

Probing non perturbative QCD with K_{e4} and $K^\pm \rightarrow \pi^\pm \gamma\gamma$ decays from the NA48/2 and NA62 experiments

Dmitry Madigozhin
(JINR, Dubna)

on behalf of the **NA48/2** and **NA62**
collaborations

DIS 2013

XXI International Workshop on Deep-Inelastic
Scattering and Related Subjects



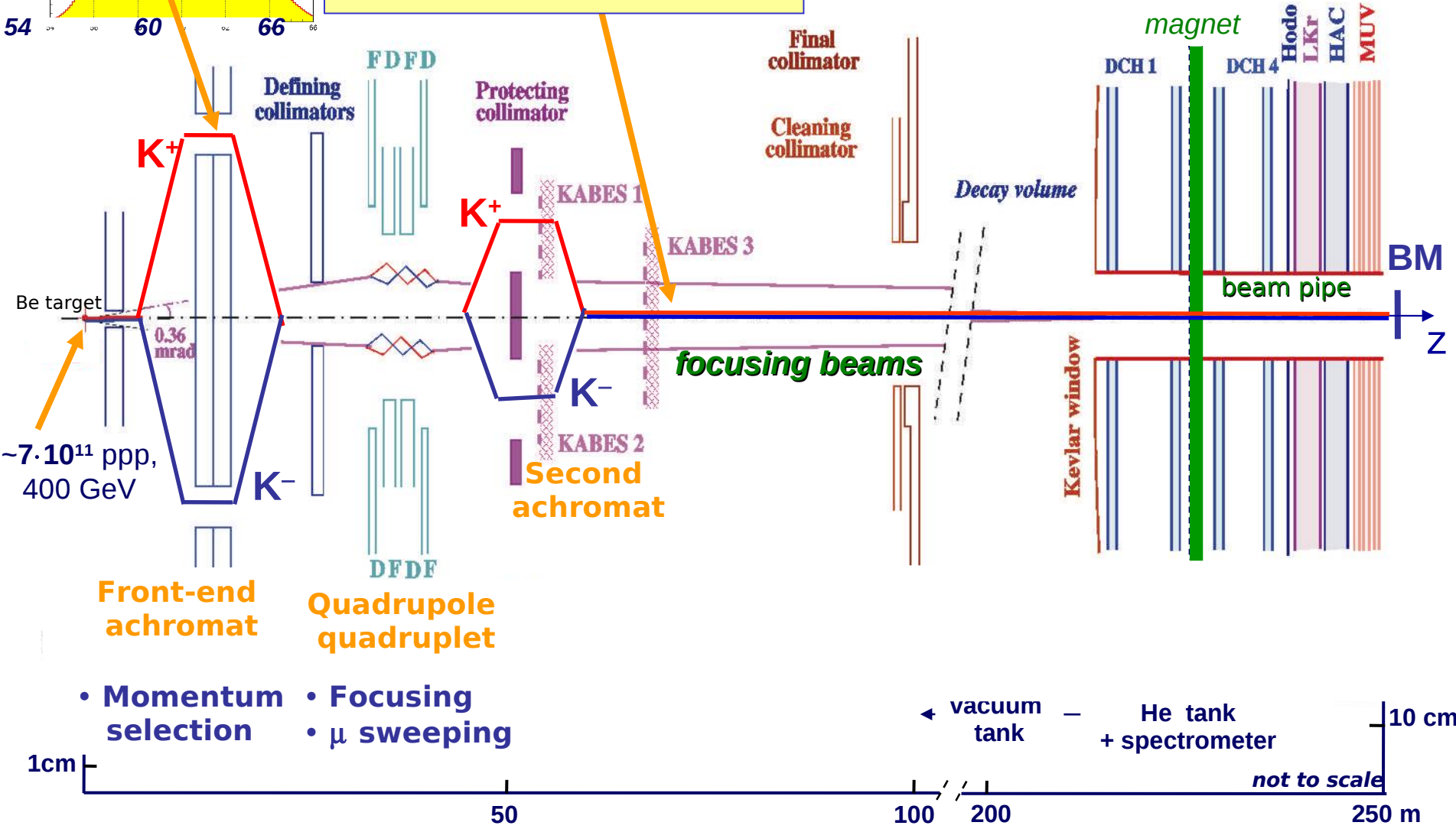
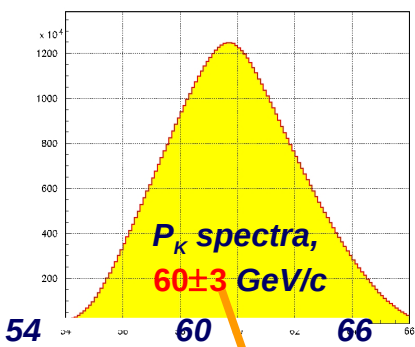
Outline

- Introduction to NA48/2 experiment
- Ke4 : theory
- NA48/2: $\mathbf{K^\pm \rightarrow \pi^+\pi^-e^\pm\nu}$ Form Factors and Branching fraction
- NA48/2: $\mathbf{K^\pm \rightarrow \pi^0\pi^0e^\pm\nu}$ Branching fraction
- NA48/2 and NA62 (Phase I): $\mathbf{K^\pm \rightarrow \pi^+\gamma\gamma}$ study
- Summary and prospects

NA48/2 beam line

2-3M K/spill ($\pi/K \sim 10$),
 π decay products stay in pipe.
 Flux ratio: $K^+/K^- \approx 1.8$

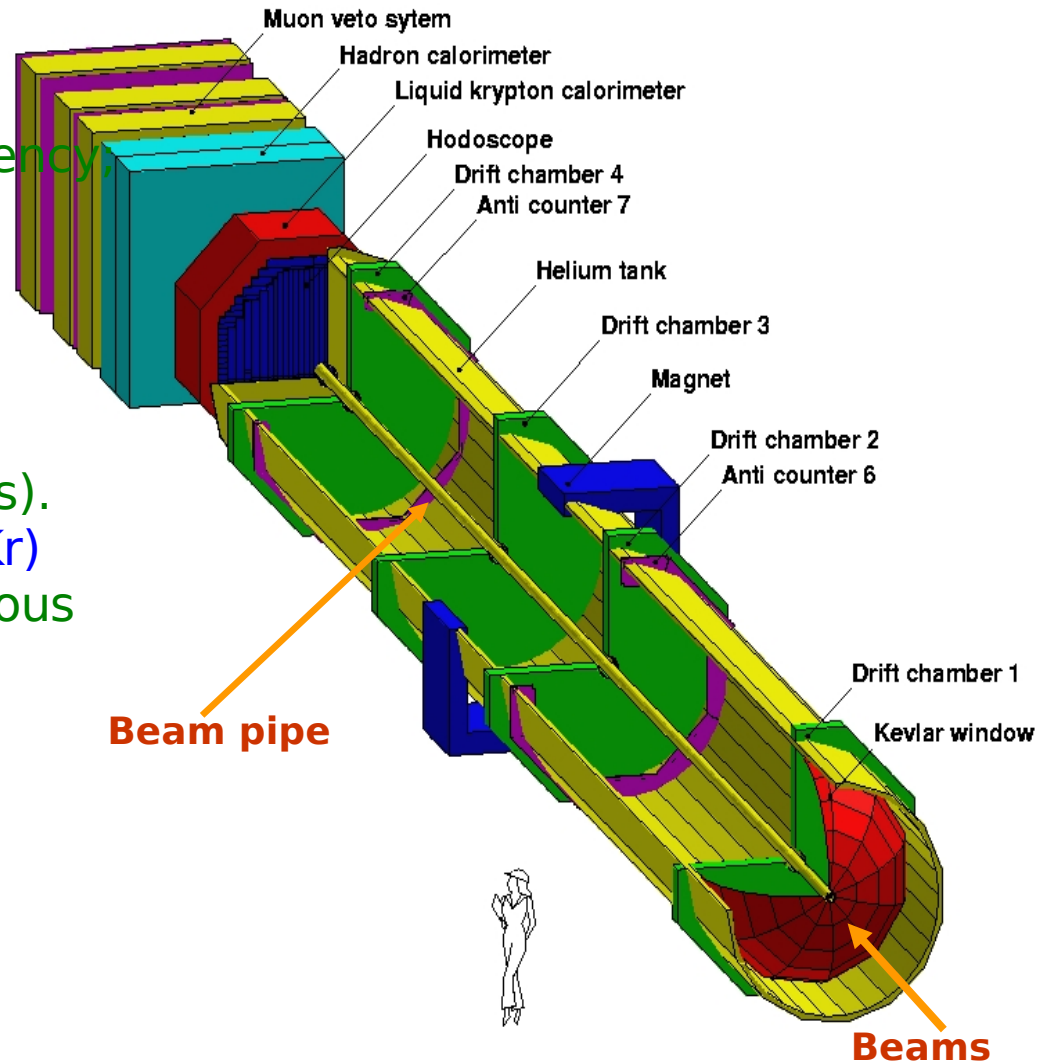
Simultaneous K^+ and K^- beams:
 large charge symmetrization of
 experimental conditions



The NA48 detector

Main detector components:

- Magnetic spectrometer (4 DCHs):
4 views/DCH: redundancy \Rightarrow efficiency;
used in trigger logic;
 $\Delta p/p = 1.0\% \oplus 0.044\%*p$
[p in GeV/c].
- Hodoscope
fast trigger;
precise time measurement (150ps).
- Liquid Krypton EM calorimeter (LKr)
High granularity, quasi-homogenous
 $\sigma_E/E = 3.2\%/E^{1/2} \oplus 9\%/E \oplus 0.42\%$
 $\sigma_x = \sigma_y = 0.42/E^{1/2} \oplus 0.06\text{cm}$
[E in GeV].
(0.15cm@10GeV).
- Hadron calorimeter, muon veto
counters, photon vetoes.



Introduction: K_{e4} amplitude

$K^\pm \rightarrow \pi^+\pi^-e^\pm\nu$ amplitude

is a product of weak leptonic current and (V-A) hadronic current:

$$\frac{G_w}{\sqrt{2}} V_{us}^* \bar{u}_\nu \gamma_\lambda (1 - \gamma_5) v_e \langle \pi^+\pi^- | V^\lambda - A^\lambda | K^+ \rangle, \quad \text{where}$$

$$\begin{aligned} \langle \pi^+\pi^- | A^\lambda | K^+ \rangle = & \frac{-i}{m_K} (F(\mathbf{p}_{\pi^+} + \mathbf{p}_{\pi^-})^\lambda \\ & + G(\mathbf{p}_{\pi^+} - \mathbf{p}_{\pi^-})^\lambda + R(\mathbf{p}_e + \mathbf{p}_\nu)^\lambda) \end{aligned}$$

R enters in the decay rate multiplied by lepton mass squared => this term is negligible for K_{e4}

and

$$\begin{aligned} \langle \pi^+\pi^- | V^\lambda | K^+ \rangle = & \frac{-H}{m_K^3} \epsilon^{\lambda\mu\rho\sigma} (\mathbf{p}_{\pi^+} + \mathbf{p}_{\pi^-} + \mathbf{p}_e + \mathbf{p}_\nu)_\mu \\ & \times (\mathbf{p}_{\pi^+} + \mathbf{p}_{\pi^-})_\rho (\mathbf{p}_{\pi^+} - \mathbf{p}_{\pi^-})_\sigma. \end{aligned}$$

In the above expressions, \mathbf{p} is the four-momentum of each particle, F , G , R are three axial-vector and H one vector complex form factors with the convention $\epsilon^{0123} = 1$.

F, G, R, H form factors (FF) depend on decay Lorentz invariants, so their parameterisation (or some tabulation) is needed to describe data.

Ke4 decays : formalism of $(\pi^+ \pi^-)$ and $(\pi^0 \pi^0)$ modes

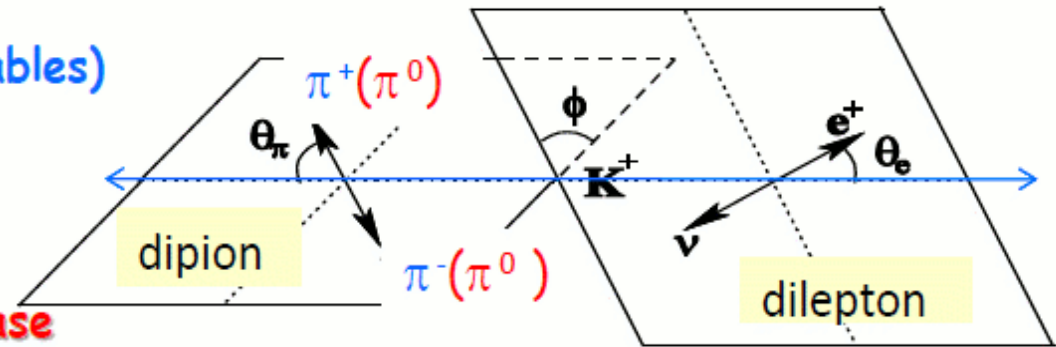
Five kinematic variables (Ca.Ma. variables)

(Cabibbo-Maksymowicz 1965)

$S_\pi (M_{\pi\pi}^2)$, $S_e (M_{e\nu}^2)$, $\cos\theta_\pi$, $\cos\theta_e$ and ϕ

Reduce to 3 variables in the $(\pi^0 \pi^0)$ case

$S_\pi (M_{\pi\pi}^2)$, $S_e (M_{e\nu}^2)$, $\cos\theta_e$



Partial Wave expansion of the amplitude

into s and p waves (Pais-Treiman 1968)

+ Watson theorem (T-invariance) for δ_l^I

$$\delta_0^0 \equiv \delta_s \text{ and } \delta_1^1 \equiv \delta_p$$

F, G = 2 complex Axial Form Factors

$$F = F_s e^{i\delta_s} + F_p e^{i\delta_p} \cos(\theta_\pi)$$

$$G = G_p e^{i\delta_g}$$

H = 1 complex Vector Form Factor

$$H = H_p e^{i\delta_h}$$

Reduces to the single F_s Form Factor

Map the distributions of the Ca.Ma. variables in the **five-dimensional space** with **4 real Form factors** and only **one phase shift**, assuming identical phases for the p-wave Form Factors F_p, G_p, H_p

Dalitz plot density proportional to F_s^2

The fit parameters (real) are :

$$F_s \quad F_p \quad G_p \quad H_p \text{ and } \delta = \delta_s - \delta_p$$

reduce to the only F_s

Ke4(+/-) : $K^\pm \rightarrow \pi^+ \pi^- e^\pm \nu$

Signal ($\pi^+ \pi^- e^\pm \nu$) topology:

- 3 charged tracks, good vertex
- Opposite sign 2π («Right Sign»)
- 1 electron ($E_{\text{LKr}} / P_{\text{DCH}} \sim 1$)

Main background sources: $K \rightarrow 3\pi$

Case of K^+ :

a $K^+ \rightarrow [\pi^+ \text{ misident. as } e^+] \pi^+ \pi^-$

$K^+ \rightarrow [\pi^+ \rightarrow e^+ \nu] \pi^+ \pi^-$

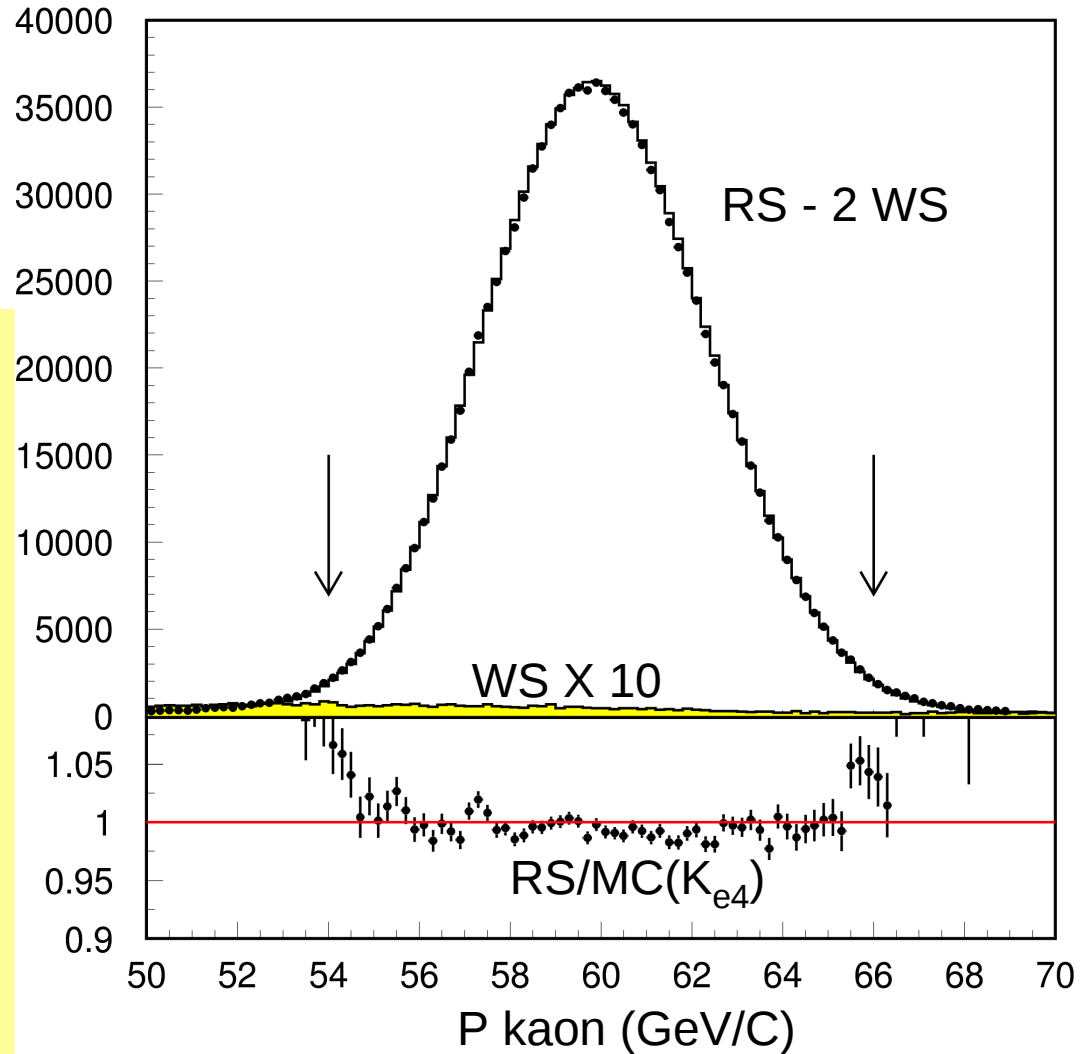
contributes twice more to «Right Sign» events:

(RS = $e^+ \pi^+ \pi^-$, 2 π^+ can decay)

than to «Wrong Sign» ones:

(WS = $e^- \pi^+ \pi^+$, 1 π^- can decay).

b $K^+ \rightarrow [\pi^0 \rightarrow e^+ e^- \gamma] \pi^0 \pi^+$
 misident. lost
 almost negligible

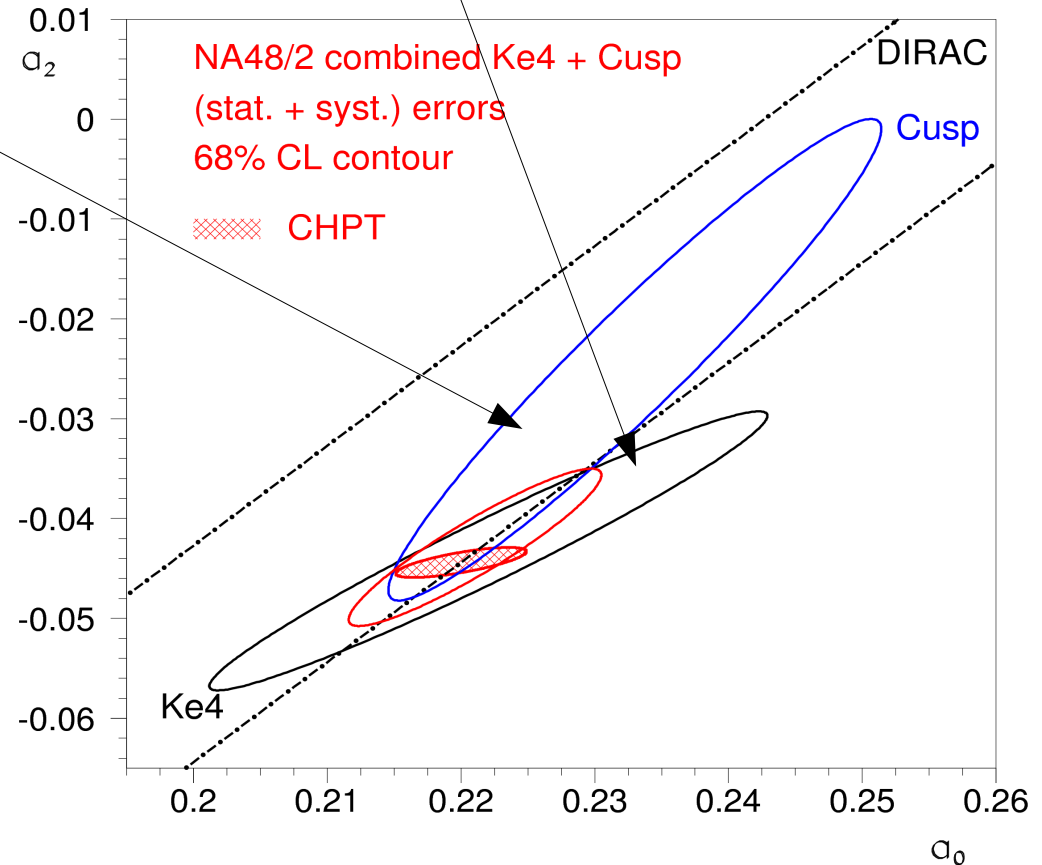
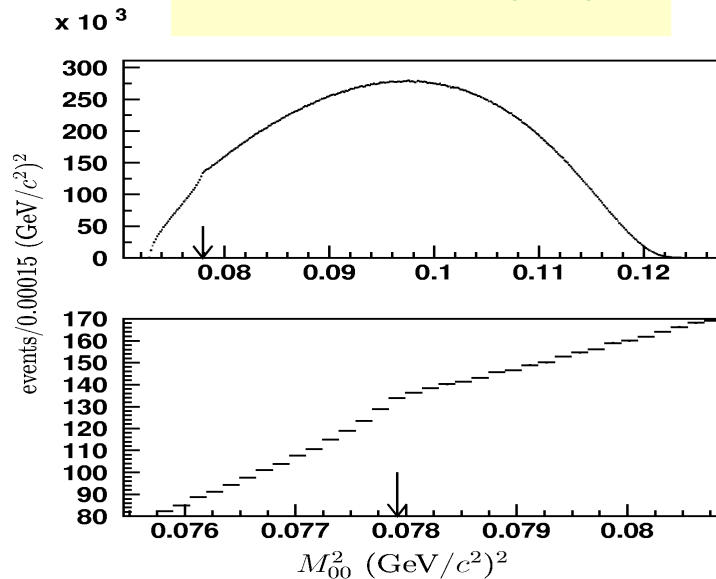


Total background is below 1% ,
 estimated from WS events (contribution **a** is dominant) and checked by MC

$\pi\pi$ scattering lengths measurement from phase shift $\delta(M_{\pi\pi}) = \delta_s - \delta_p$
 [Eur.Phys. C70 (2010) 635]

Cusp in $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

Published in EPJ C64(2009)589



combined $\pi\pi$
 scattering lengths result:

$$a_0^0 = 0.2210 \pm 0.0047_{\text{stat}} \pm 0.0040_{\text{syst}},$$

$$a_0^2 = -0.0429 \pm 0.0044_{\text{stat}} \pm 0.0028_{\text{syst}},$$

$$a_0^0 - a_0^2 = 0.2639 \pm 0.0020_{\text{stat}} \pm 0.0015_{\text{syst}}.$$

Form factors (normalized to f_s)

[Eur.Phys. C70 (2010) 635]

K_{e4} formfactors: fit results

| | value | stat | syst |
|-------------------|-------------|---------------------------|---------------------------|
| f'_s/f_s | = 0.152 | $\pm 0.007_{\text{stat}}$ | $\pm 0.005_{\text{syst}}$ |
| f''_s/f_s | = -0.073 | $\pm 0.007_{\text{stat}}$ | $\pm 0.006_{\text{syst}}$ |
| f'_e/f_s | = 0.068 | $\pm 0.006_{\text{stat}}$ | $\pm 0.007_{\text{syst}}$ |
| f_p/f_s (const) | = -0.048 | $\pm 0.003_{\text{stat}}$ | $\pm 0.004_{\text{syst}}$ |
| g_p/f_s | = 0.868 | $\pm 0.010_{\text{stat}}$ | $\pm 0.010_{\text{syst}}$ |
| g'_p/f_s | = 0.089 | $\pm 0.017_{\text{stat}}$ | $\pm 0.013_{\text{syst}}$ |
| h_p/f_s (const) | = -0.398 | $\pm 0.015_{\text{stat}}$ | $\pm 0.008_{\text{syst}}$ |
| correlations | | | |
| | f''_s/f_s | f'_e/f_s | g_p/f_s |
| f'_s/f_s | -0.954 | 0.080 | g'_p/f_s -0.914 |
| f''_s/f_s | | 0.019 | |

Series expansion with:

- $q^2 = S_\pi/(4m_\pi^2) - 1$
- $S_e/(4m_\pi^2)$

$$F_s^2 = f_s^2 \left(1 + f'_s/f_s q^2 + f''_s/f_s q^4 + f'_e/f_s S_e/4m_\pi^2 \right)^2$$

$$G_p/f_s = g'_p/f_s + g_p/f_s q^2$$

$K_{e4}(+ -)$ branching fraction measurement

[Phys.Lett.B715 (2012) 105]

$$K^{\pm} \rightarrow \pi^+ \pi^- \nu e^{\pm} / K^{\pm} \rightarrow \pi^+ \pi^- \pi^{\pm}$$

$$\text{Br}(K_{e4}) = \text{Br}(K_{3\pi}) \frac{N(K_{e4}) - N(\text{Bkg})}{N(K_{3\pi})} \frac{A(K_{3\pi})}{A(K_{e4})} \frac{\varepsilon(K_{3\pi})}{\varepsilon(K_{e4})}$$

Candidates:

$$N(K_{e4}) = 1\,108\,941 \quad (K^+ : 712\,288, K^- : 396\,653)$$

$$N(\text{bkg}) = 2 \times N(\text{WS events}) = 2 \times 5\,276$$

$$N(K_{3\pi}) = 18\,818\,920 \quad (\text{with negligible background})$$

Acceptance - GEANT3 based simulation:

$$A(K_{3\pi}) = (23.967 \pm 0.010)\%$$

$$A(K_{e4}) = (18.193 \pm 0.004)\%$$

Trigger efficiencies (measured using control triggers):

$$\varepsilon(K_{3\pi}) = (97.65 \pm 0.03)\%$$

$$\varepsilon(K_{e4}) = (98.52 \pm 0.11)\%$$

$$\text{Br}(K_{3\pi}) = (5.59 \pm 0.04)\% \quad (\text{source of } 0.72\% \text{ external error for } \text{Br}(K_{e4}))$$

$K_{e4}(+-)$ branching fraction measurement

| Source | Correction (%) to BR value | Contribution (%) to BR uncertainty |
|--|-------------------------------|---------------------------------------|
| Common to all subsamples | | |
| Acceptance stability | – | 0.18 |
| Muon vetoing efficiency | – | 0.16 |
| Accidental activity | –0.12 | 0.21 |
| Particle identification | – | 0.09 |
| Background estimate | – | 0.07 |
| Radiative events modeling | – | 0.08 |
| Subsample-dependent quoted as a global equivalent | | |
| Trigger efficiency | – | 0.11 |
| Simulation statistics | – | 0.05 |
| Total systematics | –0.12 | 0.37 |
| External error | – | 0.72 |

Relative corrections
and contributions to
uncertainty

$$\Gamma(K_{e4}(+-))/\Gamma(K_{3\pi}) = (7.615 \pm 0.008_{\text{stat}} \pm 0.028_{\text{syst}}) \times 10^{-4}$$

$$\begin{aligned} \text{Br}(K_{e4}(+-)) &= (4.257 \pm 0.004_{\text{stat}} \pm 0.016_{\text{syst}} \pm 0.031_{\text{ext}}) \times 10^{-5} \\ &= (4.257 \pm 0.035_{\text{tot}}) \times 10^{-5} \quad (\text{external error is dominating}) \end{aligned}$$

$$\text{PDG 2012: } (4.09 \pm 0.10_{\text{tot}}) \times 10^{-5}$$

Absolute form factor value (for $|V_{us}| = 0.2252 \pm 0.0009$ from PDG 2012) :

$$F_s(q^2=0, S_e=0) = 5.705 \pm 0.003_{\text{stat}} \pm 0.017_{\text{syst}} \pm 0.031_{\text{ext}}$$

Ke4(00) : $K^\pm \rightarrow \pi^0 \pi^0 \nu e^\pm$

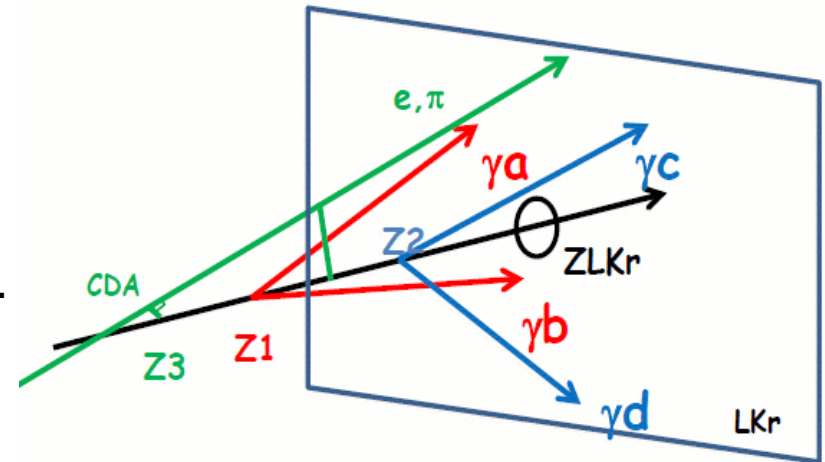
Preliminary

$K^\pm \rightarrow \pi^0 \pi^0 \nu e^\pm$ relative to $K^\pm \rightarrow \pi^0 \pi^0 \pi^\pm$ with $Br = (1.761 \pm 0.022)\%$

Common part of event reconstruction:

Find LKr γ -cluster pairs (ab) and (cd)
in-time (± 2.5 ns), $E > 3$ GeV

- Decay positions Z_1 and Z_2 assuming $\pi^0 \rightarrow \gamma\gamma$.
- $Z_n = (Z_1 + Z_2)/2$ within $(-16, +90)$ m
- $D_{Z_n} = |Z_1 - Z_2| < 500$ cm



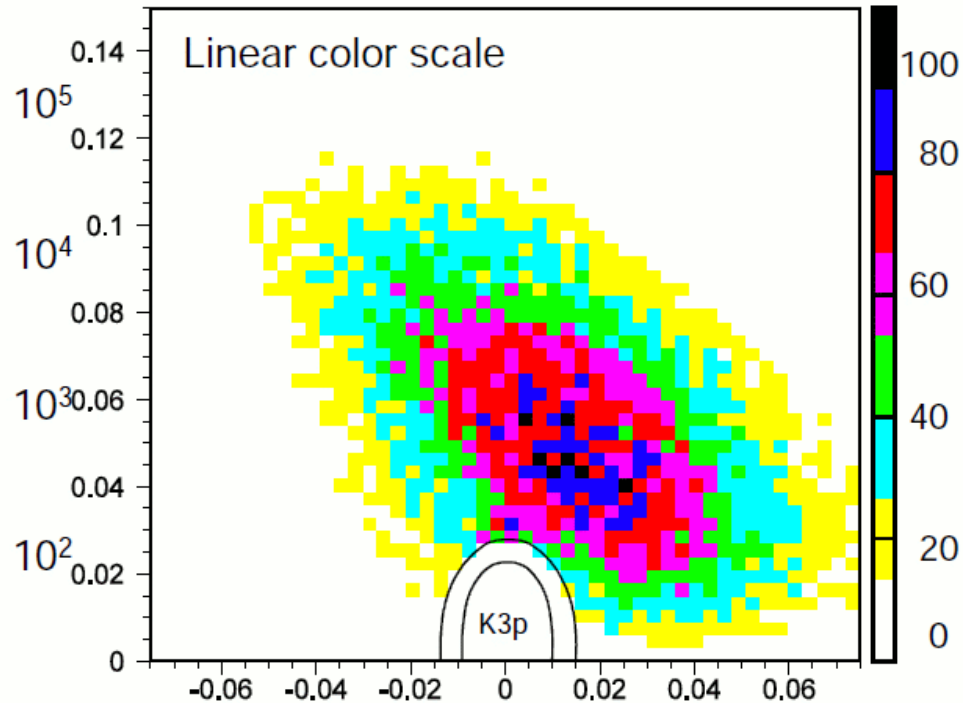
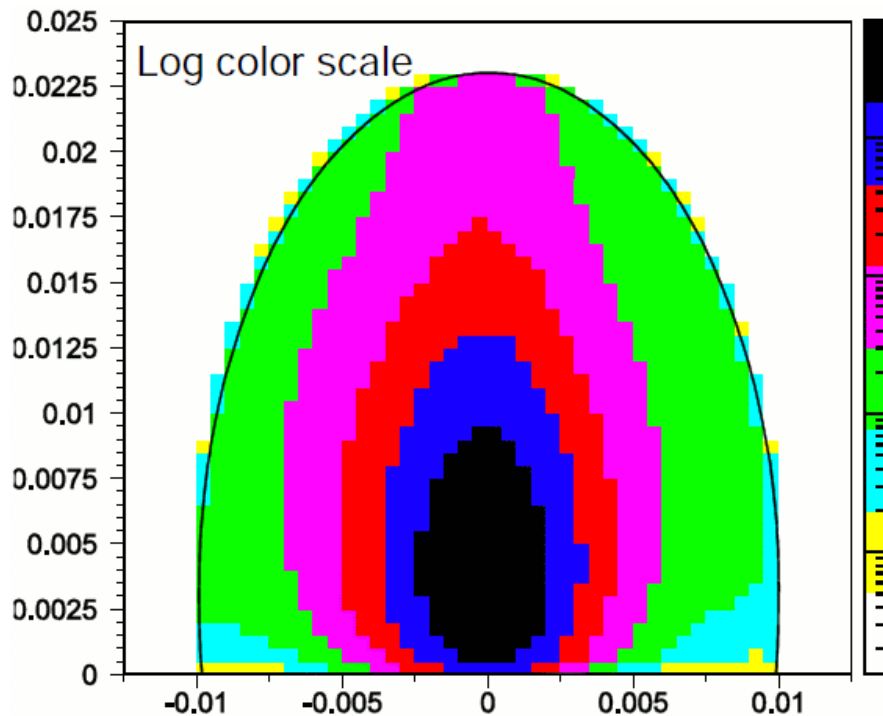
Combined with charged track (Z_3 at CDA to beam line) if:

- $D_Z = |Z_3 - Z_n| < 800$ cm

$K_{e4}(00)$ signal selection

- Assign m_π to the charged track, plot P_t (to beam) vs invariant mass
- Cut $K_{3\pi}$ events with a small P_t and \sim kaon PDG mass

Elliptic cut separates $\sim 70 \times 10^6$ $K_{3\pi}$ from ~ 45000 K_{e4} candidates



$P_t(\text{GeV}/c)$ vs $(M_{3\pi} - M_K)$ (GeV/c²)

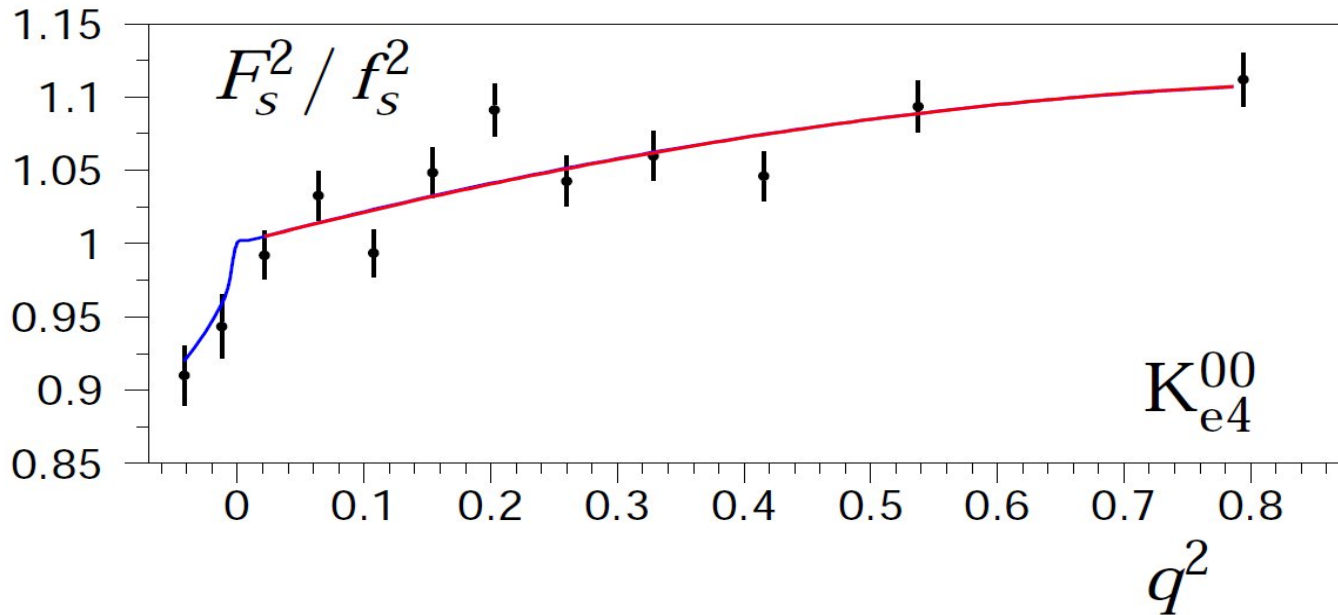
$K_{e4}(00)$ background rejection

Electron identification:

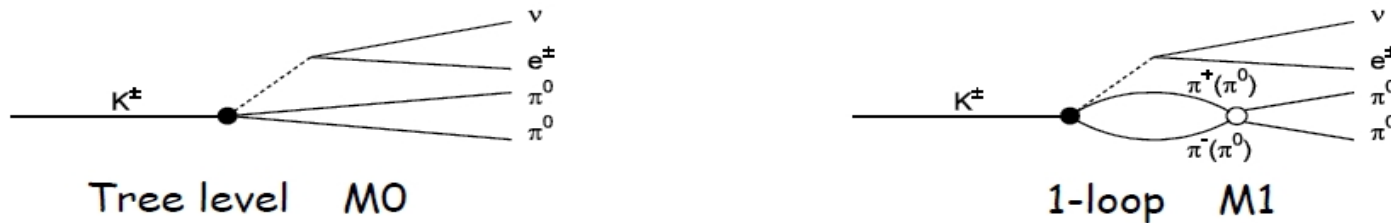
- LKr cluster associated to track is in-time (10 ns) with track and $2\pi^0$
 - $E(\text{LKr})/P(\text{DCH}) \sim 1$ [0.9-1.1]
 - Extra rejection using a dedicated **discriminant variable**. It is a linear combination of variables related to shower properties and trained on real and fake electrons from data.
-
- Fake-electron background ($K \rightarrow \pi^0 \pi^0 \pi^+$) 1.3%
 - Real electron background ($K \rightarrow \pi^0 \pi^0 \pi^+$; $\pi \rightarrow e\nu$) 0.1%

Kaon momentum reconstruction imposing energy-momentum conservation and zero neutrino mass.

$K_{e4}(00)$ Form Factor



1-loop calculation for 3π decays: Cabibbo, PRL 93(2004)121801



Above threshold: $|M|^2 = |M0 + i M1|^2 = M0^2 + M1^2$

Below threshold: $|M|^2 = |M0 + M1|^2 = M0^2 + M1^2 + 2 M0 M1$

$q^2 = S_{\pi}/4m_{\pi^+}^2 - 1$ $\sigma_{\pi} = \sqrt{(4m_{\pi^+}^2/S_{\pi} - 1)} = \sqrt{(|q^2|/(1+q^2))}$

$M0 =$ unperturbed amplitude: $F_s = f_s (1 + a q^2 + b q^4 + c S_{\pi}/4m_{\pi^+}^2)$

$M1 =$ scattering amplitude: $- 2/3 (a_0 - a_2) f_s \sqrt{(|q^2|/(1+q^2))}$

$K_{e4}(00)$: Br measurement

Br is measured in independent subsamples and then combined.

$$N(K_{e4} \text{ candidates}) = 44909$$

$$N(\text{bkg}) = 598$$

$$N(K_{3\pi} \text{ candidates}) = 70.98 \text{ M}$$

$$\text{Acceptances: } A(K_{e4}) = 1.77\% \quad A(K_{3\pi}) = 4.11\%$$

$$\text{Trigger efficiency } \varepsilon(K_{e4}) = 92\text{-}98\% \text{ (ratio to } K_{\pi3} \sim 1)$$

$$\text{Normalization: } \text{Br}(K_{3\pi}) = (1.761 \pm 0.022)\% \text{ - source of external error}$$

Systematic Uncertainty (%)

| | |
|-----------------|------|
| Background | 0.35 |
| Simulation stat | 0.12 |
| FF dependence | 0.20 |
| Rad. Corr. | 0.23 |
| Trigger | 0.80 |
| Ident. of e | 0.10 |
| Beam geometry | 0.10 |

Total **0.94**

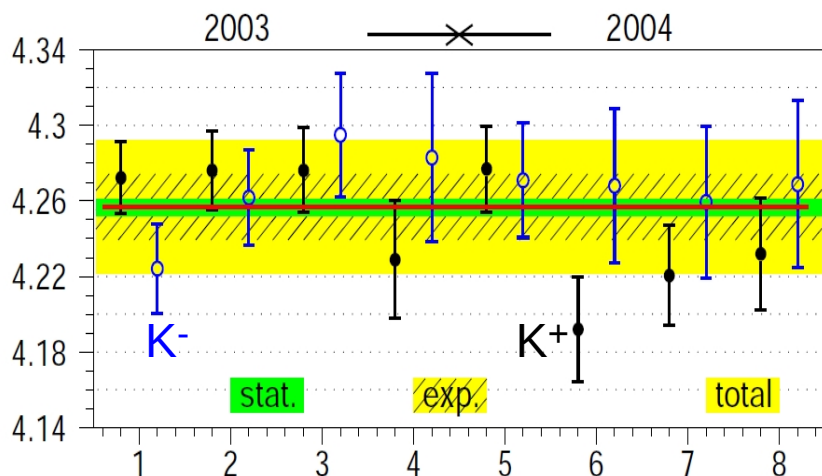
$$\text{Br}(K_{e4}^{00}) =$$

$$(2.595 \pm 0.012_{\text{stat}} \pm 0.024_{\text{syst}} \pm 0.032_{\text{ext}})10^{-5}$$

$$\text{PDG 2012 : } (2.2 \pm 0.4) 10^{-5}$$

Ke4 Br measurement in statistically independent subsamples

all in units of 10^{-5}



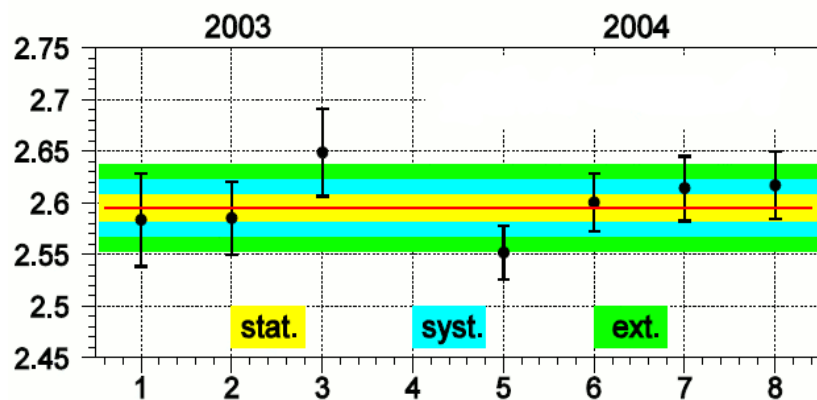
Phys.Lett. B715 (2012) 105:

$K_{e4}(+-)$ normalized to $K_{3\pi}(+-)$

$$(4.257 \pm 0.004 \pm 0.016 \pm 0.031) =$$

Stat Syst Ext

$$(4.257 \pm 0.035) \quad 0.8\% \text{ rel.err.}$$



Preliminary:

$K_{e4}(00)$ normalized to $K_{3\pi}(00)$

$$(2.595 \pm 0.012 \pm 0.024 \pm 0.032) =$$

Stat Syst Ext

$$(2.595 \pm 0.042) \quad 1.6\% \text{ rel.err.}$$

K[±] → π[±]γγ

- Dependence on a single parameter \hat{c} at O(p⁴) and O(p⁶)

$$\frac{\partial \Gamma}{\partial y \partial z}(\hat{c}, y, z) = \frac{m_K}{2^9 \pi^3} \left[z^2 \left(|A(\hat{c}, z, y^2)|^2 + |B(z)|^2 + |C(z)|^2 \right) + \left(y^2 - \frac{1}{4} \lambda(1, r_\pi^2, z) \right)^2 |B(z)|^2 \right]$$

where $z = \left(\frac{m_{\gamma\gamma}}{m_K}\right)^2$, $y = \frac{p(q_1 - q_2)}{m_K^2}$

p, q₁, q₂ : K[±], γ, γ momenta

loop contribution

pole contribution

loop O(p⁶)

Experimental status:

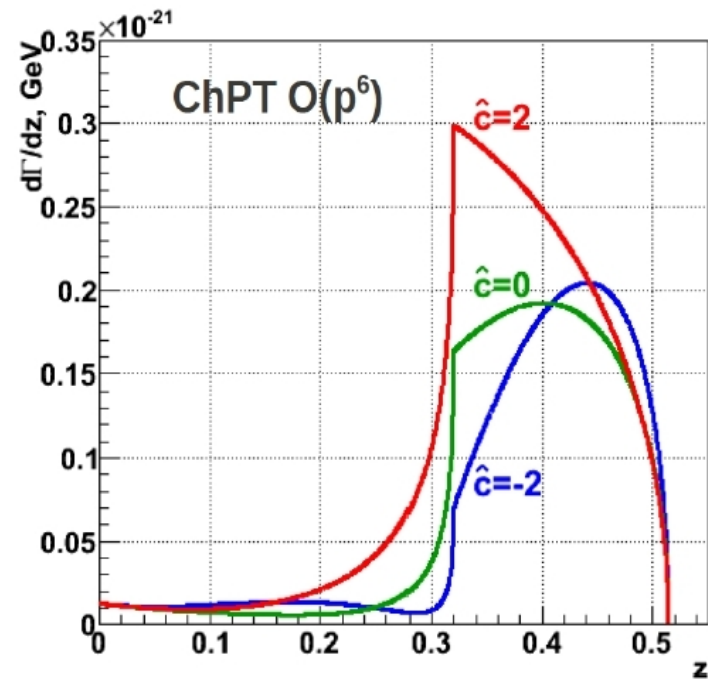
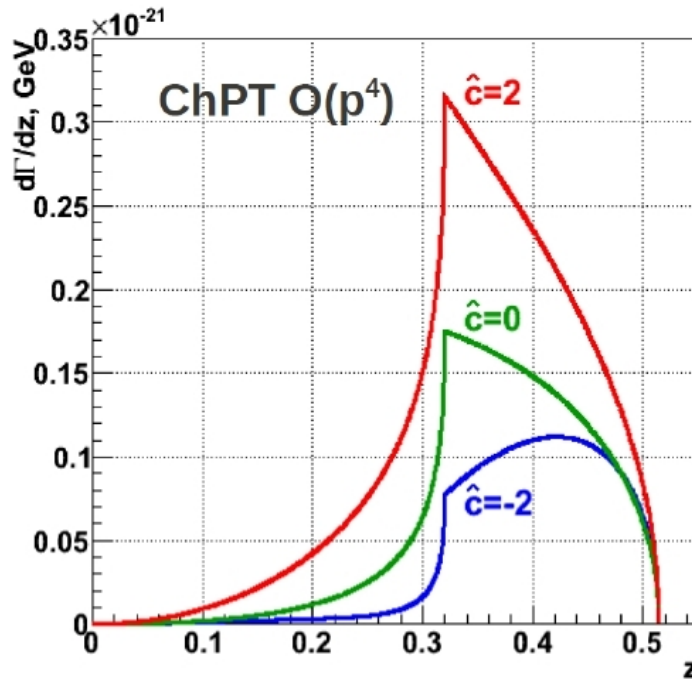
E787
[PRL 79 (1997) 4079]:

Br = (1.1 ± 0.3) 10⁻⁶

31 cand. , 5 est. bkg.

$\hat{C} = 1.1 \pm 0.6$ for O(P⁴)

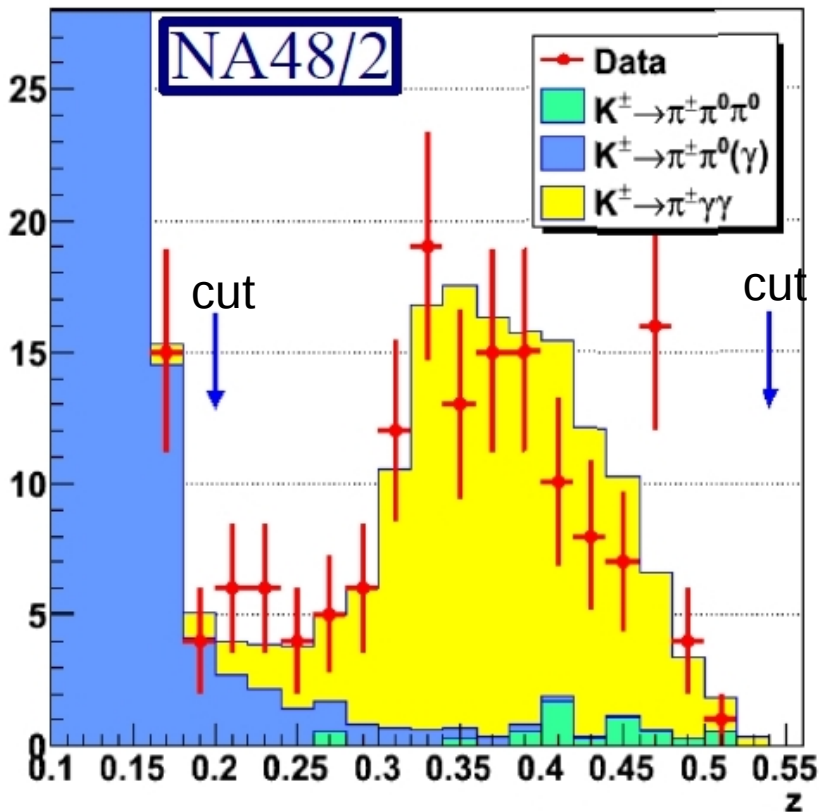
$\hat{C} = 1.8 \pm 0.6$ for O(P⁶)



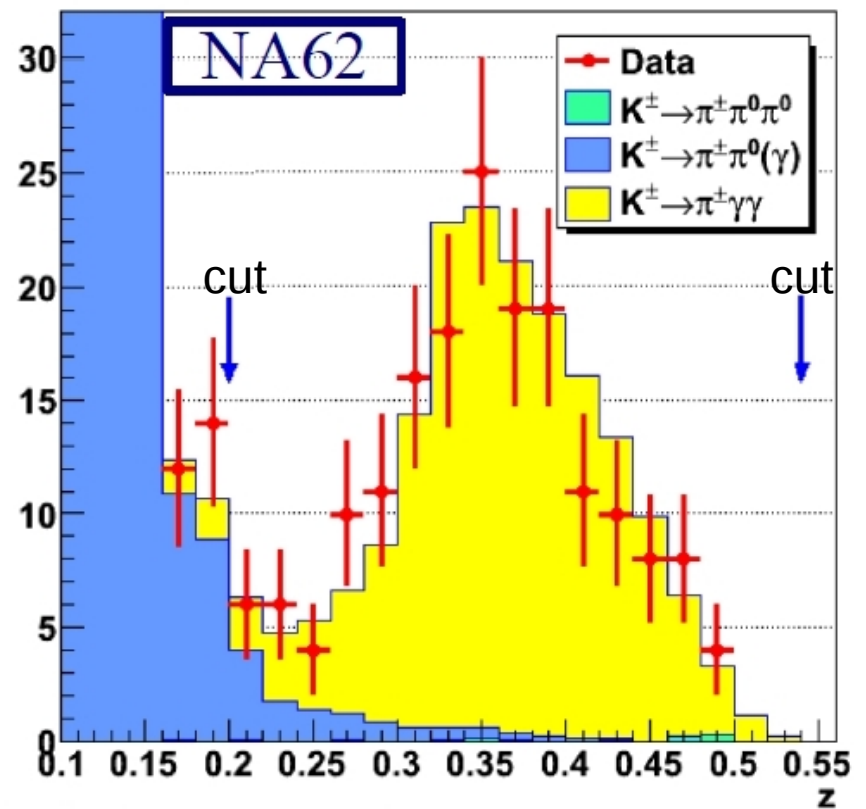
Cusp at $m_{\gamma\gamma} = 2m_\pi$ threshold

$K^\pm \rightarrow \pi^\pm \gamma \gamma$

- NA48/2 2004 data (3 days special minimum bias run)
- NA62 (phase I) 2007 data (3 month control min. bias trigger downscaled by 20)



$\pi^\pm \gamma \gamma$ cand. 147
 $\pi^\pm \pi^0 \gamma$ 11.0 ± 0.8
 $\pi^\pm \pi^0 \pi^0$ 5.9 ± 0.7
 Signal $\pi^\pm \gamma \gamma$ 130 ± 12



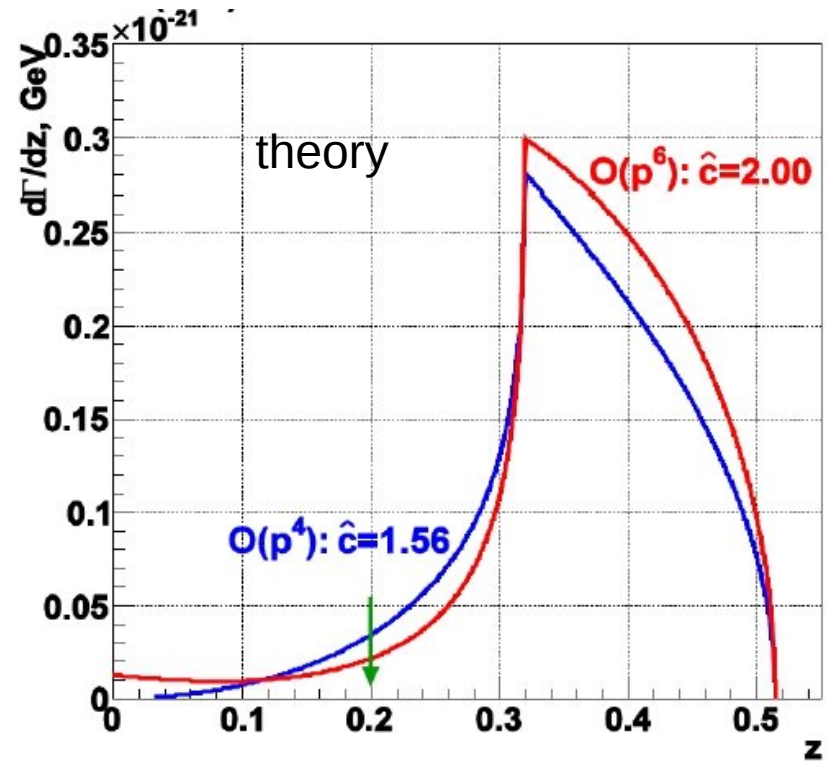
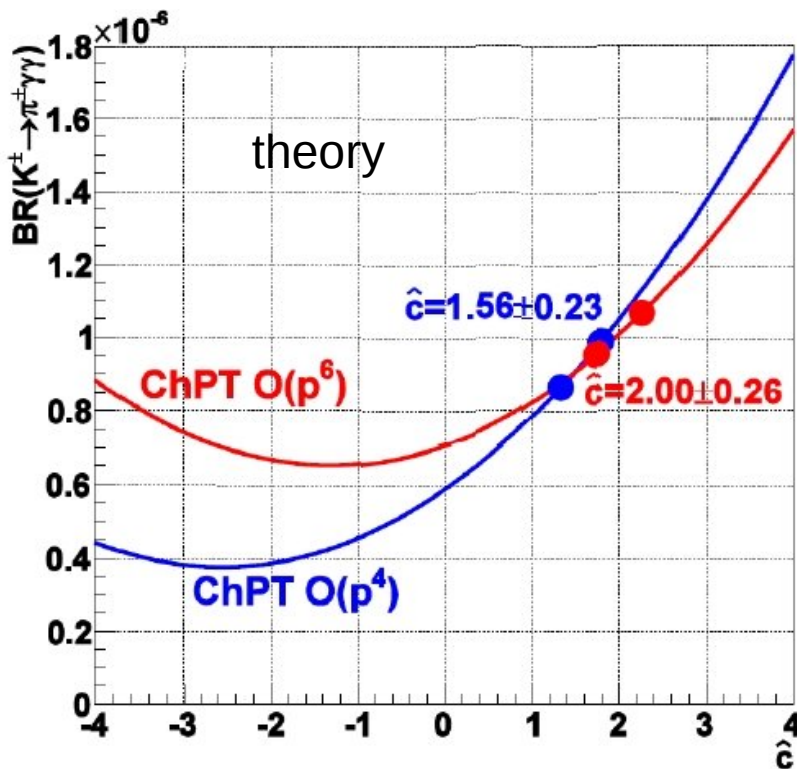
$\pi^\pm \gamma \gamma$ cand. 175
 $\pi^\pm \pi^0 \gamma$ 11.1 ± 1.0
 $\pi^\pm \pi^0 \pi^0$ 1.3 ± 0.3
 Signal $\pi^\pm \gamma \gamma$ 163 ± 13

$K^\pm \rightarrow \pi^\pm \gamma \gamma$

Combined NA48/2 and NA62 preliminary result, based on almost 300 events (10 times the present world sample):

$$\hat{c} \text{ for } O(p^4) = (1.56 \pm 0.22 \text{stat} \pm 0.07 \text{syst}) = 1.56 \pm 0.23$$

$$\hat{c} \text{ for } O(p^6) = (2.00 \pm 0.24 \text{stat} \pm 0.09 \text{syst}) = 2.00 \pm 0.26$$



Both approximations for this Z spectrum predict very similar Br values.

Measured Br for $O(p^6) = (1.01 \pm 0.06) \cdot 10^{-6}$: Preliminary!

Summary and future prospects

- **1.11 millions** of reconstructed $K^{\pm} \rightarrow \pi^+ \pi^- \nu e^{\pm}$ ($K_{e4}(+-)$) and **~45000** of $K^{\pm} \rightarrow \pi^0 \pi^0 \nu e^{\pm}$ ($K_{e4}(00)$) decays (2003+2004 data).
- Improved branching fractions:
 $\text{Br } K_{e4}(+-) = (4.257 \pm 0.035) \cdot 10^{-5}$ [Phys.Lett. B715 (2012) 105] (3 times better/PDG)
 $\text{Br } K_{e4}(00) = (2.595 \pm 0.042) \cdot 10^{-5}$ [preliminary] (10 times better/PDG)
- $K_{e4}(00)$ F_s form factor variation with q^2 looks similar to $K_{e4}(+-)$ one above $2m_{\pi^+}$ threshold. Deficit below can be due to pions rescattering.
- Prospects: the observation of several 1000 decays in similar $K_{\mu 4}(00)$ (never observed) and $K_{\mu 4}(+-)$ (7 events observed).
- **Preliminary** result for $\pi^{\pm} \gamma \gamma$
 \hat{C} for $O(p^4) = 1.56 \pm 0.23$; \hat{C} for $O(p^6) = 2.00 \pm 0.26$;
 $\text{Br}(\pi^{\pm} \gamma \gamma)$ for $O(p^6) = (1.01 \pm 0.06) \cdot 10^{-6}$