



# Measurement of Collins Asymmetries in inclusive production of pion pairs in $e^+e^-$ interaction at BaBar



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Deep Inelastic Scattering and Related Subjects

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# OUTLINE

## INTRODUCTION

- Theoretical framework
  - Collins effect in di-hadron correlations
  - Reference frames
- PEP-II and the BaBar detector at SLAC

## ANALYSIS OVERVIEW

- Analysis method
- Extraction of the asymmetry for light quarks
- Asymmetry corrections and studies of systematic uncertainty

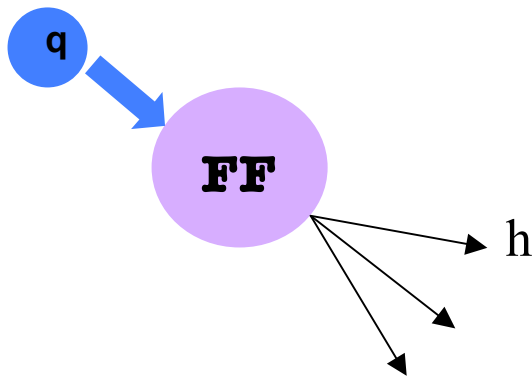
## RESULTS

- Asymmetries *vs.* fractional energies, pion transverse momentum, and analysis axis polar angle
- Comparison with Belle measurements

## CONCLUSIONS

# Collins Fragmentation Function

- Fragmentation Functions** (FFs) → dimensionless and universal functions  
→ non-perturbative information  
→ describe the final state particles in hard processes  
→ dependence on  $z=2E_h/\sqrt{s}$ ,  $P_\perp$ , and  $s_q$

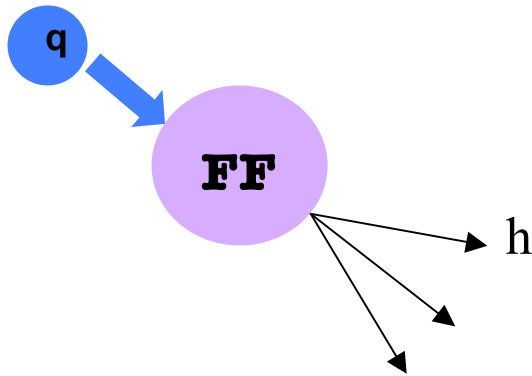


“Standard” unpolarized FF

$$D_1^{q\uparrow}(z, \mathbf{P}_\perp; s_q) = \overset{\downarrow}{D_1^q}(z, P_\perp) + \frac{P_\perp}{zM_h} H_1^{\perp q}(z, P_\perp) \mathbf{s}_q \cdot (\mathbf{k}_q \times \mathbf{P}_\perp)$$

# Collins Fragmentation Function

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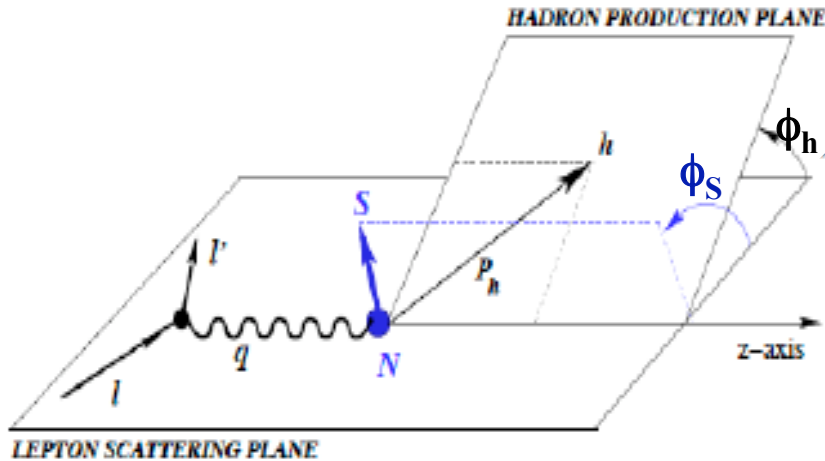


“Standard” unpolarized FF

$$D_1^{q\uparrow}(z, \mathbf{P}_\perp; s_q) = D_1^q(z, P_\perp) + \frac{P_\perp}{zM_h} \boxed{H_1^{\perp q}(z, P_\perp) \mathbf{s}_q \cdot (\mathbf{k}_q \times \mathbf{P}_\perp)}$$

- could arise from a **spin-orbit** coupling
  - leads to an asymmetry in the angular distribution of final state particles (**Collins effect**)
- $H_1^\perp$  is the **polarized** fragmentation function or **Collins FF** → it describes the fragmentation of a **transversely polarized quark into a spinless (or unpolarized) hadron  $h$**
  - J. C. Collins, Nucl.Phys. **B396**, 161 (1993)
  - **Chiral-odd** function ==> it is the ideal partner to access chiral-odd parton distribution functions in Semi-Inclusive Deep Inelastic Scattering (SIDIS)

# Collins effect



## Semi-Inclusive DIS (SIDIS)

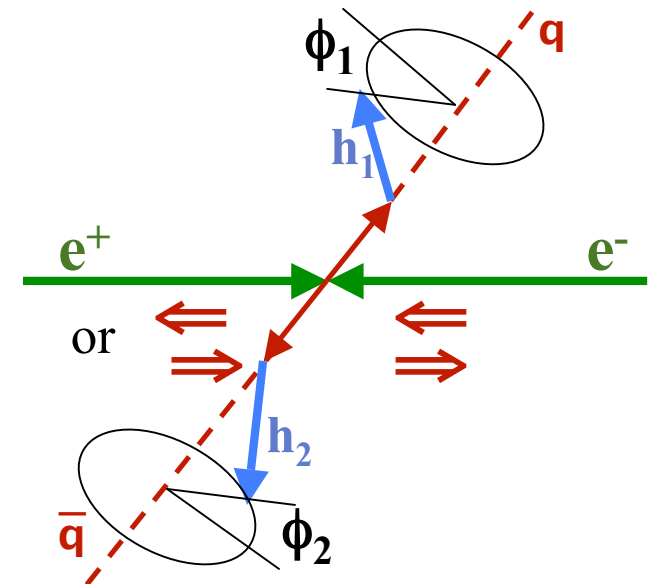
- Unpolarized lepton beam ( $l$ ) off transversely polarized target ( $N$ ) ( $lN \rightarrow l' \pi X$ )
  - non-zero Collins effects PRL 94,012002; NPB 765, 31
  - spin direction known ( $S$ )
- $\sigma \propto \sin(\phi_h + \phi_s) h_1(x_B) \otimes H_1^\perp(z_1)$ 
  - two chiral-odd functions
  - azimuthal Single Spin Asymmetry

## $e^+e^-$ annihilation

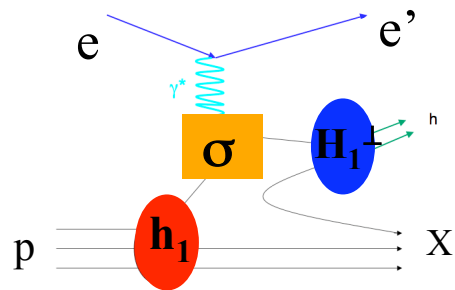
- $\gamma^*$  (spin-1)  $\rightarrow$  spin-1/2  $q$  and  $\bar{q}$ 
  - in a given event, the spin directions are unknown, but they must be parallel
  - they have a polarization component transverse to the  $q$  direction ( $\sim \sin^2\theta$ )
- exploit this correlation by using hadrons in opposite jets

$$e^+e^- \rightarrow q\bar{q} \rightarrow \pi_1\pi_2X \quad (q=u, d, s) \implies$$

$$\sigma \propto \cos(\phi_i) H_1^\perp(z_1) \otimes H_1^\perp(z_2),$$



# Extraction of Collins FF from data



**SIDIS**

HERMES: PRL **94**, 012002 (2005)  
 COMPASS: NP **B765**, 31 (2007)

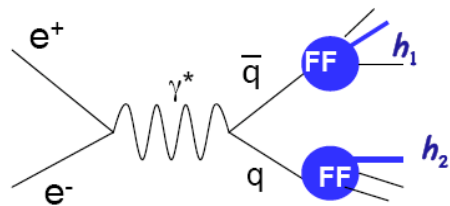
$$A_T \propto h_1(x_B) \otimes H_1^\perp(z)$$

+

**e<sup>+</sup>e<sup>-</sup> annihilation**

BELLE: PRL **96**, 232002, PRD **78**,  
 03201, PRD **86**,039905(E)

$$A \propto H_1^\perp(z_1) \otimes H_1^\perp(z_2)$$



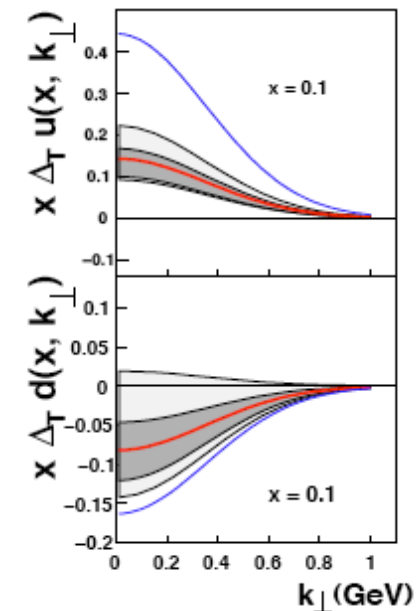
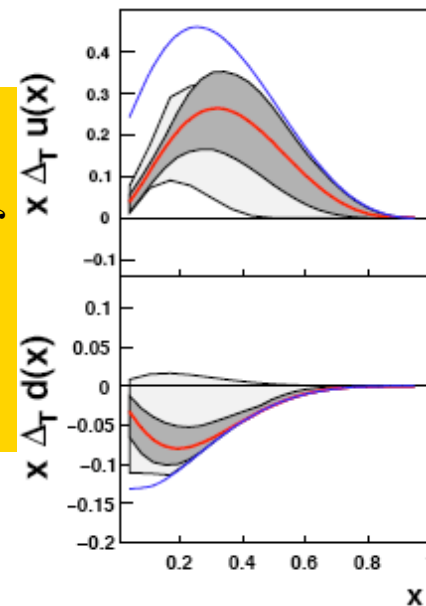
**GLOBAL ANALYSIS:** simultaneous determination of  $H_1^\perp$  and the transversity parton distribution function  $h_1$

*Anselmino et al., PRD **75**, 054032, NP Proc.Suppl. **191**, 98*

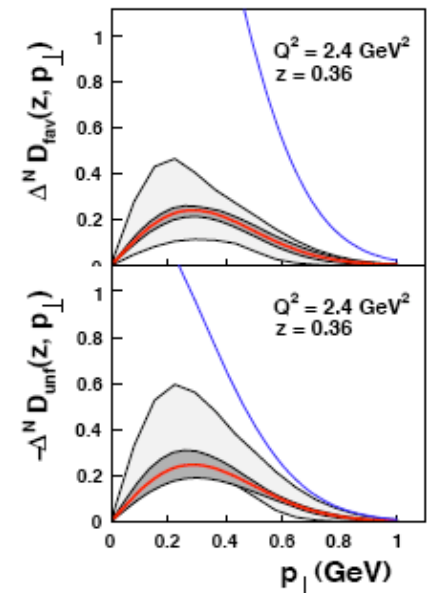
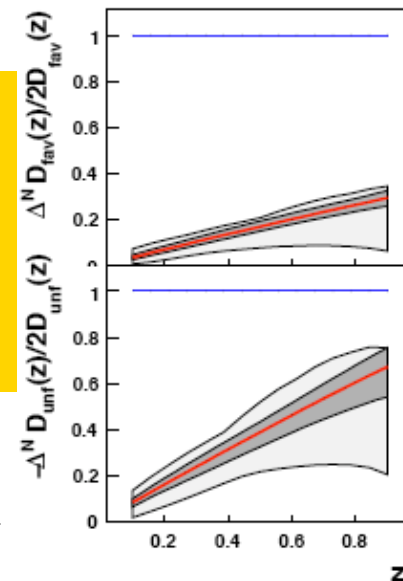
**Improvements from BABAR studies:**

- Increase in the number of pion fractional energy intervals
- Collins asymmetry behavior vs. pion transverse momenta

**Transversity PDF**



**Collins FF**



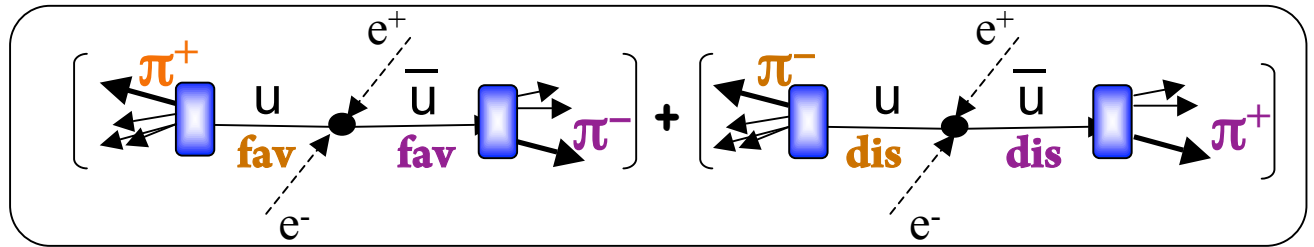
# Collins effect in $e^+e^-$ annihilation

$$e^+e^- \rightarrow q\bar{q} \rightarrow \pi_1^\pm \pi_2^\pm X \quad (q=u, d, s)$$

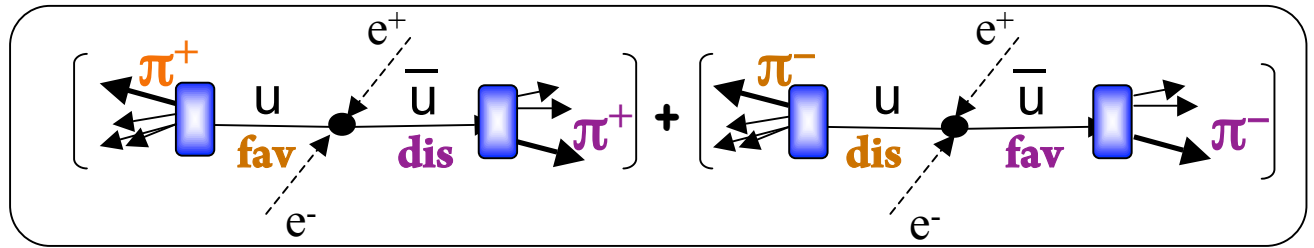
Different combination of charged pions  $\Rightarrow$  sensitivity to **favored** or **unfavored** FFs

- **favored** fragmentation process describes the fragmentation of a quark of flavor  $q$  into a hadron with a valence quark of the same flavor: i.e.:  $u \rightarrow \pi^+$ ,  $d \rightarrow \pi^-$
- **disfavored** for  $d \rightarrow \pi^+$ ,  $u \rightarrow \pi^-$ , and  $s \rightarrow \pi^\pm$

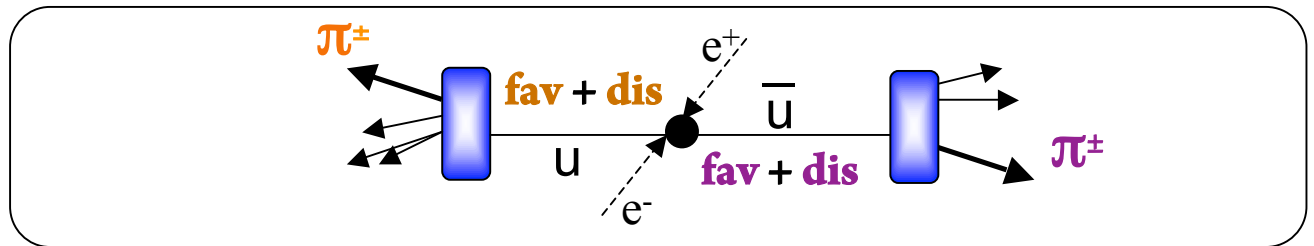
Unlike-sign pion pair = **U**:  
 $\pi^+ \pi^-$ : (**fav** x **fav**) + (**dis** x **dis**)



Like-sign pion pair = **L**:  
 $\pi^\pm \pi^\pm$ : (**fav** x **dis**) + (**dis** x **fav**)



Charged pion pair = **C (U+L)**:  
 $\pi\pi$ : (**fav** + **dis**) x (**fav** + **dis**)  
 $\pi = \pi^\pm$



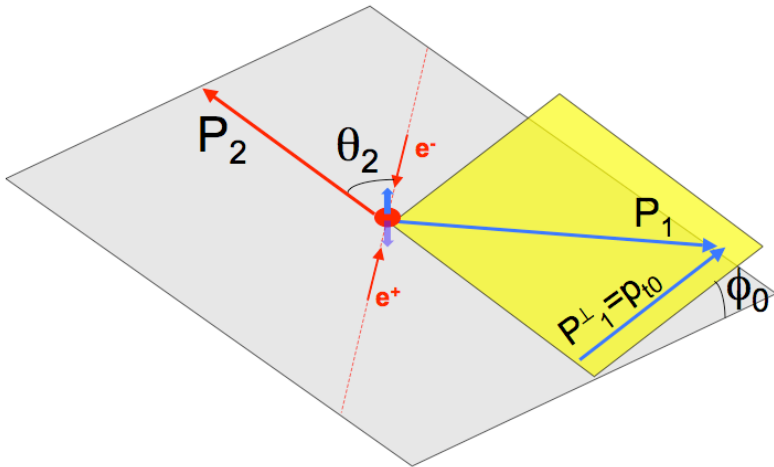
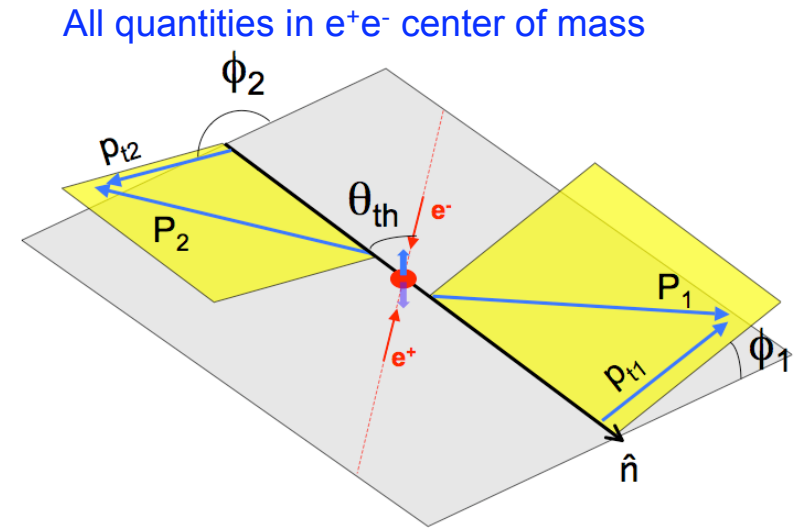
# Analysis Reference Rframe (RF)

[See NPB 806, 23 (2009)]

## RF12 or Thrust RF

- **Thrust axis** to estimate the  $q\bar{q}$  direction
- $\phi_{1,2}$  defined using thrust-beam plane
- Modulation diluted by gluon radiation, detector acceptance,...

$$\sigma \sim 1 + \frac{\sin^2 \theta_{th}}{1 + \cos^2 \theta_{th}} \cos(\phi_1 + \phi_2) \frac{H_1^\perp(z_1) \bar{H}_1^\perp(z_2)}{D_1(z_1) \bar{D}_1(z_2)}$$



All quantities in  $e^+e^-$  center of mass

## RF0 or Second hadron momentum RF

- Alternatively, just use **one track** in a pair
- Very clean experimentally (no thrust axis), less theoretically
- Gives quark direction for higher pion momentum

$$\sigma \sim 1 + \frac{\sin^2 \theta_2}{1 + \cos^2 \theta_2} \cos(2\phi_0) \mathcal{F} \left[ \frac{H_1^\perp(z_1) \bar{H}_1^\perp(z_2)}{D_1(z_1) \bar{D}_1(z_2)} \right]$$

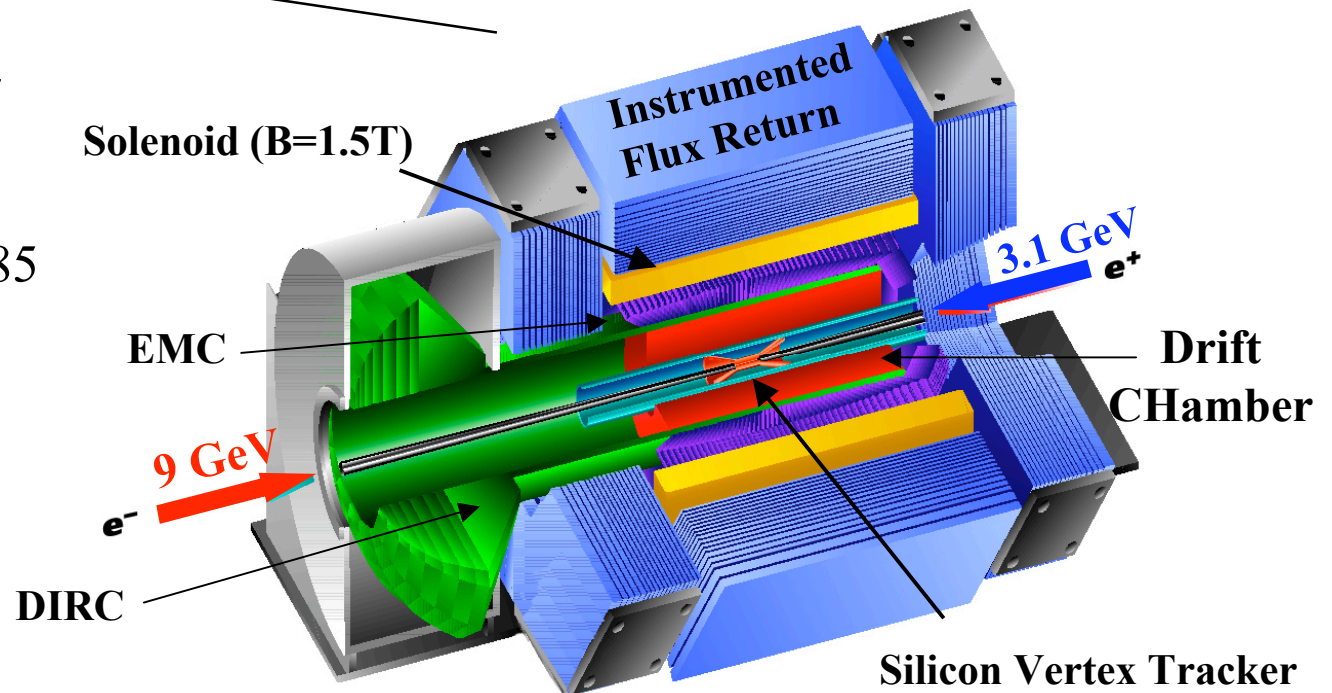


# PEP-II and the BaBar detector at SLAC



- Asymmetric  $e^+e^-$  collider operating at the  $\Upsilon(4S)$  resonance ( $\sqrt{s}=10.58$  GeV )
  - High Energy Ring (**HER**): 9.0 GeV  $e^-$
  - Low Energy Ring (**LER**): 3.1 GeV  $e^+$
  - c.m.-lab boost,  $\beta\gamma \approx 0.56$
- High luminosity:  $\mathcal{L} \sim 468 \text{ fb}^{-1}$  used here

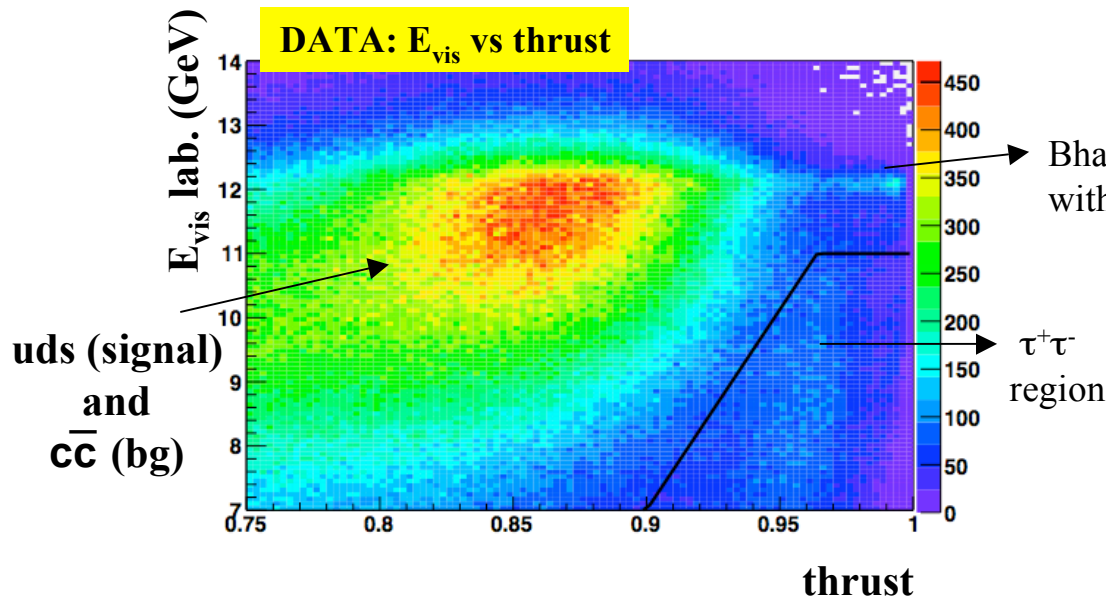
- Asymmetric detector
  - c.m. acceptance  $-0.9 < \cos\theta^* < 0.85$  wrt  $e^-$  beam
- Excellent performance
  - good tracking, mass resolution
  - good  $\gamma$ ,  $\pi^0$  reconstruction
  - full  $e$ ,  $\mu$ ,  $\pi$ ,  $K$ , and  $p$  identification



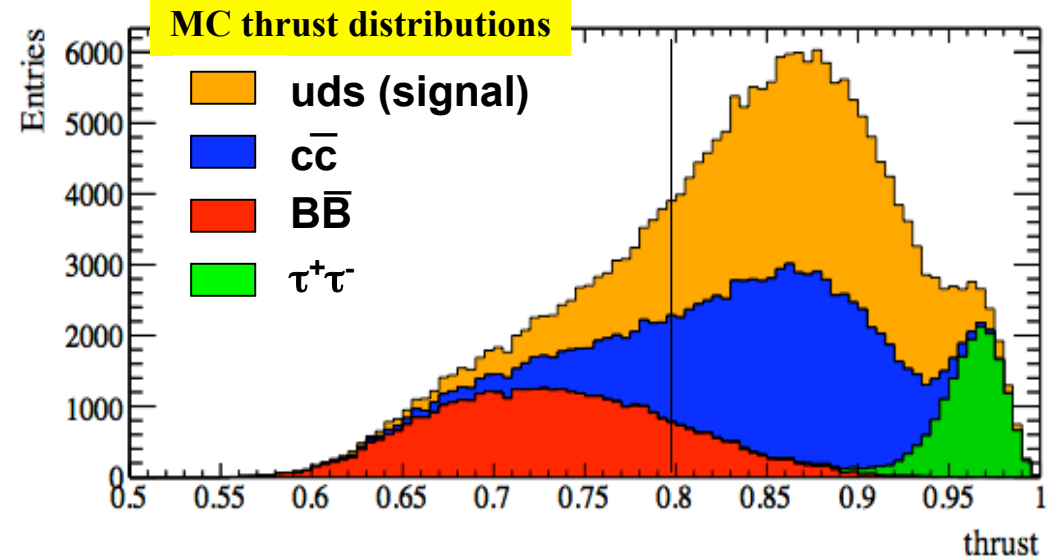
# Event and track selection

## EVENT SELECTION

- Number of charged tracks  $> 2$
- Visible energy:  $E_{\text{vis}} > 7 \text{ GeV}$
- Selection of two-jet topology events requiring **thrust $>0.8$**
- Events in the  $\tau^+\tau^-$  region removed



- Opening angle ( $\theta_{\text{pi-thrust}}$ ) of the pions with respect to the thrust axis  $< 45^\circ$
- $Q_t < 3.5 \text{ GeV}$ , where  $Q_t$  is the transverse momentum of the virtual photon in the pions CMS



## TRACK SELECTION

- $\mu^\pm$  and  $e^\pm$  veto, and pion ID required
- Tracks in the detector acceptance region:  
 $0.41 < \theta_{\text{lab}} < 2.54 \text{ rad}$
- **Pion fractional energies:**  
 $0.15 < z = 2E_h/\sqrt{s} < 0.9$

# Raw Asymmetries

- **Collins asymmetry**

- consider all the **U** and **L** pion pairs
- make histograms of  $\phi_\alpha = \phi_1 + \phi_2$  or  $2\phi_0$  ( $\alpha=12,0$ )
- normalize by the average:

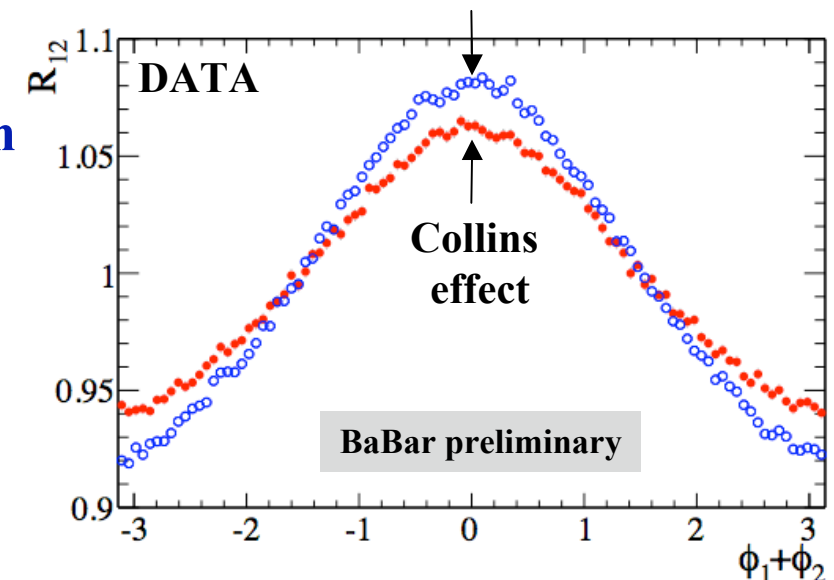
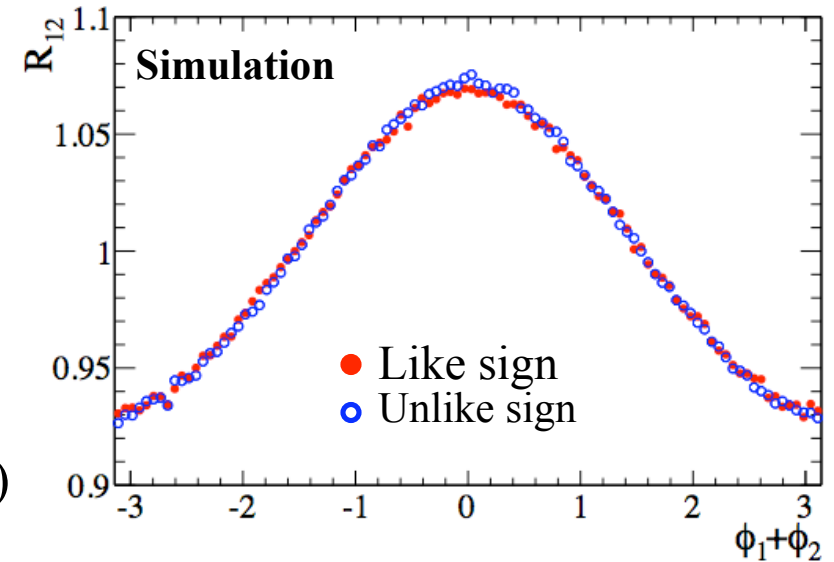
$$R_\alpha = \frac{N(\phi_\alpha)}{\langle N_\alpha \rangle} = a + b \cdot \cos(\phi_\alpha)$$

Proportional to the product (convolution)  
of the two Collins functions

- **The MC generator (JETSET) does not include the Collins effect, but it shows a strong cosine modulation**

- due to acceptance of the detector
- depends strongly on the thrust axis polar angle
- but similar distribution for **U** and **L** pairs

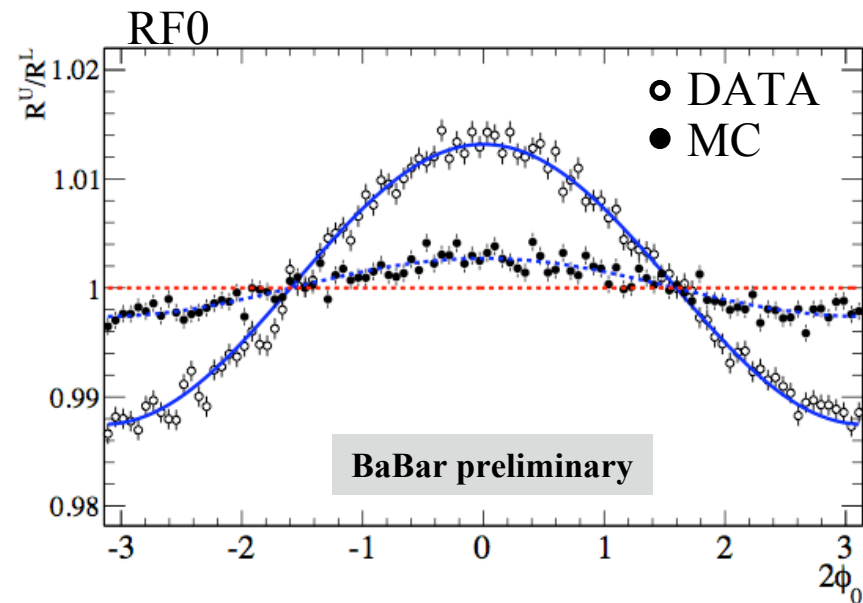
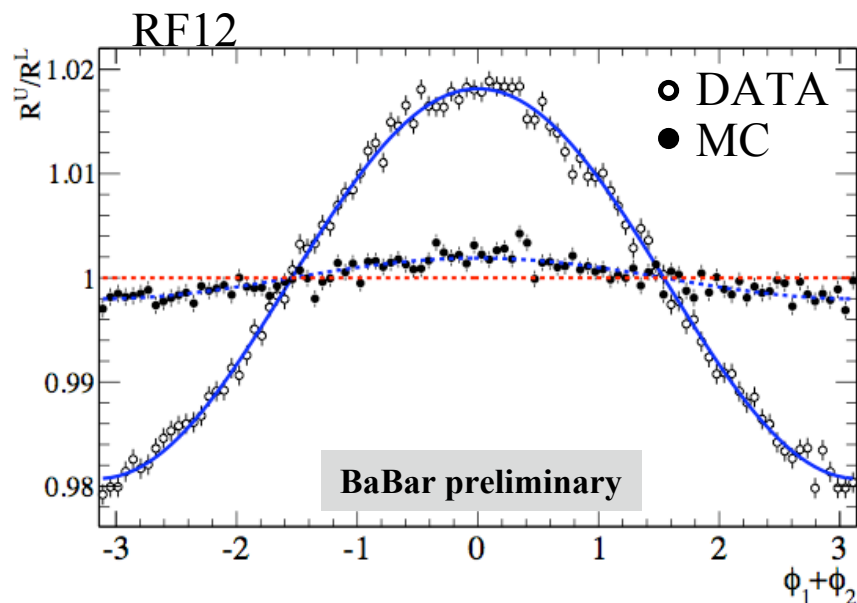
- **Data shows a large difference between U and L distributions, that can be ascribed to the Collins effect**



# Double Ratios

==> Acceptance effects can be reduced by performing the ratio of **Unlike/Like** sign pion pairs (or **Unlike/Charged**)

- small deviation from zero still present ( $\ll$  asymmetry measured in data sample)



MC: consistent with a flat distribution

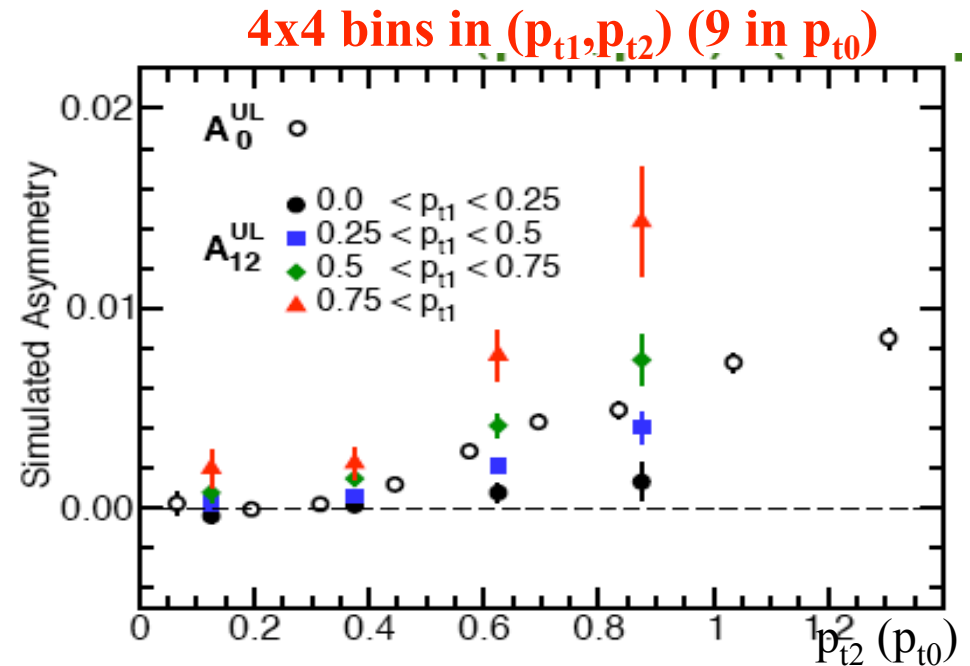
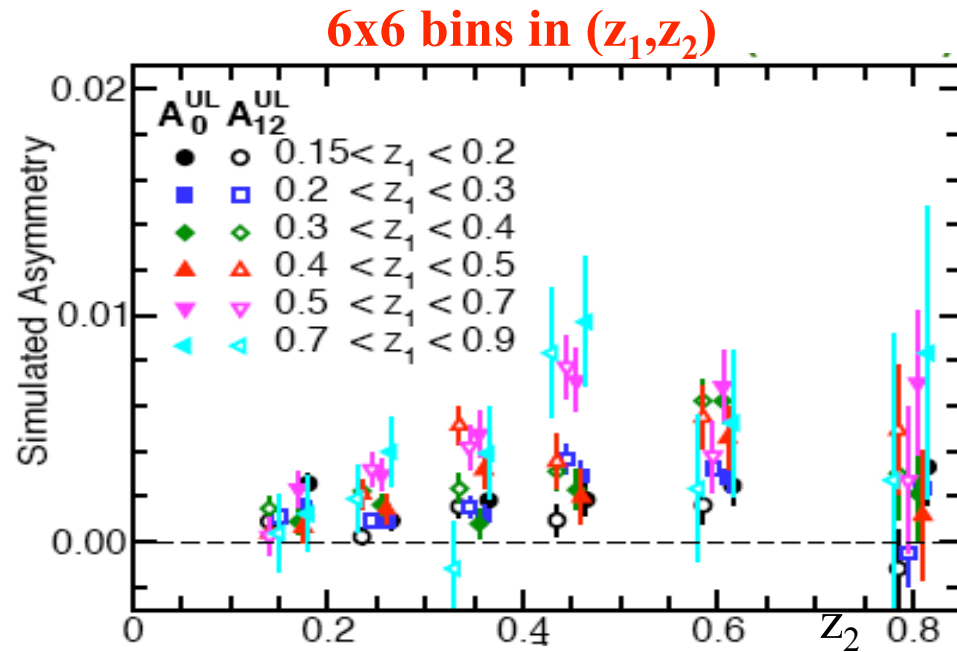
DATA: cosine modulation clearly visible

$$\frac{R_{\alpha}^U}{R_{\alpha}^{L(C)}} = \frac{N^U(\phi_{\alpha}) / \langle N^U(\phi_{\alpha}) \rangle}{N^{L(C)}(\phi_{\alpha}) / \langle N^{L(C)}(\phi_{\alpha}) \rangle} \rightarrow B_{\alpha}^{UL(UC)} + A_{\alpha}^{UL,(UC)} \cdot \cos(\phi_{\alpha})$$

$A$ : contains only the Collins effect and higher order radiative effects

# Asymmetry binning and corrections

- The Collins effect is expected to depend on  $z_1, z_2, p_{t1}, p_{t2}$  (or  $p_{t0}$ ), as well as  $\cos\theta_{th}$  (or  $\cos\theta_2$ )  
 $\Rightarrow$  analyze in bins of these quantities:



- Simulated asymmetries also depend on these quantities  $\rightarrow$  must correct in each bin independently  
 $\Rightarrow$  Systematic on MC value evaluated by varying track selection/acceptance
- Asymmetry dilution due to the thrust axis approximation. The corrections in the RF12 frame range between 1.3-2.3 as a function of  $z$ , and between 1.3-3 as a function of  $p_t$   
 $\Rightarrow$  No correction needed in the RF0 frame

# Extraction of the uds asymmetry

- In each bin, the data sample includes pairs from
  - signal uds events
  - $B\bar{B}$  events (small, mostly at low  $z$ )
  - $C\bar{C}$  events (important at low/medium  $z$ )
  - $\tau^+\tau^-$  events (important at high  $z$ )

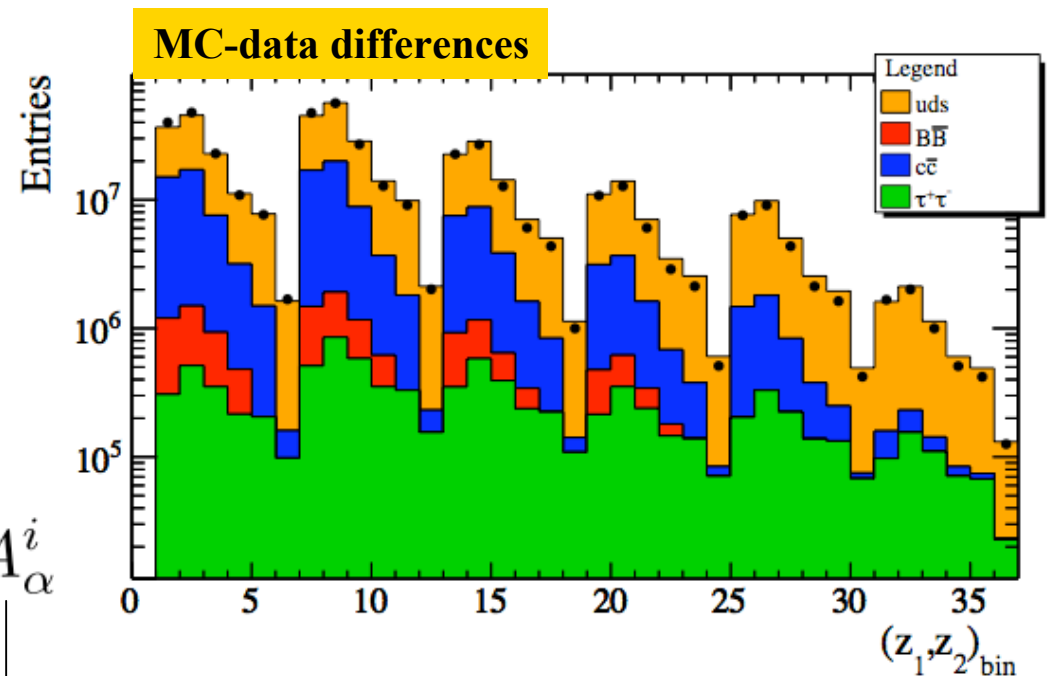
- We measure:

$$A_{\alpha}^{meas} = \left(1 - \sum_i F_i\right) \cdot A_{\alpha} + \sum_i F_i \cdot A_{\alpha}^i$$

Fraction of pion pairs due to the  $i^{\text{th}}$  background process

**True asymmetry**

Asymmetry measured in the background data control sample



- We must calculate these quantities:

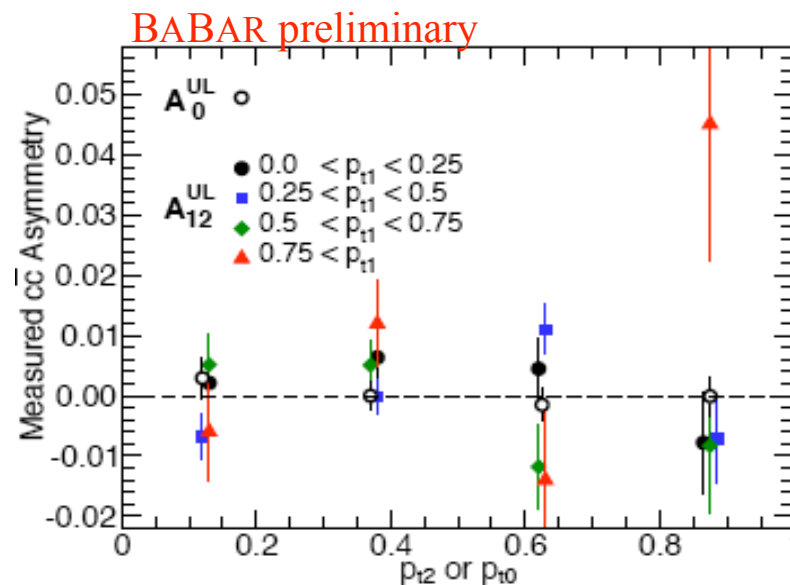
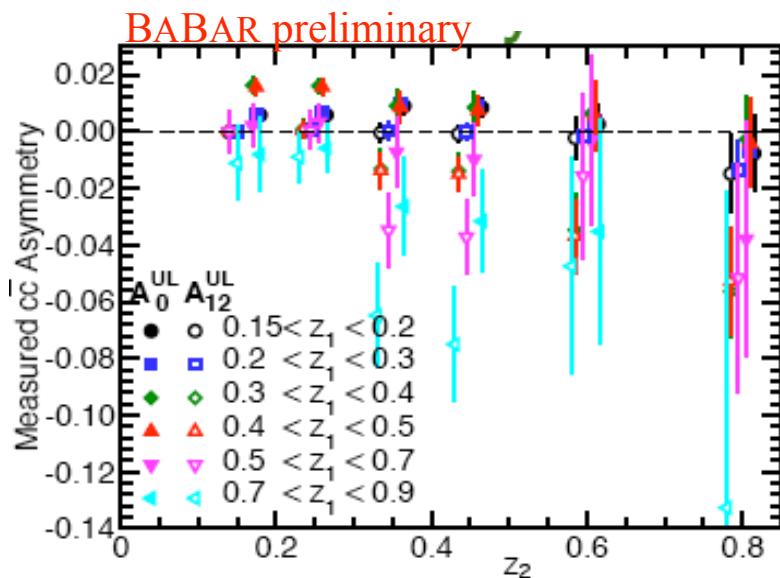
- $F_i$  using MC sample; we assign MC-data difference in each bin as systematic error
- $A^{B\bar{B}}$  must be zero; we set  $A^{B\bar{B}} = 0$
- $A^{\tau}$  small in simulation; checked in data; we set  $A^{\tau} = 0$

# Extraction of the uds asymmetry

- Charm background contribution is about 30% on average
  - Both fragmentation processes and weak decays can introduce azimuthal asymmetries
  - We used a **D<sup>\*±</sup>-enhanced control sample** to estimate its effect on a **bin-by-bin basis**
  - 4 complementary decay modes D<sup>\*±</sup>→D<sup>0</sup>π<sup>±</sup>, with D<sup>0</sup>→Kπ,K3π,Kππ<sup>0</sup>,K<sub>s</sub>ππ
  - mostly c $\bar{c}$  events, some B $\bar{B}$
- Again, f<sub>i</sub> from MC, data-MC difference as systematic error

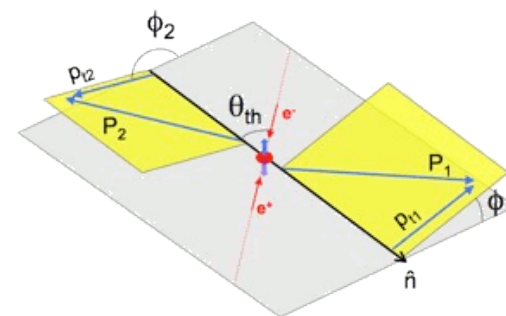
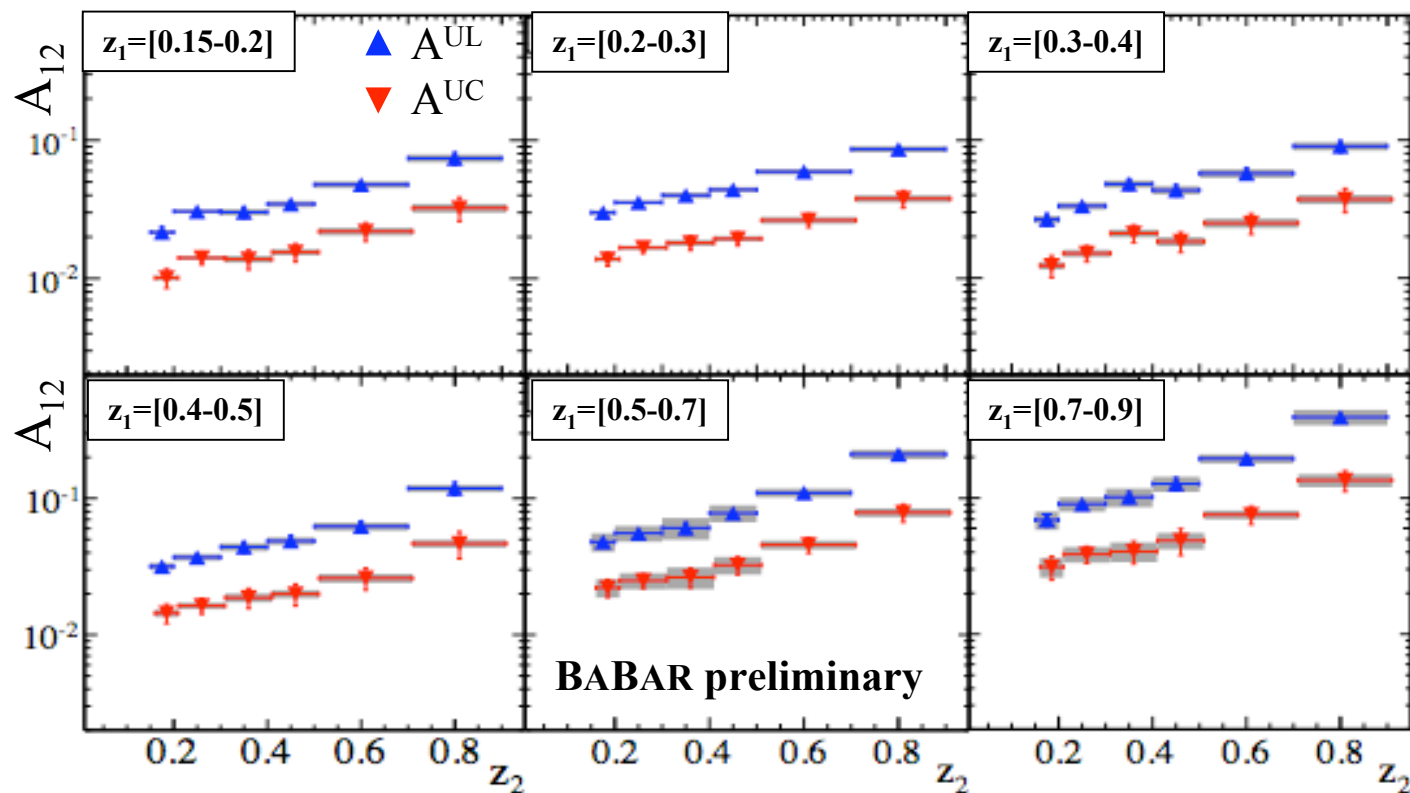
$$A_{\alpha}^{meas} = (1 - F_c - F_B - F_{\tau}) \cdot A_{\alpha} + F_c \cdot A_{\alpha}^{ch}$$

$$A_{\alpha}^{D^*} = f_c \cdot A_{\alpha}^{ch} + (1 - f_c - f_B) \cdot A_{\alpha}$$



- the A<sup>ch</sup> are very small (slightly negative?)

# Results: $A_{12}$ vs. $(z_1, z_2)$

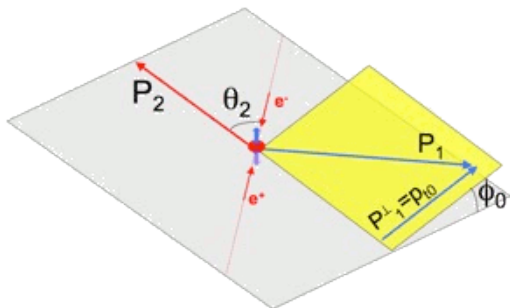


Systematic errors indicated by shaded bands

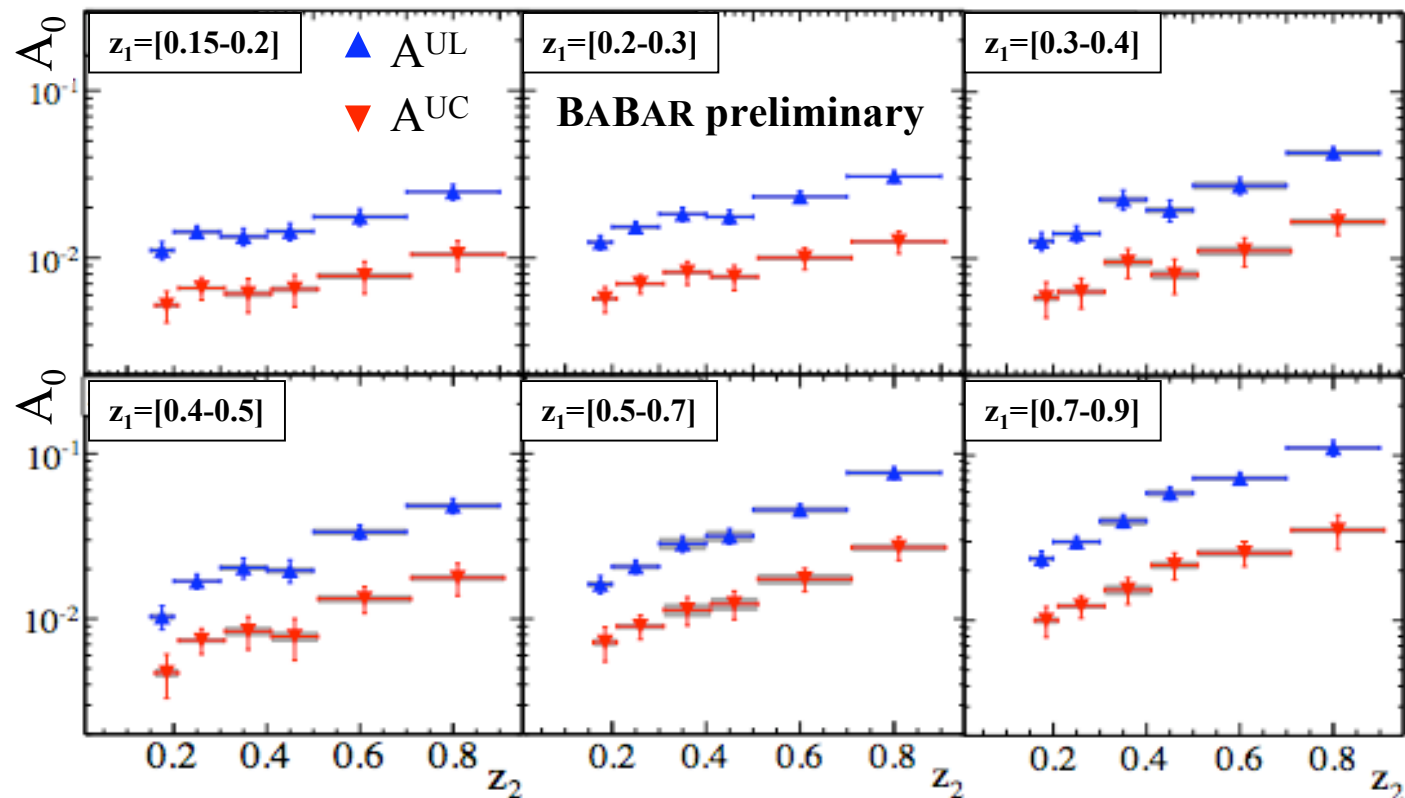
- **Very significant nonzero  $A^{\text{UL}}$  and  $A^{\text{UC}}$  in all bins**
  - $\Rightarrow$  strong dependence on  $(z_1, z_2)$ , 1-39%
  - $\Rightarrow A^{\text{UC}} < A^{\text{UL}}$  as expected; complementary information about the favored and disfavored fragmentation processes (PRD 73, 094025 (2006))
  - $\Rightarrow$  consistent with  $z_1 \Leftrightarrow z_2$  symmetry



# Results: $A_0$ vs. $(z_1, z_2)$

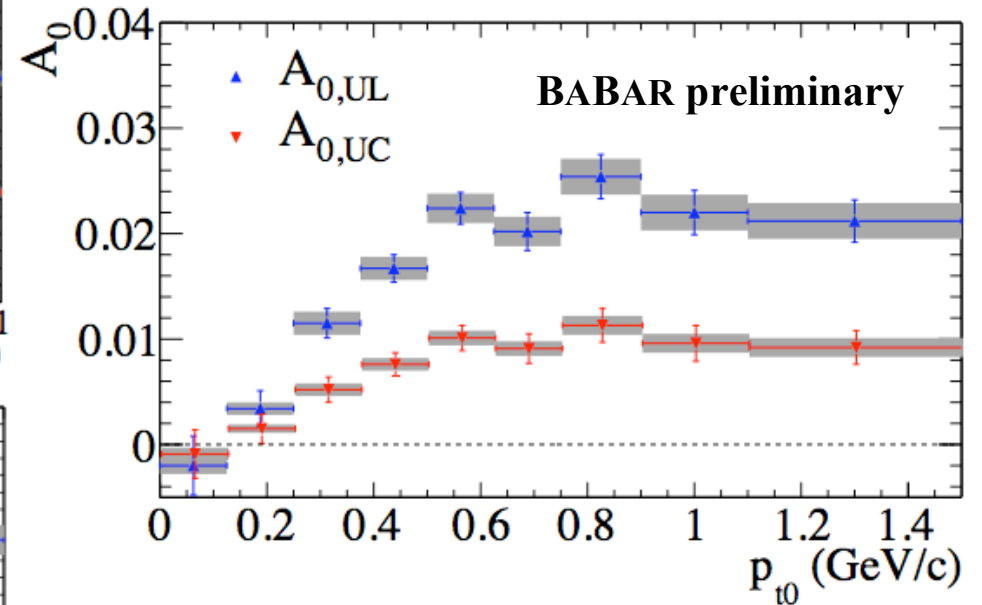
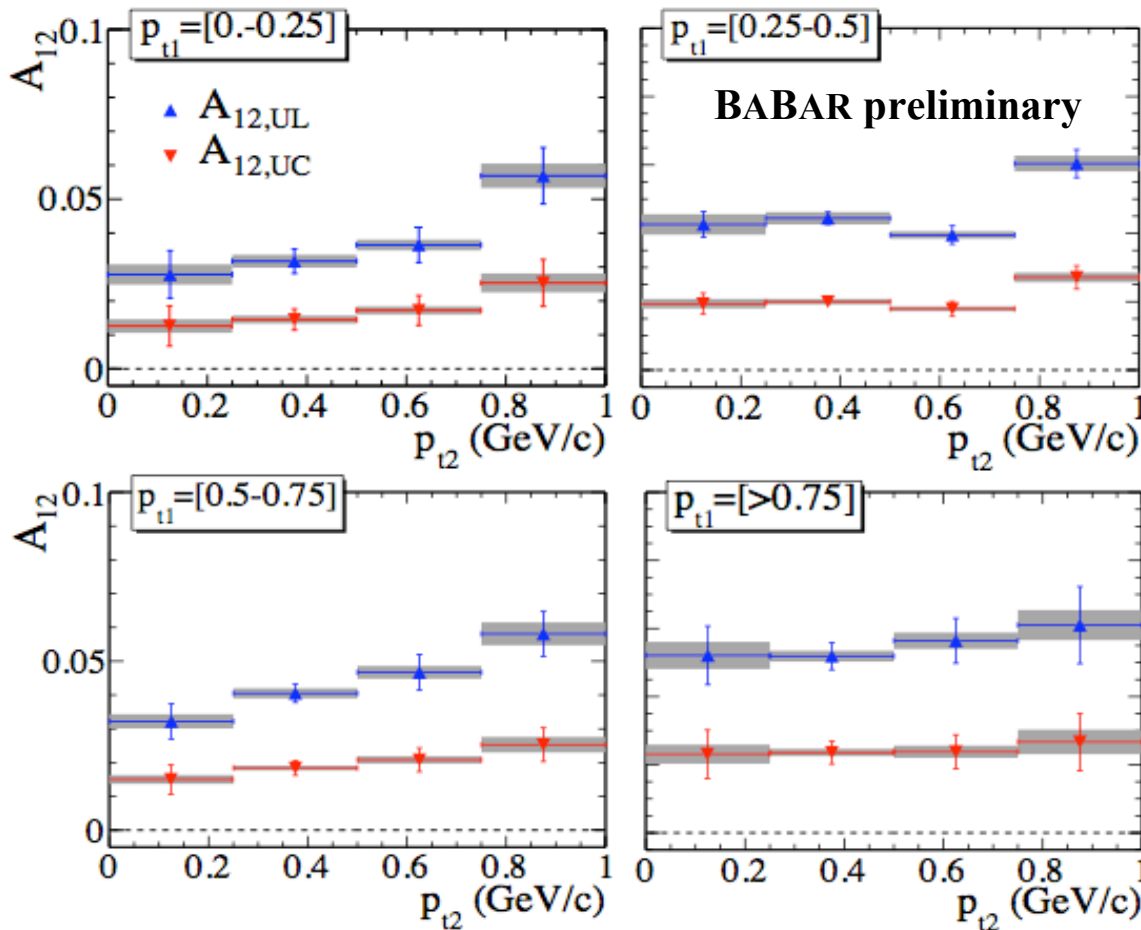


Systematic errors indicated by shaded bands



- **Very significant nonzero  $A^{\text{UL}}$  and  $A^{\text{UC}}$  in all bins**
  - ⇒ strong dependence on  $(z_1, z_2)$ , 0.5-11%
  - ⇒ smaller than  $A_{12}$ ;
  - ⇒  $A^{\text{UC}} < A^{\text{UL}}$ ; complementary information on  $H_1^{\perp, \text{fav}}$  and  $H_1^{\perp, \text{dis}}$
  - ⇒ consistent with  $z_1 \Leftrightarrow z_2$  symmetry

# Results: $A_{12}$ vs. $(p_{t1}, p_{t2})$ ; $A_0$ vs. $p_{t0}$



**FIRST MEASUREMENT of Collins asymmetries vs.  $p_t$  in  $e^+e^-$  annihilation at  $Q^2 \sim 110$  (GeV/c)<sup>2</sup> (time-like region)**

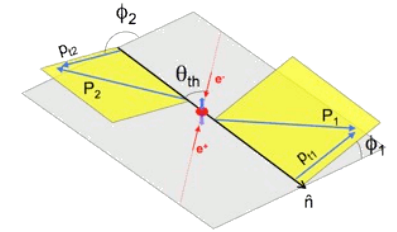
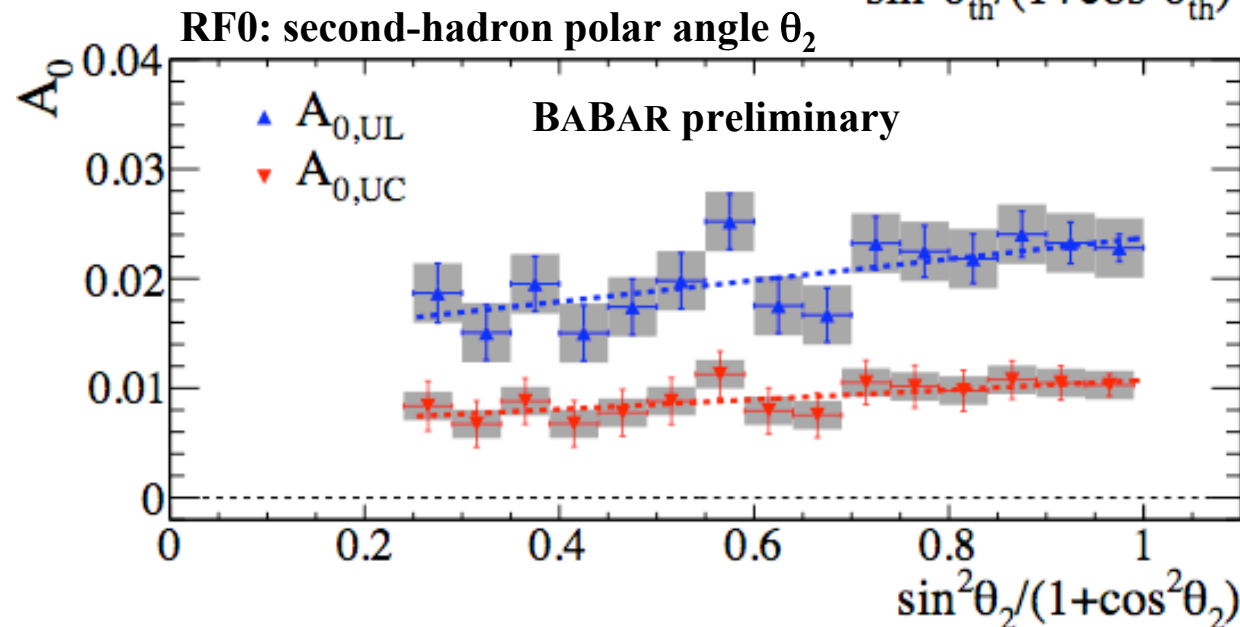
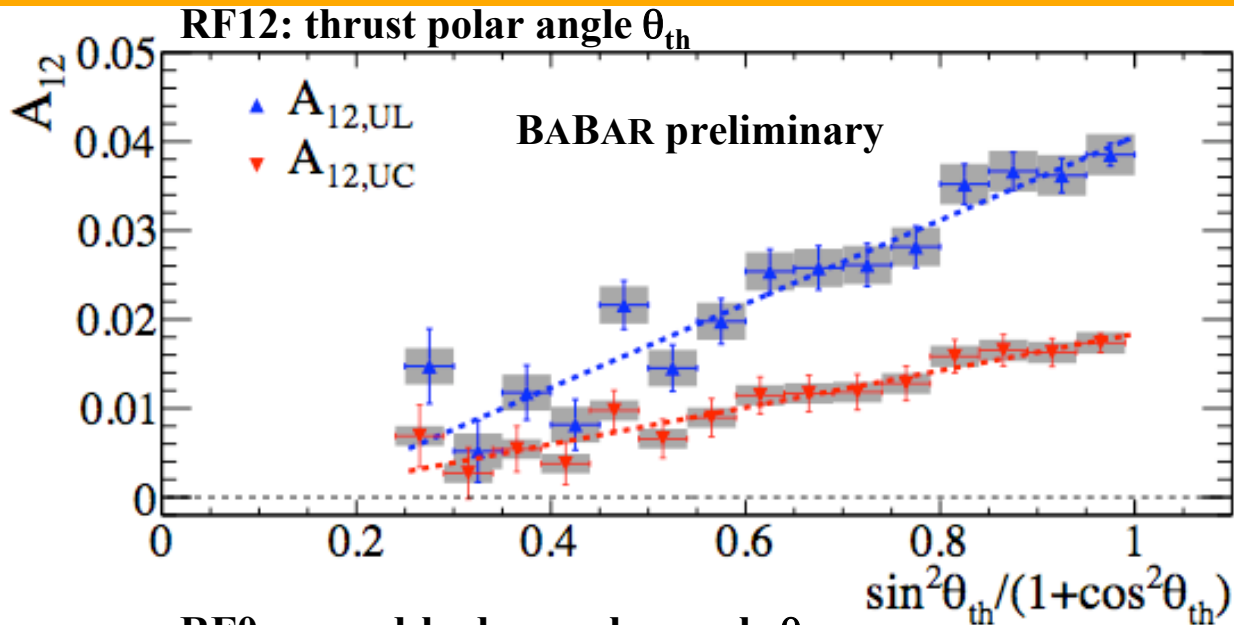
- **nonzero  $A^{\text{UL}}$  and  $A^{\text{UC}}$**

- $\Rightarrow$  only modest dependence on  $(p_{t1}, p_{t2})$ ; disagreement with the expectation ???

- $\Rightarrow A^{\text{UC}} < A^{\text{UL}}$ ; complementary information on  $H_1^{\perp, \text{fav}}$  and  $H_1^{\perp, \text{dis}}$

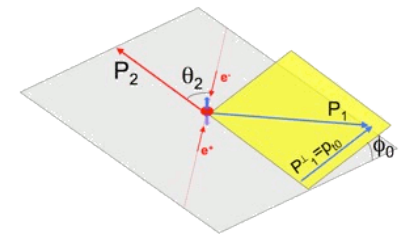
- $\Rightarrow A_0 < A_{12}$ , but interesting structure in  $p_t$

# Results: $A_{12}$ vs. $\theta_{th}$ ; $A_0$ vs. $\theta_2$



$$A_{12} \propto \frac{\sin^2 \theta_{th}}{1 + \cos^2 \theta_{th}} \cos(\phi_1 + \phi_2) \frac{H_1^\perp(z_1) \bar{H}_1^\perp(z_2)}{D_1(z_1) \bar{D}_1(z_2)}$$

**==> Intercept consistent with zero, as expected (consistent with Belle results)**



$$A_0 \propto \frac{\sin^2 \theta_2}{1 + \cos^2 \theta_2} \cos(2\phi_0) \mathcal{F} \left[ \frac{H_1^\perp(z_1) \bar{H}_1^\perp(z_2)}{D_1(z_1) \bar{D}_1(z_2)} \right]$$

**==> The linear fit gives a non-zero constant parameter  $\rightarrow$  the second hadron momentum provides a worse estimation of the  $q\bar{q}$  direction (consistent with Belle results)**

# Conclusions

BABAR has measured the Collins asymmetries for charged pion pairs in  $e^+e^- \rightarrow u\bar{u}, d\bar{d}, s\bar{s} \rightarrow \pi^\pm \pi^\pm X$

$\Rightarrow$ in two distinct reference frames	<b>RF12</b>	<b>RF0</b>
$\Rightarrow$ vs. $\pi^\pm$ fractional energy $z$	$z_1, z_2$	$z_1, z_2$
$\Rightarrow$ vs. $\pi^\pm$ transverse momentum $p_t$	$p_{t1}, p_{t2}$	$p_{t0}$
$\Rightarrow$ quark polar angle	$\theta_{th}$	$\theta_2$

$\Rightarrow$   **$A_{12}$  and  $A_0$  increase with increasing  $z_1, z_2$**

- consistent with theoretical expectations
- general agreement with Belle results (PRD 86, 039905(E) (2012))
- effect is stronger for leading particles

$\Rightarrow$   **$A_{12}$  ( $A_0$ ) increases with  $p_{t1}, p_{t2}$  ( $p_{t0}$ ) for  $p_t$  between 0 to 1 GeV/c**

- first measurement in  $e^+e^-$  annihilation at  $Q^2 \sim 110$  (GeV/c)<sup>2</sup>
- important for understanding the evolution of the fragmentation function

$\Rightarrow$   **$A_{12}$  ( $A_0$ ) increases linearly with  $\sin^2\theta/(1+\cos^2\theta)$**

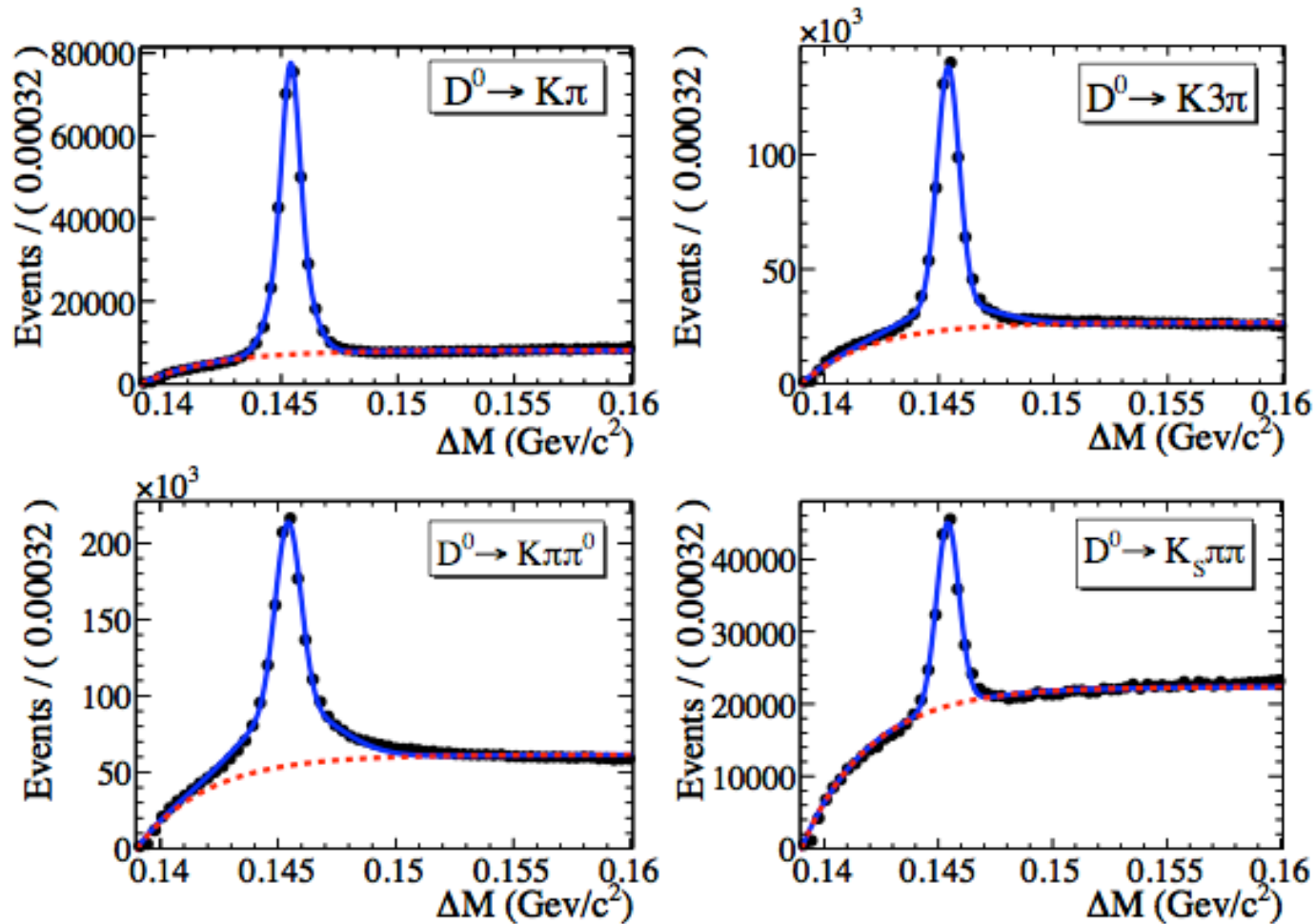
- as (might be) expected

$\Rightarrow$  **BABAR internal review in final stage for paper submission**

The slide features two decorative horizontal bars, one at the top and one at the bottom. Each bar consists of a blue upper section and an orange lower section. The text 'BACKUP SLIDES' is centered between these bars.

# BACKUP SLIDES

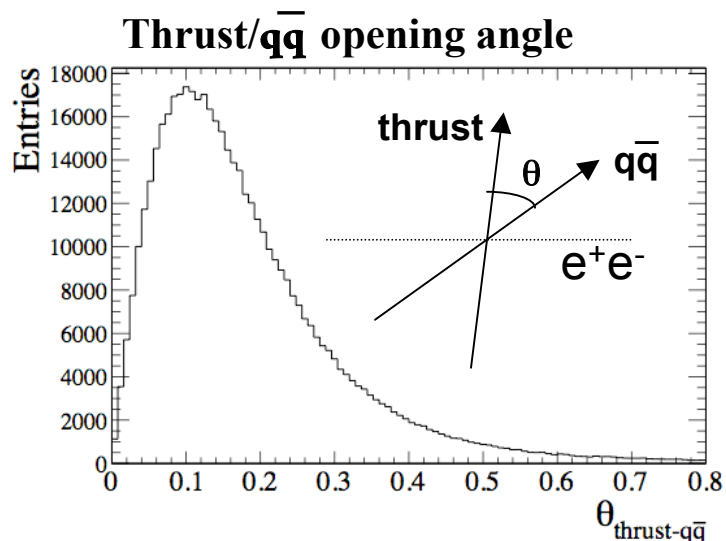
# $D^{*\pm}$ -enhanced control sample



$D^{*\pm} \rightarrow D^0\pi^\pm$ ,  $D^0 \rightarrow K\pi$  (mode 1)  
 $D^0 \rightarrow K3\pi$  (mode 2)  
 $D^0 \rightarrow K\pi\pi^0$  (mode 3)  
 $D^0 \rightarrow K_S\pi\pi$  (mode 4)

$1.835 < M_{D^0} < 1.895 \text{ GeV}/c^2$   
 $0.1425 < \Delta M < 0.149 \text{ GeV}/c^2$   
 $(\Delta M = M_{D^{*\pm}} - M_{D^0})$

# Asymmetry dilution



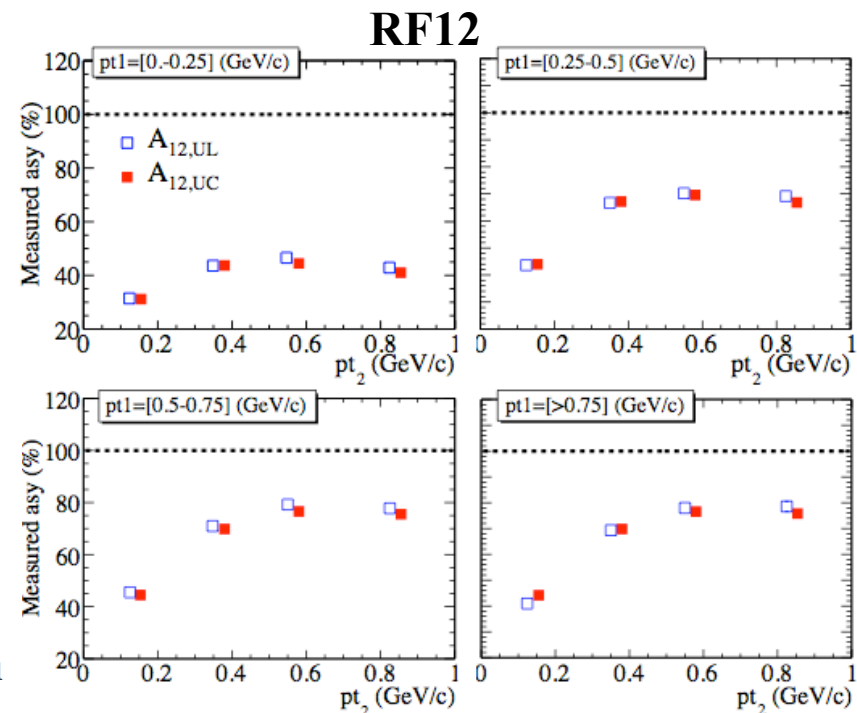
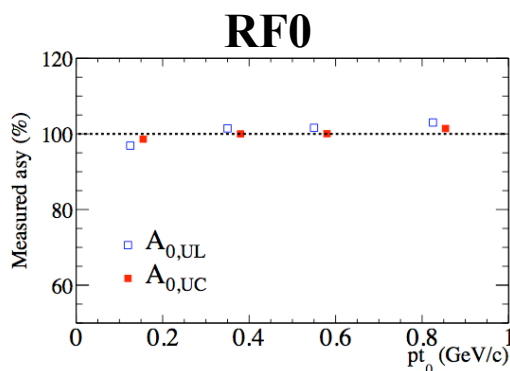
The experimental method assumes the thrust axis as  $q\bar{q}$  direction: this is only a rough approximation

**RF12:** large smearing since the azimuthal angles  $\phi_1$  and  $\phi_2$  are calculated with respect to the thrust axis; additional dilution due to very energetic tracks close to the thrust axis.

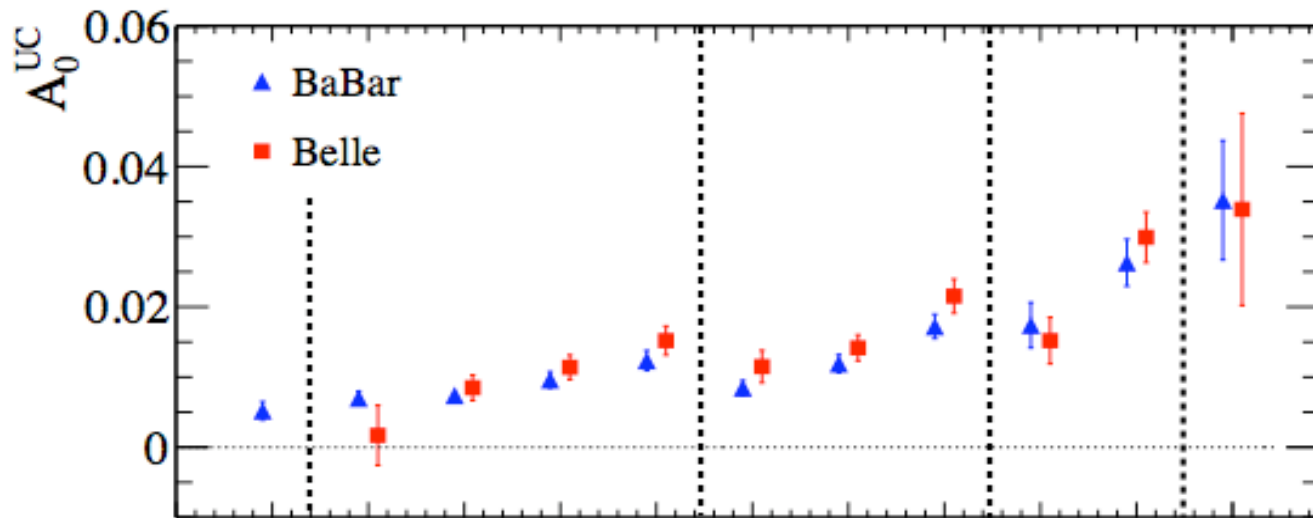
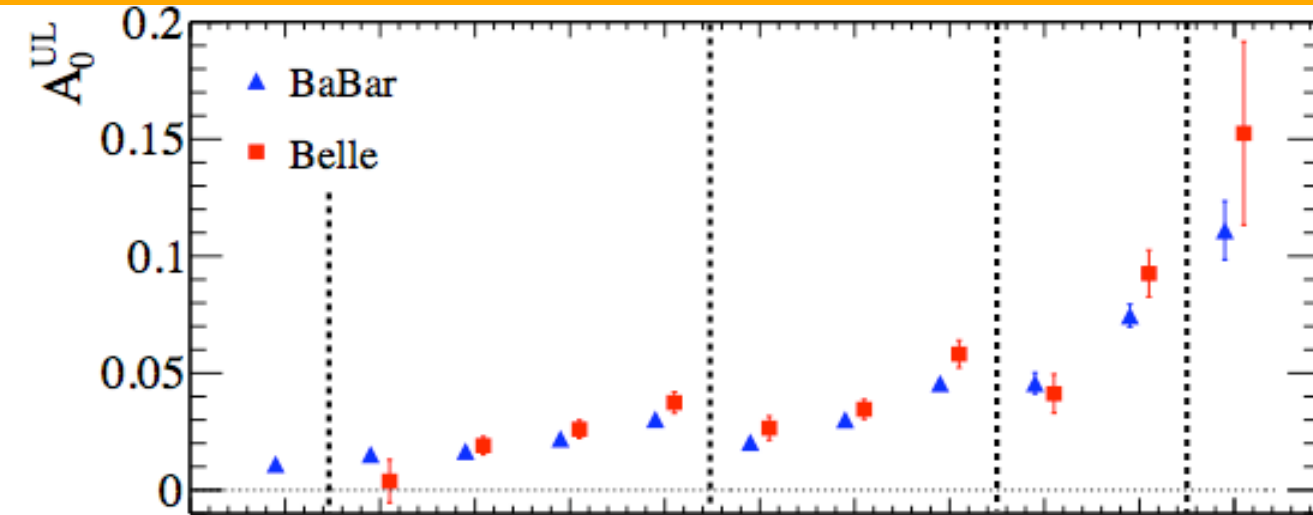
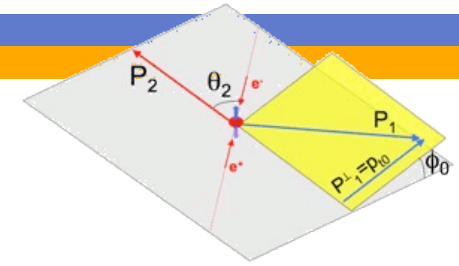
**RF0:** the azimuthal angle  $\phi_0$  is calculated with respect to the second hadron momenta  $\rightarrow$  small smearing due to PID and tracking resolution.

$\rightarrow$  We study the influence of the detector effects by correcting a posteriori the generated angular distribution: weights defined as  $w^{UL(UC)} = 1 \pm a \cdot \cos(\phi_{gen12,0})$  are applied to every selected pion pairs.

**RF12:** correction performed for each bins of  $z$  and  $p_t$ :  
 (1.3-2.3) as a function of  $z$ , and  
 (1.3-3) as a function of  $p_t$ .  
**RF0:** no correction needed.



# RFO:BaBar/Belle asymmetries comparisons



1 2 3 4 5 6 7 8 9 10 11  $(z_1, z_2)_{\text{bin}}$

0.15-0.2 | 0.2-0.3 | 0.3-0.5 | 0.5-0.7 | >0.7

0.15-0.2 | 0.2-0.3 | 0.3-0.5 | 0.5-0.7 | >0.7 | 0.3-0.5 | 0.5-0.7 | >0.7 | 0.5-0.7 | >0.7 | >0.7

0.15-0.2 | 0.2-0.3 | 0.3-0.5 | 0.5-0.7 | >0.7 | 0.3-0.5 | 0.5-0.7 | >0.7 | 0.5-0.7 | >0.7 | >0.7

**BaBar** ( $0.15 < z < 0.9$ )  $\mathcal{L} \sim 470 \text{ fb}^{-1}$

**Belle** ( $0.2 < z < 1$ )  $\mathcal{L} \sim 547 \text{ fb}^{-1}$

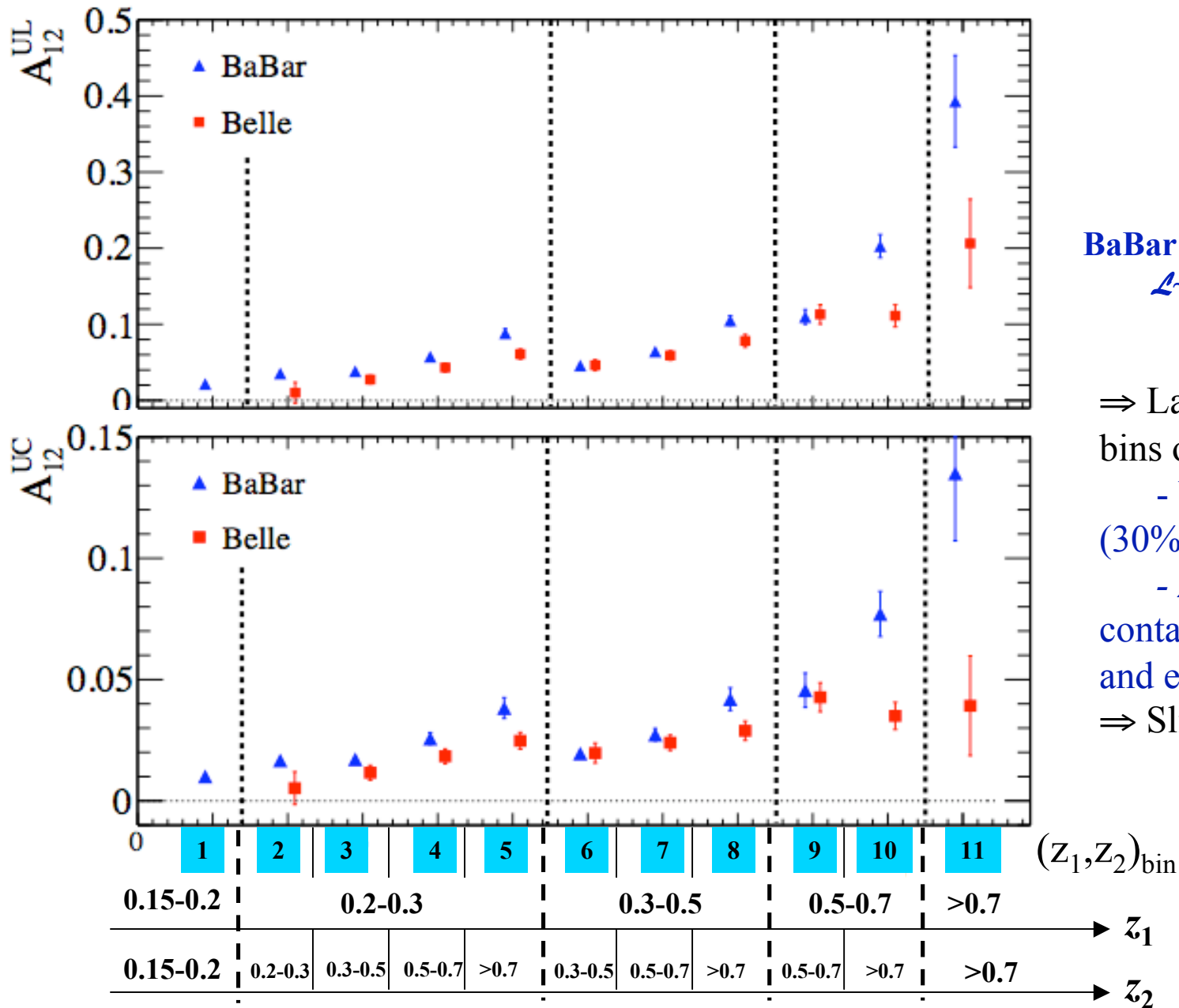
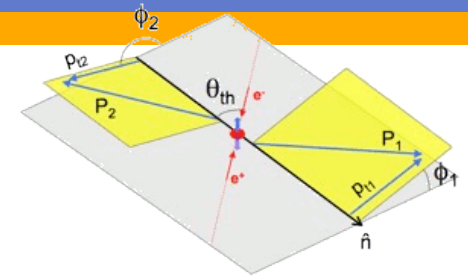
PRD 86, 039905(E) (2012)

In order to perform this comparison, we used 10 (+1) symmetrized  $z$ -bin subdivisions, averaging the measured Belle and BaBar asymmetries which fell in the same symmetric bins

$A_0^{\text{UL}}$  and  $A_0^{\text{UC}}$  : good agreement between the **BaBar** asymmetries and the **Belle** results.



# RF1 2: BaBar/Belle comparisons



**BaBar ( $0.15 < z < 0.9$ )**  $\mathcal{L} \sim 470 \text{ fb}^{-1}$   
**Belle ( $0.2 < z < 1$ )**  $\mathcal{L} \sim 547 \text{ fb}^{-1}$   
 PRD 86, 039905(E) (2012)

⇒ Large discrepancy in the last two bins of  $z$ :

- bin-by-bin correction factors (30%)
- $z < 0.9$  to remove the contamination from  $\mu\mu\gamma$  background and exclusive events

⇒ Slightly higher at lower  $z$