# **HERWIRI2**:

# Exponentiated Electroweak Corrections in a Hadronic Event Generator



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#### **Vector Boson Production**

- Vector Boson Production is an important process at the LHC, and electro-weak radiative corrections will be needed to obtain measurements on the percent level.
- While studying these corrections using the state-of-the-art electro-weak corrections of Horace, we (Nadia Adam, Valerie Halyo, and S.Y.) found that the EW contribution to  $pp \to Z/\gamma^* \to f\overline{f}$  is typically several percent, requiring precise control if measurements become possible at the percent level, as anticipated.
- For precision calculations, multiple approaches and calculations provide valuable cross-checks. Also, it is desirable to have the QCD and QED corrections fully integrated in the same event generator, e.g. NLO EWK + NLO QCD.

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# QCD \( \omega \text{QED Exponentiation} \)

- Motivation: the successful application of YFS exponentiation to BHLUMI, BHWIDE, KK MC KORALZ, KORALW, and related programs to achieve high precision in LEP processes.
- These programs benefit from a very efficient representation of N-photon phase space with complete control over the soft and collinear singularities for arbitrary numbers of photons.
- Real and Virtual IR singularities cancel exactly to infinite order.
- The non-abelian extension should have the same advantages for N-gluon amplitudes The IR singularity cancelation is more complicated, but is still gauranteed at all orders.

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# The HERWIRI Project

- The class of programs based on this idea has been named HERWIRI, for High Energy Radiation With Infra-Red Improvements, a name acknowledging the fact that our present efforts build upon one of the leading shower generators, HERWIG.
- The structure is not tied to a particular shower, and our ultimate goal is a complete shower-generator based entirely on QCD $\otimes$ QED nonabelian exponentiation with exact  $\mathcal{O}(\alpha_s^2, \alpha_s \alpha, \alpha^2)$  residuals.
- The first program to be publicly released in this series was HERWIRI1, which applied the proposed exponentiation to the shower's splitting kernels.
- Work on incorporating  $\mathcal{O}(\alpha)$  (or better) EWK corrections in the same exponentiation paradigm began in parallel, and is close to the point of producing results. This program is called HERWIRI2. It is independent of HERWIRI1, although the two will eventually be combined.

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#### HERWIRI2

- The success of YFS exponentiation in the precision event generator  $\mathcal{KK}$  MC (S. Jadach, B.F.L. Ward, and Z. Was) for  $e^+e^- \to Z\gamma^* \to f\overline{f}$  provides a natural starting point for incorporating EWK corrections to the parton-level process.
- HERWIRI2 is a hybrid of  $\mathcal{KK}$  MC with a with hadronic event generator, HERWIG in its present incarnation.
- The two programs function largely independently:
  - HERWIG generates the parton momenta and shower.
  - $^{\circ}$   $\mathcal{KK}$  MC provides a more precise calculation of the hard process and generates multiple ISR and FSR photon emission.
- $\mathcal{KK}$  MC was designed to be upgradable to processes beyond just the  $e^+e^-$  scattering of interest at LEP: thus, the ability to select incoming quarks already exists.
- See S. Yost, V. Halyo, M. Hejna, and B.F.L. Ward, PoS (RADCOR 2011), 017 [arXiv:1201.0515].

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# KKMC

- $\mathcal{KK}$  MC is a precision event generator for  $e^+e^- \to f\overline{f} + n\gamma$ ,  $f = \mu, \tau, d, u, s, c, b$  for CMS energies from  $2m_{\tau}$  to 1 TeV. The precision tag for LEP2 was 0.2%.
- ISR and FSR  $\gamma$  emission is calculated up to  $\mathcal{O}(\alpha^2)$ , including interference.
- The MC structure is based on YFS exponentiation, including residuals calculated perturbatively to the relevant orders in  $\alpha^k L^l$ . ( $L = \ln(s/m_e^2)$ ). CEEX mode:  $\alpha, \alpha L, \alpha^2 L^2, \alpha^2 L$ .
- Exact collinear bremsstrahlung for up to three  $\gamma$ 's.
- $\mathcal{O}(\alpha)$  EWK corrections and more are included via DIZET 6.21.
- Beamstrahlung can be modeled over a wide range via a built-in or user-defined distribution.
- Final state hadronization is supported via JETSET.
- $\tau$  decay is simulated using TAUOLA.

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# **Coherent Exclusive Exponentiation**

- CEEX was introduced for pragmatic reasons, the traditional exponentiation (EEX) of spin-summed cross sections suffered from a proliferation of interference terms, limiting its ability to reach the desired 0.2% precision tag for LEP2.
- CEEX works at the level of spinor helicity amplitudes, greatly facilitating the calculation of effects such as ISR-FSR interference, which are included in  $\mathcal{KK}$  MC, and therefore HERWIRI2.
- CEEX is maximally exclusive: all real photons radiated are kept in the event record, no matter how soft or collinear. There is no need to "integrate out" a region of soft phase space because the exponentiated amplitudes are well-behaved at k=0. (HERWIRI1 implements this for soft gluons.)

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### **CEEX Formalism**

The CEEX cross section for  $q\overline{q} \to f\overline{f}$  has the form

$$\sigma = \frac{1}{\text{flux}} \sum_{n=0}^{\infty} \int dPS \, \rho_{\text{CEEX}}^{(n)}(\vec{p}, \vec{k})$$

where

$$\rho_{\text{CEEX}}^{(n)} = \frac{1}{n!} e^{Y(\vec{p}, E_{\min})} \frac{1}{4} \sum_{\text{hel.}} \left| \mathcal{M} \begin{pmatrix} \vec{p} & \vec{k} \\ \vec{\lambda} & \vec{\mu} \end{pmatrix} \right|^2$$

The YFS form factor is

$$Y(\vec{p}, E_{\min}) = Q_i^2 Y(p_1, p_2, E_{\min}) + Q_f^2 Y(p_3, p_4, E_{\min}) + Q_i Q_f Y(p_1, p_3, E_{\min})$$

$$+ Q_i Q_f Y(p_2, p_4, E_{\min}) - Q_i Q_f Y(p_1, p_4, E_{\min}) - Q_i Q_f Y(p_2, p_3, E_{\min})$$

$$Y(p_i, p_j, E_{\min}) = 2\alpha \tilde{B}(p_i, p_j, E_{\min}) + 2\alpha \operatorname{Re} B(p_i, p_j)$$

$$\tilde{B} = -\int_{k^0 \leqslant E_{\min}} \frac{d^3 \vec{k}}{8\pi^2 k^0} \left(\frac{p_i}{p_i \cdot k} - \frac{p_j}{p_j \cdot k}\right)^2, \quad B = \frac{i}{(2\pi)^3} \int \frac{d^4 k}{k^2} \left(\frac{2p_i + k}{2p_i \cdot k + k^2} - \frac{2p_j - k}{2p_j \cdot k - k^2}\right).$$

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#### **CEEX Formalism**

The n-photon helicity-spinor amplitude can be expanded in terms of order  $\alpha^r$  having the form

$$\mathcal{M}_{n}^{(r)} = \sum_{\mathcal{P}} \prod_{i=1}^{n} \mathcal{S}_{i}^{(\mathcal{P}_{j})} \left[ \beta_{0}^{(r)} \left( \vec{p}; X_{\mathcal{P}} \right) + \sum_{j=1}^{n} \frac{\beta_{1}^{(r)} \left( \vec{p} \cdot k; X_{\mathcal{P}} \right)}{\mathcal{S}_{j}^{(\mathcal{P}_{j})}} \right]$$

$$+ \cdots + \sum_{1 < j_1 < \cdots < j_n} \frac{\beta_n^{(r)} \begin{pmatrix} \vec{p} & \vec{k} \\ \vec{\lambda} & \vec{\mu} \end{pmatrix}}{\mathcal{S}_{j_1}^{(\mathcal{P}_{j_1})} \cdots \mathcal{S}_{j_n}^{(\mathcal{P}_{j_n})}}$$

with residual spinor amplitudes  $eta_i^{(r)}$  and complex soft photon factors  $\mathcal{S}_j$  with the property

$$\left| \mathcal{S}_j^{(\mathcal{P}_j)} \right| = -2\pi\alpha Q^2 \left( \frac{p_a}{p_a \cdot k_j} - \frac{p_b}{p_b \cdot k_j} \right)^2$$

where  $Q, p_a, p_b$  belong to the initial or final fermions depending on the partition  $\mathcal{P}_i$ .

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#### **ElectroWeak Corrections**

KK MC incorporates the DIZET library (version 6.2) from the semi-analytical program ZFITTER by A. Akhundov, A. Arbuzov, M. Awramik, D. Bardin, M. Bilenky, P. Christova, M. Czakon, A. Frietas, M. Gruenewald, L. Kalinovskaya, A. Olchevsky, S. Riemann, T. Riemann.

• The  $\gamma$  and Z propagators are multiplied by vacuum polarization factors:

$$H_{\gamma} = \frac{1}{2 - \Pi_{\gamma}}, \qquad H_{Z} = 4\sin^{2}(2\theta_{W}) \frac{\rho_{EW}G_{\mu}M_{Z}^{2}}{8\pi\alpha\sqrt{2}}.$$

 Vertex corrections are incorporated into the coupling of Z to f via form factors in the vector coupling:

$$g_V^{(Z,f)} = \frac{T_3^{(f)}}{\sin(2\theta_W)} - Q_f F_{\mathbf{v}}^{(f)}(s) \tan \theta_W.$$

 Box diagrams contain these plus a new angle-dependent form-factor in the doubly-vector component:

$$g_V^{(Z,i)}g_V^{(Z,f)} = \frac{T_3^{(i)}T_3^{(f)} - 2T_3^{(i)}Q_fF_{\mathbf{v}}^{(f)}(s) - 2Q_iT_3^{(f)}F_{\mathbf{v}}^{(i)}(s) + 4Q_iQ_fF_{\mathrm{box}}^{(i,f)}(s,t)}{\sin^2(2\theta_W)}.$$

The correction factors are calculated at the beginning of a run and stored in tables.

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# Combining $\mathcal{KK}$ MC with a Shower

- The Drell-Yan cross section with multiple-photon emission can be expressed as an integral over the parton-level process  $q_i(p_1)\overline{q}_i(p_2) \to f(p_3)\overline{f}(p_4) + n\gamma(k)$ , integrated over phase space and summed over photons.
- The parton momenta  $p_1, p_2$  are generated using parton distribution functions giving a process at CMS energy q and momentum fractions  $x_1, x_2$  such that  $q^2 = x_1 x_2 s$ :

$$\sigma_{\text{DY}} = \int \frac{dx_1}{x_1} \frac{dx_2}{x_2} \sum_{i} f_i(q, x_1) f_{\bar{i}}(q, x_2) \sigma_i(q^2) \delta(q^2 - x_1 x_2 s),$$

where the final state phase space includes  $p_3, p_4$  and  $k_i$ ,  $i = 1, \dots, n$  and multiple gluon radiation + hadronization is included through a shower.

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# Combining $\mathcal{KK}$ MC with a Shower

- HERWIG generates the hard process at Born level and passes it through the shower routines. The event record is passed to HERWIRI2.
- HERWIRI2 finds the  $Z/\gamma^*$  and the partons interacting with it in the event record. The initial partons define  $p_1$ ,  $p_2$ , which are transformed to the CM frame and projected on-shell to create a starting point for  $\mathcal{KK}$  MC.
- $\mathcal{KK}$  MC generates the final fermion momenta  $p_3, p_4$  and photons  $k_i$  (both ISR and FSR.) The generated particles are transformed back to the lab frame and placed in the event record.
- This HERWIRI2 weight is a product of the HERWIG and  $\mathcal{KK}$  MC weights with a common factor removed and appropriate additional factors required because the scale and incoming fermion vary in  $\mathcal{KK}$  MC.

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# MC Weights

The DY cross section in HERWIG can be expressed as

$$\sigma_{\text{DY}} = \int \frac{dx_1}{x_1} \frac{dx_2}{x_2} \sum_{i} f_i(q, x_1) f_{\bar{i}}(q, x_2) \sigma_i(q^2) \delta(q^2 - x_1 x_2 s) 
= \int_{q_{\text{min}}}^{q_{\text{max}}} dq P(q) \int_{q^2/s}^{1} \frac{dx_1}{x_1} \sum_{i} P_i \quad W_{\text{HW}}^{(i)}(q^2, x_1) 
= \langle W_{\text{HW}} \rangle$$

where P(q) is a normalized, integrable, crude probability distribution for q,  $P_i$  is the crude probability of generating parton i, and  $W_{\rm HW}$  is the HERWIG event weight. This weight depends only on the hard Born cross section and is not altered by the shower.

$$P(q) = \frac{1}{2} [P_{\gamma}(q) + P_{Z}(q)], \qquad P_{\gamma}(q) = \frac{N_{\gamma}}{q^4}, \qquad P_{Z}(q) = \frac{N_{Z}q}{(q^2 - M_{Z}^2) + \Gamma_{Z}^2 M_{Z}^2}$$

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# The HERWIG Event Weight

The HERWIG event weight is

$$W_{\rm HW} = \sum_{i} W_{\rm HW}^{(i)}, \qquad W_{\rm HW}^{(i)} = \frac{1}{P(q)} f_i(q, x_1) f_{\bar{i}}(q, x_2) \ln\left(\frac{s}{q^2}\right) \sigma_{\rm HW}^{(i)}(q^2)$$

and the corresponding probability for selecting parton i is

$$P_i = W_{\rm HW}^{(i)}/W_{\rm HW}$$

 We have chosen to introduce EW corrections in a "minimally invasive" way, incorporating them in a form factor

$$F_{EW}^{(i)}(q^2) = \frac{\sigma_{KK}^{(i)}(q^2)}{\sigma_{Born}^{(i)}(q^2)}$$

•  $\mathcal{KK}$  MC will calculate the EW form factor, and multiply it by the Herwig Born cross section.  $\sigma_{\mathrm{HW+EW}} = \langle W_{\mathrm{Tot}} \rangle$ ,  $W_{\mathrm{Tot}} = F_{EW}^{(i)}(q^2)W_{\mathrm{HW}}$ .

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# KK MC Generator Structure

• The  $\mathcal{KK}$  MC cross section is calculated using a "primary distribution"

$$\frac{d\sigma_{\text{Pri}}^{(i)}(s,v)}{dv} = \sigma_{\text{Born}}^{(i)}(s(1-v))\frac{1}{2}\left(1 + \frac{1}{\sqrt{1-v}}\right)\overline{\gamma}_i v^{\overline{\gamma}_i - 1} v_{\text{min}}^{\gamma_i - \overline{\gamma}_i}$$

with

$$\gamma_i = \frac{2\alpha}{\pi} Q_i^2 \left[ \ln \left( \frac{s}{m_i^2} \right) - 1 \right], \qquad \overline{\gamma}_i = \frac{2\alpha}{\pi} Q_i^2 \ln \left( \frac{s}{m_i^2} \right)$$

to generate the factor v giving the fraction of s remaining after ISR photon emission,  $s_X = s(1-v)$ .

The KK MC cross section is

$$\sigma(q^2) = \int d\sigma_{\text{Pri}} \frac{d\sigma_{\text{Cru}}}{d\sigma_{\text{Pri}}} \frac{d\sigma_{\text{Mod}}}{d\sigma_{\text{Cru}}} = \sigma_{\text{Pri}} \langle W_{\text{Cru}} W_{\text{Mod}} \rangle.$$

 $W_{\rm Cru}$  is calculated during ISR generation and  $W_{\rm Mod}$  is generated after  $s_X$  is available.

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#### Combined Generator HERWIRI2

We want to use HERWIG and KK MC together to calculate

$$\sigma_{\text{Tot}} = \left\langle W_{\text{HW}} \frac{\sigma_i(q^2)}{\sigma_{\text{Born}}^{(i)\star}(q^2)} \right\rangle = \left\langle W_{\text{HW}} \sigma_{\text{Pri}}^{(i)}(q^2) \frac{W_{\text{Cru}}^{(i)} W_{\text{Mod}}^{(i)}}{\sigma_{\text{Born}}^{(i)\star}(q^2)} \right\rangle,$$

- This average *could* be calculated using a joint probability distribution for q and v,  $D(q,v) = P(q)d\sigma_{\rm Pri}/dv$ , with P(q) from HERWIG.
- An adaptive MC (S. Jadach's FOAM) could calculate the normalization of the distribution at the beginning of the run, in a similar manner to how KK MC presently integrates the one-dimensional primary distribution. In fact, to account for beamsstrahlung, KK MC permits such a distribution, in up to three variables, to be introduced by the user.
- As a first step, we have tried to run HERWIRI2 using  $\mathcal{KK}$  MC's one-dimensional primary distribution. This requires fixing an overall scale  $q_0$  to initialize  $\mathcal{KK}$  MC (e.g.,  $q_0 = M_Z$ ).

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#### **HERWIRI2** Without ISR

- HERWIRI2 is presently in testing. All results here are very preliminary.
- Turning off ISR is useful as a first test because the weights simplify: Since v=0, there are no scale shifts in the weights, leading to a much narrower weight distribution.
- A short test run (100,000 events) with 4 TeV proton beams, CT10 PDFs, and generated CMS energies between 30 and 300 GeV, lepton  $P_T>10$  GeV with ISR off gives cross sections

HERWIG CS 
$$1149 \pm 3 \text{ pb}$$
  
HERWIRI2 CS  $1239 \pm 4 \text{ pb}$  (+8%)

- We find an increase of 8% from EW corrections with ISR only.
- An average of 0.60 photons per event is generated, with an average total energy of 1.46 GeV.

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#### HERWIRI2 with ISR

- With ISR on, there is a much broader weight distribution.
- The cross section is  $1278 \pm 43$  pb, 11% showing an additional 3% effect from ISR.

HERWIG		$1149\pm3~\mathrm{pb}$	
HERWIRI2	No ISR	$1238\pm4~\mathrm{pb}$	(+8%)
HERWIRI2	With ISR	$1278\pm43~\mathrm{pb}$	(+11%)

- There are an average of 0.42 ISR photons per event, with an average total energy of 0.62 GeV.
- There are an average of 0.62 FSR photons per event, with an average total energy of 1.15 GeV.
- The large weight variance an issue: The fixed initialization scale creates a wide weight distribution. It appears this will just be a stop-gap until a better primary distribution is introduced.

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# Summary

- HERWIRI2 is the first implementation of CEEX in a hadronic context.
- HERWIRI2 includes multi-photon emission from both the initial and final states in Z production, with order  $\alpha$  EW corrections.
- The effect of ISR and FSR are separately expected to enter at the level of several percent, dependent on cuts, making them essential for precision calculations.
- The program is still being refined to improve the weight distribution and efficiency.
- Comparisons with other hadronic/EW MC's will be in order once HERWIRI2 passes all its internal tests.
- HERWIRI2 is a step toward our goal of an event generator based on nonabelian QED $\otimes$ QCD exponentiation and exact  $\mathcal{O}(\alpha_s^2, \alpha_s \alpha, \alpha^2)$  residuals.

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