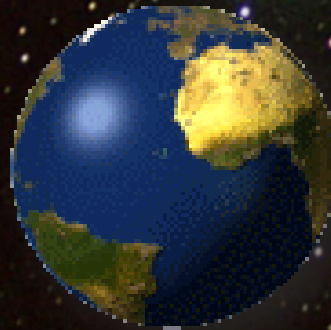


Tests of Lorentz and CPT violation with Neutrinos



Teppei Katori
Massachusetts Institute of Technology
ICHEP2012, Melbourne, Australia, July 10, 2012

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Outline

1. Spontaneous Lorentz symmetry breaking
2. What is Lorentz and CPT violation?
3. Test for Lorentz violation with neutrinos
4. Conclusion

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1. Spontaneous Lorentz symmetry breaking

2. What is Lorentz and CPT violation?

3. Test for Lorentz violation with Neutrinos

4. Conclusion

1. Spontaneous Lorentz symmetry breaking (SLSB)

Every fundamental symmetry needs to be tested, including Lorentz symmetry.

After the recognition of the theoretical processes that create Lorentz violation, testing Lorentz invariance became very exciting.

Lorentz and CPT violation has been shown to occur in Planck-scale theories, including:

- string theory
- noncommutative field theory
- quantum loop gravity
- extra dimensions
- etc

However, it is very difficult to build a self-consistent theory with Lorentz violation...

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However, it is very difficult to build a self-consistent theory with Lorentz violation...

Spontaneous
Symmetry Breaking
(SSB)!



Y. Nambu
(Nobel Prize winner 2008),
picture taken from CPT04 at
Bloomington, IN

1. Spontaneous Lorentz symmetry breaking (SLSB)

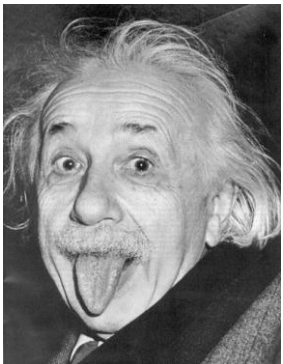
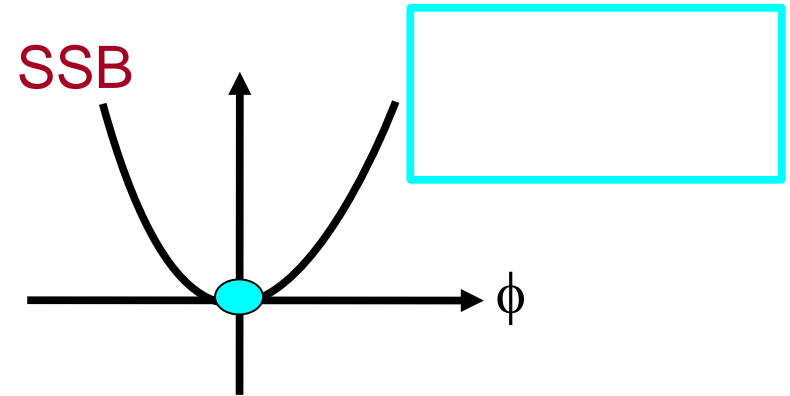
vacuum Lagrangian for fermion $\mathcal{L} = i\bar{\Psi}\gamma_\mu \partial^\mu \Psi$

e.g.) SSB of scalar field in Standard Model (SM)

- If the scalar field has Mexican hat potential

$$\mathcal{L} = \frac{1}{2}(\partial_\mu \phi)^2 - \frac{1}{2}m^2(\phi)^2 - \frac{\lambda}{4}(\phi^2)^2$$

$$M(\phi) = m^2 < 0$$



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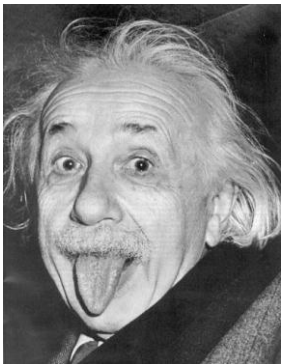
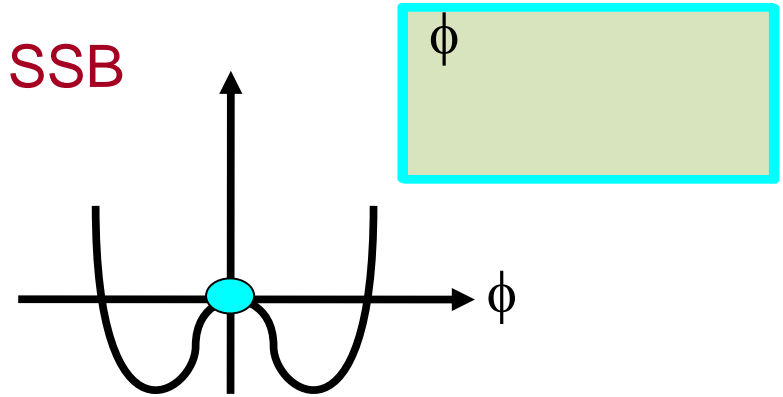
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SSB



Particle acquires
mass term!

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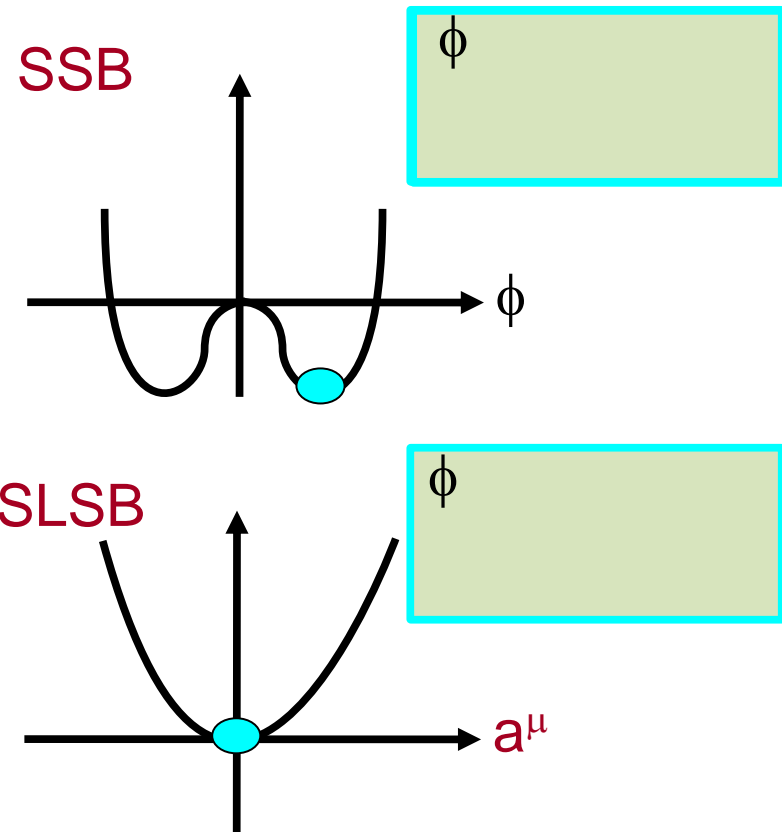
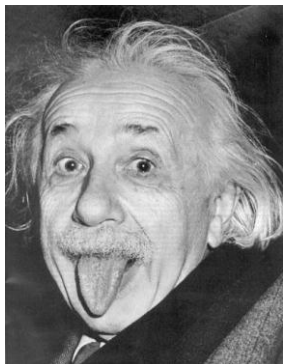
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e.g.) SLSB in string field theory

- There are many Lorentz vector fields
- If any of vector field has Mexican hat potential

$$M(a^\mu) = m^2 < 0$$



1. Spontaneous Lorentz symmetry breaking (SLSB)

$$\text{vacuum Lagrangian for fermion } \mathcal{L} = i\bar{\Psi} \gamma_m \partial^m \Psi - m \bar{\Psi} \Psi + \bar{\Psi} g_m a^m \Psi$$

e.g.) SSB of scalar field in Standard Model (SM)

- If the scalar field has Mexican hat potential

$$L = \frac{1}{2} (\partial_\mu \phi)^2 - \frac{1}{2} m^2 (\phi^* \phi) - \frac{1}{4} \lambda (\phi^* \phi)^2$$

$$M(\phi) = m^2 < 0$$

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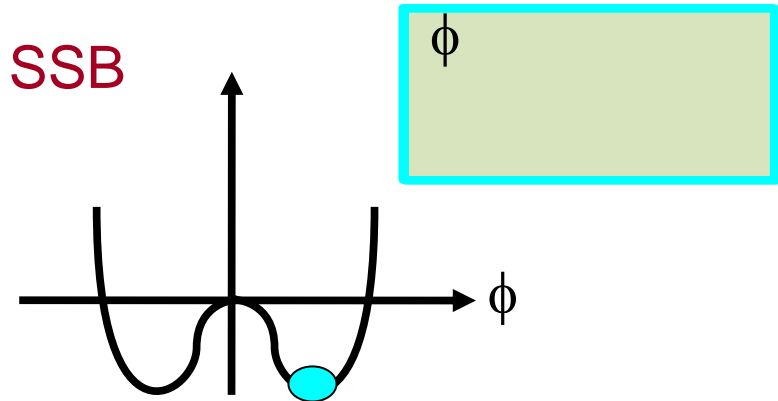
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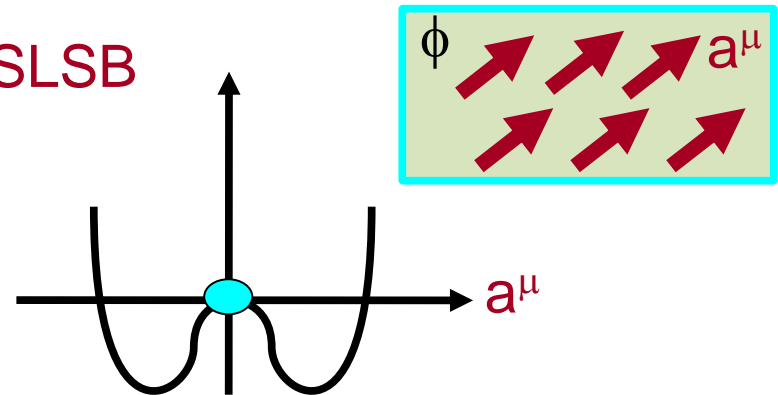


Lorentz symmetry
is spontaneously
broken!

SSB



SLSB



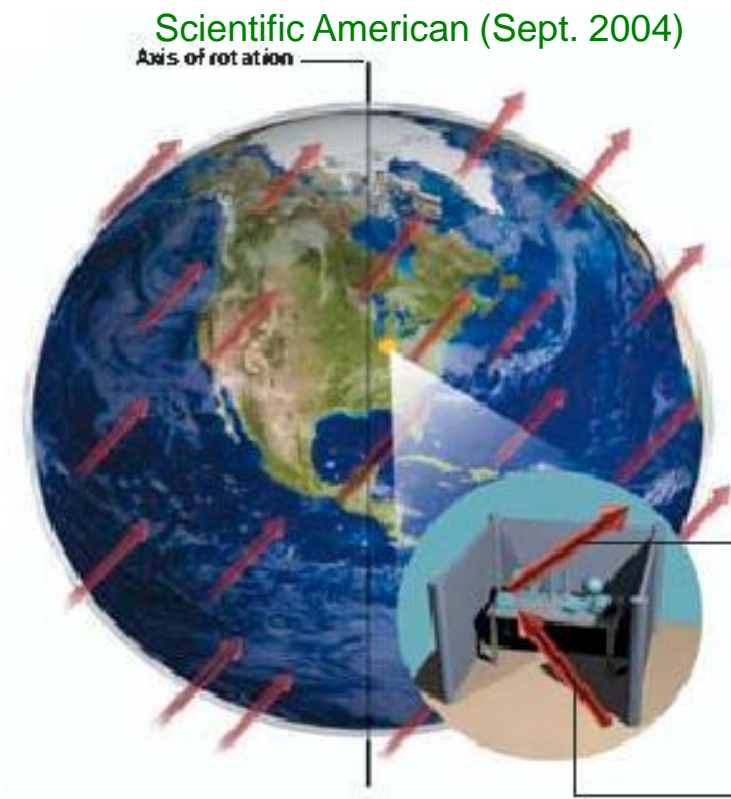
1. Test of Lorentz violation

Test of Lorentz violation is to find the coupling of these background fields and ordinary fields (electrons, muons, neutrinos, etc); then **the physical quantities may depend on the rotation of the earth (sidereal time dependence).**

vacuum Lagrangian for fermion

$$L = i\bar{\Psi}g_m\gamma^m\Psi - m\bar{\Psi}\Psi + \bar{\Psi}g_m\boxed{a^m}\Psi + \bar{\Psi}g_m\boxed{c^{mn}}\gamma_n\Psi$$

background fields
of the universe



Scientific American (Sept. 2004)

solar time: 24h 00m 00.0s
sidereal time: 23h 56m 04.1s (Earth rotation period)

1. Spontaneous Lorentz symmetry breaking

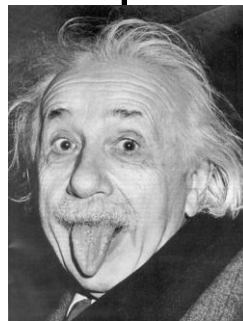
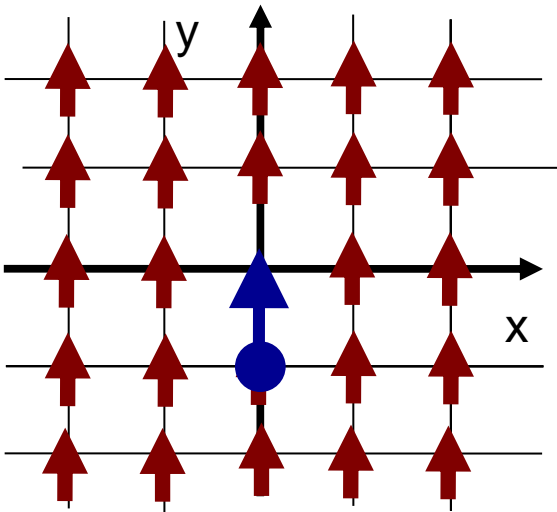
2. What is Lorentz and CPT violation?

3. Test for Lorentz violation with neutrinos

4. Conclusion

2. What is Lorentz violation?

$$\bar{\Psi}(x) g_m a^m \Psi(x)$$

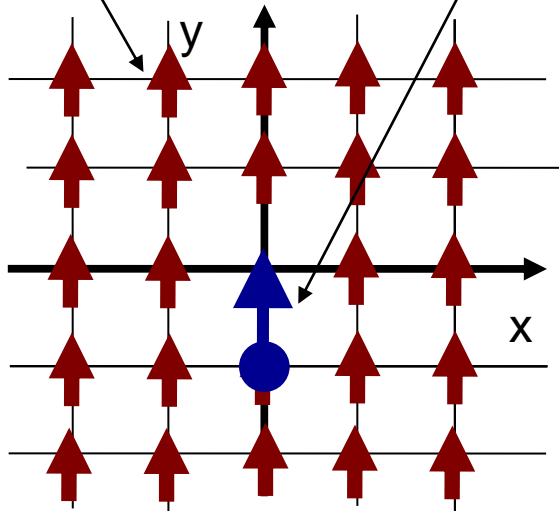


2. What is Lorentz violation?

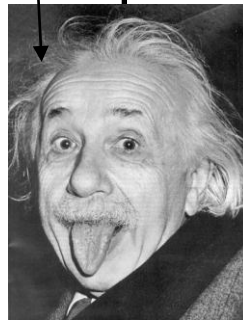
$$\nabla(x) g_m a^m \Upsilon(x)$$

hypothetical background
vector field

moving particle



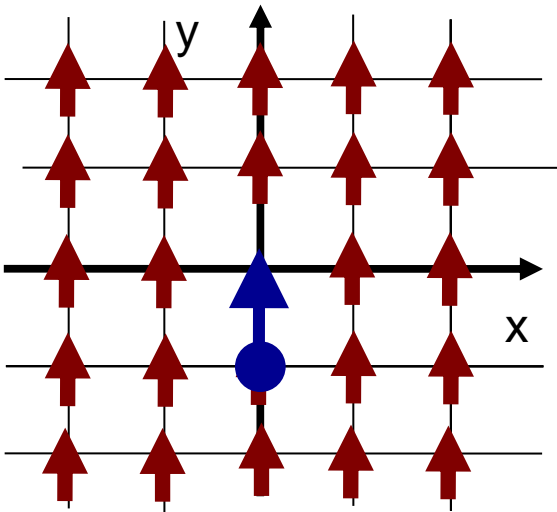
Einstein
(observer)



2. What is Lorentz violation?

Under the **particle** Lorentz transformation:

$$U \nabla(x) g_m a^m \Upsilon(x) U^{-1}$$

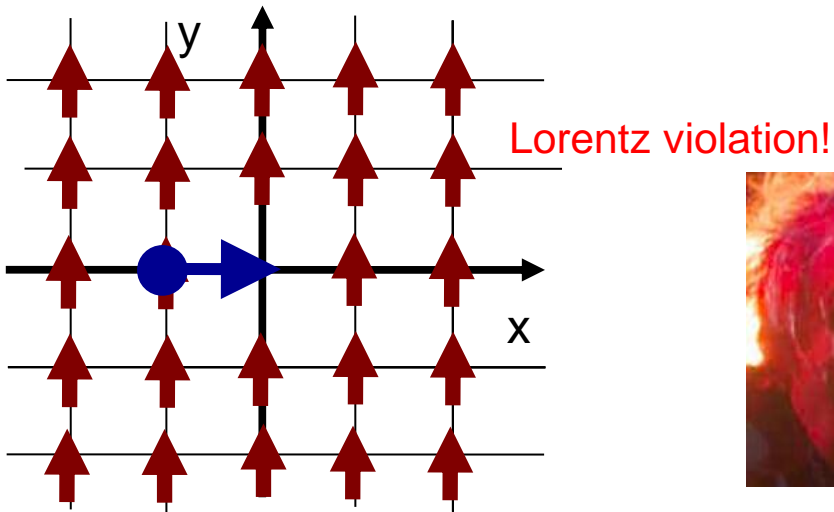


2. What is Lorentz violation?

Under the **particle** Lorentz transformation:

$$\bar{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x) \rightarrow U[\bar{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x)]U^{-1} \\ \neq \bar{\Psi}(\Lambda x)\gamma_{\mu}a^{\mu}\Psi(\Lambda x)$$

Lorentz violation is observable
when a particle is moving in the
fixed coordinate space

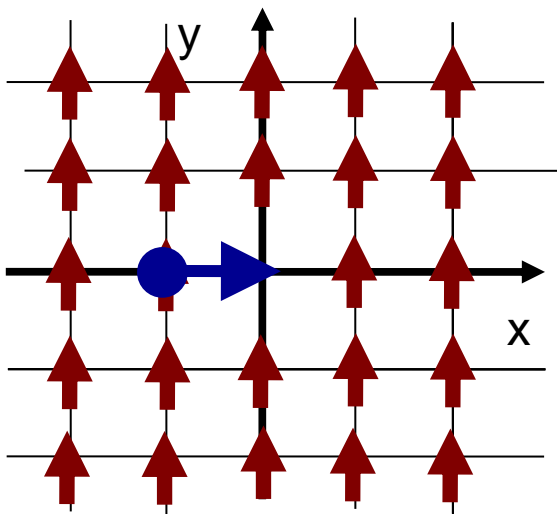


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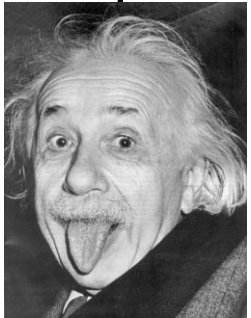
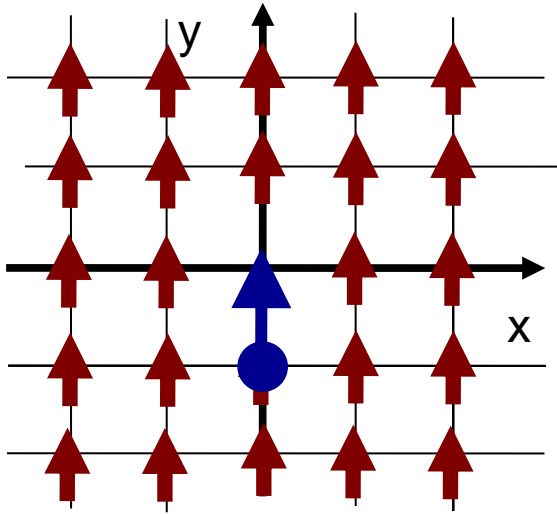
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Under the **observer** Lorentz transformation:

$$\bar{\Upsilon}(x)g_ma^m\Upsilon(x)$$



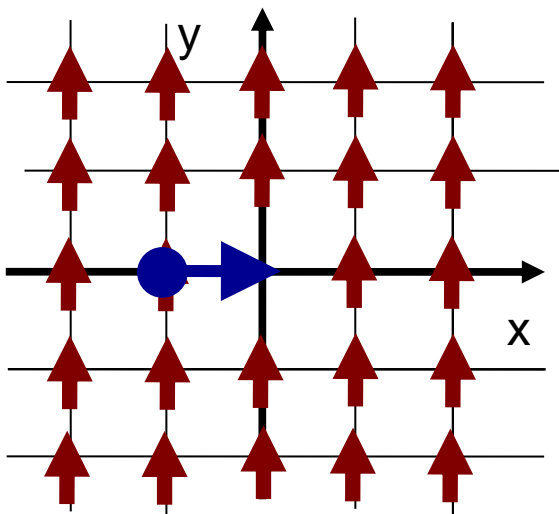
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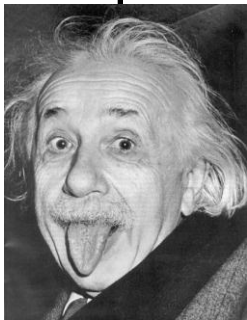
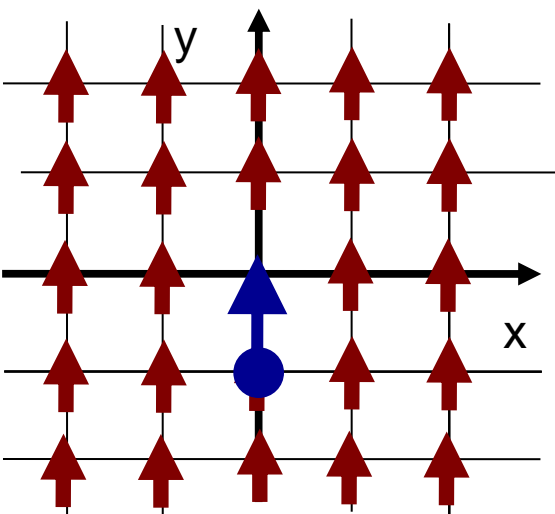
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Under the **observer** Lorentz transformation:

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$$x \rightarrow \Lambda^{-1}x$$



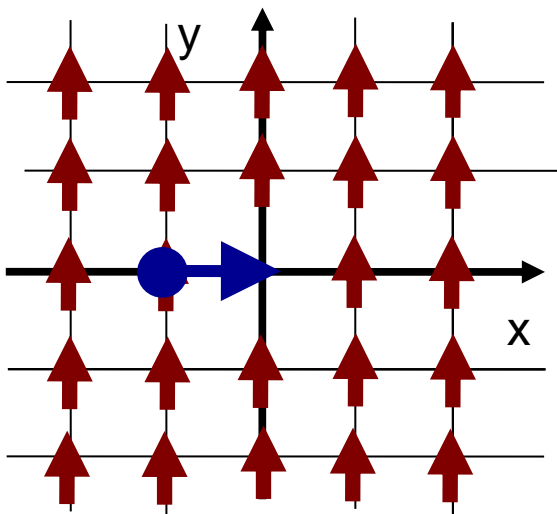
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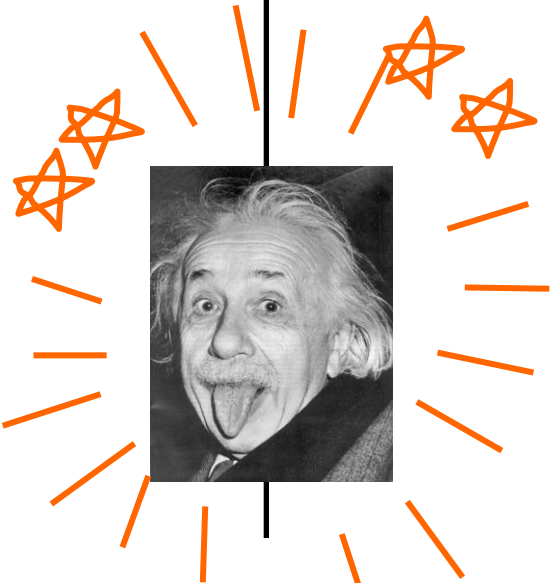
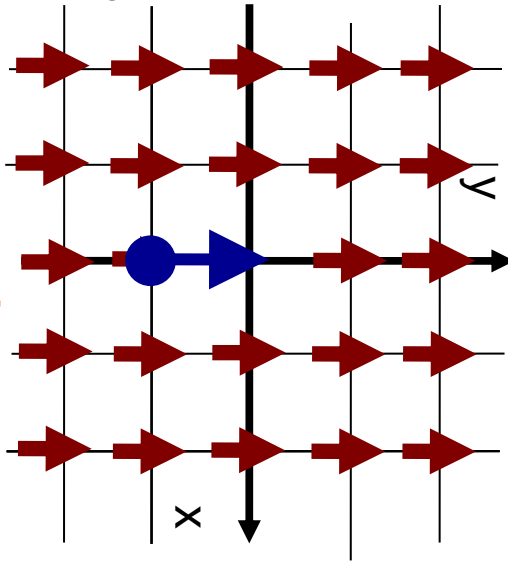


Under the **observer** Lorentz transformation:

$$\bar{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x) \xrightarrow{\Lambda^{-1}} \bar{\Psi}(\Lambda^{-1}x)\gamma_{\mu}a^{\mu}\Psi(\Lambda^{-1}x)$$

Lorentz violation cannot be generated by observers motion (coordinate transformation is unbroken)

all observers agree for all observations



1. Spontaneous Lorentz symmetry breaking

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3. Test for Lorentz violation with neutrinos

4. Conclusion

3. Test of Lorentz violation with neutrino oscillation experiments

Lorentz violation is realized as a coupling of particle fields and background fields, so the basic strategy to find Lorentz violation is:

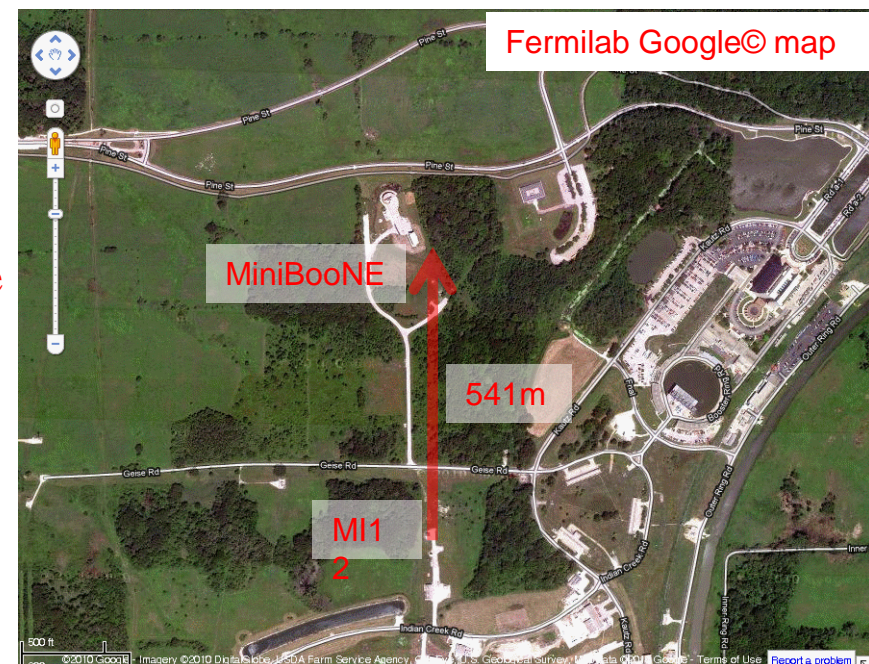
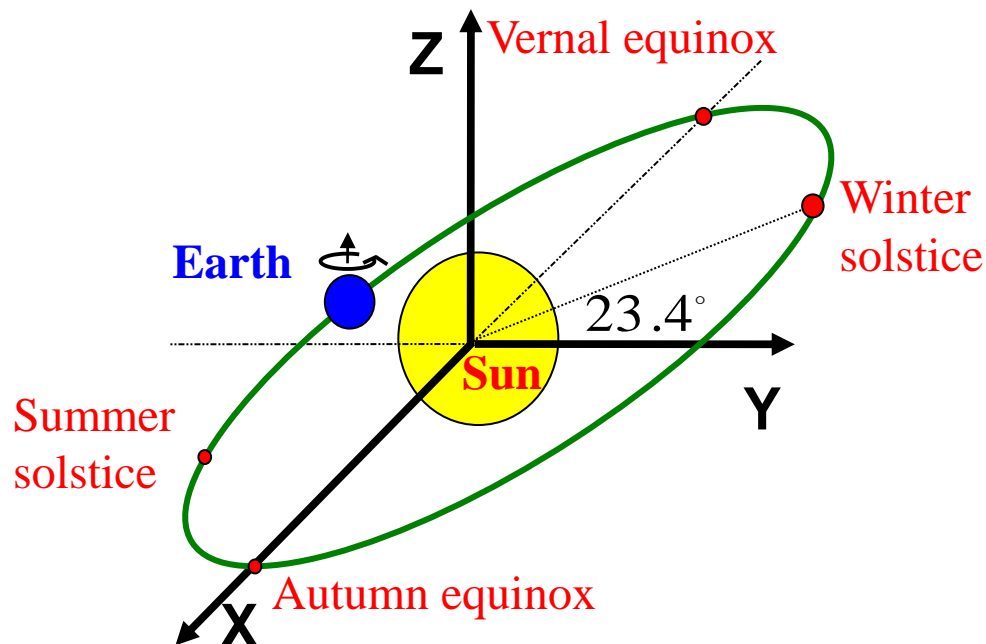
- (1) choose the coordinate system
- (2) write down the Lagrangian, including Lorentz-violating terms under the formalism
- (3) write down the observables using this Lagrangian

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- Neutrino beamline is described in **Sun-centred coordinates**



MiniBooNE beamline

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Standard Model Extension (SME) is the standard formalism for the general search for Lorentz violation. SME is a minimum extension of QFT with Particle Lorentz violation

SME Lagrangian in neutrino sector

$$L = \frac{1}{2} i \bar{\mathcal{Y}}_A G_{AB}^n \not{n} \mathcal{Y}_B - M_{AB} \bar{\mathcal{Y}}_A \mathcal{Y}_B + h.c.$$

SME coefficients

$$G_{AB}^n = g^n d_{AB} + c_{AB}^{mn} g_m + d_{AB}^{mn} g_m g_5 + e_{AB}^n + i f_{AB}^n g_5 + \frac{1}{2} g_{AB}^{lmn} S_{lm} \cdots$$

$$M_{AB} = m_{AB} + i m_{5AB} g_5 + a_{AB}^m g_m + b_{AB}^m g_5 g_m + \frac{1}{2} H_{AB}^{mn} S_{mn} \cdots$$

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Various physics are predicted under SME, but among them, the smoking gun of Lorentz violation is the **sidereal time dependence** of the observables

solar time: 24h 00m 00.0s
sidereal time: 23h 56m 04.1s

$$\begin{array}{ll} \text{sidereal frequency} & \omega_{\oplus} = \frac{2\pi}{23h56m4.1s} \\ \text{sidereal time} & T_{\oplus} \end{array}$$

Lorentz-violating neutrino oscillation probability for short-baseline experiments

$$P_{\nu_m \rightarrow \nu_e} = \left(\frac{L}{\hbar c} \right)^2 \left| (C)_{em} + (A_s)_{em} \sin \omega_{\oplus} T_{\oplus} + (A_c)_{em} \cos \omega_{\oplus} T_{\oplus} + (B_s)_{em} \sin 2\omega_{\oplus} T_{\oplus} + (B_c)_{em} \cos 2\omega_{\oplus} T_{\oplus} \right|^2$$

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Lorentz-violating neutrino oscillation probability for short-baseline experiments

$$P_{n_m \rightarrow n_e} = \left(\frac{L}{\hbar c} \right)^2 \left| \underbrace{(C)_{em}}_{\text{time independent amplitude}} + \underbrace{(A_s)_{em}}_{\text{sidereal time dependent amplitude}} \sin \omega_{\oplus} T_{\oplus} + \underbrace{(A_c)_{em}}_{\text{sidereal time dependent amplitude}} \cos \omega_{\oplus} T_{\oplus} + \underbrace{(B_s)_{em}}_{\text{sidereal time dependent amplitude}} \sin 2\omega_{\oplus} T_{\oplus} + \underbrace{(B_c)_{em}}_{\text{sidereal time dependent amplitude}} \cos 2\omega_{\oplus} T_{\oplus} \right|^2$$

Sidereal variation analysis for short baseline neutrino oscillation is 5-parameter fitting problem

3. LSND experiment

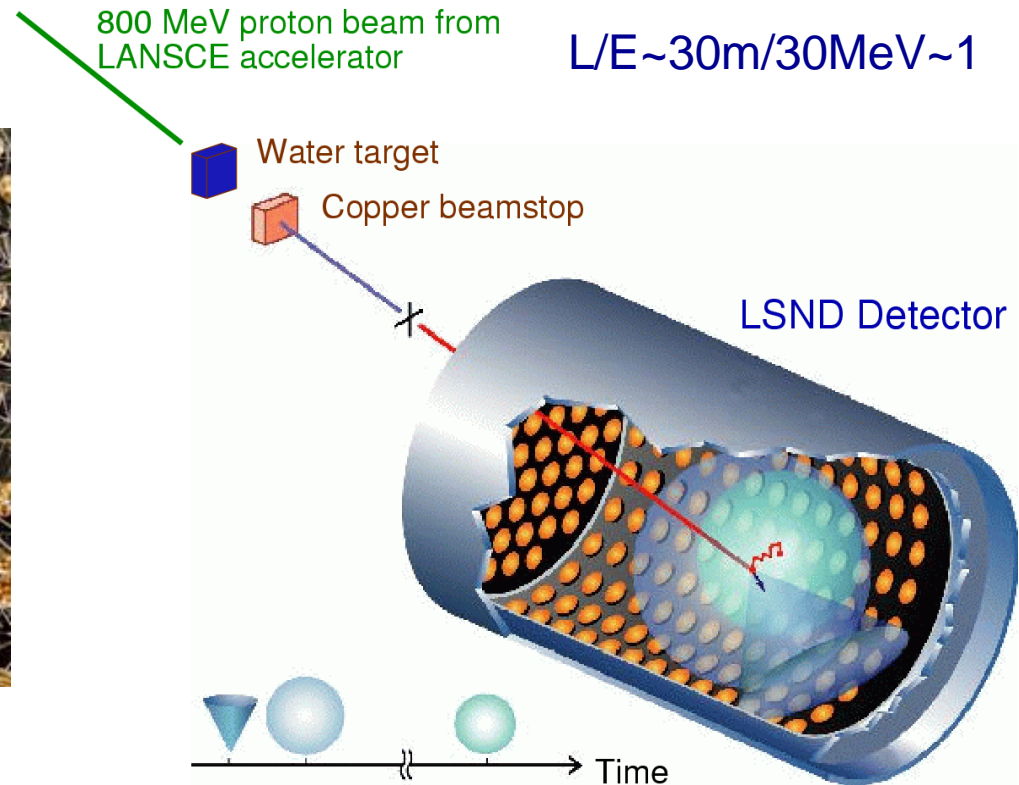
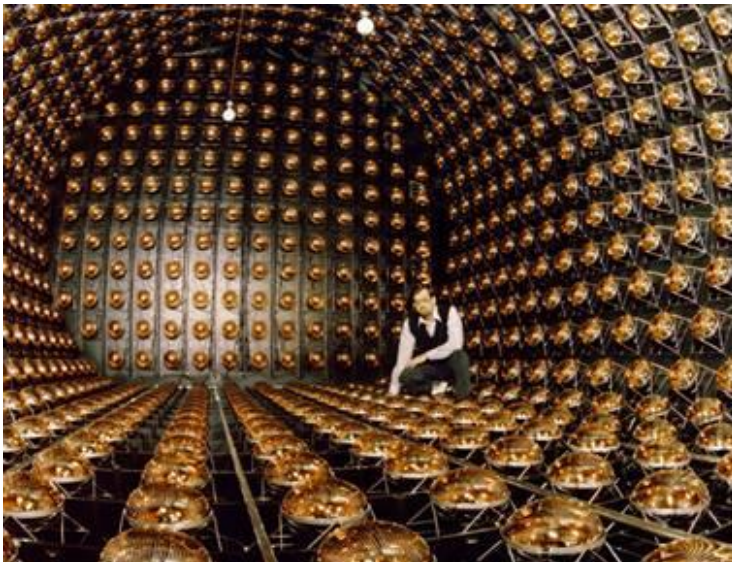
LSND is a short-baseline neutrino oscillation experiment at Los Alamos.

$$\bar{\nu}_{\mu} \xrightarrow{\text{oscillation}} \bar{\nu}_e + p \rightarrow e^+ + n$$

$$n + p \rightarrow d + \gamma$$

LSND saw the 3.8σ excess of electron antineutrinos from muon antineutrino beam; **since this excess is not understood by neutrino Standard Model, it might be new physics**

LSND detector



3. LSND experiment

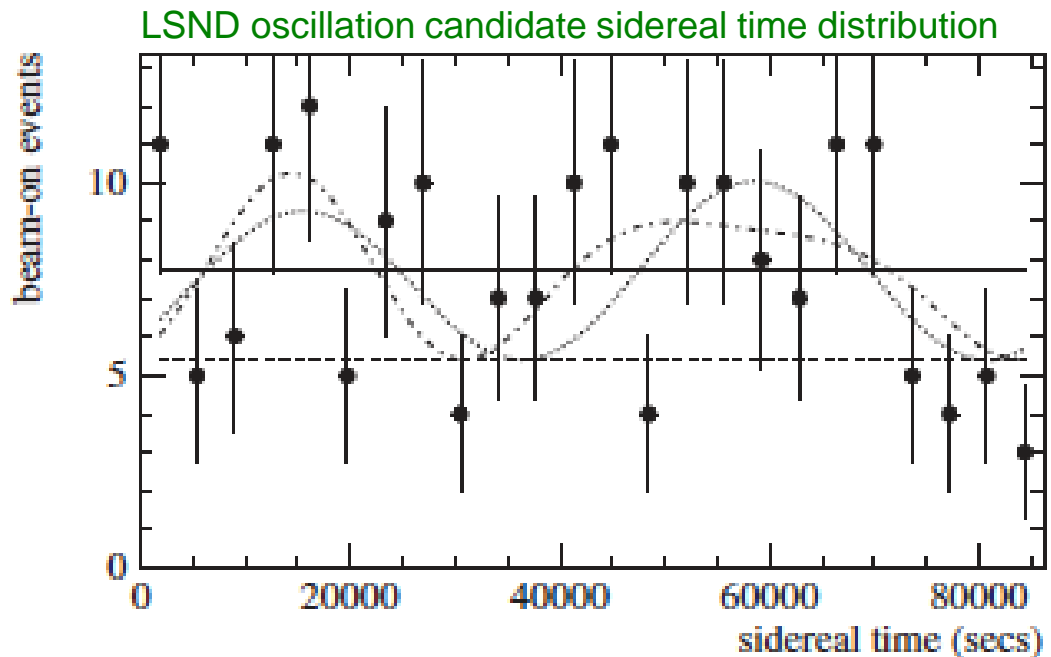
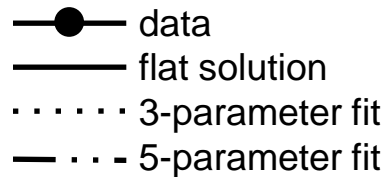
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Data is consistent with flat solution, but sidereal time solution is not excluded.



Small Lorentz violation could be the solution of LSND excess

3. Tandem Model

$$(h_{\text{eff}}^\nu)_{ab} \approx E\delta_{ab} + \frac{(m^2)_{ab}}{2E} + (a_L)_{ab} - \frac{4}{3}(c_L)_{ab}E.$$

Small Lorentz violation could be the solution of LSND excess. But can such solution be allowed by other experiments?

→ It is possible to construct a phenomenological neutrino oscillation model, based on Lorentz violation, using only 3 free parameters (tandem model).

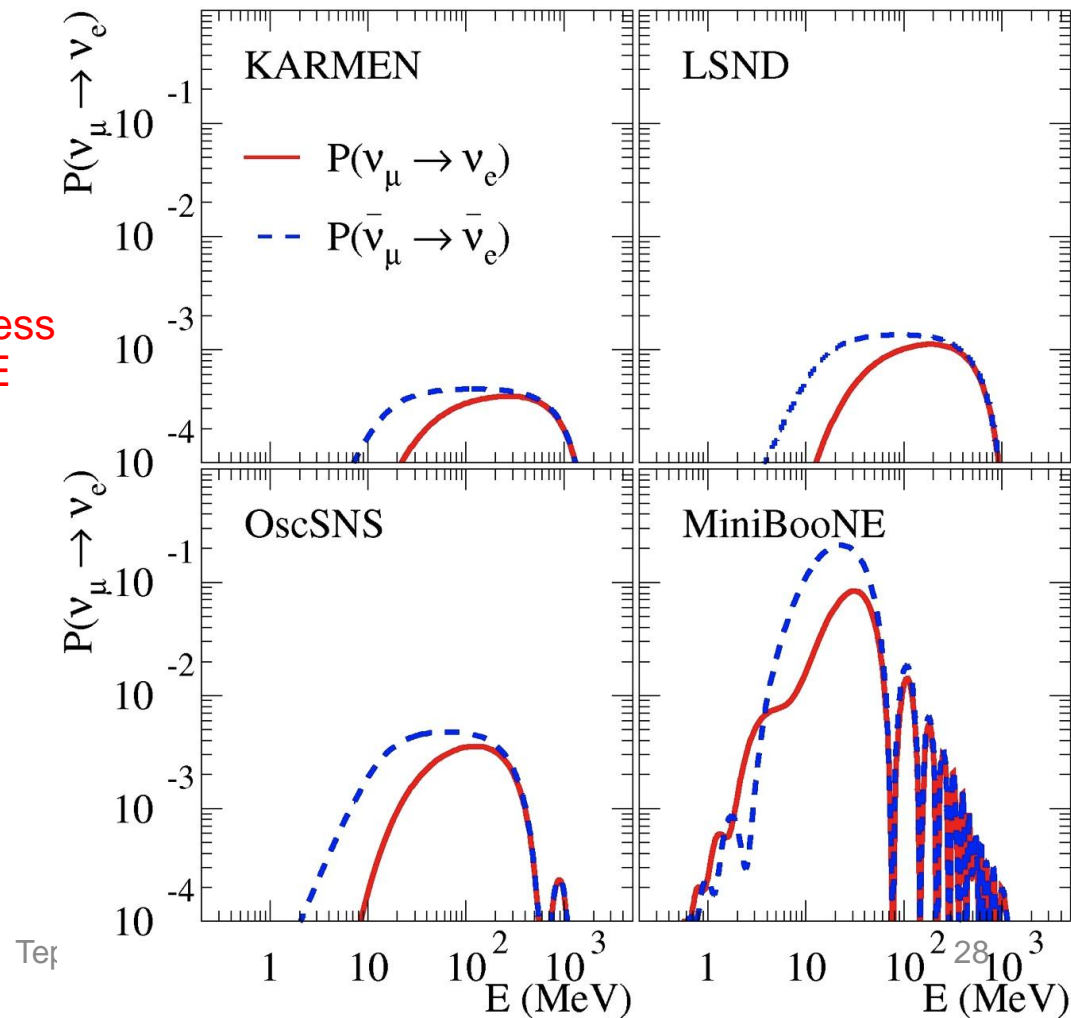
Tandem model can reproduce:

- solar neutrino oscillation
- atmospheric neutrino oscillation
- reactor neutrino oscillation
- LSND neutrino oscillation

Tandem model also predicts small excess at the low energy region for MiniBooNE

Recent development of Lorentz violating neutrino oscillation models, see for example, Diaz and Kostelecký, PRD85(2012)016013

LSND oscillation candidate sidereal time distribution



3. MiniBooNE experiment

MiniBooNE is a short-baseline neutrino oscillation experiment at Fermilab.

$$\bar{\nu}_m \xrightarrow{\text{oscillation}} \bar{\nu}_e + n \rightarrow e^- + p$$

$$\nu_m \xrightarrow{\text{oscillation}} \nu_e + p \rightarrow e^+ + n$$

Neutrino mode analysis: MiniBooNE saw the 3.0σ excess at **low energy region**

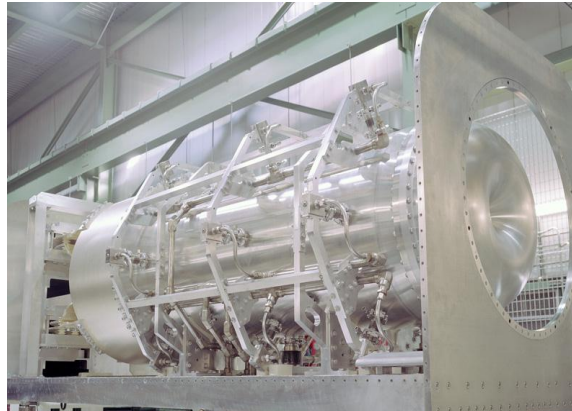
Antineutrino mode analysis: MiniBooNE saw the 1.4σ excess at **low and high energy region**

(however MiniBooNE low energy excesses are much bigger than tandem model prediction)

FNAL Booster



Magnetic focusing horn



MiniBooNE detector



~520m
→

primary beam

(8 GeV protons)

secondary beam

(2 GeV pions)

tertiary beam

(700 MeV neutrinos)

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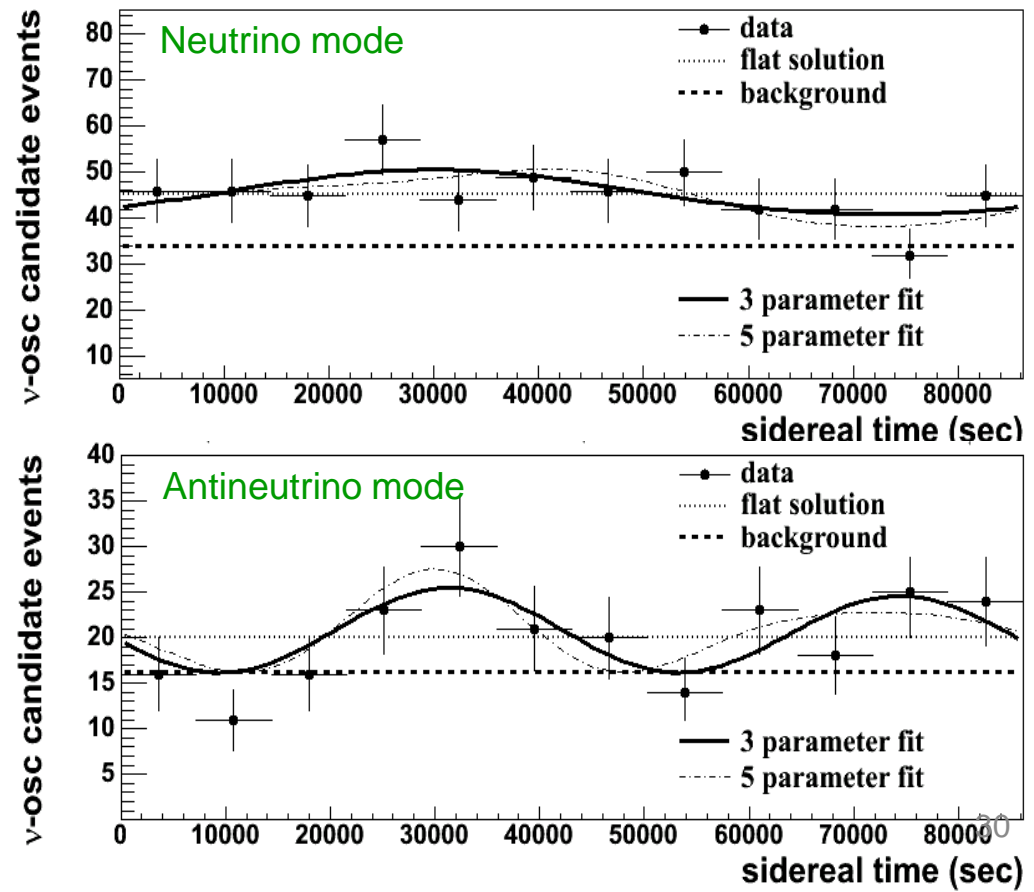
Antineutrino mode analysis: MiniBooNE saw the 1.4σ excess at low and high energy region

Electron neutrino candidate data
prefer **sidereal time independent**
solution (flat)

Electron antineutrino candidate data
prefer **sidereal time dependent**
solution, but statistical significance is
marginal

**We find no evidence of Lorentz
violation**

07/10/12



3. MiniBooNE experiment

MiniBooNE is a short-baseline neutrino oscillation experiment at Fermilab.

$$\nu_m \xrightarrow{\text{oscillation}} \nu_e + n \rightarrow e^- + p$$

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Neutrino mode analysis: MiniBooNE saw the 3.0σ excess at low energy region

Antineutrino mode analysis: MiniBooNE saw the 1.4σ excess at low and high energy region.

Since we find no evidence of Lorentz violation, we set limits on the SME coefficients.

These limits exclude SME values to explain LSND data, **therefore there is no simple Lorentz violation motivated scenario to accommodate LSND and MiniBooNE results simultaneously**

Coefficient	$e\mu$ (ν mode low energy region)	$e\mu$ ($\bar{\nu}$ mode combined region)
$\text{Re}(a_L)^T$ or $\text{Im}(a_L)^T$	4.2×10^{-20} GeV	2.6×10^{-20} GeV
$\text{Re}(a_L)^X$ or $\text{Im}(a_L)^X$	6.0×10^{-20} GeV	5.6×10^{-20} GeV
$\text{Re}(a_L)^Y$ or $\text{Im}(a_L)^Y$	5.0×10^{-20} GeV	5.9×10^{-20} GeV
$\text{Re}(a_L)^Z$ or $\text{Im}(a_L)^Z$	5.6×10^{-20} GeV	3.5×10^{-20} GeV
$\text{Re}(c_L)^{XY}$ or $\text{Im}(c_L)^{XY}$	—	—
$\text{Re}(c_L)^{XZ}$ or $\text{Im}(c_L)^{XZ}$	1.1×10^{-19}	6.2×10^{-20}
$\text{Re}(c_L)^{YZ}$ or $\text{Im}(c_L)^{YZ}$	9.2×10^{-20}	6.5×10^{-20}
$\text{Re}(c_L)^{XX}$ or $\text{Im}(c_L)^{XX}$	—	—
$\text{Re}(c_L)^{YY}$ or $\text{Im}(c_L)^{YY}$	—	—
$\text{Re}(c_L)^{ZZ}$ or $\text{Im}(c_L)^{ZZ}$	3.4×10^{-19}	1.3×10^{-19}
$\text{Re}(c_L)^{TT}$ or $\text{Im}(c_L)^{TT}$	9.6×10^{-20}	3.6×10^{-20}
$\text{Re}(c_L)^{TX}$ or $\text{Im}(c_L)^{TX}$	8.4×10^{-20}	4.6×10^{-20}
$\text{Re}(c_L)^{TY}$ or $\text{Im}(c_L)^{TY}$	6.9×10^{-20}	4.9×10^{-20}
$\text{Re}(c_L)^{TZ}$ or $\text{Im}(c_L)^{TZ}$	7.8×10^{-20}	2.9×10^{-20}

3. Double Chooz experiment

So far, we have set limits on

1. $\nu_e \leftrightarrow \nu_\mu$ channel: LSND, MiniBooNE, MINOS ($<10^{-20}$ GeV)

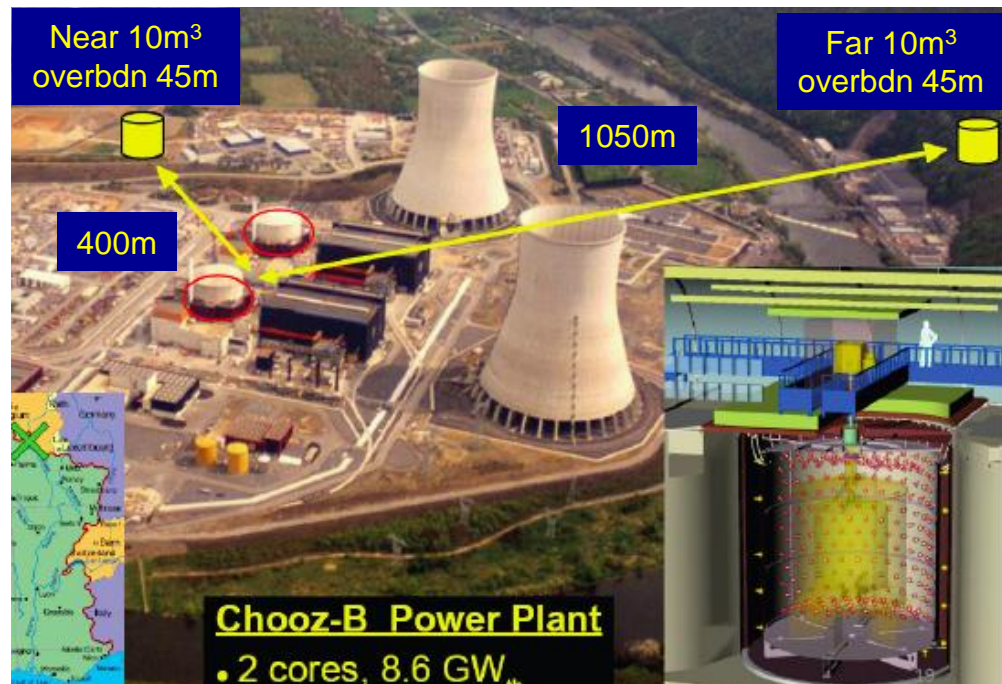
2. $\nu_\mu \leftrightarrow \nu_\tau$ channel: MINOS, IceCube ($<10^{-23}$ GeV)

The last untested channel is $\nu_e \leftrightarrow \nu_\tau$

It is possible to limit $\nu_e \leftrightarrow \nu_\tau$ channel from reactor ν_e disappearance experiment

$$P(\nu_e \leftrightarrow \nu_e) = 1 - P(\nu_e \leftrightarrow \nu_\mu) - P(\nu_e \leftrightarrow \nu_\tau) \sim 1 - P(\nu_e \leftrightarrow \nu_\tau)$$

Double Chooz observed the 3.1σ disappearance signal of electron antineutrinos from the reactor



3. Double Chooz experiment

So far, we have set limits on

1. $\nu_e \leftrightarrow \nu_\mu$ channel: LSND, MiniBooNE, MINOS ($<10^{-20}$ GeV)
2. $\nu_\mu \leftrightarrow \nu_\tau$ channel: MINOS, IceCube ($<10^{-23}$ GeV)

The last untested channel is $\nu_e \leftrightarrow \nu_\tau$

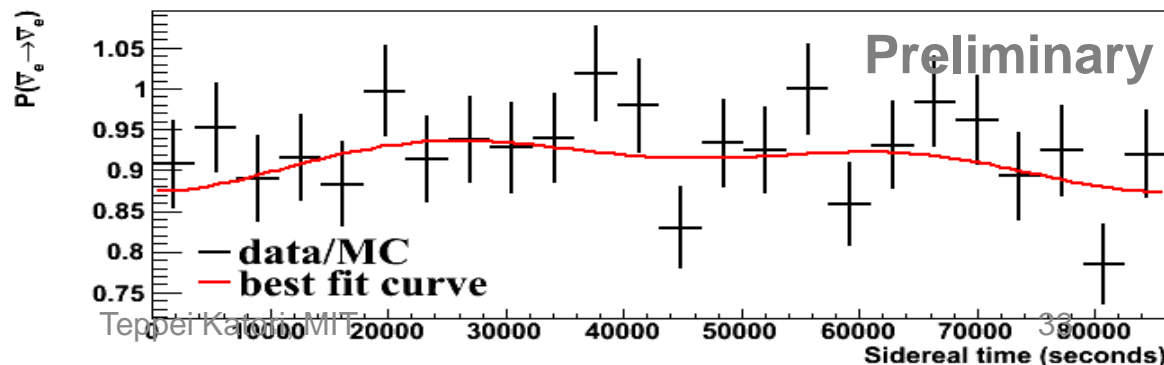
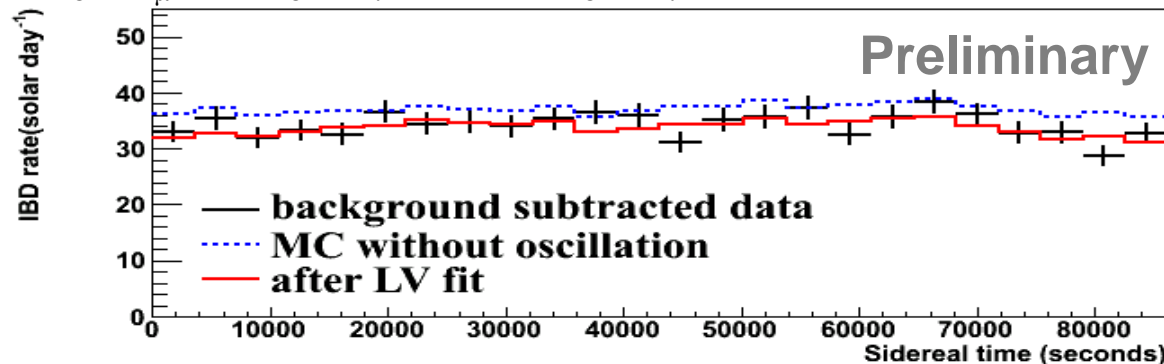
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Double Chooz observed the 3.1σ disappearance signal of electron antineutrinos from the reactor

Preliminary result shows small disappearance signal prefers
sidereal time independent solution
(flat)

We will be able to set limits in the
 e - τ sector for the first time;
 $\nu_e \leftrightarrow \nu_\tau$ ($<10^{-21}$ GeV)



Conclusion

Lorentz and CPT violation has been shown to occur in Planck-scale physics.

There is a world wide effort to test Lorentz violation with various state-of-the-art technologies.

LSND and MiniBooNE data suggest Lorentz violation is an interesting solution to neutrino oscillation.

MiniBooNE antineutrino mode data prefer sidereal time dependent solution, although statistical significance is not high. Limits from MiniBooNE exclude simple Lorentz violation motivated scenario for LSND.

MiniBooNE, LSND, MINOS, IceCube, and Double Chooz set stringent limits on Lorentz violation in neutrino sector in terrestrial level



Thank you for your attention!

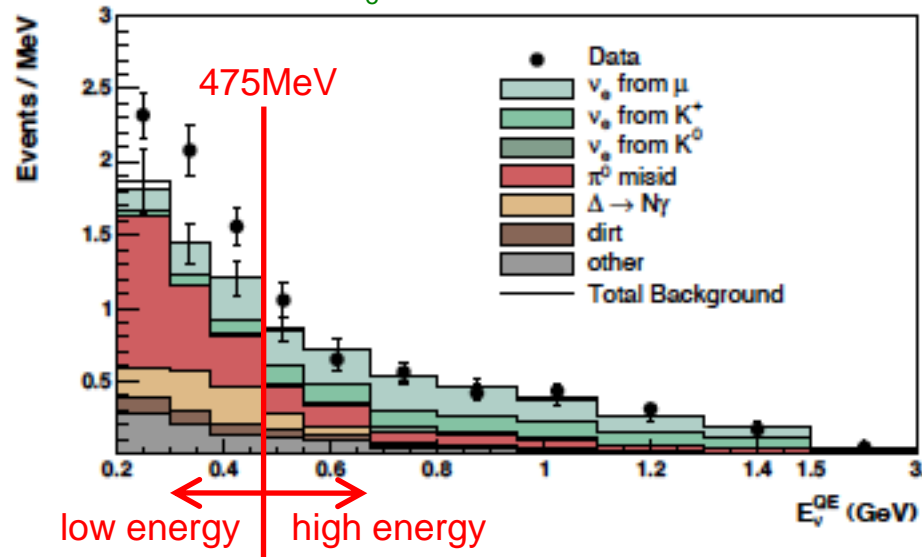
Backup

3. MiniBooNE oscillation analysis results

Neutrino mode low energy excess

MiniBooNE see the excess in low energy region.

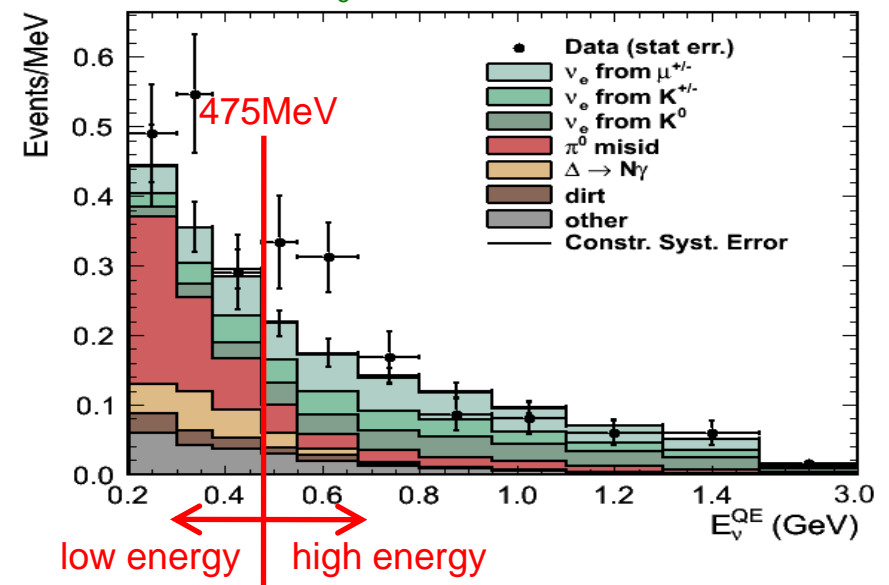
MiniBooNE low E ν_e excess



Antineutrino mode excess

MiniBooNE see the excess in combined region.

MiniBooNE anti- ν_e excess



These excesses are not predicted by neutrino Standard Model (ν SM).

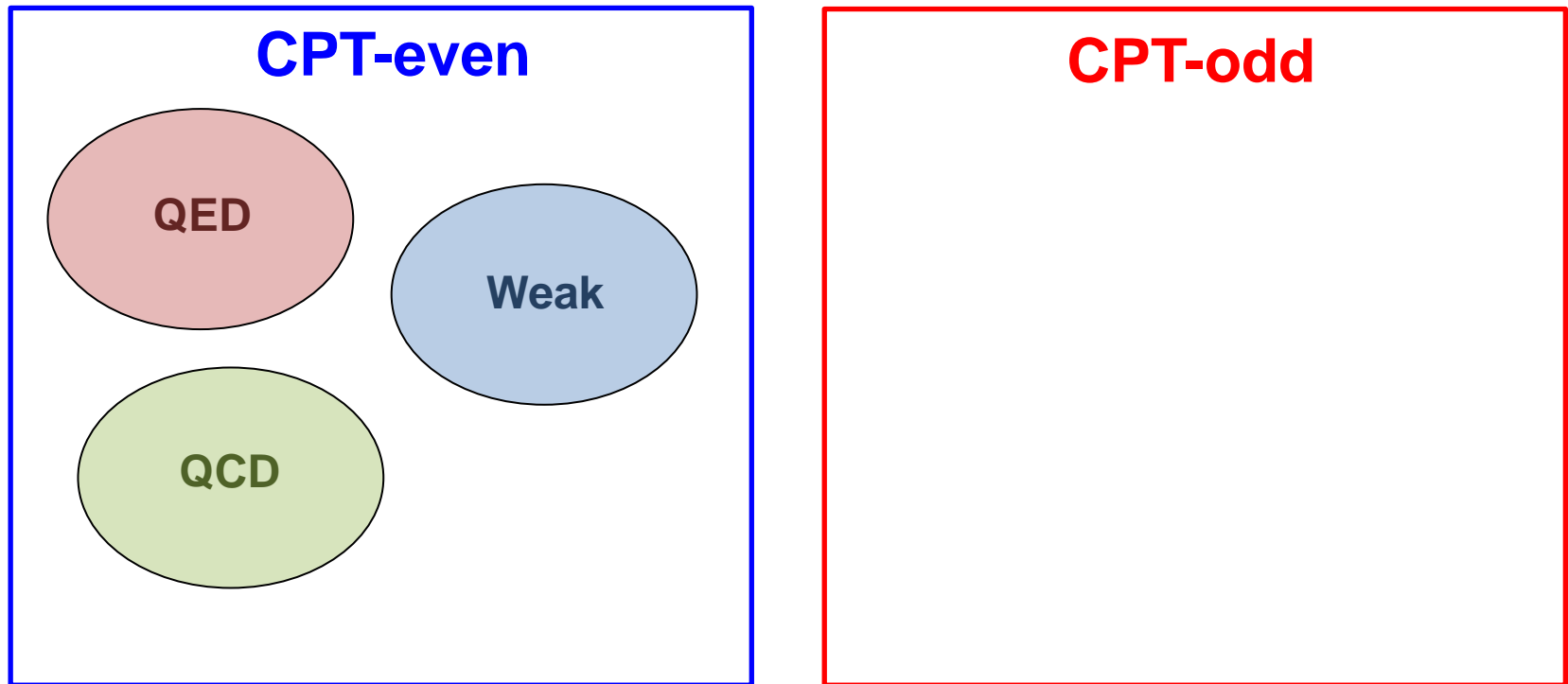
Oscillation candidate events may have sidereal time dependence.

2. What is CPT violation?

CPT symmetry is the invariance under CPT transformation

$$L \xrightarrow{\text{CPT}} \Theta L \Theta^{-1} = L' = L, \quad \Theta = \text{CPT}$$

CPT is the perfect symmetry of the Standard Model, due to CPT theorem

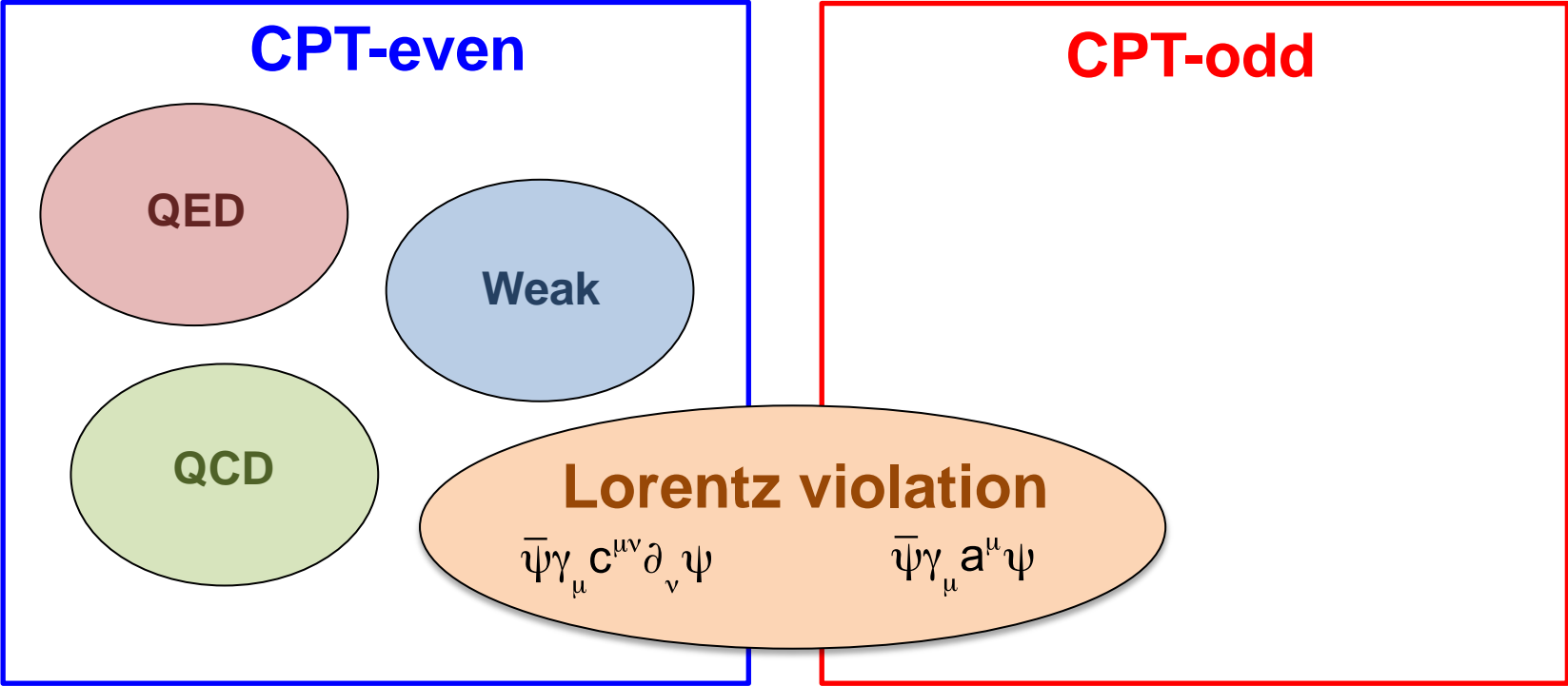


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CPT-odd Lorentz violating coefficients (odd number Lorentz indices, ex., a^{μ} , $g^{\lambda\mu\nu}$)
 CPT-even Lorentz violating coefficients (even number Lorentz indices, ex., $c^{\mu\nu}$, $\kappa^{\alpha\beta\mu\nu}$)

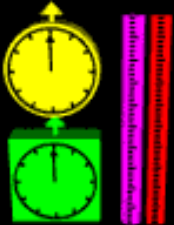
2. Modern tests of Lorentz violation

The last meeting of Lorentz and CPT violation was in summer 2010.

Next meeting will be in summer 2013

<http://www.physics.indiana.edu/~kostelec/faq.html>

CPT'10



MEETING LINKS

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[Proceedings](#)
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[IU Astronomy](#)
[IU Bloomington](#)
[Bloomington area](#)

Fifth Meeting on CPT AND LORENTZ SYMMETRY

June 28-July 2, 2010

Indiana University, Bloomington

The *Fifth Meeting on CPT and Lorentz Symmetry* will be held in the [Physics Department, Indiana University](#) in [Bloomington](#), Indiana, U.S.A. on June 28-July 2, 2010. The meeting will focus on tests of these fundamental symmetries and on related theoretical issues, including scenarios for possible violations.

Topics include:

- searches for CPT and Lorentz violations involving
 - birefringence and dispersion from cosmological sources
 - clock-comparison measurements
 - CMB polarization
 - collider experiments
 - electromagnetic resonant cavities
 - equivalence principle
 - gauge and Higgs particles
 - high-energy astrophysical observations
 - laboratory and gravimetric tests of gravity

2. Modern tests of Lorentz violation

<http://www.physics.indiana.edu/~kostelec/faq.html>

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Topics:

- * searches for CPT and Lorentz violations involving
 - birefringence and dispersion from cosmological sources
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 - equivalence principle
 - gauge and Higgs particles
 - high-energy astrophysical observations
 - laboratory and gravimetric tests of gravity
 - matter interferometry
 - neutrino oscillations
 - oscillations and decays of K, B, D mesons
 - particle-antiparticle comparisons
 - post-newtonian gravity in the solar system and beyond
 - second- and third-generation particles
 - space-based missions
 - spectroscopy of hydrogen and antihydrogen
 - spin-polarized matter
- * theoretical studies of CPT and Lorentz violation involving
 - physical effects at the level of the Standard Model, General Relativity, and beyond
 - origins and mechanisms for violations
 - classical and quantum issues in field theory, particle physics, gravity, and strings

Atomic Interferometer
(a,c)^{n,p,e} < 10⁻⁶



Steven Chu

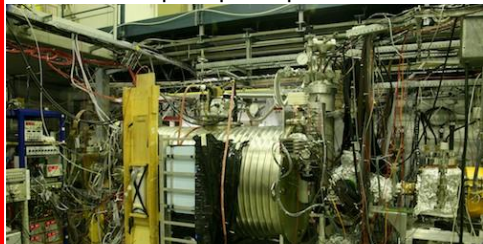
PRL106(2011)1

of Lorentz v

a.edu/~kostelec/fa

otics:

CERN Antiproton Decelerator
(M_p-M_p)/M_p < 10⁻⁸



Tevatron and LEP
-5.8x10⁻¹² < κ_{tr}-4/3c_e⁰⁰ < 1.2x10⁻¹¹



PRL102(2009)170402

ts
esonant cavities
ple
ana University, Bloomington
particles

GRB vacuum birefringence
κ_{e+}, κ_o < 10⁻³⁷



PRL97(2006)140401

ources

Double gas maser
b_n(rotation) < 10⁻³³ GeV
b_n(boost) < 10⁻²⁷ GeV



Test of Lorentz invariance with neutrinos is very interesting,
because neutrinos are the least known standard model particles!

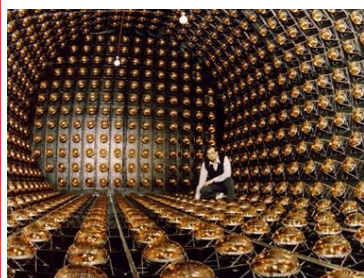
- ★ neutrino oscillations
- oscillations and decays of
- ★ particle-antiparticle comp
- post-newtonian gravity in



Cryogenic optical resonator
Δc/c < 10⁻¹⁶



LSND



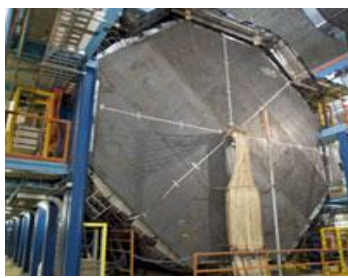
PRD72(2005)076004

MINOS ND



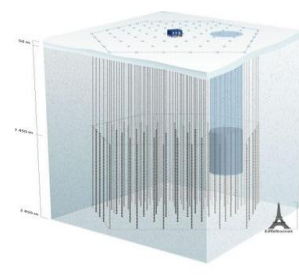
PRL101(2008)151601

MINOS FD



PRL105(2010)151601

IceCube



PRD82(2010)112003

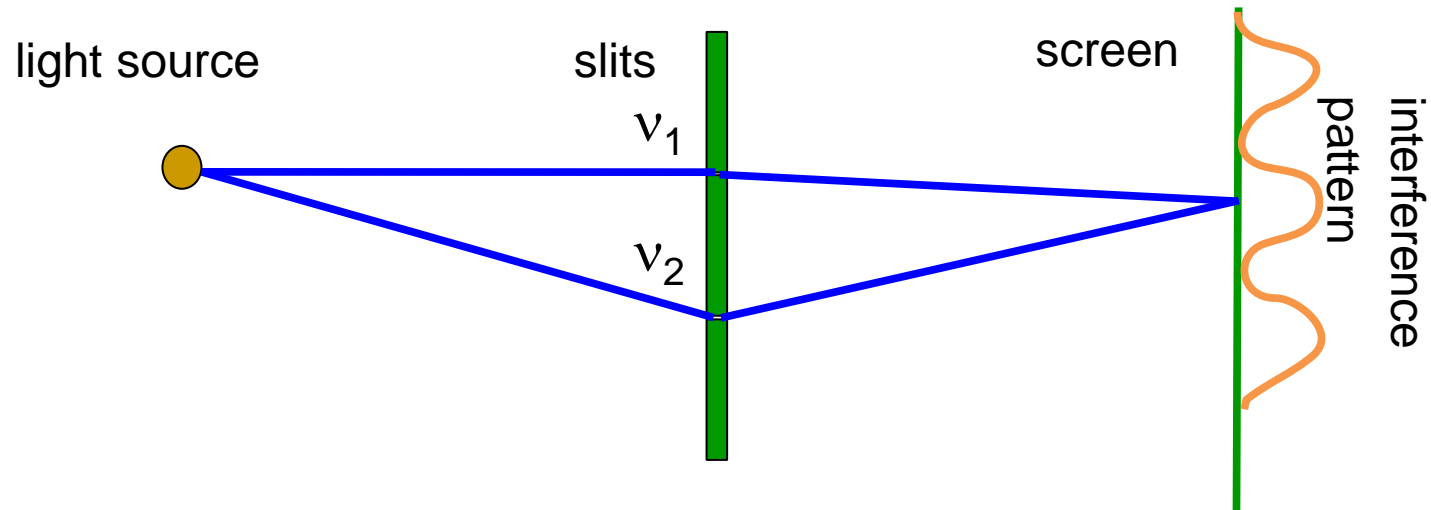
MiniBooNE



arXiv:1109.3480

2. Neutrino oscillations, natural interferometers

Neutrino oscillation is an interference experiment (e.g. double slit experiment)

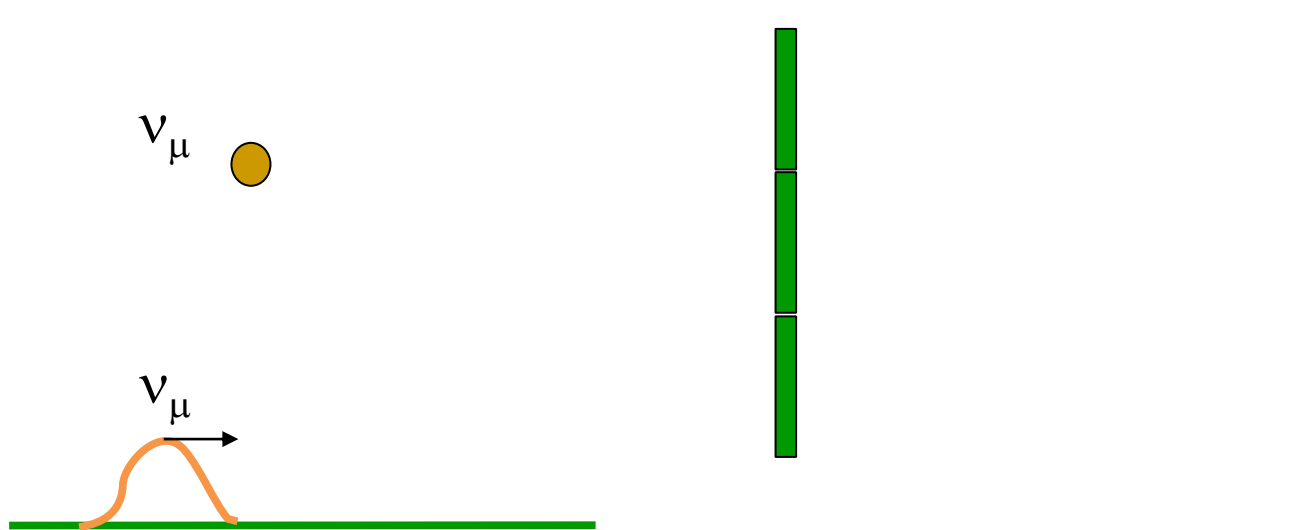


For double slit experiment, if path v_1 and path v_2 have different lengths, they have different phase rotations and it causes interference.

In terms of neutrinos, if Hamiltonian eigenstates v_1 and v_2 are different, that can be the source of neutrino oscillations.

2. Lorentz violation with neutrino oscillation

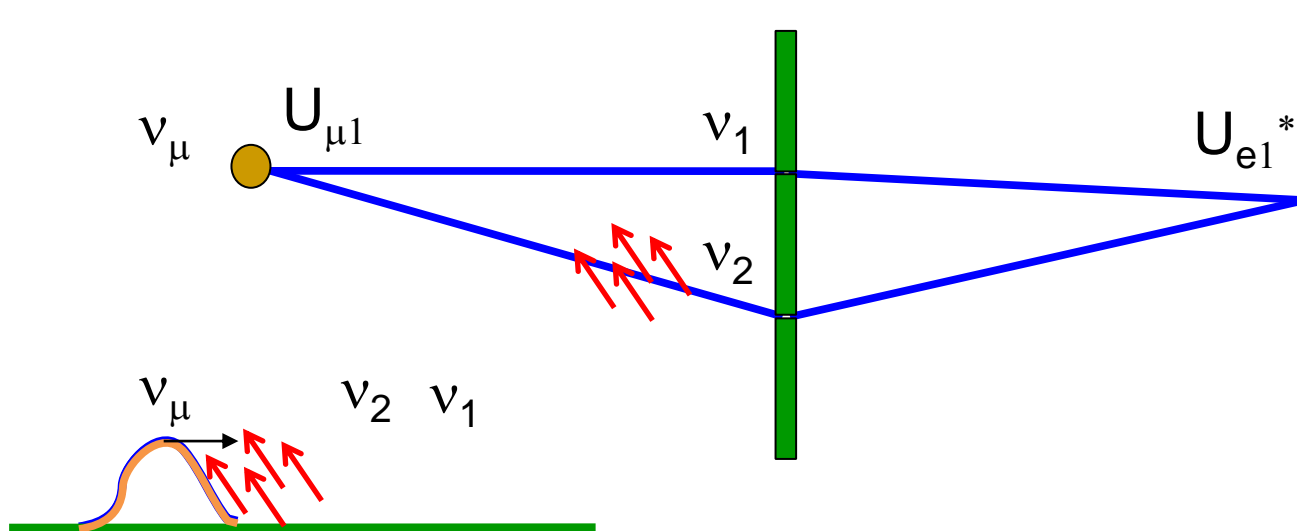
Neutrino oscillation is an interference experiment (e.g. double slit experiment)



If 2 neutrino Hamiltonian eigenstates, ν_1 and ν_2 , have different phase rotations, they cause quantum interference.

2. Lorentz violation with neutrino oscillation

Neutrino oscillation is an interference experiment (e.g. double slit experiment)

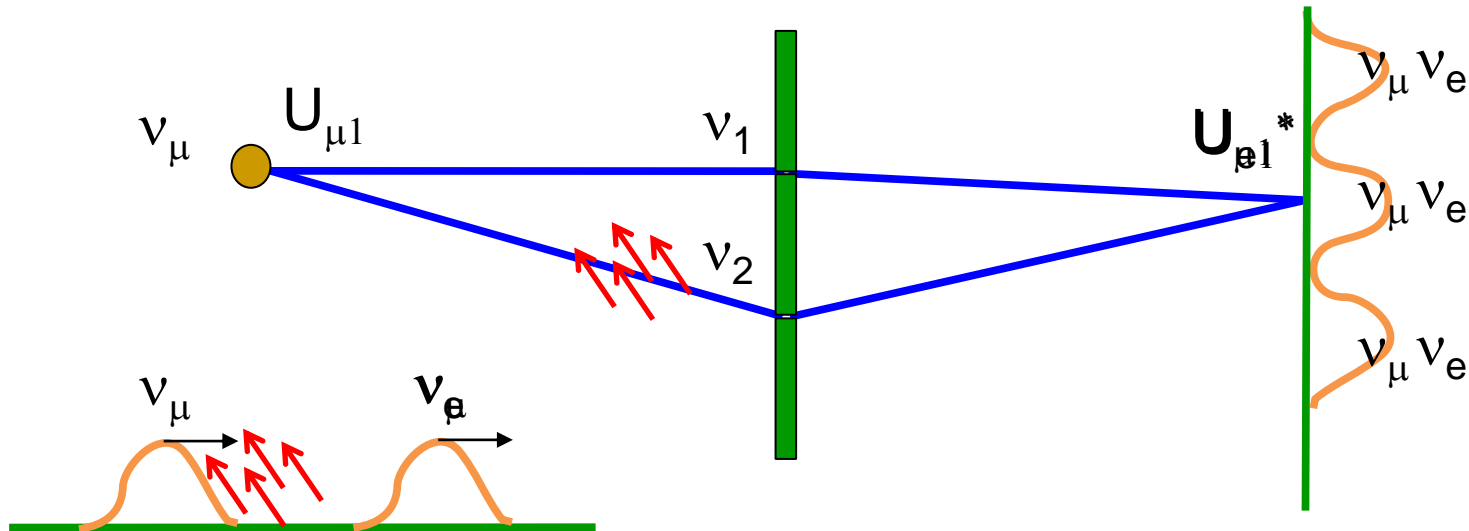


If 2 neutrino Hamiltonian eigenstates, ν_1 and ν_2 , have different phase rotations, they cause quantum interference.

If ν_1 and ν_2 have different couplings with Lorentz-violating field, that can be the source of neutrino oscillations.

2. Lorentz violation with neutrino oscillation

Neutrino oscillation is an interference experiment (e.g. double slit experiment)



If 2 neutrino Hamiltonian eigenstates, ν_1 and ν_2 , have different phase rotations, they cause quantum interference.

If ν_1 and ν_2 have different couplings with Lorentz-violating field, that can be the source of neutrino oscillations.

Interference fringe (oscillation pattern) depends on the sidereal motion. The measured scale of neutrino eigenvalue difference is comparable the target scale of Lorentz violation ($<10^{-19}\text{GeV}$).

3. Test of Lorentz violation with neutrino oscillation experiments

Lorentz violation is realized as a coupling of particle fields and background fields, so the basic strategy to find Lorentz violation is:

- (1) fix the coordinate system
- (2) write down the Lagrangian, including Lorentz-violating terms under the formalism
- (3) write down the observables using this Lagrangian

Standard Model Extension (SME) is the standard formalism for the general search for Lorentz violation. SME is a minimum extension of QFT with Particle Lorentz violation

Modified Dirac Equation (MDE) of neutrinos

$$i(G_{AB}^n \not{n} - M_{AB})n_B = 0$$

SME coefficients

$$G_{AB}^n = g^n d_{AB} + \boxed{c_{AB}^{mn}} g_m + \boxed{d_{AB}^{mn}} g_m g_5 + \boxed{e_{AB}^n} + \boxed{f_{AB}^n} g_5 + \frac{1}{2} \boxed{g_{AB}^{lmn}} S_{lm}$$

$$M_{AB} = m_{AB} + i m_{5AB} g_5 + \boxed{a_{AB}^m} g_m + \boxed{b_{AB}^m} g_5 g_m + \frac{1}{2} \boxed{H_{AB}^{mn}} S_{mn}$$

CPT even

CPT odd