

# Double Constrained Evolutions in a single Monte Carlo for the DY-type processes – A prototype

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# Outline

- Introduction, terminology
- Single QCD evolution in Cracow 2005/06
- CMC in a nutshell
- Mapping to 4momenta, single evolution
- Joining 2 single evolution into one gluonstrahlung MC (LL) for W/Z production:
  - Mapping, phase space parametrization
  - Basic distribution for double evolution
  - Realizing constraint on  $\hat{s}$  at the 4-momenta level.
  - Preliminary MC results (rapidity and  $p_T$  of W/Z and emitted gluons.
- Summary, prospects, problems...

## Acknowledgments, warnings....

**I am indebted to all my colleagues in the INP Cracow group for discussion and encouragement in pursuing this work, especially to M. Skrzypek and P. Stephens.**

**I would like to thank CERN/PH/TH for hospitality and support in realizing our TOK project on the development of Monte Carlo tools for LHC.**

**Presented new numerical results are very preliminary, only a few days/weeks old and may change.**

# Single “QCD Evolution” using Monte Carlo, various types

Evolution types and solution methods:

- Evolution: Common forward, unconstrained, (ISR, FSR):
  - Method of solving: straightforward Markovian MC algorithm (**MMC**)
- Evolution: Constrained (ISR):
  - Method: Constrained MC algorithm, non-Markovian (**CMC**)
  - Method: “Backward evolution” MC algorithm, Markovian (PYTHIA, HERWIG,...)

Terminology:

“**Markovian MC**”: Emission multiplicity generated as **last** variable in the MC,

“**Non-Markovian MC**”: Emission multiplicity generated as **first** variable (or 2nd).

“**Constrained evolution**”: Final parton type and energy fraction  $x$  in the evolution are predefined, fixed. **However**, all the distribution can be identical as in the forward evolution (Markovian style).

# Single QCD Evolution in Cracow using MC, 05/06

Single evolution programs/exercises far:

- Main emphasis on **CMC** = **C**onstrained **M**onte **C**arlo
- The long term aim is a high quality MC description of the QCD ISR in the W/Z production process at LHC. (DIS in the scope).
- **MMC** programs, **M**arkovian **M**onte **C**arlos, are developed in parallel and used as calibration tool for testing MMC.
- MMC programs implement presently:
  - DGLAP LL and NLL (xchecked with QCDnum16 and APCHEB to within 0.2%),
  - CCFM/HERWIG LL evolution with options:  $\alpha_S(q(1-z))$ ,  $\epsilon_{IR} = q_0/q$ ,  $q_{stop} = x_0 q_{max}$ , Quark-Gluon transitions. Mapping into 4-momenta.
- **CMC** programs feature presently:
  - DGLAP LL (xchecked with MMC and QCDnum16), Q-G transitions!
  - CCFM/HERWIG LL evol. (xchecked with MMC), options:  $\alpha_S(q(1-z))$ ,  $\epsilon_{IR} = q_0/q$ ,  $q_{stop} = x_0 q_{max}$ , Quark-Gluon transitions (not yet for  $q_{stop} = x_0 q_{max}$ ). Mapping into 4-momenta.

## CMC in a nutshell

- Mapping of evolution time  $t_i \rightarrow s_i$  and  $z_i \rightarrow y_i$ , such that Jacobian eliminates completely the (simplified) kernel  $zP_{ff}(z, t)$
- Ordering in  $s_i$  temporarily removed
- The constraint  $\delta(z - \prod z_i)$  is eliminated/fulfilled by means of the parallel shift  $y_i \rightarrow y_i - Y$  (for DGLAP rescaling in the mom. space,  $y = \ln(1 - z)$  ).
- Quark-Gluon transitions by “brute force” method using general purpose FOAM simulator.
- Appropriate correcting MC weights applied at the end.
- For more details see my talks in previous HERA-LHC and other places, <http://jadach.web.cern.ch/jadach/> and <http://arxiv.org/abs/hep-ph/0504263>

# Variable Mapping

$$\int_x^{1-\varepsilon(t)} dz_i \int_{t_0}^t dt_i \mathcal{P}_{kk}^\Theta(t_i, z_i) = h_k \int_{\rho(t_0-t)}^{\rho(\ln(1-x))} dy_i \int_0^1 ds_i \mathbf{1}, \quad i = 1, 2, \dots, n,$$

$$z_i(y_i) = 1 - \exp(\rho^{-1}(y_i)),$$

$$\hat{t}_i(s_i) = \hat{t}_0 \left( \frac{\hat{t} + \ln(1 - z_i)}{\hat{t}_0} \right)^{s_i} - \ln(1 - z_i).$$

where

$$\rho(v) \equiv (\hat{t} + v) \ln(\hat{t} + v) - v - v \ln \hat{t}_0 - \hat{t} \ln \hat{t}, \quad \hat{t} \equiv t - t_\Lambda = \ln Q - \ln \Lambda_0.$$

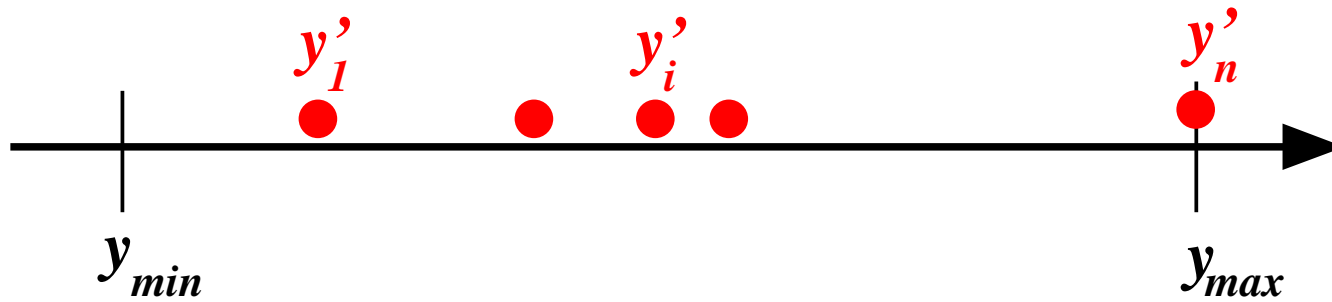
IMPORTANT:  $\rho^{-1}$  is not analytical!

Inversion has to be done numerically.  $\rho^{-1}$  will enter the constraint function  $\prod z_i!$

The above mapping leads to:

$$x \mathcal{D}_{kk}(t, t_0, x) = e^{-\Phi_k(t, t_0)} \left\{ \delta_{x=1} + \sum_{n=1}^{\infty} \frac{1}{n!} h_k^n \prod_{i=1}^n \int_{\rho(t_0-t)}^{\rho(\ln(1-x))} dy_i \delta_{x=\prod_{i=1}^n z_i(y_i)} \int_0^1 ds_i \right\}.$$

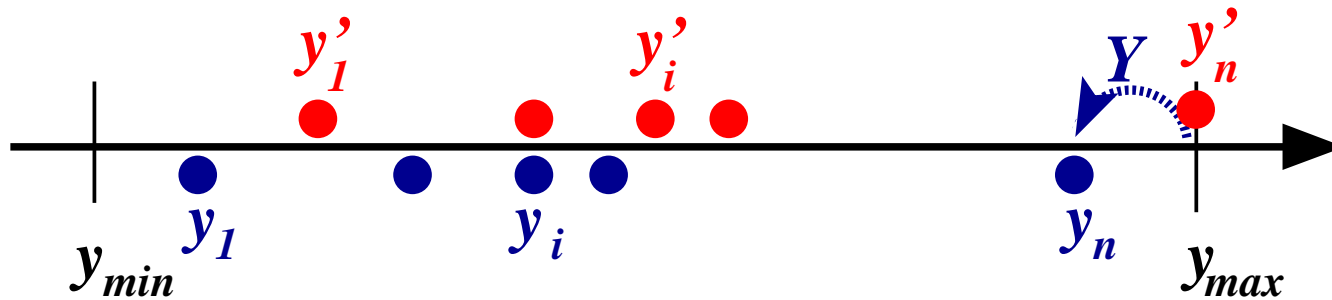
Linear shift:  $y'_i \rightarrow y_i = y'_i - Y$



- Begin with  $y'_i$  such that one of them  $y_n \equiv y_{max}$

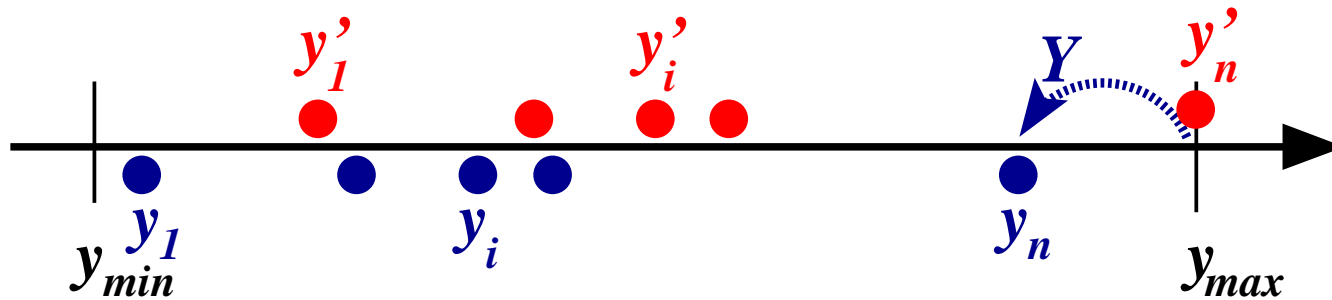


Linear shift:  $y'_i \rightarrow y_i = y'_i - Y$



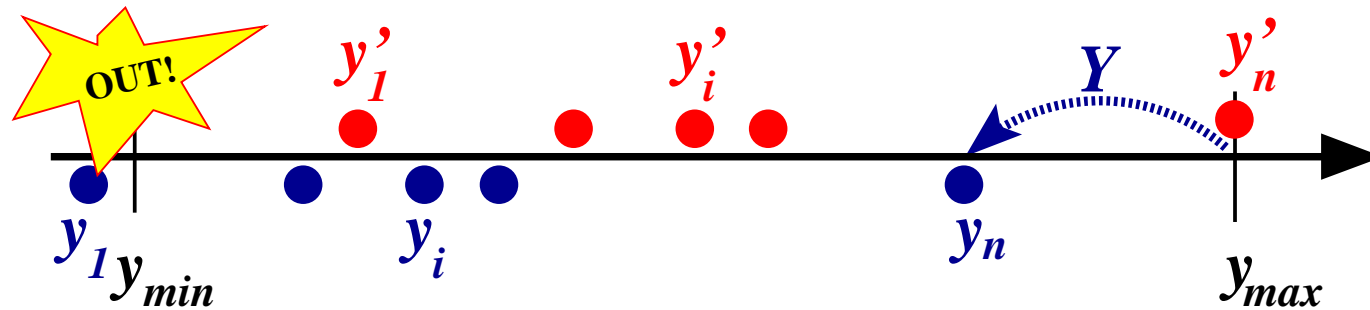
- Begin with  $y'_i$  such that one of them  $y_n \equiv y_{\max}$
- Shift  $y'_i \rightarrow y_i$  by  $Y$ , where  $Y$  solves constraint condition  $\prod z_i = x$

Linear shift:  $y'_i \rightarrow y_i = y'_i - Y(y'_1, y'_2, \dots, y'_n)$



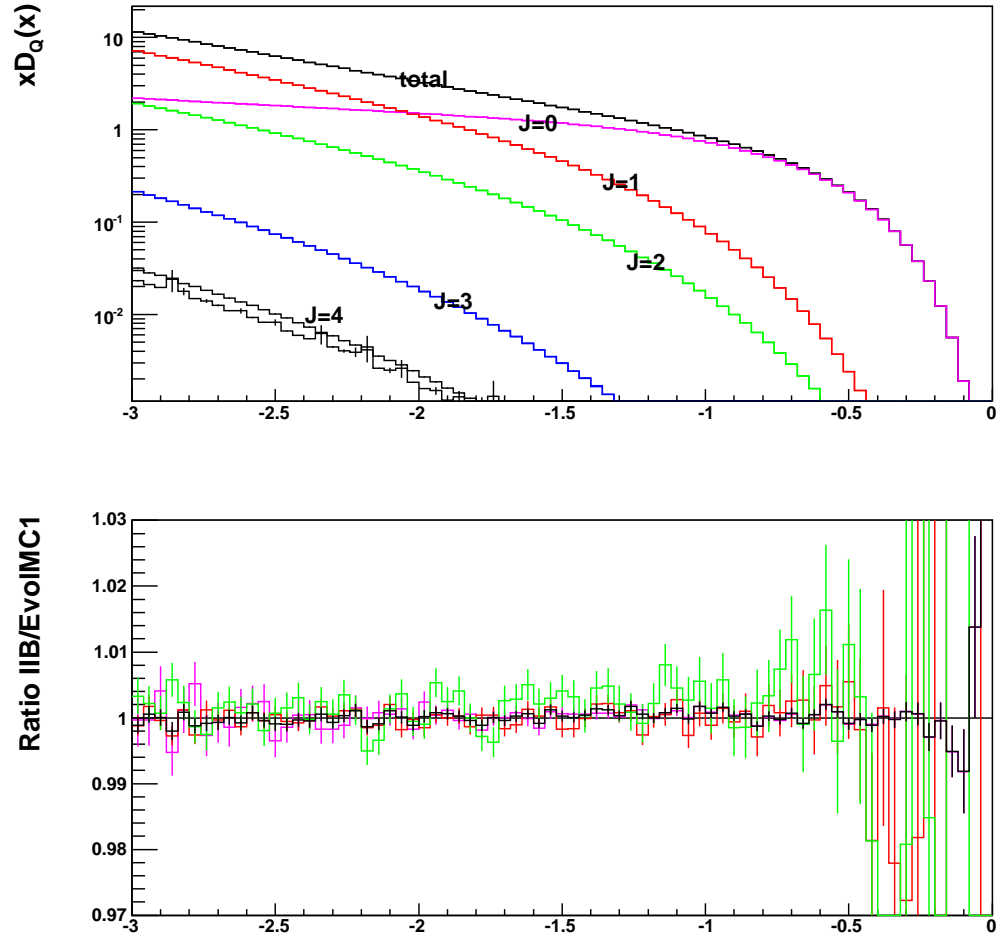
- Begin with  $y'_i$  such that one of them  $y_n \equiv y_{\max}$
- Shift  $y'_i \rightarrow y_i$  by  $Y$ , where  $Y$  solves constraint condition  $\prod z_i = x$
- $Y$  is therefore complicated function of all  $y'_i$

$$\text{Linear shift: } y'_i \rightarrow y_i = y'_i - Y(y'_1, y'_2, \dots, y'_n)$$



- Begin with  $y'_i$  such that one of them  $y_n \equiv y_{\max}$
- Shift  $y'_i \rightarrow y_i$  by  $Y$ , where  $Y$  solves constraint condition  $\prod z_i = x$
- $Y$  is therefore complicated function of all  $y'_i$
- Sometimes the smallest  $y'_i$  is shifted OUT of the phase space, below IR the limit  $y_{\min}$ . Such an event gets MC weight  $w = 0$

# Test CMC/MMC; Evolution 1GeV $\rightarrow$ 1TeV



$J = 0$ :  $Q \rightarrow Q$

$J = 1$ :  $G \rightarrow Q$  and any no. of gluon emissions out of  $Q$  and  $G$ ,

$J = 2$ :  $G \rightarrow Q \rightarrow G \rightarrow Q$ , etc.

$J = 3$ :  $G \rightarrow Q \rightarrow G \rightarrow Q$ , etc.

$J = 4$ :  $Q \rightarrow G \rightarrow Q \rightarrow G \rightarrow Q$ , etc. "Total" is the sum of  $n = 0, 1, 2, 3, 4$ .

Evolution in LL, with  $\alpha(q(1-z))$ ,  $\epsilon_{IR} = 1\text{GeV}/q$  (HERWIG/CCFM style).

This result was obtained June 2005

# Toolbox for mapping of $t_i$ and $z_i$ into phase space (4-momenta)

Emitted particle momenta in terms of lightcone  $\pm$  variables and rapidities:

$$k_i = (k_i^+, k_i^-, \vec{k}_{Ti}), \quad \vec{k}_{Ti}^2 = k_i^+ k_i^-, \quad e^{2\eta_i} = \xi_i = \frac{k_i^-}{k_i^+} = \frac{\vec{k}_{Ti}^2}{s k_i^{+2}}$$

Many equivalent parametrization of the same “eikonal phase space element”:

$$\frac{d^3 k_i}{2k_i^0} \frac{1}{k_i^- k_i^+} = \frac{dk_i^+ dk_i^- d\varphi_i}{k_i^+ k_i^-} = \frac{d\xi_i dk_i^+ d\varphi_i}{\xi_i k_i^+} = \frac{d\xi_i dz_i d\varphi_i}{\xi_i (1 - z_i)} = \frac{dp_{Ti} dz_i d\varphi_i}{p_{Ti} (1 - z_i)} = \dots$$

Identity connecting lightcone variabs. of the emitter  $z_i$  with  $k_i^+$  of the emitted particles:

$$\prod_{i=1}^n \int_0^{p_0^+} \frac{dk_i^+}{k_i^+} \theta_{\sum_{i=1}^n k_i^+ \leq p_0^+} = \int_0^1 \prod_{i=1}^n \frac{dz_i}{1 - z_i}$$

The IR boundary on  $k_i^T$  (alternatively on  $x_{i-1} k_i^T$ ):

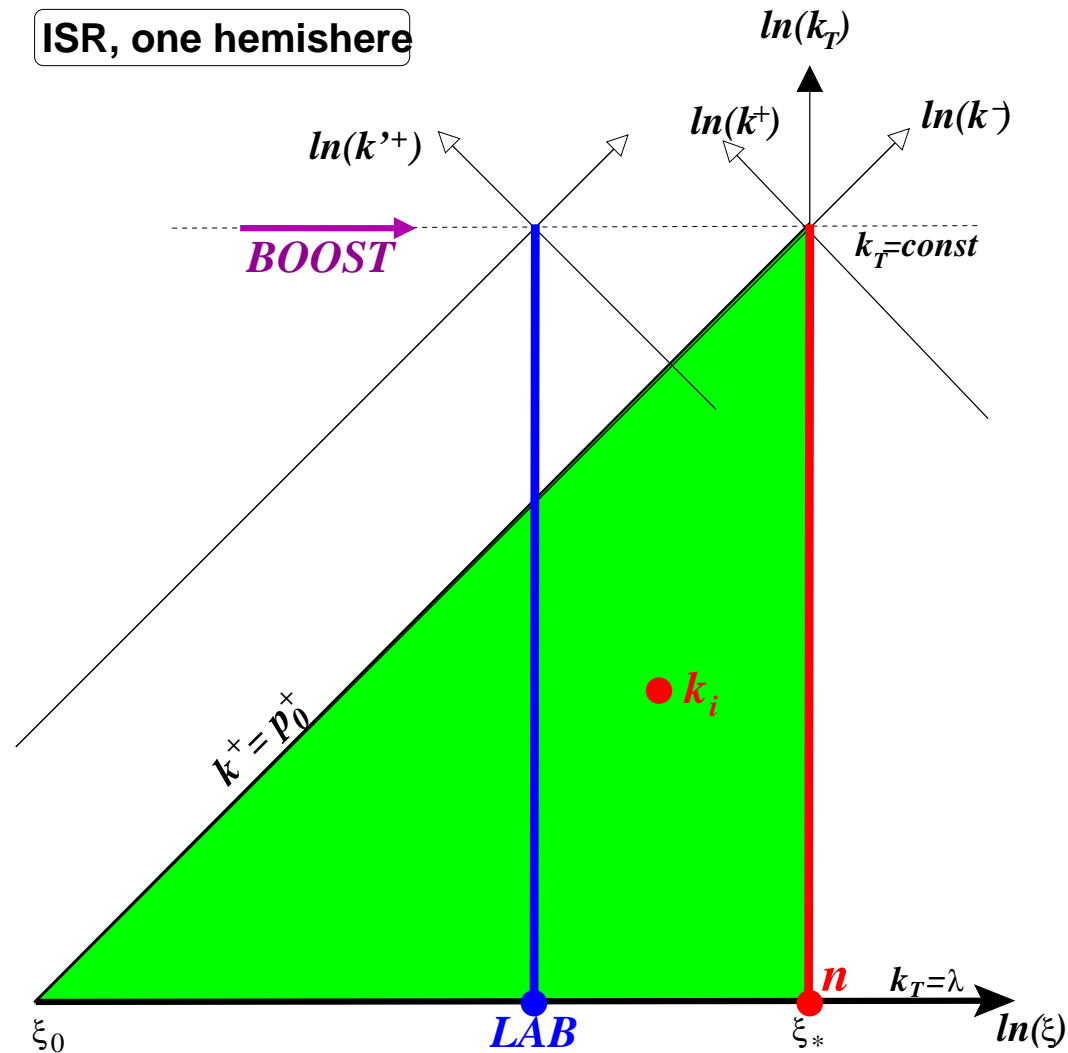
$$k_{Ti}^2 = k_i^+ k_i^- = k_i^{+2} \xi_i > \lambda^2, \quad k_i^+ = p_0^+ (1 - z_i) x_{i-1} > \frac{\lambda}{\sqrt{\xi_i}}, \quad 1 - z_i > \frac{\lambda}{p_0^+ x_{i-1} \sqrt{\xi_i}}$$

Last not least, the choice of the evolution time variable:  $q_i = p_0^+ \sqrt{\xi_i}$ ,

where  $p_0 = (p_0^+, 0, 0, 0)$  is the primary emitter, before the evolution starts.

**We chose rapidity as the evolution time!!!!** Also equal to maximum  $k_T$  of the next emission.

# Sudakov plane in (rapidity, $k_T$ ) and/or $(k^+, k^-)$



The phase space is visualized for single emitted particle as a green triangle on the logarithmic plane  $(\ln k_T, \ln \xi)$ .

It can be also mapped using variables  $(\ln k^+, \ln k^-)$  on the same plot.

The boost from one to another frame along  $p_0$  corresponds to trivial horizontal parallel shift ( $k_T$  unchanged). Trivial!!!

# Master equation for single evolution/hemisphere gluonstrahlung

Master formula for ISR gluonstrahlung out of parton  $f$  with the angular ordering:

$$\begin{aligned}
 \tilde{D}_f(\xi, x) &= e^{-\Phi_f(\xi, \xi_0)} \delta(1-x) + \\
 &+ \sum_{n=0}^{\infty} e^{-\Phi_f(\xi | \xi_n, x)} \left( \prod_{i=1}^n \int_{\xi_{i-1}}^{\xi} \frac{d\xi_i}{\xi_i} \int_{\lambda/\sqrt{\xi_i}}^{p_0^+ x_{i-1}} \frac{dk_i^+}{k_i^+} \int \frac{d\varphi_i}{2\pi} \right) \\
 &\times \left( \prod_{i=1}^n \tilde{\mathbf{P}}_{ff}(k_i, z_i) e^{-\Phi_f(\xi_i | \xi_{i-1}, x_{i-1})} \right) \delta_{x=\prod_{i=1}^n z_i} \quad (0)
 \end{aligned}$$

$$1 - z_i = \frac{k_i^+}{p_0^+ - k_1^+ - k_2^+ \dots - k_{i-1}^+} = \frac{k_i^+}{p_0^+ x_{i-1}}, \quad p_0^+ x_{i-1} = p_0^+ - \sum_{j=0}^{i-1} k_j^+,$$

where,  $\xi_0 = \lambda$ , kernel  $\tilde{\mathbf{P}}_{ff}(k, z) = z(1-z)\mathbf{P}_{ff}(k, z, x)$  includes  $\alpha_S$

$$\mathbf{P}_{ff}(k, z, x) = \frac{\alpha_S(k)}{\pi} P_{ff}(\xi, z, x) = \frac{\alpha_S(k)}{\pi} \frac{B_{ff}}{z(1-z)} \chi_f(\xi, z),$$

# Master equation, cont.

Sudakov formfactor explicitly reads:

$$\begin{aligned}
 \Phi_f(\xi_i | \xi_{i-1}, x_{i-1}) &= \int_{\xi_{i-1}}^{\xi_i} \frac{d\xi'}{\xi'} \int_{\lambda/\sqrt{\xi'}}^{p_0^+ x_{i-1}} \frac{dk'^+}{k'^+} \tilde{\mathbf{P}}_{ff}(k', x_{i-1}) \\
 &= \int_{\xi_{i-1}}^{\xi_i} \frac{d\xi'}{\xi'} \int_0^{1-\lambda/(p_0^+ x_{i-1} \sqrt{\xi_i})} \frac{dz'}{1-z'} \tilde{\mathbf{P}}_{ff}(z', x_{i-1})
 \end{aligned}$$

**Properties:**  $\tilde{D}_f(\xi, x)$  obeys an evolution equation:

$$\partial_\xi \tilde{D}_f(\xi, x) = \int_0^1 \frac{dz}{1-z} dx P_{ff}(\xi, z, x') \tilde{D}_f(\xi, x') \delta_{x=zx'}$$

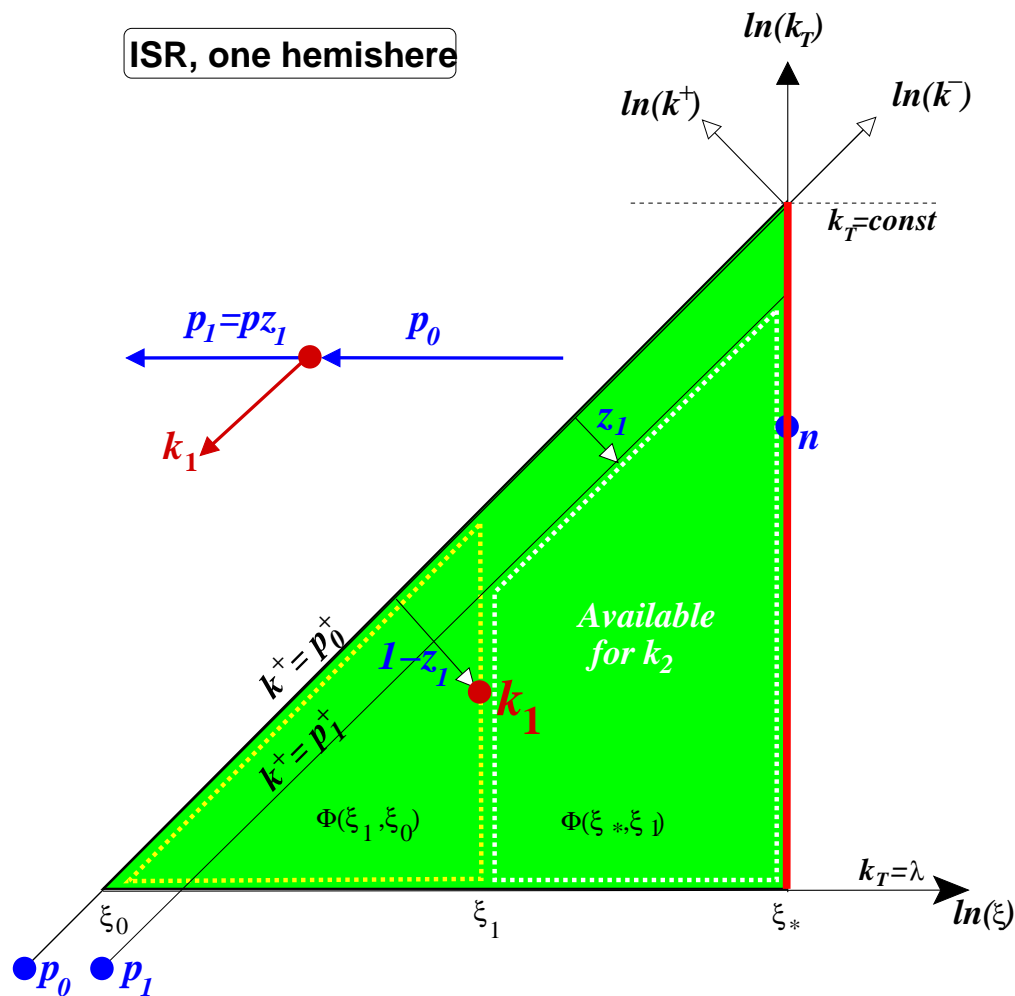
The main built in property is the “unitarity”

$$\int_0^1 dx \tilde{D}_f(\xi, x) \equiv 1, \forall \xi,$$

a synonym of the perfect cancellations of the double and single logarithmic (collinear and soft) singularities to infinite order.



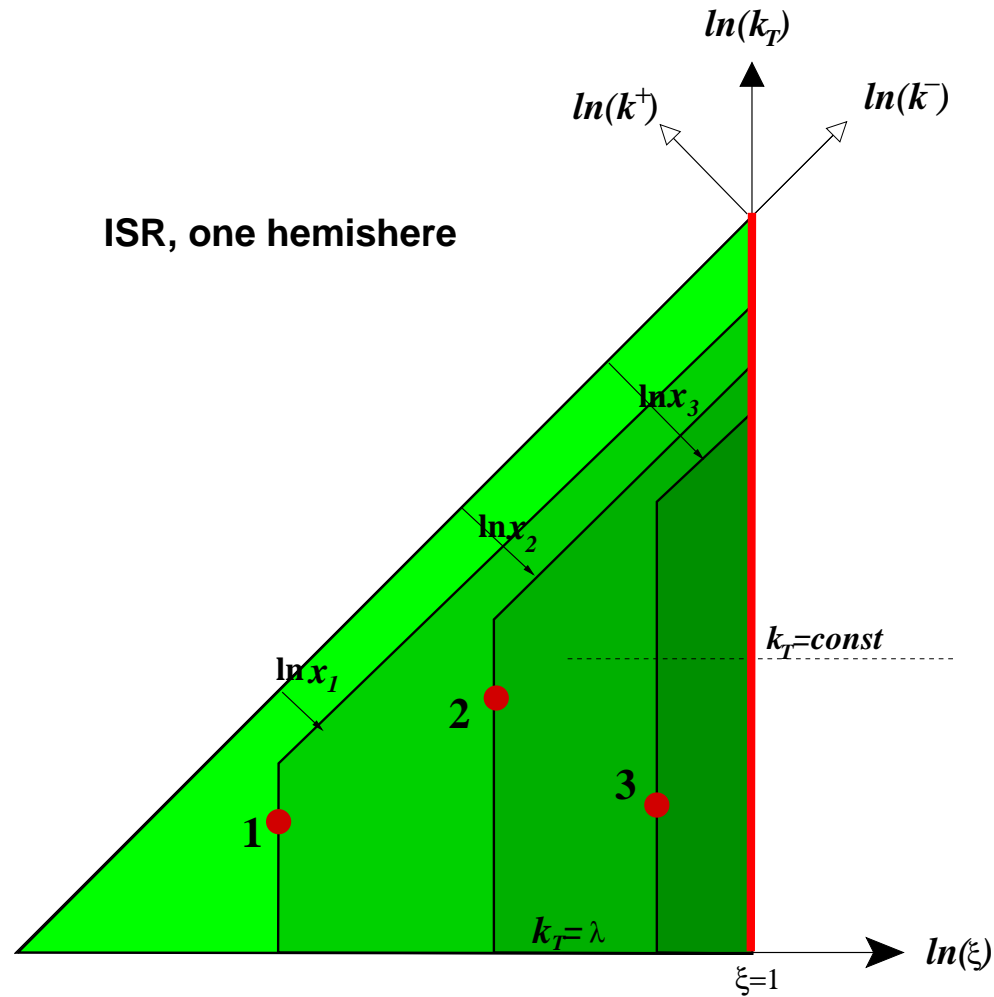
# Single emission in a detail, single evolution



$$\tilde{D}_f(\xi, x)_{n=1} = \int_{\xi_0}^{\xi} \frac{d\xi_1}{\xi_1} \int_{\lambda/\sqrt{\xi_1}}^{p_0^+} \frac{dk_1^+}{k_1^+} \int \frac{d\varphi_1}{2\pi} e^{-\Phi_f(\xi|\xi_1, x)} \tilde{\mathbf{P}}_{ff}(k_1, z_1) e^{-\Phi_f(\xi_1|\xi_0, x_0)} \delta_{x=z_1},$$



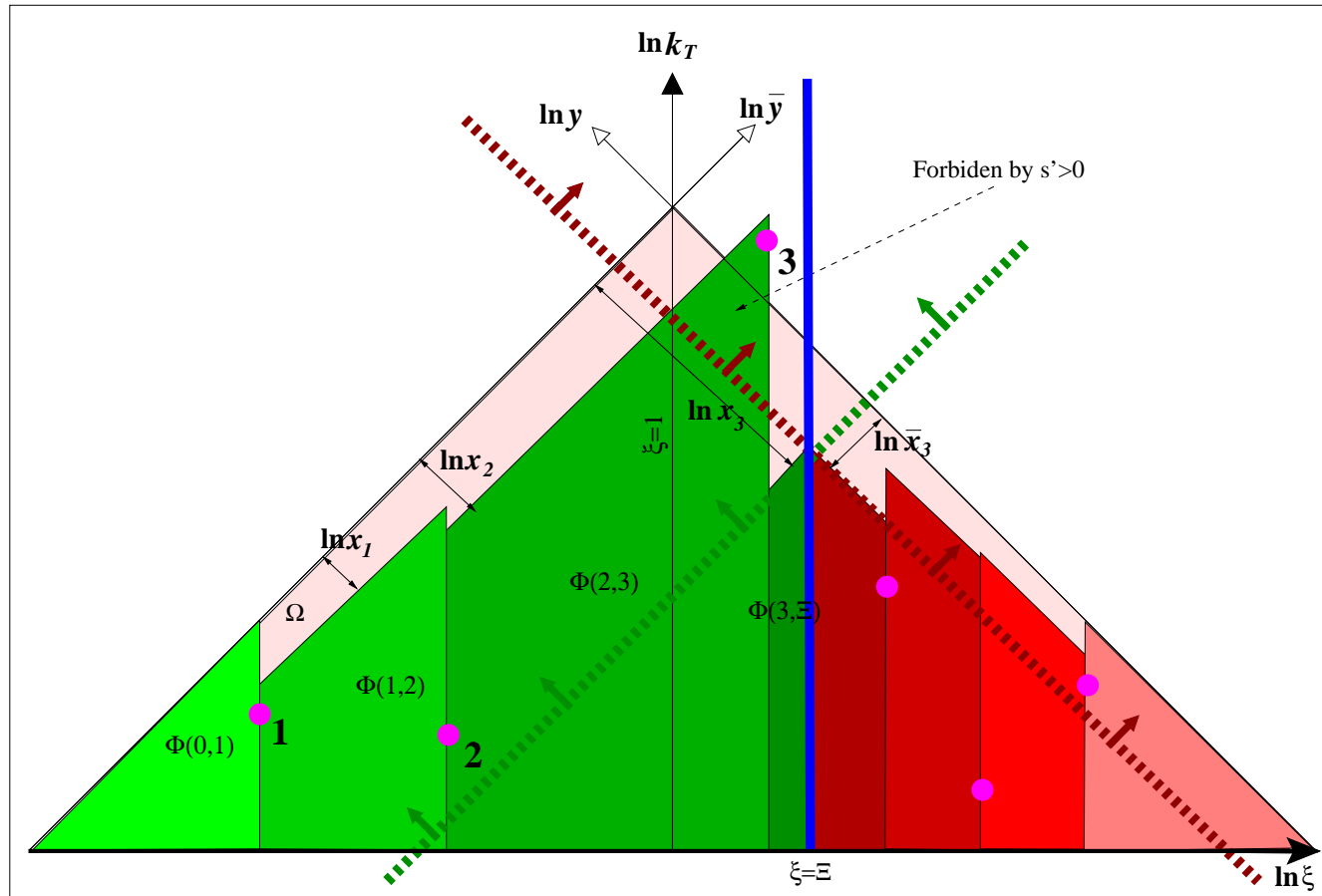
# 3 Real emissions, shrinking phase space



ISR, one hemisphere

Three ISR emissions ordered in angle. Nested trapezoids indicate (shrinking) phase space for the consecutive real emissions.

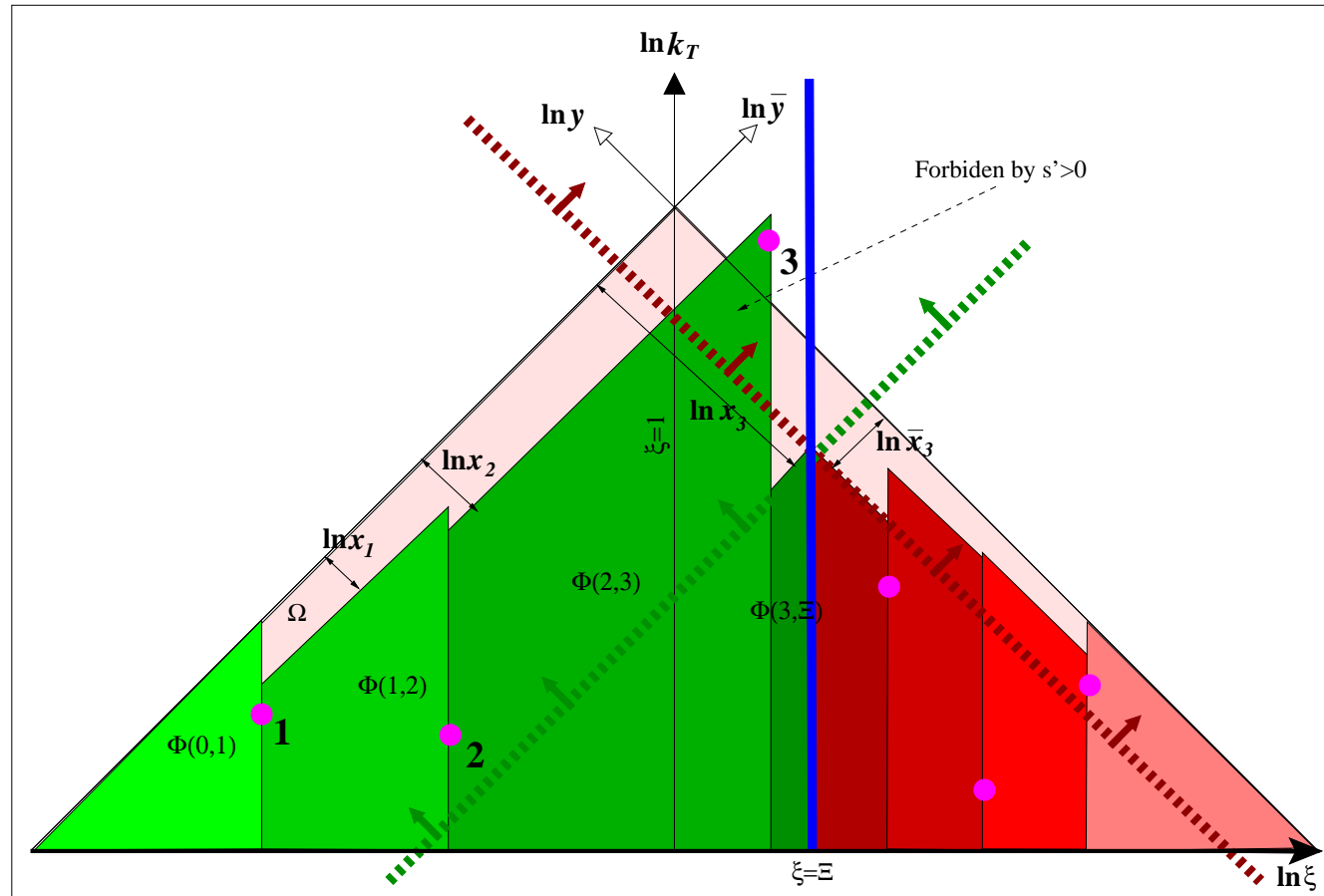
# Joining smoothly two evolutions in 2 hemispheres



Having CMC for single evolution with the strict maximum rapidity phase space limit (as we do), we may use it twice and join smoothly (without any gap or overlap) the phase space of the emitted gluons, see picture above.

The rapidity of the boundary (blue) line should coincide with rapidity of the W/Z boson, but its position is unimportant, if we are able to implement a correct soft/eikonal limit (as we do).

# Joining smoothly two evolutions in 2 hemispheres



The above scenario is already implemented in the prototype Monte Carlo.

There is however one IMPORTANT PROBLEM to be solved:

In the existing CMC for single evolution we put constraint on the  $\sum_F p_i^+$  of all gluons in the forward hemisphere and separately on the  $\sum_B p_i^-$  in the backward one.

This is not what we need! We have to put the constraint on the effective mass of the W/Z boson which involves also  $\sum_F p_i^-$ ,  $\sum_B p_i^+$  and total transverse momenta.

Additional requirement: Total control on the overall normalization.

Can we do it? Yes! We did it, it works! The method is explained in the following.

# Rescaling momenta, while keeping track of the normalization

The initial integral with the constraint:

$$I = \int dx dx_{0F} dx_{0B} D(p_0, x_{0F}) D(p_0, x_{0B}) d\rho(k_{iF}, k_{iB}) s \delta (sx - (p_{0F} + p_{0B} - K_F - K_B)^2)$$

where  $K_F = \sum_F k_{iF}$  and  $K_B = \sum_B k_{iB}$  are total momenta of **emitted** gluons in the Forw./Backward hemispheres.

$p_{0F} = x_{0F} p_{hF}$ ,  $p_{0B} = x_{0B} p_{hB}$  are 4-mom. of the **primordial** partons at low scale  $p_0$ . Momenta  $k_{iF, B}$  are the true phase space variables.

Keeping  $x, x_{0F}, x_{0B}$  fixed (external integration), consider the **constrained** subintegral:

$$I'_c(x, x_{0F}, x_{0B}) = \int s \delta (sx - (p_{0F} + p_{0B} - K_F - K_B)^2) d\rho(k_{iF}, k_{iB})$$

Also introduce explicitly **lightcone variables** separately for F and B groups of the particles:

$$I'_c = \int dK_F^+ \delta(K_F^+ - \sum_{i \in F} k_{iF}^+) \int dK_B^- \delta(K_B^- - \sum_{i \in B} k_{iB}^-) s \delta (sx - (p_{0F} + p_{0B} - K_F - K_B)^2) d\rho(k_{iF}, k_{iB})$$

## Simplified constraint

Existing CMC is able to constrain on plus-variables in Forward hemisphere and on minus-variables in Backward hemisphere.

Rewrite/simplify our basic constraint keeping this in mind:

$$\begin{aligned}
 s' = sx &\rightarrow 2p_{0F} \cdot p_{0B} - 2p_{0F} \cdot K_B - 2p_{0B} \cdot K_F + 2K_F \cdot K_B \\
 &\rightarrow 2p_{0F}^0 p_{0B}^0 + 2p_{0F}^0 K_B^- + 2p_{0B}^0 K_F^+ + 2K_F^+ \cdot K_B^- \\
 &= 2p_{0F}^0 p_{0B}^0 (1 - (1 - Z_B) - (1 - Z_F) + (1 - Z_B)(1 - Z_F)) \\
 &= 2p_{0F}^0 p_{0B}^0 Z_F Z_B = s(x_{0F} x_{0B}) Z_F Z_B,
 \end{aligned}$$

where we defined  $K_B^- = p_{0B}^0 (1 - Z_B)$  and  $K_F^+ = p_{0F}^0 (1 - Z_F)$  conventionally. Next we introduce **new**  $\delta$  with the **simplified constraint**, using auxiliary variable  $Y$ :

$$\begin{aligned}
 I_c &= \int dY \int dK_F^+ \delta(K_F^+ - \sum_{i \in F} k_{iF}^+) \int dK_B^- \delta(K_B^- - \sum_{i \in B} k_{iB}^-) \\
 &\quad \delta(sx - 2p_{0F}^0 p_{0B}^0 + 2p_{0F}^0 K_B^- Y^{-1} + 2p_{0B}^0 \cdot K_F^+ Y^{-1} - 2K_F^+ \cdot K_B^- Y^{-2}) \\
 &\quad Y^{-1} [2p_{0F}^0 K_B^- Y^{-1} + 2p_{0B}^0 K_F^+ Y^{-1} - 2K_F^+ \cdot K_B^- 2Y^{-2}] \\
 &\quad s \delta (sx - (p_{0F} + p_{0B} - K_F - K_B)^2) d\rho(p_{iF}, p_{iB})
 \end{aligned}$$

# Trading true constraint for simplified one

Rescale all emitted momenta:  $k_{iF} = Y \hat{k}_{iF}$  and  $k_{iB} = Y \hat{k}_{iB}$ ,  $K_F = Y \hat{K}_F$  and  $K_B = Y \hat{K}_B$ . Assume  $d\rho(k_{iF}, k_{iB}) = d\rho(\hat{k}_{iF}, \hat{k}_{iB})$ . It is a good (eikonal) approximation. If not true, then extra MC weight will correct for that.

$$\begin{aligned}
 I_c &= \int dY \int d\hat{K}_F^+ \delta(\hat{K}_F^+ - \sum_{i \in F} \hat{k}_{iF}^+) \int d\hat{K}_B^- \delta(\hat{K}_B^- - \sum_{i \in B} \hat{k}_{iB}^-) \\
 &\quad \delta(sx - 2p_{0F}^0 p_{0B}^0 + 2p_{0F}^0 \hat{K}_B^- + 2p_{0B}^0 \hat{K}_F^+ - 2\hat{K}_F^+ \cdot \hat{K}_B^-) \\
 &\quad Y^{-1} [2p_{0F}^0 \hat{K}_B^- + 2p_{0B}^0 \hat{K}_F^+ - 4\hat{K}_F^+ \cdot \hat{K}_B^-] \\
 &\quad s \delta \left( sx - (p_{0F} + p_{0B} - Y \hat{K}_F - Y \hat{K}_B)^2 \right) d\rho(\hat{k}_{iF}, \hat{k}_{iB})
 \end{aligned}$$

$Y$  is now “transferred” to old basic constraint, which is next eliminated by  $Y$ -integration:

$$\begin{aligned}
 I_c &= \int d\hat{K}_F^+ \delta(\hat{K}_F^+ - \sum_{i \in F} \hat{k}_{iF}^+) \int d\hat{K}_B^- \delta(\hat{K}_B^- - \sum_{i \in B} \hat{k}_{iB}^-) \\
 &\quad \delta(sx - 2p_{0F}^0 p_{0B}^0 + 2p_{0F}^0 \hat{K}_B^- + 2p_{0B}^0 \hat{K}_F^+ - 2\hat{K}_F^+ \cdot \hat{K}_B^-) \\
 &\quad Y_0^{-1} [2p_{0F}^0 \hat{K}_B^- + 2p_{0B}^0 \hat{K}_F^+ - 4\hat{K}_F^+ \cdot \hat{K}_B^-] s \mathfrak{J}(Y_0)^{-1} d\rho(\hat{k}_{iF}, \hat{k}_{iB}),
 \end{aligned}$$

where  $Y_0$  is solution of the 2nd order equation  $sx = (p_{0F} + p_{0B} - Y \hat{K}_F - Y \hat{K}_B)^2$  and  $\mathfrak{J}(Y_0) = 2(p_{0F} + p_{0B} - Y_0 \hat{K}_F - Y_0 \hat{K}_B) \cdot (\hat{K}_F + \hat{K}_B)$  is important Jacobian factor.



# MC distributions and weights

Defining  $K_{F,B}^+ = p_{0F,B}^0(1 - Z_{F,B})$  and  $s_0 = 2p_{0F}^0p_{0B}^0 = sx_{0F}x_{0B}$ , we continue “business as usual” in the two “weakly coupled” hemispheres:

$$I_c = \int dZ_F \delta(1 - \hat{Z}_F - \sum x_{iF}^+) d\rho(\hat{k}_{iF}) \int dZ_B \delta(1 - \hat{Z}_B - \sum x_{iB}^-) d\rho(\hat{k}_{iB}) \\ s\delta(sx - s_0\hat{Z}_F\hat{Z}_B) Y_0^{-1} \mathfrak{N}(Z_F, Z_B),$$

where all Jacobians are combined into single factor  $\mathfrak{N}(Z_F, Z_B)$ .

For the MC purpose it is useful to know its approximate form (for the weight stabilization):

$$\overline{\mathfrak{N}}(Z_F, Z_B) = \frac{\hat{Z}_F + \hat{Z}_B - 2\hat{Z}_F\hat{Z}_B}{[(\hat{Z}_F - \hat{Z}_B)^2 + 4(1 - \hat{Z}_F)(1 - \hat{Z}_F)\hat{Z}_F\hat{Z}_B]^{1/2}}$$

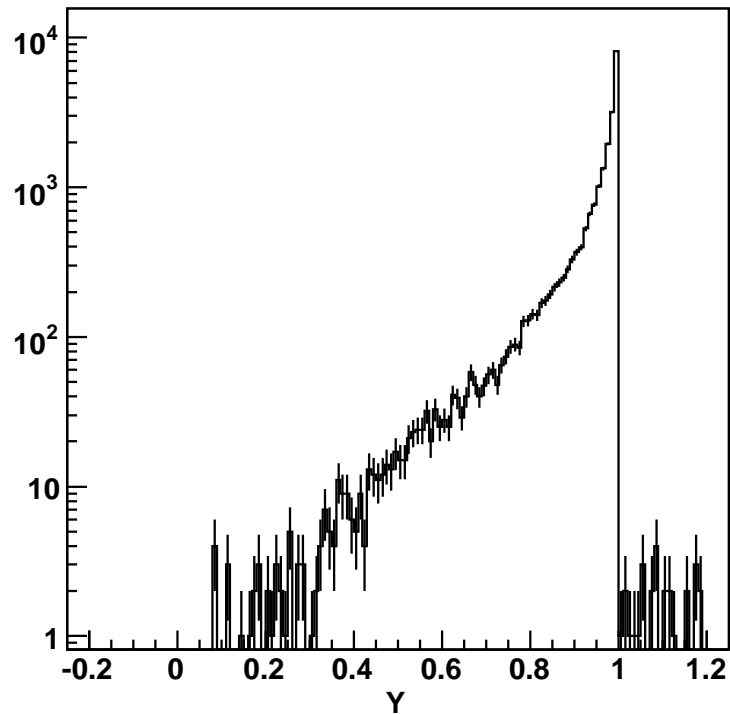
The above is treated by the Foam and the correcting MC weight includes only

$$W_{\mathfrak{N}} = \frac{s_1[(\hat{Z}_F - \hat{Z}_B)^2 + 4(1 - \hat{Z}_F)(1 - \hat{Z}_F)\hat{Z}_F\hat{Z}_B]^{1/2}}{\mathfrak{J}(Y_0, \hat{K}_F, \hat{K}_B)},$$

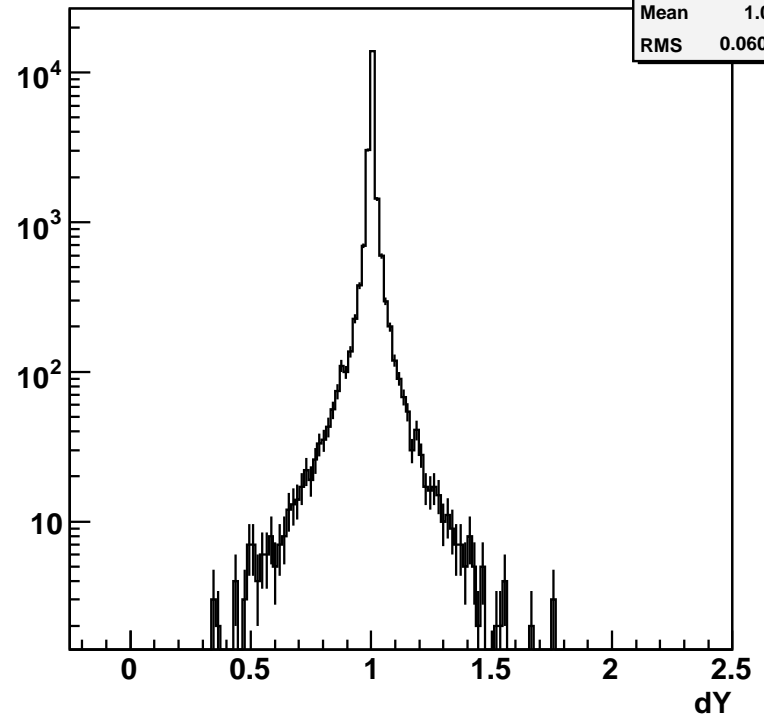
which turns out to be friendly, strongly peaked at 1.

# MC distributions and weights, numerical results

Y-factot

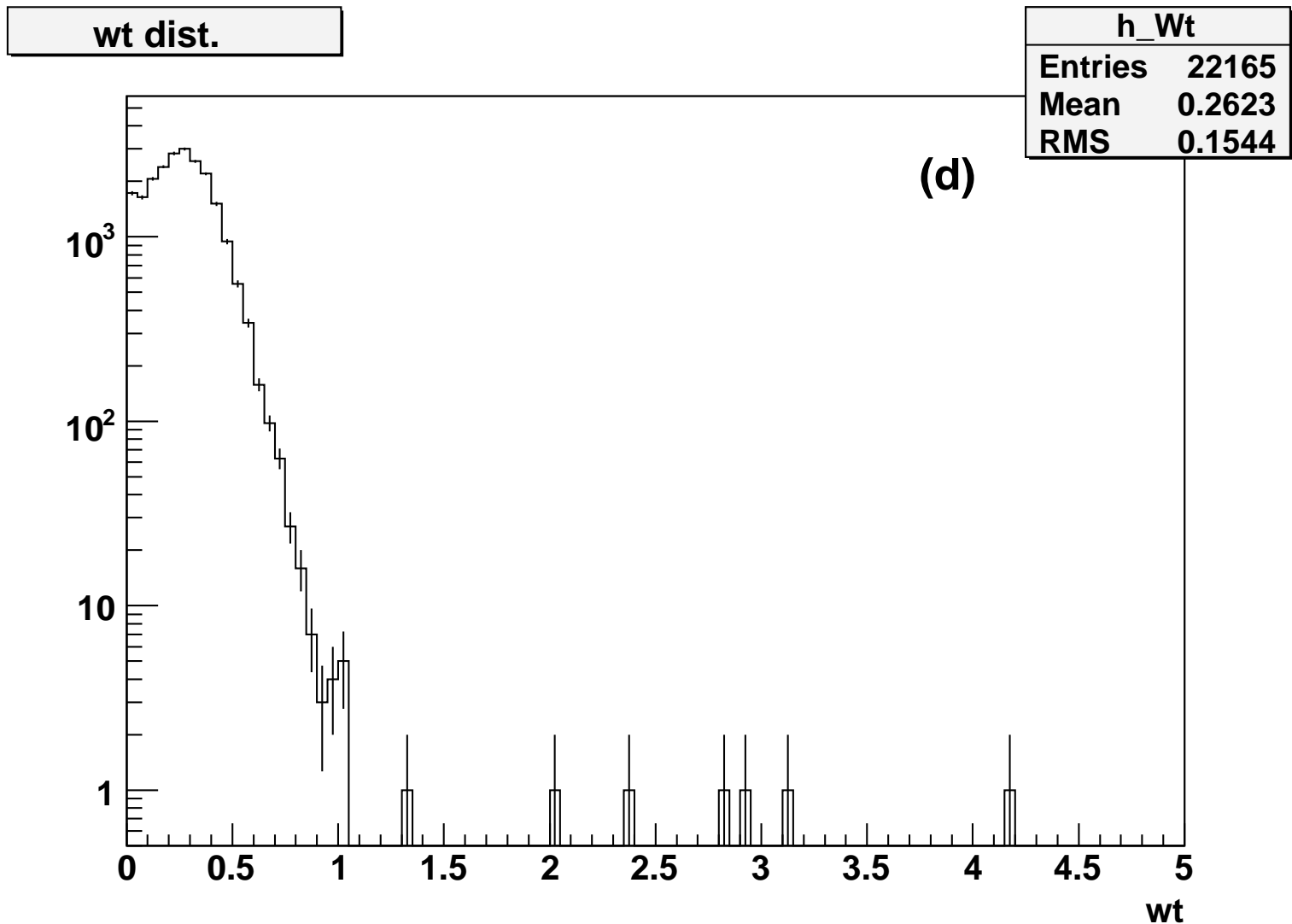


Jacobian



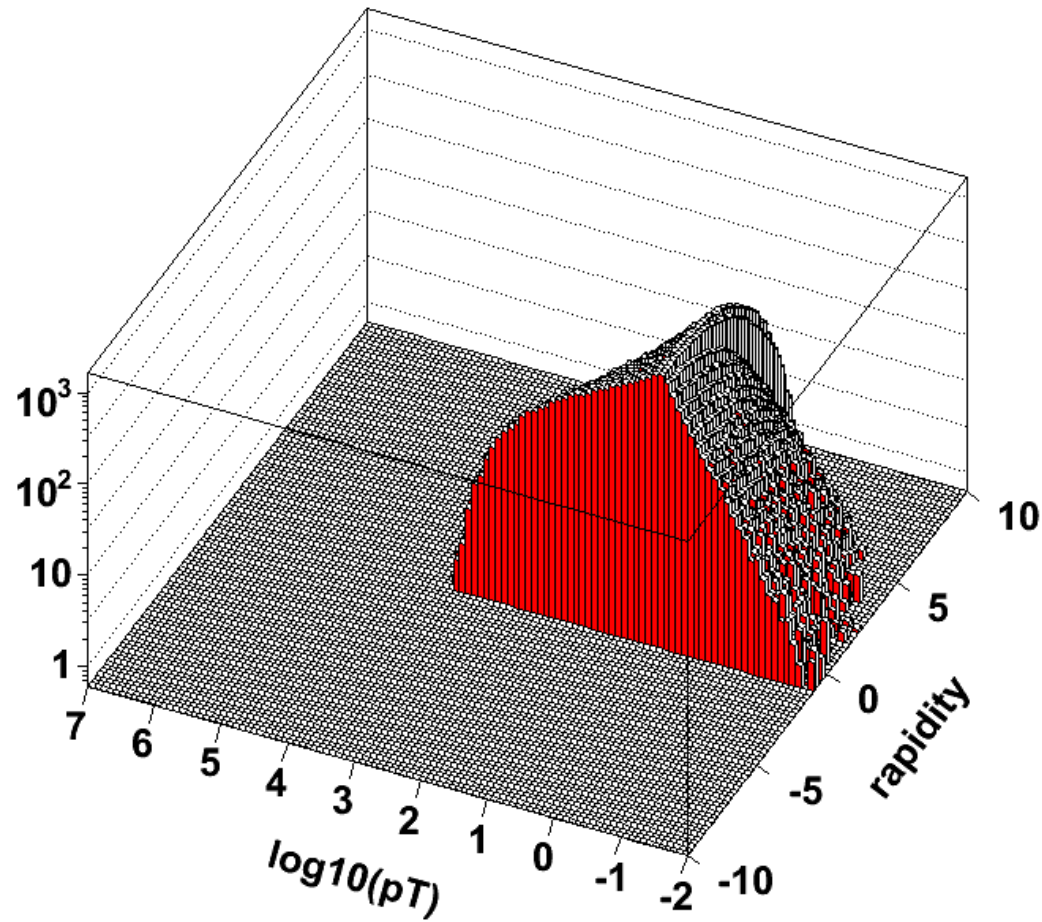
The above plots show the distribution of the rescaling factor  $Y$  (left) and of the component weight  $W_{\Omega}$  (right). The total weight is on the next slide.

# MC distributions and weights, numerical results



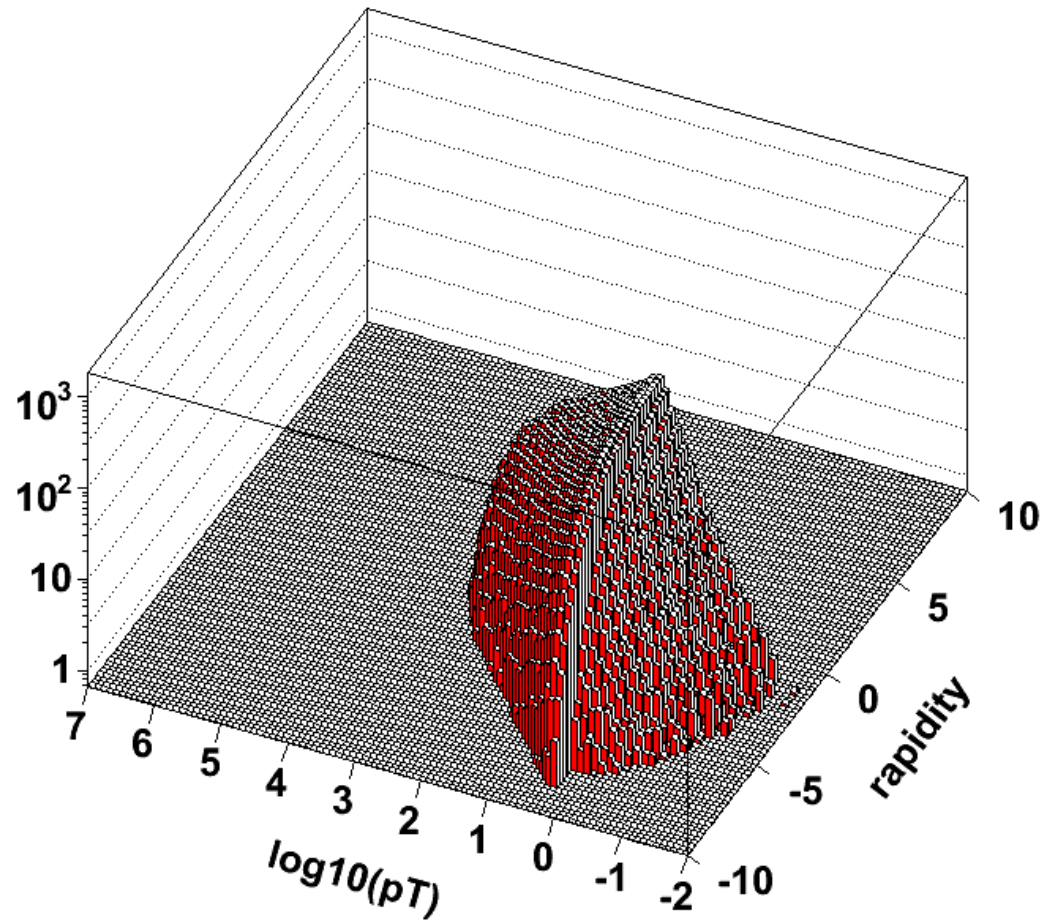
The distribution of the total MC weight looks rather good. The tail of the high weights looks insignificant. It will be examined anyway.

# Full coverage of the phase space (emitted gluons)



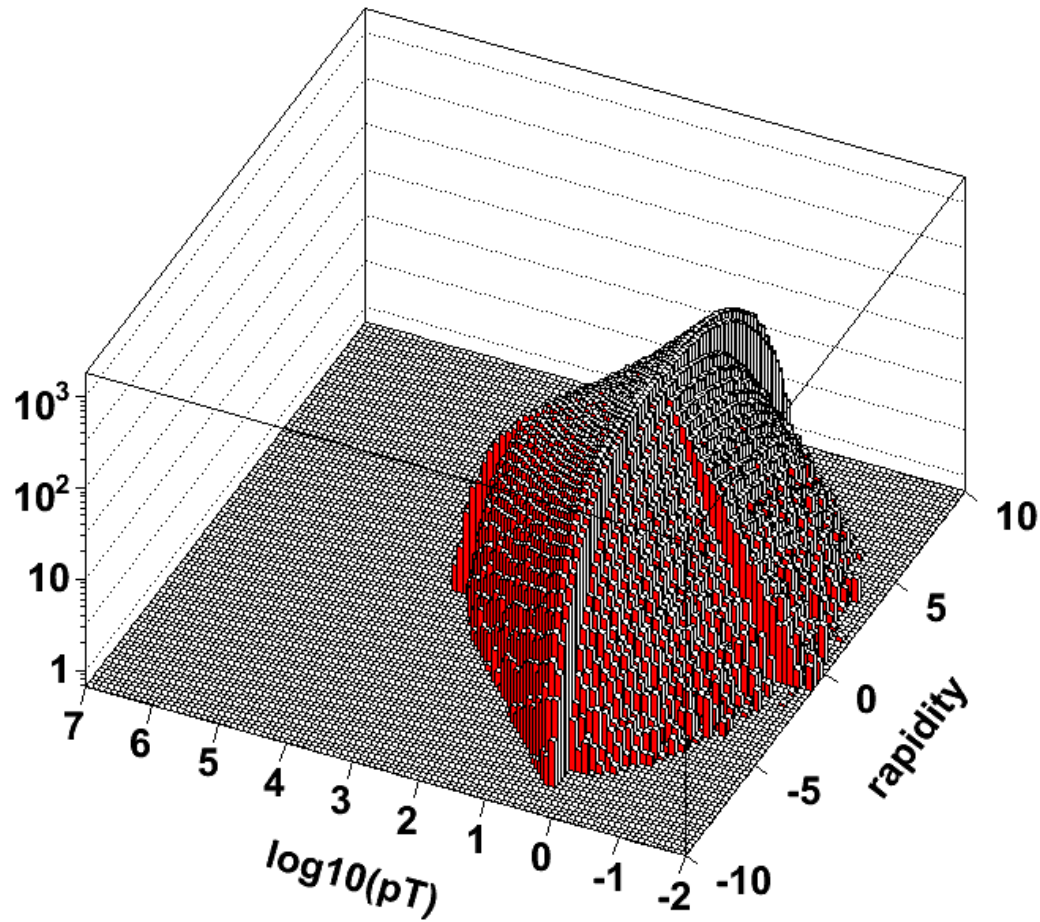
- Full coverage of the rapidity- $p_T$  space of emitted gluons, Forward hemisphere

# Full coverage of the phase space (emitted gluons)



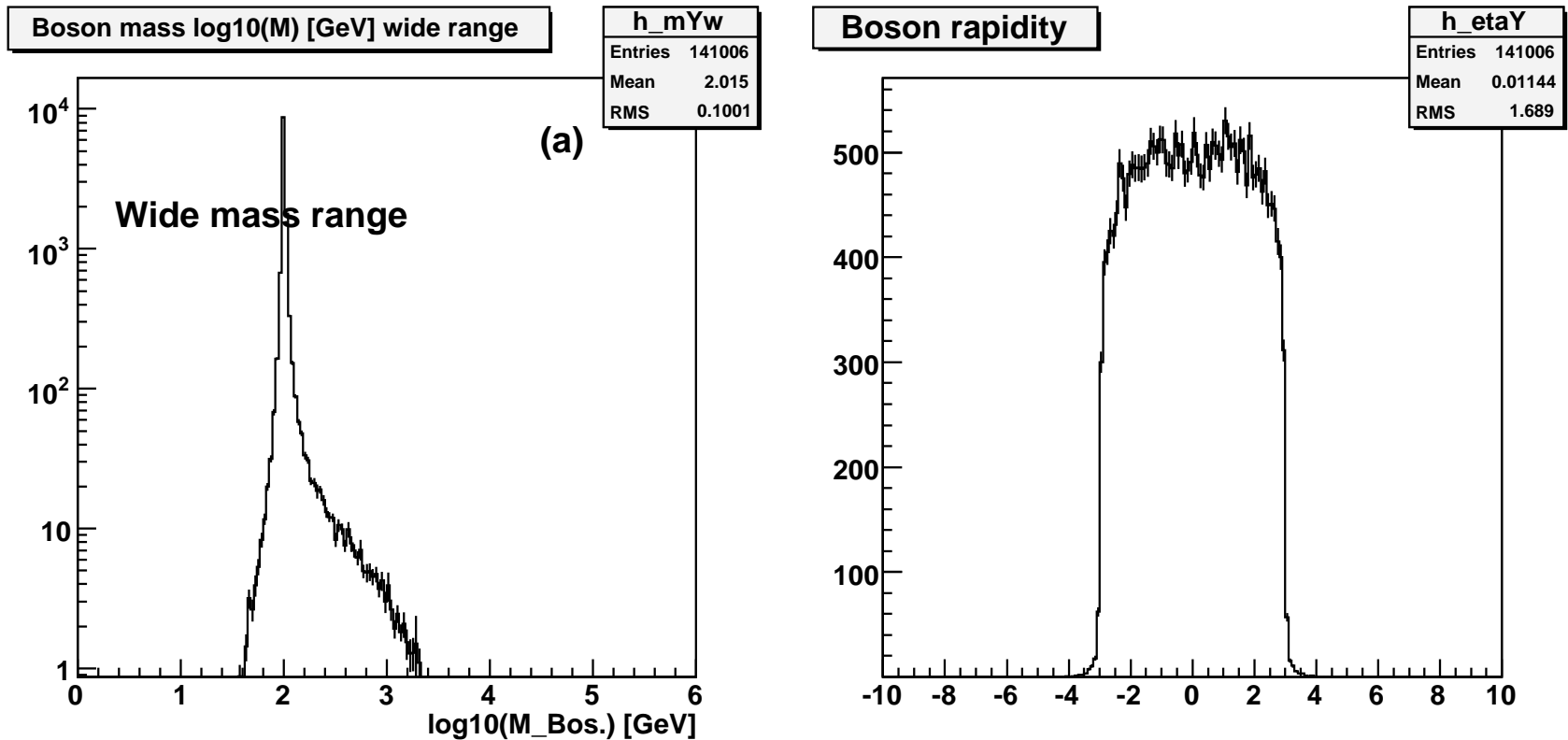
- Full coverage of the rapidity- $p_T$  space of emitted gluons, Forward hemisphere
- Full coverage of the rapidity- $p_T$  space, Backward hemisphere

# Full coverage of the phase space (emitted gluons)



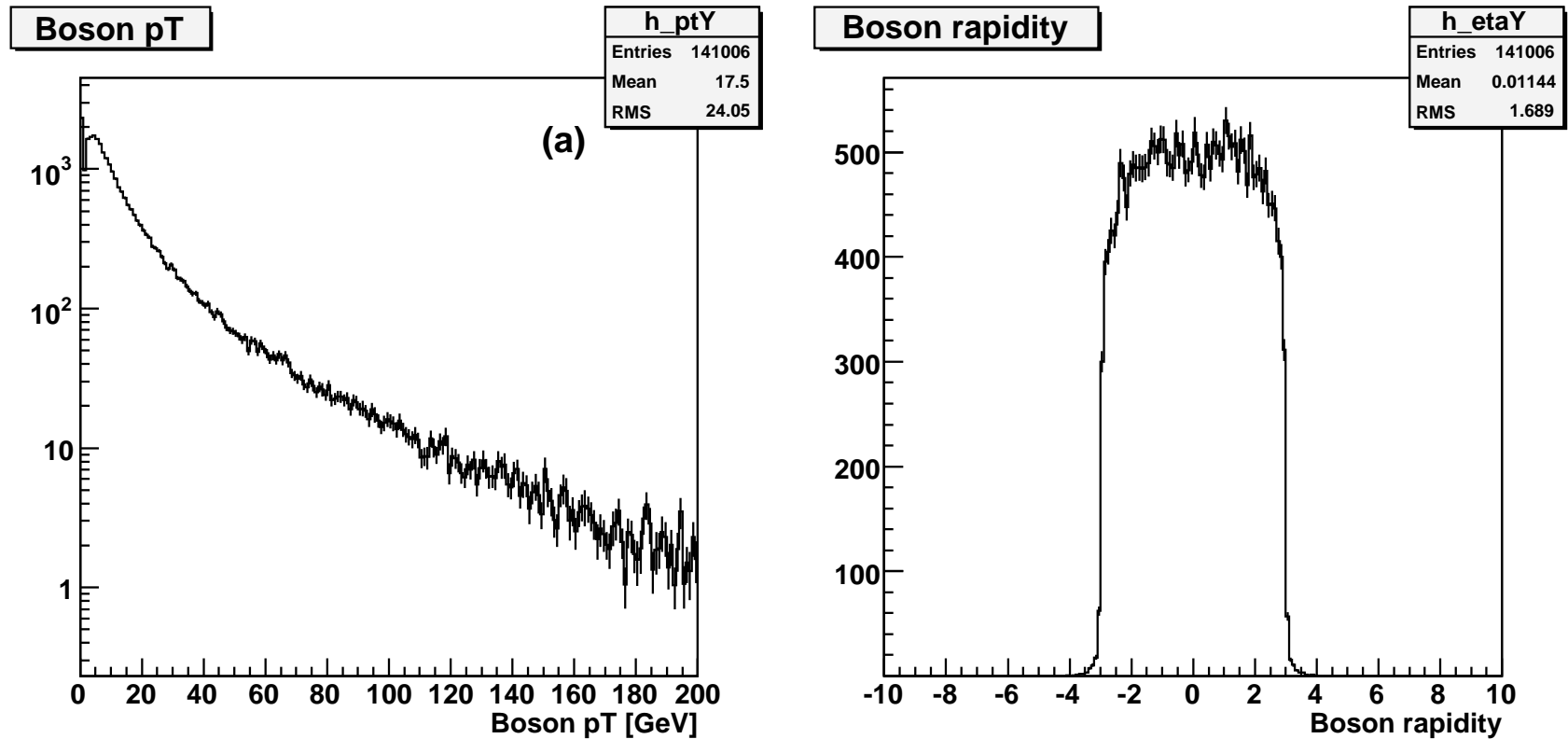
- Full coverage of the rapidity- $p_T$  space of emitted gluons, Forward hemisphere
- Full coverage of the rapidity- $p_T$  space, Backward hemisphere
- Perfect matching of 2 hemispheres, no overlap, no gaps.

# EW boson mass and rapidity distributions



The previous examples were for  $Z'$  boson of mass 1TeV and width 100GeV. Here we show mass and rapidity distribution of the EW boson (mass 100GeV). Matrix element is maximally simplified (only Breit-Wigner).

# EW boson transverse momentum and rapidity distributions



Transverse momentum and rapidity distribution of the EW boson (mass 100GeV). Matrix element is maximally simplified (only Breit-Wigner).



# Summary and outlook

- **It was demonstrated that joining two single evolutions into one Initial State radiation Monte Carlo with the constraint on the true W/Z boson mass is possible, while keeping perfect control on the overall normalization.**
- **Immediate plans:**
  - **More numerical tests against  $\text{MMC}_F \otimes \text{MMC}_B$**
  - **Inclusion of the Quark-Gluon transitions**
  - **Constructing variant with IR cut  $k_I^T > \lambda$  and  $\alpha_S(k^T)$**
- **Other plans:**
  - **Constructing variant of the same kind of the MC for DIS, fitting  $F_2$**
  - **Inclusion of NLO into hard process (coeff. funct.)**
  - **Inclusion of NLO into MC evolution at the 4-momenta level.**