

Vector boson plus multijet production

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Contents

- ① Motivation
- ② LO calculations and MEPS merging
- ③ NLO calculations, NLOPS matching and MEPS@NLO merging
- ④ NNLO calculations
- ⑤ Conclusions

Motivation

V +jets as a background to top physics

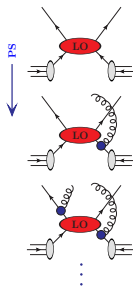
- W +jets:
 $pp \rightarrow \ell + \cancel{E}_T + \#\text{jets}$ (irreducible in semileptonic $t\bar{t}$ production)
- Z +jets:
 $pp \rightarrow \ell\ell + \#\text{jets}$ (reducible in all modes)

Need for higher accuracy

- (N)NLO calculations mandatory (QCD at large scales)
 - \Rightarrow stabilised cross sections, reliable differential distributions
- matching to parton showers (include QCD at low scales)
 - \Rightarrow hadron-level calculations
 - \Rightarrow reliable jet descriptions, leptons in jets, etc.
- multijet merging and inclusive description
 - \Rightarrow combine high-accuracy for different multiplicities
 - \Rightarrow resum multiscale logarithms

LO calculations and MEPS merging

Complementary descriptions of multiparticle final states

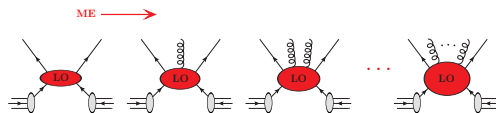


LO $pp \rightarrow 2$ with parton showers
 + exponentiation of large IR logarithms
 – poor hard/wide angle emission pattern

vs. **LO $pp \rightarrow n$ matrix elements**
 + dominant terms for hard/wide angle rad.
 – breakdown of α_s -expansion in log. region

LO calculations and MEPS merging

Complementary descriptions of multiparticle final states



LO $pp \rightarrow 2$ with parton showers

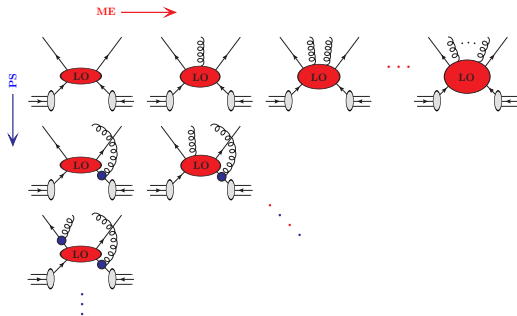
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vs. **LO** $pp \rightarrow n$ matrix elements

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LO calculations and MEPS merging

Complementary descriptions of multiparticle final states

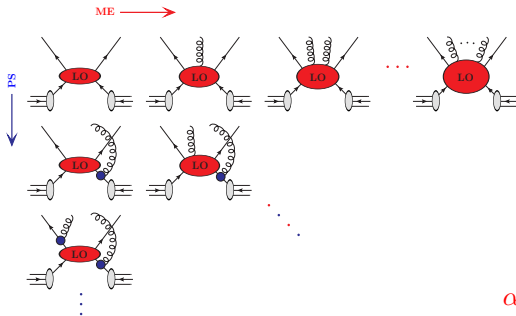


Consistent combination: MEPS-algorithms

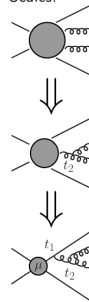
- CKKW – phase space partition into two regimes emission by emission
[Catani et.al. JHEP11\(2001\)063](#), [Lönnblad JHEP05\(2002\)046](#), [Höche et.al. JHEP05\(2009\)053](#),
[Hamilton et.al. JHEP11\(2009\)038](#), [Lönnblad, Prestel JHEP03\(2012\)019](#), ...
- MLM – phase space partition based on geometric reconstruction of jets
[Mangano et.al. Nucl.Phys.B632\(2002\)343-362](#), [Mangano et.al. JHEP01\(2007\)013](#), [Alwall et.al. JHEP02\(2009\)017](#)

LO calculations and MEPS merging

Complementary descriptions of multiparticle final states



Scales:



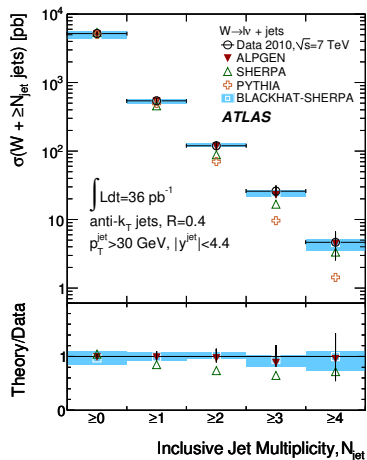
$$\alpha_s^{k+n}(\mu_{\text{eff}}) = \alpha_s^k(\mu) \alpha_s(t_1) \cdots \alpha_s(t_n)$$

Consistent combination: MEPS-algorithms

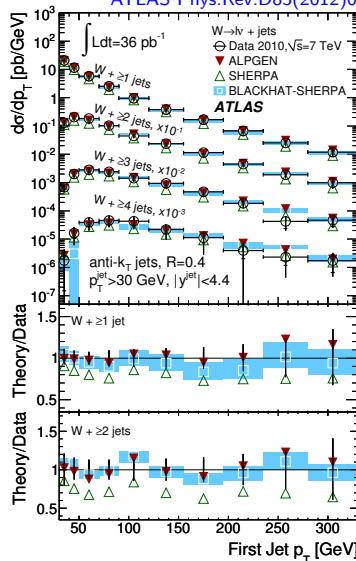
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LO calculations and MEPS merging

MEPS: LO+(N)LL accuracy
 → good agreement with data,
 but large uncertainties (not shown)

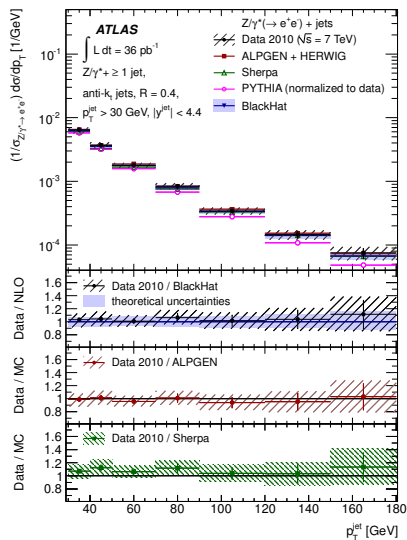
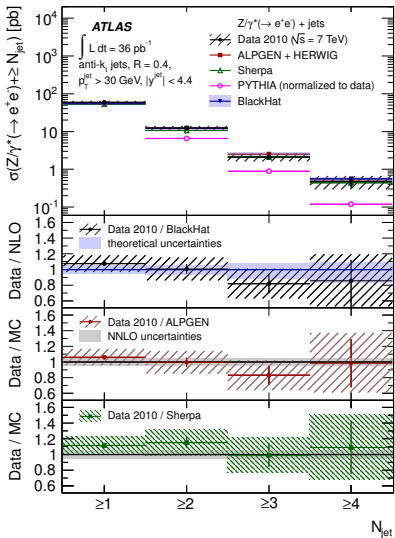


ATLAS Phys.Rev.D85(2012)092002



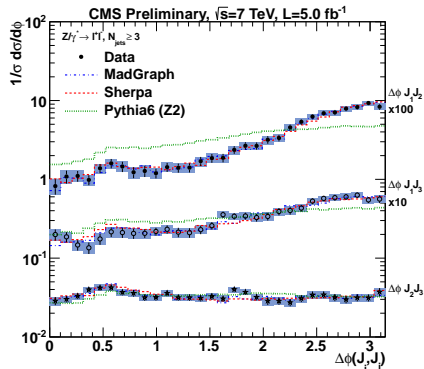
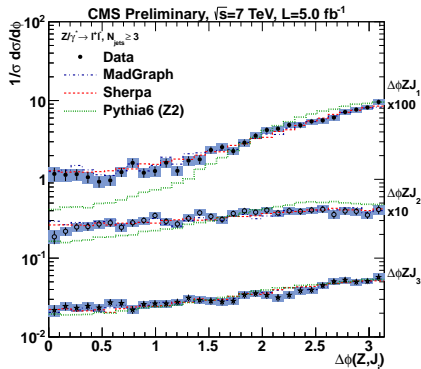
LO calculations and MEPS merging

ATLAS Phys.Rev.D85(2012)032009



LO calculations and MEPS merging

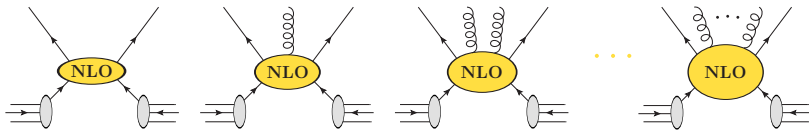
CMS-PAS-EWK-11-021



CMS measurement of correlations in Z +jets

- $Z + \geq 3$ jets
- good description of shapes by MEPS methods, norm from data

NLO calculations



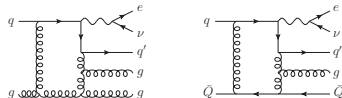
$pp \rightarrow W/Z + n \text{ jets}$

NLO calculations

- a lot of progress in recent years

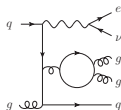
$$pp \rightarrow W + n \text{ jets}$$

n	groups
2	Campbell, Ellis Phys.Rev.D65(2002)113007
3	Ellis et.al. JHEP04(2009)077; Berger et.al. Phys.Rev.Lett.102(2009)222001
4	Berger et.al. Phys.Rev.Lett.106(2011)092001
5	BLACKHAT in preparation



$$pp \rightarrow Z + n \text{ jets}$$

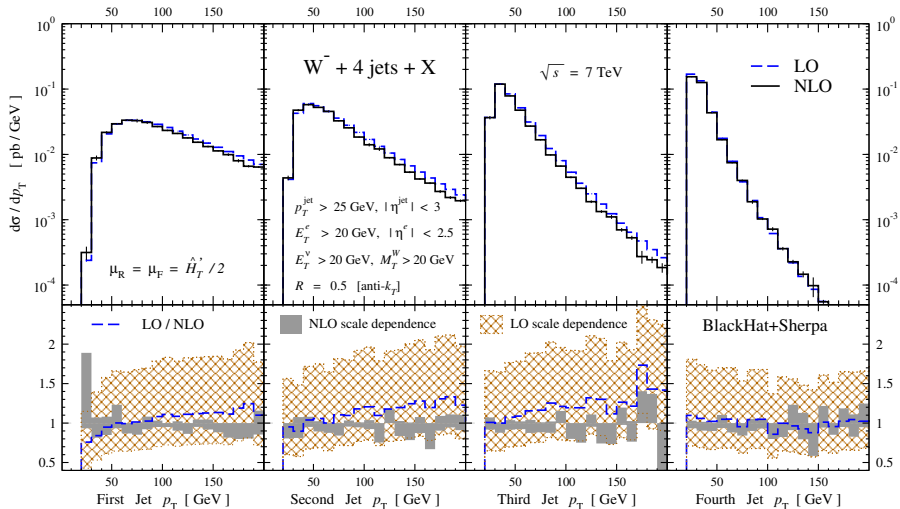
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2	Campbell, Ellis Phys.Rev.D65(2002)113007
3	Berger et.al Phys.Rev.D82(2010)074002
4	Ita et.al. Phys.Rev.D85(2012)031501



- $W/Z + \leq 2$ jets various public implementations
- $W/Z + \geq 3$ no completely public implementation/n-tuples
 - ROCKET+MCFM: generalised D -dim. unitarity
 - BLACKHAT+SHERPA: unitarity based, on-shell methods

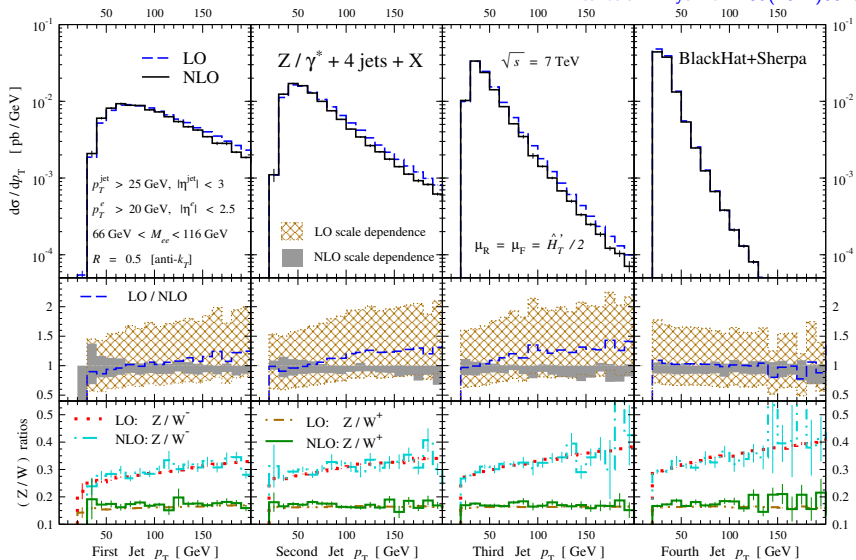
NLO state of the art

Berger et.al. Phys.Rev.Lett.106(2011)092001



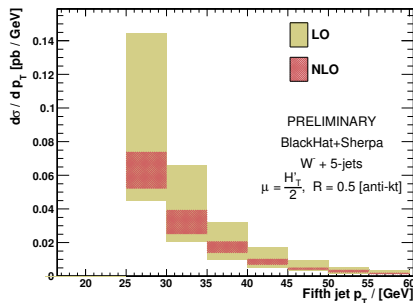
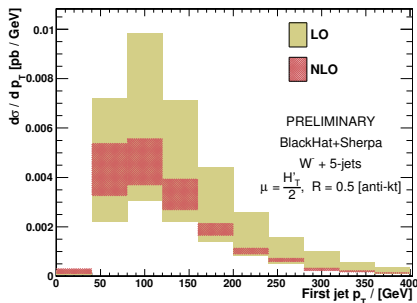
NLO state of the art

Ita et al. Phys.Rev.D85(2012)031501



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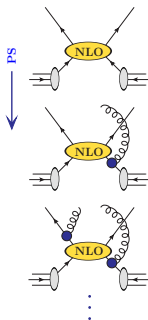
BLACKHAT in preparation



- 1st and 5th jet transverse momentum in $pp \rightarrow W + 5 \text{ jet}$ events
- BLACKHAT supplies virtual matrix elements, COMIX supplies born and real emission matrix elements, CS subtraction and phase space integration

NLOs matching

NLO calculations inclusive wrt. higher orders, therefore matching to parton showers mandatory to achieve fully exclusive description of final state.



- attach parton showers to NLO calculations
- remove overlap of real emission contribution and parton shower emission, and Sudakov and virtual correction
- retain respective accuracies \Rightarrow NLO+(N)LL

NLOs matching

NLO calculations inclusive wrt. higher orders, therefore matching to parton showers mandatory to achieve fully exclusive description of final state.

Methods:

- MC@NLO Frixione, Webber JHEP06(2002)029
 (variants of) method implemented in:
 - MC@NLO v4.0 ($V + 0$ jets) Frixione, Webber arXiv:1010.0819
 - aMC@NLO ($V + \leq 2$ jets) Frederix et.al. JHEP02(2012)048
 - SHERPA ($V + \leq 3$ jets) Höche, Krauss, MS, Siebert arXiv:1201.5882

- POWHEG Nason JHEP11(2004)040; Frixione, Nason, Oleari JHEP11(2007)070
 method implemented in:
 - POWHEG-BOX ($V + \leq 2$ jets) Alioli, Nason, Oleari, Re JHEP01(2011)095
Re arXiv:1204.5433
 - HERWIG++ ($V + 0$ jets) Hamilton, Richardson, Tully JHEP10(2008)015
 - SHERPA ($V + 0$ jets) Höche, Krauss, MS, Siebert JHEP04(2011)024

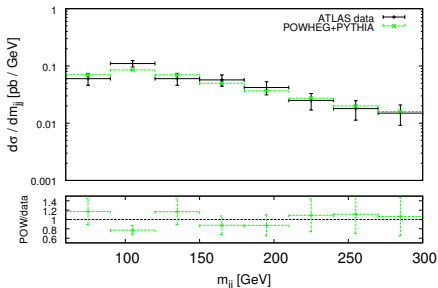
Both methods intimately related Höche, Krauss, MS, Siebert arXiv:1111.1220
Nason, Webber arXiv:1202.1251

→ differ only in choice of resummation kernel and res. phase space

NLOs matching

POWHEG $Z + 2$ jets at LHC

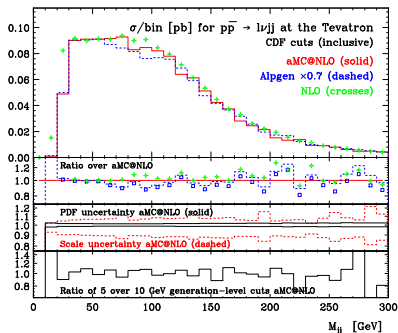
Re arXiv:1204.5433



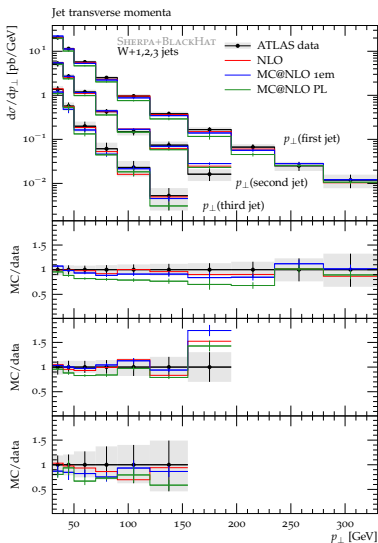
Data: ATLAS Phys.Rev.D85(2012)032009

aMC@NLO $W + 2$ jets at Tevatron

Frederix et.al. JHEP02(2012)048



NLOs matching



Höche, Krauss, MS, Siebert arXiv:1201.5882

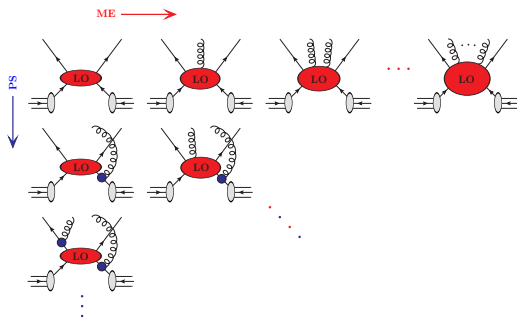
$pp \rightarrow W + 1, 2, 3$ jets with
MC@NLO-type matching

- 3 separate samples/calculations
- NLO accuracy for inclusive observables of respective jet multiplicity
- resummation of softest/LO jet, i.e. 4th jet in $pp \rightarrow W + 3$ jets
- no resummation of sample-defining jet multiplicity, i.e. first 3 jets in $pp \rightarrow W + 3$ jets
- nonetheless good description of data

Data: ATLAS Phys.Rev.D85(2012)092002

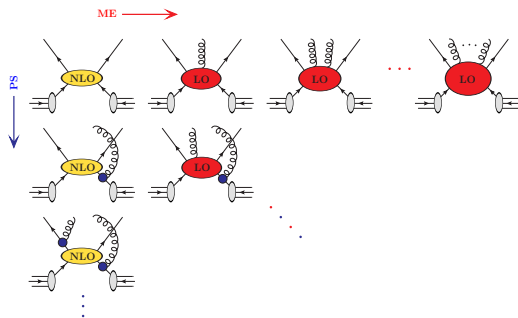
MEPs@NLO merging

Promote MEPs to higher accuracy:



MEPs@NLO merging

Promote MEPs to higher accuracy:

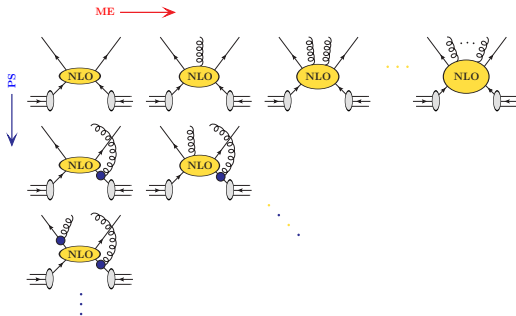


- promote lowest multiplicity to NLO:
merge one NLOs with MEPS \Rightarrow MENLOs

Bauer, Tackmann, Thaler JHEP12(2008)010
 Hamilton, Nason JHEP06(2010)039
 Höche, Krauss, MS, Siebert JHEP08(2011)123
 Höche, Krauss, MS, Siebert arXiv:1207.5031

MEPs@NLO merging

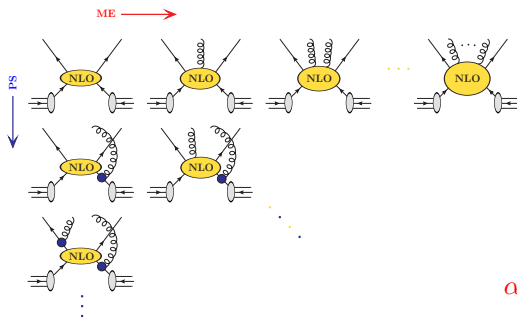
Promote MEPs to higher accuracy:



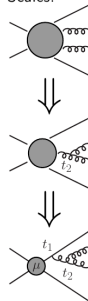
- promote all multiplicities up to n_{\max} to NLO: Lavesson, Lönnblad JHEP12(2008)070
merge NLOPS of successive multiplicity, Höche, Krauss, MS, Siebert arXiv:1207.5030
i.e. elevate MEPs to NLO \Rightarrow MEPs@NLO Höche, Krauss, MS, Siebert arXiv:1207.5031
- overlap of Sudakovs and NLO corrections spoils NLO accuracy
→ corrected for by modified truncated parton shower

MEPs@NLO merging

Promote MEPs to higher accuracy:



Scales:

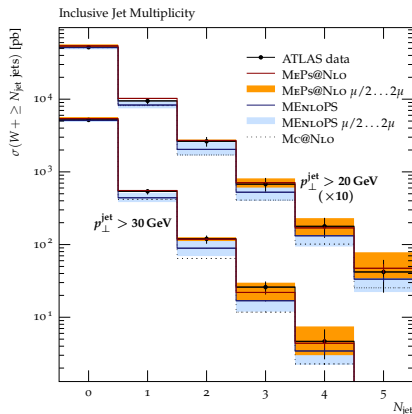


$$\alpha_s^{k+n}(\mu_{\text{eff}}) = \alpha_s^k(\mu) \alpha_s(t_1) \cdots \alpha_s(t_n)$$

defined on respective
LO configurations

- promote all multiplicities up to n_{max} to NLO:
merge NLOPS of successive multiplicity,
i.e. elevate MEPs to NLO \Rightarrow MEPs@NLO
Lavesson, Lönnblad JHEP12(2008)070
Höche, Krauss, MS, Siebert arXiv:1207.5030
Höche, Krauss, MS, Siebert arXiv:1207.5031
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MEPs@NLO merging



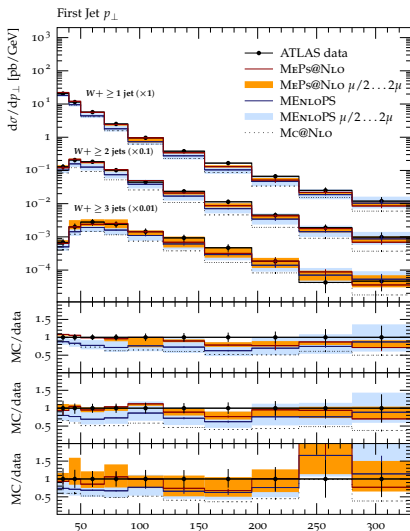
Höche, Krauss, MS, Siegert arXiv:1207.5030

$pp \rightarrow W + \text{jets}$ (0,1,2 @ NLO; 3,4 @ LO)

- NLO+(N)LL accuracy for $pp \rightarrow W + 0,1,2$ jets
- LO+(N)LL accuracy for $pp \rightarrow W + 3,4$ jets
- all jet emissions are resummed wrt. inclusive W production with $\mu_Q = m_W$
- simultaneous description of different jet multiplicities

Data: ATLAS Phys.Rev.D85(2012)092002

MEPs@NLO merging



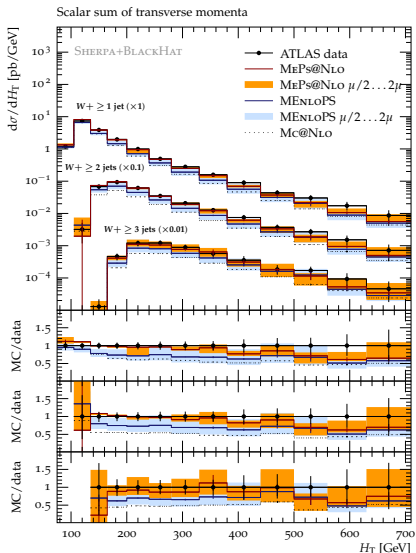
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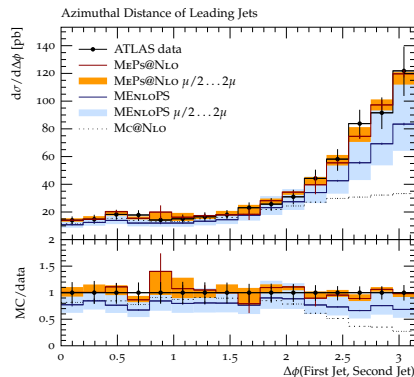
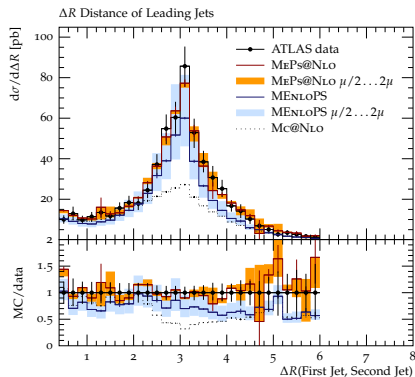
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MEPs@NLO merging

Höche, Krauss, MS, Siegert arXiv:1207.5030



Data: ATLAS data Phys.Rev.D85(2012)092002

NNLO calculations

NNLO QCD inclusive cross sections [Hamberg, van Neerven, Matsuura](#)

[Nucl.Phys.B359\(1991\)343405](#)

Fully differential NNLO QCD to inclusive W, Z production

- FEWZ [Melnikov, Petrielle Phys.Rev.Lett.96\(2006\)231803](#)
recently included NLO EW corrections [Li, Petriello arXiv:1208.5967](#)
- DYNLO [Catani, Cieri, Ferrera, de Florian, Grazzini Phys.Rev.Lett.103\(2009\)082001](#)

(N)NLO+(N)NLL resummation

- e.g. [Becher, Neubert Eur.Phys.J.C71\(2011\)1665](#), [Banfi; Salam, Zanderighi JHEP06\(2012\)159](#);
[Banfi, Dasgupta, Marzani, Tomlinson JHEP01\(2012\)044](#), ...
- observable specific resummation for inclusive production

Problems

- no matching methods to parton showers, no hadron level calculations
 - does not reach jet multiplicity relevant for top physics
- ⇒ can be used to renorm inclusive MEPS calculations

Conclusions

- highly active field
- traditional MEPS works fine for prediction of shapes, but large uncertainties (everything is LO at best)
- NLO calculations have reached final state multiplicities interesting for top physics backgrounds
- NLOPS matching techniques extended/generalised have been shown to also work with large final state multiplicities and complicated colour structures
- multijet-merging techniques have been promoted to NLO accuracy recently
- NNLO can be used for normalisation of inclusive calculations

Thank you for your attention!

Backup: MEPS merging – Scales

Divide phase space using jet measure Q_{cut} :

- emissions with $Q > Q_{\text{cut}}$ by ME
- emissions with $Q < Q_{\text{cut}}$ by PS

Shower on top of higher order ME:

Problem: ME only gives final state,
no history as PS input

Solution: Backward clustering
(inverted probabilistic PS splittings)

⇒ **ME final state with branching history and PS starting scale μ and branching scales t_i**

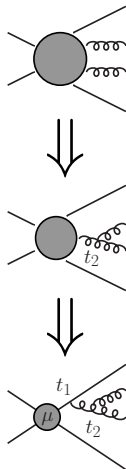
$$\alpha_s^{k+n}(\mu_{\text{eff}}) = \alpha_s^k(\mu) \alpha_s(t_1) \cdots \alpha_s(t_n)$$

Veto PS emissions with $Q > Q_{\text{cut}}$

→ Reject event → Sudakov suppression

If $t \neq Q^2$ then truncated shower necessary

Scales:



Backup: MEPS@NLO merging

Höche, Krauss, MS, Siegert arXiv:1207.5030

Gehrmann, Höche, Krauss, MS, Siegert arXiv:1207.5031

$\langle O \rangle^{\text{MEPS@NLO}}$

$$\begin{aligned}
 &= \int d\Phi_n \bar{B}_n^{(A)} \left[\Delta_n^{(A)}(t_0, \mu_Q^2) O_n \right. \\
 &\quad \left. + \int_{t_0}^{\mu_Q^2} d\Phi_1 \frac{D_n^{(A)}}{B_n} \Delta_n^{(A)}(t_{n+1}, \mu_Q^2) \Theta(Q_{\text{cut}} - Q) O_{n+1} \right] \\
 &+ \int d\Phi_{n+1} \left[R_n - D_n^{(A)} \right] \Theta(Q_{\text{cut}} - Q) \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2) O_{n+1} \\
 &+ \int d\Phi_{n+1} \bar{B}_{n+1}^{(A)} \Theta(Q - Q_{\text{cut}}) \\
 &\quad \times \left[\Delta_{n+1}^{(A)}(t_0, t_{n+1}) O_{n+1} + \int_{t_0}^{t_{n+1}} d\Phi_1 \frac{D_{n+1}^{(A)}}{B_{n+1}} \Delta_{n+1}^{(A)}(t_{n+2}, t_{n+1}) O_{n+2} \right] \\
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 &\quad \left. + \int_{t_0}^{\mu_Q^2} d\Phi_1 \frac{D_n^{(A)}}{B_n} \Delta_n^{(A)}(t_{n+1}, \mu_Q^2) \Theta(Q_{\text{cut}} - Q) O_{n+1} \right] \\
 &+ \int d\Phi_{n+1} \left[R_n - D_n^{(A)} \right] \Theta(Q_{\text{cut}} - Q) \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2) O_{n+1} \\
 &+ \int d\Phi_{n+1} \bar{B}_{n+1}^{(A)} \left[1 + \frac{B_{n+1}}{\bar{B}_{n+1}} \int_{t_{n+1}}^{\mu_Q^2} d\Phi_1 K_n \right] \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2) \Theta(Q - Q_{\text{cut}}) \\
 &\quad \times \left[\Delta_{n+1}^{(A)}(t_0, t_{n+1}) O_{n+1} + \int_{t_0}^{t_{n+1}} d\Phi_1 \frac{D_{n+1}^{(A)}}{B_{n+1}} \Delta_{n+1}^{(A)}(t_{n+2}, t_{n+1}) O_{n+2} \right] \\
 &+ \int d\Phi_{n+2} \left[R_{n+1} - D_{n+1}^{(A)} \right] \Delta_{n+1}^{(\text{PS})}(t_{n+2}, t_{n+1}) \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2) \Theta(Q - Q_{\text{cut}}) O_{n+2}
 \end{aligned}$$

Backup: MEPS@NLO merging

Höche, Krauss, MS, Siegert arXiv:1207.5030

Gehrmann, Höche, Krauss, MS, Siegert arXiv:1207.5031

$\langle O \rangle^{\text{MEPS@NLO}}$

$$\begin{aligned}
 &= \int d\Phi_n \bar{B}_n^{(A)} \left[\Delta_n^{(A)}(t_0, \mu_Q^2) O_n \right. \\
 &\quad \left. + \int_{t_0}^{\mu_Q^2} d\Phi_1 \frac{D_n^{(A)}}{B_n} \Delta_n^{(A)}(t_{n+1}, \mu_Q^2) \Theta(Q_{\text{cut}} - Q) O_{n+1} \right] \\
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 &+ \int d\Phi_{n+1} \bar{B}_{n+1}^{(A)} \left[1 + \frac{B_{n+1}}{\bar{B}_{n+1}} \int_{t_{n+1}}^{\mu_Q^2} d\Phi_1 K_n \right] \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2) \Theta(Q - Q_{\text{cut}}) \\
 &\quad \times \left[\Delta_{n+1}^{(A)}(t_0, t_{n+1}) O_{n+1} + \int_{t_0}^{t_{n+1}} d\Phi_1 \frac{D_{n+1}^{(A)}}{B_{n+1}} \Delta_{n+1}^{(A)}(t_{n+2}, t_{n+1}) O_{n+2} \right] \\
 &+ \int d\Phi_{n+2} \left[R_{n+1} - D_{n+1}^{(A)} \right] \Delta_{n+1}^{(\text{PS})}(t_{n+2}, t_{n+1}) \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2) \Theta(Q - Q_{\text{cut}}) O_{n+2}
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 &+ \int d\Phi_{n+1} \bar{B}_{n+1}^{(A)} \left[1 + \frac{B_{n+1}}{\bar{B}_{n+1}} \int_{t_{n+1}}^{\mu_Q^2} d\Phi_1 K_n \right] \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2) \Theta(Q - Q_{\text{cut}}) \\
 &\quad \times \left[\Delta_{n+1}^{(A)}(t_0, t_{n+1}) O_{n+1} + \int_{t_0}^{t_{n+1}} d\Phi_1 \frac{D_{n+1}^{(A)}}{B_{n+1}} \Delta_{n+1}^{(A)}(t_{n+2}, t_{n+1}) O_{n+2} \right] \\
 &+ \int d\Phi_{n+2} \left[R_{n+1} - D_{n+1}^{(A)} \right] \Delta_{n+1}^{(\text{PS})}(t_{n+2}, t_{n+1}) \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2) \Theta(Q - Q_{\text{cut}}) O_{n+2}
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$$\begin{aligned}
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 &\quad \left. + \int_{t_0}^{\mu_Q^2} d\Phi_1 \frac{D_n^{(A)}}{B_n} \Delta_n^{(A)}(t_{n+1}, \mu_Q^2) \Theta(Q_{\text{cut}} - Q) O_{n+1} \right] \\
 &+ \int d\Phi_{n+1} \left[R_n - D_n^{(A)} \right] \Theta(Q_{\text{cut}} - Q) \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2) O_{n+1} \\
 &+ \int d\Phi_{n+1} \bar{B}_{n+1}^{(A)} \left[1 + \frac{B_{n+1}}{\bar{B}_{n+1}} \int_{t_{n+1}}^{\mu_Q^2} d\Phi_1 K_n \right] \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2) \Theta(Q - Q_{\text{cut}}) \\
 &\quad \times \left[\Delta_{n+1}^{(A)}(t_0, t_{n+1}) O_{n+1} + \int_{t_0}^{t_{n+1}} d\Phi_1 \frac{D_{n+1}^{(A)}}{B_{n+1}} \Delta_{n+1}^{(A)}(t_{n+2}, t_{n+1}) O_{n+2} \right] \\
 &+ \int d\Phi_{n+2} \left[R_{n+1} - D_{n+1}^{(A)} \right] \Delta_{n+1}^{(\text{PS})}(t_{n+2}, t_{n+1}) \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2) \Theta(Q - Q_{\text{cut}}) O_{n+2}
 \end{aligned}$$

Backup: MEPS@NLO merging – MC counterterm

$$\left[1 + \frac{B_{n+1}}{\bar{B}_{n+1}} \int_{t_{n+1}}^{\mu_Q^2} d\Phi_1 K_n \right]$$

- same form as exponent of Sudakov form factor $\Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2)$
- truncated parton shower on n -parton configuration underlying $n + 1$ -parton event
 - ① no emission \rightarrow retain $n + 1$ -parton event as is
 - ② first emission at t' with $Q > Q_{\text{cut}}$, multiply event weight with $B_{n+1}/\bar{B}_{n+1}^{(A)}$, restart evolution at t' , do not apply emission kinematics
 - ③ treat every subsequent emission as in standard truncated vetoed shower
- generates

$$\left[1 + \frac{B_{n+1}}{\bar{B}_{n+1}} \int_{t_{n+1}}^{\mu_Q^2} d\Phi_1 K_n \right] \Delta_n^{(\text{PS})}(t_{n+1}, \mu_Q^2)$$

\Rightarrow **identify $\mathcal{O}(\alpha_s)$ counterterm with the emitted emission**

Backup: MEPS@NLO merging – scale variations

Renormalisation scales:

- determined by clustering using PS probabilities and taking the respective nodal values t_i

$$\alpha_s(\mu_R^2)^k = \prod_{i=1}^k \alpha_s(t_i)$$

- change of scales $\mu_R \rightarrow \tilde{\mu}_R$ in MEs necessitates one-loop counter term

$$\alpha_s(\tilde{\mu}_R^2)^k \left(1 - \frac{\alpha_s(\tilde{\mu}_R^2)}{2\pi} \beta_0 \sum_{i=1}^k \ln \frac{t_i}{\tilde{\mu}_R^2} \right)$$

Factorisation scale:

- μ_F determined from core n -jet process
- change of scales $\mu_F \rightarrow \tilde{\mu}_F$ in MEs necessitates one-loop counter term

$$B_n(\Phi_n) \frac{\alpha_s(\tilde{\mu}_R^2)}{2\pi} \log \frac{\mu_F^2}{\tilde{\mu}_F^2} \left(\sum_{c=q,g}^n \int_{x_a}^1 \frac{dz}{z} P_{ac}(z) f_c(x_a/z, \tilde{\mu}_F^2) + \dots \right)$$