

# SHEAR VISCOSITY OF THE QUARK-GLUON PLASMA

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# VISCOSITY

## QUESTION:

What is the shear viscosity of the quark gluon plasma?

## GOAL

- Determine the best way to extract  $\eta/s$  from data
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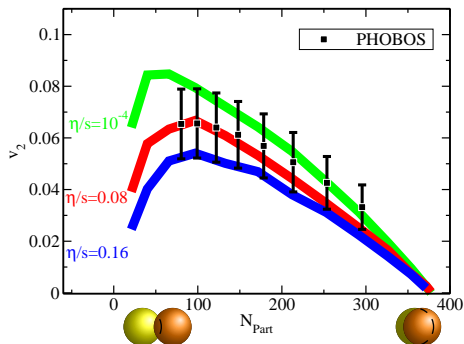
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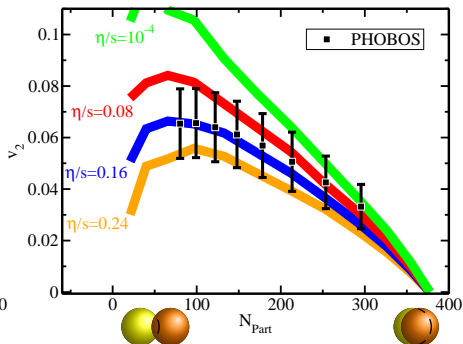
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# $\eta/s$ FROM FLOW (HISTORICAL)

“Glauber” initial conditions



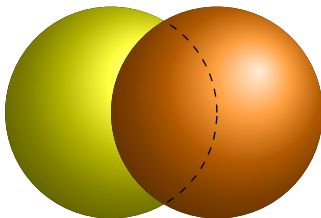
“CGC” initial conditions



(ML & Romatschke, *Phys.Rev. C78* (2008) 034915)

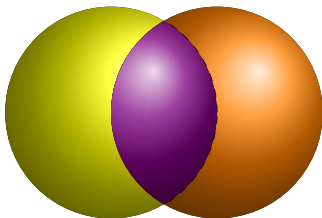
- Best extraction of  $\eta/s$  by comparing viscous hydro to flow data
- Largest uncertainty from unknown initial condition

# INITIAL ECCENTRICITY



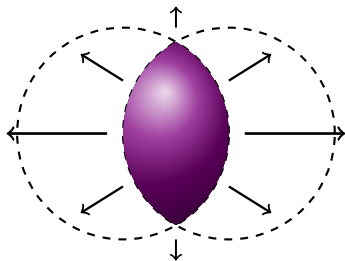
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- Different initial physics  $\implies$  different eccentricity  $\varepsilon_2$

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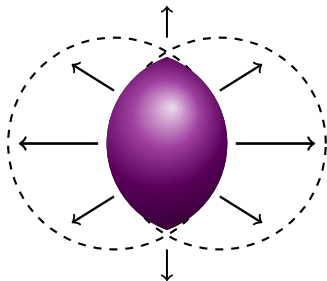
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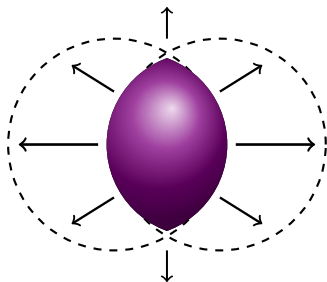


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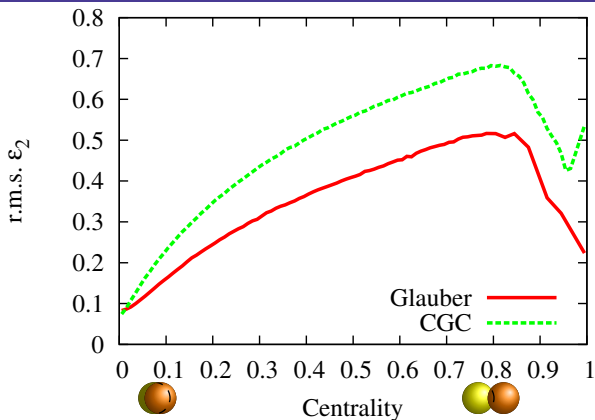
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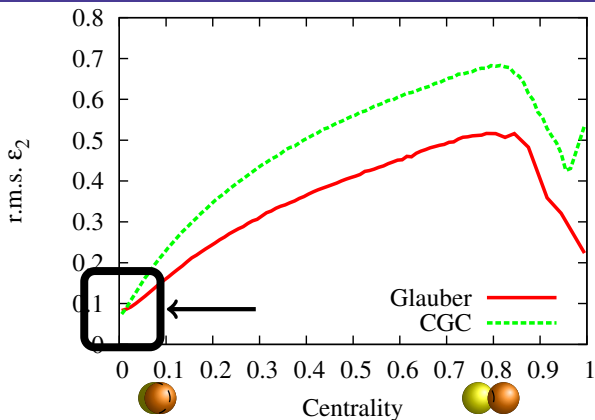
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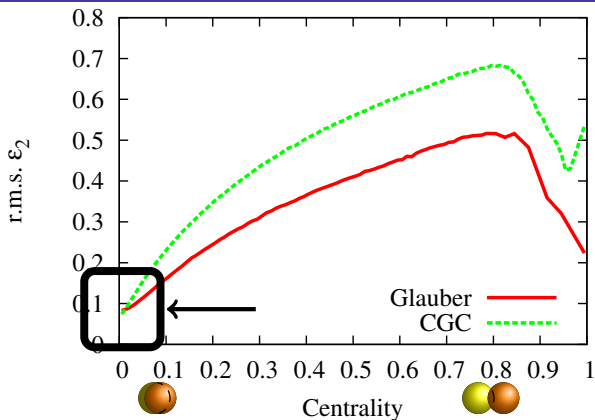
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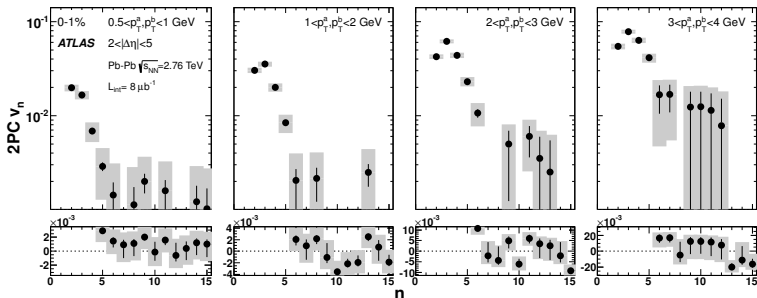
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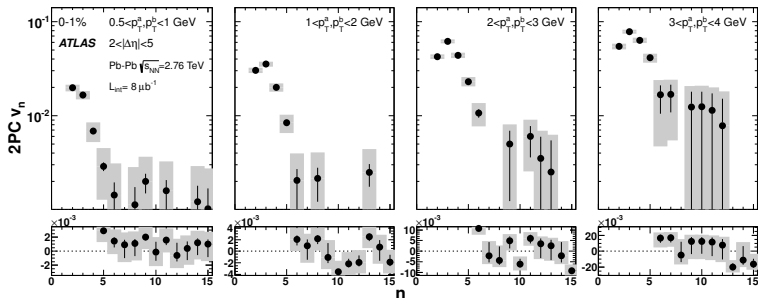
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- **Central collisions less sensitive to differences in initial physics**

# EXTRACTING $\eta/s$ FROM $v_n$ IN CENTRAL COLLISIONS



## NEW MEASUREMENTS OF CENTRAL COLLISIONS FROM ATLAS AT LHC

- Extract  $\eta/s$  from  $p_T$ -integrated  $v_n$  in ultra-central LHC collisions:
- Minimizes uncertainty from initial conditions
- LHC collisions more sensitive to viscosity in QGP phase
- $v_n \propto \varepsilon_n$  in central collisions (even for  $n > 3$ )  
(see F. Gardim, Friday 6D)

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# OUR HYDRO SETUP

- 2+1d, 2nd order conformally invariant viscous hydro
- Constant  $\eta/s$
- With or without separate chemical and kinetic freeze out
- Can directly test effects of:
  - As many models for initial conditions as we can get our hands on
  - Thermalization time, initialization of shear tensor, viscous correction to freeze out distribution function, second order transport coefficients, equation of state, chemical freeze-out, etc.
- Not directly tested in this work:
  - Longitudinal dynamics / fluctuations
  - Bulk viscosity
  - Hydro afterburners
  - Full event-by-event analysis

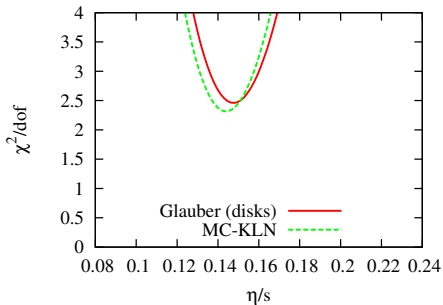
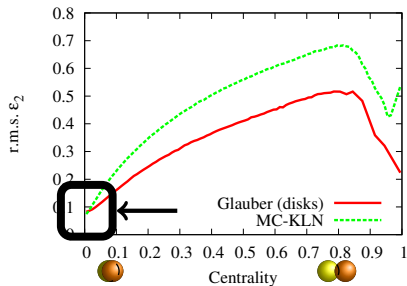


# $\eta/s$ FROM ULTRA-CENTRAL COLLISIONS

## PROCEDURE

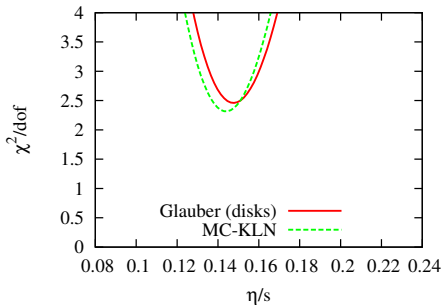
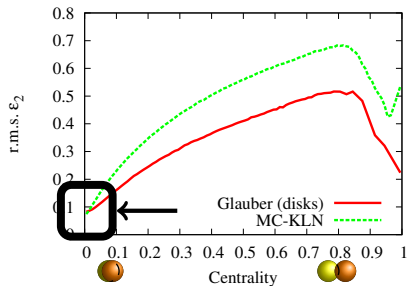
- Calculate integrated  $v_n/\varepsilon_n$  versus  $\eta/s$  in hydrodynamics
- Calculate r.m.s.  $\varepsilon_n$  from Monte-Carlo models of initial conditions  
 $\implies v_n(\eta/s)$
- Extract best-fit value for  $\eta/s$  from  $v_2-v_6$  in 0–1% central collisions
- Vary all parameters and determine effect on extracted  $\eta/s$   
 $\implies$  uncertainty in  $\eta/s$
- Estimate uncertainty from other sources
- $\implies$  measurement of  $\eta/s$  with error bar

# $\eta/s$ FROM ULTRA-CENTRAL COLLISIONS



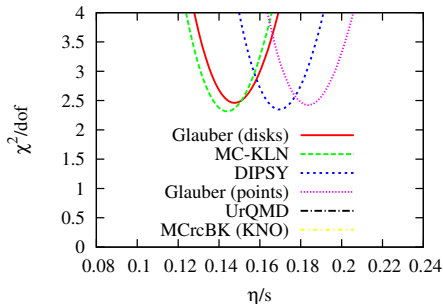
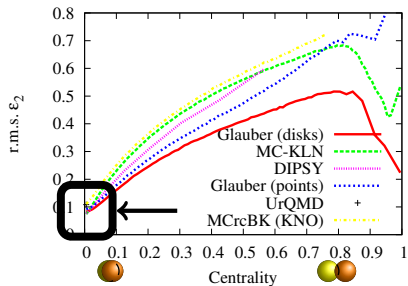
- A simultaneous fit of  $v_2-v_6$  gives a preferred extracted  $\eta/s$  for each initial condition
- Range of results quantifies uncertainty

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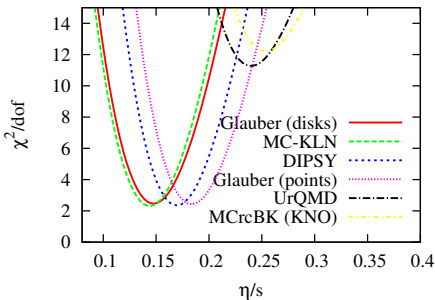
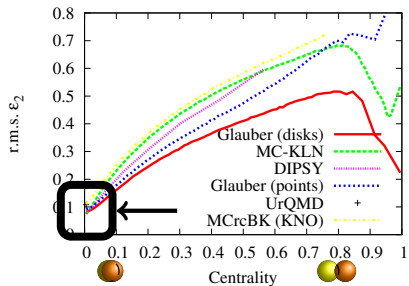
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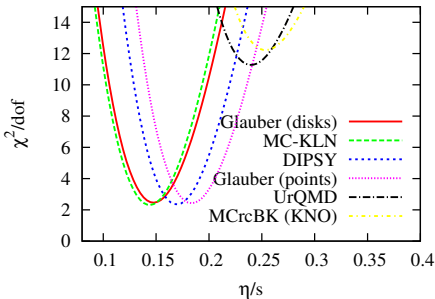
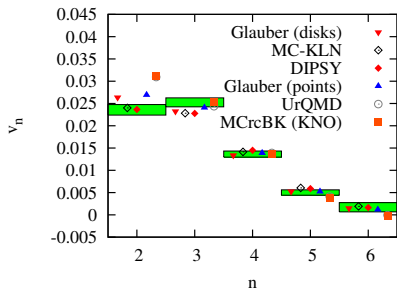
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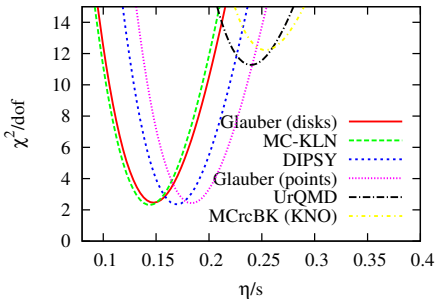
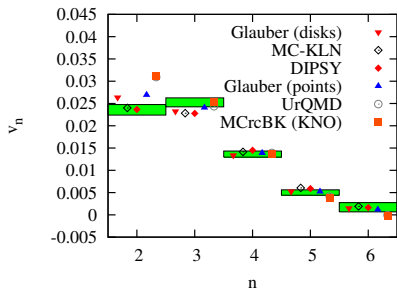
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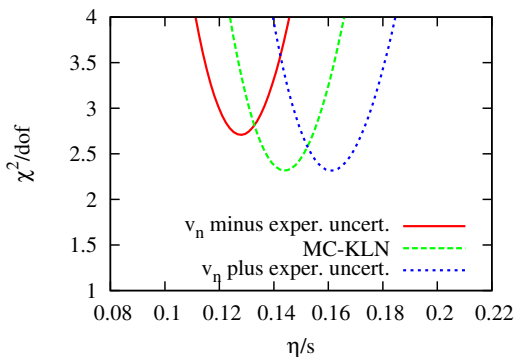
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- Range of results quantifies uncertainty
- Uncertainty due to initial  $\varepsilon_n$ :  $\sim \pm 0.05$

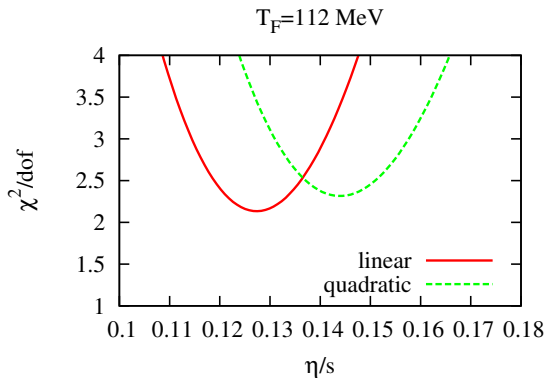
## EXPERIMENTAL UNCERTAINTY



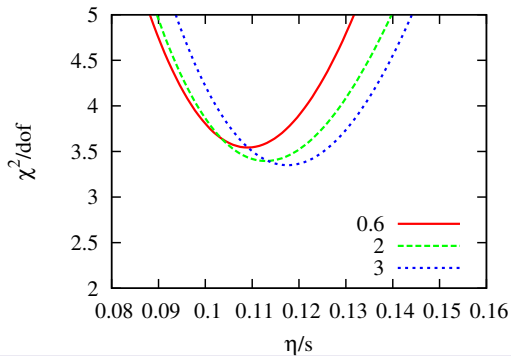
- Systematic (plus statistical) experimental error:  $\delta v_2/v_2 \simeq 5\%$ ,  $\delta v_3/v_3 \simeq 4\%$ ,  $\delta v_4/v_4 \simeq 5\%$ ,  $\delta v_5/v_5 \simeq 12\%$ ,  $\delta v_6/v_6 \simeq 61\%$
- Uncertainty due to experimental error:  $\sim \pm 0.02$



# VISCOUS CORRECTION TO DISTRIBUTION FUNCTION $\delta f$



- From fluid d.o.f. to particles:  $f(p, x) = f_{\text{equil}} + \delta f$
- Uncertainty due to momentum dependence of  $\delta f$ :  $\pm 0.015$

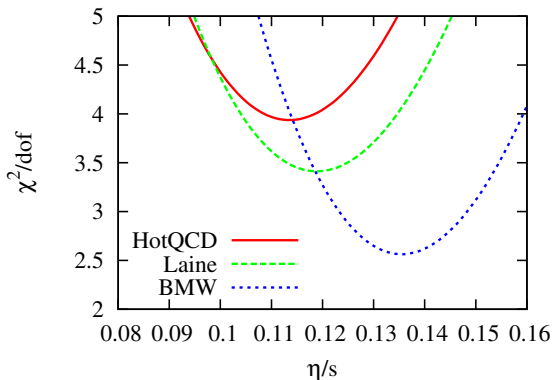
SECOND ORDER TRANSPIRE COEFFICIENTS:  $\tau_{\Pi}$ 

•

$$\tau_{\Pi} = 2 \frac{\eta}{sT} \times C$$

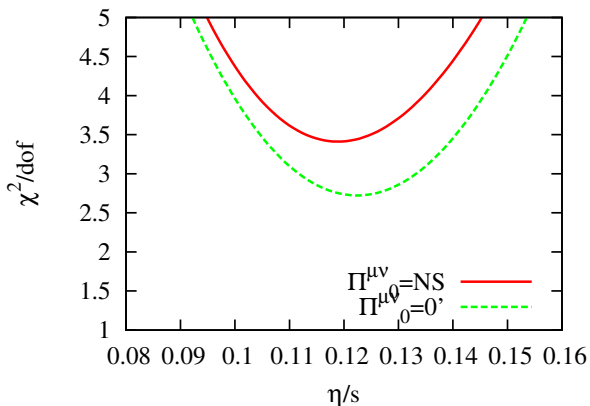
- Israel-Stewart:  $C = 3$
- SYM:  $C = 2 - \log(2) \simeq 1.3$
- Uncertainty due to 2nd order transport coeff.:  $\pm 0.005$

## EQUATION OF STATE

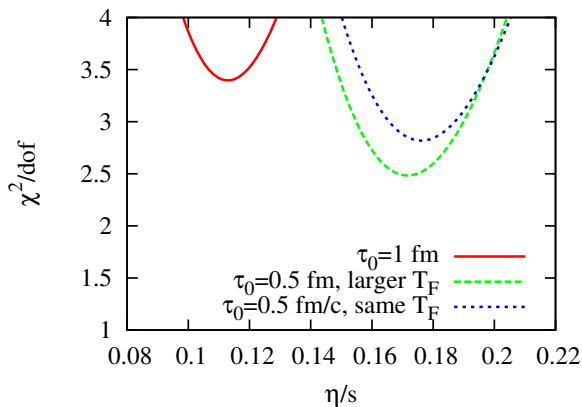


- Uncertainty due to equation of state:  $\pm 0.01$

# $\Pi^{\mu\nu}$ INITIALIZATION

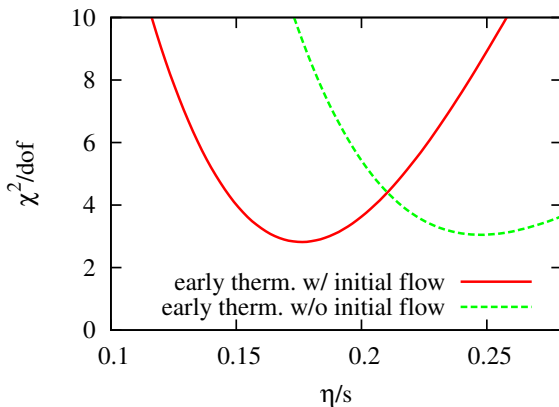


- Uncertainty due to initialization of shear tensor:  $< \pm 0.005$

THERMALIZATION TIME  $\tau_0$ 

- Uncertainty from  $\tau_0 \pm 0.03$

## INITIAL FLOW



- Uncertainty from initial flow  $\pm 0.04$

SYSTEMATIC UNCERTAINTY FOR  $\eta/s$ 

## (Preliminary!)

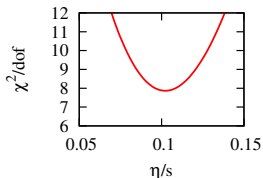
• Experimental uncertainties	$\pm 0.020$
• Initial eccentricity	$\pm 0.050$
• Thermalization time	$\pm 0.030$
• Initialization of shear tensor	$\pm 0.005$
• Initial flow	$\pm 0.040$
• Equation of State	$\pm 0.015$
• Second-order transport coeff.	$\pm 0.005$
• Viscous correction to f.o. distribution	$\pm 0.015$
• Chemical freeze out	$\pm 0.015$

## (Preliminary!)

# BOUNDS: HYDRO RUN WITH LARGEST (SMALLEST) $\eta/s$

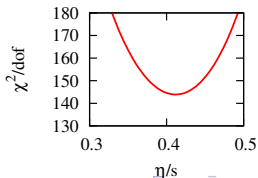
## Lower Bound:

- Data + uncert.
- MC-KLN I.C.s
- $\tau_0 = 1$  fm
- $u_0^i = 0$
- $\Pi_0^{\mu\nu} = 0$
- BMW EOS
- $\tau_\pi = \frac{6\eta}{sT}$
- $\delta f \propto p$



## Upper Bound:

- Data – uncert.
- MCrcBK (w NB)
- $\tau_0 = 0.5$  fm
- $u_0^i = \frac{-\tau}{2} \partial^i \ln s$
- $\Pi_0^{\mu\nu} = \text{Nav. St.}$
- s95p-PCE165
- $\tau_\pi = \frac{2.6\eta}{sT}$
- $\delta f \propto p^2$





# OTHER UNCERTAINTY

Next step: estimate uncertainty from other sources and add to error band

- Bulk Viscosity  $\sim \pm 0.010$
- $v_n/\varepsilon_n = \text{constant}$   $\sim \pm 0.010$
- Deviation from boost-invariance / longitudinal fluct.  $\sim \pm 0.005$
- Freezing out with (PCE +) Cooper-Frye  $\sim \pm 0.010$

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FINAL RESULT:

$$0.07 \leq \eta/s \leq 0.43$$

# SYSTEMATIC UNCERTAINTY FOR $\eta/s$

(Preliminary!)

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- Bulk Viscosity  $\sim \pm 0.010$
- Deviation from boost-invariance / longitudinal fluct.  $\sim \pm 0.005$
- Viscous correction to f.o. distribution  $\pm 0.015$
- Other aspects of freeze out  $\sim \pm 0.025$

(Preliminary!)

# SUMMARY

- **Flow in central heavy-ion collisions are less sensitive to early-time dynamics**
- $\implies$  Focusing on ultra-central collisions reduces systematic uncertainty in viscosity extraction
- First extraction of  $\eta/s$  with comprehensive study of systematics, reliable error bar:
- $0.07 \leq \eta/s \leq 0.43$  (preliminary!!)
- Largest *single* source of uncertainty still initial conditions
- Many less significant sources of error are more important in aggregate; almost all have clear potential for improvement

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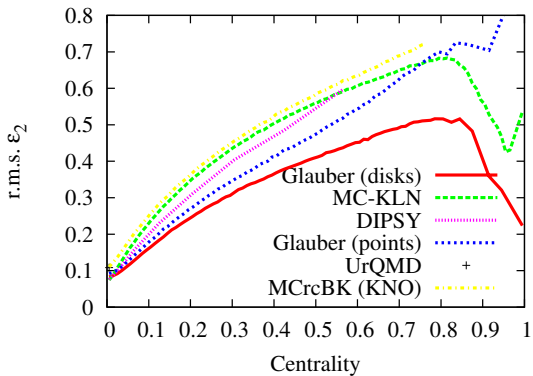
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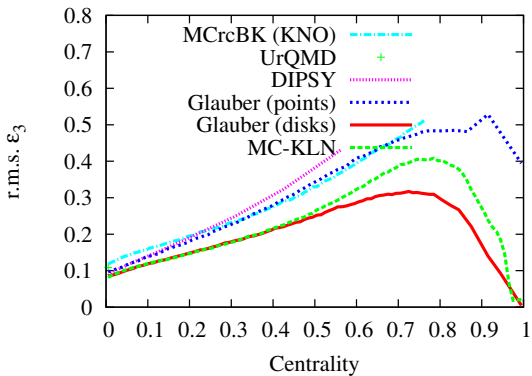
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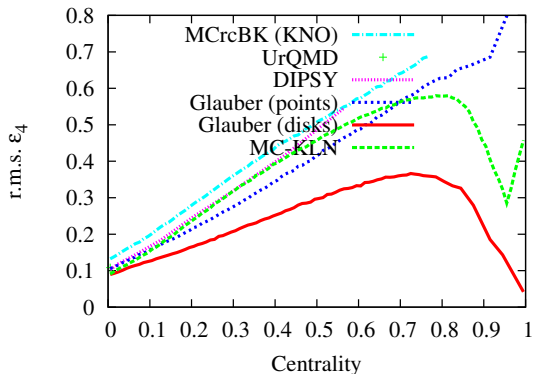
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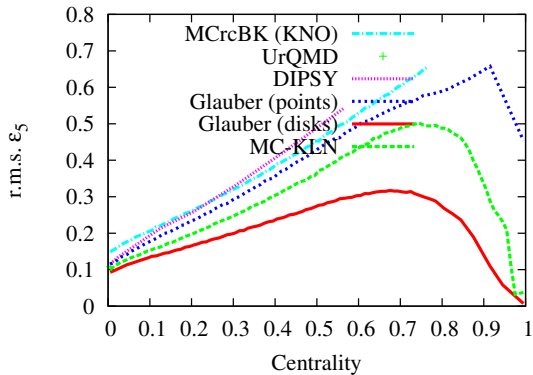
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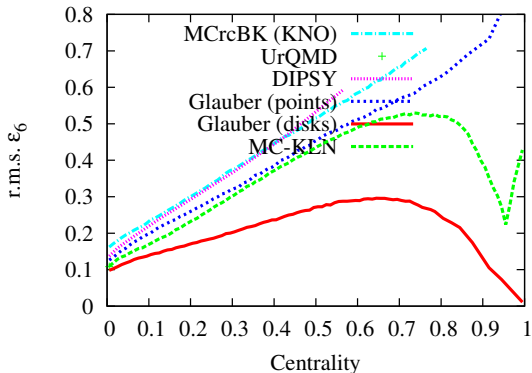
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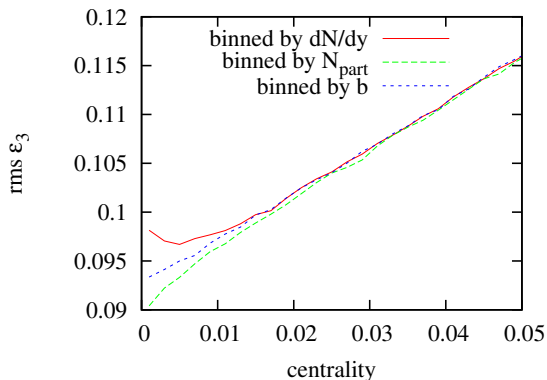
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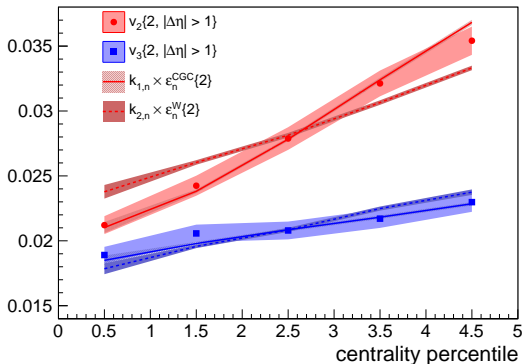


# SELECTING CENTRALITY (EXAMPLE FROM PHOBOS GLAUBER)



- Correct binning in centrality is important for very central collisions

# CENTRALITY DEPENDENCE OF $\varepsilon_n$ (ALICE ARXIV:1105.3865)



- Centrality dependence of  $v_2 \implies$  centrality dependence of  $\varepsilon_2 \implies$  intrinsic eccentricity

## EXTRA SLIDES

