



Detailed HBT measurement with respect to Event plane and collision energy in Au+Au collisions

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Quark Matter 2012



outline

- Introduction of HBT
- Azimuthal HBT w.r.t v_2 plane
- Azimuthal HBT w.r.t v_3 plane
- Low energy at PHENIX
- Summary

What is HBT ?

- Quantum interference between two identical particles
- Hadron HBT can measure the **source size** at freeze-out (not whole size but **homogeneity region** in expanding source)

$$C_2 = \frac{P(\vec{p}_1, \vec{p}_2)}{P(\vec{p}_1) \cdot P(\vec{p}_2)}$$

$P(p_1)$: Probability of detecting a particle
 $P(p_1, p_2)$: Probability of detecting pair particles

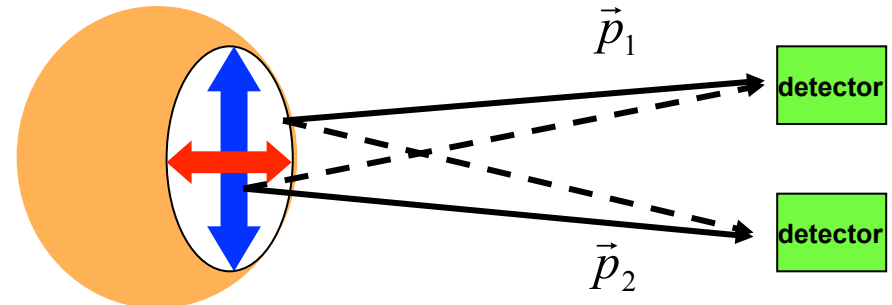
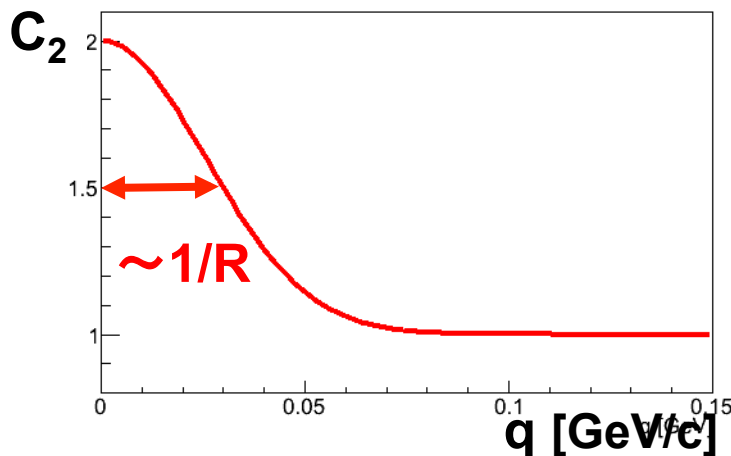
$$= 1 + |\tilde{\rho}(q)|^2 = 1 + \exp(-R_{inv}^2 q_{inv}^2)$$

assuming gaussian source

$$\vec{q} = \vec{p}_1 - \vec{p}_2$$

$$\vec{k}_T = \frac{\vec{p}_1 + \vec{p}_2}{2}$$

$$\vec{q}_{side} \perp \vec{k}_T, \quad \vec{q}_{out} \parallel \vec{k}_T$$



3D HBT radii

- “Out-Side-Long” system

- ✧ Bertsch-Pratt parameterization

- Core-halo model

- ✧ Particles in core are affected by coulomb interaction

$$C_2 = C_2^{core} + C_2^{halo}$$

$$= N[\lambda(1+G)F] + [1-\lambda]$$

$$G = \exp(-R_{inv}^2 q_{inv}^2)$$

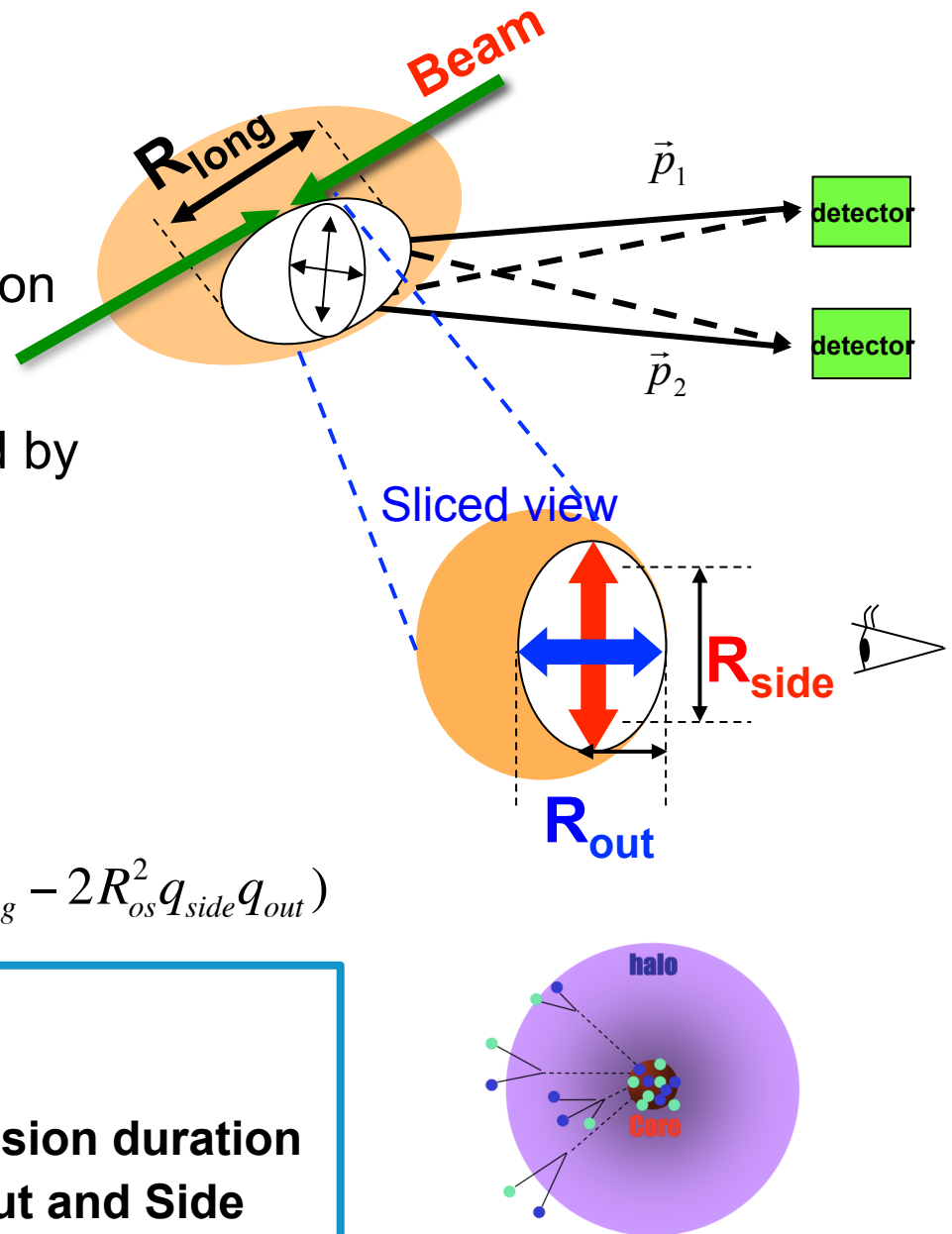
$$= \exp(-R_{side}^2 q_{side}^2 - R_{out}^2 q_{out}^2 - R_{long}^2 q_{long}^2 - 2R_{os} q_{side} q_{out})$$

R_{long} : Longitudinal size

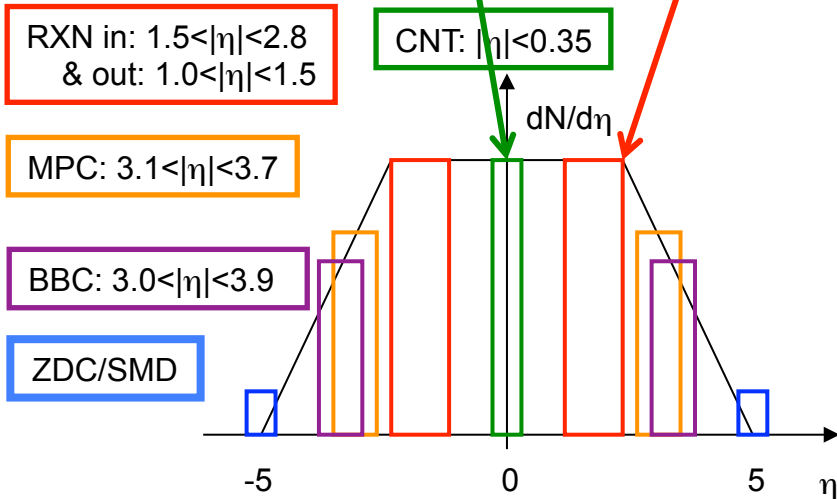
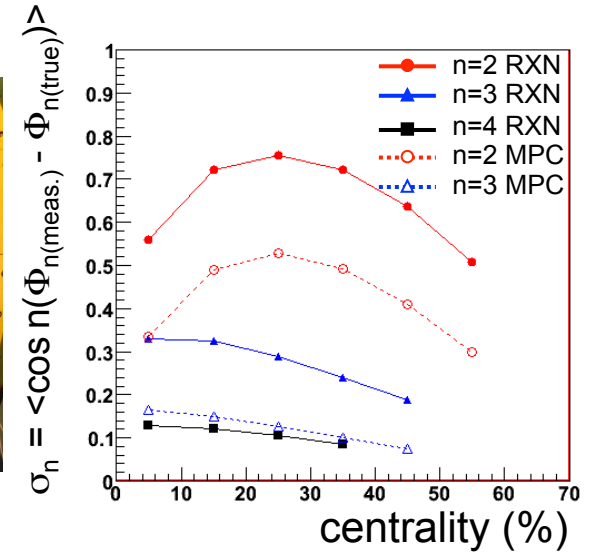
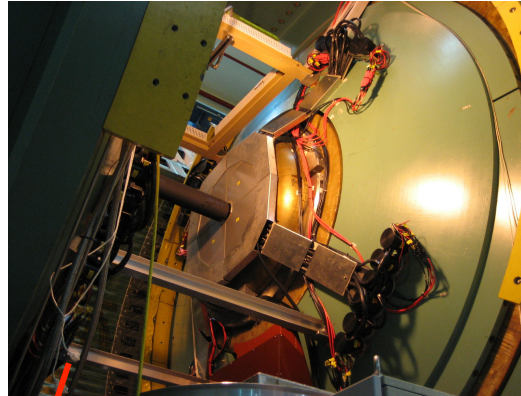
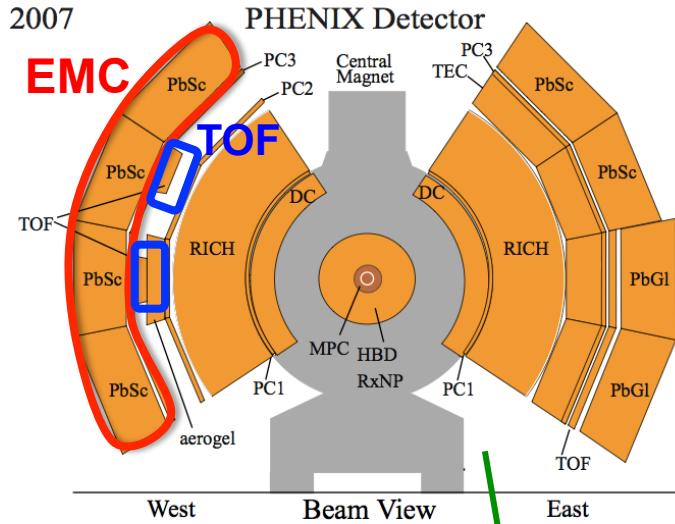
R_{side} : Transverse size

R_{out} : Transverse size + emission duration

R_{os} : Cross term between Out and Side



Measurement by PHENIX Detectors



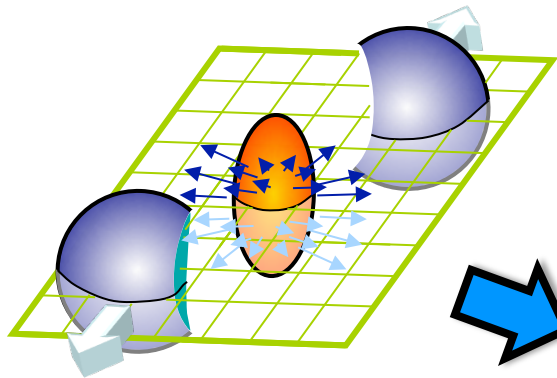
$$C_2 = \frac{R(q)}{M(q)}$$

$R(q), M(q)$:
relative momentum dist.
for real and mixed pairs

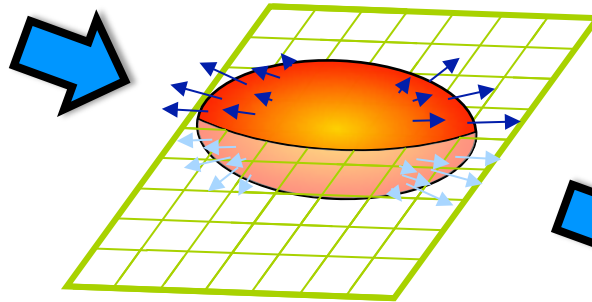
- ★ PID by EMC&TOF
 - ➡ charged π/K are selected
- ★ Ψ_n by forward detector RXN

Azimuthal HBT w.r.t v_2 plane

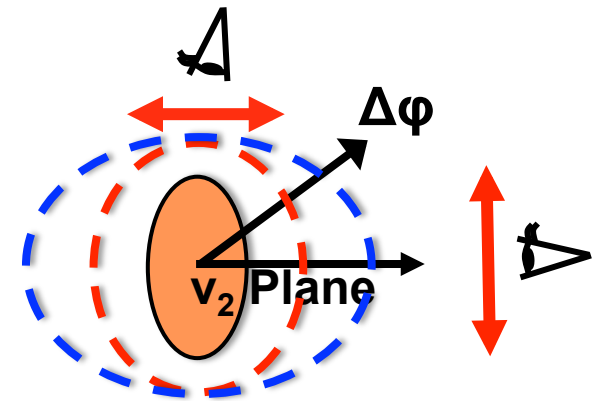
Initial spatial eccentricity



Momentum anisotropy v_2



What is the final eccentricity ?



■ Final eccentricity can be measured by azimuthal HBT

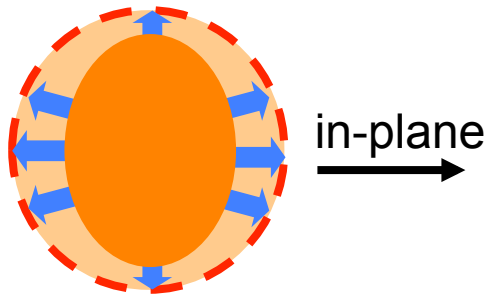
- ✧ It depends on initial eccentricity, pressure gradient, expansion time, and velocity profile, etc.
- ✧ Good probe to investigate system evolution

Eccentricity at freeze-out

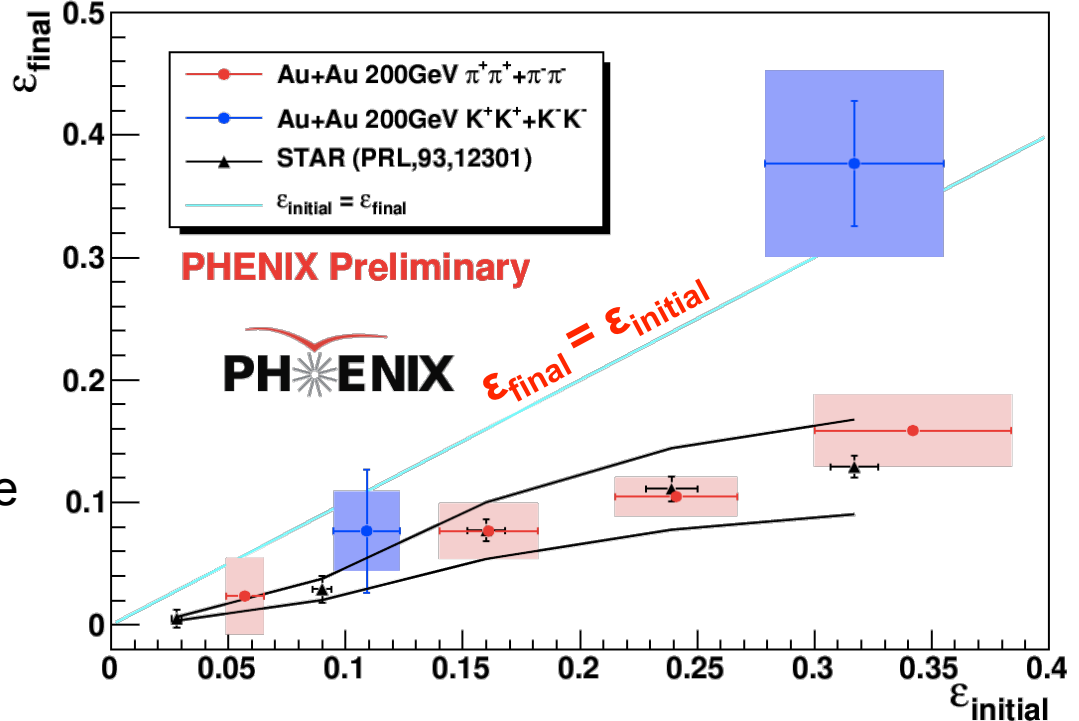
R_s^2 PRC70, 044907 (2004)

$$R_{s,n}^2 = \langle R_{s,n}^2 (\Delta\phi) \cos(n\Delta\phi) \rangle$$

$$\epsilon_{final} = 2 \frac{R_{s,2}^2}{R_{s,0}^2}$$



@WPCF2011



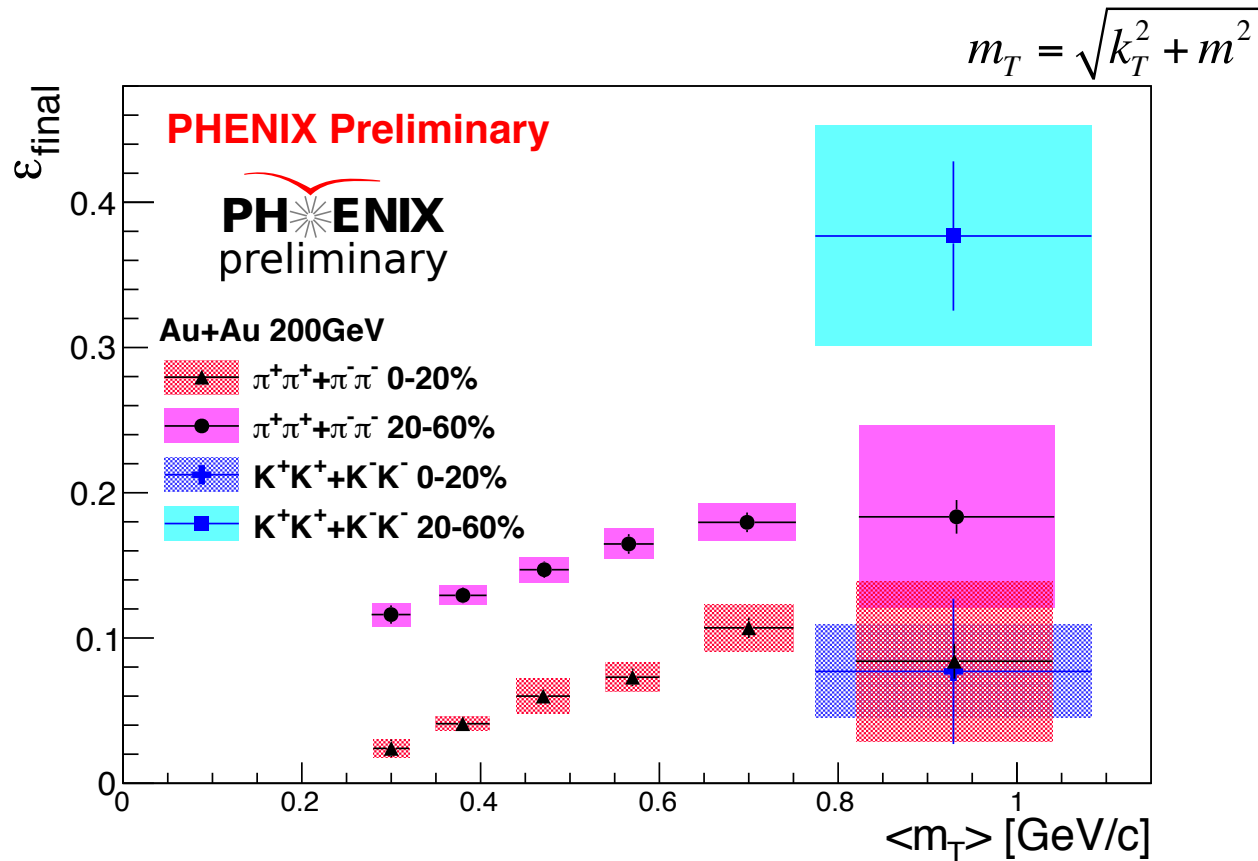
- $\epsilon_{final} \approx \epsilon_{initial}/2$ for pion

- ✧ Indicates that source expands to in-plane direction, and still elliptical shape
- ✧ PHENIX and STAR results are consistent

- $\epsilon_{final} \approx \epsilon_{initial}$ for kaon

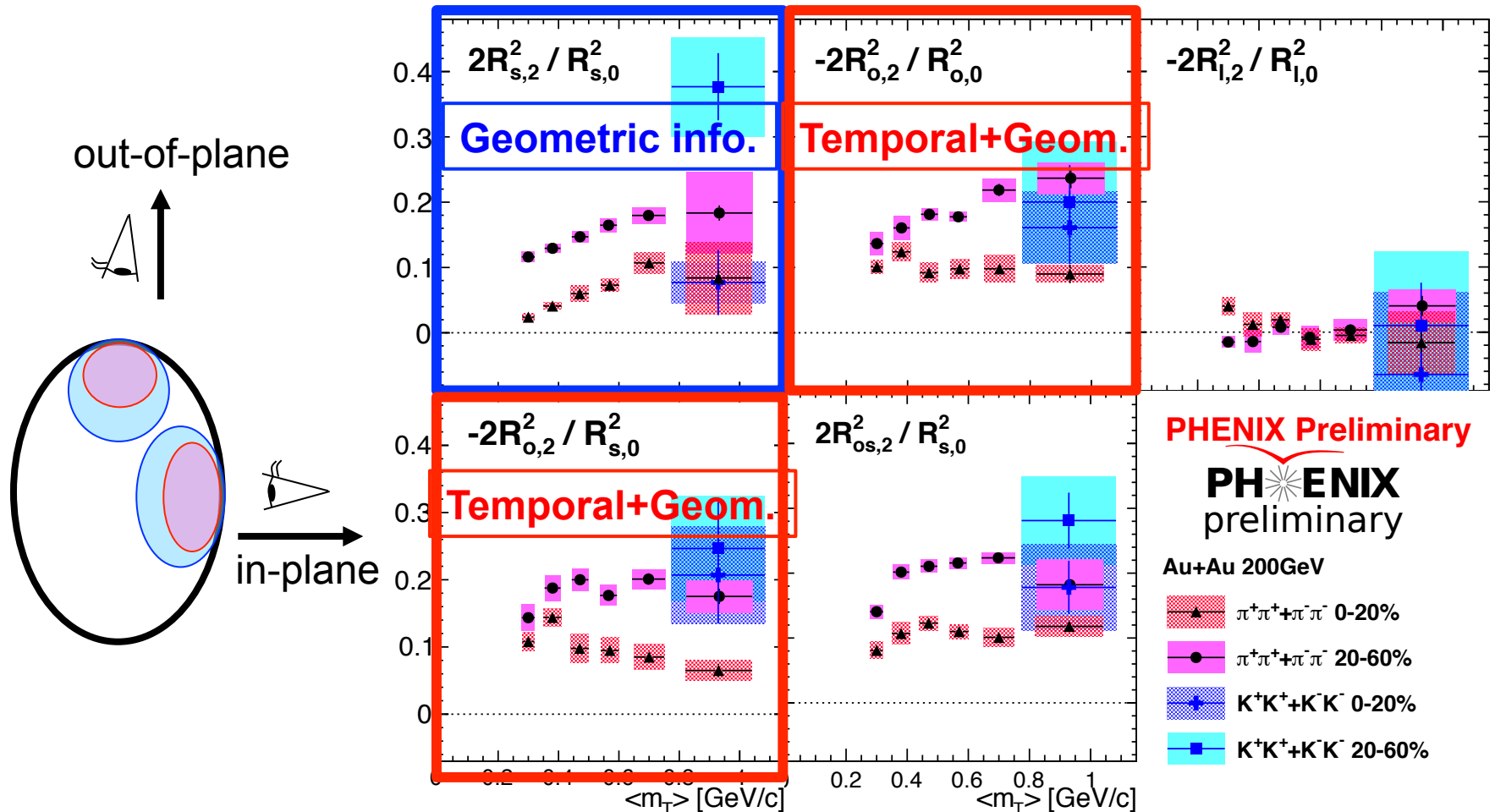
- ✧ Kaon may freeze-out sooner than pion because of less cross section
- ✧ Need to check the difference of m_T between π/K ?

m_T dependence of ϵ_{final}



- ϵ_{final} of pions increases with m_T in most/mid-central collisions
- There is still difference between π/K for mid-central collisions even in same m_T
- ✧ Indicates sooner freeze-out time of K than π ?

m_T dependence of relative amplitude

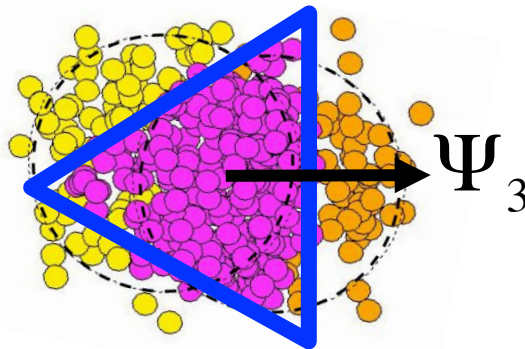


- Relative amplitude of R_{out} in 0-20% doesn't depend on m_T

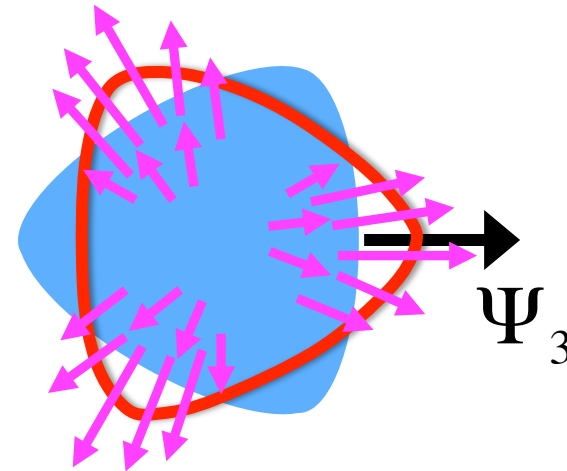
✧ Does it indicate **emission duration** between in-plane and out-of-plane is different at low m_T ?

Azimuthal HBT w.r.t v_3 plane

Initial spatial fluctuation
(triangularity)



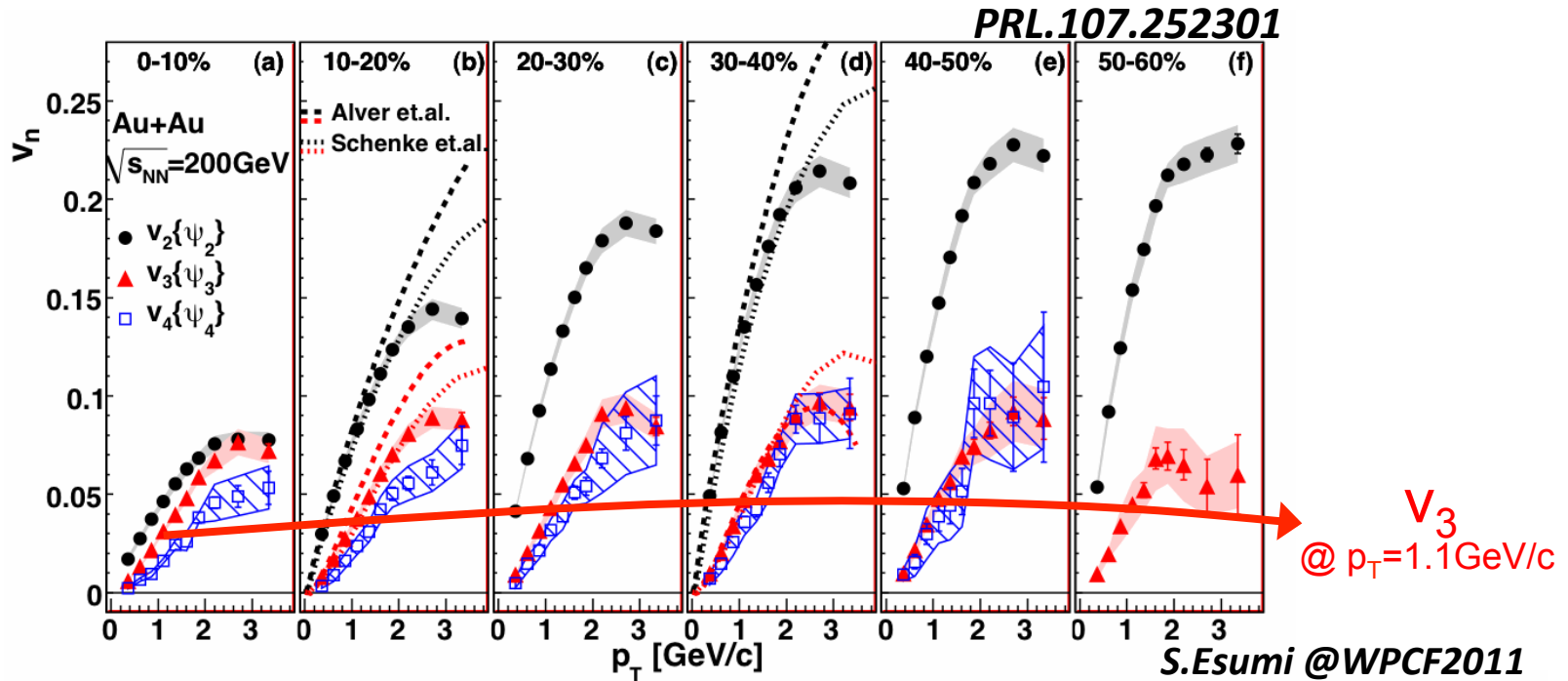
Momentum anisotropy
triangular flow v_3



- Final triangularity could be observed by azimuthal HBT w.r.t v_3 plane (Ψ_3) if it exists at freeze-out

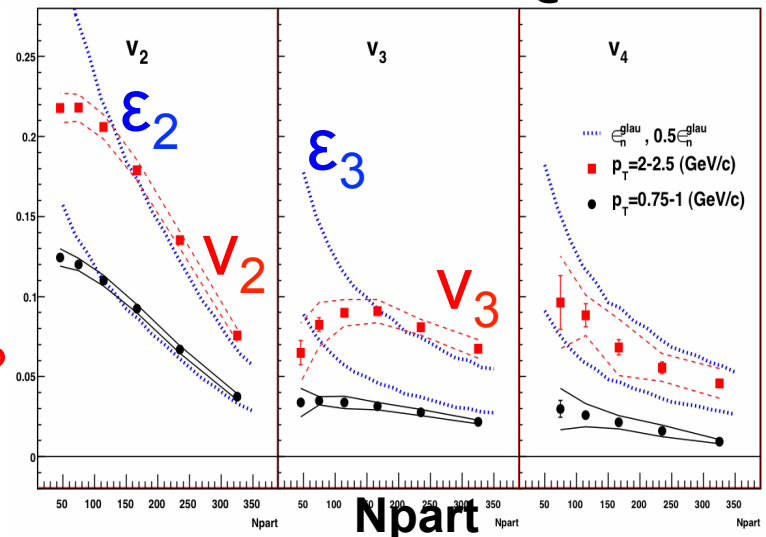
- ✧ Related to initial triangularity, v_3 , and expansion time, etc.
- ✧ Detailed information on space-time evolution can be obtained

Centrality dependence of v_3 and ϵ_3

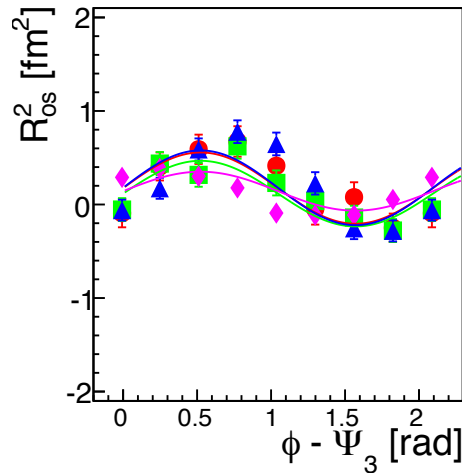
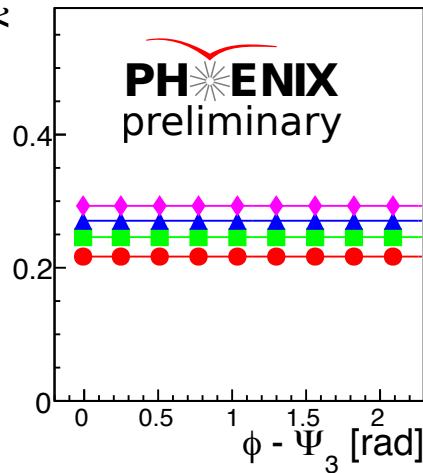
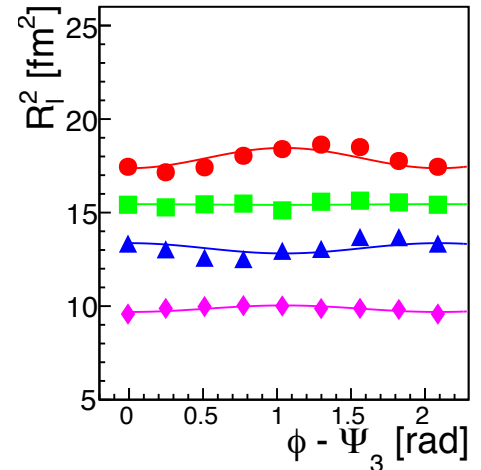
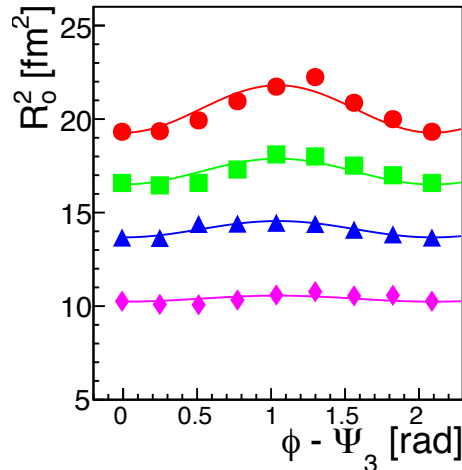
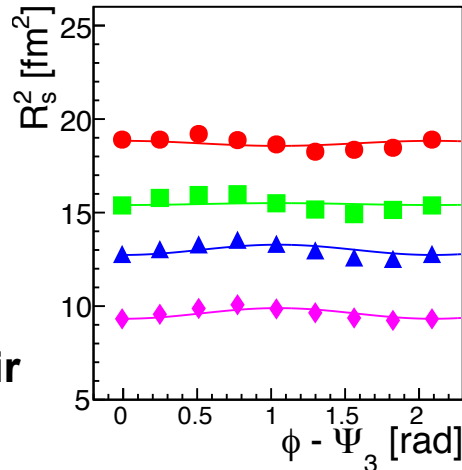
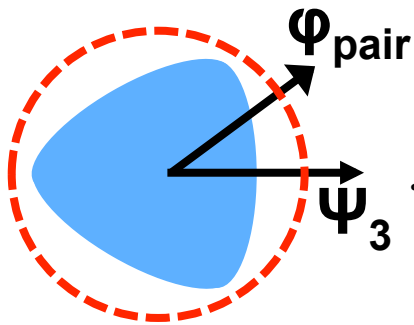


- Weak centrality dependence of v_3
- Initial ϵ_3 has centrality dependence

🍄 Final ϵ_3 has any centrality dependence?



Azimuthal HBT radii w.r.t Ψ_3



PHENIX Preliminary

Au+Au 200GeV $\pi^+\pi^+$ & $\pi^-\pi^-$

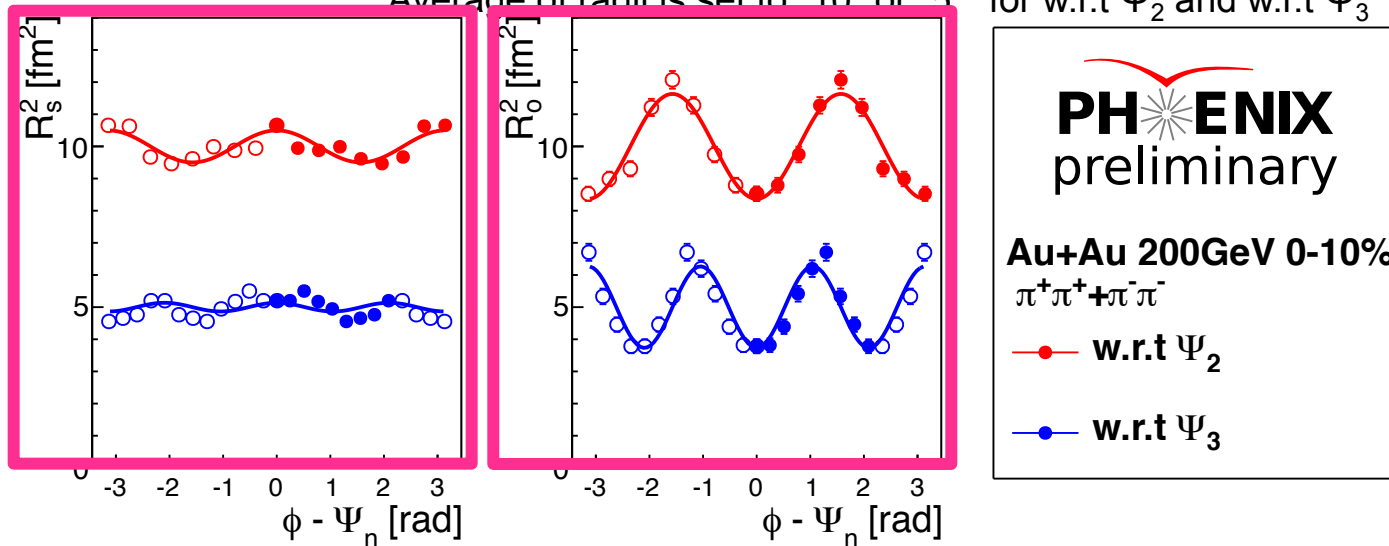
- 0-10%
- 10-20%
- ▲ 20-30%
- ◆ 30-60%

- R_{side} is almost flat
- R_{out} have a oscillation in most central collisions

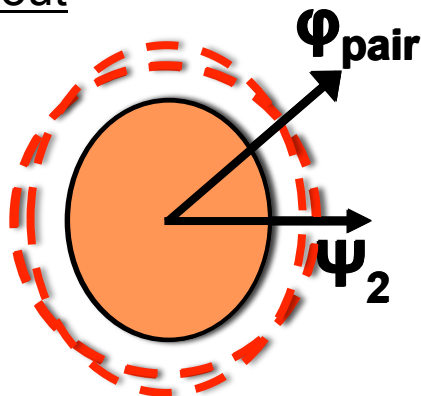
Comparison of 2nd and 3rd order component

- In 0-10%, R_{out} have stronger oscillation for Ψ_2 and Ψ_3 than R_{side}
- ✧ Its oscillation indicates different emission duration between $0^\circ/60^\circ$ w.r.t Ψ_3

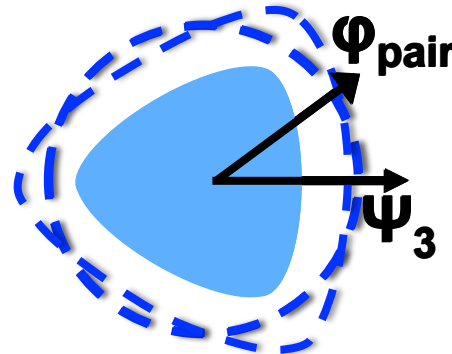
Average of radii is set to "10" or "5" for w.r.t Ψ_2 and w.r.t Ψ_3



R_{out}

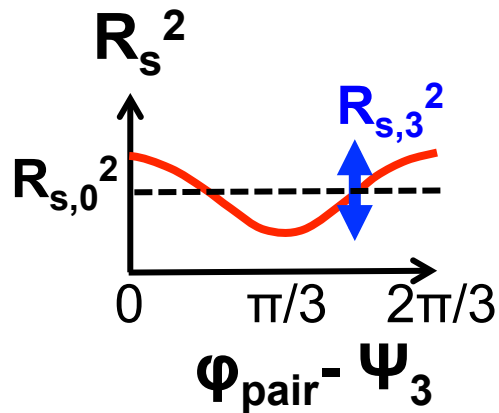


R_{side}

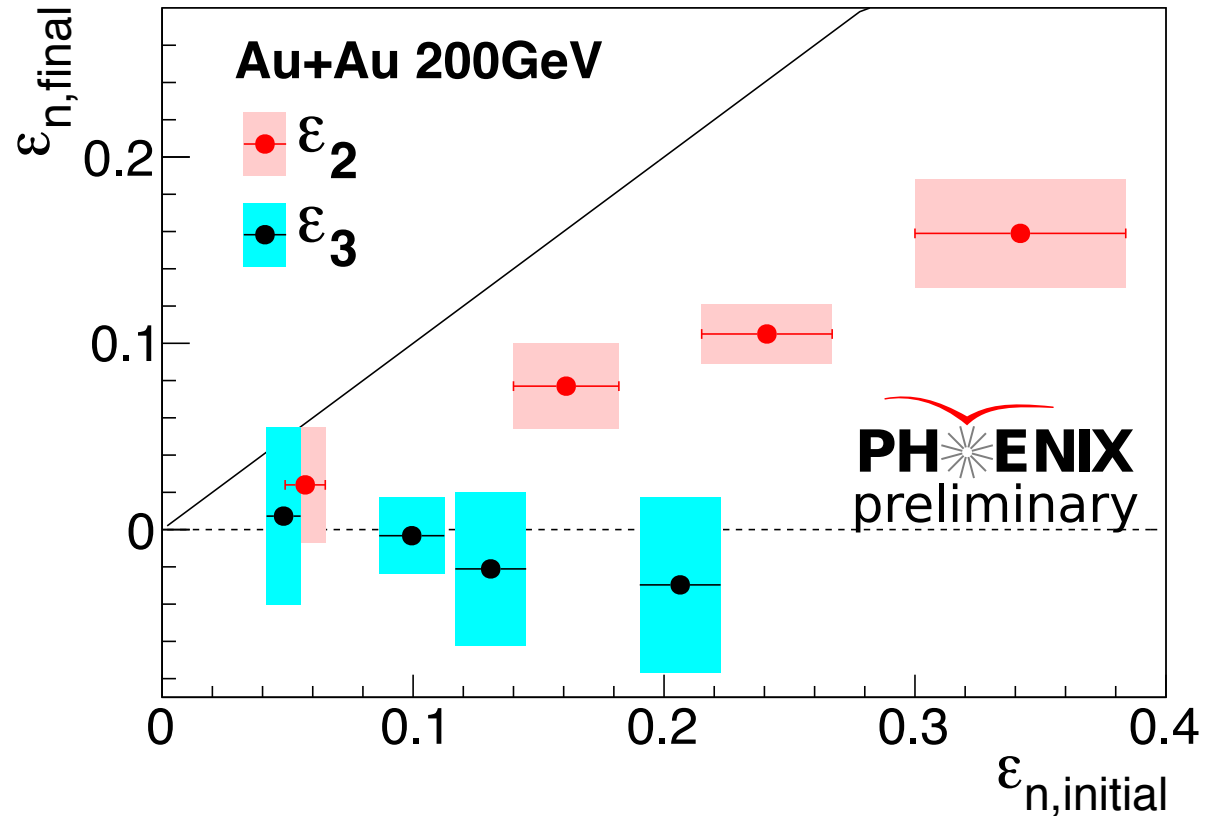


Triangularity at freeze-out

- Relative amplitude is used to represent “triangularity” at freeze-out



$$\varepsilon_{3,\text{final}} = 2 \frac{R_{s,3}^2}{R_{s,0}^2}$$



- ★ Triangular component at freeze-out seems to vanish for all centralities within systematic error

Spatial anisotropy by Blast wave model

Poster, Board #195
Sanshiro Mizuno

Blast wave fit for spectra & v_n

Parameters used in the model

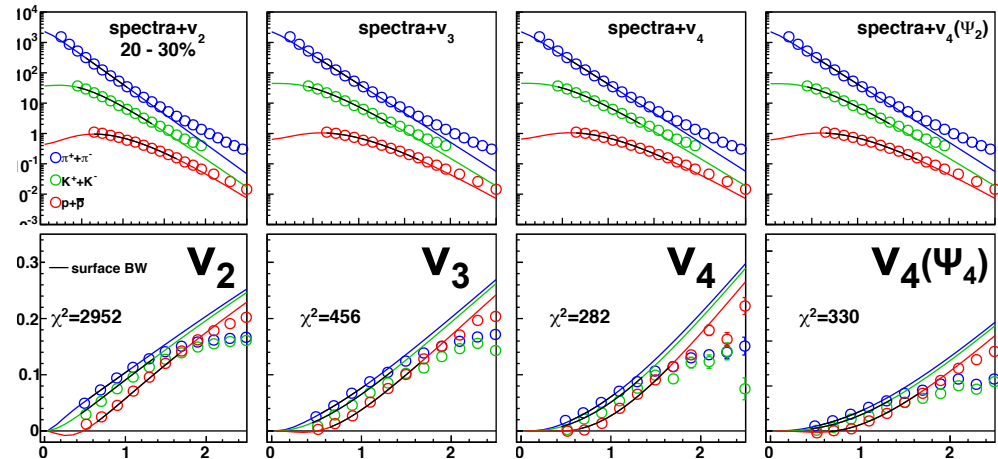
T_f : temperature at freeze-out

ρ_0 : average velocity

ρ_n : anisotropic velocity

s_n : spatial anisotropy

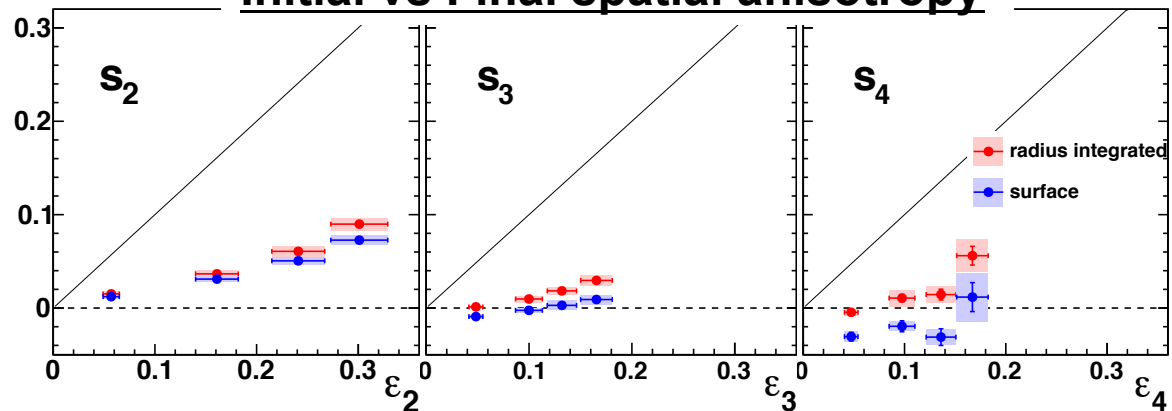
s_2 and s_3 correspond to final eccentricity and triangularity



s_2 increase with going to peripheral collisions

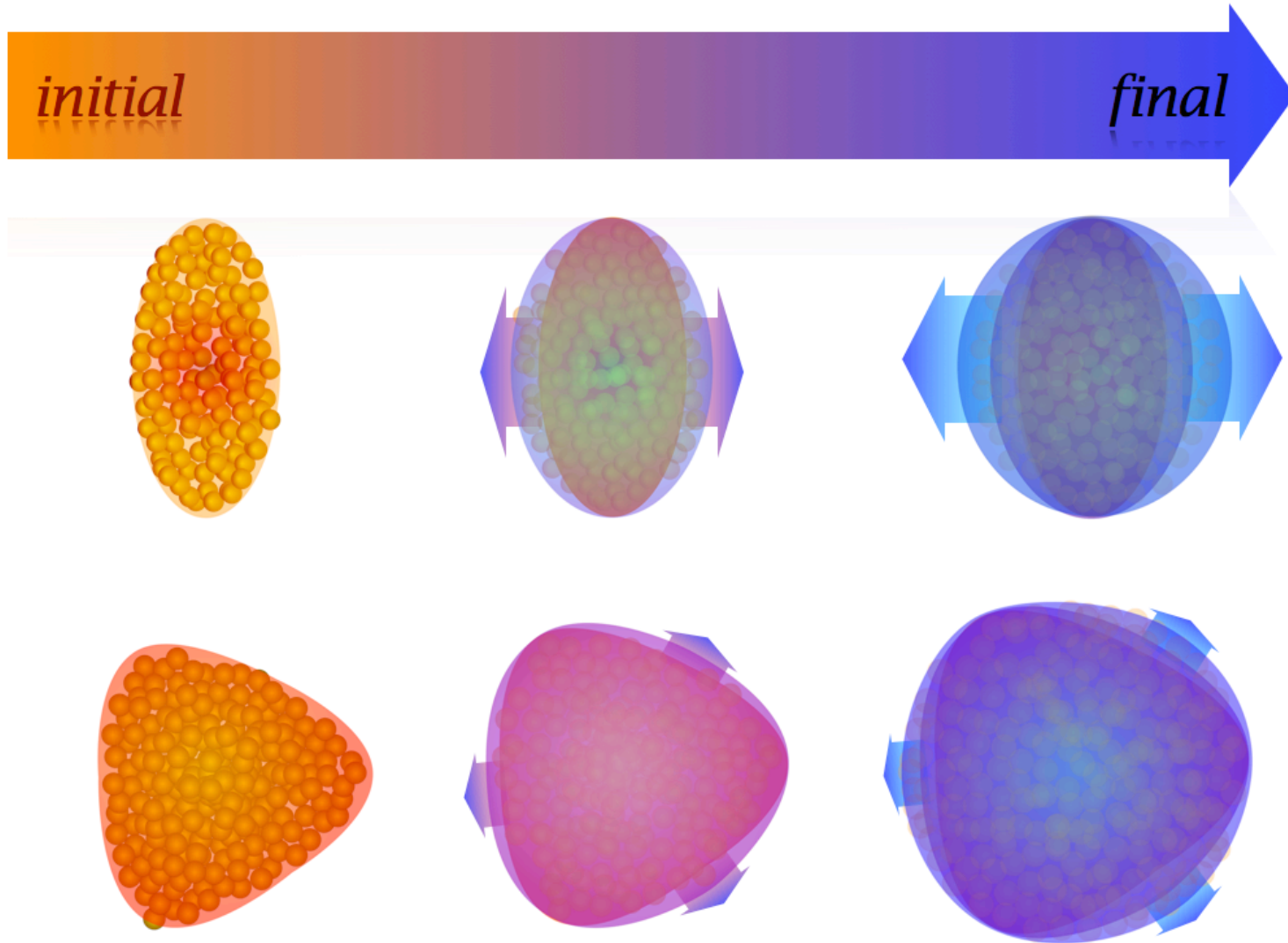
s_3 is almost zero

Initial vs Final spatial anisotropy

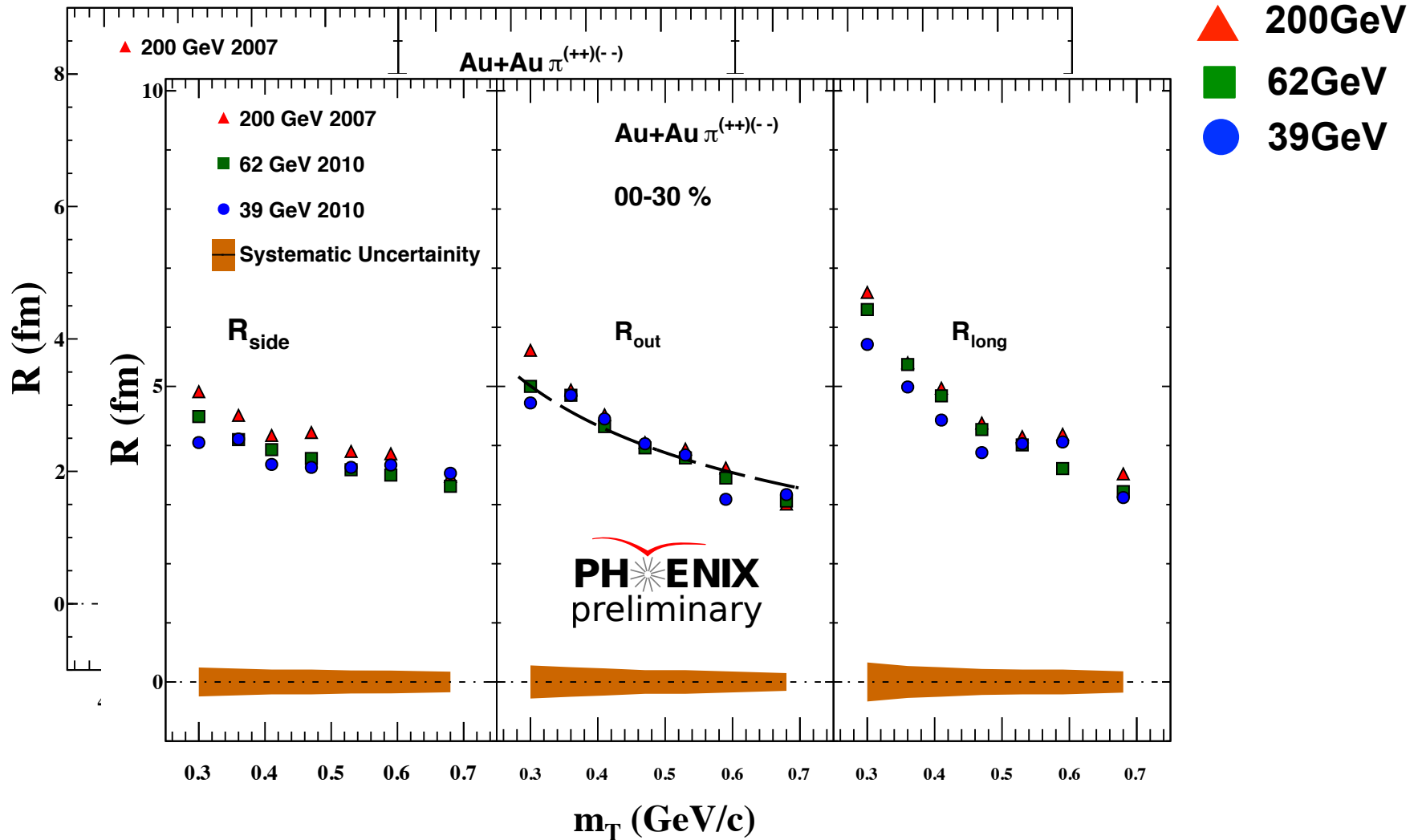


Similar results with HBT

Image of initial/final source shape



Low energy at PHENIX

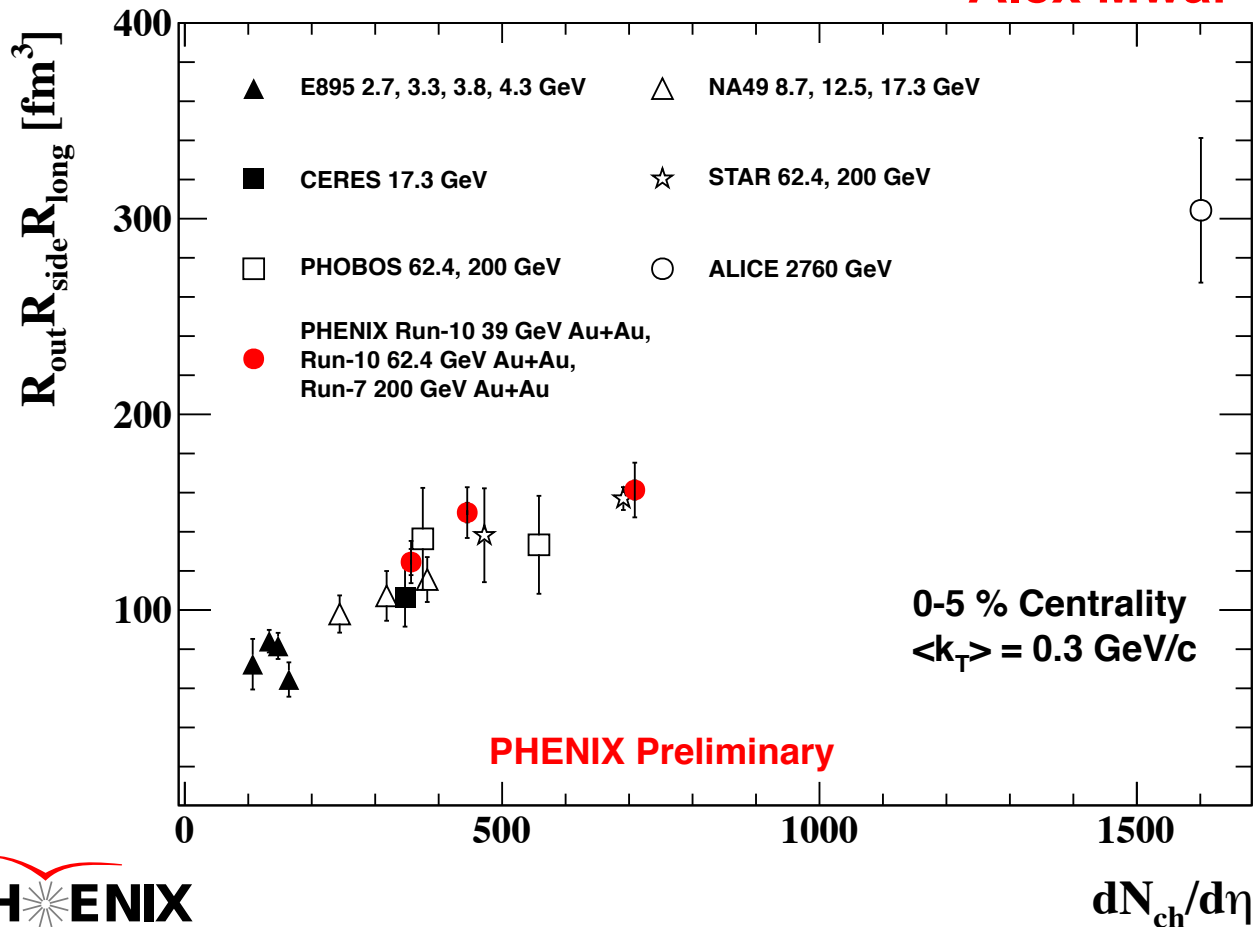


■ No significant change beyond systematic error in 200GeV, 62GeV and 39GeV for centrality and m_T dependence

Volume vs Multiplicity

- Product of 3D HBT radii shows the volume of homogeneity regions
- Consistent with global trends

Poster, Board #246
Alex Mwai



Summary

■ Azimuthal HBT radii w.r.t v_2 plane

- ✧ Final eccentricity increases with increasing m_T , but not enough to explain the difference between π/K
 - 👉 Difference may indicate faster freeze-out of K due to less cross section
- ✧ Relative amplitude of R_{out} in 0-20% doesn't depend on m_T
 - 👉 It may indicate the difference of emission duration between in-plane and out-of-plane

■ Azimuthal HBT radii w.r.t v_3 plane

- ✧ First measurement of final triangularity have been presented. It seems to vanish at freeze-out by expansion.
- ✧ while R_{out} clearly has finite oscillation in most central collisions
 - 👉 It may indicate the difference of emission duration between $\Delta\phi=0^\circ/60^\circ$ direction

■ Low energy in Au+Au collisions

- ✧ No significant change between 200, 62 and 39 [GeV]
- ✧ Volume is consistent with global trends

Thank you for your attention!

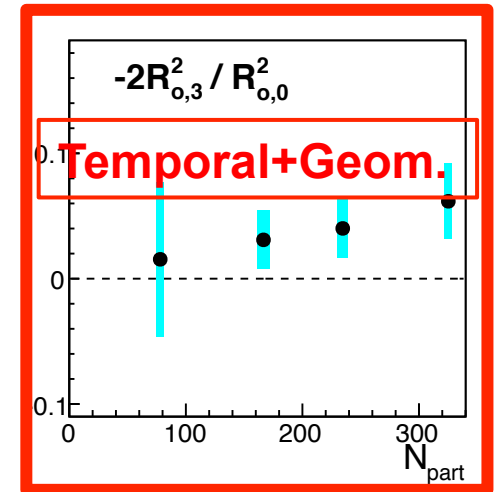
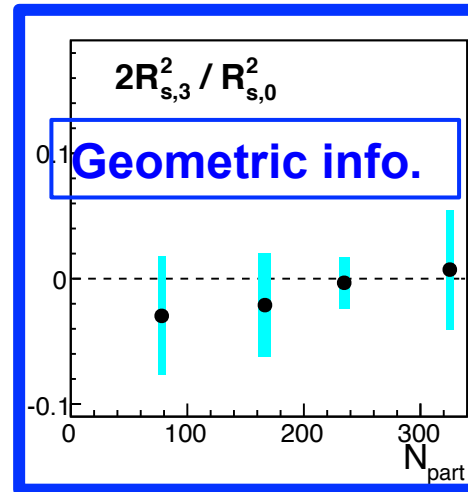
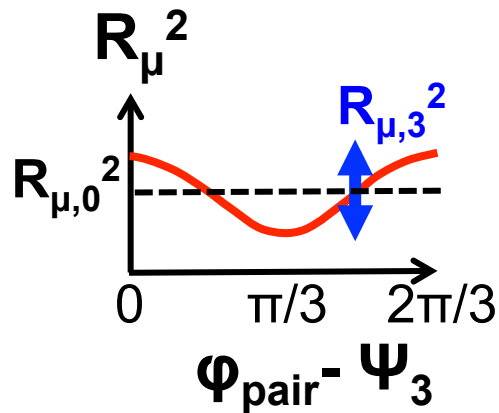


Japanese rice ball
has just “triangular shape” !!

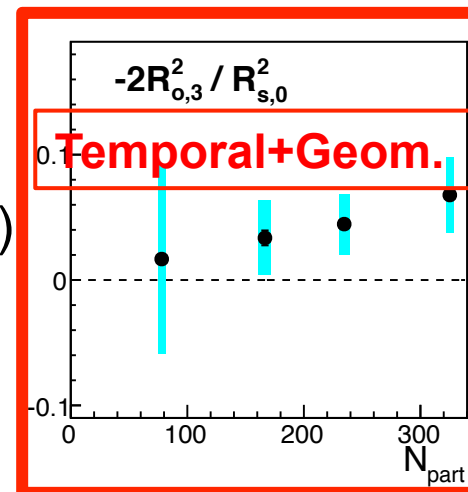
Back up

Relative amplitude of HBT radii

- Relative amplitude is used to represent “triangularity” at freeze-out
- Relative amplitude of **R_{out} increases** with increasing N_{part}



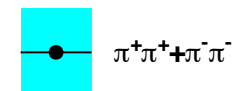
☆ Triangular component at freeze-out seems to vanish for all centralities (within systematic error)



PHENIX Preliminary

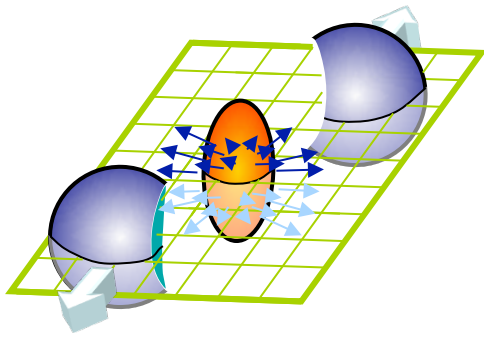
PHENIX
preliminary

Au+Au 200GeV

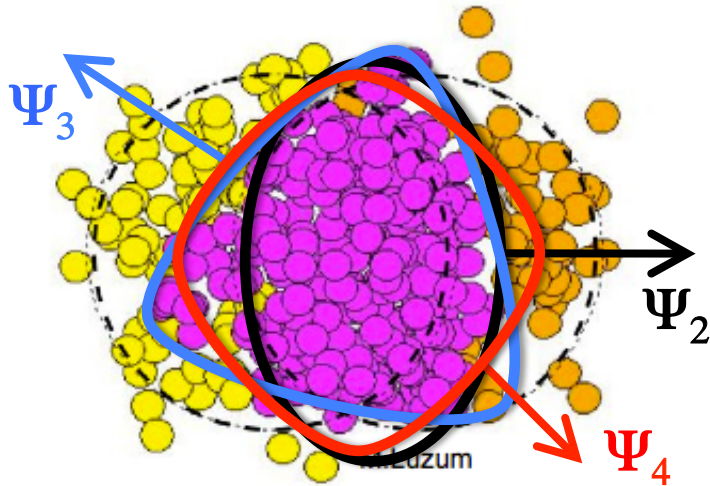


Higher harmonic event plane

- Initial density fluctuations cause higher harmonic flow v_n
- Azimuthal distribution of emitted particles:



$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos 2(\phi - \Psi_2) + 2v_3 \cos 2(\phi - \Psi_3) + 2v_4 \cos 2(\phi - \Psi_4)$$



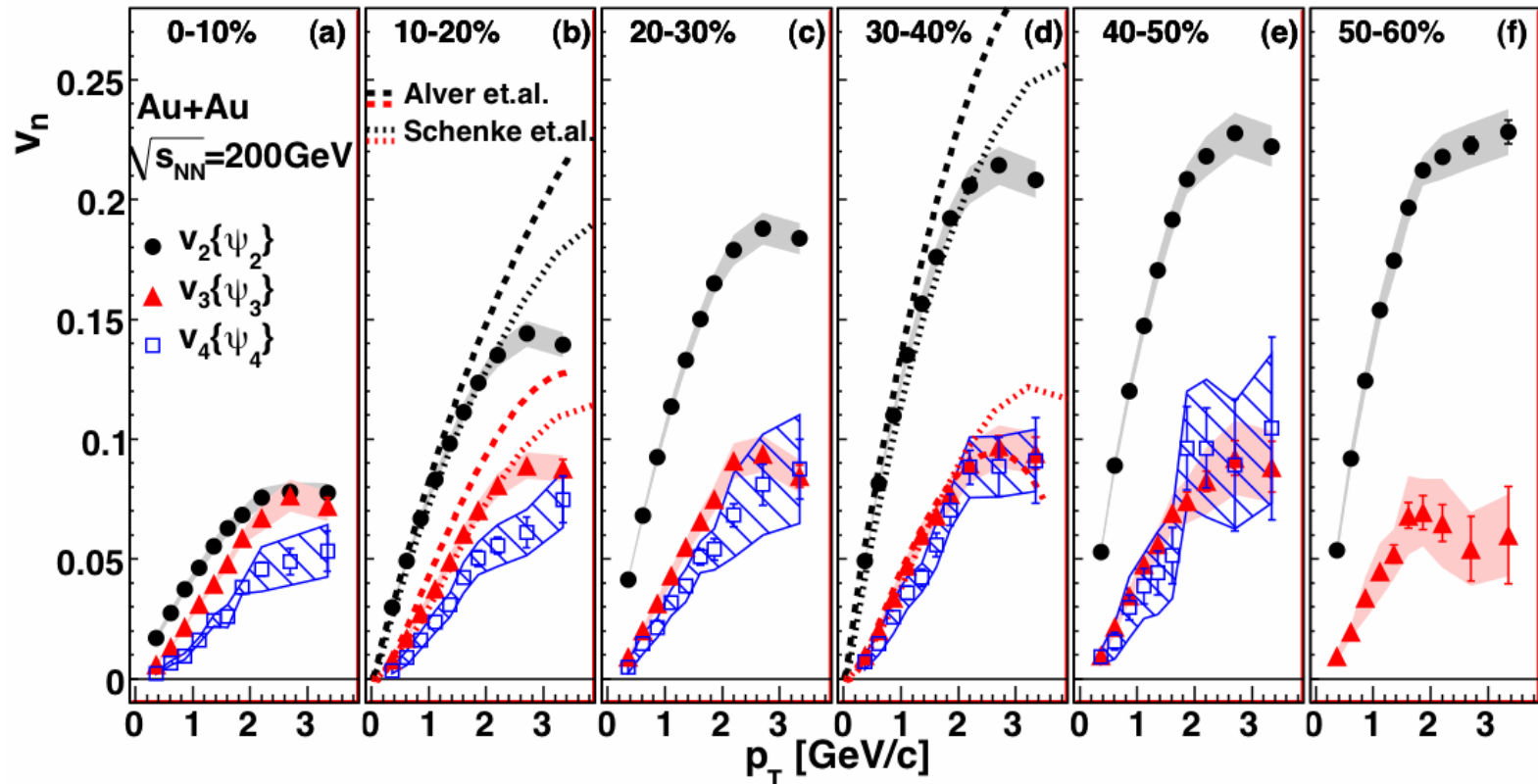
$$v_n = \langle \cos n(\phi - \Psi_n) \rangle$$

Ψ_n : Higher harmonic event plane

ϕ : Azimuthal angle of emitted particles

Charged hadron v_n at PHENIX

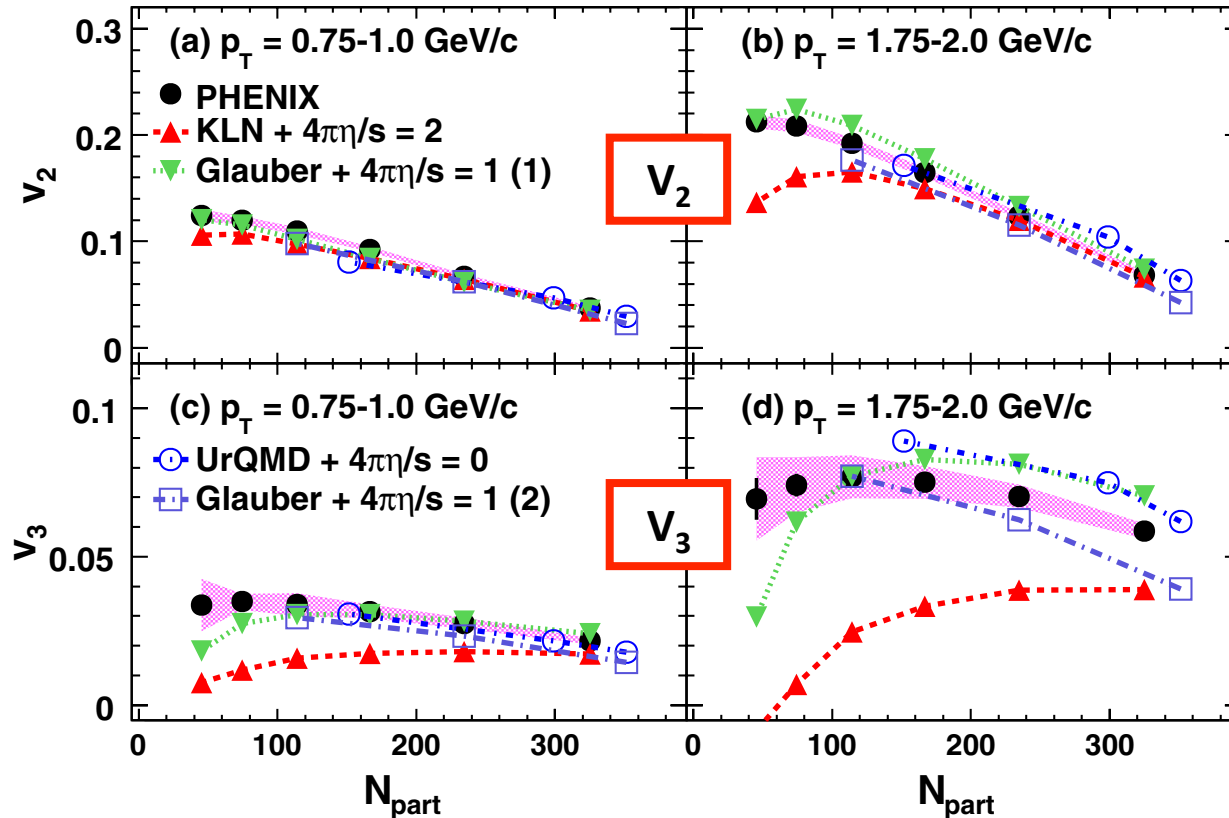
PRL.107.252301



- v_2 increases with increasing centrality, but v_3 doesn't
- v_3 is comparable to v_2 in 0-10%
- v_4 has similar dependence to v_2

v_3 breaks degeneracy

PRL.107.252301



■ v_3 provides new constraint on hydro-model parameters

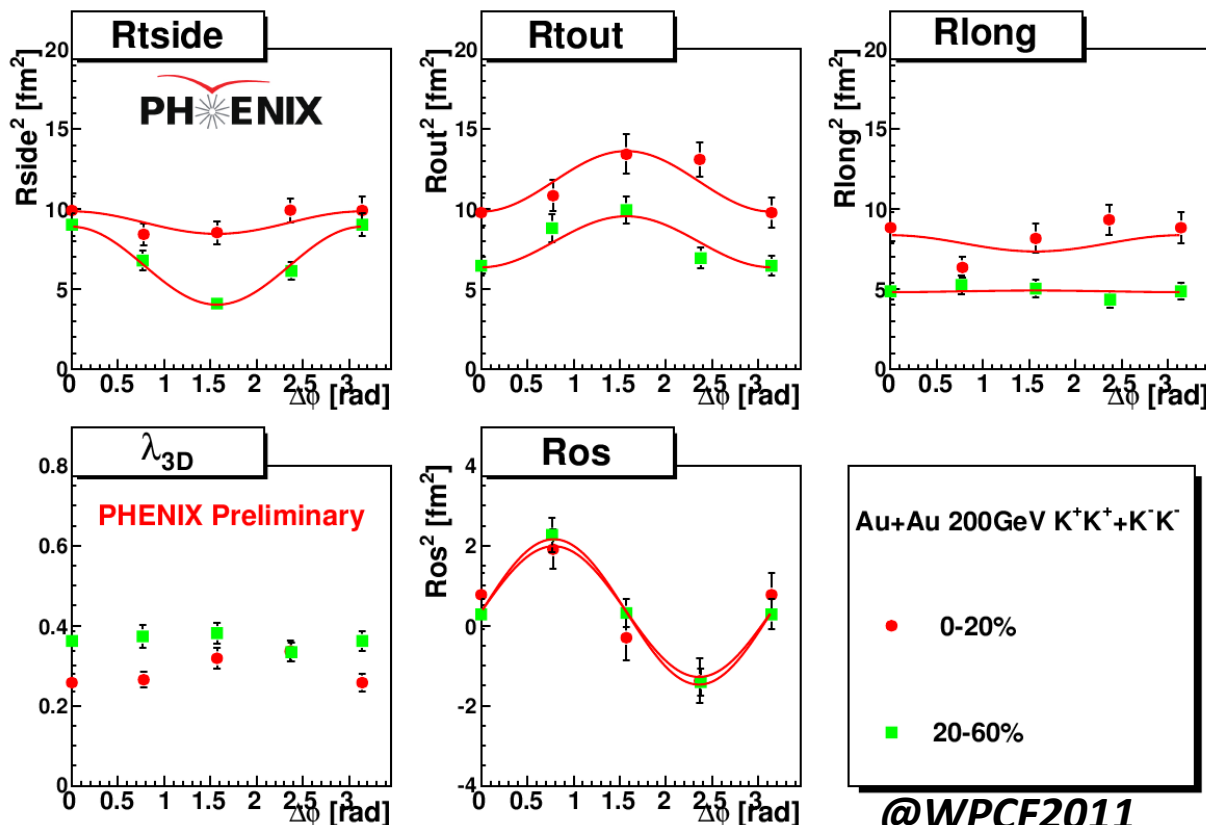
✧ Glauber & $4\pi\eta/s=1$: works better

✧ KLN & $4\pi\eta/s=2$: fails

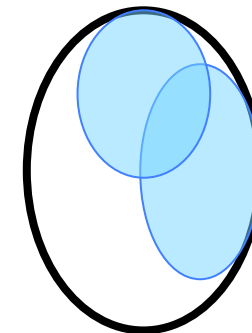
Azimuthal HBT radii for kaons

- Observed oscillation for R_{side} , R_{out} , R_{os}
- Final eccentricity is defined as $\epsilon_{\text{final}} = 2R_{s,2} / R_{s,0}$

$$\diamond R_{s,n}^2 = \langle R_{s,n}^2(\Delta\phi) \cos(n\Delta\phi) \rangle \quad \text{PRC70, 044907 (2004)}$$

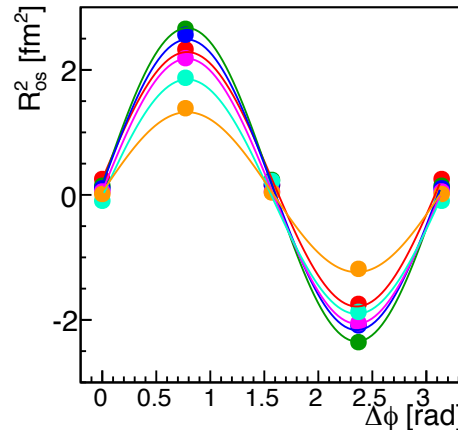
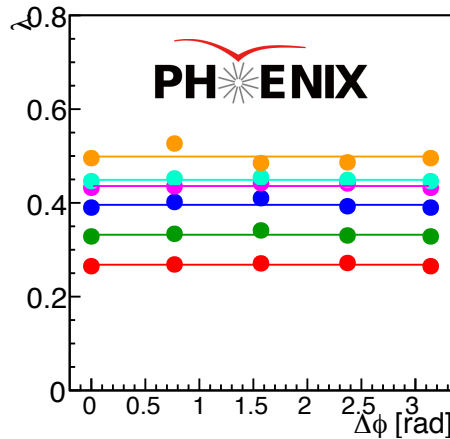
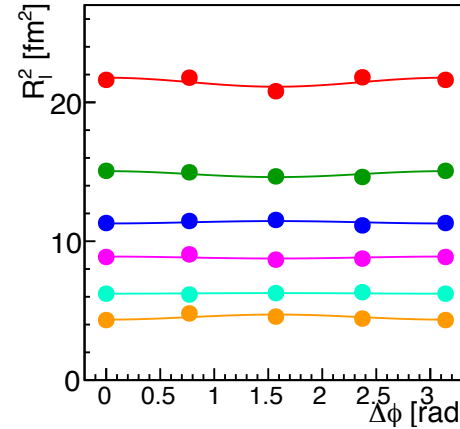
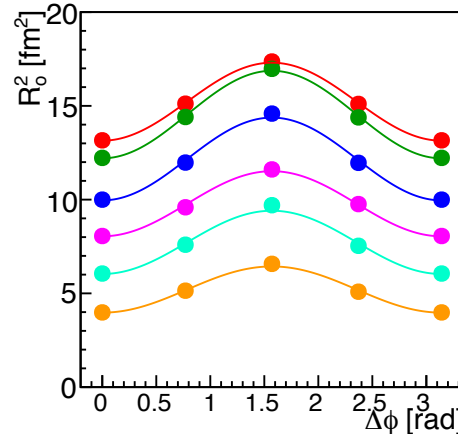
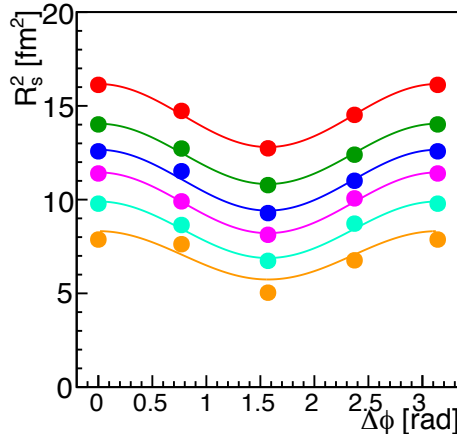


in-plane



out-of-plane

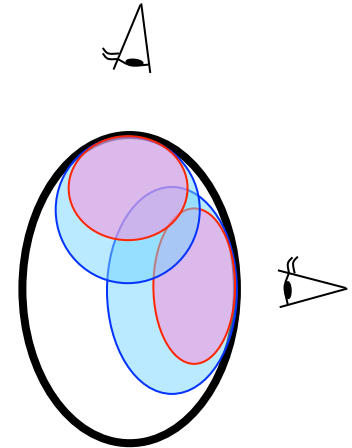
k_T dependence of azimuthal pion HBT radii in 20-60%



PHENIX Preliminary

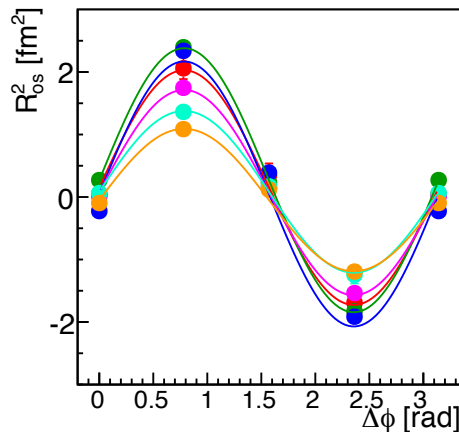
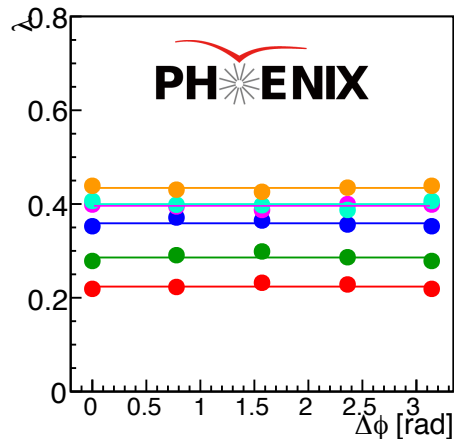
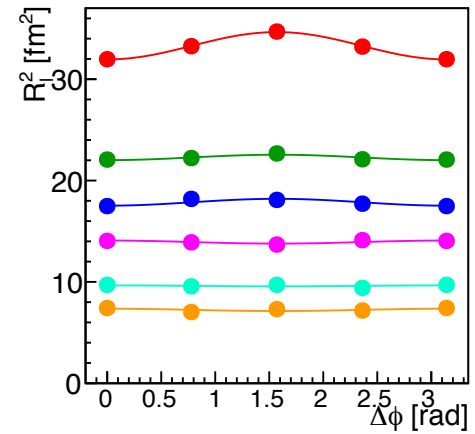
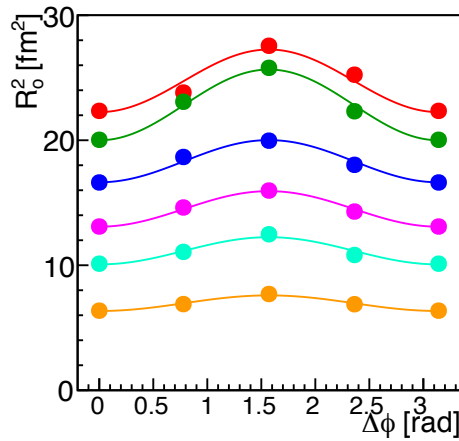
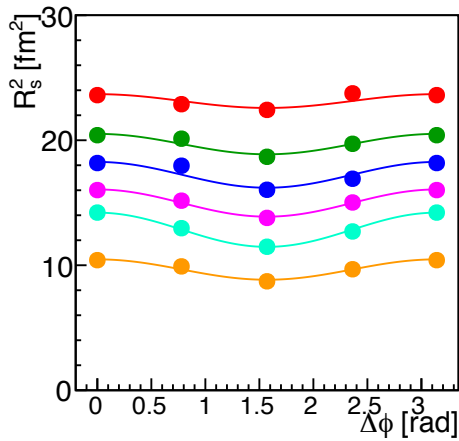
Au+Au 200GeV $\pi^+\pi^+$ & $\pi^-\pi^-$
centrality: 20-60%

- k_T 0.2-0.3
- k_T 0.3-0.4
- k_T 0.4-0.5
- k_T 0.5-0.6
- k_T 0.6-0.8
- k_T 0.8-1.5



■ Oscillation can be seen in R_s , R_o , and R_{os} for each k_T regions

k_T dependence of azimuthal pion HBT radii in 0-20%



PHENIX Preliminary

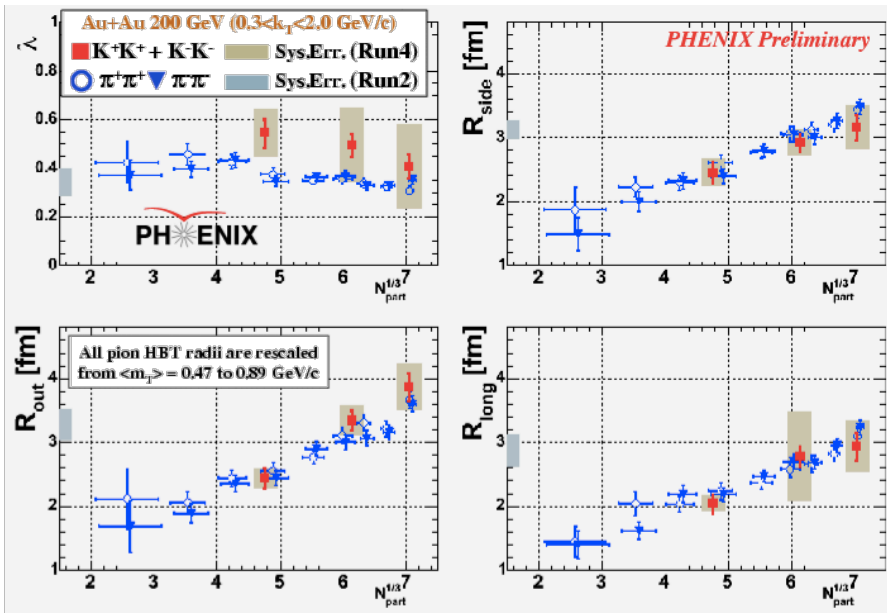
**Au+Au 200GeV $\pi^+\pi^+$ & $\pi^-\pi^-$
centrality: 0-20%**

- k_T 0.2-0.3 ● k_T 0.5-0.6
- k_T 0.3-0.4 ● k_T 0.6-0.8
- k_T 0.4-0.5 ● k_T 0.8-1.5

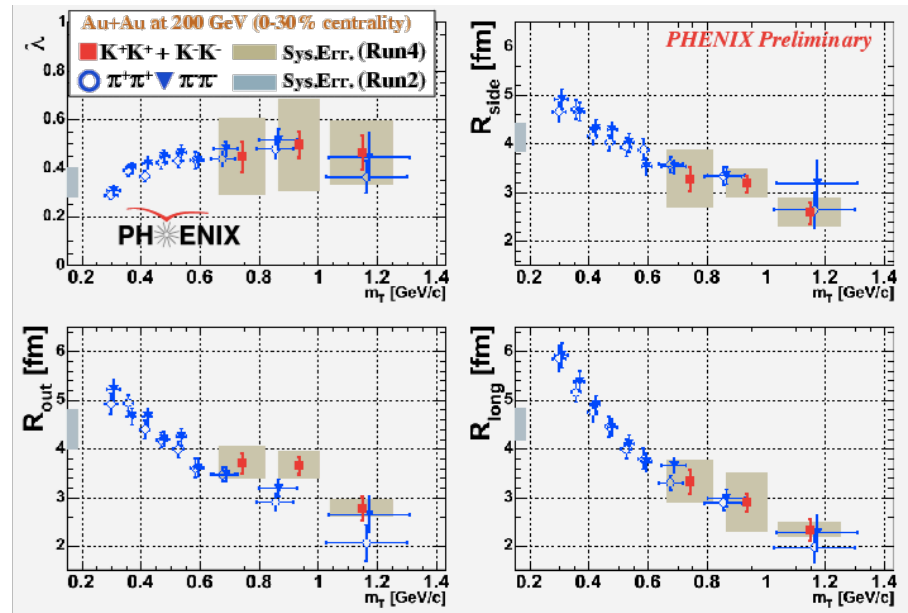
The past HBT Results for charged pions and kaons

- Centrality / m_T dependence have been measured for pions and kaons
- ✧ No significant difference between both species

centrality dependence



m_T dependence



Analysis method for HBT

■ Correlation function

$$C_2 = \frac{R(q)}{M(q)}$$

- ✧ Ratio of real and mixed q-distribution of pairs
q: relative momentum

■ Correction of event plane resolution

- ✧ U.Heinz et al, PRC66, 044903 (2002)

■ Coulomb correction and Fitting

- ✧ By Sinyukov's fit function
- ✧ Including the effect of long lived resonance decay

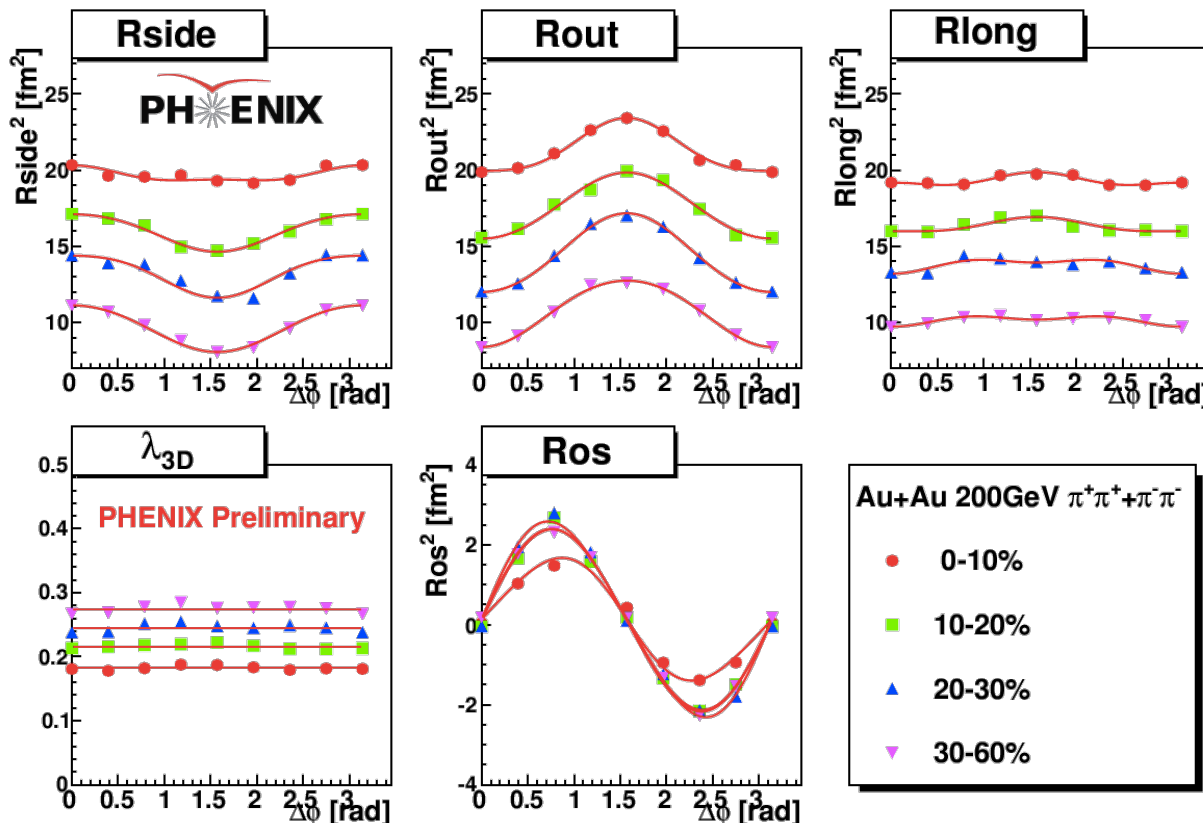
$$\begin{aligned} C_2 &= C_2^{core} + C_2^{halo} \\ &= N[\lambda(1+G)F] + [1-\lambda] \\ G &= \exp(-R_{side}^2 q_{side}^2 - R_{out}^2 q_{out}^2 - R_{long}^2 q_{long}^2 - 2R_{os}^2 q_{side} q_{out}) \end{aligned}$$

Azimuthal HBT radii for pions

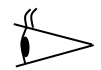
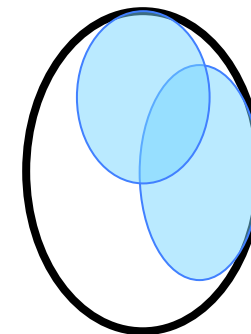
■ Observed oscillation for R_{side} , R_{out} , R_{os}

■ R_{out} in 0-10% has oscillation

✧ Different emission duration between in-plane and out-of-plane?



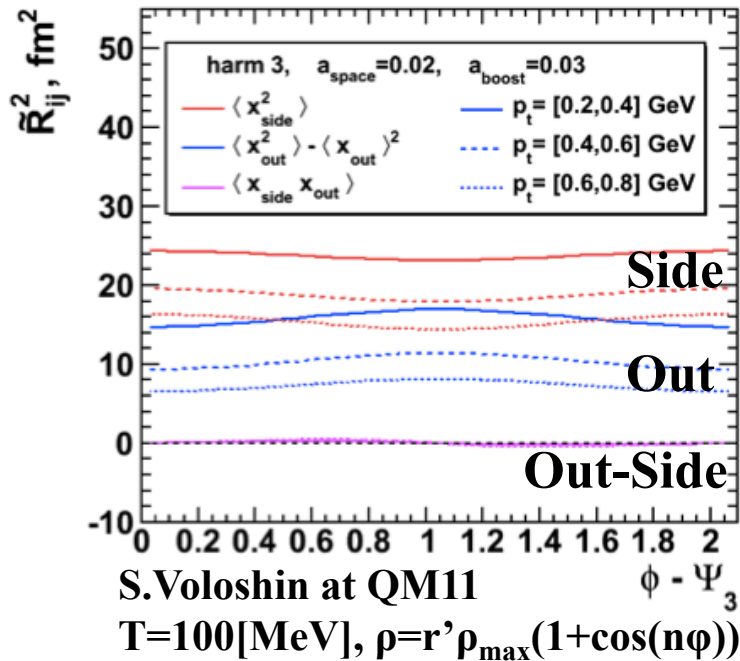
out-of-plane



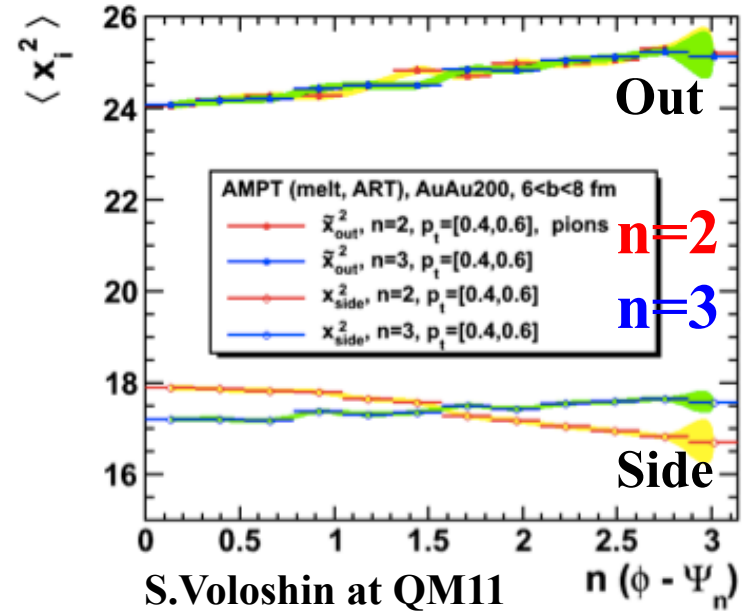
in-plane

Model predictions

Blast-wave model



AMPT



Both models predict weak oscillation will be seen in R_{side} and R_{out} .