#### A MODEL OF DIFFRACTION



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# TOPICS

□ Introduction: □ Diffractive ross sections: soft SD, DD, DPE or CD  $\rightarrow$  multigap diffraction?  $\triangleright$  also: total, elastic  $\rightarrow$  total-inelastic **and:** hard dfiffraction Final states: pt, multiplicity (track-, total-), **particle ID**  $\square$  Issues: unitarization, factorization-breaking, "gap survival"  $\square$  Implementation in PYTHIA8  $\rightarrow$  talk of Robert Ciesielski in this session

For details of the model see talk and proceedings of: DIFFRACTION 2010 "Diffractive and total pp cross sections at the LHC and beyond" (KG) http://link.aip.org/link/doi/10.1063/1.3601406

# REMARKS

RENORM (renormalization model)

Tested using MBR (Minimum Bias Rockefeller) simulation at CDF

□ Difraction derived from inclusive PDFs and QCD color factors.

Absolute normalization!

#### **Q HADRONIZATION**

Robert's talk

 $\triangleright$  MBR produces only  $\pi^{\pm}$  and  $\pi^{0}$  's using a modified gamma distribution  $\triangleright$  predicts distributions of multiplicity, dN/d $\eta$ , and  $p_T$  PYTHIA8-MBR is an update of PYTHIA8, as of PYTHIA8.165 MBR distributions with hadronization done by PYTHIA8 Work in progress: tune PYTHIA8-MBR to reproduce MBR distributions

 $\Box$  Total Cross section  $\rightarrow$  formula based on a glue-ball-like saturated-exchange.

#### DIFFRACTION IN QCD

#### Non-diffractive events

**\* color-exchange → n-gaps** exponentially suppressed

#### Diffractive events

- **❖ Colorless vacuum exchange**
- $\rightarrow$   $\eta$ -gaps not exp'ly suppressed



Goal: probe the QCD nature of the diffractive exchange

#### **DEFINITIONS**



#### DIFFRACTION AT CDF



# Basic and combined diffraction of the Basic and combined diffractive processes



4-gap diffractive process-Snowmass 2001- **<http://arxiv.org/pdf/hep-ph/0110240>**



# Regge theory – values of s<sub>o</sub> &  $g_{PPP}$ ?



# A complication ...  $\rightarrow$  Unitarity!

$$
\left(\frac{d\sigma_{el}}{dt}\right)_{t=0} \sim \left(\frac{s}{s_0}\right)^{2\epsilon}, \ \sigma_t \sim \left(\frac{s}{s_0}\right)^{\epsilon}, \text{ and } \sigma_{sd} \sim \left(\frac{s}{s_0}\right)^{2\epsilon}
$$

 $\Box$   $\sigma_{sd}$  grows faster than  $\sigma_t$  as *s* increases  $*$ → unitarity violation at high *s* (similarly for partial x-sections in impact parameter space)

the unitarity limit is already reached at √*s* ~ 2 TeV !

 $\Box$  need unitarization

\* similarly for  $(d\sigma_{el}/dt)_{t=0}$  vs  $\sigma_t$ , but this is handled differently in RENORM.



KG → CORFU-2001: http://arxiv.org/abs/hep-ph/0203141



$$
\begin{array}{c}\n\text{Color} \\
\text{factor} \\
\hline\n\end{array}\n\begin{aligned}\n\kappa &= \frac{g_{p-p-p}(t)}{\beta_{p-p-p}(0)} \approx 0.17 \\
\hline\n\text{Experimentally:} \\
\hline\n\text{RGEJM}, \text{PRD 59 (114017) 1999}\n\end{aligned}\n\begin{aligned}\n\kappa &= \frac{g_{p-p-p}}{\beta_{p-p}} = 0.17 \pm 0.02, \quad \varepsilon = 0.104 \\
\hline\n\text{RGEJM}, \text{PRD 59 (114017) 1999}\n\end{aligned}
$$
\n
$$
\text{QCD:} \quad \kappa = f_g \times \frac{1}{N_c^2 - 1} + f_g \times \frac{1}{N_c} = \frac{Q^2}{\lambda} = \frac{1}{N_c} \Rightarrow 0.75 \times \frac{1}{8} + 0.25 \times \frac{1}{3} = 0.18
$$

$$
\frac{d^2 \sigma_{sd}(s, M^2, t)}{dM^2 dt} = \left[\frac{\sigma_o}{16\pi} \sigma_o^{I\!\!Pp}\right] \frac{s^{2\epsilon}}{N(s, s_o)} \frac{e^{bt}}{(M^2)^{1+\epsilon}}
$$
\n
$$
b = b_0 + 2\alpha' \ln \frac{s}{M^2} \qquad s_o^{\text{CMG}} = (3.7 \pm 1.5) \text{ GeV}^2
$$
\n
$$
N(s, s_o) \equiv \int_{\xi_{\text{min}}}^{\xi_{\text{max}}} d\xi \int_{t=0}^{-\infty} dt f_{I\!\!P/p}(\xi, t) \stackrel{s \to \infty}{\to} \infty s_o^{\epsilon} \frac{s^{2\epsilon}}{\ln s}
$$
\n
$$
\frac{d^2 \sigma_{sd}(s, M^2, t)}{dM^2 dt} \stackrel{s \to \infty}{\to} \infty \ln s \frac{e^{bt}}{(M^2)^{1+\epsilon}}
$$
\nset to unity\n
$$
\sigma_{sd} \stackrel{s \to \infty}{\longrightarrow} \infty \frac{\ln s}{b \to \ln s} \Rightarrow const
$$
\n
$$
\sigma_{sd} \stackrel{s \to \infty}{\to} \infty \frac{\ln s}{b \to \ln s} \Rightarrow const
$$

$$
\frac{d^2 \sigma}{dt d\Delta y} = N_{gap} \cdot C \cdot F_p^2(t) \cdot \left\{ e^{(\varepsilon + \alpha' t) \Delta y} \right\}^2 \cdot \kappa \cdot \left\{ \sigma_o e^{\varepsilon \Delta y'} \right\}
$$
  
\n
$$
N_{gap}^{-1}(s) = \int_{\Delta y, t} P_{gap}(\Delta y, t) d\Delta y dt \xrightarrow{s \to \infty} C' \cdot \frac{s^{2\varepsilon}}{\ln s}
$$
  
\n
$$
\frac{d^2 \sigma}{dt d\Delta y} = C'' \left[ e^{\varepsilon (\Delta y - \ln s)} \cdot \ln s \right] e^{(b_0 + 2\alpha' \Delta y)t}
$$
  
\ngrows slower than s<sup>ε</sup>  
\n
$$
\Rightarrow
$$
 Pumplin bound obeyed at all impact parameters

### M<sup>2</sup> distribution: data  $\rightarrow$  do/dM<sup>2</sup>|<sub>t=-0.05</sub> ~ independent of s over 6 orders of magnitude!



Independent of s over 6 orders of magnitude in M<sup>2</sup>  $\rightarrow$  M<sup>2</sup> scaling



 $\rightarrow$  factorization breaks down to ensure M<sup>2</sup> scaling

# **Scale s<sub>o</sub> and PPP coupling**



### Saturation at low Q<sup>2</sup> and small-x



# DD at CDF: comparison with MBR

http://physics.rockefeller.edu/publications.html



# Multigap cross sections, e.g. SDD



## DD at CDF



## SDD at CDF



## CD/DPE at CDF



### Difractive x-sections



$$
\beta^2(t) = \beta^2(0)F^2(t)
$$

$$
F^2(t)=\left[\frac{4m_p^2-2.8t}{4m_p^2-t}\left(\frac{1}{1-\frac{t}{0.71}}\right)^2\right]^2\approx a_1e^{b_1t}+a_2e^{b_2t}
$$

 $\alpha_1$ =0.9,  $\alpha_2$ =0.1, b<sub>1</sub>=4.6 GeV<sup>-2</sup>, b<sub>2</sub>=0.6 GeV<sup>-2</sup>, s'=s e<sup>-∆y</sup>, к=0.17, κβ<sup>2</sup>(0)= $\sigma_0$ , s $_0$ =1 GeV<sup>2</sup>,  $\sigma_0$ =2.82 mb or 7.25 GeV<sup>-2</sup>



Use the Froissart formula as a *saturated* cross section r

$$
\sigma_t(s > s_F) = \sigma_t(s_F) + \frac{\pi}{m^2} \cdot \ln^2 \frac{s}{s_F}
$$



- This formula should be valid above the knee in  $\sigma_{sd}$  vs.  $\sqrt{s}$  at  $\sqrt{s_F} = 22$  GeV (Fig. 1) and therefore valid at  $\sqrt{s} = 1800$  GeV.
- Use  $m^2 = s_o$  in the Froissart formula multiplied by 1/0.389 to convert it to mb<sup>-1</sup>.
- Note that contributions from Reggeon exchanges at  $\sqrt{s} = 1800$  GeV are negligible, as can be verified from the global fit of Ref. [7].
- Obtain the total cross section at the LHC:

$$
\sigma_t^{\text{LHC}} = \sigma_t^{\text{CDF}} + \frac{\pi}{s_o} \cdot \left( \ln^2 \frac{s^{\text{LHC}}}{s_F} - \ln^2 \frac{s^{\text{CDF}}}{s_F} \right)
$$

#### **SUPERBALL MODEL**

$$
\frac{98 \pm 8 \text{ mb at 7 TeV}}{109 \pm 12 \text{ mb at 14 TeV}}
$$

# Reduce the uncertainty in  $s_0$

#### **Saturation glueball?**



## Total, elastic, and inelastic x-sections

$$
\sigma_{\text{ND}} = (\sigma_{\text{tot}} - \sigma_{\text{el}}) - (2\sigma_{\text{SD}} + \sigma_{\text{DD}} + \sigma_{\text{CD}})
$$

R. J. M. Covolan, K. Goulianos, J. Montanha, Phys. Lett. B 389, 176 (1996)

$$
\sigma_{\text{tot}}^{p^{\pm}p} = \begin{cases} 16.79s^{0.104} + 60.81s^{-0.32} \mp 31.68s^{-0.54} & \text{for } \sqrt{s} < 1.8\\ \sigma_{\text{tot}}^{\text{CDF}} + \frac{\pi}{s_0} \left[ \left( \ln \frac{s}{s_F} \right)^2 - \left( \ln \frac{s^{\text{CDF}}}{s_F} \right)^2 \right] & \text{for } \sqrt{s} \ge 1.8 \end{cases}
$$

K. Goulianos, Diffraction, Saturation and pp Cross Sections at the LHC,  $arXiv:1105.4916.$ 

$$
\sqrt{s^{CDF}} = 1.8 \text{ TeV}, \sigma_{\text{tot}}^{\text{CDF}} = 80.03 \pm 2.24 \text{ mb}
$$
  
 $\sqrt{s_F} = 22 \text{ GeV}$   $s_0 = 3.7 \pm 1.5 \text{ GeV}^2$ 

## TOTEM vs PYTHIA8-MBR



## ALICE tot-inel vs PYTHIA8-MBR



## ALICE SD and DD vs PYTHIA8-MBR



### CMS Total-Inelastic Cross Section compared to PYTHIA8 and PYTHIA8-MBR



### More on cross sections

#### Slide 12 from Uri Maor's talk at the LowX-2012



## Monte Carlo Strategy for the LHC …

### **MONTE CARLO STRATEGY**

- $\Box$   $\sigma$ <sup>T</sup>  $\rightarrow$  from SUPERBALL model
- $\Box$  optical theorem  $\rightarrow$  Im f<sub>el</sub>(t=0)
- **Q** dispersion relations  $\rightarrow$  Re f<sub>el</sub>(t=0)
- $\Box$   $\sigma$ <sup>el</sup>

 $\sigma$ <sub>T</sub>  **optical theorem**  $Im f_{el}$ ( $t=0$ )  **dispersion relations Re fel(t=0)**

 $\Box$   $\sigma$ inel

- **Q** differential σ<sup>sp</sup> → from RENORM
- **□ use nesting of final states (FSs) for**
- *pp* collisions at the *IPp* sub-energy √s'

*Strategy similar to that of MBR used in CDF based on multiplicities from: K. Goulianos, Phys. Lett. B 193 (1987) 151* pp

"A new statistical description of hardonic and e<sup>+</sup>e<sup>-</sup> multiplicity distributios "

## Monte Carlo algorithm - nesting



# SUMMARY

**Q** Introduction **□** Diffractive cross sections > basic: SD<sub>p</sub>, SD<sub>p</sub>, DD, DPE combined: multigap x-sections  $\triangleright$  ND  $\rightarrow$  no-gaps: final state from MC with no gaps ❖ this is the only final state to be tuned **□** Total, elastic, and inelastic cross sections □ Monte Carlo strategy for the LHC – "nesting" **derived from ND and QCD color factors** *Thank you for your attention*