

Constraining CP violation in neutral meson mixing with theory input

Sascha Turczyk

Work in collaboration with M. Freytsis and Z. Ligeti [1203.3545 hep-ph]
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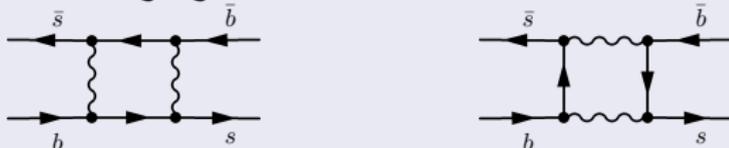
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Neutral Meson Oscillation

Description

- $\Delta F = 2$ Flavor changing neutral current interactions



- Interplay of Weak diagrams \Rightarrow (Convention dependent) phases

Sensitive to New Physics

$$\Delta M = 2\text{Re}\sqrt{(M_{12} - i/2\Gamma_{12})(M_{12}^* - i/2\Gamma_{12}^*)} \approx 2|M_{12}|$$

$$\Delta\Gamma = -4\text{Im}\sqrt{(M_{12} - i/2\Gamma_{12})(M_{12}^* - i/2\Gamma_{12}^*)} \approx 2|\Gamma_{12}| \cos[\text{Arg}(-\Gamma_{12}/M_{12})]$$

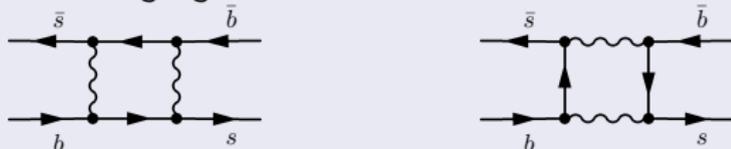
$$\delta = (1 - |q/p|^2)/(1 + |q/p|^2) \approx \frac{1}{2} \text{Im} \frac{\Gamma_{12}}{M_{12}} \approx \frac{1}{2} \frac{\Delta\Gamma}{\Delta M} \tan \phi$$

$$\approx \frac{1}{2} A_{\text{SL}}$$

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Current Experimental Situation

DØ Like-sign Di-muon measurement

[1106.6308]

$$A_{\text{SL}}^b = -[7.87 \pm 1.72 (\text{stat}) \pm 0.93 (\text{syst})] \times 10^{-3}$$

$$= (0.594 \pm 0.022) A_{\text{SL}}^d + (0.406 \pm 0.022) A_{\text{SL}}^s$$

$$\Delta M_s = (17.719 \pm 0.043) \text{ps}^{-1} \text{ [hep-ex/0609040, LHCb-CONF-2011-050(005)]}$$

$$\Delta M_d = (0.507 \pm 0.004) \text{ps}^{-1} \text{ Heavy Flavor Averaging Group (HFAG)}$$

$$\Delta \Gamma_s = (0.116 \pm 0.019) \text{ps}^{-1} \text{ LHCb}$$

$$\Delta \Gamma_s = (0.068 \pm 0.027) \text{ps}^{-1} \text{ CDF}$$

$$\Delta \Gamma_s = (0.163^{+0.065}_{-0.064}) \text{ps}^{-1} \text{ DØ}$$

LHCb measurement of time dependent CP asymmetry [LHCb-CONF-2012-002]

$$\phi_s = -0.001 \pm 0.101(\text{stat}) \pm 0.027(\text{syst}) \text{ rad}$$

- New measurement tend to agree well with SM [1102.4274, hep-ph/0612167]

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Generic Conditions on Mixing Parameter

Physical Constraints

- Mass and width of physical states have to be positive
- Unitarity has to be conserved
- Time evolution of any linear combination of $|B^0\rangle$ and $|\bar{B}^0\rangle$ determined entirely by the Γ matrix

⇒ Γ itself has positive eigenvalues

- Defining $\Gamma = (\Gamma_H + \Gamma_L)/2$, $x = (m_H - m_L)/\Gamma$ and $y = (\Gamma_L - \Gamma_H)/(2\Gamma)$

$$\delta^2 < \frac{\Gamma_H \Gamma_L}{(m_H - m_L)^2 + (\Gamma_H + \Gamma_L)^2/4} = \frac{1 - y^2}{1 + x^2}$$

- Known as unitarity bound or Bell-Steinberger inequality

[J.S. Bell, J. Steinberger, "Weak interactions of kaons", T. D. Lee, L. Wolfenstein, Phys. Rev. 138, B1490-B1496 (1965).]

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Deriving the Relation

Sketch of the Steps

- Assume theoretical knowledge

$$0 \leq y_{12} = |\Gamma_{12}| / \Gamma \leq 1$$

instead of unitarity constraint $\Gamma_{11} \geq |\Gamma_{12}|$

- Two ways of deriving

① Proceed with same steps as unitarity bound, but use y_{12} definition

② Scaling argument: Scale Γ by y_{12}

⇒ Only way to derive bound in CPT violating case for $|\delta|^2$

The Result

$$\delta^2 = \frac{y_{12}^2 - y^2}{y_{12}^2 + x^2} = \frac{|\Gamma_{12}|^2 - (\Delta\Gamma)^2/4}{|\Gamma_{12}|^2 + (\Delta m)^2}$$

- Entirely determined by solving the eigenstate problem
- Monotonic function in y_{12}

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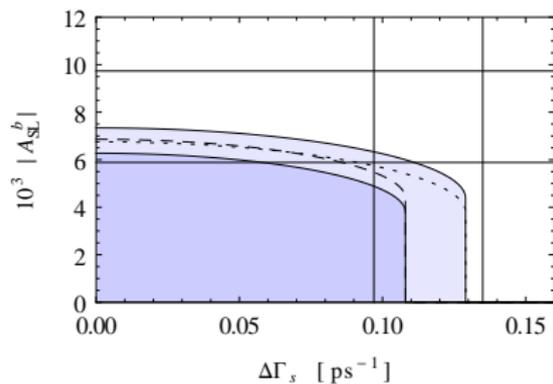
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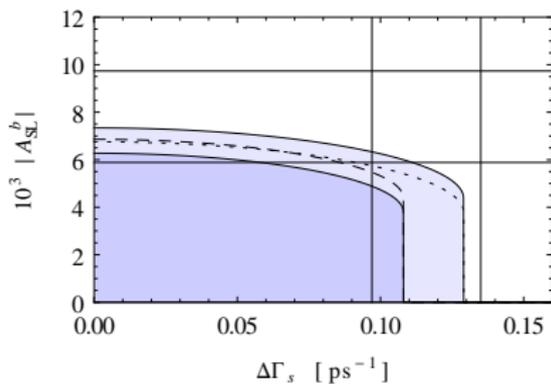
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Plot of the Bound



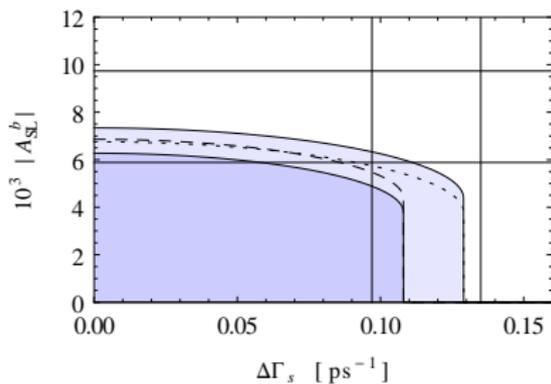
- Combined bound assuming $D\bar{D}$ production asymmetry
- Setting $\Delta\Gamma_d = 0$ and use ΔM^{exp}
- Horizontal lines: 1σ range of $|A_{\text{SL}}^b|$ $D\bar{D}$ measurement
- Vertical lines correspond to $\Delta\Gamma_s$ LHCb measurement
- Shaded regions are allowed by theory prediction of $|\Gamma_{12}|$
 [A.Lenzen,U.Nierste: 1102.4274,hep-ph/0612167]
 - 1 Darker uses 1σ upper range
 - 2 Lighter uses 2σ upper range
- Dashed [dotted] curves: Mixed sigma interval of theory predictions
- The vertical boundaries of the shaded regions arise because $|\Delta\Gamma_s| > 2|\Gamma_{12}^s|$ is unphysical.

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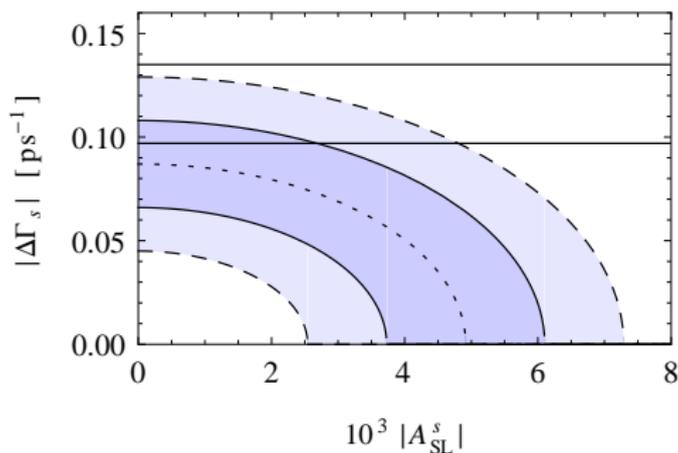


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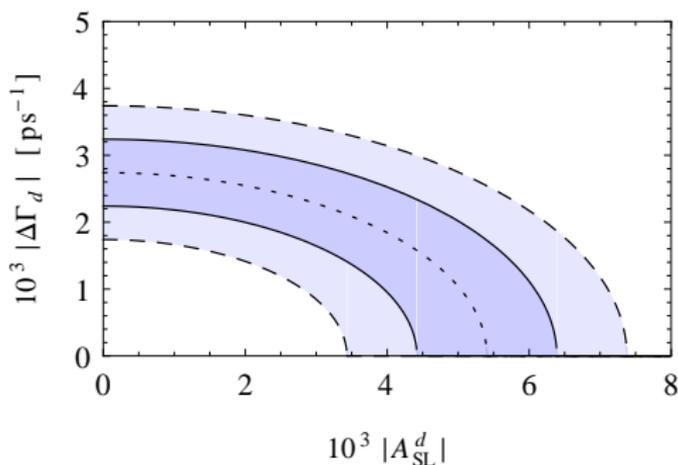


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Plot on Individual Bound on B_s 

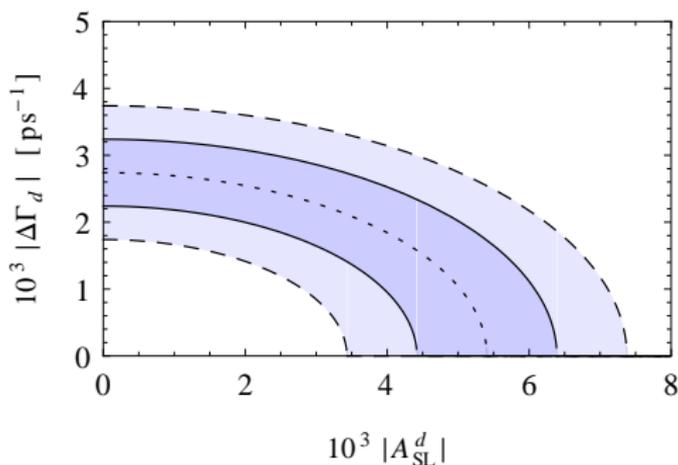
Interpretation

- Horizontal lines correspond to LHCb measurement
- Dark [light] shaded allowed by 1σ [2σ] theory variation
- No discrepancy claimed in experiment

Plot on Individual Bound on B_d 

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- Non-zero measurement of $\Delta\Gamma_d$ would strengthen upper bound

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Numerical Interpretation

Remarks

- Problematic: $|\Delta\Gamma_s|^{\text{meas.}} > 2|\Gamma_{12}^s|$ is unphysical
- Numerator of Relation can vanish \Rightarrow Upper bound
- Assume 2σ theory prediction for a conservative estimate

Results

- For B_c system we obtain taking into account the unphysical region

$$|A_{SL}^s| < 4.2 \times 10^{-3}$$
- 2-3 times better than best current experimental bound
- For the B_d system we obtain a comparable bound

$$|A_{SL}^d| < 7.4 \times 10^{-3}$$
- Significant improvement possible by observing $|\Delta\Gamma_d| > 0$

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Discussion of the Results

Strength of the Bound

- Upper bound on y_{12} implies an upper bound on $|\delta|$
- Relation is much stronger for small y_{12} , as e.g. in the B_d system

Comparing to Known Results

- $D\bar{D}$ A_{SL} measurement: 3.9σ discrepancy with SM
- ⇒ Correlated with the discrepancy found in our analysis
 - 1 SM prediction of A_{SL} uses calculation of Γ_{12}
 - 2 The relation uses $|\Gamma_{12}|$ as an input
 - 3 Calculation of $|\Gamma_{12}|$ and $\text{Im}(\Gamma_{12})$ rely on the same OPE
- Large cancellations in $\text{Im}(\Gamma_{12}) \Rightarrow$ Uncertainties could be larger than expected from NLO calculation [hep-ph/0308029, hep-ph/0307344]
- The sensitivity of Γ_{12} to NP is generally weak
- Interesting to determine δ additionally from this relation

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No Go Theorem (preliminary)

The Claim

There is no generic bound, stronger than the unitarity bound (UB)

Sketch of Derivation

- Unitarity bound is saturated if

$$\langle f|T|B_H \rangle \propto \langle f|T|B_L \rangle$$

- Start with an arbitrary, generic decaying two-state system
- Wigner-Weisskopf approximation: Any choice of parameters OK
- ⇒ Orthogonal, non CP violating system as starting point
- Arbitrary new UV physics can change M_{12} independently of Γ_{12}
- Varying M_{12} keeping mass and width of states physical
- ⇒ Unitarity bound can be saturated (relax constraint $\text{Arg } M_{12} = \text{Arg } \Gamma_{12}$)
- Explicit mathematical check of UB saturation possible

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Summary

- Provided a physical derivation of the exact relation allowing for theoretical input on $|\Gamma_{12}|$
 - ① Input is typically insensitive to New Physics
 - ② Avoids largest uncertainties of theory calculation
 - ③ Valid even if CPT is violated
- Independent of the discrepancy found from a global fit
 - ① Application to $B_{d,s}$ systems leads to the individual bounds

$$|A_{\text{SL}}^s| < 4.2 \times 10^{-3} \quad |A_{\text{SL}}^d| < 7.4 \times 10^{-3}$$

- ② Providing a bound on the individual asymmetries at comparable or better levels than the current experimental bounds
 - ③ Bounds are in tension with the $D\bar{D}$ measurement of A_{SL}^b
- Once an unambiguous determination of A_{SL} or $\Delta\Gamma$ is made, we can use it to constrain the other observable.

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