

# Implications of 125 GeV Higgs in Composite Models

Michele Redi



with Stefania de Curtis and Andrea Tesi  
1110.1613 + 1205.0232

ICHEP, 7 July

# OUTLINE

- Minimal Effective description of Goldstone boson Higgs
- Higgs and fermion masses in Composite Higgs

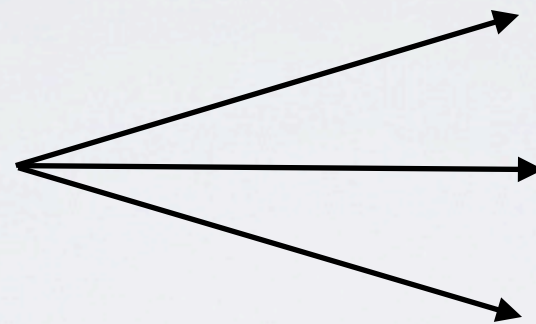


# COMPOSITE HIGGS

Georgi, Kaplan '80s

Higgs doublet could be a light remnant of strong dynamics.

Strong sector:  
resonances +  
Higgs bound state



spin 1

spin 1/2

spin 0....  $2\frac{1}{2}$

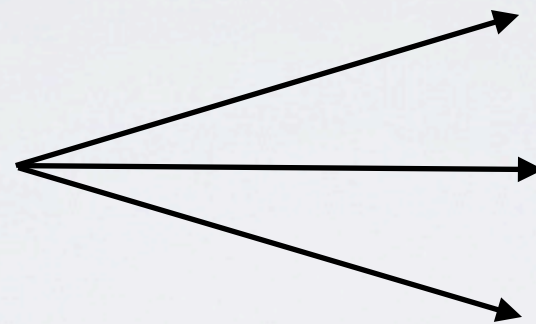
*Michele Redi, ICHEP 2012, Melbourne*

# COMPOSITE HIGGS

Georgi, Kaplan '80s

Higgs doublet could be a light remnant of strong dynamics.

Strong sector:  
resonances +  
Higgs bound state



spin 1

spin 1/2

spin 0....  $2\frac{1}{2}$

Particularly compelling if Higgs is a Goldstone Boson.  
Massless at leading order.

Ex:  $\frac{SO(5)}{SU(2)_L \otimes SU(2)_R} \longrightarrow GB = (2, 2)$

Agashe , Contino,  
Pomarol, '04

$$\mathcal{L} = f^2 D_\mu \Sigma^i D^\mu \Sigma^i + \dots$$

Michele Redi, ICHEP 2012, Melbourne



Relieves hierarchy problem:



$$\sim \frac{1}{m_\rho} = \frac{1}{\text{TeV}}$$

$$m_\rho = g_\rho f$$

$$1 < g_\rho < 4\pi$$

$$\delta m_h^2 \sim N_c \frac{y_t^2}{8\pi^2} m_\rho^2$$

Increasing  $f$  CH approximates SM.

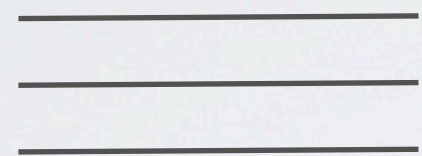
$$\text{DEVIATIONS} \sim \frac{v^2}{f^2}$$

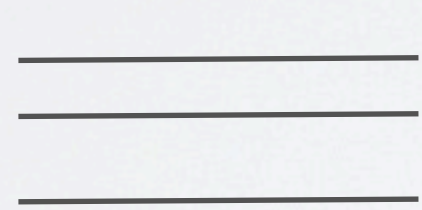


Increasing  $f$  CH approximates SM.

$$\text{DEVIATIONS} \sim \frac{v^2}{f^2}$$

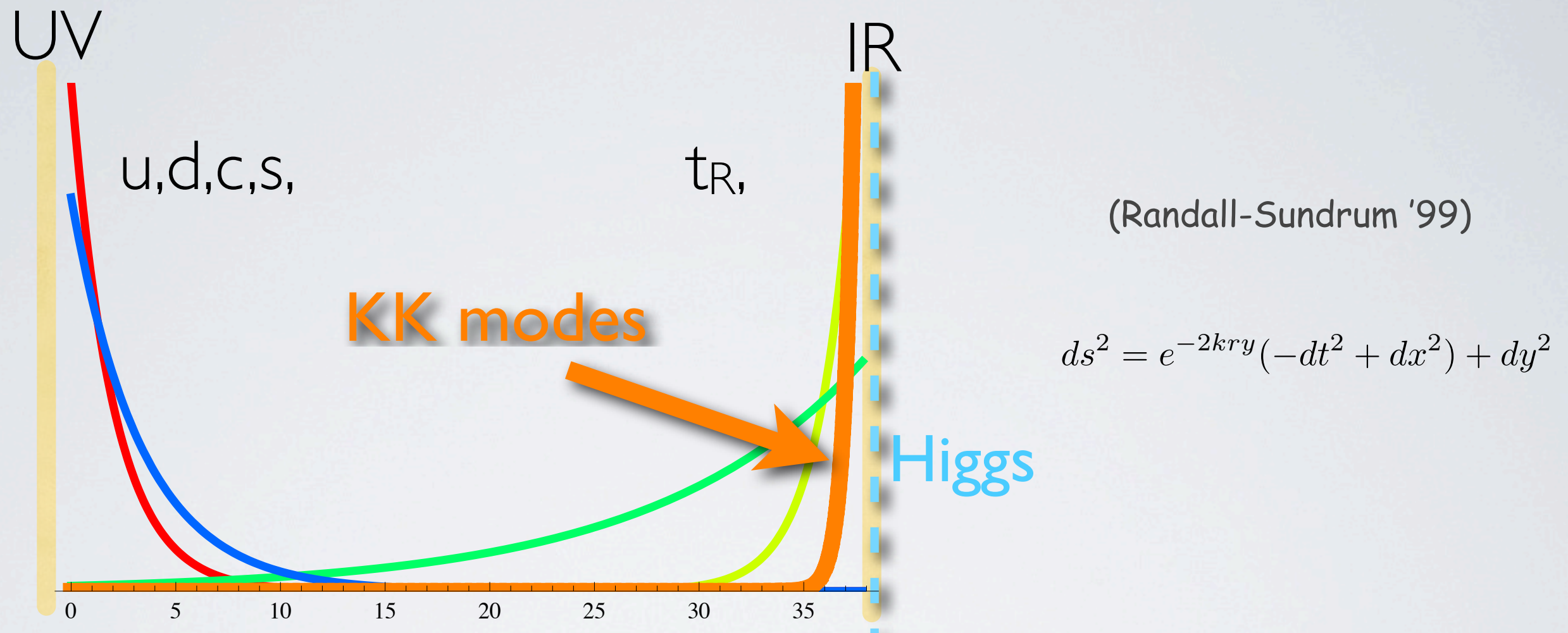
Spectrum:


$$m_\rho \sim 3 \text{ TeV}$$


$$\begin{aligned} m_h &= 125 \text{ GeV} \\ m_W &= 80 \text{ GeV} \\ 0 \end{aligned}$$

Reasonable phenomenology can be obtained for  $m_\rho \sim 3 \text{ TeV}$

Possible to realize it in Randall-Sundrum scenarios.



Through AdS/CFT correspondence dual to 4D CFTs.  
Relevant physics dominated by the lowest modes.



# MINIMAL 4D COMPOSITE HIGGS

- One resonance for each SM field

Related work:  
Contino, Kramer, Son, Sundrum '06  
Panico, Wulzer '11

*Michele Redi, ICHEP 2012, Melbourne*

# General picture:

Strong sector:  
Higgs + (top)

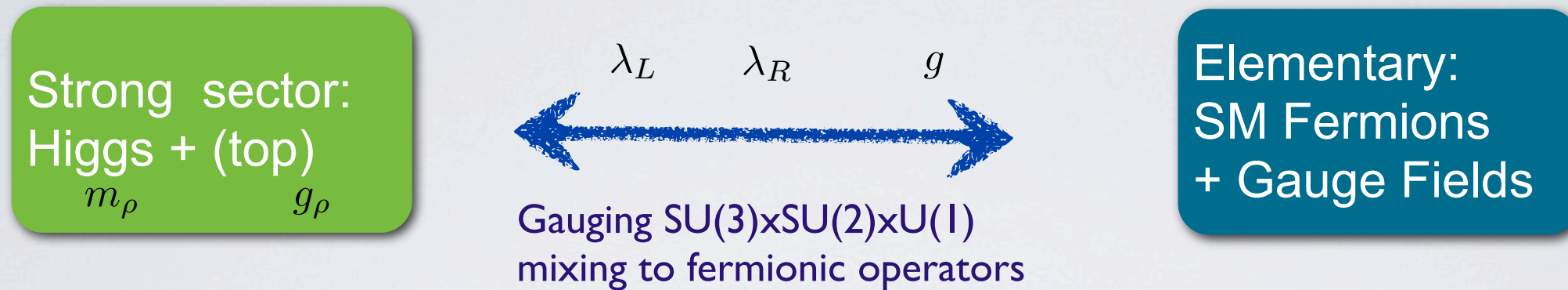
$m_\rho$

$g_\rho$

Elementary:  
SM Fermions  
+ Gauge Fields



## General picture:



They talk through linear couplings:

$$\mathcal{L}_{gauge} = g A_\mu J^\mu$$

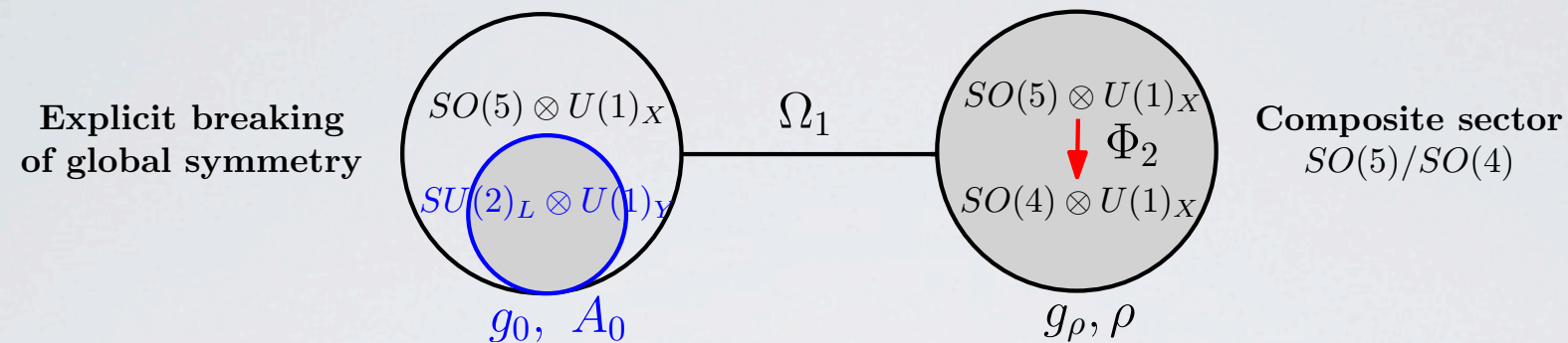
$$\mathcal{L}_{mixing} = \lambda_L \bar{f}_L O_R + \lambda_R \bar{f}_R O_R \quad \xrightarrow{\epsilon \sim \frac{\lambda}{Y}} \quad y_{SM} = \epsilon_L \cdot Y \cdot \epsilon_R$$

Higgs potential generated at 1-loop:

$$V(h) \sim \frac{N_c}{16\pi^2} \epsilon_{L,R}^2 m_\rho^4 \hat{V} \left( \frac{h}{f} \right) + \dots$$

Michele Redi, ICHEP 2012, Melbourne

- $SO(5)/SO(4)$



Composite spin-1 lagrangian:

$$\frac{f_1^2}{4} \text{Tr} |D_\mu \Omega|^2 + \frac{f_2^2}{2} (D_\mu \Phi)^T (D^\mu \Phi) - \frac{1}{4g_\rho^2} \rho_{\mu\nu}^a \rho^{a\mu\nu}$$

$$\Omega = \frac{SO(5)_L \times SO(5)_R}{SO(5)_{L+R}}$$

$$\Phi = \frac{SO(5)}{SO(4)}$$

$$D_\mu \Omega = \partial_\mu \Omega - iA_\mu \Omega + i\Omega \rho_\mu$$

$$D_\mu \Phi = \partial_\mu \Phi - i\rho_\mu \Phi$$

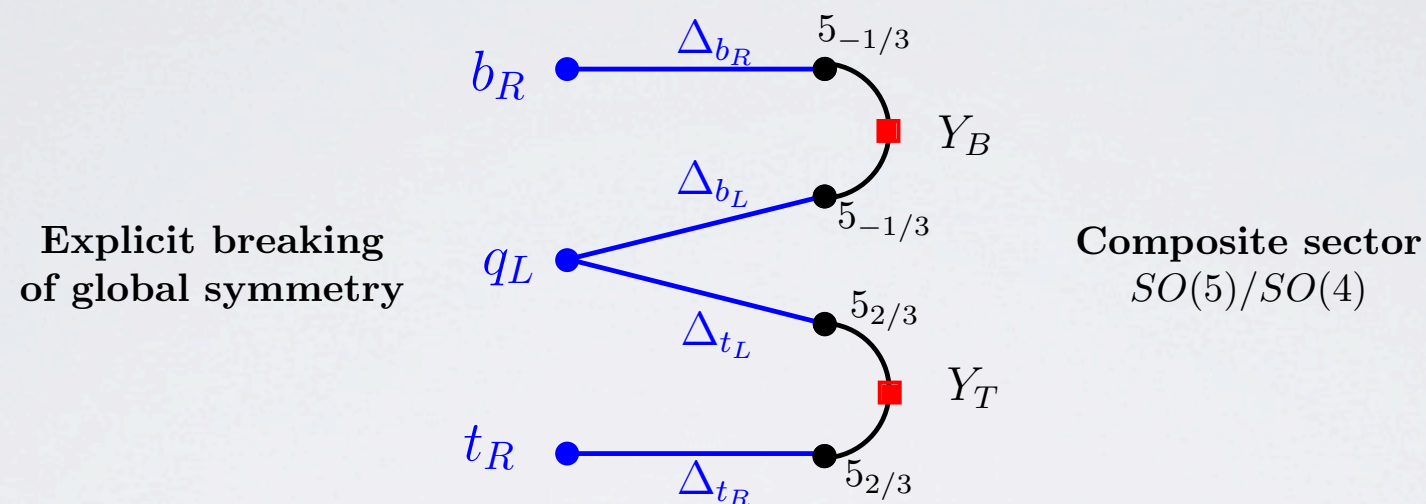
$SO(4)$  and  $SO(5)/SO(4)$  spin-1 resonances.

Michele Redi, ICHEP 2012, Melbourne



Each SM fermion couples to Dirac fermion in a rep of  $SO(5)$ .

CHM5:



Third generation:

$$\begin{aligned}
 \mathcal{L}^{\text{CHM}_5} = & \mathcal{L}_{\text{fermions}}^{\text{el}} \\
 & + \Delta_{t_L} \bar{q}_L^{\text{el}} \Omega_1 \Psi_T + \Delta_{t_R} \bar{t}_R^{\text{el}} \Omega_1 \Psi_{\tilde{T}} + h.c. \\
 & + \bar{\Psi}_T (i \not{D}^\rho - m_T) \Psi_T + \bar{\Psi}_{\tilde{T}} (i \not{D}^\rho - m_{\tilde{T}}) \Psi_{\tilde{T}} \\
 & - Y_T \bar{\Psi}_{T,L} \Phi_2^T \Phi_2 \Psi_{\tilde{T},R} - m_{Y_T} \bar{\Psi}_{T,L} \Psi_{\tilde{T},R} + h.c. \\
 & + (T \rightarrow B)
 \end{aligned}$$

Explicit  $SO(5)$  breaking

Composite physics  
 $SO(5)/SO(4)$

Michele Redi, ICHEP 2012, Melbourne

Coleman-Weinberg effective potential:

$$V(h)_{fermions} = -2N_c \int \frac{d^4 p}{(2\pi)^4} [\ln \Pi_{b_L} + \ln (p^2 \Pi_{t_L} \Pi_{t_R} - \Pi_{t_L t_R}^2)]$$

Contino, da Rold, Pomarol, '06

Form factors are simple functions:

$$\widehat{\Pi}[m_1, m_2, m_3] = \frac{(m_2^2 + m_3^2 - p^2)}{p^4 - p^2(m_1^2 + m_2^2 + m_3^2) + m_1^2 m_2^2}$$
$$\widehat{M}[m_1, m_2, m_3] = -\frac{m_1 m_2 m_3}{p^4 - p^2(m_1^2 + m_2^2 + m_3^2) + m_1^2 m_2^2}$$

Potential is finite with a single SO(5) multiplet per SM field!

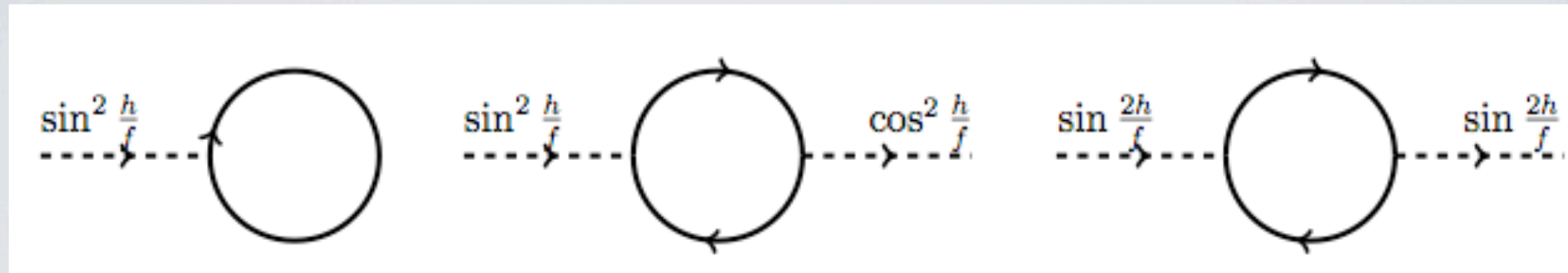
Michele Redi, ICHEP 2012, Melbourne



# What is the Higgs mass?

*Michele Redi, ICHEP 2012, Melbourne*

# CHM5 ESTIMATES

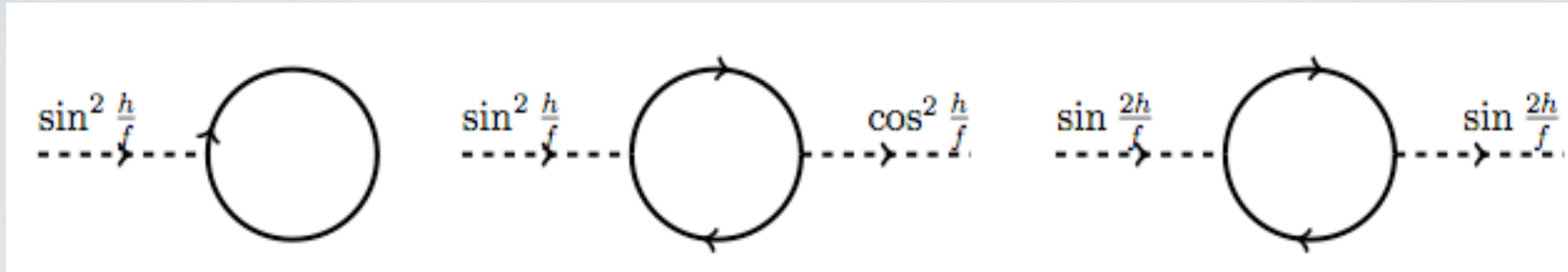


$$\mathcal{L}_{Yuk} = y_t f \frac{s_h c_h}{h} (\bar{q}_L H^c t_R + h.c.) \longrightarrow V(h)_{Yuk} \sim N_c \frac{y_t^2}{16\pi^2} m_f^2 f^2 s_h^2 c_h^2$$

$$\mathcal{L}_{kin} = \epsilon_L^2 s_h^2 \bar{t}_L \not{D} t_L + 2 \epsilon_R^2 s_h^2 \bar{t}_R \not{D} t_R \longrightarrow V(h)_{kin} \sim N_c \frac{2\epsilon_R^2 - \epsilon_L^2}{32\pi^2} m_f^4 s_h^2$$



# CHM5 ESTIMATES



$$\mathcal{L}_{Yuk} = y_t f \frac{s_h c_h}{h} (\bar{q}_L H^c t_R + h.c.) \longrightarrow V(h)_{Yuk} \sim N_c \frac{y_t^2}{16\pi^2} m_f^2 f^2 s_h^2 c_h^2$$

$$\mathcal{L}_{kin} = \epsilon_L^2 s_h^2 \bar{t}_L \not{D} t_L + 2 \epsilon_R^2 s_h^2 \bar{t}_R \not{D} t_R \longrightarrow V(h)_{kin} \sim N_c \frac{2\epsilon_R^2 - \epsilon_L^2}{32\pi^2} m_f^4 s_h^2$$

Potential:

$$V(h) \approx \alpha s_h^2 - \beta s_h^2 c_h^2 \qquad s_h \equiv \sin \frac{h}{f} = \frac{v}{f}$$

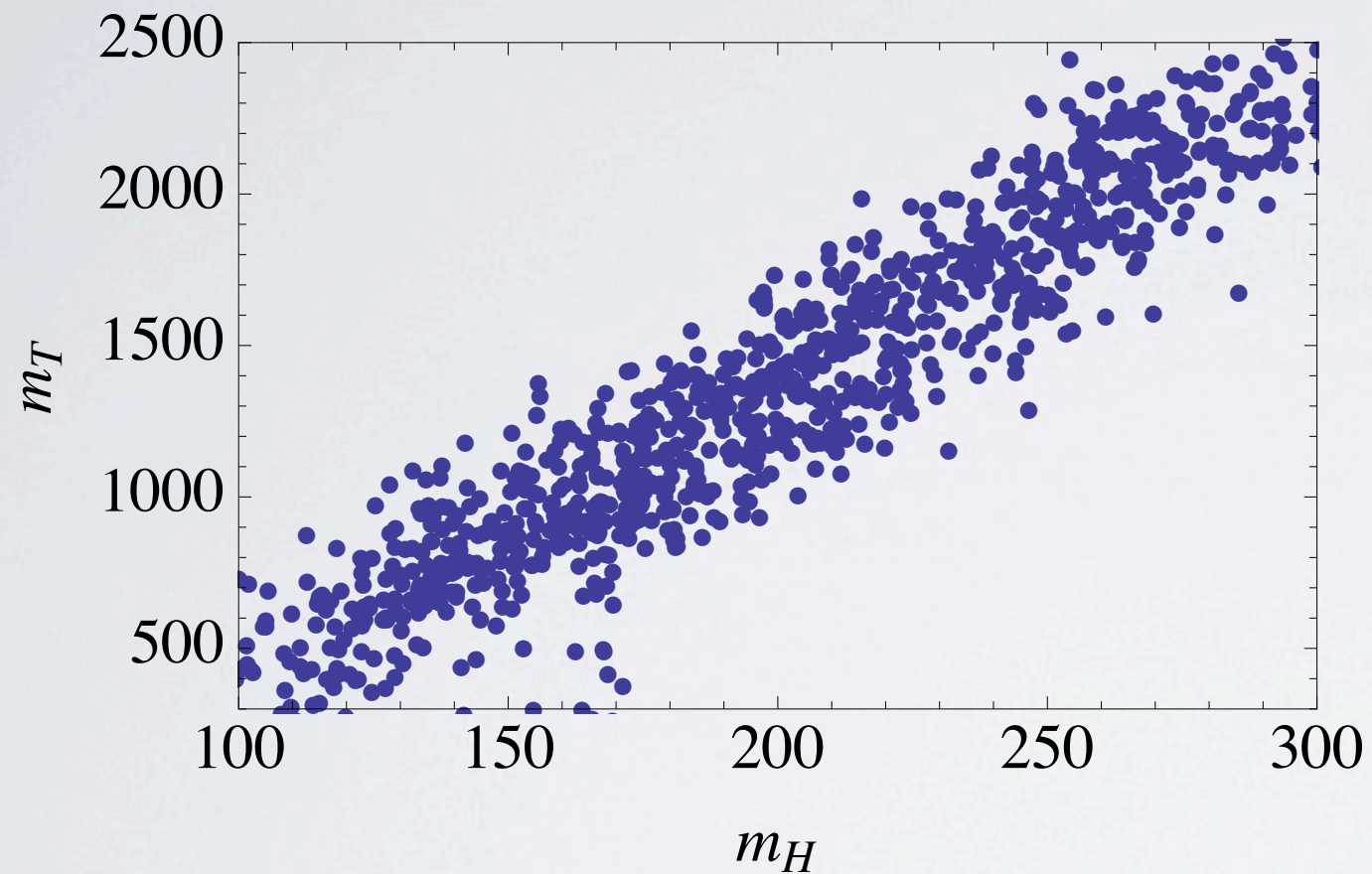
Quartic is determined by top Yukawa,

$$m_h \sim \sqrt{\frac{N_c}{2}} \frac{y_t}{\pi} \frac{m_f}{f} v$$

- CHM5

General scan:

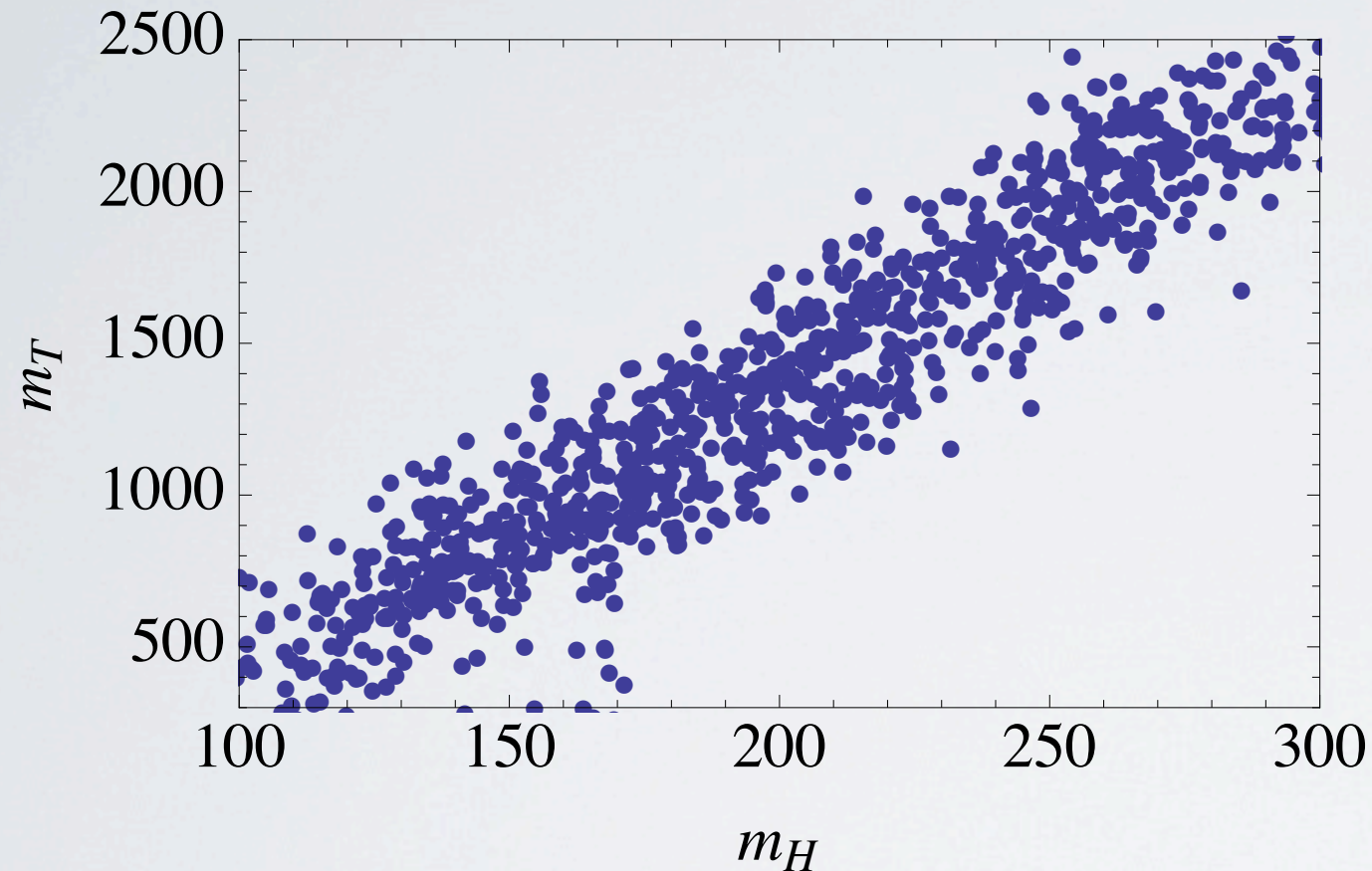
$$f = 500 \text{ GeV}$$





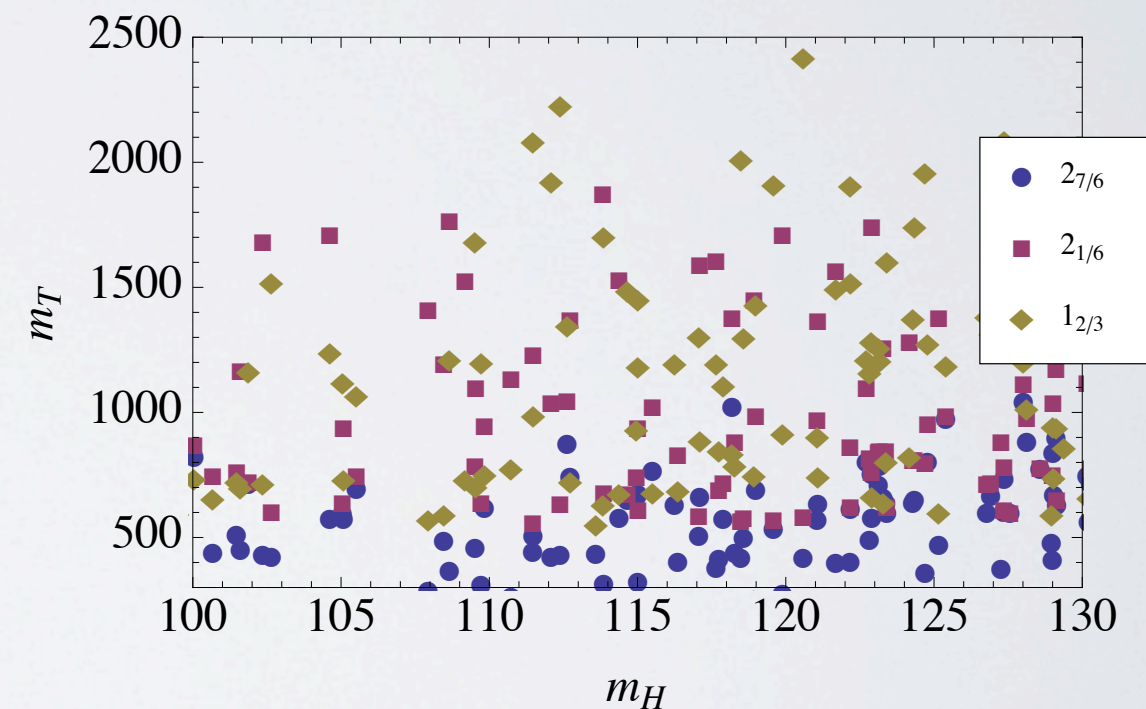
- CHM5

General scan:



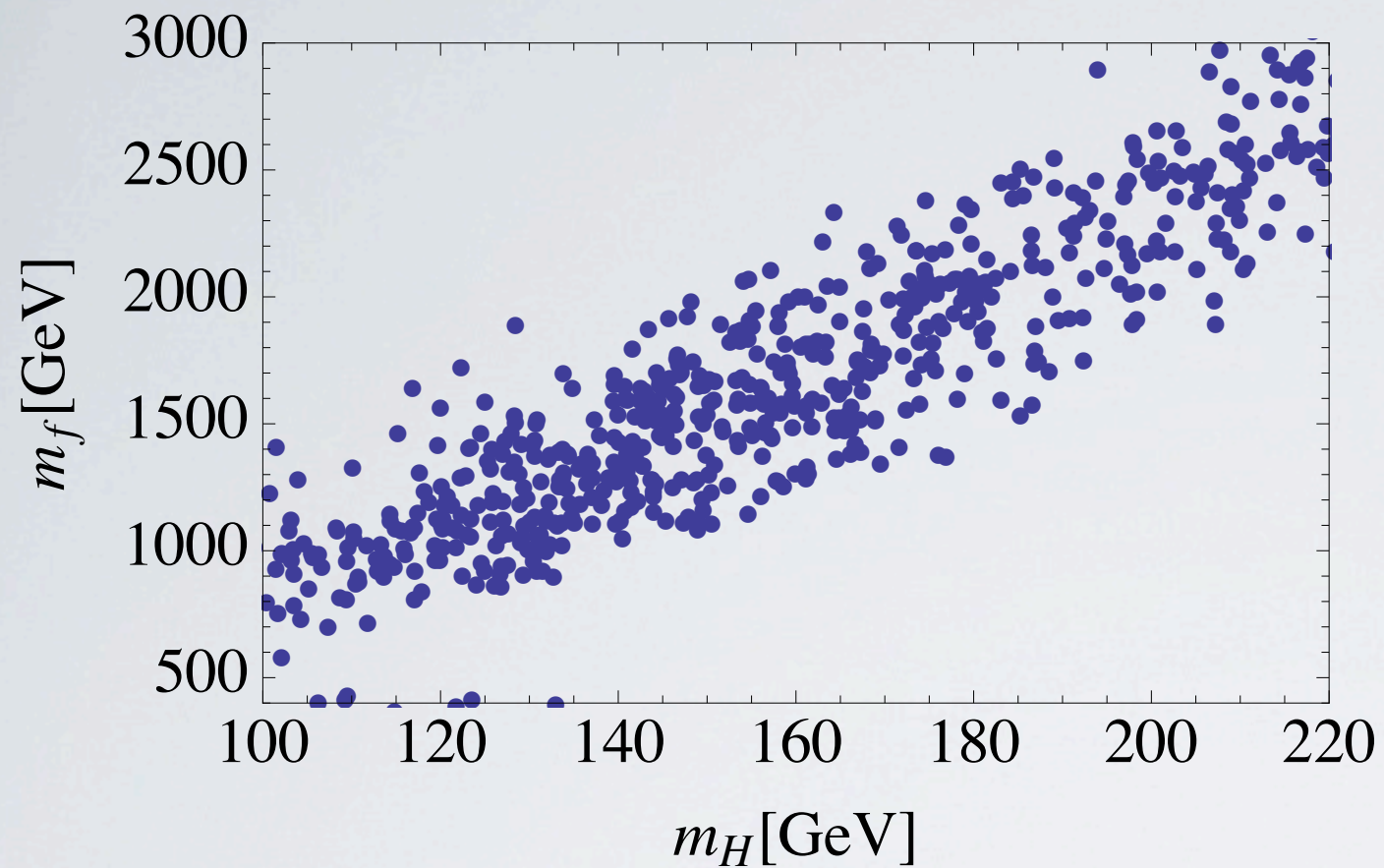
$$f = 500 \text{ GeV}$$

Low mass:



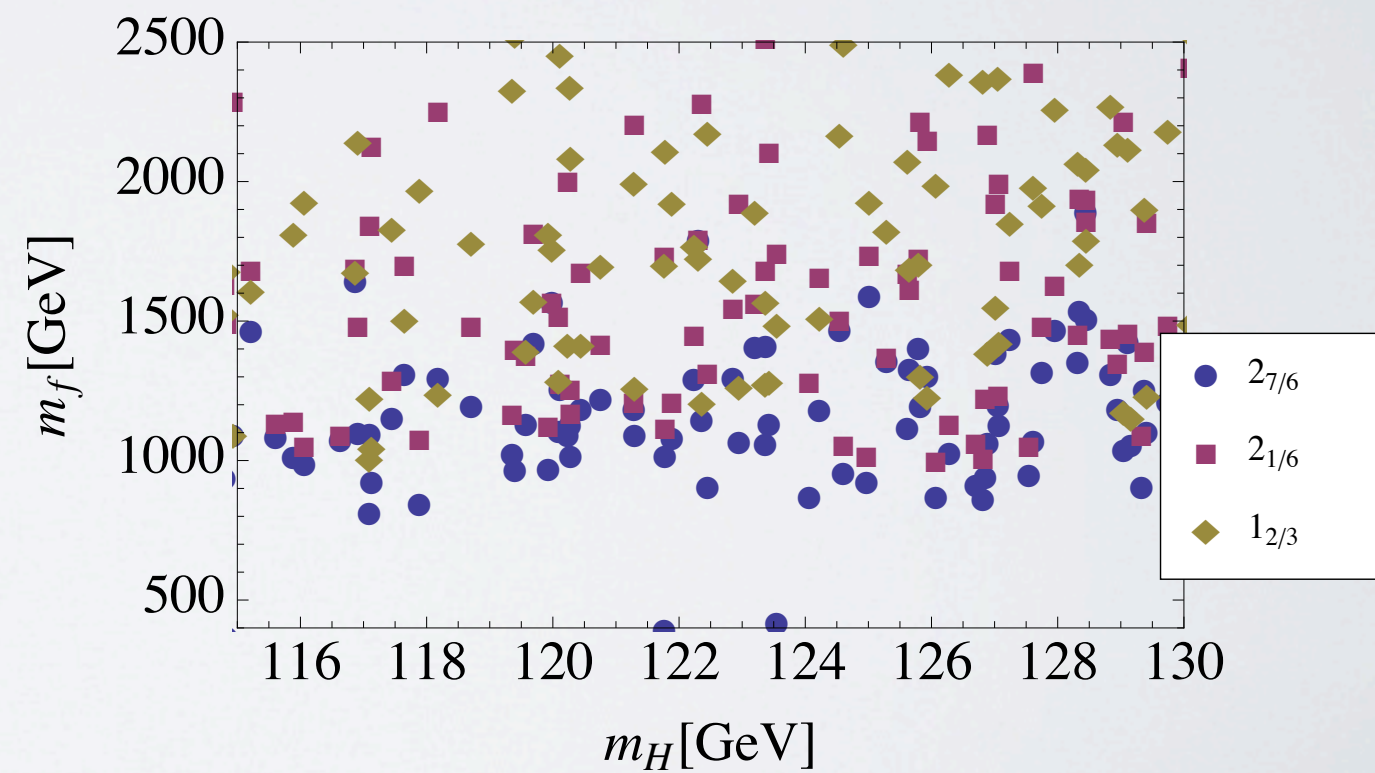
For  $m_H = 125 \text{ GeV}$ , fermionic partners VERY close.  
Should be visible at LHC7!

*Michele Redi, ICHEP 2012, Melbourne*



$$f = 800 \text{ GeV}$$

Low mass:



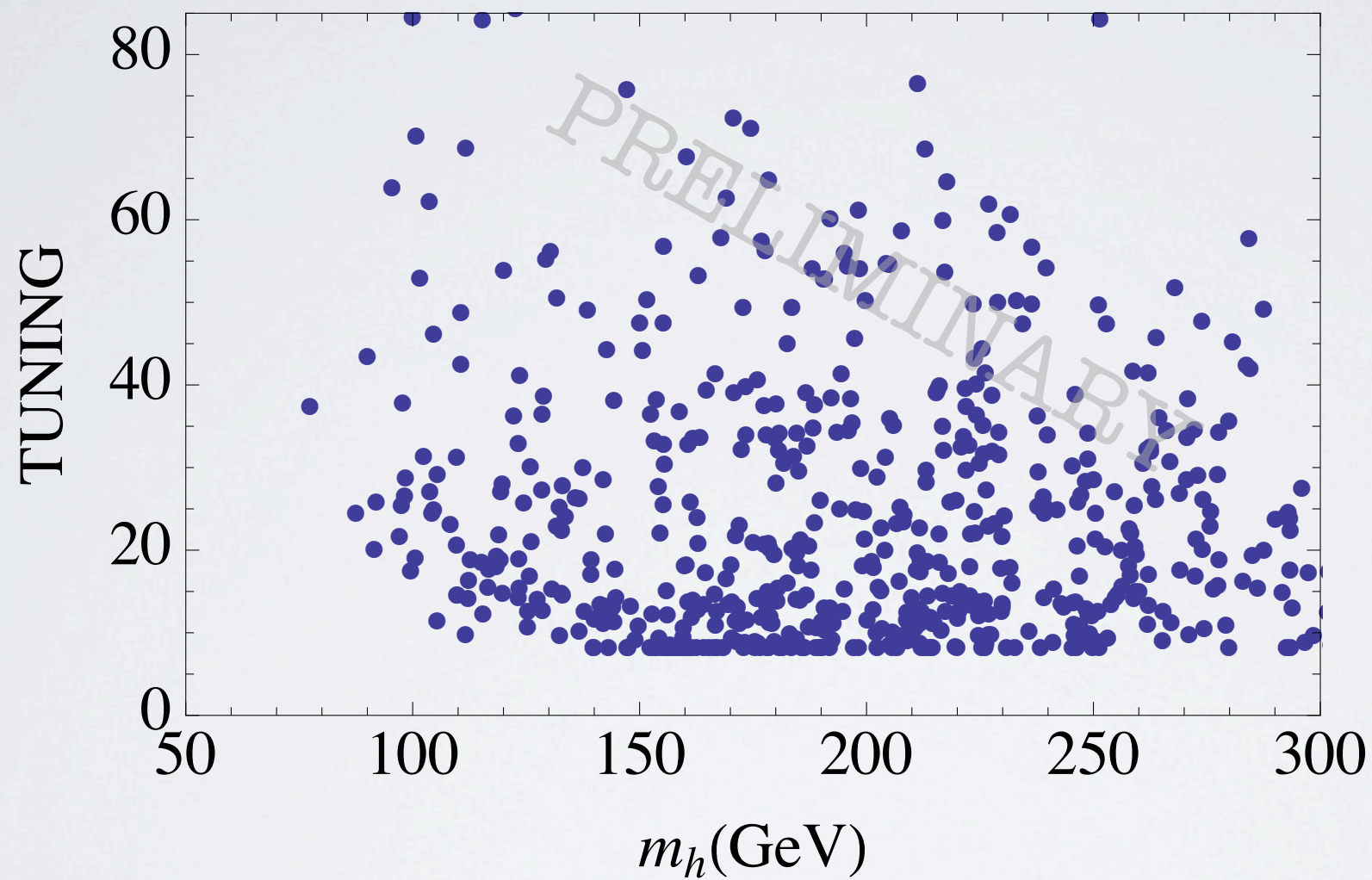
Partners above experimental bound  $\sim \text{TeV}$

*Michele Redi, ICHEP 2012, Melbourne*



# Tuning:

$$\Delta = \text{Max}_i \left| \frac{\partial \log m_Z}{\partial \log x_i} \right|$$



$$f = 800 \text{ GeV}$$

$$\Delta_{avg} \sim 30$$

*Michele Redi, ICHEP 2012, Melbourne*

$SO(6)/SO(5)$ :

Gripaios, Pomarol, Riva, Serra '09

5 GBs:

$$5 = (2, 2) + 1$$

Fermions can be coupled to the  $6=(2,2)+2 \times 1$

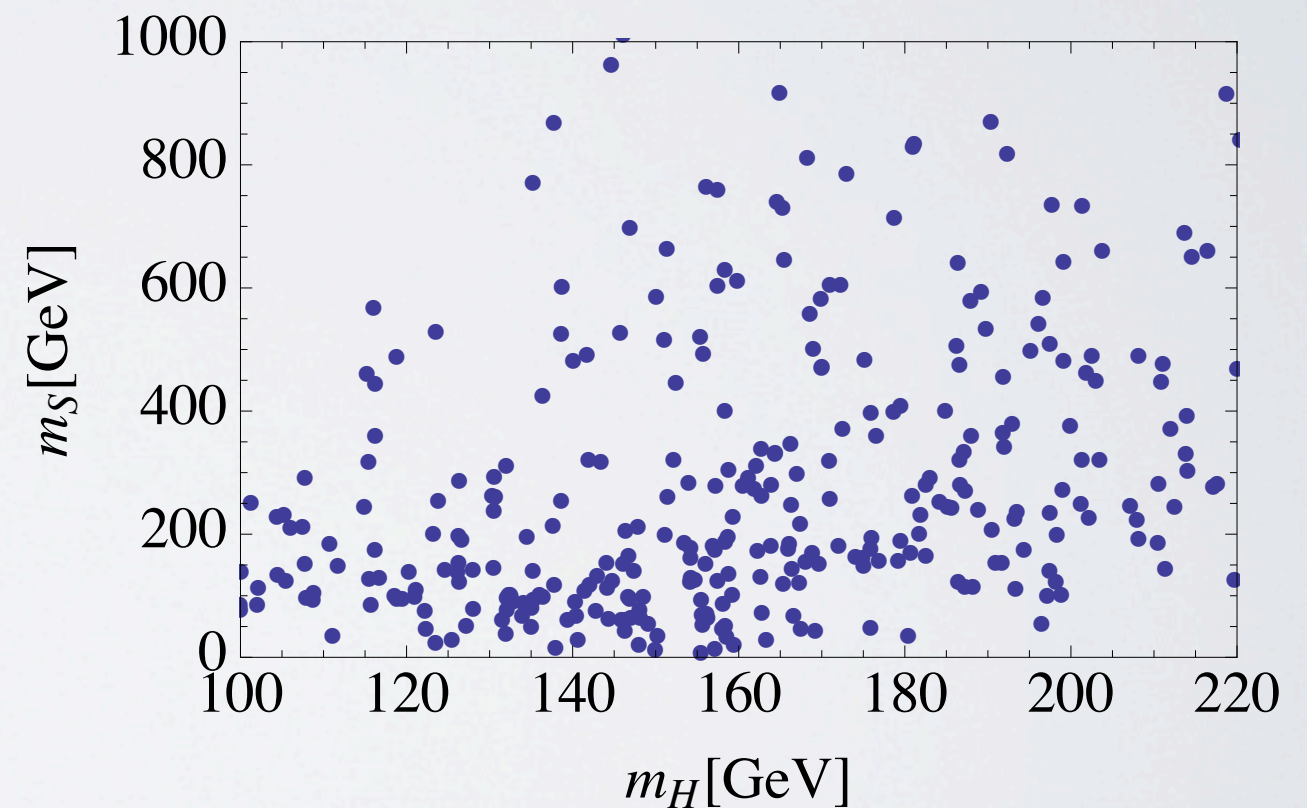
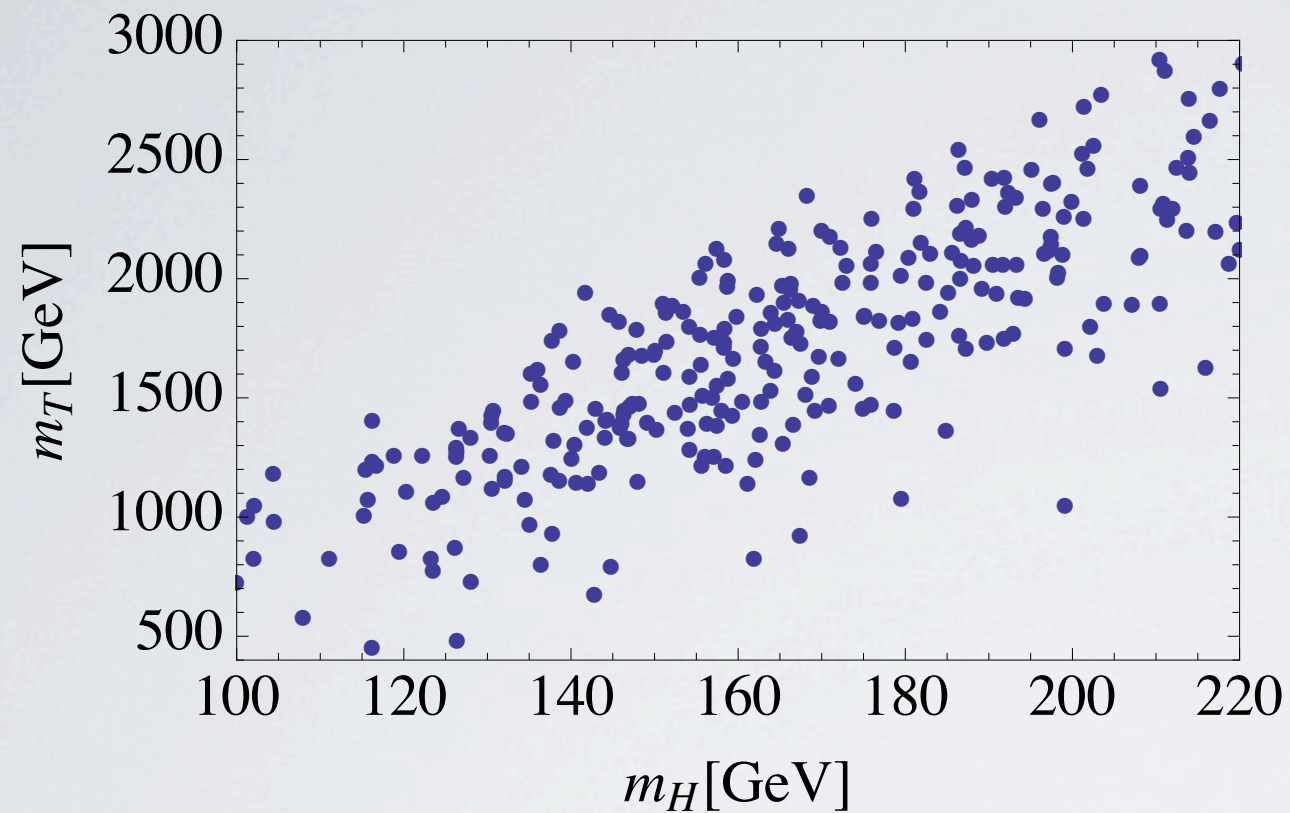
$$q_L \rightarrow \frac{1}{\sqrt{2}} \begin{pmatrix} b_L \\ -ib_L \\ t_L \\ it_L \\ 0 \\ 0 \end{pmatrix} \quad t_R \rightarrow \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ i \cos \theta t_R \\ \sin \theta t_R \end{pmatrix}$$

For  $\theta = \frac{\pi}{4}$  singlet becomes exact GB.

*Michele Redi, ICHEP 2012, Melbourne*



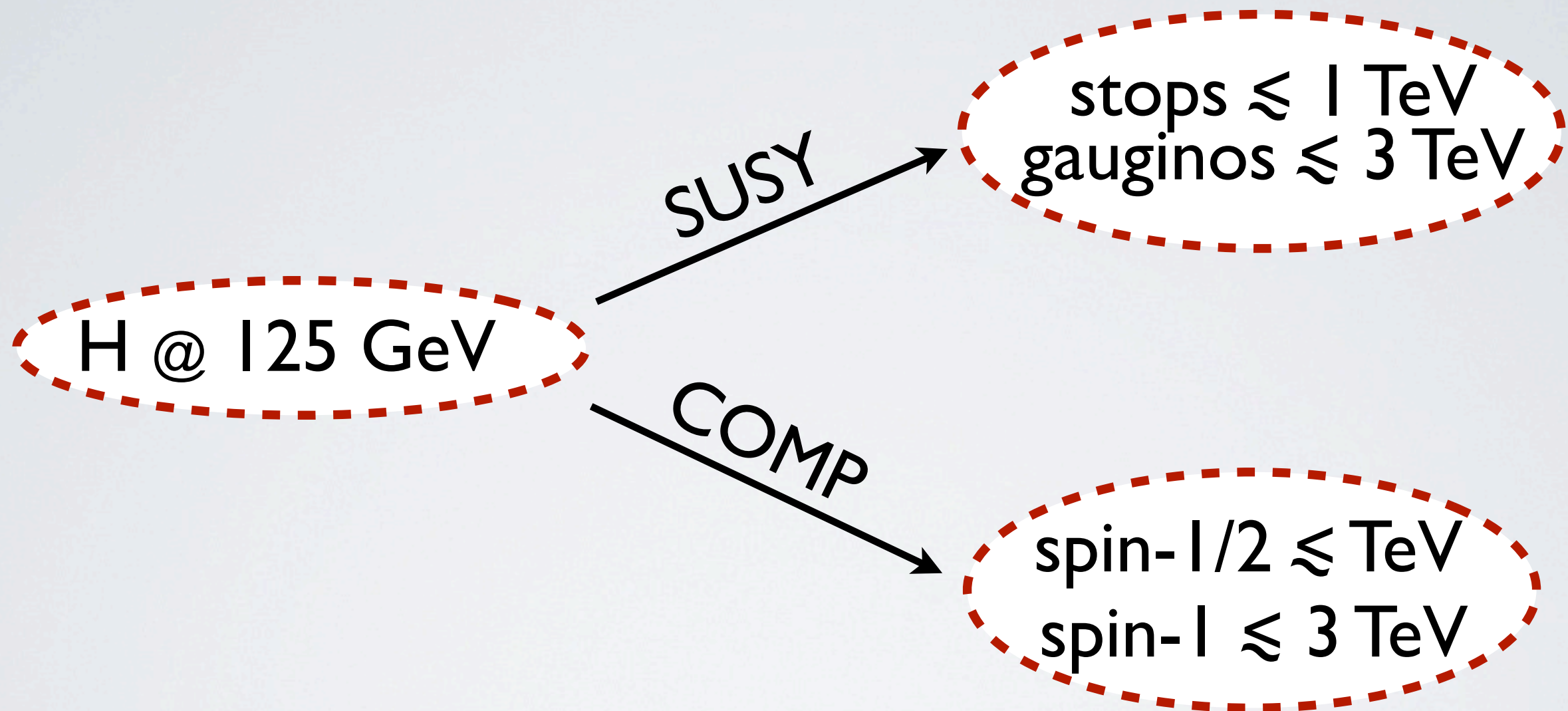
$$f = 800 \text{ GeV}$$



Same correlation Higgs-fermions.

Singlet typically heavier than Higgs unless  $\theta \approx \frac{\pi}{4}$

*Michele Redi, ICHEP 2012, Melbourne*





# CONCLUSIONS

- All relevant features of CHM can be reproduced from a 4D point view. First resonance sufficient for theory & LHC.
- 125 GeV Higgs requires light fermionic partners that may be seen in 2012 or early LHC14.
- Not all models have been fully explored.

# ESTIMATES

$$\mathcal{L} = \left(1 + \epsilon_L^2 \sum_i I_L^{(i)}(s_h)\right) \bar{q}_L \partial q_L + \left(1 + \epsilon_R^2 \sum_i I_R^{(i)}(s_h)\right) \bar{t}_R \partial t_R \\ + y_t f M(s_h) \bar{t}_L t_R + h.c.,$$

Loops of SM fields generate:

$$V_{\text{leading}} \sim \frac{N_c}{16\pi^2} m_\psi^4 \sum_i \left[ \epsilon_L^2 I_L^{(i)}(s_h) + \epsilon_R^2 I_R^{(i)}(s_h) \right]$$

$$V_{\text{sub-leading}} \sim \frac{N_c}{16\pi^2} m_\psi^2 f^2 \left[ y_t^2 M^2(s_h) + \dots \right] \quad \left( y_t \sim \epsilon_L \epsilon_R \frac{m_\psi}{f} \right)$$

$$s_h \equiv \sin \frac{h}{f} = \frac{v}{f}$$

Two different trigonometric structures needed to tune.

*Michele Redi, ICHEP 2012, Melbourne*



- Tuning at leading order

$$m_h^2 \sim \frac{N_c}{2\pi^2} y_t \frac{m_\psi^3}{f^3} v^2 \quad \longrightarrow \quad \Delta = \frac{\delta m_h^2}{m_h^2} \sim \frac{f^2}{v^2}$$

- Tuning with sub-leading terms (CHM5, CHM10...)

$$m_h^2 \sim \frac{N_c}{2\pi^2} y_t^2 \frac{m_\psi^2}{f^2} v^2 \quad \longrightarrow \quad \Delta = \frac{\delta m_h^2}{m_h^2} \sim \frac{m_\psi}{y_t f} \times \frac{f^2}{v^2}$$

- Composite tR

$$m_h^2 \sim \frac{N_c}{2\pi^2} y_t^2 \frac{m_\psi^2}{f^2} v^2 \quad \longrightarrow \quad \Delta = \frac{\delta m_h^2}{m_h^2} \sim \frac{f^2}{v^2}$$