

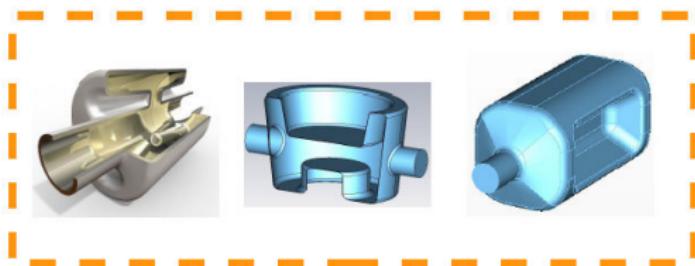
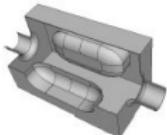
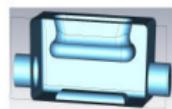
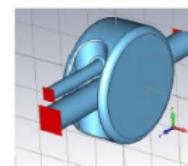
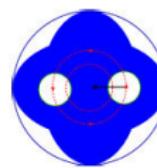
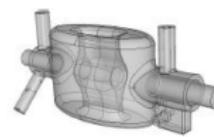
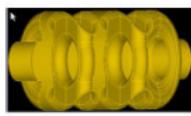
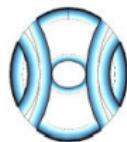
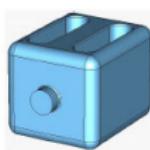
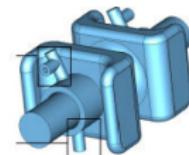
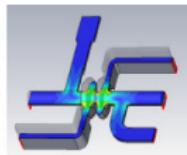
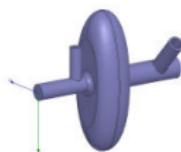
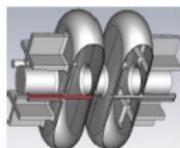
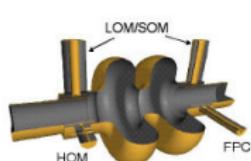
# Update on $n$ -Pole Error in Actual Compact Crab-Cavities Designs

María Navarro-Tapia    Alexej Grudiev    Rama Calaga

Radiofrequency Group, Beams Department  
CERN, Geneva (Switzerland)

**2nd Joint HiLumi-LARP Annual Meeting 2012**

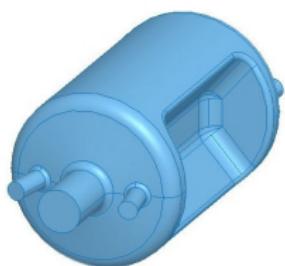
# Cavity Designs Proposed for LHC



R. Calaga

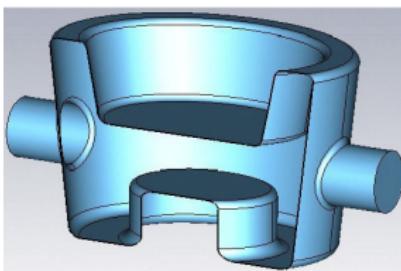
# LHC CC Prototypes Already Studied

RF dipole



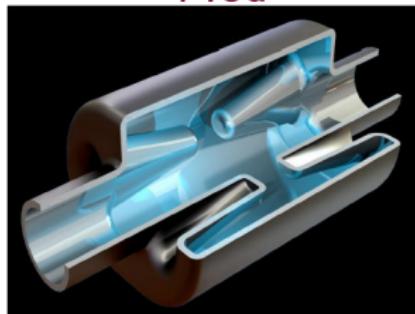
Courtesy of  
Z. Li, J. Delayen *et al.*  
ODU/SLAC

$\frac{1}{4}$ -wave



I. Ben-Zvi *et al.*  
BNL

4-rod



G. Bull, B. Hall  
UK

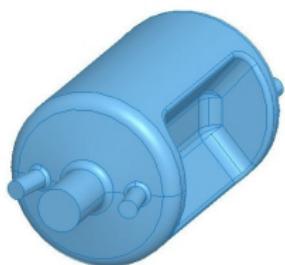
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Higher order multipolar  
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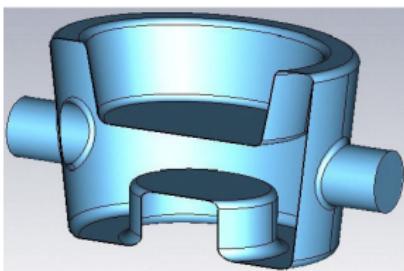
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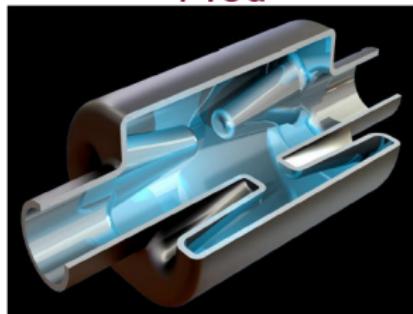
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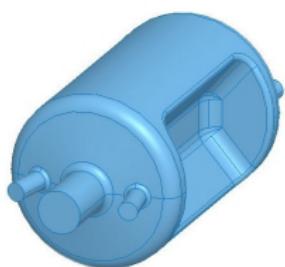
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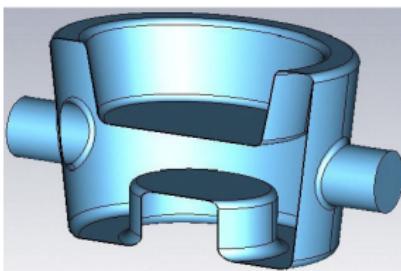
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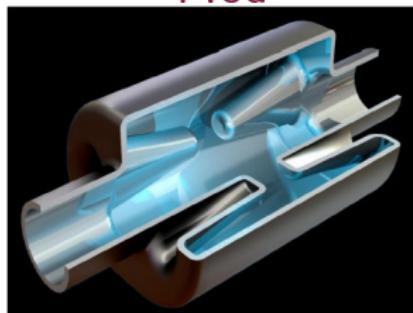
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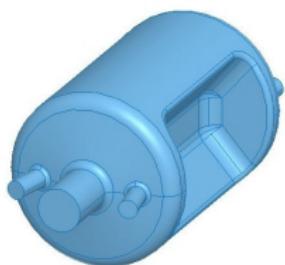
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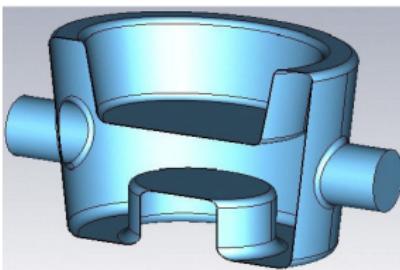
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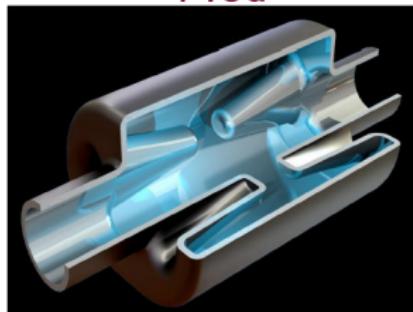
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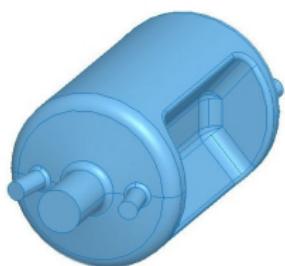
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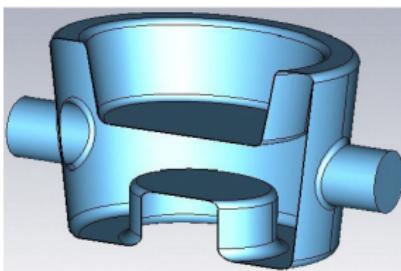
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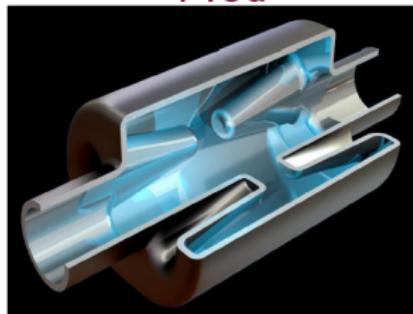
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# Studies on Multipolar RF Quicks

## Non-Linearity of Deflecting Field in LHC crab-cavities

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15.11.2011

LHC-CC11, 14-15.11.2011, CERN

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TUPPR027

### STUDY OF MULTIPOLAR RF KICKS FROM THE MAIN DEFLECTING MODE IN COMPACT CRAB CAVITIES FOR LHC\*

J. Barranco García, R. Calaga, R. De Maria, M. Giovannozzi, A. Grudiev, R. Tomás  
CERN, Geneva, Switzerland

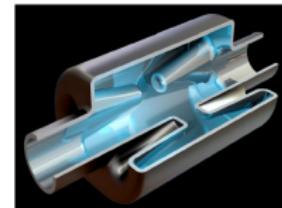
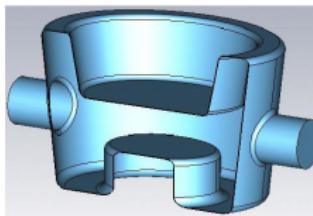
#### *Abstract*

A crab cavity (CC) system is under design in the framework of the High Luminosity LHC project. Due to

where  $Z_0$  is vacuum impedance,  $u_z$  the unit vector in Z direction,  $E_{kick} = E_{\perp} \cdot e^{j\omega/c}$ ;  $H_{kick} = H_{\perp} \cdot e^{j\omega/c}$  are the electric and magnetic fields in the particle frame,

# Updated Geometries

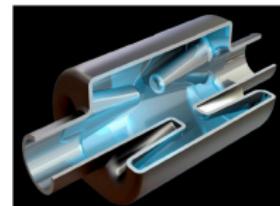
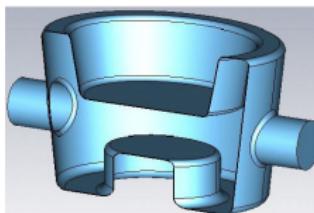
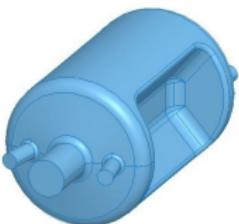
Prototypes  
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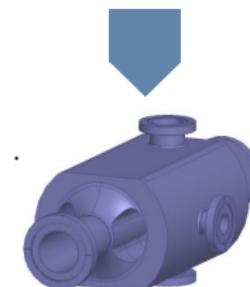
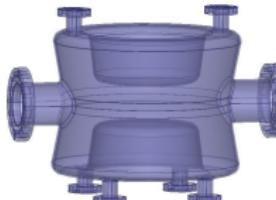
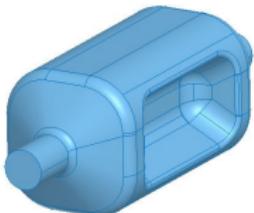
Latest  
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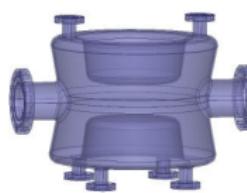
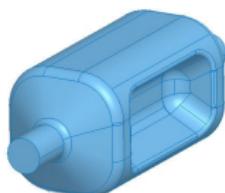
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\* No couplers yet

# Motivation and Objectives

Updated  
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Aim of this work

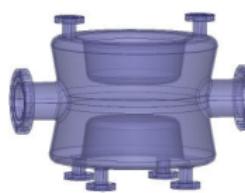
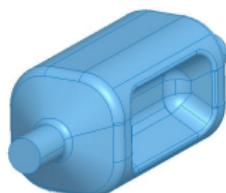
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Tolerances from the beam-dynamic study

- Assess the strengths of the higher-order terms.
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# Outline

- 1 Introduction
- 2 RF-Multipole Analysis Guideline
- 3 Results
- 4 Future Work
- 5 Summary and Conclusions
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# Fields Harmonics or Multipole Coefficients

Fields in the aperture of  
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described  
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Fourier coefficients  
(*field harmonics* or  
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Fourier expansion of the radial field components

$$B_r(r_0, \phi) = \sum_{n=1}^{\infty} [B_n(r_0) \sin n\phi + A_n(r_0) \cos n\phi]$$

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Applying the **field expansion** to  
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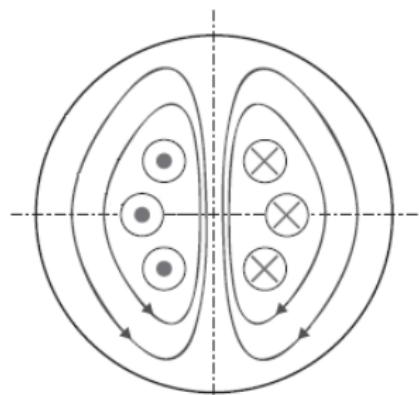
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# Effects of the cavity symmetry



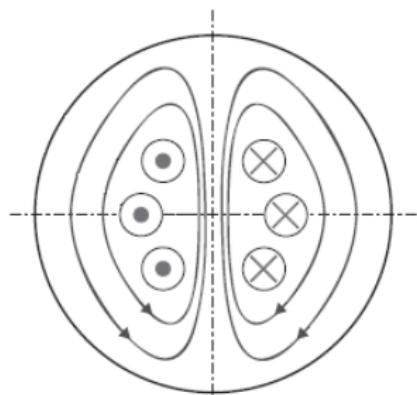
Main deflecting mode (TM<sub>110</sub> mode) of an axially symmetric cavity:

- Only dipolar variation ( $n = 1$ )

As long as the cavity is far from axial symmetry...

All the remaining multipolar components ( $n > 1$ ) might be present!

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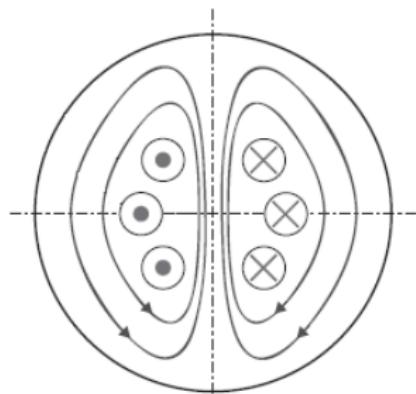
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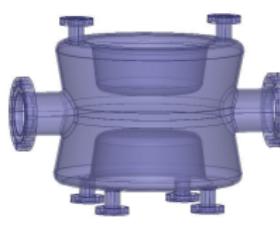
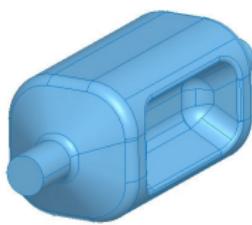


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# Some comments on the analysis

Calculation of the multipolar components of the transverse kicks:

- ① Lorentz force.

$$F_{\perp} = q [E_{\perp} + v_z \times B_{\perp}]$$

- ② Panofsky-Wenzel theorem

$$\Delta p_{\perp}(r, \phi) = \frac{jq}{\omega} \int_0^L \nabla_{\perp} E_{acc}(r, \phi, z) dz,$$

where  $E_{acc} = E_z e^{jkz}$  is the accelerating field.

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# Transverse RF Kick Summary

## Lorentz Force

$$\Delta p_{\perp}^{(n)} = \frac{1}{v_z} r^{n-1} [\vec{u}_r \cos(n\phi) + \vec{u}_{\phi} \sin(n\phi)] \int_0^L F_{\perp}^{(n)} dz$$

## Panofsky-Wenzel

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# RF Multipoles versus Magnetic Multipoles

## Magnetic multipoles

- Static.
- Kick non-dependent on the longitudinal position of particles.

## RF multipoles

- Harmonically oscillating ( $\omega_{RF}$ ).
- Kick does depend on the RF phase of the particle.

Equating the RF and magnetic multipoles...

$$B_{\perp}^{(n)} = \frac{1}{qc} F_{\perp}^{(n)} = \frac{n j}{\omega} E_{acc}^{(n)} \quad [Tm/m^n]$$

The RF kick coefficients...

$$b_n = \int_0^L B_{\perp}^{(n)} dz \in \mathbb{C} \quad [Tm/m^{n-1}]$$

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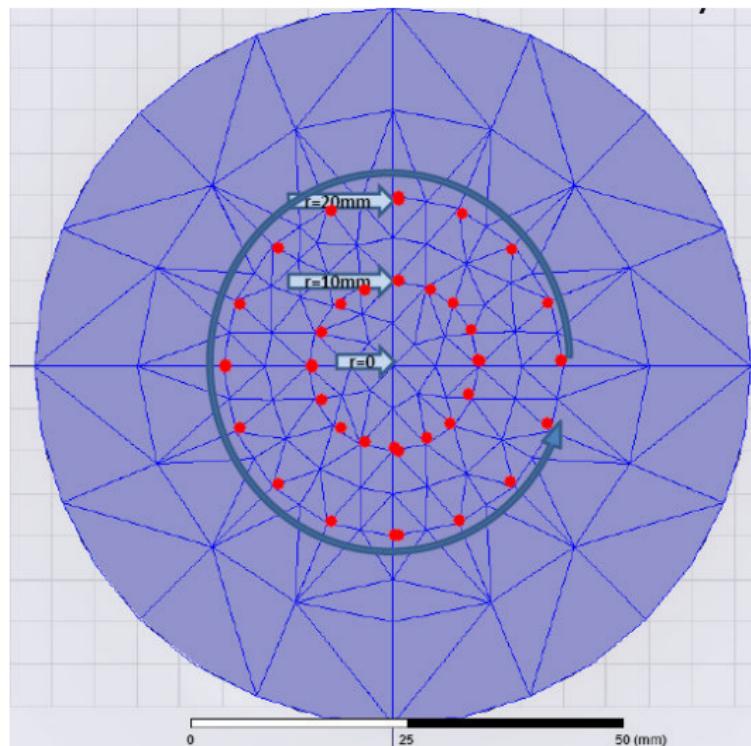
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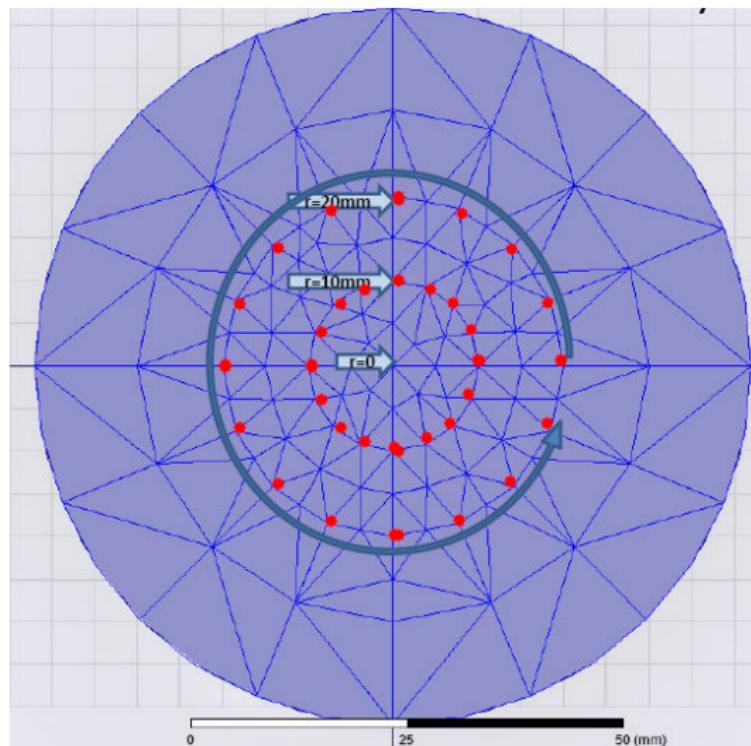
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- Mesh in the vicinity of the beam axis:
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  - 15 mm for  $r < 30$  mm
- Surface approx. of 1mm.
- # tetrahedra  $\sim 3.8 \cdot 10^5$
- Server: 1.00 TB of RAM, 4 processors @ 2.67 GHz
- Simulation time  $\sim 6 - 12$  hours



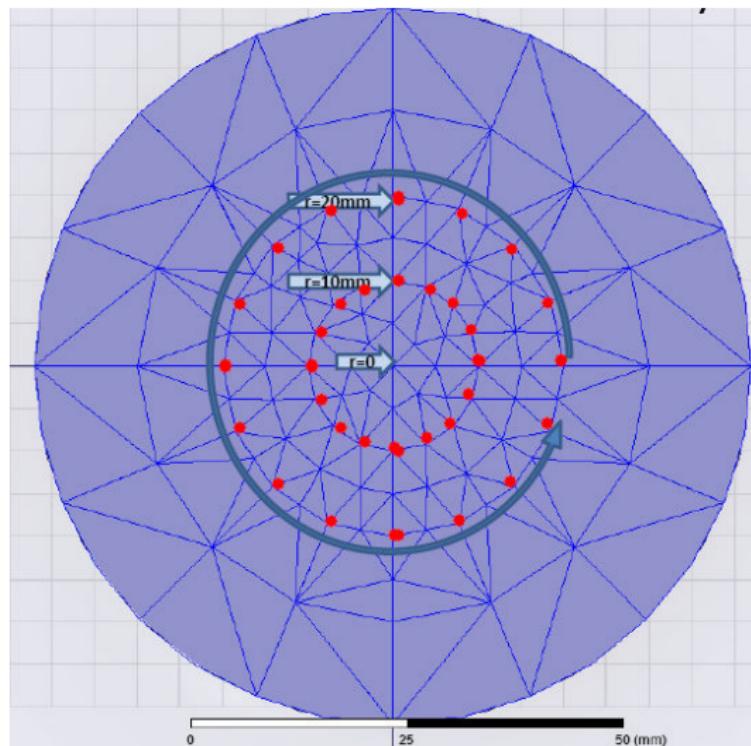
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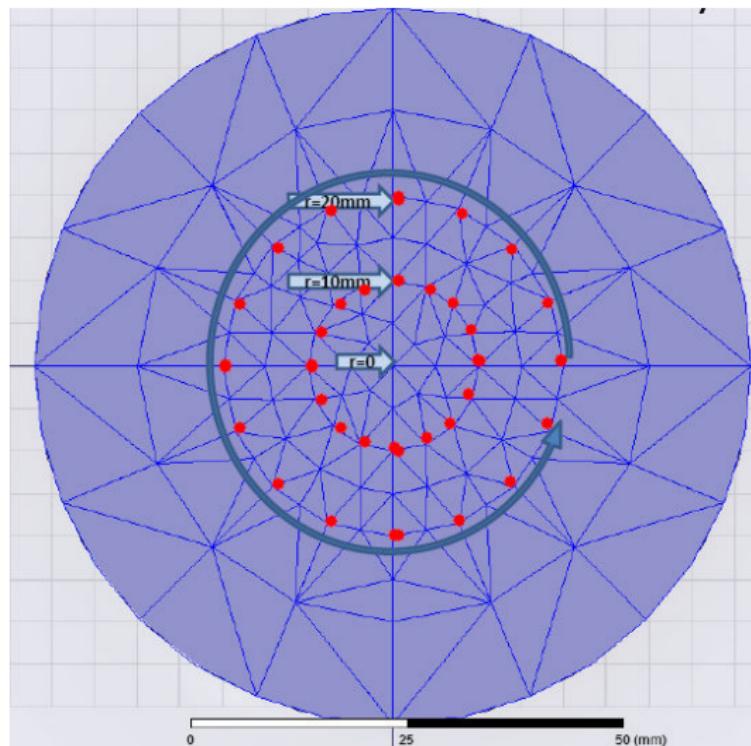
# Mesh definition

- Mesh in the vicinity of the beam axis:
  - 7 mm for  $r < 20$  mm
  - 15 mm for  $r < 30$  mm
- Surface approx. of 1mm.
- # tetrahedra  $\sim 3.8 \cdot 10^5$
- Server: 1.00 TB of RAM, 4 processors @ 2.67 GHz
- Simulation time  $\sim 6 - 12$  hours



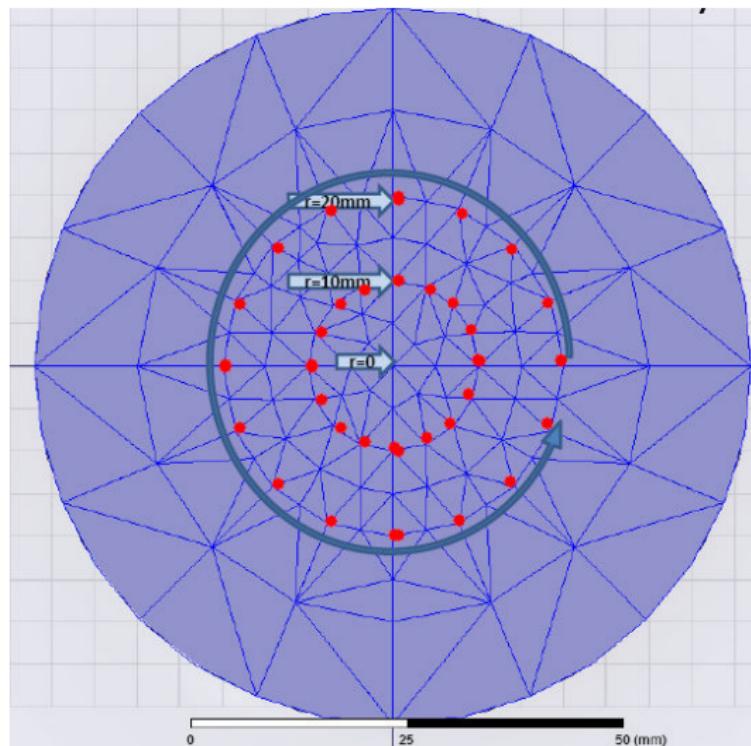
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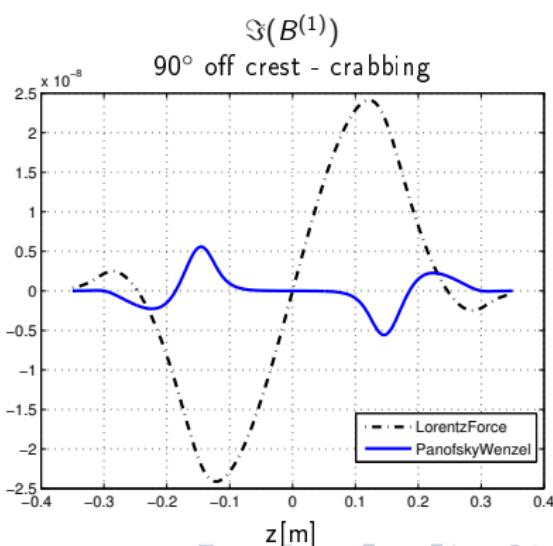
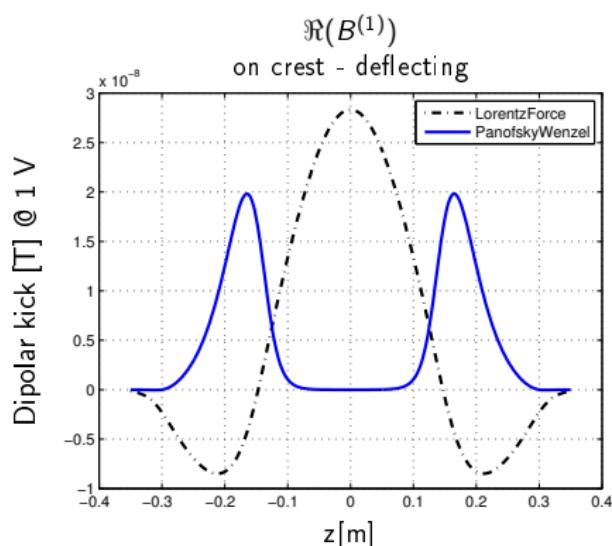
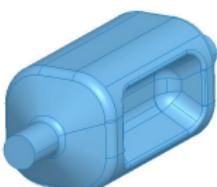
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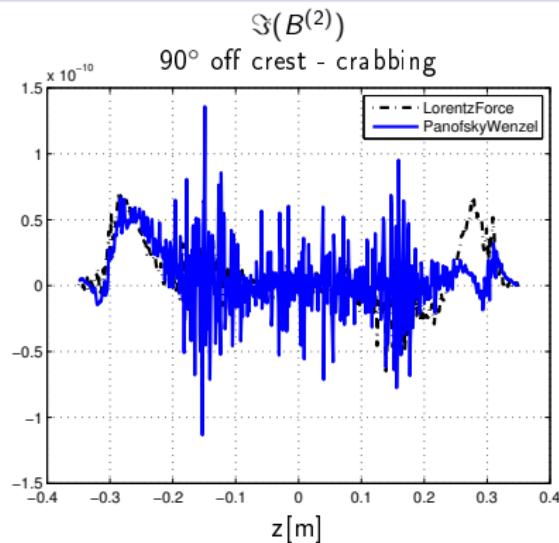
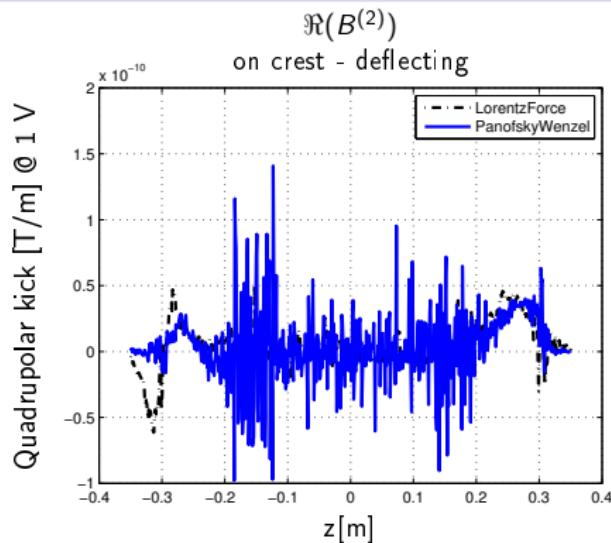
# Dipolar Kick at $V_x = 1$ V

Example: RF dipole (ridge) cavity



# Quadrupolar Kick at $V_x = 1$ V

Example: RF dipole (ridge) cavity

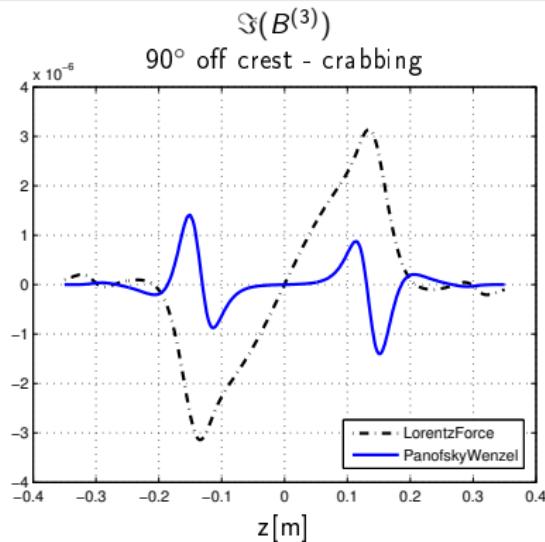
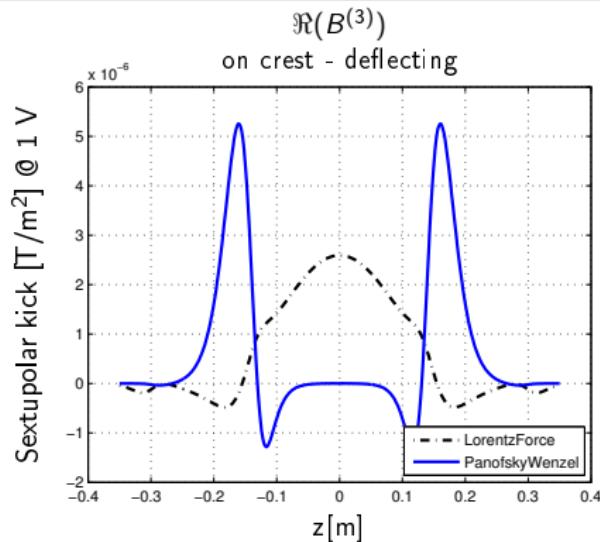


$$b_2(LF) = \int_0^L \frac{1}{qc} F_{\perp}^{(2)} dz = 0.00 + j0.01 \quad [n Tm/m]$$

$$b_2(PW) = \int_0^L \frac{j2}{\omega} E_{acc}^{(2)} dz = 0.00 + j0.01 \quad [n Tm/m]$$

# Sextupolar Kick at $V_x = 1$ V

Example: RF dipole (ridge) cavity

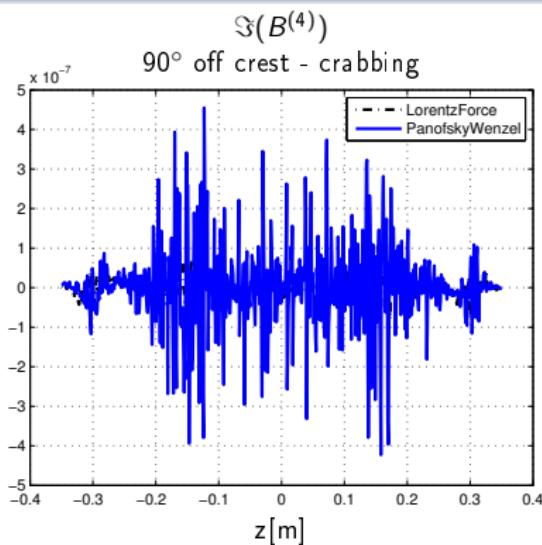
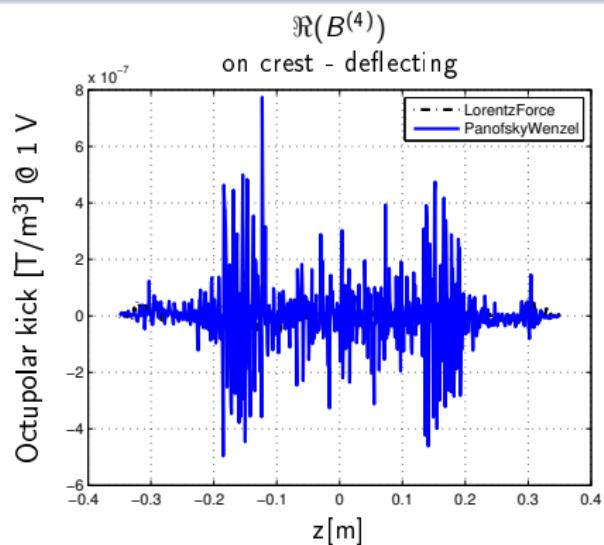


$$b_3(LF) = \int_0^L \frac{1}{qc} F_{\perp}^{(3)} dz = 452.67 - j0.04 \quad [nTm/m^2]$$

$$b_3(PW) = \int_0^L \frac{j3}{\omega} E_{acc}^{(3)} dz = 451.73 - j0.04 \quad [nTm/m^2]$$

# Octupolar Kick at $V_x = 1$ V

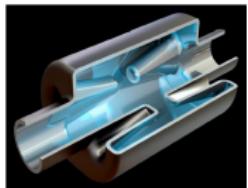
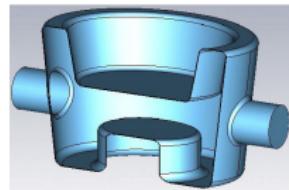
Example: RF dipole (ridge) cavity



$$b_4(LF) = \int_0^L \frac{1}{qc} F_{\perp}^{(4)} dz = -0.24 + j1.11 \quad [\text{n Tm/m}^3]$$

$$b_4(PW) = \int_0^L \frac{j4}{\omega} E_{acc}^{(4)} dz = 1.26 + j0.52 \quad [\text{n Tm/m}^3]$$

**2011  
prototypes**

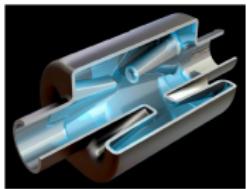


$V_x = 10$ MV	$b_2[mTm/m]$		$b_3[mTm/m^2]$		$b_4[mTm/m^3]$	
	$\Re(b_2)$	$\Im(b_2)$	$\Re(b_3)$	$\Im(b_3)$	$\Re(b_4)$	$\Im(b_4)$
RF dipole	-0.01	0.22	3203.29	-0.17	50.03	59.66
$\frac{1}{4}$ -wave	111.34	0.00	1266.72	-0.15	1821.02	11.48
4-rod	0.02	0.02	900.90	-0.33	74.31	40.57

RF dipole	0.03	0.05	4526.66	-0.41	-2.39	11.12
$\frac{1}{4}$ -wave	0.36	0.06	1076.75	0.01	90.86	-17.94
4-rod	-3.66	-1.91	-21561.95	692.32	-2100.47	699.00

\* Geometry for this cavity should be revised.

**2011  
prototypes**



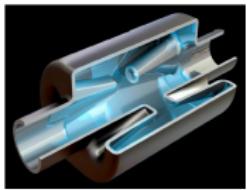
$V_x = 10$ MV	$b_2[mTm/m]$		$b_3[mTm/m^2]$		$b_4[mTm/m^3]$	
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**2012  
Updated  
geometries**

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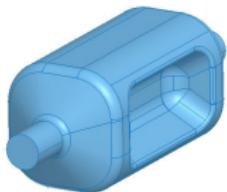
**2011  
prototypes**



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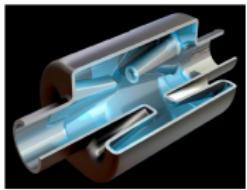
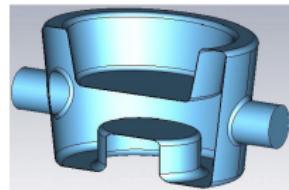
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**2012  
Updated  
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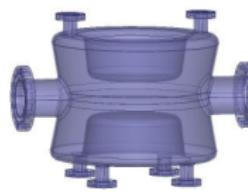
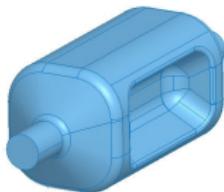
**2011  
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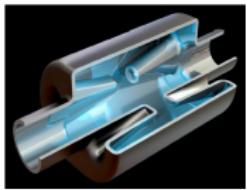
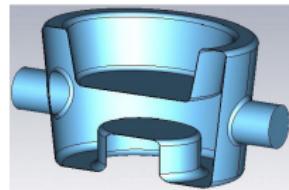
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**2012  
Updated  
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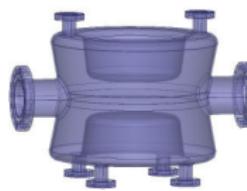
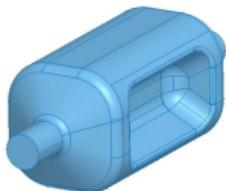
**2011  
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**2012  
Updated  
geometries**



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# Outline

1 Introduction

2 RF-Multipole Analysis Guideline

3 Results

4 Future Work

5 Summary and Conclusions

6 Acknowledgements

# Future Work (i)

## Accuracy

- Obtain an **estimation** of the **numerical accuracy** achieved.
- Error analysis.

## Measurements. Feasibility Study

- Aluminium prototype of the 1/4-wave cavity.
- A bead-pull set up is being under consideration (3D).

# Future Work (i)

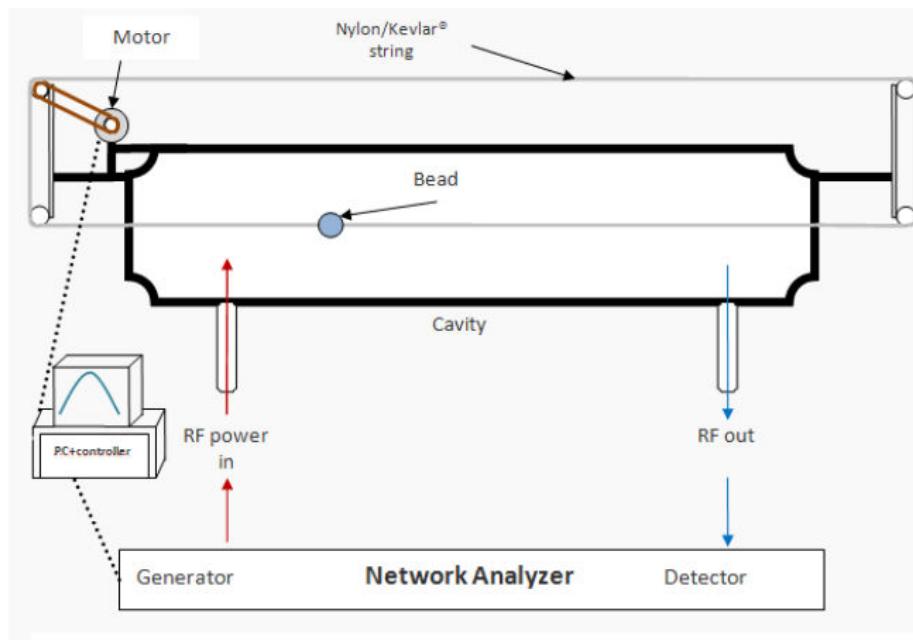
## Accuracy

- Obtain an **estimation** of the **numerical accuracy** achieved.
- Error analysis.

## Measurements. Feasibility Study

- Aluminium prototype of the 1/4-wave cavity.
- A bead-pull set up is being under consideration (3D).

## Future Work (ii)



Source: Michal Jarosz, "Bead-Pull Measurements", CERN project report.

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# Summary and conclusions

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- The **old prototypes** previously analyzed by Alexej have been considered as a **benchmark** to validate the actual multipole analysis employed.
- The **multipole coefficients** for the 3 updated cavities have been computed.
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# Acknowledgements

The HiLumi LHC Design Study (a sub-system of HL-LHC) is cofunded by the European Commission within the Framework Programme 7 Capacities Specific Programme, Grant Agreement 284404

# Update on $n$ -Pole Error in Actual Compact Crab-Cavities Designs

María Navarro-Tapia   Alexej Grudiev   Rama Calaga

Radiofrequency Group, Beams Department  
CERN, Geneva (Switzerland)

**2nd Joint HiLumi-LARP Annual Meeting 2012**