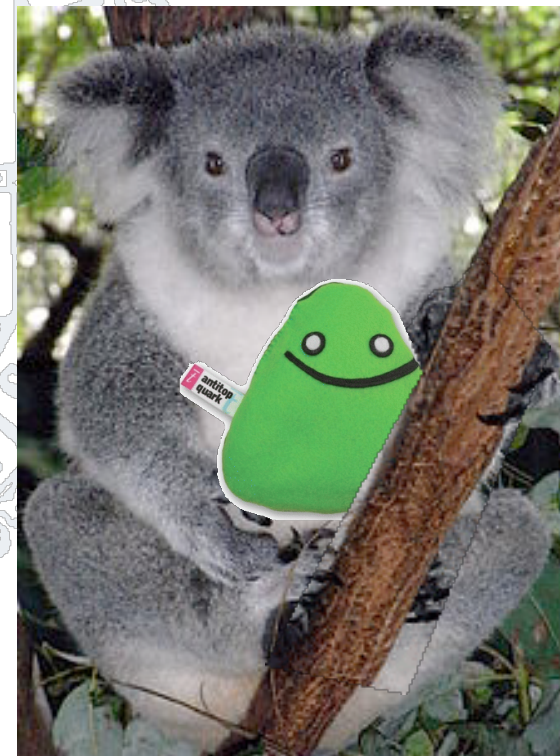


# Measurements of the Top Quark Mass at DØ

**Oleg Brandt** for the DØ collaboration

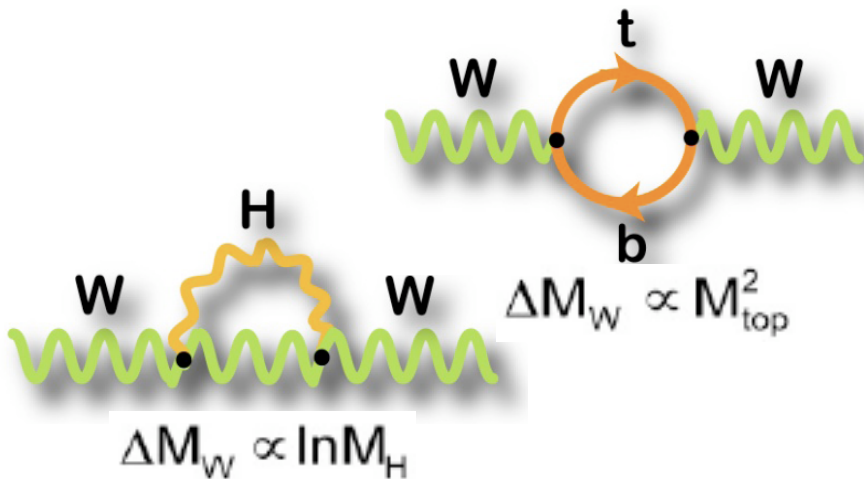
*II. Physikalisches Institut, Georg-August-Universität Göttingen*



- The top is special:
  - Heaviest particle of the SM
  - Yukawa coupling is  $\sim 1$
  - $\Gamma_{\text{top}} \ll \Lambda_{\text{QCD}}$ 
    - $\rightarrow$  top is the only “bare” quark!

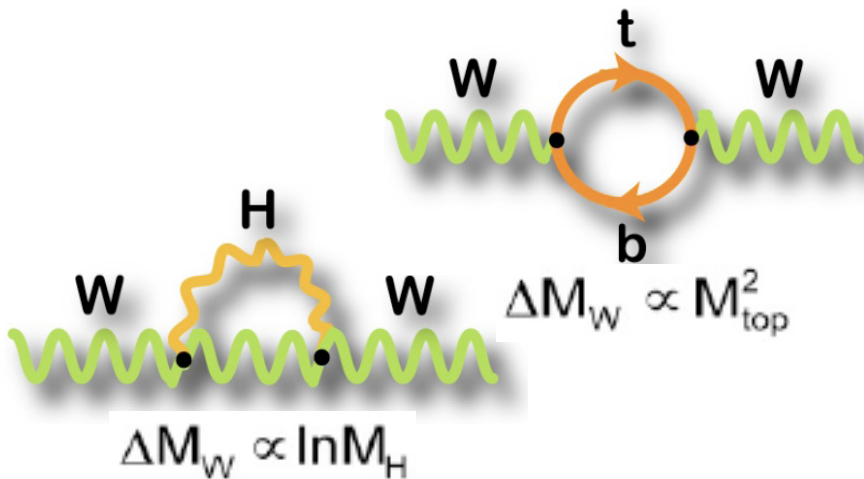


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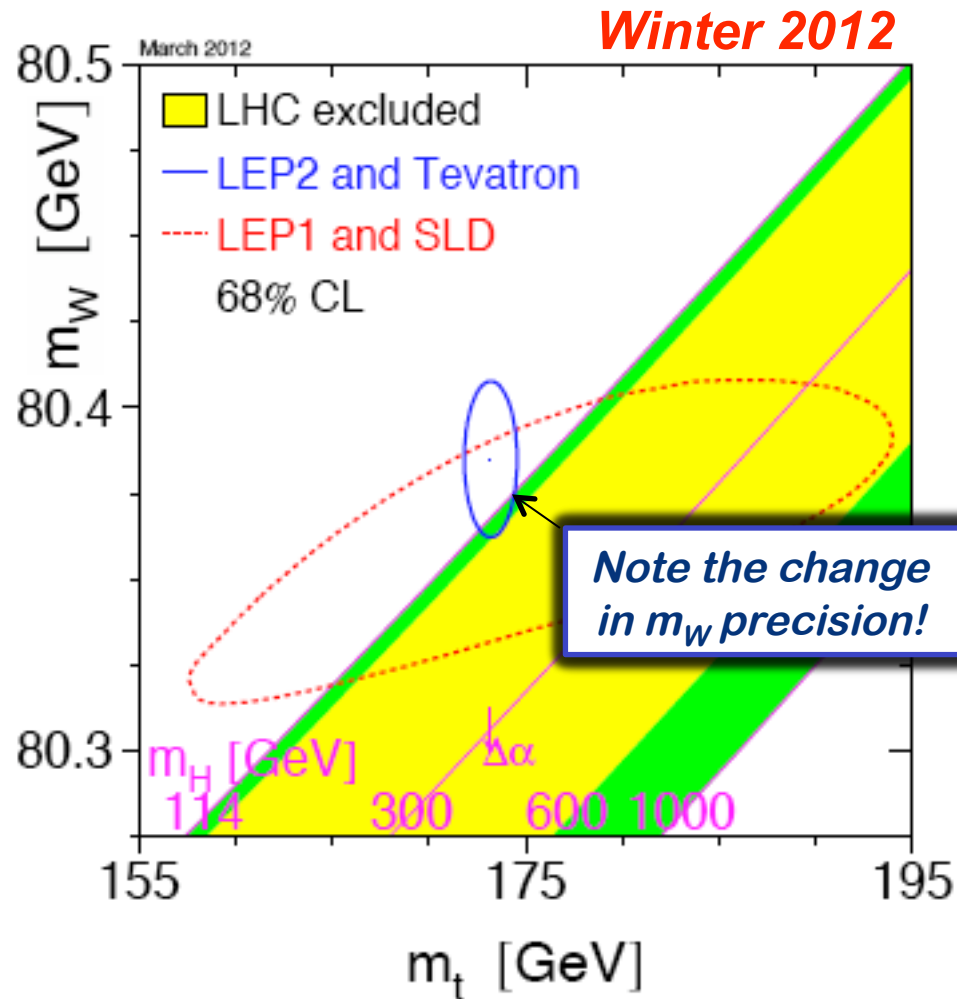


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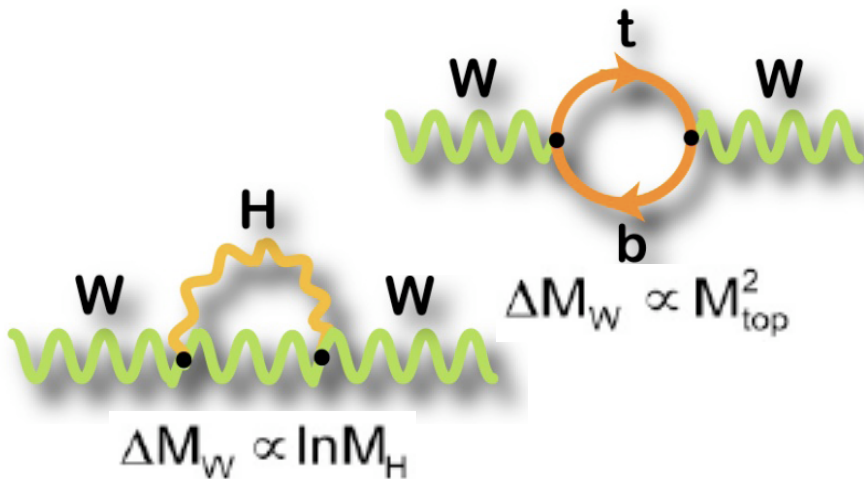


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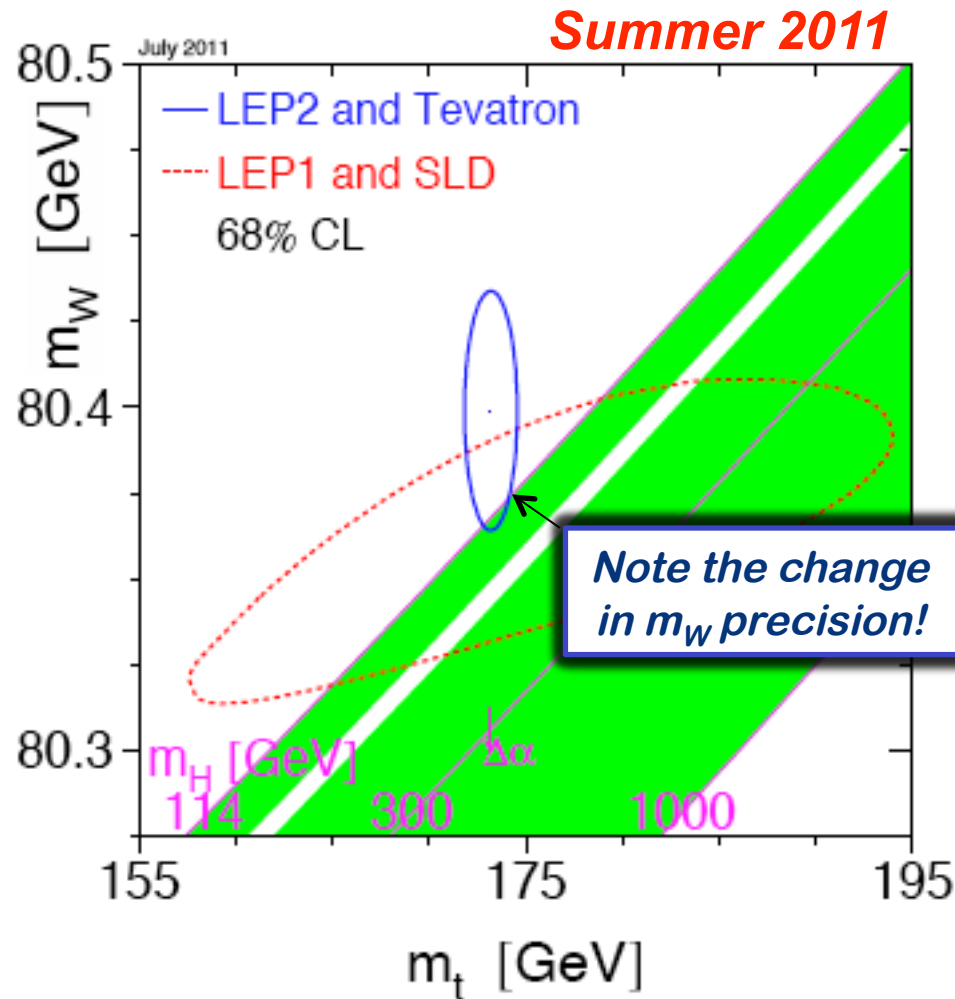


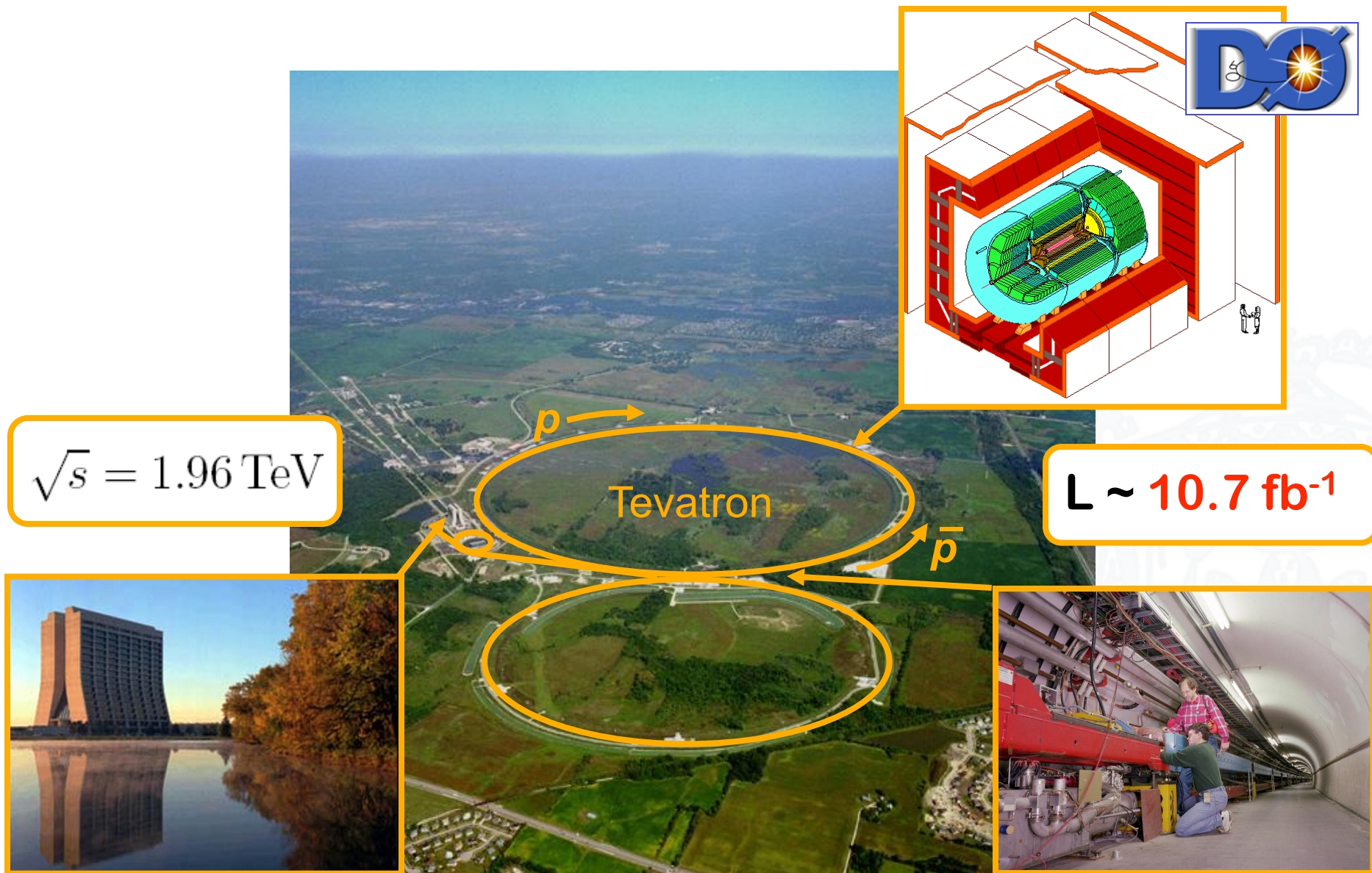


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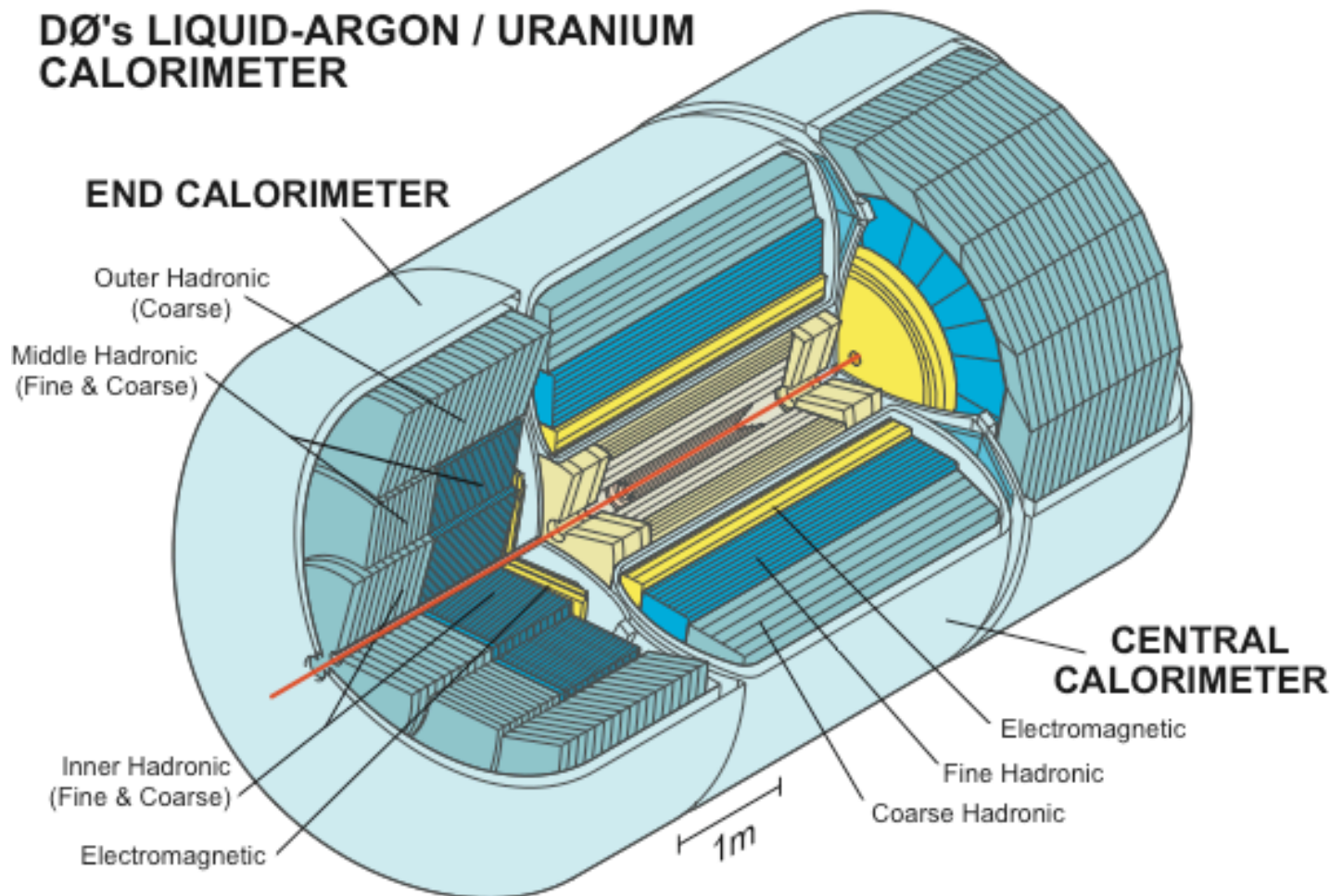


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## DØ's LIQUID-ARGON / URANIUM CALORIMETER



**EM calorimeter**

**$22\%/\sqrt{E} + 4\%$**

**Hadronic calorimeter**

**$68\%/\sqrt{E} + 5\%$**



- **Matrix Element method ( $3.6 \text{ fb}^{-1}$ )**
  - Calculate probability on an event-by-event basis:

$$P_{\text{evt}}(x, m_{\text{top}}) \propto f P_{\text{sig}}(x, m_{\text{top}}) + (1 - f) P_{\text{bgr}}(x)$$

*Phys. Rev. D 84, 032004 (2011)*



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- The clue:

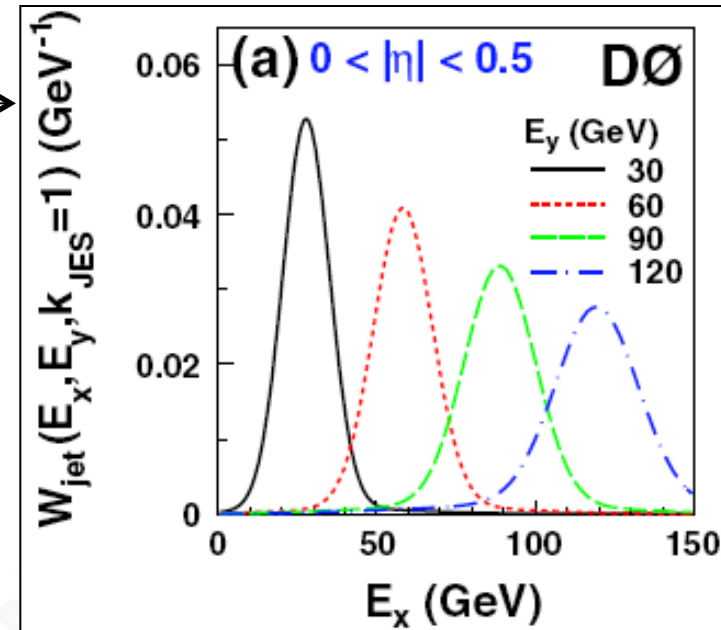
$$P_{\text{sig}}(x, m_{\text{top}}) \equiv \frac{1}{\sigma_{t\bar{t}}(m_{\text{top}})} \int W(x, y) d\sigma_{t\bar{t}}(y, m_{\text{top}})$$

$$\propto |\mathcal{M}_{t\bar{t}}|^2(y, m_{\text{top}})$$

- For each event, we calculate  $P_{\text{sig}}(x, m_{\text{top}})$  based on its consistency to come from  $t\bar{t}$  production, depending on  $m_{\text{top}}$ .
- **Maximal use of stat. information on event-by-event basis!**
  - (Disadvantage: high computational demand)

*Phys. Rev. D 84, 032004 (2011)*

- The Transfer Functions  $W(x, y; JES)$  to map parton-level quantities  $y$  to reconstruction-level ones  $x$ .
  - Treat separately:
    - Light quark jets
    - b-tagged jets w/ soft muon tag
    - All other b-jets
  - x 4  $|\eta|$  regions for each



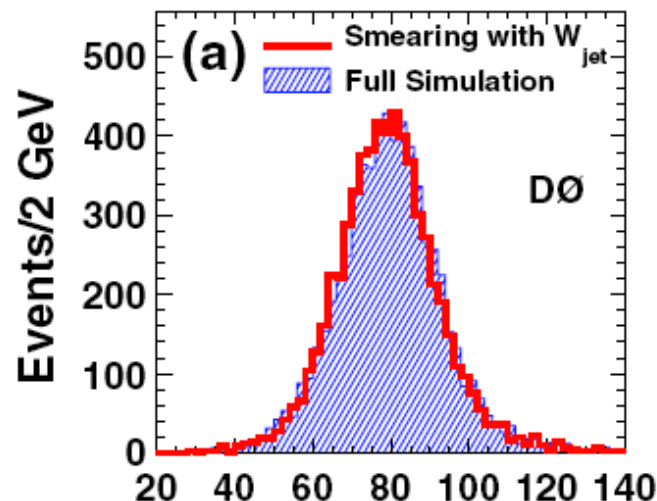
*Phys. Rev. D 84, 032004 (2011)*

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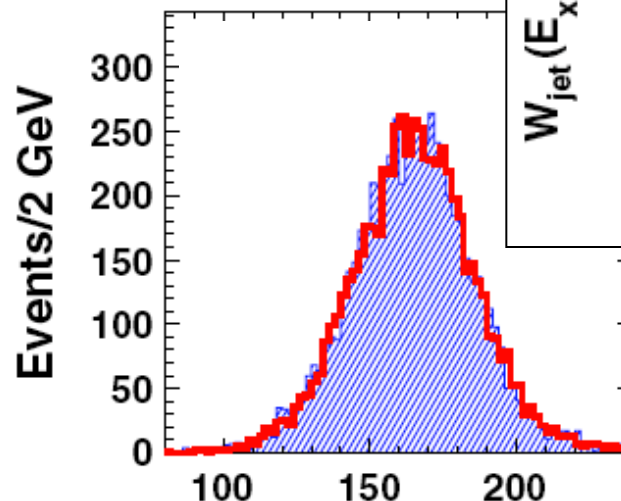
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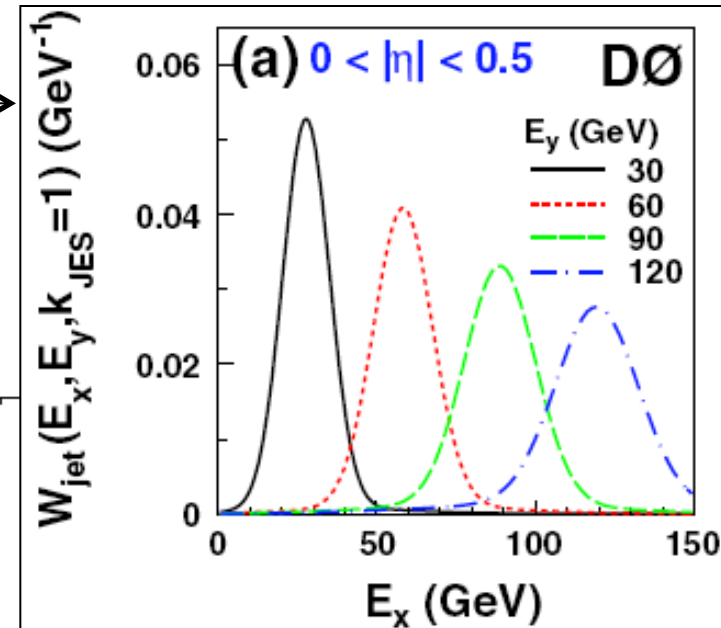
- x 4  $|\eta|$  regions for each



hadronic  
W decays



hadronic  
top decays



Phys. Rev. D 84, 032004 (2011)

- **Matrix Element method (3.6 fb<sup>-1</sup>)**
  - Define the **signal probability** for 4-jet events as:

$$P_{\text{sig}} = \frac{1}{\sigma_{t\bar{t}}^{\text{obs}}} \sum_{i=1}^{24} w_i \int \sum_{\text{flavors}, \nu} |\mathcal{M}_{t\bar{t}}|^2 \frac{f'(q_1)f'(q_2)}{\sqrt{(\eta_{\alpha\beta}q_1^\alpha q_2^\beta)^2 - m_{q_1}^2 m_{q_2}^2}} \Phi_6 W(x, y; k_{\text{JES}})$$

Permutation weight, b-tag based

LO Matrix Element,  $\sim m_{\text{top}}$   
[from Phys. Lett. B 411, 173 (1997)]

Transfer Function  
 $\sim k_{\text{JES}}$



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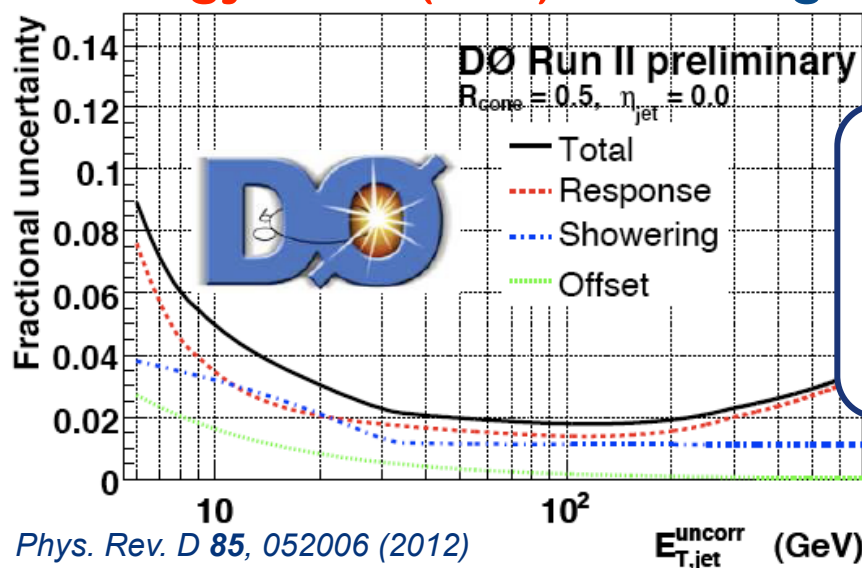
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Transfer Function  
 $\sim k_{\text{JES}}$

- **Jet energy scale (JES)** is the largest systematic uncertainty



$\delta(\text{JES}) \approx 2\%$   
for  $\eta \approx 0, p_T > 20 \text{ GeV}$   
 $\rightarrow$   
 $\delta_{\text{JES}}^{\text{direct}}(m_{\text{top}}) \approx 2-3\%$

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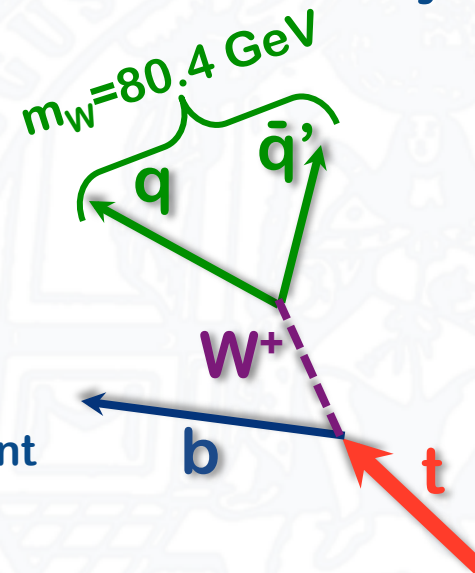
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LO Matrix Element,  $\sim m_{\text{top}}$   
[from Phys. Lett. B 411, 173 (1997)]

Transfer Function  
 $\sim k_{\text{JES}}$

- Jet energy scale (JES)** is the largest systematic uncertainty
  - Determine the JES in situ:
    - Constrain the **mass** of the **dijet** system from hadronic W decay to  $m_W = 80.4 \text{ GeV}$
    - $\rightarrow \delta_{\text{JES}}^{\text{in situ}}(m_{\text{top}}) \approx 0.5\%$  and  $\propto \frac{1}{\sqrt{N}}$ !
  - Background probability** similar (no  $m_{\text{top}}$  dependence)
    - use ME for W+4 jets from VECBOS, event-by-event



- Derive a **correction** for particle jets matched to reconstructed jets in MC:

$$\mathcal{D} = \frac{\sum E_i \cdot R_i^{\text{Data}}}{\sum E_i \cdot R_i^{\text{MC}}}$$

- Sum runs over all particles
- $R_i \rightarrow$  single particle response
- $R_i = R_i(\text{particle type}, E, \eta)$

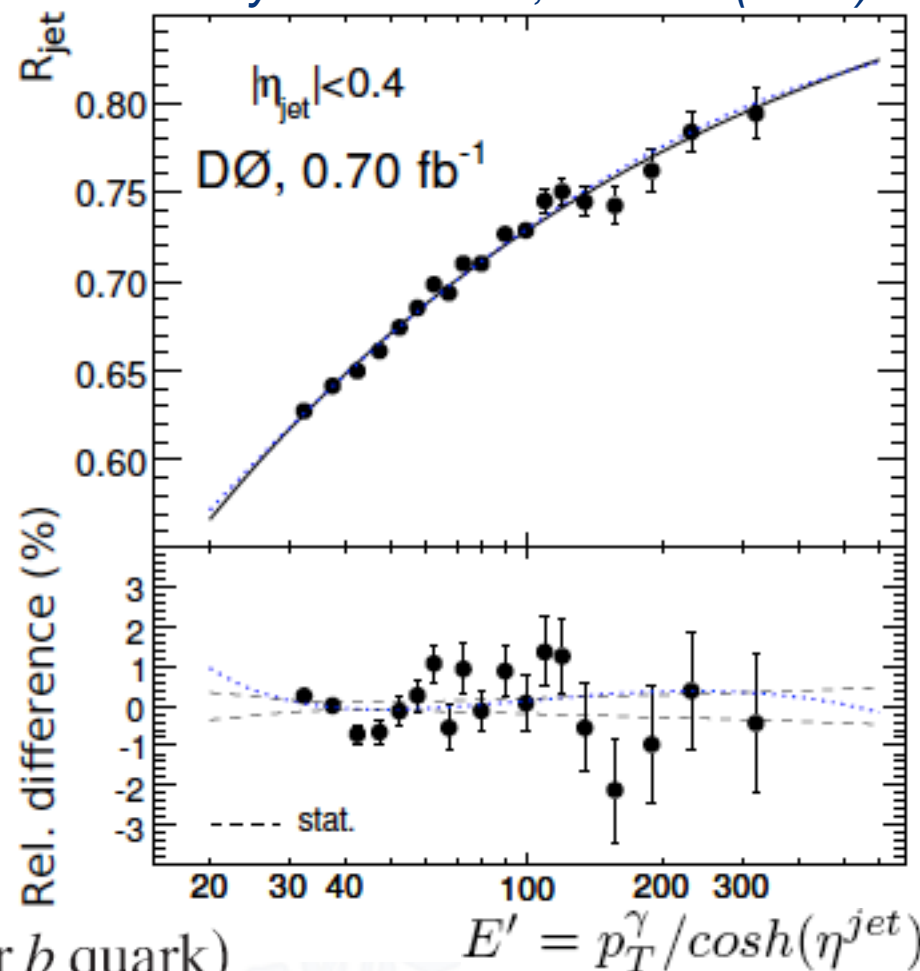
- Derive **flavour-dependent** correction for the MC:

$$F_{\text{corr}}^{\beta} = \mathcal{D}^{\beta} / \langle \mathcal{D}^{\gamma+\text{jet}} \rangle$$

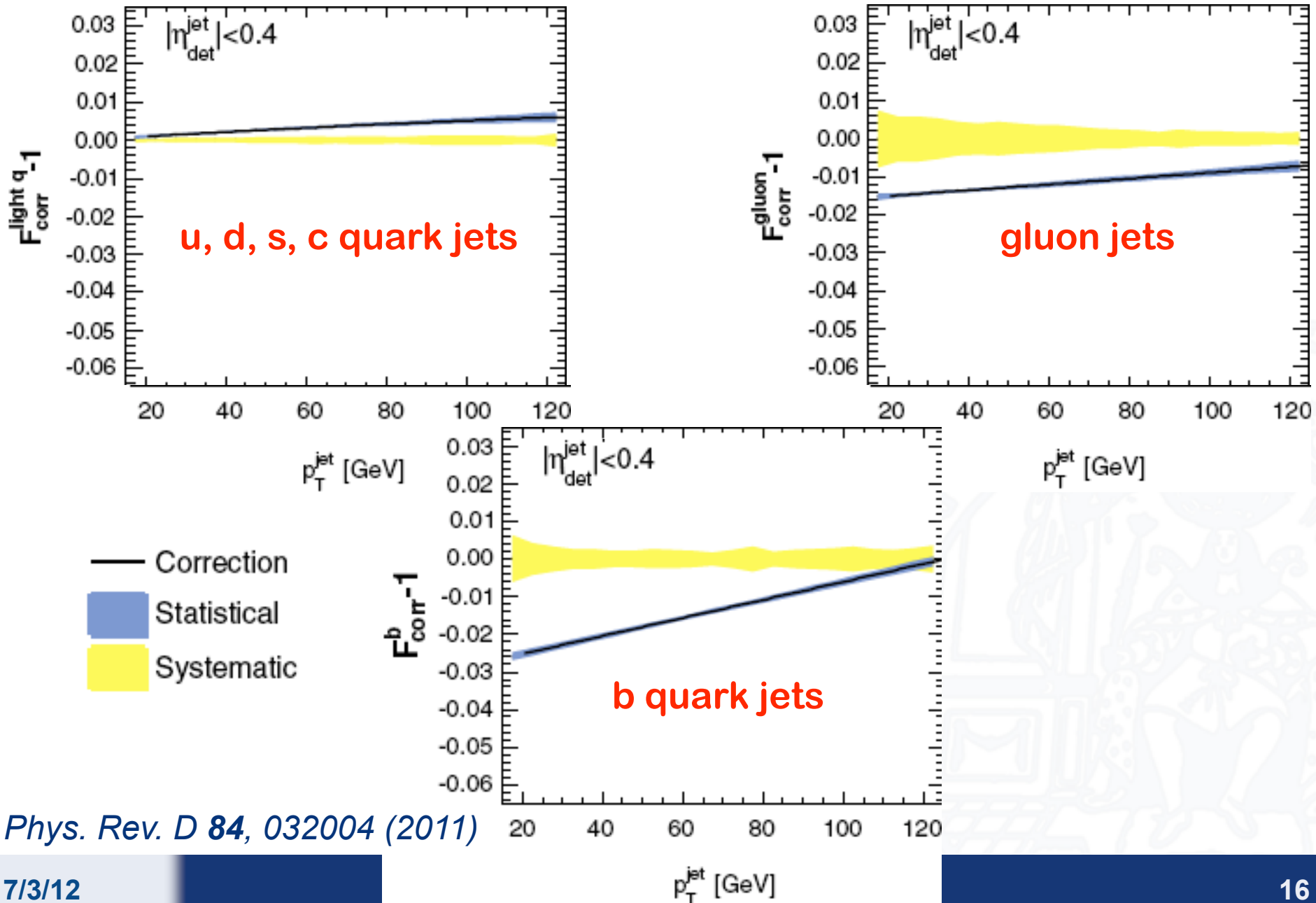
- Where  $\beta$  (= light quark, gluon or  $b$  quark)

- $\rightarrow$  preserves default JES!**

*Phys. Rev. D 85, 052006 (2012)*



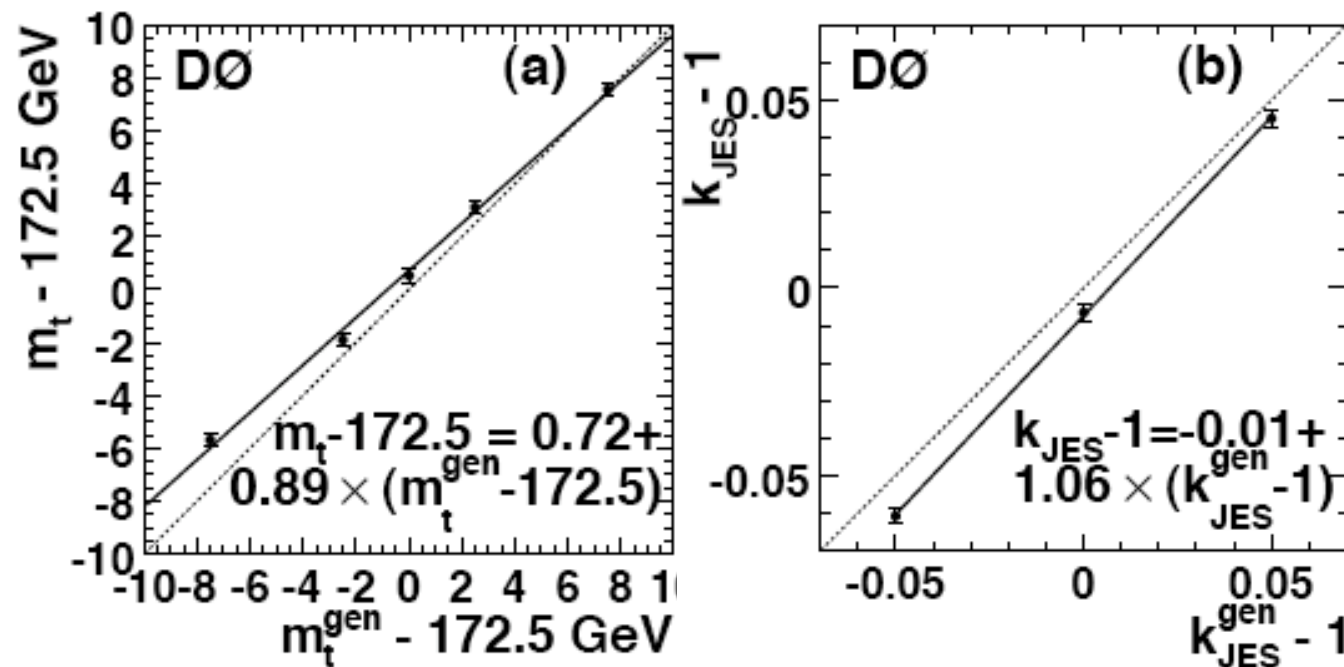
# Single particle response correction



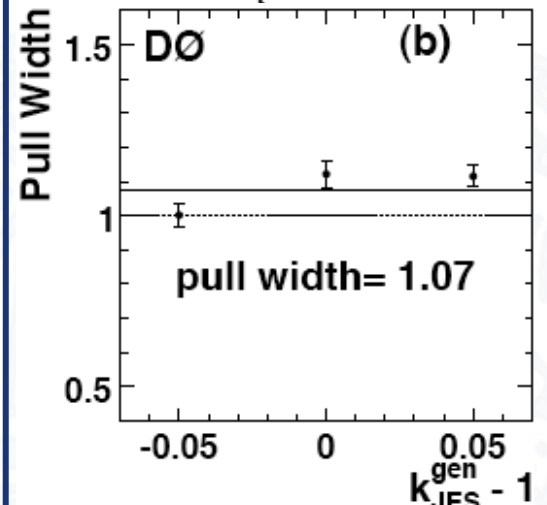
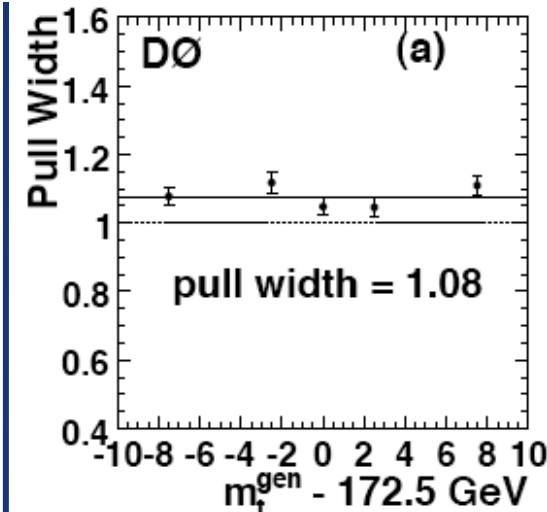
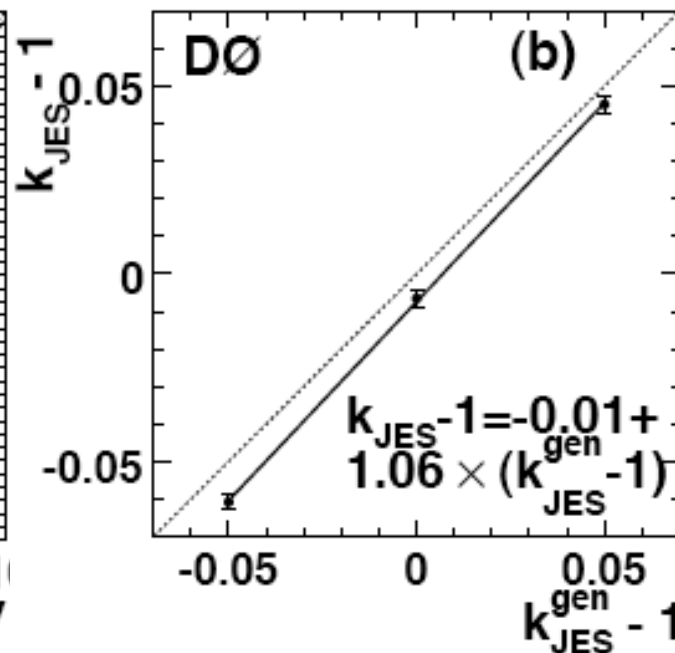
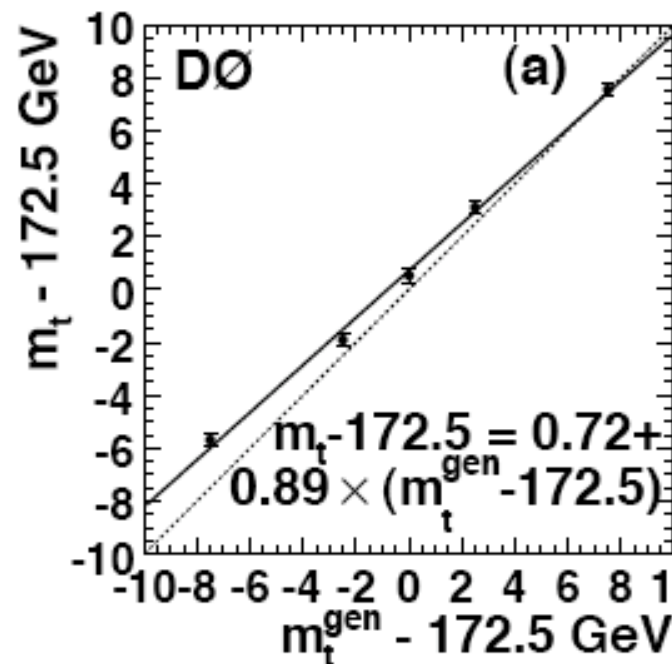
*Phys. Rev. D* **84**, 032004 (2011)



- Behold!** We need to calibrate the method:
  - is the extracted **central value unbiased?**

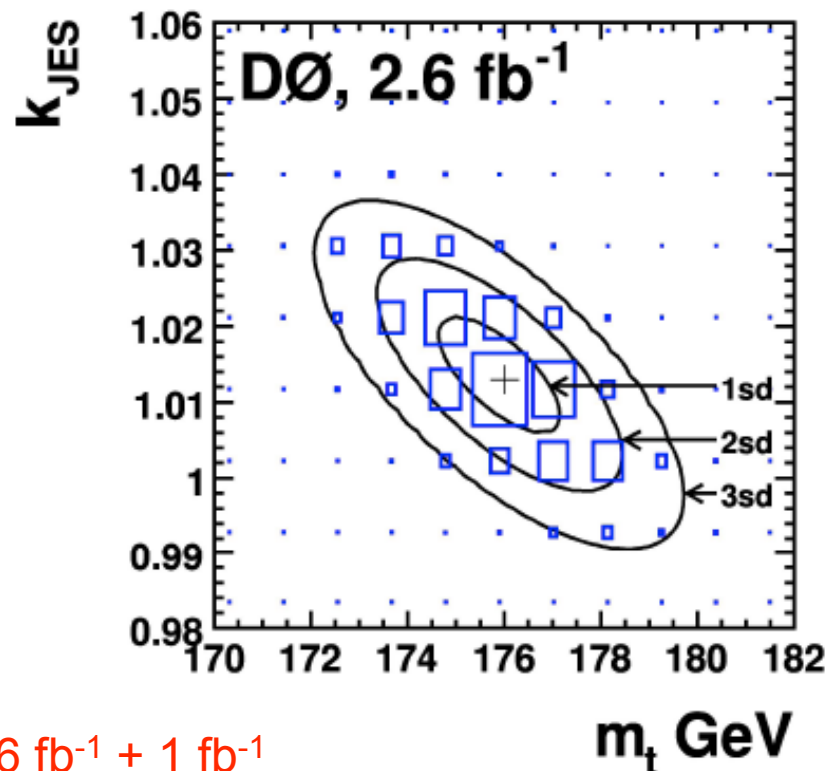


- Behold! We need to calibrate the method:
  - is the extracted central value unbiased?
  - is the statistical uncertainty over/underestimated?



**pull:**  

$$(m_t - \langle m_t \rangle) / \sigma(m_t)$$



Combine  $2.6 \text{ fb}^{-1} + 1 \text{ fb}^{-1}$

$$m_t(3.6 \text{ fb}^{-1}) = 174.9 \pm 0.8(\text{stat}) \pm 0.8(\text{JES}) \pm 1.0(\text{syst}) \text{ GeV}$$

$$= 174.9 \pm 1.5 (\text{GeV})$$

**Relative uncertainty: 0.9%!**

## - Main systematic uncertainties:

*Phys. Rev. D 84, 032004 (2011)*

- Signal modeling: **Hadronisation + UE (0.6 GeV), colour reconnection (0.3 GeV)**
- Detector modeling: **jet energy resolution (0.3 GeV), particle response (0.3 GeV)**

- Apply the **ME method** to the **dilepton channel** ( $5.4 \text{ fb}^{-1}$ )
  - Additional challenge: the  $t\bar{t}$  system is kinematically 1x underconstrained if  $m_{\text{top}}$  is a free parameter!
    - $\rightarrow$  assume prior for  $p_T(t\bar{t})$  from MC simulation
    - $\rightarrow$  integrate over neutrino momenta (with Jacobian)
  - Use LO ME like l+jets analysis
  - Dominant **background: Z+2jets** processes
    - $\rightarrow$  calculate  $P_{\text{bkg}} = P_{\text{Z+2jets}}$  using VECBOS
  - **No in-situ calibration of the JES** possible
    - Large syst. uncertainty from JES calibration
    - Similarly large syst. uncertainty from b-quark JES
    - $\rightarrow$  will improve for full dataset

*Phys. Rev. Lett.* **107**, 082004 (2011)



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  - **Final result:**

$$m_t = 174.0 \pm 1.8(\text{stat}) \pm 2.4(\text{syst}) \text{ GeV}$$

**Relative uncertainty: 1.8%!**

*Phys. Rev. Lett.* **107**, 082004 (2011)

- **Neutrino weighting method ( $5.4 \text{ fb}^{-1}$ ):**
  - dilepton events are kinematically underconstrained
    - Postulate distributions in pseudorapidity of neutrinos from MC
    - Calculate weight distribution vs.  $m_{\text{top}}$
    - Use 1<sup>st</sup> and 2<sup>nd</sup> moment of this distribution to form templates
  - Apply **in-situ JES** calibration from **l+jets channel**:  
 $1.013 \pm 0.008(\text{stat})$ 
    - Caveat:  
 **$k_{\text{JES}}$  can be final state-dependent**, so we derive a dedicated response correction and estimate the corresponding systematic uncertainty (we'll do this for all future  $m_{\text{top}}$  measurements in  $l\bar{l}$ )

*arXiv:1201.5172 [hep-ex] (2011)*

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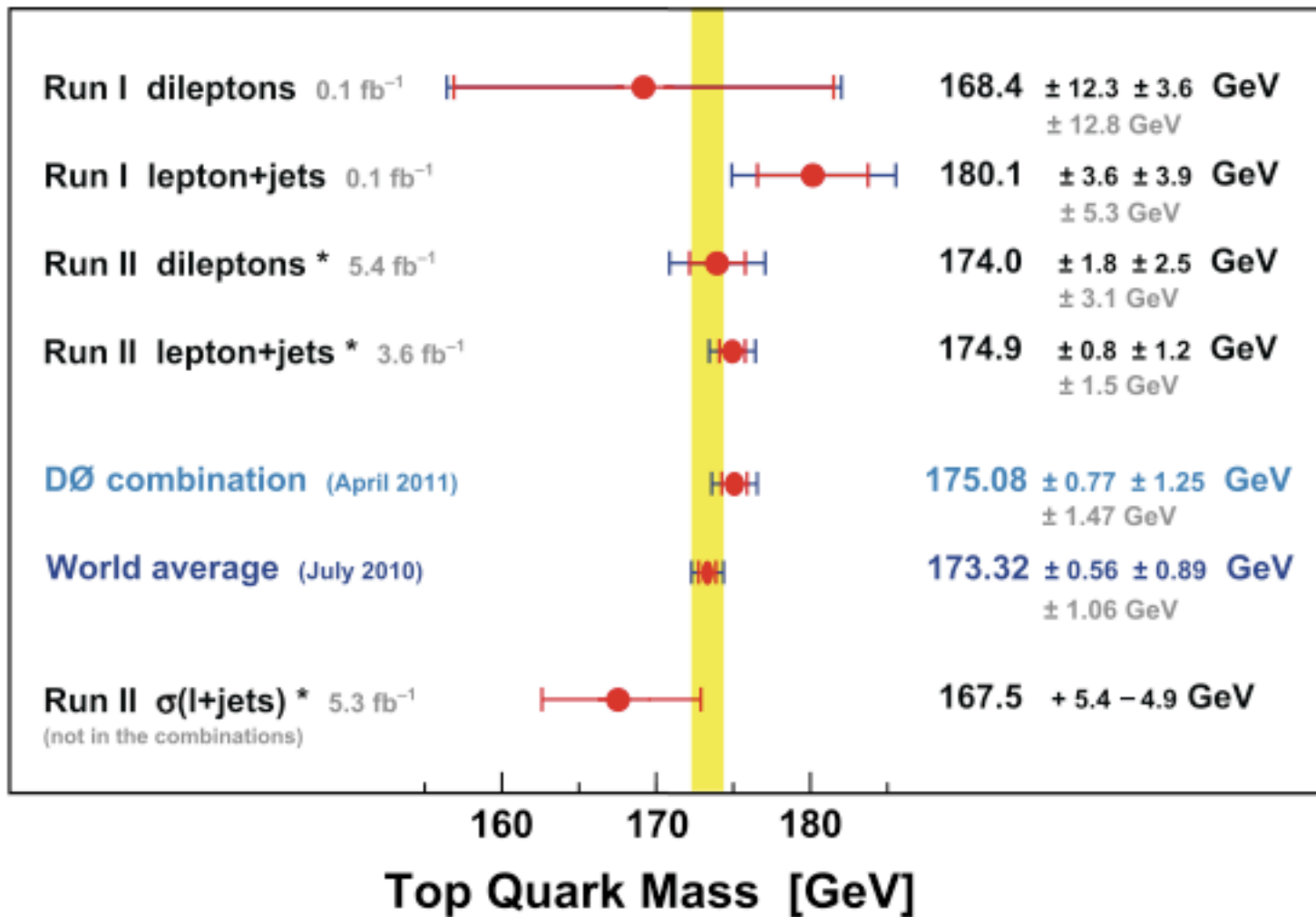
**Relative uncertainty: 1.6%**  
**Best Tevatron dilepton result!**

*arXiv:1201.5172 [hep-ex] (2011)*

**DØ**

\* = preliminary

April 2011



DØ Note 6189

	Run II	
	$\ell + \text{jets}$	$\ell\ell$
Luminosity	$3.6 \text{ fb}^{-1}$	$5.4 \text{ fb}^{-1}$
$m_{\text{top}}$	174.94 GeV	173.97 GeV
iJES	0.53	0.00
aJES	0.00	1.57
bJES	0.07	0.40
cJES	0.00	0.00
dJES	0.63	1.50
rJES	0.00	0.00
Det. Modeling	0.36	0.33
Lepton pt	0.18	0.49
Signal Modeling	0.72	0.74
Bkg from MC	0.18	0.00
Bkg from Data	0.23	0.47
Method	0.16	0.10
CR	0.28	0.10
MHI	0.05	0.00
UN/MI	0.00	0.00
syst. uncertainty	1.24	2.45
stat. uncertainty	0.83	1.83
total	1.50	3.06

**In-situ JES calibration from hadronic W's**  
 $\sim 1/\sqrt{N}$

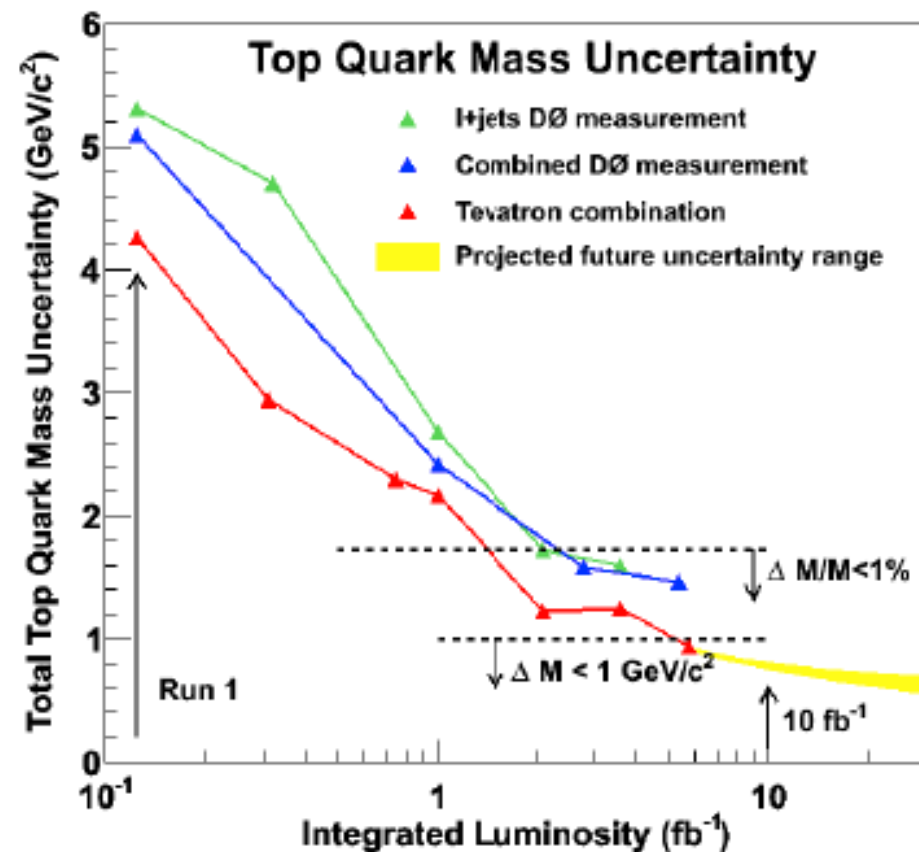
**Limited size of calibration samples for the JES measurement (residual JES)**  
**+ single particle response systematic:**  
 $\sim 1/\sqrt{N}$

**Signal modeling uncertainties**  
**(NLO corrections, hadronisation+UE,**  
**ISR / FSR, PDF uncertainty):**  
 $\sim \sqrt{\text{brain effort}}$

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stat. uncertainty	0.83	1.83
total	1.50	3.06



**Relative uncertainty: 0.8%**  
**Expect this limit to be improved...**

DØ Note 6189

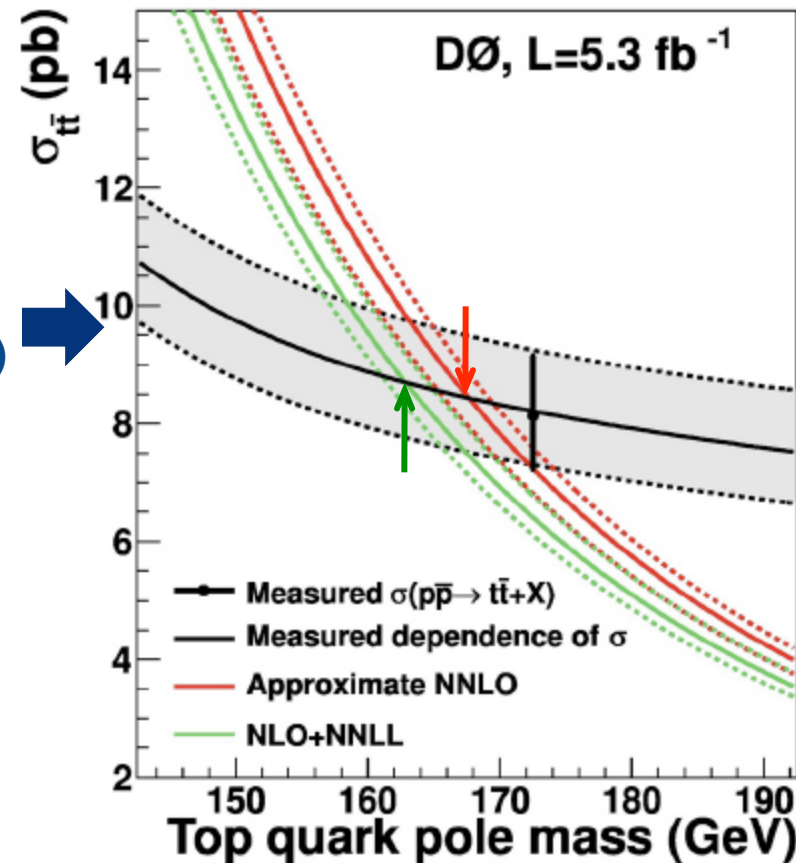
- Different **mass definitions** in fixed order calculations:
  - $m_t^{\text{pole}}$ ,  $m_t^{\overline{\text{MS}}}$ ,  $m_t^{\text{min subtraction}}$ , ...
  - What we typically measure in **kinematic fits** is  $m_t^{\text{MC}}$ 
    - Theory interpretation difficult
    - Arguably,  $m_t^{\text{MC}}$  closer to  $m_t^{\text{pole}}$



*Phys. Lett. B 703 422 (2011)*


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- Can measure  $m_t^{\overline{\text{MS}}}$  or  $m_t^{\text{pole}}$  from comparison with  $\sigma_{t\bar{t}}^{\overline{\text{MS}}}$  or  $\sigma_{t\bar{t}}^{\text{pole}}$  !
  - Account for the **weak dependence** of  $\sigma_{t\bar{t}}$  on  $m_t^{\text{MC}}$  (acceptance effect)



*Phys. Lett. B 703 422 (2011)*

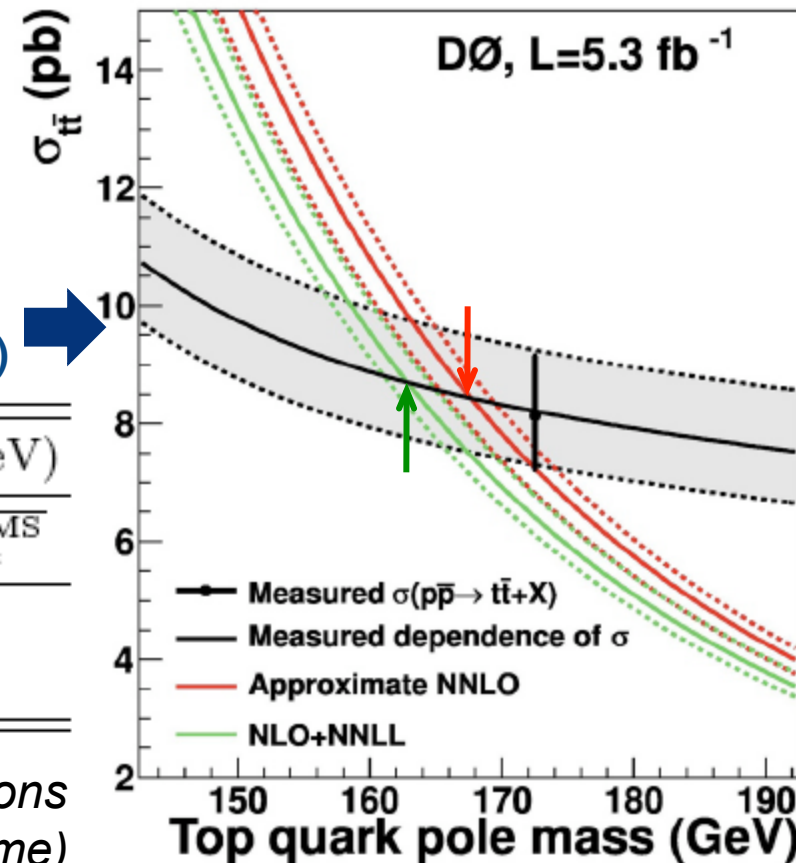
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Theoretical prediction	$m_t^{\text{pole}}$ (GeV)	$\Delta m_t^{\text{pole}}$ (GeV)
MC mass assumption	$m_t^{\text{MC}} = m_t^{\text{pole}}$	$m_t^{\text{MC}} = m_t^{\overline{\text{MS}}}$
NLO+NNLL [14]	$163.0^{+5.1}_{-4.6}$	-3.3
Approximate NNLO [15]	$167.5^{+5.2}_{-4.7}$	-2.7

- [14] V. Ahrens, A. Ferroglia, M. Neubert, B. D. Pecjak, and L. L. Yang, J. High Energy Phys. **1009**, 097 (2010); V. Ahrens, A. Ferroglia, M. Neubert, B. D. Pecjak, and L. L. Yang, Nucl. Phys. Proc. Suppl. **205–206**, 48 (2010).  
 [15] S. Moch and P. Uwer, Phys. Rev. D **78**, 034003 (2008); U. Langenfeld, S. Moch, and P. Uwer, Phys. Rev. D **80**, 054009 (2009).

+ other calculations  
(also  $\overline{\text{MS}}$  scheme)



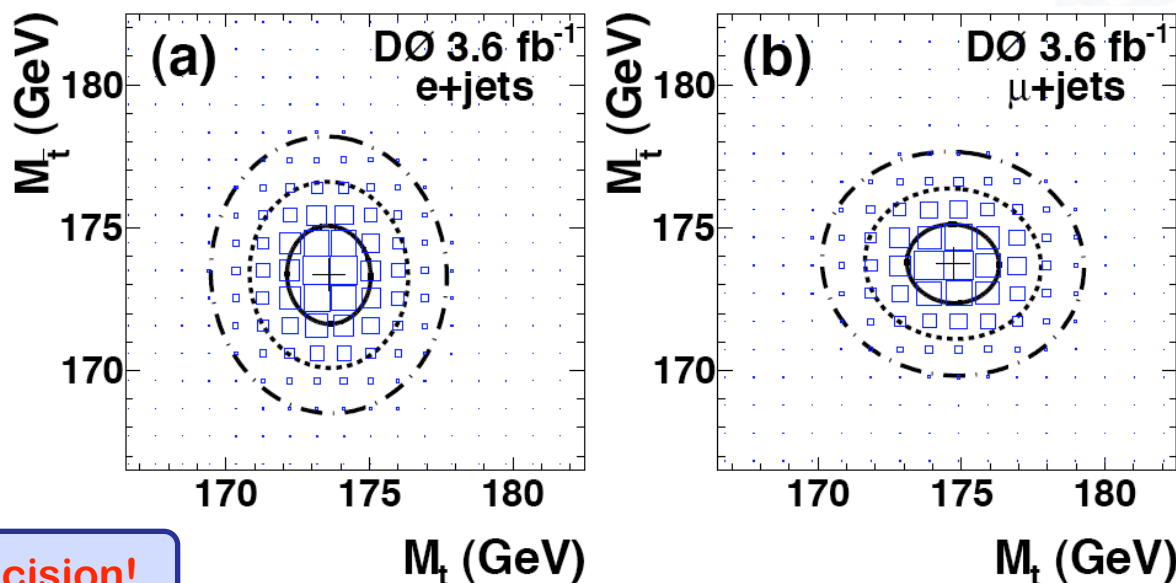
Phys. Lett. B **703** 422 (2011)

- **CPT is essential for a locally Lorentz-invariant QFT**
  - $m_{\text{particle}} \neq m_{\text{antiparticle}} \rightarrow \text{CPT violated!}$ 
    - Top is the only quark where this test is possible:  $\tau_t = (3.3^{+1.3}_{-0.9}) \times 10^{-25} \text{ s}$



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  - Use the most statistically sensitive method at hand (ME):
    - $P(m_{\text{top}}, k_{\text{JES}}) \rightarrow P(m_t, m_{t\text{bar}})$
    - Use lepton charge to tag  $t$  and  $\bar{t}$
  - **Direct and independent** measurement of  $m_t$  and  $m_{\bar{t}}$ !

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<1% relative precision!

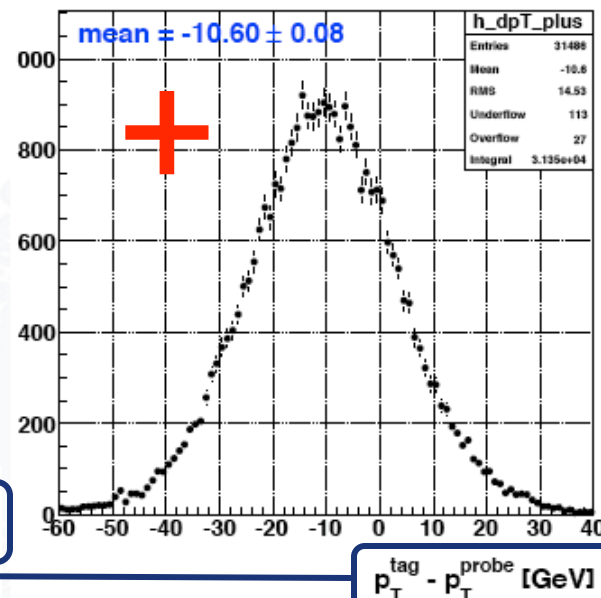
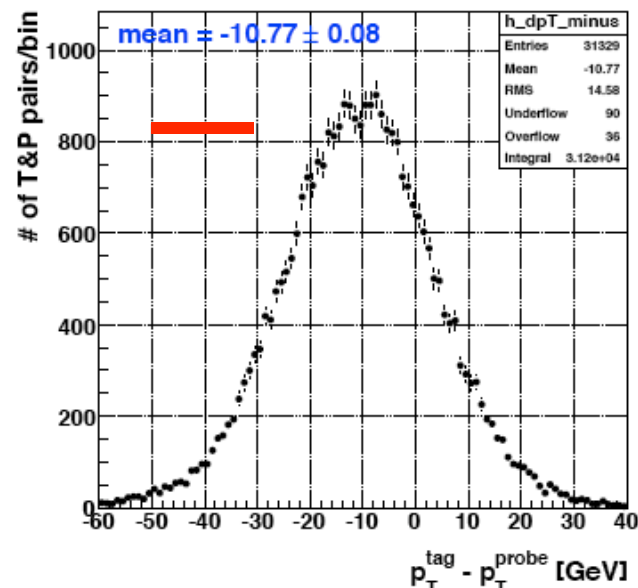
$$\Delta m \equiv m_t - m_{\bar{t}} = 0.8 \pm 1.8 \text{ (stat)} \pm 0.5 \text{ (syst) GeV}$$

- Lots of work went into evaluating the systematic uncertainties for this precision measurement:

Source	Uncertainty on $\Delta m$ (GeV)
Modeling of detector:	
Jet energy scale	0.15
Remaining jet energy scale	0.05
Response to $b$ and light quarks	0.09
Response to $b$ and $\bar{b}$ quarks	0.23
Response to $c$ and $\bar{c}$ quarks	0.11
Jet identification efficiency	0.03
Jet energy resolution	0.30
Determination of lepton charge	0.01
ME method:	
Signal fraction	0.04
Background from multijet events	0.04
Calibration of the ME method	0.18
Total	0.47

fractional response difference

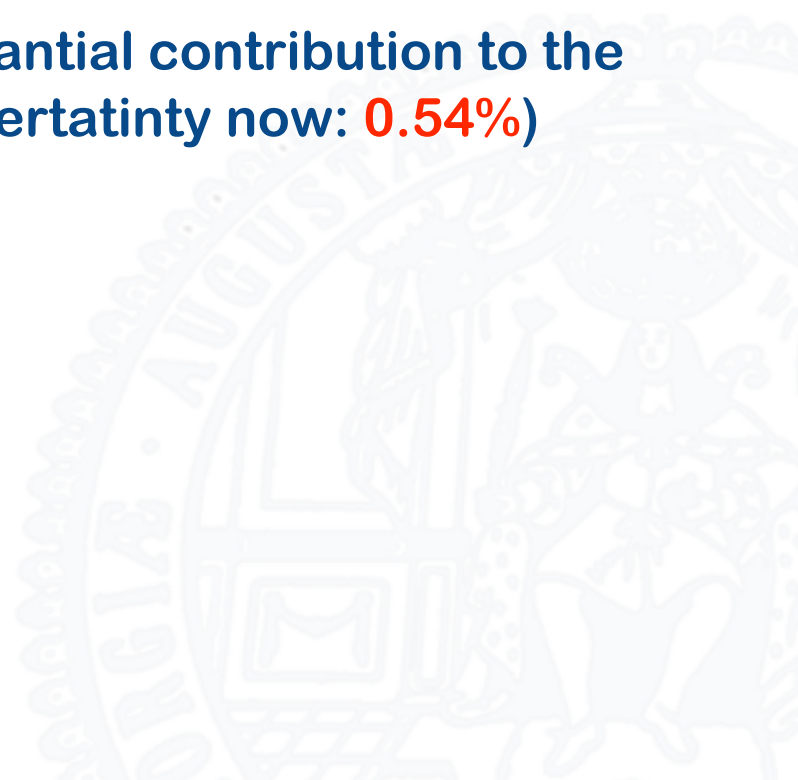
$$f_{\Delta\mathcal{R}} \equiv \frac{\Delta\mathcal{R}}{\langle 1/2 \cdot (p_T^{\text{tag}} + p_T^{\text{probe}}) \rangle} = 0.0042$$



Use soft leptons to tag  $b$  and  $b\bar{b}$  jets

Phys. Rev. D 84, 052005 (2011)

- **Top quark mass measurement is a Tevatron legacy:**
  - Many **systematic uncertainties** generically smaller at the Tevatron compared to the LHC:
    - tt signal modeling: **ISR, kinematics of production**
    - Run conditions: **more uniform + substantially less pile-up**
  - → we need to capitalise on this
  - The Tevatron will provide a substantial contribution to the world average  $m_{\text{top}}$  until ILC (uncertainty now: **0.54%**)



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  - → we need to capitalise on this
  - The Tevatron will provide a substantial contribution to the world average  $m_{\text{top}}$  until ILC (uncertainty now: 0.54%)
- We are expecting many more exciting results from the Tevatron and the LHC in the coming years:
  - CDF: <http://www-cdf.fnal.gov/physics/new/top/top.html>
  - DØ: [http://www-d0.fnal.gov/Run2Physics/top/top\\_public\\_web\\_pages/top\\_public.html](http://www-d0.fnal.gov/Run2Physics/top/top_public_web_pages/top_public.html)
- 15 years after the top quark discovery, the era of precision measurements in the top sector has begun!

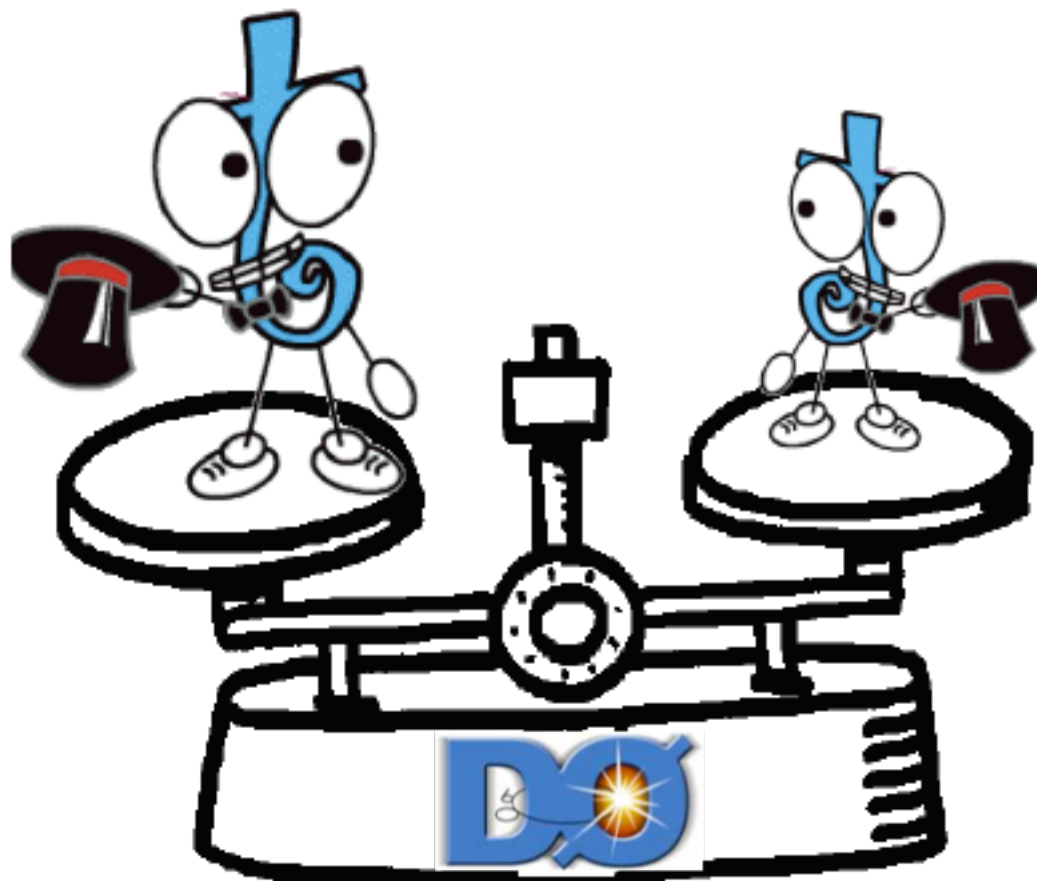


*GAME OVER*

*... FOR THE TEVATRON (2011)*



**We are looking ahead to more  
exciting measurements from the Tevatron!**



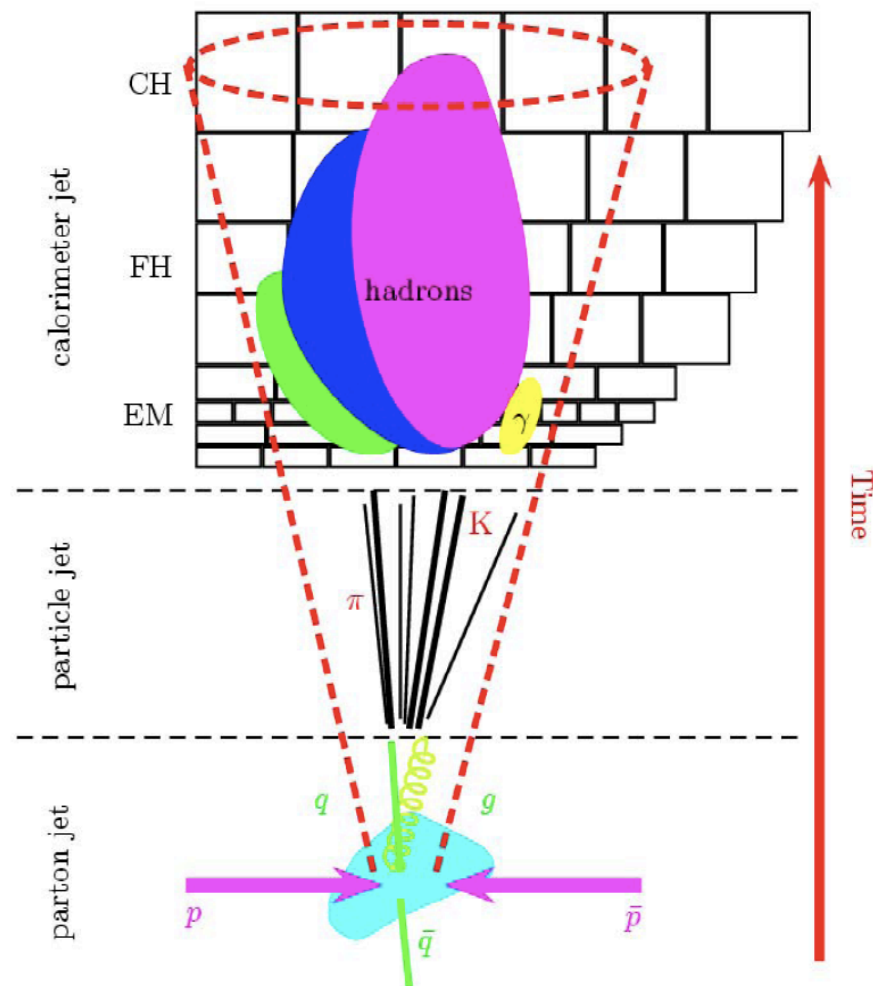
Source	Uncertainty (GeV)
<i>Modeling of production:</i>	
<i>Modeling of signal:</i>	
Higher-order effects	$\pm 0.25$
➔ ISR/FSR	$\pm 0.26$
➔ Hadronization and UE	$\pm 0.58$
➔ Color reconnection	$\pm 0.28$
Multiple $p\bar{p}$ interactions	$\pm 0.07$
Modeling of background	$\pm 0.16$
$W$ +jets heavy-flavor scale factor	$\pm 0.07$
Modeling of $b$ jets	$\pm 0.09$
Choice of PDF	$\pm 0.24$
<i>Modeling of detector:</i>	
Residual jet energy scale	$\pm 0.21$
➔ Data-MC jet response difference	$\pm 0.28$
$b$ -tagging efficiency	$\pm 0.08$
Trigger efficiency	$\pm 0.01$
Lepton momentum scale	$\pm 0.17$
➔ Jet energy resolution	$\pm 0.32$
Jet ID efficiency	$\pm 0.26$
<i>Method:</i>	
Multijet contamination	$\pm 0.14$
Signal fraction	$\pm 0.10$
MC calibration	$\pm 0.20$
Total	$\pm 1.02$

Modeling of signal: 0.8 GeV

Modeling of detector: 0.6 GeV

Method: 0.3 GeV

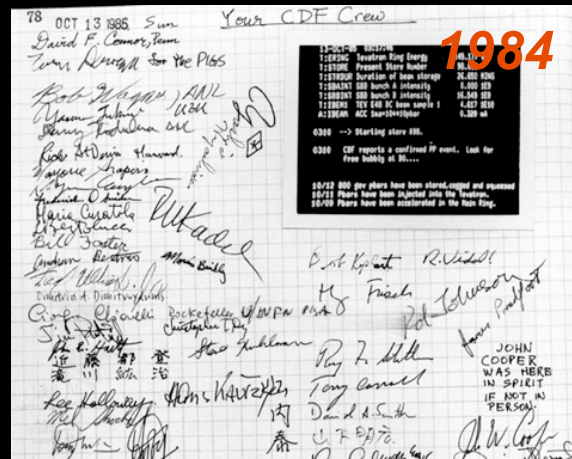
- We are interested in **parton-level quantities** for our top measurements
  - Map the energies of reco-level jets particle jets (D0) / partons (CDF)
  - This is referred to as a Energy Scale (JES) corr'n
  - With the current size of samples:
    - $s(\text{JES})/\text{JES} \sim 1.5\%$  (D0)
    - $s(\text{JES})/\text{JES} \sim 2.5\%$  (CDF)
- And many more:
  - Lepton ID,  $p_T$  scale







1983



1984



1985



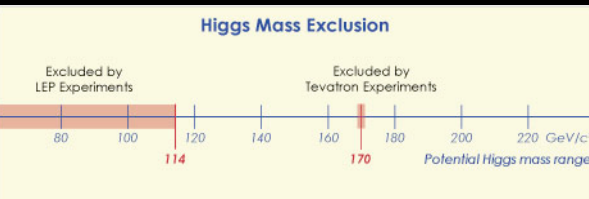
1991



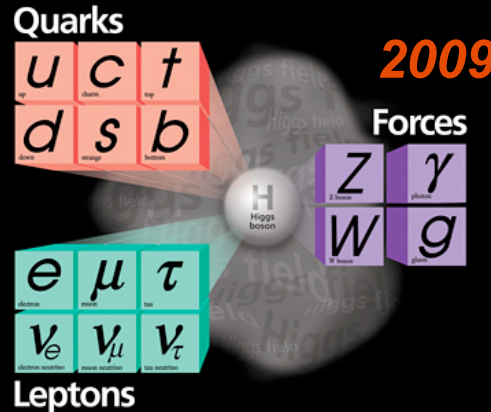
1992



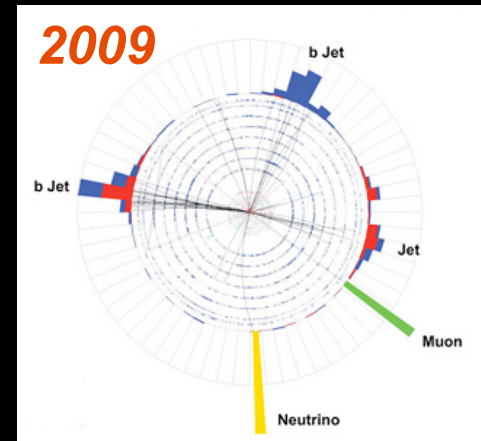
1995



2008

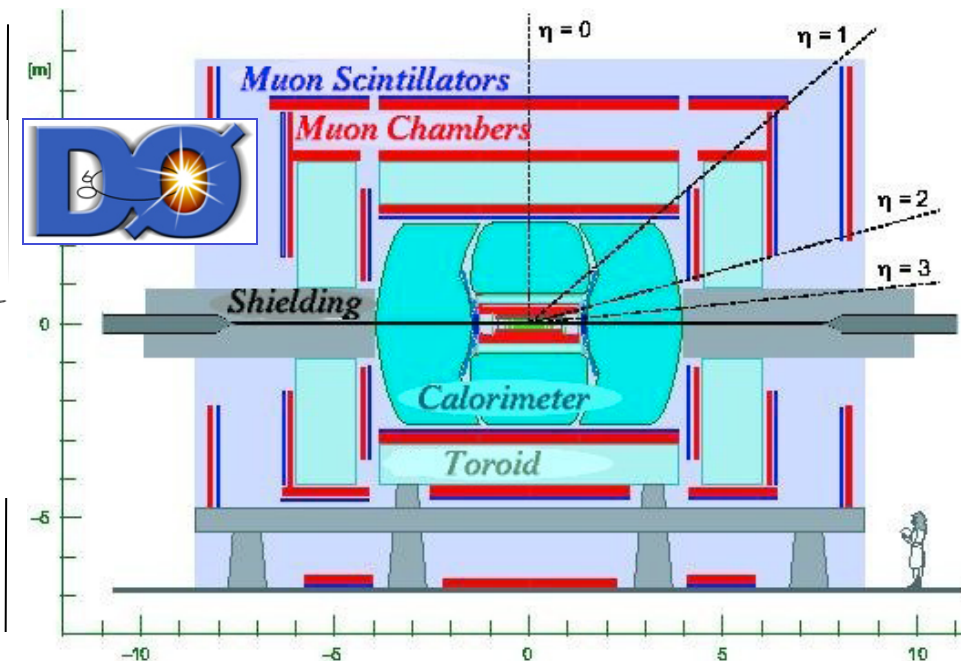
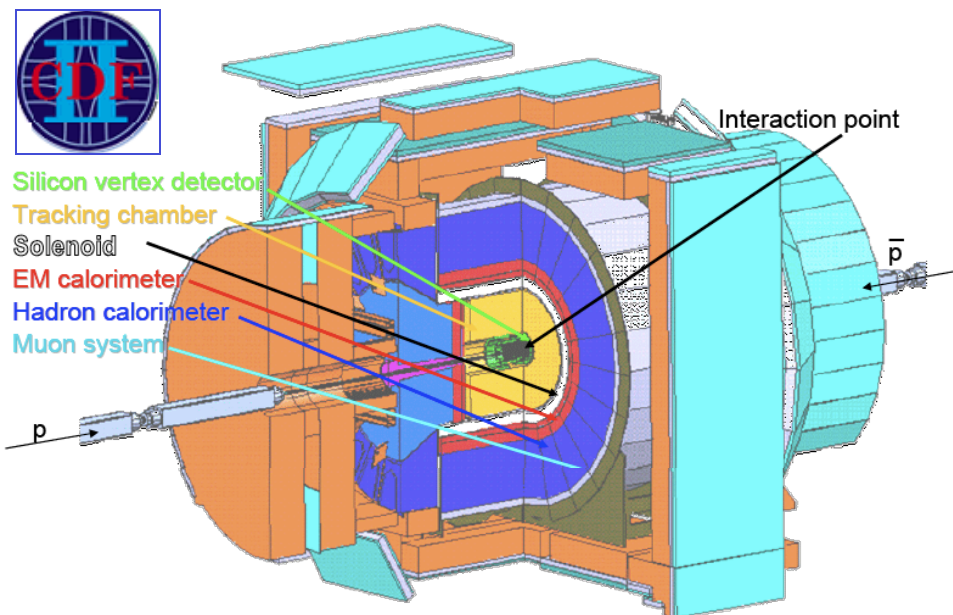


2009

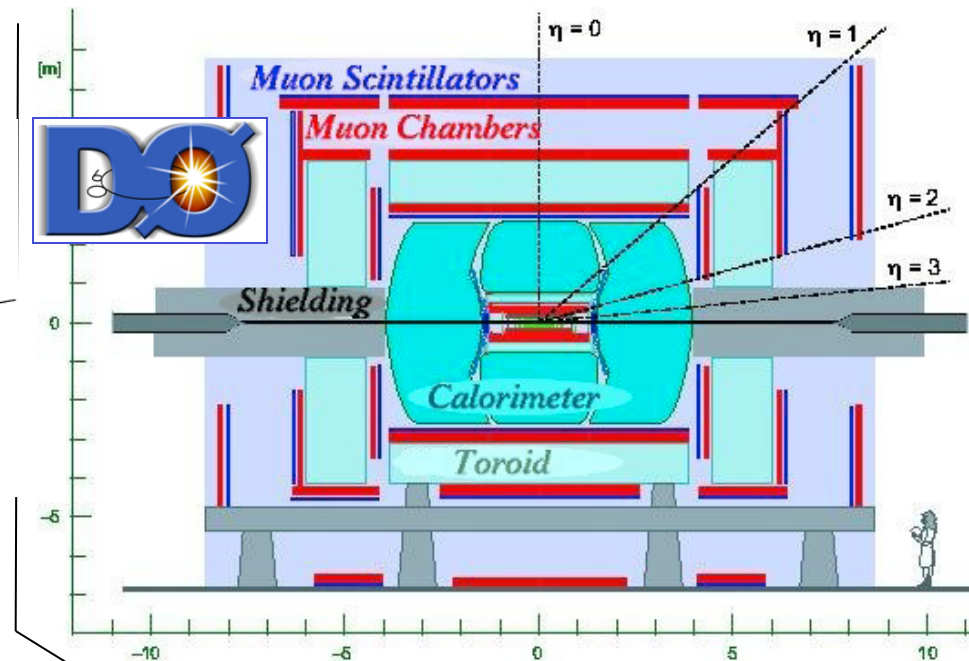
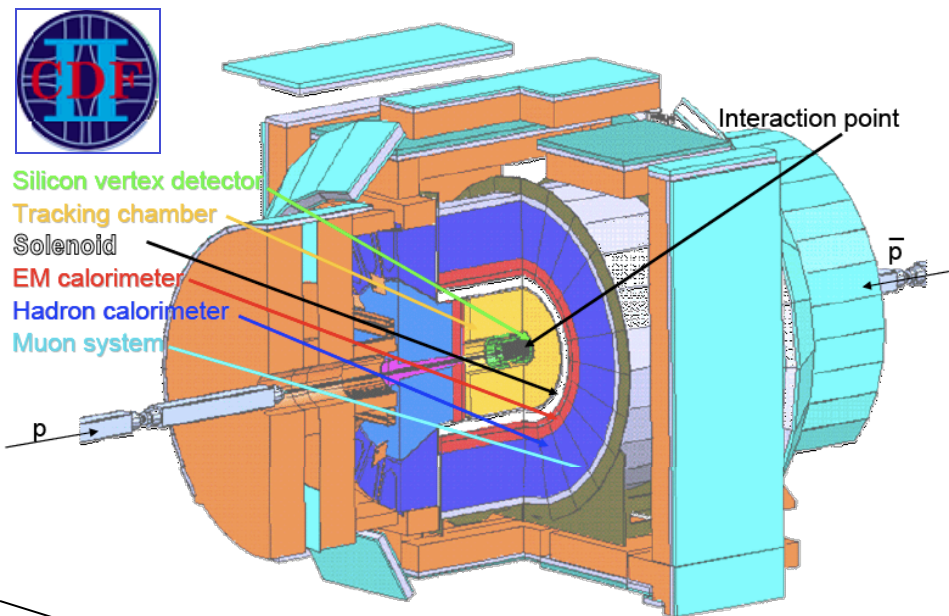


2009

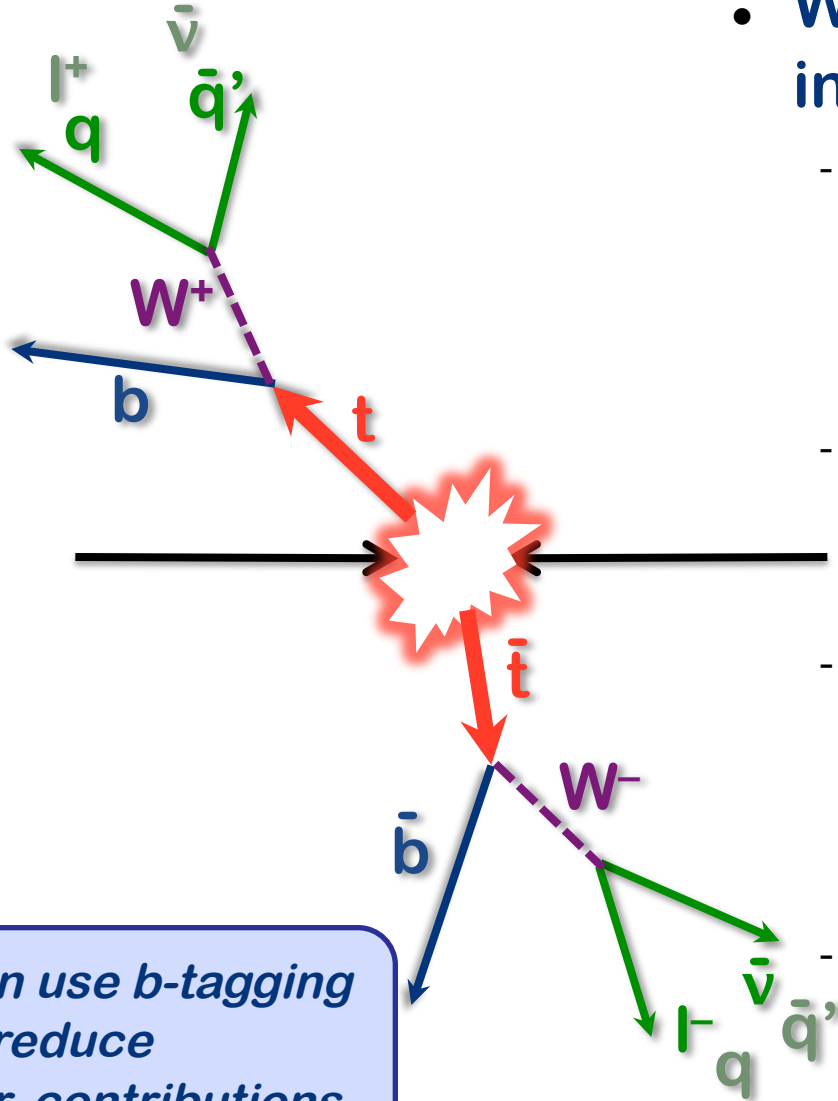




	CDF	DØ
EM calorimeter	$14\%/\sqrt{E} + 1\%$	$22\%/\sqrt{E} + 4\%$
Hadronic calorimeter	$70\%/\sqrt{E} + 5\%$	$68\%/\sqrt{E} + 5\%$



Tracking	Silicon	$ \eta  < 2 - 2.5$	Silicon	$ \eta  < 3$
	Drift cell	$ \eta  < 1.1$	Fiber	$ \eta  < 1.7$
Calorimetry	Scintillators	$ \eta  < 3.6$	LAr/DU	$ \eta  < 4$
Muon chambers	Drift	$ \eta  < 1.5$	Drift	$ \eta  < 2.0$
	Scintillators		Scintillators	



- We measure the top mass in  $t\bar{t}$  events:
  - **Dilepton channel:** low backgrounds, but underconstrained kinematics for  $m_{\text{top}}$  measurement and low rate
  - **$l$ +jets channel:** good compromise between kinematic reconstruction, high rate, and backgrounds
  - **All-hadronic channel:** highest branching ratio, very high backgrounds from QCD multijet production
  - **Other orthogonal channels:**
    - MET + jets
    - ...

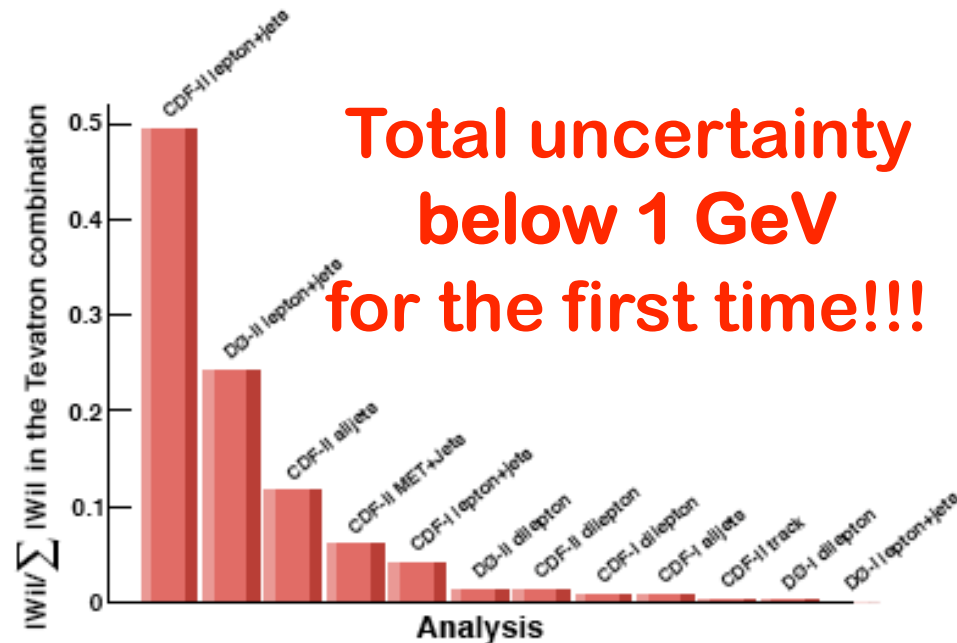
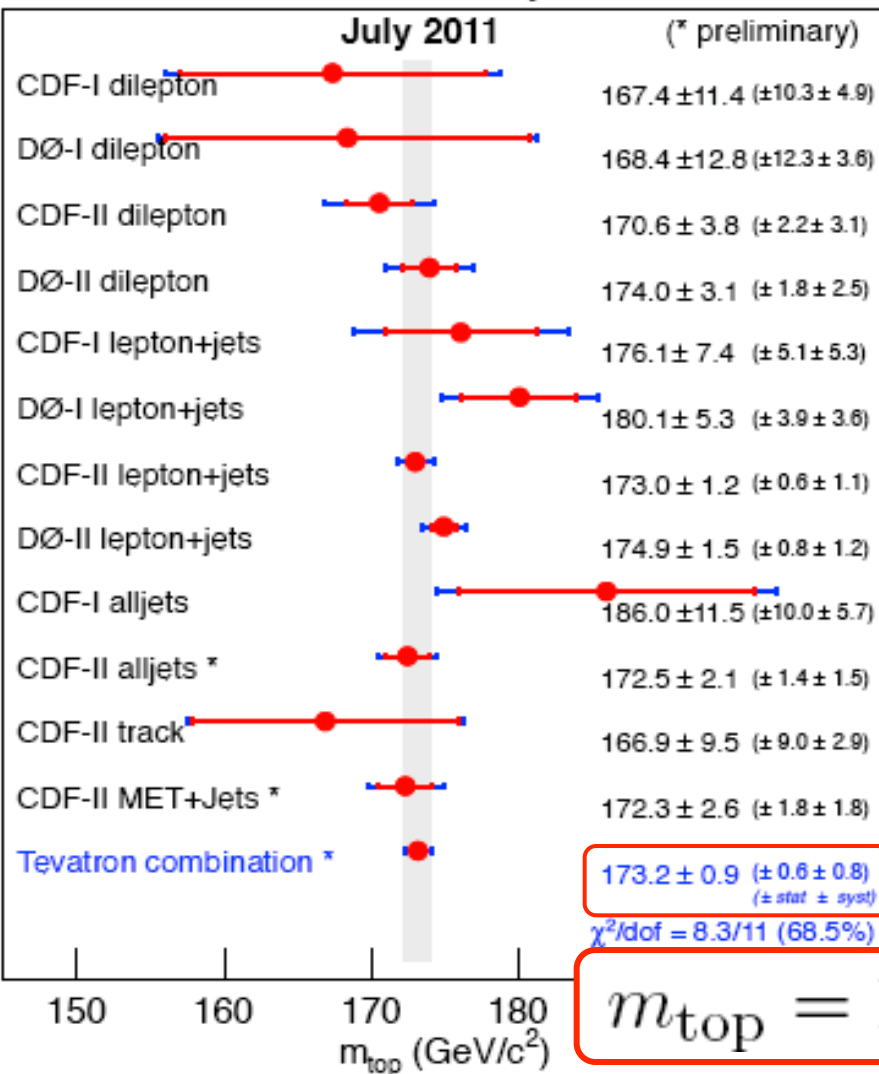
Property	Measurement	SM Prediction	Luminosity (fb <sup>-1</sup> )
$\sigma_{t\bar{t}}$ (for $M_t = 172.5$ GeV)	CDF: $7.5 \pm 0.31(\text{stat}) \pm 0.34(\text{syst}) \pm 0.15(\text{theory})$ pb D0: $7.56^{+0.63}_{-0.56}$ (stat + syst + lumi) pb	$7.46^{+0.48}_{-0.67}$ pb	up to 4.6 5.6
$\sigma_{tbq}$ (for $M_t = 172.5$ GeV)	CDF: $0.8 \pm 0.4$ pb ( $M_t = 175$ GeV) D0: $2.90 \pm 0.59$ pb	$2.26 \pm 0.12$ pb	3.2 5.4
$\sigma_{tb}$ (for $M_t = 172.5$ GeV)	CDF: $1.8^{+0.7}_{-0.5}$ pb ( $M_t = 175$ GeV) D0: $0.68^{+0.38}_{-0.35}$ pb	$1.04 \pm 0.04$ pb	3.2 5.4
Charge asymmetry	CDF: $0.158 \pm 0.074$ D0: $0.196 \pm 0.065$	0.06	5.3 5.4
spin correlation	CDF: $0.72 \pm 0.64(\text{stat}) \pm 0.26(\text{syst})$ D0: $0.66 \pm 0.23(\text{stat} + \text{syst})$	$0.777^{+0.027}_{-0.042}$	5.3 5.4
$M_t$	Tev: $173.2 \pm 0.9$ GeV	-	up to 5.8
$\sigma_{t\bar{t}\gamma}$	CDF: $0.18 \pm 0.08$ pb	$0.17 \pm 0.03$ pb	6.0
$ V_{tb} $	CDF: $ V_{tb}  = 0.91 \pm 0.11(\text{stat} + \text{syst}) \pm 0.07(\text{theory})$ D0: $ V_{tb}  = 1.02^{+0.10}_{-0.11}$	1	3.2 5.4
$R = B(t \rightarrow Wb)/B(t \rightarrow Wq)$	CDF: $> 0.61$ @ 95% CL D0: $0.90 \pm 0.04$	1	0.2 5.4
$\sigma(gg \rightarrow t\bar{t})/\sigma(p\bar{p} \rightarrow t\bar{t})$	CDF: $0.07^{+0.15}_{-0.07}$	0.18	1
$M_t - M_{\bar{t}}$	CDF: $-3.3 \pm 1.4(\text{stat}) \pm 1.0(\text{syst})$ GeV D0: $0.8 \pm 1.8(\text{stat}) \pm 0.5(\text{syst})$ GeV	0	5.6 3.6
W helicity fraction	Tev: $f_0 = 0.732 \pm 0.063(\text{stat}) \pm 0.052(\text{syst})$	0.7	up to 5.4
Charge	CDF: -4/3 excluded @ 95% CL D0: 4/3 excluded @ 92% CL	2/3	5.6 0.37
$\Gamma_t$	CDF: $< 7.6$ GeV @ 95% CL D0: $1.99^{+0.69}_{-0.55}$ GeV	1.26 GeV	4.3 up to 2.3



## Mass of the Top Quark

July 2011

(\* preliminary)

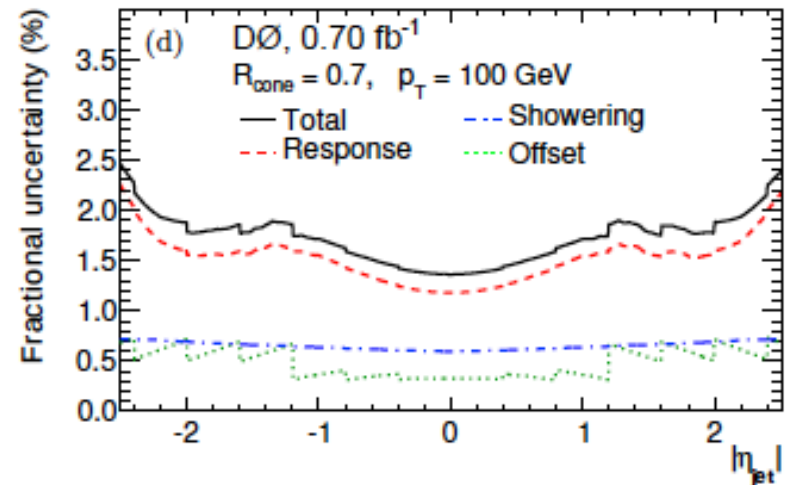
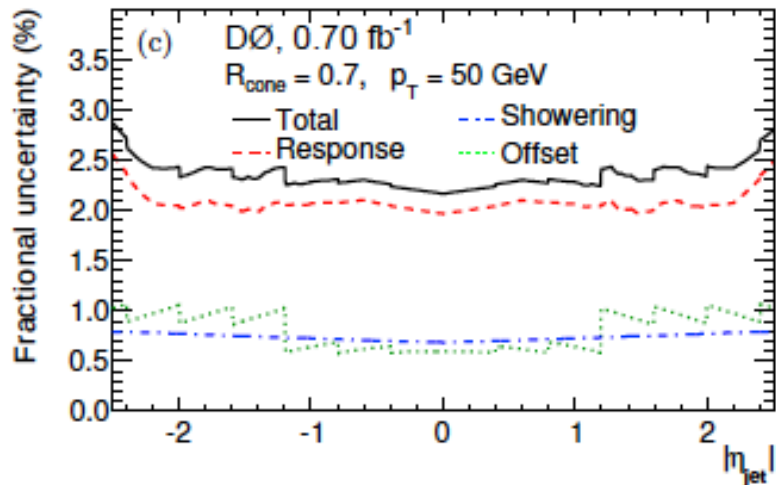
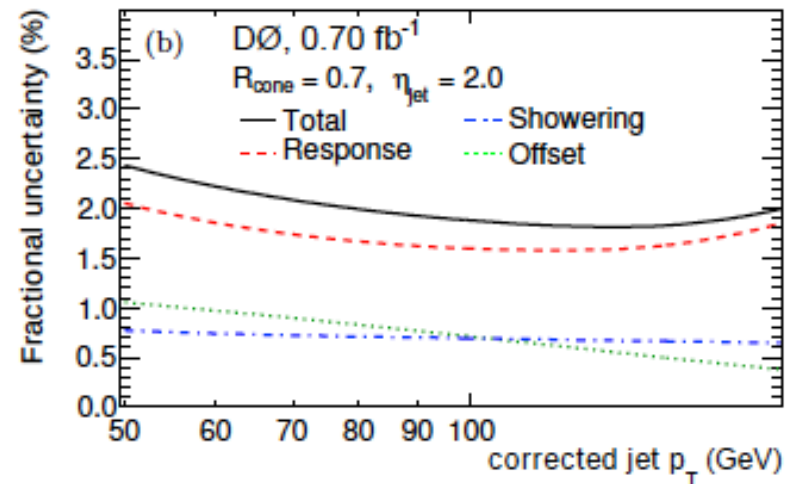
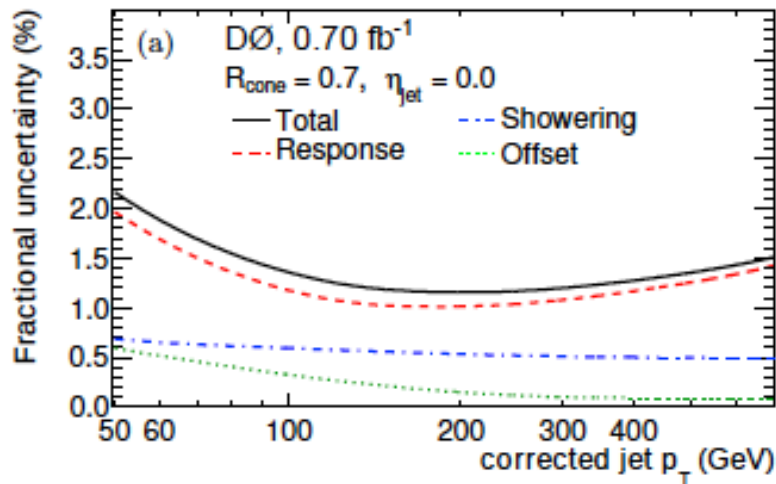


$$m_{\text{top}} = 173.2 \pm 0.6 (\text{stat}) \pm 0.8 (\text{syst})$$

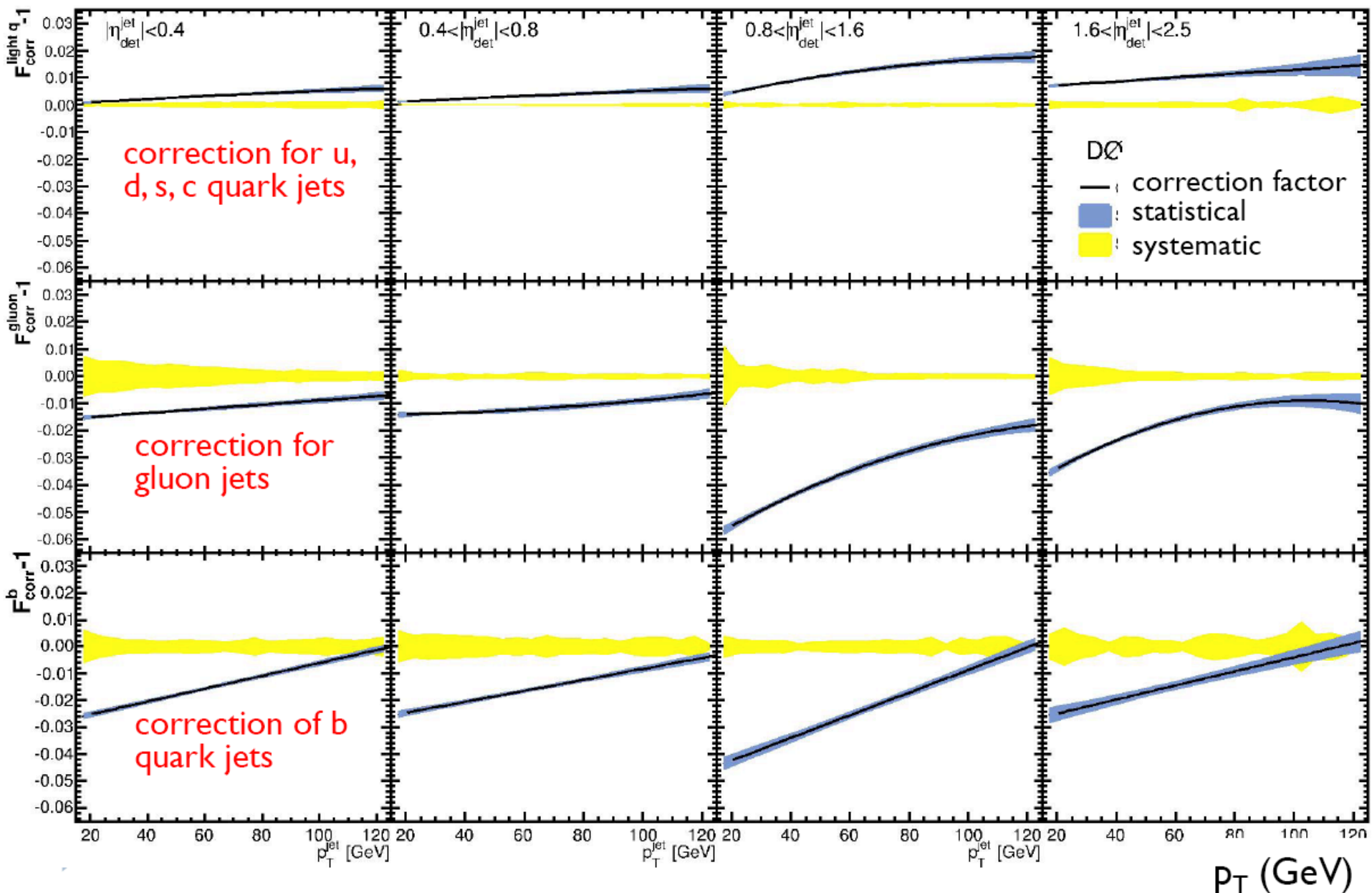
arXiv:1107.5255 [hep-ex]



- **Typical JES uncertainty 2-3 %**
  - → can lead to an uncertainty on  $m_{\text{top}}$  as large as **2 GeV!**



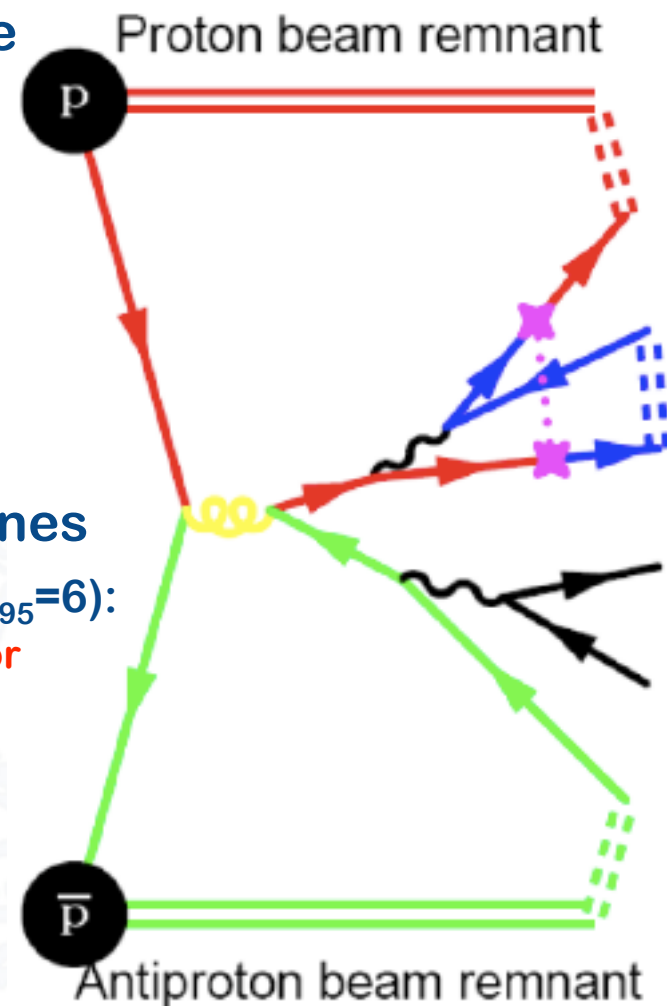
# Single particle response correction



- **Hadronisation and underlying event:**
  - Uncertainty for the current l+jets analysis: **0.58 GeV**
    - We evaluated this uncertainty by comparing
      - **alpgen+herwig** vs.
      - **alpgen+pythia** events
  - This is the **dominant** systematic uncertainty
  - It contains:
    - Statistical component
    - JES component
    - **The actual effects from hadronisation & UE**
  - → working out strategies to remove the former two
- **$Q^2$  vs  $p_T^2$  ordered shower:**
  - Currently not included in systematic uncertainties
    - Will cross-check:
      - **Pythia with D0 Tune A**
      - **Pythia with Perugia 2011C** (same CTEQ6L1 pdf)

- **Colour reconnection (CR)**

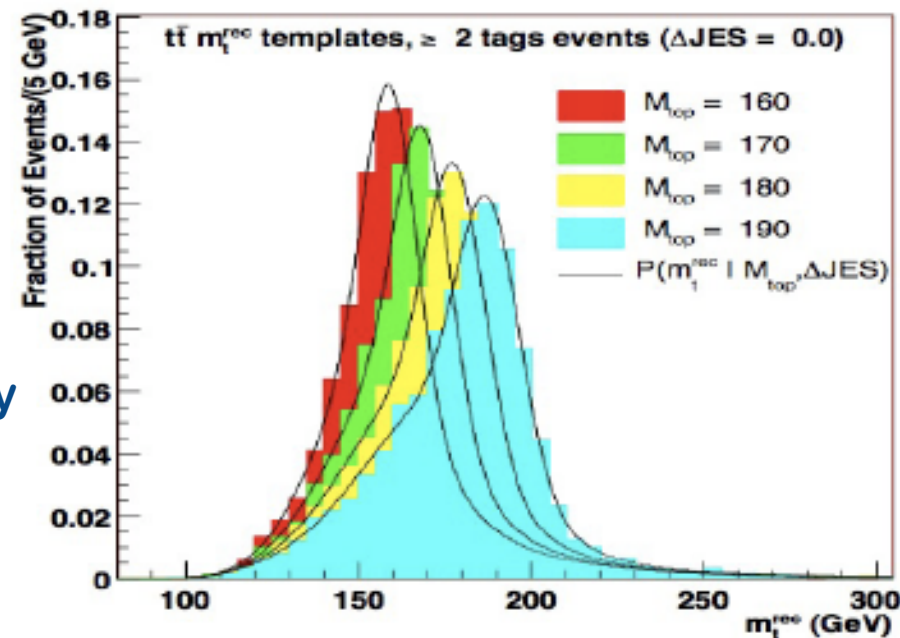
- could be an important systematic uncertainty
- cf. [arXiv:0807.3248] by Skands+Wicke
- **Hadronisation** regions of jets from **W** and **b** decay can **overlap**:
  - Possible effect on  $m_{\text{top}}$  due to colour reconnection
- Very few experimental handles to constrain CR effects...
- Currently compare Apro vs ACRpro tunes
  - This was pythia authors' first shot ( $\text{MSTP}_{95}=6$ ):
    - $P_{\text{keep}} = (1 - \zeta P_{78})^{n_{\text{int}}}$  : **probability for a string piece to survive the annealing**
      - $n_{\text{int}}$ : **# of p-pbar interactions in event**
      - $\zeta = 1$  (for ACRpro)
      - $P_{78} = 0.09$  (for ACRpro)
- → Looking at more realistic models



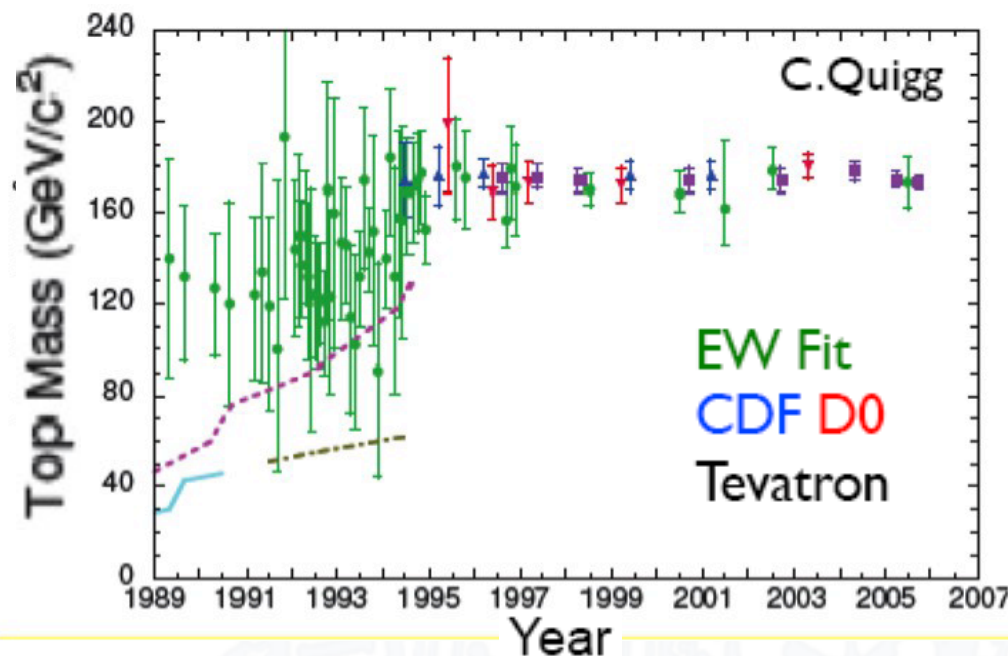
- **Higher order corrections:**
  - 0.10 +/- 0.25 GeV in the current l+jets analysis. Compare:
    - mc@nlo (+ herwig)
    - alpgen + herwig
- **Initial/final state radiation (ISR/FSR):**
  - 0.26 +/- 0.19 GeV in the current l+jets analysis.
  - Use pythia stand-alone with variations to:
    - $\alpha_s$  in the parton shower (ISR/FSR)
    - $\Lambda_{\text{QCD}}$  in the parton shower (ISR/FSR)
    - Derived from the  $p_T$  spectrum of  $Z \rightarrow \ell\ell$  events
      - This is possible for **ISR** (and of course FSR) only at the Tevatron: both are dominated by quark lines (LHC: ISR dominated by gluon lines!)
  - Look at other more realistic possibilities (alpgen-based) using the novel  $\phi^*$  variable in  $Z \rightarrow \ell\ell$  events



- The measurements shown today are based on:
  - Template method
  - Matrix Element method
- **Template method:**
  - Pick a set of variables  $x$  sensitive to  $m_{\text{top}}$ , e.g.  $x = m_{\text{top}}^{\text{reco}}$
  - Create “templates” = distributions in  $x$  using MC:
  - Maximise the likelihood of their consistence with the data
  - → **Advantages:**
    - few assumptions
    - fairly straight forward
    - combination of channels easy



- **1976: discovery of the Ypsilon at Fermilab**
  - indicates the existence of the top quark
  - from here on, the race for the top has begun!
- **1984: PETRA  $m_{\text{top}} > 23.3$  GeV**
- **1988: UA1  $m_{\text{top}} > 44$  GeV**
- **1990:**
  - TRISTAN  $m_{\text{top}} > 30.2$  GeV
  - SLC  $m_{\text{top}} > 40.7$  GeV
  - LEP  $m_{\text{top}} > 45.8$  GeV
  - UA1  $m_{\text{top}} > 60$  GeV
  - UA2  $m_{\text{top}} > 69$  GeV
- **1992: CDF  $m_{\text{top}} > 91$  GeV**
- **1994: DØ  $m_{\text{top}} > 128$  GeV**
- **1994: evidence of top quark from CDF**



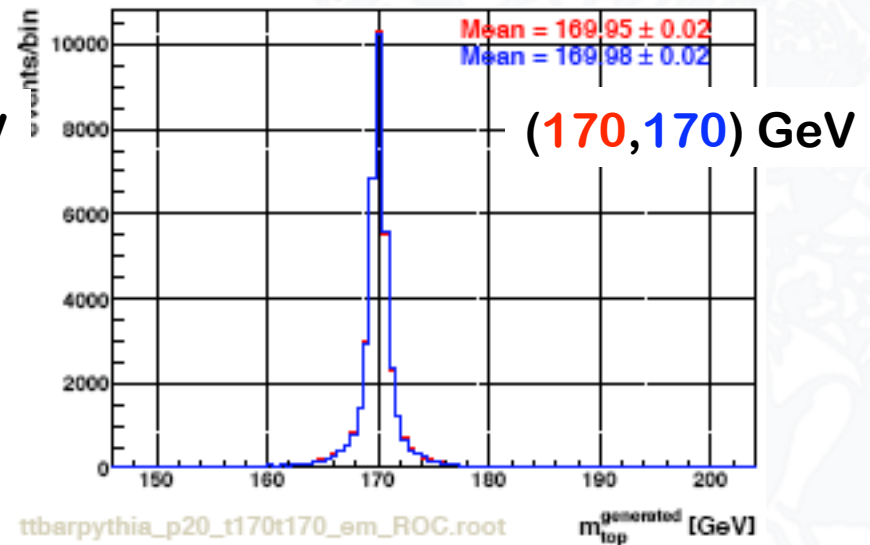
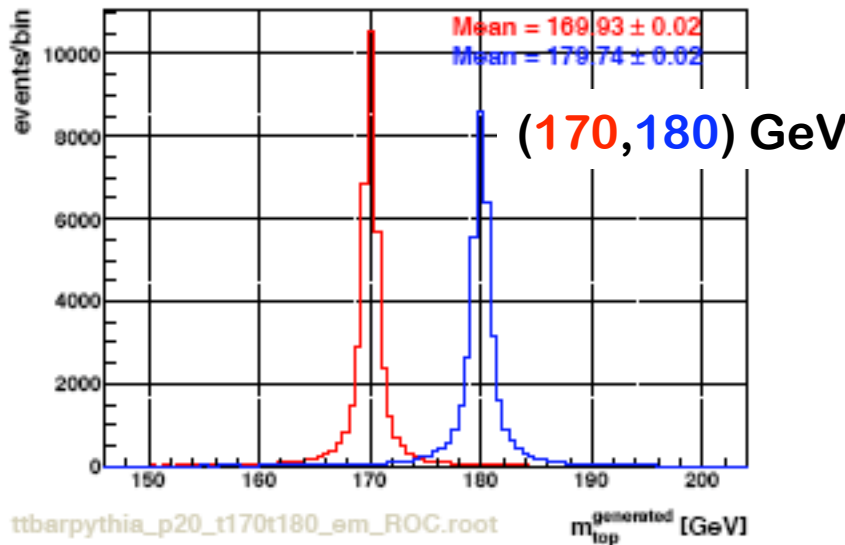
- **CPT invariance** is a necessary prerequisite for a **locally Lorentz-invariant QFT**
  - An established CPT invariance would be the end of not only the SM itself, but its theoretical footing!
- **If  $M_{\text{particle}} \neq M_{\text{antiparticle}} \rightarrow \text{CPT violated!}$** 
  - We have never tested this on a bare quark (status 2yrs ago)
- The top quark is the only known quark where this **test is possible**:
  - Hadronisation time scale  $\gg \tau_t = (3.3_{-0.9}^{+1.3}) \times 10^{-25} \text{ s}$

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  - Hadronisation time scale  $\gg \tau_t = (3.3^{+1.3}_{-0.9}) \times 10^{-25} \text{ s}$
- **First result (D0, 1 fb<sup>-1</sup>):** PRL 103, 132001 (2009)

$$\Delta m_t = 3.8 \pm 3.4(\text{stat}) \pm 1.2(\text{syst}) \text{ GeV}$$
- **First result from CDF (5.4 fb<sup>-1</sup>):** PRL 106, 152001 (2011)

$$\Delta m_t = -3.3 \pm 1.4(\text{stat}) \pm 1.0(\text{syst}) \text{ GeV}$$
  - $\rightarrow$  **LSJ effect?**

- In standard pythia, it is impossible to generate  $t\bar{t}$  events with  $M_t \neq M_{t\bar{t}}$ , modify pythia (6.413):
  - Allow for separate setting of  $M_t$ ,  $M_{t\bar{t}}$
  - Adjust description of all  $M_t$ ,  $M_{t\bar{t}}$  related kinematic quantities:
    - e.g. resonance widths  $\Gamma_t, \Gamma_{\bar{t}}$
  - Use standard CTEQ6L1 PDFs at scale:
    - $Q^2 = (p_T^{\text{scat}})^2 + \frac{1}{2} \{P_1^2 + P_2^2 + M_t^2 + M_{\bar{t}}^2\}$



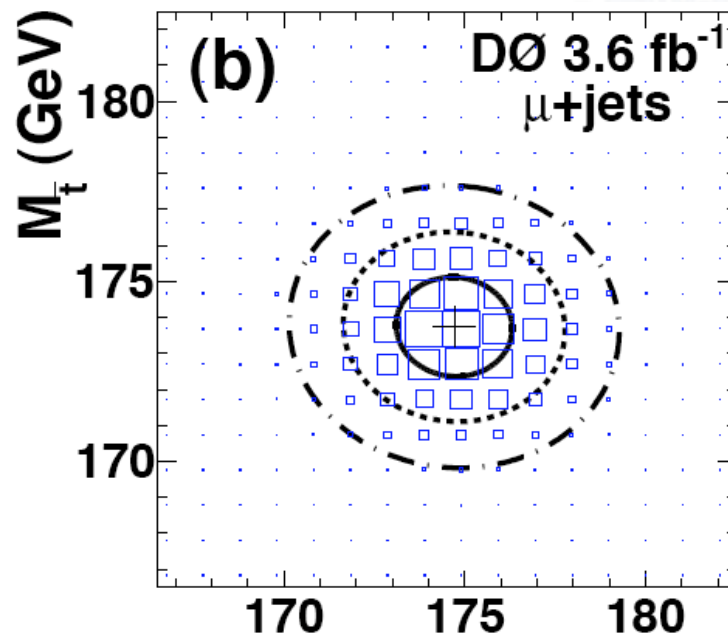
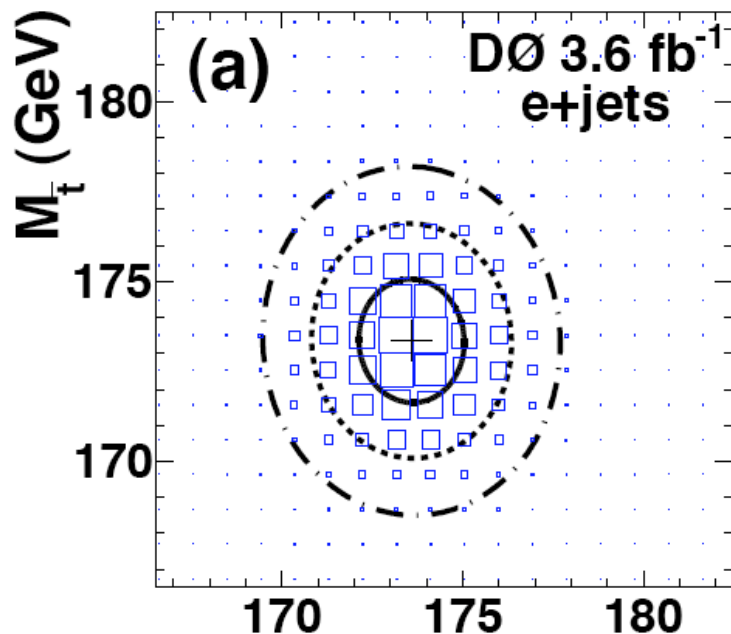


- Use the most statistically sensitive technique – ME

- $P(m_{\text{top}}, k_{\text{JES}}) \rightarrow P(m_t, m_{t\text{bar}})$ 
  - **Direct** and **independent** measurement of  $m_t$  and  $m_{t\text{bar}}$ !
- Use lepton charge to tag  $t$  and  $t\text{bar}$ :

$$\Delta m_t = 0.8 \pm 1.8(\text{stat}) \pm 0.5(\text{syst}) \text{ GeV}$$

*Relative  
precision:  
1%*



PRD 84, 052005 (2011)  $M_t$  (GeV)

$M_t$  (GeV)

- Apply the **ME method** to the **dilepton channel**

- Additional challenge: the  $t\bar{t}$  system is kinematically 1x underconstrained if  $m_{\text{top}}$  is a free parameter!

- → assume prior for  $p_T(t\bar{t})$  from MC simulation
- → integrate over neutrino momenta (with Jacobian)

- The ME used here is:

$$P_{t\bar{t}}(x; m_t) = \frac{1}{\sigma_{\text{obs}}(m_t)} \cdot \sum_{i=1}^8 \int dq_1 dq_2 f_{\text{PDF}}(q_1) f_{\text{PDF}}(q_2) \frac{(2\pi)^4 |M(y; m_t)|^2}{q_1 q_2 s} d\Phi_6 W(x, y) W(p_T^{t\bar{t}}).$$

- Dominant **background: Z+2jets** processes

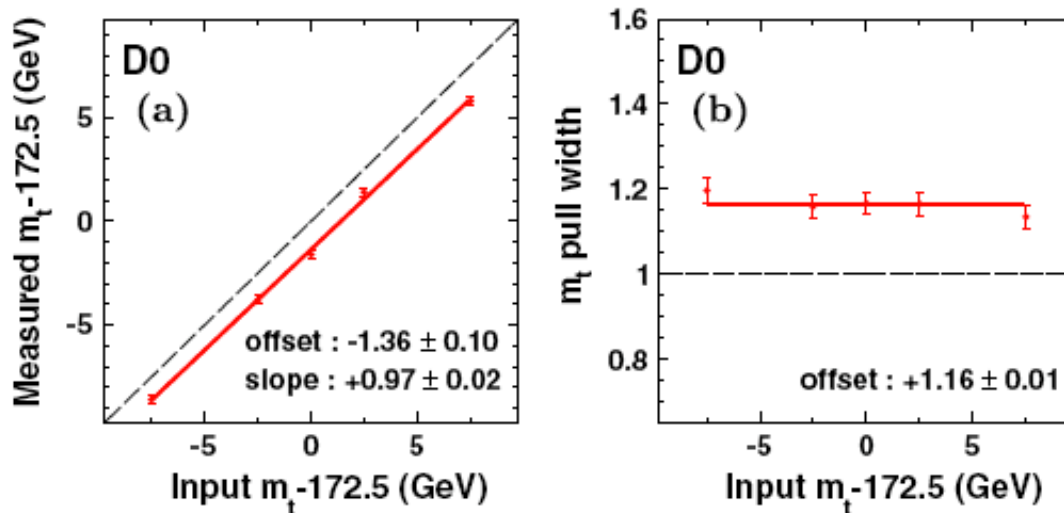
- → calculate  $P_{\text{bkg}} = P_{\text{Z+2jets}}$  using VECBOS

- **No in-situ calibration of the JES** possible

- Large systematic uncertainty from JES calibration
- Similarly large systematic uncertainty from b-quark JES

*Phys. Rev. Lett.* **107**, 082004 (2011)

## Method calibration:

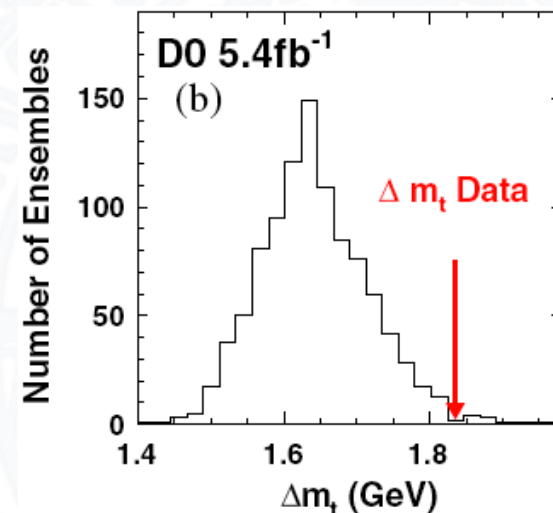


## Final result:

$$m_t = 174.0 \pm 1.8(\text{stat}) \pm 2.4(\text{syst}) \text{ GeV}$$

Relative uncertainty: 1.8%!

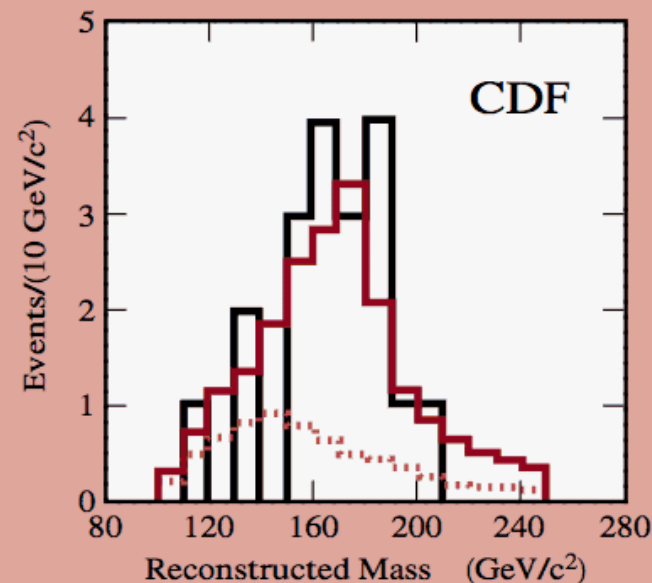
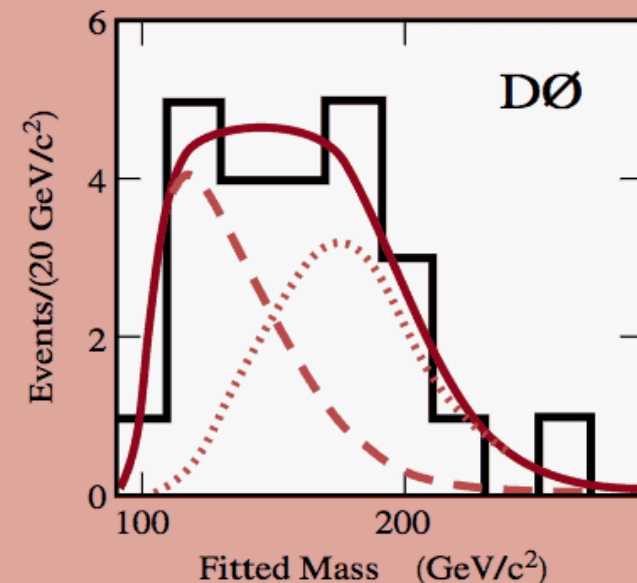
*Phys. Rev. Lett. 107, 082004 (2011)*



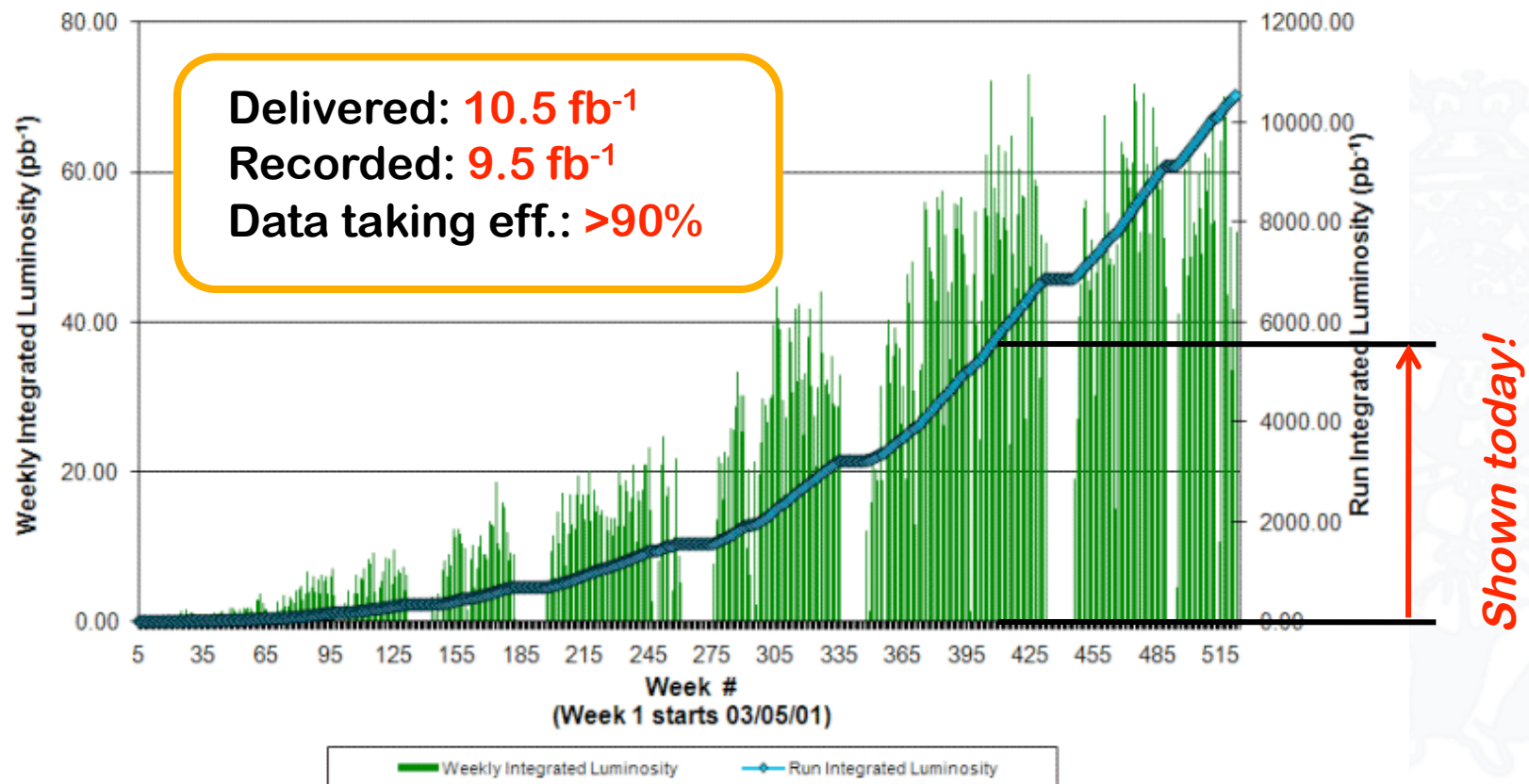
- **DØ (50 pb<sup>-1</sup>, 4.6σ):**
  - $\sigma = 6.4 \pm 2.2$  pb
  - $m_{\text{top}} = 199 \pm 30$  GeV



- **CDF (67 pb<sup>-1</sup>, 4.8σ):**
  - $\sigma = 6.8^{+3.6}_{-2.4}$  pb
  - $m_{\text{top}} = 176 \pm 13$  GeV



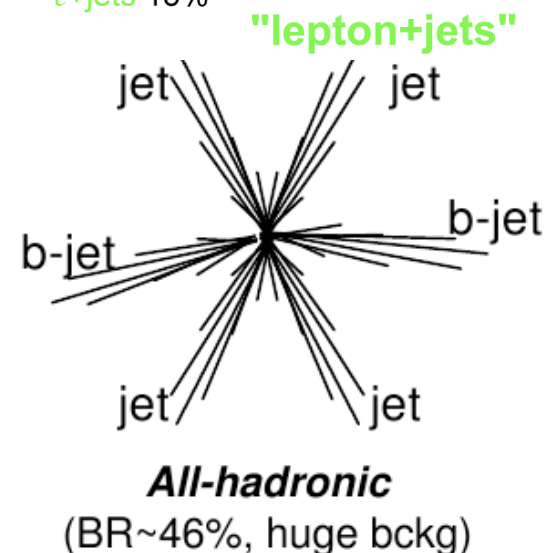
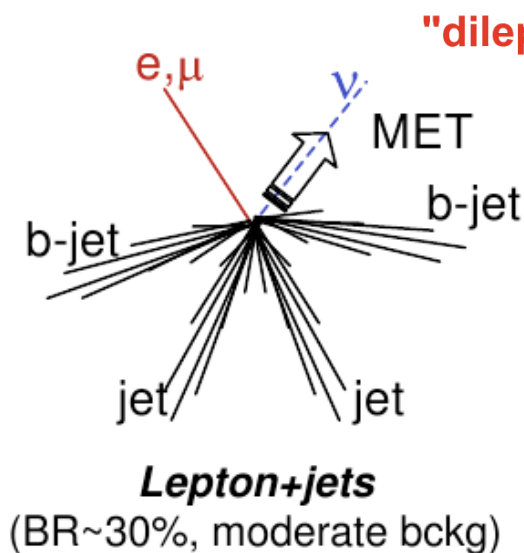
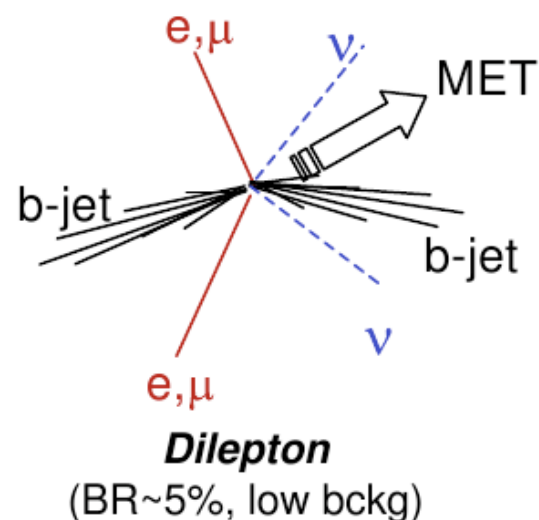
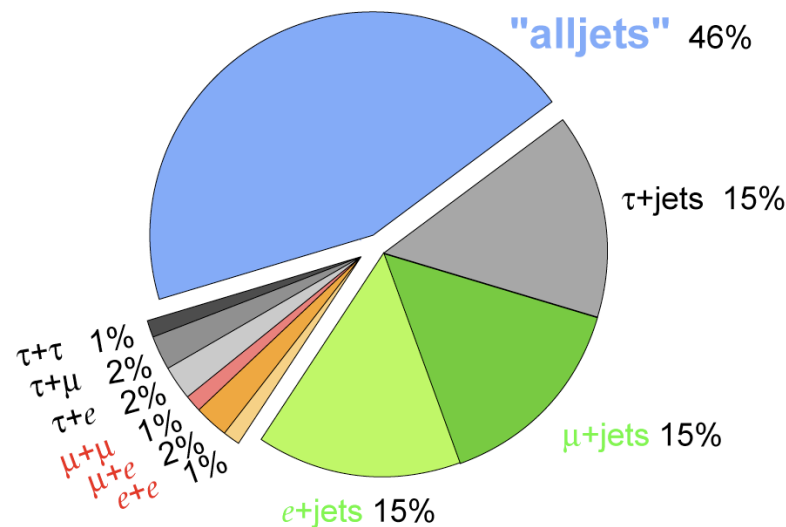
- Tevatron has shown a great performance in FY 2010!
- We keep enlarging our calibration samples
  - Better handles on experimental uncertainties:
    - e.g. Jet Energy Scale (JES), Jet Energy Resolution, etc.





- In the SM:**
  - $|V_{tb}| = 0.9990-0.9992$   
@ 95% C.L. assuming  
3 CKM generations
- Characterise  $t\bar{t}$  final states by top decays!**

**Top Pair Branching Fractions**



## Dilepton

2 high- $p_T$  leptons

Missing  $E_T$

2 jets

$\geq 0$  b-tags

S/B:

## Lepton+jets

1 high- $p_T$  lepton ( $>20$  GeV)

Missing  $E_T$  ( $>40$  GeV)

4 jets ( $> 20$  GeV)

$\geq 1$  b-tag

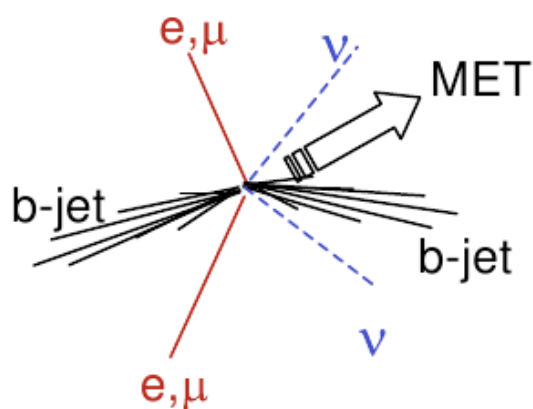
## All-hadronic

No leptons

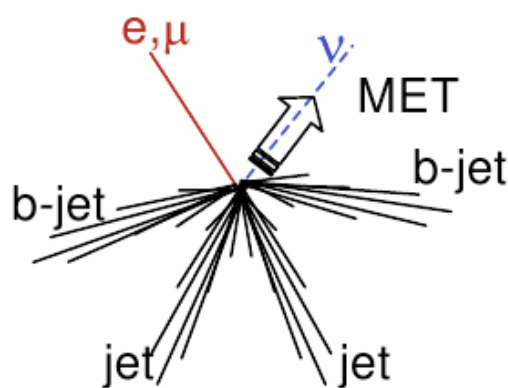
No missing  $E_T$

6 jets

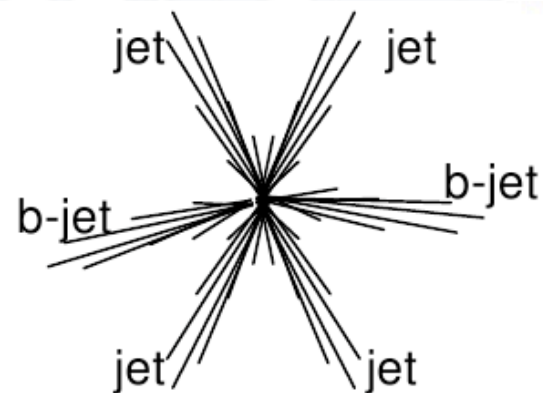
$\geq 1$  b-tag



**Dilepton**  
 (BR~5%, low bckg)



**Lepton+jets**  
 (BR~30%, moderate bckg)



**All-hadronic**  
 (BR~46%, huge bckg)

