

Relativistic Correction to Charmonium Dissociation Temperature

GUO Xingyu

In collaboration with Shi Shuzhe and Prof. Zhuang Pengfei

Department of Physics,
Tsinghua University

J/ ψ as a probe of QGP

- J/ ψ suppression as a sign of QGP formation
- J/ ψ is deeply bounded, which leads to a high dissociation temperature

$$T_d = (1.2 \sim 2)T_c$$

- m_c is very big (in our case 1.4 GeV)

Normally non-relativistic model is used

Question: The relativistic correction of the dissociation temperature?

A qualitative estimation

$$H = \sqrt{\mu^2 + p^2} - \mu + V(r)$$

$$\approx \frac{p^2}{2\mu} + V_{eff}$$

$$V_{eff} = V - \frac{p^4}{8\mu^3}$$

A deeper potential well should lead to a higher T_d

The covariant relativistic Schödinger equations

Derived from the two-body Dirac equation(TBDE)

for spin singlet u_0 ($n^1 L_L$)

$$\left[-\frac{d^2}{dr^2} + \frac{J(J+1)}{r^2} + 2m_w B + B^2 - A^2 + 2\epsilon_w A + \Phi_D - 3\Phi_{SS} \right] u_0 = b^2 u_0$$

for spin triplet u_1^0 ($n^3 L_L$), u_1^+ ($n^3 L_{L+1}$) and u_1^- ($n^3 L_{L-1}$)

$$\begin{aligned} & \left[-\frac{d^2}{dr^2} + \frac{J(J+1)}{r^2} + 2m_w B + B^2 - A^2 + 2\epsilon_w A + \Phi_D - 2\Phi_{SO} + \Phi_{SS} + 2\Phi_T - 2\Phi_{SOT} \right] u_1^0 = b^2 u_1^0, \\ & \left[-\frac{d^2}{dr^2} + \frac{J(J-1)}{r^2} + 2m_w B + B^2 - A^2 + 2\epsilon_w A + \Phi_D + 2(J-1)\Phi_{SO} + \Phi_{SS} + \frac{2(J-1)}{2J+1}(\Phi_{SOT} - \Phi_T) \right] u_1^+ \\ & + \frac{2\sqrt{J(J+1)}}{2J+1} (3\Phi_T - 2(J+2)\Phi_{SOT}) u_1^- = b^2 u_1^+, \\ & \left[-\frac{d^2}{dr^2} + \frac{(J+1)(J+2)}{r^2} + 2m_w B + B^2 - A^2 + 2\epsilon_w A + \Phi_D - 2(J+2)\Phi_{SO} + \Phi_{SS} + \frac{2(J+2)}{2J+1}(\Phi_{SOT} - \Phi_T) \right] u_1^- \\ & + \frac{2\sqrt{J(J+1)}}{2J+1} (3\Phi_T + 2(J-1)\Phi_{SOT}) u_1^+ = b^2 u_1^- \end{aligned}$$

u_1^+ ($L = J - 1$) and u_1^- ($L = J + 1$) are coupled.

Interaction models

- $T = 0$, Cornell form

$$V(r) = -\frac{\alpha}{r} + \sigma r$$

- $T \neq 0$, two limits

$$V(r, T) = F \quad \text{or} \\ V(r, T) = U = F + TS = F - T\partial F / \partial T$$

Considering Debye screening (fitting the lattice data)

[S. Digal et al., Eur. Phys. J. C 43 (2005) 71]:

$$F = -\frac{\alpha}{r} (e^{-\mu r} + \mu r) + \frac{\sigma}{\mu} \left[\frac{\Gamma\left(\frac{1}{4}\right)}{2^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)} - \frac{\sqrt{\mu r}}{2^{\frac{3}{4}}\Gamma\left(\frac{3}{4}\right)} K_{\frac{1}{4}}(\mu^2 r^2) \right]$$

Interaction models

Separate the potential into two parts:

$$V(r, T) = A(r, T) + B(r, T)$$

For $V = F$

$$A(r, T) = -\frac{\alpha}{r} e^{-\mu r}$$

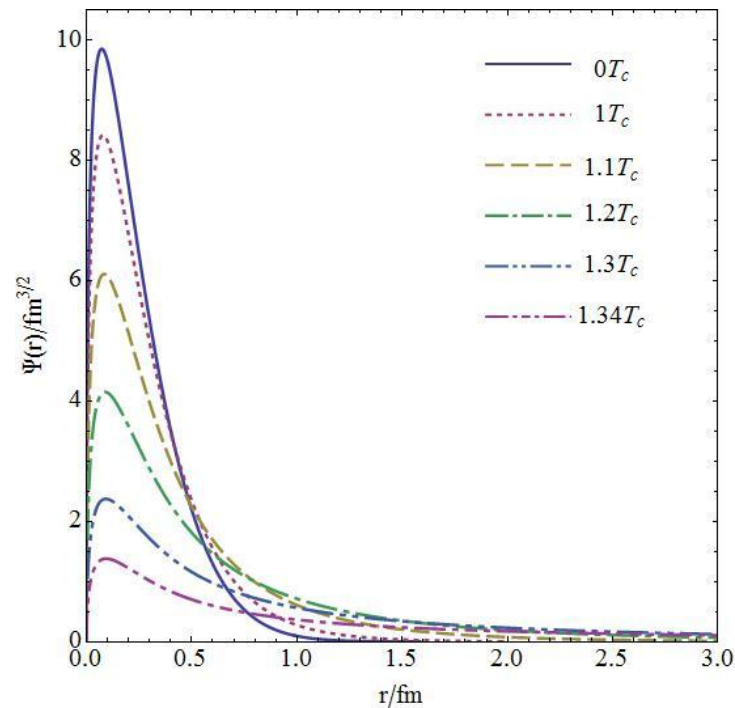
$$B(r, T) = \frac{\sigma}{\mu} \left[\frac{\Gamma\left(\frac{1}{4}\right)}{2^{\frac{3}{2}}\Gamma\left(\frac{3}{4}\right)} - \frac{\sqrt{\mu r}}{2^{\frac{3}{4}}\Gamma\left(\frac{3}{4}\right)} K_{\frac{1}{4}}(\mu^2 r^2) \right] - \alpha\mu$$

All terms in the equations can be expressed in A and B

Numerical results

$J/\psi : 1^3S_1$

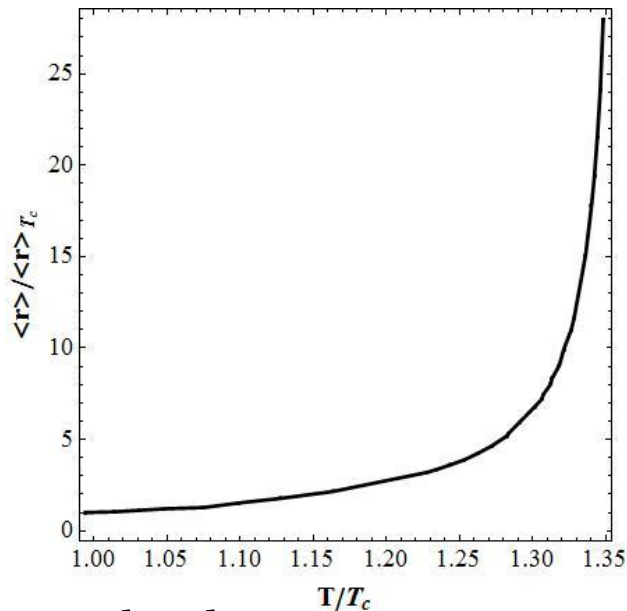
S-wave functions at different temperature for $V = F$:



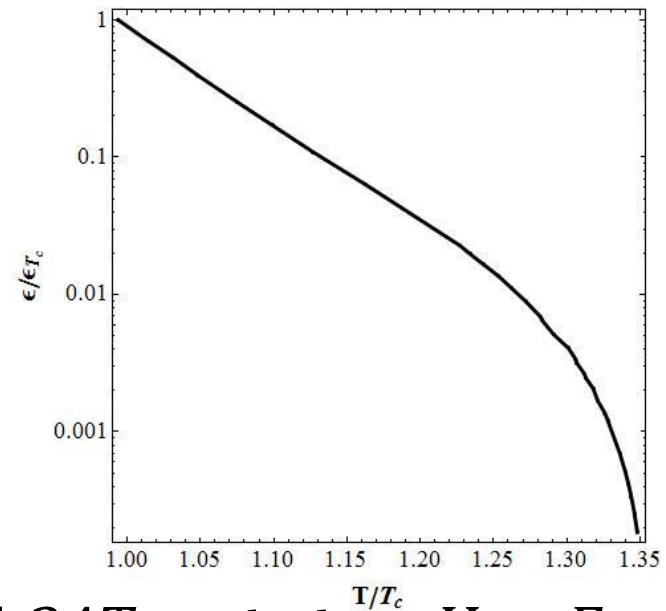
The wave functions expand rapidly above T_c

Numerical results

The average size of \mathbf{J}/ψ for
 $V = F$:



The binding energy of \mathbf{J}/ψ for
 $V = F$:



The dissociation temperature is $1.34T_c$ in the limit $V = F$.
In the other limit $V = U$, it is $2.38T_c$.
For χ_0 , T_d is just around T_c .

Conclusion

- The relativistic effect makes Charmonium survive a higher temperature.
- The dissociation temperature of J/ψ increases from $1.26T_c$ to $1.34T_c$ (7%) in the limit $V = F$ and in the other limit $V = U$, it increases from $2.1T_c$ to $2.38T_c$ (13%)
- On average, there is a relativistic correction of about 10% for Charmonium dissociation temperature.