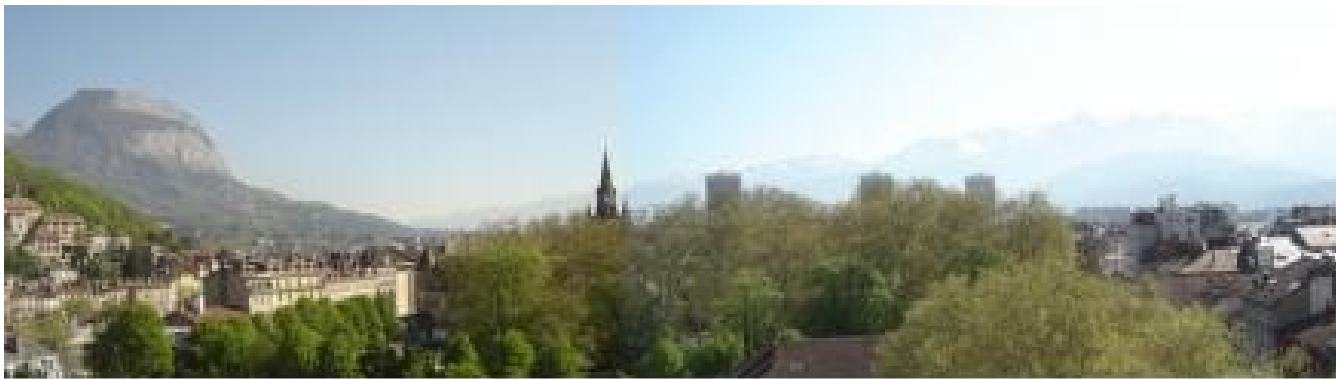


Measurement of the W boson mass at DØ New Tevatron and world averages

Jan Stark

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Grenoble, France

for the DØ Collaboration



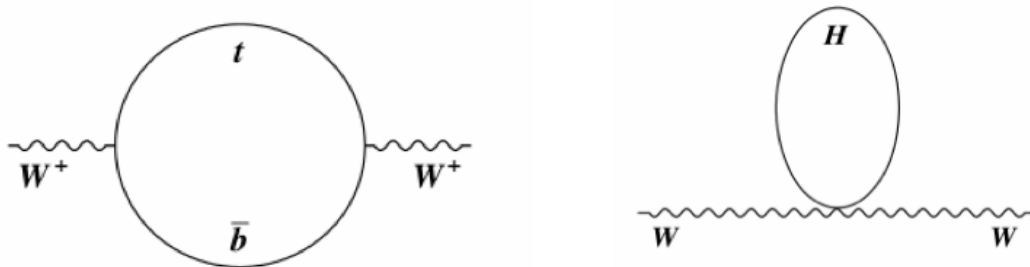
ICHEP 2012, Melbourne

Motivation

W mass is a key parameter in the Standard Model. This model does not predict the value of the W mass, but it predicts this **relation between the W mass and other experimental observables**:

$$M_W = \sqrt{\frac{\pi\alpha}{\sqrt{2}G_F}} \frac{1}{\sin\theta_W \sqrt{1-\Delta r}}$$

Radiative corrections (Δr) depend on M_t as $\sim M_t^2$ and on M_H as $\sim \log M_H$. They include diagrams like these:



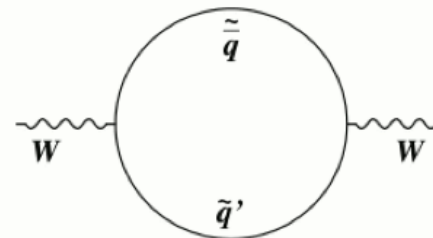
Precise measurements of M_W and M_t constrain SM Higgs mass.

For equal contribution to the Higgs mass uncertainty need:

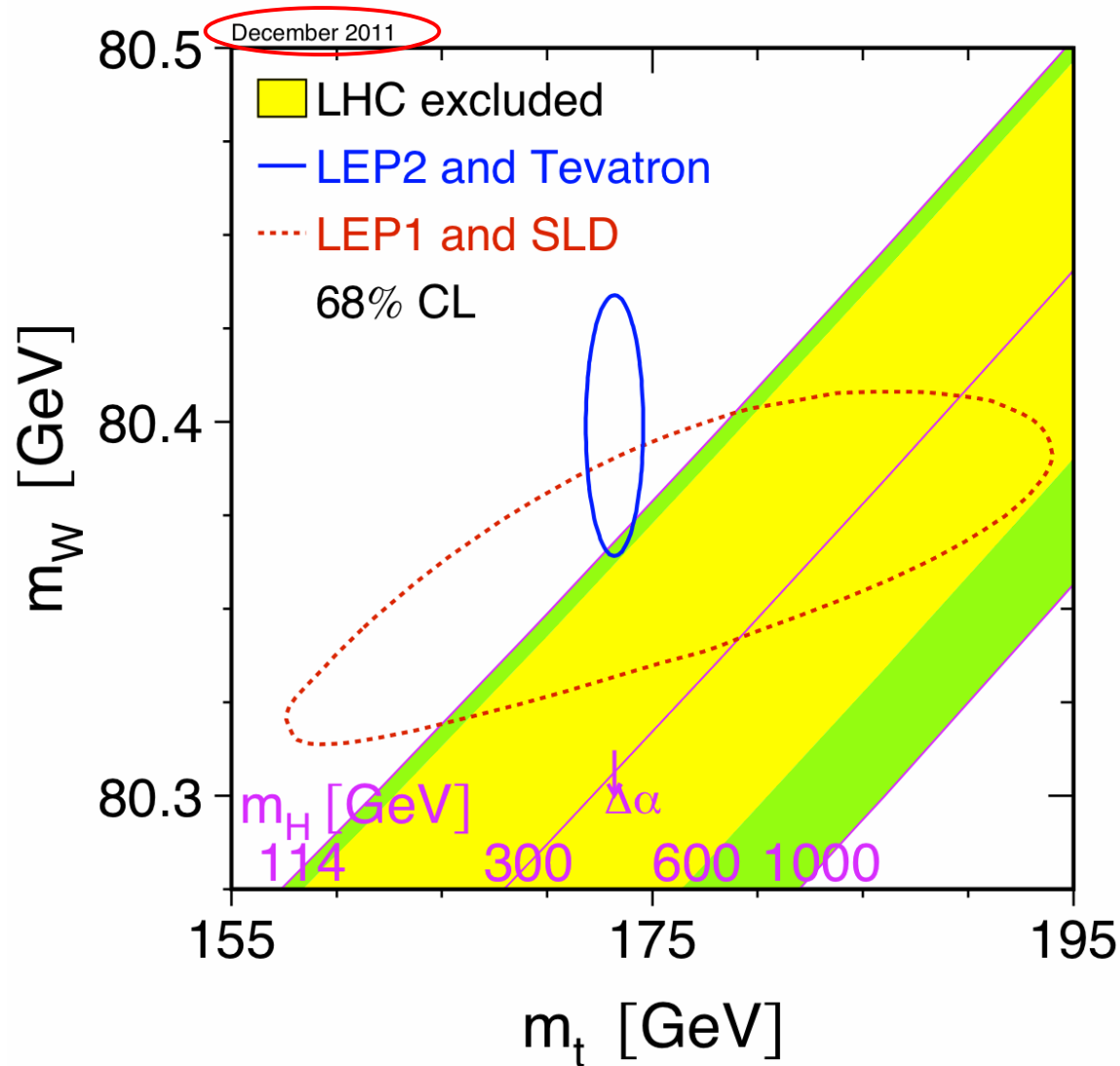
$$\Delta M_W \approx 0.006 \Delta M_t.$$

Additional contributions to Δr arise in various extensions to the Standard Model,

e.g. in SUSY:



Motivation



For equal contribution to the Higgs mass uncertainty need:

$$\Delta M_W \approx 0.006 \Delta M_t.$$

Current Tevatron average:

$$\Delta M_t = 0.9 \text{ GeV} \quad (\text{arXiv:1107.5255})$$

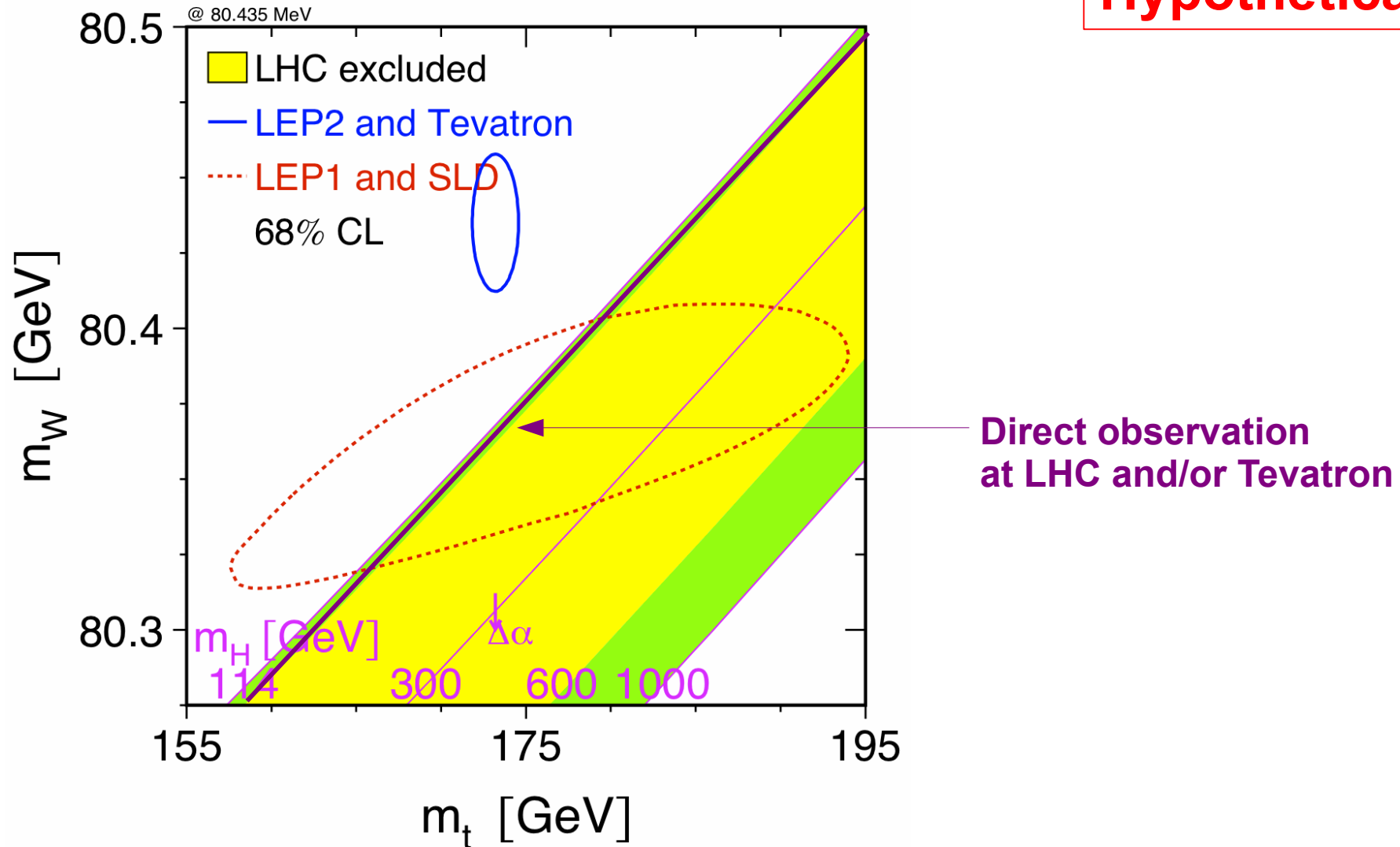
$$\Rightarrow \text{would need: } \Delta M_W = 5 \text{ MeV}$$

$$\text{Currently have: } \Delta M_W = 23 \text{ MeV}$$

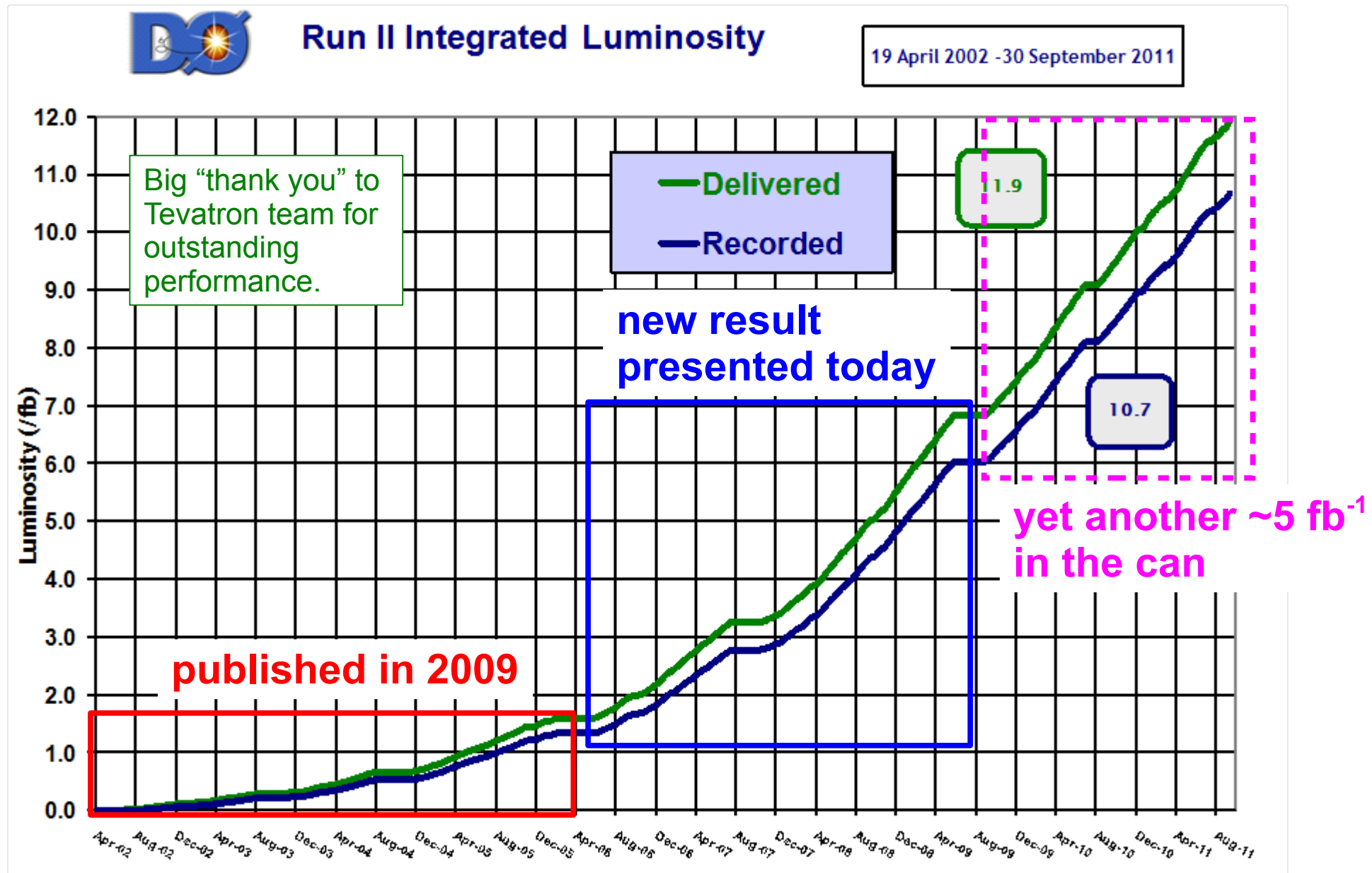
At this point, *i.e.* after all the precise top mass measurements from the Tevatron, the limiting factor here is ΔM_W , not ΔM_t .

A possible scenario for ICHEP 2012

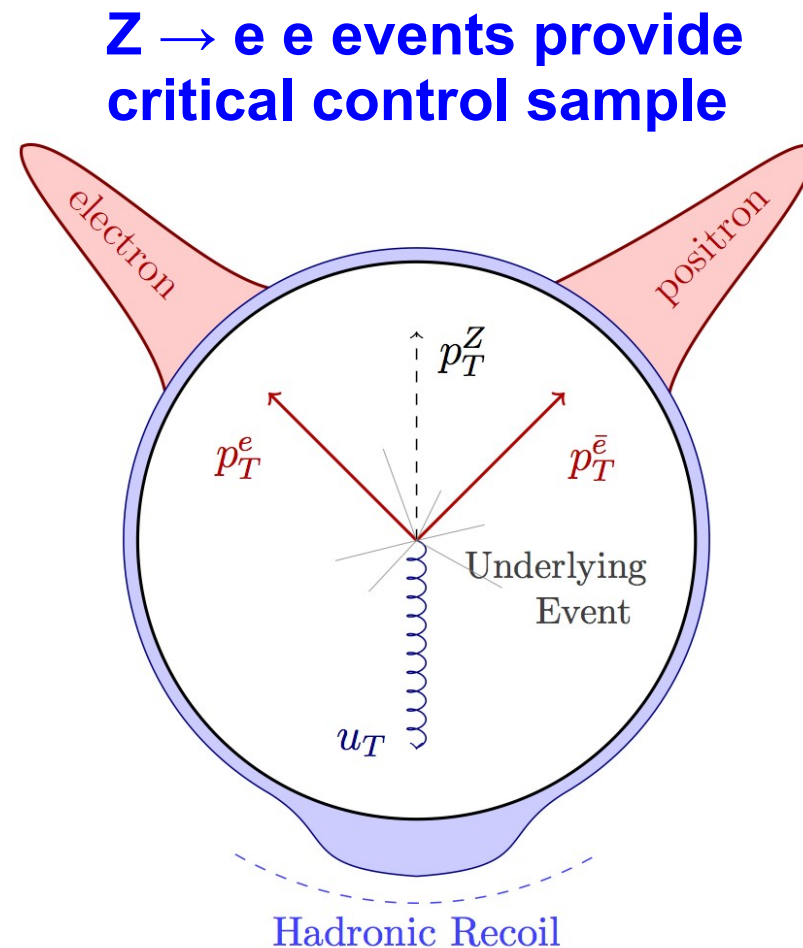
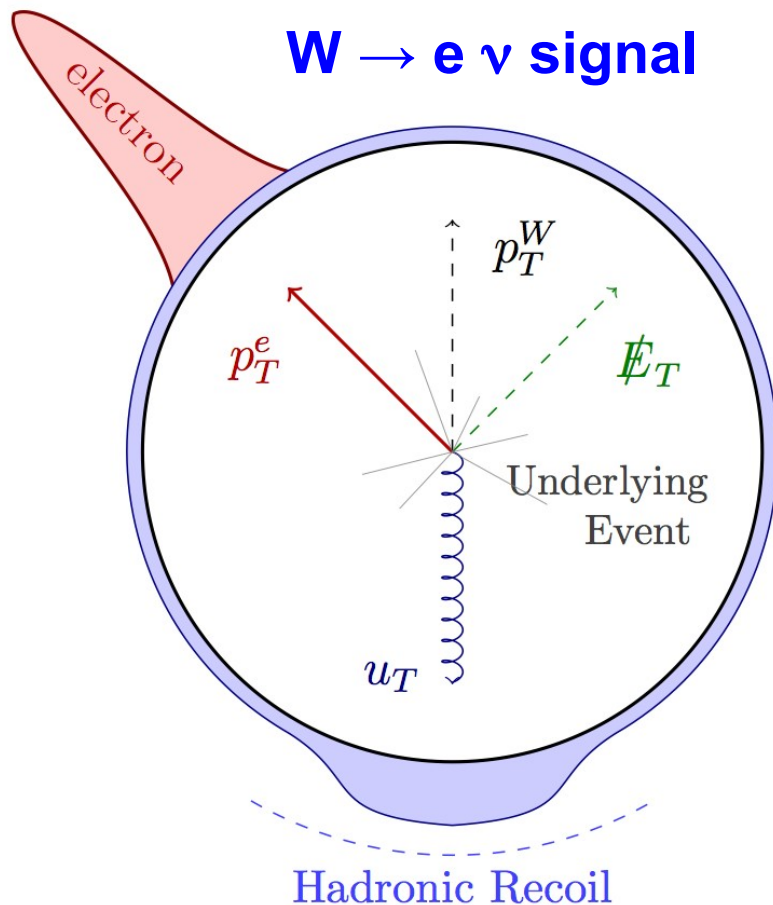
Hypothetical



Data periods and analysis iterations



W mass: measurement method

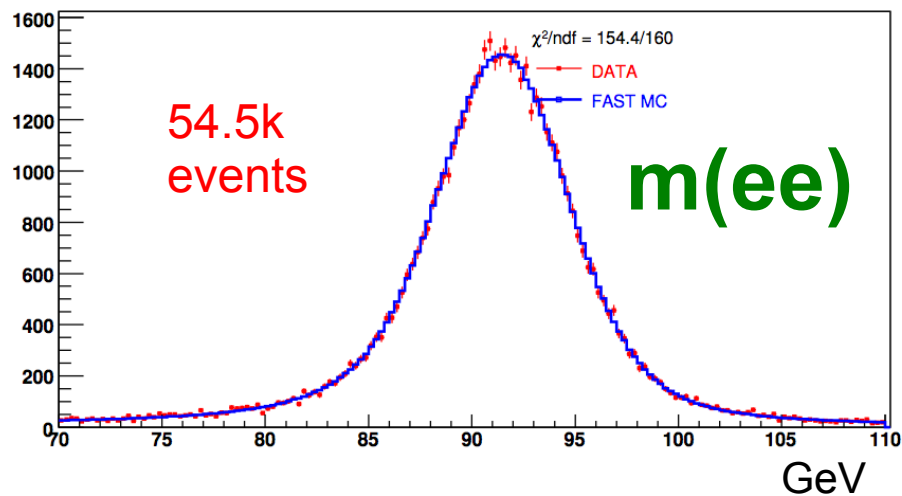


In a nutshell: measure two objects in the detector:

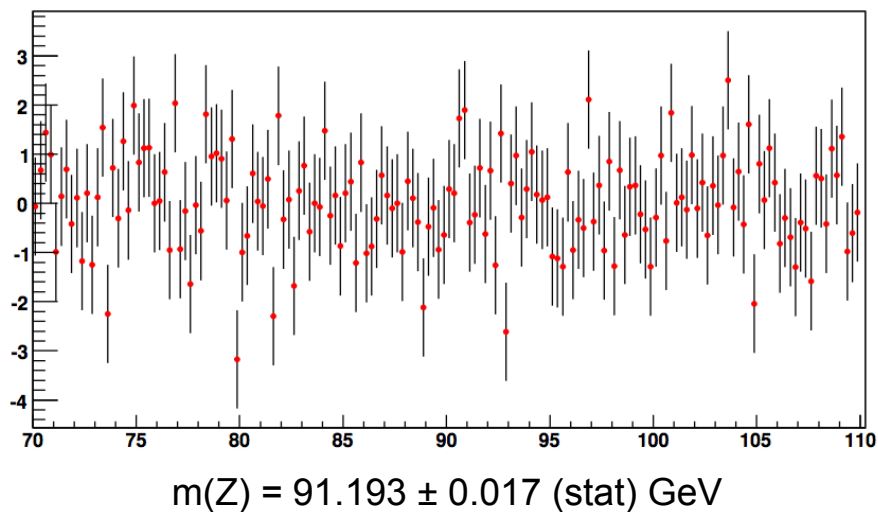
- Lepton (in our case an electron), need energy measurement with 0.1 per-mil precision (!!)
- Hadronic recoil, need $\sim 1\%$ precision

Z data

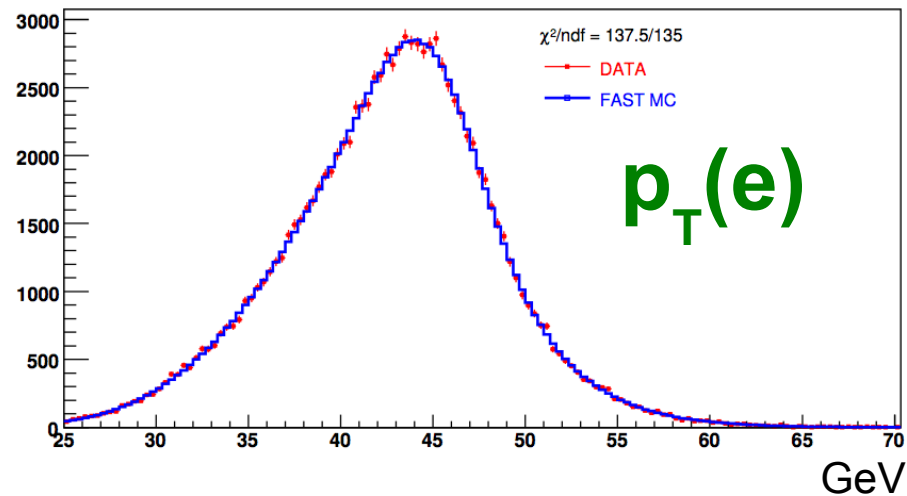
ZCandMass_CCCC_Trks



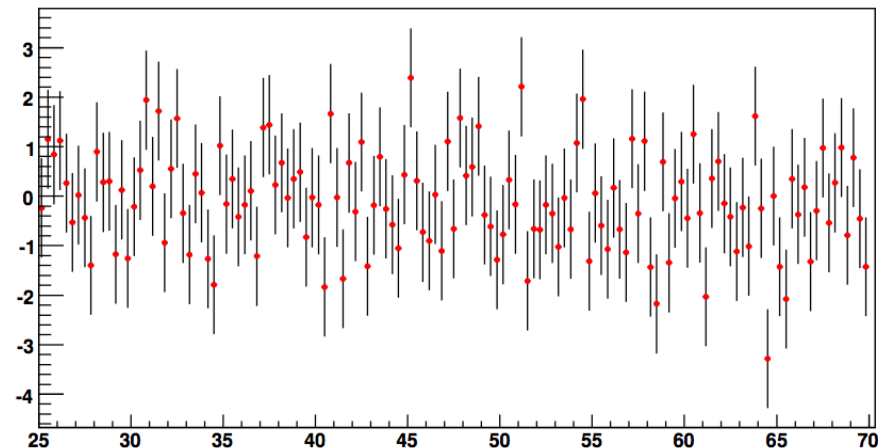
χ distribution with overall $\chi^2 = 154.4$ for 160 bins



ZCandElecPt_0

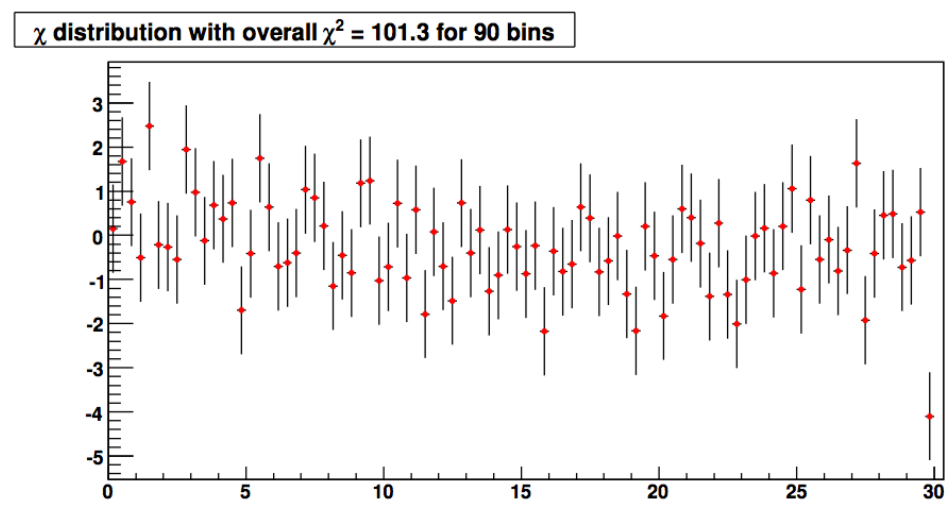
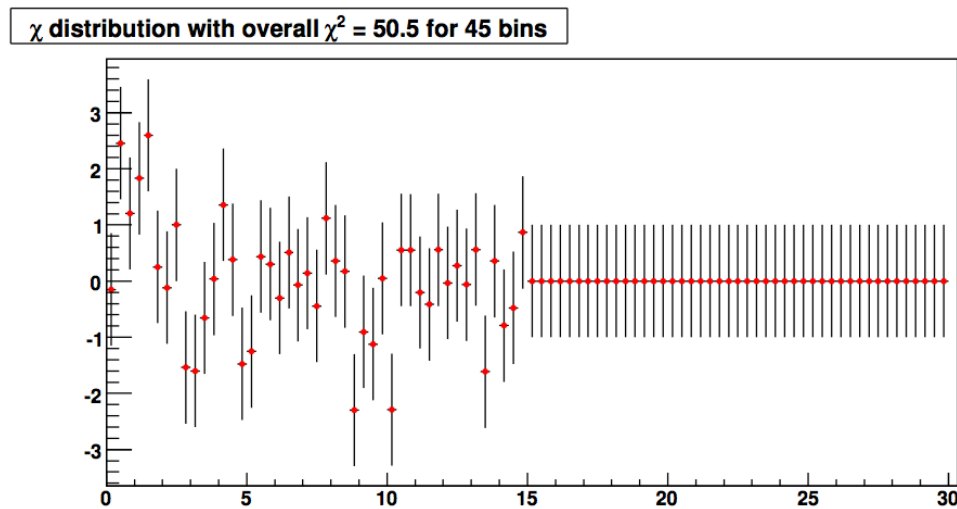
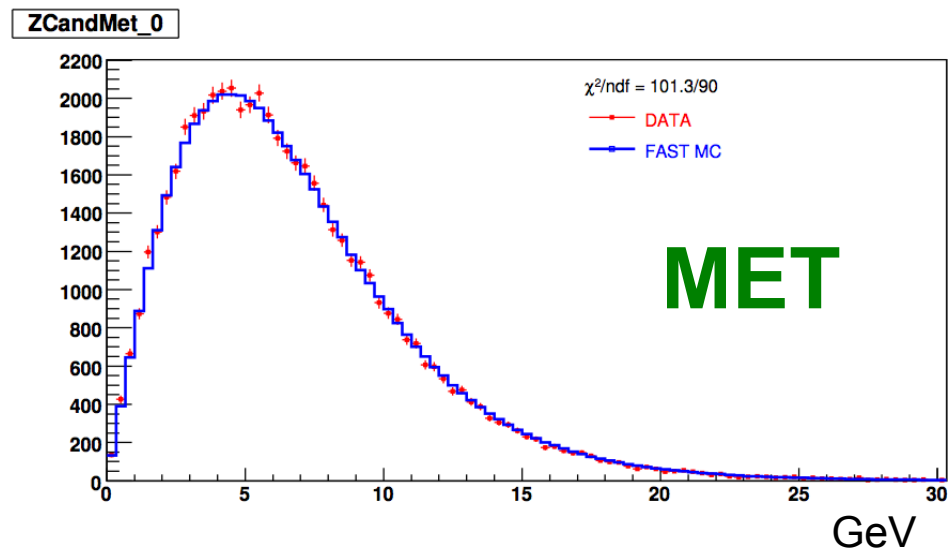
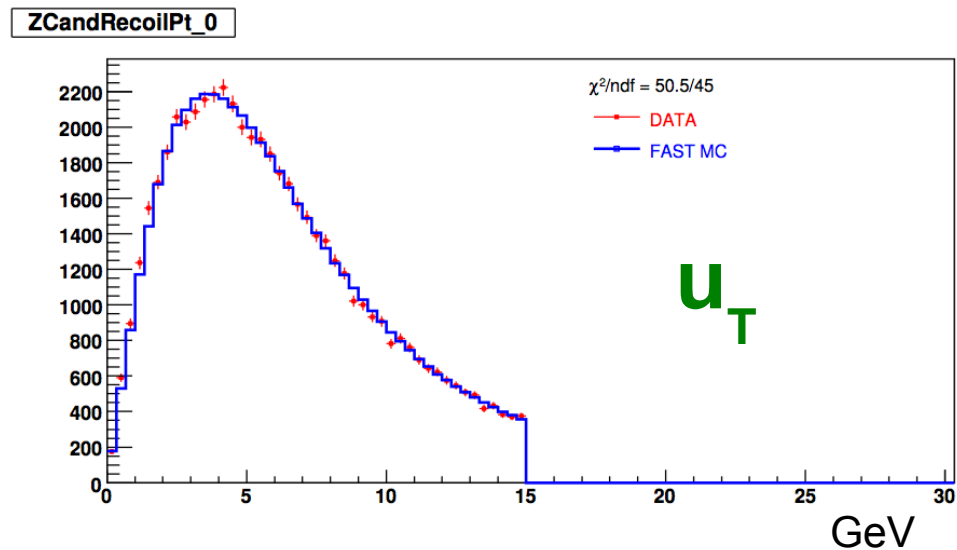


χ distribution with overall $\chi^2 = 137.5$ for 135 bins



Good agreement between data and parameterised Monte Carlo.

Z data

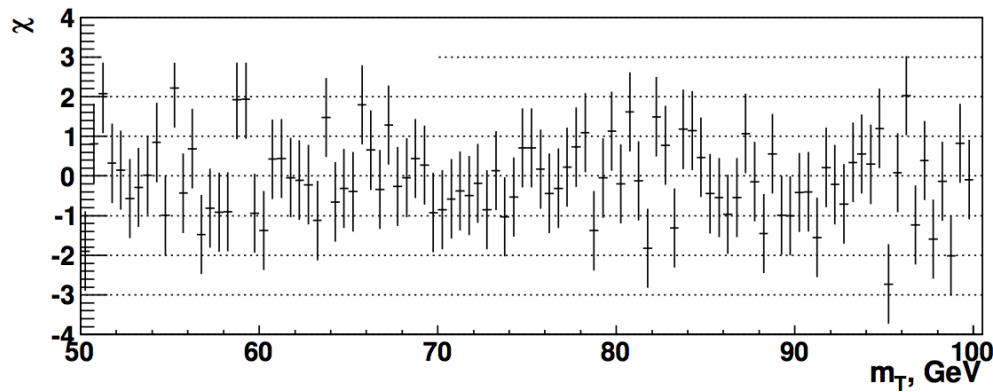
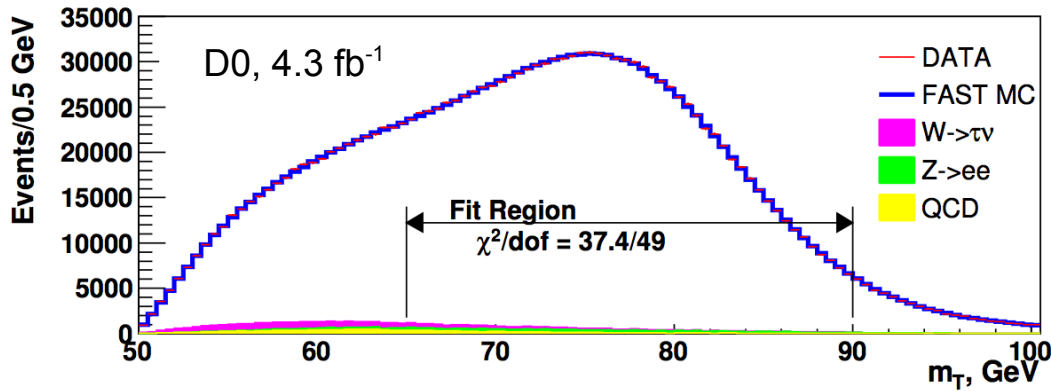


Good agreement between data and parameterised Monte Carlo.

1.68M events
central electrons ($|\eta| < 1.05$)

W data

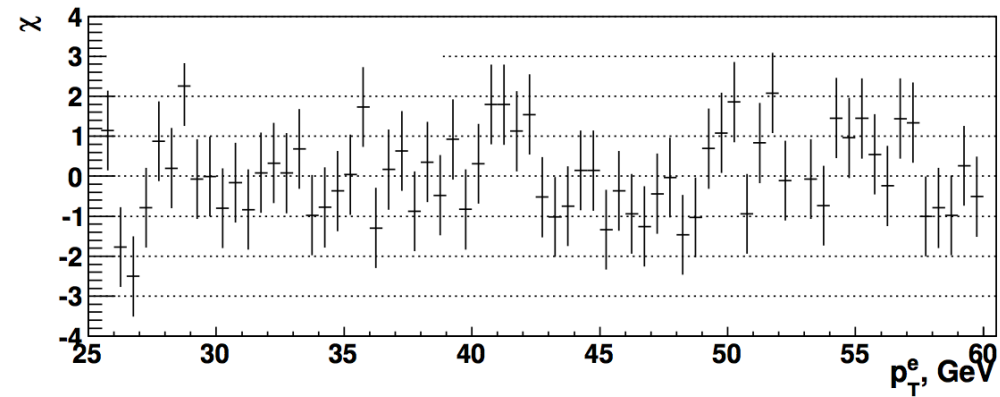
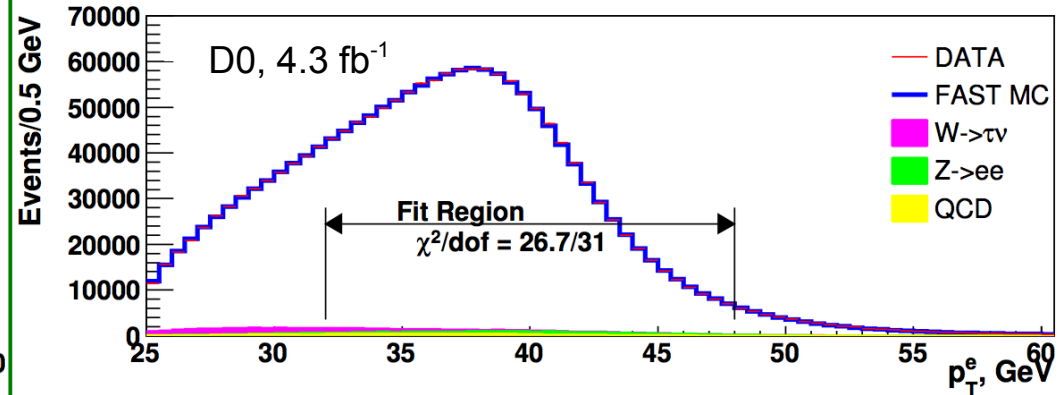
m_T



Fit results:

$$m(W) = 80371 \pm 13 \text{ MeV (stat)}$$

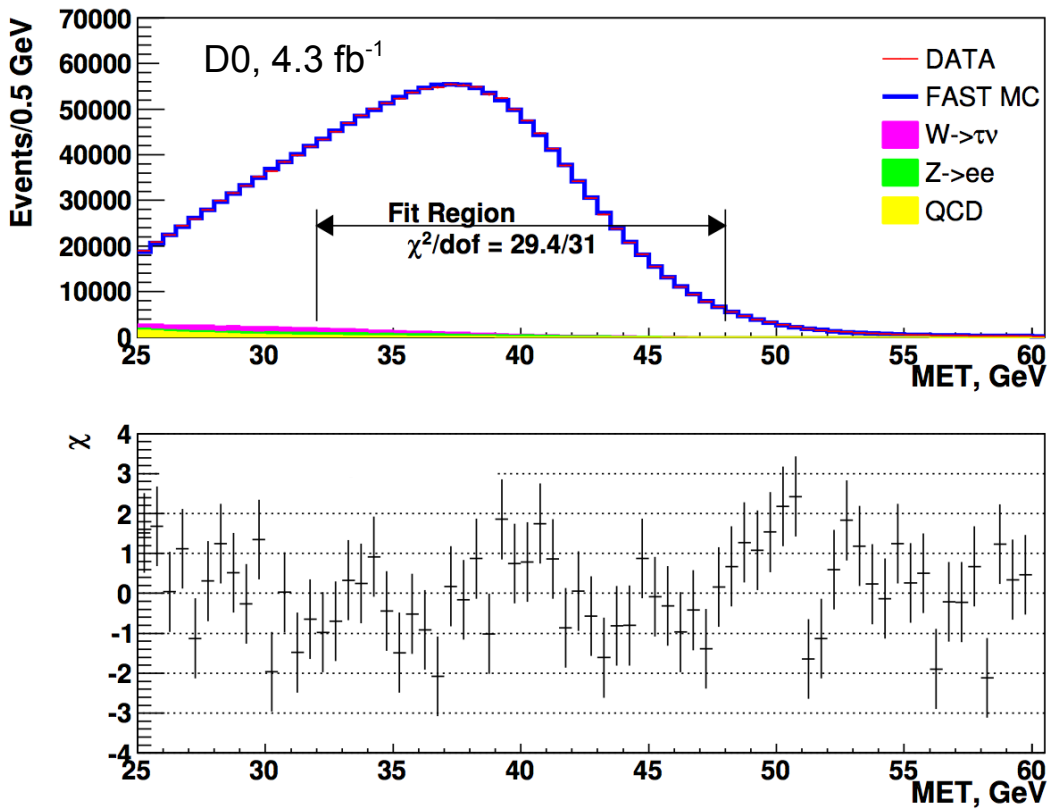
$p_T(e)$



$$m(W) = 80343 \pm 14 \text{ MeV (stat)}$$

W data

MET



Fit results:

$$m(W) = 80355 \pm 15 \text{ MeV (stat)}$$

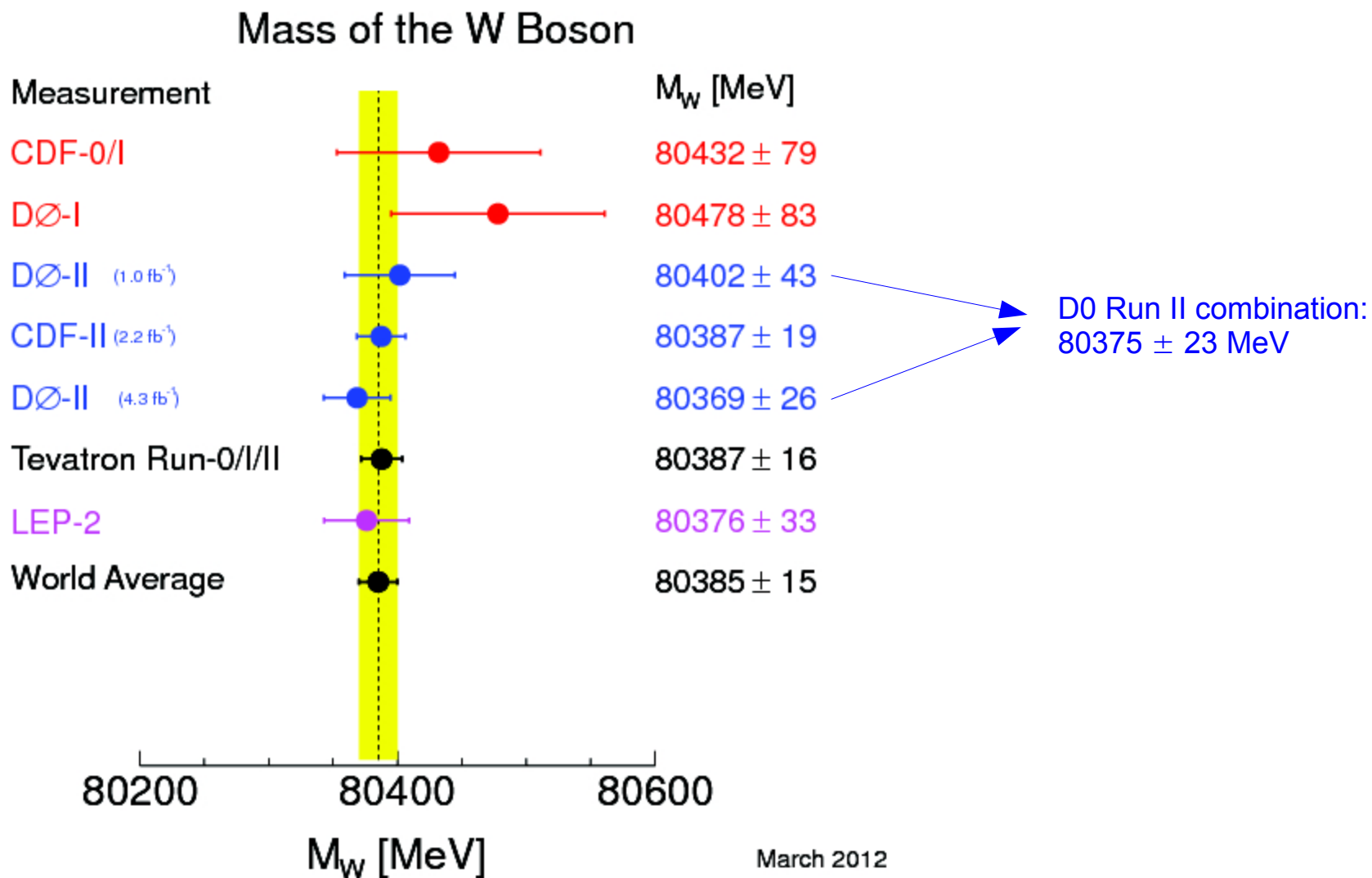
Systematic uncertainties, CDF and D0

Comparison of systematic uncertainties in the $m_T(\ell, \nu)$ measurement
(values in MeV)

Source	CDF $m_T(\mu, \nu)$	CDF $m_T(e, \nu)$	DØ $m_T(e, \nu)$
Experimental – Statistical power of the calibration sample.			
Lepton Energy Scale	7	10	16
Lepton Energy Resolution	1	4	2
Lepton Energy Non-Linearity			4
Lepton Energy Loss			4
Recoil Energy Scale	5	5	
Recoil Energy Resolution	7	7	
Lepton Removal	2	3	
Recoil Model			5
Efficiency Model			1
Background	3	4	2
W production and decay model – Not statistically driven.			
PDF	10	10	11
QED	4	4	7
Boson p_T	3	3	2

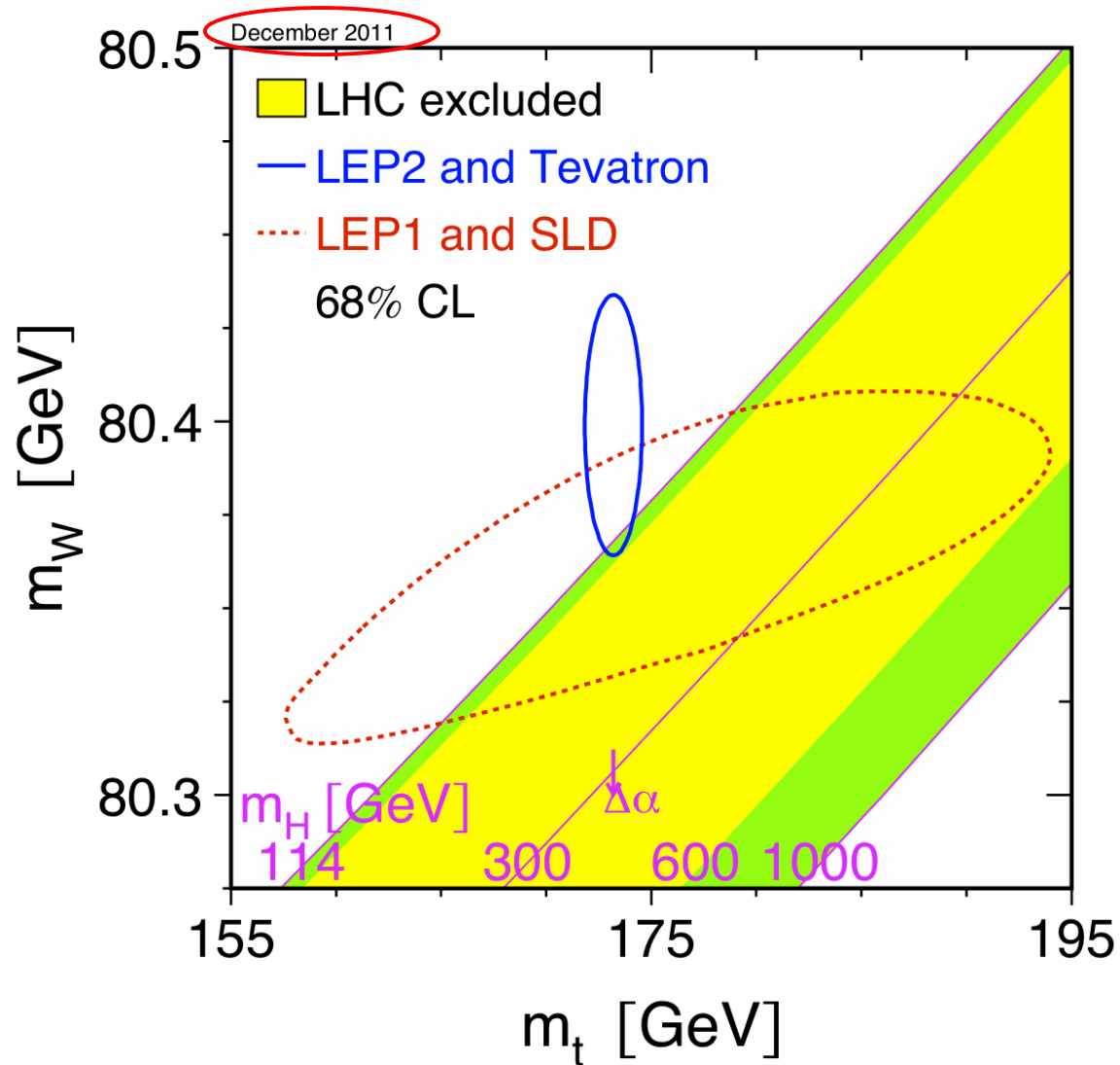


Comparison with previous results; New averages



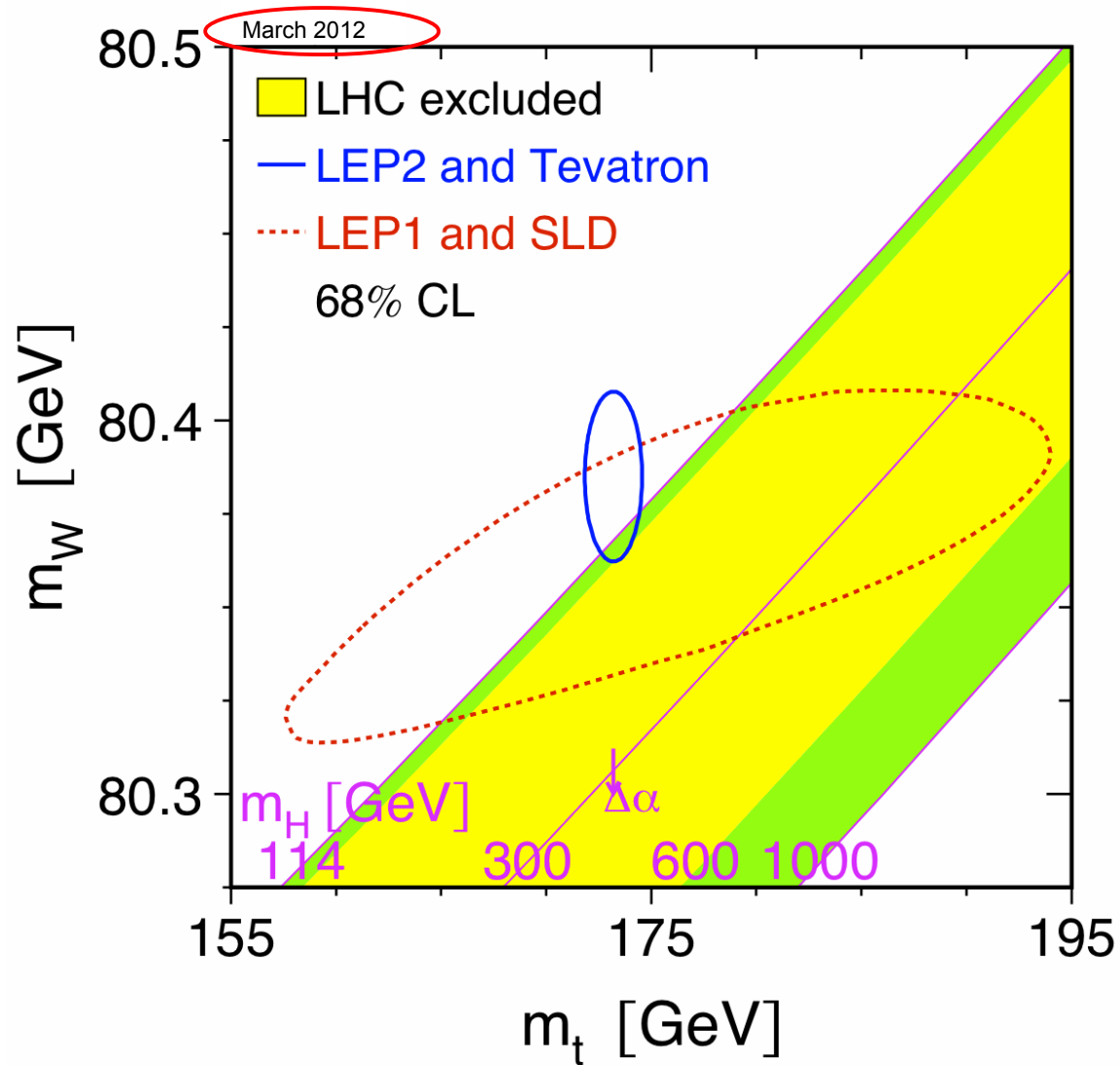
[arXiv:1204.0042 \[hep-ex\]](https://arxiv.org/abs/1204.0042)

New summary graph



This is from December 2011
(same as on slide 3).

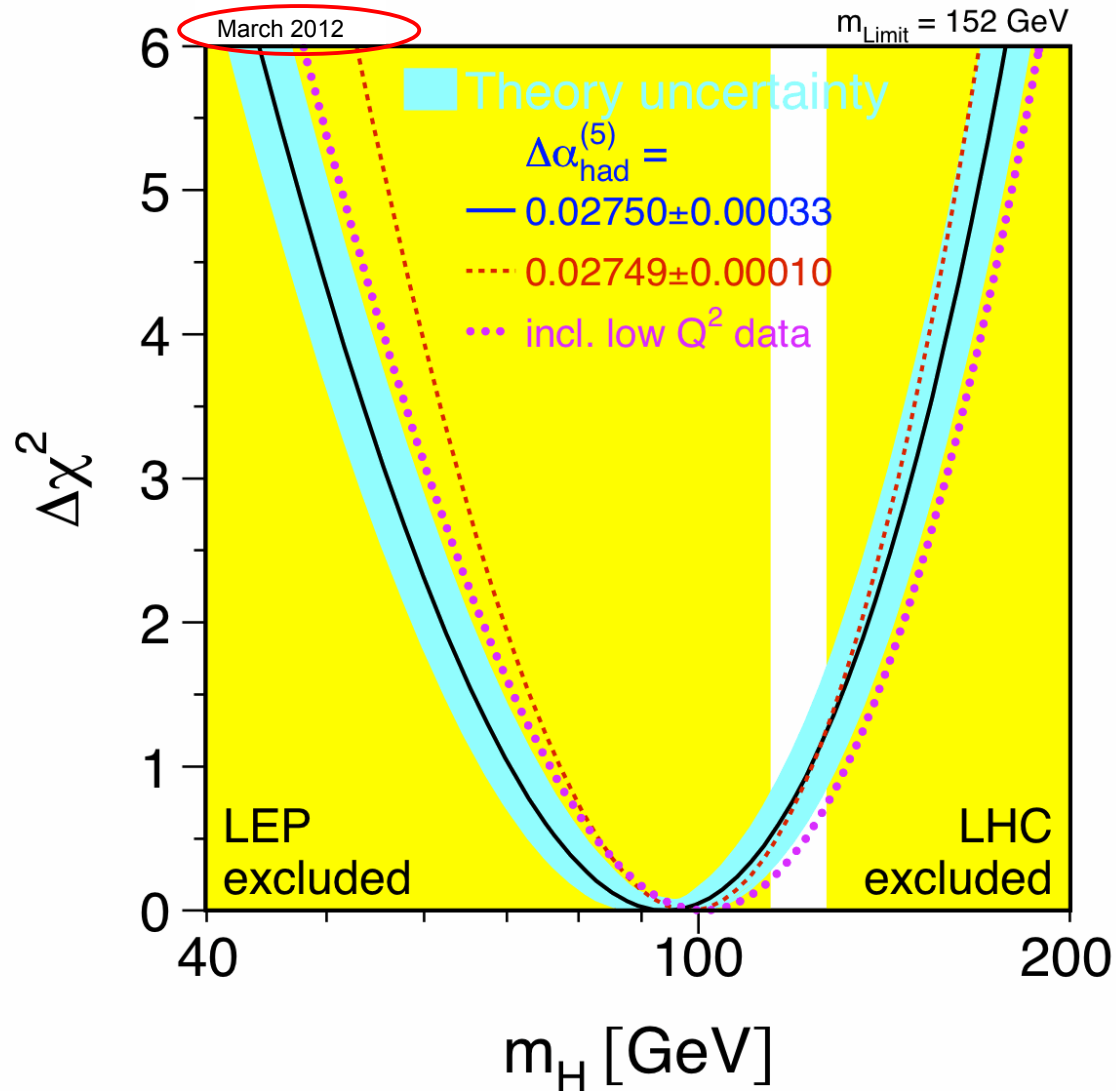
New summary graph



And this is what it looks like now !

Constraints on the Higgs boson mass

Zfitter, LEPEWWG



Previous SM Higgs fit:

$$m_H = 92^{+34}_{-26} \text{ GeV}$$

$$m_H < 161 \text{ @ 95\% C.L.}$$

New preliminary SM Higgs fit:

$$m_H = 94^{+29}_{-24} \text{ GeV}$$

$$m_H < 152 \text{ @ 95\% C.L.}$$

PDF uncertainties

In principle:

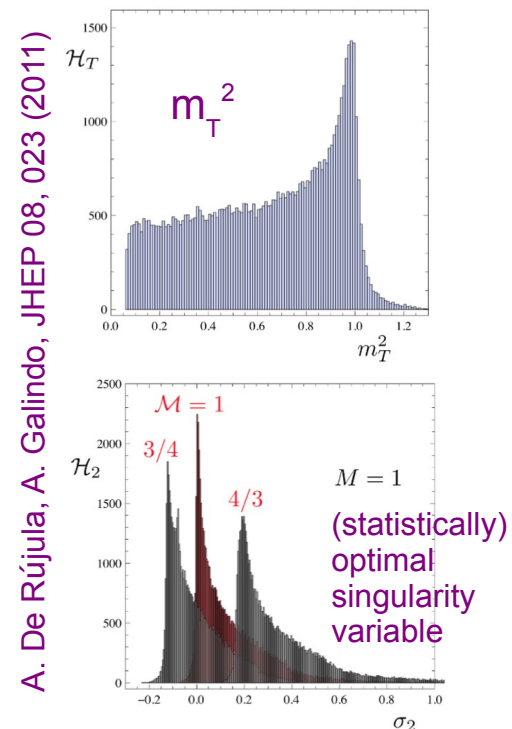
transverse observables (e.g. m_T) are insensitive to the uncertainties in the (longitudinal) parton distribution functions (PDFs)

In practice:

the uncertainties are to some extent reintroduced via the limited η coverage of experiments, which are not invariant under longitudinal boosts

How to reduce the impact of the PDF uncertainties in measurements of the W boson mass ?

- Reduce the uncertainties in the PDFs
e.g. via measurements of the W charge asymmetry at the Tevatron and the LHC (complementarity of the two colliders)
- Reduce the impact of the PDF uncertainties on W boson mass
by extending the η coverage as much as possible
(challenging: understanding lepton energy scale and pile-up and backgrounds in the forward detectors)
- Possibly reduce the impact of the PDF uncertainties on W boson mass
by exploring even more robust observables
("single out events with small longitudinal momentum") to replace/complement m_T



These three approaches are not mutually exclusive, *i.e.* they can be pursued at the same time and gains should “add up”.

Conclusions

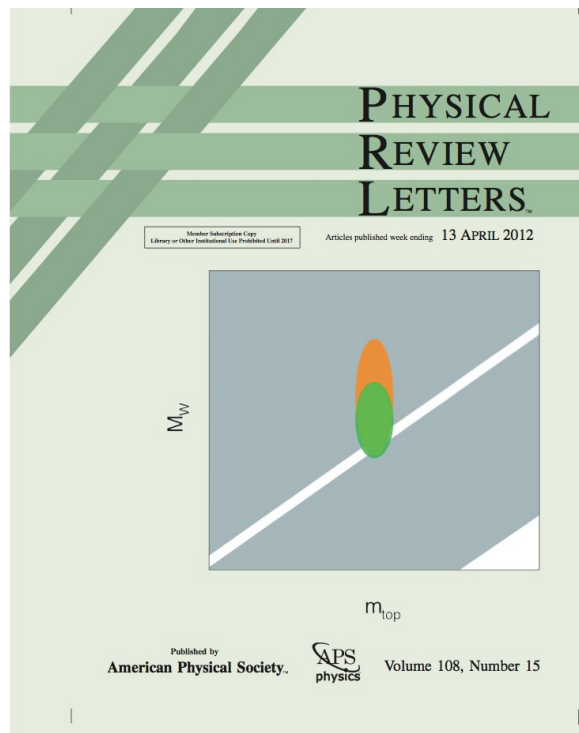
We present a new measurement of the W boson mass based on 4.3 fb^{-1} of D0 Run II data.

Combined with our earlier Run II measurement (1 fb^{-1}), we obtain:

$$M_W = 80.375 \pm 0.011 \text{ (stat)} \pm 0.020 \text{ (syst)} \text{ GeV}$$

$$= 80.375 \pm 0.023 \text{ GeV.}$$

Phys. Rev. Lett. **108**, 151804 (2012)



New preliminary Tevatron average: 16 MeV uncertainty.
New preliminary world average: **15 MeV** uncertainty.

Have shown exciting new **indirect constraints** on the mass of the Higgs boson.

"We have discovered a boson, and now we have to determine what kind of boson it is." – Prof. Heuer

Have twice more data in the can.

Have the means to reduce PDF uncertainties by factor two.

=> looking forward to even smaller uncertainties in the future.

Backup Slides

Global electroweak fit



May 12

May 12 version of Gfitter
standard model fit:

<http://gfitter.desy.de/>

Parameter	Input value	Free in fit	Results from global EW fits:		<i>Complete fit w/o exp. input in line</i>
			<i>Standard fit</i>	<i>Complete fit</i>	
M_Z [GeV]	91.1875 ± 0.0021	yes	91.1874 ± 0.0021	91.1878 ± 0.0021	$91.1951^{+0.0136}_{-0.0112}$
Γ_Z [GeV]	2.4952 ± 0.0023	–	2.4958 ± 0.0015	2.4955 ± 0.0014	2.4952 ± 0.0016
σ_{had}^0 [nb]	41.540 ± 0.037	–	41.478 ± 0.014	$41.477^{+0.016}_{-0.013}$	41.470 ± 0.015
R_ℓ^0	20.767 ± 0.025	–	20.743 ± 0.018	20.741 ± 0.017	$20.717^{+0.027}_{-0.008}$
$A_{\text{FB}}^{0,\ell}$	0.0171 ± 0.0010	–	0.01637 ± 0.0002	$0.01627^{+0.0002}_{-0.0001}$	$0.01620^{+0.0002}_{-0.0001}$
$A_\ell^{(*)}$	0.1499 ± 0.0018	–	$0.1477^{+0.0009}_{-0.0008}$	$0.1473^{+0.0008}_{-0.0006}$	–
A_c	0.670 ± 0.027	–	$0.6682^{+0.00042}_{-0.00035}$	$0.6680^{+0.00037}_{-0.00028}$	$0.6680^{+0.00034}_{-0.00030}$
A_b	0.923 ± 0.020	–	$0.93468^{+0.00008}_{-0.00007}$	$0.93463^{+0.00007}_{-0.00005}$	0.93466 ± 0.00005
$A_{\text{FB}}^{0,c}$	0.0707 ± 0.0035	–	$0.0740^{+0.0005}_{-0.0004}$	$0.0738^{+0.0005}_{-0.0003}$	0.0738 ± 0.0004
$A_{\text{FB}}^{0,b}$	0.0992 ± 0.0016	–	$0.1036^{+0.0007}_{-0.0006}$	$0.1032^{+0.0006}_{-0.0005}$	$0.1037^{+0.0003}_{-0.0005}$
R_c^0	0.1721 ± 0.0030	–	0.17223 ± 0.00006	0.17223 ± 0.00006	0.17223 ± 0.00006
R_b^0	0.21629 ± 0.00066	–	0.21474 ± 0.00003	0.21474 ± 0.00003	0.21474 ± 0.00003
$\sin^2\theta_{\text{eff}}^\ell(Q_{\text{FB}})$	0.2324 ± 0.0012	–	$0.23144^{+0.00010}_{-0.00013}$	$0.23150^{+0.00008}_{-0.00011}$	$0.23145^{+0.00012}_{-0.00006}$
M_H [GeV] ^(◊)	95% CL limits	yes	$94^{+25[+59]}_{-22[-41]}$	–	$94^{+25[+59]}_{-22[-41]}$
M_W [GeV]	80.385 ± 0.015	–	$80.380^{+0.011}_{-0.012}$	$80.370^{+0.006}_{-0.007}$	$80.360^{+0.014}_{-0.012}$
Γ_W [GeV]	2.085 ± 0.042	–	2.092 ± 0.001	2.092 ± 0.001	2.092 ± 0.001
\overline{m}_c [GeV]	$1.27^{+0.07}_{-0.11}$	yes	$1.27^{+0.07}_{-0.11}$	$1.27^{+0.07}_{-0.11}$	–
\overline{m}_b [GeV]	$4.20^{+0.17}_{-0.07}$	yes	$4.20^{+0.17}_{-0.07}$	$4.20^{+0.17}_{-0.07}$	–
m_t [GeV]	173.2 ± 0.9	yes	173.2 ± 0.9	173.4 ± 0.8	$175.1^{+3.3}_{-2.4}$
$\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$ ^(†Δ)	2757 ± 10	yes	2757 ± 11	2756 ± 11	2728^{+51}_{-50}
$\alpha_s(M_Z^2)$	–	yes	$0.1192^{+0.0028}_{-0.0027}$	0.1191 ± 0.0028	0.1191 ± 0.0028
$\delta_{\text{th}} M_W$ [MeV]	$[-4, 4]_{\text{theo}}$	yes	4	4	–
$\delta_{\text{th}} \sin^2\theta_{\text{eff}}^\ell$ ^(†)	$[-4.7, 4.7]_{\text{theo}}$	yes	4.7	1.5	–

(*) Average of LEP ($A_\ell = 0.1465 \pm 0.0033$) and SLD ($A_\ell = 0.1513 \pm 0.0021$) measurements. The *complete fit w/o* the LEP (SLD) measurement gives $A_\ell = 0.1474^{+0.0006}_{-0.0007}$ ($A_\ell = 0.1469 \pm 0.0006$). ^(◊)In brackets the 2σ . ^(†)In units of 10^{-5} . ^(Δ)Rescaled due to α_s dependency.

Global electroweak fit

Complete fit:

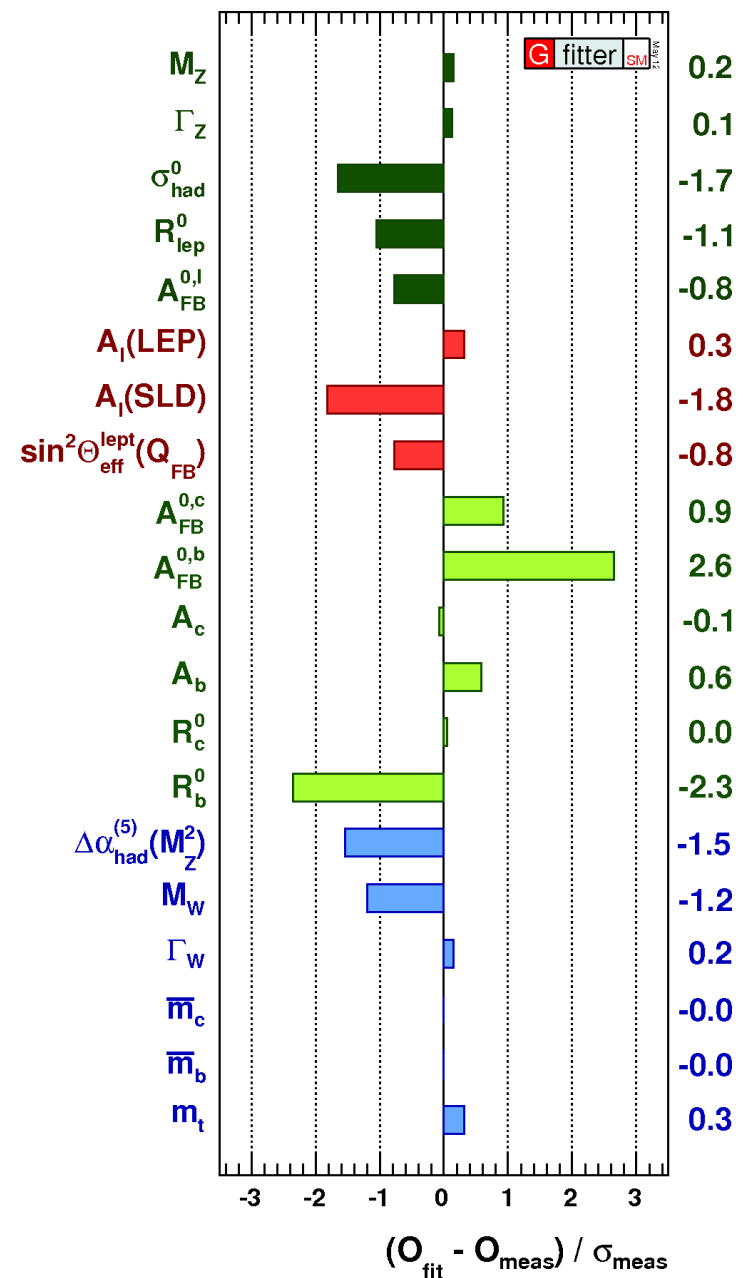
$\chi^2_{\min} = 21.8$ for 14 degrees of freedom.

Pull values for the different observables are shown on the right.

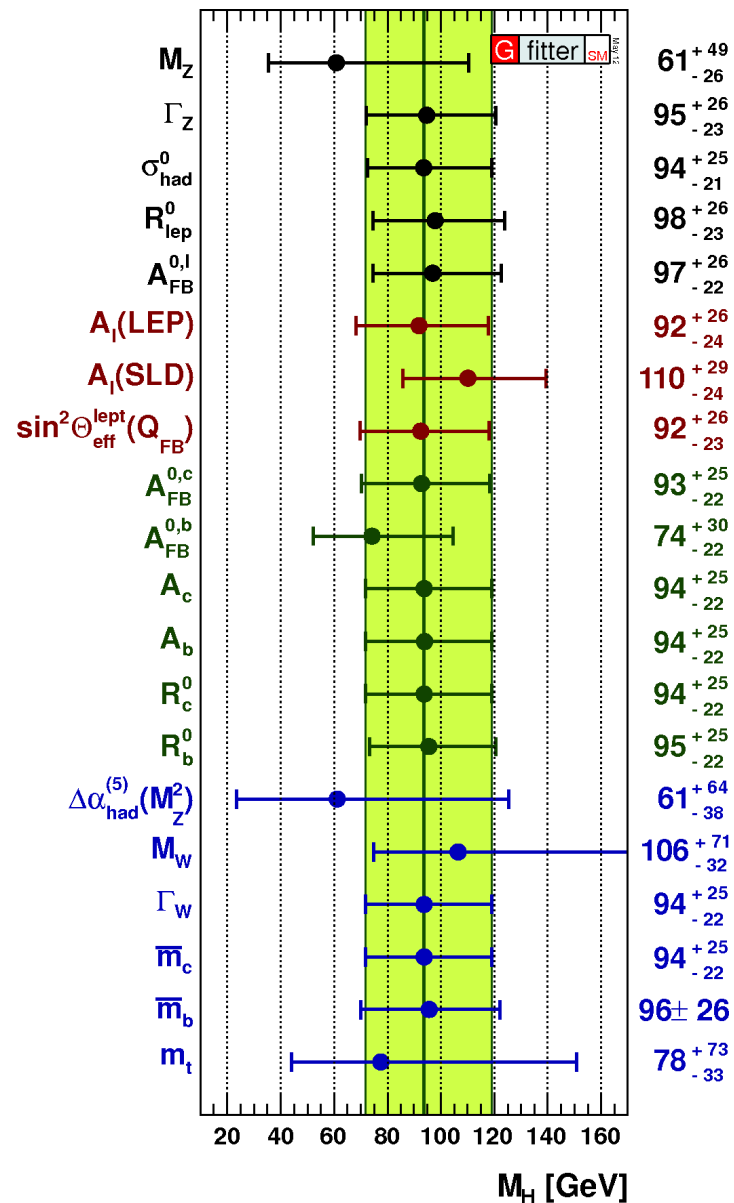
- no value exceeds 3 sigma
- largest individual contribution to χ^2 from FB asymmetry of bottom quarks.

Overall good agreement between precision data and standard model.

As is well known, some tension between $A_l(\text{SLD})$ and $A_{\text{FB}}^{0,b}$ from LEP.



Global electroweak fit

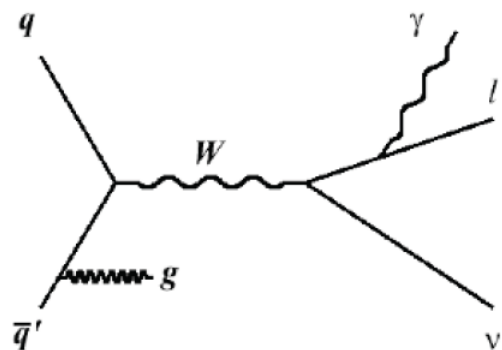


Measurement strategy

W mass is extracted from transverse mass, transverse momentum and transverse missing momentum:

Need Monte Carlo simulation to predict shapes of these observables for given mass hypothesis

NLO event generator with non-perturbative form factor which resums large logarithmic terms from emission of multiple soft gluons:
DØ uses **ResBos** + **Photos** for W/Z production and decay



Detector calibration

- calorimeter energy scale
- recoil

+

Parameterised detector model

W mass templates

+

backgrounds

data

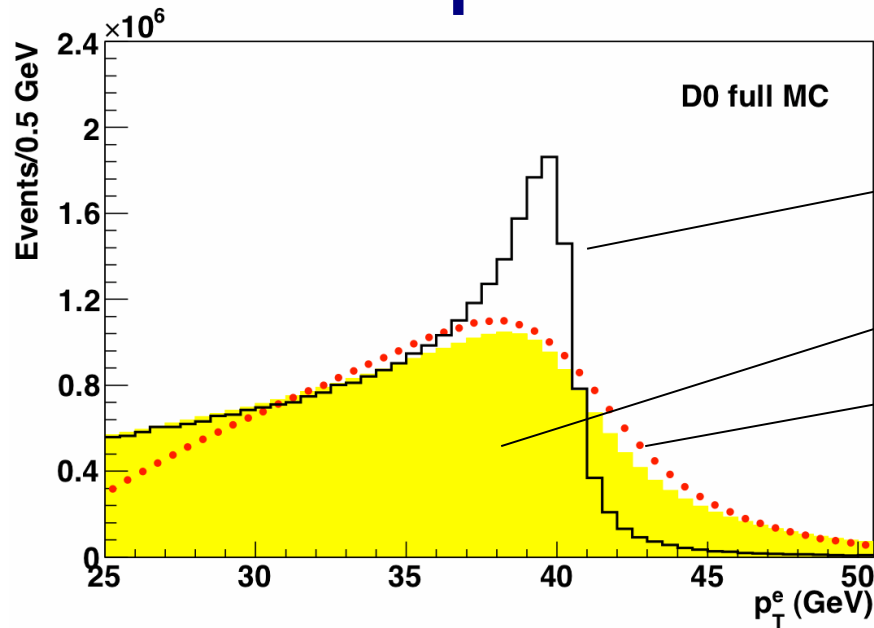
binned likelihood fit




W mass

Validated in
“MC closure test”

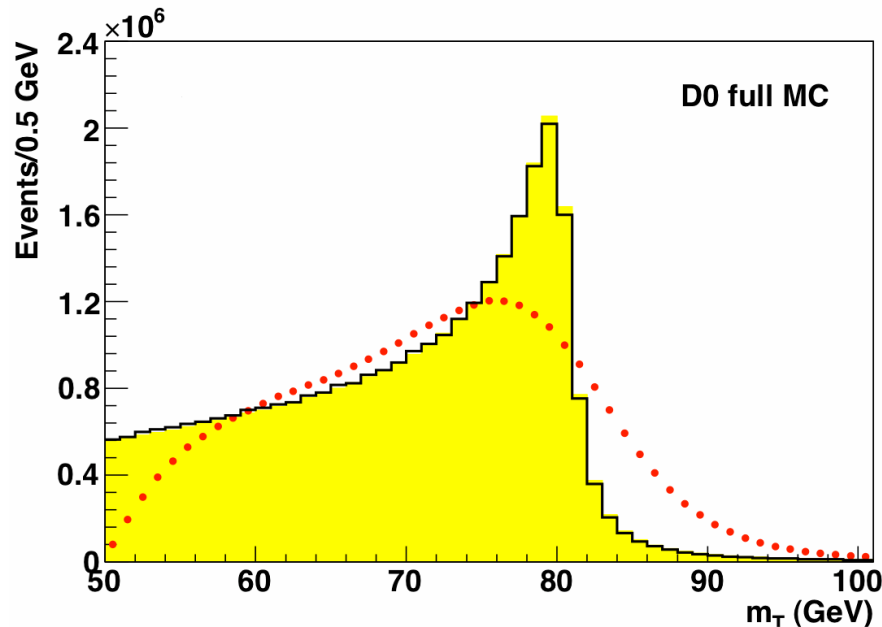
Blind analysis:
true value of mass hidden from the
analysers until the analysis was completed

Experimental observables



 No $p_T(W)$
 $p_T(W)$ included
 Detector Effects added

p_T^e most affected by $p_T(W)$



$$m_T = \sqrt{2 p_T^e E_T (1 - \cos \Delta \phi)}$$

m_T most affected by measurement of recoil transverse momentum

Model of W production and decay

Tool	Process	QCD	EW
RESBOS	W, Z	NLO	-
WGRAD	W	LO	complete $\mathcal{O}(\alpha)$, Matrix Element, ≤ 1 photon
ZGRAD	Z	LO	complete $\mathcal{O}(\alpha)$, Matrix Element, ≤ 1 photon
PHOTOS			QED FSR, ≤ 2 photons

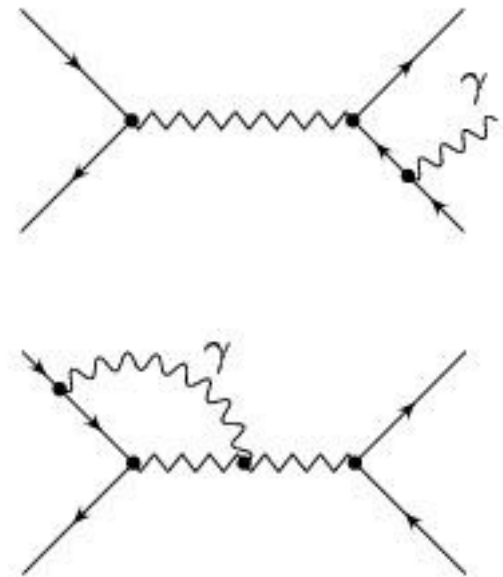
Our main generator is “**ResBos+Photos**”. The NLO QCD in **ResBos** allows us to get a reasonable description of the p_T of the vector bosons. The two leading EWK effects are the first FSR photon and the second FSR photon. **Photos** gives us a reasonable model for both.

We use **W/ZGRAD** to get a feeling for the effect of the full EWK corrections.

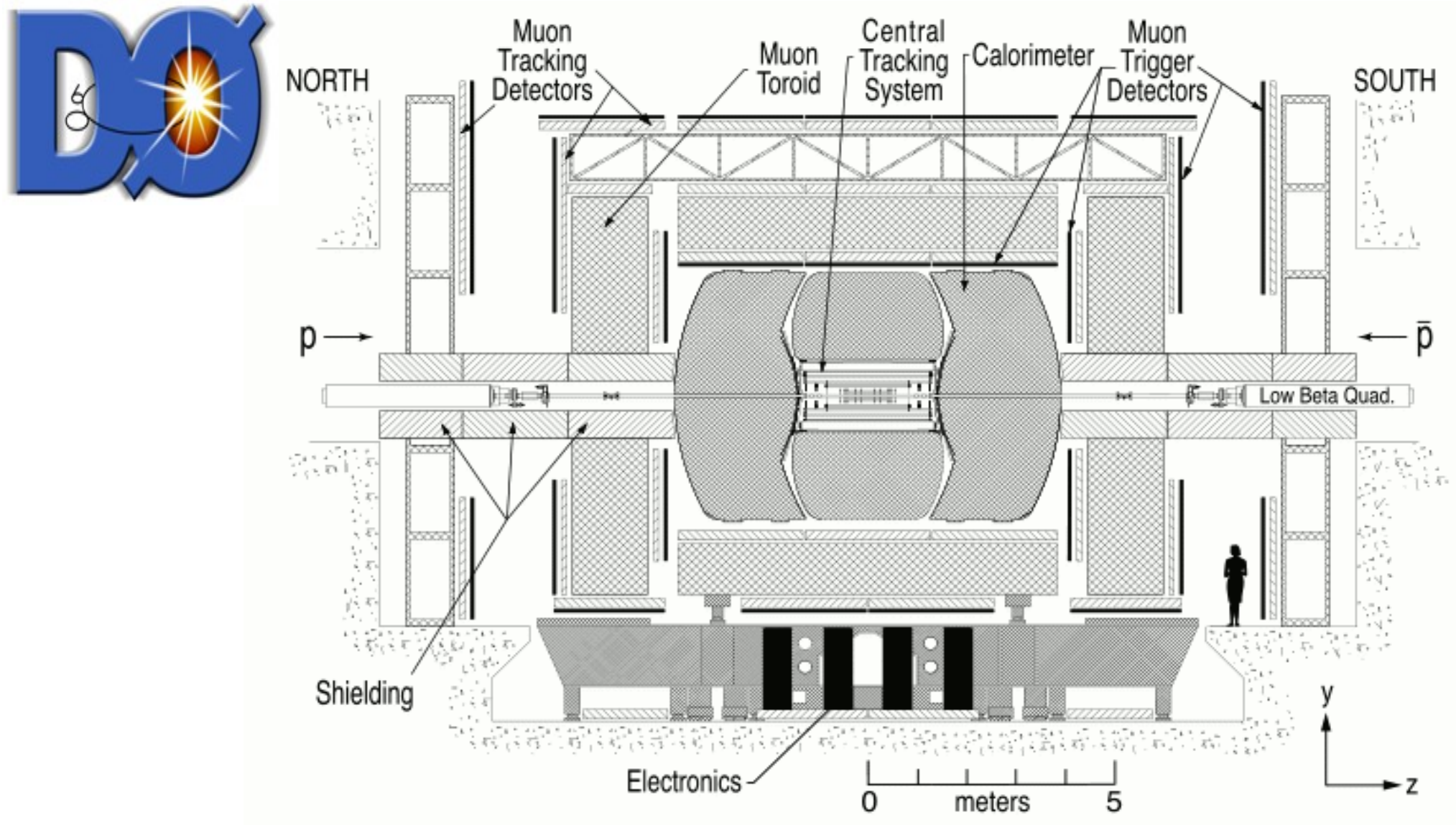
The final “QED” uncertainty we quote is **7/7/9 MeV** (m_T, p_T, MET).

This is the sum of different effects; the two main ones are:

- Effect of full EWK corrections, from comparison of W/ZGRAD in “FSR only” and in “full EWK” modes (**5/5/5 MeV**).
- Very simple estimate of “quality of FSR model”, from comparison of W/ZGRAD in FSR-only mode vs **Photos** (**5/5/5 MeV**).

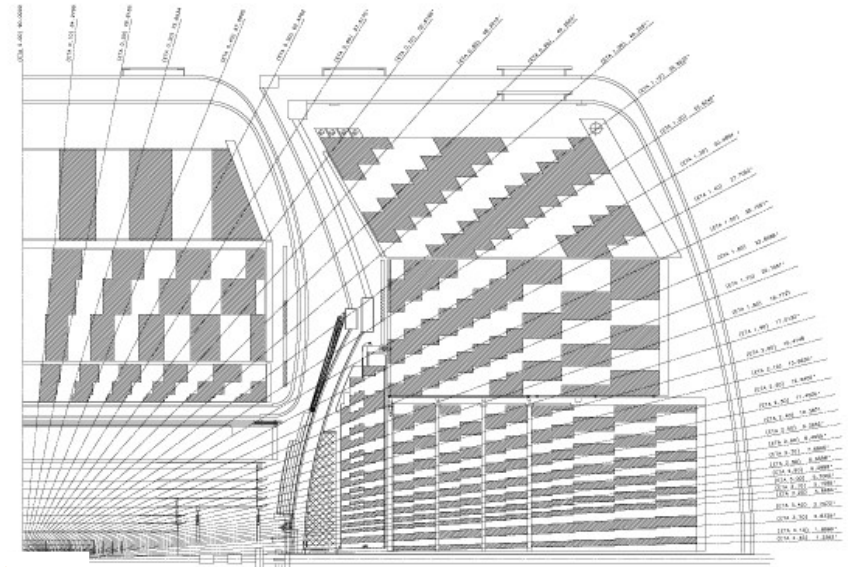
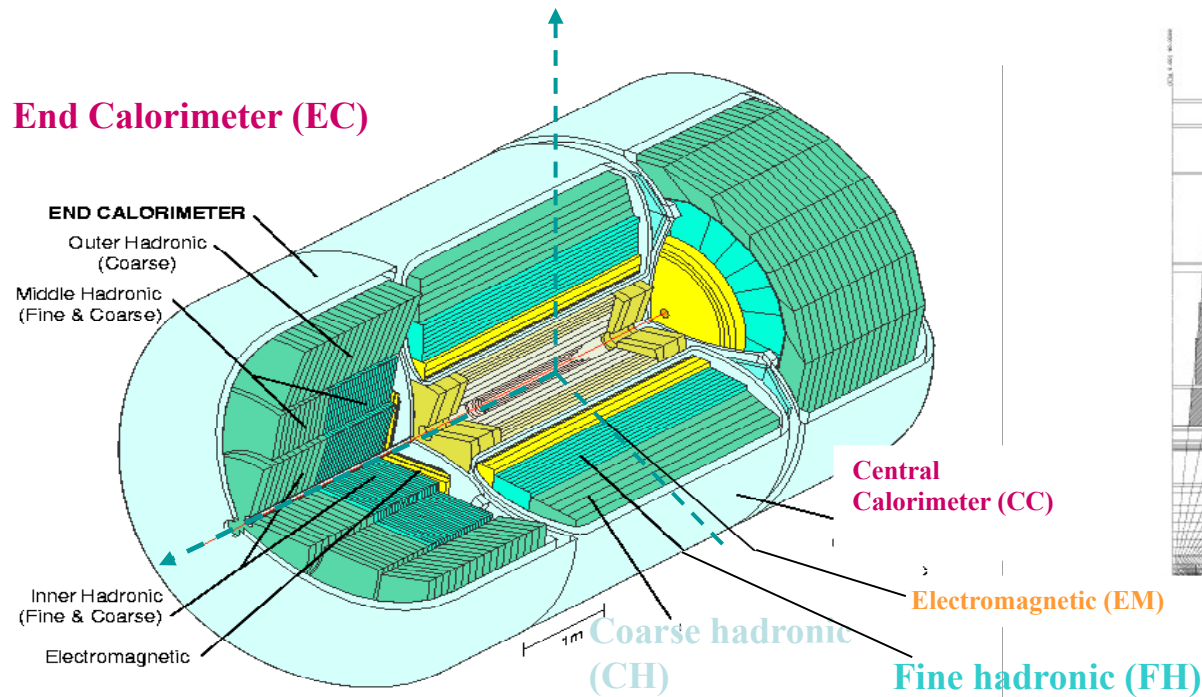


The upgraded DØ detector



Overview of the calorimeter

End Calorimeter (EC)

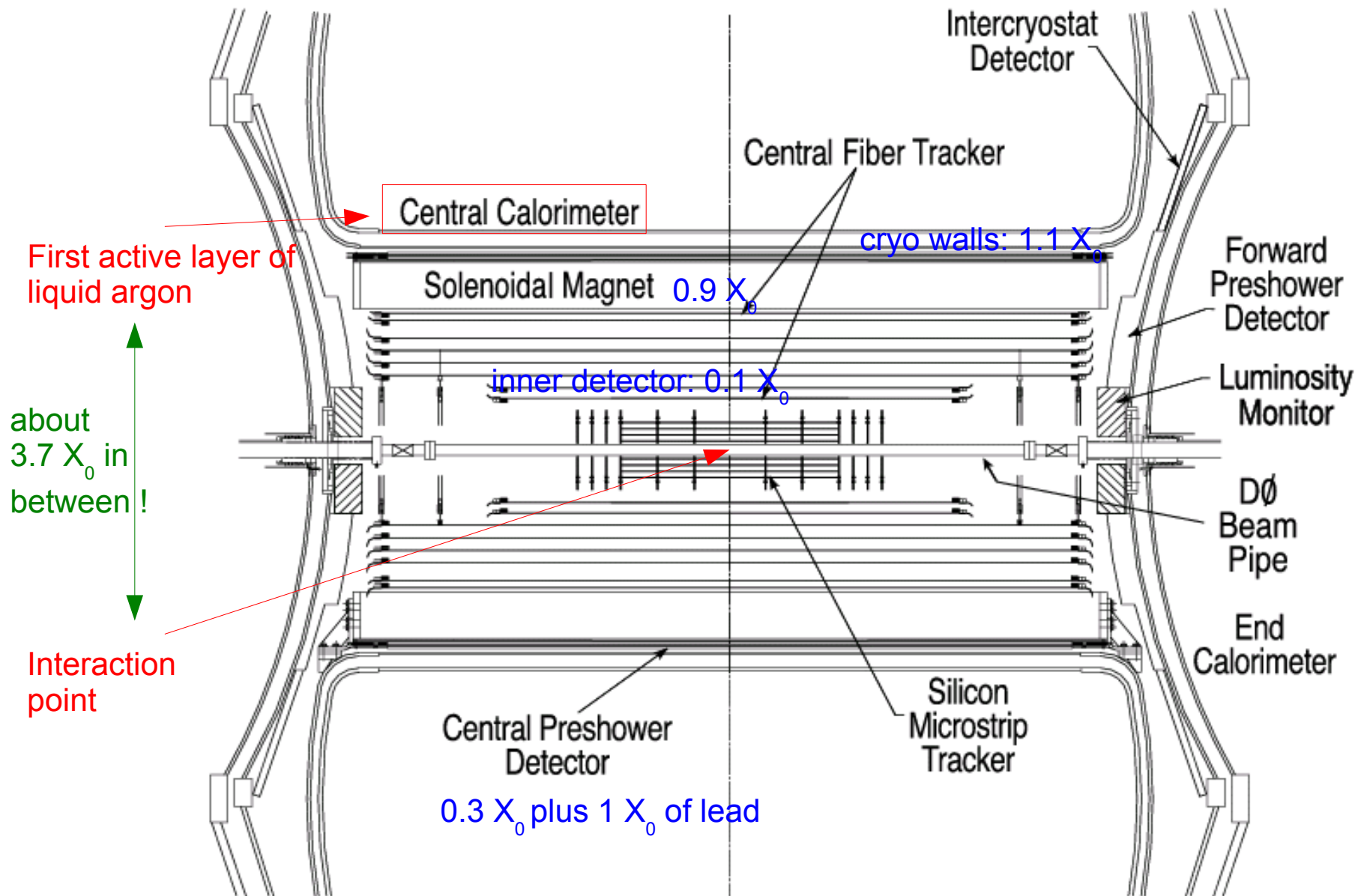


46000 cells

50 dead channels

- Liquid argon active medium and (mostly) uranium absorber
- Hermetic with full coverage : $|\eta| < 4$
- Segmentation (towers): $\Delta\eta \times \Delta\phi = 0.1 \times 0.1$
(0.05x0.05 in third EM layer, near shower maximum)

Keep in mind: the CAL is not alone !



Final electron energy scale calibration

AFTER calorimeter calibration, simulation of effect of inst. luminosity, corrections for dead material, modeling of underlying energy flow:

final electron energy response calibration, using $Z \rightarrow e e$, the known Z mass value from LEP and the standard “ f_z method”:

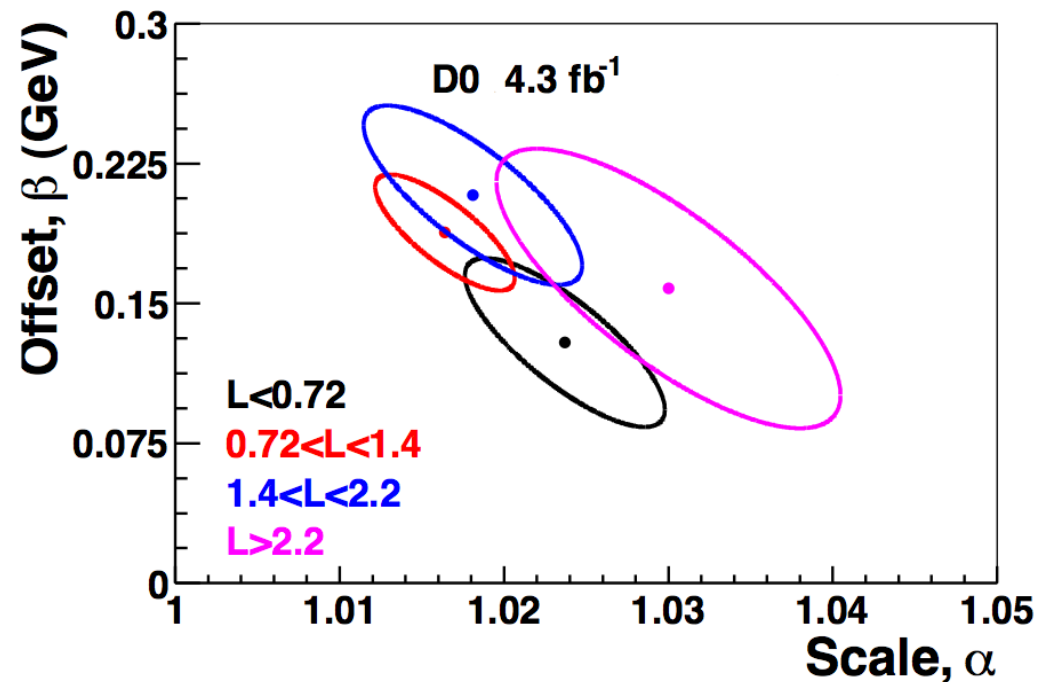
$$E_{\text{measured}} = \text{scale} * (E_{\text{true}} - 43 \text{ GeV}) + \text{offset} + 43 \text{ GeV}$$

We are effectively measuring m_W/m_Z .

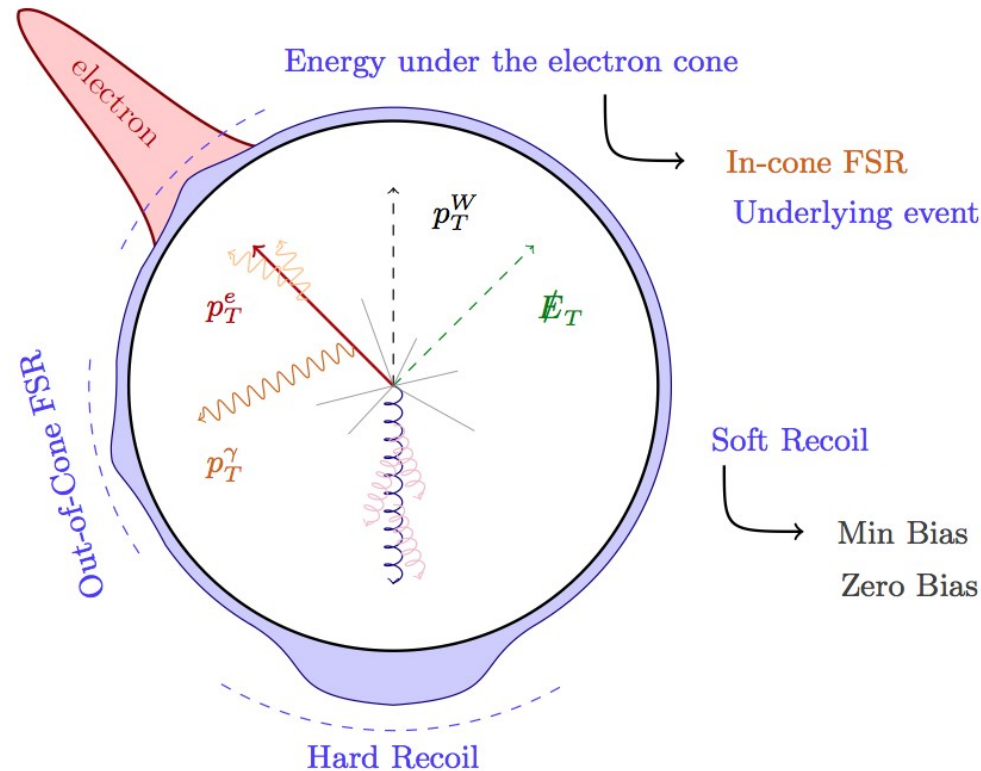
Use energy spread of electrons in Z decay (e.g. due to Z boost) to constrain scale *and* offset .

In a nutshell: the f_z observable allows you to split your sample of electrons from $Z \rightarrow e e$ into subsamples of different true energy; this way you can “scan” the electron energy response as a function of energy.

In Run IIb we do this separately for four bins of instantaneous luminosity (plot on the right).



Recoil model



$$\vec{u}_T = \vec{u}_T^{\text{HARD}} + \vec{u}_T^{\text{SOFT}} + \vec{u}_T^{\text{ELEC}} + \vec{u}_T^{\text{FSR}}$$

- \vec{u}_T^{HARD} models the hard hadronic energy from the W recoil.
- \vec{u}_T^{SOFT} models the soft hadronic activity from zero bias and minimum bias activity.
- $\vec{u}_T^{\text{ELEC}} = -\sum_e \Delta u_{\parallel} \cdot \hat{p}_T(e) + \vec{p}_T^{\text{LEAK}}$ models the recoil energy that was reconstructed under the electron cone, as well as any energy from the electron that leaked outside the cone.
- \vec{u}_T^{FSR} models the out-of-cone FSR that is reconstructed as hadronic recoil.

Recoil model

Have five **tunable parameters** in the recoil model that allow us to adjust the response to the hard recoil as well as the resolution (separately for hard and soft components):

$$\vec{u}_{T,smear}^{soft} = \sqrt{\alpha_{MB}} \vec{u}_T^{MB} + \vec{u}_T^{ZB}$$

model of spectator partons
(based on soft collisions
in collider data)

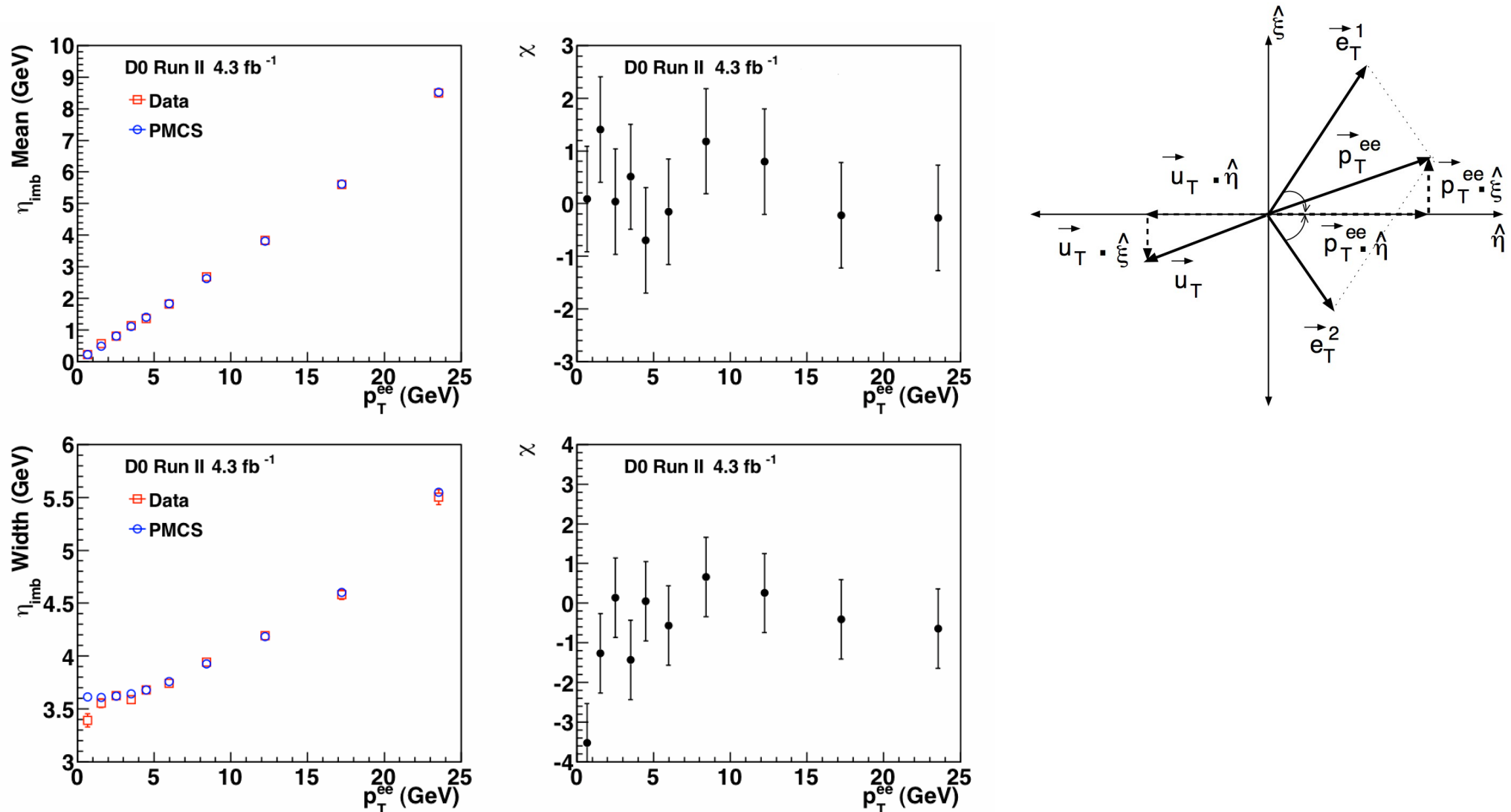
model of pileup/noise
(from collider data, random trigger)

$$u_{T,smear}^{\parallel,hard} = \left(R_A + R_B \cdot e^{-p_T^Z / \tau_{HAD}} \right) p_T^Z \left\langle \frac{u_T}{p_T^Z} \right\rangle^{\parallel} + S_A \left(u_T^{\parallel} - p_T^Z \left\langle \frac{u_T}{p_T^Z} \right\rangle^{\parallel} \right)$$

model of hard recoil response
(from detailed first-principles simulation)

Recoil calibration

Final adjustment of free parameters in the recoil model is done *in situ* using balancing in $Z \rightarrow e e$ events and the standard UA2 observables.



Electron energy resolution

Electron energy resolution is driven by two components:
sampling fluctuations and constant term

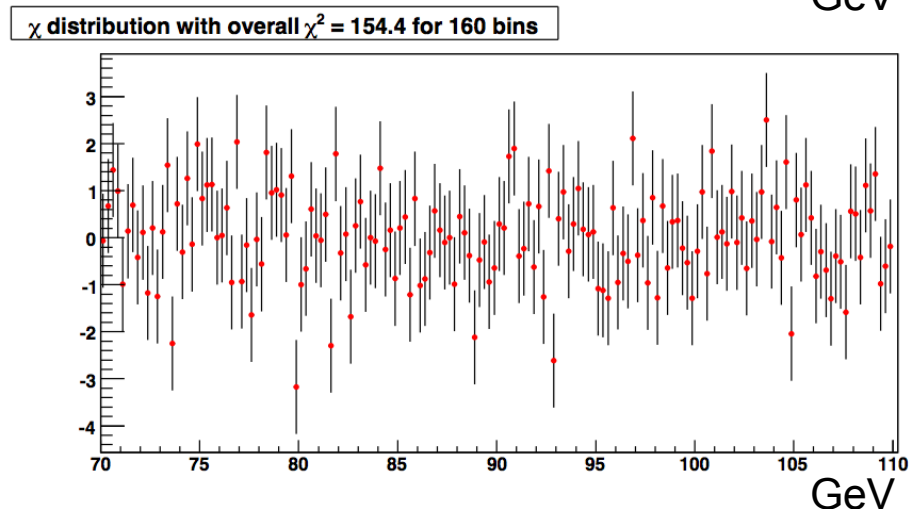
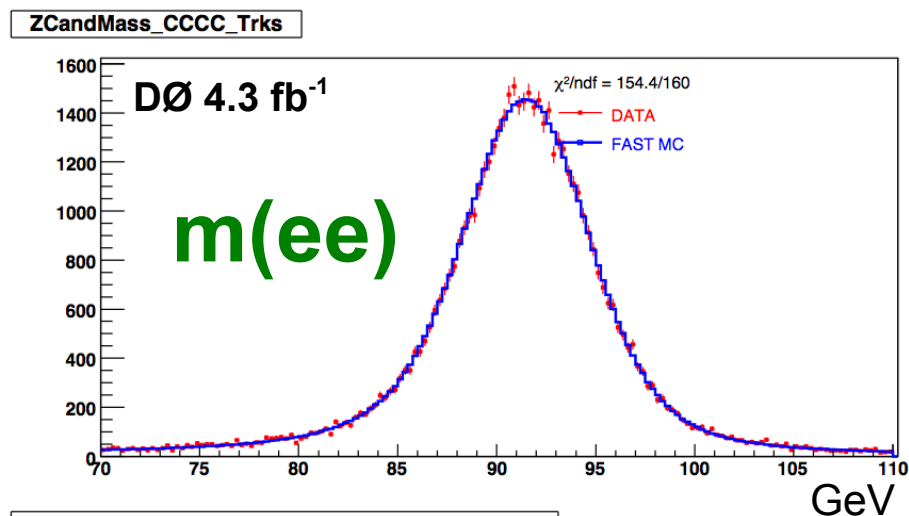
Sampling fluctuations are driven by sampling fraction of CAL modules (well known from simulation and testbeam) and by uninstrumented material. As discussed before, amount of material has been quantified with good precision.

Constant term is extracted from $Z \rightarrow e e$ data (essentially fit to observed width of Z peak).

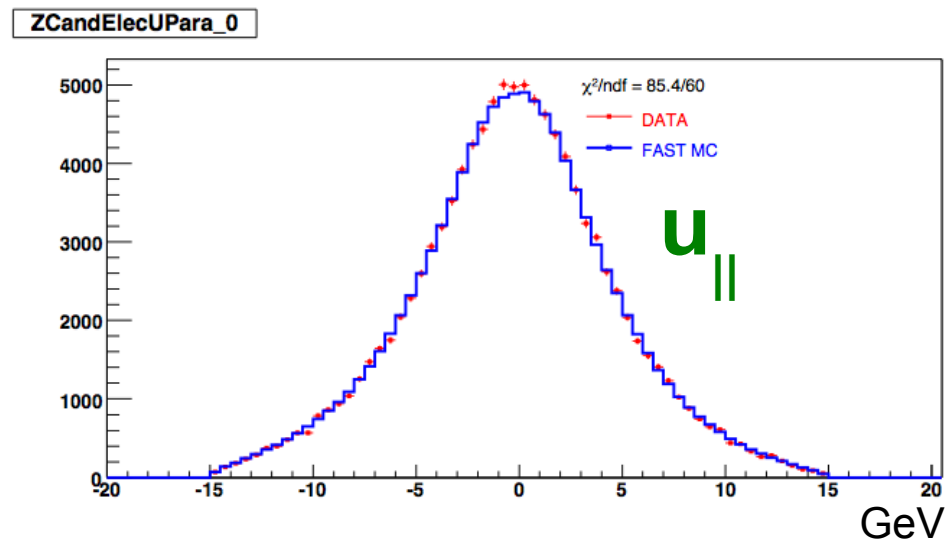
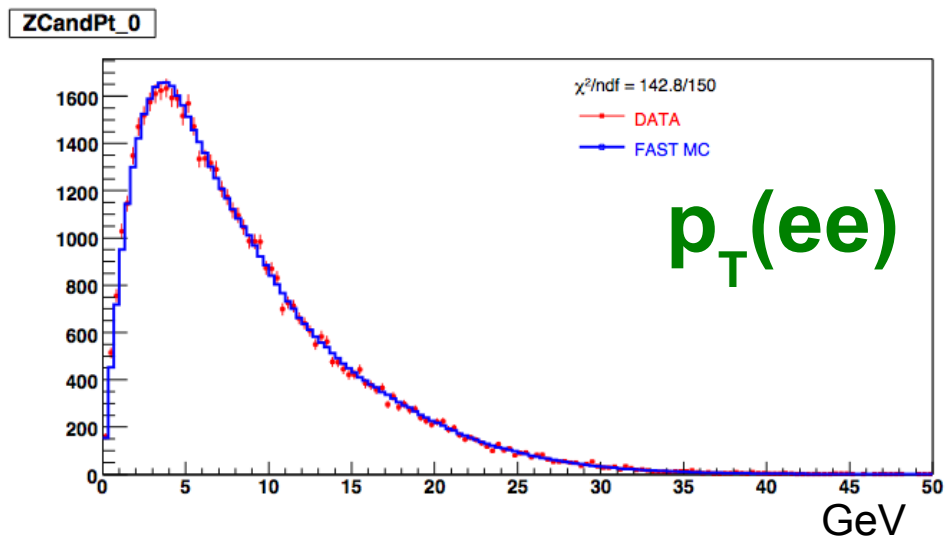
Result:

$$C = (2.00 \pm 0.07) \%$$

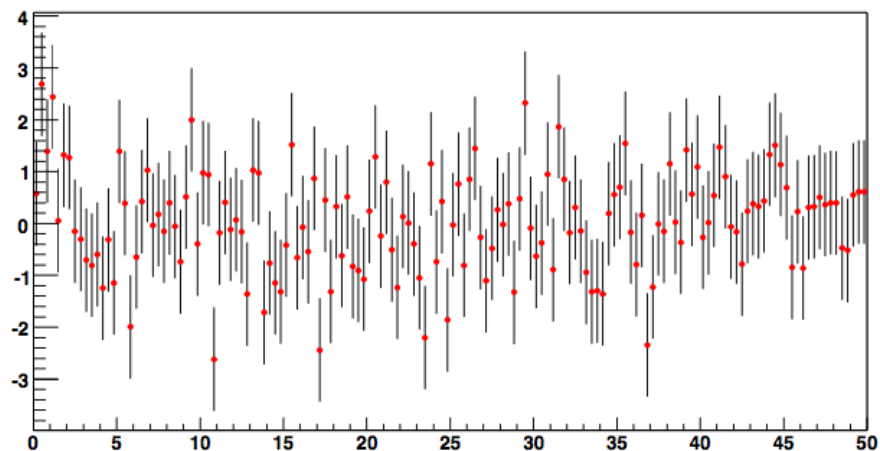
in excellent agreement with Run II design goal (2%)



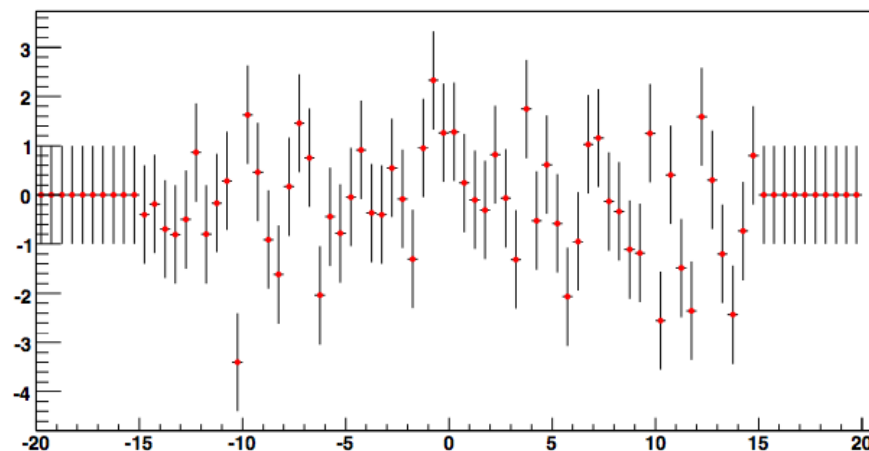
Z data



χ distribution with overall $\chi^2 = 142.8$ for 150 bins



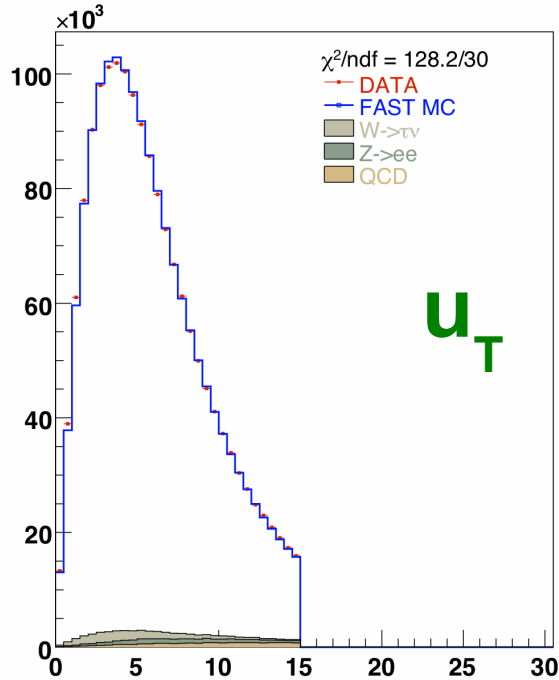
χ distribution with overall $\chi^2 = 85.4$ for 60 bins



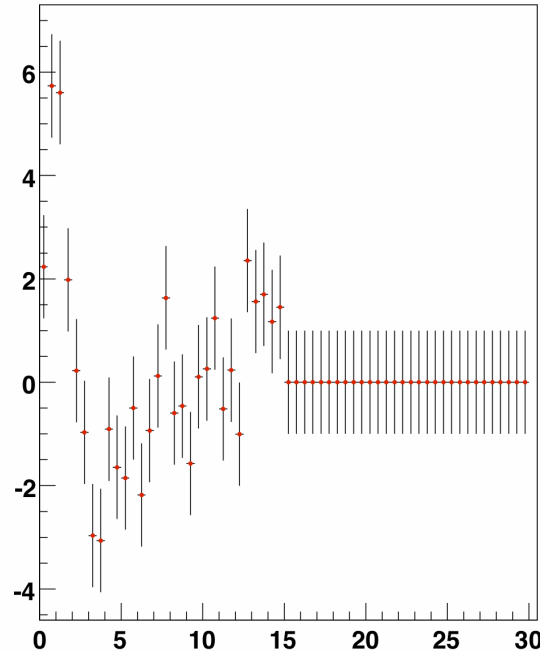
Good agreement between data and parameterised Monte Carlo.

W data

WCandRecoilPt_Spatial_Match_0

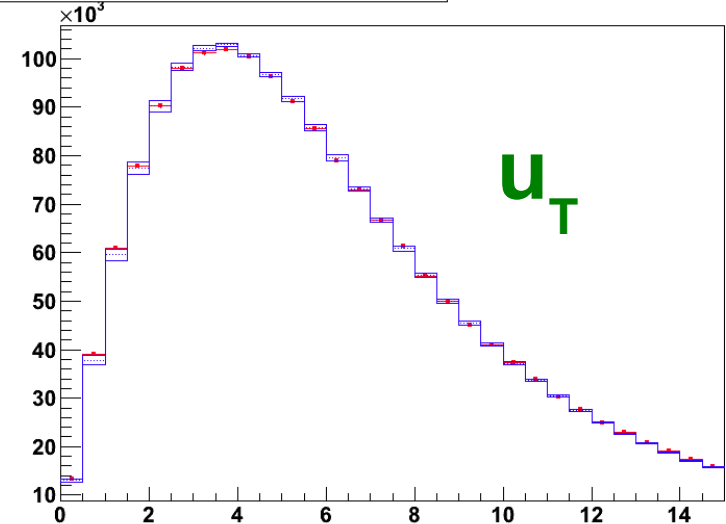


χ distribution with overall $\chi^2 = 128.2$ for 30 bins



Here the error bars only reflect the finite statistics of the W candidate sample.

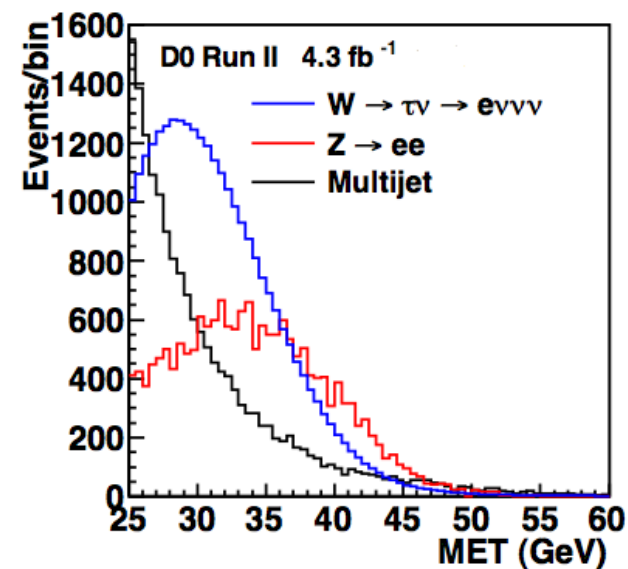
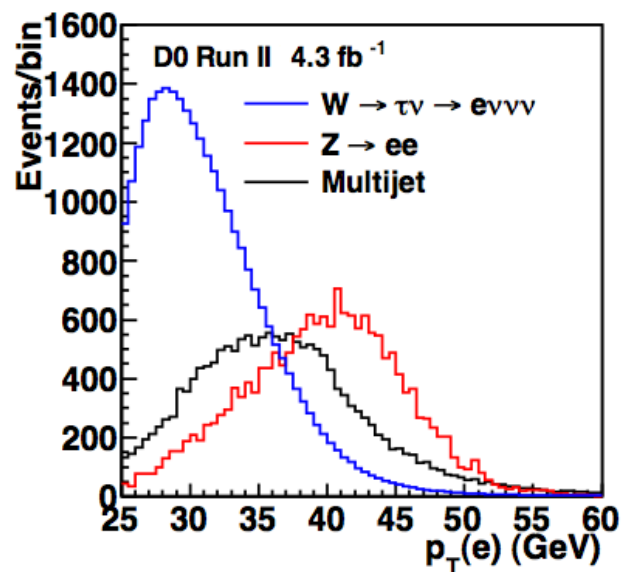
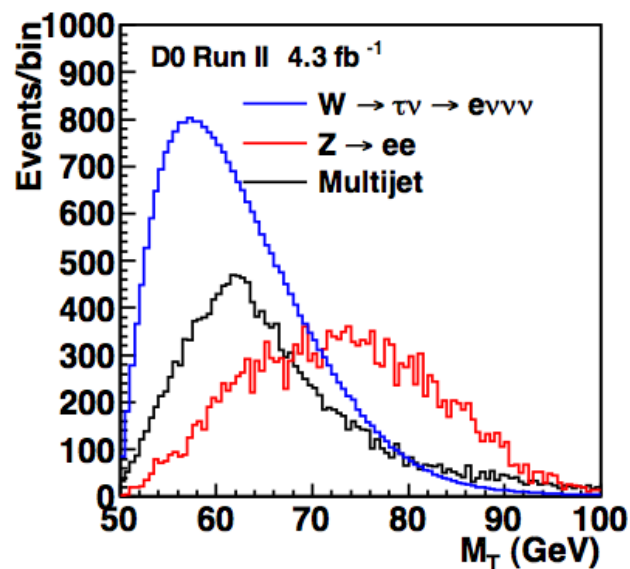
WCandRecoilPt_Spatial_Match_0



These are the same W candidates in the data. The blue band represents the uncertainties in the fast MC prediction due to the uncertainties in the recoil tune from the finite Z statistics.

Good agreement between data and parameterised Monte Carlo.

Backgrounds



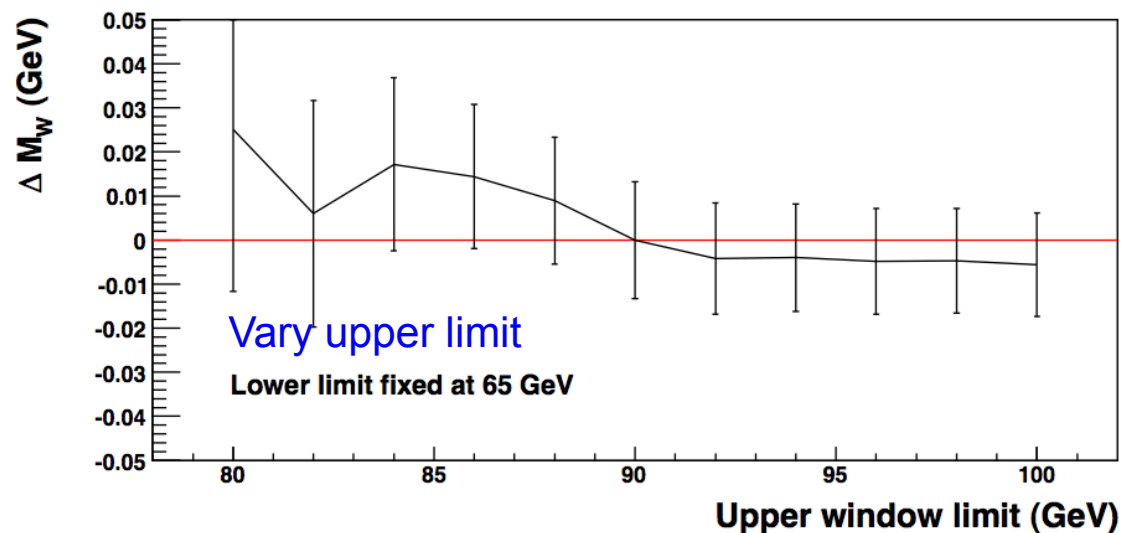
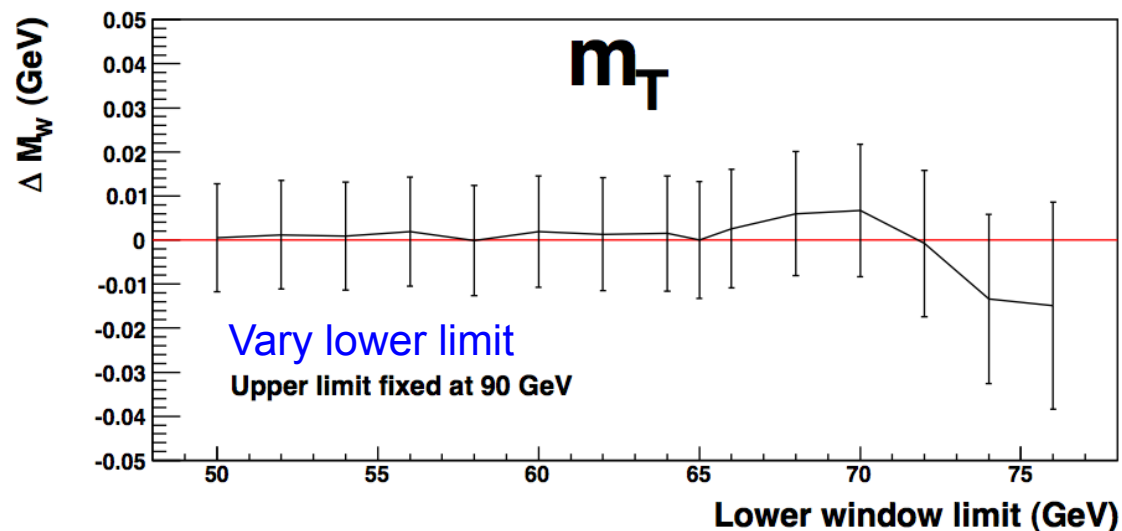
Summary of uncertainties

systematic uncertainties	Source	$\sigma(m_W)$ MeV m_T	$\sigma(m_W)$ MeV $p_T(e)$	$\sigma(m_W)$ MeV E_T
	Experimental			
	Electron Energy Scale	16	17	16
	Electron Energy Resolution	2	2	3
	Electron Energy Nonlinearity	4	6	7
	W and Z Electron energy loss differences	4	4	4
	Recoil Model	5	6	14
	Electron Efficiencies	1	3	5
	Backgrounds	2	2	2
	Experimental Total	18	20	24
	W production and decay model			
	PDF	11	11	14
	QED	7	7	9
	Boson p_T	2	5	2
	W model Total	13	14	17
	Total	22	24	29
statistical		13	14	15
total		26	28	33

Keep in mind that this analysis uses *only* Run IIb data, *i.e.* it is intended to be combined with our Run IIa result.
23 MeV uncertainty for the combination with Run IIa.

Consistency checks

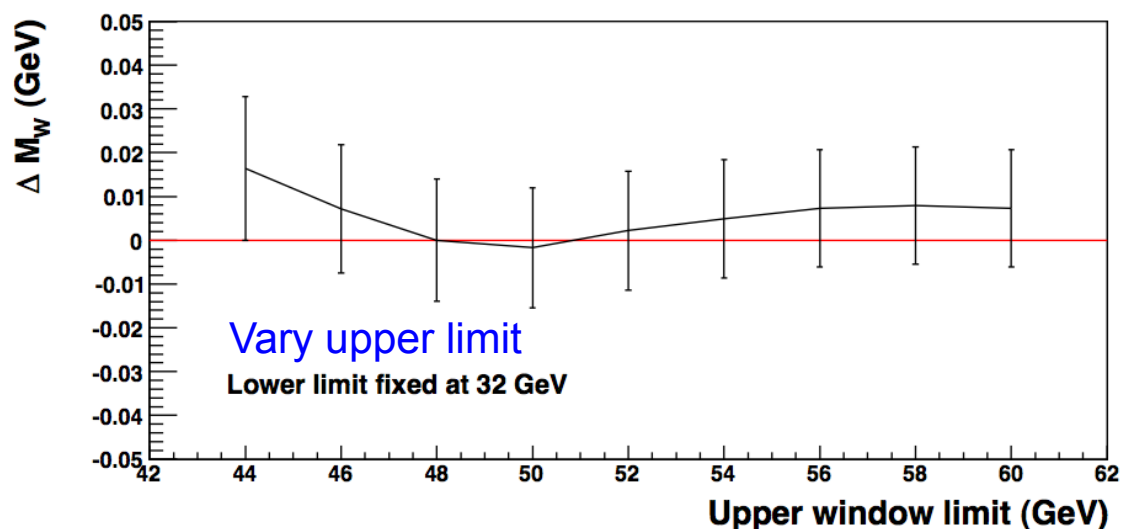
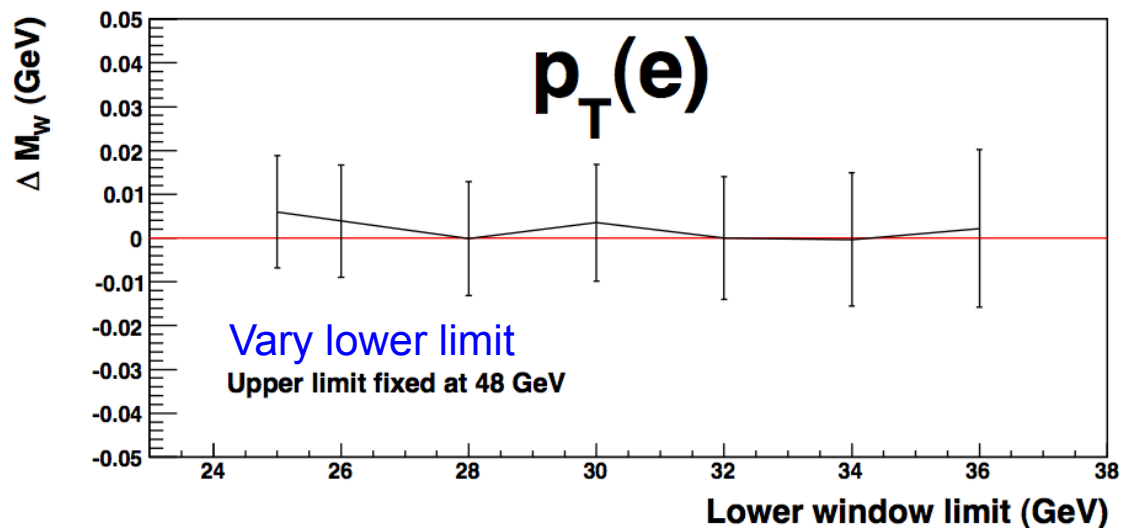
Vary the range used in the m_T fit:



Measurement is stable

Consistency checks

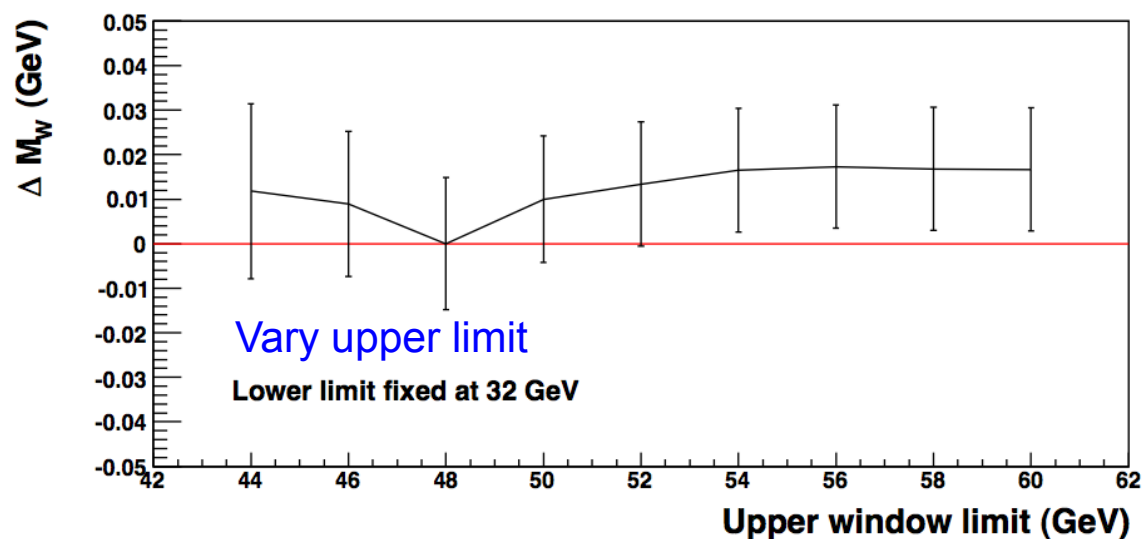
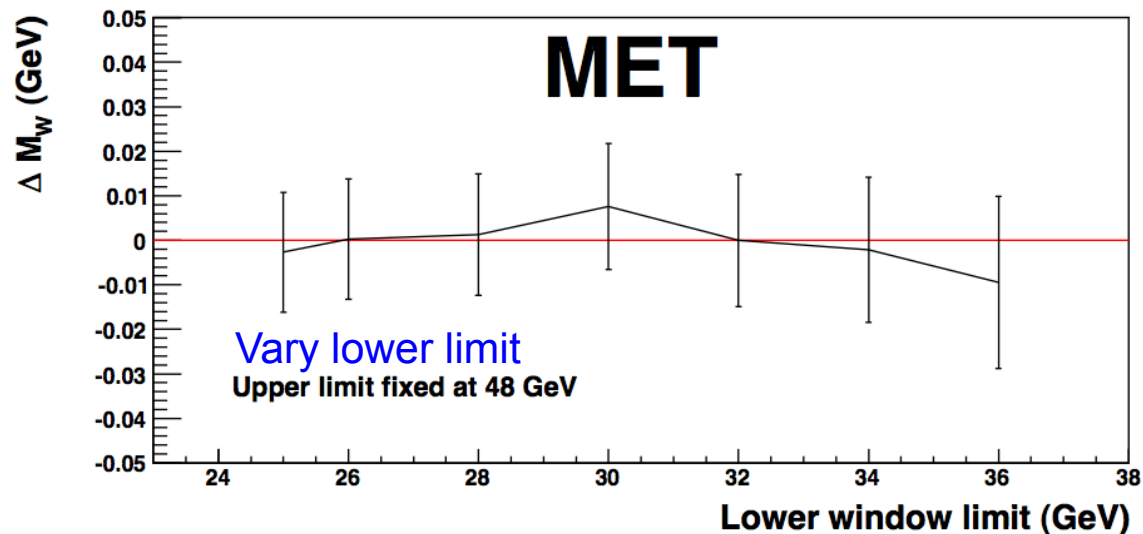
Vary the range used in the $p_T(e)$ fit:



Measurement is stable

Consistency checks

Vary the range used in the MET fit:

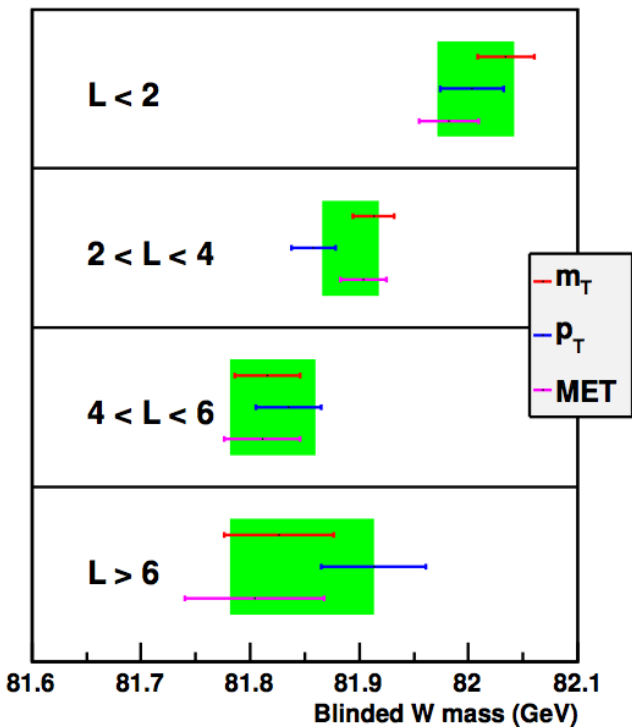


Measurement is stable

Consistency checks

Split data sample into four bins of instantaneous luminosity and measure W mass separately for each bin:

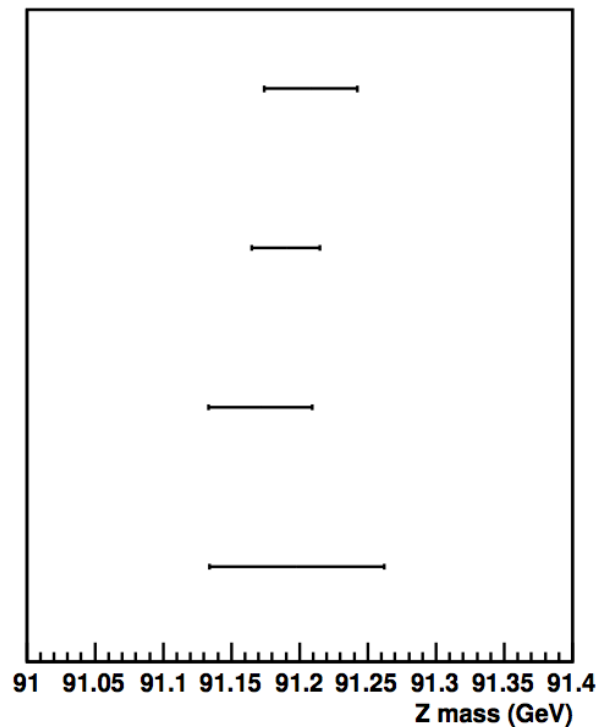
W



Error bars represent W statistics.

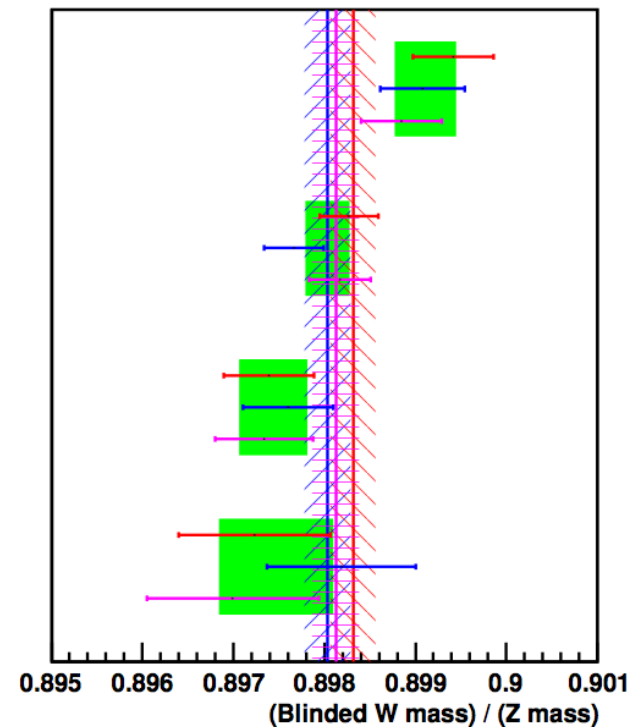
Green bands represent EM scale uncertainty (100 % correlated for m_T , p_T and MET).

Z



Sorry, still using blinded mass in these plots.
But it does not matter here ...
differences between observables and subsamples
are preserved by the blinding.

“W/Z”



Error bars represent W and Z statistics.

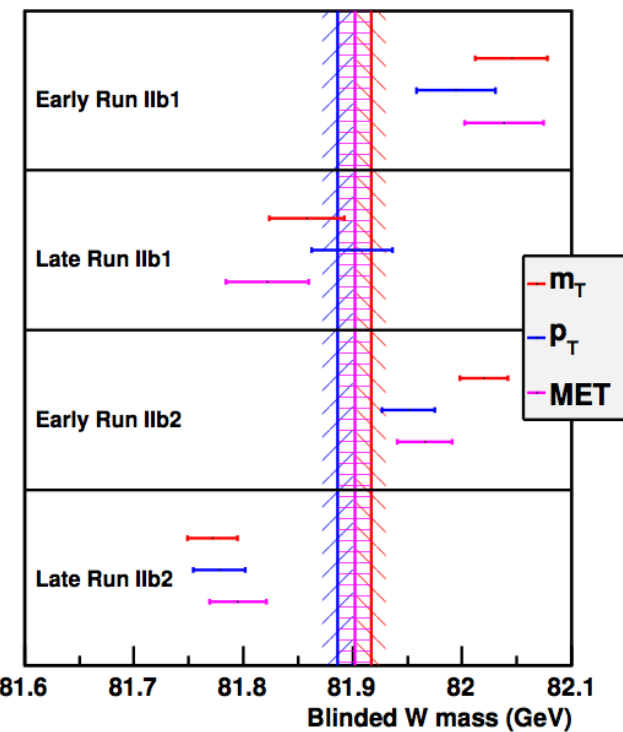
Green bands represent contribution from Z alone (100 % correlated for m_T , p_T and MET).

Mass ratio is stable with lumi.

Consistency checks

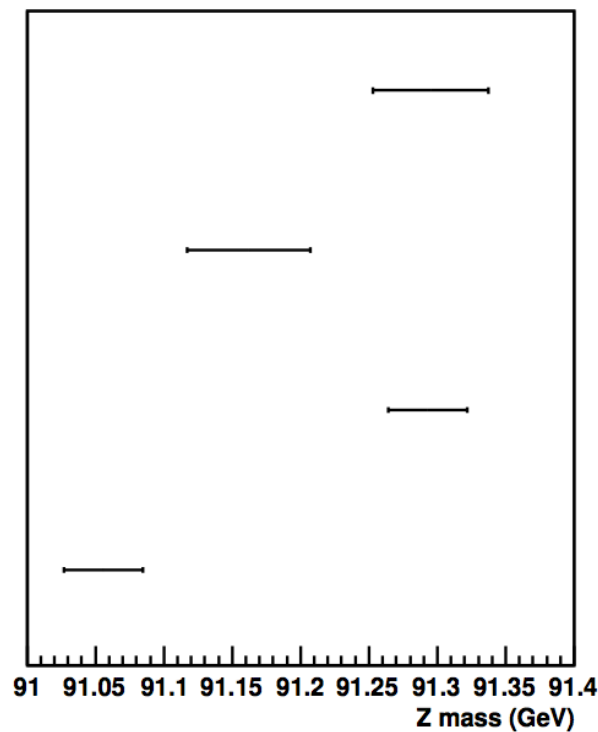
Split data sample into four data taking periods and measure W mass separately for each period:

W

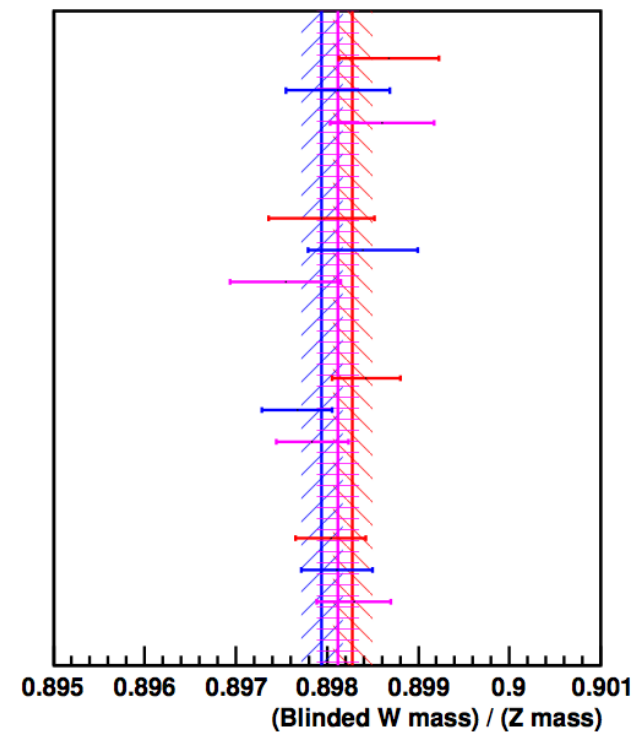


Error bars represent W statistics.

Z



“W/Z”



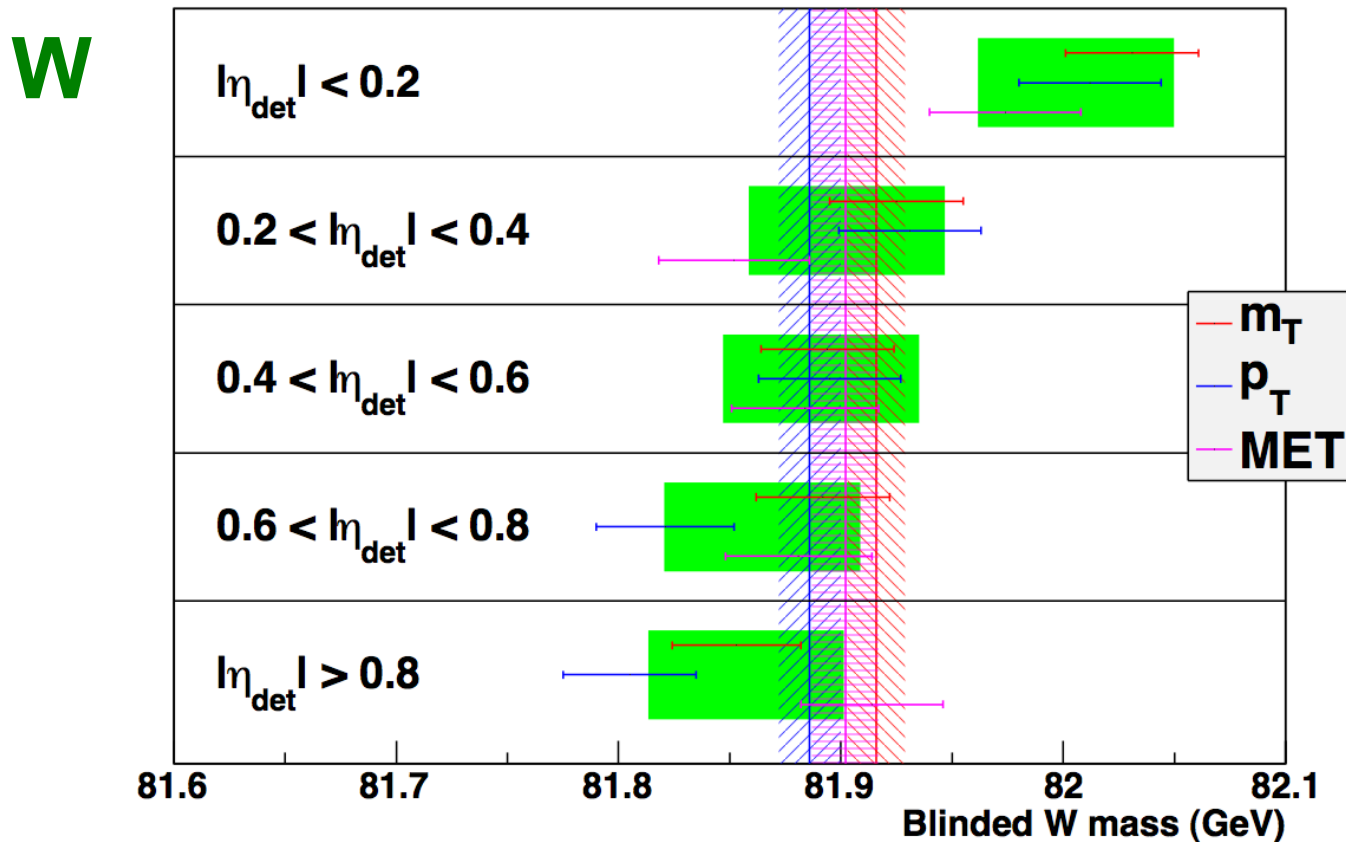
Error bars represent
W and Z statistics.

Mass ratio is stable over time.

These are just a few examples. Many more cross-checks have been performed.

Consistency checks

Split data sample into five bins of detector eta and measure W mass separately for each bin:



Error bars represent W statistics.

Green bands represent the part of the EM scale uncertainty that is uncorrelated from one eta bin to another (100 % correlated for m_T , p_T and MET).

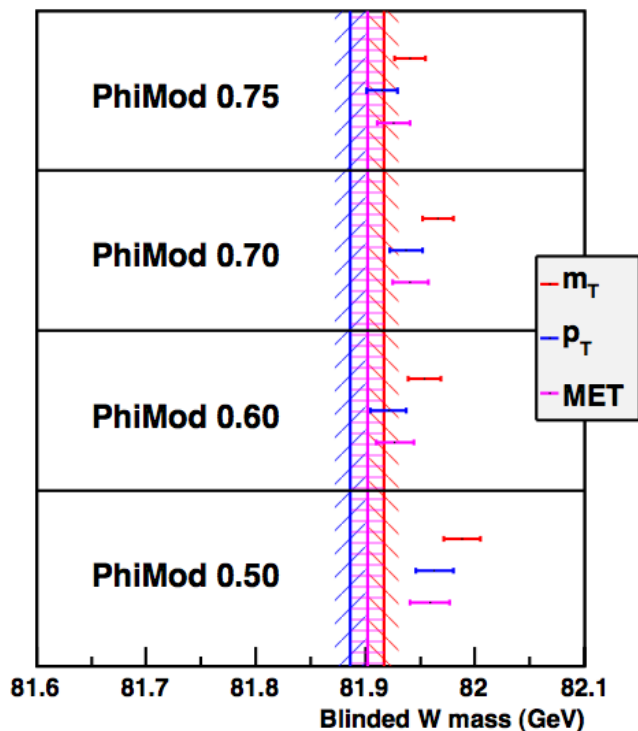
Sorry, still using blinded mass in these plots. But it does not matter here ... differences between observables and subsamples are preserved by the blinding.

Mass is stable with eta.

Consistency checks

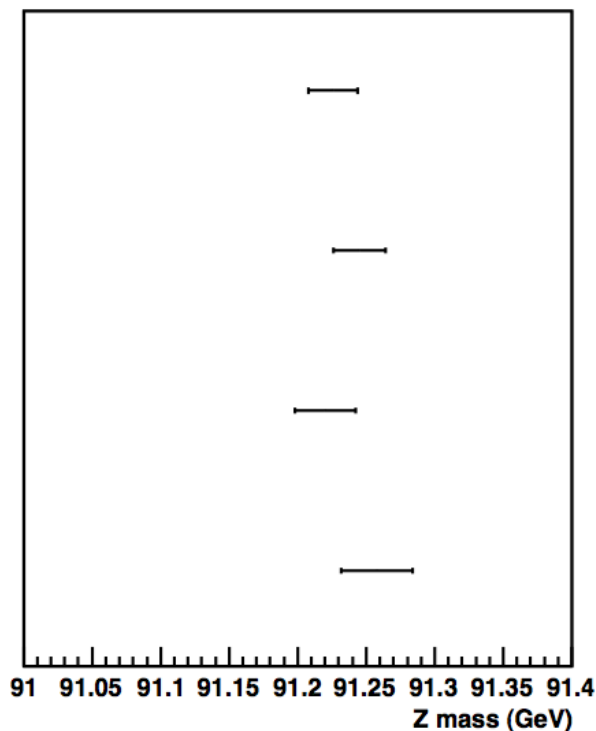
Vary phi fiducial cut. In default analysis, keep 80 % of acceptance. Here we test four tighter requirements.

W

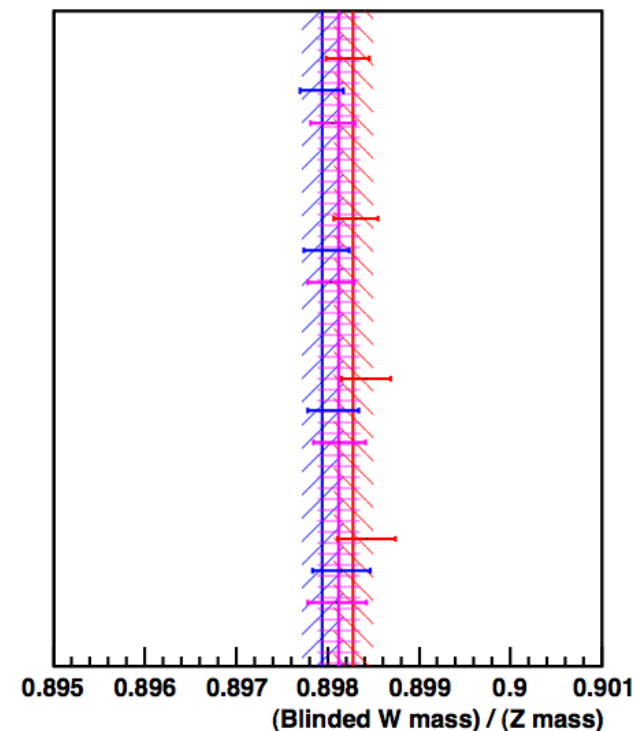


Error bars represent W statistics.

Z



“W/Z”



Error bars represent
W and Z statistics.

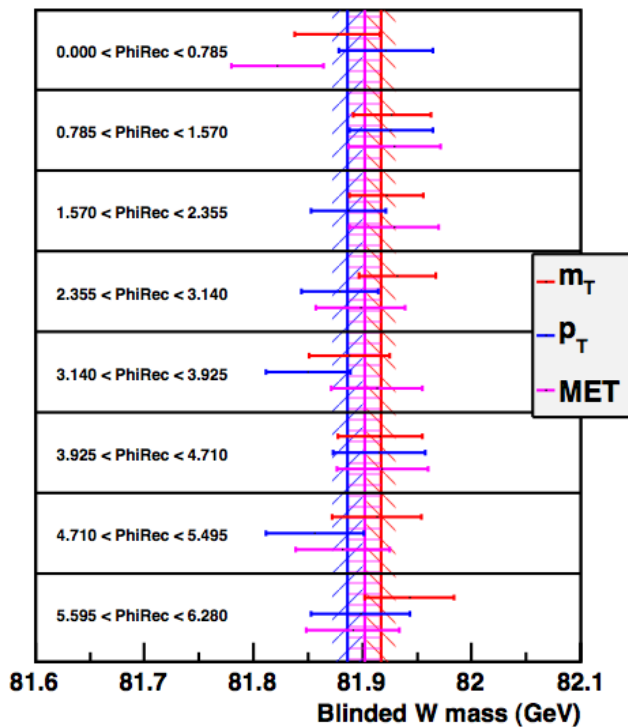
Sorry, still using blinded mass in these plots.
But it does not matter here ...
differences between observables and subsamples
are preserved by the blinding.

Mass ratio is stable with fiducial requirement

Consistency checks

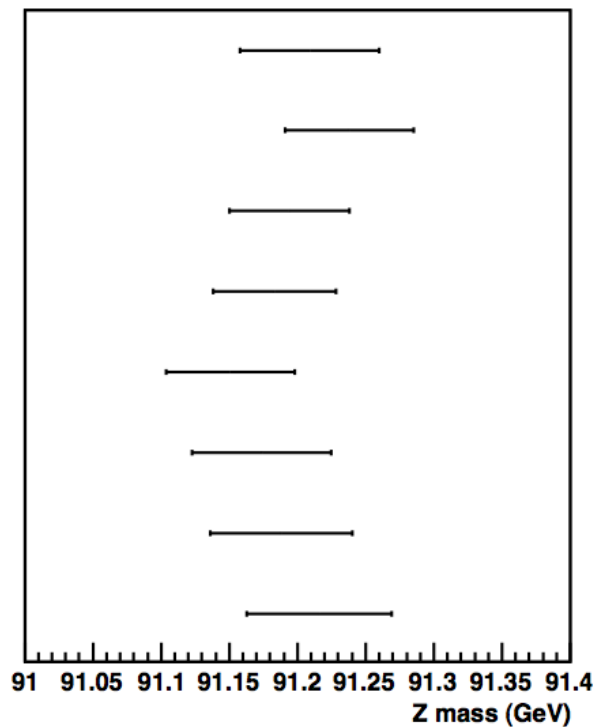
Split data sample into eight bins according to the direction in phi of the measured recoil vector, and measure W boson mass separately in each bin.

W

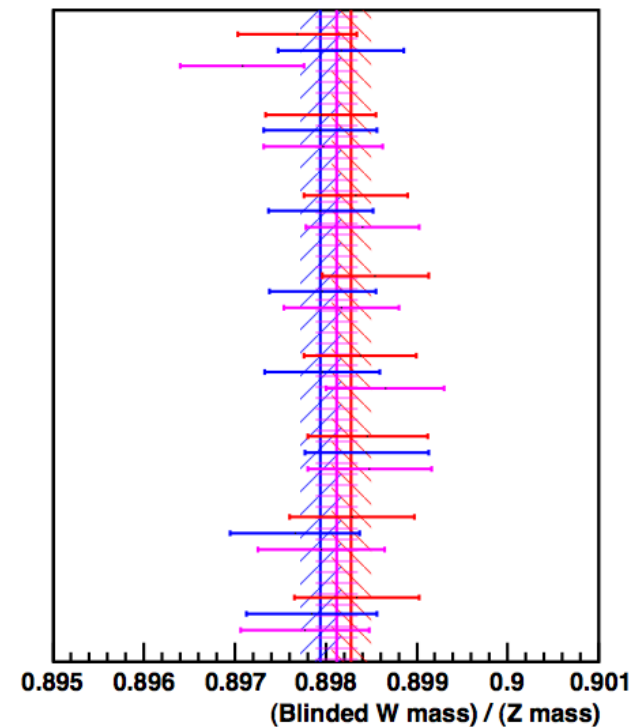


Error bars represent W statistics.

Z



“W/Z”



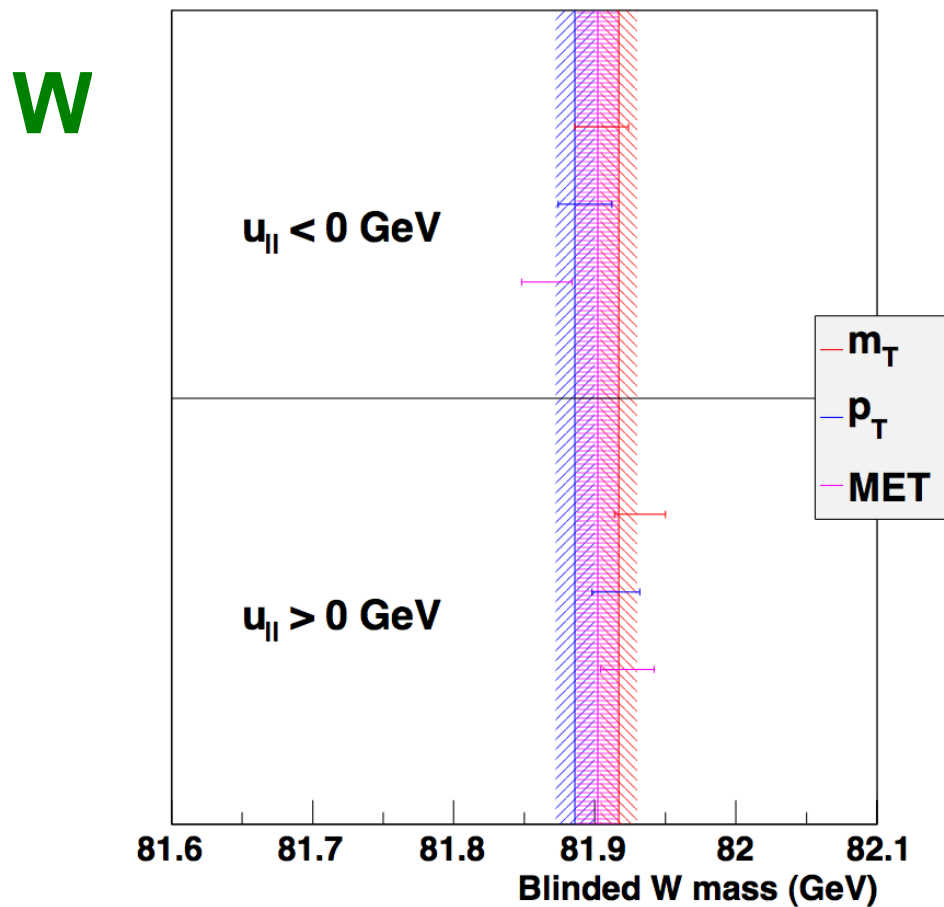
Error bars represent
W and Z statistics.

Sorry, still using blinded mass in these plots.
But it does not matter here ...
differences between observables and subsamples
are preserved by the blinding.

Mass ratio is stable with recoil phi.

Consistency checks

Split data sample into two bins of $u_{||}$ and measure W mass separately for each bin:



Error bars represent W statistics.

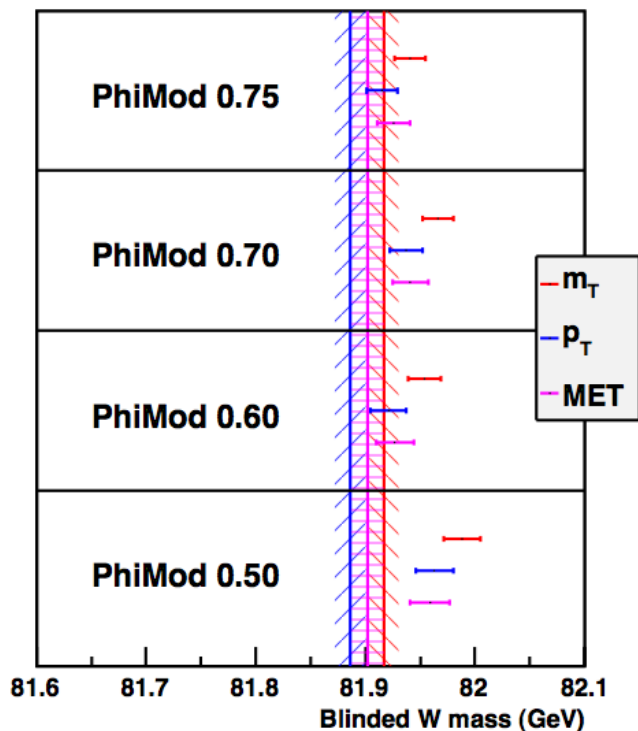
Sorry, still using blinded mass in these plots.
But it does not matter here ...
differences between observables and subsamples
are preserved by the blinding.

Mass is stable with $u_{||}$.

Consistency checks

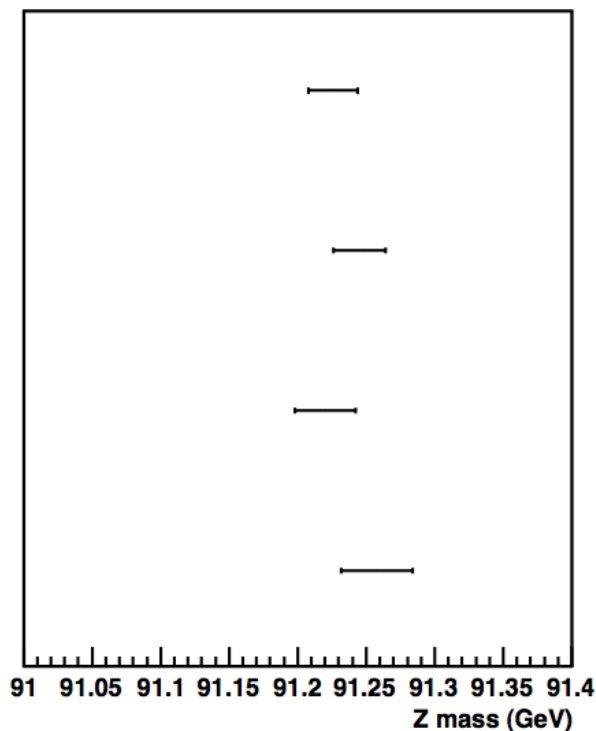
Vary phi fiducial cut. In default analysis, keep 80 % of acceptance. Here we test four tighter requirements.

W

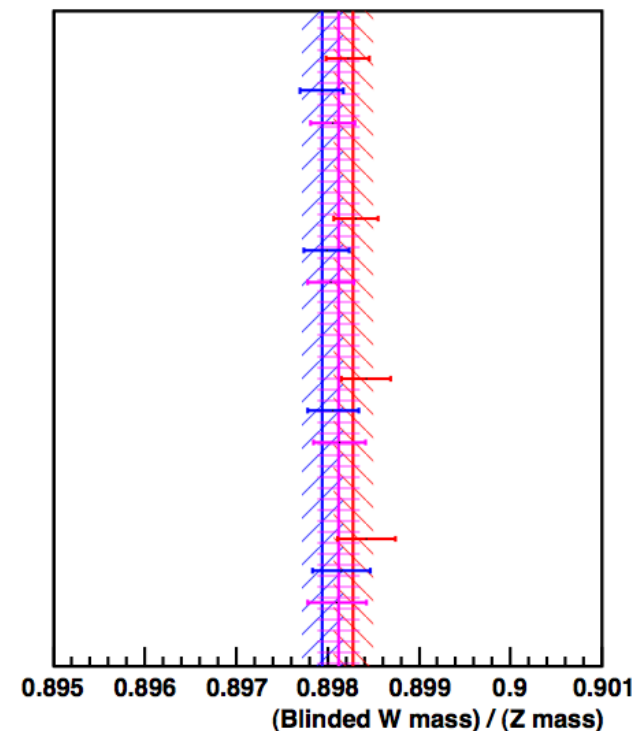


Error bars represent W statistics.

Z



“W/Z”



Error bars represent W and Z statistics.

Sorry, still using blinded mass in these plots.
But it does not matter here ...
differences between observables and subsamples
are preserved by the blinding.

Mass ratio is stable with fiducial requirement

Combination of the three observables

We take the results from the three observables (with their correlations) and combine them:

$$m_{\tau}: 80.371 \pm 0.013 \text{ (stat)} \pm 0.022 \text{ (syst)}$$

$$p_{\tau}^e: 80.343 \pm 0.014 \text{ (stat)} \pm 0.024 \text{ (syst)}$$

$$\text{MET: } 80.355 \pm 0.015 \text{ (stat)} \pm 0.029 \text{ (syst)}$$

$$\rho = \begin{pmatrix} \rho_{m_{\tau}m_{\tau}} & \rho_{m_{\tau}p_{\tau}^e} & \rho_{m_{\tau}\cancel{E}_T} \\ \rho_{m_{\tau}p_{\tau}^e} & \rho_{p_{\tau}^ep_{\tau}^e} & \rho_{p_{\tau}^e\cancel{E}_T} \\ \rho_{m_{\tau}\cancel{E}_T} & \rho_{p_{\tau}^e\cancel{E}_T} & \rho_{\cancel{E}_T\cancel{E}_T} \end{pmatrix} = \begin{pmatrix} 1.0 & 0.89 & 0.86 \\ 0.89 & 1.0 & 0.75 \\ 0.86 & 0.75 & 1.0 \end{pmatrix}$$

When considering only the uncertainties which are allowed to decrease in the combination (i.e. *not* QED and PDF), we find that the MET measurement has negligible weight. We therefore only retain p_{τ}^e and m_{τ} for the combination.

The combined result is:

$$\begin{aligned} M_W &= 80.367 \pm 0.013 \text{ (stat)} \pm 0.022 \text{ (syst)} \text{ GeV} \\ &= 80.367 \pm 0.026 \text{ GeV.} \end{aligned}$$

The probability to observe a larger spread between the three measurements than in the data is 5 %.

We further combine with our earlier Run II result (1 fb^{-1}) to obtain the new D0 Run II result:

$$\boxed{\phantom{M_W = 80.367 \pm 0.026 \text{ GeV}}}$$