

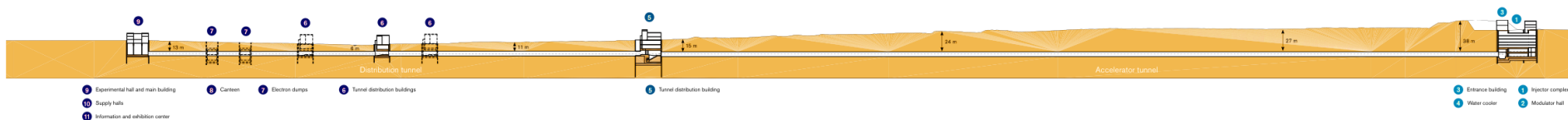
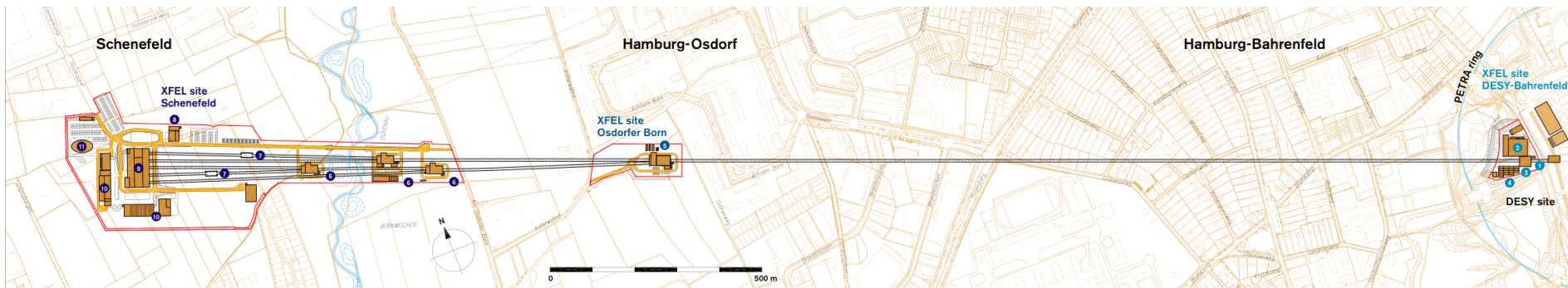
Optical laser requirements, developments and simulations at the European XFEL

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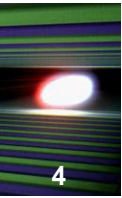


A. The European XFEL project

B. Experimental laser requirements at XFEL

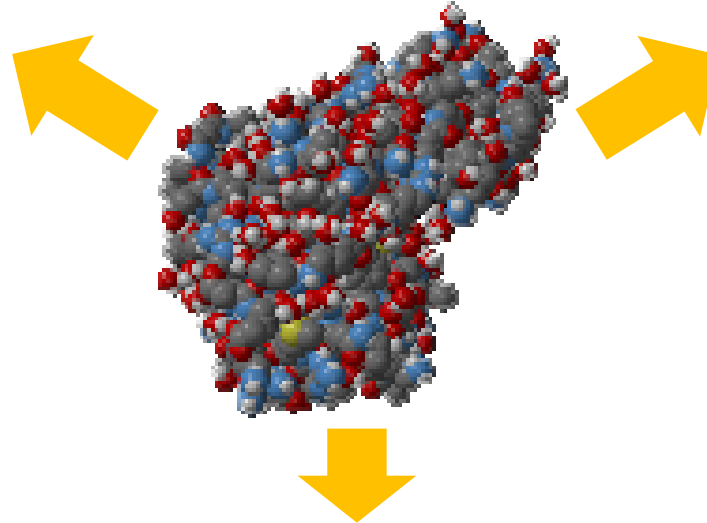
C. Pump-probe laser development and supporting simulations

A. The European XFEL project



Investigation of nano-scale ultrafast dynamic processes and highly excited states of matter require a „different kind of microscope“.

Observation wavelength /
Diffraction limit < desired resolution

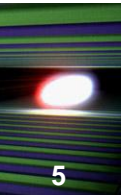


Shutter speed /
Pulse duration < vibration period

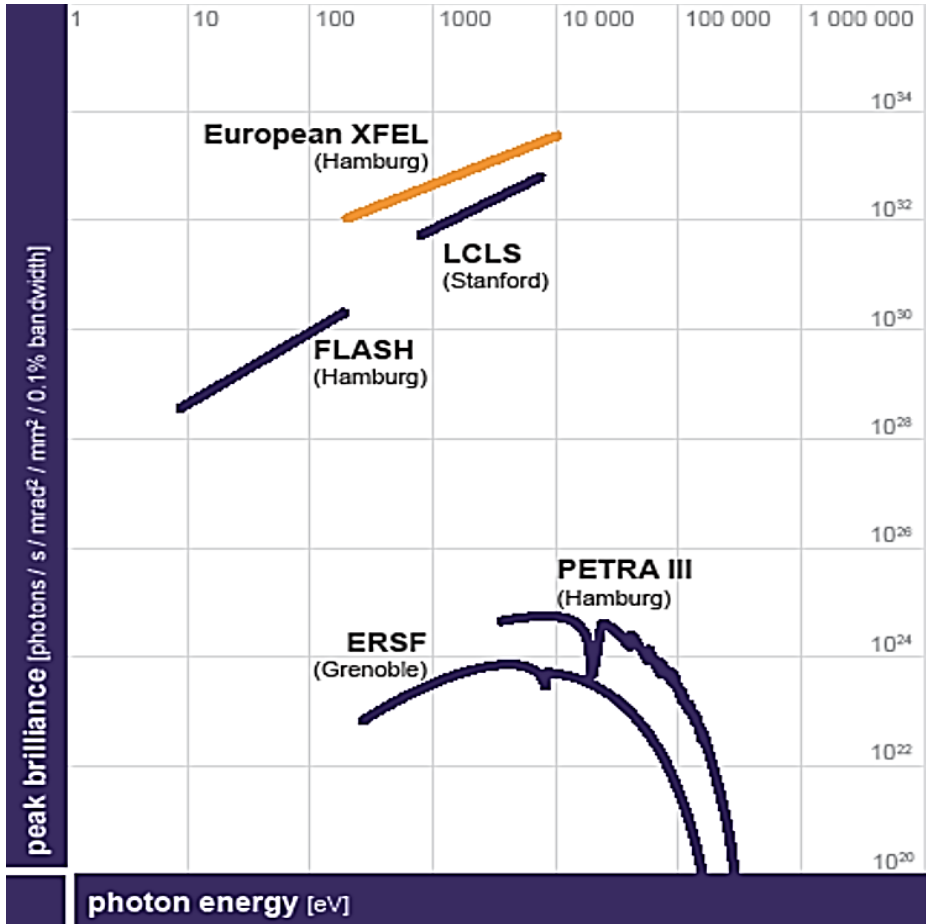
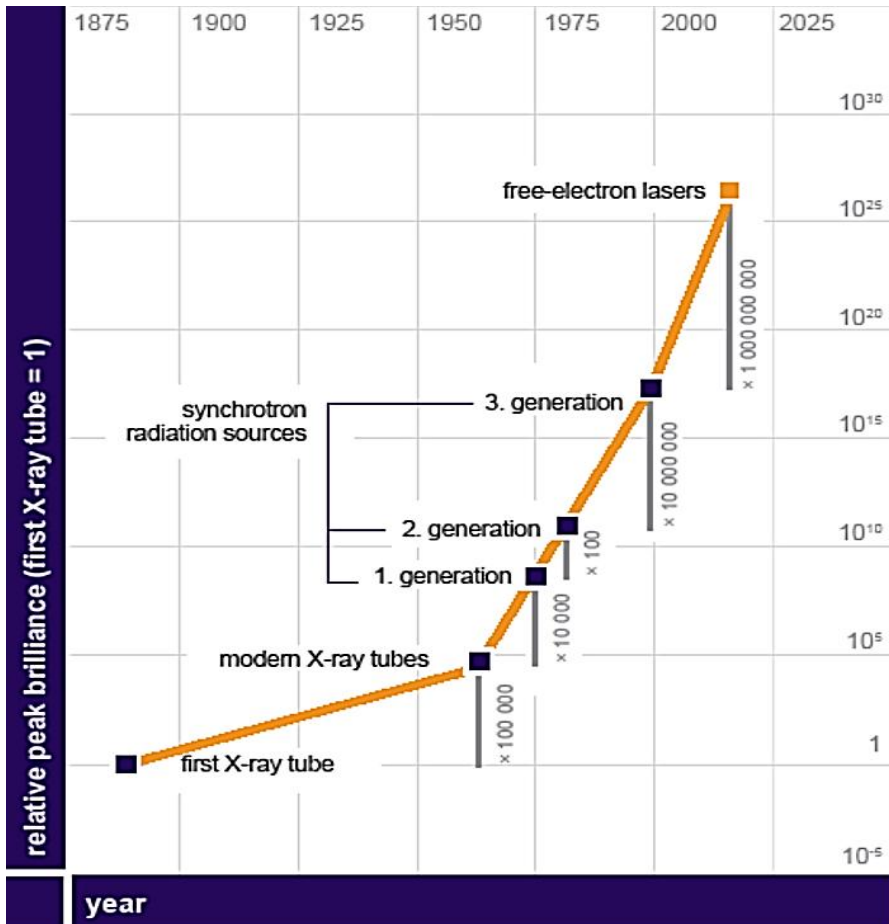
Scattering power /
Single pulse intensity > noise

⇒ X-Ray Free-Electron Laser sources open new scientific possibilities

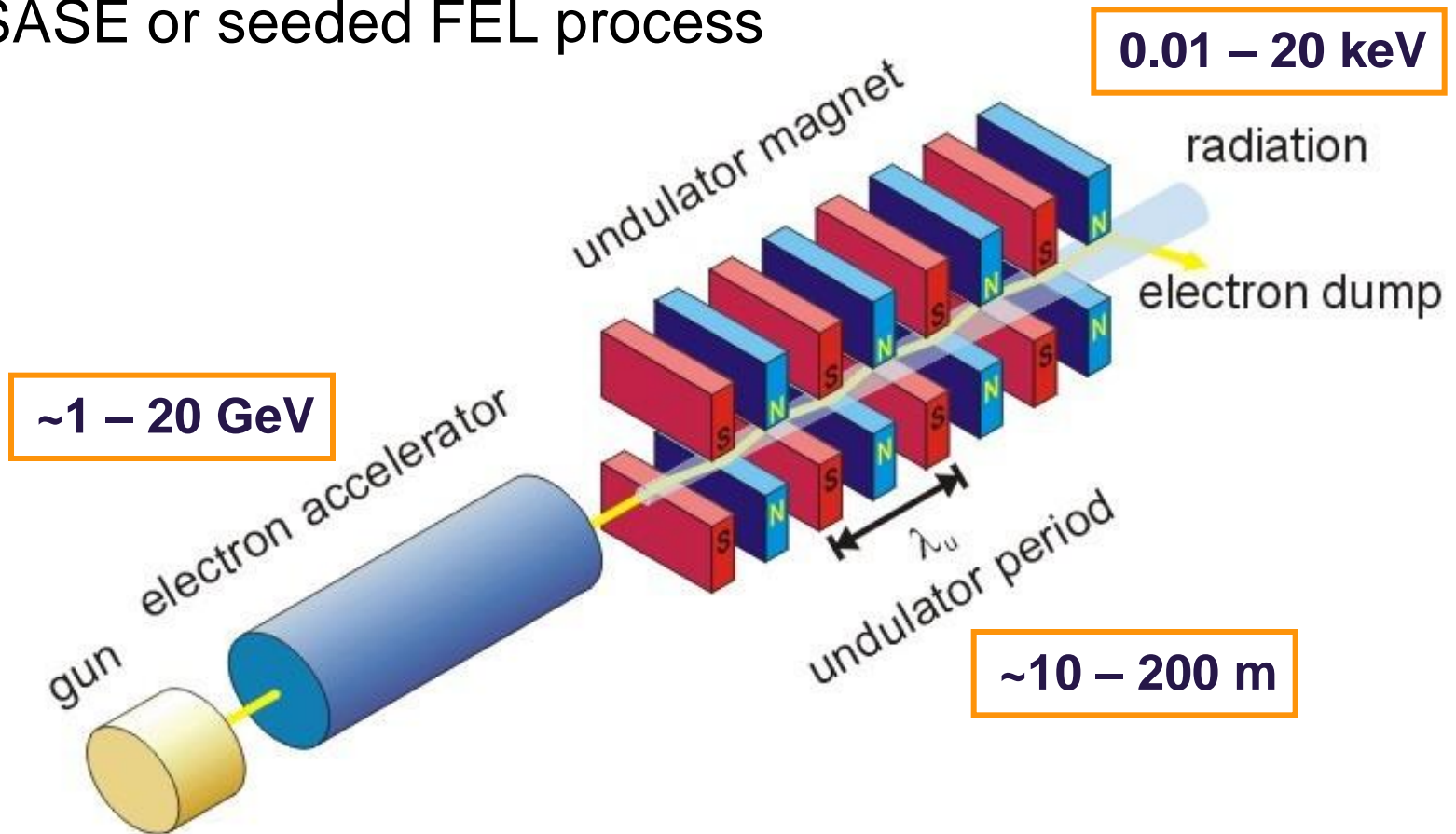
Courtesy T. Tschentscher



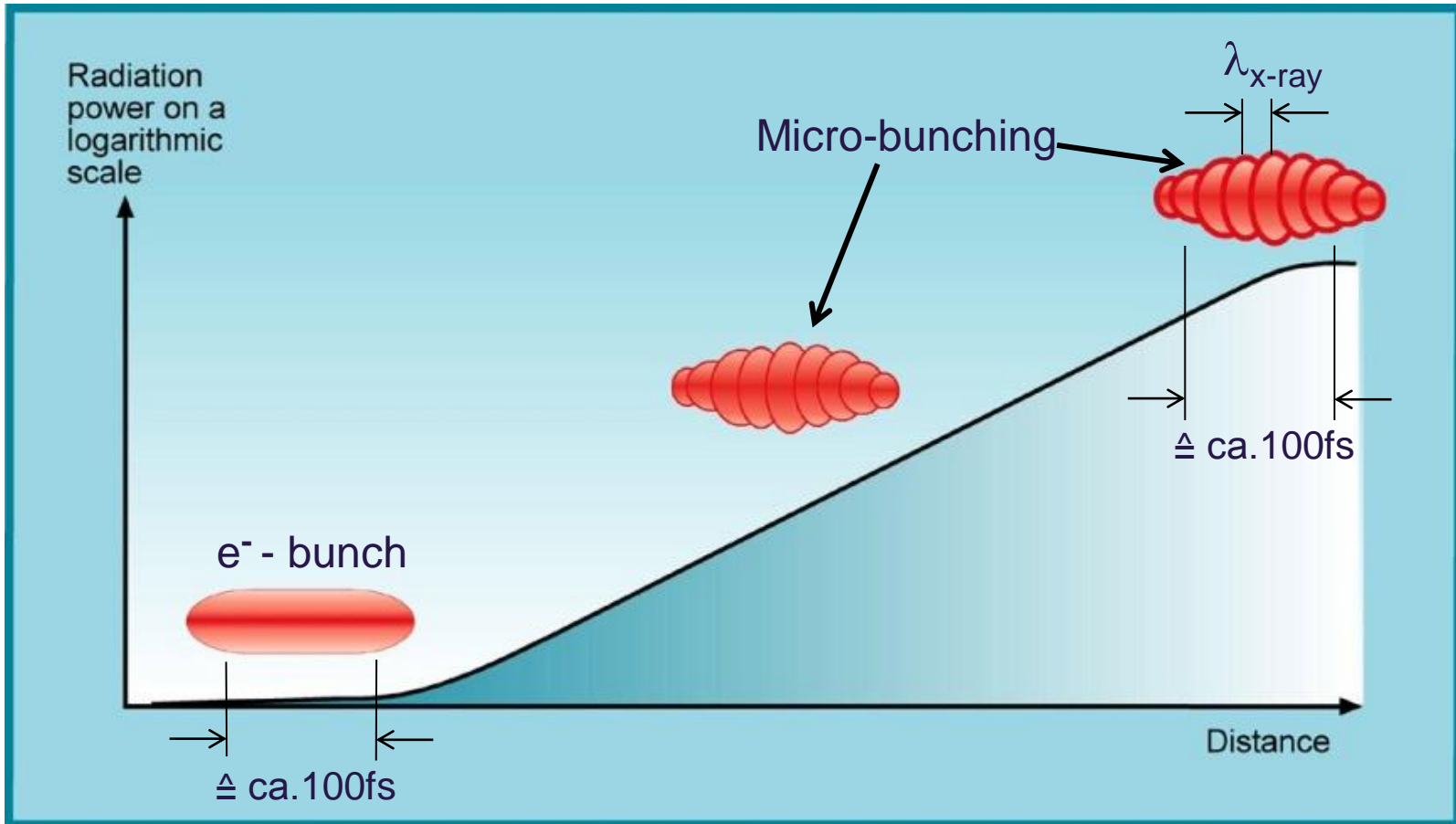
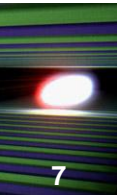
$$\text{Peak brilliance} = \frac{\text{Number of photons}}{\Delta x \Delta x' \times \Delta y \Delta y' \times \Delta \frac{\omega}{\omega_0} \times \Delta \tau}$$



- low emittance high energy linac.
- SASE or seeded FEL process



Courtesy T. Tschentscher



Light generation in the undulator:

SASE - Self-Amplified Spontaneous Emission

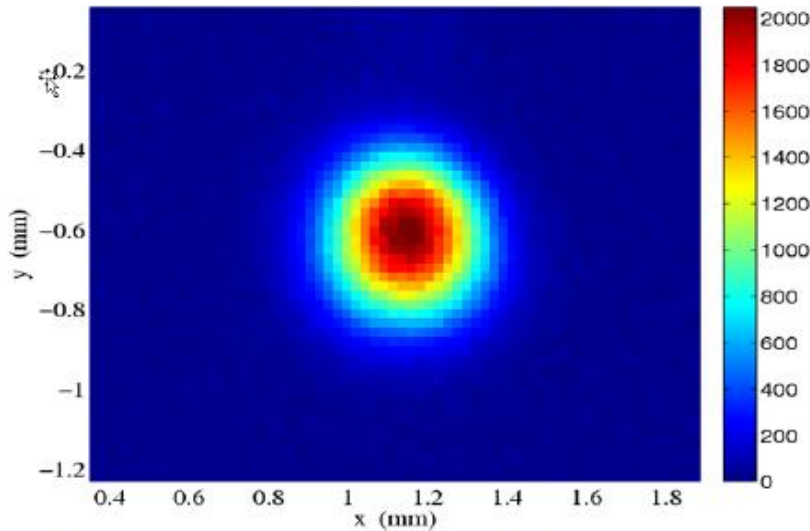
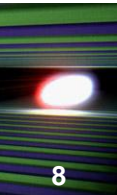
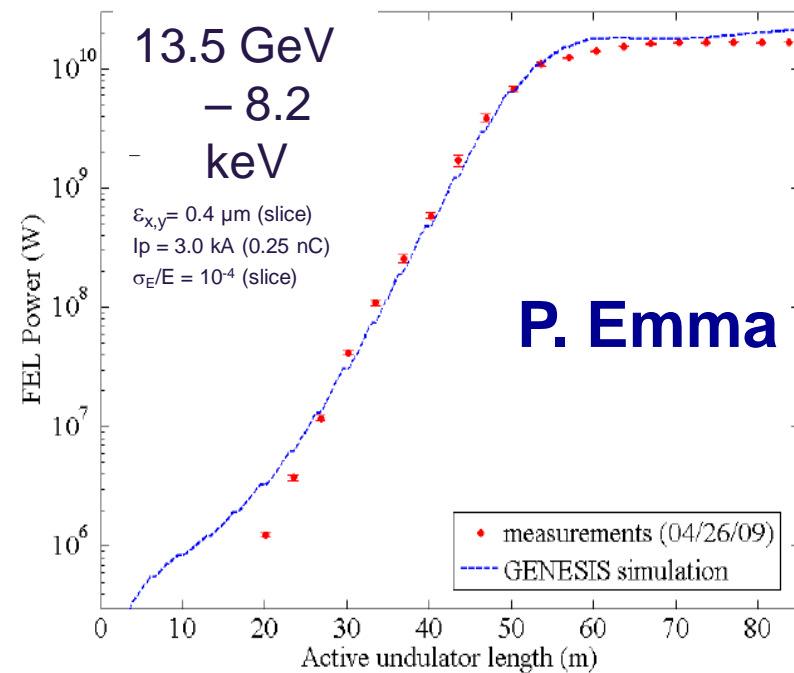
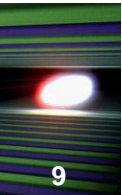


Figure 10: FEL x-rays at 1.5 Å on a YAG screen 50 m after the last inserted undulator (see Table 1 for measured parameters).

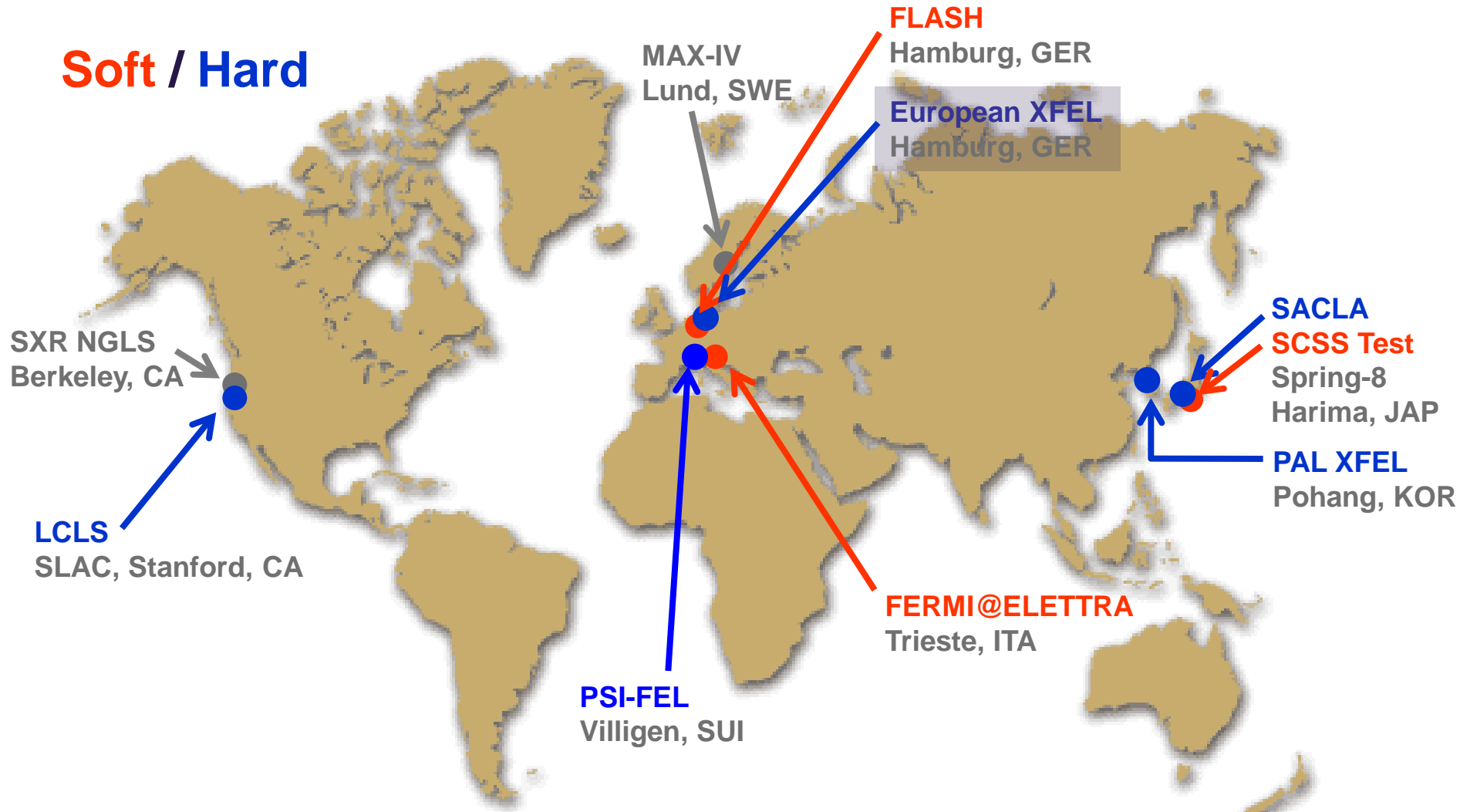
- New short-wavelength SASE record
- First spatially coherent hard x-rays
- **Rep-rate: 60-120Hz**

SASE process very robust at x-ray wavelengths.

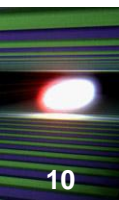




Soft / Hard



Courtesy T. Tschentscher



What is the European XFEL adding in 2016?

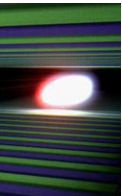
up to 5 beam lines (3 in base line)

simultaneous operation

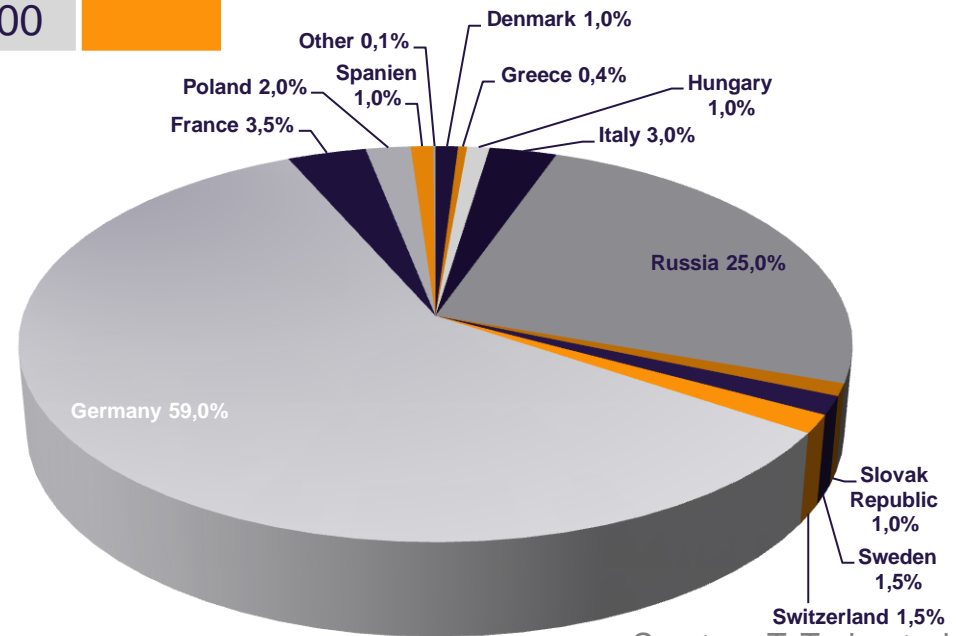
0.25 ... 24keV photon energy

much higher pulse rate: up to 27000 pulses / sec

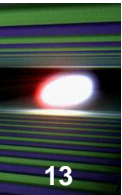
- 12 participating countries
- DESY, Hamburg
 - is host laboratory for the project team
 - responsible for injector and linac
- XFEL GmbH established in fall 2009
 - Currently ca. 150 international staff, final staffing 230
 - responsible for photon beam lines and experiments
- First beam: end of 2015
- XFEL Laser Group established in Nov. 2010
 - currently 6 members, final staffing ca. 10 - 15



Total construction cost	1147	M€*
In-Kind contributions	~500	M€*
External funding (up to 2011)	~6	M€
Staff European XFEL GmbH	~230	
Total staff (incl. DESY staff)	~400	
Start of user operation	2016	
Science users per year	~1000	



Courtesy T. Tschentscher

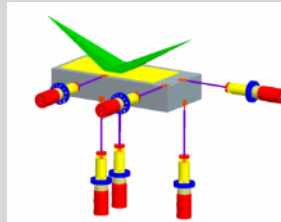


Scientific instruments & ancillary instrumentation

- 6 stations

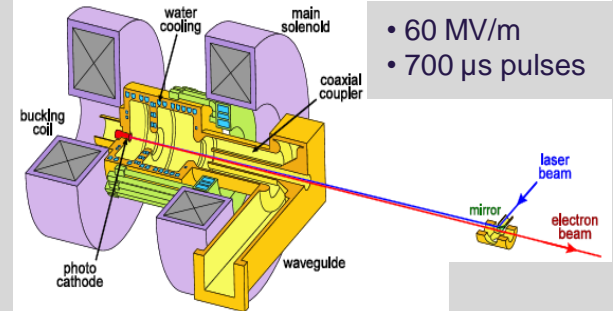


X-ray optics & beam transport



- 3 systems
- ~2000 m
- 1 m mirrors

Low emittance electron injector



Schenefeld

Osdorfer Bohn

Undulator systems



- 3 systems
- >450 m

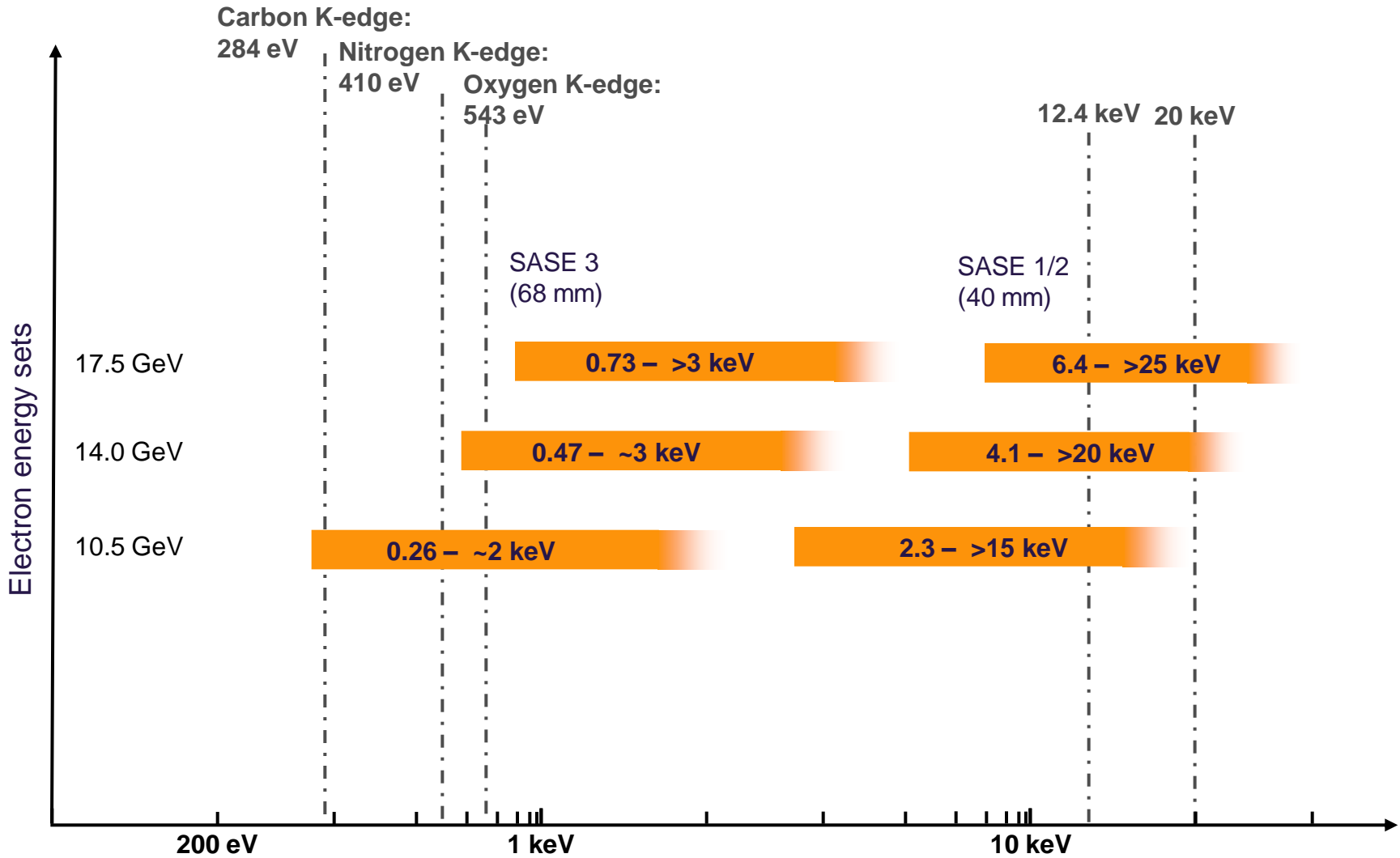
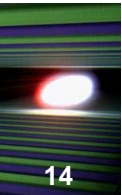
Superconducting electron accelerator

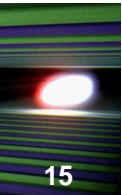
- 23 MV/m
- 800 cavities
- 17.5 GeV



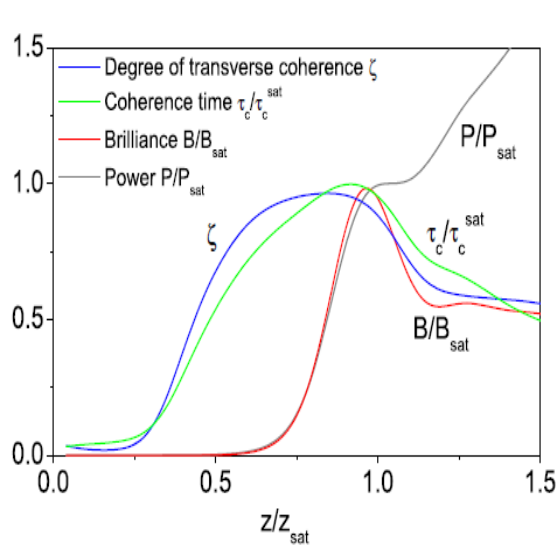
Hamburg -
Bahrenfeld

Courtesy T. Tschentscher

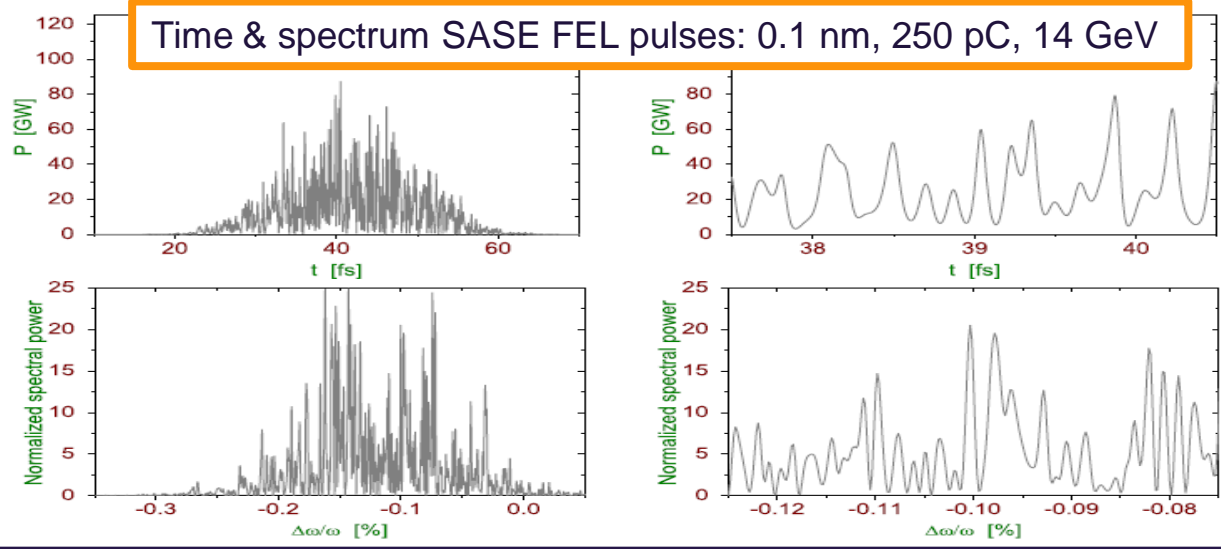


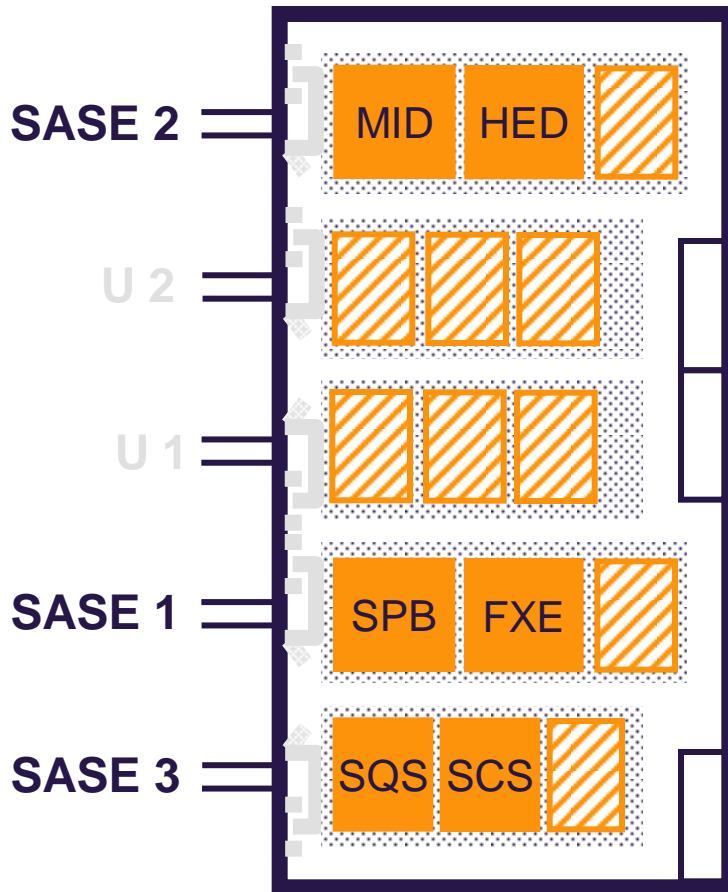


Parameter	Unit	
Photon energy	keV	0.27 – 24
Pulse energies (@saturation)	μJ	0.2 - ~4000
Pulse duration	fs	2 - 107
Power density	W/cm^2	$\sim 10^{13} - 10^{18}$
Spectral bandwidth		$\sim 10^{-3}$
Source size	μm	30 - 60 (100)
Coherence degree		0.4 - 0.96



Time & spectrum SASE FEL pulses: 0.1 nm, 250 pC, 14 GeV





MID Materials Imaging & Dynamics

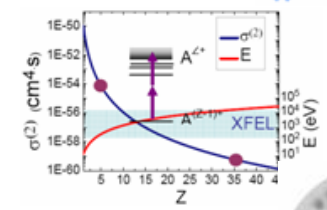
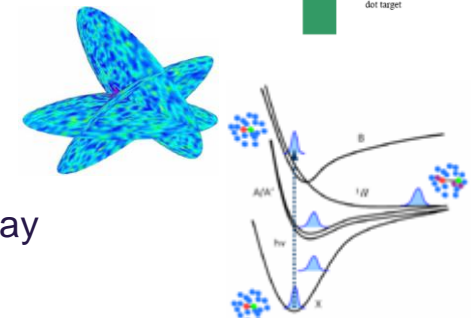
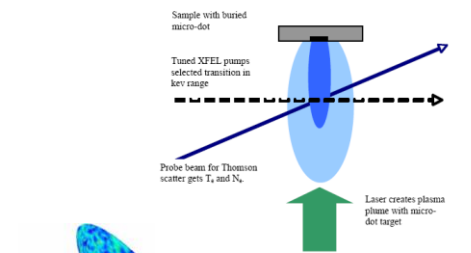
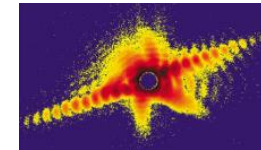
HED High Energy Density Science

SPB Single Particle & Biomolecules

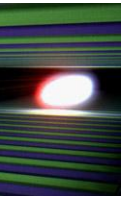
FXE Femtosecond X-ray Experiments

SQS Small Quantum Systems

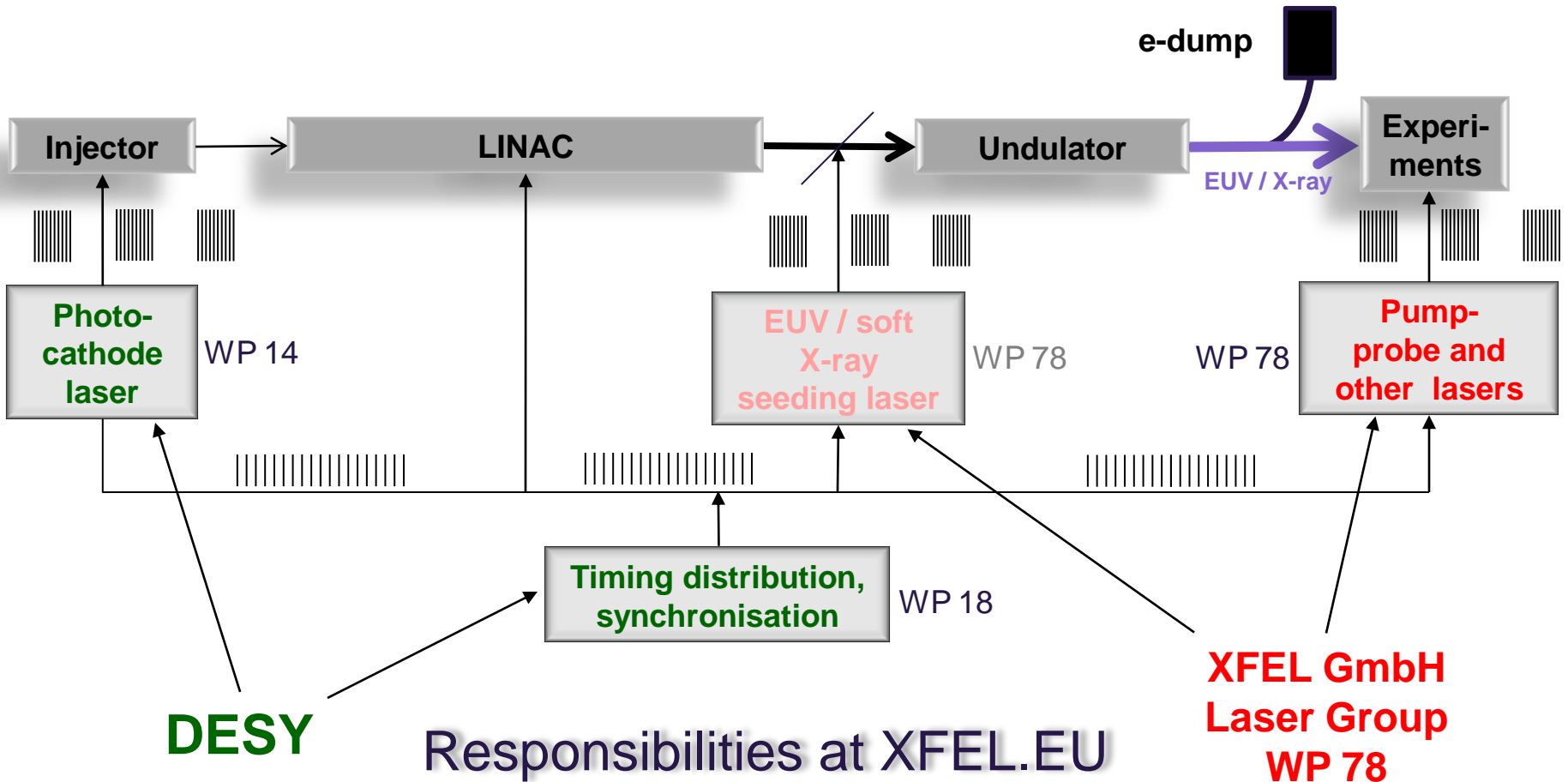
SCS Spectroscopy & Coherent Scattering

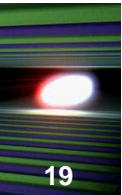


B. Experimental laser requirements at XFEL

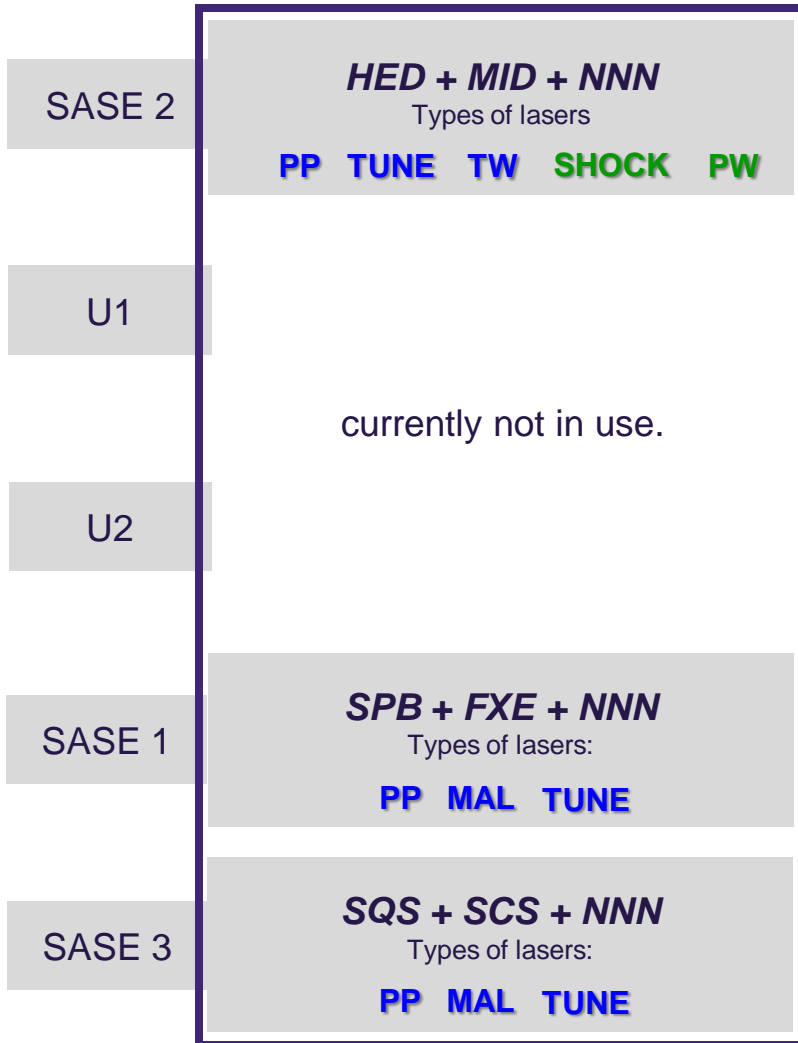


Simplified schematic of a SASE Free-Electron Laser:





Experiment Hall



Types of lasers - *a wish list*:

PP (pump-probe):

→ sub-15...100fs, 0.2mJ, 10Hz *burst*, 0...4.5MHz, 800nm

MAL (molecular alignment):

→ sub-20fs, 3...10mJ, 800nm („kick“)

or

→ 1J, 10Hz, ns („adiabatic“)

TUNE (tunability, freq. conversion):

→ UV...mid-IR, THz (not in hutch, in coll. with instr. sci.)

TW (Terawatt):

→ <30fs, 5-10Hz, 100 Terawatt-class laser, Ti:sapphire

SHOCK (high energy):

→ kJ-class ns-laser

PW (Petawatt):

→ 30fs, 1Hz, Ti:sapphire

or

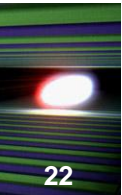
→ 150fs, 1Hz, diode-pumped Yb:CaF₂

- Fixed
- Future (potential User Consortium)

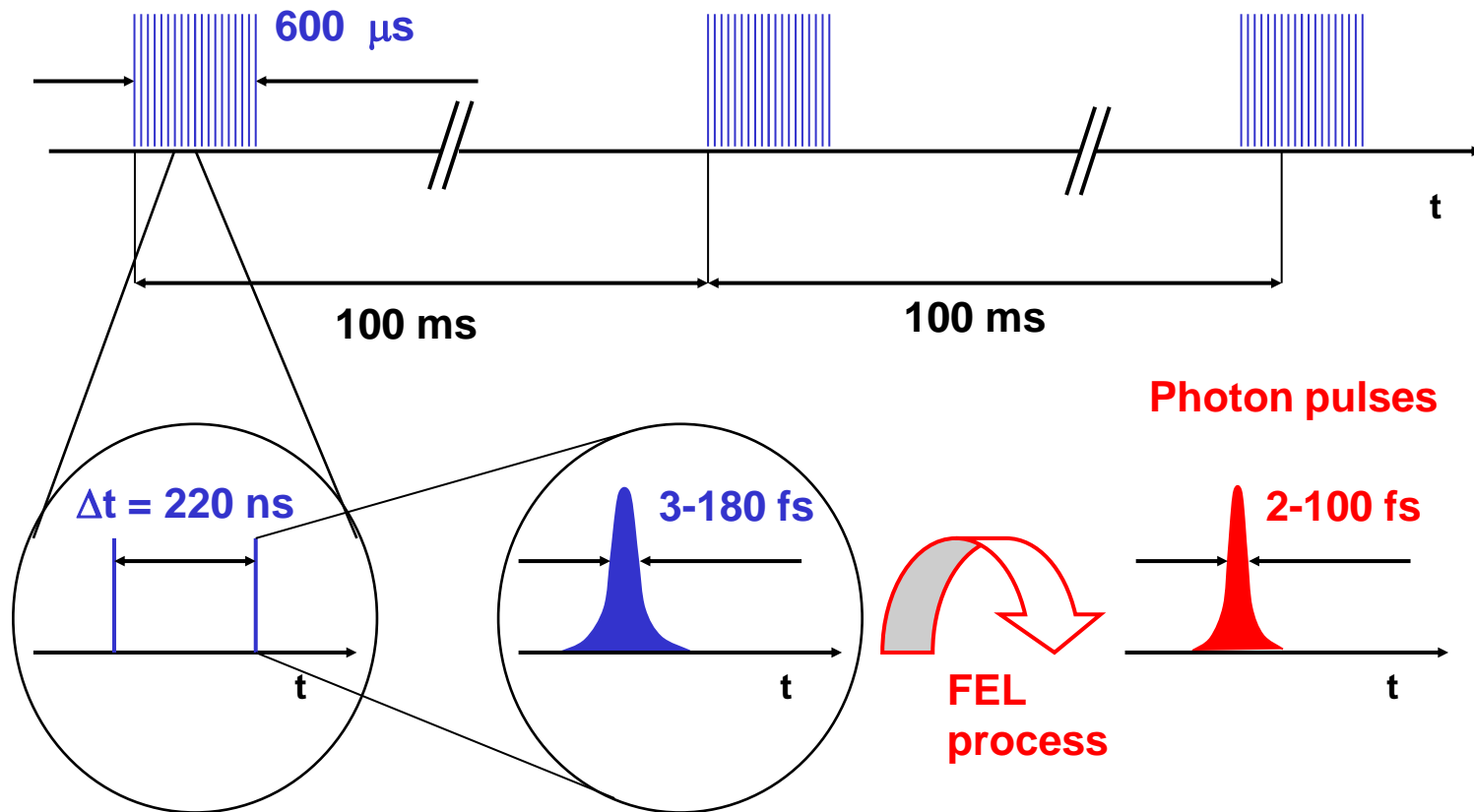
- **100TW-class** laser technology is mature and commercially available from several vendors.
 - ➔ Plan for installation in time with start of operation phase of the XFEL.EU.
- **PW- and kJ-class** lasers are also becoming commercially available and are being installed (e. g. BELLA Ti:sapphire 1.3PW).
 - ➔ Future of these efforts at XFEL.EU depends on external user consortium.
 - ➔ Due to the size of these lasers, an additional external building will be required.
- **PP-laser will require major development effort, no commercial system is available.**
 - ➔ 10Hz burst operation with up to 4.5MHz intra-burst rep-rates.
 - ➔ mJ-class pulse energies, shorter and longer pulses.
 - ➔ Attempt to also achieve specs useful for MAL.
- **Tunability** will have to be derived from PP-laser and adapted to needs of instruments and users.
 - ➔ In cooperation with instruments scientists.

high flexibility
AND
high uptime

C. Pump-probe laser development and supporting simulations

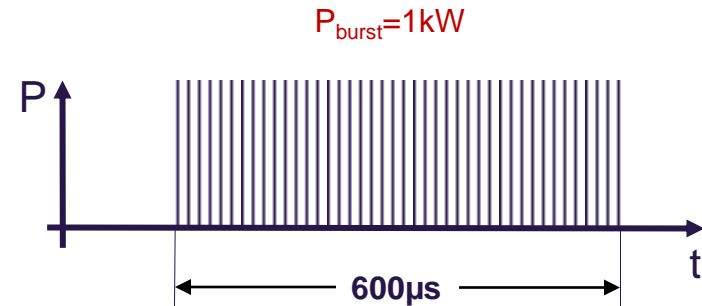


Electron bunch trains (with up to 2700 bunches à 20-1000 pC)



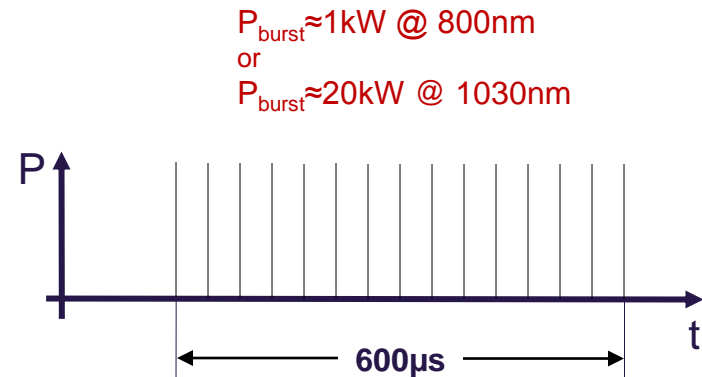
High-rep-rate operation (PP-mode):

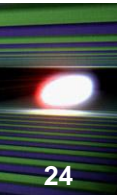
- 10Hz **burst**, 0.6% duty cycle,
- 15 ... 100fs,
- 1 ... 4.5MHz intra-burst, „PoD“,
- 1...0.2mJ per pulse, ca. 800nm



Low-rep-rate operation (MAL-mode):

- 10Hz **burst**, 0.6% duty cycle,
 - 200kHz intra-burst, „PoD“
 - sub-20fs, >3mJ per pulse, 800nm.
- or
- ps or ns, $\approx 0.1J$ per pulse, 1030nm.

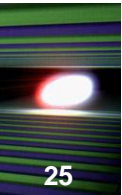




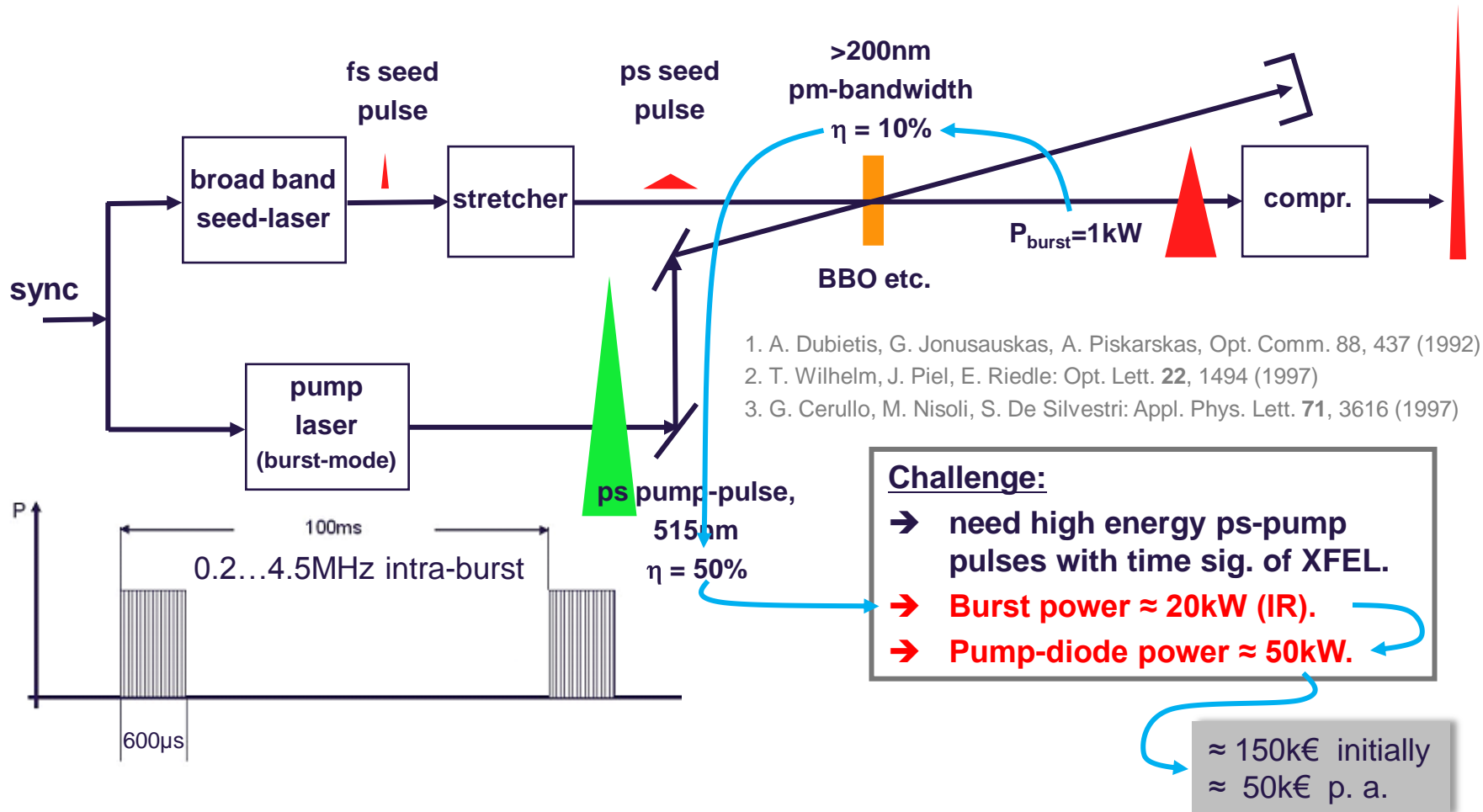
	Ti:Sapphire		OPCPA	
Operation mode	Cryo, staged multi-pass amps, ns-sync-pumped, burst		Non-collinear, staged single pass amps, ps-sync-pumped, burst	
Average power scaling	XFEL duty cycle is 1%, i. e. 10W, therefore no problem	😊	No problem	😊
15fs capable	borderline	😐	yes	😊
Gain per length	low	😞	high	😊
Thermal transients	Cryo-management	😐	negligible	😊
Pump efficiency	≈ 20%	😐	≈ 20%	😐
Flexibility	low	😞	high	😊
Misalignment sensitivity	medium	😐	High angular and temporal	😞

➔ Require **5-10kW burst-power green ns/ps pump lasers** for synchronous pumping in both cases.

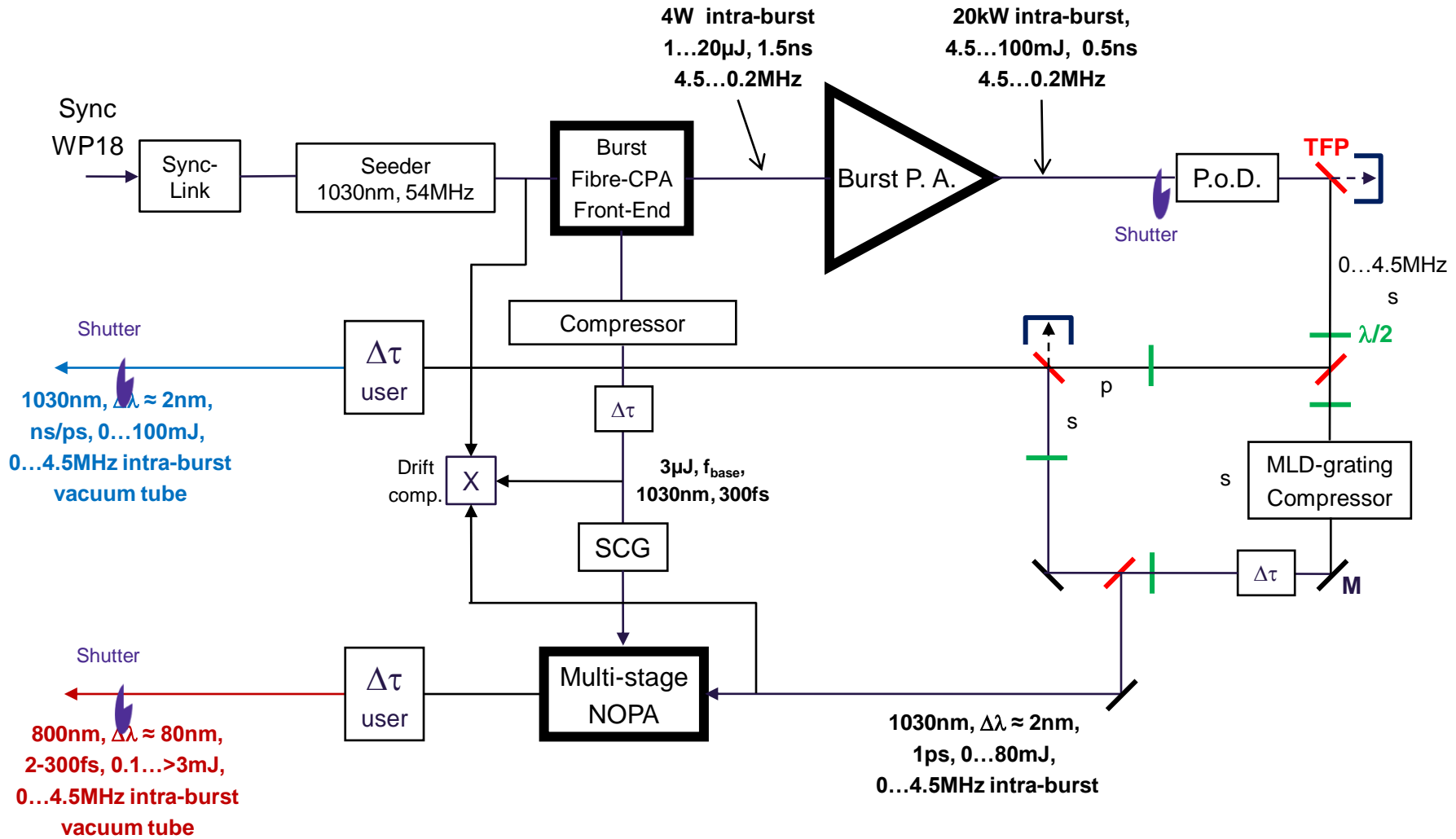
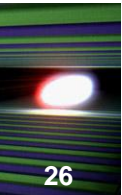
Choose OPCPA in non-collinear configuration: NOPA



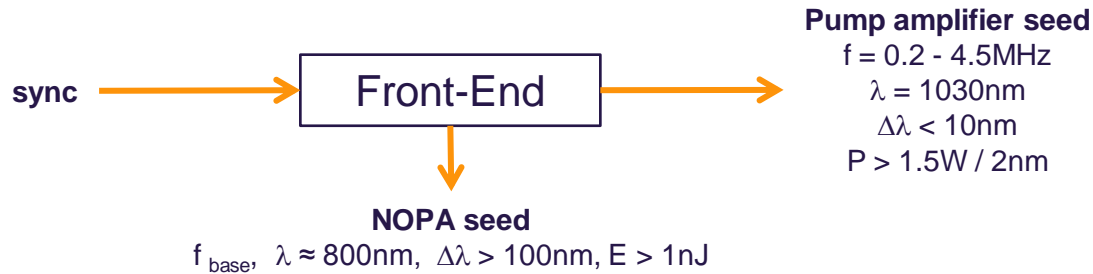
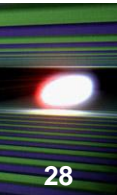
NOPA ⇒ Non-collinear Optical Parametric Amplifier



Pump-Probe laser conceptual layout

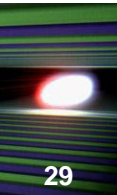


Burst-mode 1030nm CPA fibre front end

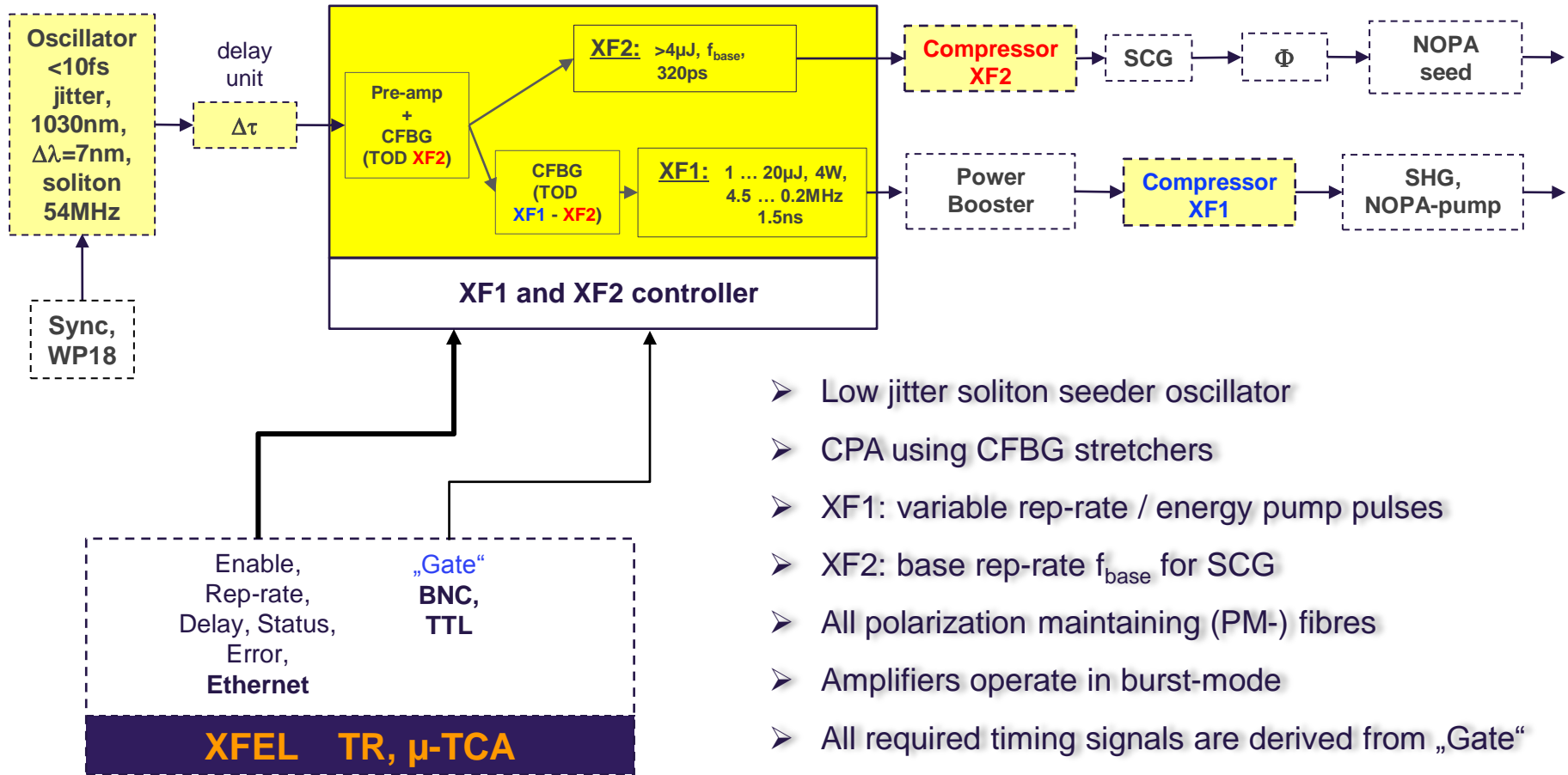


NOPA seed	Pros	Cons
Ultra-broadband TiSa oscillator, $\Delta\lambda \approx 300\text{nm}$ for 800nm and 1030nm	- „all-in-one“ oscillator	- poor long-term stability
Standard TiSa oscillator, $\Delta\lambda \approx 100\text{nm}$ + fibre amp and Raman-Soliton in PCF for 1030nm	- only one oscillator	- complexity of Raman-Soliton setup
Yb-oscillator, 1030nm, $\Delta\lambda < 10\text{nm}$ + Standard TiSa, $\Delta\lambda \approx 100\text{nm}$	- jitter only depends on TiSa	- uneconomical
Yb-oscillator, 1030nm, $\Delta\lambda < 10\text{nm}$ + supercontinuum in YAG, $\Delta\lambda \approx 100\text{nm}$	- one oscillator with proven longterm stability and low jitter - efficient and economic	- unknown, if jitter of compressed supercontinuum is worse than that of oscillator.

Pump amplifier seed	Pros	cons
Yb regenerative amplifier	- energy scaling at constant power is easy, moderate CPA	- drift due to long length - 4.5MHz switching ...
Yb rod-type-fibre amplifier	- envisaged energy scaling at constant power is easy - no rep-rate limitation	- bulk-like, not all-in-fibre - need substantial CPA
Yb all-fibre amplifier	- high thermomechanical stability - no rep-rate limitation	- energy scaling at constant power is not straight forward, need substantial CPA.

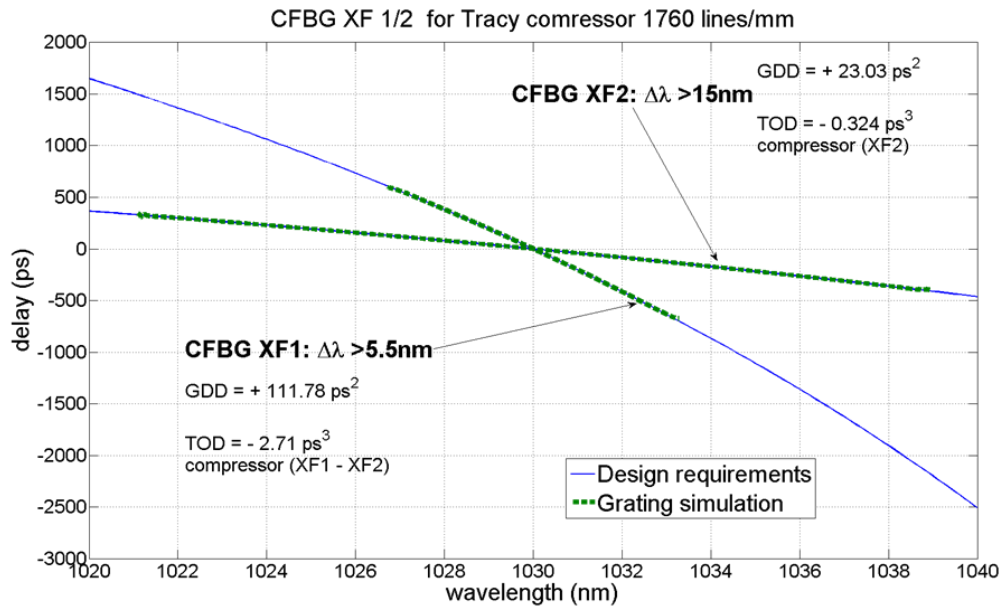
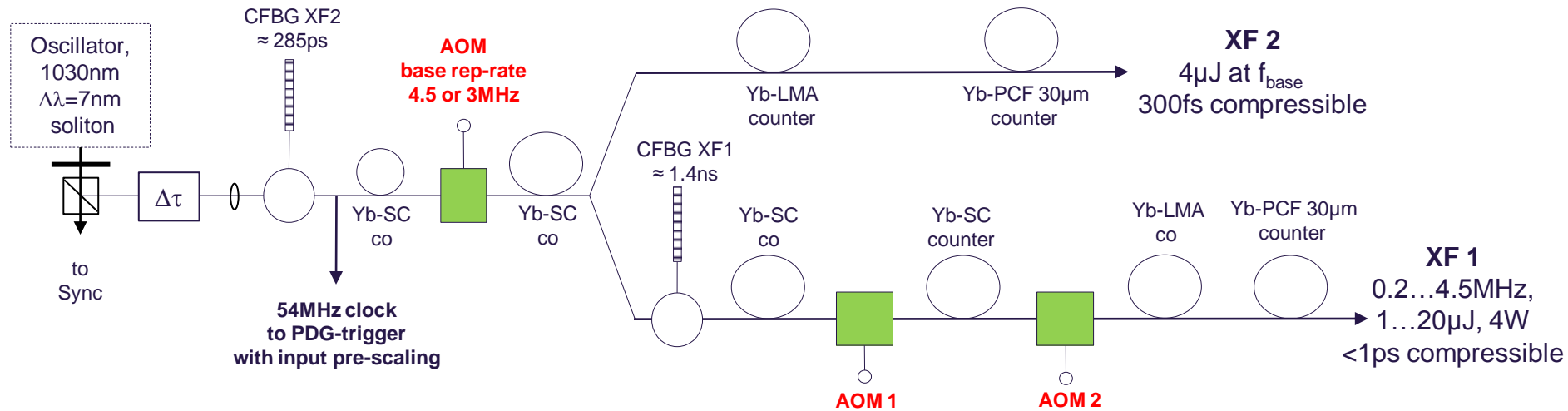
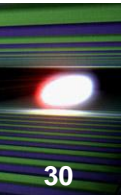


All-fibre

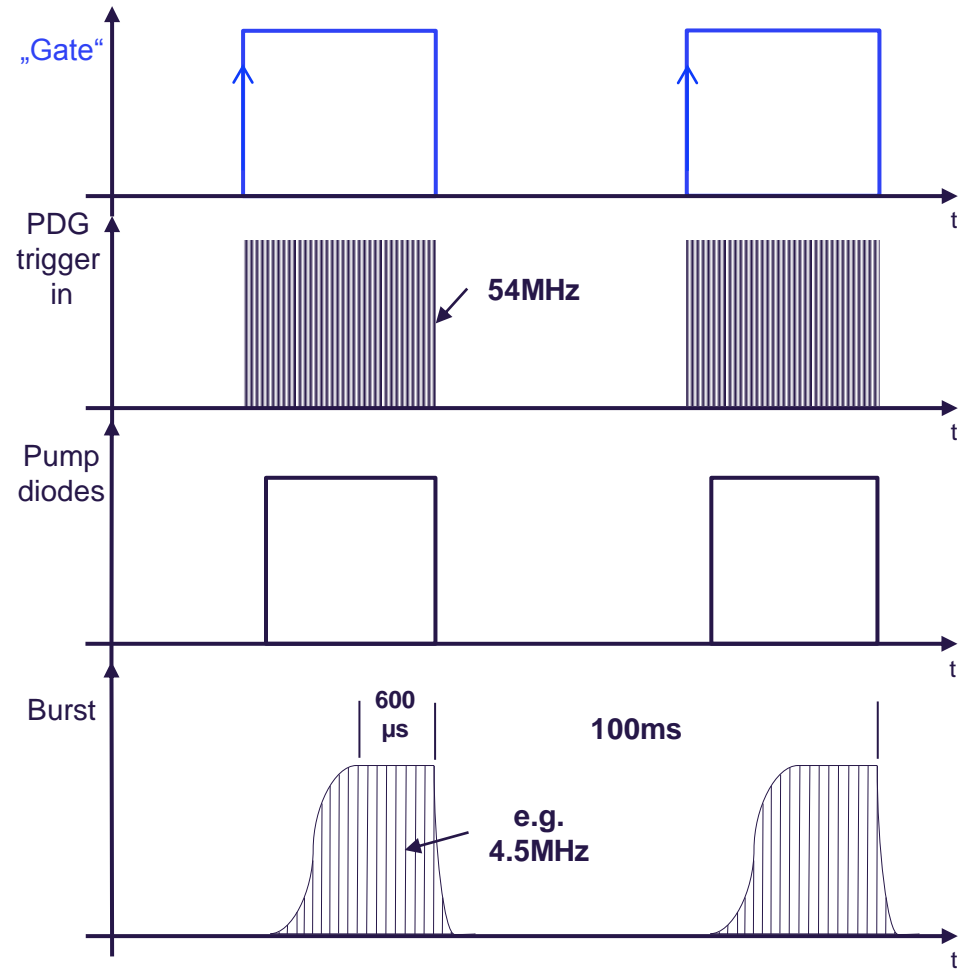
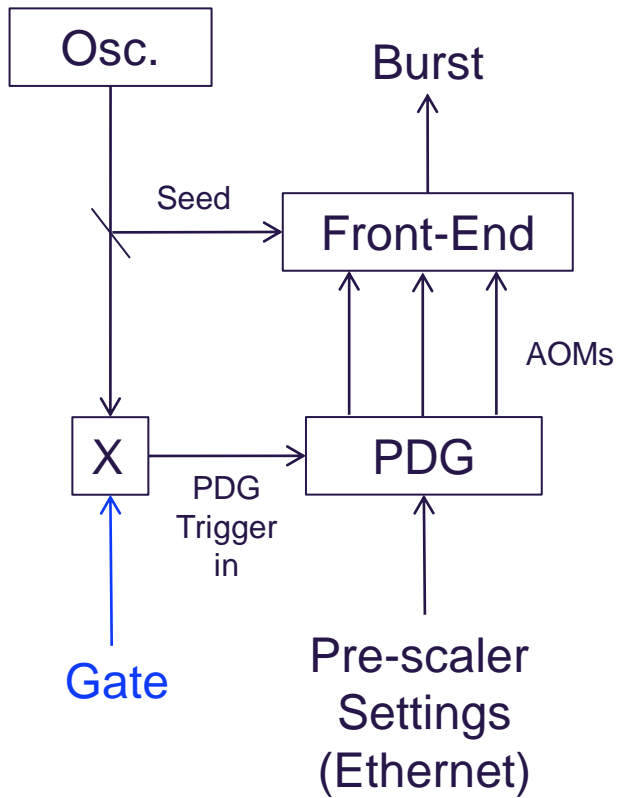
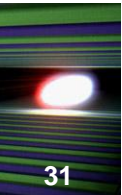


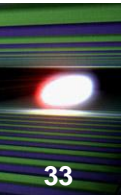
- Low jitter soliton seeder oscillator
- CPA using CFBG stretchers
- XF1: variable rep-rate / energy pump pulses
- XF2: base rep-rate f_{base} for SCG
- All polarization maintaining (PM-) fibres
- Amplifiers operate in burst-mode
- All required timing signals are derived from „Gate“

Burst-mode 1030nm CPA fibre front-end



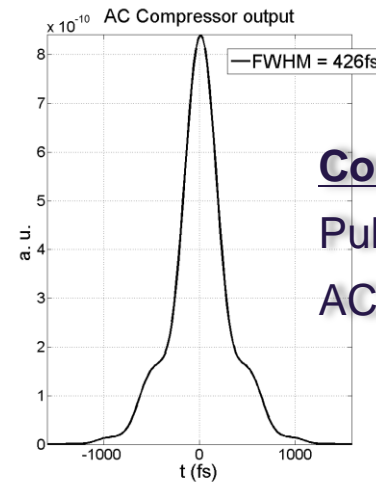
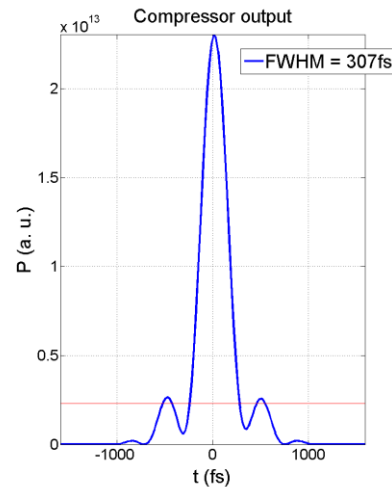
- XF2 base rep-rate of 4.5 and 3MHz possible.
- Various XF1 rep-rates through AOM1 and AOM2 plus gain adjustments.
- Apodized PM-CFBGs with GD conjugate to compressors.





Typical case (long PCF, some gain narrowing):

Pulse energy: 3.3 μ J
 Bandwidth: 6nm
 Rep-rate: 4.5MHz
 B-integral: 3.5

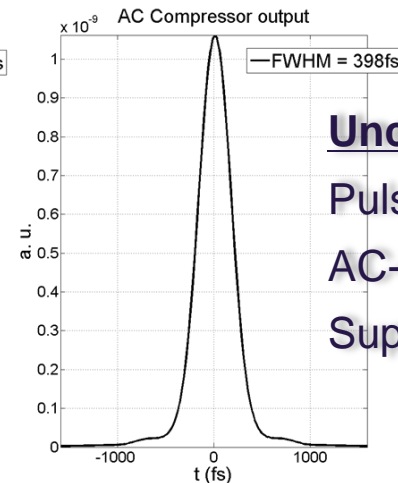
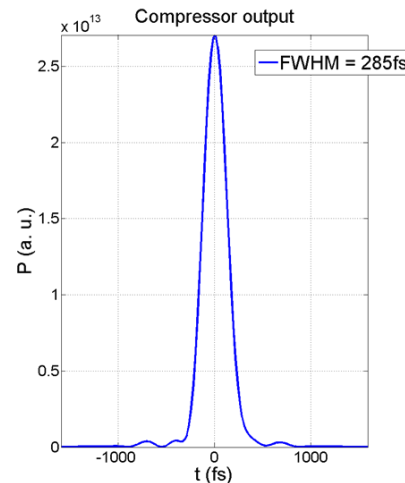


Compensated FOD:

Pulsewidth: 307fs
 AC-width: 426fs

Limiting factors:

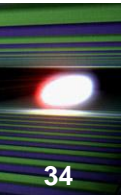
- SPM
- Gain narrowing
- Poor FOD control



Uncompensated FOD:

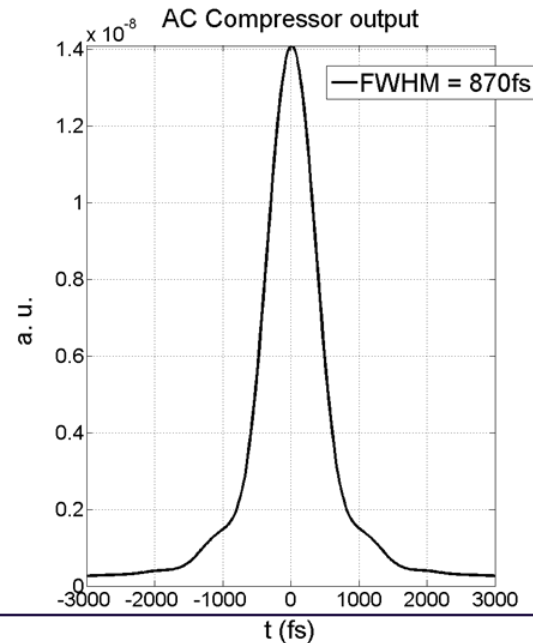
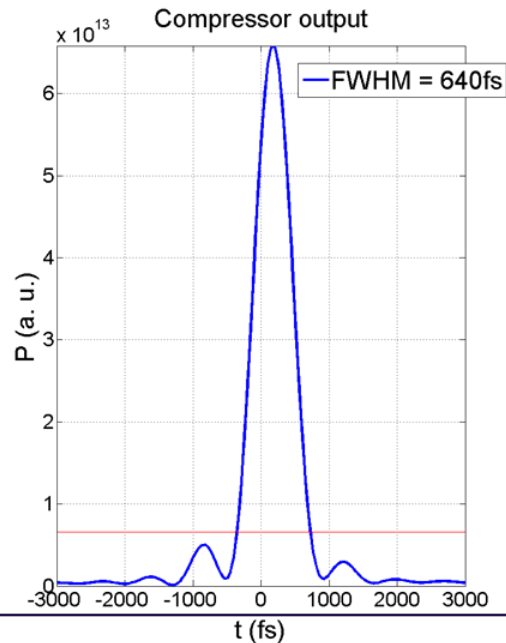
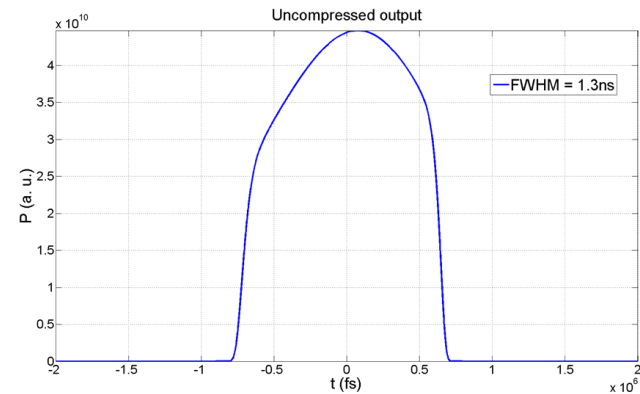
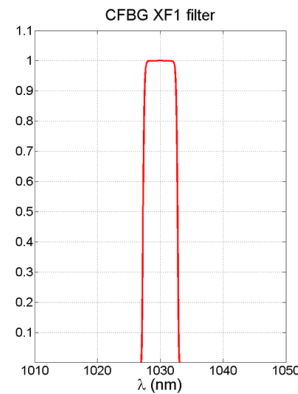
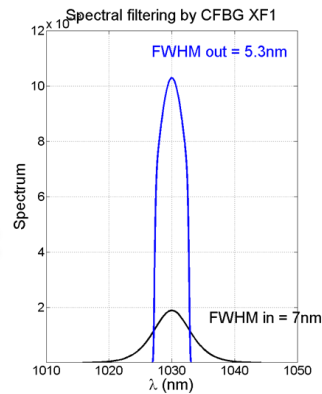
Pulsewidth: 285fs
 AC-width: 398fs
 Suppr. SPM-satellites.

Similar to TOD:
 S. Zhou et al,
 Opt. Expr. 13, 4869, (2005).



Typical worst case (highest pulse energy):

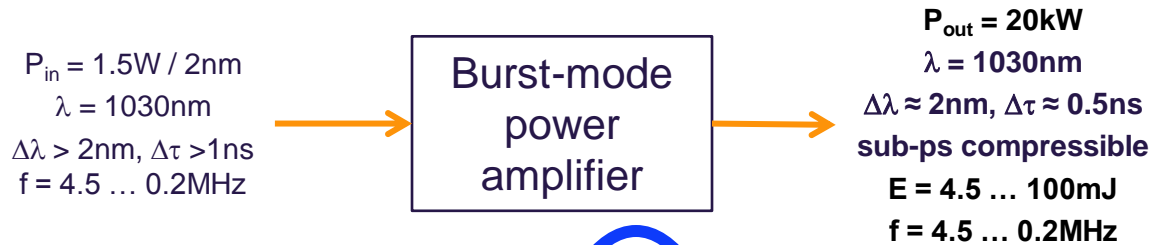
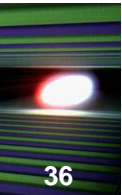
Pulse energy: 20 μ J
 Bandwidth: 5nm
 Rep-rate: 200kHz
 B-integral: 11.8



Limiting factors:

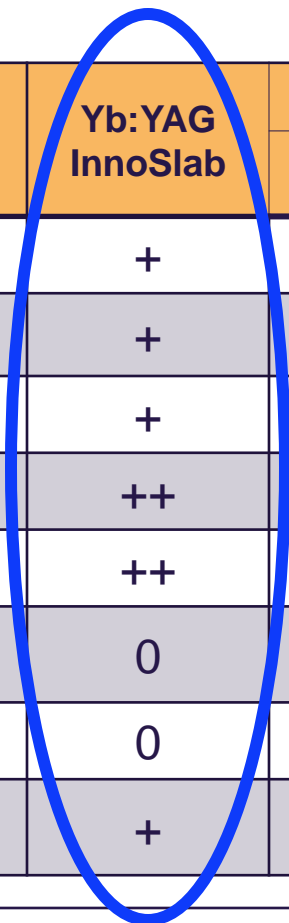
- SPM
- CFBG bandwidth

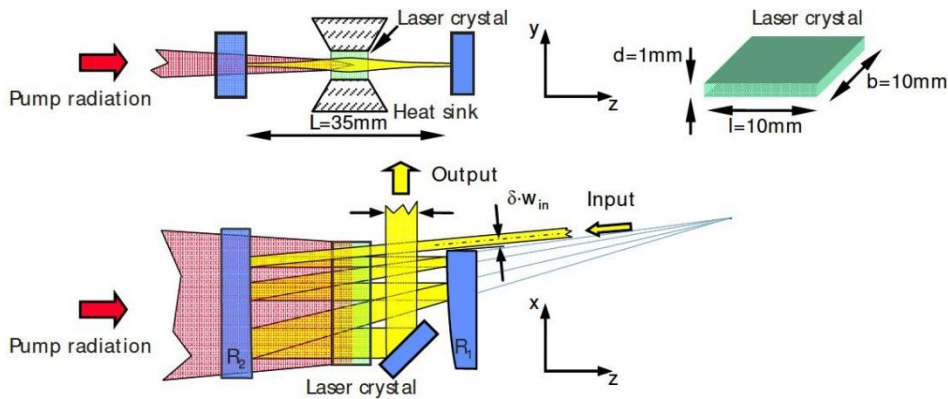
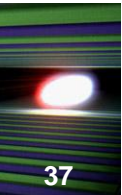
Burst-mode 1030nm CPA power amplifier



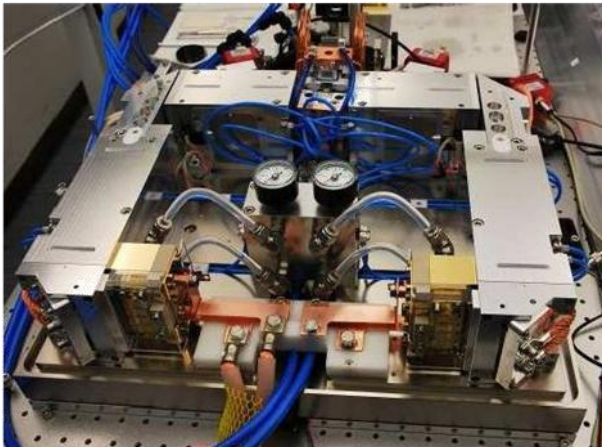
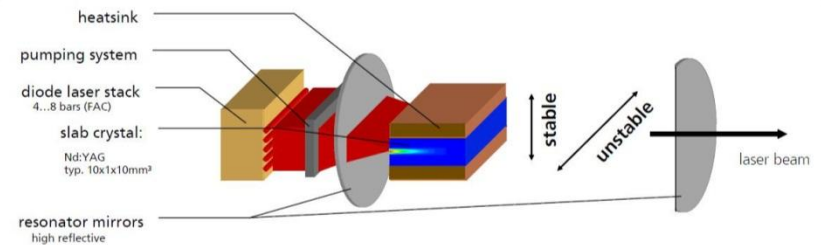
OPTICS EXPRESS, Vol. 17, No. 15, p. 12234, 2009 as well as own.

Property \ Amp. Technology	Yb-Fibre	Yb-Fibre + coherent combining	Yb:YAG InnoSlab	Yb:XXX Thin-Disk		Cryo-XXX
				Regen	Multi-pass	
<i>TEM₀₀ av. power</i>	++	++	+	+	+	+
<i>CPA pulse energy</i>	--	??	+	+	+	+
<i>Sub-ps capable</i>	+	+	+	+	+	--
<i>MHz rep-rate</i>	++	++	++	--	++	++
<i>Gain / amp-length</i>	++	++	++	--	--	++
<i>Thermal transients</i>	++	++	0	0	0	0
<i>Complexity</i>	+	--	0	-	-	LN ₂
<i>Availability (near term)</i>	+	--	+	+	+	-

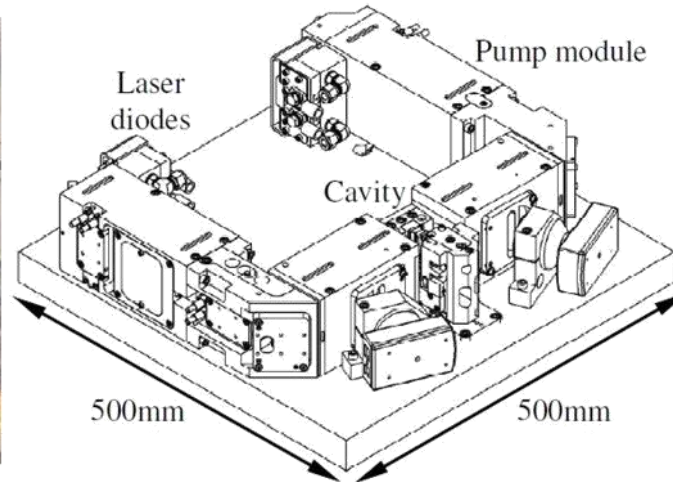


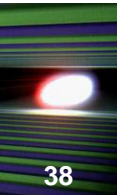


- Multi-pass stabilized by therm. lens in fast axis.
 - ➔ constant beam size.
- No thermal lens in slow axis.
 - ➔ increasing beam size.
- Intensity always around saturation.
 - ➔ Efficient extraction.



2009 Prototype setup at ILT





- First 50W Nd:YVO₄ amplifier in 2000 by Fraunhofer ILT, Aachen ¹.
- First Yb:YAG picosecond amplifiers in 2007 by Fraunhofer ILT, Aachen ².
- **Current state of the art Yb:YAG InnoSlab amplifiers :**
 - ✓ >600W, ~600fs, 20MHz from a single amplifier module with multi-passes.
 - ✓ 1100W total power or >500W power extraction (~600fs, 20MHz) from a booster amplifier with a single pass ³
 - ✓ 20mJ @ 2.25ns with 250W average power ⁴
 - ✓ non-saturated single pass gain >10 shown ⁵
 - ✓ Saturated gain approaching a value of 2 with a single pass power extraction of >40%
 - ✓ damage threshold of the optics used exceeds 5J/cm² (@ 2,25ns)

¹ J. Gieseke et al, "High power diode end pumped slab MOPA system," CLEO, paper CThI3, (2001)

² P. Rußbüldt et al, "High Power Yb:YAG InnoSlab fs-Amplifier", CLEO, paper CTuK5, (2008)

³ P. Rußbüldt et al, "Compact diode-pumped 1.1 kW Yb:YAG InnoSlab femtosecond amplifier," Opt. Lett. **35**, 4169-4171 (2010)

⁴ M. Schulz et al, "Yb:YAG InnoSlab amplifier: efficient high repetition rate subpicosecond pumping system for optical parametric chirped pulse amplification," Opt. Lett. **36**, 2456-2458 (2011)

⁵ P. Russbüldt et al, "400W Yb:YAG InnoSlab fs-Amplifier," Opt. Express **17**, 12230-12245 (2009)

- AMPHOS GmbH (ILT spin-off) was commissioned to show feasibility of an Yb:YAG InnoSlab amplifier system with these core parameters:



- Burst-rate: 10Hz
- Burst length: 200 μ s ... 1ms
- Burst av. Power: >20kW
- Intra-burst: 100kHz or higher
- Pulse energy: 200mJ or lower
- P_{in} : 1.5W / 2nm
- Pulse duration: 500ps
- M^2 : <1.5, round, smooth

- **Calculated effects include:**

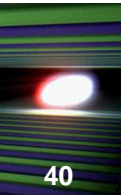
- Amplification (3D gain model)
- Thermally induced stress (3D thermo-mechanical FE-simulations)
- Thermal lensing (bulging and refractive), calculated and compared with known standard.
- Dynamic thermal lensing and path length variation during burst.
- B-Integral

- **Design constraints:**

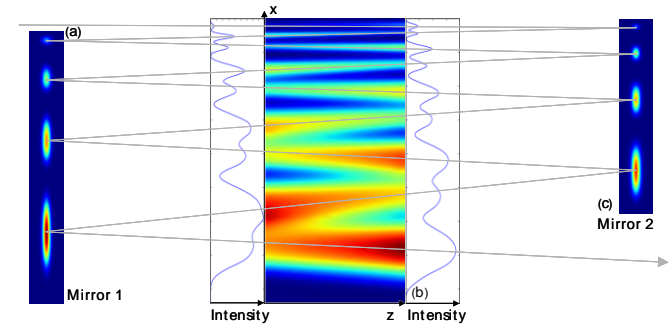
- Beam quality limitations of the pump source
- ASE and parasitic lasing
- Cost and lifetime of pump diodes
- Complexity and cost of pumping optics
- Exchangeability of pump diodes
- Handling, availability and cost of laser crystals

- **Output:**

- System design
- Cost estimation and time-line.
- Risk analysis



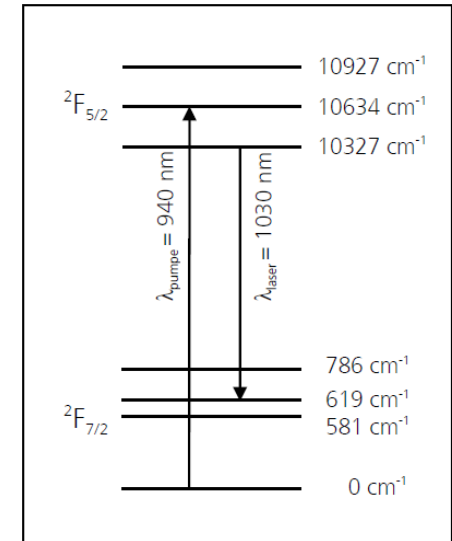
- 3d intensity distribution (laser/pump) inside crystal
- in good agreement with standard Amphos400



- recursive calculation of steady state solution (quasi-three-level-scheme*):

$$\frac{1}{\alpha_p L} \frac{I_p}{I_p^{Sat}} (1 - \exp(\alpha_p (\beta - f_p) L)) + \frac{1}{\alpha_l L} \frac{I_l}{I_l^{Sat}} (1 - \exp(\alpha_l (\beta - f_l) L)) - \beta = 0$$

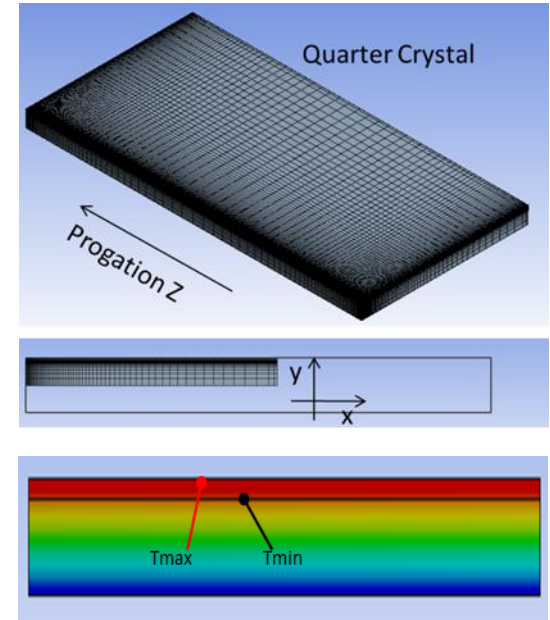
λ_{Pump}	λ_{Laser}	$\sigma_{Abs}(940nm; 300K)$	$\sigma_{Ems}(940nm; 300K)$	$\sigma_{Abs}(1030nm; 300K)$	$\sigma_{Ems}(1030nm; 300K)$
940nm	1030nm	$0.7 \cdot 10^{-20} cm^2$	$0.2 \cdot 10^{-20} cm^2$	$0.15 \cdot 10^{-20} cm^2$	$2.0 \cdot 10^{-20} cm^2$
τ	n_{YAG}	n_{2YAG}	dn_{YAG}/dT	$\rho_{Yb3+}(1\%)$	
951 μs	1.82	$9.34 \cdot 10^{-16} cm^2/W$	$7.3 \cdot 10^{-6} K^{-1}$	$1.38 \cdot 10^{20} cm^{-3}$	



*Gilbert L. Bourdet "Theoretical investigation of quasi-three-level longitudinally pumped continuous wave lasers", Applied Optics (2000)

- ANSYS Workbench Simulation
- Standard (Material-)Parameters:

Density	Thermal Expansion Coefficient @22°C	Youngs Modulus	Thermal Conductivity ⁸
4,56g/cm ³	7,8*10 ⁻⁶ K ⁻¹	3*10 ¹¹ Pa	10W/(m*K)@:23°C 8,6W/(m*K)@27°C
Specific Heat ⁸	Poisson Ratio	Heating Ratio	Heat Sink Temperature
574J/kg*K	0.3	15%	22°C



- (transient) Temperature-Gradient for

➔ thermal lens

$$f_{th} = \frac{r_{pump}^2}{2 \frac{dn_{YAG}}{dT} L_{crystal}} \frac{1}{\Delta T}$$

➔ Optical path length

$$\Delta L_{opt_total} = n_{YAG} \cdot \Delta z_{mech} + \frac{dn_{YAG}}{dT} \cdot \Delta T_{avg} \cdot L_{crystal}$$

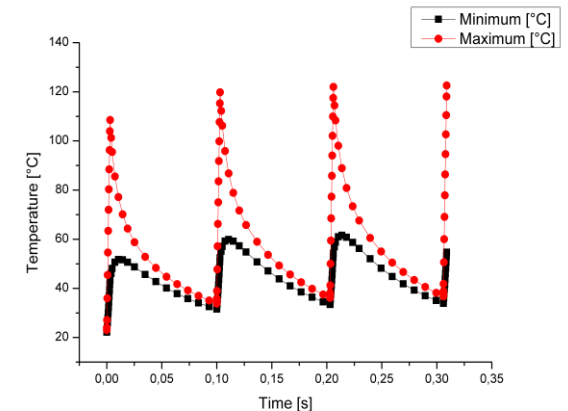
- Thermally induced stress for

➔ Mechanically induced lens (bulging)

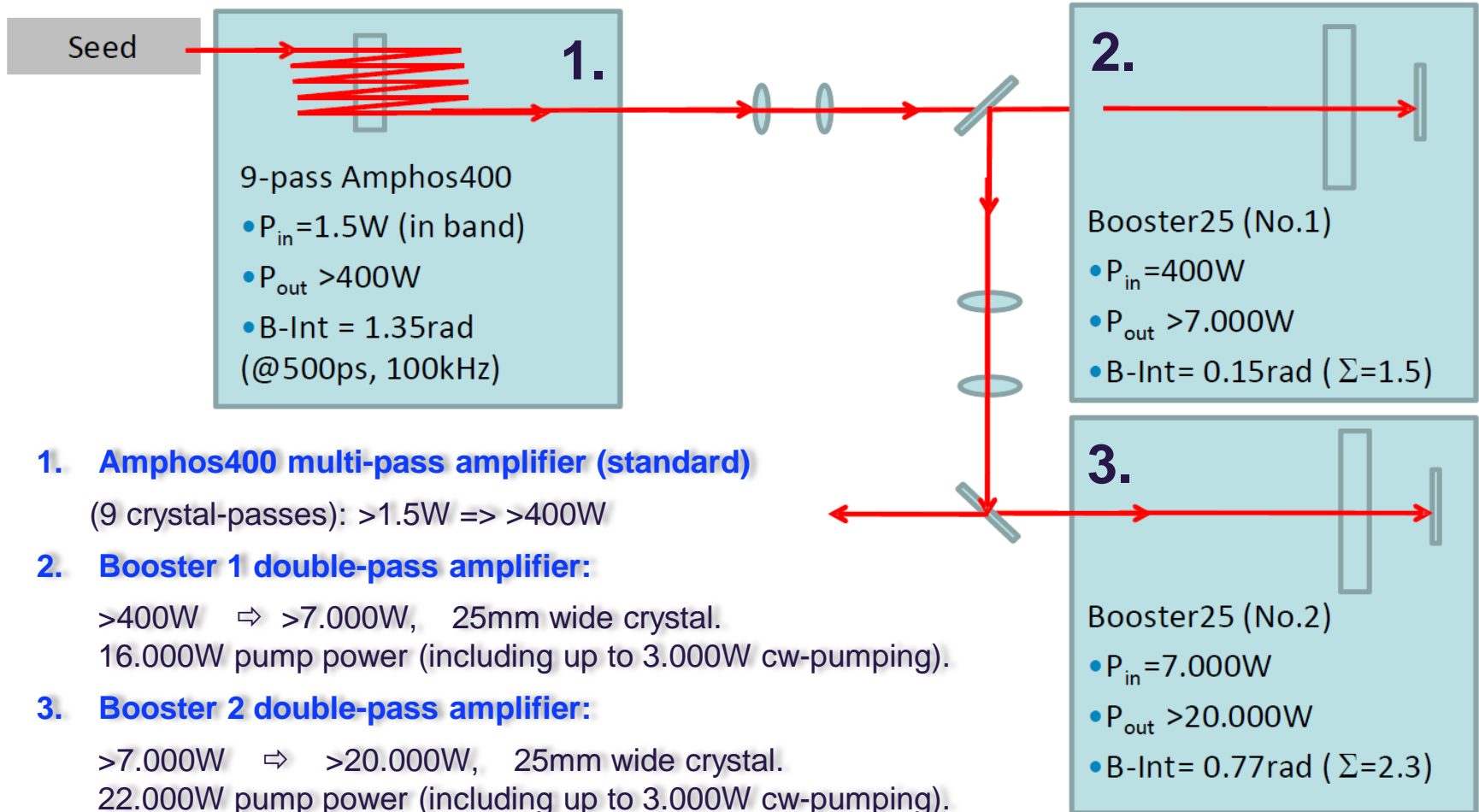
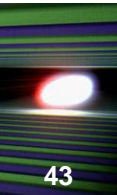
$$f_{mech} = \frac{r_{crystal}^2}{2(n_{YAG} - 1)\Delta z_{mech}}$$

➔ Fracture limit

(Tensile Stress for thermal fracture of YAG-rod: 120MPa-240MPa*)



*R. Weber, B. Neuenschwander, H. P. Weber, Thermal effects in solid-state laser materials, Optical Materials, Volume 11, Issues 2-3, January 1999, Pages 245-254



1. Amphos400 multi-pass amplifier (standard)

(9 crystal-passes): $>1.5W \Rightarrow >400W$

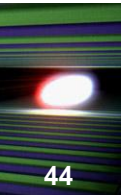
2. Booster 1 double-pass amplifier:

$>400W \Rightarrow >7.000W$, 25mm wide crystal.
 16.000W pump power (including up to 3.000W cw-pumping).

3. Booster 2 double-pass amplifier:

$>7.000W \Rightarrow >20.000W$, 25mm wide crystal.
 22.000W pump power (including up to 3.000W cw-pumping).

- ➔ Variation in total optical path length is below $5\mu m$ (~17fs) for the last 1ms of the pump pulse.
- ➔ Variation of the length of the thermal lens can be kept below 10% during this time window.



Output of XF1:

Inpulse energy: 20 μ J
 Rep-rate: 200kHz
 B-integral: 11.8
 Bandwidth: 5nm
 Pulselwidth: 1.3ns

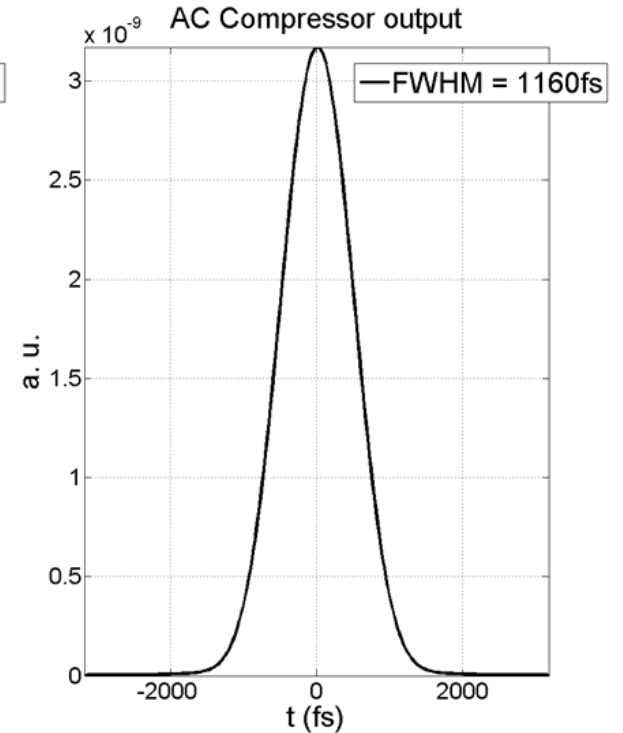
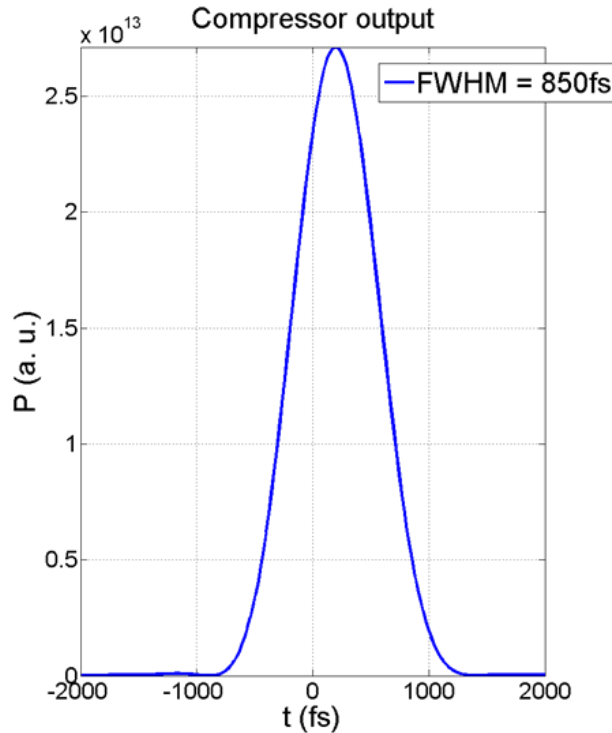


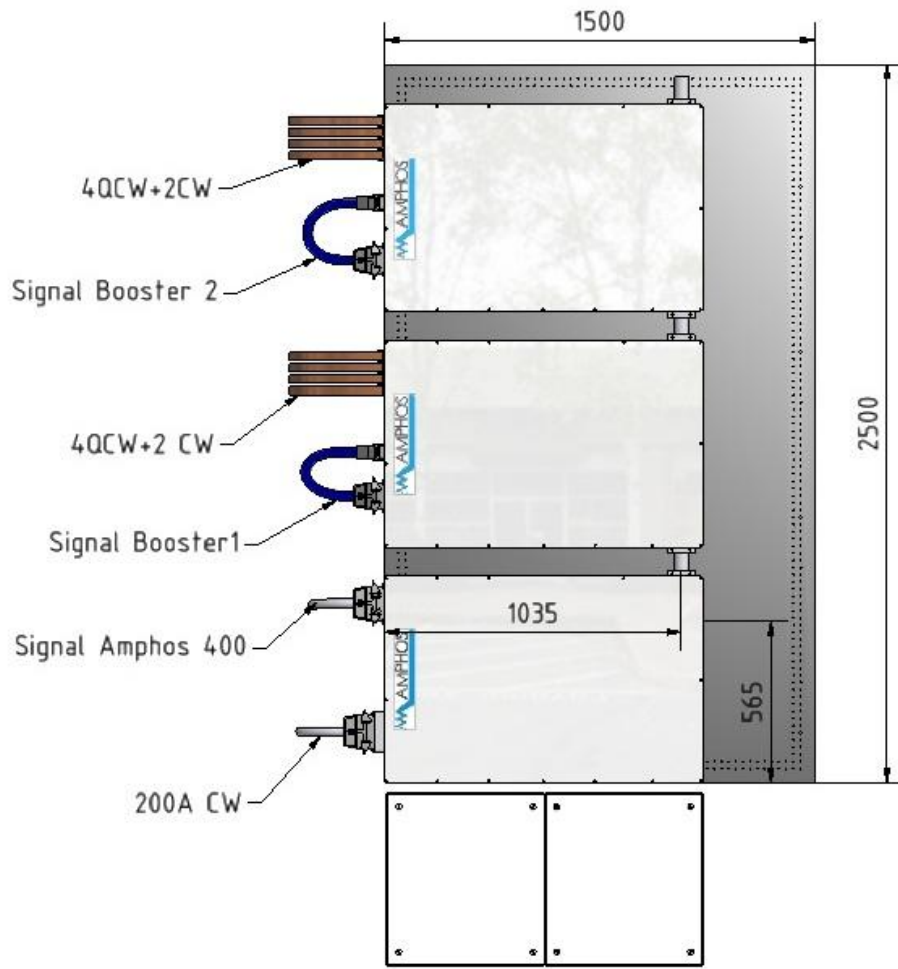
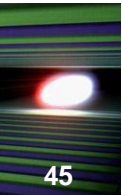
Gain-filter



Output pulse:

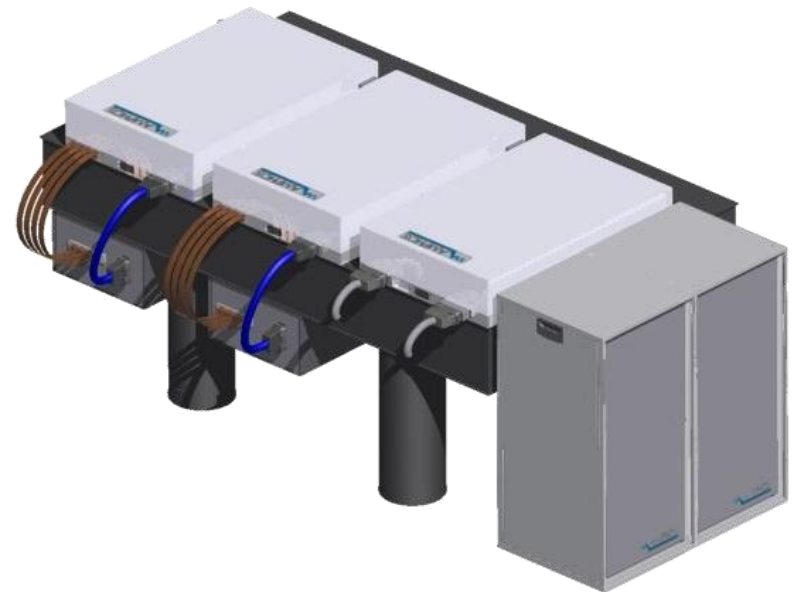
Bandwidth:	2nm	Compressed pulselwidth:	850fs
Uncompressed pulselwidth:	0.5ns	AC-width:	1160fs



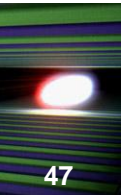


Shutter-box at output will include:

- Potential-free shutter: „Guillotine“
- Water-cooled beam dump
- Motorized attenuator
- Fast PD
- Average power
- Port for beam pointing measurement



Multi-stage NOPA



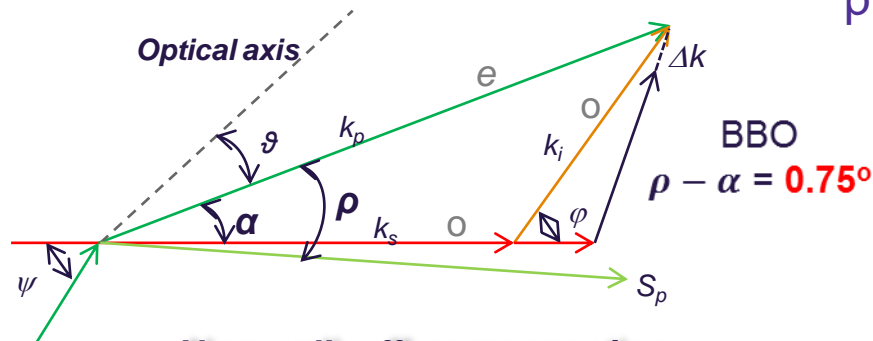
- Use non-collinearity with angle α between pump and signal to match the group velocity of signal and idler over larger bandwidth.
- Typical nonlinear materials: BBO, BIBO, LBO, KD*P

1. A. Dubietis, G. Jonusauskas, A. Piskarskas, Opt. Comm. 88, 437 (1992)
2. T. Wilhelm, J. Piel, E. Riedle: Opt. Lett. 22, 1494 (1997)
3. G. Cerullo, M. Nisoli, S. De Silvestri: Appl. Phys. Lett. 71, 3616 (1997)

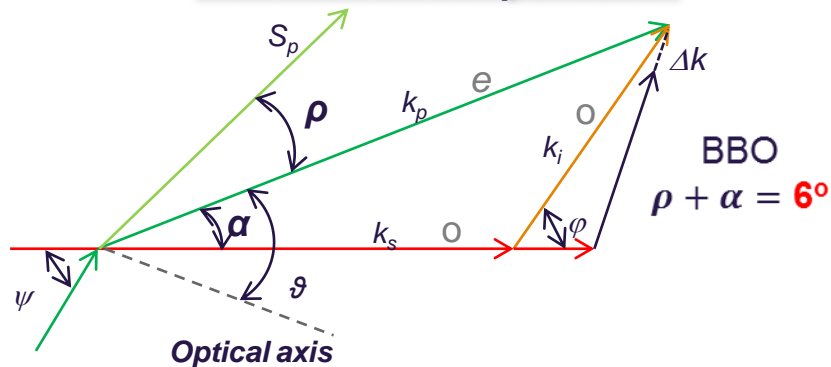
$$\Delta \vec{k} = \vec{k}_p - \vec{k}_s - \vec{k}_i$$

phase-matching:
 $\Delta k = 0$

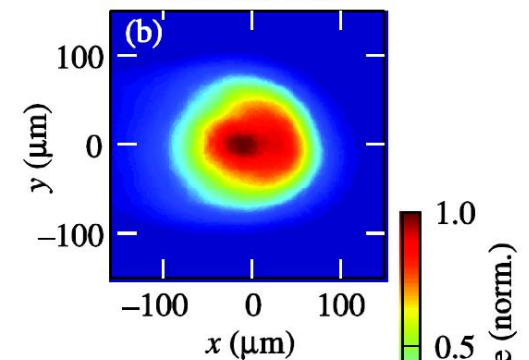
Walk-off compensation



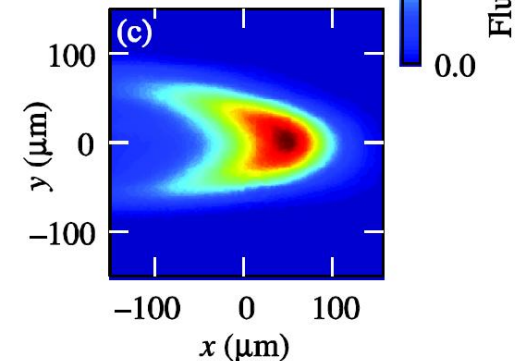
Non-walk-off compensation

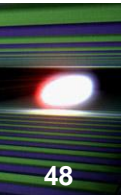


WC near field



NWC near field





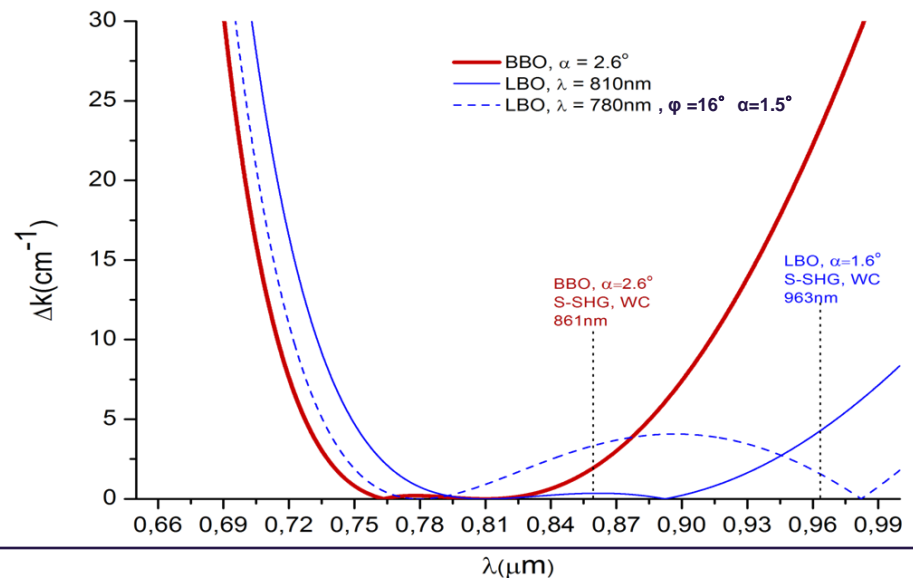
NOPA crystal	Pros	Cons
BBO 1st stage in WC 2nd stage	<ul style="list-style-type: none"> - Large bandwidth - High damage threshold - High gain - Medium apertures - Medium residual absorption 	<ul style="list-style-type: none"> - Large walk-off - Parasitic SHG of signal and idler in WC
BiBO	<ul style="list-style-type: none"> - High gain 	<ul style="list-style-type: none"> - Somewhat restricted bandwidth - Material quality is questionable
LBO 3rd + 4th stage	<ul style="list-style-type: none"> - Large bandwidth - No parasitic SHG of signal and idler in WC - Medium to large apertures - Very low residual absorption - Small walk-off 	<ul style="list-style-type: none"> - Low gain - Somewhat lower damage threshold
KD*P	<ul style="list-style-type: none"> - Very large apertures - Economical 	<ul style="list-style-type: none"> - Low gain - High residual absorption

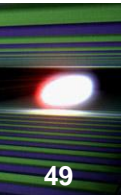
BBO

Optimised for 810nm,
 $\theta = 24.7^\circ$ (pump internal
 angle), $\varphi = 90^\circ$
 $\alpha = 2.6^\circ$

LBO

Optimised for 810nm
 $\varphi = 16.5^\circ$ (pump internal
 angle), $\theta = 90^\circ$
 $\alpha = 1.6^\circ$

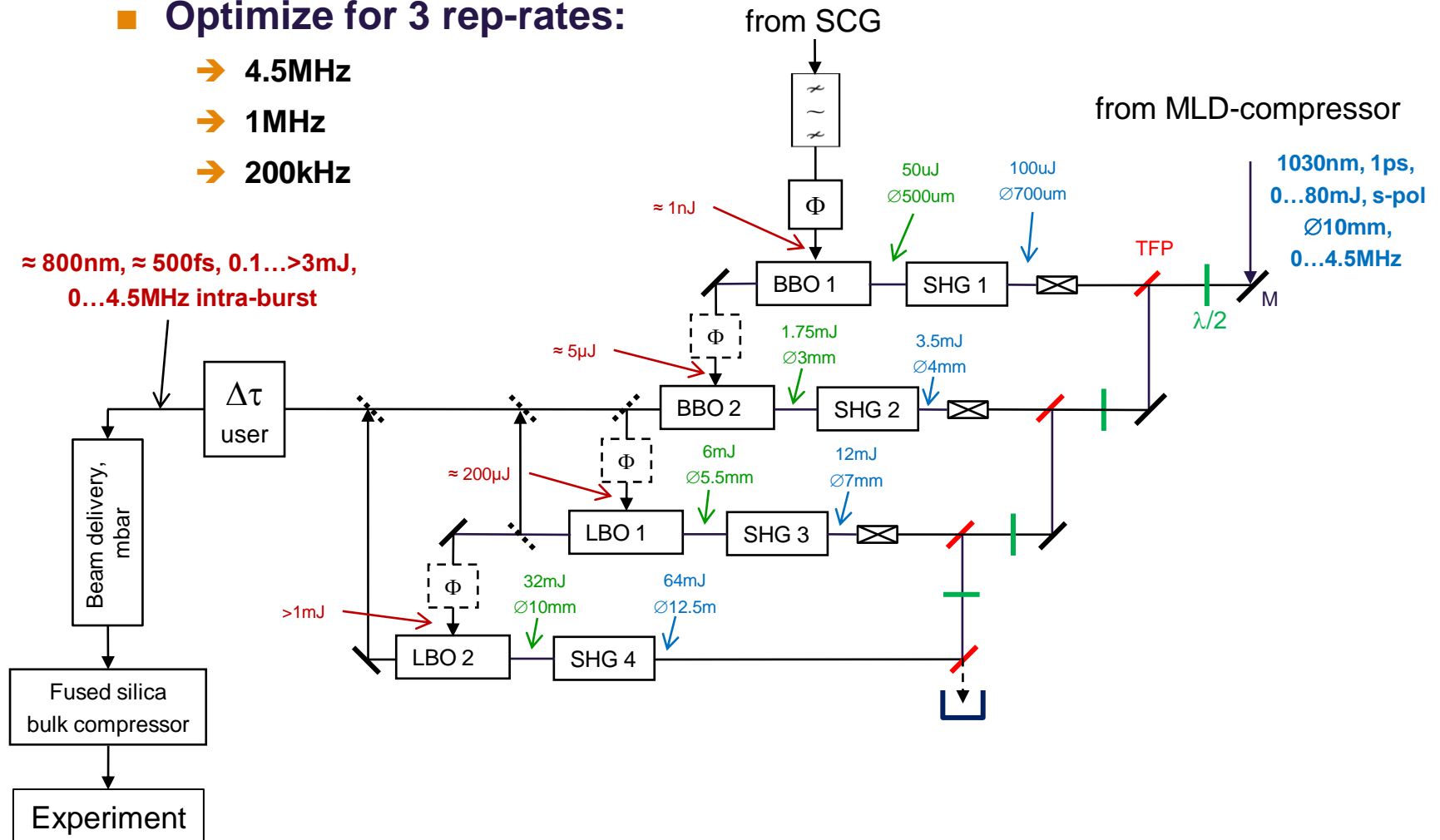


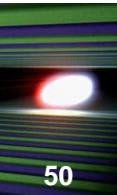


■ Optimize for 3 rep-rates:

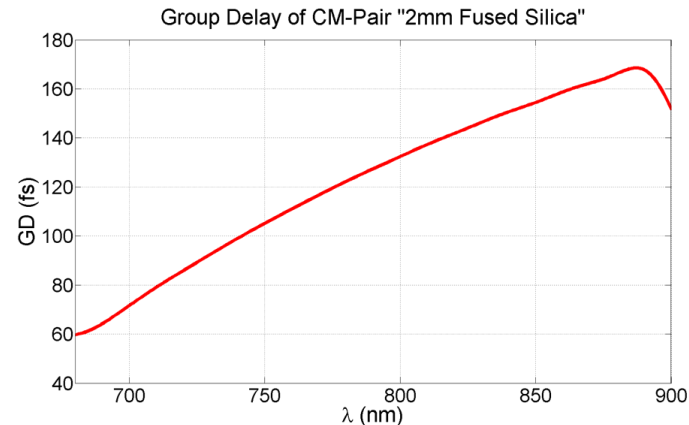
- ➔ 4.5MHz
- ➔ 1MHz
- ➔ 200kHz

≈ 800nm, ≈ 500fs, 0.1...>3mJ,
0...4.5MHz intra-burst



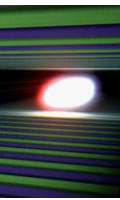


- Use passive dispersion management : chirped mirrors (CMs)
- Limit amplified signal bandwidth to 15fs (transform limited)
- Pre-chirp continuum before amplification
 - ➔ Stretcher is made from compensated CM-pair.
 - ➔ Amount of chirp is chosen to amplify $\approx 80\text{nm}$ by the $\approx 800\text{fs}$ pump pulse.
- Compressor: bulk fused silica at experiment.
 - ➔ Fused silica is dominating element.
 - ➔ GDD / TOD ratio of BBO is similar to that of fused silica.
 - ➔ Use CM-design optimised for GDD and TOD to be conjugate to fused silica.



■ Flexibility of scheme:

- ➔ Bandwidth of CM-pair might support shorter pulses \Rightarrow reduce input chirp.
- ➔ For longer pulses \Rightarrow increase input chirp ($\approx 15\text{nm}$, i. e. 50fs compressed) .



Time domain:

$$E(r, t) = \frac{1}{2} \sum \{ \mathbf{e}_m A_m(r, t) \exp[i(\omega_{n0}t - \mathbf{k}_m r)] + c. c. \}$$

With m replaced by s, p, i, ssh, ish , the coupled equations in (r, t) space are :

$$\left\{ \begin{array}{l} \widehat{M}_s A_s = i\sigma_s A_i^* A_p \exp(i\Delta k z) - i\sigma_s A_s^* A_{ssh} \exp(-i\Delta k_{ssh} z) \\ \widehat{M}_i A_i = i\sigma_i A_s^* A_p \exp(i\Delta k z) - i\sigma_i A_i^* A_{ish} \exp(-i\Delta k_{ish} z) \\ \widehat{M}_p A_p = -i\sigma_p A_s A_i \exp(-i\Delta k z) \\ \widehat{M}_{ssh} A_{ssh} = i\sigma_{ssh} A_s^2 \exp(i\Delta k_{ssh} z) \\ \widehat{M}_{ish} A_{ish} = i\sigma_{ish} A_i^2 \exp(i\Delta k_{ish} z) \end{array} \right.$$

Where

$$\widehat{M}_m = \frac{\partial}{\partial z} + \frac{\alpha_m}{2} + \rho_m \frac{\partial}{\partial x} + \frac{i}{2k_m} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) + \frac{1}{v_m} \frac{\partial}{\partial t} + \frac{i}{2} \beta_{2m} \frac{\partial^2}{\partial t^2} + \dots$$

α_m absorption

v_m group velocity,

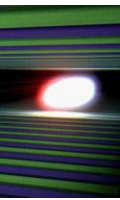
$$\sigma_n = \frac{\omega_n d_{eff}}{n_n c}$$

$\rho_m = -1/n(\vartheta) * dn(\vartheta)/d\vartheta$ walk-off angle extra-ordinary wave,

β_{2m} group velocity dispersion

Δk phase mismatch at carrier frequencies

e. g. Dmitriev V.G., Gurzadyan G.G., Nikogosyan D.N. "Handbook of Nonlinear Optical Crystals". Springer, Berlin, 1997.



Frequency domain:

$$E(r, \omega) = \frac{1}{2} \sum \{E_m(r, \omega) + c.c\}$$

With m replaced by s, p, i, ssh, ish , the coupled equations in (r, ω) space are:

$$\frac{\partial}{\partial z} E_s + \frac{\alpha_s}{2} E_s + \frac{i}{2k_l} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) E_s + ik_s E_s = i\sigma_s \mathcal{F}\{E_i^* E_p\} - i\sigma_s \mathcal{F}\{E_s^* E_{SSH}\}$$

$$\frac{\partial}{\partial z} E_l + \frac{\alpha_l}{2} E_l + \frac{i}{2k_l} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) E_l + ik_l E_l = i\sigma_l \mathcal{F}\{E_s^* E_p\} - i\sigma_l \mathcal{F}\{E_l^* E_{ISH}\}$$

$$\frac{\partial}{\partial z} E_p + \frac{\alpha_p}{2} E_p + \rho_p \frac{\partial}{\partial x} E_p + \frac{i}{2k_p} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) E_p + ik_p E_p = -i\sigma_p \mathcal{F}\{E_s E_l\}$$

$$\frac{\partial}{\partial z} E_{SSH} + \frac{\alpha_{SSH}}{2} E_{SSH} + \rho_{SSH} \frac{\partial}{\partial x} E_{SSH} + \frac{i}{2k_{SSH}} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) E_{SSH} + ik_{SSH} E_{SSH} = i\sigma_{SSH} \mathcal{F}\{E_s E_s\}$$

$$\frac{\partial}{\partial z} E_{ISH} + \frac{\alpha_{ISH}}{2} E_{ISH} + \rho_{ISH} \frac{\partial}{\partial x} E_{ISH} + \frac{i}{2k_{ISH}} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) E_{ISH} + ik_{ISH} E_{ISH} = i\sigma_{ISH} \mathcal{F}\{E_l E_l\}$$

Where

α_m absorption

$$\rho_m = -1/n(\vartheta) * dn(\vartheta)/d\vartheta$$

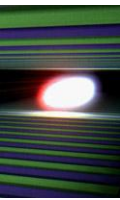
walk-off angle extra-ordinary wave

$\sigma_m = \frac{\omega_m d_{eff}}{n_m c}$ nonlinear coefficient

$$k_m = \frac{\omega_m n_m(\omega)}{c}$$

propagation constant

e. g. J. Zheng, H. Zacharias, Appl. Phys. B 97, 765–779, (2009)



Fourier space Method

- Calculations:
 - linear and nonlinear parts in $\{\omega, k_n\}$ space by Runge Kutta 4th order
- 😊 Standard solving technique like 4-order Runge Kutta
- ☹ Calculations of all equation components at the same time (time consuming).
- 😊 Error scales with power ~ 5 with the step size

1. S. C. Sheng and A. E. Siegman, "Nonlinear-optical calculations using fast-transform methods: second-harmonic generation with depletion and diffraction," Phys. Rev. A 21, 599606 (1980)

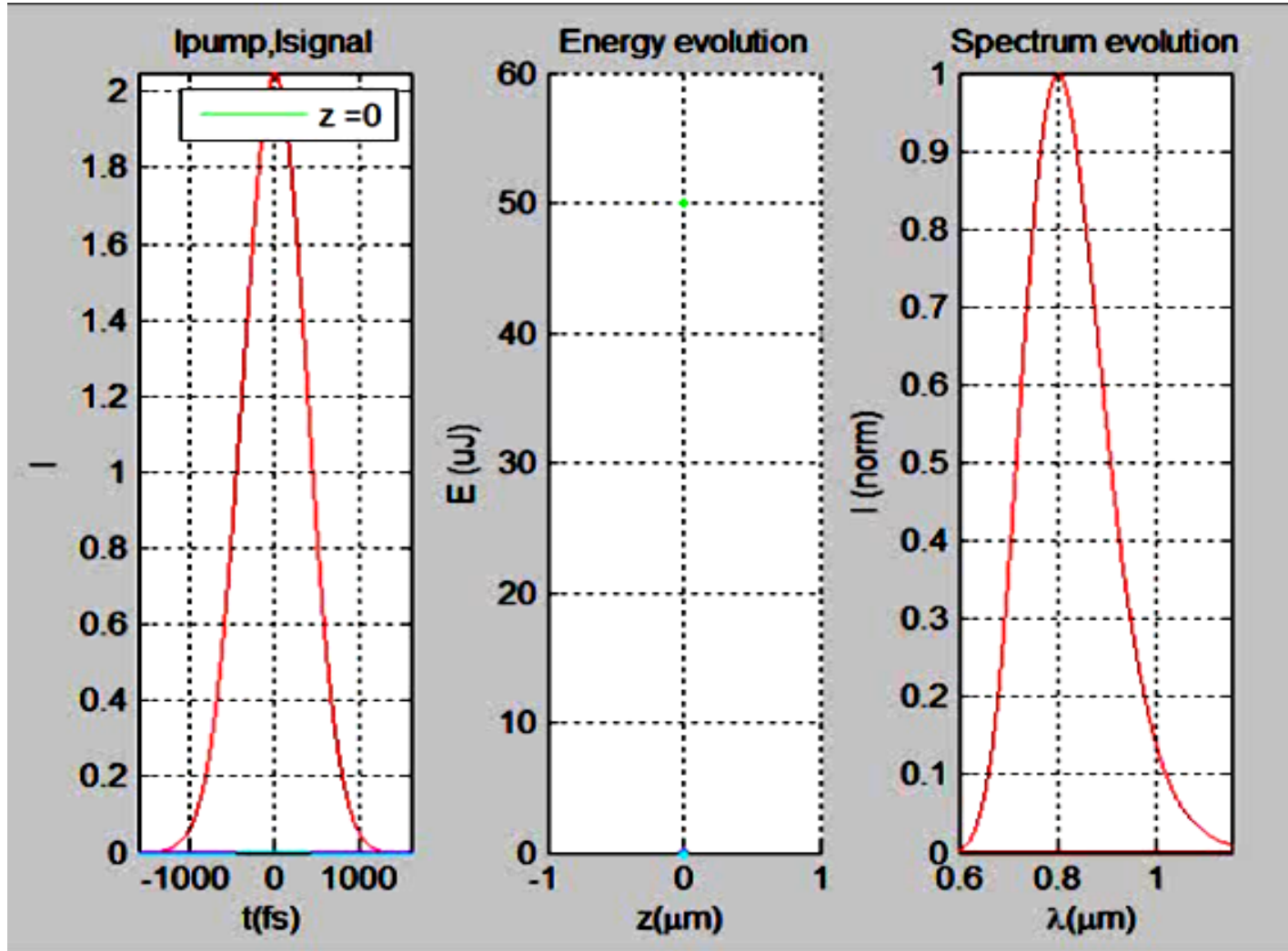
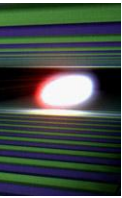
3. G. Arisholm, "General numerical methods for simulating second-order nonlinear interactions in birefringent media," 14, J. Opt. Soc. Am. B, 2543, (1997)

Split Step Method

- Calculations:
 - linear parts analytical solution in $\{\omega, k_n\}$ space
 - nonlinear parts by Runge Kutta 4th order in time domain
- 😊 Standard solving technique like 4-order Runge Kutta
- 😊 Evaluation of linear propagation with FFT
- 😊 Nonlinear differential for each spatial element independent
- ☹ Error scales with power ~ 2 with the step size

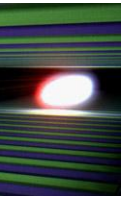
2. G. P. Agrawal, "Nonlinear Fiber Optics (3rd ed.) Academic Press, San Diego (2001).

Split-step Method (1D + time)

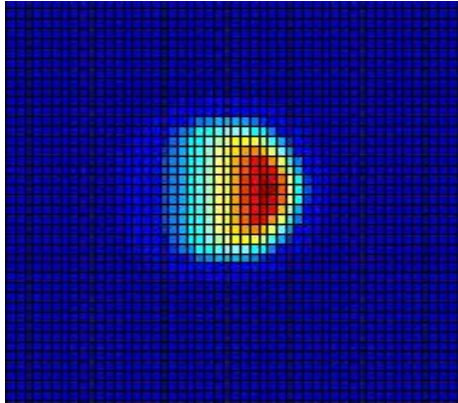


- BBO
- Walk-off compensation scheme
- Energy
- Temporal
- Spectral

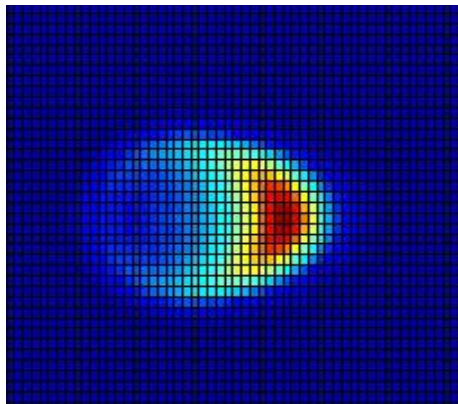
Fourier space method (3D+time)



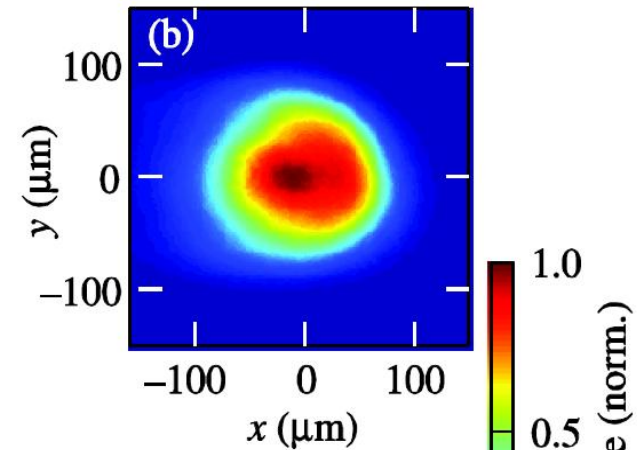
WC near field



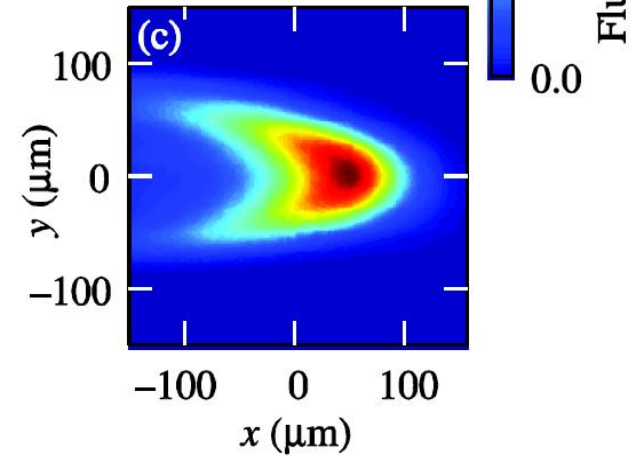
NWC near field



WC near field



NWC near field

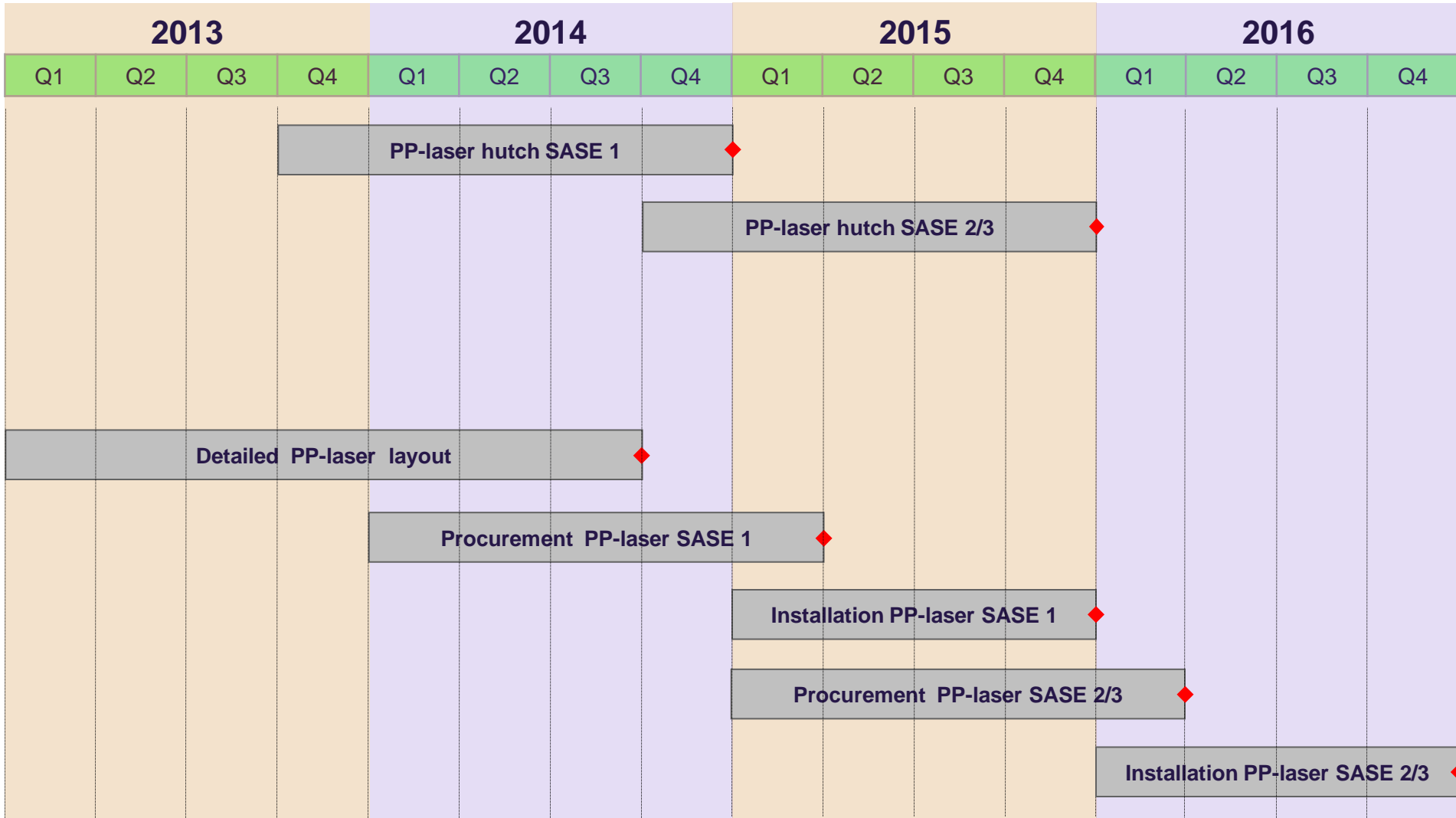
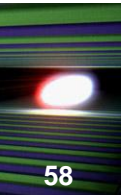


Simulations: nonlinear propagation code “Sisyfos”, developed at Forsvarets ForskningsInstitut:

G. Arisholm, “General numerical methods for simulating second-order nonlinear interactions in birefringent media,” **14**, J. Opt. Soc. Am. B, 2543, (1997)

Experiment: “Analysis and suppression of parasitic processes in noncollinear optical parametric amplifiers” J. Bromage et al, Vol. 19, Opt. Expr., 16797, (2011)

Planning



X-ray FELs for the soft and hard regimes have proven to show excellent beam properties. The European XFEL has started constructions and early experiments are scheduled for 2016.



FEL science has only just started. Experiments have exploratory character and fields have to be established. In the soft x-ray regime this process is in full swing. Hard x-ray experiments only started in 2010. Coming years will enable to establish new fields.



We are facing an exciting period of R&D at the highest level, including high power ultrafast laser development.



Due to the burst-mode emission pattern of the European XFEL and the pulse requirements, the pump-probe laser development faces unique challenges, both technological as well as time line.

Thank You!