

8th International Workshop on High p<sub>T</sub> Physics at LHC (HPT2012) 21-24 October 2012, Central China Normal University, Wuhan, China

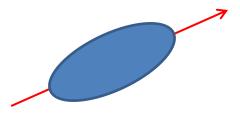
# Initial States and Global Dynamics versus Fluctuations

For hard processes, from the most energetic initial stages we need to know the ST configuration of the background

Laszlo P. Csernai, University of Bergen, Norway

## Global Dynamics versus Fluctuations

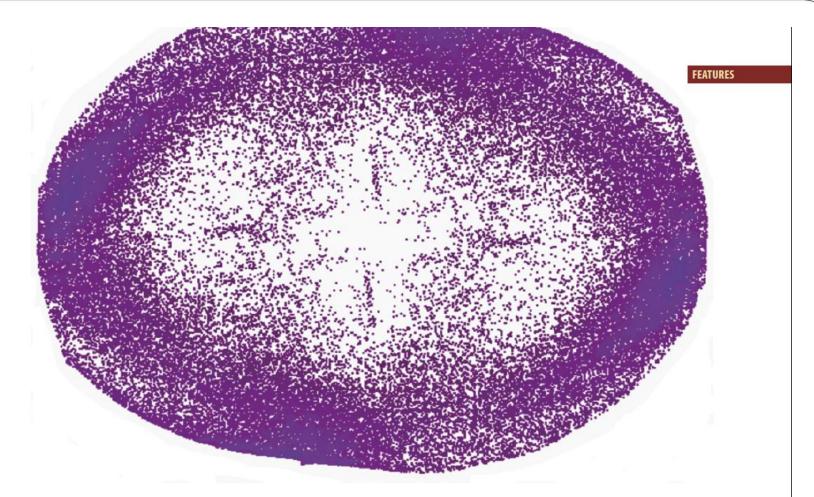
### **Central Collisions (A+A)**



- ☐ Global Symmetries
- ☐ One symmetry axis: z-axis given by the beam direction
  - ☐ Azimuthal symmetry
  - ☐ Longitudinal, +/- z symmetry → rapidity even
  - ☐ Spherical or ellipsoidal flow, expansion
  - $\Box$  Global  $v_1, v_2, v_3, ... v_n = 0 !!$

- ☐ Fluctuations
- ☐ Perfect conditions for fluctuation studies
  - ☐ Azimuthal fluctuations no interference perfect, odd & even harmonics
  - ☐ Longitudinal fluctuations global rapidity-even flow interference
    - → (slight) dominance for rapidity-even fluctuations
  - ☐ Best for critical fluctuation studies :

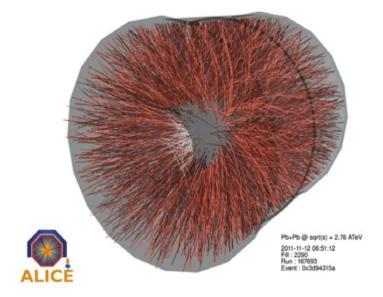
$$\frac{d^3N}{dydp_td\phi} = \frac{1}{2\pi} \frac{d^2N}{dydp_t} \left[ 1 + 2v_1(y, p_t)\cos(\phi - \Psi_1^{EP}) + 2v_2(y, p_t)\cos(2(\phi - \Psi_2^{EP})) + \cdots \right]$$

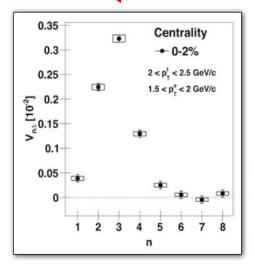


## The Quark-Gluon Plasma, a nearly perfect fluid

■ L. Cifarelli 1, L.P. Csernai 2 and H. Stöcker 3 - DOI: 10.1051/epn/2012206

europhysicsnews THE MAGAZINE OF THE EUROPEAN PHYSICAL SOCIETY





A FIG 3: The final particles created in a lead on lead collision as reconstructed by the Time Projection Chamber of the ALICE detector. The chamber is filled in by the charged particle tracks rather evenly and densely in a near central collision. As flow fluctuation studies indicate the multipole moments up to 5 can be significantly identified. At higher energy and so higher charged particle multiplicity one can expect to see even higher multipole moments.

◆FIG 4: Multipole moments of the azimuthal distribution of emitted particles in central lead on lead collisions detected by the Time **Projection Chamber** of the ALICE detector. From ref. [2b].

and according to present expectations it is around the low RHIC and the SPS energies. The present CERN studies could be well complemented by studying a system where the QGP is just created and critical fluctuations in dense hadronic of baryonic matter can be studied. Apart from the drop of collective directed flow due to the rapid softening of the matter at the critical point, there are many other observables, which open new ways of studies. The revolutionary fluctuation studies have an effect on the studies at the critical point also, with many new results coming from

#### References

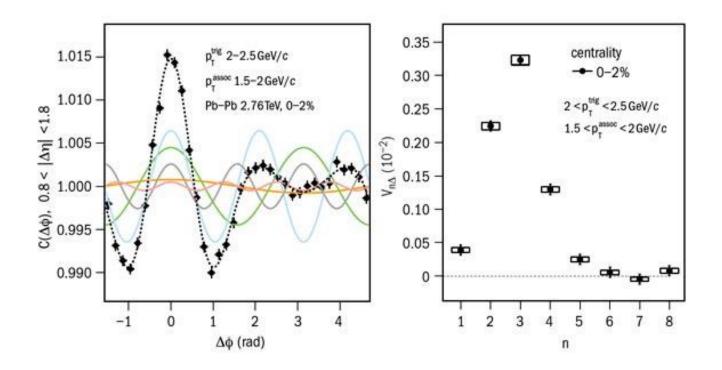
- [1] K. Aamodt et al., (ALICE Collaboration), Phys. Rev. Lett. 105, 252302 (2010)
- [2] K. Aamodt et al., (ALICE Collaboration) arXiv:1105.3865v1 [nucl-ex], and CERN Courier, October 2011, p. 6
- [3] P.K. Kovtun, D.T. Son and A.O. Starinets, Phys. Rev. Lett. 94, 111601 (2005)
- [4] L.P. Csernai, J.I. Kapusta, L.D. McLerran, Phys. Rev. Lett. 97, 152303 (2006)

▼ FIG 5: Yields of anti-particle clusters in the mid rapidity region (|y| < 0.5) of most central collisions of Pb+Pb/ Au+Au as a function of the center-ofmass beam energy.

Sep 23, 2011

Oct. 2011, p. 6

#### ALICE measures the shape of head-on lead-lead collisions



Flow originating from initial state fluctuations is significant and dominant in central and semi-central collisions (where from global symmetry no azimuthal asymmetry could occur)!

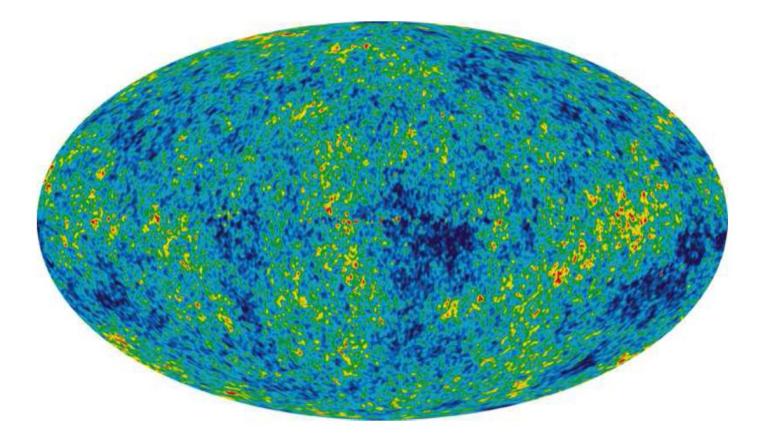
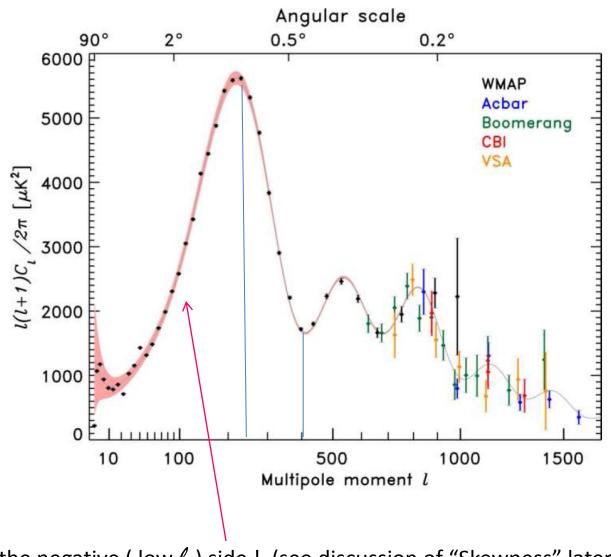


Figure 32: The CMB radiation temperature fluctuations from the 5-year WMAP data seen over the full sky. The average temperature is 2.725K, and the colors represents small temperature fluctuations. Red regions are warmer, and blue colder by about 0.0002 K.

~ spherical with many (16) nearly equal perturbations

 $\ell = 2$ 

 $\ell = 16$ 



Longer tail on the negative (low  $\ell$ ) side! (see discussion of "Skewness" later)

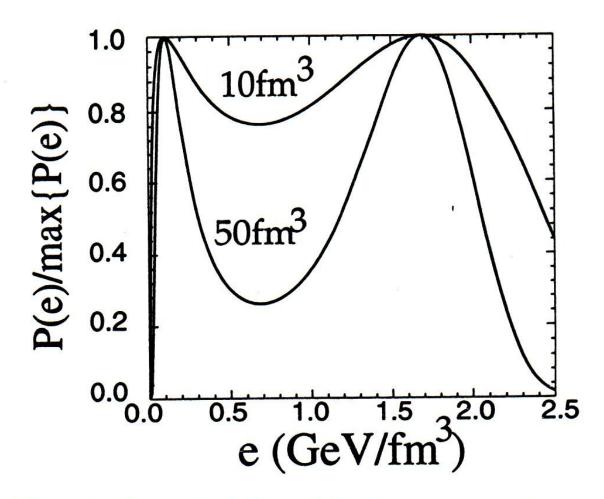


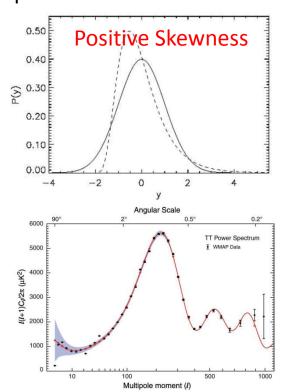
Fig. 2. The relative probability of finding a state of a given energy density, e, in a system of given volume,  $\Omega = 10,50$  fm<sup>3</sup>, at a constant temperature,  $T = T_c$ .

#### Fluctuations in Hadronizing QGP

L.P. Csernai<sup>1,2</sup>, G. Mocanu<sup>3</sup> and Z. Néda<sup>3</sup>

#### PHYSICAL REVIEW C 85, 068201 (2012)

Higher order moments can be obtained from fluctuations around the critical point. → Skewness and Kurtosis are calculated for the QGP → HM phase transition



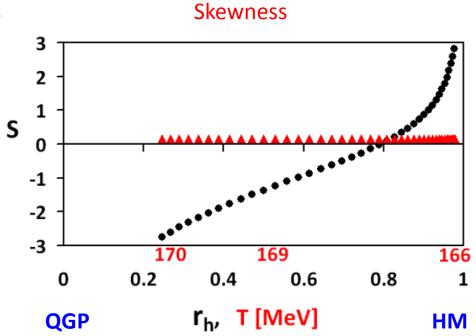


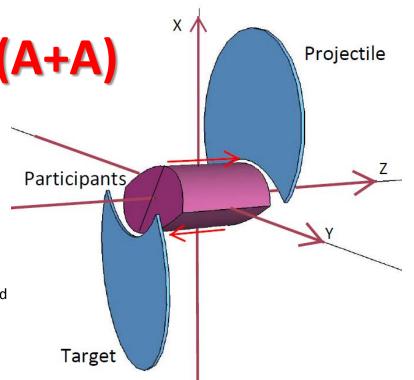
FIG. 4: (color online) Skewness as a function of the volume abundance of the hadronic matter (denoted as  $r_h$ , where 1 represents complete hadronization). The temperature scale is also indicated for clarity, the identifiers represent increments of 0.1 MeV in T. Results for  $\Omega = 500 fm^3$ .

Negative Skewness indicates Freeze-out mainly still on the QGP side.

### Peripheral Collisions (A+A)

- ☐ Global Symmetries
- ☐ Symmetry axes in the global CM-frame:
  - $\Box$  (y  $\leftrightarrow$  -y)

  - □ Azimuthal symmetry: φ-even (cos nφ)
  - ☐ Longitudinal z-odd, (rap.-odd) for v<sub>odd</sub>
  - ☐ Spherical or ellipsoidal flow, expansion



$$\frac{d^3N}{dydp_t d\phi} = \frac{1}{2\pi} \frac{d^2N}{dydp_t} \left[ 1 + 2v_1(y, p_t) \cos(\phi) + 2v_2(y, p_t) \cos(2\phi) + \cdots \right] 
\frac{d^3N}{dydp_t d\phi} = \frac{1}{2\pi} \frac{d^2N}{dydp_t} \left[ 1 + 2v_1(y - y_{CM}, p_t) \cos(\phi - \Psi_{RP}) + 2v_2(y - y_{CM}, p_t) \cos(2(\phi - \Psi_{RP})) + \cdots \right]$$

- ☐ Fluctuations
- ☐ Global flow and Fluctuations are simultaneously present → ∃ interference
  - ☐ Azimuth Global: even harmonics Fluctuations : odd & even harmonics
  - ☐ Longitudinal Global: v1, v3 y-odd Fluctuations : odd & even harmonics
  - ☐ The separation of Global & Fluctuating flow is a must !! (not done yet)

#### **Analysis of Global Flow:**

$$\frac{d^3N}{dydp_t d\phi} = \frac{1}{2\pi} \frac{d^2N}{dydp_t} \left[ 1 + 2v_1(y, p_t) \cos(\phi) + 2v_2(y, p_t) \cos(2\phi) + \cdots \right]$$

where  $\phi = 0$  is the reaction plane azimuth angle  $\Psi_{RP}$ 

$$\frac{d^3N}{dudp_t d\phi} = \frac{1}{2\pi} \frac{d^2N}{dudp_t} \left[ 1 + 2v_1(y, p_t) \cos(\phi - \Psi_{RP}) + 2v_2(y, p_t) \cos(2(\phi - \Psi_{RP})) + \cdots \right]$$

$$\frac{d^3N}{dydp_t d\phi} = \frac{1}{2\pi} \frac{d^2N}{dydp_t} \left[ 1 + 2v_1(y - y_{CM}, p_t) \cos(\phi - \Psi_{RP}) + 2v_2(y - y_{CM}, p_t) \cos(2(\phi - \Psi_{RP})) + \cdots \right]$$

 $\Psi_{RP}$  and  $y_{CM}$  can be determined experimentally L. P. Csernai, G. Eyyubova, and V. K. Magas<sup>4</sup>

PHYSICAL REVIEW C 86, 024912 (2012)

$$\frac{d^3N}{dydp_t d\phi} = \frac{1}{2\pi} \frac{d^2N}{dydp_t} \left[ 1 + 2v_1(y, p_t) \cos(\phi - \Psi_1^{EP}) + 2v_2(y, p_t) \cos(2(\phi - \Psi_2^{EP})) + \cdots \right]$$

#### and Fluctuating Flow:

$$\Psi_n^{EP}$$
 maximizes  $v_2(y, p_t)$  or  $v_2(p_t)$  or  $v_2$  
$$\Psi_n^{EP}\{2\} \text{ or } \Psi_n^{EP}\{4\} \dots$$

$$v_n \cos[n(\phi - \Psi_n)] = (v_n \cos(n\Psi_n)) \cdot \cos(n\phi) + (v_n \sin(n\Psi_n)) \cdot \sin(n\phi)$$
ortho-normal series expansion for both  $\phi$ -even and  $\phi$ -odd functions

#### Method to compensate for C.M. rapidity fluctuations

- 1. Determining experimentally EbE the C.M. rapidity
- 2. Shifting each event to its own C.M. and evaluate flow-harmonics there

L.P. Csernai<sup>1,2</sup>, G. Eyyubova<sup>3</sup> and V.K. Magas<sup>4</sup> arXiv:1204.5885v1 [hep-ph]

#### **Determining the C.M. rapidity**

The rapidity acceptance of a central TPC is usually constrained (e.g. for ALICE  $|\eta| < \eta_{lim} = 0.8$ , and so:  $|\eta_{C.M.}| << \eta_{lim}$ , so it is not adequate for determining the C.M. rapidity of participants.

#### Participant rapidity from spectators

$$E_B = A_B \ m_{B\perp} \cosh(y^B) = E_{tot} - E_A - E_C ,$$

$$M_B = A_B \ m_{B\perp} \sinh(y^B) = -(M_A + M_C)$$

$$E_{AB} = A_B \ m_{B\perp} \cosh(y^B) = -(M_A + M_C)$$

$$E_A = A_P m_N \cosh(y_0),$$
  

$$E_C = A_T m_N \cosh(-y_0),$$

give the spectator numbers,  $A_P$  and  $A_T$ ,

$$M_A = A_P m_N \sinh(y_0),$$
  

$$M_C = A_T m_N \sinh(-y_0),$$

$$y_E^{CM} \approx y^B = \operatorname{artanh}\left(\frac{M_A + M_C}{E_{tot} - E_A - E_C}\right)$$

$$y_0 = 7.986$$

В

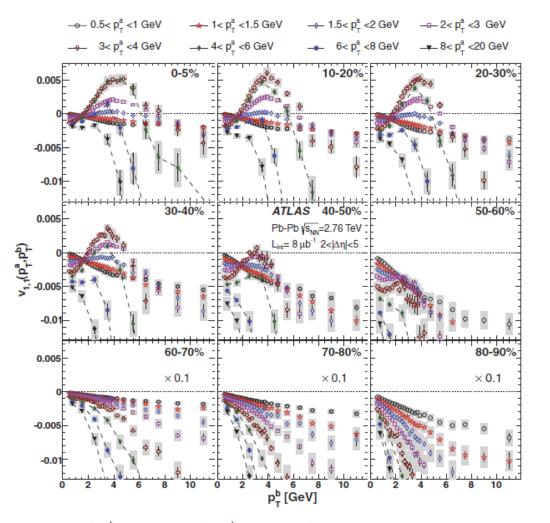


$$E_{tot} = 2A_{Pb} \, m_N \, \cosh(y_0)$$

#### Interplay between global collective flow and fluctuating flow

MEASUREMENT OF THE AZIMUTHAL ANISOTROPY FOR ...

PHYSICAL REVIEW C 86, 014907 (2012)



**ATLAS** 

FIG. 19. (Color online)  $v_{1,1}(p_T^a, p_T^b)$  for  $2 < |\Delta \eta| < 5$  vs  $p_T^b$  for different  $p_T^a$  ranges. Each panel presents results in one centrality interval. The error bars and shaded bands represent statistical and systematic uncertainties, respectively. The data points for the three highest  $p_T^a$  intervals have coarser binning in  $p_T^b$ , hence are connected by dashed lines to guide the eye. The data in the bottom three panels are scaled down by a factor of ten to fit within the same vertical range.

## Global Flow in Peripheral Collisions (A+A)

- Many interesting phenomena:
  - $\square$  Historically: Bounce off / Side splash; Squeeze out  $\rightarrow$  pressure & EoS
  - ☐ 3<sup>rd</sup> flow or Anti-flow (QGP), Rotation, KHI, Polarization, etc
  - ☐ These occur only if viscosity is low! → viscosity
  - ☐ With increasing energy flow becomes strongly F/B directed & v₁ decreases

#### Fluctuating initial states

[1] Gardim FG, Grassi F, Hama Y, Luzum M, Ollitraut PHYSICAL REVIEW C **83**, 064901 (2011); ( $v_1$  also) [2] Qin GY, Petersen H, Bass SA, Mueller B PHYSICAL REVIEW C **82**, 064903 (2010)

QIN, PETERSEN, BASS, AND MÜLLER

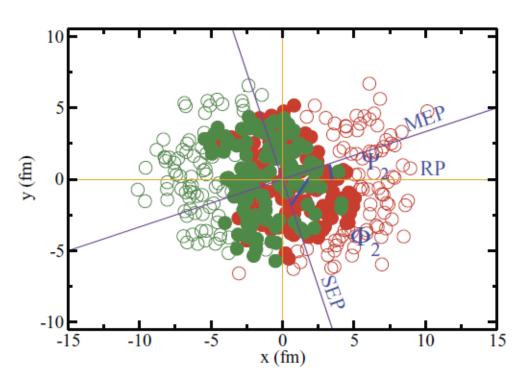


FIG. 3. (Color online) The transverse plane for one typical collision event, where the circles represent nucleons from two nuclei, with shaded ones for participating nucleons. Also shown are the locations of different planes: the reaction plane (RP), the spatial event plane (SEP), and the momentum event plane (MEP) for n = 2.

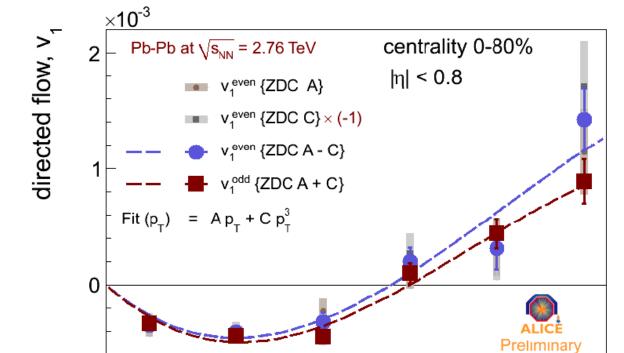
Cumulative event planes show weak correlation with the global collective reaction plane (RP).

If the MEP is set to zero (by definition) then CM rapidity fluctuations do not appear, and  $v_1$  by definition is zero.

In [2] v1(pt) is analyzed (for RHIC) and the effect is dominated by fluctuations. (Similar to later LHC measurements.)

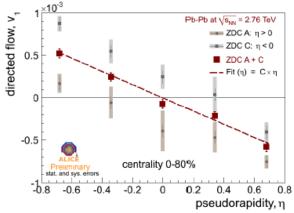


### Extracting even and odd parts of v<sub>1</sub>



0.2 0.4 0.6 0.8

what we expect for even and odd projections:



V<sub>1</sub> from Global Collective flow → v<sub>1</sub>(p<sub>t</sub>) = 0!!!

Even and odd parts of  $v_{_{\! 1}}$  have similar shape and magnitude

stat. and syst. errors





transverse momentum, p<sub>\_</sub> (GeV/c)

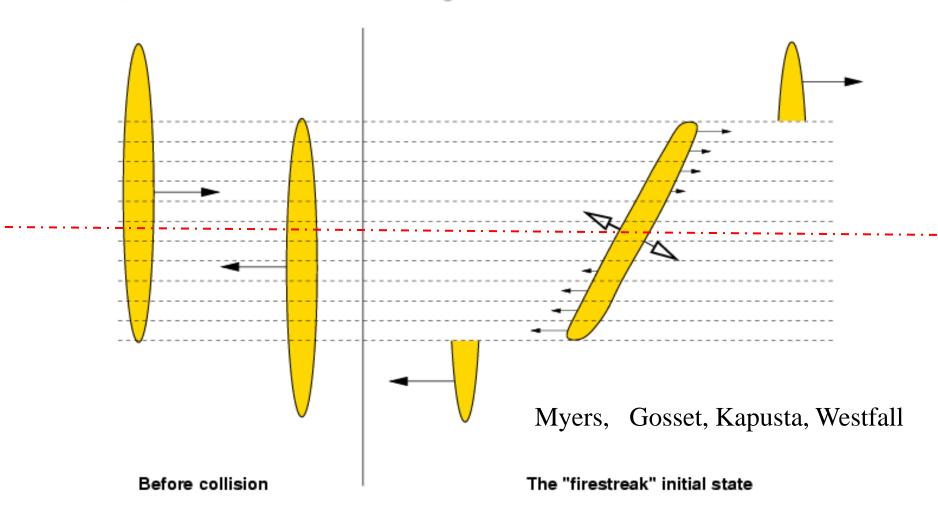
### **Initial States**

### **Collective flow**

- There are alternative origins:
- (a) Global collective flow (RP from spectators)
- (b) Asymmetries from random <u>I.S.</u> fluctuations
- (c) Asymmetries from <u>Critical Point</u> fluctuations

- Goal is to separate the these
  - This provides more insight
- How can we see the flow of QGP?
  - → Rapid hadronization and freeze-out

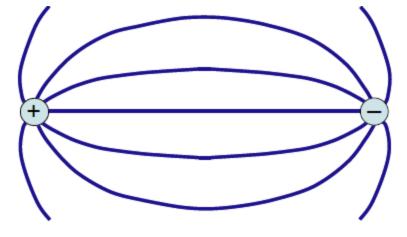
### "Fire streak" picture – 3 dim.



Symmetry axis = z-axis. Transverse plane divided into streaks.

### Flux – tubes

ED or QED:



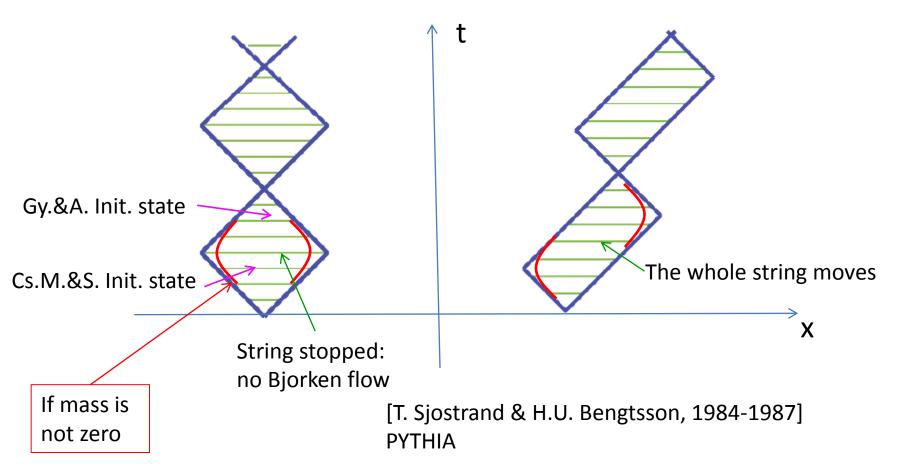
Gluon self-interaction makes field lines attract each other. → QCD:



→ linear potential → confinement

### String model of mesons / PYTHIA

Light quarks connected by string → mesons have 'yo-yo' modes:



#### Nuclear Physics A460 (1986) 723-754 North-Holland, Amsterdam

#### BARYON RECOIL AND THE FRAGMENTATION REGIONS IN ULTRA-RELATIVISTIC NUCLEAR COLLISIONS\*

#### M. GYULASSY

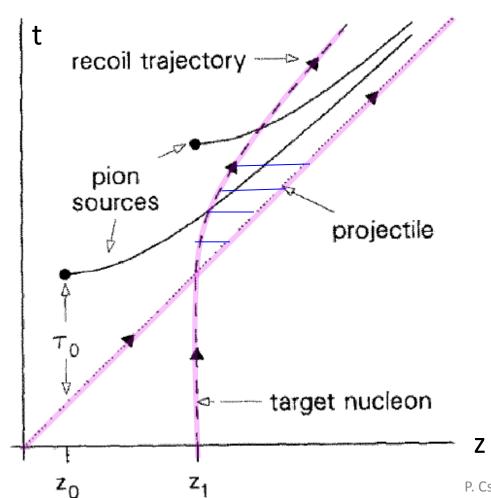
Nuclear Science Division, Lawrence Berkeley Laboratory, University of California, Berkeley, California 94720, USA

#### L.P. CSERNAI1

School of Physics and Astronomy, University of Minnesota, Minnesota, Minnesota 55455, USA

Received 1 June 1986

Yo-yo in the fixed target frame → target recoil → density and energy density increase in the "fragmentation region"



### **Initial stage: Coherent Yang-Mills model**

[Magas, Csernai, Strottman, Pys. Rev. C '2001]

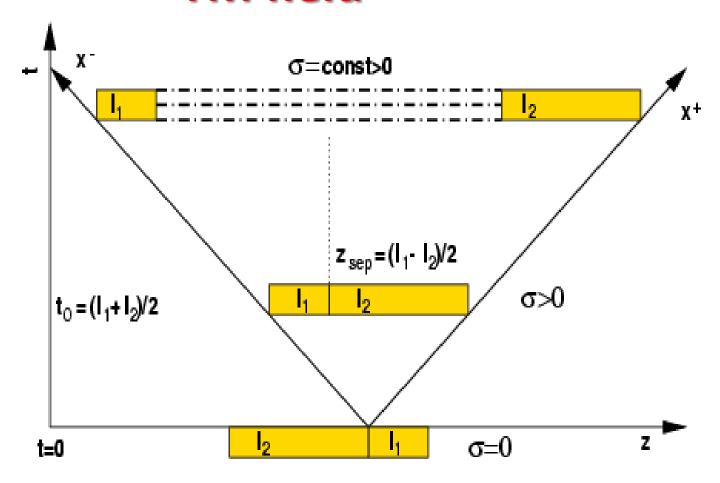
M. Gyulassy, L. Csernai Nucl. Phys. A660 (1986) 723-754.

$$\partial_{\mu}T^{\mu\nu} = F^{\nu\mu}n_{\mu} + \Sigma^{\nu}_{\pi}$$
$$\partial_{\mu}n^{\mu} = 0$$

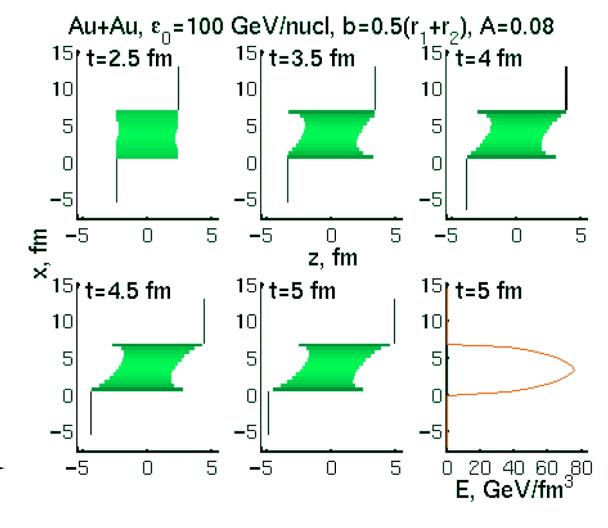
- $T^{\mu\nu} = e_t \left( \left( 1 + c_0^2 \right) u_t^{\mu} u_t^{\nu} c_0^2 g^{\mu\nu} \right)$
- $\Sigma_{\pi}^{\nu}$  pion source term.
- $F^{\mu\nu}$  effective field, describes interaction between target and projectile.

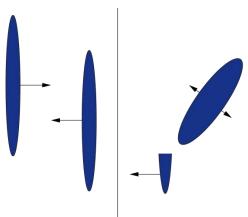
$$F^{\mu\nu} = \begin{pmatrix} 0 & -\sigma \\ \sigma & 0 \end{pmatrix} \quad ,$$

## String rope --- Flux tube --- Coherent YM field



### Initial State



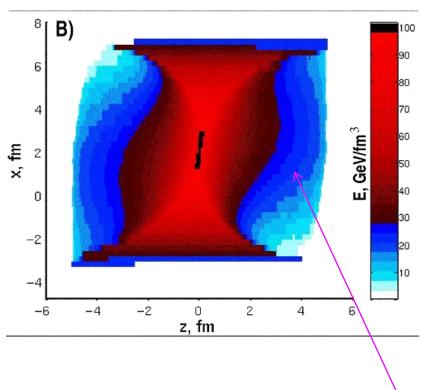


Tilted initial Landau's disk

Before collision L.P. Csernai This shape is confirmed by STAR HBT: PLB496 (2000) 1; & M.Lisa &al. PLB 489 (2000) 287.

3<sup>rd</sup> flow component

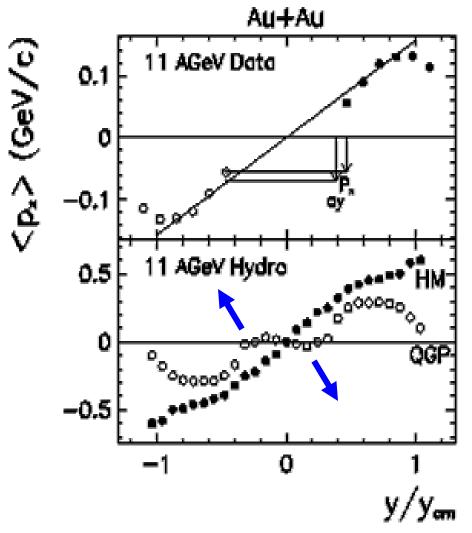
### Initial state – reaching equilibrium



Initial state by V. Magas, L.P. Csernai and D. Strottman Phys. Rev. C64 (01) 014901

Relativistic, 1D Riemann expansion is added to each stopped streak

### 3<sup>rd</sup> flow component



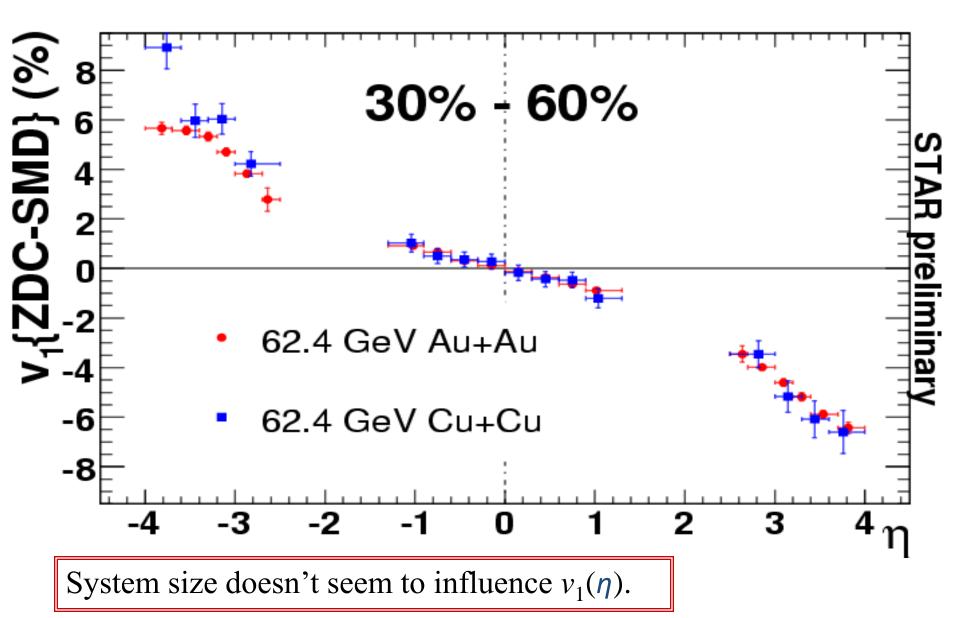


Hydro

[Csernai, HIPAGS'93] & [Csernai, Röhrich, 1999]

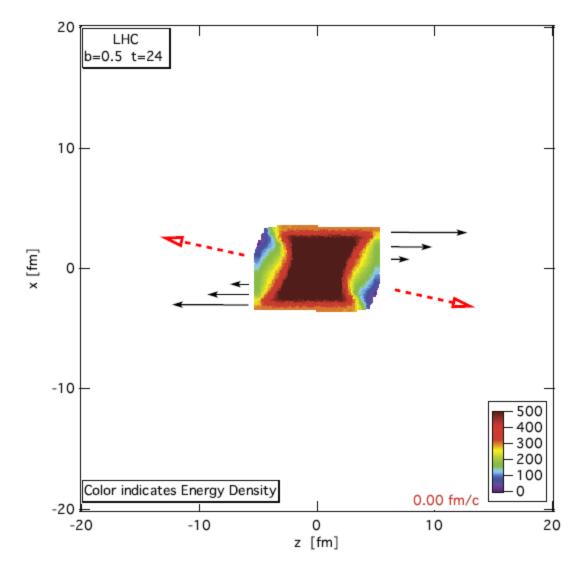
G. Wang / STAR QM 2006 :

### $v_1(\eta)$ : system-size dependence



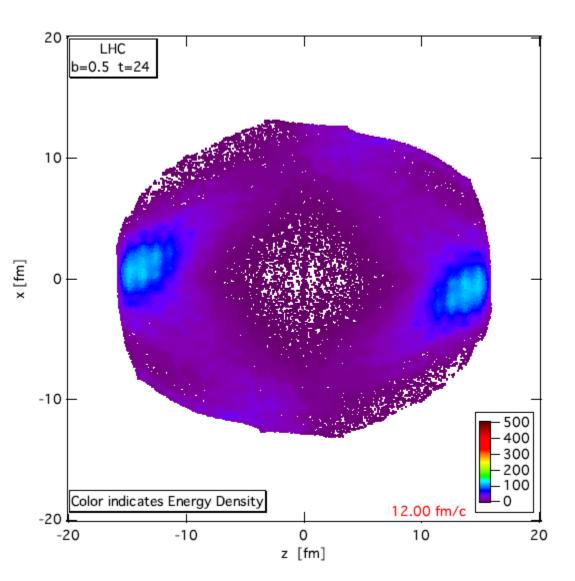
PHYSICAL REVIEW C 84, 024914 (2011)

### Anti-flow (v1) at LHC



Initial energy density [GeV/fm3] distribution in the reaction plane, [x,y] for a Pb+Pb reaction at 1.38 + 1.38 ATeV collision energy and impact parameter b = 0.5 bmax at time 4 fm/c after the first touch of the colliding nuclei, this is when the hydro stage begins. The calculations are performed according to the effective string rope model. This tilted initial state has a flow velocity distribution, qualitatively shown by the arrows. The dashed arrows indicate the direction of the largest pressure gradient at this given moment.

### Anti-flow (v1)

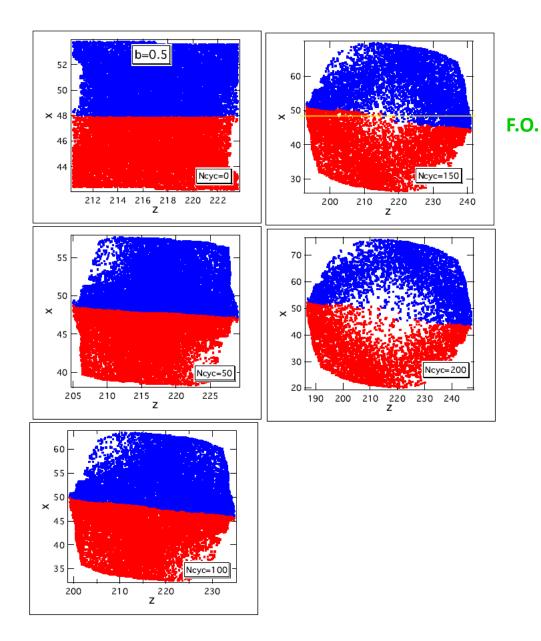


The energy density [GeV/fm3] distribution in the reaction plane, [x,z] for a Pb+Pb reaction at 1.38 + 1.38 A.TeV collision energy and impact parameter b = 0.5b\_max at time 12 fm/c after the formation of the hydro initial state. The expected physical FO point is earlier but this post FO configuration illustrates the flow pattern.

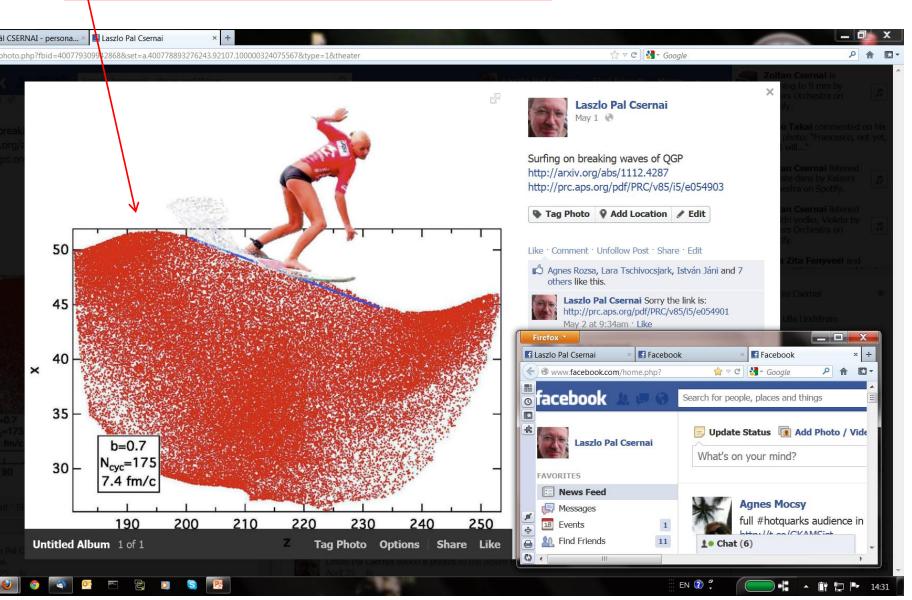
[ LP. Csernai, V.K. Magas, H. Stöcker, D. Strottman, Phys. Rev. **C84** (2011) 02914 ]

#### **Rotation**

The rotation is illustrated by dividing the upper / lower part (blue/red) of the initial state, and following the trajectories of the marker particles.



### **Kelvin-Helmholtz Instability (KHI)**



#### [Du-Juan Wang, Bergen, et al.,]

$$\Omega(z,x) \equiv w(z,x)\omega(z,x)$$

Relativistic

$$w_{ik} \equiv (N_{cell}/E_{tot}) \quad E_{ik}.$$
 Relativistic 
$$\Theta \equiv \nabla_{\mu} u^{\mu} = \partial_{\mu} u^{\mu},$$

$$\Theta \equiv \nabla_{\mu} u^{\mu} = \partial_{\mu} u^{\mu}$$

#### Classical

$$\omega_y \equiv \omega_{xz} \equiv \frac{1}{2} (\partial_z v_x - \partial_x v_z)$$

$$\omega^{\mu}_{\nu} \equiv \frac{1}{2} (\nabla_{\nu} u^{\mu} - \nabla^{\mu} u_{\nu}),$$

 $\partial_{\tau}u^{\mu} \equiv \dot{u}^{\mu} = u^{\alpha}\partial_{\alpha}u^{\mu}$  is negligible

$$\omega_z^x = -\omega_x^z = \frac{1}{2}(\partial_z \gamma v_x - \partial_x \gamma v_z) = \frac{1}{2}\gamma(\partial_z v_x - \partial_x v_z) + \frac{1}{2}(v_x \partial_z \gamma - v_z \partial_x \gamma)$$
 
$$\Omega(z,x)$$

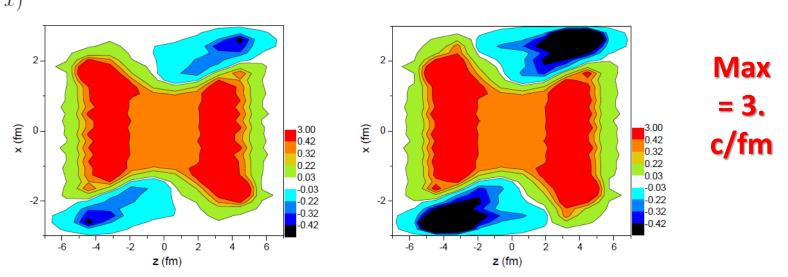
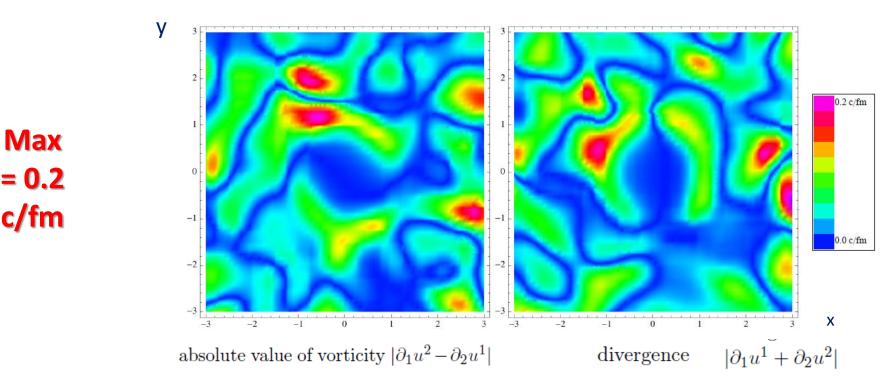


FIG. 1: The classical (left) and relativistic (right) weighted vorticity,  $\Omega_{zx}$ , calculated in the reaction, [x-z] plane at  $\underline{t=0.17 \text{ fm/c}}$ . The collision energy is  $\sqrt{s_{NN}} = 2.76 \text{ TeV}$  and  $b = 0.7b_{max}$ , the cell size is dx = dy = dz = 0.4375 fm. The average vorticity in the reaction plane is 0.1434 / 0.1185 for the classical / relativistic weighted vorticity respectively.

#### **Onset of turbulence around the Bjorken flow**

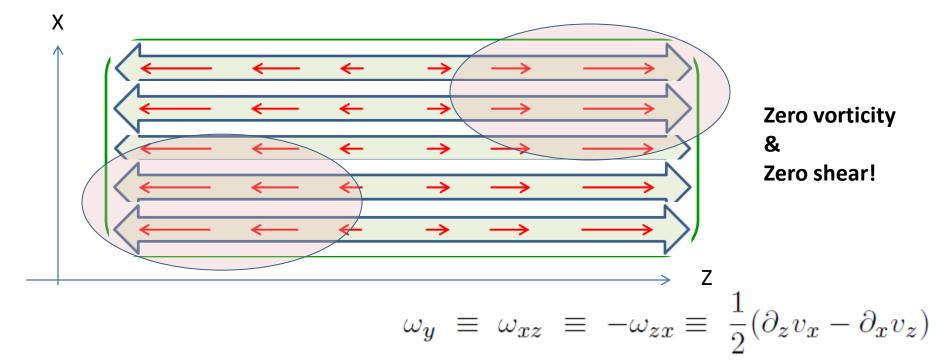
S. Floerchinger & U. A. Wiedemann, JHEP 1111:100, 2011; arXiv: 1108.5535v1



- Initial state Event by Event vorticity and divergence fluctuations.
- Amplitude of random vorticity and divergence fluctuations are the same
- In dynamical development viscous corrections are negligible (→ no damping)
- Initial transverse expansion in the middle (±3fm) is neglected (→ no damping)
- High frequency, high wave number fluctuations may feed lower wave numbers

### Typical I.S. model – scaling flow

The same longitudinal expansion velocity profile in the whole [x,y]-plane! No shear flow. Usually **angular momentum is vanishing!** 



Such a re-arrangement of the matter density is dynamically not possible in a short time!

$$\boldsymbol{\omega} \equiv \frac{1}{2} \mathbf{rot} \ \boldsymbol{v} = \frac{1}{2} \nabla \times \boldsymbol{v}$$

### Adil & Gyulassy (2005) initial state

 $x, y, \eta, \tau$  coordinates  $\rightarrow$  Bjorken scaling flow

PHYSICAL REVIEW C 72, 034907 (2005)

Considering a longitudinal "local relative rapidity slope", based on observations in D+Au collisions:

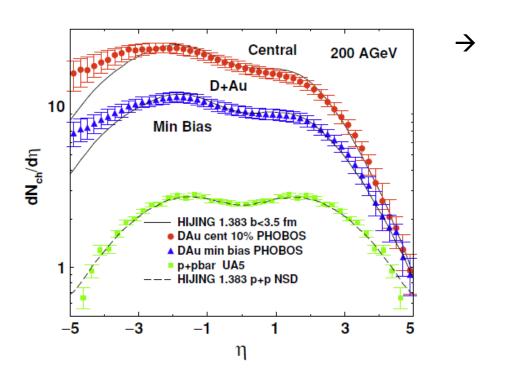
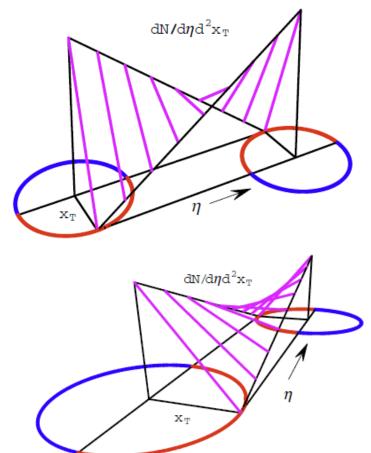
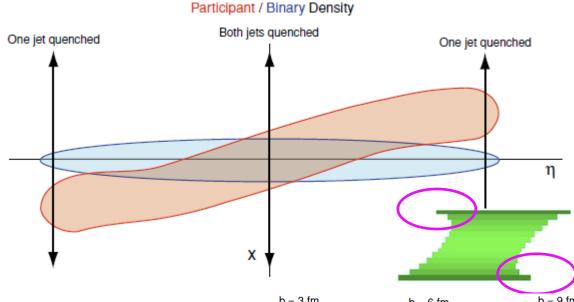


FIG. 2. (Color online) Asymmetric pseudorapidity distributions of charged hadrons produced in D+Au minimum bias and central 0–10% reactions at 200A GeV from PHOBOS [12] are compared to  $p+\bar{p}$  data from UA5 [13]. The curves show predictions using the HIJING v1.383 code [14,15].



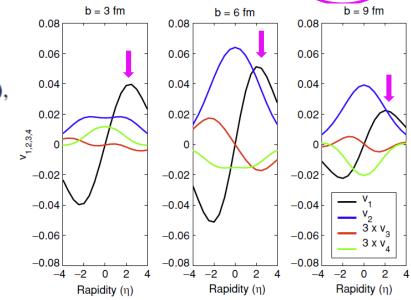
This is similar to our model, with several flux-tubes in each fire-streak, with different rapidities at their ends. This leads to a "diffuse nuclear geometry":

Here in a given streak on the projectile side, there is a distribution<sup>[1]</sup> of the ends of the flux tubes, so that the energy is shifter more to the positive rapidity side. [1: Wounded nucleon model, Brodsky et al. PRC (1977)]



$$R_{BA}(\eta; \mathbf{b}) = \frac{dN^{BA}/d\eta}{dN^{pp}/d\eta} \approx \frac{1}{2}(N_A + N_B) + \frac{\eta}{2Y}(N_B - N_A),$$

The consequence is that the energy is shifted forward on the projectile side  $\rightarrow$  (RHIC - 200 A.GeV, -  $v_1$  is black!)  $v_1$  is opposite side then in the experiment.

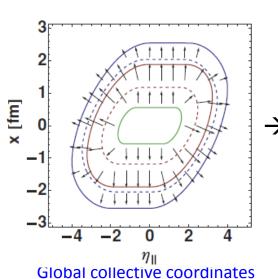


#### Bozek, Wyskiel (2010): Directed flow

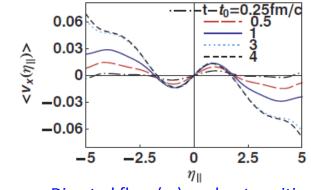
#### x, y, $\eta$ , $\tau$ coordinates

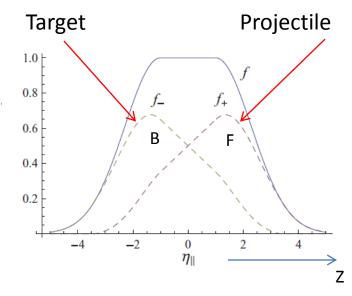
PHYSICAL REVIEW C 81, 054902 (2010)

Similarly to Adil & Gyulassy this is also based on the Wounded nucleon picture.  $\eta$  and x coordinates are used. The P & T distributions are given  $\rightarrow$ 



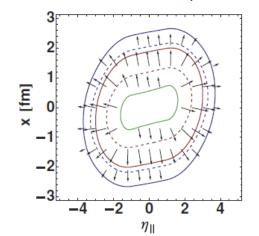
 $u^{\mu}(\tau_0,x,y,\eta_{\parallel})=(\cosh\eta_{\parallel},0,0,\sinh\eta_{\parallel}).$  Bjorken flow





Directed flow (v<sub>1</sub>) peaks at positive rapidities! (as A&D)

Notice: the arrows are pressure gradients!

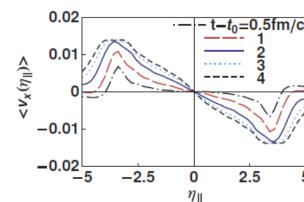


 $\rightarrow$ 

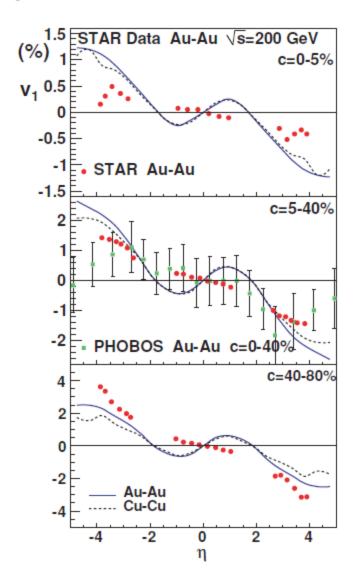
 $RHIC \rightarrow$ 

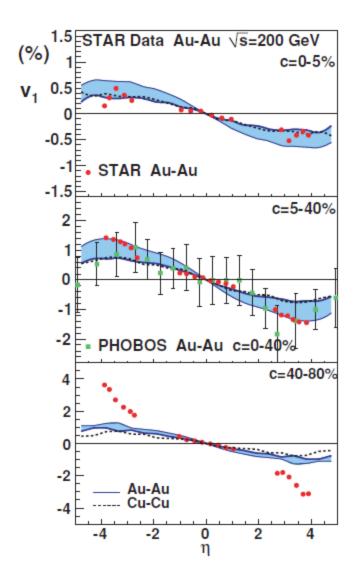
Not a dynamical model

The authors re-parametrized their initial state to a **'tilted' i.s.** and with modified distributions, and this could reproduce the observations at



#### 3, Directed flow at different centralities





'tilted' i.s.

### Summary

- The I.S. is decisive in causing global collective flow
- Consistent I.S. is needed based on a dynamical picture, satisfying causality, etc.
- Several I.S. models exist, some of these are oversimplified beyond physical principles.
- Experimental outcome strongly depends on the I.S.

### Thank you

#### Kristian Birkeland 1867 - 1917

Assessment of the evaluation committee for Yara's **Birkeland prize 2012**.

Yara's Birkeland prize for 2012 is awarded to *dr. Yun Cheng* for her thesis Hydrodynamics and Freeze Out Problems in Energetic Heavy Ion reactions, for which she was awarded the degree of Philosophiae Doctor at the University of Bergen in 2010. The work was carried out under the supervision of professor László Csernai the Department of Physics and Technology. ... ... ...

In her thesis, *dr. Yun Cheng* has investigated how theoretical models for the the various phases of a plasma-forming heavy ion collision can be fitted coherently together, and how well the resulting description agrees with experimental measurements. This represents a valuable contribution to our understanding of fundamental aspects of hot strongly interacting matter. Her work is pure basic research, aiming at understanding and testing the validity of quantum chromodynamics, one of the main components of the current Standard Model of elementary particles.