

Revising the Impact-Parameter dependent Saturation model with combined HERA data

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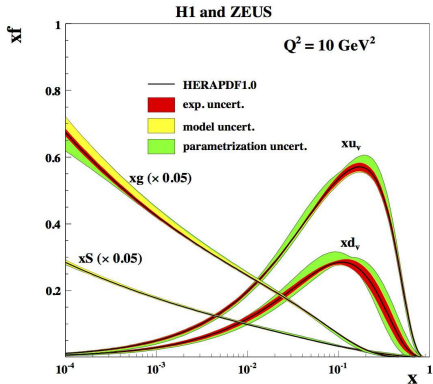
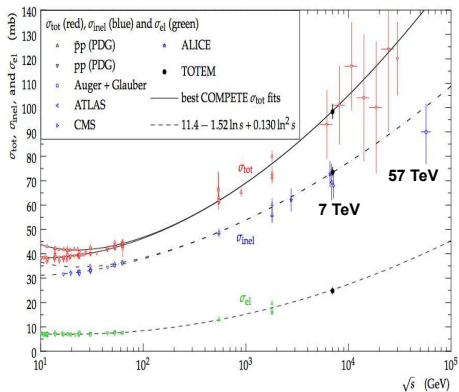
XXI. International Workshop on Deep-Inelastic Scattering and Related Subjects (DIS 2013)

- Motivation, why color dipole approach at small- x ?
- The importance of impact-parameter dependence of dipole amplitude.
- Fitting the model parameters with the recent H1+ZEUS combined data for σ_r .
- Confronting the model's results with all available data at $x < 0.01$ for $F_2, F_L, F_2^{c\bar{c}}$, and also exclusive diffractive & DVCS data.

This talk is based on:

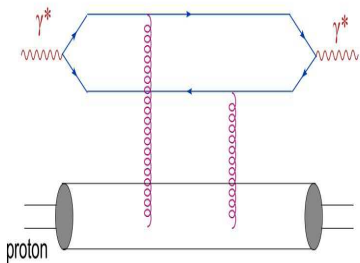
Rezaeian, Siddikov, Van de Klundert, Venugopalan, **PRD 87**, 034002 (2013) [arXiv:1212.2974].

Growth of the gluon distribution at small-x, where do gluons go?



• Unitarity or Froissart bound: $\sigma_{tot} < c \ln^2(s)$: Gluon saturation at small-x

Connection between unitarization and saturation: Kovner & Wiedemann, hep-ph/0112140

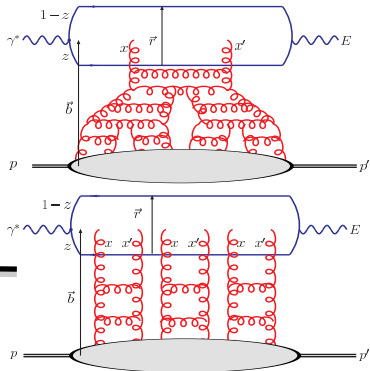


$$T(x, r, b) \simeq \alpha_s r^2 \frac{xG(x, 1/r^2)}{\pi R^2} \equiv \alpha_s n(x, Q^2 \sim 1/r^2)$$

Unitarization



This talk



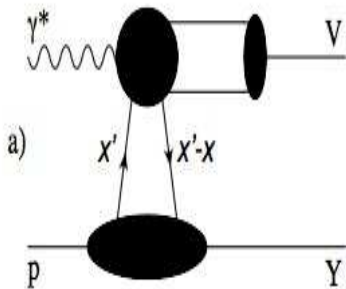
Strong scattering $T \sim 1 \iff$ High gluon density $n \sim 1/\alpha_s \implies$ gluon saturation

To preserve unitarity \iff Multiple scattering is important: $(\alpha_s n)^n \sim 1$

Inclusive and exclusive (diffractive vector meson production and DVCS)

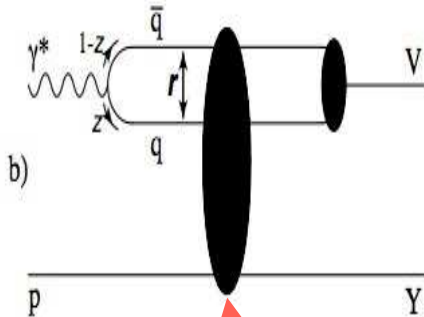
processes : $\gamma^* + p \rightarrow V + p$ with $V = J/\psi, \rho, \phi, \gamma, \gamma^*$

Collinear factorization (GPD+DGLAP)



$$GPD_{i/p} \otimes H_{ij} \otimes \Psi_j^V$$

Color dipole factorization (dipole + small-x evolution)



$$\psi_{q\bar{q}}^\gamma \otimes \mathcal{N}^{q\bar{q}-p} \otimes \phi_{q\bar{q}}^V$$

Exclusive diffractive process: $\psi_{q\bar{q}}^\gamma \otimes \phi_{q\bar{q}}^V \otimes \mathcal{N}^{q\bar{q}-p}$

$$\mathcal{A}_{T,L}^{\gamma^* p \rightarrow V p}(x, Q, \Delta) = 2i \int d^2\mathbf{r} \int_0^1 dz \int d^2\mathbf{b} (\Psi_E^* \Psi)_{T,L} e^{-i[\mathbf{b} - (1-z)\mathbf{r}] \cdot \Delta} \mathcal{N}(x, r, b)$$

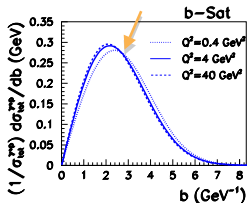
$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow E p}}{dt} = \frac{1}{16\pi} \left| \mathcal{A}_{T,L}^{\gamma^* p \rightarrow E p} \right|^2 \quad (r \rightarrow Q) \text{ and } (b \rightarrow \Delta) \text{ with } t = -\Delta^2$$

- With corrections from the real part of the amplitude and from skewedness $x \neq x'$ [Shuvaev et al., hep-ph/9902410].

Inclusive deep-inelastic scattering (DIS)

$$\begin{aligned} \sigma_{L,T}^{\gamma^* p}(Q^2, x) &= \text{Im} \mathcal{A}_{L,T}^{\gamma^* p \rightarrow \gamma^* p}(x, Q, \Delta = 0) \\ &= 2 \sum_f \int \int d^2b d^2r \int_0^1 dz |\Psi_{L,T}^{(f)}(r, z; Q^2)|^2 \mathcal{N}(x, r, b) \end{aligned}$$

Importance of impact-parameter dependence of dipole amplitude

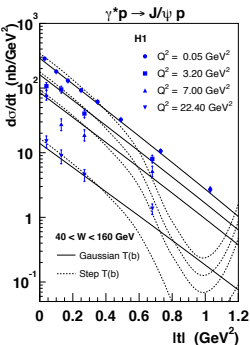


- Saturation scale strongly depends on impact-parameter.

Median values of b are between 2 and 3 GeV².

Kowalski, Motyka, Watt [hep-ph/0606272]

Watt, Kowalski [0712.2670].

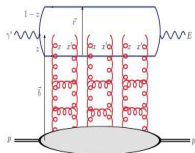


- $\sigma_{q\bar{q}} = 2 \int d^2\mathbf{b} \mathcal{N}(\mathbf{x}, \mathbf{r}, \mathbf{b})$

Any factorizable step-like impact-parameter profile $T(b) = \theta(R_p - b)$ is ruled out by diffractive data.

$$\sigma_{q\bar{q}} = 2 \int d^2\mathbf{b} \mathbf{T}(\mathbf{b}) \mathcal{N}(\mathbf{x}, \mathbf{r}) = \sigma_0 \mathcal{N}(\mathbf{x}, \mathbf{r})$$

- $T(b)$ can be fixed by a simultaneous description of t-distribution of exclusive diffractive and inclusive processes



- Kowalski, Teaney [hep-ph/0304189]
- Kowalski, Motyka, Watt [hep-ph/0606272]
- Rezaeian, Siddikov, Van de Klundert, Venugopalan [arXiv:1212.2974]

- Eikonalized DGLAP-evolved gluon density with Gaussian b dependence (Glauber-Mueller amplitude):

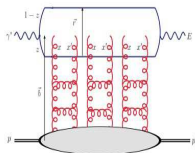
$$\mathcal{N}(x, r, b) = 1 - \exp\left(-\frac{\pi^2 r^2}{2N_c} \alpha_s(\mu^2) xg(x, \mu^2) T_G(b)\right)$$

$$T_G(b) = \frac{1}{2\pi B_G} \exp(-b^2/2B_G)$$

The IP-Sat dipole amplitude gives at large Q^2 (or small r):

$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow Ep}}{dt} \approx e^{-B_G|t|}$$

- Supported by data from t -distribution of exclusive vector meson & DVCS.



$$\mathcal{N}(x, r, b) = 1 - \exp\left(-\frac{\pi^2 r^2}{2N_c} \alpha_s(\mu^2) xg(x, \mu^2) T_G(b)\right)$$

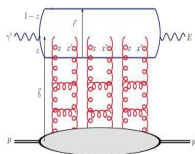
$$T_G(b) = \frac{1}{2\pi B_G} \exp(-b^2/2B_G)$$

- with a scale related to dipole size, and initial gluon distribution:

$$\mu^2 = C/r^2 + \mu_0^2,$$

$$xg(x, \mu_0^2) = A_g x^{-\lambda_g} (1-x)^{5.6}$$

- 4 free parameters: B_G is fixed from t-slope of exclusive J/Ψ production; and A_g, μ_0, λ_g are fixed by DIS **combined data for σ_r for $x \leq 0.01$ and $Q^2 \in [0.75, 650] \text{ GeV}^2$.**
- Data for F_2, F_L and $F_2^{c\bar{c}}$, exclusive diffractive (for ρ and ϕ) and DVCS are **NOT** included into the fit, but are predictions of the model.



$$\mathcal{N}(x, r, b) = 1 - \exp\left(-\frac{\pi^2 r^2}{2N_c} \alpha_s(\mu^2) xg(x, \mu^2) T_G(b)\right)$$

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- with a scale related to dipole size, and initial gluon distribution:

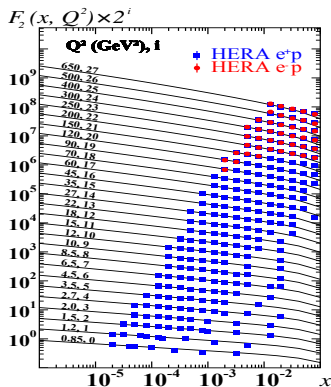
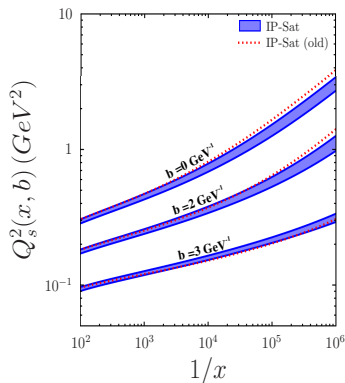
$$\mu^2 = C/r^2 + \mu_0^2, \quad xg(x, \mu_0^2) = A_g x^{-\lambda_g} (1-x)^{5.6}$$

B_G/GeV^2	$m_{u,d,s}/\text{GeV}$	m_c/GeV	μ_0^2/GeV^2	A_g	λ_g	$\chi^2/\text{d.o.f.}$
4	≈ 0	1.27	1.51	2.308	0.058	298.89/259 = 1.15
4	≈ 0	1.4	1.428	2.373	0.052	316.61/259 = 1.22

old v. new fit obtained from combined H1+ZEUS data

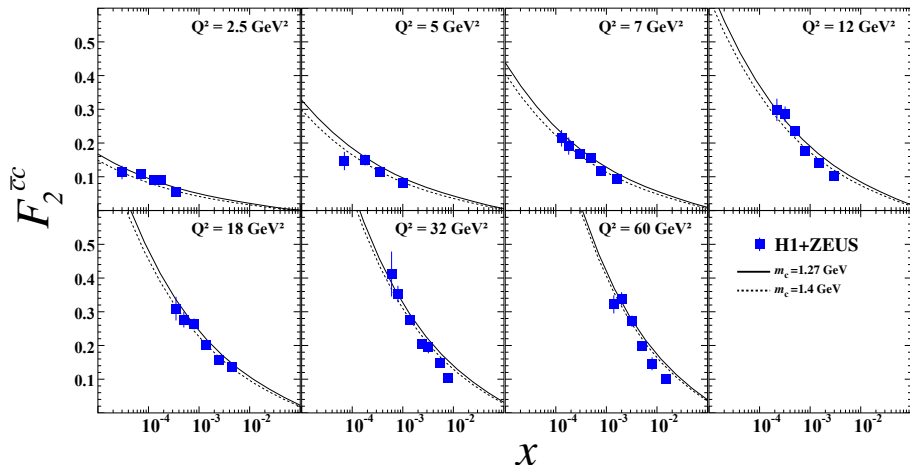
- Old IP-Sat parameters & combined σ_r data: $\chi^2/\text{d.o.f.} \approx 3 \rightarrow$ parameters of new fit are different.
 - Old IP-Sat: $m_{u,d,s} = 50 - 100 \text{ MeV}$, and $\lambda_g < 0$.
 - New IP-Sat: $m_{u,d,s} = 0$, and $\lambda_g > 0 \rightarrow$ makes more sense at small- x !

Saturation (IP-Sat) description of recent combined HERA data



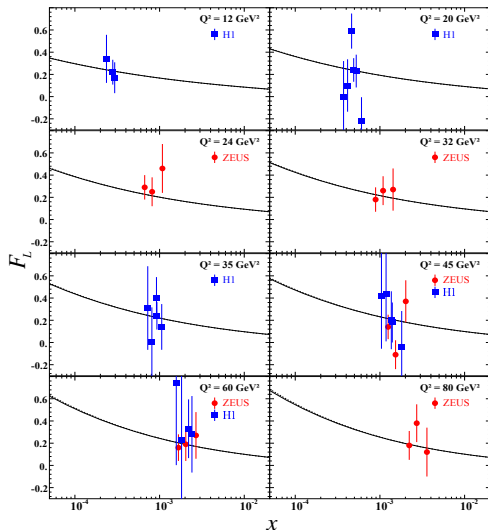
- Saturation scale extracted from **old** and **new** combined data have similar trend although parameters of the model change significantly.
- $Q_s(x, b) < 1$ GeV at HERA kinematics.
- The power-law behavior of $Q_s^2 \approx x^{-\lambda}$ changes from $\lambda \approx 0.3$ (central) to $\lambda \approx 0.1$ (peripheral).

CGC description of recent combined HERA data: Charm structure function

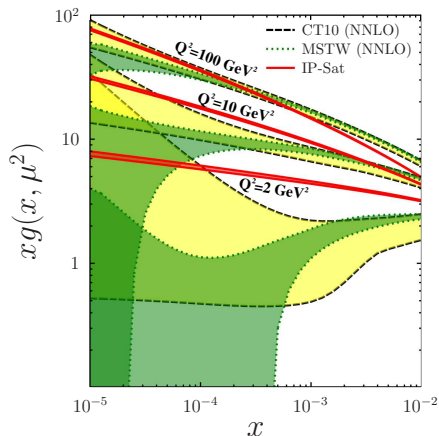


- $F_2^{c\bar{c}}$ data (combined from HERA) not included in the fit!
- Theoretical uncertainties are due to charm mass: $1.27 \leq m_c \leq 1.4 \text{ GeV}$.

CGC description of recent combined HERA data: F_L structure function

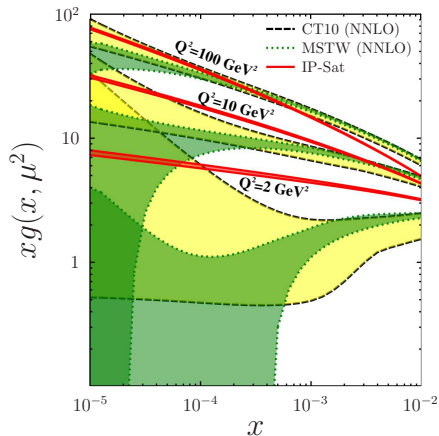


● F_L data not included in the fit (Combined data are not yet available).



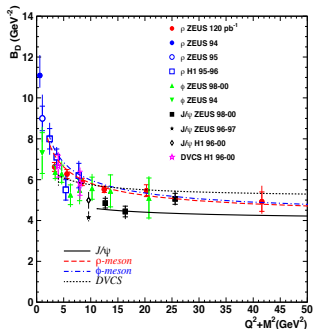
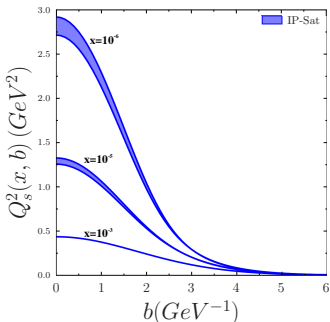
In the Color dipole (or CGC) approach:

- Ground state constructed from classical color field background + Non-linear gluon saturation effect (small- x resummation) \rightarrow stable results at small- x .



- In IP-Sat model we have **only 4 free parameters** fixed by low- x data \rightarrow better constrains on parameters \rightarrow smaller errors (mainly due to charm mass)
- At large Q^2 two pictures match.

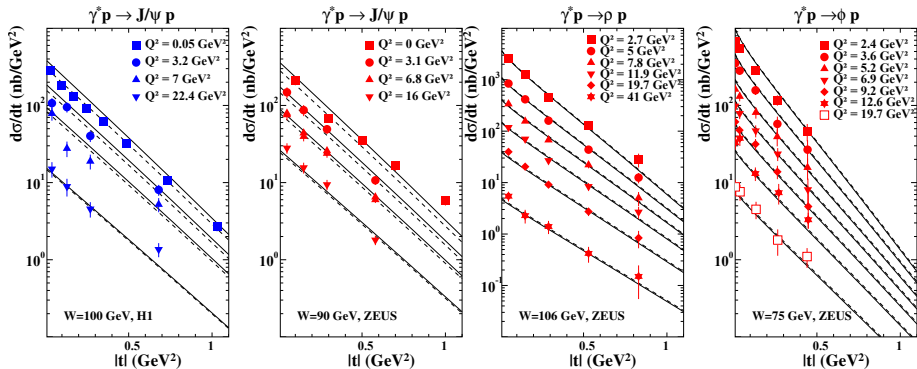
Slope of t -distribution of exclusive processes, a unified picture



$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow Ep}}{dt} \approx e^{-B_D |t|} \text{ (large } Q^2) \iff Q_s^2(x, b) \approx Q_s^2(x) e^{-b^2/2B_D} \text{ (dilute regime)}$$

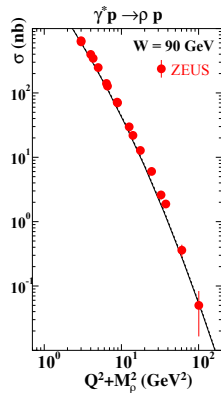
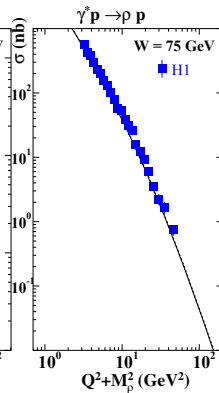
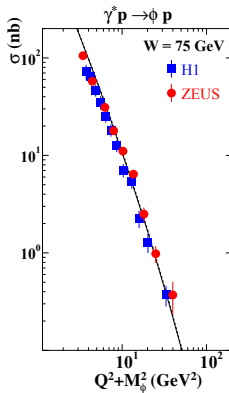
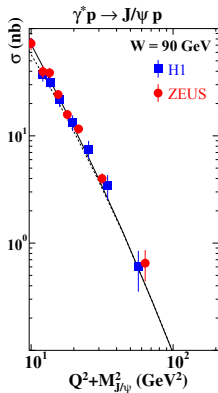
- At a fixed Q^2 , the typical dipole size is bigger for lighter vector meson \implies validity of the above asymptotic expression is postponed to a higher Q^2 .
- Universality of extracted impact-parameter distribution of the proton. t -slope B_D gives the width of saturation scale distribution in proton.

t -distribution of exclusive processes

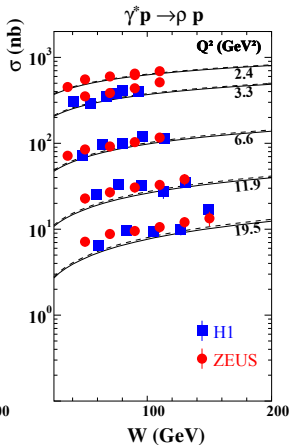
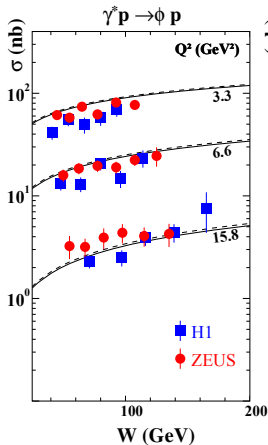
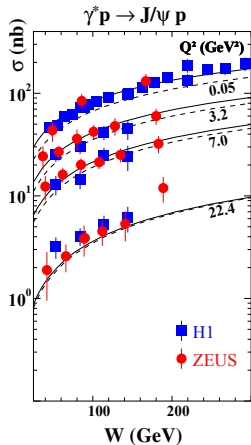


- The J/ψ production cross-section is more sensitive to m_c at low Q^2 compared to ρ, ϕ, γ production cross-sections.
- t -dependence is described by $\sim \exp(-B_D t)$ at low- t , but B_D depends on Q^2 and M^2 .

Q^2 -dependence of exclusive processes

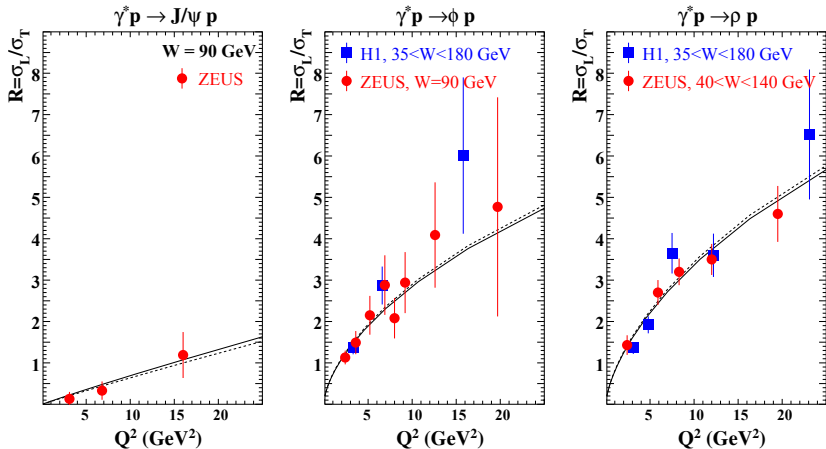


W -dependence of exclusive processes

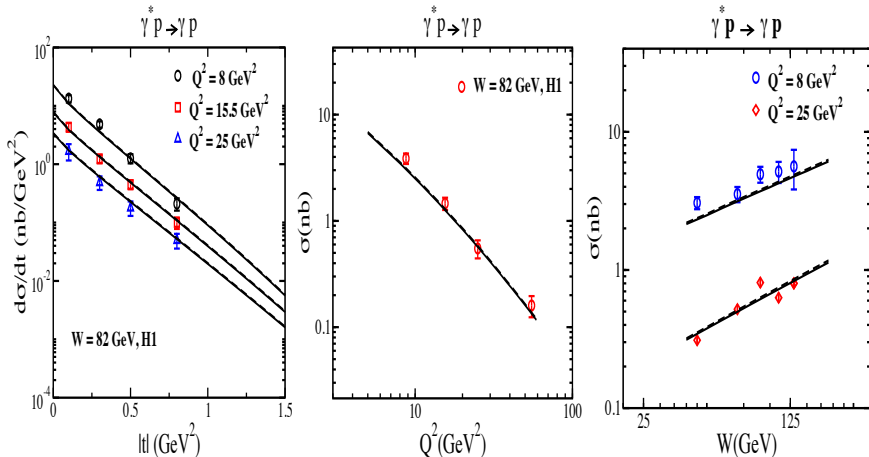


- The W -dependence of the cross-section follows a power-law behavior $\sigma \sim W^\delta \rightarrow$ Indication of geometric scaling in diffractive data: Marquet and Schoeffel, hep-ph/0606079.

Q^2 -dependence of exclusive processes



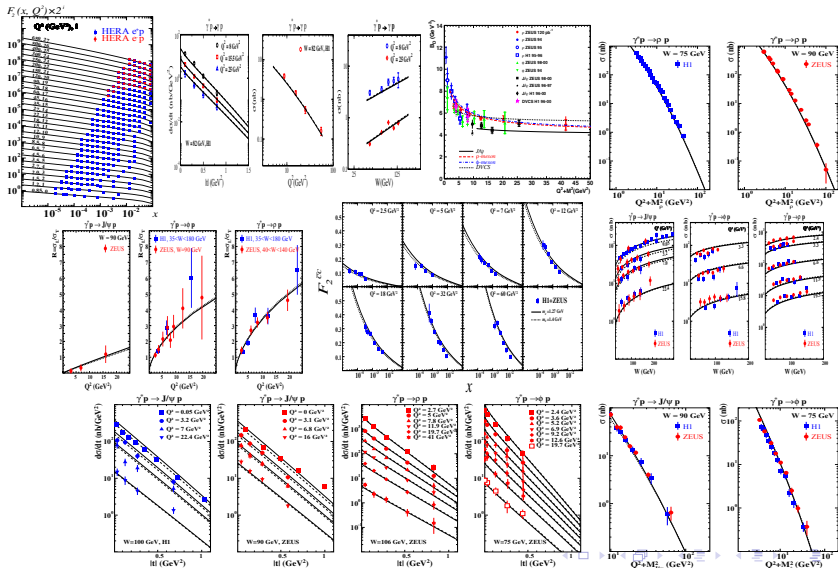
- σ_T is generally dominated by larger dipole sizes than $\sigma_L \rightarrow$ relative increase of t -slope of σ_T compared to longitudinal one, i.e. $B_{DT} > B_{DL} \rightarrow R = \sigma_L / \sigma_T$ to increase with Q^2 .



- DVCS is the cleanest exclusive process since wavefunctions is well-known, t -dependence is described by $\sim \exp(-B_D t)$.

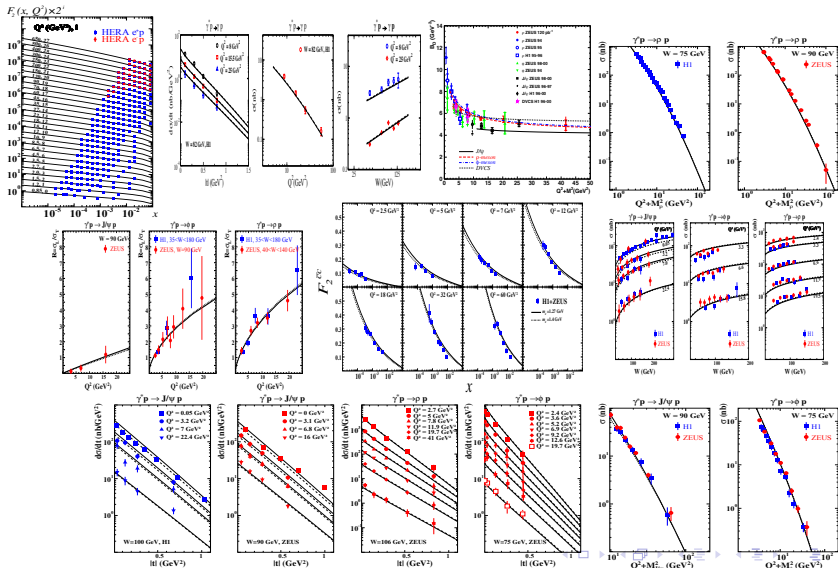
Conclusion: IP-Sat mostly gives a perfect description of all HERA data at $x \leq 0.01$.

A unified description of x , Q^2 , W and t dependence of data.

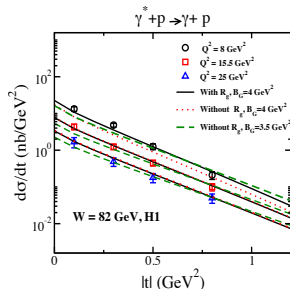
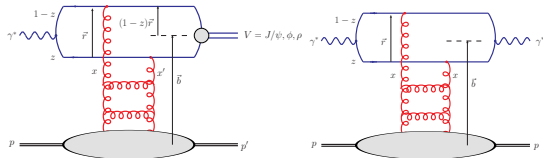


Conclusion: IP-Sat mostly gives a perfect description of all HERA data at $x \leq 0.01$.

Fortran code for the IP-Sat dipole (with evolved-DGLAP) is available for public.



Backup: The skewedness $x \neq x'$ effect



- At NLO level, in the limit that $x' \ll x \ll 1$, the skewedness effect can be effectively accounted for by multiplying the gluon distribution $xg(x, \mu^2)$ by a factor R_g [Shuvaev et al. hep-ph/9902410]:

$$R_g(\gamma) = \frac{2^{2\gamma+3}}{\sqrt{\pi}} \frac{\Gamma(\gamma + 5/2)}{\Gamma(\gamma + 4)}, \quad \text{with } \gamma \equiv \frac{\partial \ln [xg(x, \mu^2)]}{\partial \ln(1/x)}.$$

- The inclusion of R_g improves the results, but large part of the effect can be also absorbed into the uncertainty of t-slope parameter B_D .
 - The dipole factorization needs to be proven with the inclusion of skewing effect.