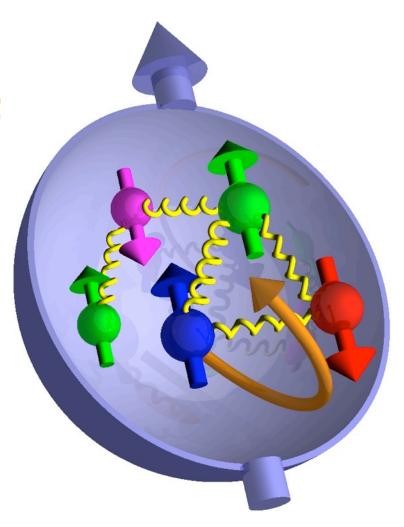


An Experimental(ist's) Overview of TMDs

N.C.R. Makins

University of Illinois at Urbana-Champaign

- L + QCD = World's Greatest Puzzle!
 intuition out the window
- The State of the Data data from COMPASS, HERMES, JLab, and RHIC
- The State of L parton orbital angular momentum
- The Missing Spin Programme
 Drell-Yan + spin



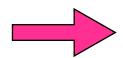
L + Relativity = Weirdness

Boosting a Dirac Spinor

at rest $\vec{p} = 0$

$$\psi = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} e^{-imt}$$

BOOST



$$\beta = p'/E' = \tanh q$$

$$\hat{B}(\hat{x},\phi) = e^{\frac{\phi}{2}\bar{\alpha}\cdot\hat{x}} = \cosh\frac{\phi}{2} \mathbf{1} + \sinh\frac{\phi}{2} \boldsymbol{\alpha}_{x}$$

$$\vec{p}' = p'\hat{x}$$

$$\psi = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} e^{-imt}$$

$$\beta = p'/E' = \tanh \phi$$

$$\hat{B}(\hat{x}, \phi) = e^{\frac{\phi}{2}\hat{a}\cdot\hat{x}} = \cosh \frac{\phi}{2} \mathbf{1} + \sinh \frac{\phi}{2} \alpha_{x}$$

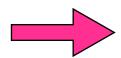
$$\psi' = N \begin{pmatrix} 1 \\ 0 \\ 0 \\ \frac{p'}{E' + m} \end{pmatrix} e^{i(p'x' - E't')}$$

Boosting a Dirac Spinor

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$$\beta = p'/E' = \tanh \phi$$

$$\hat{B}(\hat{x}, \phi) = e^{\frac{\phi}{2}\tilde{\alpha} \cdot \hat{x}} = \cosh \frac{\phi}{2} \mathbf{1} + \sinh \frac{\phi}{2} \alpha_{x}$$

$$\psi' = N \begin{pmatrix} 1 \\ 0 \\ 0 \\ \frac{p'}{E' + m} \end{pmatrix} e^{i(p'x' - E't')}$$

What's its spin?

$$\vec{\Sigma} = \left(\begin{array}{cc} \vec{\boldsymbol{\sigma}} & 0 \\ 0 & \vec{\boldsymbol{\sigma}} \end{array} \right)$$

$$\vec{\sigma} = \begin{pmatrix} \hat{z} & \hat{x} - i\hat{y} \\ \hat{x} + i\hat{y} & -\hat{z} \end{pmatrix}$$

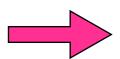
Boosting a Dirac Spinor

at rest $\vec{p} = 0$

$$\psi = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} e^{-imt}$$

BOOST

in **-x direc**ⁿ with



$$\beta = p'/E' = \tanh \phi$$

$$\hat{B}(\hat{x},\phi) = e^{\frac{\phi}{2}\vec{\alpha}\cdot\hat{x}} = \cosh\frac{\phi}{2} \mathbf{1} + \sinh\frac{\phi}{2} \boldsymbol{\alpha}_{\mathbf{x}}$$

$$\vec{p}' = p'\hat{x}$$

$$\psi = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} e^{-imt} \qquad \qquad \psi' = N \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} e^{i(p'x' - E't')}$$

$$\beta = p'/E' = \tanh \phi$$

$$\hat{B}(\hat{x}, \phi) = e^{\frac{\phi}{2}\hat{\alpha} \cdot \hat{x}} = \cosh \frac{\phi}{2} \mathbf{1} + \sinh \frac{\phi}{2} \alpha_{x}$$

$$\psi' = N \begin{pmatrix} 1 \\ 0 \\ 0 \\ \frac{p'}{E' + m} \end{pmatrix}$$



What's its spin?

$$\frac{\boldsymbol{\psi}^{\dagger} \vec{\boldsymbol{\Sigma}} \; \boldsymbol{\psi}}{\boldsymbol{\psi}^{\dagger} \boldsymbol{\psi}} = \hat{\boldsymbol{z}}$$

$$\vec{\Sigma} = \begin{pmatrix} \vec{\boldsymbol{\sigma}} & 0 \\ 0 & \vec{\boldsymbol{\sigma}} \end{pmatrix}$$

$$\vec{\sigma} = \begin{pmatrix} \hat{z} & \hat{x} - i\hat{y} \\ \hat{x} + i\hat{y} & -\hat{z} \end{pmatrix}$$

Boosting a Dirac Spinor

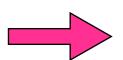
How is Lz affected by boosts?

at rest $\vec{p} = 0$

$$\boldsymbol{\psi} = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} e^{-imt}$$

BOOST

in -x direcⁿ with



$$\beta = p'/E' = \tanh \phi$$

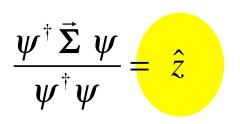
$$\hat{B}(\hat{x},\phi) = e^{\frac{\phi}{2}\bar{\alpha}\cdot\hat{x}} = \cosh\frac{\phi}{2} \mathbf{1} + \sinh\frac{\phi}{2} \boldsymbol{\alpha}_{\mathbf{x}}$$



$$\psi = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} e^{-imt} \qquad \qquad \psi' = N \begin{pmatrix} 1 \\ 0 \\ 0 \\ \beta = p'/E' = \tanh \phi \\ \hat{B}(\hat{x}, \phi) = e^{\frac{\phi}{2}\vec{\alpha} \cdot \hat{x}} = \cosh \frac{\phi}{2} \mathbf{1} + \sinh \frac{\phi}{2} \alpha_{x} \qquad \qquad e^{i(p'x' - E't')}$$



What's its spin?



$$\vec{\Sigma} = \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & \vec{\sigma} \end{pmatrix}$$

$$\vec{\sigma} = \begin{pmatrix} \hat{z} & \hat{x} - i\hat{y} \\ \hat{x} + i\hat{y} & -\hat{z} \end{pmatrix}$$

$$\vec{\Sigma} = \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & \vec{\sigma} \end{pmatrix} \qquad \frac{\psi'^{\dagger} \vec{\Sigma} \psi'}{\psi'^{\dagger} \psi'} = \hat{z} \left[1 - \left(\frac{p'}{E' + m} \right)^{2} \right]$$

$$\vec{\sigma} = \begin{pmatrix} \hat{z} & \hat{x} - i\hat{y} \\ \hat{x} + i\hat{y} & -\hat{z} \end{pmatrix} \qquad \approx \hat{z} \frac{1}{\gamma^{2}} \quad \text{for } \gamma \gg 1$$

Why there are no transversely polarized electron machines!

Boosting L
$$M^{\mu\nu} = x^{\mu} p^{\nu} - x^{\nu} p^{\mu} = \begin{pmatrix} 0 & tp_{x} - xE & tp_{y} - yE & tp_{z} - zE \\ \cdot & 0 & L_{z} & -L_{y} \\ \cdot & \cdot & 0 & L_{x} \\ \cdot & \cdot & 0 & 0 \end{pmatrix}$$

Simple orbit with L_z only: $p_z=0$, $z=0 \rightarrow L_x=L_y=0$ and apply boost β in –x direction

Boosting L

sting L
$$M^{\mu\nu} = x^{\mu} p^{\nu} - x^{\nu} p^{\mu} = \begin{pmatrix} 0 & tp_{x} - xE & tp_{y} - yE & tp_{z} - zE \\ \cdot & 0 & L_{z} & -L_{y} \\ \cdot & \cdot & 0 & L_{x} \\ \cdot & \cdot & \cdot & 0 \end{pmatrix}$$

Simple orbit with L_z only: $p_z=0$, $z=0 \rightarrow L_x=L_y=0$ and apply boost β in -x direction

$$\rightarrow L'_z = \gamma L_z - \gamma \beta p_v(ct) + \gamma \beta y(E/c)$$

Boosting L

sting L
$$M^{\mu\nu} = x^{\mu}p^{\nu} - x^{\nu}p^{\mu} = \begin{pmatrix} 0 & tp_{x} - xE & tp_{y} - yE & tp_{z} - zE \\ \cdot & 0 & L_{z} & -L_{y} \\ \cdot & \cdot & 0 & L_{x} \\ \cdot & \cdot & \cdot & 0 \end{pmatrix}$$

Simple orbit with L_z only: $p_z=0$, $z=0 \rightarrow L_x=L_y=0$ and apply boost β in -x direction

$$\vec{r}_{CM}(t) \times \vec{p}$$

$$\mathbf{H} = \boldsymbol{\alpha} \cdot \vec{p} + \boldsymbol{\beta} \, m = \begin{pmatrix} m\mathbf{1} & -i\vec{\boldsymbol{\sigma}} \cdot \vec{\nabla} \\ -i\vec{\boldsymbol{\sigma}} \cdot \vec{\nabla} & m\mathbf{1} \end{pmatrix}$$

$$\vec{\mathbf{L}}(\vec{x}) = 1 \ \vec{x} \times \vec{p}$$
$$= -1 \ i \ \vec{x} \times \vec{\nabla}$$

$$\vec{\Sigma} = \left(\begin{array}{cc} \vec{\boldsymbol{\sigma}} & 0 \\ 0 & \vec{\boldsymbol{\sigma}} \end{array} \right)$$

$$[\boldsymbol{\sigma}_{i}, \boldsymbol{\sigma}_{j}] = 2i \varepsilon_{ijk} \boldsymbol{\sigma}_{k}$$

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$$\vec{\mathbf{L}}(\vec{x}) = 1 \ \vec{x} \times \vec{p}$$

$$= -1 \ i \ \vec{x} \times \vec{\nabla}$$

L position-dependent, doesn't commute w ∂_i in **H**

$$[\mathbf{H}, \vec{\mathbf{L}}(x_i)] = -\vec{\boldsymbol{\alpha}} \times \vec{\nabla}$$

L NOT CONSERVED

$$\vec{\Sigma} = \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & \vec{\sigma} \end{pmatrix}$$

$$[\boldsymbol{\sigma}_{i}, \boldsymbol{\sigma}_{j}] = 2i \varepsilon_{ijk} \boldsymbol{\sigma}_{k}$$

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L NOT CONSERVED

$$\vec{\Sigma} = \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & \vec{\sigma} \end{pmatrix}$$
 Pauli matrices in Σ and H don't commute

$$[\mathbf{H}, \vec{\Sigma}] = 2\vec{\alpha} \times \vec{\nabla}$$

$$[\boldsymbol{\sigma}_i, \boldsymbol{\sigma}_j] = 2i \, \varepsilon_{ijk} \, \boldsymbol{\sigma}_k$$

SPIN NOT CONSERVED

$$\mathbf{H} = \boldsymbol{\alpha} \cdot \vec{p} + \boldsymbol{\beta} \, m = \begin{pmatrix} m\mathbf{1} & -i\vec{\boldsymbol{\sigma}} \cdot \vec{\nabla} \\ -i\vec{\boldsymbol{\sigma}} \cdot \vec{\nabla} & m\mathbf{1} \end{pmatrix}$$

$$\vec{\mathbf{L}}(\vec{x}) = 1 \ \vec{x} \times \vec{p}$$

$$= -1 \ i \ \vec{x} \times \vec{\nabla}$$

L position-dependent, doesn't commute w ∂_i in **H**

$$[\mathbf{H}, \vec{\mathbf{L}}(x_i)] = -\vec{\boldsymbol{\alpha}} \times \vec{\nabla}$$

L NOT CONSERVED

no shells!

$$\vec{\Sigma} = \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & \vec{\sigma} \end{pmatrix}$$
 Pauli matrices in Σ and H don't commute

$$[\mathbf{H}, \vec{\Sigma}] = 2\vec{\alpha} \times \vec{\nabla}$$

SPIN NOT CONSERVED

intuition?

$$[\boldsymbol{\sigma}_i, \boldsymbol{\sigma}_j] = 2i \, \varepsilon_{ijk} \, \boldsymbol{\sigma}_k$$

Dirac particle in a central potential

We denote the solution of the above-mentioned equation by the Dirac four-spinor ψ and/or its upper- and lower-component, the corresponding two-spinors φ and χ . The stationary states are characterized by the following set of quantum numbers ε , j, m and P which are respectively the eigenvalues of the operators \hat{H} (the Hamiltonian), \hat{j}^2 , \hat{j}_z (total angular momentum and its z-component) and \hat{P} (the parity). Since every eigenstate of the valence quark characterized by ε , j, m and P corresponds to two different orbital angular momenta l and $l' = l \pm 1$, (see Appendix A), it is clear that orbital motion is involved in every stationary state. This is true also when the valence quark is in its ground state ($\psi_{\varepsilon jmP}$ where $\varepsilon = \varepsilon_0$, j = 1/2, $m = \pm 1/2$, $P = +^2$). This state can be expressed as follows:

$$\psi_{\varepsilon_0 1/2 m+}(r, \theta, \phi) = \begin{pmatrix} f_0(r) \Omega_0^{1/2 m}(\theta, \phi) \\ g_1(r) \Omega_1^{1/2 m}(\theta, \phi) \end{pmatrix}.$$
 (2.1)

The angular part of the two-spinors can be written in terms of spherical functions $Y_{ll_z}(\theta,\phi)$ and (non-relativistic) spin-eigenfunctions which are nothing else but the Pauli-spinors $\xi(\pm 1/2)$:

$$\Omega_0^{1/2 m}(\theta, \phi) = Y_{00}(\theta, \phi) \xi(m),$$

The spherical solutions of a Dirac particle in a central potential are discussed in some of the text books (see, for example, Landau, L.D., Lifshitz, E.M.: Course of theoretical physics. Vol. 4: Relativistic quantum theory. New York: Pergamon 1971). The notations and conventions we use here are slightly different. In order to avoid possible misunderstanding, we list the general form of some of the key formulae in the following:

In terms of spherical variables, a state with given ε , j, m and P can be written as:

$$\psi_{\varepsilon_{jmP}}(r,\theta,\phi) = \begin{pmatrix} f_{\varepsilon l}(r)\Omega_{l}^{jm}(\theta,\phi) \\ (-1)^{(l-l'+1)/2}g_{\varepsilon l'}(r)\Omega_{l'}^{jm}(\theta,\phi) \end{pmatrix}.$$
(A1)

Here $l=j\pm 1/2$, l'=2j-l and $P=(-1)^l$; Ω_l^{lm} and Ω_l^{lm} are two-spinors which, for the possible values of l, are given by:

$$\Omega_{l=j-1/2}^{jm}(\theta,\phi) = \sqrt{\frac{j+m}{2j}} Y_{l l_z=m-1/2}(\theta,\phi) \xi(1/2) + \sqrt{\frac{j-m}{2j}} Y_{l l_z=m+1/2}(\theta,\phi) \xi(-1/2), \tag{A2}$$

$$\Omega_{l=j+1/2}^{jm}(heta,\phi)$$

$$= -\sqrt{\frac{j-m+1}{2j+2}} Y_{ll_z=m-1/2}(\theta,\phi) \xi (1/2)$$

$$+\sqrt{\frac{j+m+1}{2j+2}} Y_{ll_z=m+1/2}(\theta,\phi) \xi (-1/2). \tag{A3}$$

Here, $\xi(\pm 1/2)$ stand for the eigenfunctions for the spin-operator $\hat{\sigma}_z$ with eigenvalues ± 1 , and $Y_{I/z}(\theta, \phi)$ for the spherical harmonics which form a standard basis for the orbital angular momentum operators $(\hat{\mathbf{I}}^2, \hat{I}_z)$. The function $f_{eI}(r)$ and $g_{eI'}(r)$ are solutions of the coupled differential equations:

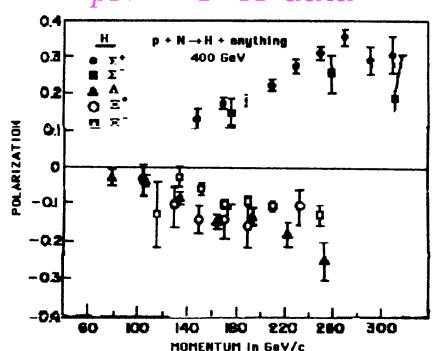
The Wacky World of Hyperon Polarization

Unpolarized beams on unpolarized targets produce hyperons which are strongly polarized!

... direction is
$$\hat{n} = \mathbf{p}_{\mathrm{beam}} \times \mathbf{p}_Y$$

$$d\sigma_{UUT} \sim \sin(\phi_h^l - \phi_{S_h}^l) \cdot f_1(x) D_{1T}^{\perp(1)}(z) = \bullet - \bullet$$

$pN \to Y^{\uparrow}X$ data



Hyperon spin structure in CQM:

$$egin{array}{lll} m{p} & \Delta u = +4/3, \; \Delta d = -1/3, \; \; \; \Delta s = 0 \\ m{\Lambda} & \Delta s = +1, \; \; \; \Delta u = \Delta d = 0 \\ m{\Sigma}^{\pm} & \Delta s = -1/3, \; \; \Delta u, d = +4/3 \\ m{\Xi}^{\pm} & \Delta s = +4/3, \; \; \Delta u, d = -1/3 \end{array}$$

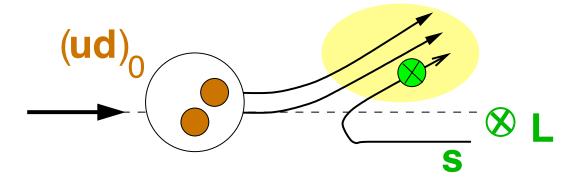
 \Rightarrow sign of polarization is opposite to Δs ...

Thomas Precession & the DGM Model

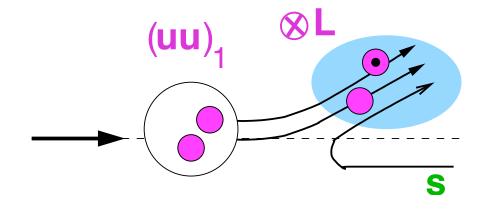
Thomas precession: relativistic effect due [boost, rotation] ≠ 0 ...

→ 'spin-orbit' pseudo-force that aligns L and S of accelerating particle

 Λ : $\Delta s = +1$ P_{Λ} from accelerated sea s quark



 Σ^+ : $\Delta u = +4/3$ P_{Σ} from accelerated valence $(uu)_1$ diquark



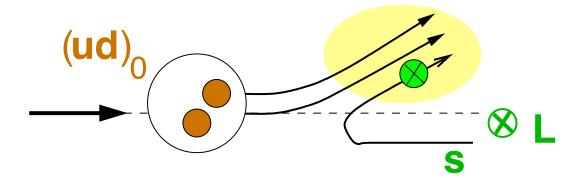
DGM model did pretty well

Thomas Precession & the DGM Model

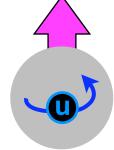
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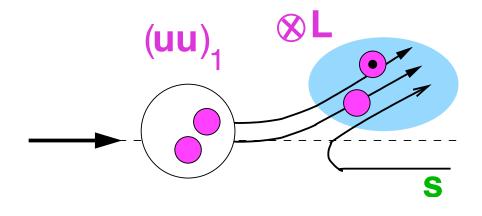
 Λ : $\Delta s = +1$ P_{Λ} from accelerated sea s quark

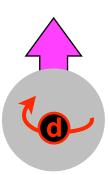


relevant?



 Σ^+ : $\Delta u = +4/3$ P_{Σ} from accelerated valence $(uu)_1$ diquark





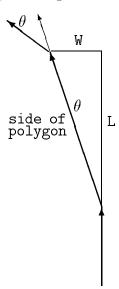
DGM model did pretty well

3 A Simple Derivation of the Thomas Precession

The following derivation is based upon a suggestion by E.M. Purcell.

Imagine an aricraft flying in a large circular orbit. Approximate the orbit by a polygon of N sides, with N a very large number. As the aircraft traverses each of the N sides, it changes its angle of flight by the angle $\theta = 2\pi/N$ as shown in the figure.

G.F. Smoot lecture notes



After the aircraft has flown N segments, it is back at its starting point. IN the laboratory frame, the aircraft has rotated through an angle of 2π radians. However in the aircraft's instantaneous rest frame, the triangles shown have a Lorentz-contraction along the direction it is flying but not transversely. Thus at the end of each segment, in the aircraft frame, the aircraft turns by a larger angle than the laboratory $\theta = 2\pi/N$, but by an angle $\theta' = \gamma \theta = W/(L/\gamma) = 2\pi\gamma/N$. After all N segements in the aircraft instanteous rest frame the total angle of rotation is $2\pi\gamma$.

The difference in the reference frame is

$$\Delta\theta = 2\pi(\gamma - 1)$$

Since N has dropped out of the formula for the angle and angle difference, one can let it go to infinity and the motion is circular and the formula is for the rate of precession.

$$\frac{\omega_P}{\omega} = \frac{\Delta\theta/T}{2\pi/T} = \gamma - 1$$

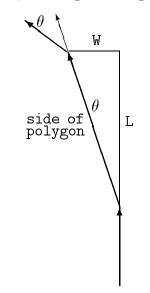
This equation, dispite the simplicity of the derivation, is the exact expression for the Thomas precession. The equation does not include the oscillationg term because the derivation neglected the fact that the front and rear of the inertial bars IWHSS'12, Lisboa, Apr 16-18, 2012 are not accelerated simultaneously.

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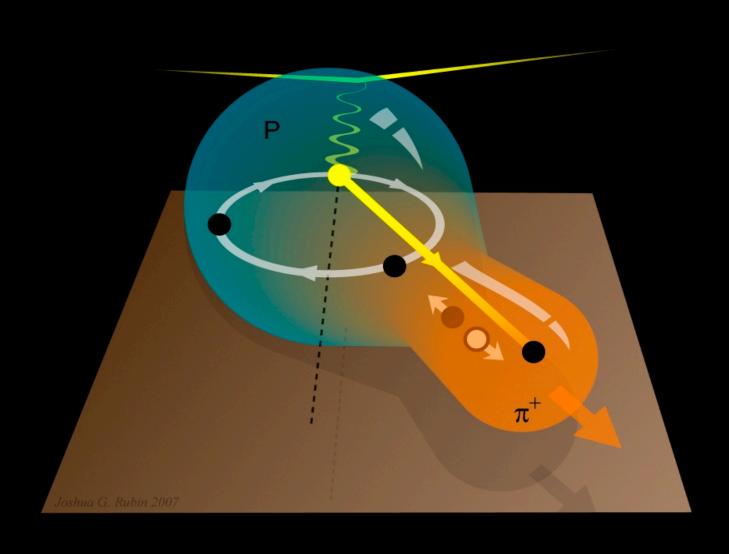
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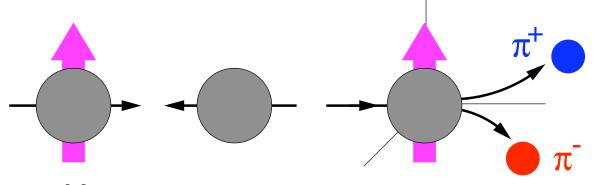
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TMDs and Single Spin Asymmetries



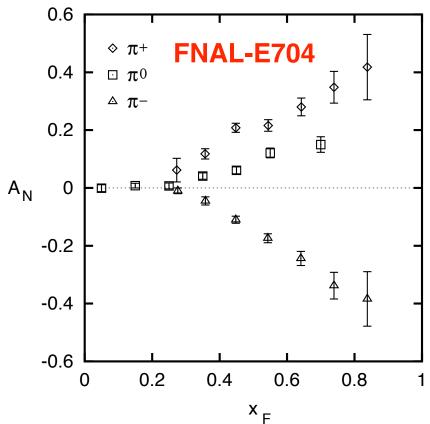
Single-spin asymmetries in $p^{\uparrow}p \rightarrow \pi X$

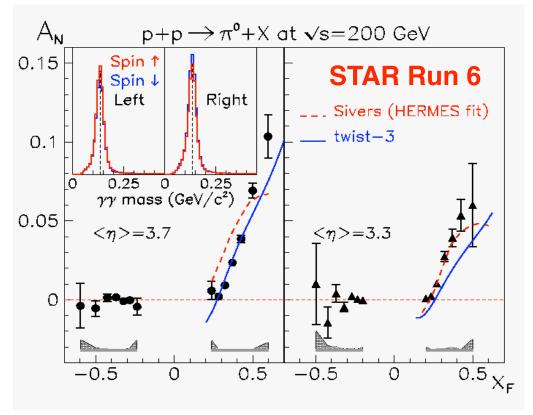
Analyzing Power



$$A_N = \frac{1}{P_{\text{beam}}} \frac{N_{\text{left}}^{\pi} - N_{\text{right}}^{\pi}}{N_{\text{left}}^{\pi} + N_{\text{right}}^{\pi}}$$

Huge <u>single-spin asymmetry</u> for *forward* meson production

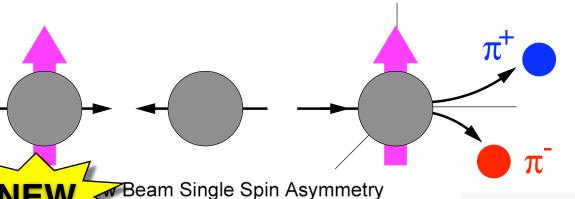




Observable $\vec{S}_{\text{beam}} \cdot (\vec{p}_{\text{beam}} imes \vec{p}_{\pi})$ odd under naive Time-Reversal

Single-spin asymmetries in $p^{\uparrow}p \rightarrow \pi X$

Analyzing Power



Eta

Pi₀

.60

.65

.55

 X_{F}

STAR 2006 PRELIMINARY

0.8

0.6

0.4

0.2

.35

.40

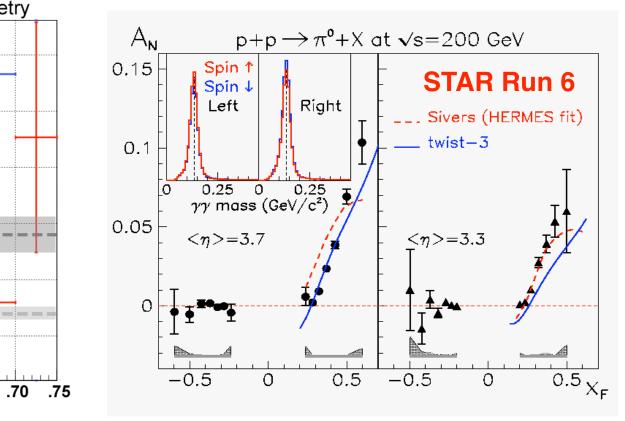
.45

.50

 A_N

$$A_N = \frac{1}{P_{\text{beam}}} \frac{N_{\text{left}}^{\pi} - N_{\text{right}}^{\pi}}{N_{\text{left}}^{\pi} + N_{\text{right}}^{\pi}}$$

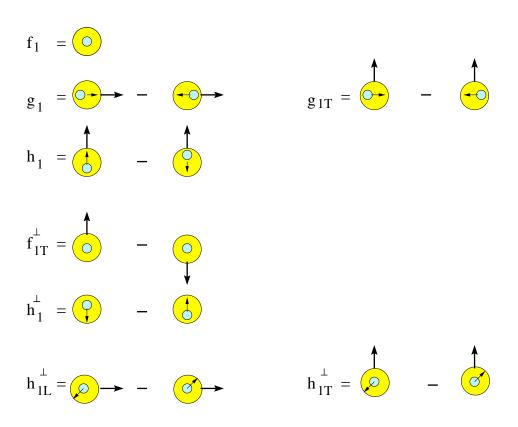
Huge <u>single-spin asymmetry</u> for *forward* meson production

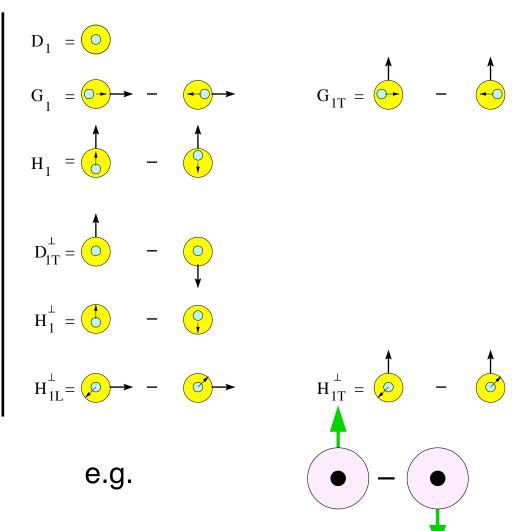


Observable $\vec{S}_{\text{beam}} \cdot (\vec{p}_{\text{beam}} \times \vec{p}_{\pi})$ odd under naive Time-Reversal

Distribution Functions

Fragmentation Functions



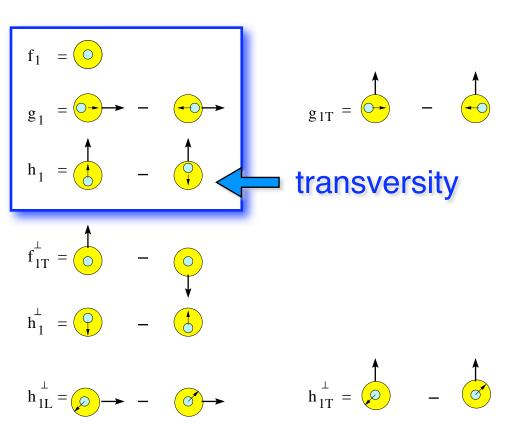


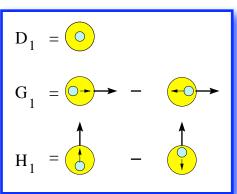
PDFs *surviving* on integration over Transverse Momentum

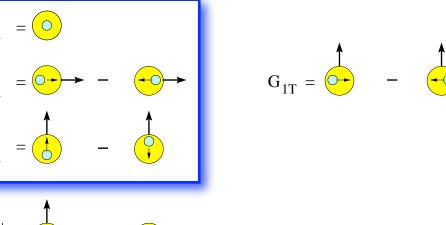
Mulders & Tangerman, NPB 461 (1996) 197

Distribution Functions

Fragmentation Functions







$$H_{1}^{\perp} = \bigcirc \qquad - \qquad \bigcirc$$

$$H_{1L}^{\perp} = \bigcirc \rightarrow \qquad - \qquad \bigcirc$$

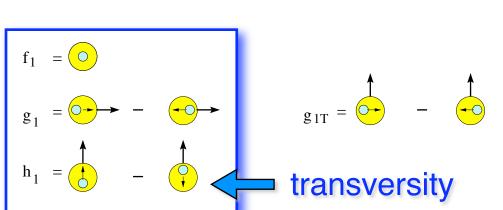
e.g.

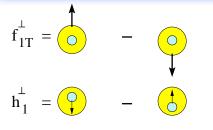
PDFs *surviving* on integration over Transverse Momentum The others are sensitive to *intrinsic* k_T in the nucleon & in the fragmentation process

→ **TMD** = transv-momentum dependent func

Mulders & Tangerman, NPB 461 (1996) 197

Distribution Functions

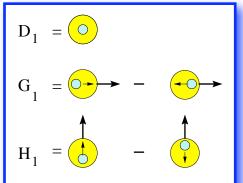


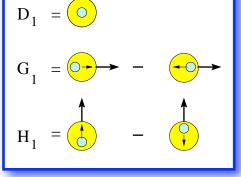


$$h_{1L}^{\perp} = \bigcirc \longrightarrow - \bigcirc \bigcirc$$

$$a_{1T}^{\perp} = \bigcirc$$
 -

Fragmentation Functions



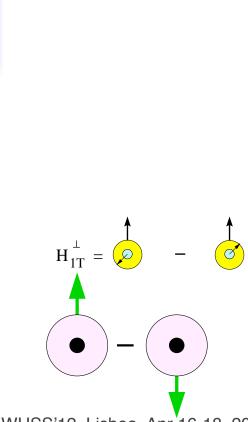


$$D_{1T}^{\perp} = \bigcirc$$
 -

$$H_1^{\perp} = \bigcirc$$
 -

$$H_{1L}^{\perp} = \bigcirc \longrightarrow - \bigcirc \bigcirc$$

e.g.

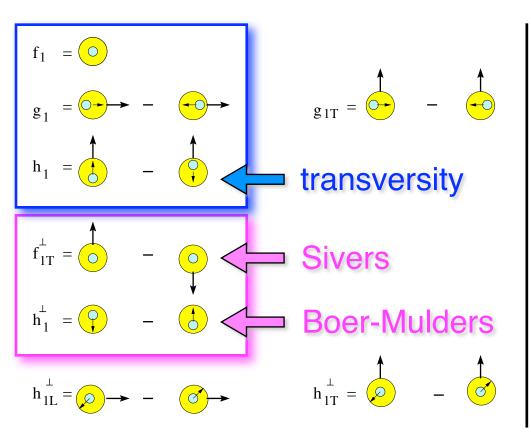


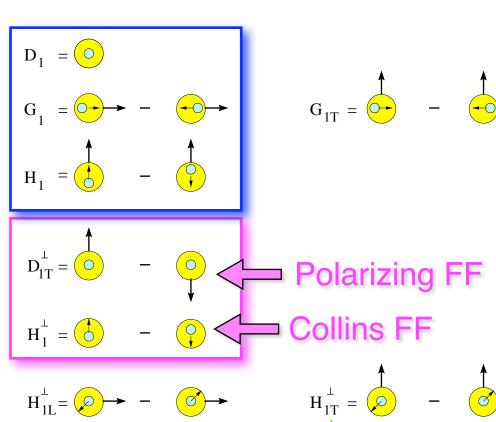
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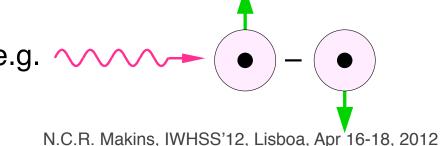




Fragmentation Functions

One <u>T-odd</u> function required to produce <u>SSA</u> = single-spin asymmetries in

hard-scattering → related to parton *L* (OAM)

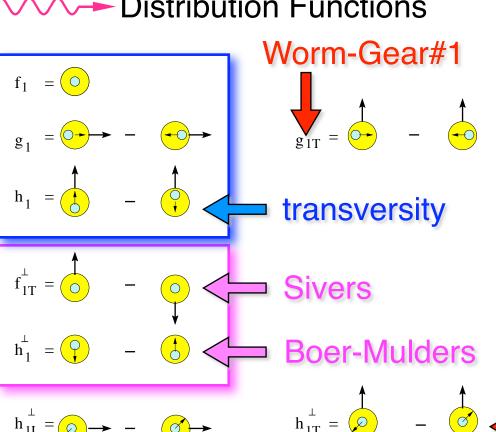


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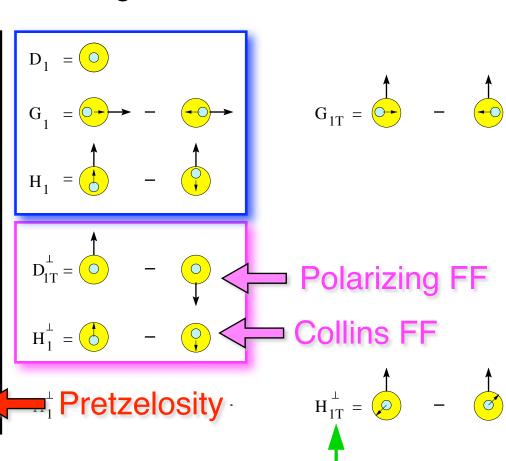
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Distribution Functions



Fragmentation Functions

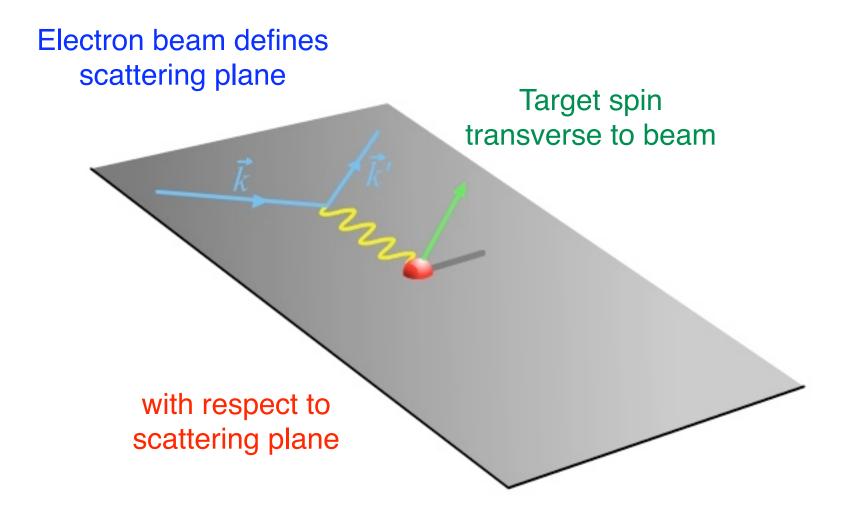


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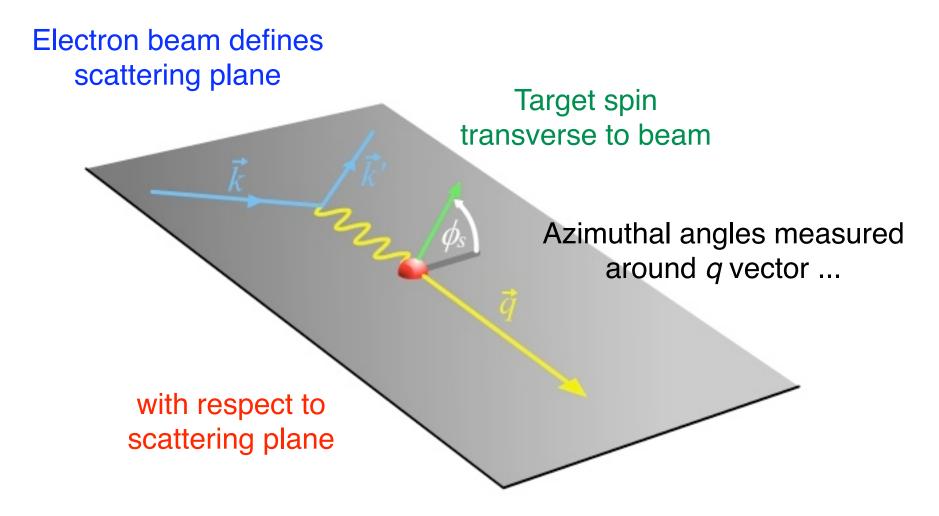
hard-scattering → related to parton *L* (*OAM*)

N.C.R. Makins, IWHSS'12, Lisboa, Apr 16-18, 2012

Measure dependence of hadron production on two azimuthal angles

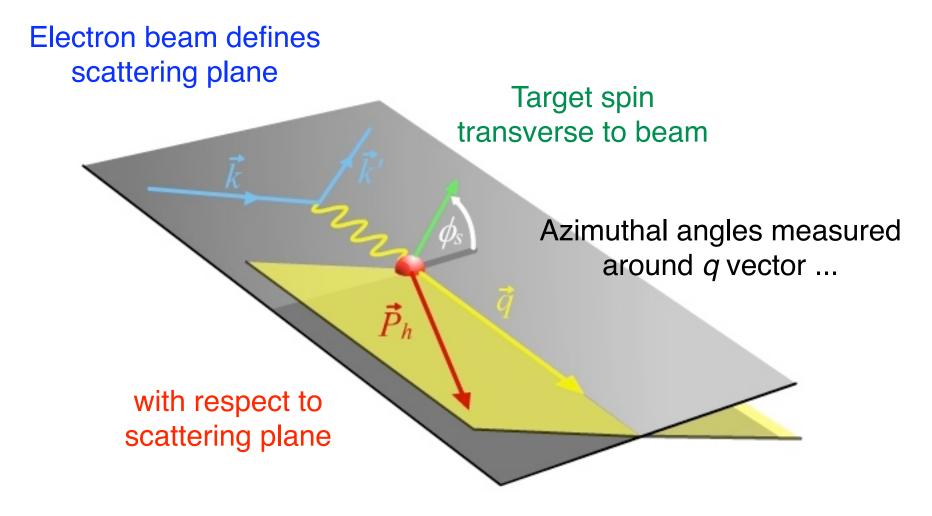


Measure dependence of hadron production on two azimuthal angles



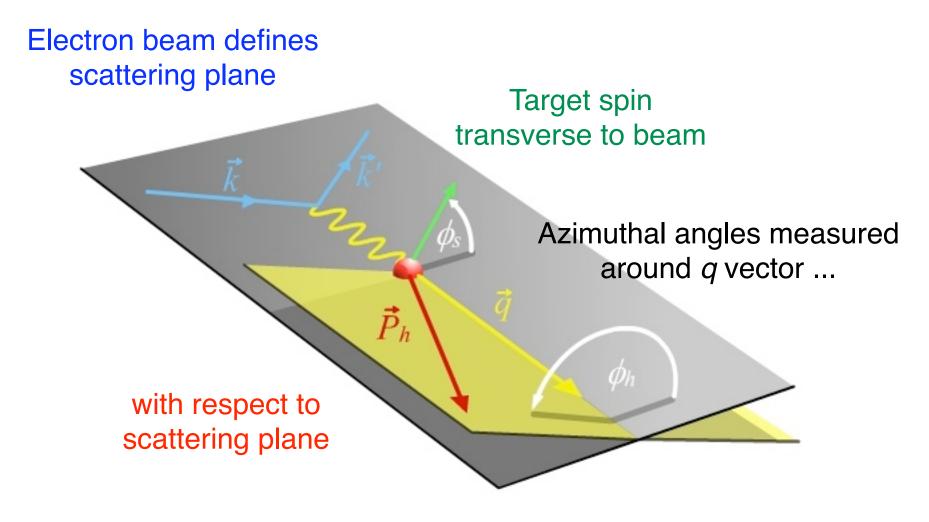
 Φ_S = target spin orientation

Measure dependence of hadron production on two azimuthal angles



 ϕ_S = target spin orientation

Measure dependence of hadron production on two azimuthal angles



 Φ_S = target spin orientation

 Φ_h = hadron direction

beam target pol<u>n</u> poln

Measuring: Azimuthal Asymmetries

SIDIS, at leading twist

 $\cos(2\phi_h^l)$

$$\otimes f_1 = \bullet$$

$$\otimes h_1^{\perp} = \bullet - \bullet$$

$$\otimes D_1 = \bullet$$

$$\otimes H_1^{\perp} = \bullet$$

 $\sin(2\phi_h^l)$

$$\otimes h_{1L}^{\perp} = \bullet - \bullet - \bullet - \bullet$$

$$\otimes H_1^{\perp} = \bullet$$

 $\otimes H_1^{\perp} = \textcircled{-}$

UT $\sin(\phi_h^l + \phi_S^l)$

$$\sin(\phi_h^l + \phi_S^l)$$

$$\otimes h_1 = \bullet$$

$$\otimes f_{1T}^{\perp} = \bullet_{-\bullet}$$

$$\otimes D_1 = \bullet$$

$$\sin(3\phi_h^l - \phi_S^l)$$

$$\sin(3\phi_h^l - \phi_S^l) \quad \otimes h_{1T}^{\perp} = \bullet$$

$$\otimes H_1^{\perp} = \bullet$$

$$\otimes g_1 = \bullet \bullet \bullet$$

$$\otimes D_1 = \bullet$$

LT
$$\cos(\phi_h^l - \phi_S^l)$$

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UL
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$$\otimes h_{1L}^{\perp} = \bullet - \bullet - \bullet$$

$$\otimes H_1^{\perp} = \bullet$$

$$\mathsf{UT} \quad \sin(\phi_h^l + \phi_S^l)$$

$$\sin(\phi_h^l - \phi_S^l)$$

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$$\otimes H_1^{\perp} = \textcircled{1}^{-} \textcircled{7}$$

$$\otimes D_1 = \bullet$$

$$\sin(3\phi_h^l - \phi_S^l)$$

$$\otimes h_{1T}^{\perp} = \bullet - \bullet$$

$$\otimes H_1^{\perp} = \textcircled{1} - \textcircled{1}$$

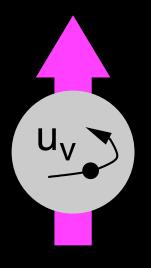
$$\otimes g_1 = \bullet \bullet \bullet$$

$$\otimes D_1 = \bullet$$

LT
$$\cos(\phi_h^l - \phi_S^l)$$

$$\cos(\phi_h^l - \phi_S^l) \qquad \otimes g_{1T} = \bullet - \bullet$$

$$\otimes D_1 = \bullet$$



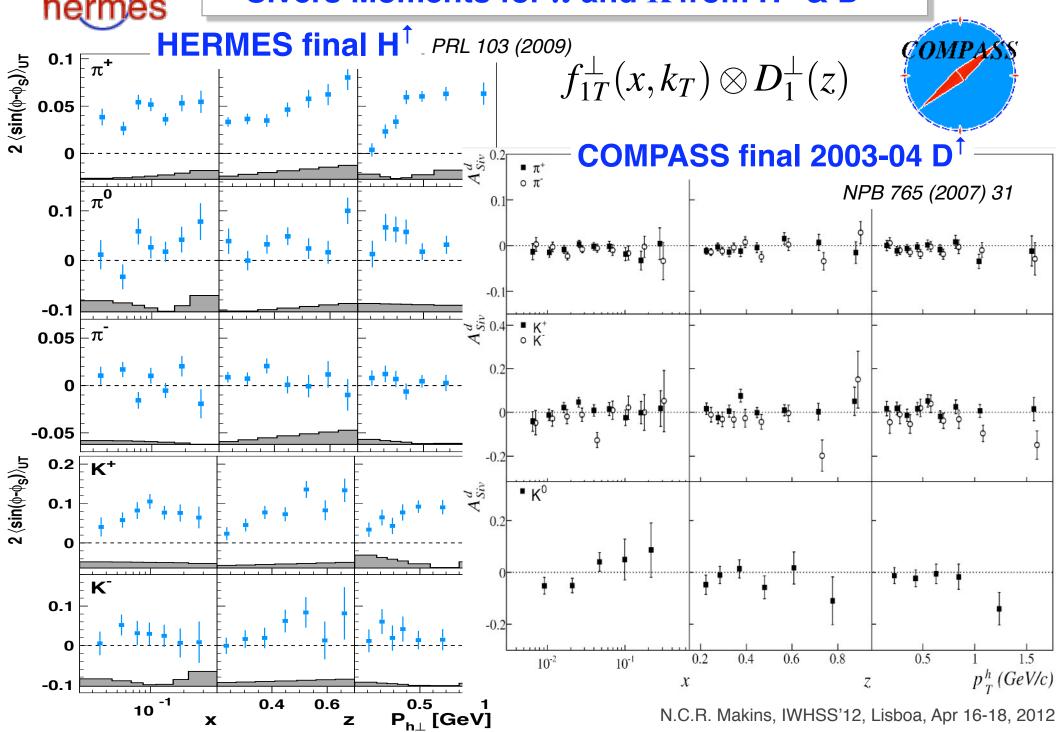
correlated with the

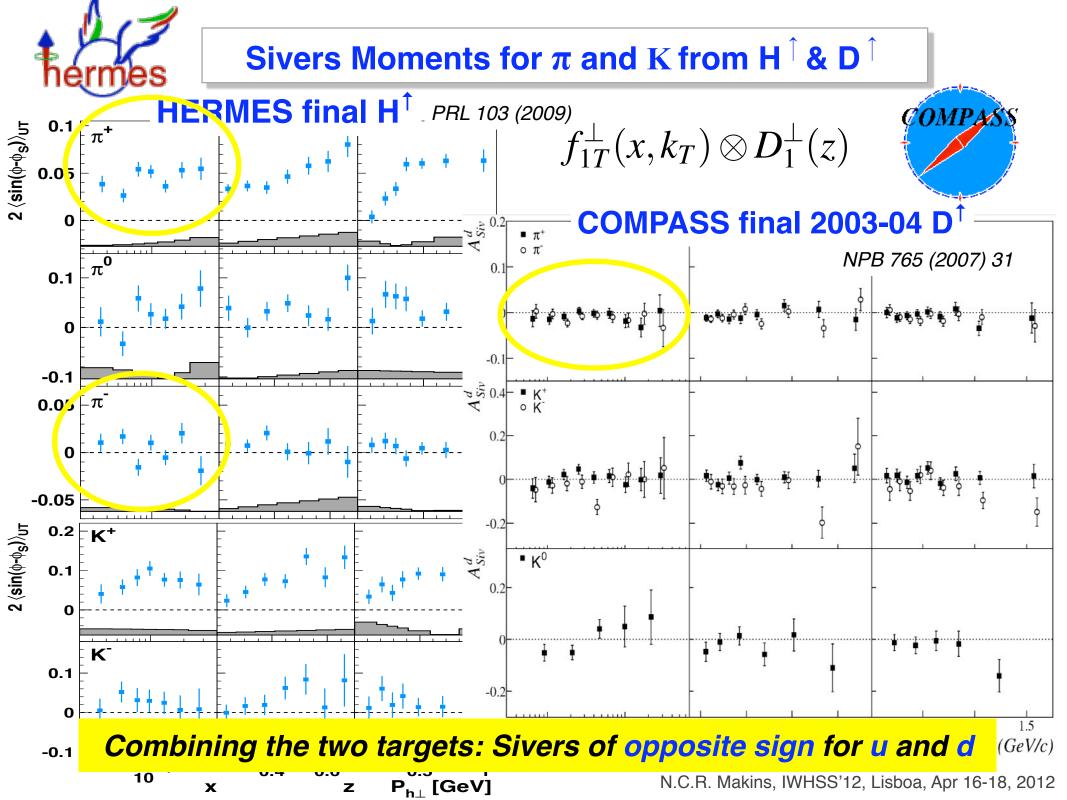
The Sivers Function

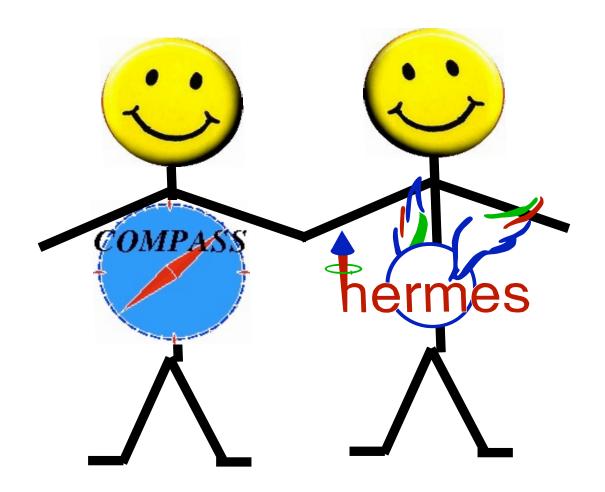
$$f_{1T}^{\perp}(x,k_T)$$



Sivers Moments for π and K from H $^{\uparrow}$ & D $^{\uparrow}$



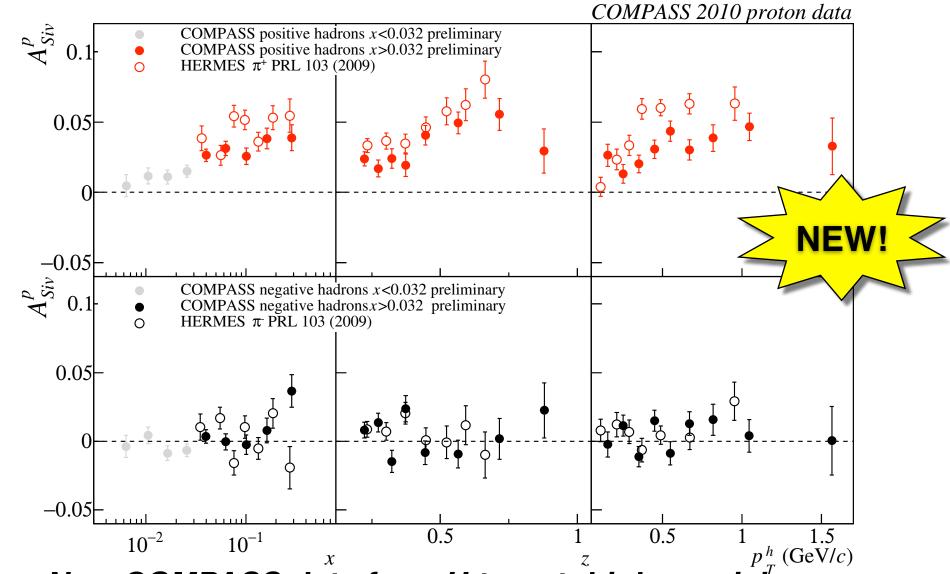






COMPASS proton data: confirmation!



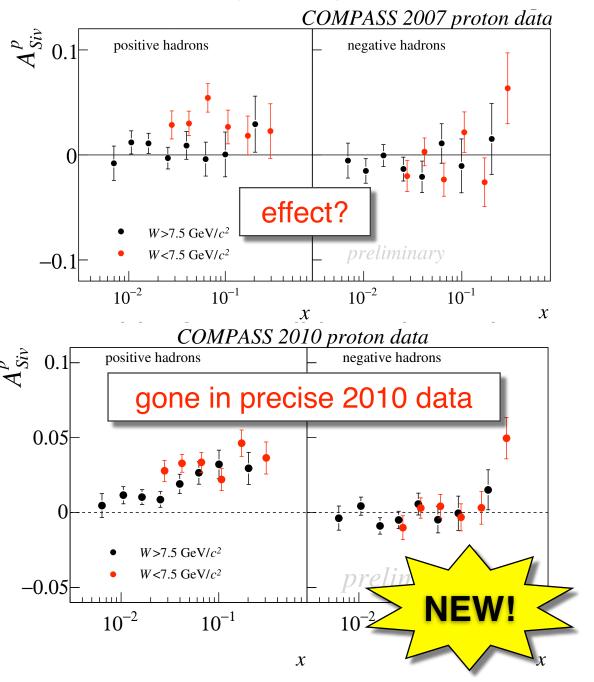


New COMPASS data from H target: high-precision confirmation of non-zero Sivers effect in SIDIS, Lisboa, Apr 16-18, 2012

W-dependence of Sivers

looking for higher twist, factorization breaking

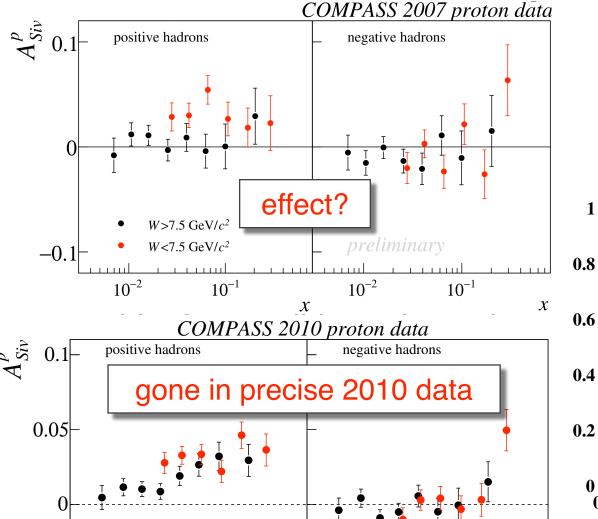




W-dependence of Sivers

looking for higher twist, factorization breaking





 $\boldsymbol{\mathcal{X}}$

 $W > 7.5 \text{ GeV}/c^2$

 $W < 7.5 \text{ GeV}/c^2$

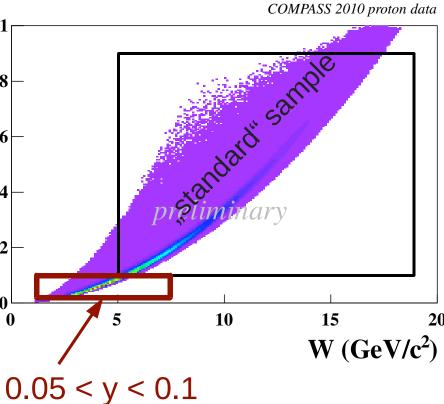
 10^{-1}

 10^{-2}

-0.05

next, push the test to ...

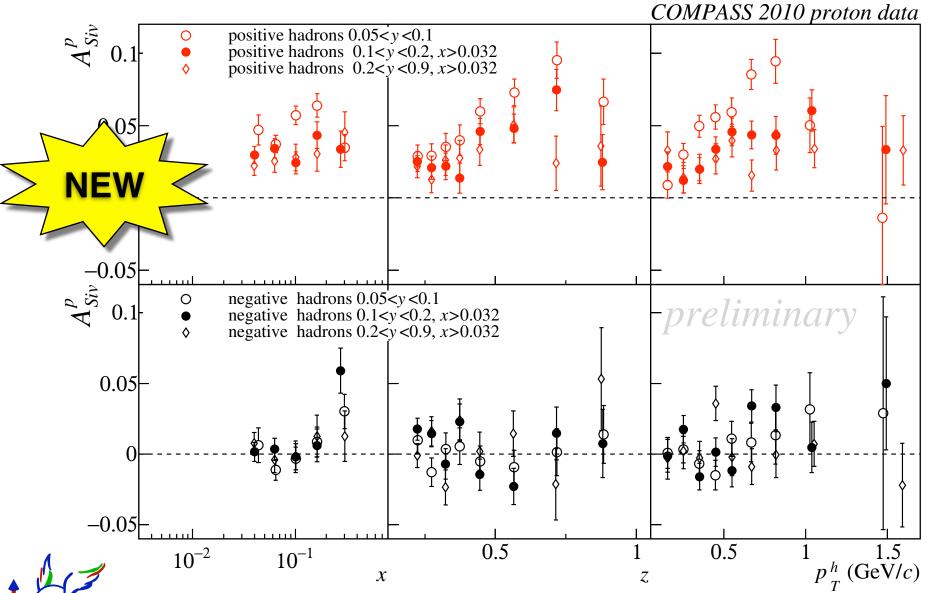
low y: 0.05 < y < 0.1



y-dependence of Sivers



it's baaaack ... ○ at very low y (and so low W < 5 GeV)



Note: HERMES range is 3.2 < W < 7 GeV

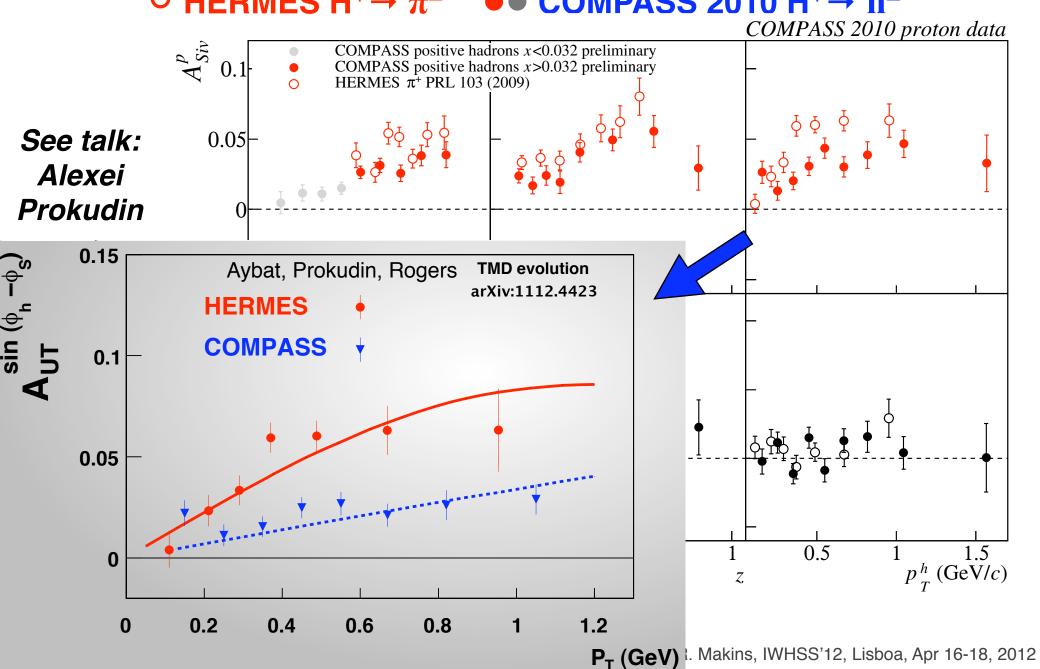
hermes

but TMD Evolution looking good!







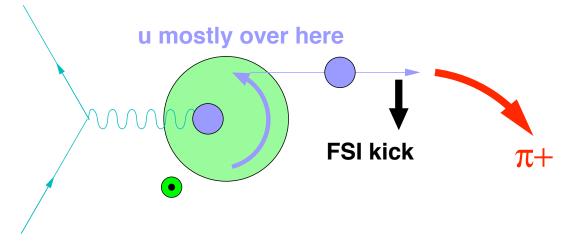


Phenomenology: Sivers Mechanism

Assuming L_u > 0 ...

M. Burkardt: Chromodynamic lensing

Electromagnetic coupling $\sim (J_0 + J_3)$ stronger for oncoming quarks

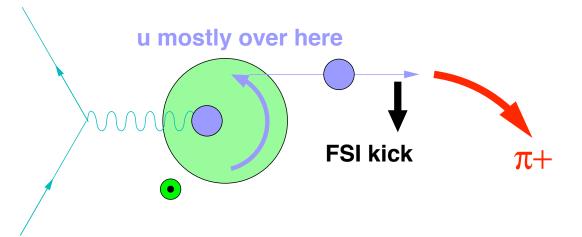


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We observe $\langle \sin(\phi_h^l - \phi_S^l) \rangle_{\mathrm{UT}}^{\pi^+} > 0$ (and opposite for π^-)

 \therefore for $\phi_S^l = 0$, $\phi_h^l = \pi/2$ preferred

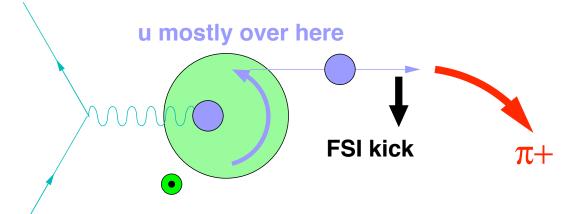
Model agrees!

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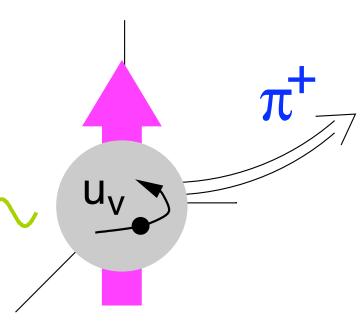
Model agrees!

D. Sivers: Jet Shadowing

Parton energy loss considerations suggest quenching of jets from "near" surface of target

→ quarks from "far" surface should dominate

Opposite sign to data ... assuming $L_u > 0$...



 $2 \langle \sin(\phi - \phi) \rangle_{\text{U}}$

0.1

 $2\left\langle \sin(\phi - \phi_{S}) \right\rangle_{
m UT}$

-0.1 (sφ-φ)011 0.05 π

-0.05

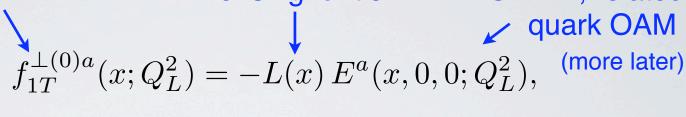
New Global Fit to Sivers SIDIS Data

Using available data

Sivers

X

"lensing funtion" GPD E, related to



Use SIDIS Sivers asymmetry data to constrain shape





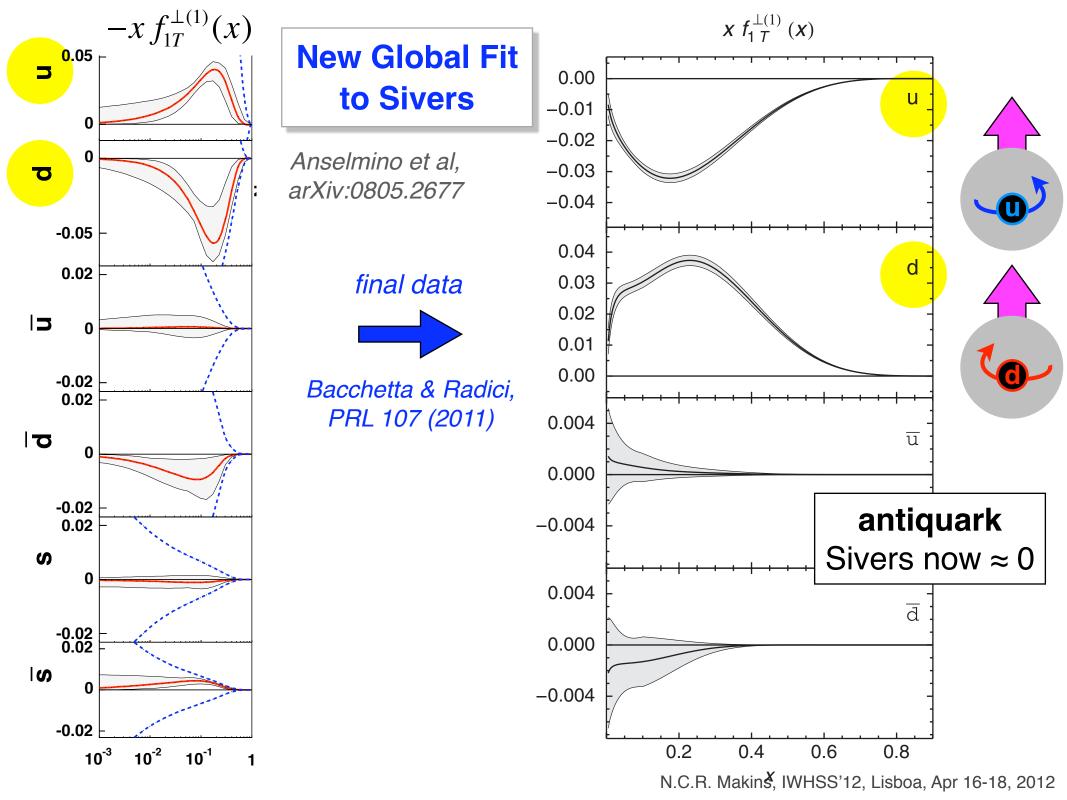


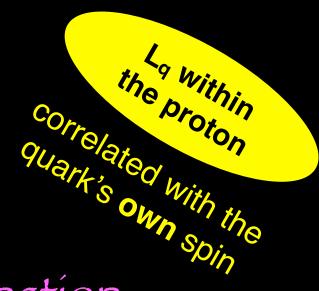
$$\kappa^{p} = \int_{0}^{1} \frac{dx}{3} \left[2E^{u_{v}}(x,0,0) - E^{d_{v}}(x,0,0) - E^{s_{v}}(x,0,0) \right]$$

$$\kappa^{n} = \int_{0}^{1} \frac{dx}{3} \left[2E^{d_{v}}(x,0,0) - E^{u_{v}}(x,0,0) - E^{s_{v}}(x,0,0) \right]$$

Use anomalous magnetic moments to constrain integral

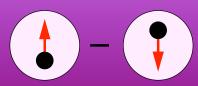
Alessandro Bacchetta, INT Workshop on OAM

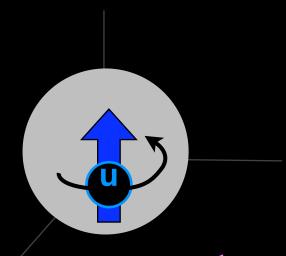


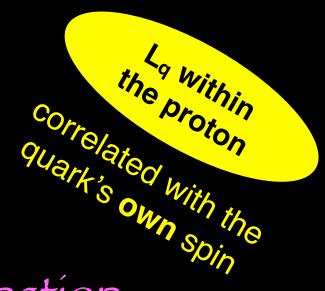


The Boer-Mulders function

 $h_1^{\perp}(x,k_T)$

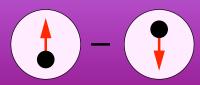






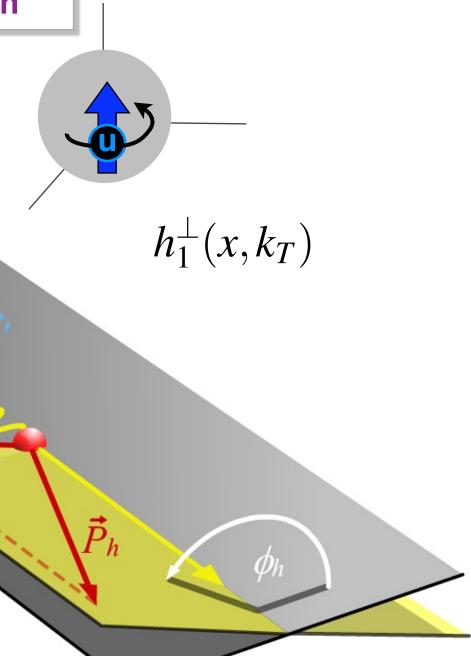
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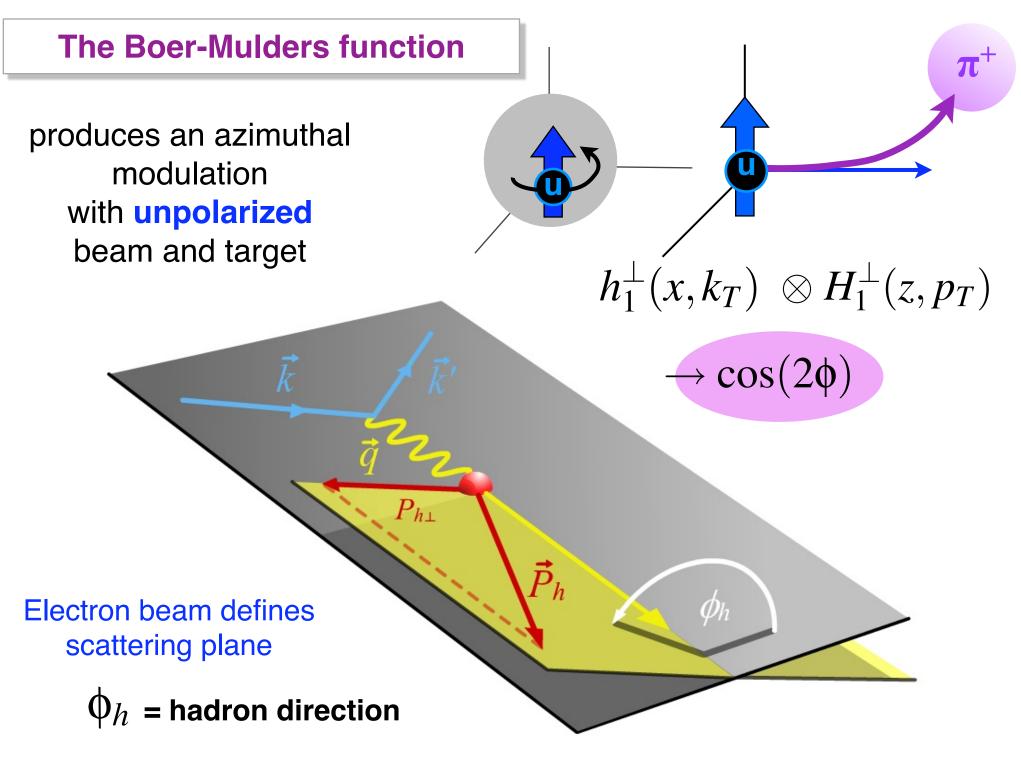
The Boer-Mulders function

produces an azimuthal modulation with unpolarized beam and target



Electron beam defines scattering plane

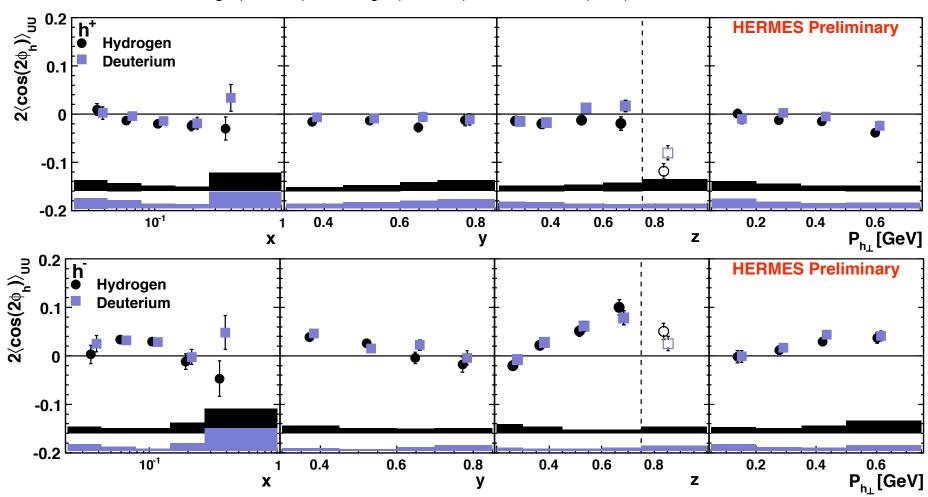
 Φ_h = hadron direction



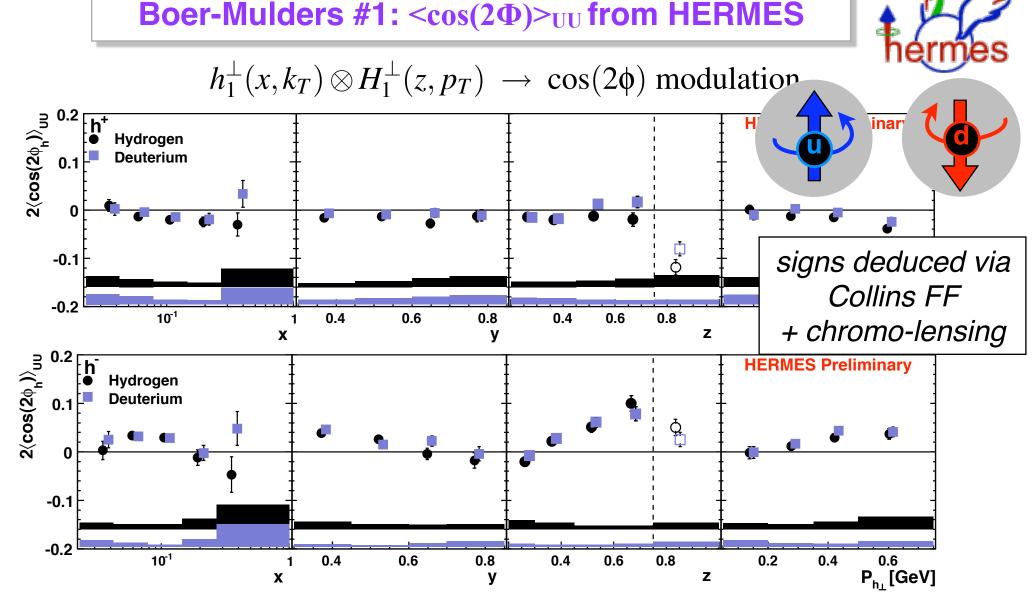
Boer-Mulders #1: $\langle \cos(2\Phi) \rangle_{UU}$ from HERMES



$$h_1^{\perp}(x,k_T) \otimes H_1^{\perp}(z,p_T) \rightarrow \cos(2\phi)$$
 modulation



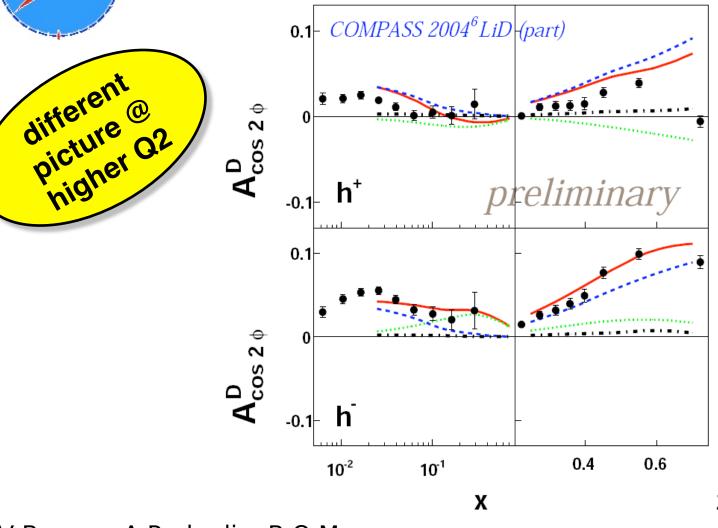
Deuterium ≈ Hydrogen values → indicate Boer-Mulders functions of SAME SIGN for up and down quarks (both negative, similar magnitudes)



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Boer-Mulders #2: $<\cos(2\Phi)>_{UU}$ from COMPASS



COMPASS cos(2Φ)
well explained by
dominant

twist-4 Cahn effect

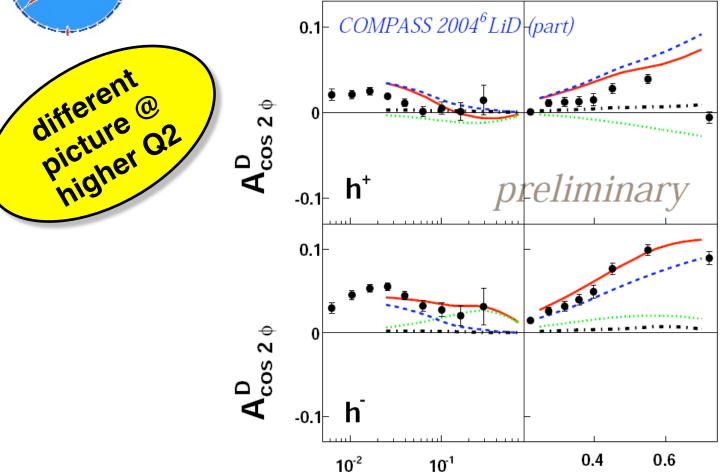
V.Barone, A.Prokudin, B.Q.Ma arXiv:0804.3024 [hep-ph]

total Boer Mulders
Cahn pQCD

errors shown are statistical only

COMPASS

Boer-Mulders #2: $<\cos(2\Phi)>_{UU}$ from COMPASS



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... but Cahn contribⁿ seems <u>small</u> in **HERMES** data, at lower **Q**²

V.Barone, A.Prokudin, B.Q.Ma arXiv:0804.3024 [hep-ph]

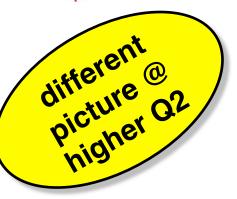
total Boer Mulders
Cahn pQCD

errors shown are statistical only

X

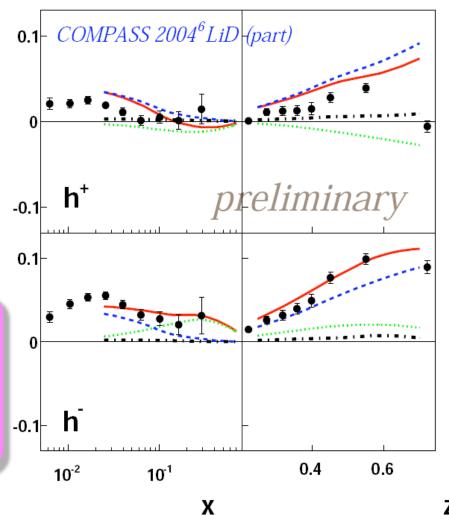
COMPASS

Boer-Mulders #2: $<\cos(2\Phi)>_{UU}$ from COMPASS



 $A_{\cos2\,\phi}^D$

Scale-dependence challenges: TMD evolution & higher twist



COMPASS cos(2Φ)

well explained by dominant

twist-4 Cahn effect

... but Cahn contribⁿ seems <u>small</u> in **HERMES** data, at lower **Q**²

... Can **BELLE** data on Collins FF be evolved to all SIDIS scales?

V.Barone, A.Prokudin, B.Q.Ma arXiv:0804.3024 [hep-ph]

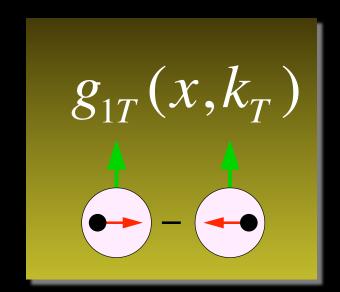
total Boer Mulders
Cahn pQCD

errors shown are statistical only

Pretzelosity & the Worm Gears

$$h_{1T}^{\perp}(x,k_T)$$

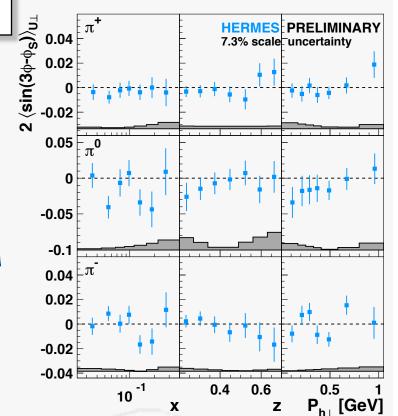
$$h_{1L}^{\perp}(x,k_T)$$



	U	L	$oxed{T}$
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^{\perp}
Т	f_{1T}^{\perp}	g_{1T}	$h_1, rac{h_{1T}^\perp}{}$

In several models, related to $g_1^q-h_1^q \rightarrow$ relativistic effects

Pretzelosity



all hadrons

0.6

0.8

- chiral-odd → needs Collins FF (or similar)
- leads to $sin(3 \phi \phi_s)$ modulation in A_{UT}
- proton and deuteron data consistent with zero
- cancelations? pretzelosity=zero? or just the additional suppression by two powers of $P_{h\perp}$



1.5

Pt (GeV/c)

0.5

2002-2004 data COMPASS

10-1

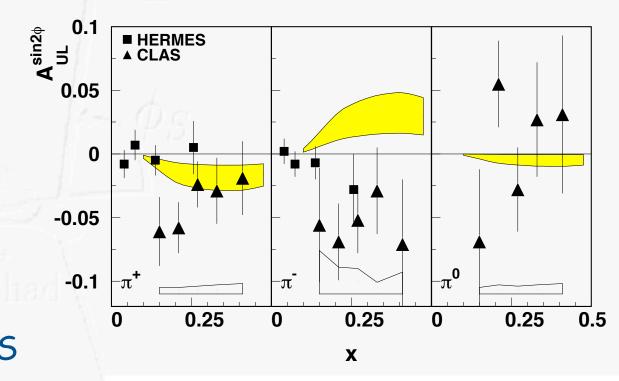
10⁻²

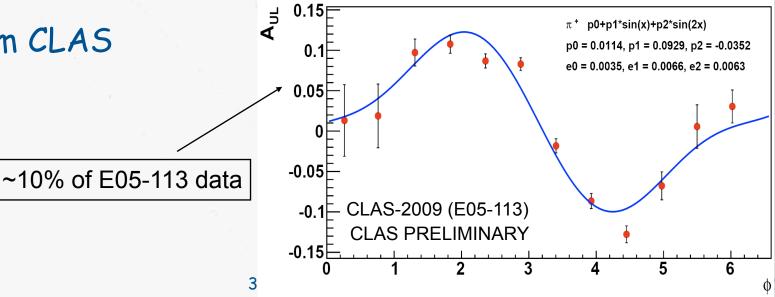
	U	L	Т
U	f_1		h_1^{\perp}
L		g_{1L}	h_{1L}^{\perp}
Т	f_{1T}^{\perp}	g_{1T}	h_1,h_{1T}^\perp



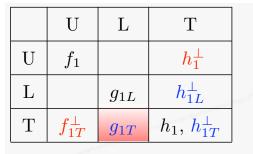
Worm-Gear I

- again chiral-odd
- evidence from CLAS (violating isospin symmetry?)
- consistent with zero at COMPASS and HERMES
- new data from CLAS





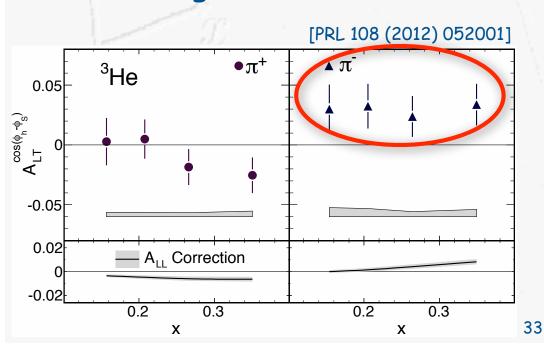
Gunar Schnell

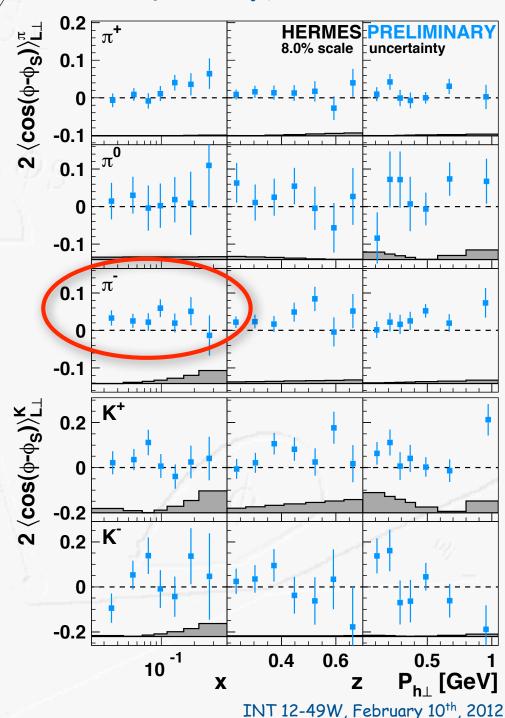


- Worm-Gear II



- first direct evidence for worm-gear g_{1T} on
 - ³He target at JLab
 - H target at HERMES



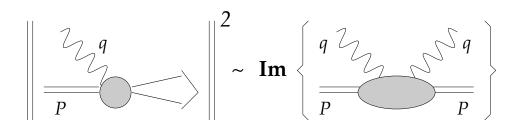


L, Sivers, the Sea, and the Missing Spin Programme

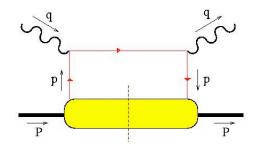


T-odd TMDs → gauge links and L

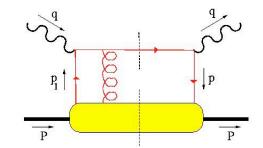
A T-odd function like f_{1T}^{\perp} <u>must</u> arise from <u>interference</u> ... but a distribution function is just a forward scattering amplitude, how can it contain an interference?



Brodsky, Hwang, & Schmidt 2002



can interfere with

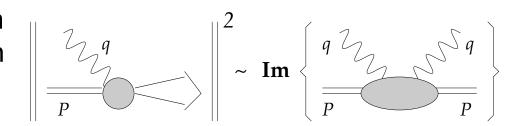


and produce a T-odd effect! (also need $L_z \neq 0$)

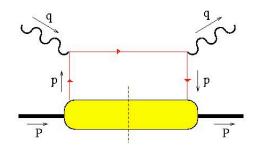
It looks like higher-twist ... but no, these are <u>soft gluons</u>: "gauge links" required for color gauge invariance

T-odd TMDs → gauge links and L

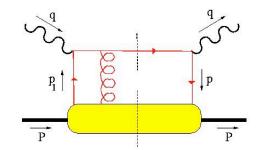
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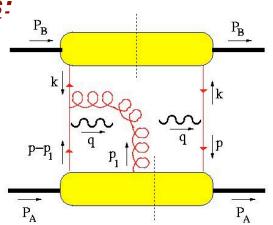
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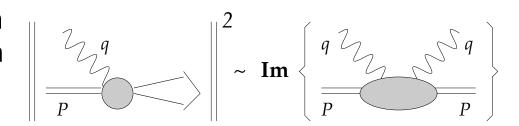
It looks like higher-twist ... but no, these are <u>soft gluons</u>: "gauge links" required for color gauge invariance

Such soft-gluon reinteractions with the soft wavefunction are final / initial state interactions ... and process-dependent ... e.g. *Drell-Yan*: →
Sivers effect
should have
opposite sign
cf. SIDIS

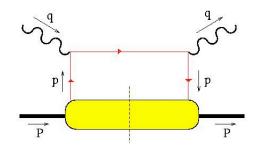


T-odd TMDs → gauge links and L

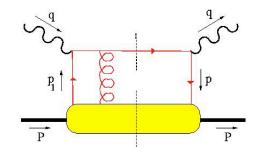
A T-odd function like f_{1T}^{\perp} <u>must</u> arise from <u>interference</u> ... but a distribution function is just a forward scattering amplitude, how can it contain an interference?



Brodsky, Hwang, & Schmidt 2002



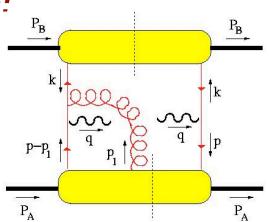
can interfere with



and produce a T-odd effect! (also need $L_z \neq 0$)

It looks like higher-twist ... but no, these are <u>soft gluons</u>: "gauge links" required for color gauge invariance

Such soft-gluon reinteractions with the soft wavefunction are final / initial state interactions ... and process-dependent ... e.g. *Drell-Yan*: →
Sivers effect
should have
opposite sign
cf. SIDIS



A Tantalizing Picture

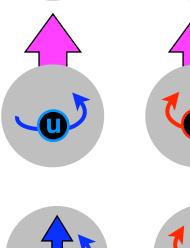
- Transversity: $h_{1,u} > 0$ $h_{1,d} < 0$
 - \rightarrow same as $g_{1,u}$ and $g_{1,d}$ in NR limit
- Sivers: $f_{1T^{\perp},u} < 0$ $f_{1T^{\perp},d} > 0$
 - → relatⁿ to anomalous magnetic moment*

$$f_{1T}^{\perp}, q \sim \kappa_q$$
 where $\kappa_u \approx +1.67$ $\kappa_d \approx -2.03$

values achieve $\kappa^{p,n} = \sum_q e_q \kappa_q$ with u,d only



 \rightarrow results on $<\cos(2\Phi)>_{UU}$ suggest yes:



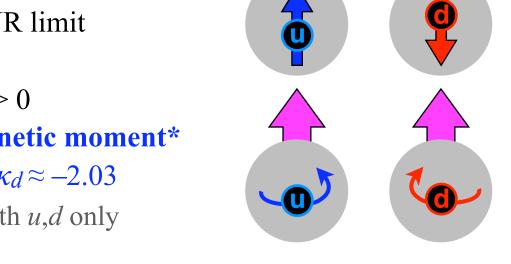


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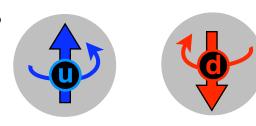
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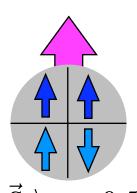
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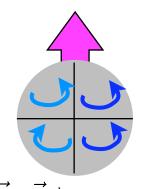


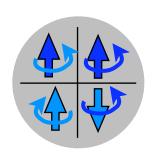
- Boer-Mulders: follows that $h_{1^{\perp},u}$ and $h_{1^{\perp},d} < 0$?
 - \rightarrow results on $\langle \cos(2\Phi) \rangle_{UU}$ suggest yes:



N.B. these TMDs are all independent







* Burkardt PRD72 (2005) 094020; Barone et al PRD78 (1008) 045022;

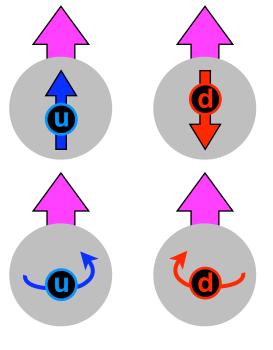
 $\langle \vec{s}_u \cdot \vec{S}_p \rangle = +0.5 \quad \langle \vec{l}_u \cdot \vec{S}_p \rangle = +0.5 \quad \langle \vec{s}_u \cdot \vec{l}_u \rangle = 0$ Nakins, IWHSS'12, Lisboa, Apr 16-18, 2012

is it a HAPPY picture?

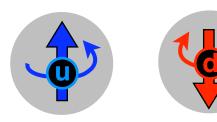
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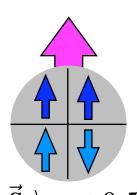
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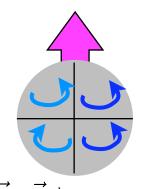


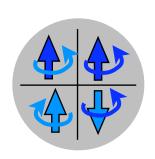
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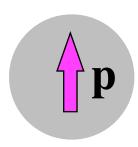




$$\langle \vec{s}_u \cdot \vec{l}_u \rangle = 0$$

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 $\langle \vec{s}_u \cdot \vec{S}_p \rangle = +0.5 \quad \langle \vec{l}_u \cdot \vec{S}_p \rangle = +0.5 \quad \langle \vec{s}_u \cdot \vec{l}_u \rangle = 0$ Nakins, IWHSS'12, Lisboa, Apr 16-18, 2012

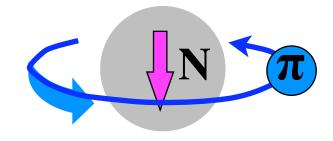


$$|p>=p+N\pi$$
 Pions have $J^P=0^-=$ negative parity ... $+\Delta\pi+...$ Pions have $J^P=0^-=$ negative parity $...$

$N\pi$ cloud:

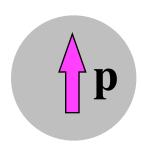
2/3
$$n \pi^+$$
 1/3 $p \pi^0$





2/3
$$L_z = +1$$

1/3
$$L_z = 0$$



$$|p\rangle = p + N\pi + \Delta\pi + \dots$$

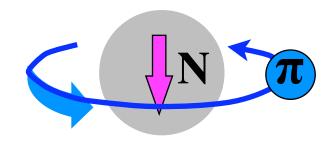
Pions have $J^P = 0^- =$ **negative parity** ...

 $+\Delta\pi + ... \rightarrow NEED L = 1$ to get proton's $J^P = \frac{1}{2}$

$N\pi$ cloud:

2/3 n
$$\pi^+$$
 1/3 p π^0





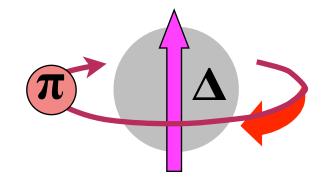
$$L_z = +1$$

1/3
$$L_z = 0$$

$\Delta\pi$ cloud:

1/2
$$\Delta^{++} \pi^{-}$$
1/3 $\Delta^{+} \pi^{0}$
1/6 $\Delta^{0} \pi^{+}$

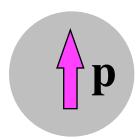




$$1/2$$
 $L_z = -1$

1/3
$$L_z = 0$$

1/6
$$L_z = +1$$



$$|p>=p+N\pi \ +\Delta\pi+...$$

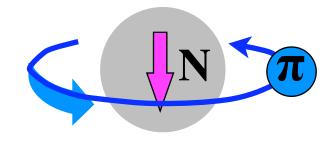
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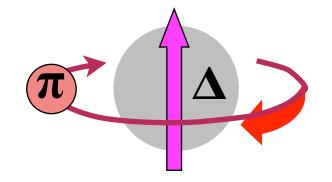
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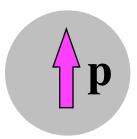
$$1/2$$
 $L_z = -1$

1/3
$$L_z = 0$$

1/6
$$L_z = +1$$

Dominant source of:

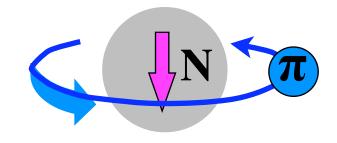
orbiting U: $n \pi^+$ with $L_z(\pi) > 0$



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$N\pi$ cloud:





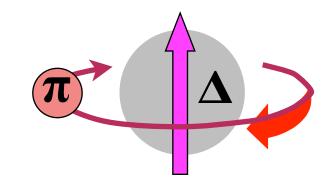
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1/3
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$$\Delta^{++} \pi^{-}$$
1/3 $\Delta^{+} \pi^{0}$
1/6 $\Delta^{0} \pi^{+}$





$$1/2$$
 $L_z = -1$

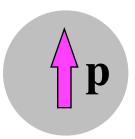
1/3
$$L_z = 0$$

1/6
$$L_z = +1$$

Dominant source of:

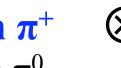
orbiting U: $n \pi^+$ with $L_z(\pi) > 0$

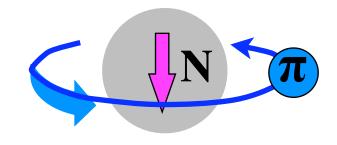
orbiting d: $\Delta^{++} \pi^{-}$ with $L_z(\pi) < 0$



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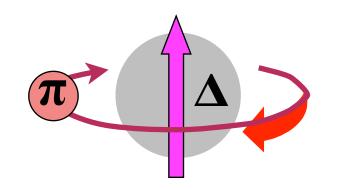
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1/6 $\Delta^{0} \pi^{+}$





$$1/2$$
 $L_z = -1$

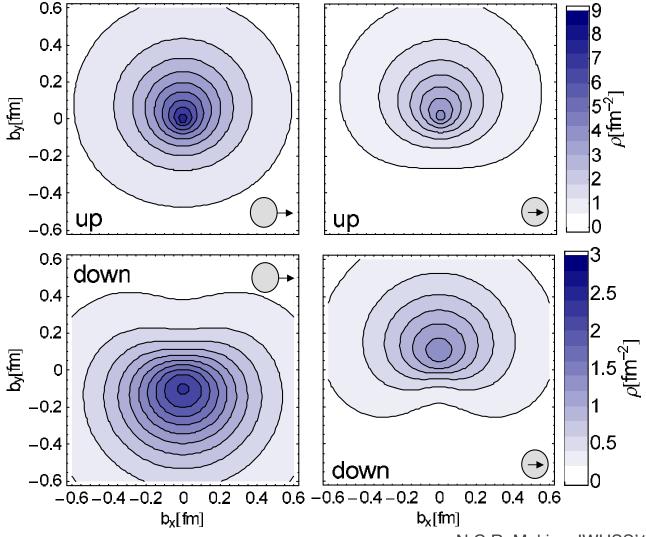
1/3
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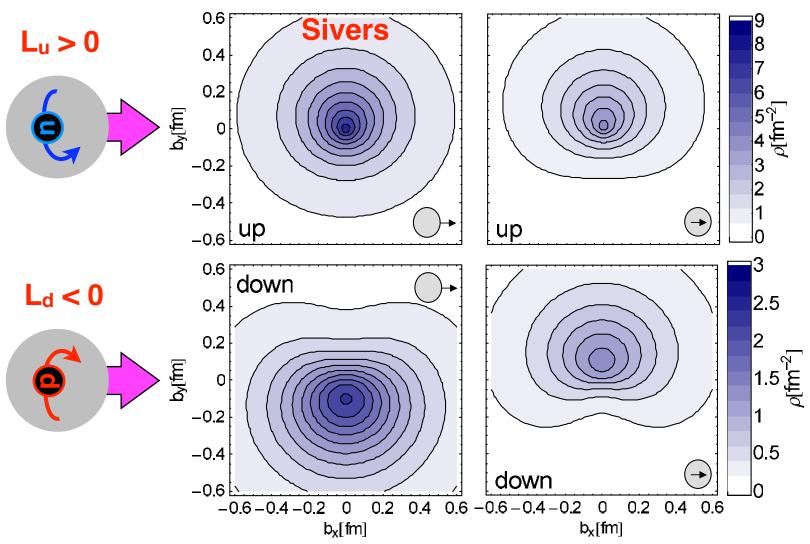
Dominant source of: orbiting U: $n \pi^+$ with $L_z(\pi) > 0$

orbiting d: $\Delta^{++} \pi^{-}$ with $L_z(\pi) < 0$

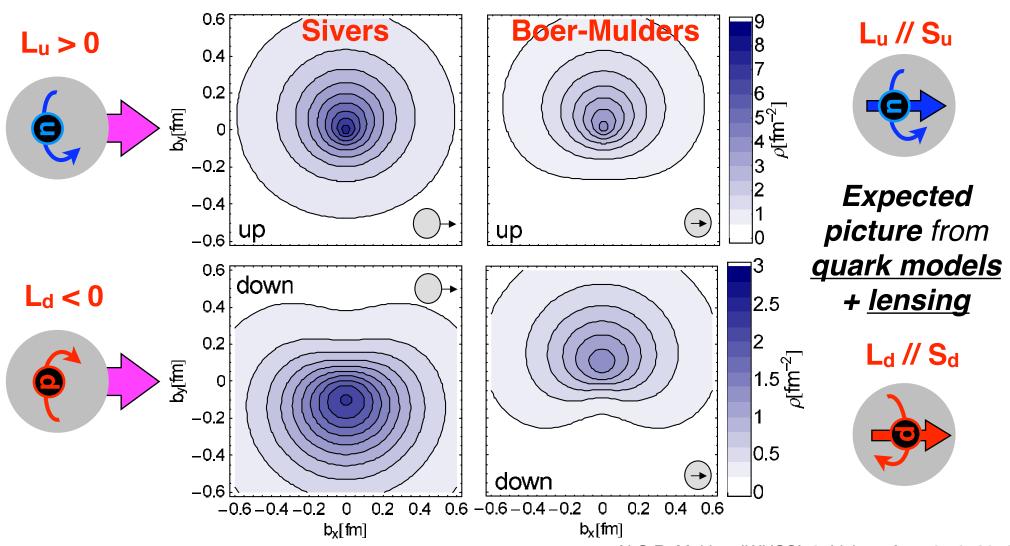
 $L_{\rm u} > 0$ L_{qbar} ≠ 0 Compute quark densities in impact-parameter space via GPD formalism nucleon coming out of page ... observe spin-dependent shifts in quark densities:



Compute quark densities in impact-parameter space via GPD formalism nucleon coming out of page ... observe spin-dependent shifts in quark densities:

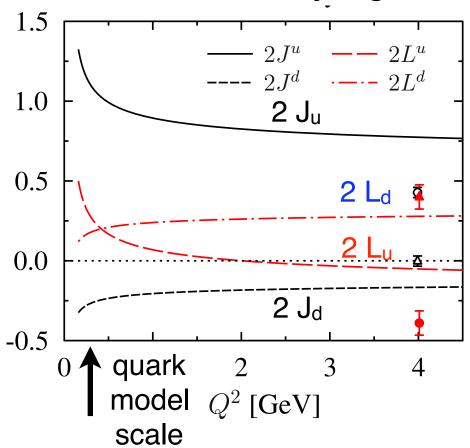


Compute quark densities in impact-parameter space via GPD formalism nucleon coming out of page ... observe spin-dependent shifts in quark densities:



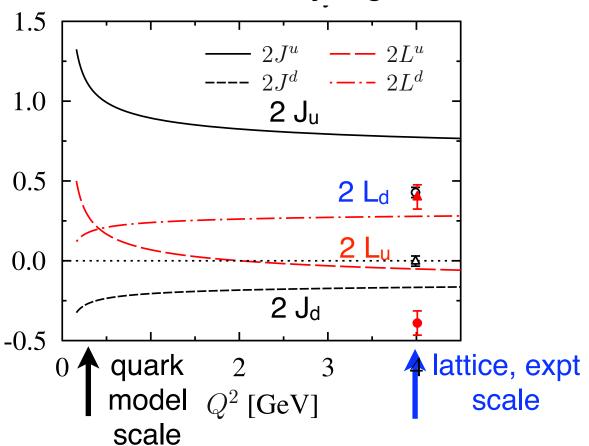
... and Longitudinal spin on the lattice ...

Thomas: cloudy bag model evolved up to Q2 of expt / lattice



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 \rightarrow lattice shows $L_u < 0$ and $L_d > 0$ in longitudinal case at expt'al scales!

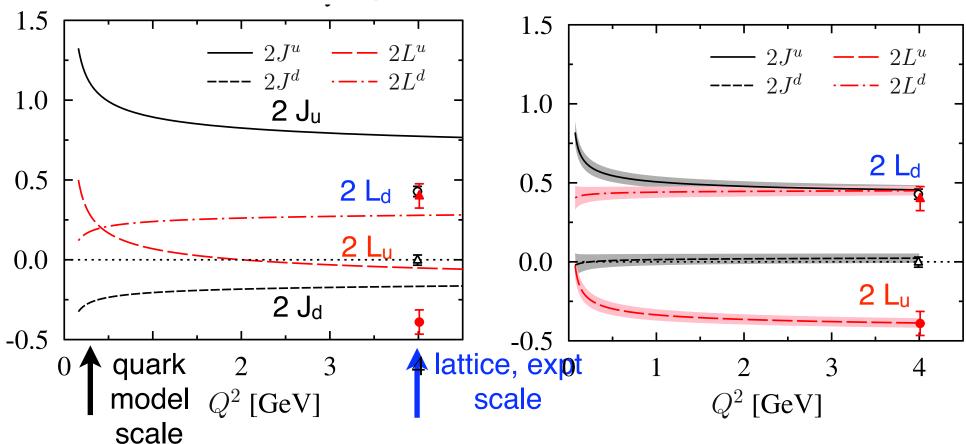
Evolution might explain disagreement with quark models ...



... and Longitudinal spin on the lattice ...

Wakamatsu, EPJA44 (2010)

Thomas: cloudy bag model evolved up to Q² of expt / lattice



→ lattice shows L_u < 0 and L_d > 0 in longitudinal case at expt'al scales!

Evolution might explain disagreement with quark models ...

or not. Wakamatsu evolves down → insensitive to uncertain scale of quark models

Density shifts + lensing function = Sivers (model-dependent)

The Mysterious E

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The Mysterious E

E requires L

Brodksy, Drell (1980); Burkardt, Schnell, PRD 74 (2006)

- $\int \mathbf{E} \, d\mathbf{x} = \text{Pauli } \mathbf{F}_2 \rightarrow_{(t=0)} \text{ anomalous mag moment } \mathbf{k}$:: GPD basics
- both F₂ and κ require L ≠ 0

∴ N <u>spin-flip</u> amplitudes

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E is not L

$$2 J_q = \int x H_q|_{t=0} dx + \int x E_q|_{t=0} dx$$

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E is not L

Ji Sum
$$2 J_q = \int x H_q|_{t=0} \, dx + \int x E_q|_{t=0} \, dx$$
 momentum
$$\int x \, q(x) \, dx \longleftarrow \langle \mathbf{X} \rangle_{\mathbf{q}} + \mathbf{E}_{\mathbf{q}}^{(2)} \longrightarrow \text{"anomalous gravitomagnetic moment"}$$

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Spin Sum
$$2 J_q = \Delta q + 2 L_q$$

$$\therefore 2L_q = \left[\langle x \rangle_q + E_q^{(2)} \right]_{=J_q} - \Delta q$$

Contradiction?

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Jaffe L?

both F₂ and κ require L ≠ 0

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E is not L

$$2 J_q = \int x H_q|_{t=0} dx + \int x E_q|_{t=0} dx$$

Rule
$$\uparrow \qquad \uparrow \qquad \uparrow \qquad \downarrow \\ \text{momentum} \int x \, q(x) \, dx \leftarrow \langle \mathbf{X} \rangle_{\mathbf{q}} \qquad + \qquad \mathbf{E}_{\mathbf{q}}^{(2)} \longrightarrow \text{"anomalous gravito-magnetic moment"}$$

Spin Sum $2 J_q = \Delta q + 2 L_q$ Rule

$$\mathbf{2} \; \boldsymbol{J_q}$$

$$\Delta q$$

$$\mathbf{L}_{q}$$

Rule
$$\therefore 2L_q = \left[\langle x \rangle_q + E_q^{(2)} \right]_{=J_q} - \Delta q$$
 "L" not uniquely defined

Contradiction?

Proton Spin Decompositions

$$\mathbf{J^{Ji}} = \frac{i}{2}q^{\dagger}(\vec{r} \times \vec{D})^{z}q + \frac{1}{2}q^{\dagger}\sigma^{z}q + 2\operatorname{Tr}E^{j}(\vec{r} \times \vec{D})^{z}A^{j} + \operatorname{Tr}(\vec{E} \times \vec{A})^{z}$$

$$\mathbf{L_{q}} \qquad \mathbf{\Delta q} \qquad \mathbf{L_{g}} \qquad \mathbf{\Delta g}$$

$$\boldsymbol{J}^{\textbf{Jaffe}} = \frac{1}{2} q_+^{\dagger} (\vec{r} \times i \vec{\nabla})^z q_+ + \frac{1}{2} q_+^{\dagger} \gamma_5 q_+ + 2 \operatorname{Tr} F^{+j} (\vec{r} \times i \vec{\nabla})^z A^j + \varepsilon^{+-ij} \operatorname{Tr} \vec{F}^{+i} \vec{A}^j$$

Ji, PRL 78 (1997)

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Ji: **3** gauge invariant Δq , L_q , J_g

- **x** access Δg : no GI sepⁿ of Δg , L_g
- ✓ measure L_q (expt & lattice): yes → via GPDs & DVCS
- **x** interpret L_q : covariant derivative $D^{\mu} = \partial^{\mu} + ig^{\mu} \leftarrow$ gluon interac's

Ji, PRL 78 (1997)

Proton Spin Decompositions

Jaffe & Bashinsky, NPB 536 (1998)

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Jaffe: $oldsymbol{\Phi}$ gauge invar $\Delta q, L_q, \Delta g, L_g$

- \checkmark access Δg : this <u>is</u> what's being measured at RHIC, COMPASS
- ✓ interpret L_q : $\vec{r} \times \vec{p} \rightarrow \underline{\text{field-free}}$ OAM ... in ∞ momentum frame
- *** measure** L_q (expt & lattice): involves **non-local** operators except in **lightcone gauge** A^+ =0

Ji, PRL 78 (1997)

Proton Spin Decompositions

Jaffe & Bashinsky, NPB 536 (1998)

$$J^{Ji} = \frac{i}{2}q^{\dagger}(\vec{r} \times \vec{D})^{z}q + \frac{1}{2}q^{\dagger}\sigma^{z}q + 2\operatorname{Tr}E^{j}(\vec{r} \times \vec{D})^{z}A^{j} + \operatorname{Tr}(\vec{E} \times \vec{A})^{z}$$

$$L_{q} \qquad \Delta q \qquad L_{g} \qquad \Delta g$$

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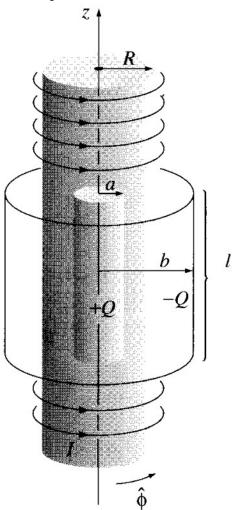
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- **Jaffe**: $oldsymbol{\Phi}$ gauge invar Δq , L_q , Δg , L_g
- $m{\times}$ access Δg : no GI sepⁿ of Δg , L_g
- ✓ measure L_q (expt & lattice): yes → via GPDs & DVCS
- **x** interpret L_q : covariant derivative $D^{\mu} = \partial^{\mu} + ig^{\mu} \leftarrow$ gluon interac's

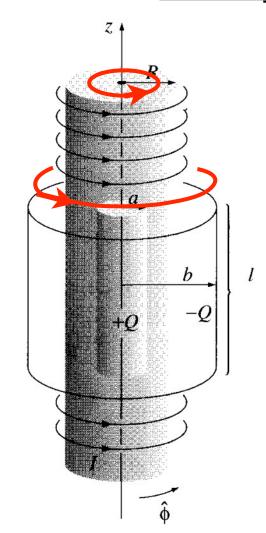
- \checkmark access Δg : this <u>is</u> what's being measured at RHIC, COMPASS
- ✓ interpret L_q : $\vec{r} \times \vec{p} \rightarrow \underline{\text{field-free}}$ OAM ... in ∞ momentum frame
- *** measure** L_q (expt & lattice): involves **non-local** operators except in **lightcone** gauge $A^+=0$

see ongoing work of **Wakamatsu** *PRD* 81 (2010), 83 (2011) & **Chen** et al *PRL* 100 (2008), 103 (2009)

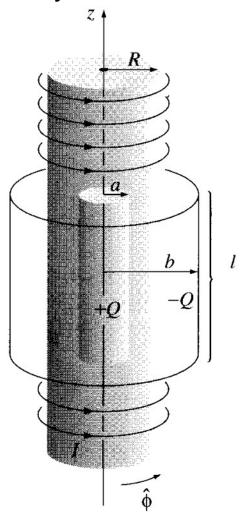
Solenoid with constant *I;* charged cylinders stationary



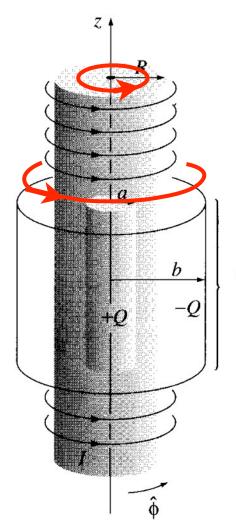
Solenoid I <u>decreases</u> to zero ... dB/dt induces $E \rightarrow \text{rotates cylinders}$



Solenoid with constant *I;* charged cylinders stationary



Solenoid I <u>decreases</u> to zero ... dB/dt induces $E \rightarrow \text{rotates cylinders}$



$$\vec{E}_{\text{ind}} = \hat{\phi} \frac{\mu_0 n | \dot{I} | s}{2}$$

$$\text{for } s < R$$

$$\vec{E}_{\text{ind}} = \hat{\phi} \frac{\mu_0 n | \dot{I} | R^2}{2 s}$$

inner +Q cylinder:

for s > R

$$\vec{L}_{+} = \int a\hat{s} \times Q \vec{E}_{ind} \Big|_{s=a} dt$$
$$= \hat{z} \frac{\mu_0 n I Q}{2} a^2$$

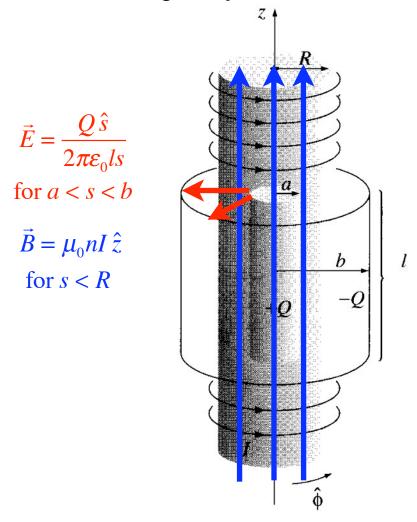
outer –*Q* cylinder:

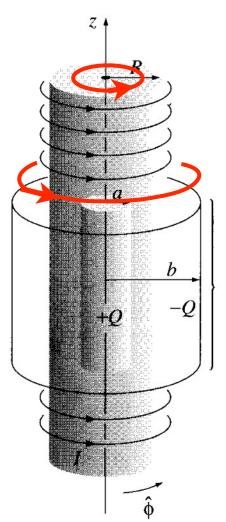
$$\vec{L}_{-} = -\hat{z} \; \frac{\mu_0 n I Q}{2} R^2$$

$$\therefore \vec{\mathbf{L}}_{\text{cylinders}} = -\hat{z} \; \frac{\mu_0 n I Q}{2} (R^2 - a^2)$$

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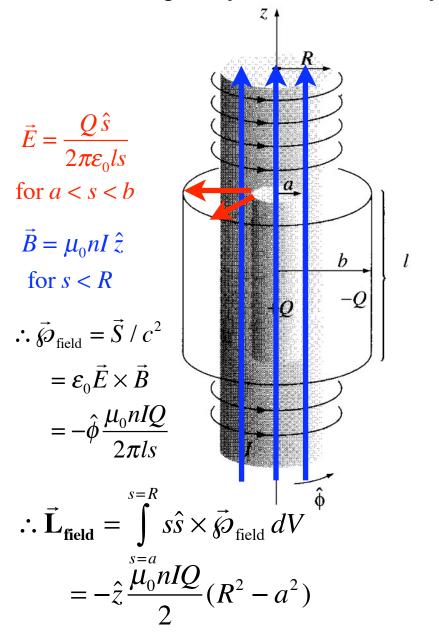
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outer $-Q$ cylinder:

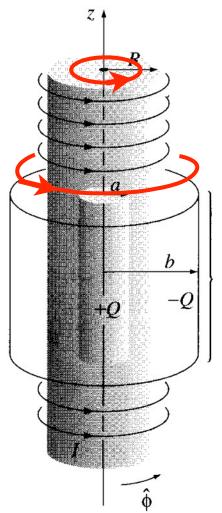
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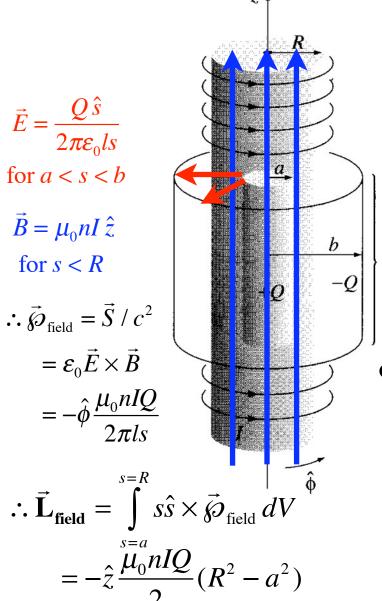
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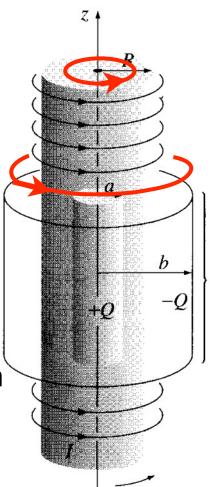
Both needed to conserve L, but ...

,mechanical

L_{cylinder} = r x p is

measurable

distinct from r x (E x B)



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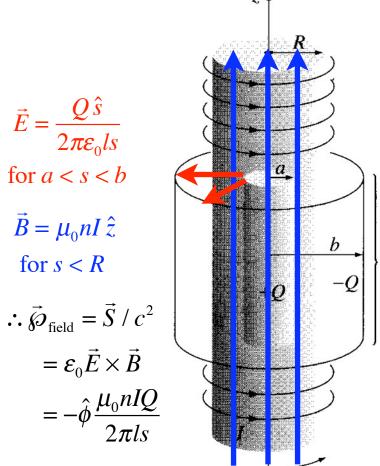
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 $\therefore \vec{\mathbf{L}}_{\text{field}} = \int_{0}^{\infty} s\hat{s} \times \vec{\wp}_{\text{field}} dV$

 $= -\hat{z} \frac{\ddot{\mu_0} n I Q}{2} (R^2 - a^2)$

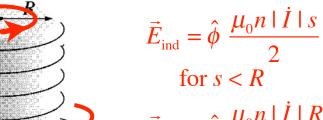
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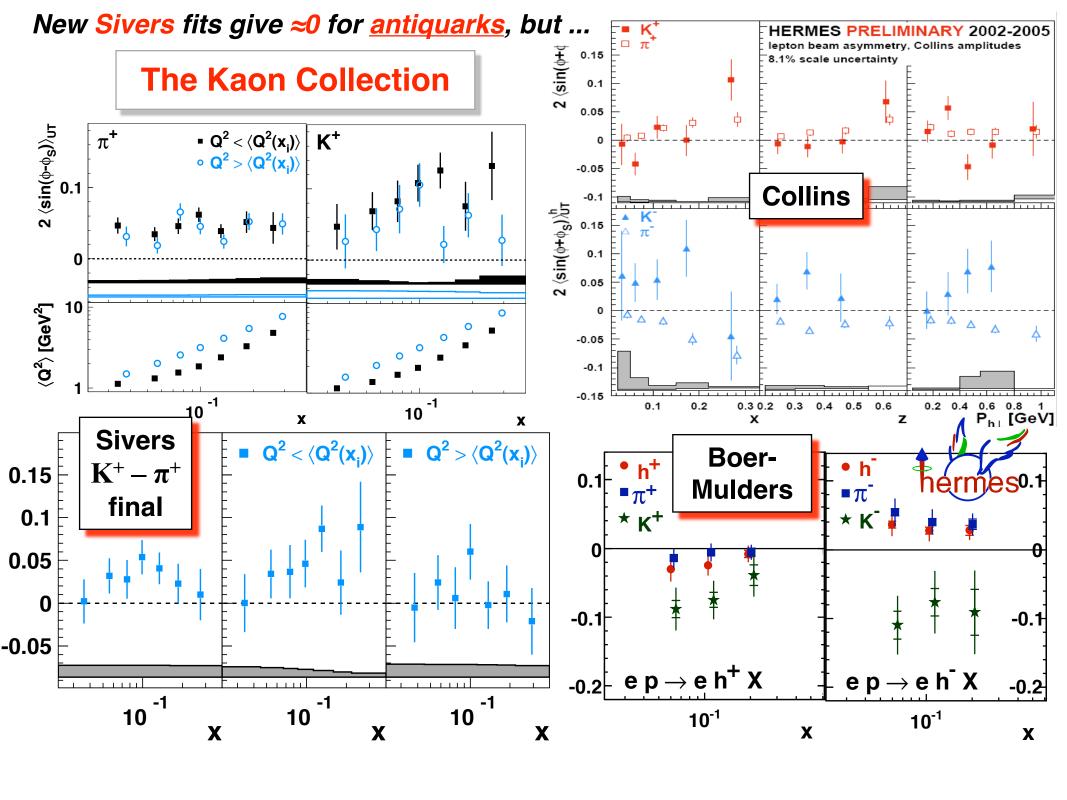
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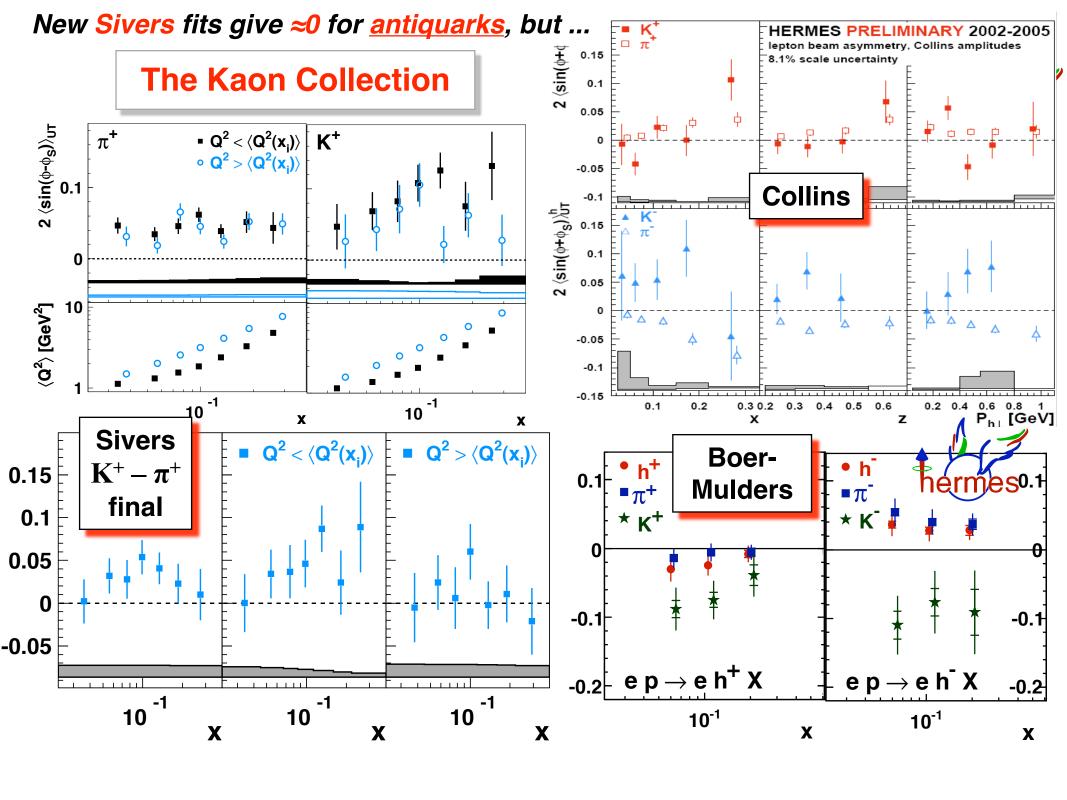
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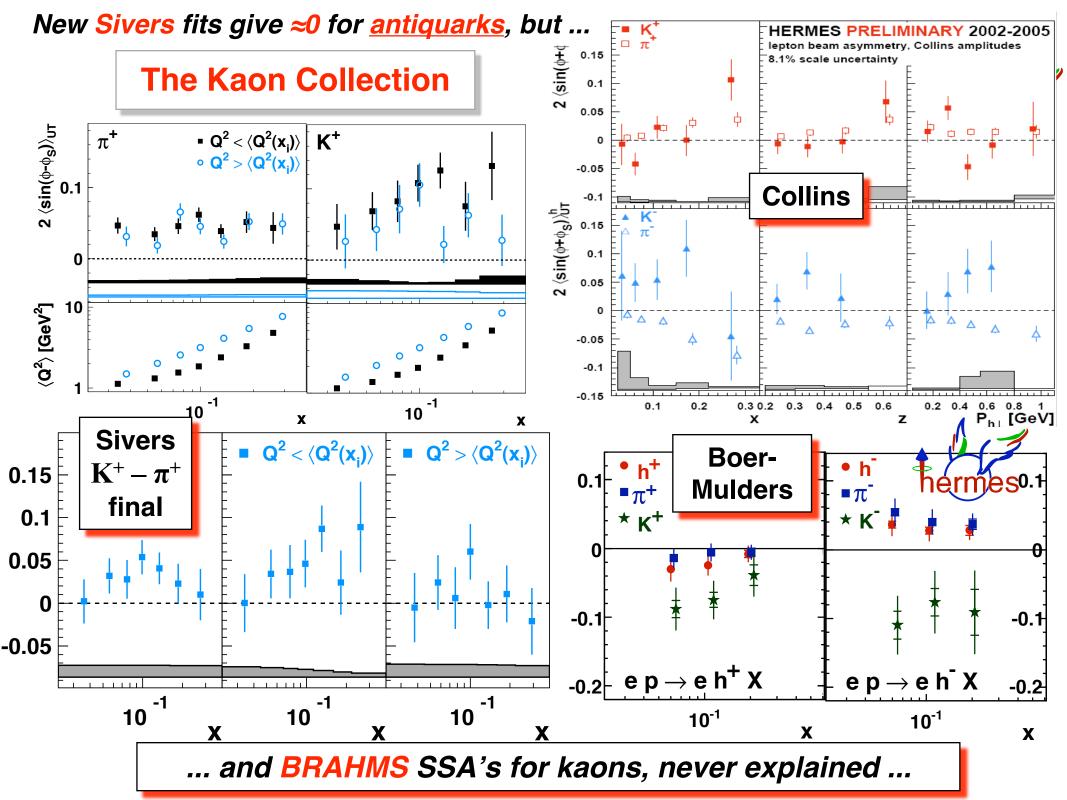
classical intuition doesn't help with the meaning of gaugecovariant $iD^{\mu} = i\partial^{\mu} - eA^{\mu}$

$$\therefore \vec{\mathbf{L}}_{\text{cylinders}} = -\hat{z} \; \frac{\mu_0 n I Q}{2} (R^2 - a^2)$$

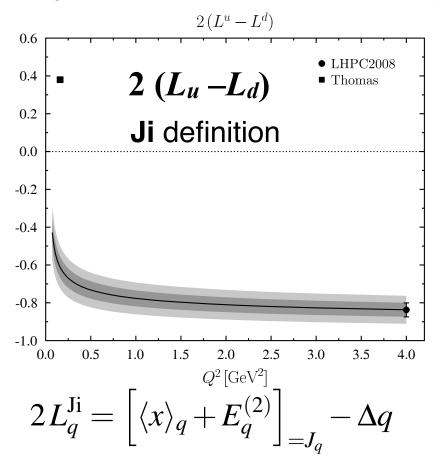
N.C.R. Makins, IWHSS'12, Lisboa, Apr 16-18, 2012





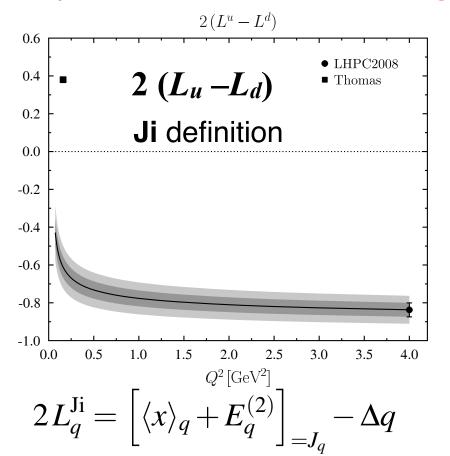


Theory: Ji's L_{u-d} is rock-solid & negative



- $< x>_{u-d}$: well known
- $\Delta u \Delta d = g_A$: well known
- $E^{(2)}_{u-d}$: <u>all</u> lattice calculatⁿs <u>and</u> XQSM agree

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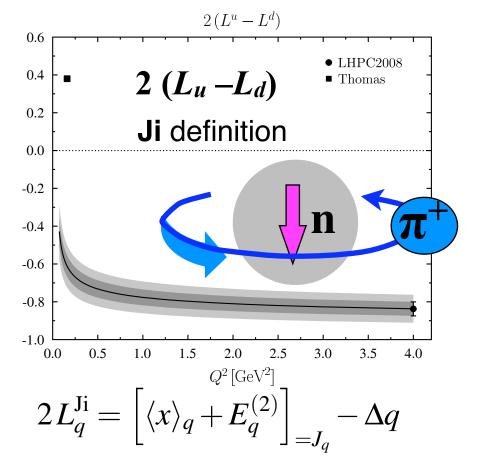
Compare Jaffe & Ji

calculate explicitly in χQSM; at quark-model scale:

	<i>L_{u−d}</i> Jaffe	<i>L_{u−d}</i> Ji
Valence	+0.147	-0.142
Sea	-0.265	-0.188
Total	-0.115	-0.330

Negative model value dominated by sea quark L!

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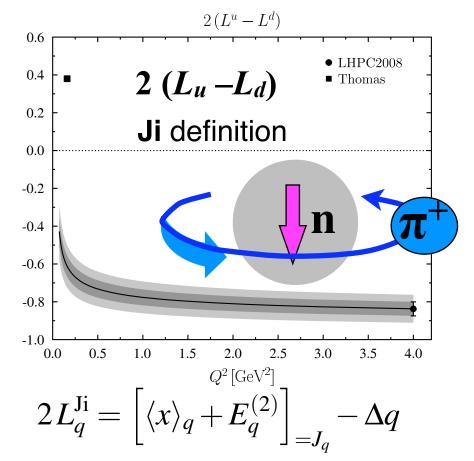
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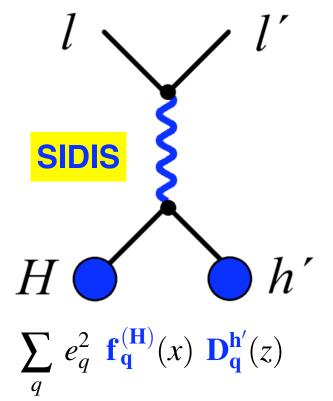
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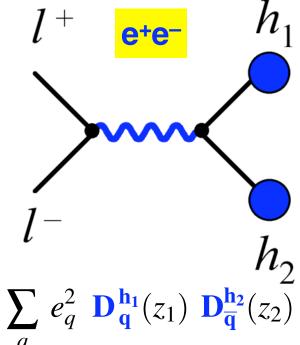
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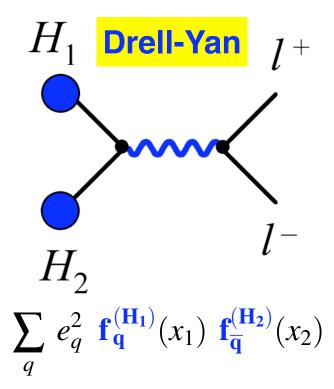
Need <u>direct measurement</u> of Sivers for <u>sea quarks</u>:

Spin-dependent Drell-Yan with p or π^+ beam & pol'd target



SIDIS $\sum e_q^2 \mathbf{f}_{\mathbf{q}}^{(\mathbf{H})}(x) \mathbf{D}_{\mathbf{q}}^{\mathbf{h}'}(z)$

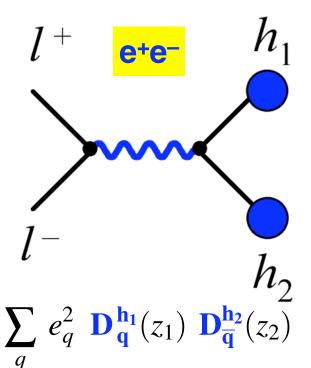


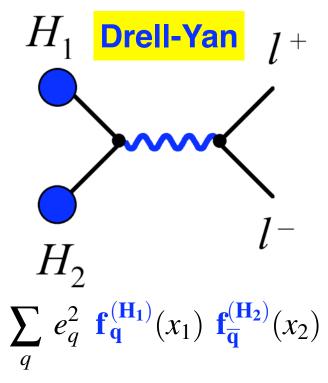


SIDIS H h'

 $\sum e_q^2 \mathbf{f}_{\mathbf{q}}^{(\mathbf{H})}(x) \mathbf{D}_{\mathbf{q}}^{\mathbf{h}'}(z)$

- Disentangle distribution (f) and fragmentation (D) functions → measure all process
 - Disentangle quark flavours q → measure as many <u>hadron species</u> H,h as possible



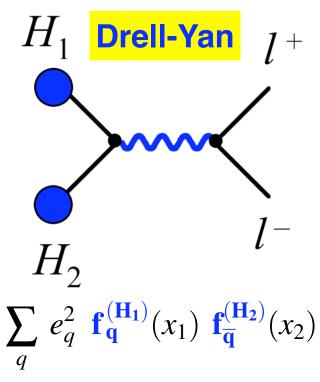


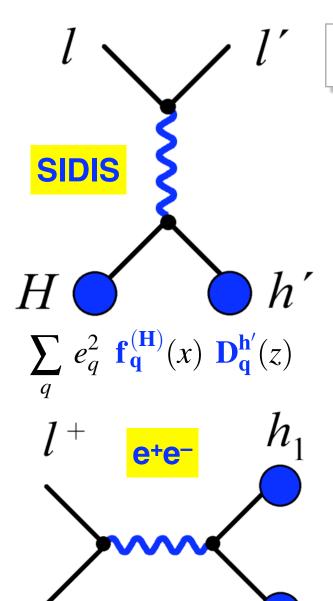
l^+ eter h_1 $l^ h_2$ $\sum_{q} e_q^2 \mathbf{D}_{\mathbf{q}}^{\mathbf{h}_1}(z_1) \mathbf{D}_{\mathbf{q}}^{\mathbf{h}_2}(z_2)$

Leptons: clean, surgical tools

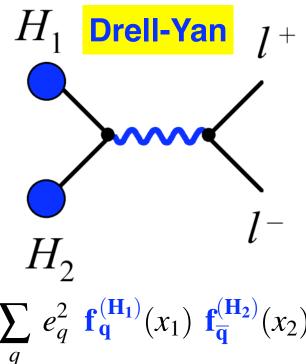
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These are the **only** processes where TMD factorization is proven

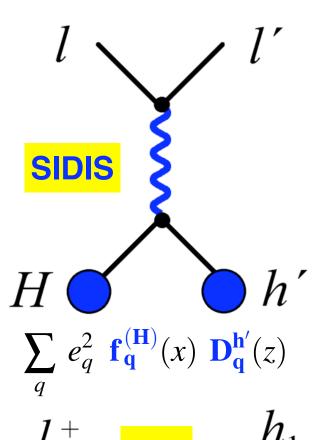




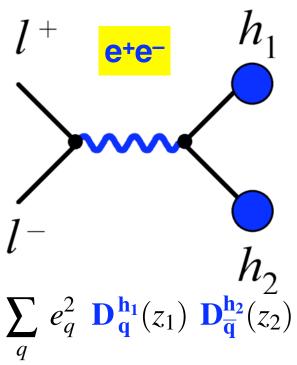
 $\sum e_q^2 \mathbf{D}_{\mathbf{q}}^{\mathbf{h_1}}(z_1) \mathbf{D}_{\overline{\mathbf{q}}}^{\mathbf{h_2}}(z_2)$

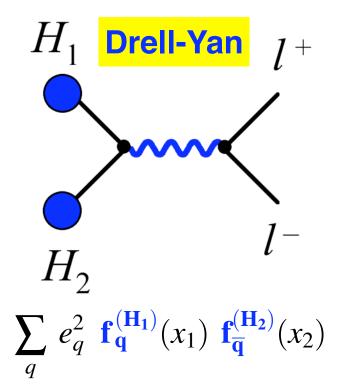


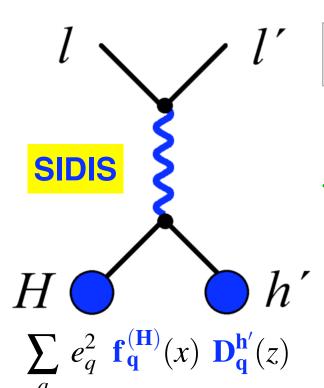
$$\sum_{q} e_q^2 \mathbf{f}_{\mathbf{q}}^{(\mathbf{H_1})}(x_1) \mathbf{f}_{\overline{\mathbf{q}}}^{(\mathbf{H_2})}(x_2)$$











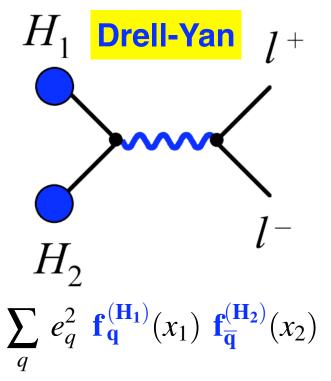


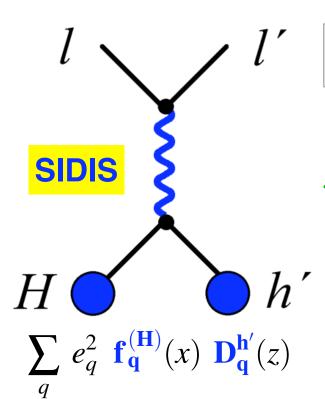


Spin Programs



$$l^+$$
 $e^+e^ h_1$
 $l^ h_2$
 $\sum e_q^2 \mathbf{D}_{\mathbf{q}}^{\mathbf{h}_1}(z_1) \mathbf{D}_{\mathbf{q}}^{\mathbf{h}_2}(z_2)$



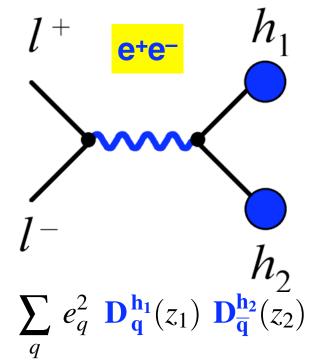


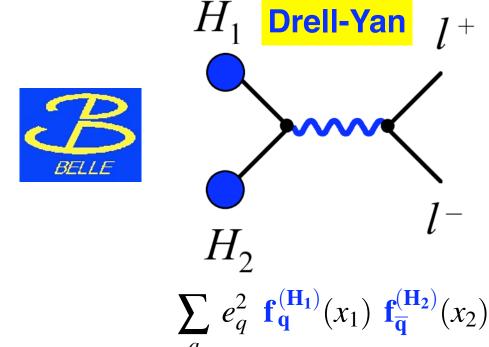


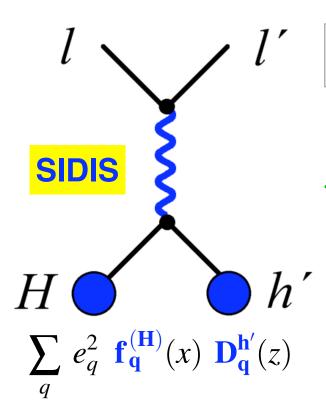


Spin Programs







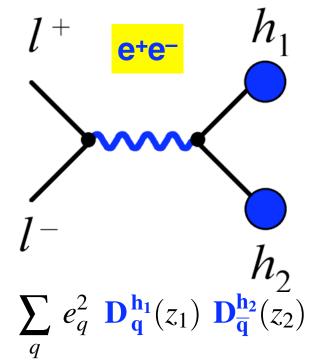




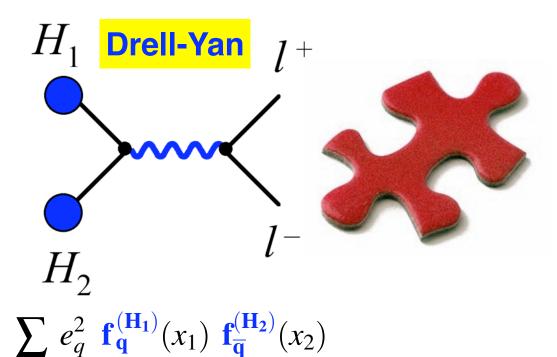


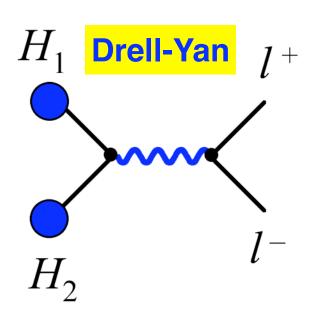
Spin Programs











The Missing Spin Program: Drell-Yan

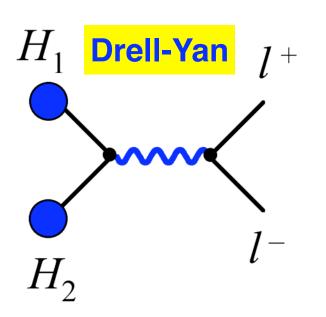


$$\sum_{q} e_{q}^{2} \mathbf{f}_{\mathbf{q}}^{(\mathbf{H}_{1})}(x_{1}) \mathbf{f}_{\overline{\mathbf{q}}}^{(\mathbf{H}_{2})}(x_{2})$$



$$H_1$$
 l
 V
 H_2

• Clean access to sea quarks e.g. $\Delta \overline{u}(x), \Delta \overline{d}(x)$ at RHIC



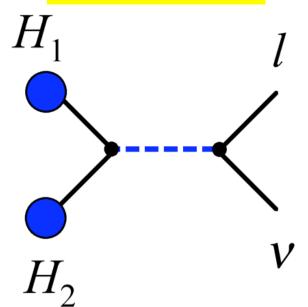
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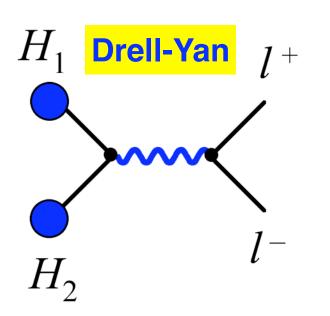
$$\sum_{q} e_q^2 \mathbf{f}_{\mathbf{q}}^{(\mathbf{H_1})}(x_1) \mathbf{f}_{\overline{\mathbf{q}}}^{(\mathbf{H_2})}(x_2)$$



W production



- Clean access to sea quarks e.g. $\Delta \overline{u}(x), \Delta \overline{d}(x)$ at RHIC
- Crucial test of TMD formalism
 - → sign change of T-odd functions

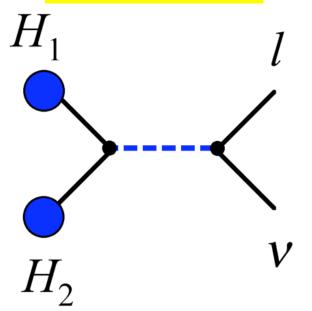


The Missing Spin Program: Drell-Yan



$$\sum_{q} e_q^2 \mathbf{f}_{\mathbf{q}}^{(\mathbf{H_1})}(x_1) \mathbf{f}_{\overline{\mathbf{q}}}^{(\mathbf{H_2})}(x_2)$$





• Clean access to sea quarks e.g. $\Delta \overline{u}(x), \Delta \overline{d}(x)$ at RHIC

- Crucial test of TMD formalism
 - → sign change of T-odd functions
- A complete spin program requires multiple hadron species
 - → nucleon & meson beams

