

Charmless Two-Body B Decays Involving a Tensor Meson

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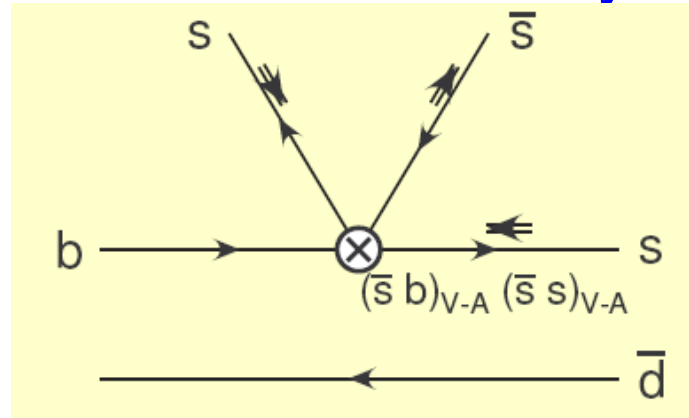


Outline

- ◆ Polarization puzzles in $B \rightarrow V V$
---- SM or New-Physics
- ◆ B decays involving a tensor meson
----further test: SM or New-Physics
- ◆ Conclusion

Introduction

■ Polarization puzzle in charmless $\bar{B} \rightarrow VV$ decays



$$H_{00} : H_{--} : H_{++} = 1 : \frac{\Lambda}{m_b} : \left(\frac{\Lambda}{m_b} \right)^2$$

In transversity basis $A_{\perp} = (H^{--} + H^{++}) / \sqrt{2}$, $A_{\parallel} = (H^{--} - H^{++}) / \sqrt{2}$

$$f_T \equiv f_{\parallel} + f_{\perp} = 1 - f_L = O(m_V^2 / m_B^2), \quad f_{\parallel} / f_{\perp} = 1 + O(m_V / m_B)$$

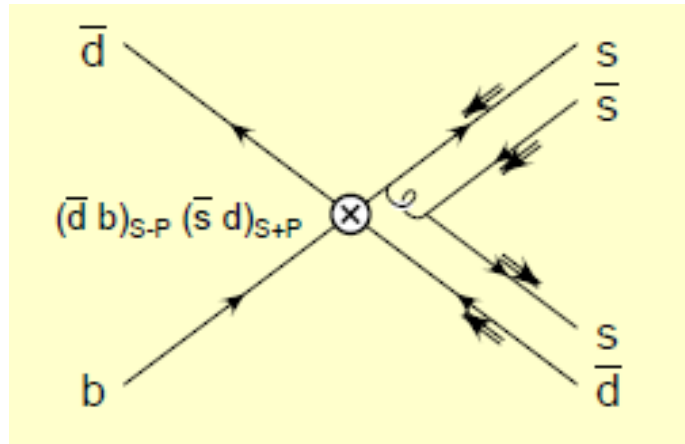
Why is f_T sizable ~ 0.5 in $B \rightarrow K^* \phi$ decays ?

■ Search of new physics in $B \rightarrow VV$ decays ?

Explanation within the SM: Annihilation

In SM, the Annihilation effect is important:

■ Annihilation $H_{00}: H_{--}: H_{++} = \frac{1}{m_b^2} \ln^2 \frac{m_b}{\Lambda} : \frac{1}{m_b^2} \ln^2 \frac{m_b}{\Lambda} : \frac{1}{m_b^4}$ (Kagan, 04)



Annihilation topology: \Rightarrow overall $1/m_b$

Helicity-flips: \Rightarrow $1/m_b$

Parametrization $\int_0^1 \frac{dx}{x} = \ln \frac{m_B}{\Lambda} (1 + \rho_A e^{i\phi_A})$

B → K* φ (without annihilation)

$$\mathcal{A}_{\bar{B} \rightarrow \bar{K}^* \phi}^h \approx V_c (\alpha_3^h + \alpha_4^{c,h} + \beta_3^h - \frac{1}{2} \alpha_{3,EW}^h) X_{\bar{K}^* \phi}^h.$$

$$\alpha_3 = \mathbf{a}_3 + \mathbf{a}_5, \quad \alpha_4 = \mathbf{a}_4 - r_\chi^\phi \mathbf{a}_6, \quad \alpha_{3,EW} = \mathbf{a}_9 + \mathbf{a}_7, \quad \beta_3 = \text{penguin ann}$$

$$X_{\bar{K}^* \phi}^h = \langle \phi | J_\mu | 0 \rangle \langle \bar{K}^* | J^\mu | B \rangle, \quad |X_{\bar{K}^* \phi}^0| : |X_{\bar{K}^* \phi}^-| : |X_{\bar{K}^* \phi}^+| = 1 : 0.35 : 0.007$$

	h=0		h=-			h=0		h=-	
$\alpha_3(K^* \phi)$	<u>0.005</u>	- 0.001i	<u>-0.004</u>	- 0.001i	$\alpha_{3,EW}(K^* \phi)$	<u>-0.009</u>	- 0.000i	<u>0.002</u>	- 0.000i
$\alpha_4^u(K^* \phi)$	<u>-0.022</u>	- 0.014i	<u>-0.047</u>	- 0.016i	$\alpha_4^c(K^* \phi)$	<u>-0.027</u>	- 0.014i	<u>-0.049</u>	- 0.006i

Coefficients are helicity dependent !

PRD, 2008, Hai-Yang Cheng, KCY

$$\frac{\mathcal{A}^-}{\mathcal{A}^0} \Big|_{\bar{B} \rightarrow \bar{K}^* \phi} \approx \left(\frac{\alpha_3^- + \alpha_4^{c,-} - \frac{1}{2} \alpha_{3,EW}^-}{\alpha_3^0 + \alpha_4^{c,0} - \frac{1}{2} \alpha_{3,EW}^0} \right) \left(\frac{X_{\bar{K}^* \phi}^-}{X_{\bar{K}^* \phi}^0} \right) \quad \text{with } \beta_3 = 0$$

constructive (destructive) interference in A⁻ (A⁰) ⇒ f_L ~ 0.58

NLO corrections alone will bring down f_L significantly !

Br ~ 4.3 * 10⁻⁶ (without annihilation), too small compared with data

Although f_{\perp} is reduced to 60% level, polarization puzzle is not resolved as the predicted rate, $BR \sim 4.3 \cdot 10^{-6}$, is too small compared to the data, $\sim 10 \cdot 10^{-6}$ for $B \rightarrow K^* \phi$

$$P^c = [a_4^c + r_{\chi} a_6^c]_{SD} + \beta_3^c + \dots$$

penguin annihilation

■ Br & f_{\perp} are fit by adjusting $\Rightarrow \rho_A \simeq 0.65, \phi_A \simeq -53^{\circ}$

Decay	\mathcal{B}		f_L		f_{\perp}	
	Theory	Expt	Theory	Expt	Theory	Expt
$B^- \rightarrow K^{*-} \phi^c$	$10.0^{+1.4+12.3}_{-1.3-6.1}$	10.0 ± 1.1	$0.49^{+0.51}_{-0.42}$	0.50 ± 0.05	$0.25^{+0.21}_{-0.25}$	0.20 ± 0.05
$\bar{B}^0 \rightarrow \bar{K}^{*0} \phi$	$9.5^{+1.3+11.9}_{-1.2-5.9}$	9.5 ± 0.8	$0.50^{+0.50}_{-0.42}$	0.484 ± 0.034	$0.25^{+0.21}_{-0.25}$	0.256 ± 0.032

$$f_{\parallel} \doteq f_{\perp} \doteq 0.25$$

Parameter	$h = 0$	$h = -$	Parameter	$h = 0$	$h = -$
$\alpha_1(\rho K^*)$	$0.96 + 0.02i$	$1.11 + 0.03i$	$\alpha_{3,EW}(K^*\rho)$	$-0.009 - 0.000i$	$0.005 - 0.000i$
$\alpha_2(K^*\rho)$	$0.28 - 0.08i$	$-0.17 - 0.17i$	$\alpha_{4,EW}(K^*\rho)$	$-0.002 + 0.001i$	$0.001 + 0.001i$
$\alpha_4^u(\rho K^*)$	$-0.022 - 0.014i$	$-0.048 - 0.016i$	$\beta_3(\rho K^*)$	$0.015 - 0.020i$	$-0.012 + 0.016i$
$\alpha_4^c(\rho K^*)$	$-0.026 - 0.014i$	$-0.050 - 0.006i$			

$$\frac{\mathcal{A}^-}{\mathcal{A}^0} \Big|_{\bar{B}^0 \rightarrow \bar{K}^{*0} \rho^0} \approx \begin{pmatrix} \alpha_4^{c,-} - \frac{3}{2} \alpha_{3,EW}^- \\ \alpha_4^{c,0} - \frac{3}{2} \alpha_{3,EW}^0 \end{pmatrix} \begin{pmatrix} X_{\bar{K}^* \rho}^- \\ X_{\bar{K}^* \rho}^0 \end{pmatrix}$$

$$\frac{\mathcal{A}^-}{\mathcal{A}^0} \Big|_{B^- \rightarrow K^{*-} \rho^0} \approx \begin{pmatrix} \alpha_4^{c,-} + \frac{3}{2} \alpha_{3,EW}^- \\ \alpha_4^{c,0} + \frac{3}{2} \alpha_{3,EW}^0 \end{pmatrix} \begin{pmatrix} X_{\bar{K}^* \rho}^- \\ X_{\bar{K}^* \rho}^0 \end{pmatrix}$$

constructive
destructive
destructive
constructive

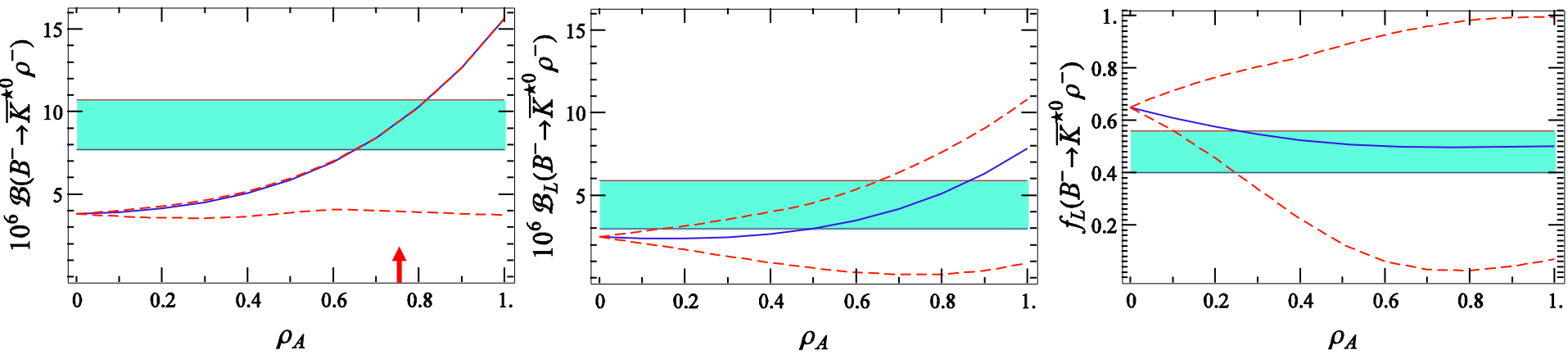
with $\beta_3=0$

$\Rightarrow f_L(K^{*-} \rho^0) = 0.96, f_L(\bar{K}^{*0} \rho^0) = 0.47$ (=0.91 if a_i^h are helicity indep)

Decay	Expt		(i)	
	\mathcal{B}	f_L	\mathcal{B}	f_L
$B^- \rightarrow \bar{K}^{*0} \rho^-$	<u>9.2 ± 1.5</u>	0.48 ± 0.08	<u>3.8</u>	0.78
$B^- \rightarrow K^{*-} \rho^0$	< 6.1	$0.96^{+0.06}_{-0.16}$	3.6	<u>0.96</u>
$\bar{B}^0 \rightarrow K^{*-} \rho^+$	< 12	—	3.6	0.84
$\bar{B}^0 \rightarrow \bar{K}^{*0} \rho^0$	<u>5.6 ± 1.6</u>	<u>0.57 ± 0.12</u>	<u>1.1</u>	<u>0.47</u>

Without Annihilation

But, the predicted rates for $K^{*-} \rho^0$ & $\bar{K}^{*0} \rho^0$ are too small !



Choose $K^{*0}\rho^-$ as an input, a fit to BR and f_L yields $\rho_A \simeq 0.78$, $\phi_A \simeq -43^\circ$, slightly different from the ones $\rho_A \simeq 0.65$, $\phi_A \simeq -53^\circ$ inferred from $B \rightarrow K^*\phi$

Process dependent

Decay	\mathcal{B}		f_L		f_\perp	
	Theory	Expt	Theory	Expt	Theory	Expt
$B^- \rightarrow \bar{K}^{*0}\rho^-$ ^a	$9.2^{+1.2+3.6}_{-1.1-5.4}$	9.2 ± 1.5	$0.48^{+0.52}_{-0.40}$	0.48 ± 0.08	$0.26^{+0.20}_{-0.26}$	
$B^- \rightarrow K^{*-}\rho^0$	$5.5^{+0.6+1.3}_{-0.5-2.5}$	4.6 ± 1.1	$0.67^{+0.31}_{-0.48}$	0.78 ± 0.12	$0.16^{+0.24}_{-0.15}$	
$\bar{B}^0 \rightarrow K^{*-}\rho^+$	$8.9^{+1.1+4.8}_{-1.0-5.5}$	< 12	$0.53^{+0.45}_{-0.32}$		$0.24^{+0.16}_{-0.22}$	
$\bar{B}^0 \rightarrow \bar{K}^{*0}\rho^0$	$4.6^{+0.6+3.5}_{-0.5-3.5}$	3.4 ± 1.0	$0.39^{+0.60}_{-0.31}$	0.40 ± 0.14	$0.30^{+0.15}_{-0.30}$	

$$f_L(K^{*-}\rho^0) > f_L(K^{*-}\rho^+) > f_L(\bar{K}^{*0}\rho^-) > f_L(\bar{K}^{*0}\rho^0)$$

Tree-dominated VV modes

Decay	\mathcal{B}		f_L		f_\perp	
	Theory	Expt	Theory	Expt	Theory	Expt
$B^- \rightarrow \rho^- \rho^0$	$20.0^{+4.0+2.0}_{-1.9-0.9}$	$24.0^{+1.9}_{-2.0}$	$0.96^{+0.02}_{-0.02}$	0.950 ± 0.016	0.02 ± 0.01	
$\overline{B}^0 \rightarrow \rho^+ \rho^-$	$25.5^{+1.5+2.4}_{-2.6-1.5}$	$24.2^{+3.1}_{-3.2}$	$0.92^{+0.01}_{-0.02}$	$0.978^{+0.025}_{-0.022}$	$0.04^{+0.01}_{-0.00}$	
$\overline{B}^0 \rightarrow \rho^0 \rho^0$	$0.9^{+1.5+1.1}_{-0.4-0.2}$	$0.73^{+0.27}_{-0.28}$	$0.92^{+0.06}_{-0.36}$	$0.75^{+0.12}_{-0.15}$	$0.04^{+0.14}_{-0.03}$	
$B^- \rightarrow \rho^- \omega$	$19.2^{+3.3+1.7}_{-1.6-1.0}$	15.9 ± 2.1	$0.96^{+0.02}_{-0.02}$	0.90 ± 0.06	0.02 ± 0.01	
$\overline{B}^0 \rightarrow \rho^0 \omega$	$0.1^{+0.1+0.4}_{-0.1-0.0}$	< 1.5	$0.55^{+0.47}_{-0.29}$		$0.22^{+0.16}_{-0.23}$	

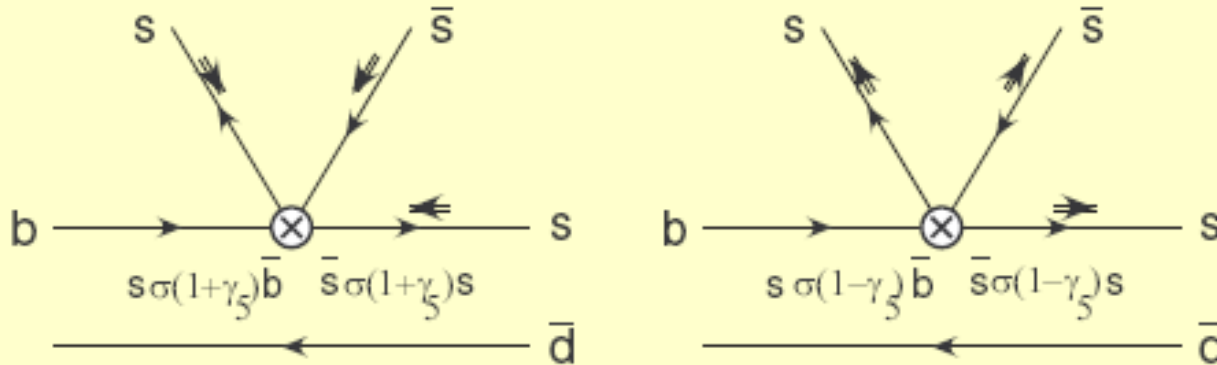
- Longitudinal amplitude dominates tree-dominated decays except for $\rho^0 \omega$
- Predicted $B \rightarrow \rho \rho, \omega \rho$ rates agree with the data.

H.Y. Cheng & KCY, PRD, 2008 vs. data (2010)

Central values correspond to $\rho_A = \phi_A = 0$

Scenario with New Physics

Possible New Physics



$$\otimes \bar{s} \sigma^{\mu\nu} (1 + \gamma_5) b \bar{s} \sigma_{\mu\nu} (1 + \gamma_5) s, \bar{s} (1 + \gamma_5) b \bar{s} (1 + \gamma_5) s$$

$$\bar{H}_{00} : \bar{H}_{--} : \bar{H}_{++} \sim \mathcal{O}(1/m_b) : \mathcal{O}(1) : \mathcal{O}(1/m_b^2)$$

$$\otimes \bar{s} \sigma^{\mu\nu} (1 - \gamma_5) b \bar{s} \sigma_{\mu\nu} (1 - \gamma_5) s, \bar{s} (1 - \gamma_5) b \bar{s} (1 - \gamma_5) s$$

$$\bar{H}_{00} : \bar{H}_{--} : \bar{H}_{++} \sim \mathcal{O}(1/m_b) : \mathcal{O}(1/m_b^2) : \mathcal{O}(1)$$

TENSOR operators can be related to the SCALAR operators by Fierz transformation.

Phys. Rev. D71, 094002 (2005), KCY& Das

See also works by Alex Kagan; C.S. Kim, Y.D. Yang;

Table 2: Possible NP operators and their candidacy in satisfying the anomaly resolution criteria. We have adopted the convention $\Gamma_1 \otimes \Gamma_2 \equiv \bar{s}\Gamma_1 b \bar{s}\Gamma_2 s$.

Model	Operators	H_{00}	H_{--}	H_{++}	Choice
SM	$\gamma^\mu(1 - \gamma_5) \otimes \gamma_\mu(1 \mp \gamma_5)$	$\mathcal{O}(1)$	$\mathcal{O}(1/m_b)$	$\mathcal{O}(1/m_b^2)$	
NP	$\gamma^\mu(1 + \gamma_5) \otimes \gamma_\mu(1 + \gamma_5)$	$\mathcal{O}(1)$	$\mathcal{O}(1/m_b^2)$	$\mathcal{O}(1/m_b)$	N
NP	$\gamma^\mu(1 + \gamma_5) \otimes \gamma_\mu(1 - \gamma_5)$	$\mathcal{O}(1)$	$\mathcal{O}(1/m_b^2)$	$\mathcal{O}(1/m_b)$	N
NP	$(1 + \gamma_5) \otimes (1 + \gamma_5)$	$\mathcal{O}(1/m_b)$	$\mathcal{O}(1)$	$\mathcal{O}(1/m_b^2)$	Y
NP	$(1 - \gamma_5) \otimes (1 - \gamma_5)$	$\mathcal{O}(1/m_b)$	$\mathcal{O}(1/m_b^2)$	$\mathcal{O}(1)$	Y
NP	$(1 + \gamma_5) \otimes (1 - \gamma_5)$	$\mathcal{O}(1)$	$\mathcal{O}(1/m_b^2)$	$\mathcal{O}(1/m_b)$	N
NP	$(1 - \gamma_5) \otimes (1 + \gamma_5)$	$\mathcal{O}(1)$	$\mathcal{O}(1/m_b)$	$\mathcal{O}(1/m_b^2)$	N
NP	$\sigma^{\mu\nu}(1 + \gamma_5) \otimes \sigma_{\mu\nu}(1 + \gamma_5)$	$\mathcal{O}(1/m_b)$	$\mathcal{O}(1)$	$\mathcal{O}(1/m_b^2)$	Y
NP	$\sigma^{\mu\nu}(1 - \gamma_5) \otimes \sigma_{\mu\nu}(1 - \gamma_5)$	$\mathcal{O}(1/m_b)$	$\mathcal{O}(1/m_b^2)$	$\mathcal{O}(1)$	Y
NP	$\sigma^{\mu\nu}(1 + \gamma_5) \otimes \sigma_{\mu\nu}(1 - \gamma_5)$	$\mathcal{O}(1)$	$\mathcal{O}(1/m_b^2)$	$\mathcal{O}(1/m_b)$	N
NP	$\sigma^{\mu\nu}(1 - \gamma_5) \otimes \sigma_{\mu\nu}(1 + \gamma_5)$	$\mathcal{O}(1)$	$\mathcal{O}(1/m_b)$	$\mathcal{O}(1/m_b^2)$	N

Two-body B decays
involving a tensor meson

Light-cone distribution amplitudes for a tensor meson

chiral-even

$$\langle T(P, \lambda) | \bar{q}_1(y) \gamma_\mu q_2(x) | 0 \rangle = -i f_T m_T^2 \int_0^1 du e^{i(uPy + \bar{u}Px)} \left\{ P_\mu \frac{\epsilon_{\alpha\beta}^{(\lambda)*} z^\alpha z^\beta}{(Pz)^2} \Phi_{\parallel}^T(u) + \left(\frac{\epsilon_{\mu\alpha}^{(\lambda)*} z^\alpha}{Pz} - P_\mu \frac{\epsilon_{\beta\alpha}^{(\lambda)*} z^\beta z^\alpha}{(Pz)^2} \right) g_v(u) - \frac{1}{2} z_\mu \frac{\epsilon_{\alpha\beta}^{(\lambda)*} z^\alpha z^\beta}{(Pz)^3} m_T^2 \bar{g}_3(u) + \mathcal{O}(z^2) \right\},$$

$$\langle T(P, \lambda) | \bar{q}_1(y) \gamma_\mu \gamma_5 q_2(x) | 0 \rangle = -i f_T m_T^2 \int_0^1 du e^{i(uPy + \bar{u}Px)} \epsilon_{\mu\nu\alpha\beta} z^\nu P^\alpha \epsilon_{(\lambda)}^{*\beta\delta} z^\delta \frac{1}{2Pz} g_a(u)$$

chiral-odd

$$\langle T(P, \lambda) | \bar{q}_1(y) \sigma_{\mu\nu} q_2(x) | 0 \rangle = -f_T^\perp m_T \int_0^1 du e^{i(uPy + \bar{u}Px)} \left\{ \left[\epsilon_{\mu\alpha}^{(\lambda)*} z^\alpha P_\nu - \epsilon_{\nu\alpha}^{(\lambda)*} z^\alpha P_\mu \right] \frac{1}{Pz} \Phi_{\perp}^T(u) + (P_\mu z_\nu - P_\nu z_\mu) \frac{m_T^2 \epsilon_{\alpha\beta}^{(\lambda)*} z^\alpha z^\beta}{(Pz)^3} \bar{h}_t(u) + \frac{1}{2} \left[\epsilon_{\mu\alpha}^{(\lambda)*} z^\alpha z_\nu - \epsilon_{\nu\alpha}^{(\lambda)*} z^\alpha z_\mu \right] \frac{m_T^2}{(Pz)^2} \bar{h}_3(u) + \mathcal{O}(z^2) \right\},$$

twist-2: $\Phi_{\parallel}, \Phi_{\perp}$

twist-3: g_v, g_a, h_t, h_s

twist-4: g_3, h_3

$$\langle T(P, \lambda) | \bar{q}_1(y) q_2(x) | 0 \rangle = -f_T^\perp m_T^3 \int_0^1 du e^{i(uPy + \bar{u}Px)} \frac{\epsilon_{\alpha\beta}^{(\lambda)*} z^\alpha z^\beta}{2Pz} h_s(u)$$

3P_2 tensor meson

Due to G -parity, Φ_{\perp} , $h_{\parallel}^{(t)}$, $h_{\parallel}^{(p)}$, Φ_{\parallel} , $g_{\perp}^{(v)}$, $g_{\perp}^{(a)}$ are antisymmetric with the replacement $u \rightarrow 1-u$ in $SU(3)$ limit

$$\int_0^1 du \Phi_{\parallel}(u) = \int_0^1 du g_{\perp}^{(a)}(u) = \int_0^1 du g_{\perp}^{(v)}(u) = \int_0^1 du g_3(u) = 0$$

$$\Phi_{\parallel,\perp}^T(u, \mu) = 6u(1-u) \sum_{\ell=0}^{\infty} a_{\ell}^{(\parallel,\perp),T}(\mu) C_{\ell}^{3/2}(2u-1),$$

$C_i^{3/2}$: Gegenbauer polynomial

$$\Phi_{\parallel,\perp}(u) \simeq 6u(1-u)(2u-1) a_1^{\parallel,\perp}$$

twist-2: $\Phi_{\parallel}, \Phi_{\perp}$

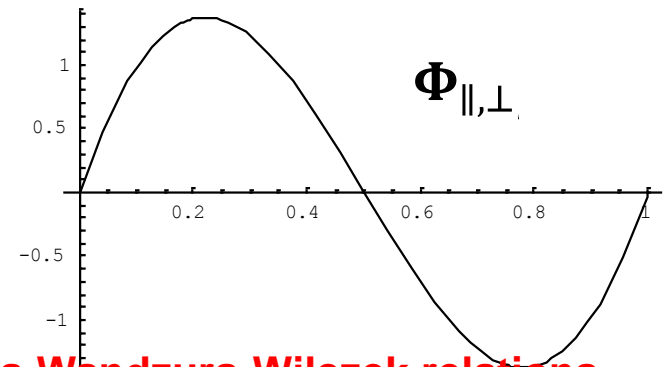
twist-3: $g_{\perp}^{(v)}, g_{\perp}^{(a)}, h_{\perp}^{(t)}, h_{\parallel}^{(p)}$ related to twist-2 ones via Wandzura-Wilczek relations (neglecting 3-parton distributions)

$$g_v^{WW}(u) = \int_0^u dv \frac{\Phi_{\parallel}^T(v)}{\bar{v}} + \int_u^1 dv \frac{\Phi_{\parallel}^T(v)}{v},$$

$$g_a^{WW}(u) = 2\bar{u} \int_0^u dv \frac{\Phi_{\parallel}^T(v)}{\bar{v}} + 2u \int_u^1 dv \frac{\Phi_{\parallel}^T(v)}{v},$$

$$h_t^{WW}(u) = \frac{3}{2}(2u-1) \left(\int_0^u dv \frac{\Phi_{\perp}^T(v)}{\bar{v}} - \int_u^1 dv \frac{\Phi_{\perp}^T(v)}{v} \right)$$

$$h_s^{WW}(u) = 3 \left(\bar{u} \int_0^u dv \frac{\Phi_{\perp}^T(v)}{\bar{v}} + u \int_u^1 dv \frac{\Phi_{\perp}^T(v)}{v} \right).$$



Decay constants

- Tensor meson cannot be produced from local V-A current owing

to $\varepsilon_{\mu\nu}\mathbf{p}^\nu=0$ $\langle T(p, \lambda) | V_\mu, A_\mu | 0 \rangle = 0$

- Can be created from local current involving covariant derivatives

$$\langle T(P, \lambda) | J_{\mu\nu}(0) | 0 \rangle = f_T m_T^2 \varepsilon_{\mu\nu}^{*(\lambda)},$$

$$\langle T(P, \lambda) | J_{\mu\nu\alpha}^\perp(0) | 0 \rangle = -i f_T^\perp m_T (\varepsilon_{\mu\alpha}^{(\lambda)*} P_\nu - \varepsilon_{\nu\alpha}^{(\lambda)*} P_\mu),$$

with

$$J_{\mu\nu}(0) = \frac{1}{2} \left(\bar{q}_1(0) \gamma_\mu i \overleftrightarrow{D}_\nu q_2(0) + \bar{q}_1(0) \gamma_\nu i \overleftrightarrow{D}_\mu q_2(0) \right)$$

$$J_{\mu\nu\alpha}^\perp(0) = \bar{q}_1(0) \sigma_{\mu\nu} i \overleftrightarrow{D}_\alpha q_2(0), \quad \text{Normalized with } a_1^\parallel = a_1^\perp = \frac{5}{3}$$

Previous estimates: Aliev & Shifman ('82); Aliev, Azizi, Bashiry ('10)

Based on QCD sum rules we obtain (Cheng, Koike, KCY, arXiv:1007.3526)

Light tensor mesons [40]

T	f_T (MeV)	f_T^\perp (MeV)
$f_2(1270)$	102 ± 6	117 ± 25
$f_2'(1525)$	126 ± 4	65 ± 12
$a_2(1320)$	107 ± 6	105 ± 21
$K_2^*(1430)$	118 ± 5	77 ± 14

VT modes

Data from BaBar

branching fractions (in units of 10^{-6})

Mode	\mathcal{B}	f_L	Mode	\mathcal{B}	f_L
$\mathcal{B}(B^+ \rightarrow K_2^*(1430)^+\omega)$	21.5 ± 4.3	0.56 ± 0.11	$\mathcal{B}(B^0 \rightarrow K_2^*(1430)^0\omega)$	10.1 ± 2.3	0.45 ± 0.12
$\mathcal{B}(B^+ \rightarrow K_2^*(1430)^+\phi)$	8.4 ± 2.1	0.80 ± 0.10	$\mathcal{B}(B^0 \rightarrow K_2^*(1430)^0\phi)$	7.5 ± 1.0	$0.901^{+0.059}_{-0.069}$

$$K_2^*\omega = 0.05 \sim 0.1$$

$$K_2^*\phi = 2 \sim 9$$



Naïve factorization,

Kim, Lee & Oh, PRD (2003);

Munoz, Quintero, J.Phys.G (2009)

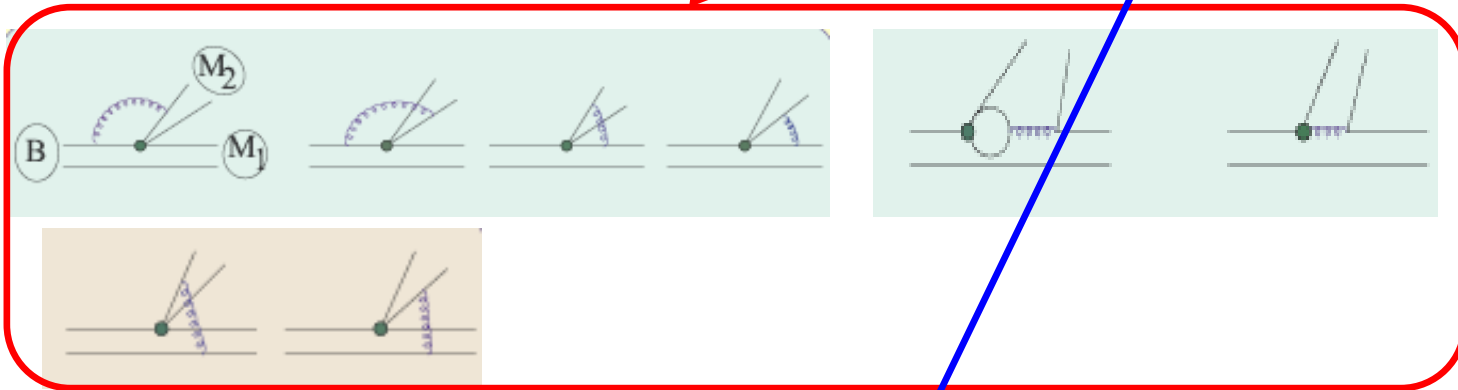
QCD factorization (without annihilation) $K_2^*\omega \sim 0.2$, $K_2^*\phi = 3$ too small

Within SM, to account for data,
penguin annihilation is necessary

PRD83:034001,2011, Hai-Yang Cheng, KCY

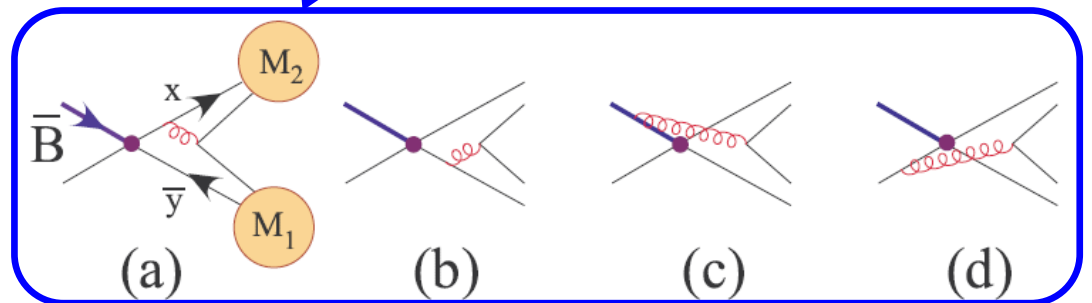
$$\sqrt{2}\mathcal{A}_{B^- \rightarrow K_2^{*-}\omega}^h \approx \sqrt{2}\mathcal{A}_{B^0 \rightarrow \bar{K}_2^{*0}\omega}^h \approx \left\{ [\alpha_4^{p,h} + \beta_3^{p,h}] \bar{X}_h^{(\bar{B}\omega, \bar{K}_2^*)} + [2\alpha_3^{p,h}] X_h^{(\bar{B}K_2^*, \omega)} \right\}$$

$$\mathcal{A}_{B^- \rightarrow K_2^{*-}\phi}^h \approx \mathcal{A}_{B^0 \rightarrow \bar{K}_2^{*0}\phi}^h \approx [\alpha_3^{p,h} + \alpha_4^{p,h} + \beta_3^{p,h} + \beta_{3,EW}^{p,h}] X_h^{(\bar{B}K_2^*, \phi)}$$



Ann is dominant for

$$(M_1, M_2) = \begin{cases} (K_2^* \phi) \\ (\omega K_2^*) \end{cases}$$



To account for data, penguin annihilation is necessary

$$\neq \begin{cases} \rho_A^{TV} \simeq 0.65, \phi_A^{TV} \simeq -33^\circ, (K_2^* \phi) \text{ where } M_1 = T, M_2 = V \\ \rho_A^{VT} \simeq 1.20, \phi_A^{VT} \simeq -60^\circ, (\omega K_2^*) \text{ where } M_1 = V, M_2 = T \end{cases}$$

Process-dependent ?

Polarization puzzle in $B \rightarrow K_2^* \phi$

$$f_L(K_2^{*+}\omega) = 0.56 \pm 0.11, \quad f_L(K_2^{*0}\omega) = 0.45 \pm 0.12,$$

BaBar

$$f_L(K_2^{*+}\phi) = 0.80 \pm 0.10, \quad f_L(K_2^{*0}\phi) = 0.901^{+0.059}_{-0.069}$$

Why is $f_T/f_L \ll 1$ for $B \rightarrow K_2^* \phi$ and $f_T/f_L \sim 1$ for $B \rightarrow K_2^* \omega$?

Why is that f_T behaves differently in $K_2^* \phi$ and $K^* \phi$?

In QCDF, f_L is very sensitive to the phase ϕ_A^{TV} for $B \rightarrow K_2^* \phi$, but not so sensitive to ϕ_A^{VT} for $B \rightarrow K_2^* \omega$

$$f_L(K_2^* \phi) = 0.88, 0.72, 0.48 \quad \text{for } \phi_A^{TV} = -30^\circ, -45^\circ, -60^\circ,$$
$$f_L(K_2^* \omega) = 0.68, 0.66, 0.64 \quad \text{for } \phi_A^{VT} = -30^\circ, -45^\circ, -60^\circ$$

Rates & polarization fractions can be accommodated in QCDF

$$\rho_A^{TV} = 0.65, \quad \phi_A^{TV} = -33^\circ, \quad \rho_A^{VT} = 1.20, \quad \phi_A^{VT} = -60^\circ$$

but no dynamical explanation is offered

Fine-tuning!

Sizable BR

Further test

$f_L = 0.65$

Decay	\mathcal{B}			f_L		ACP	
	QCDF	KLO [20]	MQ [21]	Expt.	QCDF		Expt.
$B^- \rightarrow \bar{K}_2^*(1430)^0 \rho^-$	$18.6^{+50.1}_{-17.2}$				$0.63^{+0.10}_{-0.09}$		$-1.0^{+0.8}_{-1.0}$
$B^- \rightarrow K_2^*(1430)^- \rho^0$	$10.4^{+18.8}_{-9.2}$	0.253	0.74		$0.66^{+0.06}_{-0.07}$		$2.1^{+11.1}_{-9.9}$
$\bar{B}^0 \rightarrow K_2^*(1430)^- \rho^+$	$19.8^{+52.0}_{-18.2}$				$0.64^{+0.07}_{-0.03}$		$-1.5^{+2.6}_{-2.0}$
$\bar{B}^0 \rightarrow \bar{K}_2^*(1430)^0 \rho^0$	$9.5^{+33.4}_{-9.5}$	0.235	0.68		$0.64^{+0.15}_{-0.37}$		$-4.0^{+14.1}_{-10.8}$
$B^- \rightarrow K_2^*(1430)^- \omega$	$7.5^{+19.7}_{-7.0}$	0.112	0.06	21.5 ± 4.3	$0.64^{+0.08}_{-0.07}$	0.56 ± 0.11	$2.0^{+12.2}_{-10.5}$
$\bar{B}^0 \rightarrow \bar{K}_2^*(1430)^0 \omega$	$8.1^{+21.7}_{-7.6}$	0.104	0.053	10.1 ± 2.3	$0.66^{+0.11}_{-0.15}$	0.45 ± 0.12	$4.4^{+10.9}_{-10.0}$
$B^- \rightarrow K_2^*(1430)^- \phi$	$7.4^{+25.8}_{-5.2}$	2.180	9.24	8.4 ± 2.1	$0.85^{+0.16}_{-0.77}$	0.80 ± 0.10	$0.1^{+1.2}_{-0.5}$
$\bar{B}^0 \rightarrow \bar{K}_2^*(1430)^0 \phi$	$7.7^{+26.9}_{-5.5}$	2.024	8.51	7.5 ± 1.0	$0.86^{+0.16}_{-0.77}$	$0.901^{+0.059}_{-0.069}$	$0.09^{+0.82}_{-0.21}$
$B^- \rightarrow a_2(1320)^0 K^{*-}$	$2.9^{+11.7}_{-2.5}$	1.852	2.80		$0.73^{+0.22}_{-0.33}$		$-15.0^{+56.0}_{-15.0}$
$B^- \rightarrow a_2(1320)^- \bar{K}^{*0}$	$6.1^{+23.8}_{-5.4}$	4.495	8.62		$0.79^{+0.20}_{-0.64}$		$-0.1^{+1.3}_{-0.3}$
$\bar{B}^0 \rightarrow a_2(1320)^+ K^{*-}$	$6.1^{+24.3}_{-5.3}$	3.477	7.25		$0.77^{+0.19}_{-0.46}$	$f_L = 0.93$	$-13.3^{+38.2}_{-7.0}$
$\bar{B}^0 \rightarrow a_2(1320)^0 \bar{K}^{*0}$	$3.4^{+12.4}_{-2.8}$	2.109	4.03		$0.82^{+0.14}_{-0.67}$		$1.2^{+7.0}_{-13.3}$
$B^- \rightarrow f_2(1270) K^{*-}$	$8.3^{+17.3}_{-6.7}$	2.032			$0.93^{+0.09}_{-0.63}$		$-8.1^{+13.7}_{-7.1}$
$\bar{B}^0 \rightarrow f_2(1270) \bar{K}^{*0}$	$9.1^{+18.8}_{-7.3}$	2.314			$0.94^{+0.06}_{-0.69}$		$-0.08^{+4.3}_{-3.1}$
$B^- \rightarrow f_2'(1525) K^{*-}$	$12.6^{+24.0}_{-11.1}$	0.025			$0.65^{+0.28}_{-0.38}$		$0.6^{+2.5}_{-2.9}$
$\bar{B}^0 \rightarrow f_2'(1525) \bar{K}^{*0}$	$13.5^{+25.4}_{-11.9}$	0.029			$0.66^{+0.27}_{-0.38}$		$0.2^{+0.3}_{-0.4}$

New Physics due to tensor currents

$$\mathbf{B} \rightarrow \mathbf{K}_2^* \phi$$

$$\overline{A}_0^{NP} = 4i f_\phi^T m_B^2 [\tilde{a}_{23} - \tilde{a}_{25}] [h_2 T_2(m_\phi^2) - h_3 T_3(m_\phi^2)] \frac{p_3}{m_{K_2^*}} \sqrt{\frac{2}{3}}$$

$$\overline{A}_\parallel^{NP} = -4i \sqrt{2} f_\phi^T m_B^2 (\tilde{a}_{23} - \tilde{a}_{25}) f_2 T_2(m_\phi^2) \frac{p_3}{m_{K_2^*}} \sqrt{\frac{1}{2}}$$

$$\overline{A}_\perp^{NP} = -4i \sqrt{2} f_\phi^T m_B^2 (\tilde{a}_{23} + \tilde{a}_{25}) f_1 T_1(m_\phi^2) \frac{p_3}{m_{K_2^*}} \sqrt{\frac{1}{2}}$$

Relatively smaller

Larger f_L compared with ϕK^*

$$\mathbf{B} \rightarrow \mathbf{K}^* \phi$$

$$\overline{A}_0^{NP} = +4i f_\phi^T m_B^2 [\tilde{a}_{23} - \tilde{a}_{25}] [h_2 T_2(m_\phi^2) - h_3 T_3(m_\phi^2)]$$

$$\overline{A}_\parallel^{NP} = -4i \sqrt{2} f_\phi^T m_B^2 (\tilde{a}_{23} - \tilde{a}_{25}) f_2 T_2(m_\phi^2),$$

$$\overline{A}_\perp^{NP} = -4i \sqrt{2} f_\phi^T m_B^2 (\tilde{a}_{23} + \tilde{a}_{25}) f_1 T_1(m_\phi^2),$$

Conclusions

Possible solutions for polarization in $B \rightarrow VV$ decays:

- ◆ In SM, we need large constructive annihilation corrections to the transverse amplitudes via the $O_6 = -2\bar{d}(1 - \gamma_5)b \bar{s}(1 + \gamma_5)d$
- the annihilation corrections are only significant for penguin dominant processes $\phi K^*, \rho K^*, \dots$

New physics solutions:

the only candidates are the tensor operators
(Pure $(S \pm P)(S \pm P)$ operators are unlikely)

Further information ($b \rightarrow \bar{s} s s$) can be extracted from

$$B \rightarrow \phi K_2^*, \omega K_2^*$$

and some other modes involving the tensor meson

(pseudo-)scalar-type operators

$$\begin{aligned} O_{15} &= \bar{s}(1 + \gamma^5)b \bar{s}(1 + \gamma^5)s, & O_{16} &= \bar{s}_\alpha(1 + \gamma^5)b_\beta \bar{s}_\beta(1 + \gamma^5)s_\alpha, \\ O_{17} &= \bar{s}(1 - \gamma^5)b \bar{s}(1 - \gamma^5)s, & O_{18} &= \bar{s}_\alpha(1 - \gamma^5)b_\beta s \bar{s}_\beta(1 - \gamma^5)s_\alpha, \end{aligned}$$

tensor-type operators

$$\begin{aligned} O_{23} &= \bar{s}\sigma^{\mu\nu}(1 + \gamma^5)b \bar{s}\sigma_{\mu\nu}(1 + \gamma^5)s, & O_{24} &= \bar{s}_\alpha\sigma^{\mu\nu}(1 + \gamma^5)b_\beta \bar{s}_\beta\sigma_{\mu\nu}(1 + \gamma^5)s_\alpha, \\ O_{25} &= \bar{s}\sigma^{\mu\nu}(1 - \gamma^5)b \bar{s}\sigma_{\mu\nu}(1 - \gamma^5)s, & O_{26} &= \bar{s}_\alpha\sigma^{\mu\nu}(1 - \gamma^5)b_\beta \bar{s}_\beta\sigma_{\mu\nu}(1 - \gamma^5)s_\alpha. \end{aligned}$$

By Fierz transformation

$$\begin{aligned} O_{15} &= \frac{1}{12}O_{23} - \frac{1}{6}O_{24}, & O_{16} &= \frac{1}{12}O_{24} - \frac{1}{6}O_{23} \\ O_{17} &= \frac{1}{12}O_{25} - \frac{1}{6}O_{26}, & O_{18} &= \frac{1}{12}O_{26} - \frac{1}{6}O_{25} \end{aligned}$$

Can only (pseudo-)scalar-type operators explain the data?

Answer: NO

In the minimal supersymmetric standard model (MSSM), such scalar/pseudoscalar operators can be induced by the penguin diagrams of neutral-Higgs bosons.

A combined analysis of the decays $B \rightarrow K \eta^{(\prime)}$, ϕK^* decays and to be consistent with the data for $B_s \rightarrow \mu^+ \mu^-$ shows that the NP effects only due to (pseudo-)scalar-type operators is much smaller in $B \rightarrow K^* \phi$ modes.

Penguin-dominated $B \rightarrow TP$

Decay	QCDF	\mathcal{B}		Experiment
		Kim-Lim-Oh [20]	Munoz-Quintero [21]	
$B^- \rightarrow \bar{K}_2^*(1430)^0 \pi^-$	$3.1^{+8.3}_{-3.1}$			$5.6^{+2.2}_{-1.4}$
$B^- \rightarrow K_2^*(1430)^- \pi^0$	$2.2^{+4.7}_{-1.9}$	0.090	0.15	
$\bar{B}^0 \rightarrow K_2^*(1430)^- \pi^+$	$3.3^{+8.5}_{-3.2}$			<6.3
$\bar{B}^0 \rightarrow \bar{K}_2^*(1430)^0 \pi^0$	$1.2^{+4.3}_{-1.3}$	0.084	0.13	<4.0
$B^- \rightarrow a_2(1320)^0 K^-$	$4.9^{+8.4}_{-4.2}$	0.311	0.39	<45
$B^- \rightarrow a_2(1320)^- \bar{K}^0$	$8.4^{+16.1}_{-7.2}$	0.011	0.015	
$\bar{B}^0 \rightarrow a_2(1320)^+ K^-$	$9.7^{+17.2}_{-8.1}$	0.584	0.73	
$\bar{B}^0 \rightarrow a_2(1320)^0 \bar{K}^0$	$4.2^{+8.3}_{-3.5}$	0.005	0.014	
$B^- \rightarrow f_2(1270) K^-$	$3.8^{+7.8}_{-3.0}$	0.344		$1.06^{+0.28}_{-0.29}$
$\bar{B}^0 \rightarrow f_2(1270) \bar{K}^0$	$3.4^{+8.5}_{-3.1}$	0.005		$2.7^{+1.3}_{-1.2}$
$B^- \rightarrow f_2'(1525) K^-$	$4.0^{+7.4}_{-3.6}$	0.004		<7.7
$\bar{B}^0 \rightarrow f_2'(1525) \bar{K}^0$	$3.8^{+7.3}_{-3.5}$	7×10^{-5}		
$B^- \rightarrow K_2^*(1430)^- \eta$	$6.8^{+13.5}_{-8.7}$	0.031	1.19	9.1 ± 3.0
$B^- \rightarrow K_2^*(1430)^- \eta'$	$12.1^{+20.7}_{-12.1}$	1.405	2.70	$28.0^{+5.3}_{-5.0}$
$\bar{B}^0 \rightarrow \bar{K}_2^*(1430)^0 \eta$	$6.6^{+13.5}_{-8.7}$	0.029	1.09	9.6 ± 2.1
$\bar{B}^0 \rightarrow \bar{K}_2^*(1430)^0 \eta'$	$12.4^{+21.3}_{-12.4}$	1.304	2.46	$13.7^{+3.2}_{-3.1}$

branching fractions (in units of 10^{-6})

$B^- \rightarrow \underline{K}_2^{*0} \pi^-$ vanishes in naïve factorization, while its BR is measured to be $\sim 5.6 \times 10^{-6}$
 \Rightarrow importance of nonfactorizable effects

■ Penguin annihilation is needed in QCDF to account for rates & CP asymmetries

$$X_A \equiv \int_0^1 \frac{dy}{y} = \ln \frac{m_B}{\Lambda_h} (1 + \rho_A e^{i\phi_A})$$

$$\rho_A^{\text{TP}} = 0.83, \quad \phi_A^{\text{TP}} = -70^\circ$$

$$\rho_A^{\text{PT}} = 0.75, \quad \phi_A^{\text{PT}} = -30^\circ$$

similar to the parameters
for $B \rightarrow PP$