


Radiative B decays

$$B \rightarrow V + \gamma$$

Light vector mesons $V = \rho, K^*, \dots$

2.4 MeV $\frac{2}{3}$ u up	1.27 GeV $\frac{2}{3}$ c charm	171.2 GeV $\frac{2}{3}$ t top
4.8 MeV $-\frac{1}{3}$ d down	104 MeV $-\frac{1}{3}$ s strange	4.2 GeV $-\frac{1}{3}$ b bottom



- Driven by Flavor Changing Neutral Current (FCNC)
- Heavily suppressed at tree level in SM: rare decays
- Sensitive to New Physics that allows FCNC at tree level
- Very important to have reliable SM predictions to detect any New Physics

Theory of B decays

Bosch & Buchalla 2002

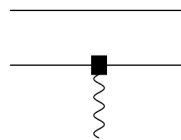
Effective Hamiltonian

$$H_{eff} = \frac{G_F}{\sqrt{2}} \sum_{p=u,c} \lambda_p^{(s)} [C_1 Q_1^p + C_2 Q_2^p + \sum_{i=3..8} C_i Q_i]$$

QCD factorization (QCDF): matrix element factorizes to leading power in the heavy quark limit

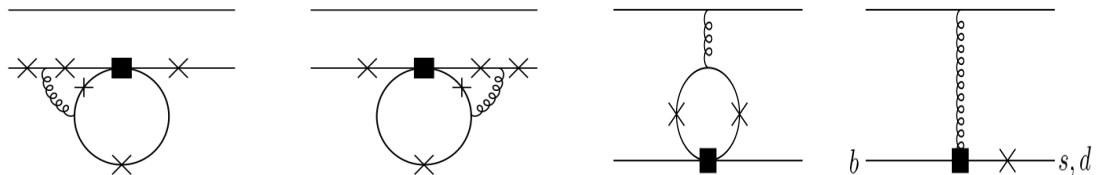
$$\left(\frac{\Lambda_{QCD}}{m_b}\right)^0 \quad \langle V\gamma | Q_i | \bar{B} \rangle = F^{B \rightarrow V} T_i^I + \int_0^1 d\xi du T_i^{II}(\xi, u) \Phi_B(\xi) \phi_V(u) \cdot e + \dots$$

α_s^0



Twist-2 DA of vector meson

α_s^1



Predictive power of QCDF

The predictive power of QCDF is limited by

- ❑ Hadronic uncertainties encoded in non-perturbative form factors and the twist-2 DAs of the vector meson.

- ❑ Power corrections to the leading power amplitude (may involve higher twist-3 DAs)

Power corrections

Flavor Physics and CP Violation Conference, Taipei, 2008

Theory review of exclusive rare radiative decays

Ben D. Pecjak
DESY theory group, Hamburg, Germany

I briefly review the theory status of exclusive rare radiative decays.

- Computation of power corrections suffer from **end-point divergences**
- Occur with standard Sum-Rules DAs

6. Summary

Rare radiative $B \rightarrow V\gamma$ decays are of increasing interest as experimental measurements become more precise. QCD factorization and SCET have provided a theoretical framework which can be used to calculate observables for these decays to leading order in $1/m_b$. The perturbative hard-scattering kernels have been known at NLO in α_s for some time, and recently a set of NNLO results have been obtained for the operators Q_1 , Q_7 , and Q_8 , although results for the four-quark operators Q_1 and Q_2 are not yet complete. The interesting observables such as isospin asymmetries and branching fractions in the $b \rightarrow d\gamma$ modes are sensitive to power corrections in $1/m_b$. Some of these have been estimated in the framework of light-cone sum rules, but a systematic treatment in SCET or QCD factorization is still missing due to the presence of endpoint divergences; a solution to this problem would be a much desired advance in this field.

Holographic AdS/QCD DAs offer a possibility to avoid end-point divergences

Phys. Rev. Lett. 102, 081601 (2009) [4 pages]

Light-Front Holography: A First Approximation to QCD

Abstract

References

Citing Articles (48)

Download: [PDF \(104 kB\)](#) [Buy this article](#) Export: [BibTeX](#) or [EndNote \(RIS\)](#)

Guy F. de Téramond¹ and Stanley J. Brodsky²

¹*Universidad de Costa Rica, San José, Costa Rica*

²*SLAC National Accelerator Laboratory, Stanford University, Stanford, California 94309, USA*

Received 29 September 2008; published 24 February 2009

Starting from the Hamiltonian equation of motion in QCD, we identify an invariant light-front coordinate ζ which allows the separation of the dynamics of quark and gluon binding from the kinematics of constituent spin and internal orbital angular momentum. The result is a single-variable light-front Schrödinger equation for QCD which determines the eigenspectrum and the light-front wave functions of hadrons for general spin and orbital angular momentum. This light-front wave equation is equivalent to the equations of motion which describe the propagation of spin- J modes on anti-de Sitter (AdS) space.

© 2009 The American Physical Society

URL: <http://link.aps.org/doi/10.1103/PhysRevLett.102.081601>

DOI: 10.1103/PhysRevLett.102.081601

PACS: 11.15.Tk, 12.38.Aw

A correspondence between light-front QCD in 4D and a string theory in 5D anti-de Sitter

A holographic light-front Schroedinger equation for mesons

- A relativistic QM equation for a meson in physical 4D spacetime which maps onto the classical wave equation for strings propagating in a modified 5D anti-de Sitter (AdS) space

$$\left(-\frac{d^2}{d\xi^2} - \frac{1-4L^2}{4\xi^2} + U(\xi) \right) \Phi(\xi) = M^2 \Phi(\xi) \quad \xi = \sqrt{z(1-z)}r$$

- Transverse distance in 4D maps onto fifth dimension in 5D AdS

$$\xi \leftrightarrow z_5$$

- Angular momentum in 4D maps onto 5D mass times curvature radius of anti-de Sitter space

$$(m_5 R)^2 \leftrightarrow L^2 - (J - 2)^2$$

- Interacting potential in 4D driven by the geometry in fifth dimension of AdS

$$U(z_5) = \frac{1}{2} \varphi''(z_5) + \frac{1}{4} \varphi'(z_5)^2 + \frac{2J-3}{2z_5} \varphi'(z_5)$$

AdS/QCD wavefunction for the ρ tested

PRL 109, 081601 (2012)

PHYSICAL REVIEW LETTERS

week ending
24 AUGUST 2012

AdS/QCD Holographic Wave Function for the ρ Meson and Diffractive ρ Meson Electroproduction

J. R. Forshaw*

Consortium for Fundamental Physics, School of Physics and Astronomy, University of Manchester, Oxford Road, Manchester M13 9PL, United Kingdom

R. Sandapen†

Département de Physique et d'Astronomie, Université de Moncton, Moncton, New Brunswick E1A3E9, Canada
(Received 5 April 2012; published 20 August 2012)

We show that anti-de Sitter/quantum chromodynamics generates predictions for the rate of diffractive ρ -meson electroproduction that are in agreement with data collected at the Hadron Electron Ring Accelerator electron-proton collider.

DOI: 10.1103/PhysRevLett.109.081601

PACS numbers: 11.25.Tq, 12.38.Aw, 12.38.-t, 13.60.Lc

Introduction.—To date, the correspondence between string theory in five-dimensional anti-de Sitter (AdS) space and four-dimensional quantum chromodynamics (QCD) has enjoyed a number of successes (see Refs. [1–4] and references therein). In this Letter, we demonstrate another success by showing that parameter-free AdS/QCD wave functions for the ρ meson lead to predictions for the rate of diffractive ρ meson production ($\gamma^* p \rightarrow \rho p$) that agree with the data collected at the Hadron Electron Ring Accelerator (HERA) ep collider.

In previous papers [5,6], we took a phenomenological approach and extracted the light-front wave functions of the ρ meson using the HERA data. We follow the same formalism here, except that we now use the AdS/QCD wave functions predicted in Refs. [7,8].

The AdS/QCD wavefunction.—Brodsky and de Téramond have recently shown that, in what they call a first semiclassical approximation to light-front QCD [9], the meson wave function can be written in the following factorized form

$$\phi(x, \zeta, \varphi) = \frac{\Phi(\zeta)}{\sqrt{2\pi\zeta}} f(x) e^{iL\varphi} \quad (1)$$

where L is the orbital quantum number and $\zeta = \sqrt{x(1-x)}b$ (x is the light-front longitudinal momentum fraction of the quark, and b is the quark-antiquark transverse separation). The function $\Phi(\zeta)$ satisfies a Schrödinger-like wave equation

$$U(\zeta) = \kappa^4 \zeta^2 + 2\kappa^2(J-1). \quad (3)$$

This potential encodes the confinement dynamics of QCD, and the challenge remains to derive it from first-principles QCD.

Solving Eq. (2) with this potential results in eigenvalues

$$M^2 = 4\kappa^2(n + J/2 + L/2), \quad (4)$$

which reproduces the correct meson mass spectrum. In particular, it predicts a massless pion ($S=0, n=0, L=0$) and $M_\rho^2 = 2\kappa^2$ for the ρ meson ($S=1, n=0, L=0$). The corresponding eigenfunctions are [11]

$$\Phi(\zeta) = \kappa\sqrt{2}\zeta \exp\left(-\frac{\kappa^2 \zeta^2}{2}\right). \quad (5)$$

It remains to specify the function $f(x)$ in Eq. (1). This can be done by comparing the expressions for the pion electromagnetic form factor obtained in the light-front formalism and in AdS space [7], and it results in

$$f(x) = \mathcal{N}\sqrt{x(1-x)}. \quad (6)$$

The resulting wave function is thus

$$\phi(x, \zeta) = \mathcal{N} \frac{\kappa}{\sqrt{\pi}} \sqrt{x(1-x)} \exp\left(-\frac{\kappa^2 \zeta^2}{2}\right), \quad (7)$$

where \mathcal{N} is a normalization constant. Assuming the meson is dominated by its leading $q\bar{q}$ Fock component, \mathcal{N} is fixed by

Successful predictions for diffractive ρ production

In collaboration with J.R. Forshaw (Manchester U)

See talk by RS in WG2 at 15h tomorrow

Distribution Amplitudes are related to AdS/QCD light-front wavefunctions

We are then able to deduce that

$$\phi_{\rho}^{\parallel}(z, \mu) = \frac{N_c}{\pi f_{\rho} M_{\rho}} \int dr \mu J_1(\mu r) [M_{\rho}^2 z(1-z) + m_f^2 - \nabla_r^2] \frac{\phi_L(r, z)}{z(1-z)},$$

$$\phi_{\rho}^{\perp}(z, \mu) = \frac{N_c m_f}{\pi f_{\rho}^{\perp}} \int dr \mu J_1(\mu r) \frac{\phi_T(r, z)}{z(1-z)},$$

$$g_{\rho}^{\perp(v)}(z, \mu) = \frac{N_c}{2\pi f_{\rho} M_{\rho}} \int dr \mu J_1(\mu r) [m_f^2 - (z^2 + (1-z)^2) \nabla_r^2] \frac{\phi_T(r, z)}{z^2(1-z)^2}$$

and

$$\frac{dg_{\rho}^{\perp(a)}}{dz}(z, \mu) = \frac{\sqrt{2} N_c}{\pi f_{\rho} M_{\rho}} \int dr \mu J_1(\mu r) (1-2z) [m_f^2 - \nabla_r^2] \frac{\phi_T(r, z)}{z^2(1-z)^2}. \quad (51)$$

M. Ahmady & RS
PRD 87 (2013) 054013

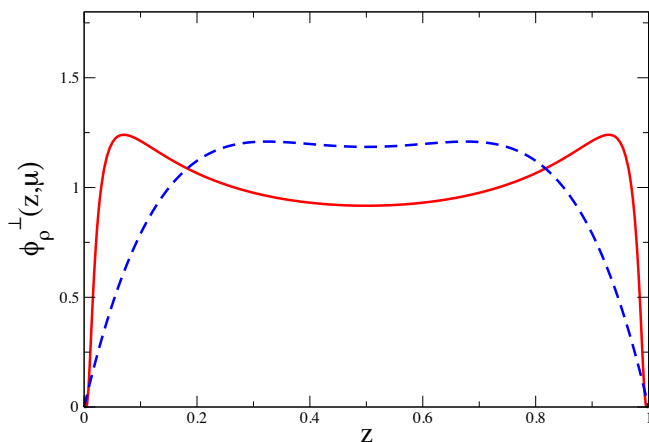
Also
J. R. Forshaw & RS
JHEP 1110 (2011) 093

Earlier: S. Brodsky & G. Lepage
(1980)

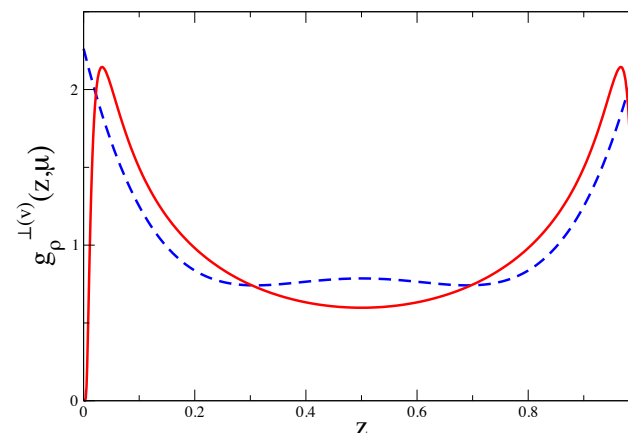
4 DAs: Twist-2 (long & trans), Twist-3(vector & axial vector)

Comparing AdS/QCD to Sum Rules

Twist-2 DA



Twist-3 DA

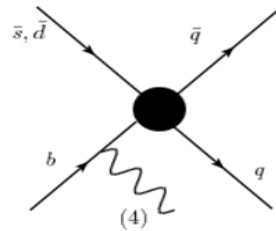
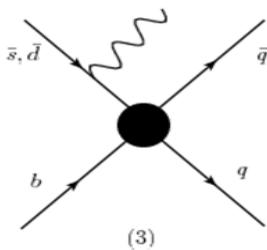
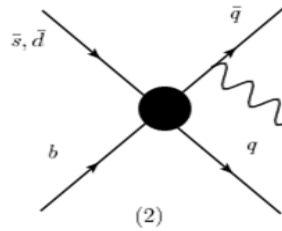
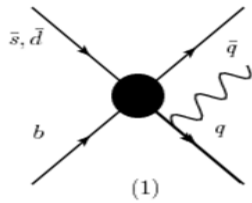


- Different end-point behavior for the (transverse) twist-2 and (vector) twist-3 DAs
- The transverse twist-2 DA enters the computation of the leading power decay amplitude
- The vector twist-3 DA enters the computation of some power corrections to the leading amplitude

Annihilation power corrections

M. Ahmady & RS
PRD 2013

- Two divergent integrals from diagram (1) and (2) with twist-3 SR DA
- **No divergence** with twist-3 AdS/QCD DA



Integral	SR	AdS/QCD
$I_{1(s)}^{\text{tw}3}(\mu)$	∞	0.237(0.229)
$I_{2(s)}^{\text{tw}3}(\mu)$	∞	0.036(0.034)

Branching ratio

M. Ahmady & RS
PRD 2013

$$Br(B \rightarrow V\gamma) = \frac{\Gamma(B \rightarrow V\gamma)}{\Gamma_{tot}}$$

Branching ratio ($\times 10^{-7}$) for $\bar{B}^0 \rightarrow \rho^0 \gamma$

DA	Accuracy	SR	AdS/QCD	PDG	Belle	BaBar
tw2 + tw3	Lead. (α_s^1) + Anni. $[\alpha_s^0, (1/m_b)^2]$		7.67	8.6 ± 1.5	$7.8 \pm_{1.6}^{1.7} \pm_{1.0}^{0.9}$	$9.7 \pm_{2.2}^{2.4} \pm_{0.6}^{0.6}$
tw2	Lead. (α_s^1) + Anni. $[\alpha_s^0, (1/m_b)]$	7.86	7.65			
tw2	Leading (α_s^1)	7.87	7.68			
None	Leading (α_s^0)	4.76	4.76			

- Power corrections are numerically small
- Divergence problem has no practical consequence when computing BR
- But it is a conceptual problem

Branching ratio for a very rare decay

M. Ahmady & RS
PRD 2013

$$\bar{B}_s^0 \rightarrow \rho + \gamma$$

- This decay proceeds **only** via **annihilation**
- AdS/QCD prediction for Branching Ratio is 5.5×10^{-10}
- Likely to be enhanced by New Physics
- Can it be investigated at LHCb ?

The isospin asymmetry

Work in progress with
M. Ahmady (Mount Allison U)

- Branching ratios are
 - sensitive to hadronic uncertainties
 - but less sensitive to power corrections

$$Br(B \rightarrow K^* \gamma) = \frac{\Gamma(B \rightarrow K^* \gamma)}{\Gamma_{tot}}$$

- Isospin asymmetry is
 - less sensitive to hadronic uncertainties
 - but is a power correction

$$\Delta_{0-} \equiv \frac{\Gamma(\bar{B}^0 \rightarrow \bar{K}^{*0} \gamma) - \Gamma(B^- \rightarrow K^{*-} \gamma)}{\Gamma(\bar{B}^0 \rightarrow \bar{K}^{*0} \gamma) + \Gamma(B^- \rightarrow K^{*-} \gamma)}$$

- Crucial to deal with the divergence problem when predicting the isospin asymmetry

Branching ratio for K^*

Branching ratio	BABAR	BELLE	CLEO	PDG
$\mathcal{B}(B^0 \rightarrow K^{*0}\gamma) \times 10^6$	$44.7 \pm 1.0 \pm 1.6$	$45.5^{+7.2}_{-6.8} \pm 3.4$	$40.1 \pm 2.1 \pm 1.7$	43.3 ± 1.5
$\mathcal{B}(B^+ \rightarrow K^{*+}\gamma) \times 10^6$	$42.2 \pm 1.4 \pm 1.6$	$42.5 \pm 3.1 \pm 2.4$	$37.6^{+8.9}_{-8.3} \pm 2.8$	42.1 ± 1.8
$\Delta_{0-}(B \rightarrow K^*\gamma)$	$6.6 \pm 2.1 \pm 2.2$	$1.2 \pm 4.4 \pm 2.6$		5.2 ± 2.6

Our AdS/QCD for the branching ratio is 44.8×10^{-6} in agreement with the SR prediction and data

Isospin asymmetry for K*

Preliminary

$$F_{\perp} = \int_0^1 dz \frac{\phi_{\perp}(z)}{3(1-z)}$$

$$G_{\perp}(s_c) = \int_0^1 dz \frac{\phi_{\perp}(z)}{3(1-z)} G(s_c, \bar{z})$$

$$H_{\perp}(s_c) = \int_0^1 dz \left(g_{\perp}^{(v)} - \frac{1}{4} \frac{dg_{\perp}^{(a)}}{dz} \right) G(s_c, \bar{z})$$

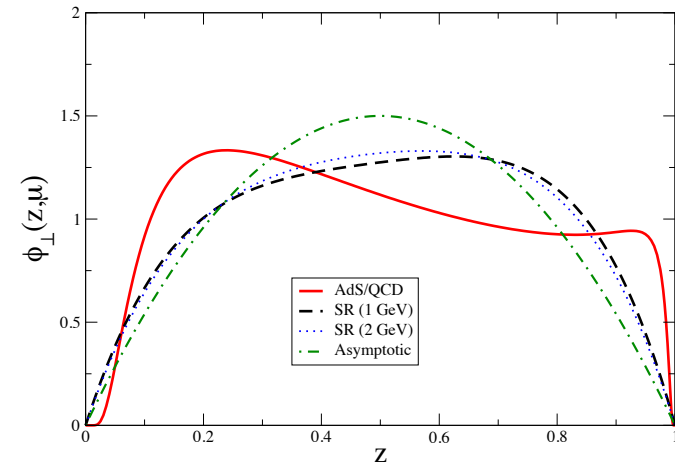
$$X_{\perp} = \int_0^1 dz \phi_{\perp}(z) \left(\frac{1+\bar{z}}{3\bar{x}^2} \right)$$

Integral	SR	AdS/QCD
X_{\perp}	∞	26.9
F_{\perp}	1.14	1.38
G_{\perp}	$2.55 + 0.43i$	$2.89 + 0.30i$
H_{\perp}	$2.48 + 0.50i$	$2.12 + 0.21i$

No diverging integral with AdS/QCD DA

Our prediction: $\Delta_{0-} = 4.6\%$

Particle Data Group: $\Delta_{0-} = (5.2 \pm 2.6)\%$



Conclusions

- Computed observables in radiative B decays to vector mesons (ρ, K^*) using new AdS/QCD DAs for the vector mesons
- Agreement with data for branching ratios and isospin asymmetry
- Agreement with Sum Rules DAs for leading power predictions but avoids end-point divergences for power-suppressed contributions

Acknowledgements

- This research is supported by the Canadian National Science and Engineering Research Council (NSERC)
- Financial support from Universite de Moncton and Mount Allison University

Back up slide 1

Definition of DAs

Distribution Amplitudes parameterize the operator product expansion of vacuum-to-meson transition matrix elements of quark-antiquark non-local gauge invariant operators at light-like separations. At equal light-front time $x^+ = 0$ and in the light-front gauge $A^+ = 0$, we have [4, 5]

$$\begin{aligned} \langle 0 | \bar{q}(0) \gamma^\mu q(x^-) | \rho(P, \lambda) \rangle &= f_\rho M_\rho \frac{e_\lambda \cdot x}{P^+ x^-} P^\mu \int_0^1 du e^{-iuP^+ x^-} \phi_\rho^\parallel(u, \mu) \\ &+ f_\rho M_\rho \left(e_\lambda^\mu - P^\mu \frac{e_\lambda \cdot x}{P^+ x^-} \right) \int_0^1 du e^{-iuP^+ x^-} g_\rho^{\perp(v)}(u, \mu), \end{aligned} \quad (27)$$

$$\langle 0 | \bar{q}(0) [\gamma^\mu, \gamma^\nu] q(x^-) | \rho(P, \lambda) \rangle = 2f_\rho^\perp (e_\lambda^\mu P^\nu - e_\lambda^\nu P^\mu) \int_0^1 du e^{-iuP^+ x^-} \phi_\rho^\perp(u, \mu) \quad (28)$$

and

$$\langle 0 | \bar{q}(0) \gamma^\mu \gamma^5 q(x^-) | \rho(P, \lambda) \rangle = -\frac{1}{4} \epsilon_{\nu\rho\sigma}^\mu e_\lambda^\nu P^\rho x^\sigma f_\rho M_\rho \int_0^1 du e^{-iuP^+ x^-} g_\rho^{\perp(a)}(u, \mu) \quad (29)$$

for the vector, tensor and axial-vector current respectively. The polarization vectors e_λ are

Back-up slide 2

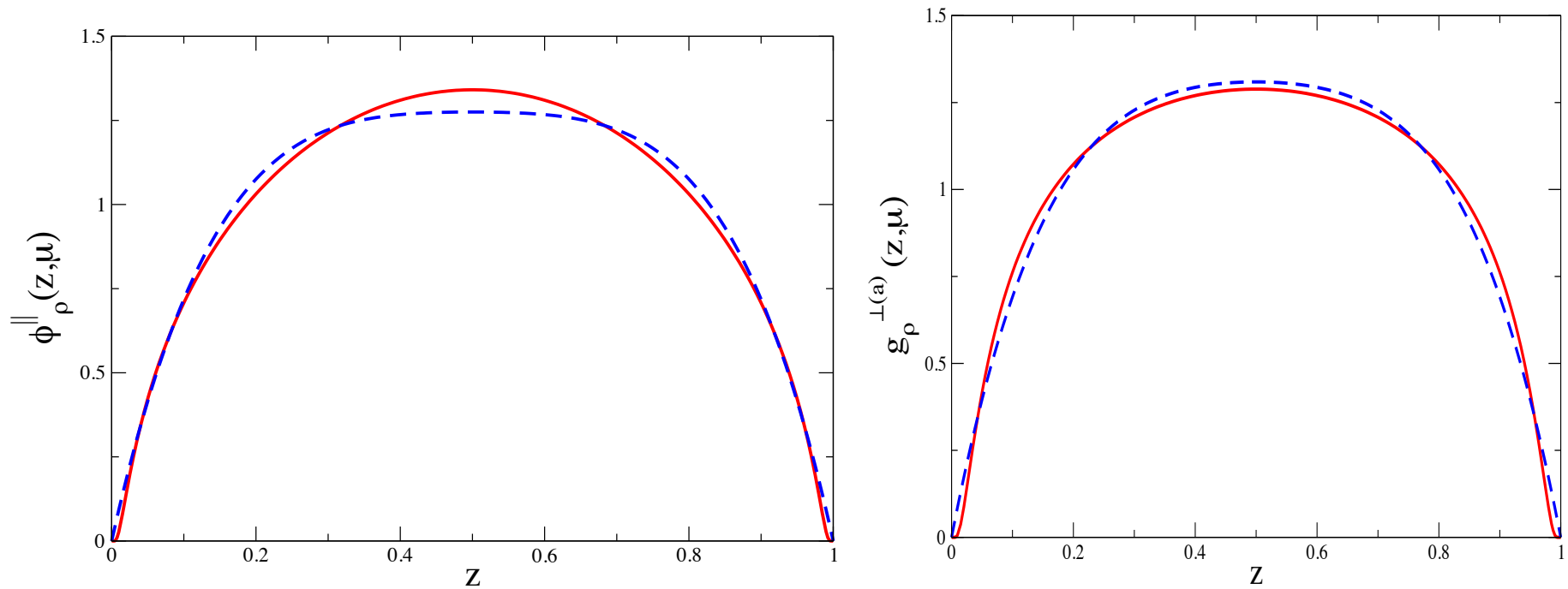
Explicit expressions for SR DAs for the ρ

$$\phi_{\rho}^{\parallel,\perp}(z, \mu) = 6z(1-z) \left[1 + a_2^{\parallel,\perp}(\mu) \frac{3}{2}(5\xi^2 - 1) \right]$$

$$\begin{aligned} g_{\rho}^{\perp(v)}(z, \mu) &= \frac{3}{4}(1 + \xi^2) + \left(\frac{3}{7} a_2^{\parallel}(\mu) + 5\zeta_3(\mu) \right) (3\xi^2 - 1) \\ &+ \left[\frac{9}{112} a_2^{\parallel}(\mu) + \frac{15}{32} \omega_3^{\parallel}(\mu) - \frac{15}{64} \tilde{\omega}_3^{\parallel}(\mu) \right] (3 - 30\xi^2 + 35\xi^4) \end{aligned}$$

Back-up slide 3

Longitudinal twist-2 DA and axial vector twist-3 DA: AdS/QCD Red, SR Blue



Back-up slide 4

Longitudinal twist-2 and vector twist-3 DAs for K^*

