# Distribution of azimuthal momentum anisotropies in event-by-event fluid dynamics

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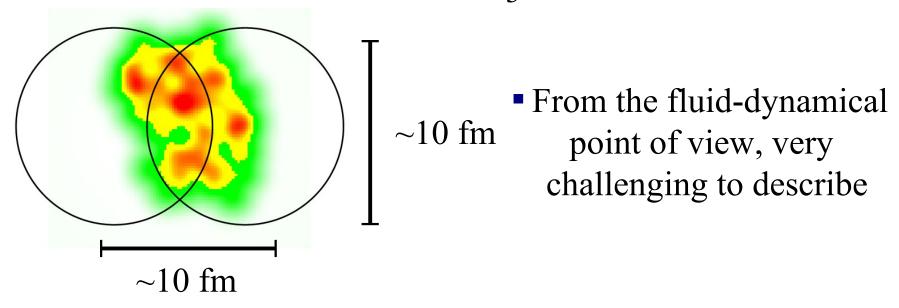
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with: H. Niemi, H. Holopainen, P. Huovinen



### Motivation

Now, we finally accept that fluid dynamics must be applied event by event (v<sub>3</sub>, ridge, etc)



→ Hydrodynamics should describe, not only event-averaged observables, but also **distributions** of observables

### In this talk

→ Is there correlation between the initial condition and the momentum anisotropies in an event-by-event level?

→ What can we learn from event-by-event distribution of flow? and flow correlations?

→ Can we find fluid-dynamical signatures for event-by-event **thermalization**? (not look only at averages)

# Fluid dynamics: inputs

$$\partial_{\mu}T^{\mu\nu} = 0$$

energy-momentum conservation

### Transient theory of fluid dynamics

$$\Delta^{\mu\nu}_{\alpha\beta}\tau_{\pi}D\pi^{\alpha\beta} + \pi^{\mu\nu} = 2\eta\sigma^{\mu\nu} - \frac{4}{3}\pi^{\mu\nu}\theta - \frac{10}{7}\Delta^{\mu\nu}_{\alpha\beta}\sigma^{\alpha}_{\ \lambda}\pi^{\beta\lambda} + \frac{74}{315\eta}\Delta^{\mu\nu}_{\alpha\beta}\pi^{\alpha}_{\ \lambda}\pi^{\beta\lambda},$$

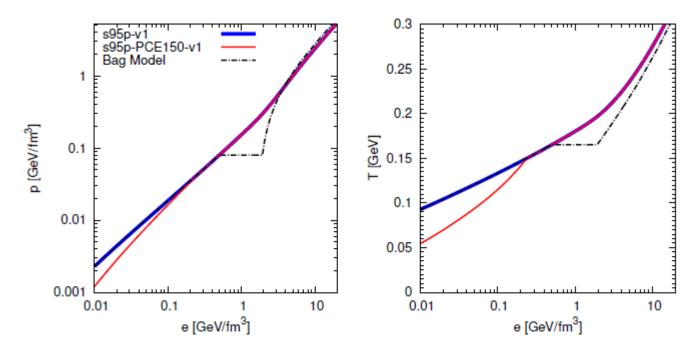
GSD et al, PRD85 114047 (2012)

$$\begin{array}{lll} \sigma^{\mu\nu} & = & \Delta^{\mu\nu}_{\alpha\beta} \nabla^{\alpha} u^{\beta} \\ \theta & = & \nabla_{\mu} u^{\mu} & \Delta^{\mu\nu}_{\alpha\beta} & = & \left( \Delta^{\mu}_{\alpha} \Delta^{\nu}_{\beta} + \Delta^{\nu}_{\alpha} \Delta^{\mu}_{\beta} - 2/3 \Delta^{\mu\nu} \Delta_{\alpha\beta} \right)/2 \\ \omega^{\mu\nu} & = & \frac{1}{2} \left( \nabla^{\mu} u^{\nu} - \nabla^{\nu} u^{\mu} \right) \\ \textbf{Still one term missing} \dots & \Delta^{\mu\nu}_{\alpha\beta} \pi^{\alpha}_{\lambda} \omega^{\beta\lambda} & \tau_{\pi} & = & 5 \frac{\eta}{\varepsilon + P} \end{array}$$

$$\Delta^{\mu\nu}_{\alpha\beta}\pi^{\alpha}_{\lambda}\omega^{\beta\lambda}$$

$$\tau_{\pi} = 5 \frac{\eta}{\varepsilon + P}$$

### Input - EoS



- → Lattice parametrization by Petreczky/Huovinen, arXiv:0912.2541
- → Chemical Freeze-out at 150 MeV (s95p-PCE150-v1)
- → Hadron Resonance Gas includes all hadronic states up to 2 GeV

### Input - Initial Condition

■ Event-by-event IC: Monte Carlo Glauber (Hannu's; ~2400 events)

$$s(x,y) = W \sum_{i=1}^{N_{\text{part,bin}}} \exp\left\{-\left[(x-x_i)^2 + (y-y_i)^2\right]/(2\sigma^2)\right\}$$

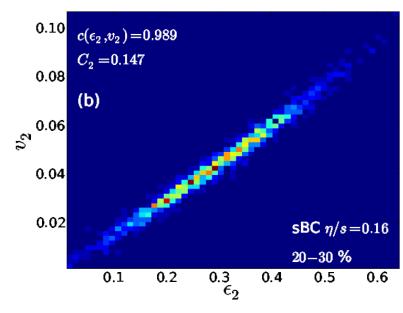
#### Npart: sWN and Nbin: sBC

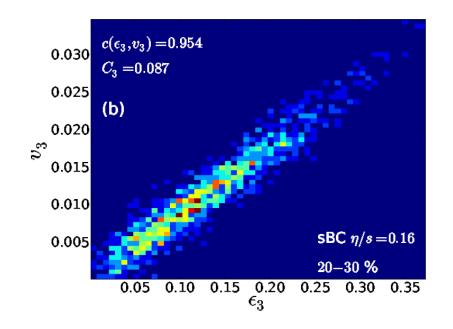
- Initial conditions in local thermal equilibrium; no initial velocity
- $\tau_0 = 0.5 1.0 \text{ fm}$

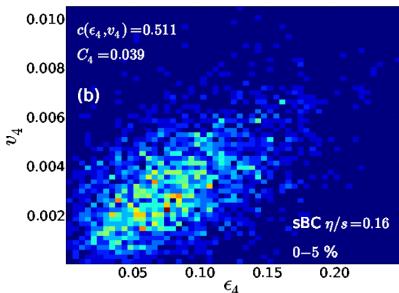
# Input - Freezeout

- Standard Cooper-Frye (Israel-Stewart *ansatz*), T<sub>f</sub>=100 MeV
- Decays included no re-scatterings

### Correlation with the initial state





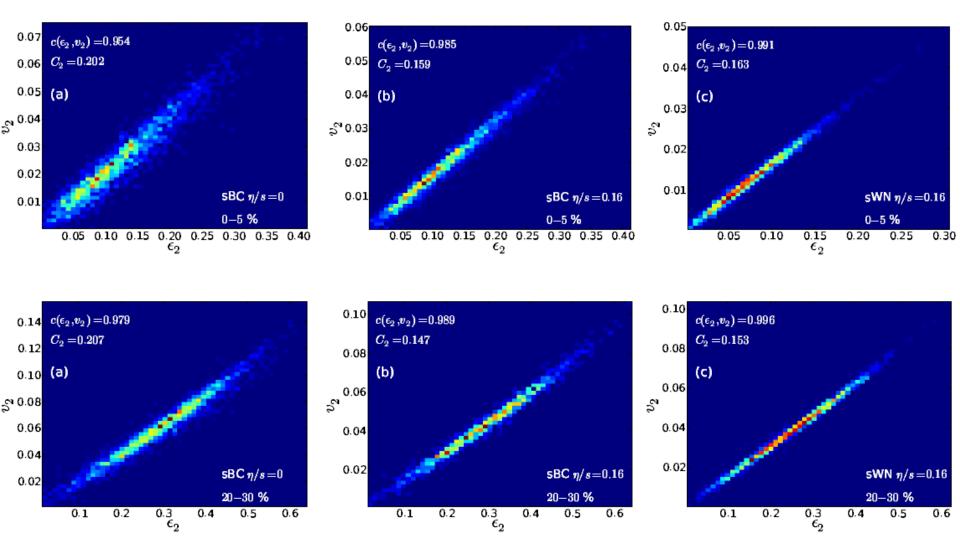


$$c(a,b) = \left\langle \frac{(a_i - \langle a \rangle)(b_i - \langle b \rangle)}{\sigma_a \sigma_b} \right\rangle$$

v<sub>2,3</sub> linearly correlated

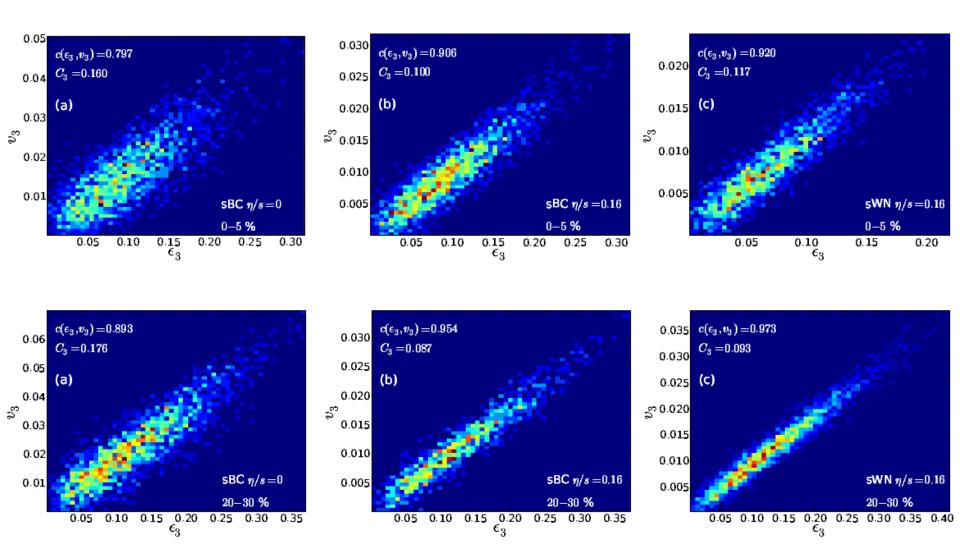
**v**<sub>4</sub> not linearly correlated

# $v_2$ and $\varepsilon_2 - 0-5\%$ , 20-30%



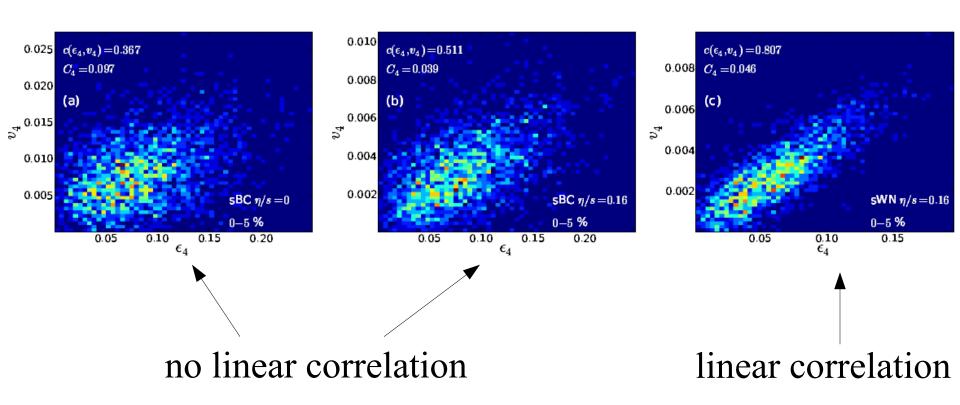
Strong linear correlation

# $v_3$ and $\varepsilon_3 - 0-5\%$ , 20-30%



Strong linear correlation

 $v_4$  and  $\varepsilon_4 - 0-5\%$ 20-30% – no linear correlation



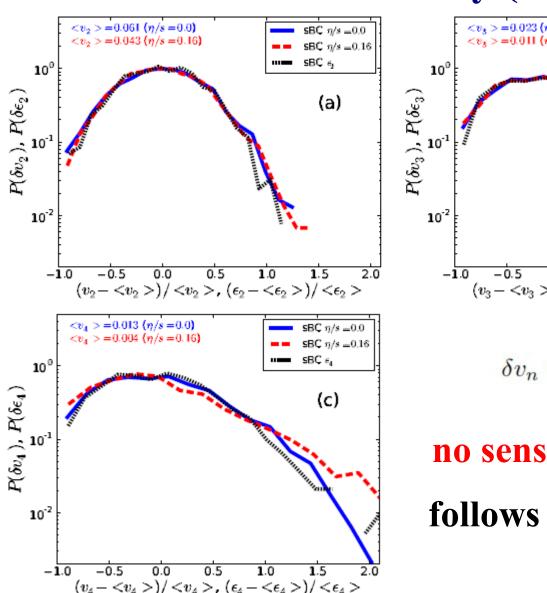
Depends on initial condition and viscosity

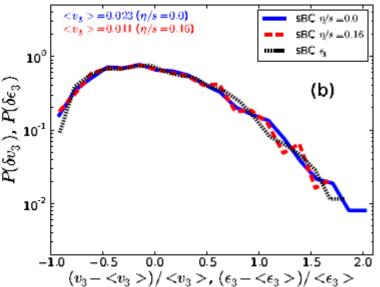
### Conclusions so far (n=2,3)

- Only the event-averaged v<sub>n</sub> carries information about the fluid
- The rest of the distribution is solely determined by the initial eccentricity fluctuations

lets see how this shows up in  $v_n$  distributions

# Distributions of $v_2$ , $v_3$ , and $v_4$ Effect of viscosity (RHIC)



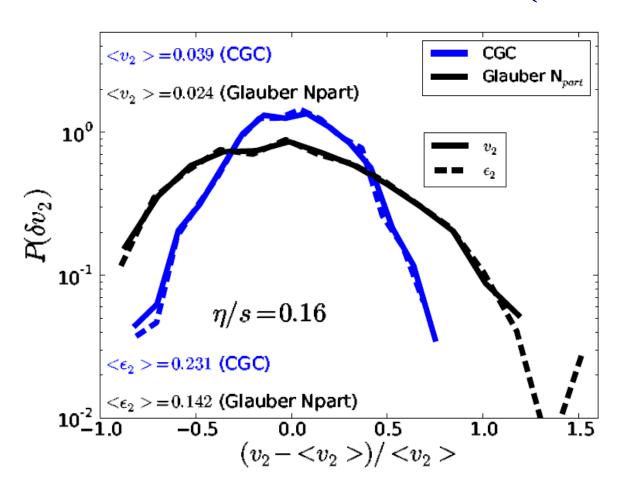


$$\delta v_n \equiv \frac{v_n - \langle v_n \rangle_{\text{ev}}}{\langle v_n \rangle_{\text{ev}}}$$

no sensitivity to viscosity!

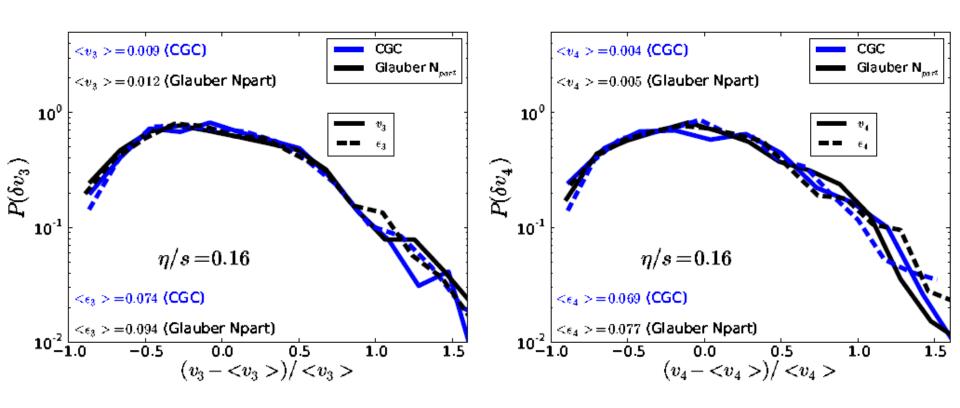
follows initial condition!

# Distributions of v<sub>2</sub> CGC mcKLN vs Glauber (LHC)



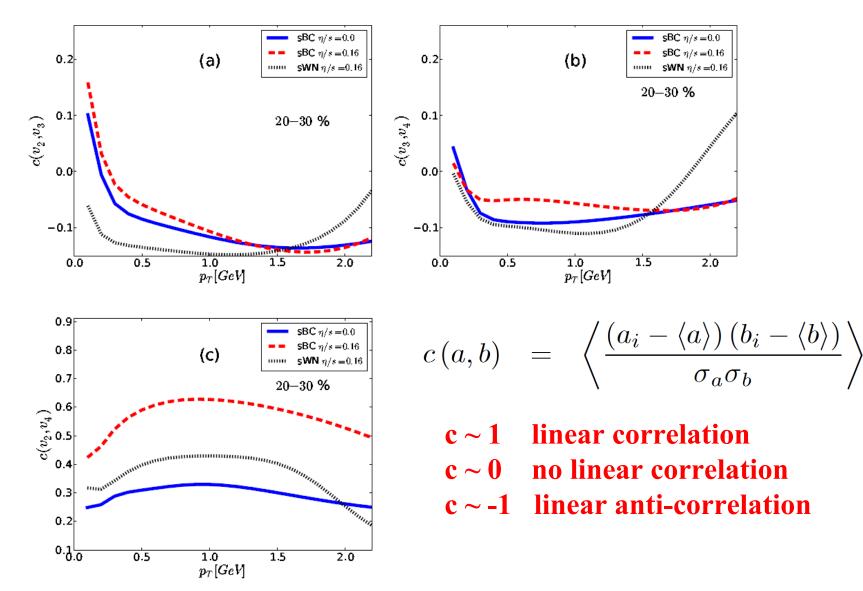
distributions are different, but still follow the initial condition

# Distributions of v<sub>3</sub> and v<sub>4</sub> CGC mcKLN vs Glauber

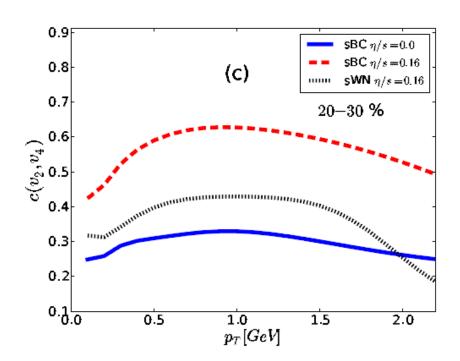


n=3,4 fluctuations are the same for all initial conditions

## $(v_n, v_m)$ linear correlations (RHIC)



# $(v_2, v_4)$ correlation



Huge effect of viscosity and of eccentricity correlations

Good observable to constraint the validity of event by event fluid dynamics

### Summary

- → We found strong EbyE linear correlation between eccentricities and momentum anisotropy
- $\rightarrow$  Distributions of  $v_n$  can provide robust constraints on initial condition models
- → Correlation functions between different v<sub>n</sub>'s can be a good signature of event-by-event fluid-dynamical behavior

# **BACK UP**

### We use the event plane method

### We compute $v_n$ as:

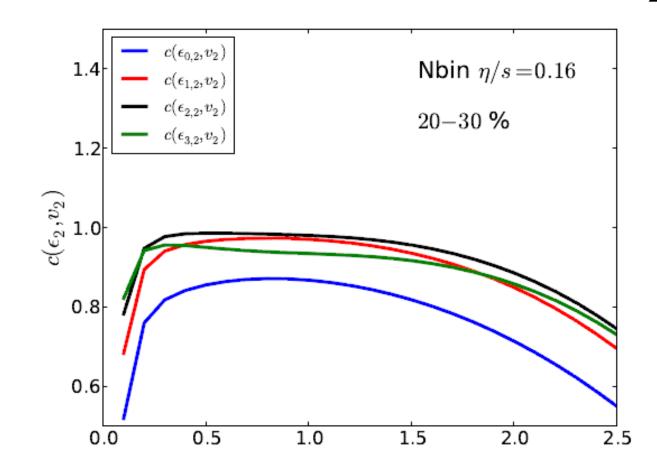
$$v_n e^{in\Psi_n} \equiv \langle e^{in\phi} \rangle$$

$$\psi_n \equiv \frac{1}{n} \arctan \frac{\langle p_T \sin n\phi \rangle}{\langle p_T \cos n\phi \rangle}$$

### We compute $\varepsilon_n$ as:

$$\varepsilon_{p,n} \equiv \frac{\langle r^p \cos [n (\phi - \psi_{PP})] \rangle_{\varepsilon}}{\langle r^p \rangle_{\varepsilon}} \qquad \varepsilon_n \equiv \varepsilon_{2,n}$$

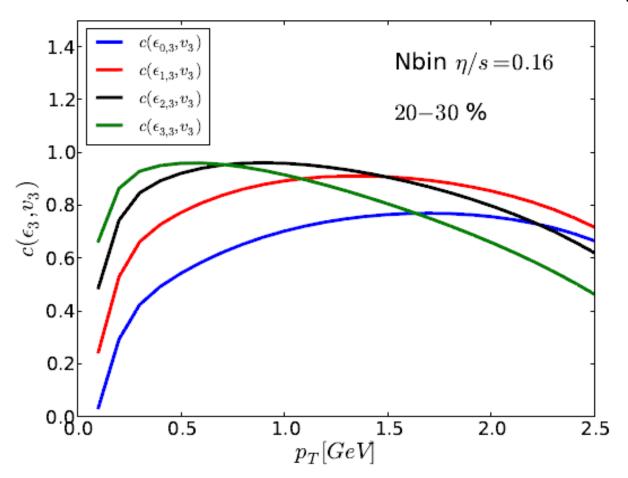
### Correlation with eccentricities $-v_2$



ullet high- $p_T$  and low- $p_T$   $v_n$ 's correlate with different  $\varepsilon_{p,n}$ 's

$$\varepsilon_{p,n} \equiv \frac{\langle r^p \cos [n (\phi - \psi_{PP})] \rangle_{\varepsilon}}{\langle r^p \rangle_{\varepsilon}} \quad \varepsilon_n \equiv \varepsilon_{2,n}$$

### Correlation with eccentricities $-v_3$

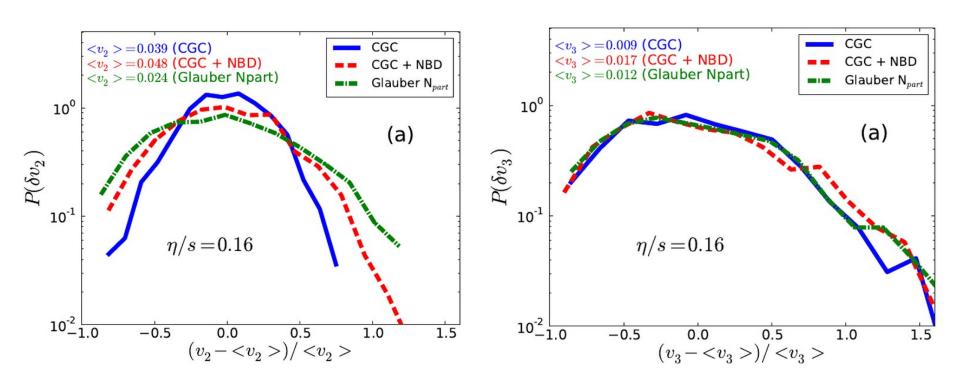


ullet high- $p_T$  and low- $p_T$   $v_n$ 's correlate with different  $\varepsilon_{p,n}$ 's

$$\varepsilon_{p,n} \equiv \frac{\langle r^p \cos [n (\phi - \psi_{PP})] \rangle_{\varepsilon}}{\langle r^p \rangle_{\varepsilon}} \quad \varepsilon_n \equiv \varepsilon_{2,n}$$

## Also, inclusion of multiplicity fluctuations

#### Goes in the correct direction ...



Work in progress

### $(v_n, v_m)$ linear correlations

