

2nd HERA-LHC Workshop

(Working Group 3)

Heavy Quarks

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Conveners

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**Review of the 1st workshop (theory)
including some news from DIS2006**

1st HERA-LHC Workshop

(Start-up meeting: March 2004, final presentation: March 2005)

Theory aspects:

- **Production: Benchmark cross sections**
Schemes: fixed-order / resummed; Monte Carlo
- **Fragmentation**
- **Soft-gluon resummation**
- **k_T factorization**
(correlations in $Q\bar{Q}$ production, quarkonium production, associated Higgs + jet production)
- **$\Lambda / \bar{\Lambda}$ asymmetries in the QGSM**

Experimental aspects:

- **Overview of HERA results**
(open charm, open beauty, quarkonium, $F_2^c, F_2^b, Q\bar{Q}$ correlations, $c \rightarrow H_c$ fragmentation)
- **Detection: Trigger and Reconstruction at the LHC experiments**

Heavy Quarks as a Test of QCD

- **Basic formulae:**

$$d\sigma_Q = \int dx_1 dx_2 \int dz$$

$$f_{a/h_1}(x_1, \mu_F) f_{b/h_2}(x_2, \mu_F)$$

$$\times d\hat{\sigma}(a + b \rightarrow Q + X)$$

$$d\sigma_H = \int dz d\sigma_Q \times D_{H/Q}(z, \mu_F)$$

PDFs for partons a, b

× **hard scattering, produce heavy quark** $Q = c, b$

× **fragmentation into hadron** H

+ **power corrections**

- **Schemes:**

massive scheme (FFNS):

$m_Q \neq 0$, initial state: $a, b = g, q, \bar{q}$, final state: Q, \bar{Q}
threshold region OK, large logs: $\ln(p_T^2/m_Q^2)$

massless scheme (ZM-VFNS):

$m_Q = 0$, initial state: $a, b = g, q, \bar{q}, Q, \bar{Q}$
improvement at large p_T : resums large logs
in heavy quark **PDFs**

- **Matching:**

transition region ? → **FONLL, GM-VFNS**

Heavy Quark PDFs

- **CTeQ**: simplified ACOT (SACOT $_{\chi}$)
a general-mass (**GM**) scheme

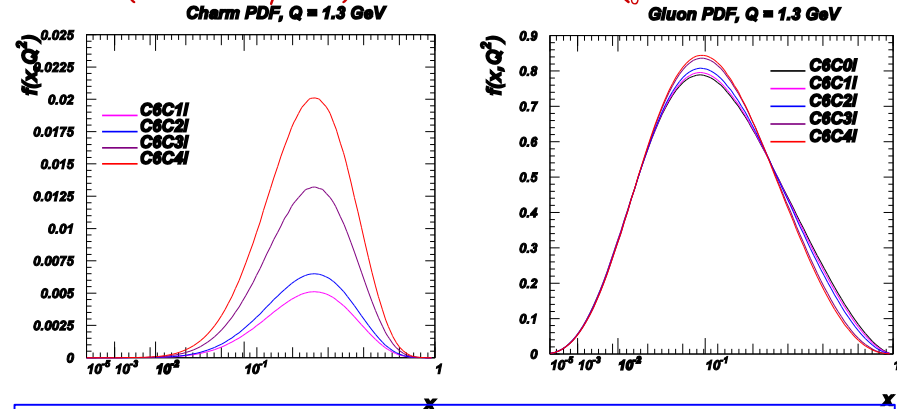
more natural parton kinematics:

$$\chi = x \left(1 + \frac{(\sum M)_{\text{final}}^2}{Q^2} \right)$$

- smooth and physical
threshold behavior (F_2 , F_L)
- simplicity
- Is there a non-perturbative charm component in the nucleon?
 - preliminary results shown at DIS2006
 - await more accurate data from **HERA II**
impact on phenomenology at LHC

Charm and Gluon Distributions at $Q = 1.3 \text{ GeV}$

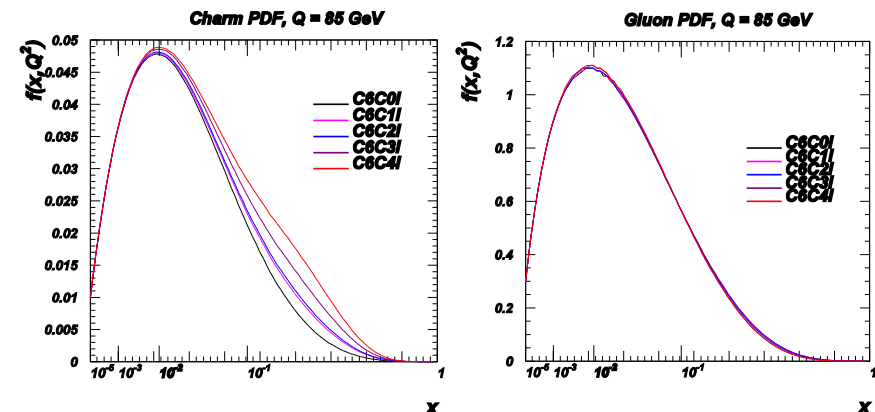
Varying amounts of input lightcone charm components
(à la Brodsky et al.): Momentum frac. at $Q_0 = 0 - 0.02$.



Horizontal axis is scaled in $x^{1/3}$ —in between linear and log—in order to exhibit the behavior at both large and small x .

Charm and Gluon Distributions at $Q^2 = (85 \text{ GeV})^2$

Varying amounts of input lightcone charm components
(à la Brodsky et al.): Momentum frac. at $Q_0 = 0 - 0.02$.



* Very substantial amount of charm, over the radiatively generated component (C6C0I), still persists at this very large scale → there can be interesting phenomenological consequences even at LHC.

Heavy Quark PDFs: NNLO ?

W K Tung: NNLO not urgent: out-weighted by other sources of uncertainties, like parametrizations, power-law corrections

Roberts, Thorne: detailed prescription for DIS structure function at NNLO

ZM-VFNS not feasible at NNLO: discontinuities in F_2^c !

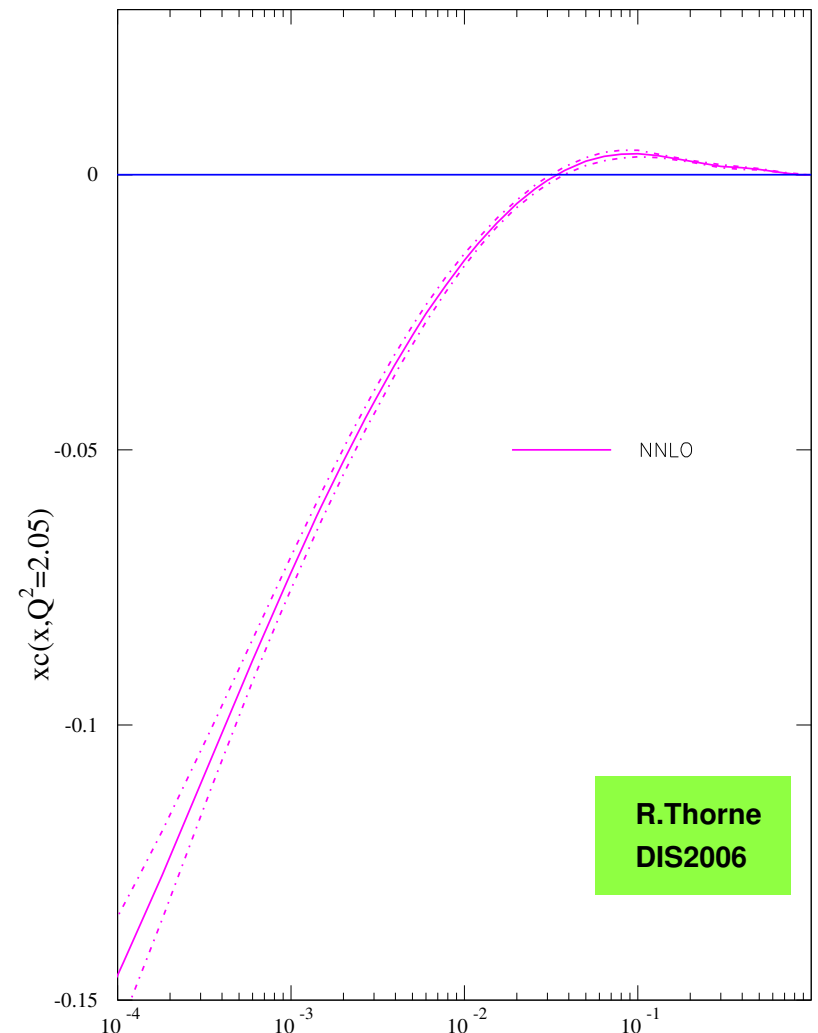
TR-VFNS: shift m^2/Q^2 terms between coefficient functions imposing constraints (smoothness of $dF_2/d\ln Q^2$, freeze higher-order α_s terms when going through threshold $Q^2 = m_c^2$)

→ continuous F_2 , but discontinuous and **negative PDFs**

F_2^c not well-defined at NNLO: not IR-safe

sophisticated and complicated

unclear how this works for other processes



Heavy Quark Fragmentation

up to now: FFs for $g, q, \bar{q}, Q, \bar{Q} \rightarrow H$ fitted to phenomenological forms, HQ contribution “switched on” at threshold **but**

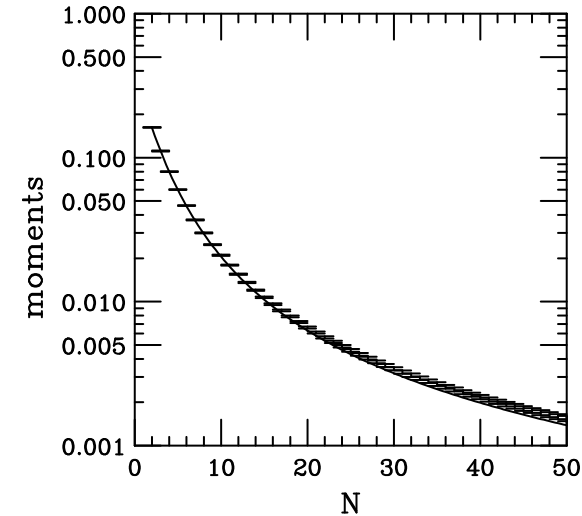
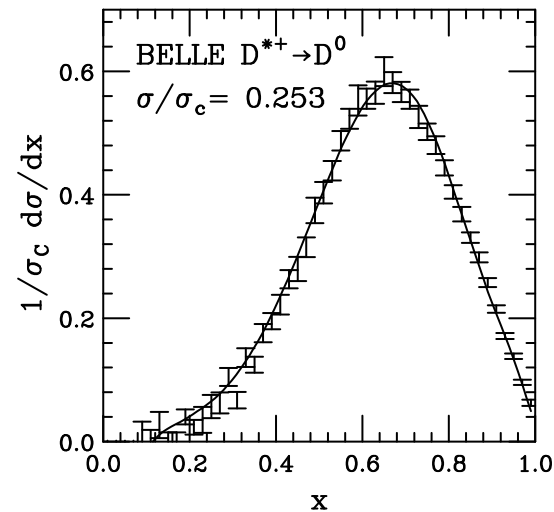
FFs have thresholds like PDFs, need matching across threshold (Cacciari, Nason, Oleari, see DIS2006)

now available: time-like equivalent of Collins-Tung relations for PDFs: parametrize light partons (g, q, \bar{q}), generate HQ FFs radiatively

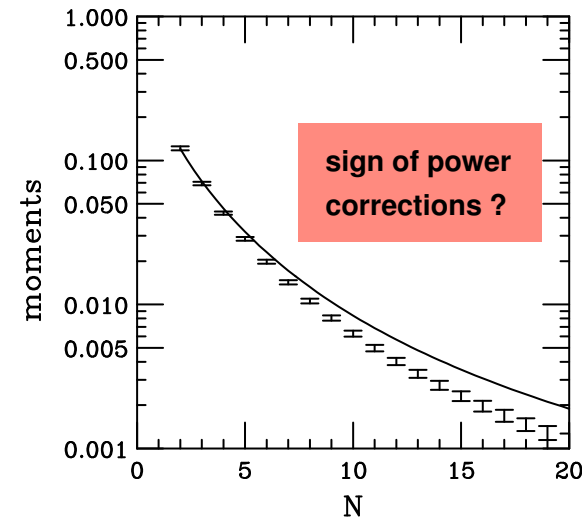
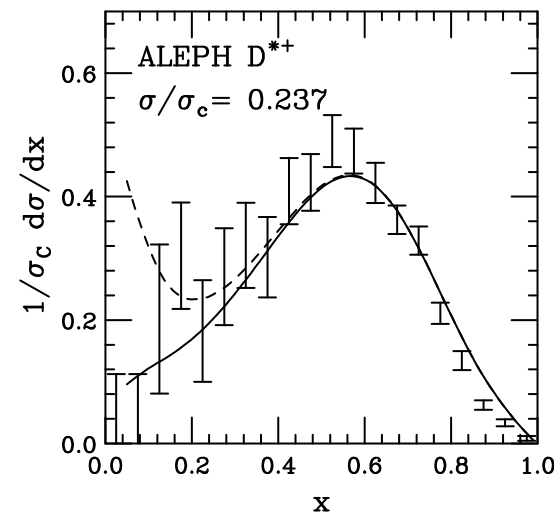
→ allow global fits

Oleari (DIS2006): fit to BELLE, CLEO and ALEPH data

include Tevatron and HERA II data



C.Oleari
DIS2006



Benchmark Cross Sections

Different theoretical approaches, for **single-inclusive HQ production**:

- **(F)MNR**: fixed-order at NLO (for γp and pp)
- **HVQDIS**: fixed-order at NLO (for DIS)
- **FONLL**: NLO + leading log's resummed
- **GM-VFNS**: NLO + leading log's resummed
- **CASCADE**: MC, k_T factorization
- **RAPGAP**: MC, LO $\gamma^* g \rightarrow Q\bar{Q}$

same input (as far as possible: $\alpha_s, m_c, m_b, \text{PDF}$)

uncertainty bands – mainly from scale variation: $\frac{1}{2}\mu_0 < \mu_F, \mu_R < 2\mu_0$ with $\mu_0 = m_T =$

$\sqrt{m_Q^2 + p_T^2}$ or $\sqrt{4m_Q^2 + Q^2}$ (for DIS)

- To be improved:**
- dependence on PDF
 - dependence on fragmentation
 - MC implementation

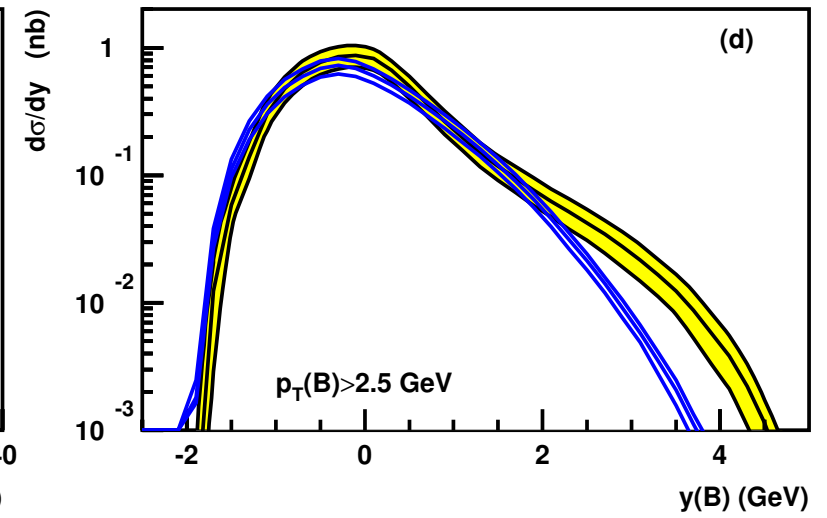
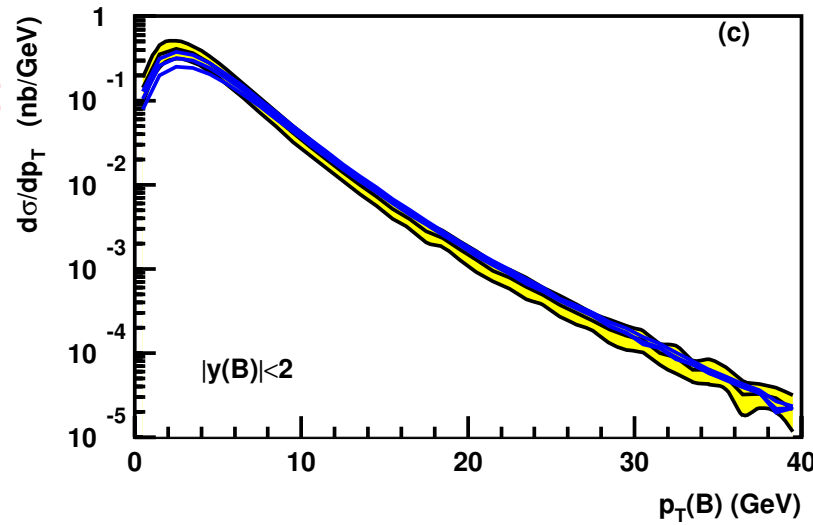
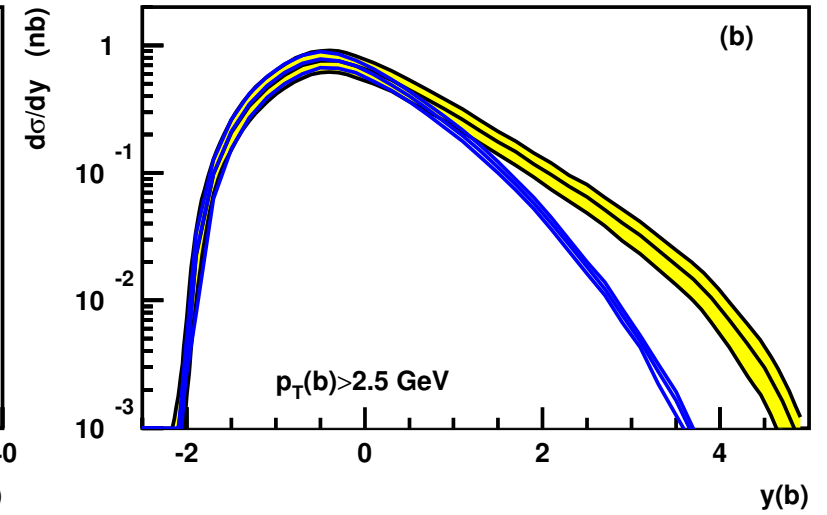
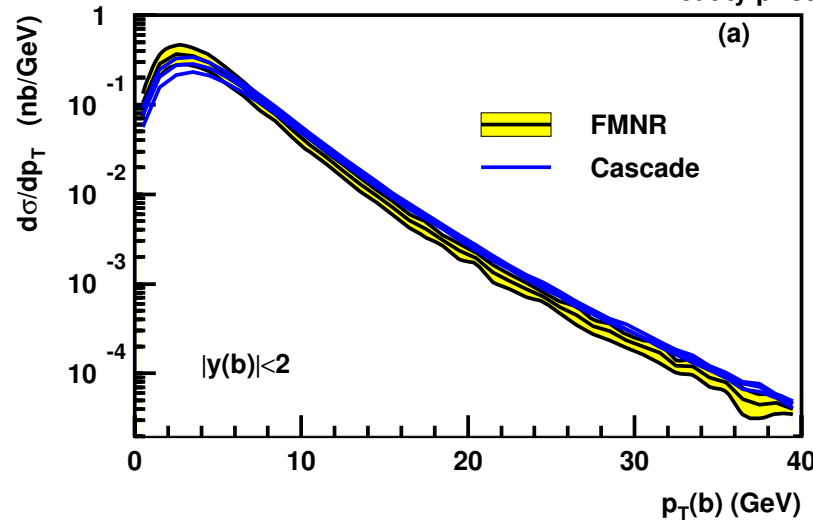
Example: Beauty Photoproduction

Predictions from

- FMNR
- CASCADE

Need improvement
at high y

Beauty photoproduction at HERA

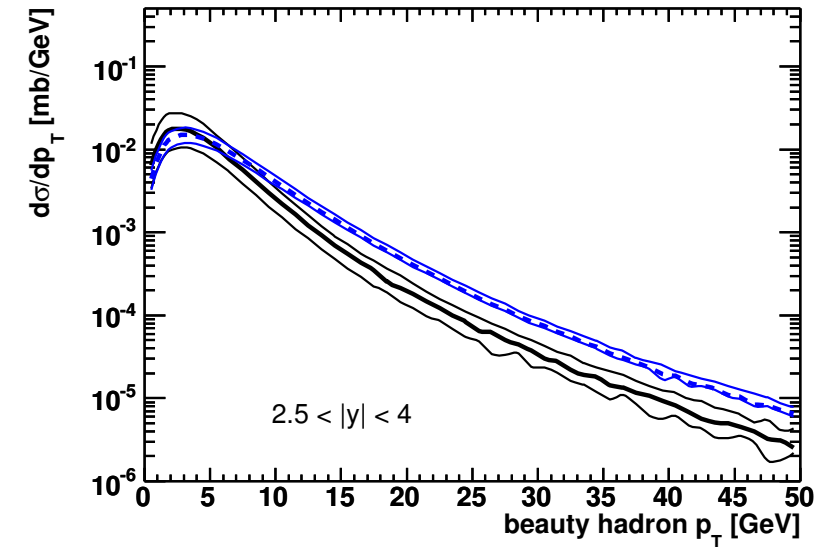
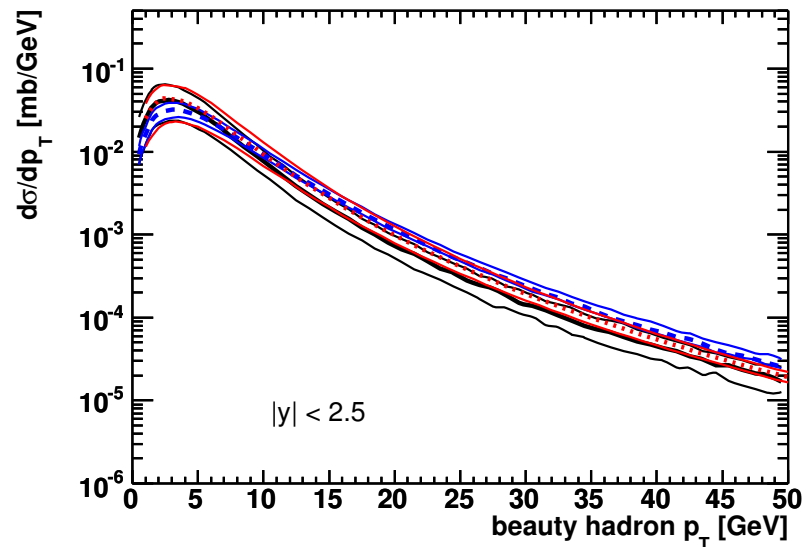
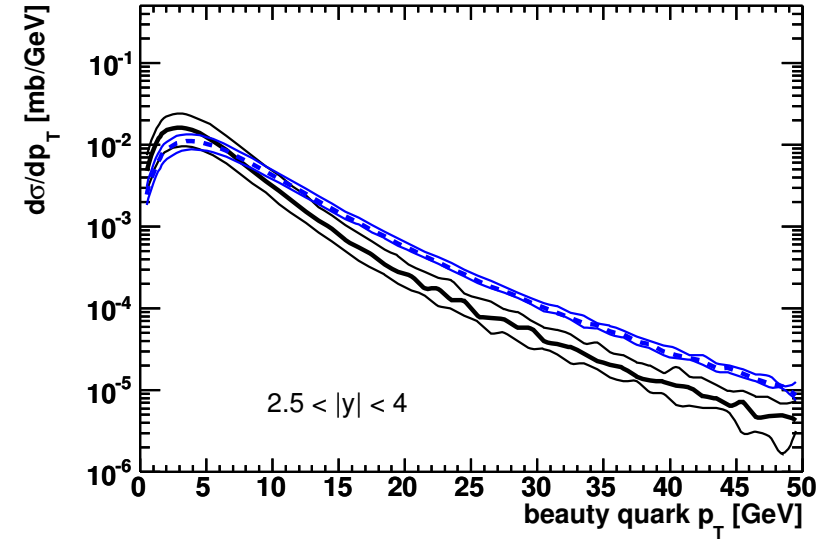
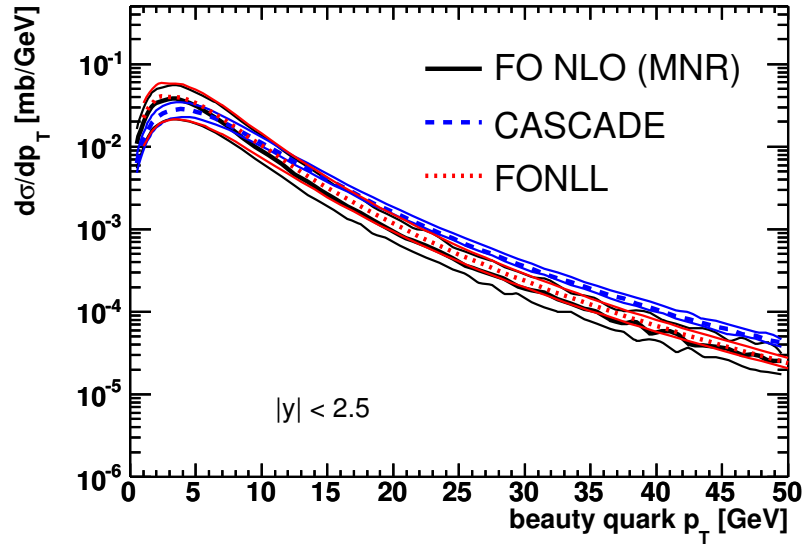


Example: Beauty Production at the LHC

Predictions from

- MNR
- FONLL
- CASCADE

Factor of up to 5
uncertainty
at high p_T, y



Soft-Gluon Resummation

Remnants of long-distance dynamics \rightarrow logarithmic terms, singular near edges of phase space.

Threshold resummation

perturbative result for observable ω

$$\omega = 1 + \alpha_s (L^2 + L + 1) + \alpha_s^2 (L^4 + L^3 + L^2 + L + 1) + \dots$$

resummed:

$$\omega = \exp \{ L g_1(\alpha_s L) + g_2(\alpha_s L) + \dots \} + \text{suppressed terms}$$

for the differential structure function $d^2 F_2^Q / dT dU$ (**Eynck, Laenen, Moch**):

$$g_1(\lambda) = \frac{C_F}{\pi b_0 \lambda} (\lambda + (1 - \lambda) \ln(1 - \lambda))$$

with $\lambda = b_0 \alpha_s \ln N$ and $L^i = \left(\frac{\ln^{i-1}(\rho)}{\rho} \right)_+$, $\rho = \frac{s_4}{m_Q^2}$, $M_{X'}^2 = m_Q^2 + s_4$

\rightarrow reduced scale dependence

Other observables ? e.g. heavy quark + jet

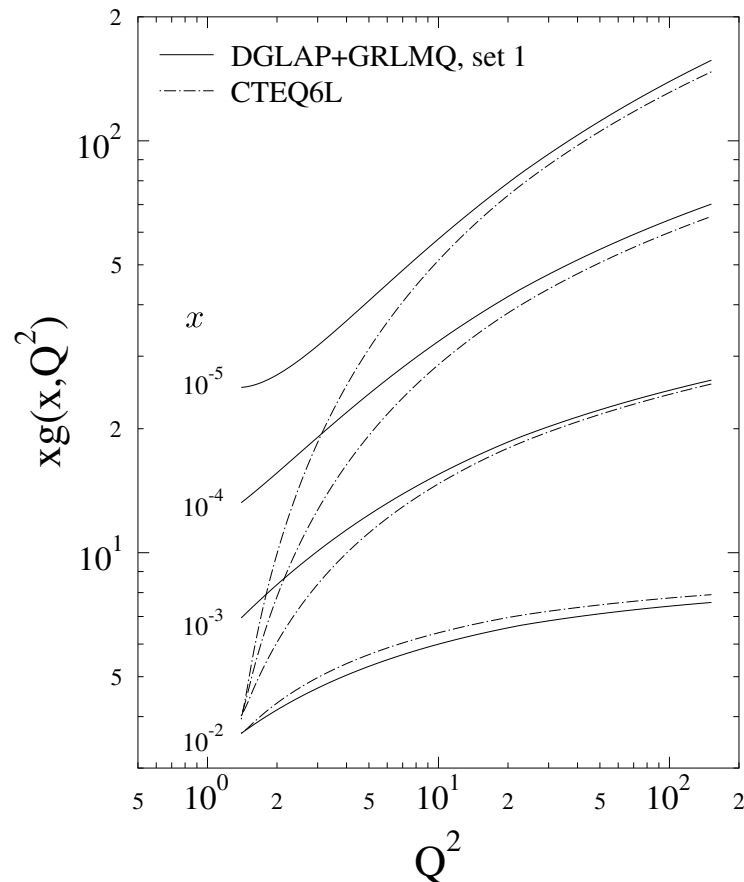
Small-x Effects

($x < 10^{-4}$, Q^2 in perturbative regime)

GLRMQ

DGLAP + non-linear g recombination

- enhanced gluon
- enhanced b production at LHC

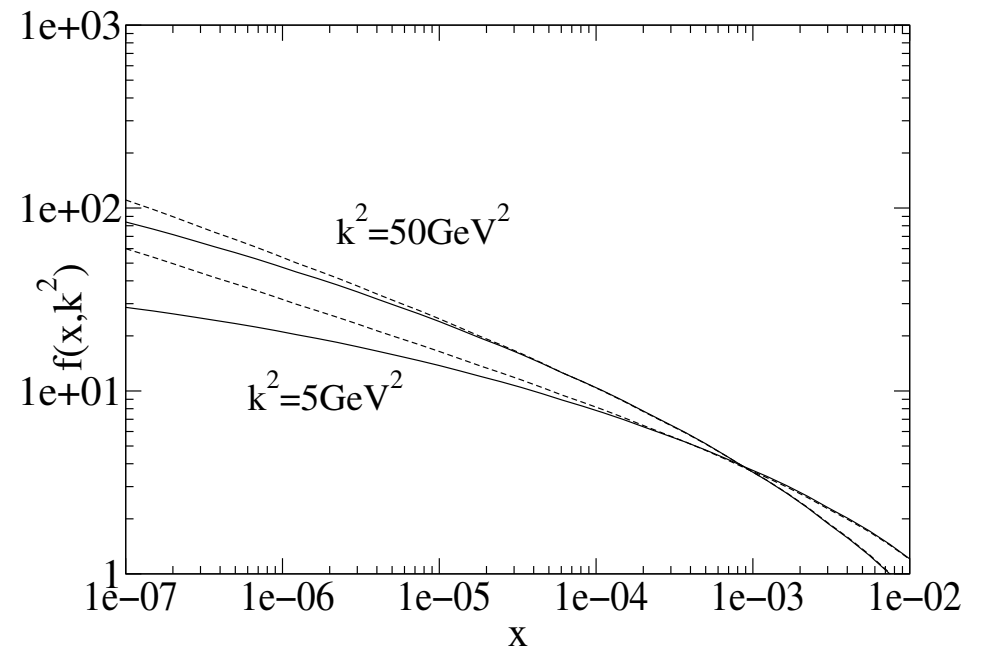


KKMS

DGLAP + BK saturation effects

k_T -factorization (unintegrated PDF)

- suppressed gluon
- suppressed b production at LHC ?



Small- x Effects

GLRMQ

(Eskola, Kolhinen, Vogt)

- based on LO evolution
- include NLO corrections !

KKMS*

(Jung, Kutak, Peters, Motyka)

- comprises:
 - + BFKL with subleading $\ln 1/x$ terms
 - + non-singular parts of DGLAP
 - + quark singlet from DGLAP
 - + non-linear terms from **BK**
 - + choice of scale in α_s
 - unified prescription?
- no significant effect within ALICE/
CMS acceptance (Peters DIS2006)

Let $pp \rightarrow c + X$ at the LHC decide?

* Kutak, Kwiecinski, Martin, Stasto

Conclusion for Heavy Quarks at the LHC

- **PDFs**: input comes from **HERA I/II**
compare TR-VFNS and SACOT _{χ} ! Do we need NNLO ?
- **FFs**: global fits ? Include Tevatron and **HERA II** data !
- **Benchmark cross sections**: source of discrepancies (FF?), improve MC implementation and test at **HERA II** !
- **HQ schemes**: work out also for signal processes ($b + \bar{b} \rightarrow H$, $c + s \rightarrow H^+$, but also $W/Z/\gamma +$ tagged HQ) !
- k_T **factorization**: use **HERA II** data to determine unintegrated PDFs \rightarrow work out predictions for LHC !