

# Laser optical clocks and accelerator timing systems

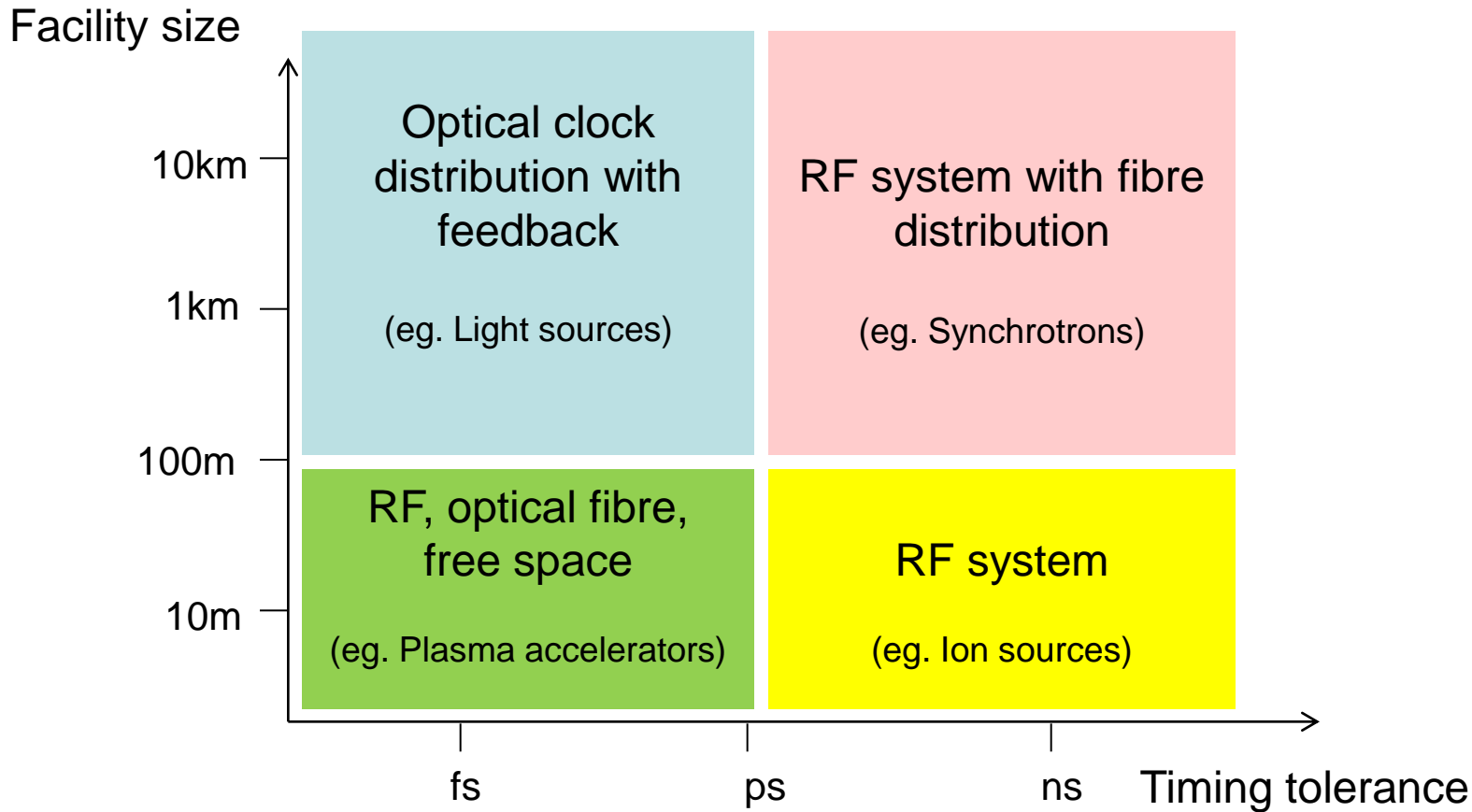
**Trina T. Thakker**

**STFC, Daresbury, UK**

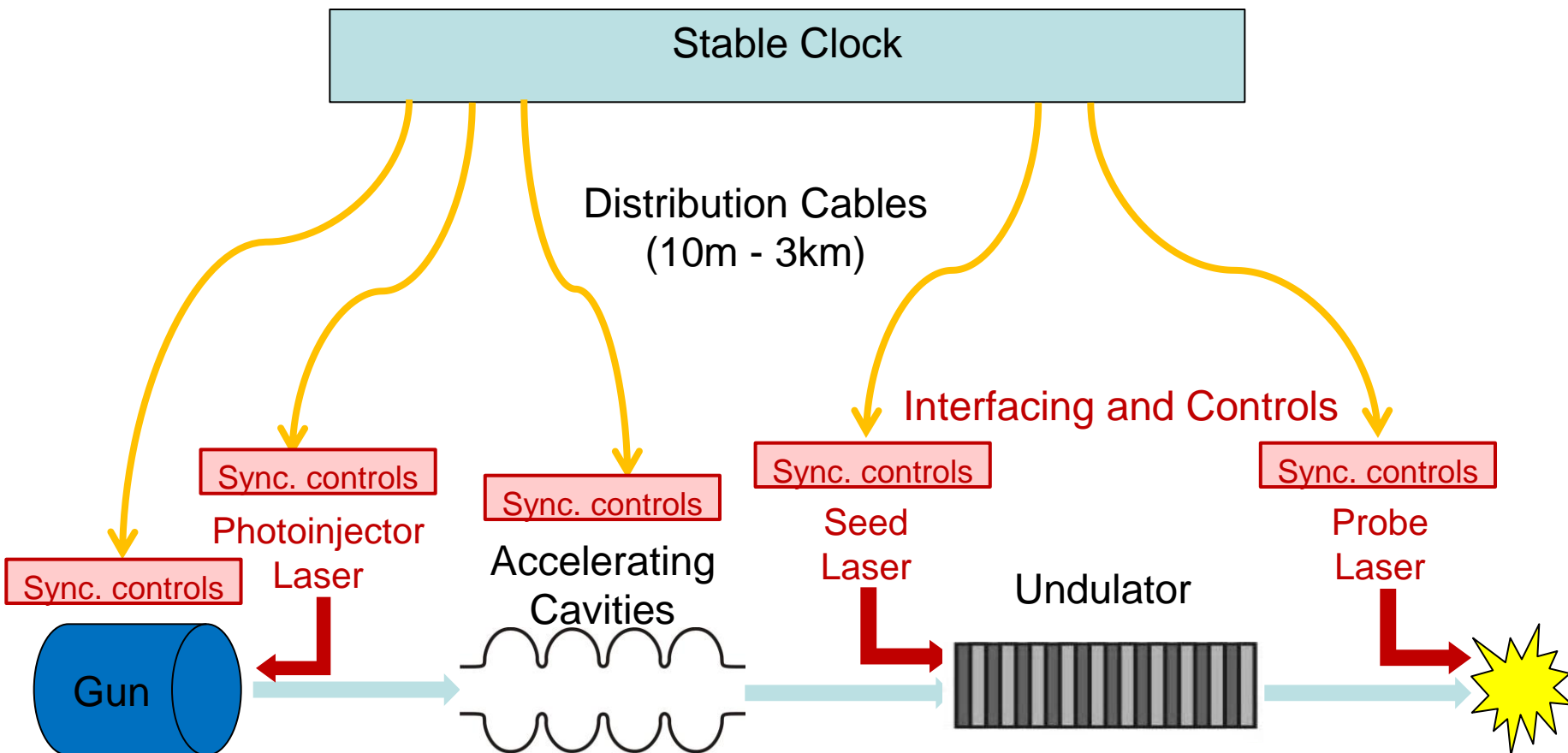


- Timing requirements for accelerators
- ‘Conventional’ RF timing systems
- Going optical
  - The pulsed approach
  - The CW approach
- Challenges for the future...

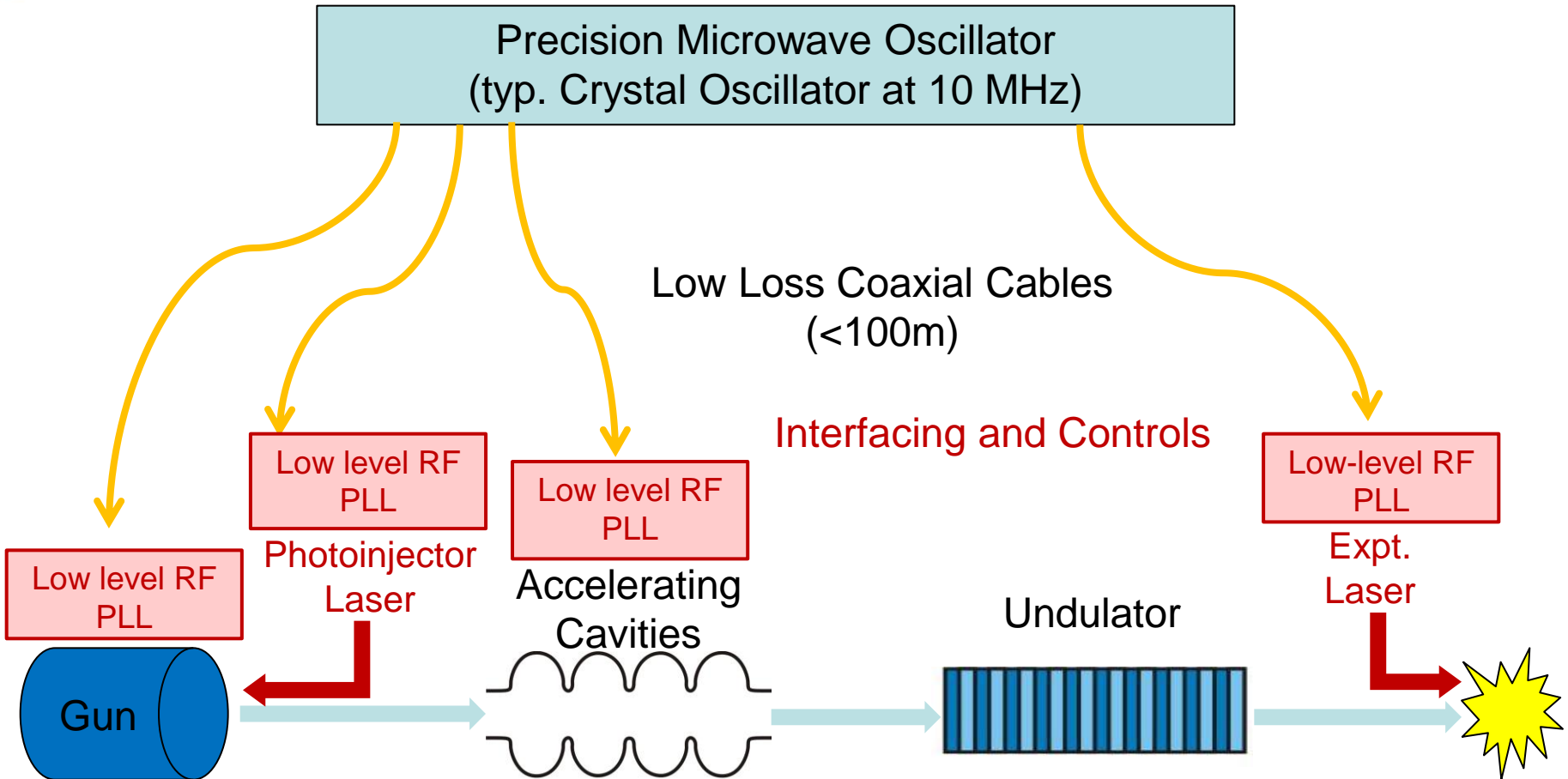
# Timing requirements



# Introduction to timing systems

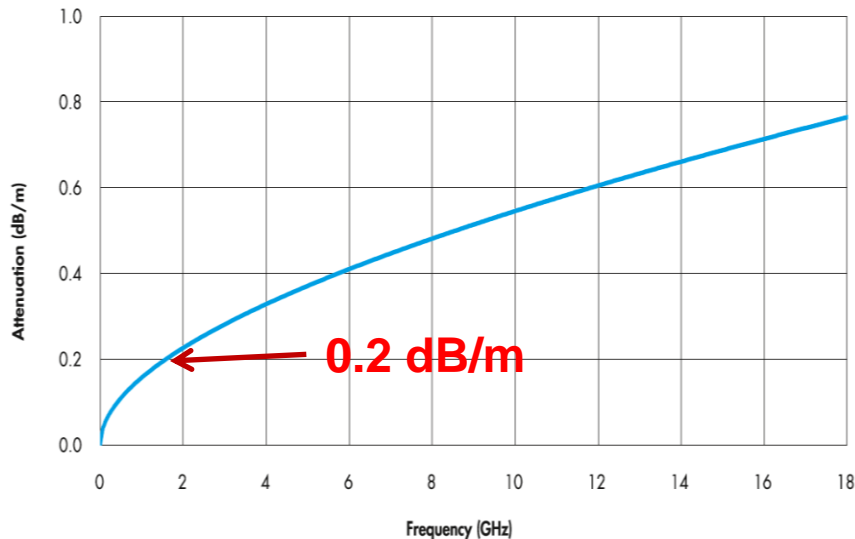


# Basic RF timing (small facility)

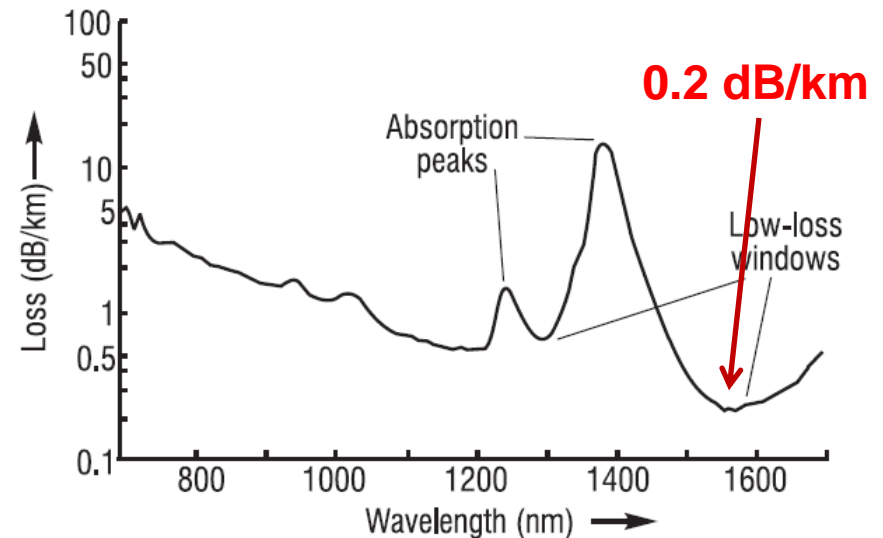


## ■ Attenuation over large distances

Coaxial cable attenuation (dB/m)



Optical fibre attenuation (dB/m)



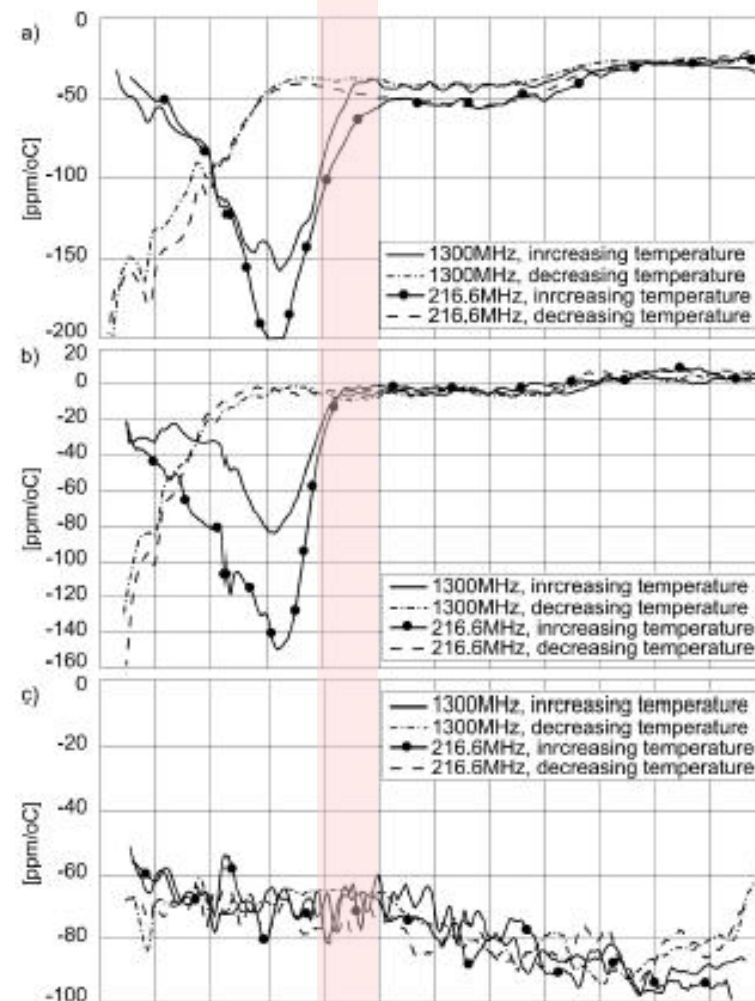
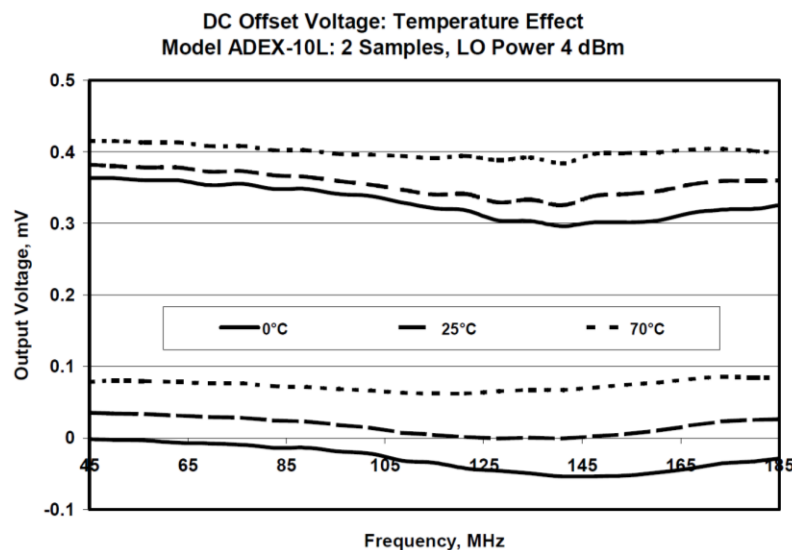
[adapted from Miya, Hasaka, and Miyashita].

# Challenges in RF distribution

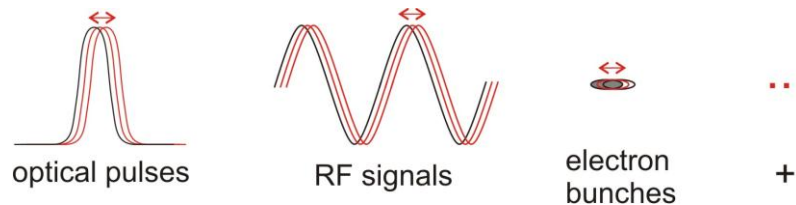


## ■ Timing jitter

- Temperature
- Vibrations
- Dynamics in oscillators
- Dynamics in distribution cables

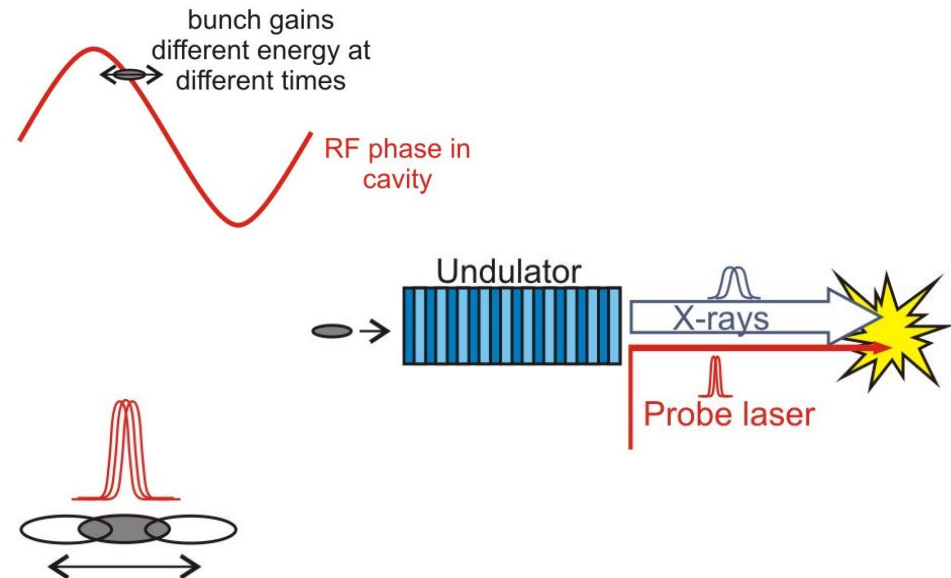


## ■ What is timing jitter?



## ■ Why does it matter?

- Beam energy spread
- Pump-probe experiments
- FEL seeding





# Characterizing timing jitter



## How is jitter measured?

Assuming no amplitude noise:

Time domain description

$$v(t) = V_0 \sin(2\pi f_c t + \varphi(t))$$

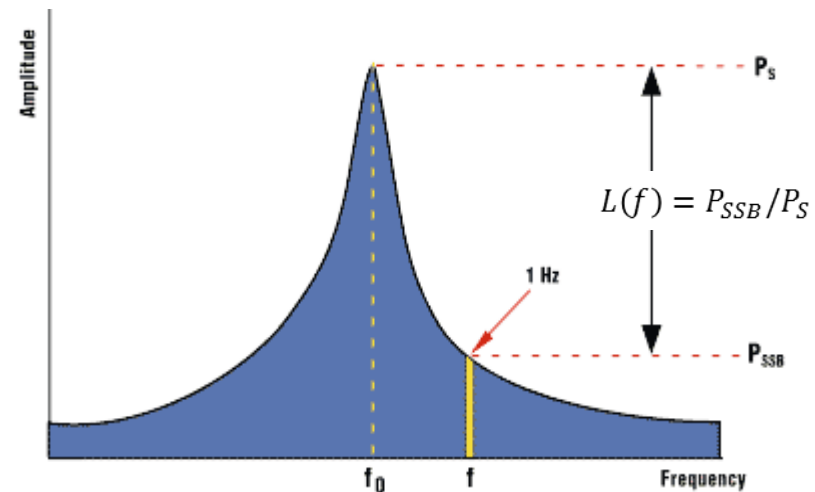
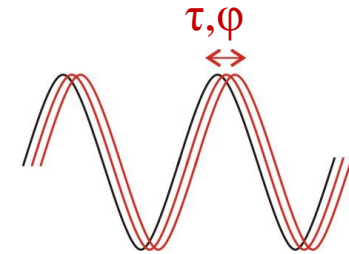
Mean-squared spectrum

$$\overline{\varphi^2(t)} = \int_{-\infty}^{\infty} S_{\varphi}(f) df$$

For small modulation ( $\ll 1$  rad.):

$$L(f) \approx S_{\varphi}(f)/2$$

Conventional form (dBc/Hz)



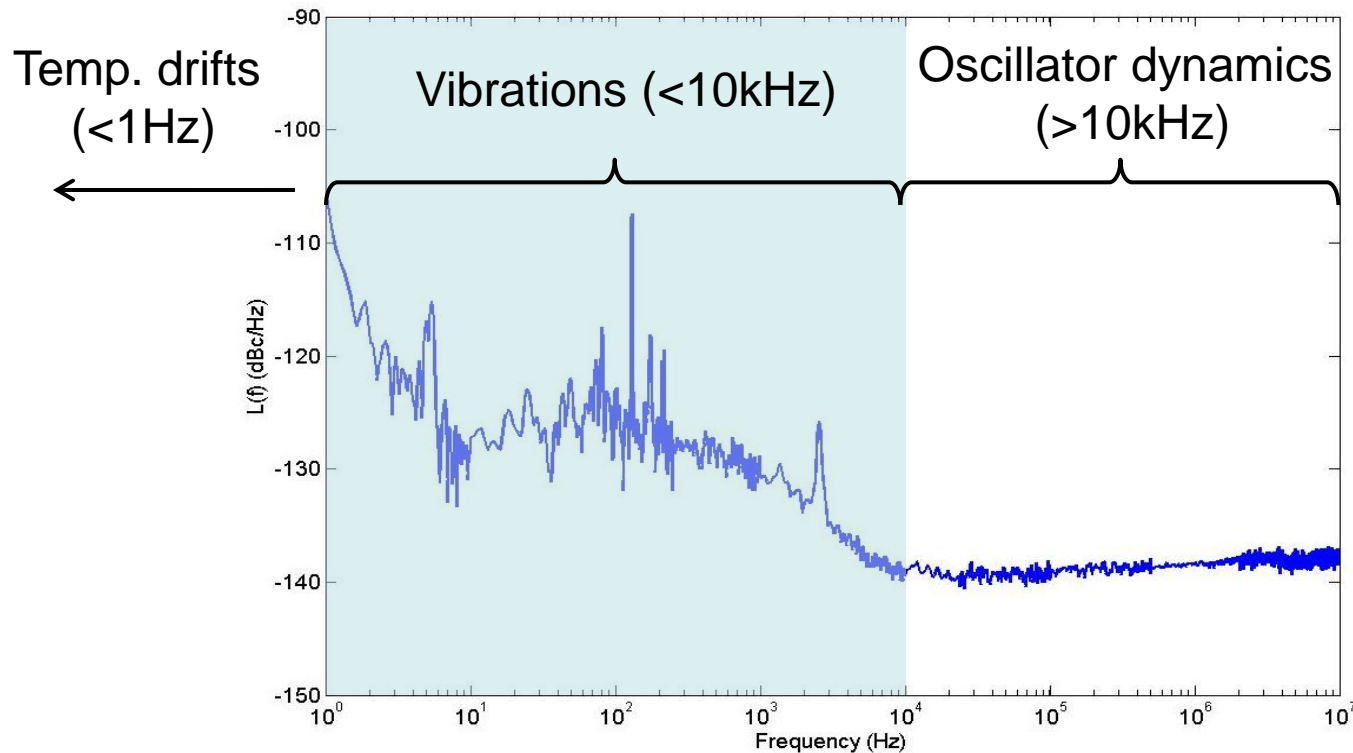
## RMS jitter:

$$\tau_{rms}(f_1, f_2) = \frac{1}{2\pi f_c} \sqrt{2 \int_{f_1}^{f_2} 10^{L(f)/10} df}$$

# Jitter in timing systems

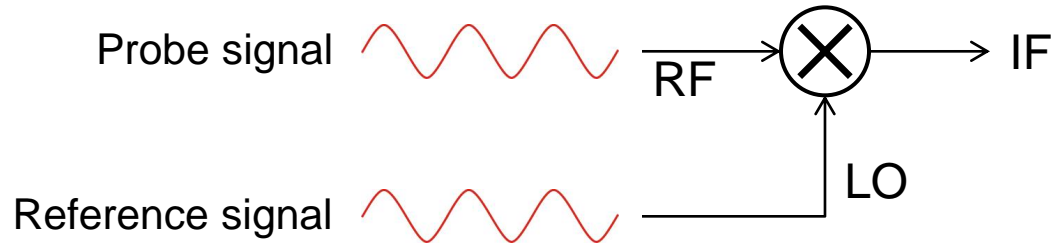


## ■ Sources of jitter



$$\tau_{rms}(f_1, f_2) = \frac{1}{2\pi f_c} \sqrt{2 \int_{f_1}^{f_2} f^2 10^{L(f)/10} df}$$

## RF phase detection with a mixer



## Ideal mixer multiplies the probe and reference signals

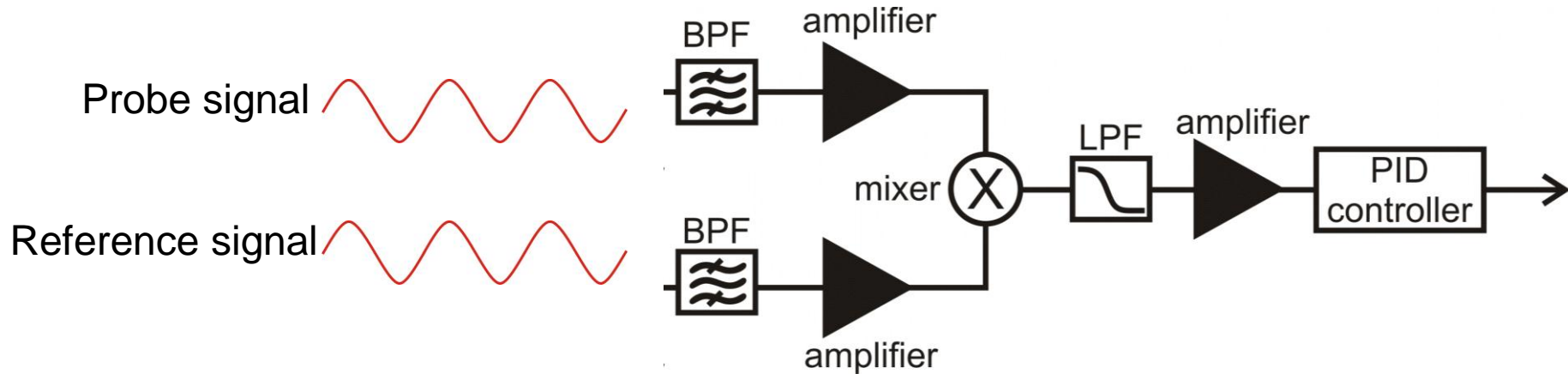
$$V_{IF}(t) = A_{LO} \cos(\omega_{LO}t) * A_{RF} \cos(\omega_{RF}t + \varphi)$$
$$= \frac{A_{LO}A_{RF}}{2} \{ \cos((\omega_{LO} - \omega_{RF})t - \varphi) + \cos((\omega_{LO} + \omega_{RF})t + \varphi) \}$$

if  $\omega_{LO} = \omega_{RF}$  →

$$= \frac{A_{LO}A_{RF}}{2} \{ \cos \varphi + \cos(2\omega_{LO}t + \varphi) \}$$

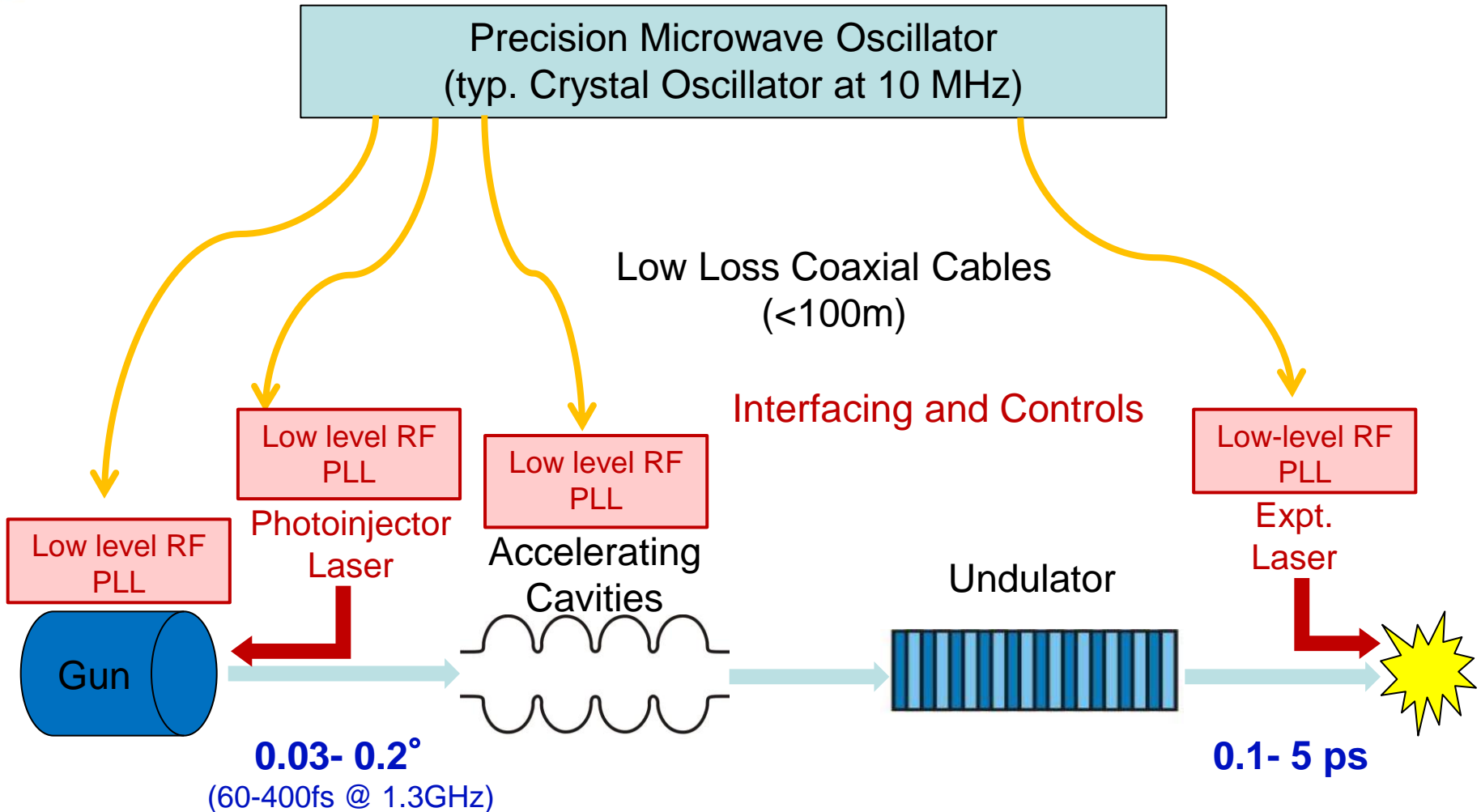
DC Voltage  
Linear for  $\varphi \sim \pi/2$

Needs to be filtered out  
with a low pass filter



- Resolution limits of a low noise mixer  $\sim 0.02^\circ$ 
  - At 1.3 GHz  $\approx 42$  fs
  - At 3 GHz  $\approx 18.5$  fs
  - At 10 GHz  $\approx 5.5$  fs

# Basic RF timing (small facility)



## ■ Advantages of an optical system

- Quieter clock
- High bandwidth
- Low attenuation

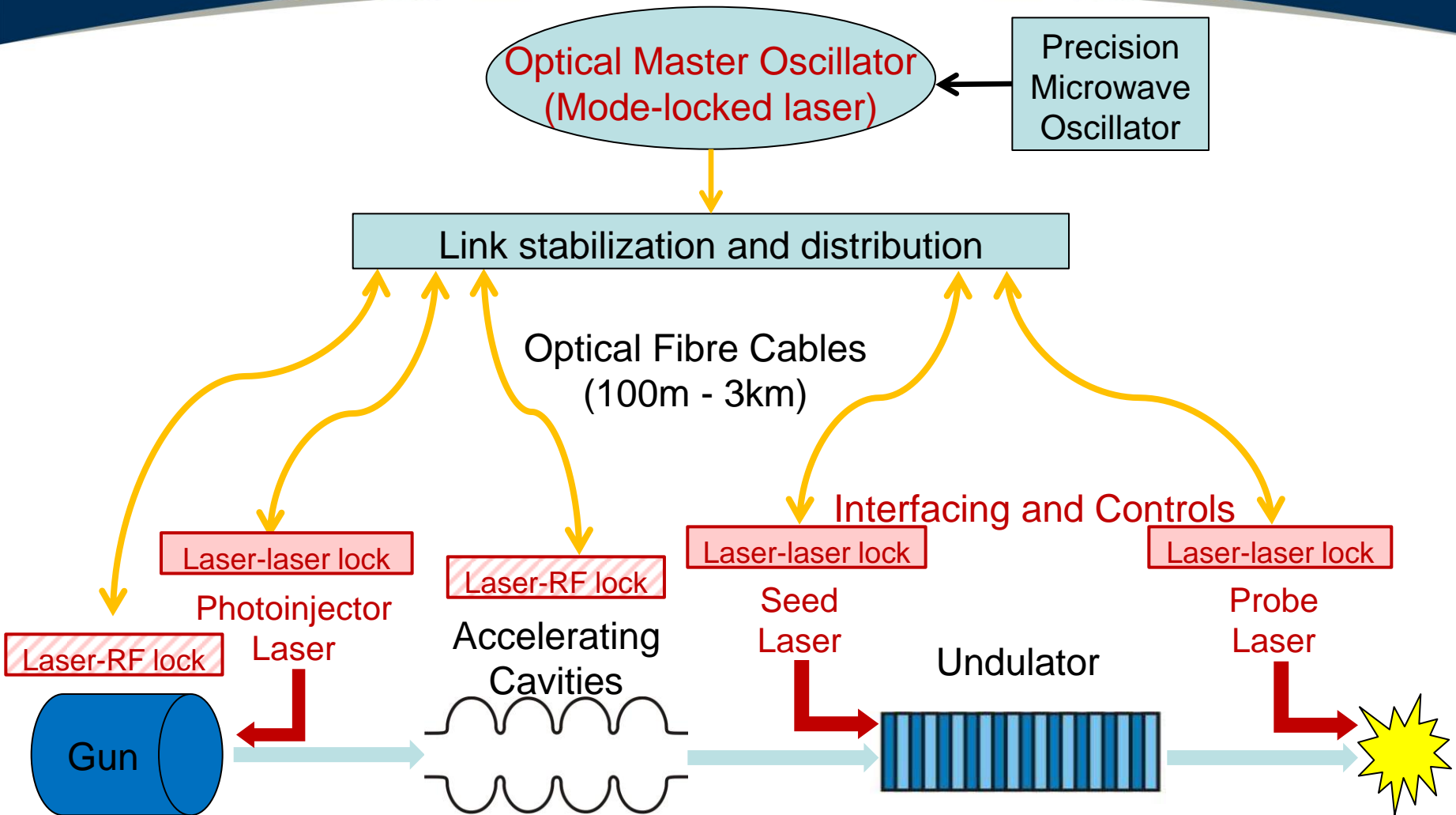
## ■ New challenges

- Phase change with temperature
- Dispersion compensation
- Polarisation effects: Polarisation mode dispersion (PMD)
- Conversion back to RF
- Reliability ???

Similar to coax  
~ 40 fs/° C/m



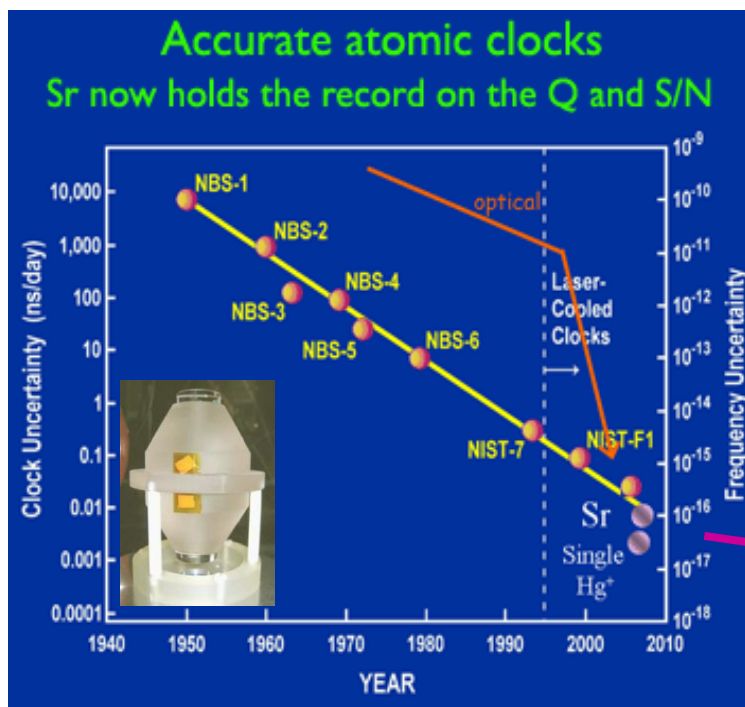
# Introduction to timing systems



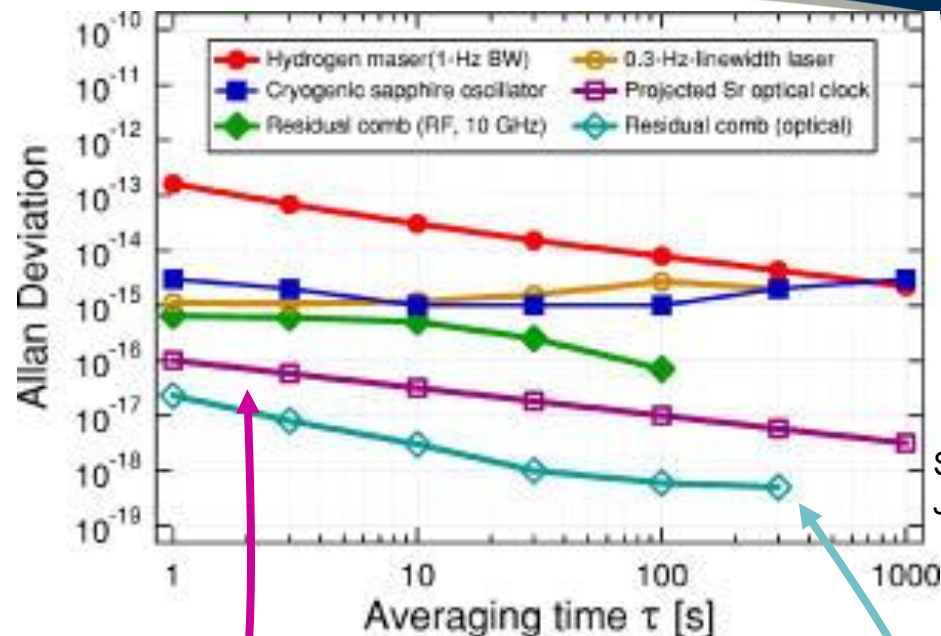
# Ultrastable clocks



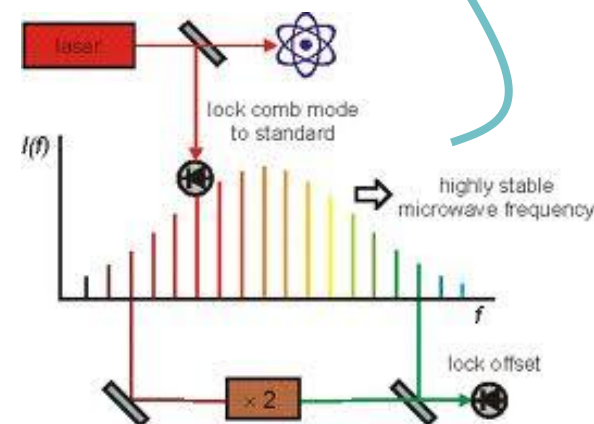
What is the most stable clock you can get?



NIST, USA



S. Foreman,  
JILA





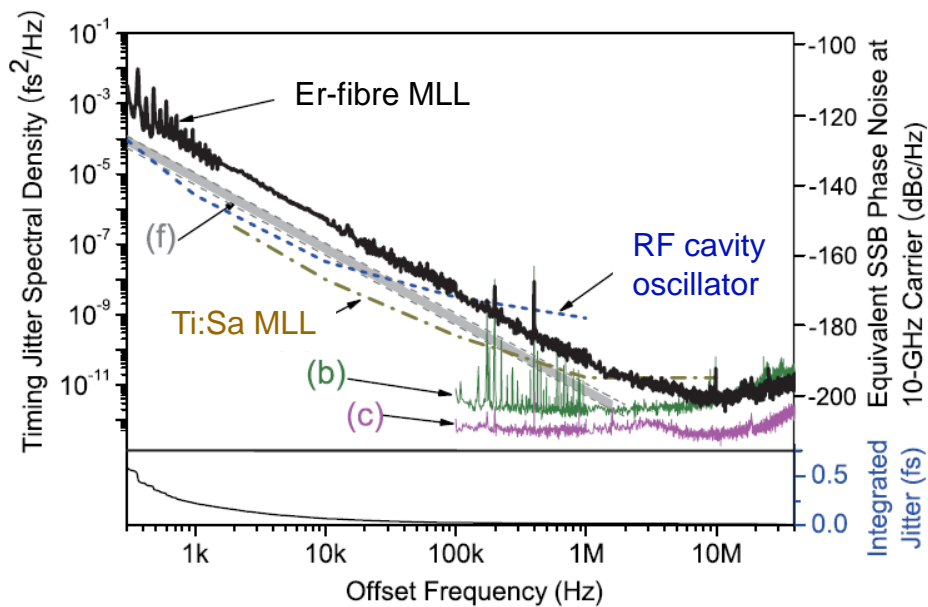


## 2 main approaches

Pulsed Distribution

CW Distribution

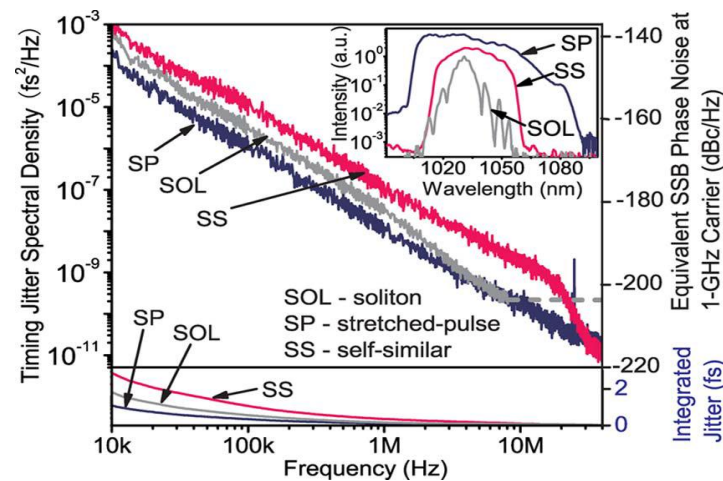
# Ultrastable clocks



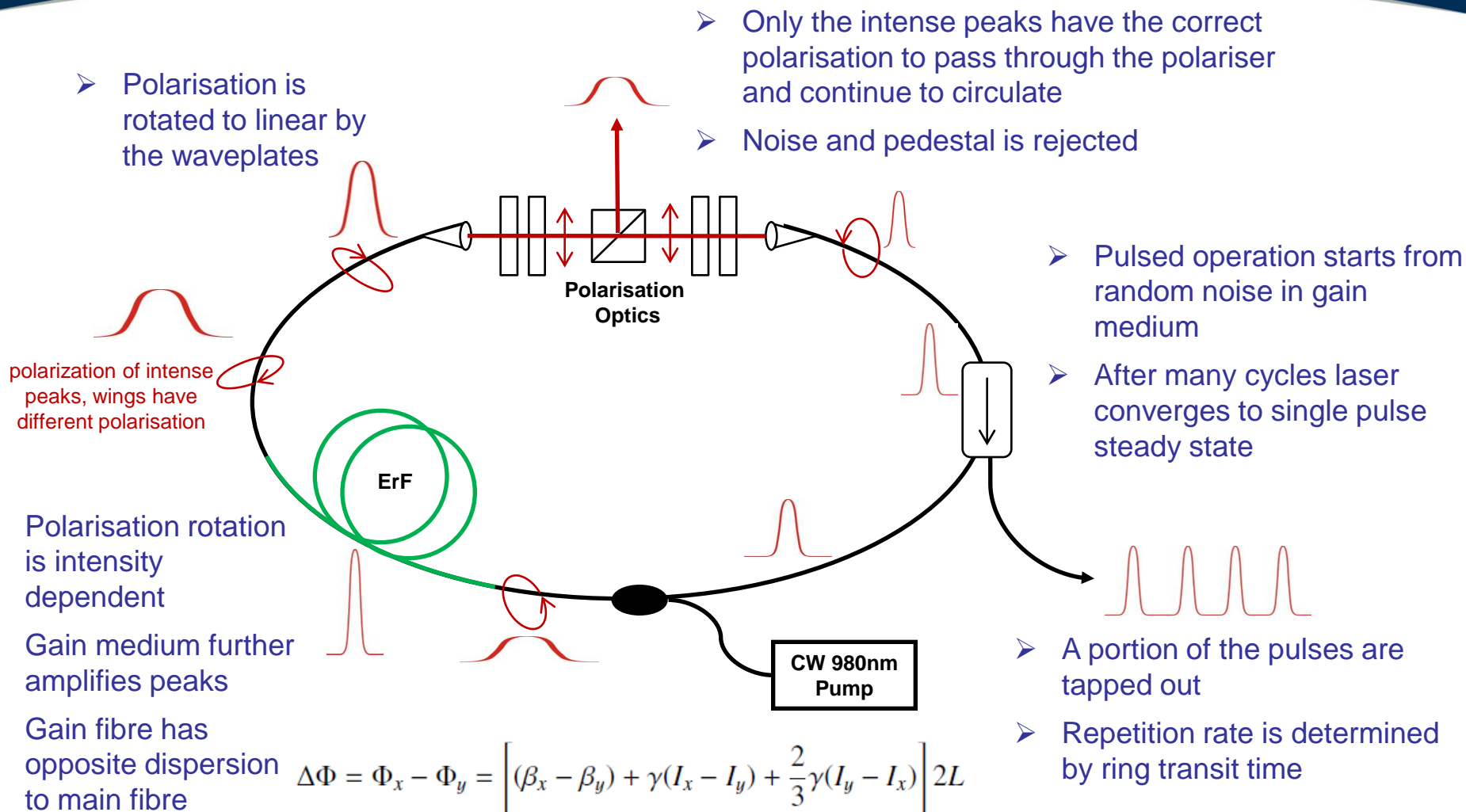
- Some of the most stable microwave and optical clocks
- Passively mode-locked lasers (MLL) are quieter at high frequencies than microwave oscillators
- Ti:Sa oscillators are some of the quietest clocks currently available

■ Fibre lasers at telecommunications wavelengths are particularly suitable for distribution

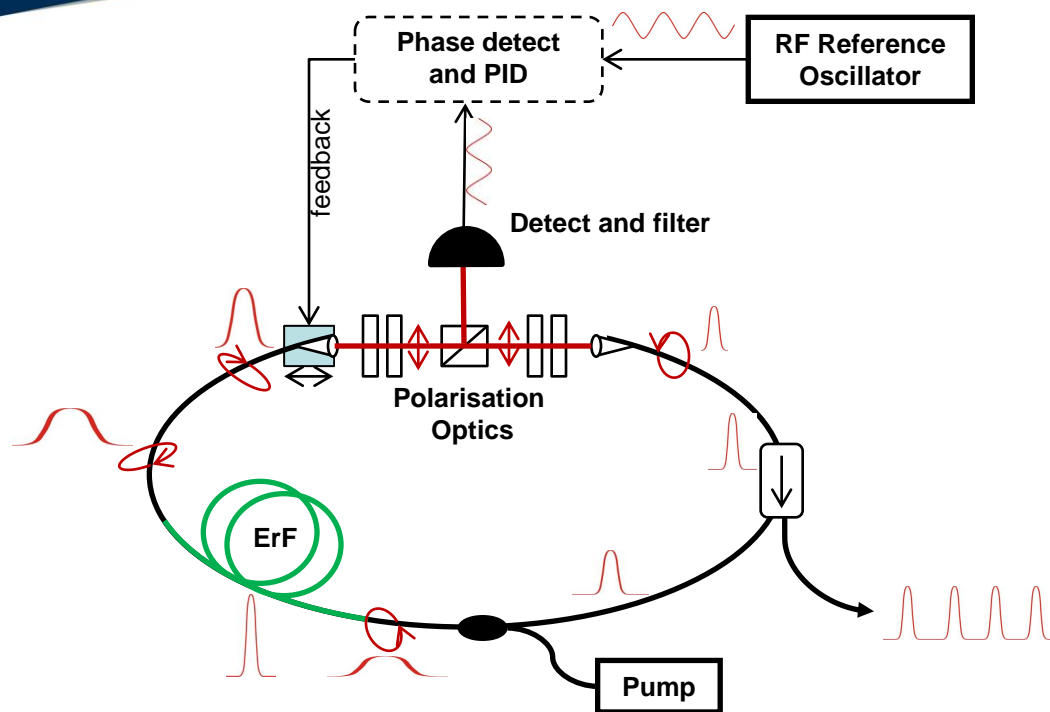
- Low loss
- mature components
- high bandwidth components



# Stretched-pulse fibre lasers



# Ultrastable clocks

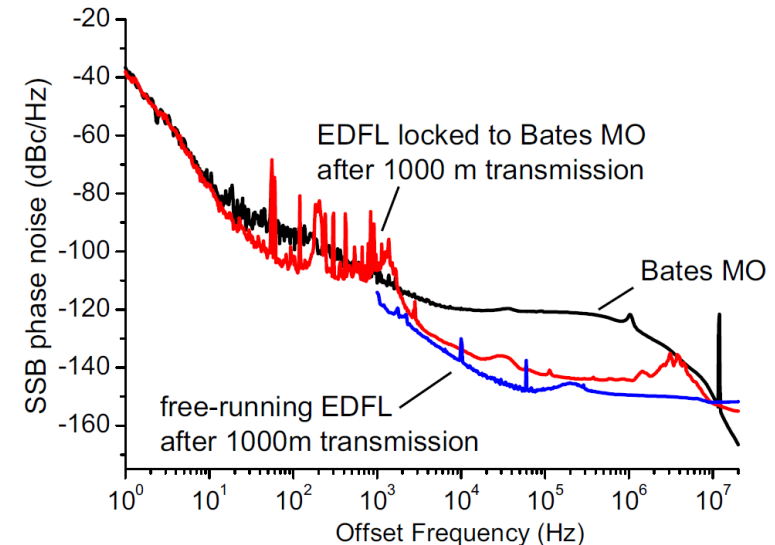


2.637... m cavity length  $\rightarrow$  81,250,000 Hz  
add **28 nm**  $\rightarrow$  81,250,001 Hz

## Cavity length susceptible to low frequency noise/drifts...

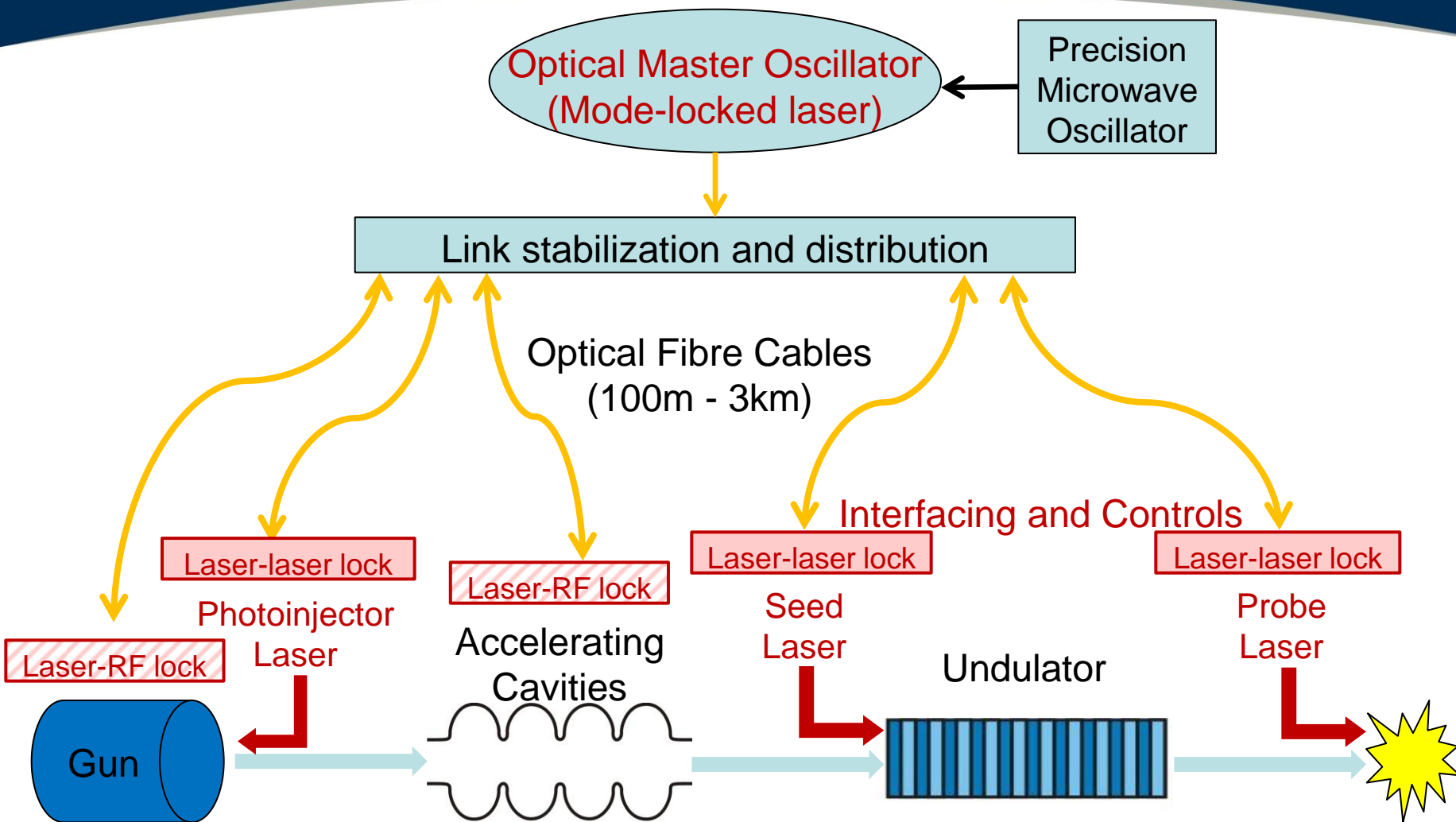
- Fibre length changes are detected through phase comparison to RF
- Feedback signal compensates for changes in path length

## but very low noise at high frequencies



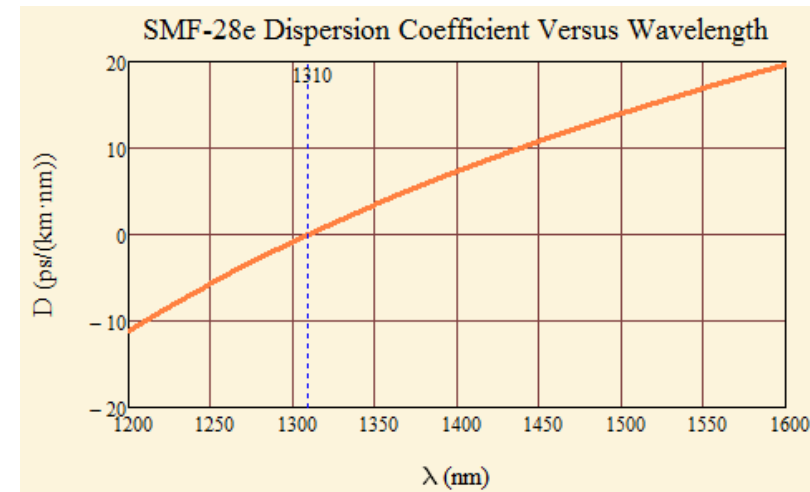
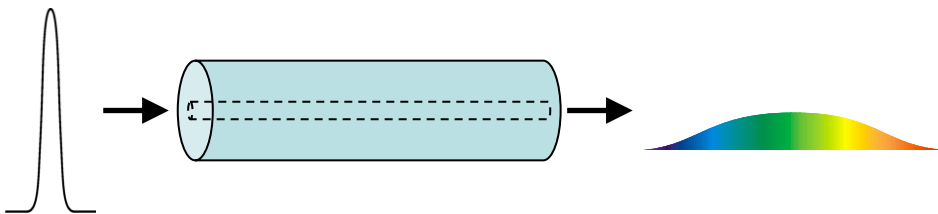
(Source: A. Winter, DESY)

# Pulsed timing systems



- 'Undesirable' effects in fibres:
  - Chromatic dispersion
  - Polarisation mode dispersion
  - Fibre nonlinearities (specifically self-phase modulation)
  - **Temperature sensitivity**
  - **Vibration sensitivity**
  - Radiation darkening

## ■ Dispersion in optical fibres



# Dispersion in optical fibres



- Dispersion in optical fibres:
  - In standard fibre (SMF 28e<sup>+</sup>):  $\beta_2 \approx 21 \text{ ps}^2/\text{km}$

$$L_D = \frac{T_0^2}{|\beta_2|} \quad T_0 = \frac{T_{FWHM}}{2\sqrt{\ln 2}} \quad (\text{1/e-point of Gaussian})$$

$$T_{fwhm} = 100 \text{ fs}; L_D = 17 \text{ cm}$$

$$T(z) = T(0) \sqrt{1 + (z/L_D)^2}$$

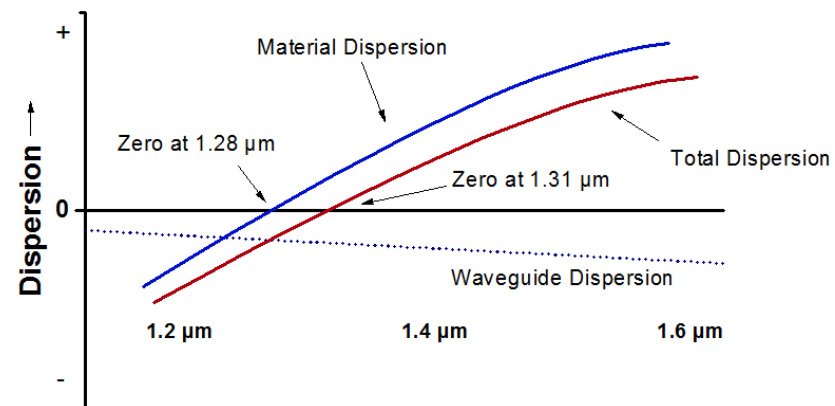
$$T_{fwhm} = 200 \text{ fs}; L = 30 \text{ cm}$$

- Dispersion in waveguides is composed of two parts

$$D = D_m + D_w = -\frac{2\pi c}{\lambda^2} \beta_2$$

Material dispersion    Waveguide dispersion

1.31  $\mu\text{m}$  Zero-Dispersion in Step-Index SM Fiber



# Dispersion compensation



- Combatting dispersion using Dispersion Compensating Fibre (DCF)

$$D_m = \frac{\lambda}{c} \left( \frac{d^2 n}{d\lambda^2} \right)$$

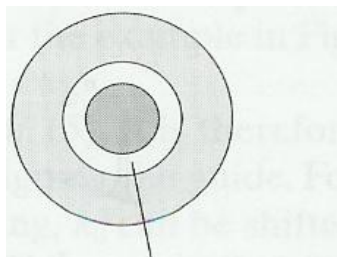
$$D_w = -\frac{n_2(n_1 - n_2)}{c\lambda} V \frac{d^2(Vb)}{dV^2}$$

V-number

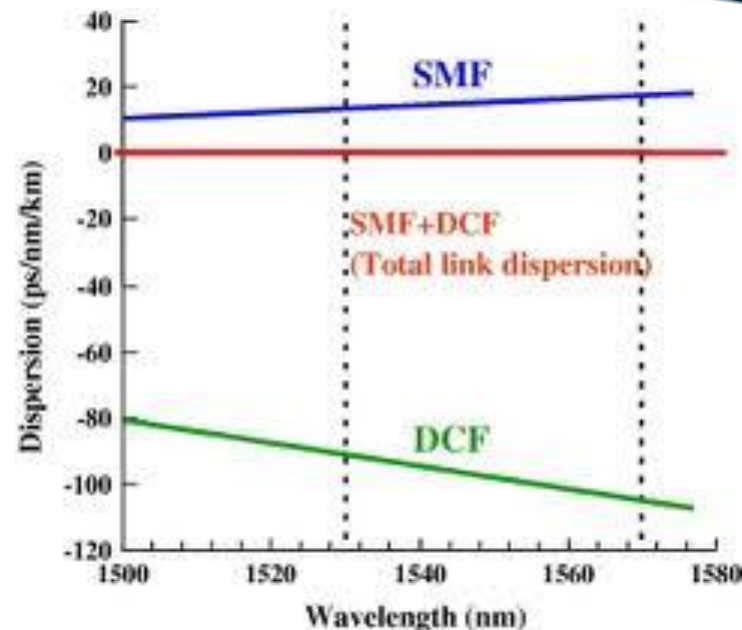
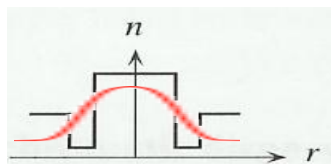
$$V = \frac{2\pi a}{\lambda} (n_1^2 - n_2^2)^{1/2}$$

Normalized propagation constant

$$b = \frac{n_{eff}^2 - n_2^2}{n_1^2 - n_2^2}$$

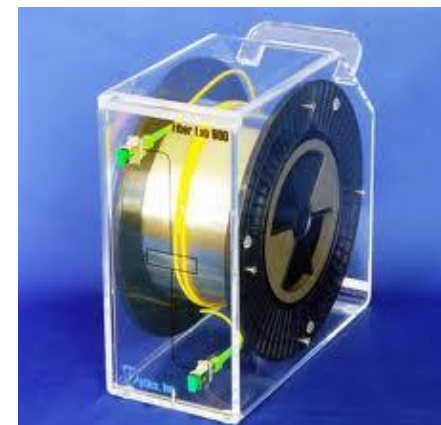


Thin layer of cladding with a depressed index



$$D_{SMF} \approx 17 \text{ ps/nm/km}$$

$$D_{DCF} \approx -135 \text{ ps/nm/km}$$

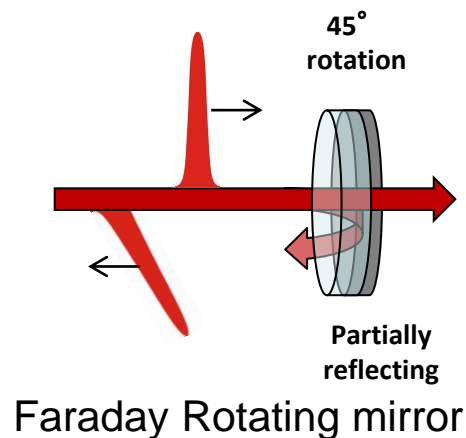
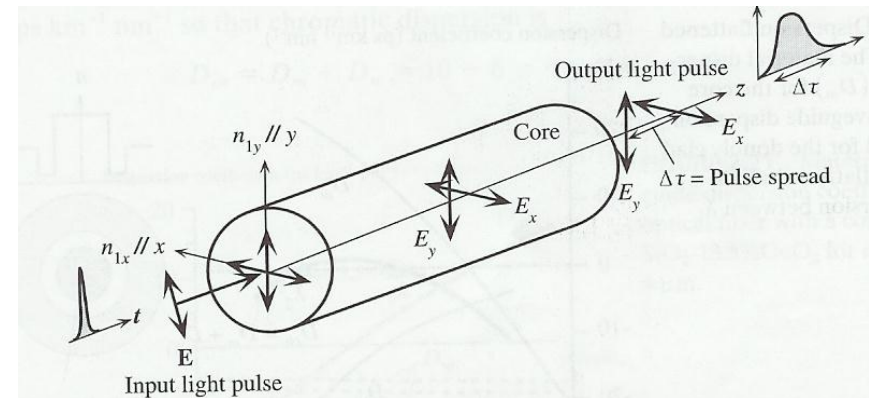




## What is PMD?

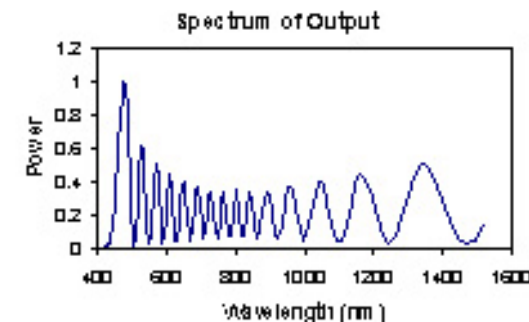
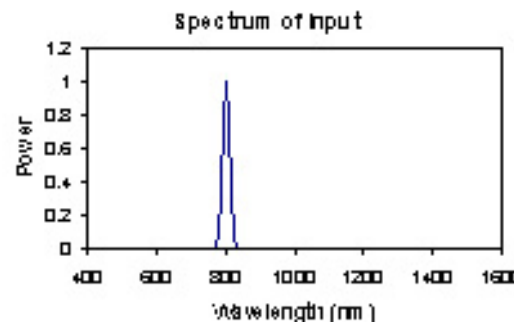
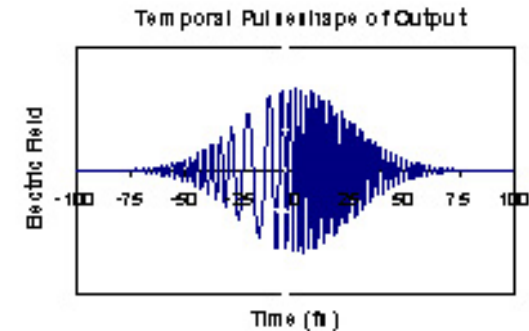
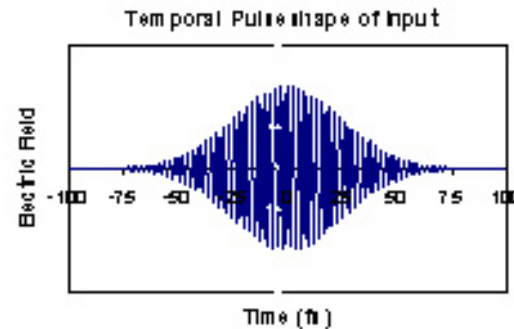
- fiber is not perfectly symmetric, inhomogeneous.
- refractive index is not isotropic
- Polarisation will walk off from each other randomly

## Solutions:



Polarization maintaining fibre

- Self-phase modulation
  - Keep your peak powers low!
- Radiation darkening
  - Commercial fibre
- Temperature and vibration sensitivity
  - Difficult to control or predict



→ Compensate

# Length stabilization



- Estimate how much optical phase change you expect

$$\Delta\phi = \frac{2\pi}{\lambda} \left( \frac{n}{L} \frac{dL}{dT} + \frac{dn}{dT} \right) \Delta T \cdot L$$

$$\approx 47.5 \times 10^3 \text{ rad}/^\circ\text{C}$$

$$\frac{dn}{dT} \approx 1.1 \times 10^{-5} / ^\circ\text{C}$$

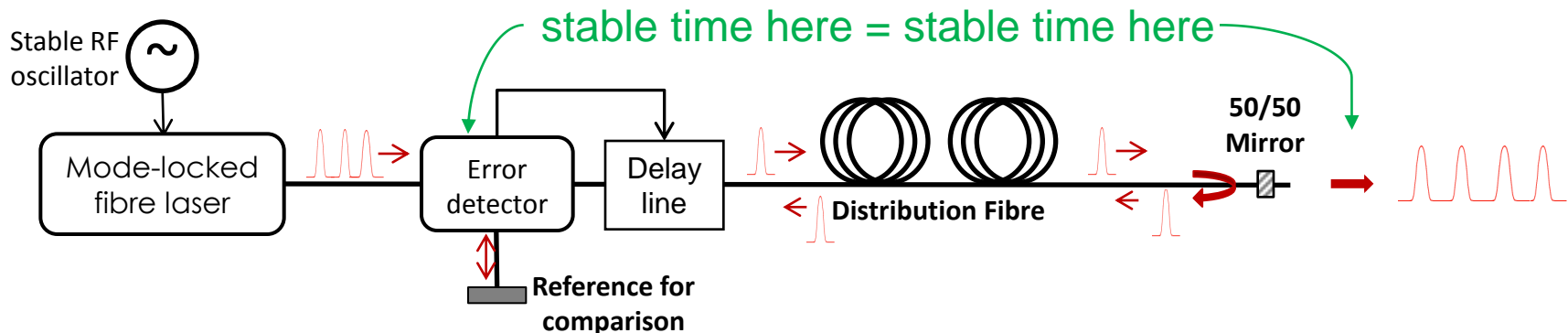
$$\frac{1}{L} \frac{dL}{dT} \approx 5 \times 10^{-7} / ^\circ\text{C}$$

over 1km:

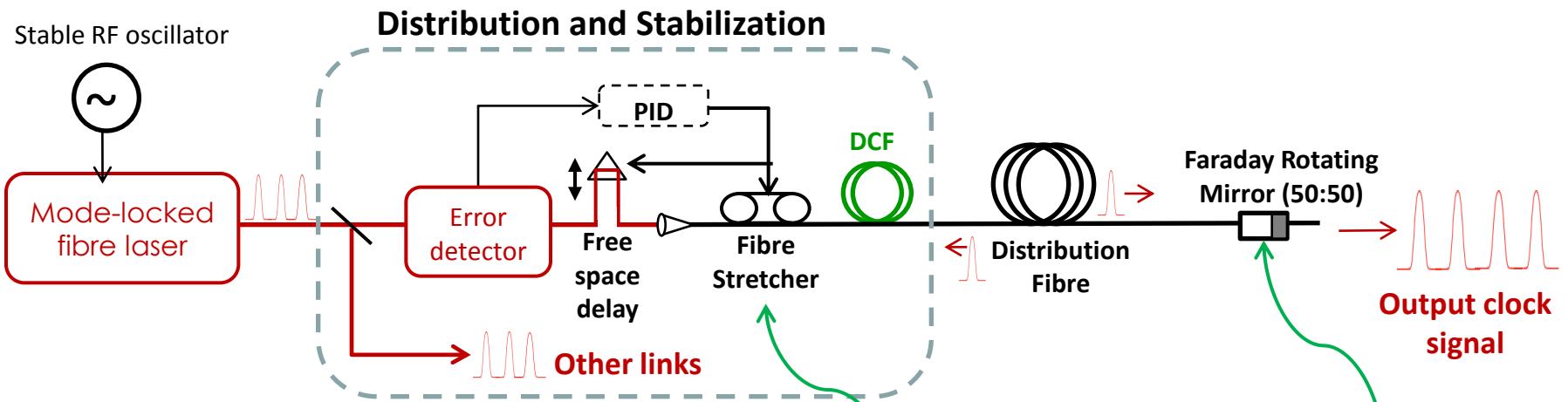
$$= 11.7 \text{ mm}/^\circ\text{C}$$

(Assuming your facility has this stability)

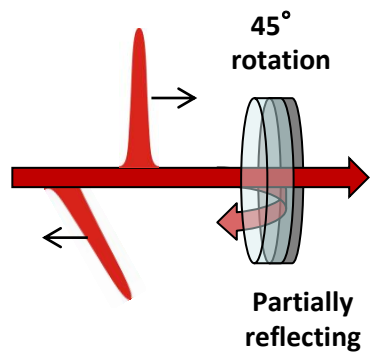
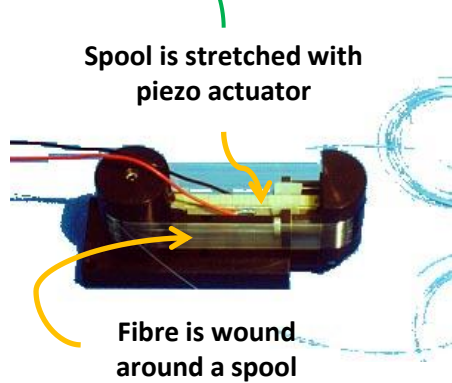
- How to detect and compensate for length changes?
- The 'same return path' assumption



# Length stabilization



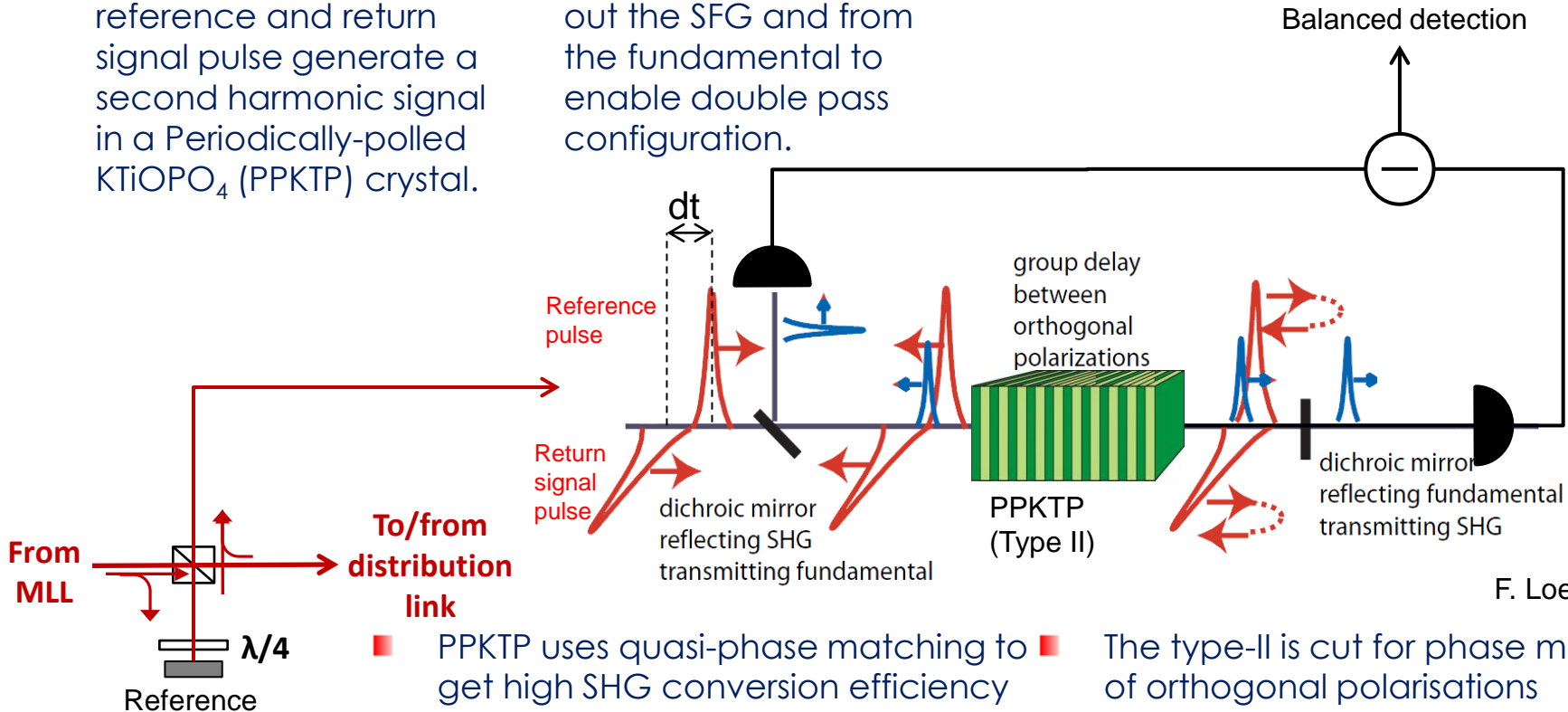
- Coarse delay (free space) provides enough range for max expected drift:  
eg. 390ps for 1km facility with  $\Delta T=5$  deg.
- Piezo wafer resonance > locking bandwidth
- 90° rotation at FRM cancels out accumulated PMD in link (within link bandwidth)





- Overlap between the reference and return signal pulse generate a second harmonic signal in a Periodically-polled  $\text{KTiOPO}_4$  (PPKTP) crystal.

- Dichroic mirrors select out the SFG and from the fundamental to enable double pass configuration.

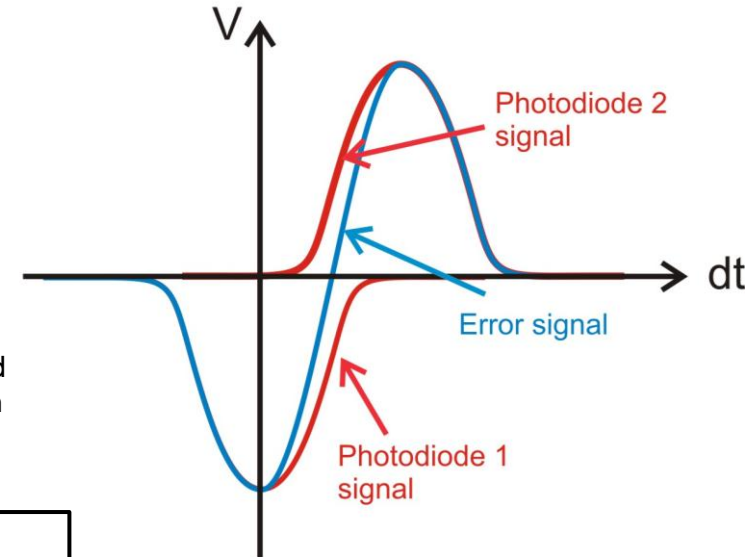


F. Loehl, DESY

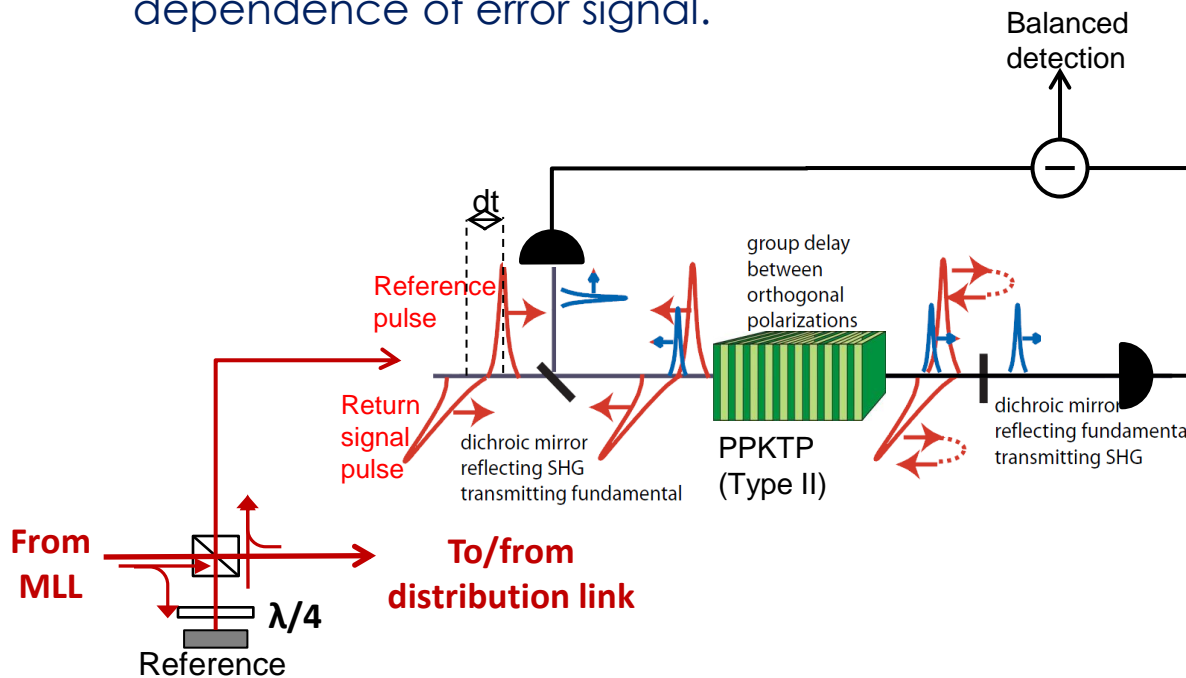
- PPKTP uses quasi-phase matching to get high SHG conversion efficiency
- The KTP is reverse polled when phase mismatch between the pulses walks off to  $\pi$ , to maintain phase matching.

The type-II is cut for phase matching of orthogonal polarisations  
Using type-II eliminates the background signal associated with each pulse's own SHG and generates only the SFG generated when overlapped

- The difference signal between the forward and backward SHG detectors give an S-curve error signal with respect to  $dt$
- Balanced configuration increases sensitivity and reduces amplitude dependence of error signal.



- Error signal will be at zero crossing when the pulses have perfect overlap at the **EXIT** of the PPKTP.

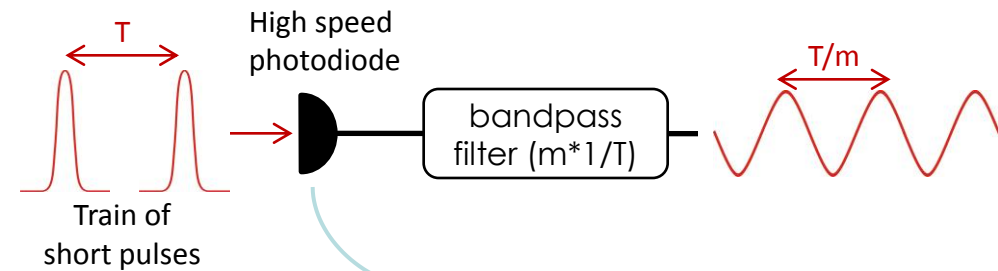




# Laser to RF locking

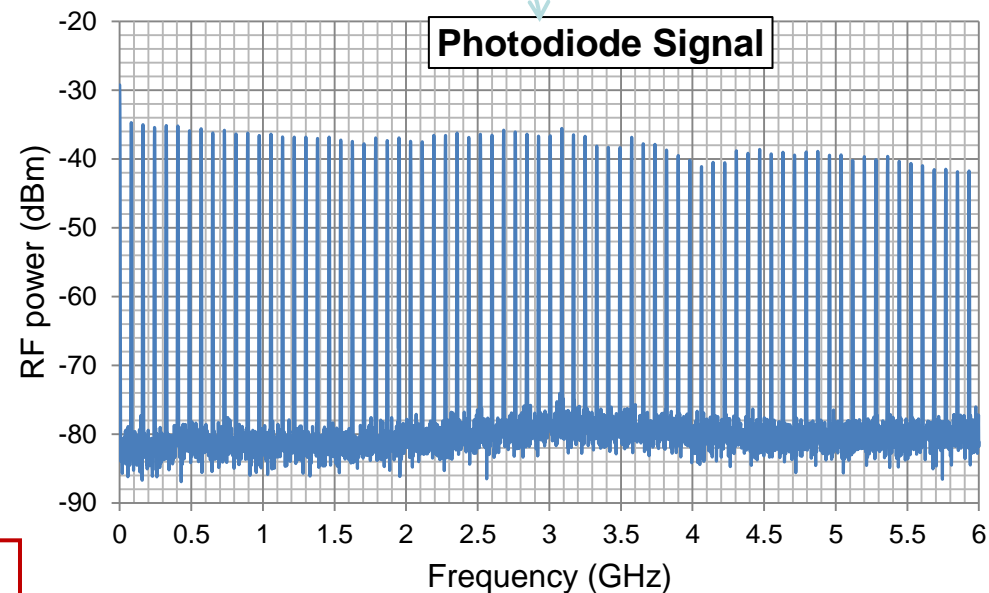
## Direct Clock Delivery

- The clock signal can be directly extracted from the optical signal by detection on a photodiode and filtering.
- Delivered clocks can be used to lock to RF components with phase detection technique
- Potential errors in amplitude to phase conversion



## Short pulse delivery

- Generates high harmonics in high speed photodiodes
- RF filter is used to extract desired harmonic
- Using higher harmonic improves locking resolution



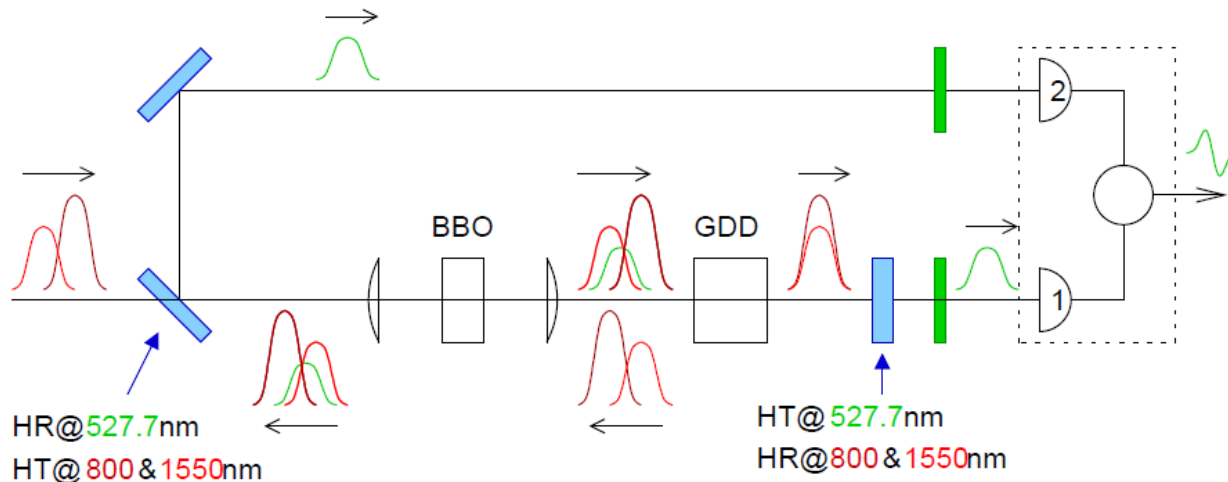
**Stable clocks signals can be delivered at harmonics far above the laser repetition rate**

# Locking to other lasers



- Can modify balanced cross-correlator to lock 2 lasers at different wavelengths
- SFG signal gives the overlap between the pulses

**Eg. Locking Ti:Sa (800nm) to optical clock (1550nm) -> SFG at 527nm**



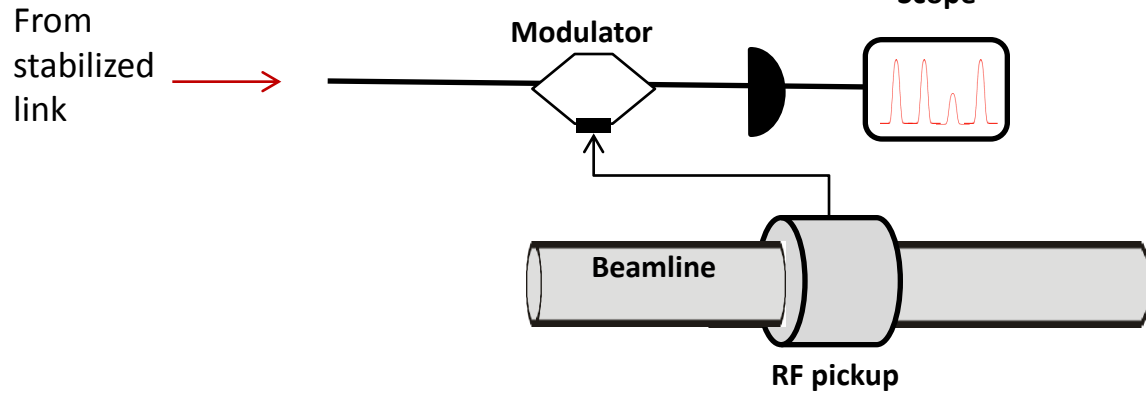
- Since BBO is not birefringent, the delay between the two pulses is generated with a dispersive block.



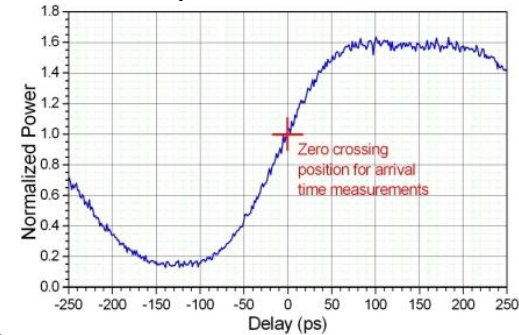
# Timing Monitoring



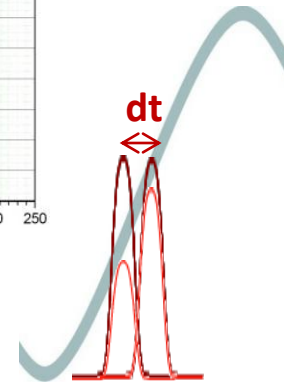
## ➤ Beam Arrival Monitor



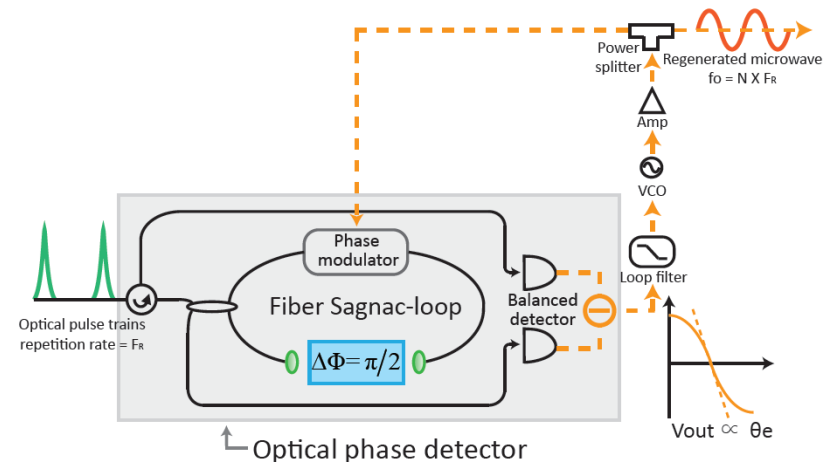
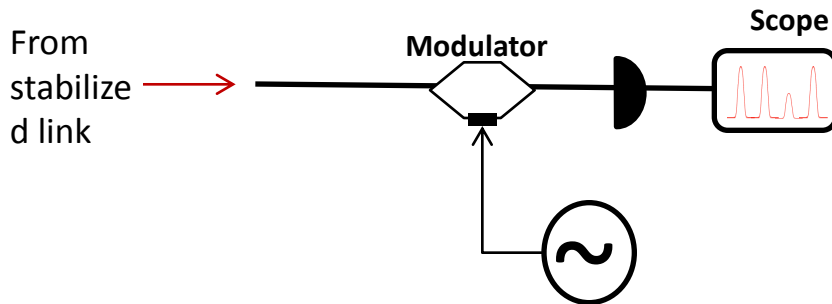
Pickup characteristic



RF signal



## ➤ RF phase monitoring



J.Kim, FLS12

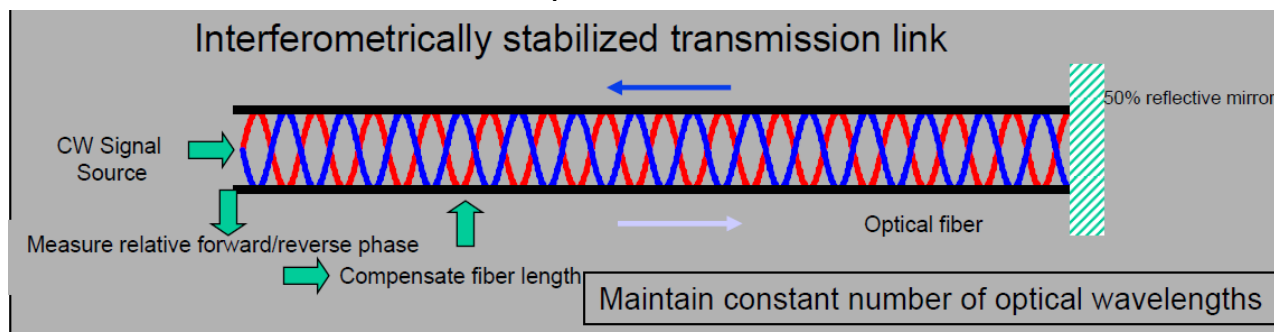


2 main approaches

Pulsed Distribution

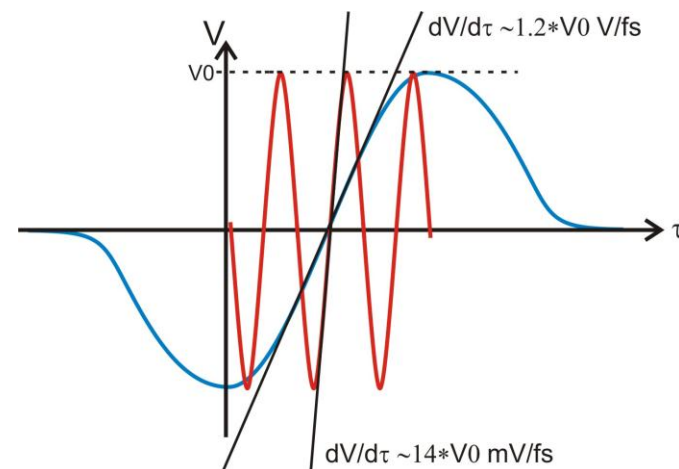
CW Distribution

- Transmit CW laser instead of pulsed



- Detect delay in phase shift of optical **carrier** rather than pulse

- Much higher sensitivity can be achieved:
  - S-curve from cross-correlator has max sensitivity **14.1 mV/fs** for 100fs pulse
  - Zero crossing of interference fringes has max sensitivity **1.21 V/fs** at 1550nm

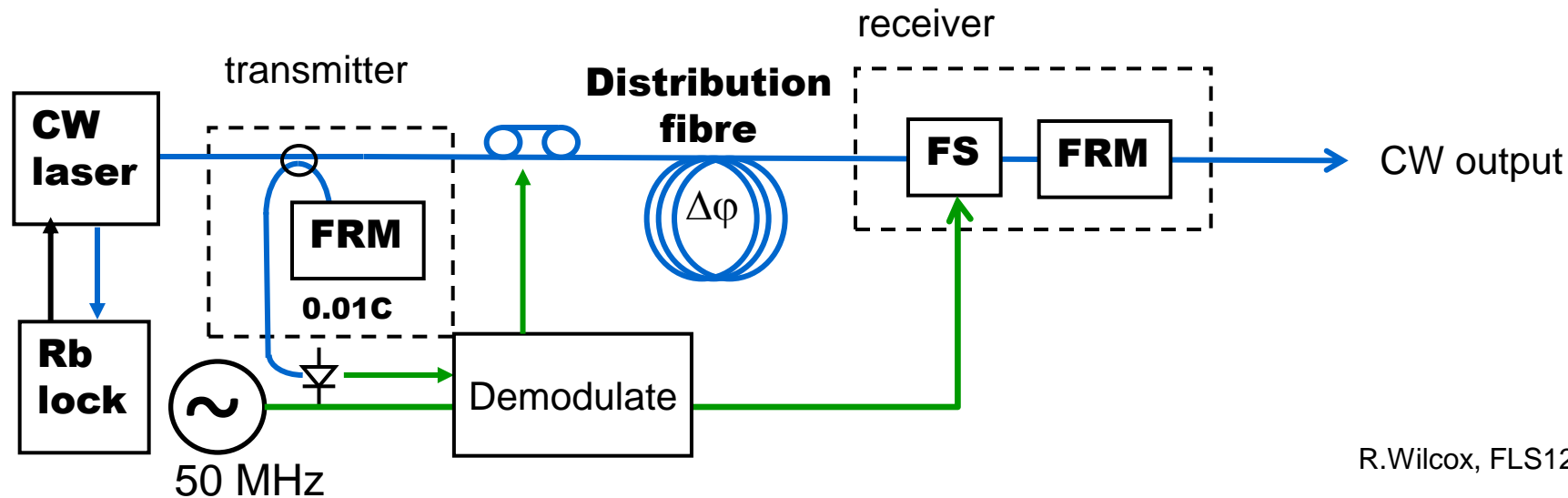


- Problems avoided – PMD, dispersion, SPM

# CW timing systems



- Timing stability = Frequency stability
- Lock to a frequency standard.



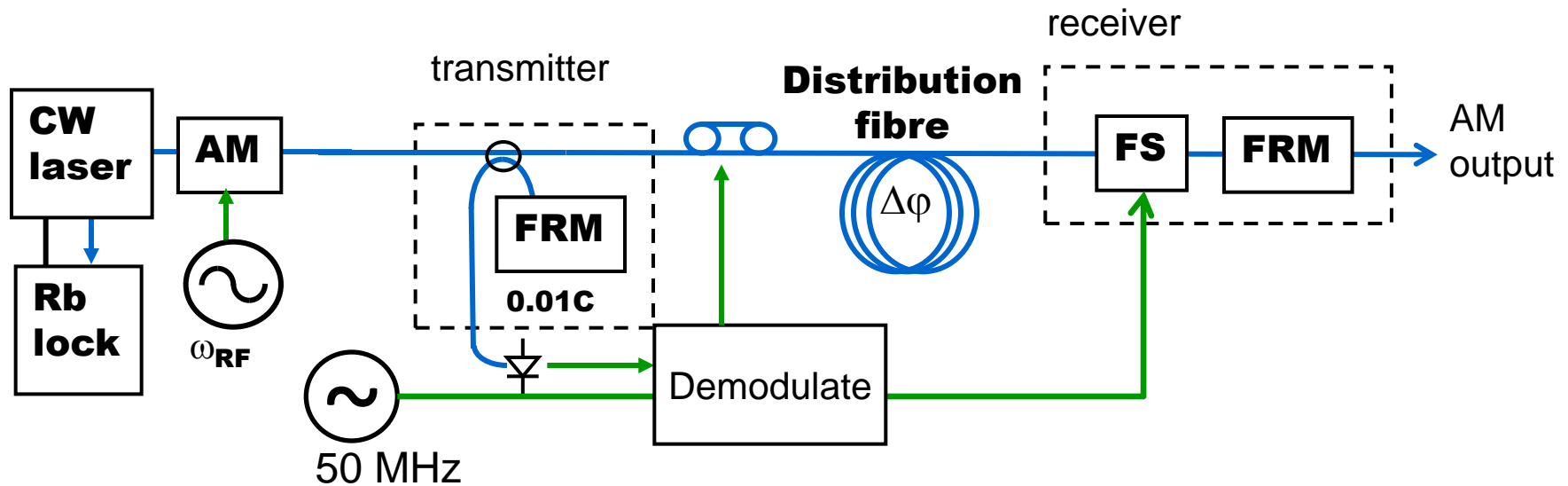
R.Wilcox, FLS12

- New Challenge – Fringe counting, Fringe jumps!
- Divide down to lower frequency (but we're optical, so have lots of headroom to do this)
- Down-convert the phase information to a lower band

# CW timing systems



- Optical frequencies much too high for accelerators to operate on. Need clocking information in the RF range.
- Once fibre is stabilized, amplitude modulation required to transmit clock frequency



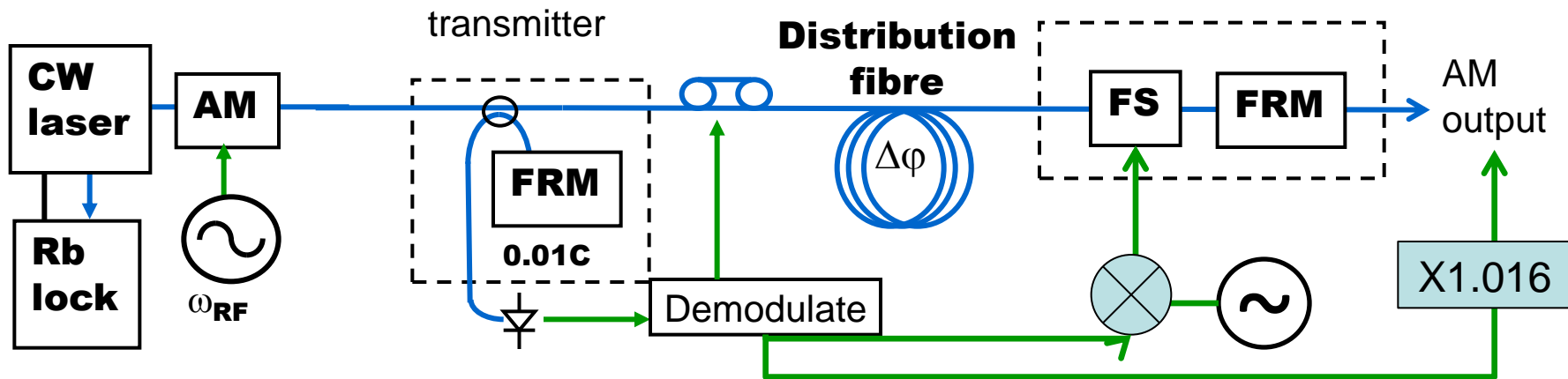
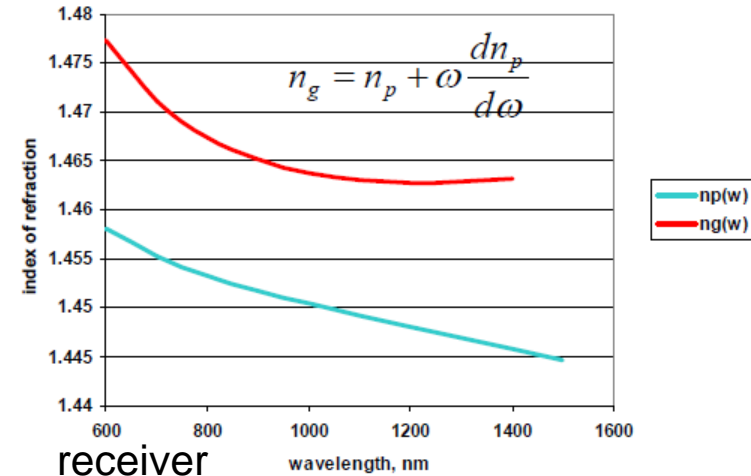
R.Wilcox, FLS12

# We will stabilize group delay while measuring phase delay



**BUT.... phase delay  $\neq$  group delay**

- Difference has been measured to be 1.6%
- Add this to the 'feed forward'

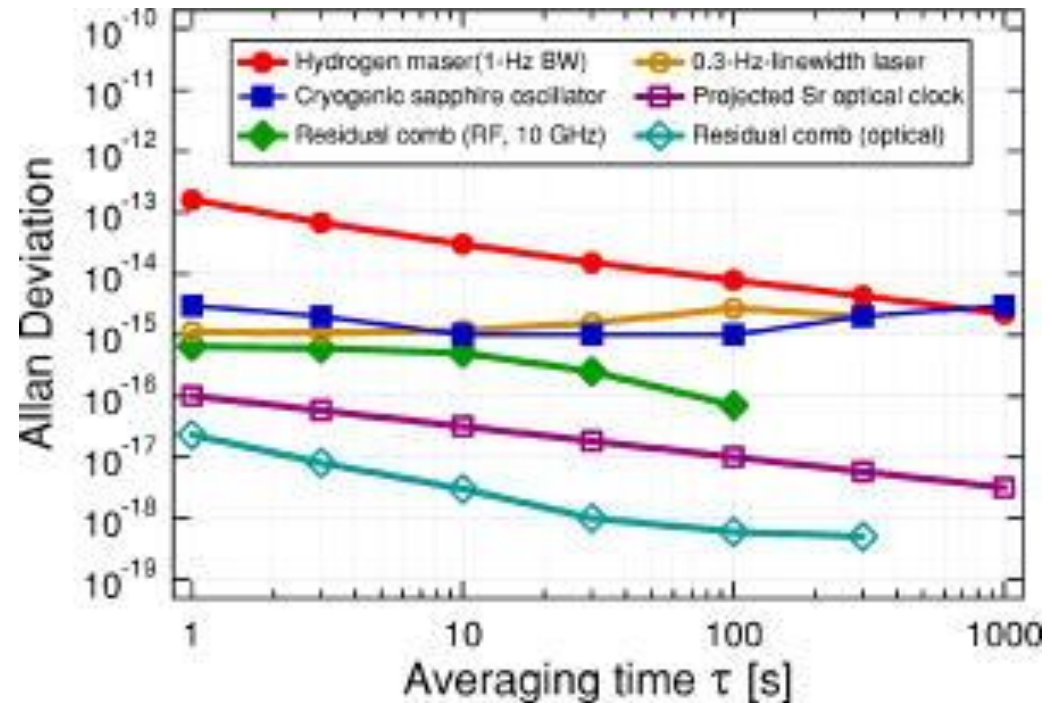


R.Wilcox, FLS12

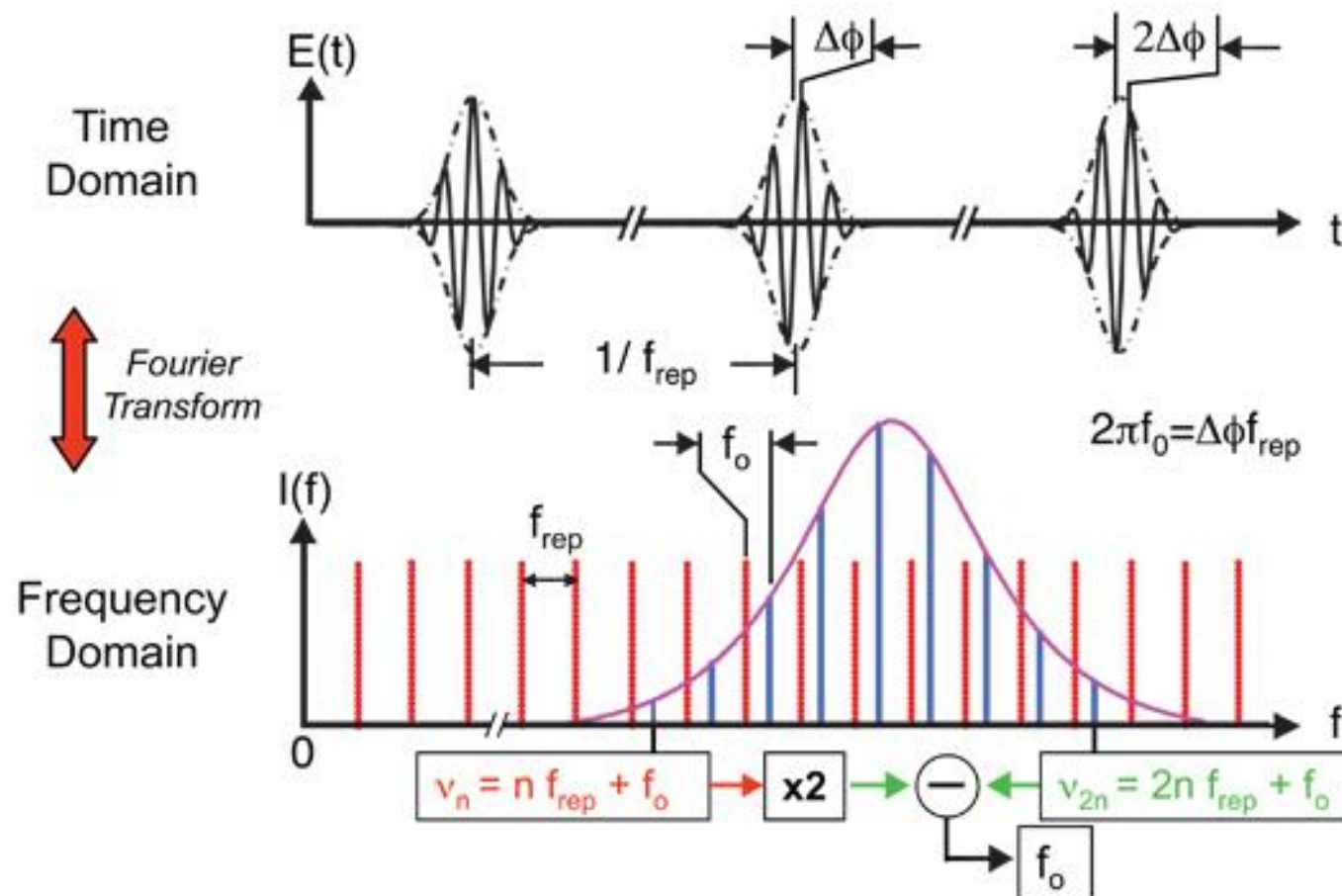
# Laser-to-Laser locking



- Required for:
  - Photoinjector laser
  - Seed lasers
  - Pump-probe lasers
  - Diagnostics
- Can we take advantage of the very best clocks?

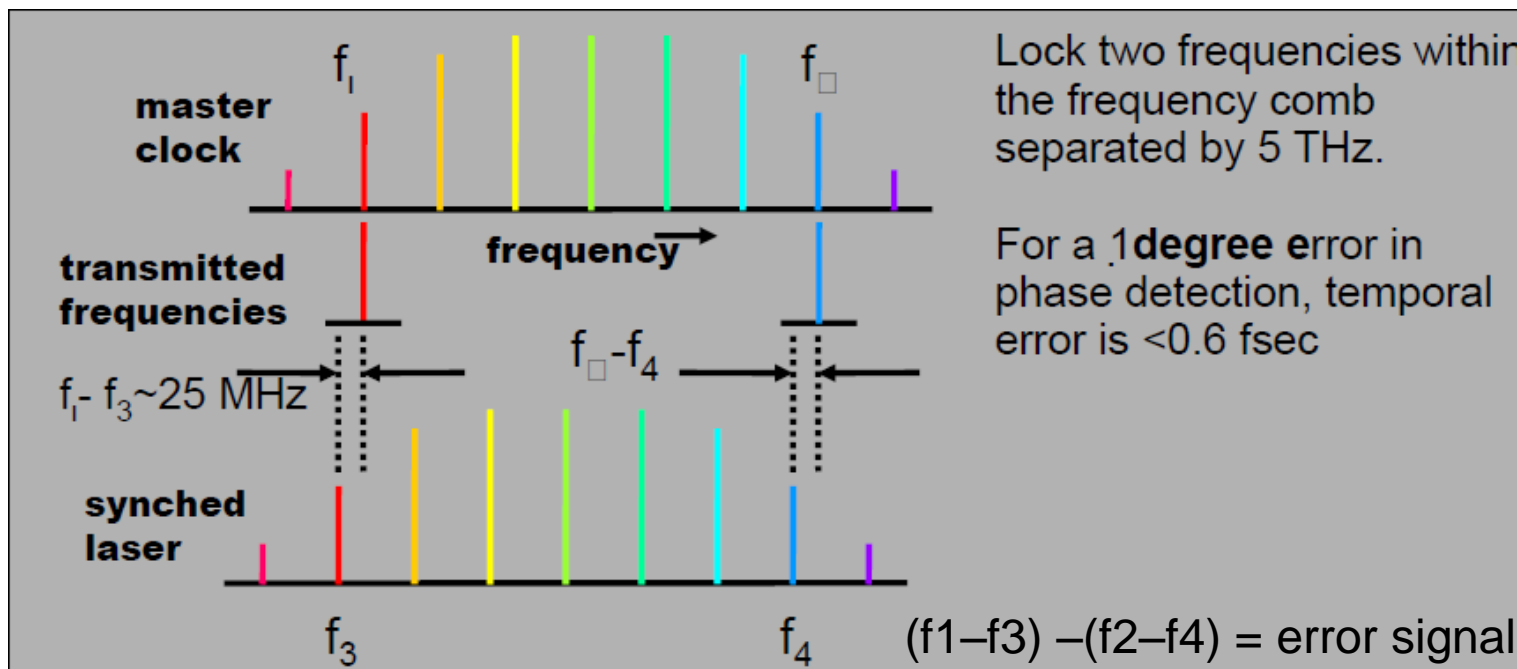


# Optical frequency combs



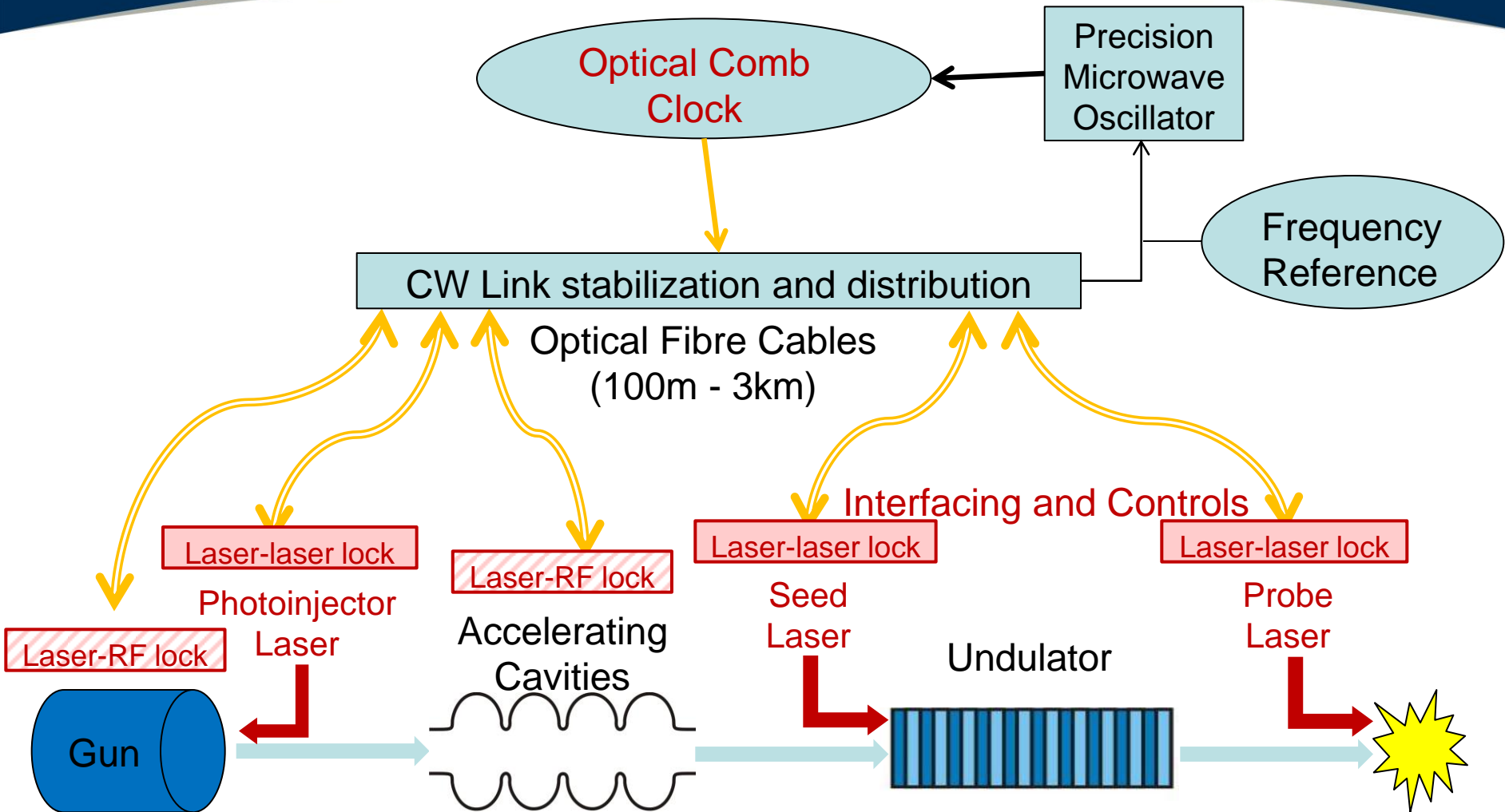


# Laser-to-laser locking

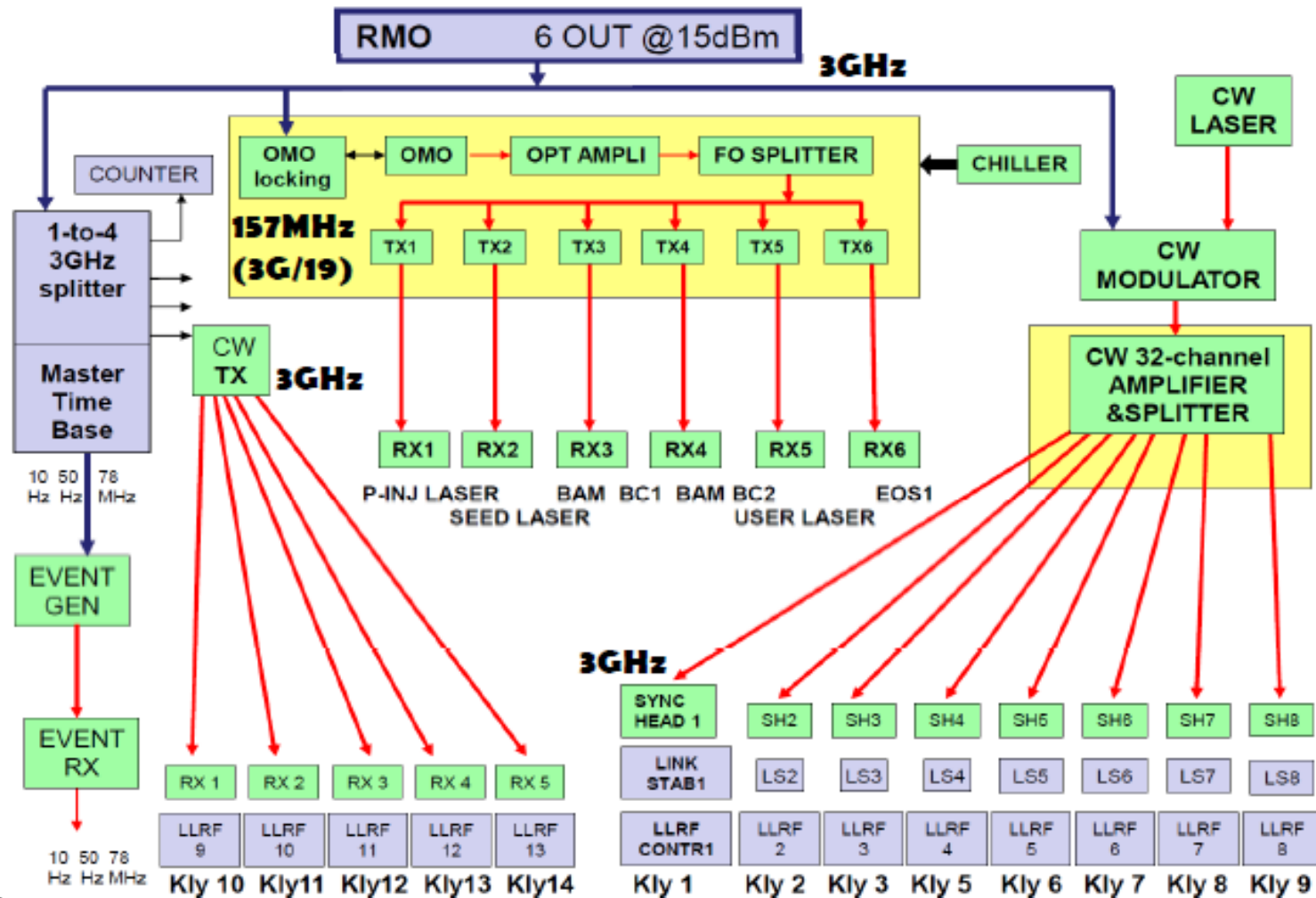


Neither laser needs to be CEP stabilized

# CW timing systems



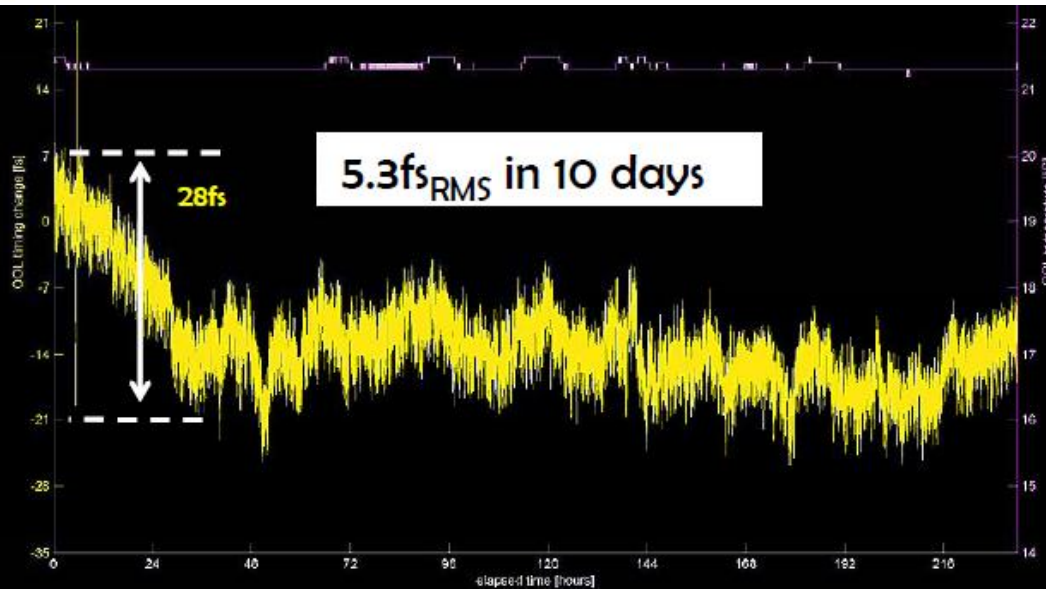
# Hybrid system at Fermi



# Hybrid system at Fermi



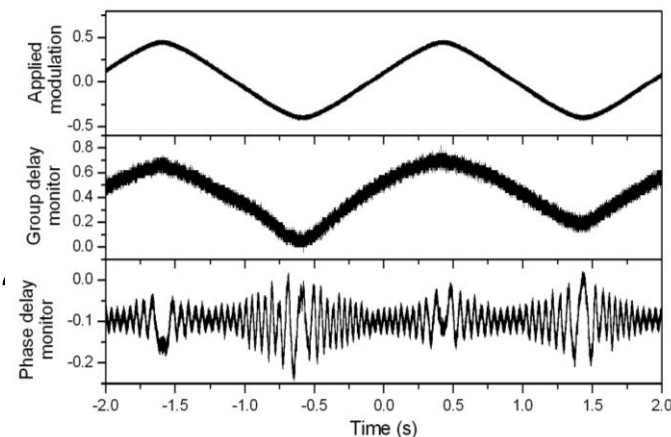
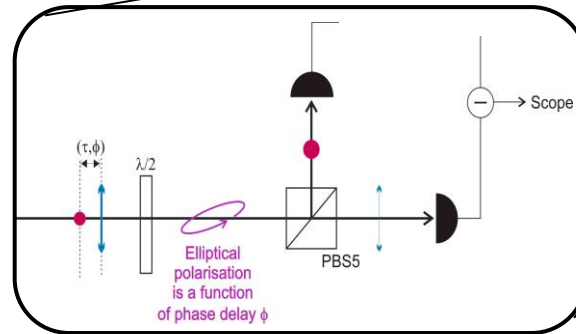
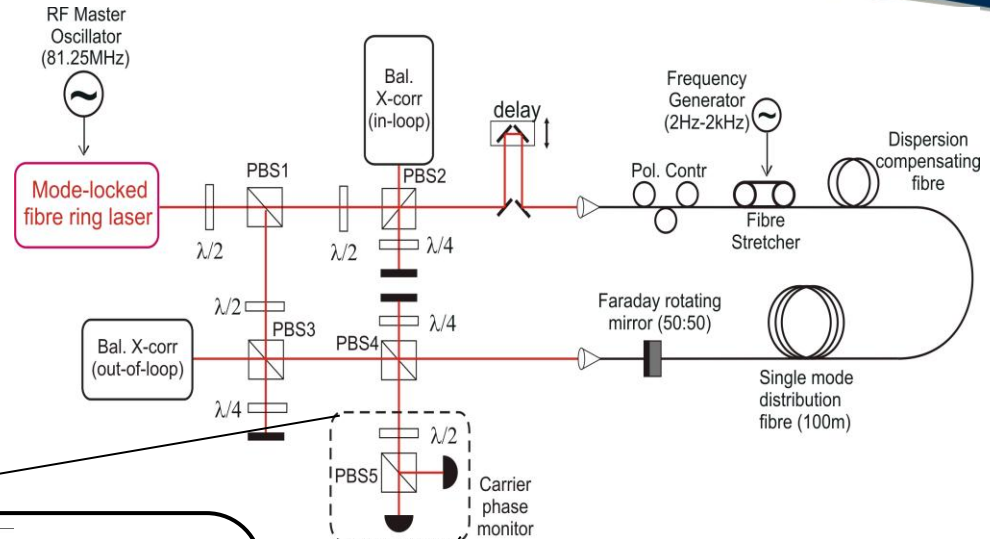
Science & Technology  
Facilities Council



Mario. Ferianis, FEL 2011  
All-optical femtosecond timing system  
for the Fermi@Elettra FEL

- RF timing schemes:
  - Simple distribution, cost effective for small facilities
  - Low resolution, very expensive for large facilities
  
- Pulsed timing schemes:
  - $>5\text{fs}$  resolution, easy to integrate, high bandwidth output, commercially available
  - $>5\text{fs}$  resolution, scalability?
  
- CW timing schemes:
  - Attosecond distribution, long distances
  - Complex, costly, difficult to integrate

- Higher resolution with pulsed inteferometric system
- Integration with electro-optic techniques



- What lengths do we need to reach' (Recall 'same return path' assumption)



Thanks for your attention!

$5 \times 10^{-13}$  stability



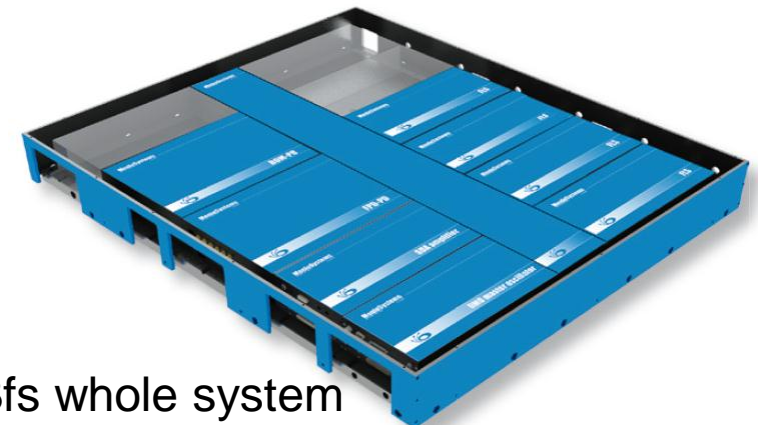
<35 fs rms jitter



em



40fs distribution



5.3fs whole system