

SM single-top production at hadron colliders

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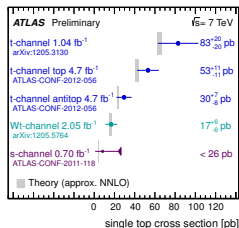
Why single-top production?

Electroweak single-top production rate competitive with QCD-mediated $t\bar{t}$ cross section

$$\begin{aligned} \text{LHC}(7 \text{ TeV}) : \quad \sigma_{t\bar{t}} &= 162.4 \text{ pb} \\ \sigma_t + \sigma_{\bar{t}} &= 78.3 \text{ pb} \end{aligned}$$

⇒ **complementary informations on top-quark properties!**

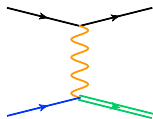
- sensitive to charged-current interactions of the top quark
⇒ test $V - A$ nature of the Wtb vertex
- $\sigma \propto |V_{tb}|^2 \rightarrow$ direct extraction of CKM matrix element V_{tb}
- probes bottom PDF inside the proton
- beside being an important signal, single- t production is background to Higgs production
- generally relevant to new physics searches (top anomalous couplings, 4th generation searches, FCNC, charged-Higgs production,...)



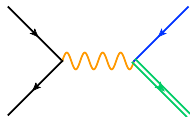
Almost too good to be true! Unfortunately experimental extraction of the single-top signal much more challenging than top-pair measurements due to **large background from Wj and $t\bar{t}$**



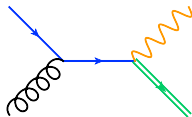
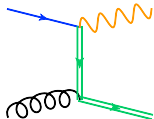
Single-top production in the SM



t-channel



s-channel

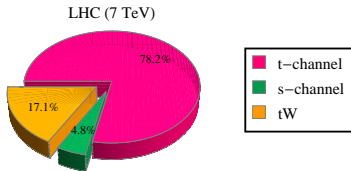
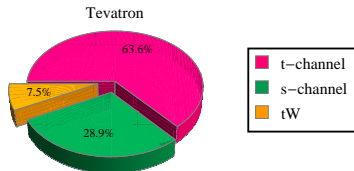


associated W-*t* production

In the SM **three production modes**:

- *t*-channel production ($k_W^2 < 0$)
- *s*-channel production ($k_W^2 > 0$)
- associated *tW* production ($k_W^2 \sim M_W^2$)

***t*-channel production is dominant channel at both Tevatron and LHC**

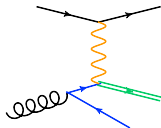


Different production channels?

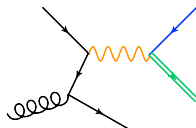


Note that distinction into 3 production channels is somewhat ambiguous...

- t -channel and s -channel mix beyond LO (though no interf. at NLO due to colour)

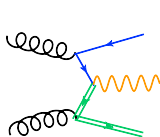


t -channel

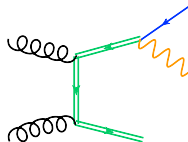


s -channel

- More seriously tW production mixes with (much bigger) $t\bar{t}$ production at NLO



associated tW production



$t\bar{t}$ production

⇒ from a theoretical point of view most satisfactory solution is fixing a specific **physical final state** (i.e. jets+leptons+ \cancel{E}_T) and include the full **gauge-invariant set of relevant contributions**

Single-top production at NLO

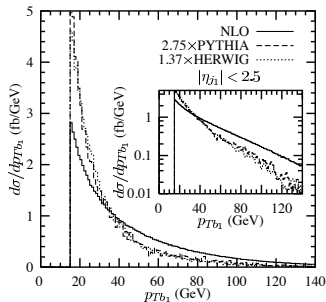
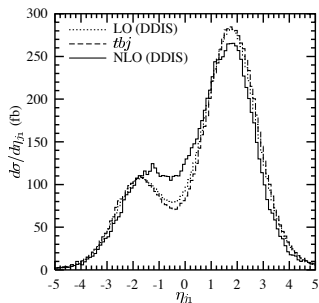


$\mathcal{O}(\alpha_s)$ corrections to the tree-level **inclusive** cross sections have been known for a while:

- ***t*-channel** [Bordes, van Eijk '95; Stelzer, Sullivan, Willenbrock '97]: $\Delta\sigma^{\text{NLO}}/\sigma^{\text{LO}} \sim 10\%$
- ***s*-channel** [Smith, Willenbrock '96]: $\Delta\sigma^{\text{NLO}}/\sigma^{\text{LO}} \sim 40 - 50\%$
- ***tW* production** [Zhu '02; Cao '08]: $\Delta\sigma^{\text{NLO}}/\sigma^{\text{LO}} \sim 50\%$

and **differential** cross section computed by [Harris, Laenen, Phaf, Sullivan, Weinzierl '02; ZTOP '04]

t-channel

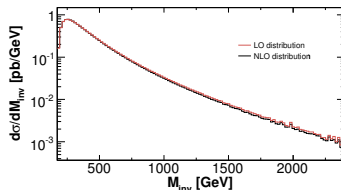


big differences between NLO calc. and LO showers \Rightarrow shows necessity of full NLO result!

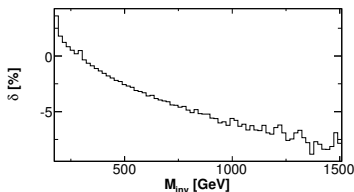


NLO EW corrections and SUSY QCD corrections also available for t -channel production and associated production [Beccaria, Carloni Calame, Mirabella, Piccinini, Renard, Verzegnassi '07/'08]

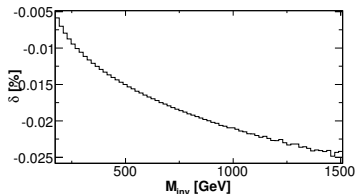
t -channel $[M_{inv}(t, j_1)]$



EW



SUSY-QCD



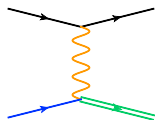
EW corrections small ($\lesssim 5\%$) and SUSY QCD corr. negligible ($< 1\%$ for mSUGRA SU1)

5-flavour vs 4-flavour scheme

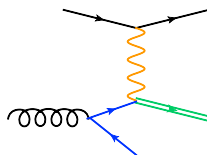


t -chan. NLO results first computed in the [5-flavour scheme](#) (5F). Recently NLO results in the [4-flavour scheme](#) (4F) have also become available [Campbell, Frederix, Maltoni, Tramontano '09].

What are the main differences between the two schemes?



5-flavour scheme



4-flavour scheme

5F: initial b from PDF inside proton

- [large logs](#) $\ln \mu^2/m_b^2$ resummed by bottom PDF evolution
- [exact factorization](#) of QCD corrections to heavy/light currents at NLO and simpler calculation
- m_b dependence and spectator b -jet only described from NLO onwards

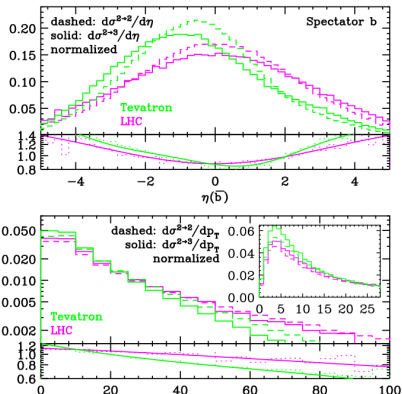
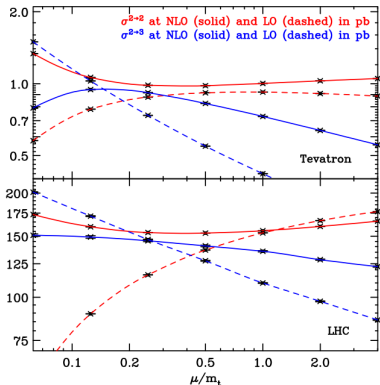
4F: initial b -quark from gluon splitting

- potentially large logs not resummed
- almost exact heavy/light current factorization. More complicated calculation due to additional mass and additional external leg.
- [spectator \$b\$ -jet](#) observables and m_b dependence already at LO



NLO calculation in 4F scheme

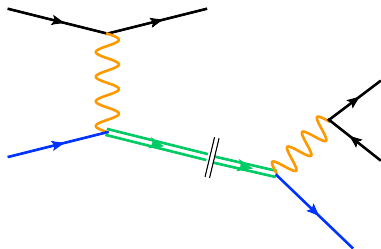
[Campbell, Frederix, Maltoni, Tramontano '09]



- small differences between 4F and 5F results for total cross section ($\sim 6\%$, compatible with theory uncertainty)
- larger differences in distributions (10 – 20%), especially for spectator b -jet (expected, since effectively LO in 5F calculation)



Precise description of the single top production requires consistent inclusion of [top quark decay](#) (theoretically a delicate business due to gauge-invariance issues...)



Decay commonly treated in **Narrow-Width Approximation (NWA)**

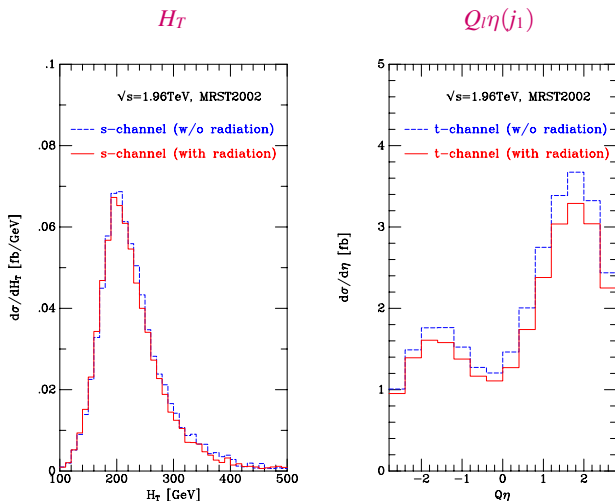
$$\frac{1}{|p^2 - m_t^2 + im_t\Gamma_t|^2} = \frac{\pi}{\Gamma_t} \delta(p_t^2 - m_t^2) + \mathcal{O}\left(\frac{\Gamma_t}{m_t}\right)$$

- matrix element [factorizes into production AND decay](#) of an **on-shell** top ($p_t^2 = m_t^2$)
- preserves top-quark [spin correlations](#) between production and decay
- includes [NLO corrections to production AND decay](#), but no production/decay interferences (expect effect $\sim \Gamma_t/m_t \sim 1\%$ on total cross section)
- off-shell effects are completely lost (again expect effect $\sim \Gamma_t/m_t$).

Single-top production and decay at NLO



[Campbell, Ellis, Tramontano '04; MCFM; Cao, Schwienhorst, Yuan '04+Benitez, Brock '05]



Decay corrections modify significantly the normalization (though shape is preserved...)



Beyond fixed-order on-shell NLO

inclusion of off-shell effects and production/decay interferences

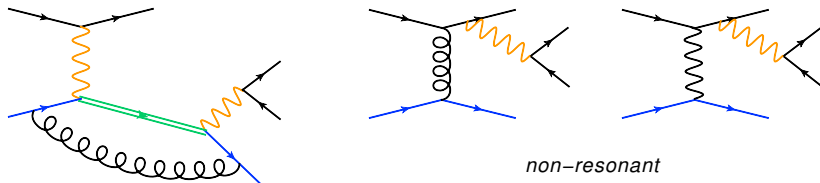
resummation of threshold logarithms

matching of fixed-order NLO results and MC parton showers



NWA only includes factorizable corrections to on-shell production and decay!

⇒ no information on off-shell effects ($p_t^2 \neq m_t^2$), non-factorizable corrections and non-resonant (background) diagrams



These effects are expected to be of order $\Gamma_t/m_t \sim 1\%$ (true for the **total cross section**).

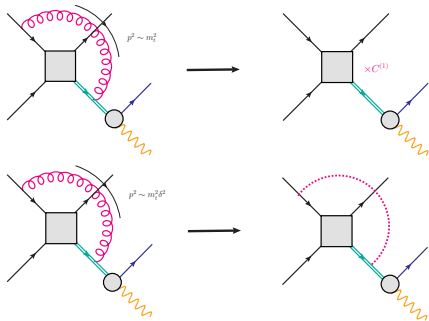
However: small effect is partly due to **large cancellations** between virtual and real non-factorizable corrections ⇒ off-shell and non-factorizable effects could be larger for arbitrary kinematical distributions



Effective-theory approach to single t production

[PF, Giannuzzi, Mellor, Signer '10, '11]

Consider a resonant unstable top (rather than on-shell) and use the small virtuality of t as an expansion parameter, $\delta \equiv (p_t^2 - m_t^2)/m_t^2 \ll 1$



- **Hard region** ($q^2 \sim m_t^2$)
⇒ **factorizable corrections**
(⇔ corrections in the NWA)

- **Soft region** ($q^2 \sim m_t^2 \delta^2$)
⇒ **non-factorizable corrections**
(⇔ off-shell effects and production/decay interferences)

Effective-theory expansion resums **finite-width effects**, includes leading **non-factorizable corrections** and preserves **gauge invariance**

+ much simpler than full 1-loop calculation in the **Complex Mass Scheme!**

Integrated cross section ($m_t = 172 \text{ GeV}$, $\mu_{F/R} = m_t/2$)



$pp \rightarrow J_b J_l e^+ \cancel{E}_T + X$	$pp \rightarrow J_b J_{\bar{b}} e^+ \cancel{E}_T + X$
$p_T(J_b) > 20 \text{ GeV}$	$p_T(J_b) > 20 \text{ GeV}$
$p_T(\text{hardest } J_l) > 20 \text{ GeV}$	$p_T(J_{\bar{b}}) > 30 \text{ GeV}$
$p_T(\text{extra } J_{\bar{b}}) < 15 \text{ GeV}$	$p_T(\text{extra } J_l) < 15 \text{ GeV}$
$\cancel{E}_T + p_T(e) > 60 \text{ GeV}$	$\cancel{E}_T + p_T(e) > 60 \text{ GeV}$

LHC@7TeV

$pp \rightarrow J_b J_l e^+ \cancel{E}_T + X$ ($\sim t$ -channel)		Eff. Theory	NWA
	LO[pb]	$3.460^{+0.278}_{-0.403}$	3.505
NLO[pb]	$1.609^{+0.303}_{-0.240}$	1.642	
$pp \rightarrow J_b J_{\bar{b}} e^+ \cancel{E}_T + X$ ($\sim s$ -channel)		Eff. Theory	NWA
	LO[pb]	$0.1654^{+0.0001}_{-0.0010}$	0.1677
NLO[pb]	$0.1618^{+0.0021}_{-0.0005}$	0.1635	

Differences between effective-theory calculation and NWA $\sim 2\%$

\Rightarrow consistent with expectation $\sim \Gamma_t/m_t \dots$

Similar effects found in $t\bar{t}$ production [Bevilacqua et al. '10, Denner et al. '10]

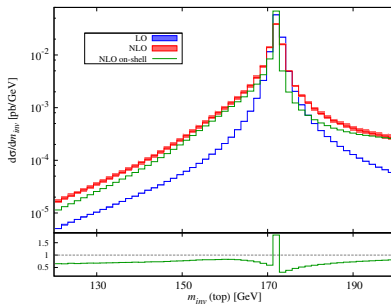
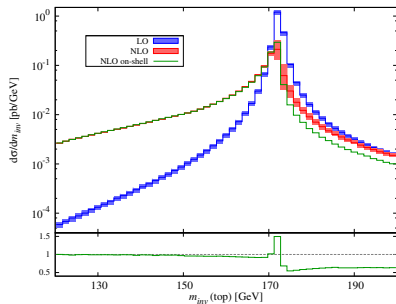
LHC@7TeV

$$pp \rightarrow J_b J_l e^+ \cancel{E}_T + X$$

$\sim t$ -channel

$$pp \rightarrow J_b J_{\bar{b}} e^+ \cancel{E}_T + X$$

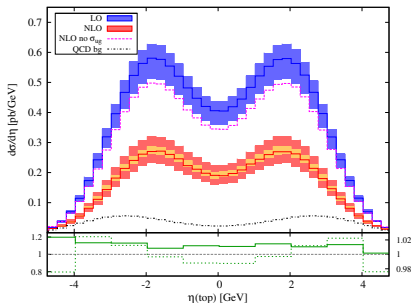
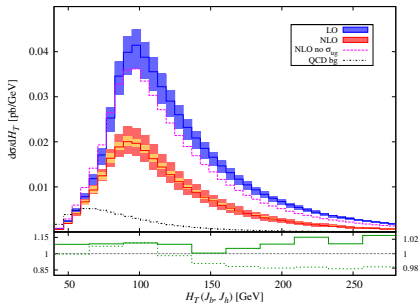
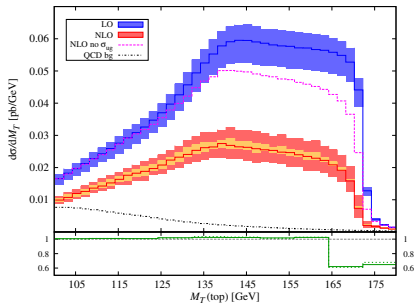
$\sim s$ -channel



- large off-shell effects (up to 50%) close to the peak
- non-factorizable corrections change sign around the peak
 \Leftrightarrow **explains small effect on the total cross section**



$pp \rightarrow J_b J_l e^+ \cancel{E}_T + X$ (LHC @ 7 TeV)



- off-shell and non-factorizable effects **generally small** ($\sim 2\%$) due to averaging effect over m_{inv}
- **sizeable corrections** (up to 40%) close to kinematics edges, e.g. $M_T \sim m_t$ (relevant for m_t extraction)



Single-top cross sections affected by potentially large corrections related to suppression of [soft emission](#) near kinematical thresholds

$$p_1 p_2 \rightarrow t(p_t) q(k) + X(p_X)$$
$$\sigma^{\text{N}^n\text{LO}} \sim \alpha_s^n \left[\frac{\ln^m s_4}{s_4} \right]_+ \quad m \leq 2n - 1 \quad s_4 = (p_t + p_X)^2 - m_t^2$$

partonic cross section kinematically enhanced when $s_4 \rightarrow 0$

⇒ **all-order resummation of the enhanced terms is desirable!**

(leads to accurate normalization of the cross section and reduced theoretical uncertainties)

State of the art for single-top is [NNLL resummation](#) (i.e. $m = 2n - 1, 2n - 2, 2n - 3$)

- NNLL resummation performed recently by two independent groups with different formalisms (Mellin space VS SCET) [[Kidonakis '10, '11](#); [Li, Wang, Zhang, Zhu '10](#)]
- NNLL resummed results usually re-expanded to obtain approximated fixed-order NNLO cross section (more convenient for numerical implementation...)



Threshold resummation

Resummation based on factorization of different relevant scales [Kidonakis, Sterman '97].
In Mellin space:

$$\begin{aligned}
\hat{\sigma}^{res}(N) = & \overbrace{\exp \left[\sum_{i=1,2} E(N_i) + E'(N') \right]}^{\text{soft-coll. radiation from external massless p.}} \overbrace{\exp \left[\sum_{i=1,2} 2 \int_{\mu_F}^{\sqrt{s}} \frac{d\mu}{\mu} \gamma_{q/q}(\tilde{N}_i, \alpha_s(\mu)) \right]}^{\text{scale dep. from PDFs}} \\
& \times \text{Tr} \left\{ \underbrace{H(\alpha_s(\sqrt{s}))}_{\text{hard scatt.}} \underbrace{\exp \left[\int_{\sqrt{s}}^{\sqrt{s}/\tilde{N}'} \frac{d\mu}{\mu} \Gamma_S^\dagger(\alpha_s(\mu)) \right] S(\alpha_s(\sqrt{s}/\tilde{N}')) \exp \left[\int_{\sqrt{s}}^{\sqrt{s}/\tilde{N}'} \frac{d\mu}{\mu} \Gamma_S(\alpha_s(\mu)) \right]}_{\text{large-angle soft radiation}} \right\}
\end{aligned}$$

- H, S, Γ_S are matrices in colour-state space!
- NNLL resummation requires recently-computed two-loop Γ_S [Neubert, Becher '09; Kidonakis '10]

Analogous factorization in SCET: $\sigma \sim f \otimes f \otimes \text{Tr}[H \times S] \otimes J$ [Li, Wang, Zhang, Zhu '10]
+ resummation in momentum space via RG evolution equations.



Effects of threshold resummation

Results for t - and s -channel available in both formalisms

[Kidonakis '10, '11; Li, Wang, Zhang, Zhu '10]

For t -channel small NNLO effects in both approaches (few percents at both Tevatron and LHC) but large discrepancies for s -channel production...

s -channel	SCET	Mellin sp.
Tevatron	$0.463^{+0.002}_{-0.004} (+5\%)$	$0.523^{+0.001}_{-0.005} (+15\%)$
LHC@7	$2.82^{+0.06}_{-0.07} (+4\%)$	$3.17^{+0.06}_{-0.06} (+13\%)$
LHC@14	$7.17^{+0.20}_{-0.25} (+4\%)$	$7.93^{+0.14}_{-0.14} (+13\%)$

What's the source of the discrepancy?

- two formalisms resum different logs

$$s_{4,\text{Mellin}} = (p_t + p_X)^2 - m_t^2 \quad s_{4,\text{SCET}} = (k + p_X)^2$$

formally equivalent for the total cross section, but power-suppressed terms can be large.

- is one parameterization better than the other? Not completely clear...
- estimate of theory uncertainty by scale variation only is probably too optimistic



One of most recent developments in single-top physics is matching of fixed-order NLO cross section with Monte Carlo parton shower (MCPS)

- NLO:**
$$d\sigma = d\Phi_n \left\{ \underbrace{B(\Phi_n)}_{\text{LO}} + \frac{\alpha_s}{2\pi} \left[\underbrace{V(\Phi_n)}_{\text{virt.}} + \underbrace{R(\Phi_{n+1})}_{\text{real}} \right] d\Phi_r \right\}$$

- normalization of the cross section correct to order $\mathcal{O}(\alpha_s)$
- reduced renormalization and factorization scale dependence
- correct description of wide-angle radiation

- MCPS:**
$$d\sigma = d\Phi_n \underbrace{B(\Phi_n)}_{\text{LO}} \left\{ \overbrace{\Delta(t_m, t_0) + \Delta(t_m, t)}^{\text{Sudakov}} \underbrace{\frac{\alpha_s}{2\pi} \frac{1}{t} P(z) d\Phi_r}_{\text{coll.}} \right\}$$

- $\Delta(t_m, t) = \exp \left[-\frac{\alpha_s}{2\pi} \int_t^{t_m} d\Phi_r' \frac{P(z')}{t'} \right]$
- correctly describes multiple collinear emission at low p_T
- can be used to generate events down to the hadronic level

...ideal solution is clearly to combine the two approaches!

Issue: how to avoid double-counting in the collinear region?



Two different frameworks have been tested: **POWHEG** and **MC@NLO**

POWHEG: [Nason '04; Frixione, Nason, Oleari '07; ...]

Modifies Sudakov factor for hardest emission such that collinear limit is preserved and expansion in α_s of matched result reproduces exact NLO

$$\begin{aligned}
 d\sigma_{\text{POWHEG}} &= d\Phi_n \bar{B}(\Phi_n) \left\{ \overbrace{\Delta(\Phi_n, k_T^{\min})}^{\text{POWHEG Sudakov}} + \Delta(\Phi_n, k_T) \frac{\alpha_s}{2\pi} \frac{R(\Phi_{n+1})}{B(\Phi_n)} d\Phi_r \right\} \\
 \bar{B}(\Phi_n) &= B(\Phi_n) + \frac{\alpha_s}{2\pi} \left[V(\Phi_n) + \int R(\Phi_{n+1}) d\Phi_r \right] \\
 \Delta(\Phi_n, k_T) &= \exp \left[-\frac{\alpha_s}{2\pi} \int d\Phi_r \frac{R(\Phi_{n+1})}{B(\Phi_n)} \theta(k_T' - k_T) \right]
 \end{aligned}$$

MC@NLO: [Frixione, Webber '02; Frixione, Nason, Webber '03; ...]

Subtract hardest collinear emission from exact NLO matrix element and then shower

$$\begin{aligned}
 d\sigma_{\text{MC@NLO}} &= d\Phi_n \bar{B}(\Phi_n) \left\{ \Delta(t_m, t_0) + \Delta(t_m, t) \frac{\alpha_s}{2\pi} \frac{P(z)}{t} d\Phi_r \right\} \\
 &\quad + d\Phi_n d\Phi_r \left[R(\Phi_{n+1}) - R_{\text{MCS}}(\Phi_{n+1}) \right] \\
 \bar{B}(\Phi_n) &= B(\Phi_n) + \frac{\alpha_s}{2\pi} \left[V(\Phi_n) + \int R_{\text{MCS}}(\Phi_{n+1}) d\Phi_r \right]
 \end{aligned}$$



Similarities and differences between MC@NLO and POWHEG:

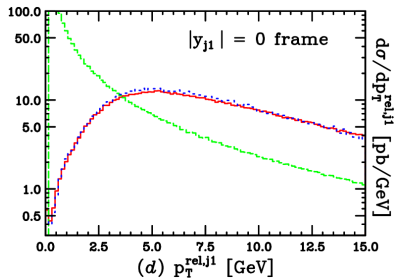
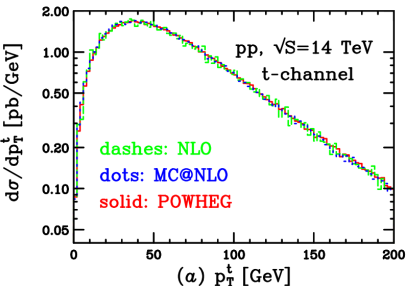
- in both frameworks double-counting is avoided
- exact NLO result reproduced upon expansion in α_s
- in MC@NLO matching depends on the MCPS used
- positive weights in POWHEG, while small number of negative-weighted events appear in MC@NLO (theoretically not a problem...)

How do POWHEG and MC@NLO numerically compare to each other (and to NLO)?

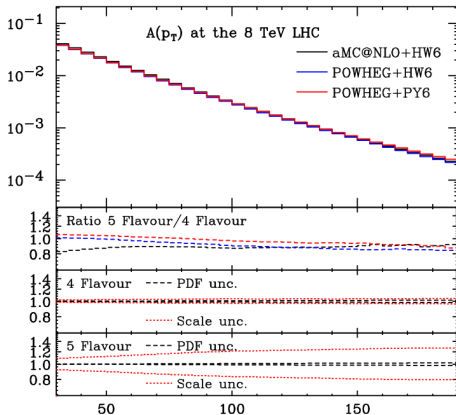
POWHEG vs MC@NLO: t-channel production



5F: [Alioli, Nason, Oleari, Re '09]; **4F**: [Frederix, Re, Torrielli '12]



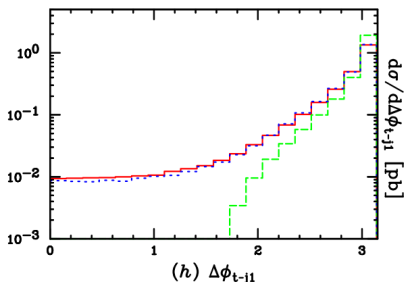
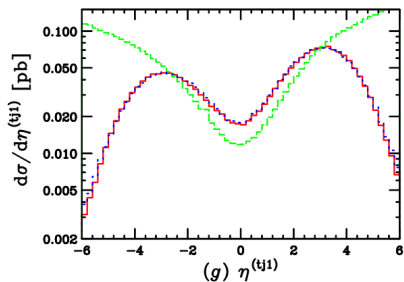
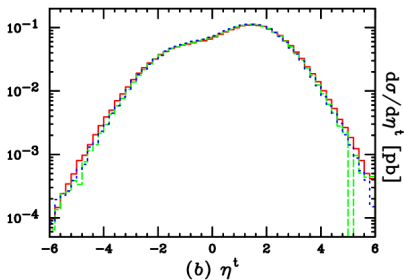
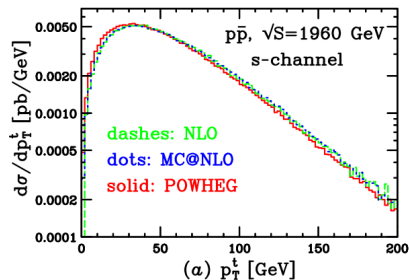
$$A(p_T) = \frac{1}{\sigma} \int_{p_T}^{\infty} dp_T^{(j_{b,2})} \frac{d\sigma}{dp_T^{(j_{b,2})}}$$



POWHEG vs MC@NLO: s-channel production



[Alioli, Nason, Oleari, Re '09]





POWHEG vs MC@NLO: tW production

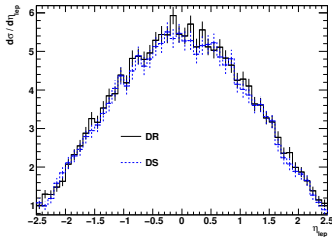
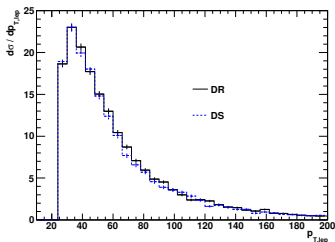
Unambiguous theoretical definition of tW production is difficult due to **interference with $\bar{t}\bar{t}$ production at NLO**

$$\mathcal{A}_{WWbb} = \overbrace{\mathcal{A}_{WWbb,tW}}^{\text{NLO single } t \text{ prod.}} + \overbrace{\mathcal{A}_{WWbb,\bar{t}\bar{t}}}^{\text{LO top-pair prod.}}$$

One can still try to define the tW signal subject to a certain set of [kinematical cuts](#).

Two schemes implemented in MC@NLO and POWHEG [[Frixione, Laenen, Motylinski, Webber, White '08](#); [White, Frixione, Laenen, Maltoni '09](#)]

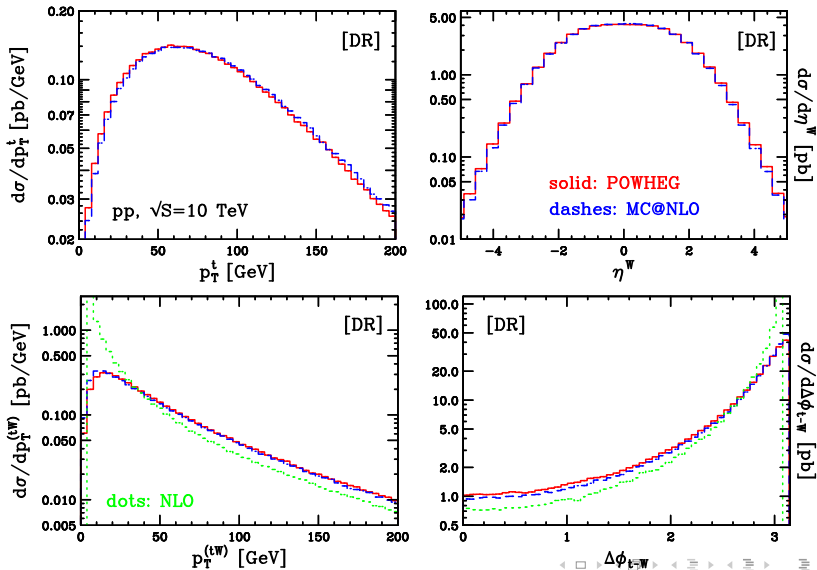
- **Diagram removal (DR):** $d\sigma_{tW}^{\text{NLO}} = d\phi_n |\mathcal{A}_{WWbb,tW}|^2$
- **Diagram subtraction (DS):** $d\sigma_{tW}^{\text{NLO}} = d\phi_n \left(|\mathcal{A}_{WWbb,tW} + \mathcal{A}_{WWbb,\bar{t}\bar{t}}|^2 - \mathcal{M}_{\text{subt.}} \right)$
 $\mathcal{M}_{\text{subt.}} \rightarrow |\mathcal{A}_{WWbb,\bar{t}\bar{t}}|^2$ when $m_{bW} \rightarrow m_t$



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[Re '10]





Theoretical understanding and modelling of single-top production in the SM has progressed significantly in the last few years!

- ⇒ NLO results for the 3 production channels matched to MC parton shower (MC@NLO and POWHEG)
- ⇒ (matched) results in the 4F scheme have also become available
 - precise (NLO) modelling of spectator- b jet observables
- ⇒ contribution of off-shell and non-factorizable corrections has been assessed
 - generally small, but can be locally large (up to 40%) near kinematical edges
- ⇒ some additional information on higher-order corrections might be inferred from soft resummation, though some discrepancies have to be clarified first...

In this talk we focused only on the SM. However **beyond-SM single-top production** has also been studied

- ⇒ anomalous couplings
- ⇒ associated $H^- t$ production
- ⇒ ...