

Lattice QCD thermodynamics in the presence of the charm quark

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Wuppertal-Budapest collaboration: S. Borsanyi, Z. Fodor, S. Katz, S. Krieg, C. Schröder, K. Szabó

Outline

- ❖ update on $N_f = 2 + 1$ EoS
 - ⇒ $\mu = 0$ continuum limit
 - ⇒ finite μ EoS at order μ^2
- ❖ new results on $N_f = 2 + 1 + 1$ EoS
 - ⇒ fully dynamical
 - ⇒ comparison to partial quenching analysis
- ❖ introduction of new **4stout** action and $N_f = 2 + 1 + 1$ results
- ❖ conclusions and outlook

$$N_f = 2 + 1$$

dynamical quark flavors

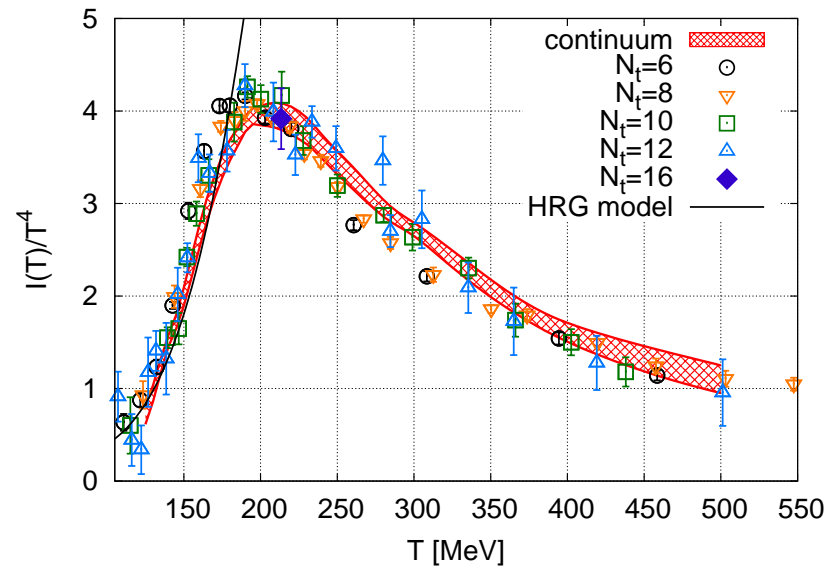
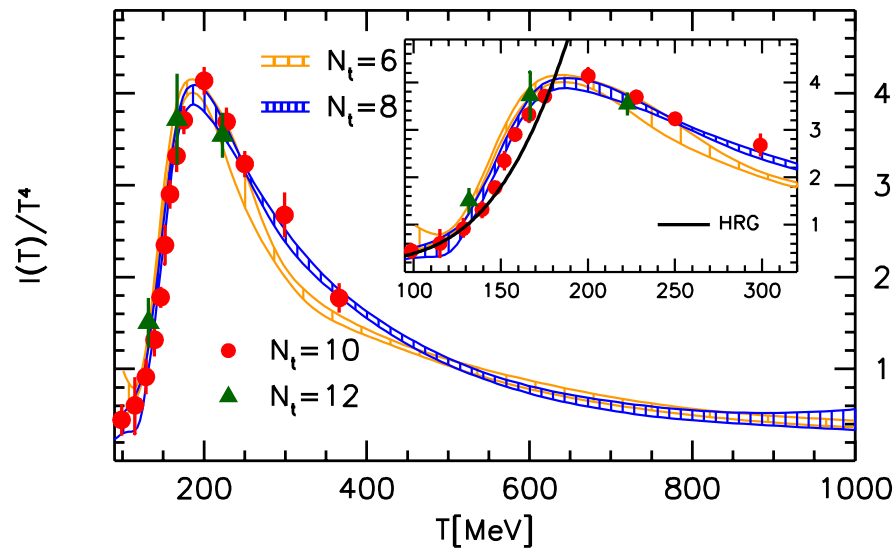
$$m_s/m_{u,d} \simeq 28$$

Results: trace anomaly

$$\frac{I(T)}{T^4} = \frac{\epsilon - 3p}{T^4} = T \frac{\partial}{\partial T} (p/T^4)$$

QM 2011

QM 2012



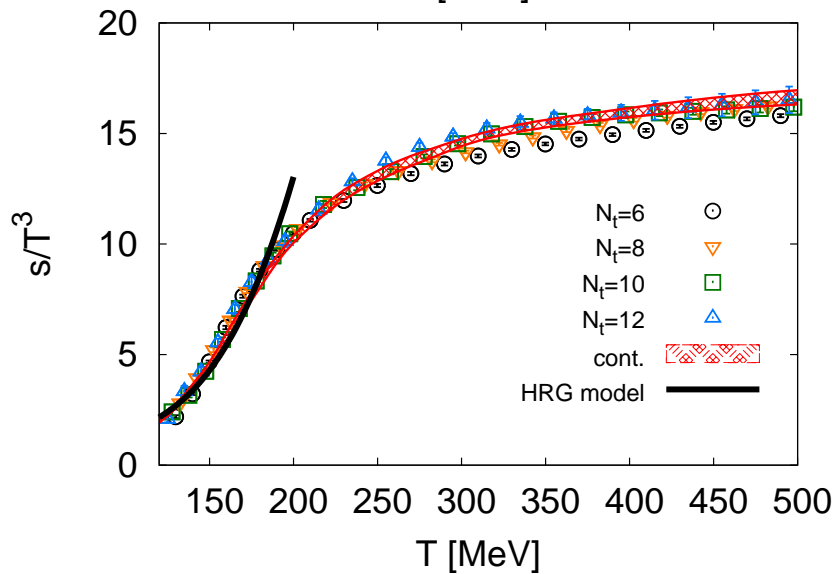
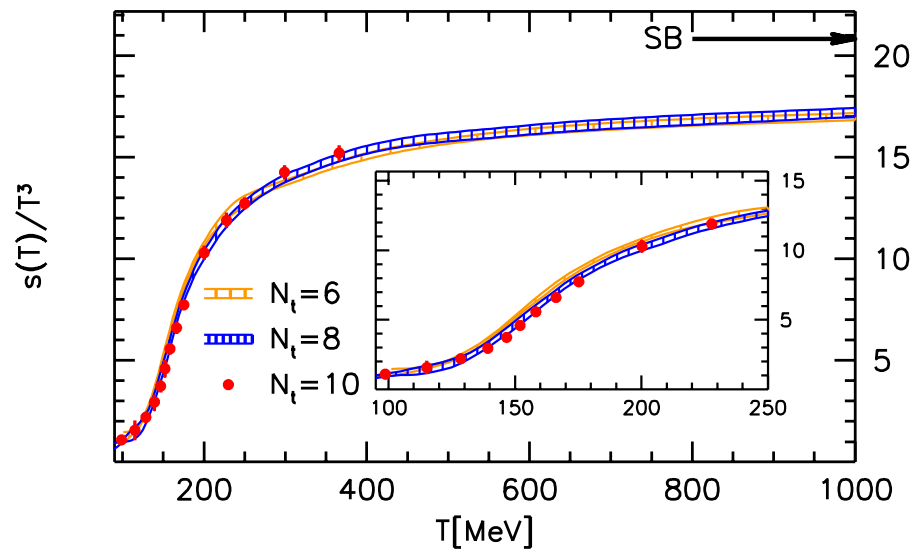
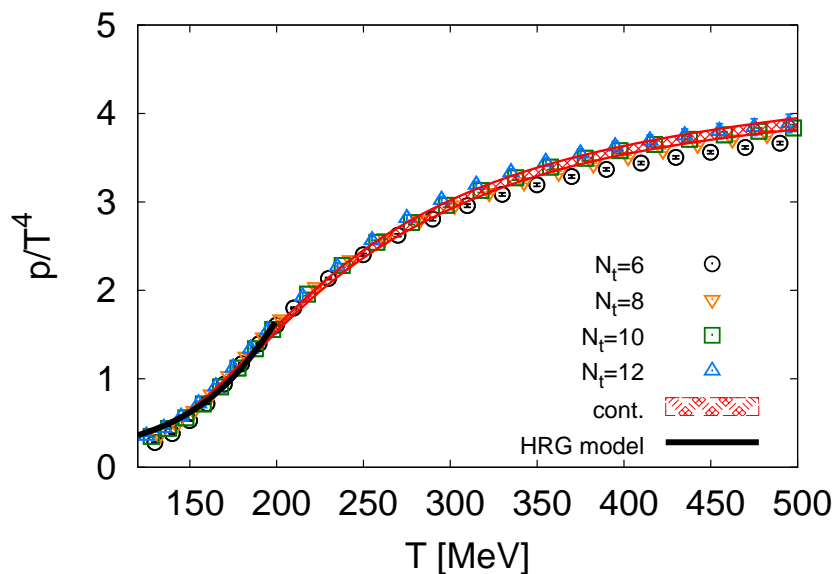
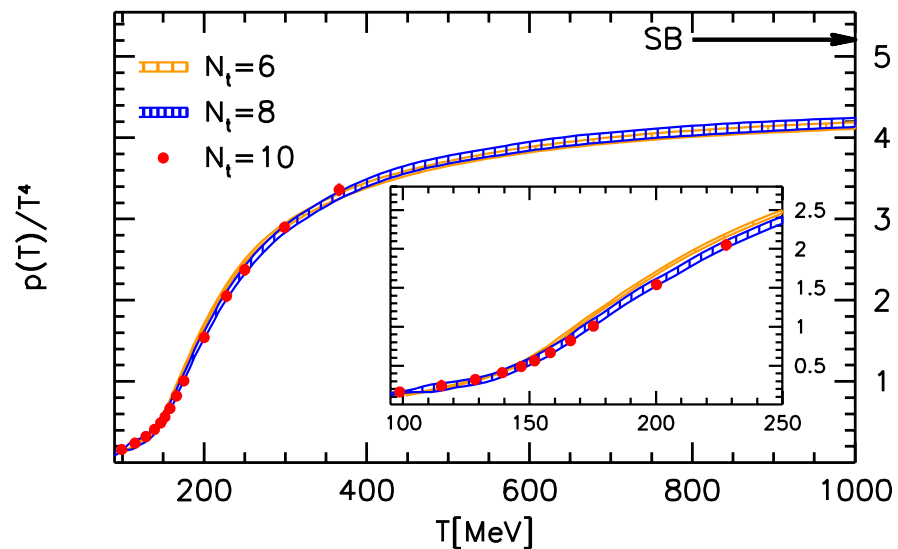
- ◆ New $N_t = 12$ points and one $N_t = 16$ check point
- ◆ consistent continuum extrapolation

S. Borsanyi *et al.* (Wuppertal-Budapest collaboration): JHEP (2010) and in preparation

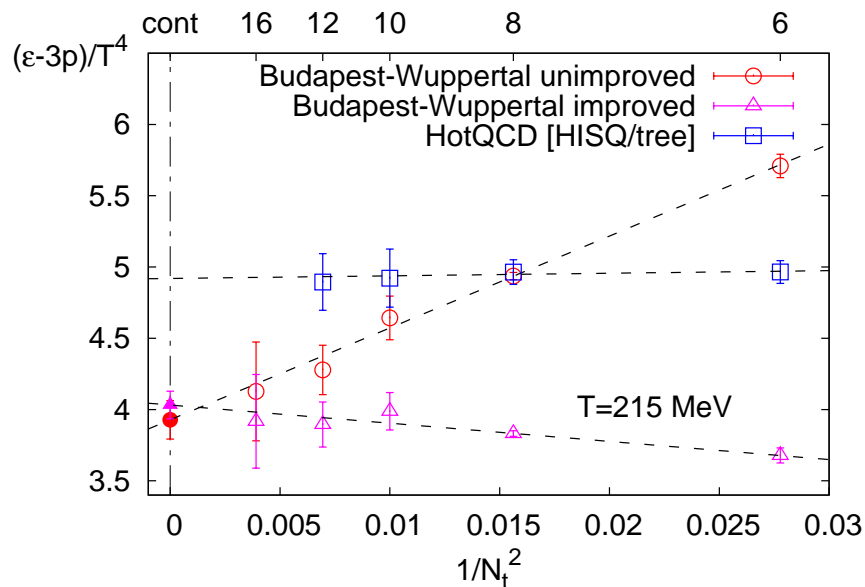
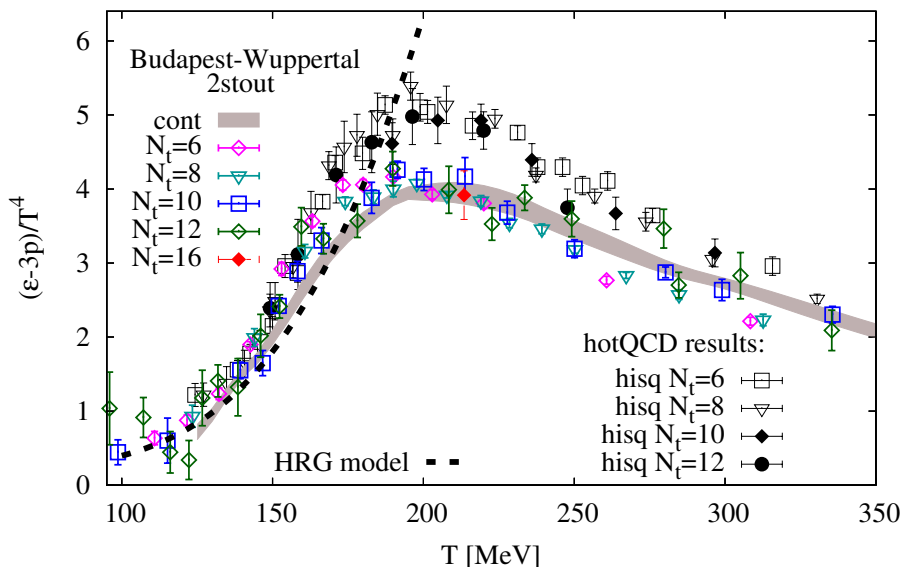
Pressure and entropy density

QM 2011

QM 2012



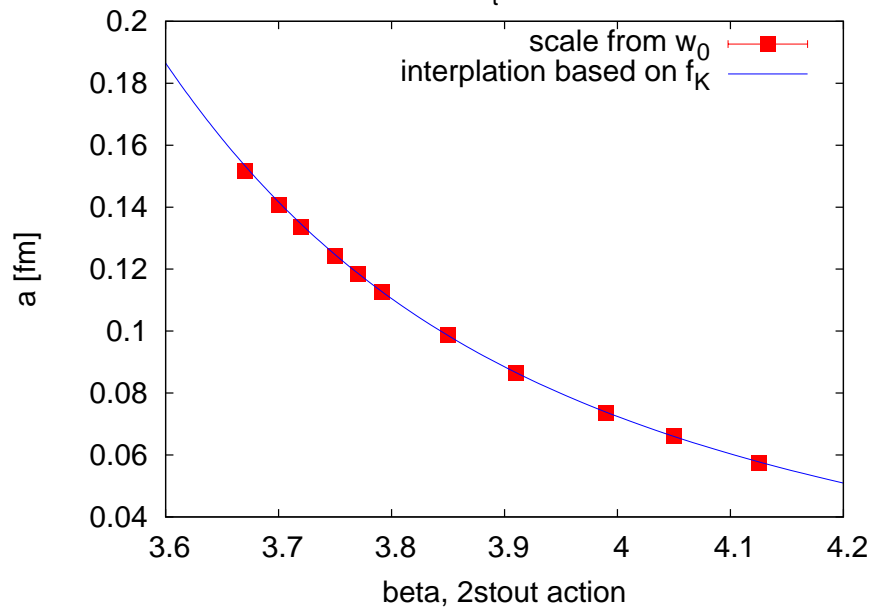
Trace anomaly discrepancy



- ❖ Discrepancy between 2stout (WB) and hisq (hotQCD) on the trace anomaly
- ❖ continuum limits do not seem to converge to the same result

hotQCD: 1005.1131

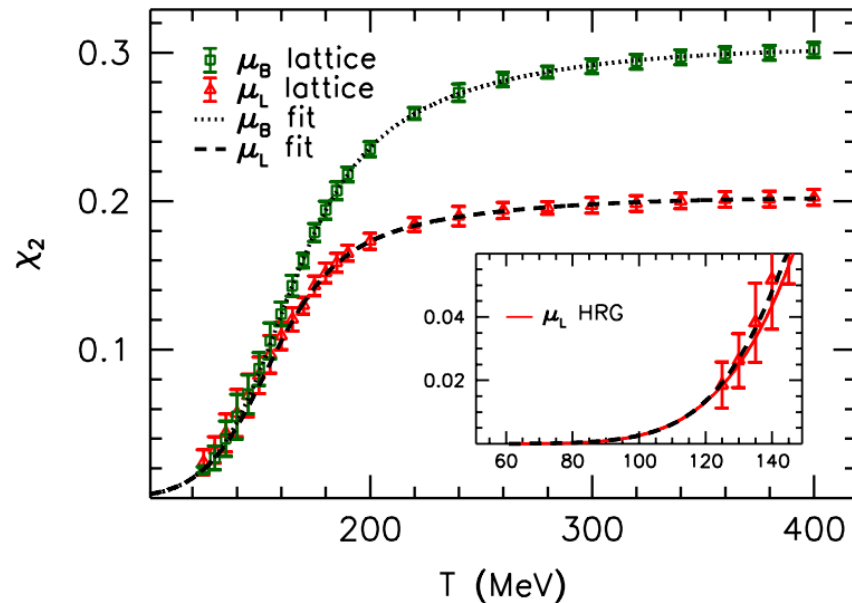
WB: 1204.0995



Finite μ EoS at order μ^2

$$\frac{I(T, \mu)}{T^4} = T \frac{\partial}{\partial T} \frac{p(T, \mu)}{T^4} + \frac{\mu^2}{T^2} \chi_2 = \frac{I(T, 0)}{T^4} + \frac{\mu^2}{2T} \frac{\partial \chi_2}{\partial T} \quad \mu_L/3 \equiv \mu_u = \mu_d,$$

$$\frac{p(T, \{\mu_i\})}{T^4} = \frac{p(T, \{0\})}{T^4} + \frac{1}{2} \sum_{i,j} \frac{\mu_i \mu_j}{T^2} \chi_2^{ij} \quad \chi_2^{ij} \equiv \frac{T}{V} \frac{1}{T^2} \left. \frac{\partial^2 \log}{\partial \mu_i \partial \mu_j} \right|_{\mu_i = \mu_j = 0}$$



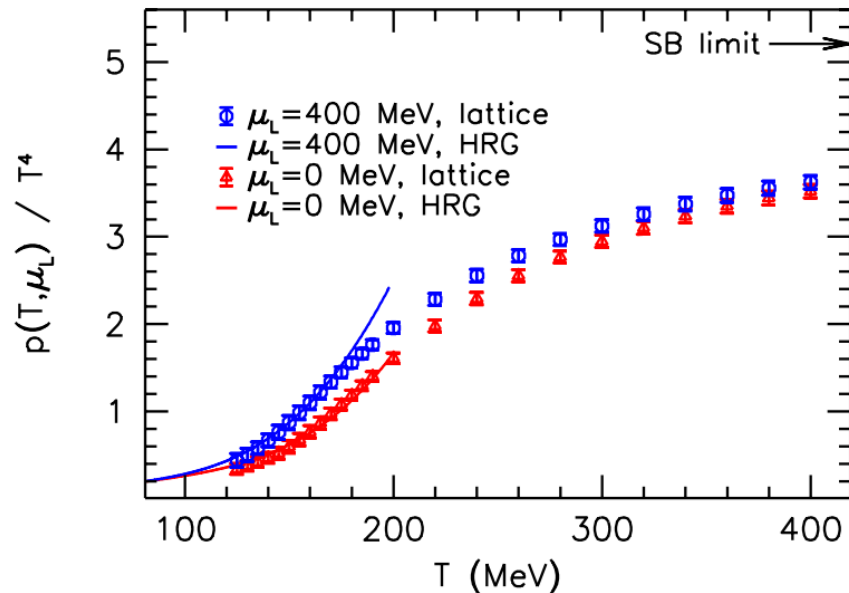
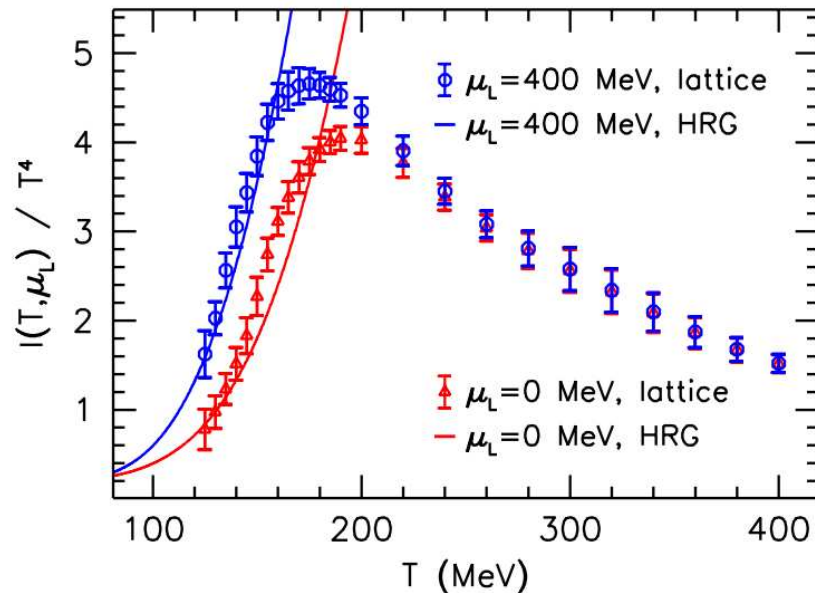
- ❖ Simulate the Taylor expansion coefficients at $\mu = 0$

S. Borsanyi *et al.* (Wuppertal-Budapest collaboration): JHEP (2012)

Finite μ EoS at order μ^2

$$\frac{I(T, \mu)}{T^4} = T \frac{\partial}{\partial T} \frac{p(T, \mu)}{T^4} + \frac{\mu^2}{T^2} \chi_2 = \frac{I(T, 0)}{T^4} + \frac{\mu^2}{2T} \frac{\partial \chi_2}{\partial T} \quad \mu_L/3 \equiv \mu_u = \mu_d,$$

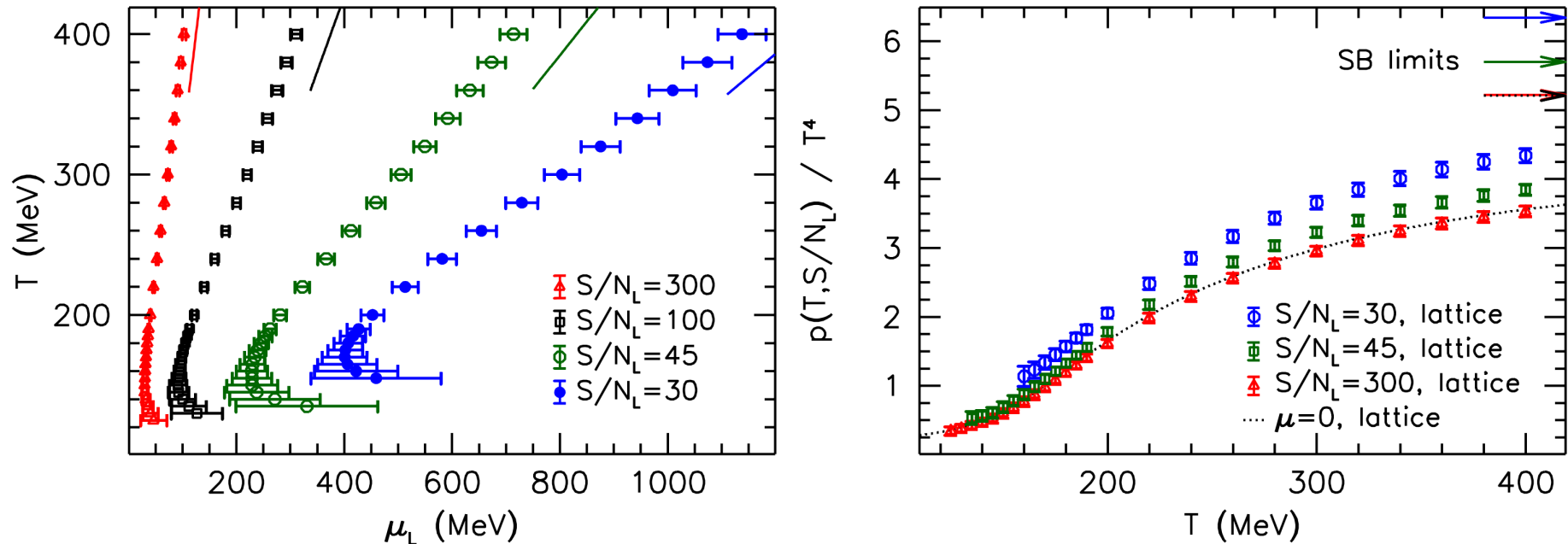
$$\frac{p(T, \{\mu_i\})}{T^4} = \frac{p(T, \{0\})}{T^4} + \frac{1}{2} \sum_{i,j} \frac{\mu_i \mu_j}{T^2} \chi_2^{ij} \quad \chi_2^{ij} \equiv \frac{T}{V} \frac{1}{T^2} \left. \frac{\partial^2 \log}{\partial \mu_i \partial \mu_j} \right|_{\mu_i = \mu_j = 0}$$



❖ Obtain the observables at **finite μ**

S. Borsanyi *et al.* (Wuppertal-Budapest collaboration): JHEP (2012)

Isentropic equation of state



- ◆ Isentropic trajectories in the T, μ plane
- ◆ Obtain the equation of state along these trajectories

S. Borsanyi *et al.* (Wuppertal-Budapest collaboration): JHEP (2012)

$$N_f = 2 + 1 + 1$$

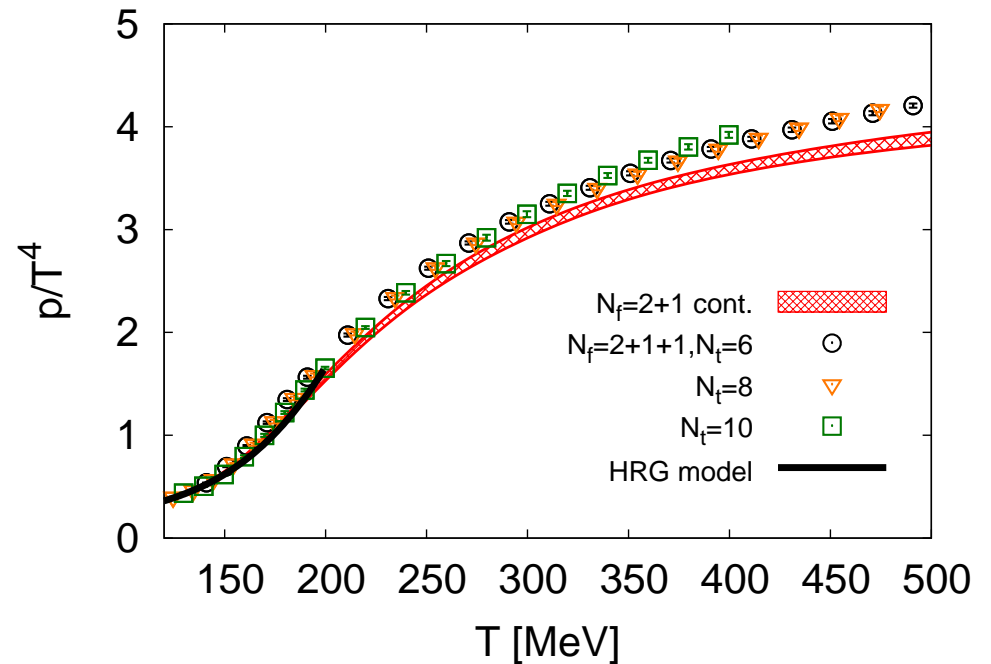
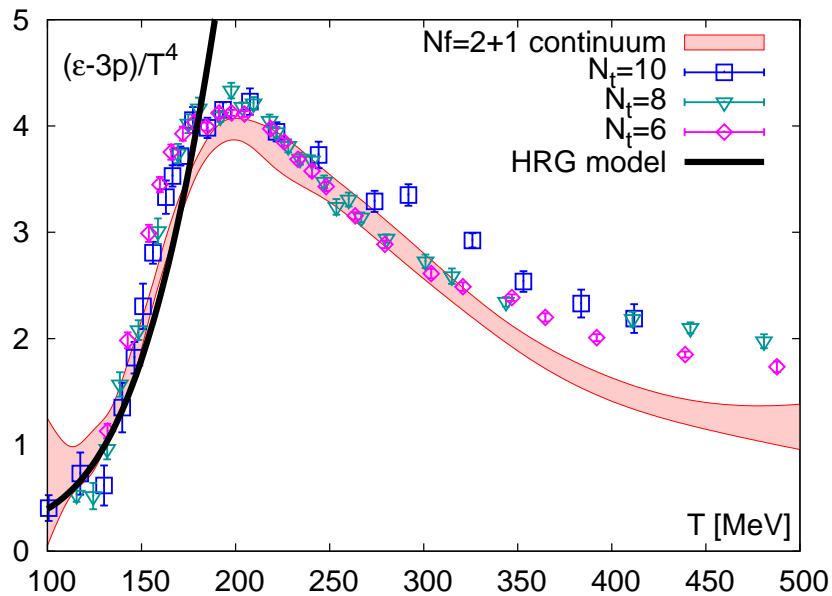
dynamical quark flavors

$$m_s/m_{u,d} \simeq 28$$

$$m_c/m_s \simeq 11.8$$

Trace anomaly and pressure

$$\frac{I(T)}{T^4} = \frac{\epsilon - 3p}{T^4} = T \frac{\partial}{\partial T} (p/T^4)$$

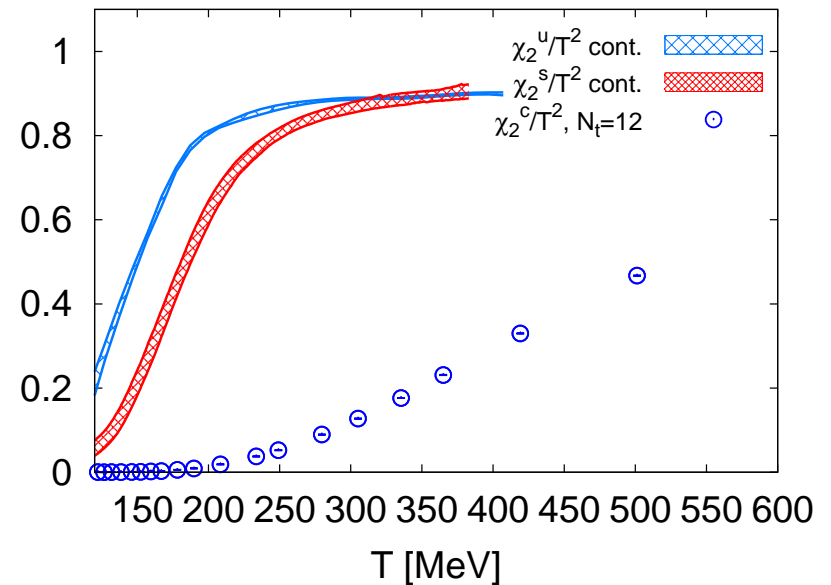
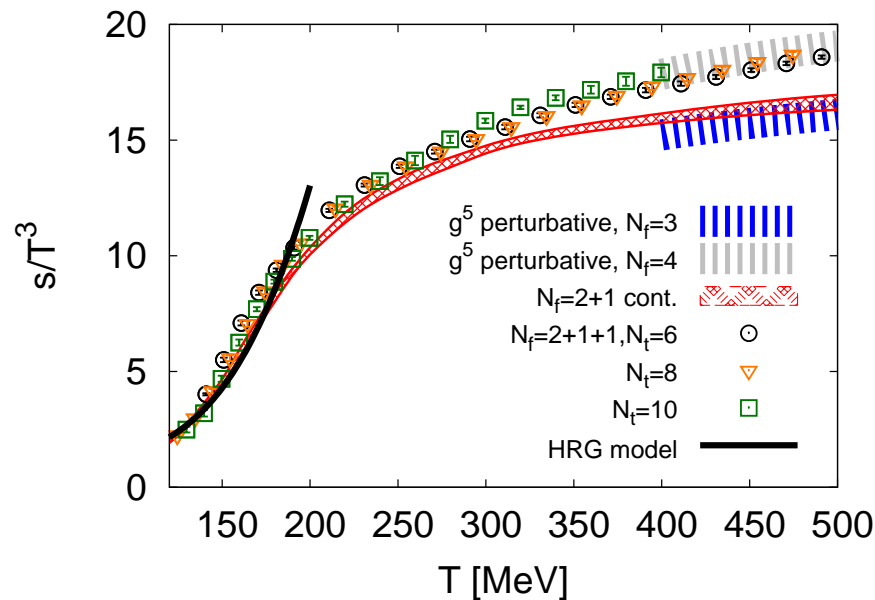


◆ Effect of charm quark relevant for $T > 250 - 300$ MeV

S. Borsanyi *et al.* (Wuppertal-Budapest collaboration): in preparation

Entropy and charm susceptibility

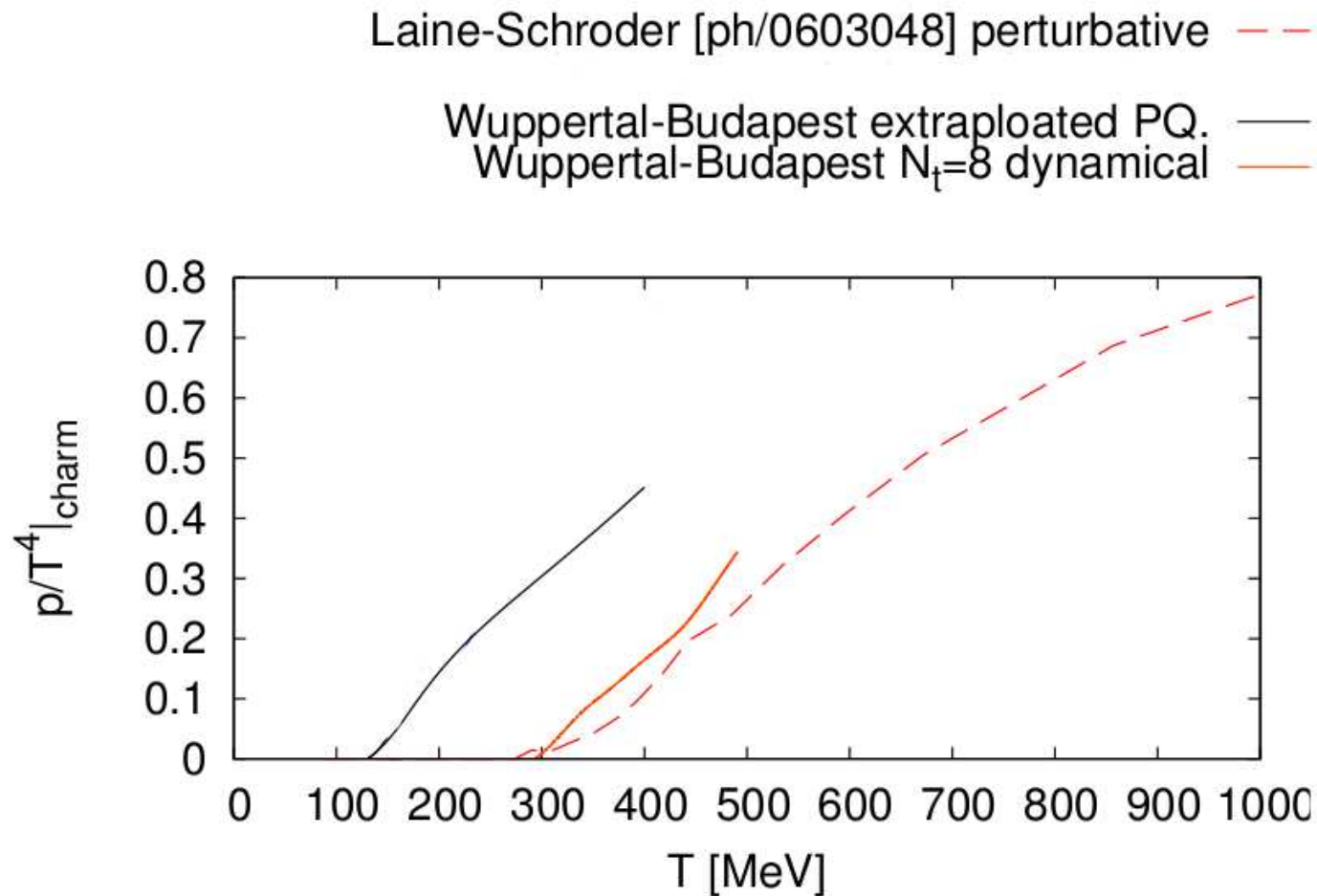
$$s = \frac{\epsilon + p}{T} \quad \chi_2^q = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial \mu_q \partial \mu_q} \Big|_{\mu_i=0}$$



◆ Effect of charm quark relevant for $T > 250 - 300$ MeV

S. Borsanyi *et al.* (Wuppertal-Budapest collaboration): in preparation

Comparison to partial quenching



- ❖ contribution of charm quark **moves to higher temperatures** when treated fully dynamically
- ❖ agreement with **perturbative QCD** is recovered

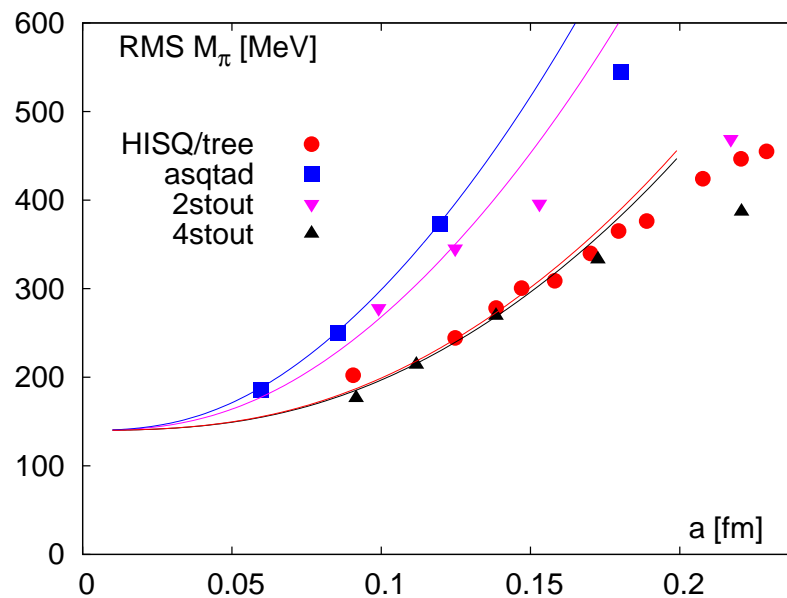
Results with
new 4stout action

$$N_f = 2 + 1 + 1$$

$$N_t = 8, 10$$

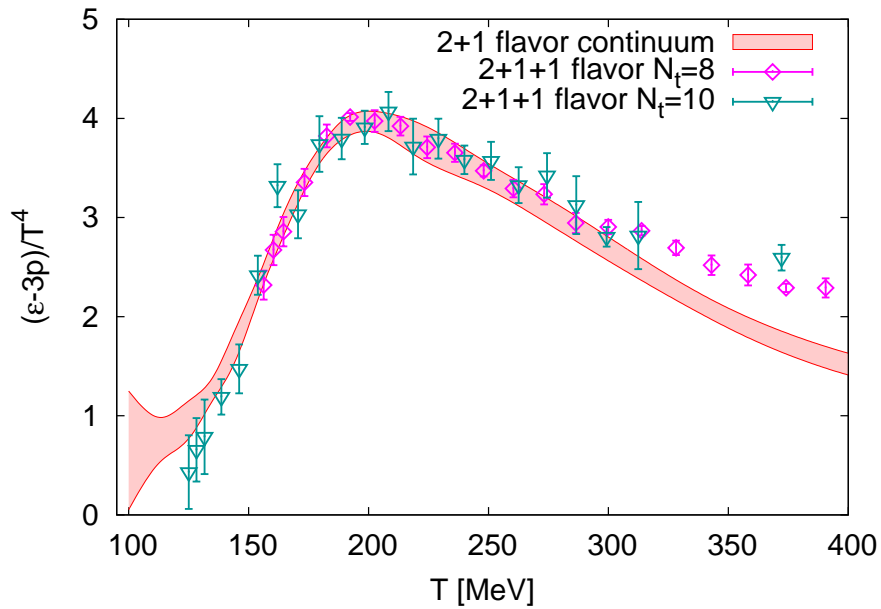
4stout action

- ❖ 4-level (stout) smeared improved staggered fermions
- ❖ reduced taste symmetry violation comparable to **hisq action**



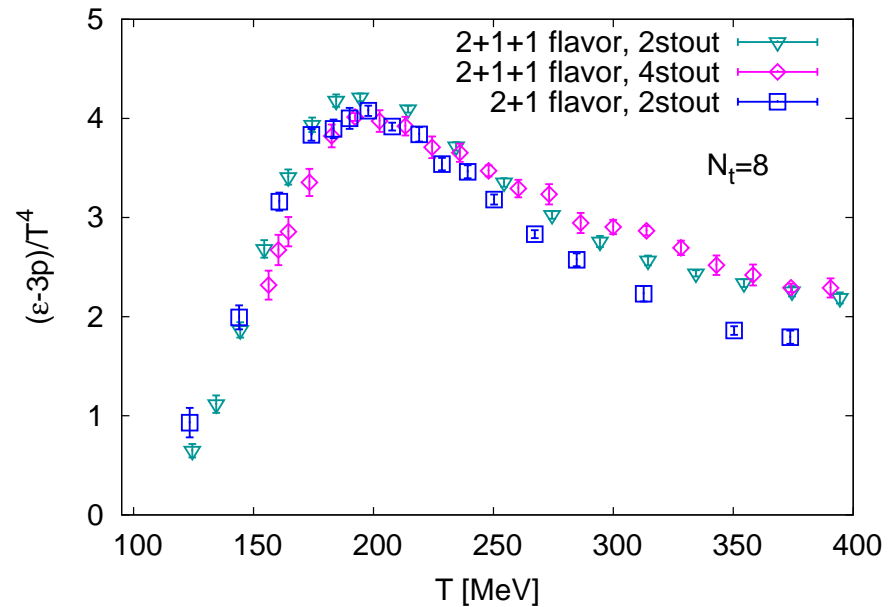
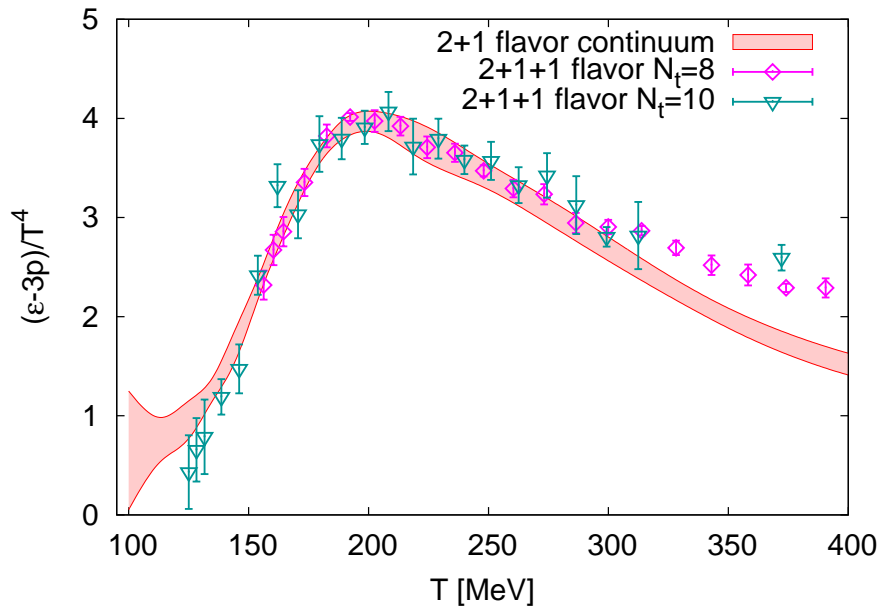
- ❖ taste breaking measured for $N_f = 2$ with $m_\pi = 350$ MeV
- ❖ taste breaking information is then **converted to physical point**
- ❖ taste breaking measurement at physical point is **in progress**: we expect above plot to be a **good approximation of the physical case**

Trace anomaly with 4stout action



- ❖ charm quark gives non-negligible contribution for $T > 250 - 300$ MeV

Trace anomaly with 4stout action



- ❖ **no difference** between 2stout and 4stout results
- ❖ **origin of discrepancy** in the trace anomaly between WB and hotQCD does not lie in different taste symmetry violation

Conclusions

- ❖ progress in $N_f = 2 + 1$ EoS
- ❖ EoS for $N_f = 2 + 1$ at order μ^2
- ❖ $N_f = 2 + 1 + 1$ fully dynamical EoS
- ❖ introduction of new **4stout action**: smaller taste symmetry violation
- ❖ results with **4stout action** fully agree with **2stout action** results

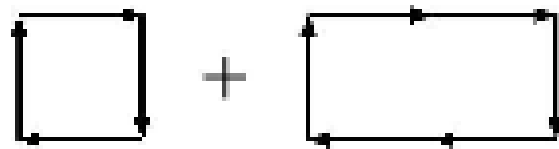
Backup slides

Choice of the action

- ❖ **no consensus**: which action offers the most cost effective approach

Aoki, Fodor, Katz, Szabo, JHEP 0601, 089 (2006)

- ❖ **our choice** tree-level $O(a^2)$ -improved Symanzik gauge action



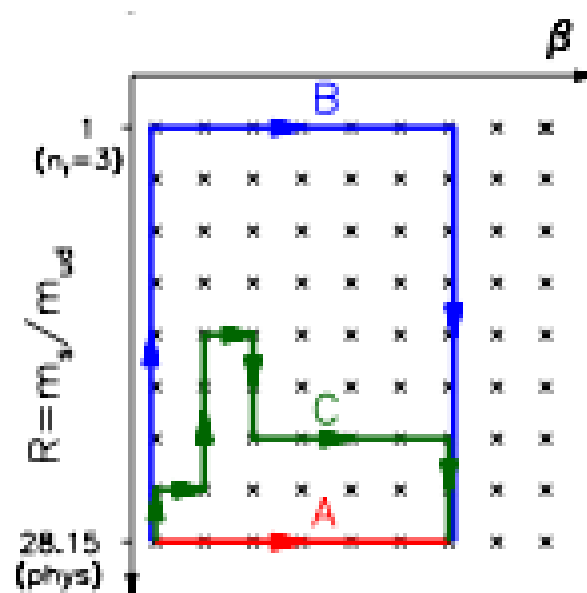
2-level (stout) smeared improved staggered fermions

$$V = P \left[\longrightarrow + \rho \left(\begin{array}{c} \nearrow \\ \searrow \end{array} + \begin{array}{c} \nwarrow \\ \swarrow \end{array} + \begin{array}{c} \uparrow \\ \downarrow \end{array} + \begin{array}{c} \leftarrow \\ \rightarrow \end{array} \right) \right]$$

All path approach

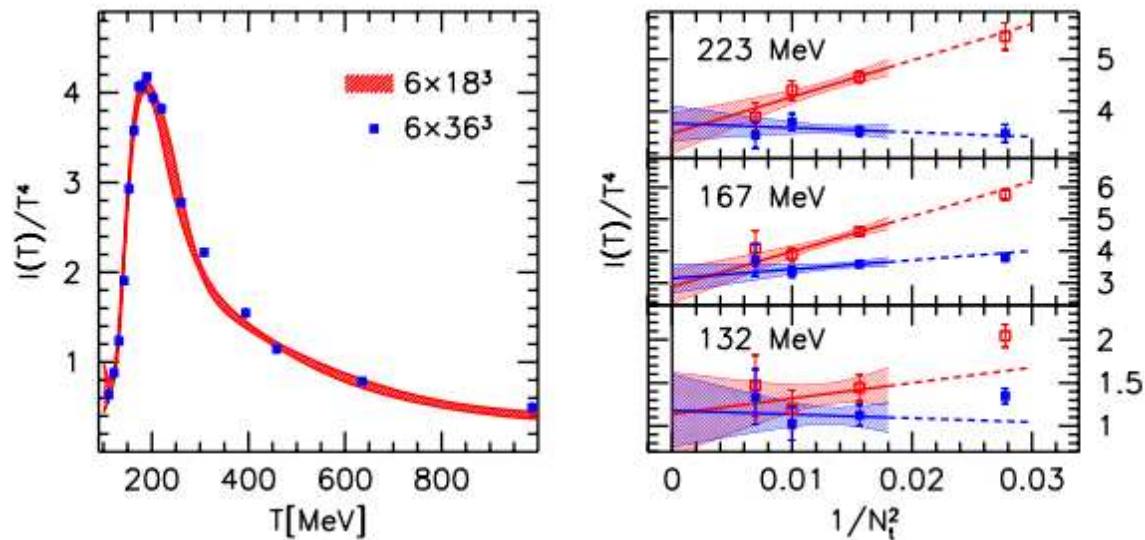
❖ Our goal:

- ➡ determine the equation of state for several pion masses
- ➡ reduce the uncertainty related to the choice of β^0



- ❖ conventional path: A, though B, C or any other paths are possible
- ❖ generalize: take all paths into account

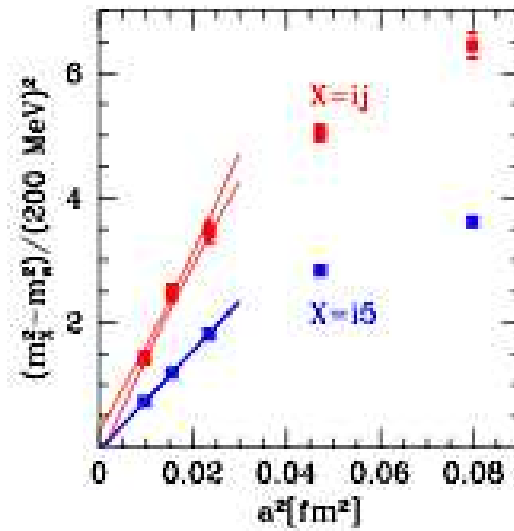
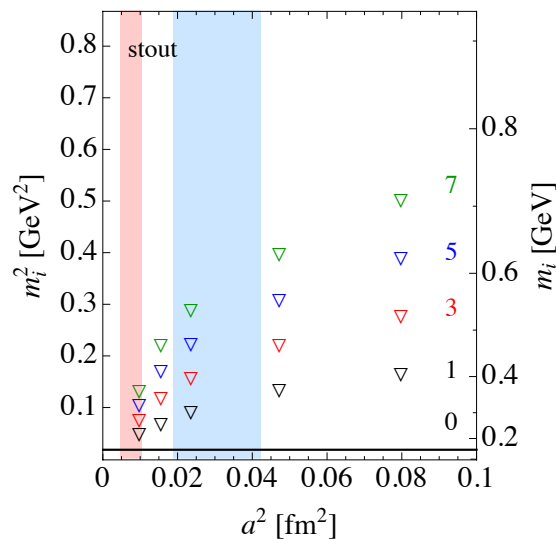
Finite volume and discretization effects



- ❖ finite V : $N_s/N_t = 3$ and 6 (8 times larger volume): **no sizable difference**
- ❖ finite a : improvement program of lattice QCD (action observables)
 - ➡ tree-level improvement for p (thermodynamic relations fix the others)
 - ➡ trace anomaly for three T -s: high T , transition T , low T
 - ➡ continuum limit $N_t = 6, 8, 10, 12$: same with or without improvement
- ❖ improvement strongly reduces cutoff effects: slope $\simeq 0$ ($1 - 2\sigma$ level)

Pseudo-scalar mesons in staggered formulation

- ❖ Staggered formulation: **four degenerate quark flavors** ('tastes') in the continuum limit
- ❖ **Rooting procedure**: replace fermion determinant in the partition function by its **fourth root**
- ❖ At **finite lattice spacing** the four tastes are not degenerate
 - ➡ **each pion** is split into **16**
 - ➡ the sixteen pseudo-scalar mesons have **unequal masses**
 - ➡ **only one** of them has vanishing mass in the chiral limit



- ❖ Scaling starts for $N_t \geq 8$.