



Heavy Quark Evolution and Flow in Hot and Dense Medium

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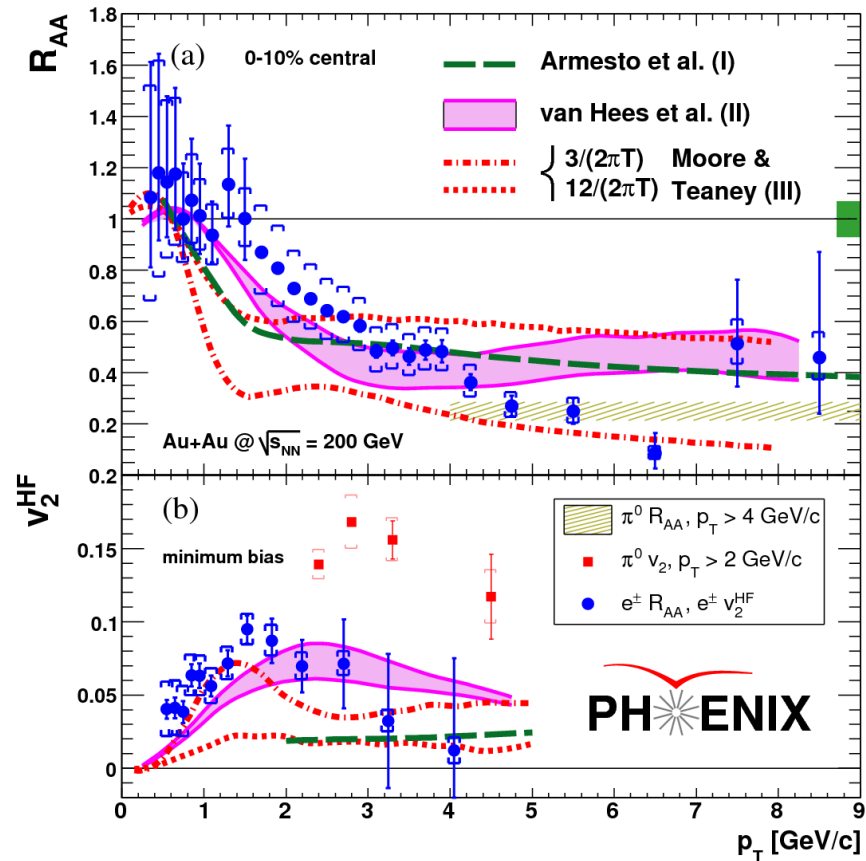
Outline

- **Introduction and motivation**
- **Methodology**
Improved Langevin approach incorporating gluon radiation mechanism
- **Results of heavy flavor suppression and flow and comparison with experimental data**
- **Summary and outlook**



Why to Study Heavy Quark

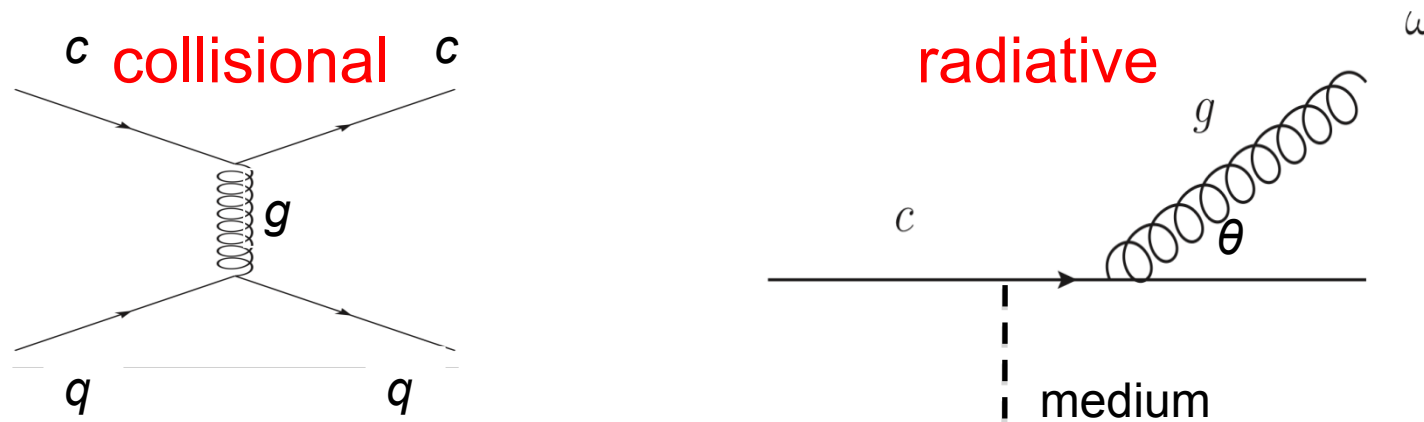
- Mainly produced at early stage: act as a hard probe
- Heavy: supposed to be influenced less by the medium
- Partially thermalized with medium – SC, Bass, *PRC 84, 064902*



- Surprisingly small R_{AA} and large v_2 of non-photonic electrons
- Strong coupling between heavy quark and the medium
- **How to describe heavy quark energy loss process inside QGP?**

Energy Loss Mechanisms

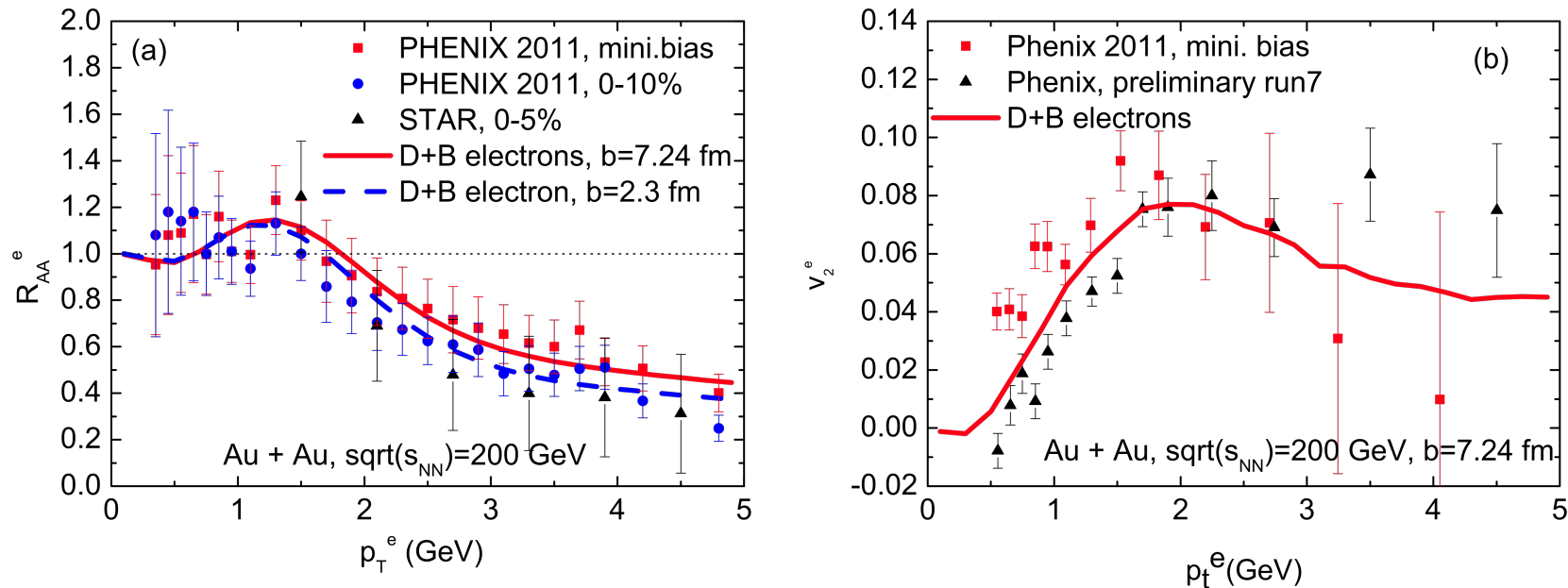
- Two ways for heavy quarks to lose energy:



- Unless in the ultra-relativistic limit ($\gamma v \gg 1/g$), gluon radiation is suppressed by the “dead cone effect” \rightarrow consider collisional energy loss as the dominant factor
- Heavy quark inside QGP medium: Brownian motion
- Description: Langevin equation
$$\frac{d\vec{p}}{dt} = -\eta_D(p)\vec{p} + \vec{\xi}$$

From RHIC to LHC

Successful description of RHIC data: **Langevin for HQ + coal. & frag. for hadronization + heavy meson diffusion in hadron gas**



He, Fries, Rapp, *PRC86, 014903, arXiv:1208.0256*, and private communication with He

What shall we modify to go from RHIC to LHC?

- Even heavy quark is ultrarelativistic
 → radiative energy loss may not be ignored
- At high energy, frag. might be sufficient for hadronization



Improved Langevin Approach Incorporating Gluon Radiation

Modified Langevin Equation: $\frac{d\vec{p}}{dt} = -\eta_D(p)\vec{p} + \vec{\xi} + \vec{f}_g$

Fluctuation-dissipation relation between drag and thermal random force: $\eta_D(p) = \frac{\kappa}{2TE} \quad \langle \xi^i(t) \xi^j(t') \rangle = \kappa \delta^{ij} \delta(t - t')$

Force from gluon radiation: $\vec{f}_g = -\frac{d\vec{p}_g}{dt}$

Gluon distribution taken from Higher Twist calculation:

$$\frac{dN_g}{dx dk_{\perp}^2 dt} = \frac{2\alpha_s(k_{\perp})}{\pi} P(x) \frac{\hat{q}}{k_{\perp}^4} \sin^2 \left(\frac{t - t_i}{2\tau_f} \right) \left(\frac{k_{\perp}^2}{k_{\perp}^2 + x^2 M^2} \right)^4$$

Guo and Wang, *PRL* 85, 3591; Majumder, *PRD* 85, 014023; Zhang, Wang and Wang, *PRL* 93, 072301.

Transport Coefficients: $D = \frac{T}{M\eta_D(0)} = \frac{2T^2}{\kappa} \quad \hat{q} = 2\kappa C_A / C_F$



Improved Langevin Approach Incorporating Gluon Radiation

Numerical Implementation (Ito Discretization)

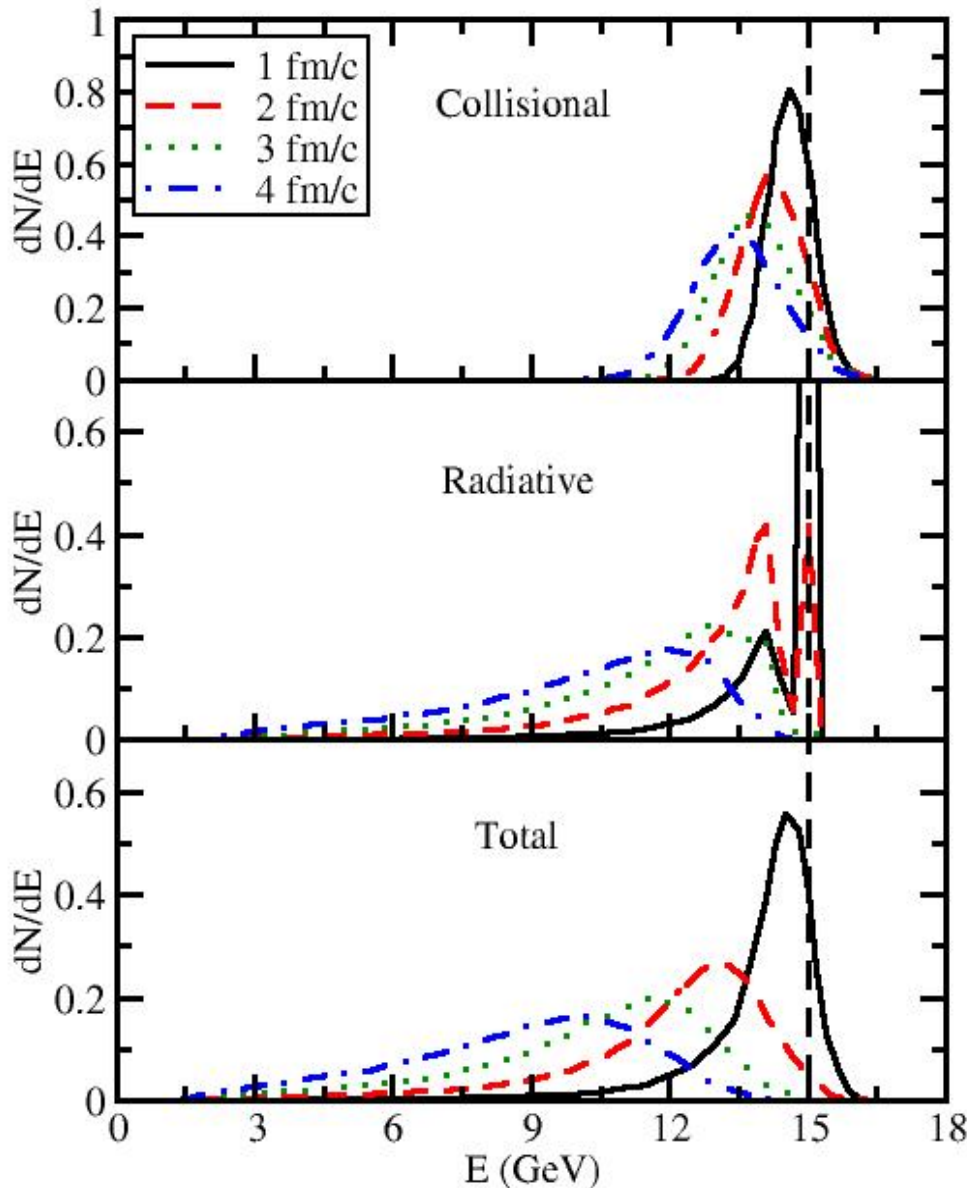
$$\vec{p}(t + \Delta t) = \vec{p}(t) - \vec{d}_{\text{Ito}}(\vec{p}(t))\Delta t + \vec{\xi}\Delta t - \Delta\vec{p}_{\text{gluon}}$$

Drag force: $\vec{d}_{\text{Ito}}(\vec{p}) = \eta_D(p)\vec{p}$

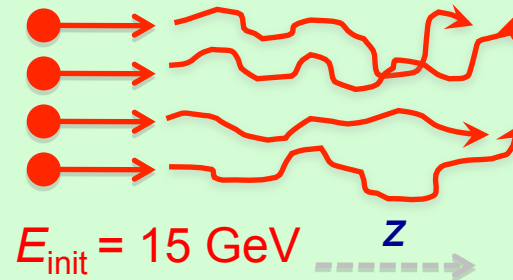
Thermal random force: $\langle \xi^i(t)\xi^j(t - n\Delta t) \rangle = \frac{\kappa}{\Delta t} \delta^{ij} \delta^{0n}$

Momentum of gluon radiated during Δt : $\Delta\vec{p}_{\text{gluon}}$

Charm Quark Evolution in Static Medium



$T = 300$ MeV, $D = 7/(2\pi T)$, i.e.,
 $\hat{q} \sim 1.1$ GeV²/fm



Evolution of E distribution

- Before 2 fm/c, collisional energy loss dominates; after 2 fm/c, radiative dominates;
- Collisional energy loss leads to Gaussian distribution, while radiative generates long tail.

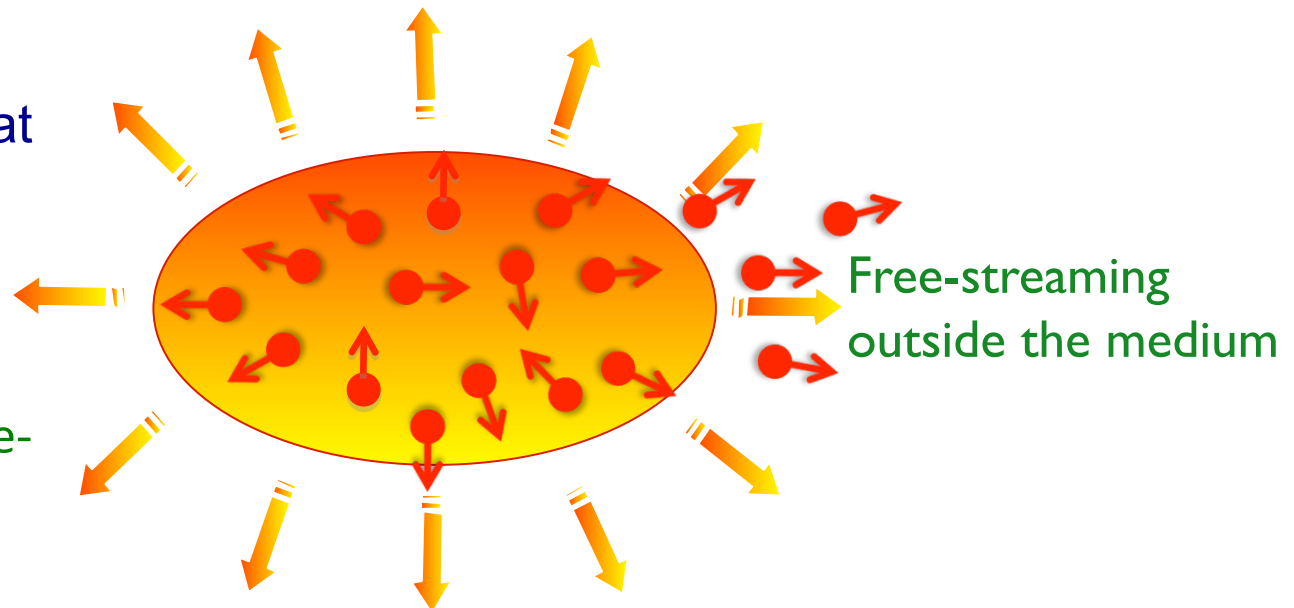


Heavy Quark Evolution in LHC QGP

- Generation of QGP medium: 2D viscous hydro from OSU group (thanks to Qiu, Shen, Song, and Heinz)
- Initialization of heavy quarks: MC-Glauber for position space and pQCD calculation for momentum space
- **Simulation of heavy quark evolution: the improved Langevin algorithm in the local rest frame of the medium**
- Fragmentation of HQ into heavy flavor mesons: PYTHIA 6.4

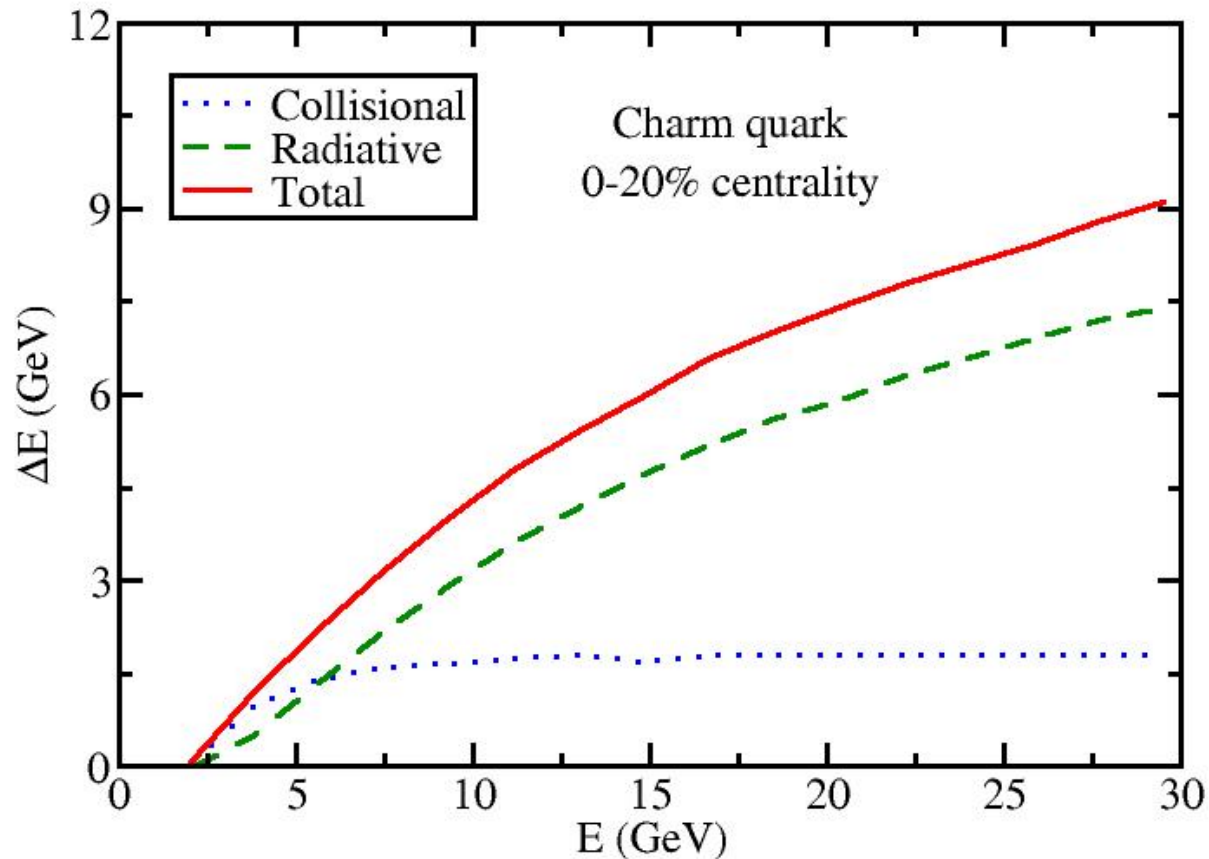
$D=7/(2\pi T)$, i.e., q hat
 $\sim 2.6 \text{ GeV}^2/\text{fm}$ at
initial temperature
(around 400 MeV)

After freeze-out: free-streaming





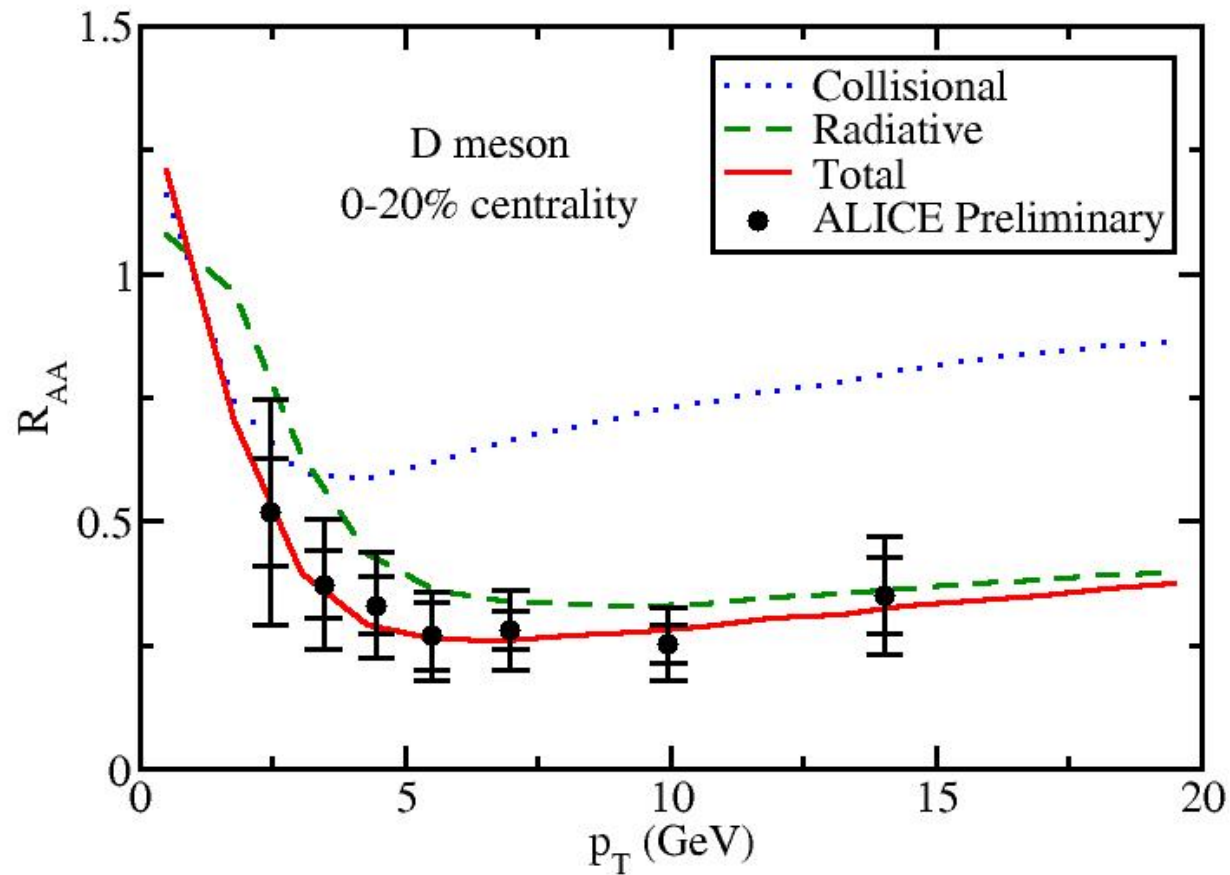
Heavy Quark Energy Loss



- Collisional energy loss dominates low energy region, while radiative dominates high energy region.
- Crossing point: around 6 GeV.



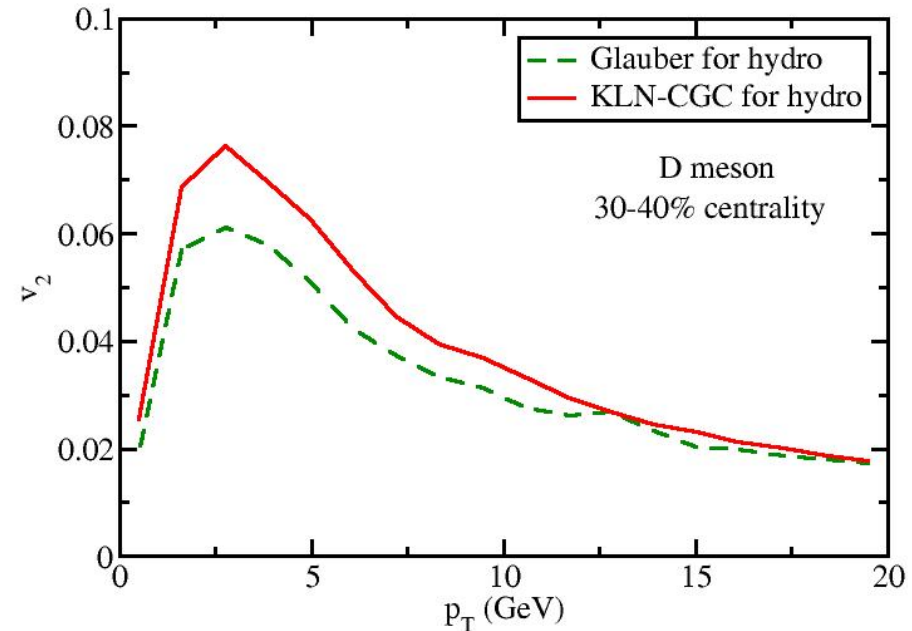
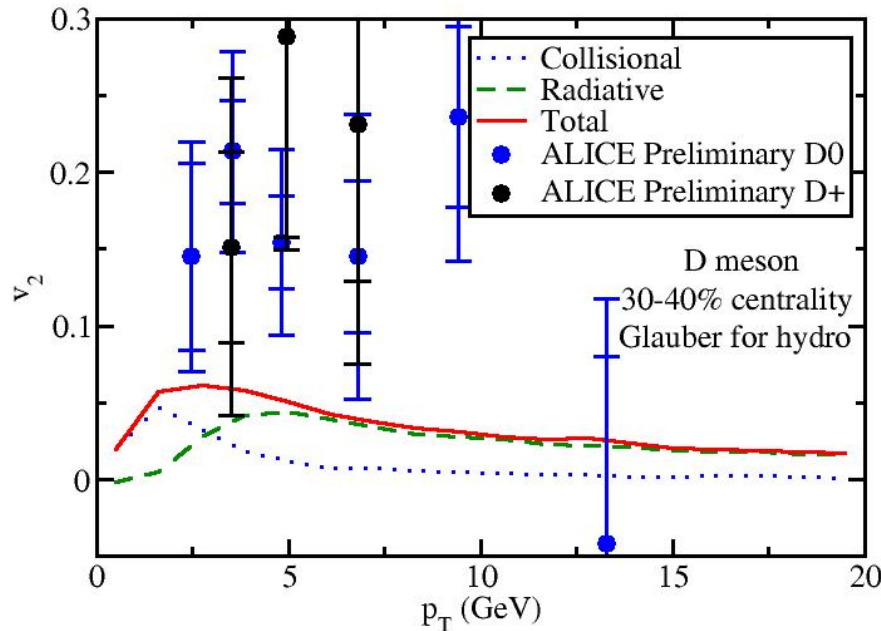
R_{AA} of D meson



- Collisional dominates low p_T , radiative dominates high p_T .
- The combination of the two mechanisms provides a good description of experimental data.



v_2 of D meson



Similar trend of competition between the two energy loss mechanisms as revealed by R_{AA}

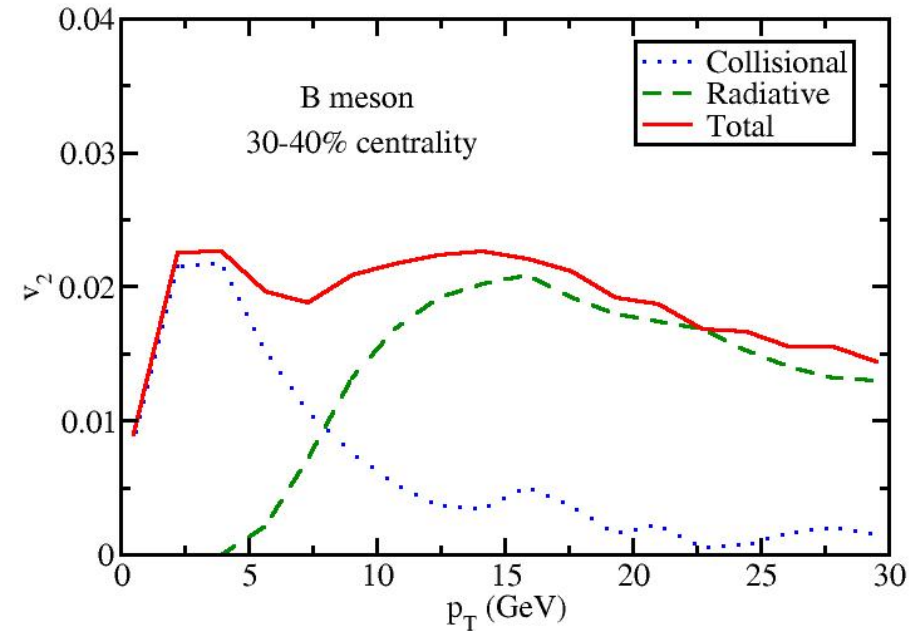
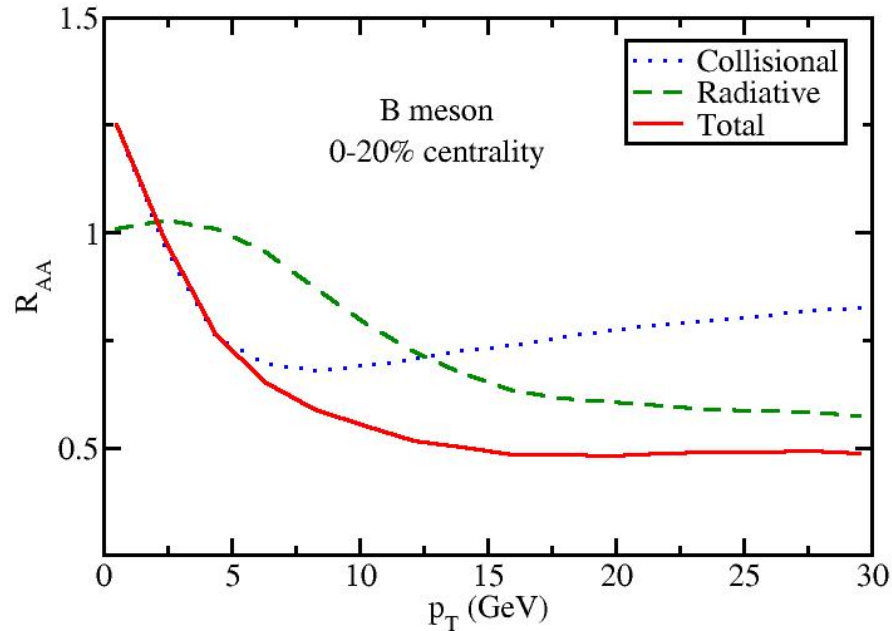
Different geometries and flow behaviors of the QGP medium may have impact heavy flavor v_2 while does not significantly influence the overall suppression (SC, Qin and Bass, *arXiv:1205.2396*)

Influence of coalescence mechanism and hadronic interaction

KLN provides larger eccentricity for the QGP profile than Glauber and therefore larger D meson v_2



Prediction for B Meson



- Similar behaviors as D meson – collisional energy loss dominates low p_T region, while radiative dominates high p_T .
- The crossing point is significantly higher because of the much larger mass of bottom quark than charm quark.
- B meson has larger R_{AA} and smaller v_2 than D meson.



Summary and Outlook

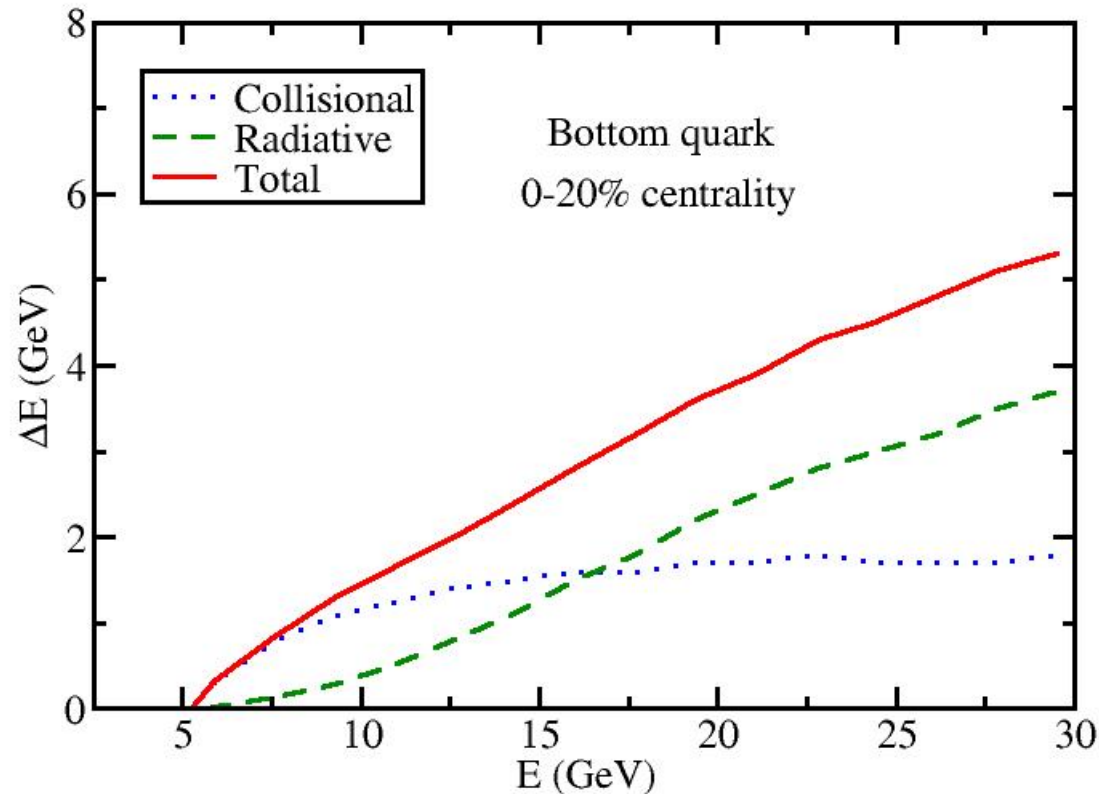
- Study the heavy quark energy loss in hot and dense medium in the framework of the Langevin approach
- Improve the Langevin algorithm to incorporate radiative energy loss by treating gluon radiation as an extra force term
- Reveal the significant effect of radiative energy loss at the LHC energy level and provide description of D meson suppression consistent with LHC data
- ***Two issues for further improvement:***
 - Anomalous transport of heavy quark in the pre-equilibrium stage after heavy-ion collisions
 - Interaction between heavy mesons and hadron gas



Thank you!



Backup: Bottom Quark Energy Loss



- Collisional energy loss dominates low energy region, while radiative dominates high energy region.
- Crossing point: around 17 GeV, much larger than charm quark because of heavier mass.