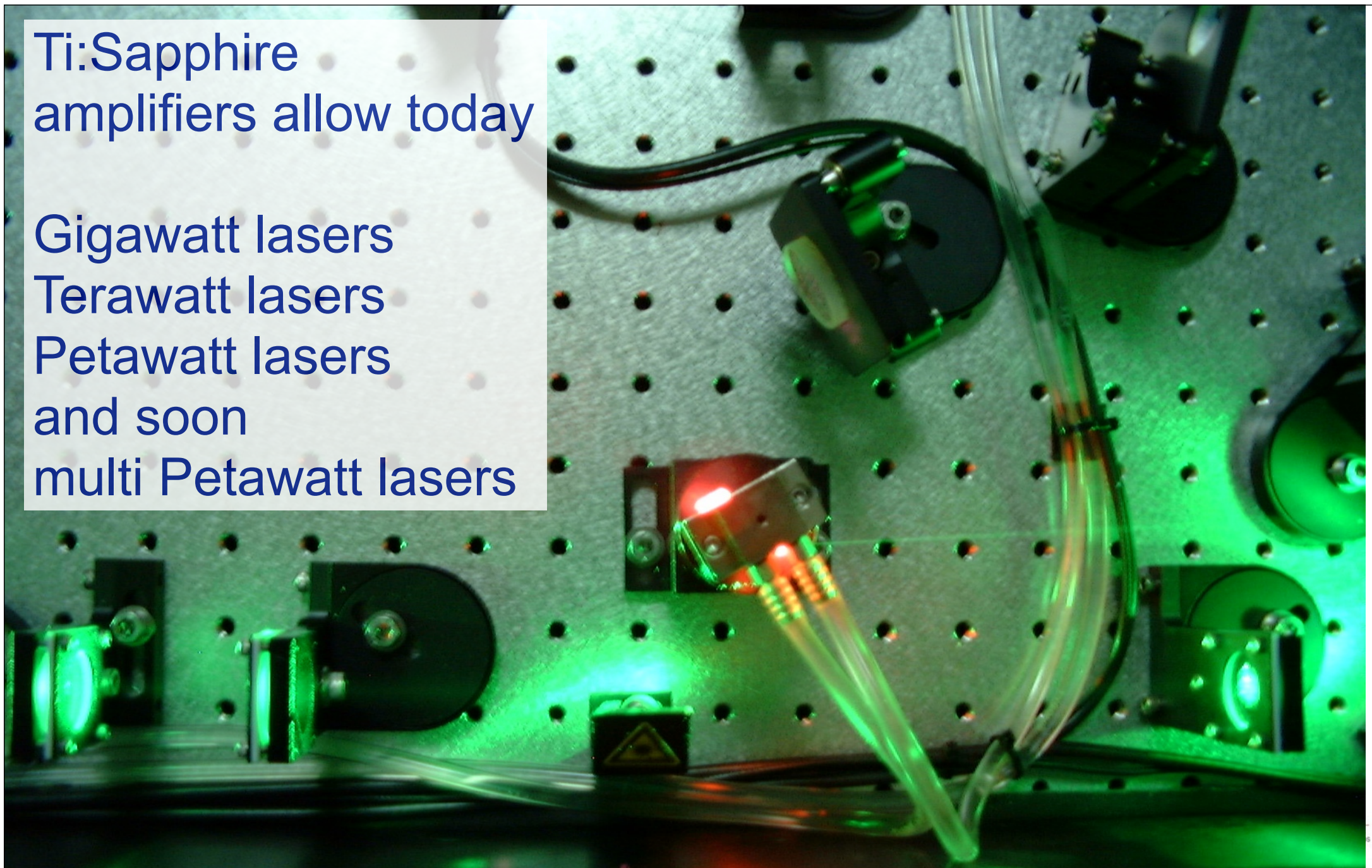
Gigawatt lasers

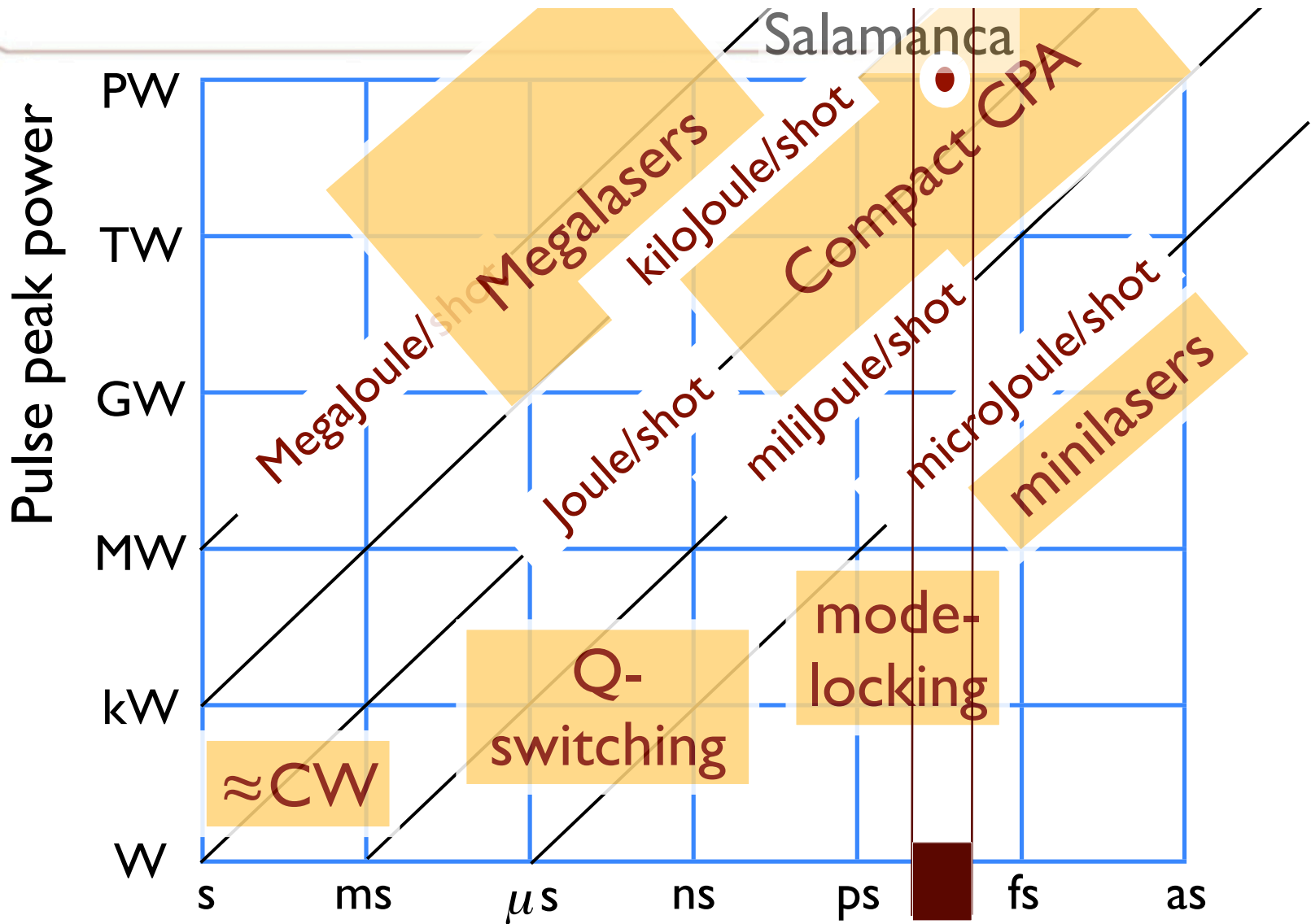
Terawatt lasers

Petawatt lasers

and soon

multi Petawatt lasers





Other schemes for laser light ...

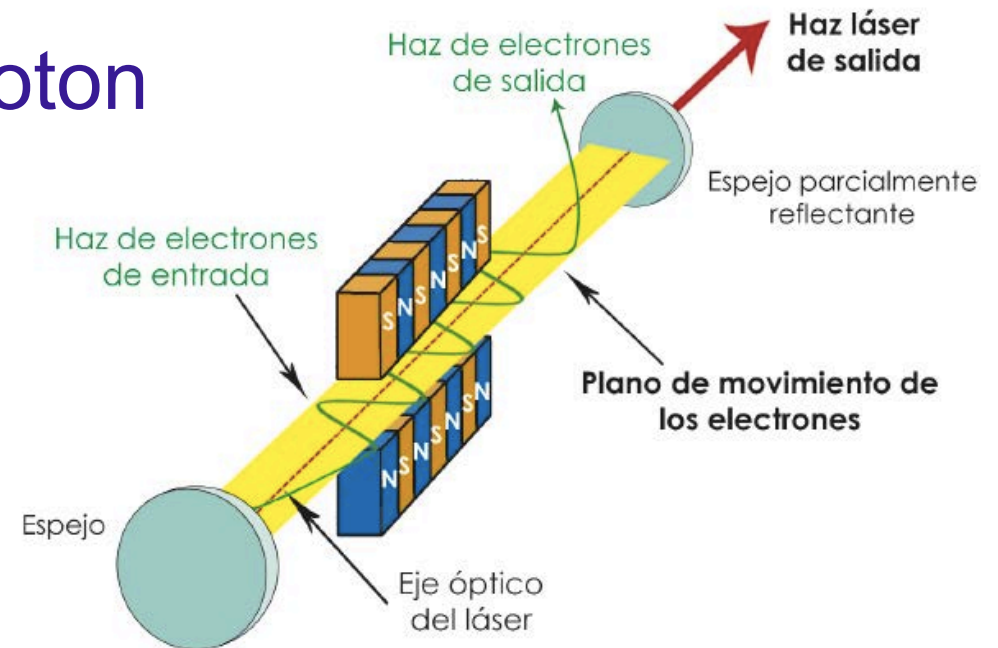
Inversion-less lasers

Quantum lasers ... single photon

X-ray lasers

Nuclear lasers

Free electron lasers



Natural lasers (astrophysical lasers)



Introduction to Lasers I

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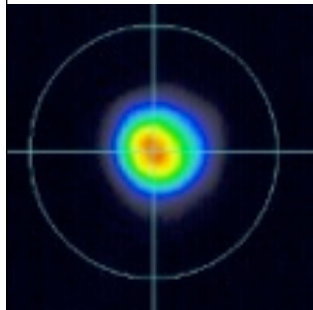
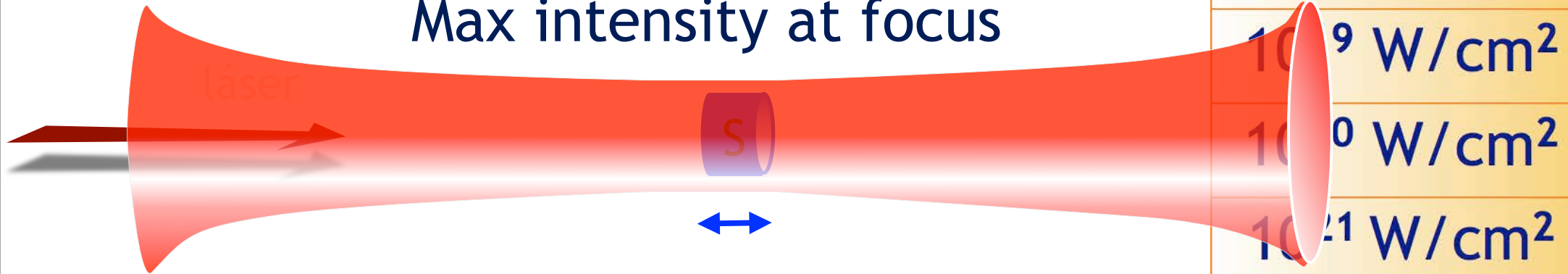
- Final considerations

Intensity is the key parameter



$$Intensity = \frac{power}{surface}$$

Max intensity at focus



Today's world record



10^{15} W/cm²

10^{16} W/cm²

10^{17} W/cm²

10^{18} W/cm²

10^{19} W/cm²

10^{20} W/cm²

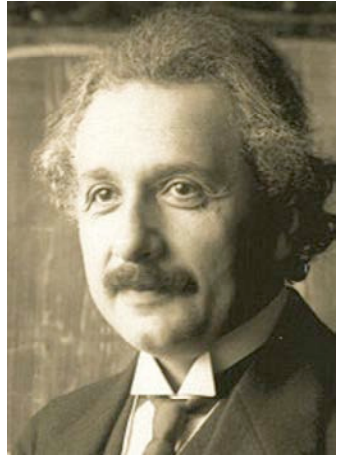
10^{21} W/cm²

10^{22} W/cm²

10^{23} W/cm²

10^{24} W/cm²

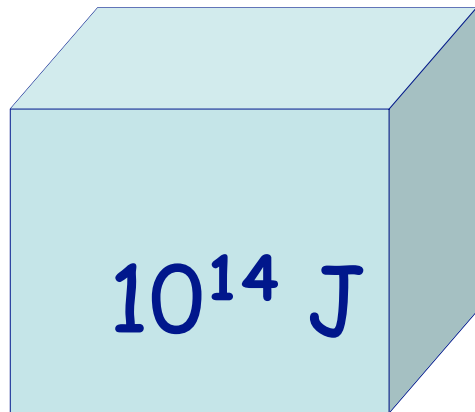
Energy and mass



$$E=mc^2$$

$$E=8.9876 \cdot 10^{16} \text{ J/kg}$$

water density 1 gram/cm³

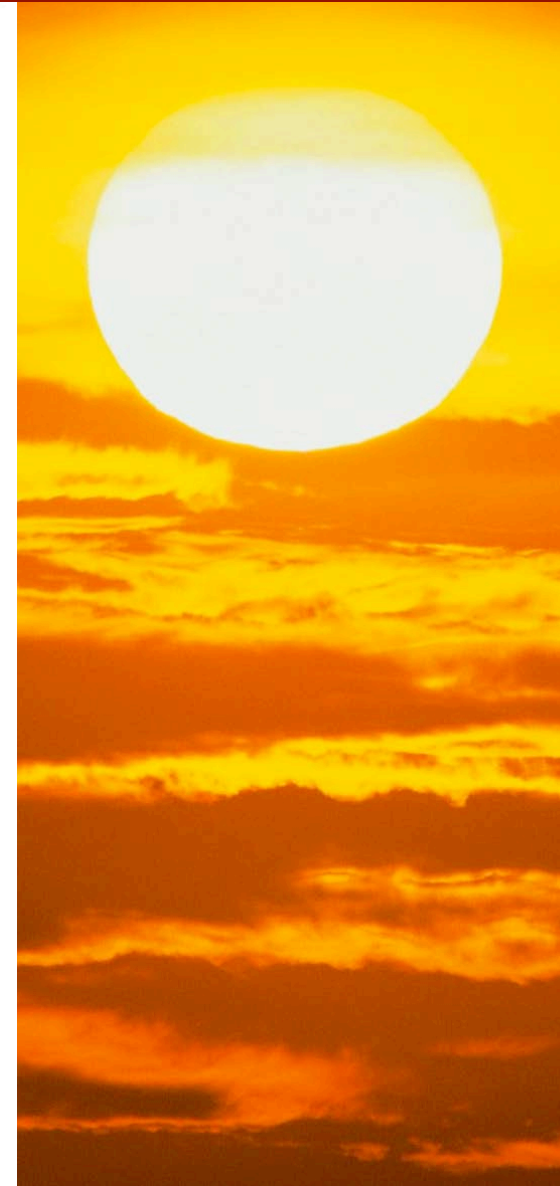


1 cm

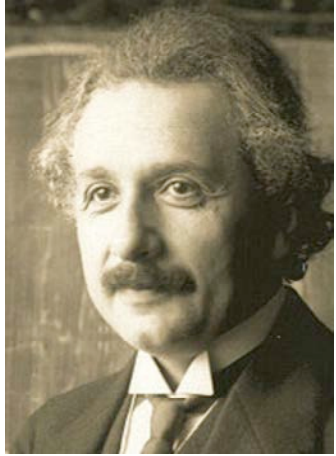
100 Joule



1 micron



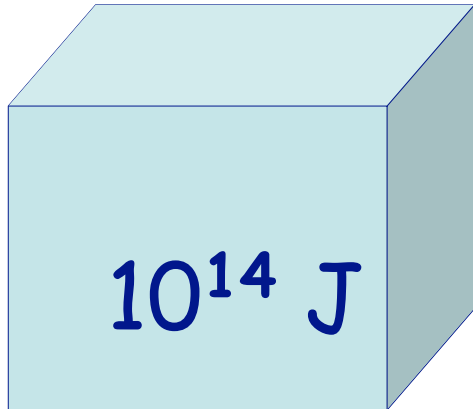
Energy and mass



$$E = mc^2$$

$$I = \rho c^3$$

water density 1 gram/cm³



1 cm

100 Joule



1 micron



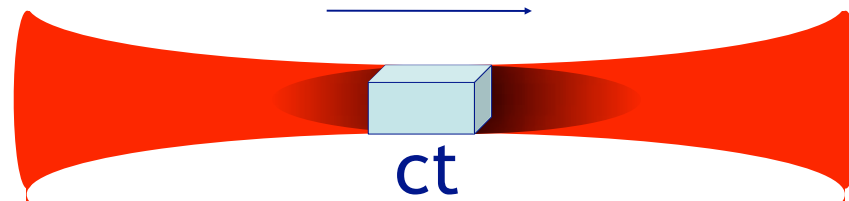
Intensity



$$E=mc^2$$

Air ... 1 mgr/cm³

$$E/V = 90 \text{ mJ}/\mu\text{m}^3 \\ = 2.7 \cdot 10^{21} \text{ W}/\text{cm}^2$$



$$E/V = 90 \text{ J}/\mu\text{m}^3 \\ 2.7 \cdot 10^{24} \text{ W}/\text{cm}^2$$

Water ... 1 gr/cm³



Energy concentration

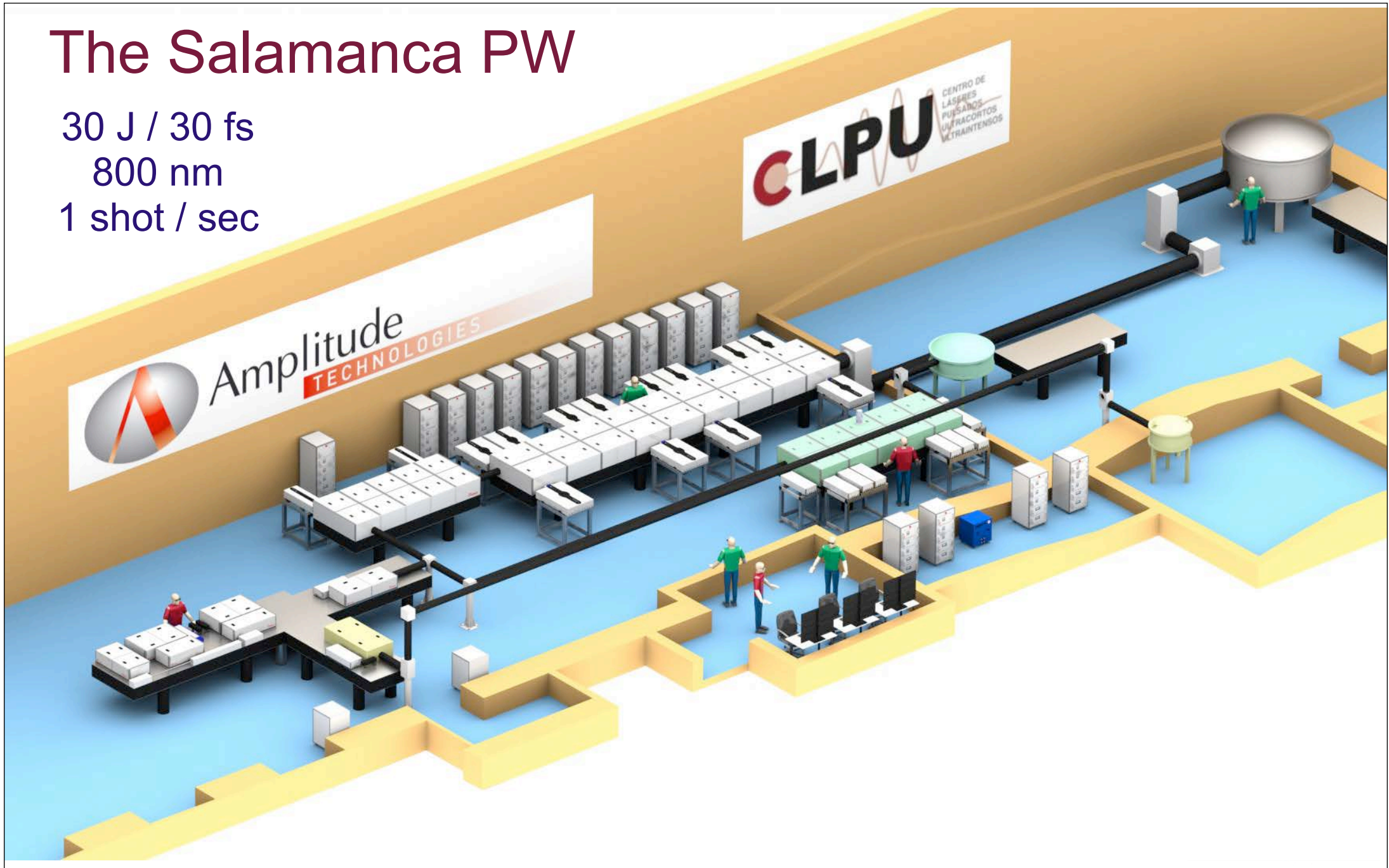
light *denser* than matter

The Salamanca PW

30 J / 30 fs

800 nm

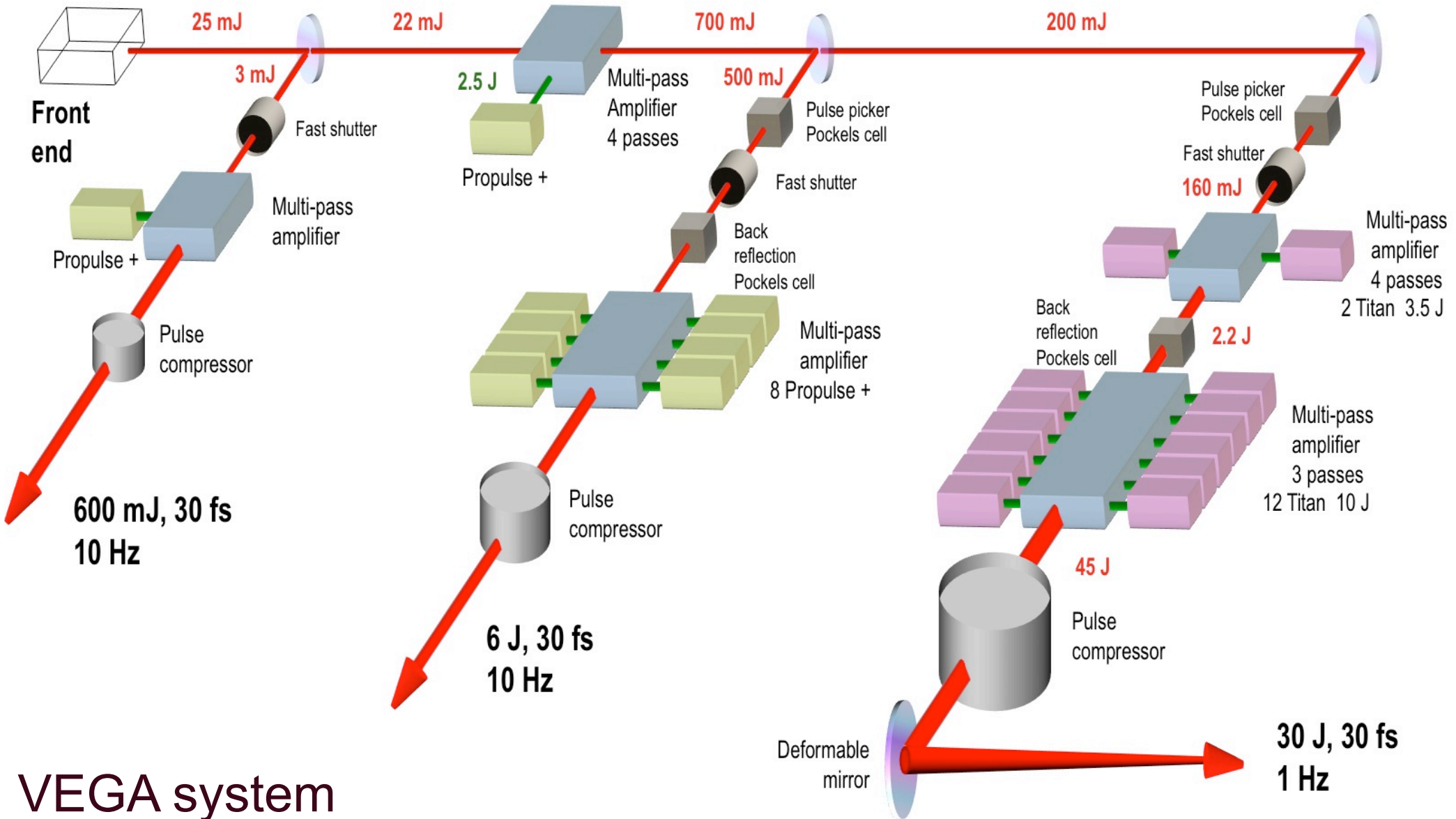
1 shot / sec



Phase I – 20 TW

Phase II – 200 TW

Phase III – 1 PW



VEGA system

 Laser Fundamentals I arrives to the end ...

Thanks !