




Factorization Breaking in Diffractive Dijet Production

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Publications

☛ With G. Kramer

- ☛ PLB 508 (2001) 259: $\gamma p \rightarrow 2 \text{ jets} + n$
- ☛ EPJC 38 (2004) 39: $\gamma p \rightarrow 2 \text{ jets} + p$
- ☛ PRL 93 (2004) 232002: $\gamma^* p \rightarrow 2 \text{ jets} + p$
- ☛ JPG 31 (2005) 1391: New fact. scheme

Motivation

Hard diffraction:

→ Does factorization hold?

Deep inelastic scattering: Yes

→ Direct photoproduction

Hadroproduction: No

→ Resolved photoproduction

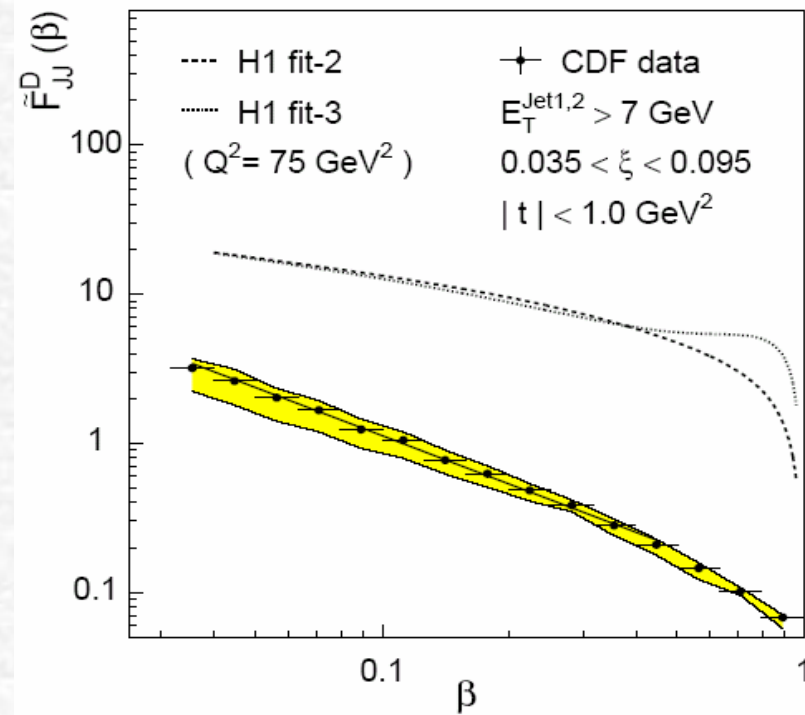
Why next-to-leading order?

→ $\sigma_{\text{tot}} = \sigma_{\text{dir}}(x_\gamma, M_\gamma) + \sigma_{\text{res}}(x_\gamma, M_\gamma)$

→ At LO $x_\gamma = 1$, but at NLO $x_\gamma \leq 1$

→ $\log(M_\gamma)$ -dependence cancels

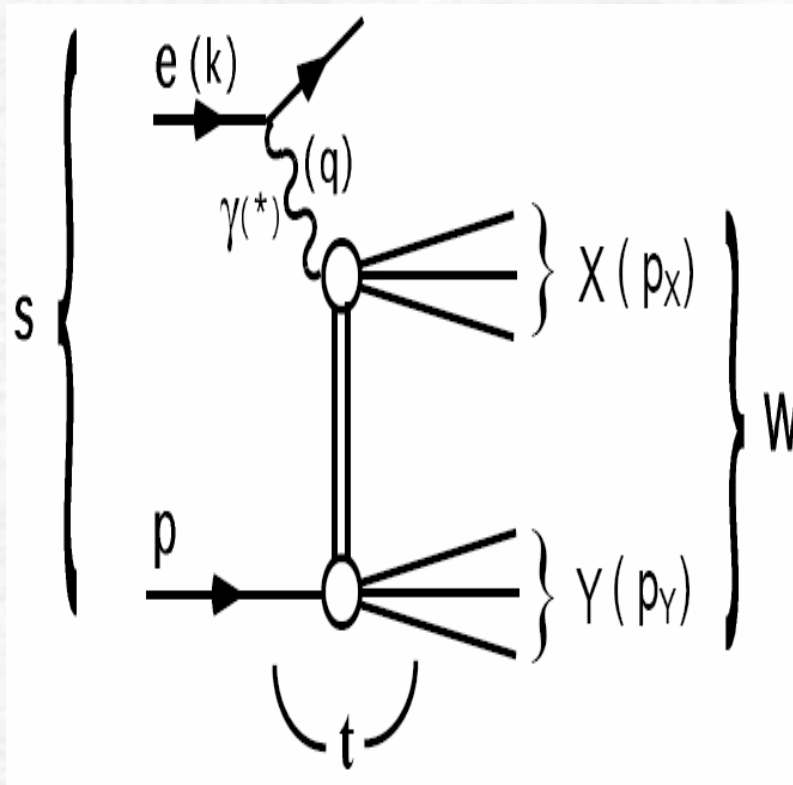
Diffr. hadroproduction of dijets:



CDF Coll., PRL 84 (2000) 5043

Kinematics

Diffractive processes at HERA:



H1 Coll., EPS 2003 and DIS 2004

Inclusive DIS:

$$s = (k + p)^2, \quad Q^2 = -q^2, \quad \text{and} \quad y = \frac{qp}{kp}$$

Diffractive DIS:

$$M_X^2 = p_X^2 \quad \text{and} \quad t = (p - p_Y)^2,$$

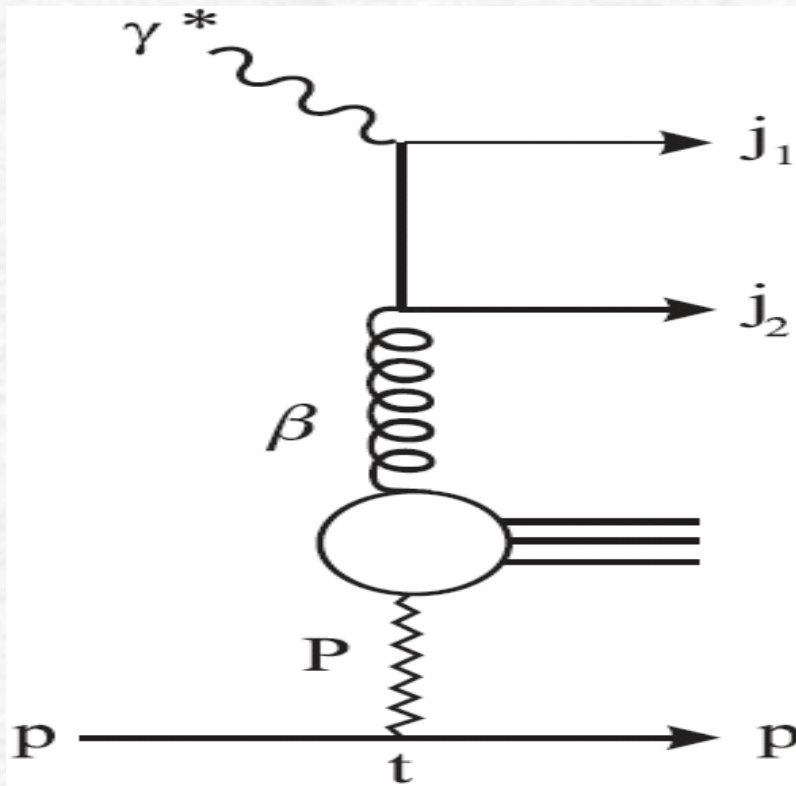
$$M_Y^2 = p_Y^2 \quad \text{and} \quad x_{\mathbb{P}} = \frac{q(p - p_Y)}{qp}$$

Experimental cuts:

0.3	<	y	<	0.65
		Q^2	<	0.01 GeV ²
		E_T^{jet1}	>	5 GeV
		E_T^{jet2}	>	4 GeV
-1	<	$\eta_{\text{lab}}^{\text{jet1,2}}$	<	2
		$x_{\mathbb{P}}$	<	0.03
		M_Y	<	1.6 GeV
		$-t$	<	1 GeV ²

Diffractive Parton Distributions

Double factorization:



G. Ingelman, P. Schlein, PLB 152 (1985) 256

Hard QCD factorization:

$$\frac{d^2\sigma}{dx_{\mathbb{P}}dt} = \sum_a \int_x^{x_{\mathbb{P}}} d\xi \sigma_a^{\gamma^*}(x, Q^2, \xi) f_a^D(\xi, Q^2; x_{\mathbb{P}}, t)$$

Regge factorization:

$$f_a^D(x, Q^2; x_{\mathbb{P}}, t) = f_{\mathbb{P}/p}(x_{\mathbb{P}}, t) f_{a/\mathbb{P}}(\beta = x/x_{\mathbb{P}}, Q^2)$$

Pomeron flux factor:

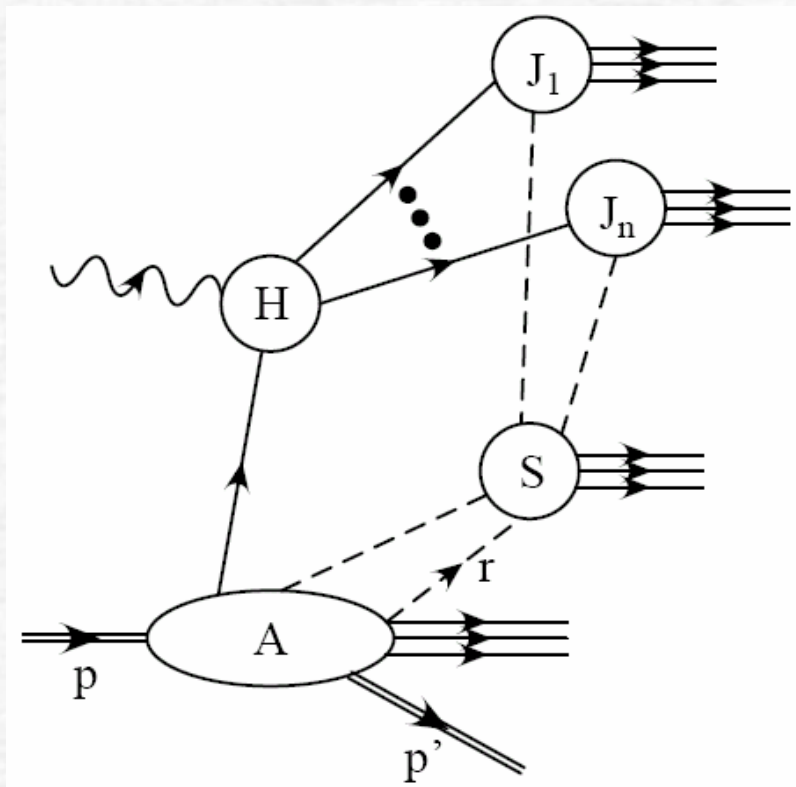
$$f_{\mathbb{P}/p}(x_{\mathbb{P}}, t) = x_{\mathbb{P}}^{1-2\alpha_{\mathbb{P}}(t)} \exp(B_{\mathbb{P}}t)$$

Pomeron trajectory:

$$\alpha_{\mathbb{P}}(t) = \alpha_{\mathbb{P}}(0) + \alpha'_{\mathbb{P}}t$$

Proof of Hard Factorization

Diffractive deep inelastic scattering:



J.C. Collins, PRD 57 (1998) 3051

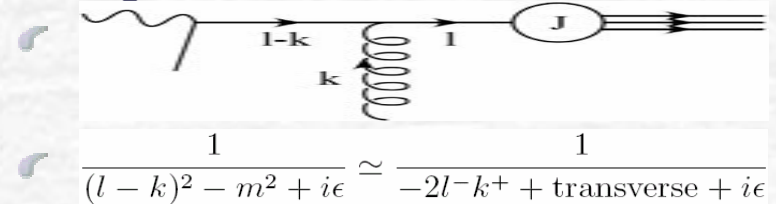
Light cone coordinates:

- $q^\mu = (q^+, q^-, \mathbf{q}_T)$

Leading regions:

- $H: q^\mu \approx O(Q)$
- $J: l^\mu \approx (0, Q/\sqrt{2}, \mathbf{0}_T)$
- $A: |k^\mu| \ll O(Q)$

Soft gluon attachments:

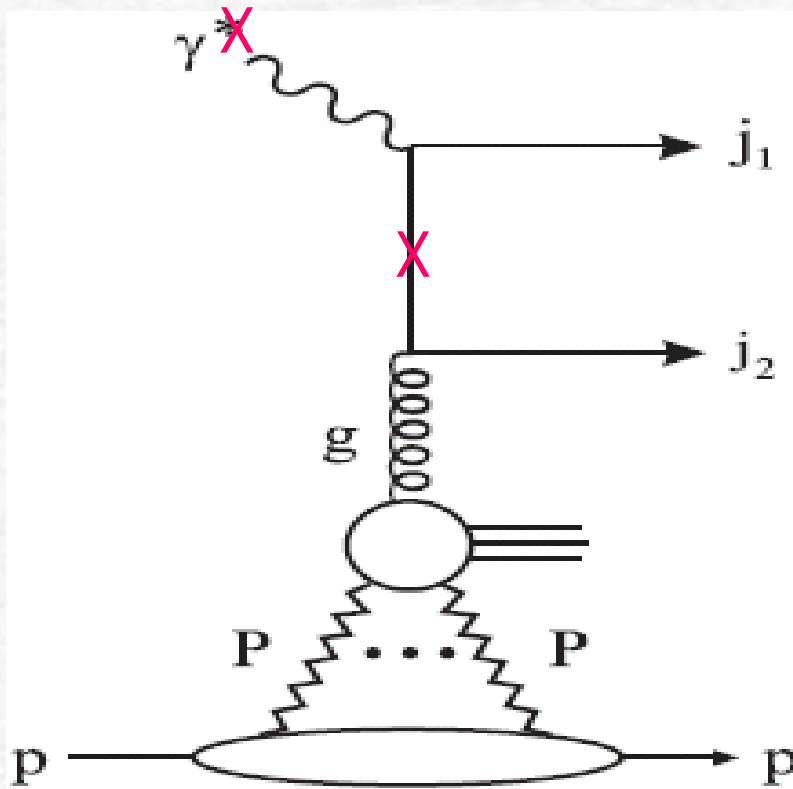


Poles in k^+ -plane:

- Final state: Upper half-plane
- Initial state: Lower half-plane**

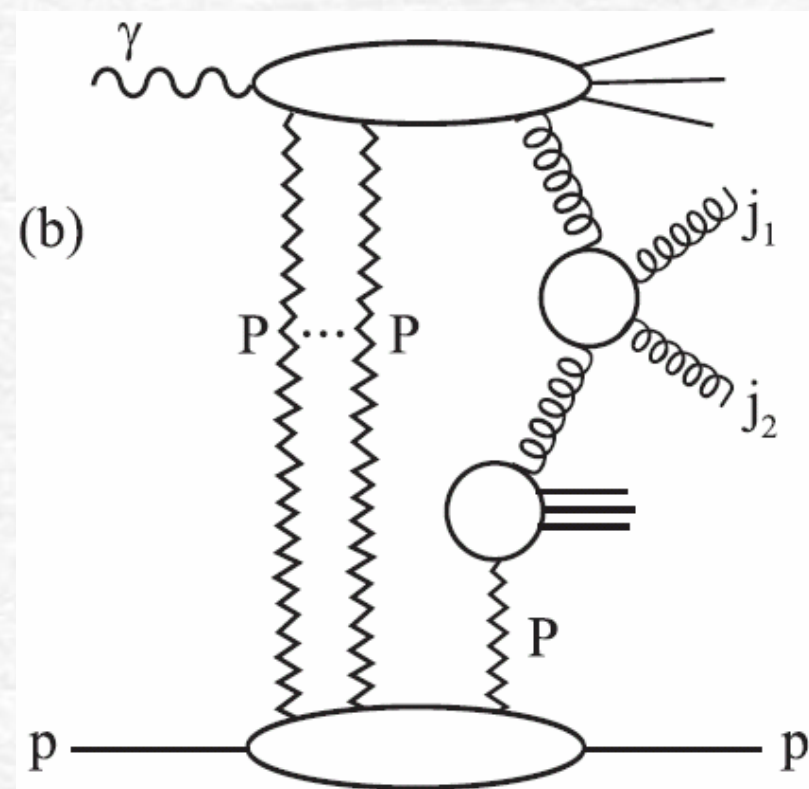
Multipomeron Exchanges

Direct photoproduction:



→ Modify the Regge trajectory

Resolved photoproduction:



→ Factorization breaking

Diffractive Photoproduction of Dijets

Cross section:

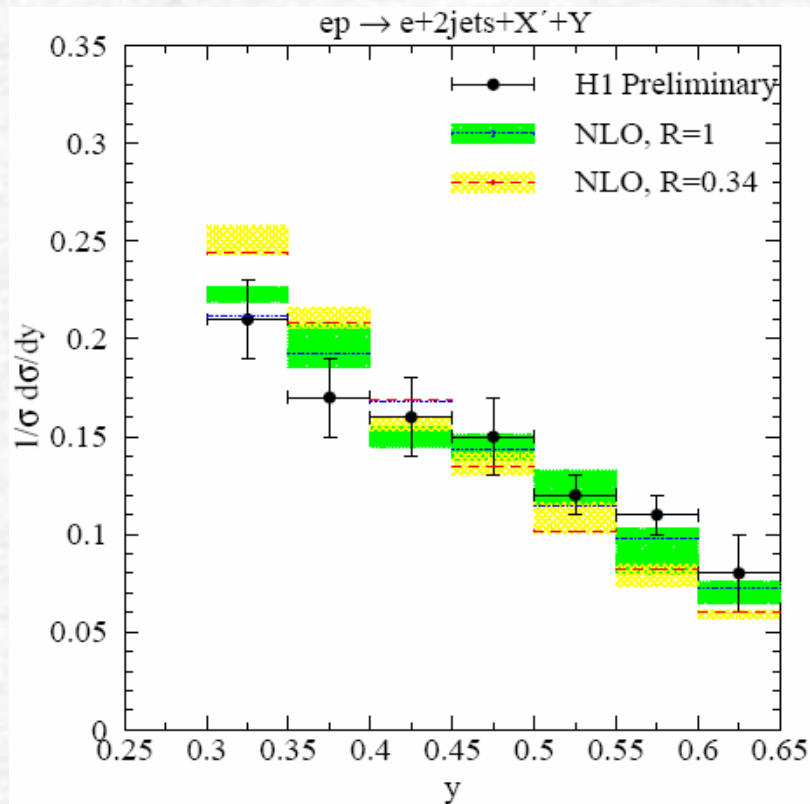
$$\begin{aligned} d\sigma^D(ep \rightarrow e + 2 \text{ jets} + X' + Y) = \\ \sum_{a,b} \int_{t_{\text{cut}}}^{t_{\text{min}}} dt \int_{x_{\mathbb{P}}^{\text{min}}}^{x_{\mathbb{P}}^{\text{max}}} dx_{\mathbb{P}} \int_0^1 dz_{\mathbb{P}} \int_{y_{\text{min}}}^{y_{\text{max}}} dy \int_0^1 dx_{\gamma} \\ f_{\gamma/e}(y) f_{a/\gamma}(x_{\gamma}, M_{\gamma}^2) f_{\mathbb{P}/p}(x_{\mathbb{P}}, t) f_{b/\mathbb{P}}(z_{\mathbb{P}}, M_{\mathbb{P}}^2) \\ d\sigma^{(n)}(ab \rightarrow \text{jets}). \end{aligned}$$

Photon flux: Weizsäcker-Williams approximation

$$f_{\gamma/e}(y) = \frac{\alpha}{2\pi} \left[\frac{1 + (1-y)^2}{y} \ln \frac{Q_{\text{max}}^2(1-y)}{m_e^2 y^2} + 2m_e^2 y \left(\frac{1-y}{m_e^2 y^2} - \frac{1}{Q_{\text{max}}^2} \right) \right]$$

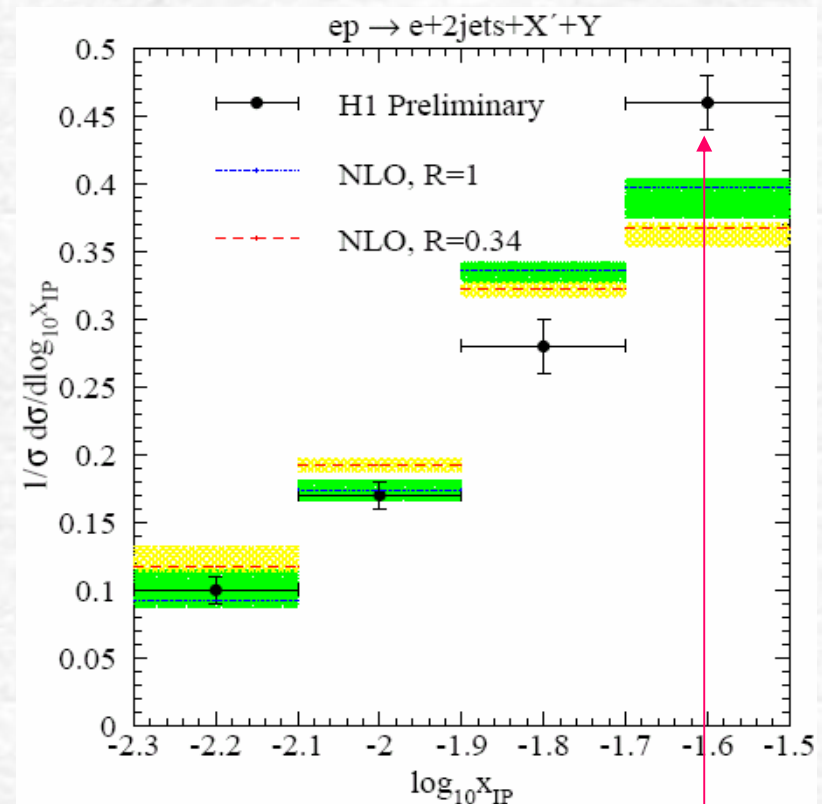
Factorizable Multipomeron Exchanges

y-dependence: Photon flux



→ Small correlations due to exp. cuts

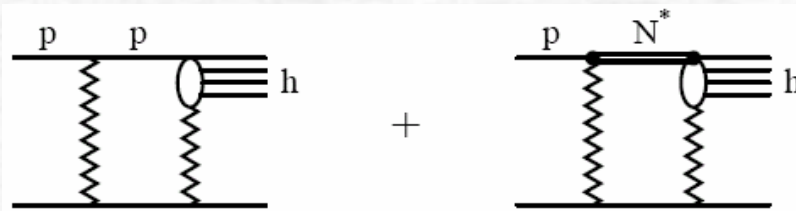
x_{IP} -dependence: Pomeron flux



→ Subleading Reggeon contribution

Two-Channel Eikonal Model

Hadronic collisions:



Survival probability:

$$|S|^2 = \frac{\int d^2b (|\mathcal{M}_v|^2 e^{-\Omega_v(s,b)} + |\mathcal{M}_{\text{sea}}|^2 e^{-\Omega_{\text{sea}}(s,b)})}{\int d^2b (|\mathcal{M}_v|^2 + |\mathcal{M}_{\text{sea}}|^2)}$$

Opacity / optical density: $K_i = 1 \pm \gamma$

$$\Omega_i = K_i \frac{(g_{pp}^{IP})^2 (s/s_0)^\Delta}{4\pi B} e^{-b^2/4B}$$

Kaidalov et al., EPJC 21 (2001) 521

Photoproduction:

Generalized vector meson dominance:

$$J^{PC} = 1^{--}: \gamma \rightarrow \rho, \omega, \dots$$

Fitted parameters ($W = 200$ GeV):

- Total cross section: $\sigma^{\text{tot}}(pp) = 34$ mb
- Pomeron slope: $B = 11.3$ GeV⁻²
- Transition probability: $\gamma = 0.6$

→ ZEUS Coll., EPJ C2 (1998) 247

→ H1 Coll., EPJ C13 (2000) 371

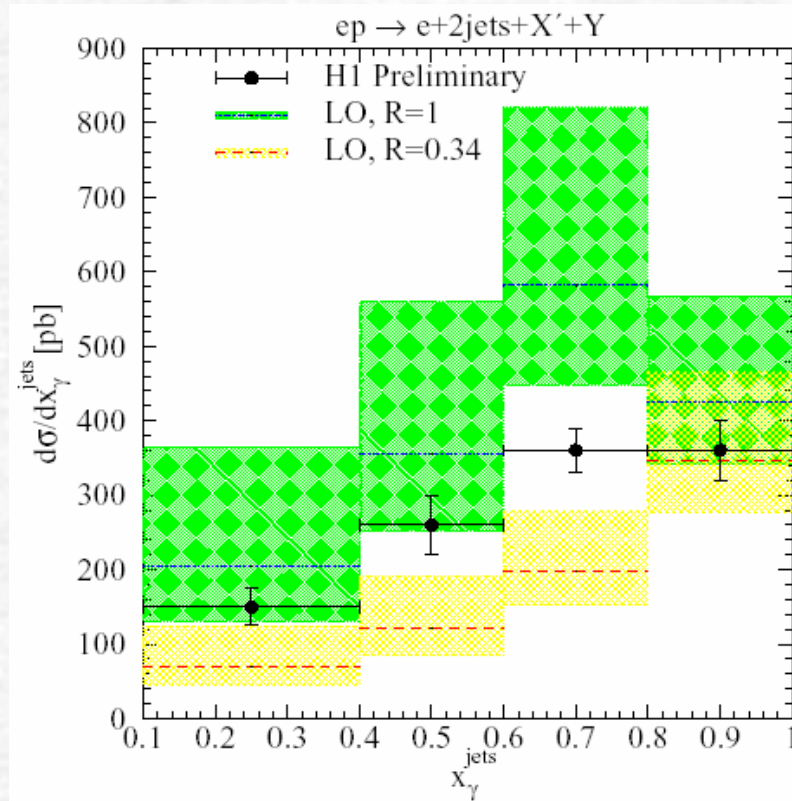
Survival probability:

$$R \equiv |S|^2 \approx 0.34$$

Kaidalov et al., PLB 567 (2003) 61

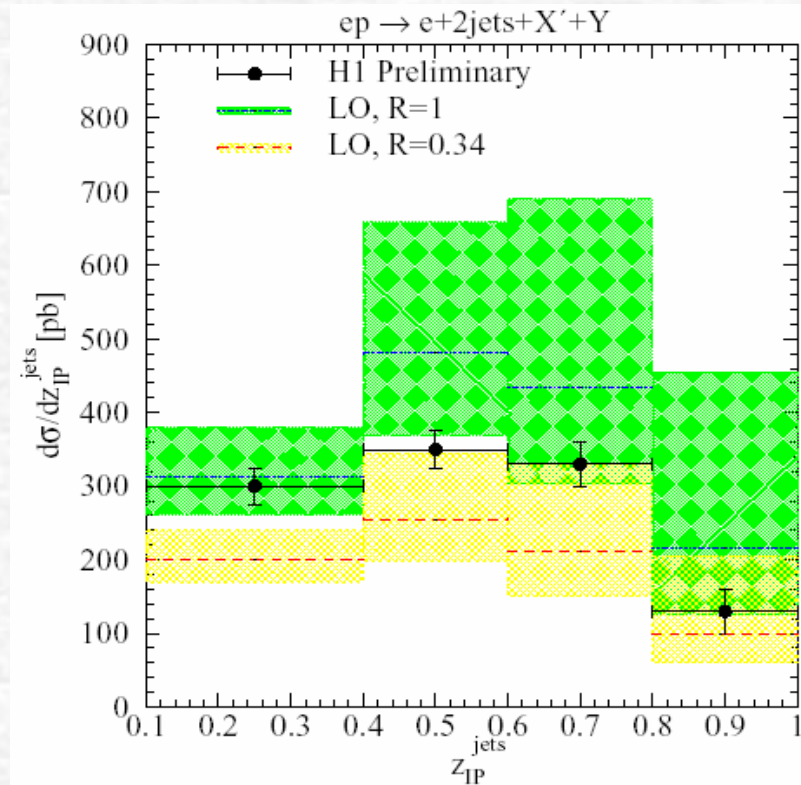
No Sign of Factorization Breaking at LO

x_γ -dependence: Direct/resolved photons



→ At LO, $R = 1$ agrees better with data!

z_{IP} -dependence: Gluon density in pom.

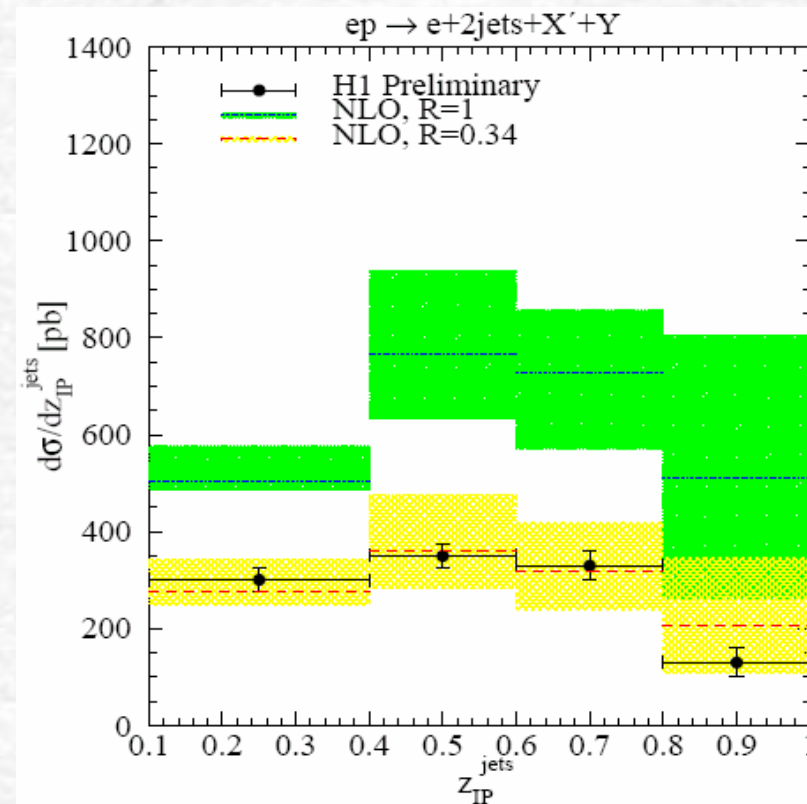
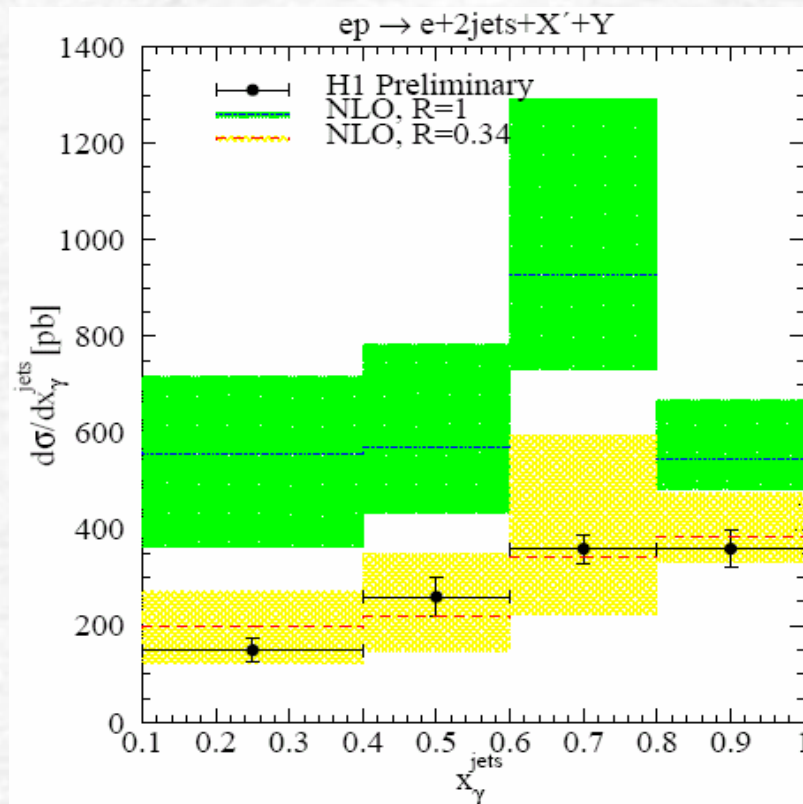


→ Smaller uncertainties in $1/\sigma d\sigma/dz_{\text{IP}}$

Non-Factorizable Multipomeron Exchanges

x_γ -dependence: Direct/resolved photons

z_{IP} -dependence: Gluon density in pom.



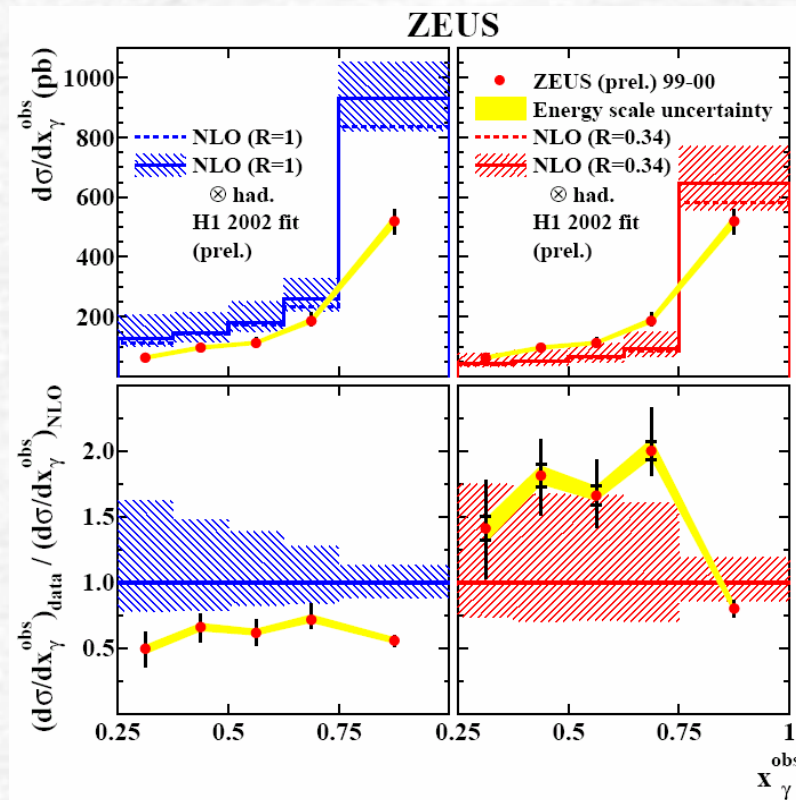
→ Large K-Factor \leftrightarrow Survival probability

→ Reduced scale uncertainties at NLO

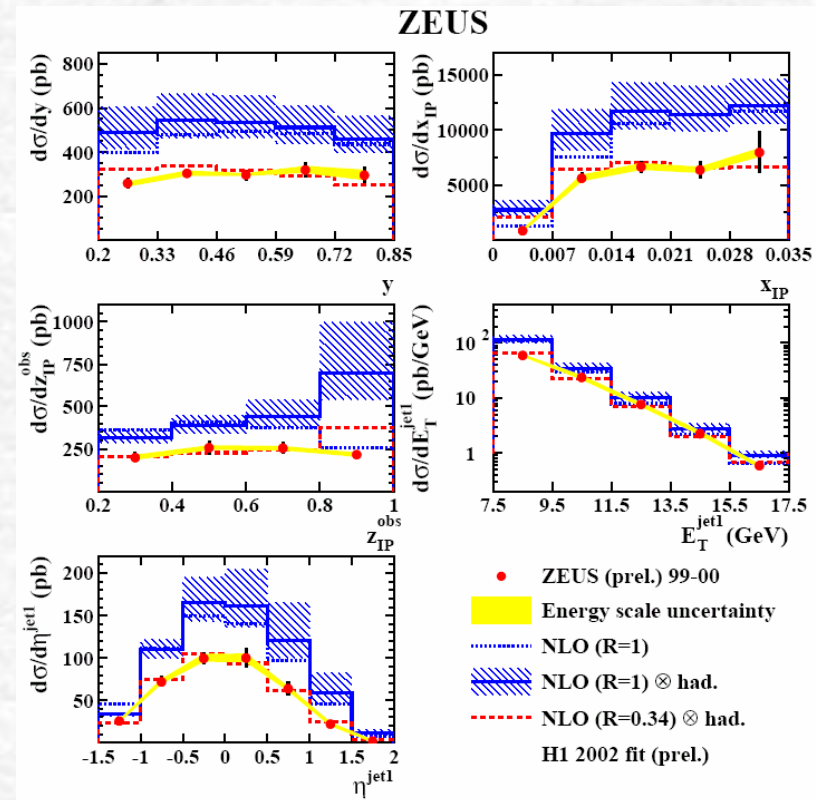
ZEUS Analysis

x_γ -dependence: Direct/resolved photons

Other observables:



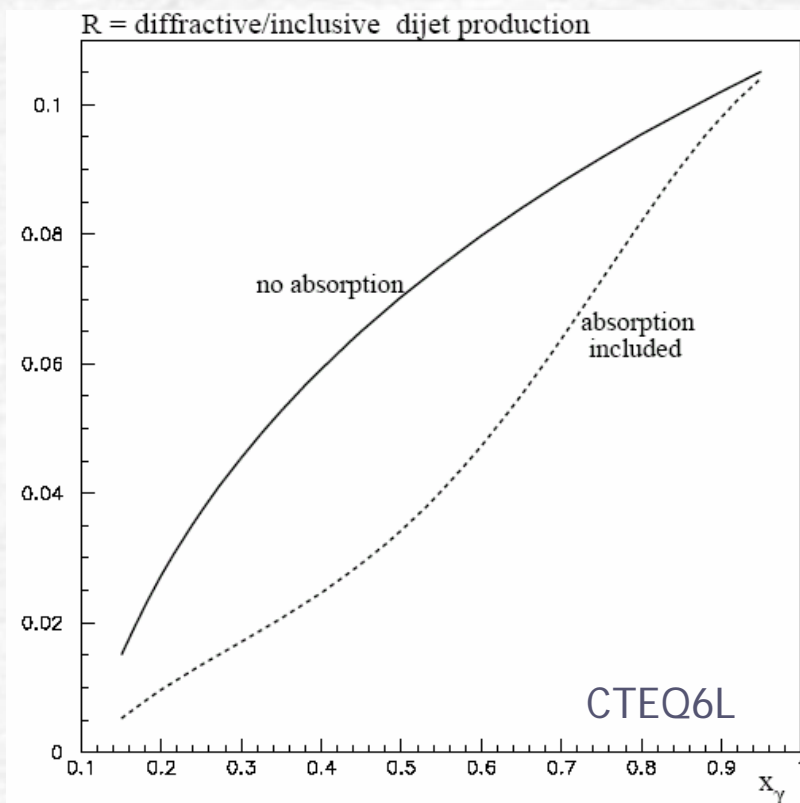
→ At LO, R = 1 agrees better with data!



→ Excellent agreement for absolute σ 's!

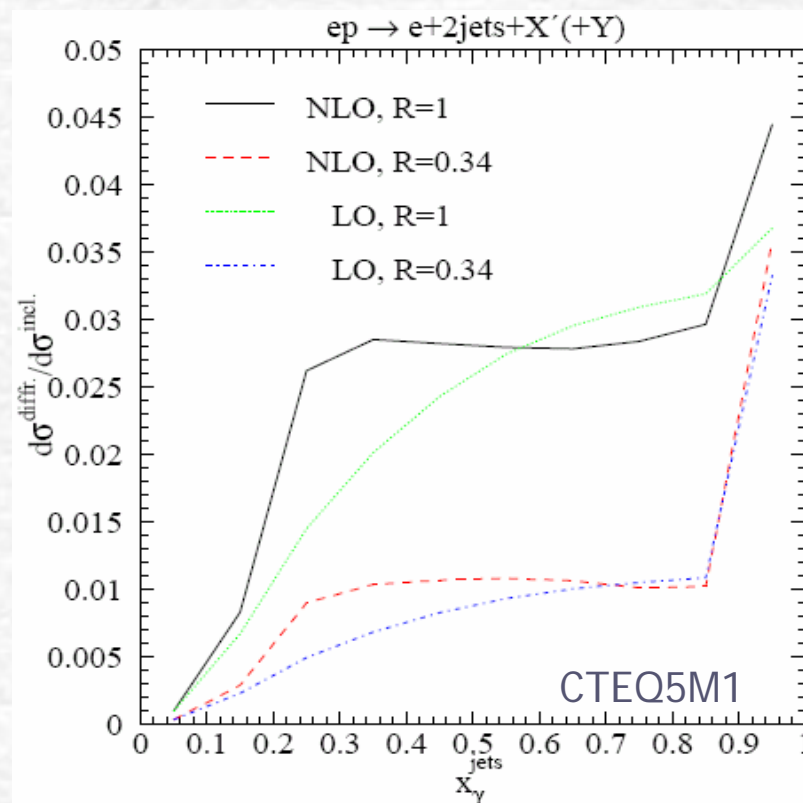
Diffraction / Inclusive Production

$$R = f_{g/IP} \otimes f_{IP/p} / f_{g/p} \text{ with } M_{12} = x_Y Z_{IP} X_{IP} W:$$



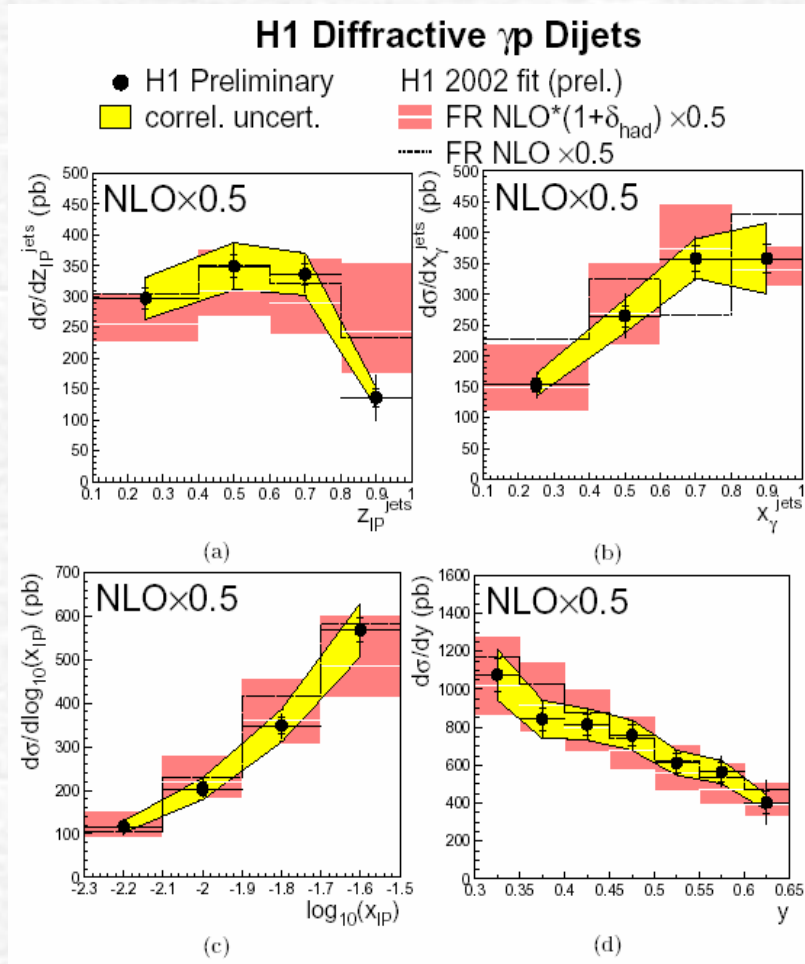
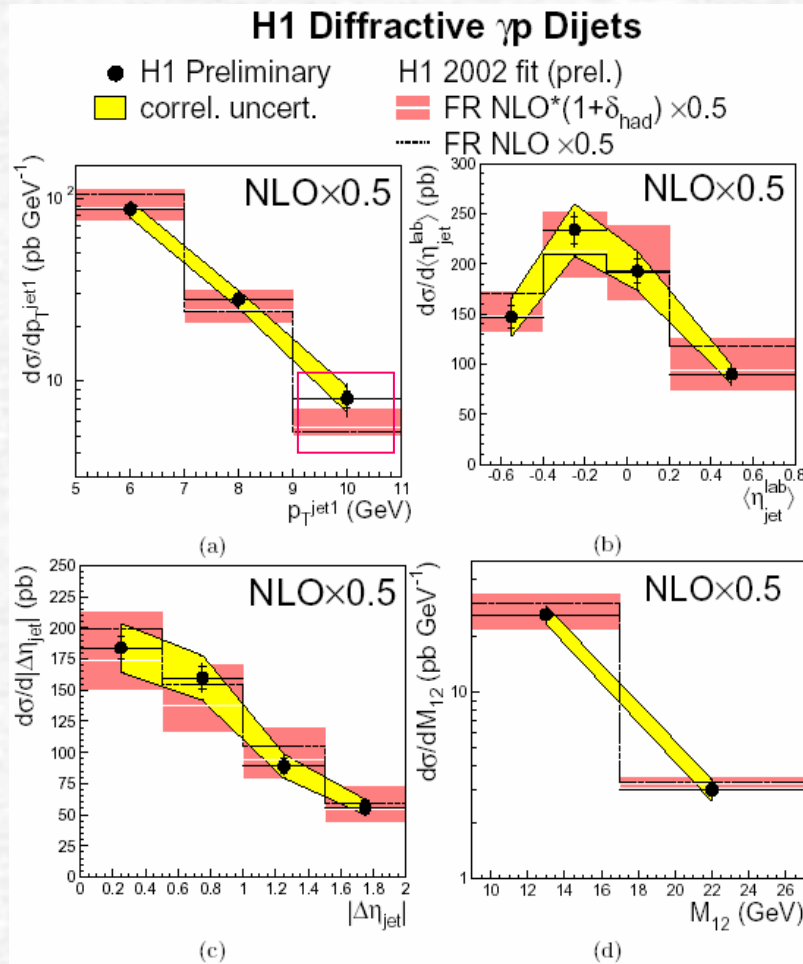
A. Kaidalov et al., PLB 567 (2003) 61

$$R = \sigma^{\text{diffr.}} / \sigma^{\text{incl.}} \text{ with full kinematics:}$$



MK, G. Kramer, EPJC 38 (2004) 39

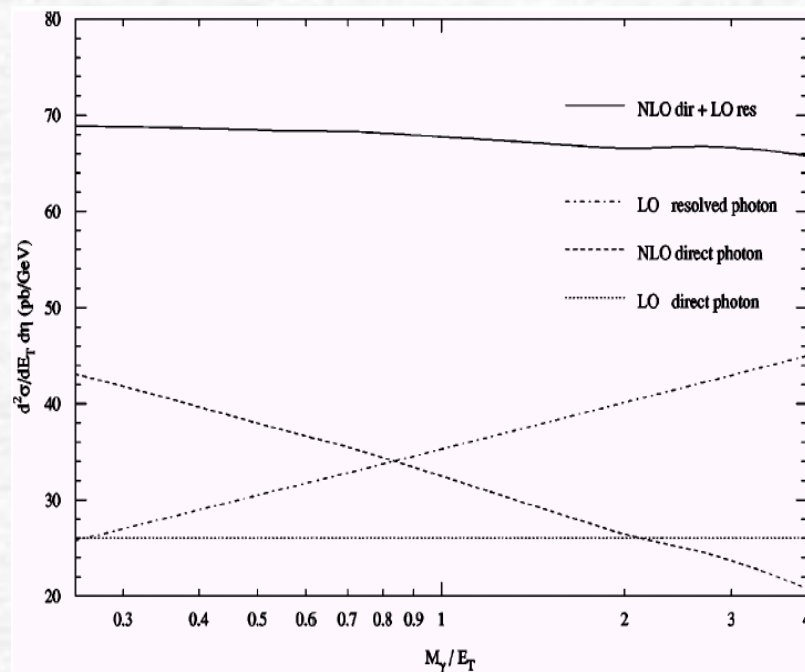
But: Data also support direct suppression!



Factorization Scale Dependence

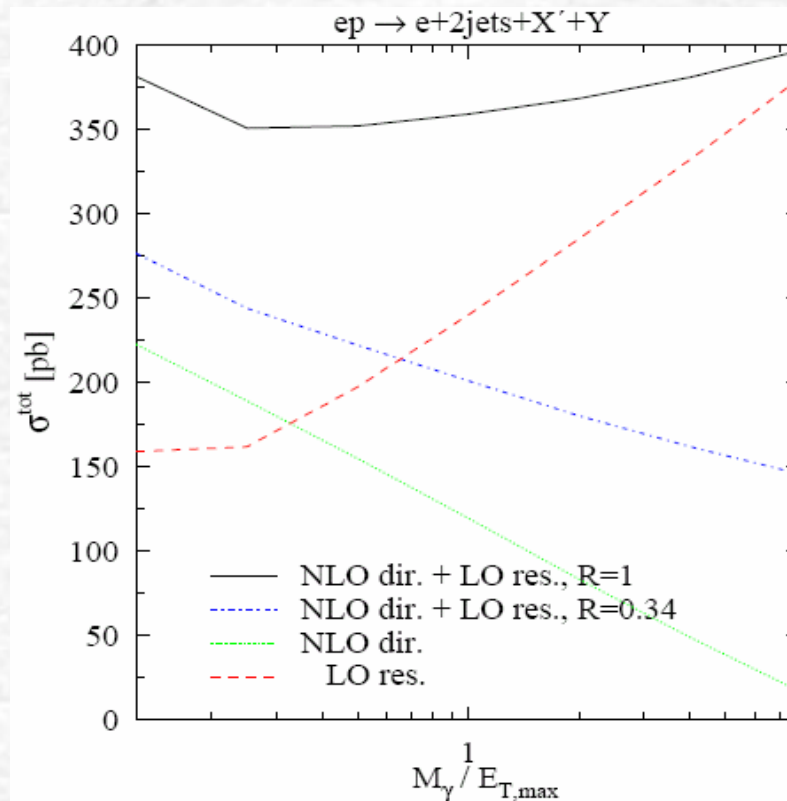
Inclusive photoproduction:

$$|\mathcal{M}^I|_{ab \rightarrow 123}^2 = \ln\left(\frac{M^2}{Q^2}\right) |\mathcal{M}^B|_{cb \rightarrow 12}^2 P_{c \leftarrow a}(x) + \dots$$



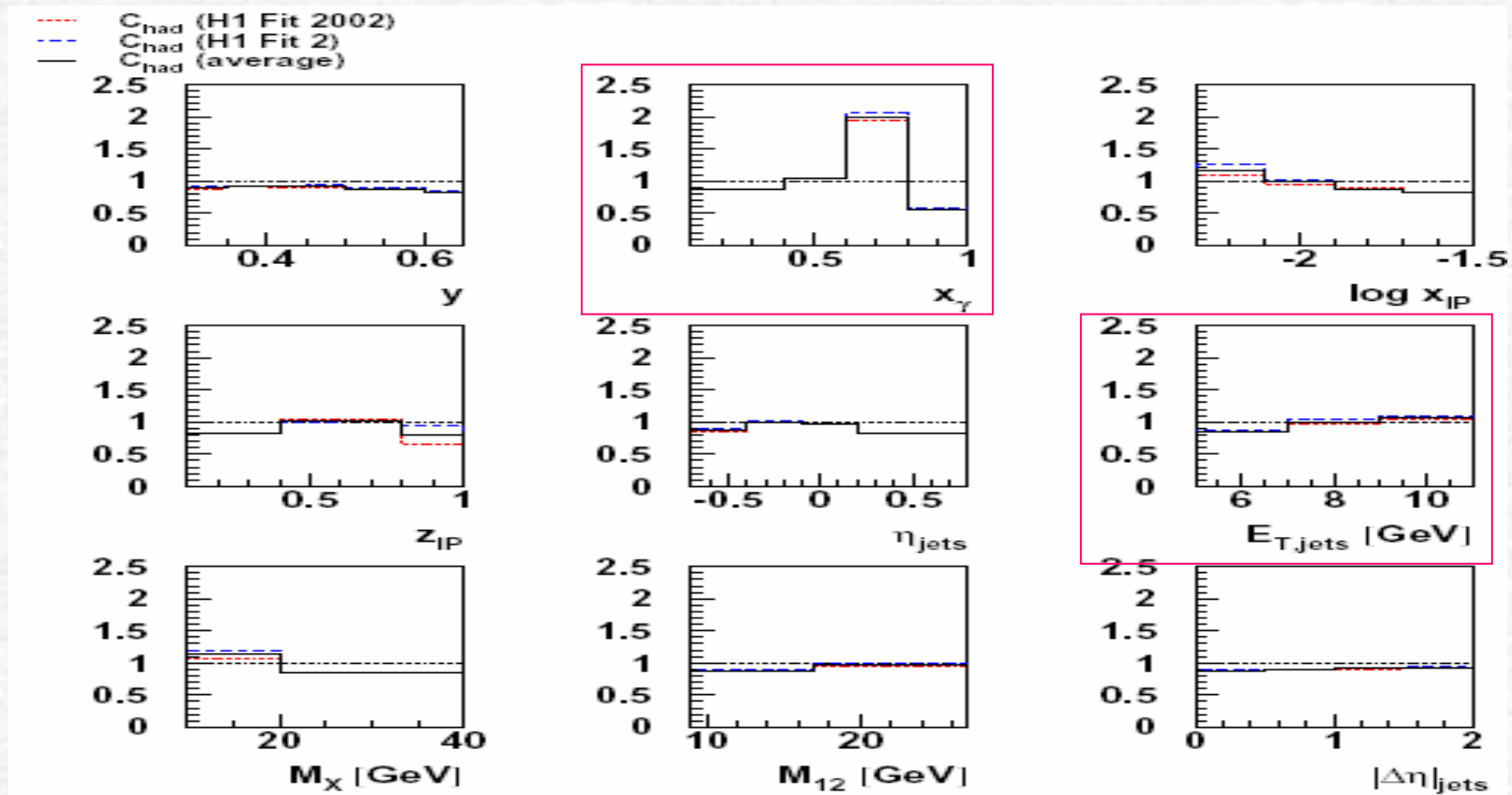
MK, Rev. Mod. Phys. 74 (2002) 1221

Diffractive photoproduction:



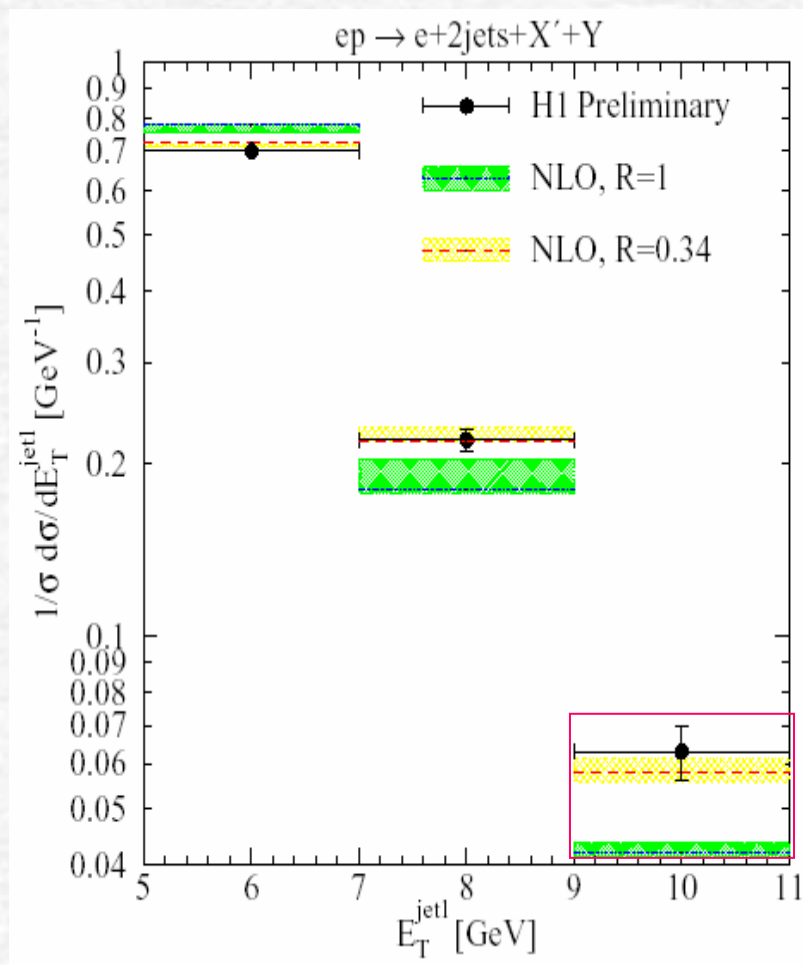
MK, G. Kramer, EPJC 38 (2004) 39

Hadronization Corrections



→ Observable and model dependent!

E_T -Distribution



Importance of large E_T :

- Direct process dominates
- IS singularity less important
- Hadronization corrections small
- Experimentally directly accessible
- Less sensitive than $x\gamma$

Result:

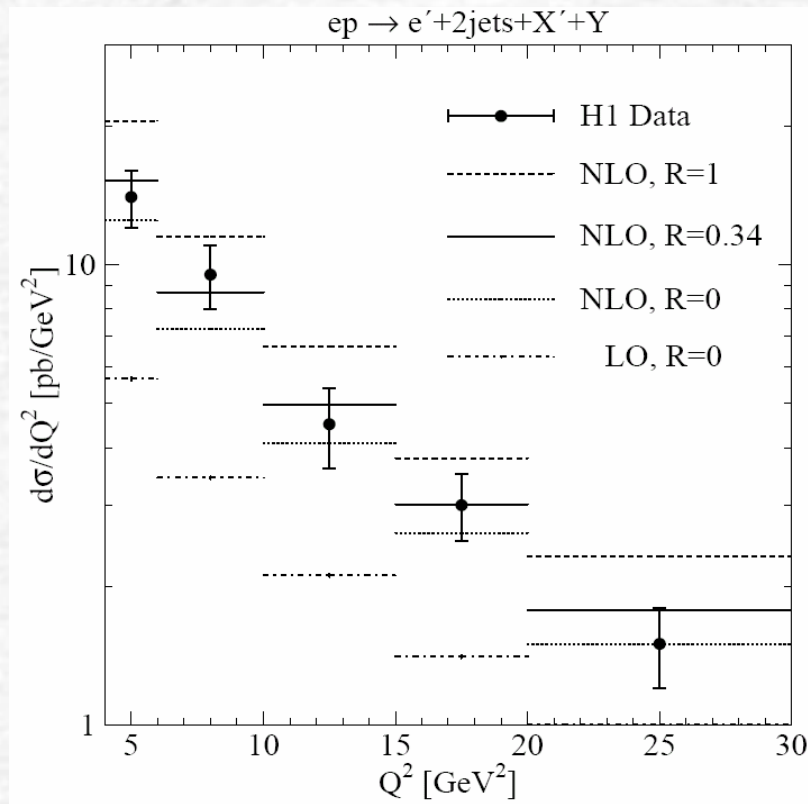
- Suppressed result agrees
- Unsuppressed 50% too low

How can we learn more?

- Critical role of IS singularity
- Transition from γp to DIS

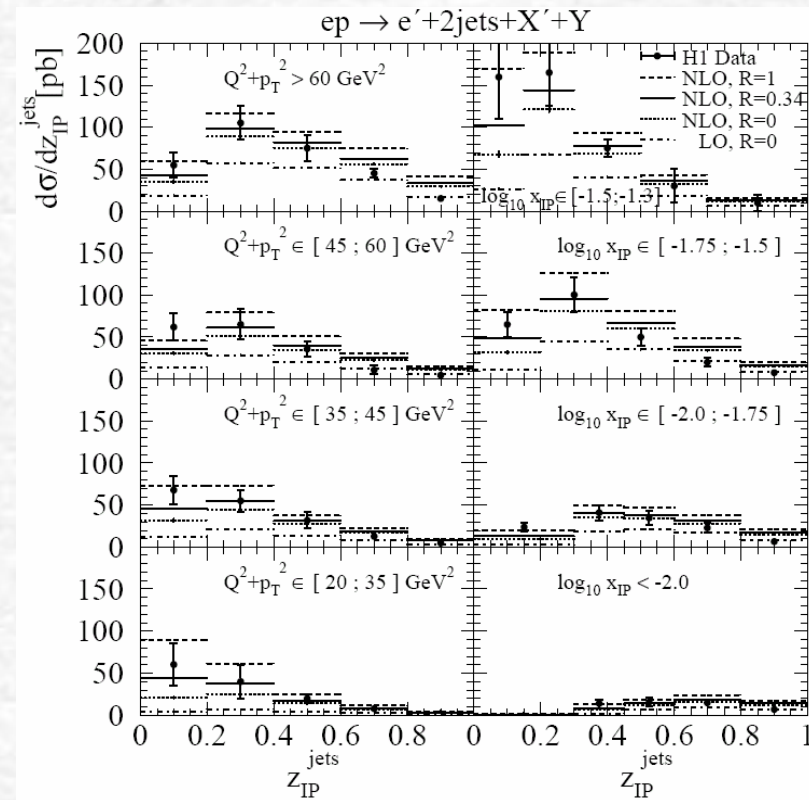
High- to Low- Q^2 Transition in DIS

Q^2 -dependence:



MK, G. Kramer, PRL 93 (2004) 232002

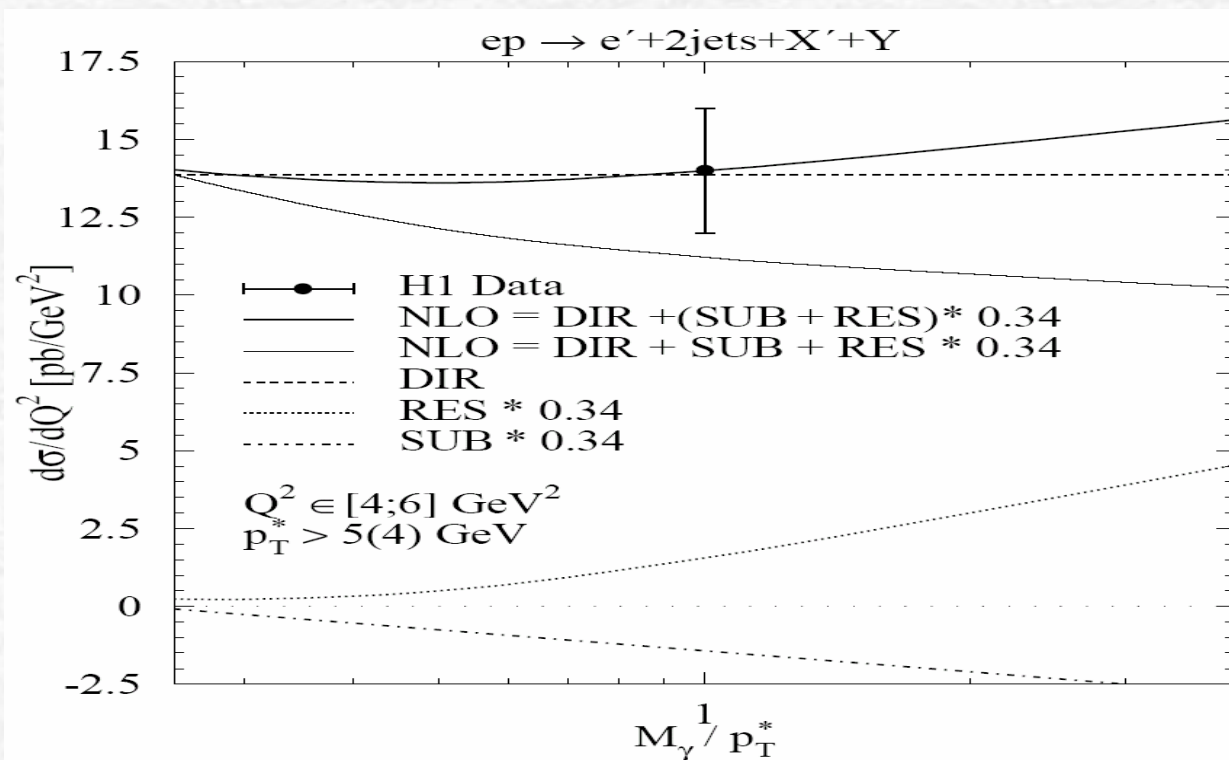
z_{IP} -dependence:



MK, G. Kramer, PRL 93 (2004) 232002

Factorization Scale Dependence (1)

$$M(P^2)_{\overline{MS}} = -\frac{1}{2N_c} P_{q_i \leftarrow \gamma}(z_a) \ln \left(\frac{M_\gamma^2 z_a}{(z_a P^2 + y_s s)(1 - z_a)} \right) + \frac{Q_i^2}{2}$$

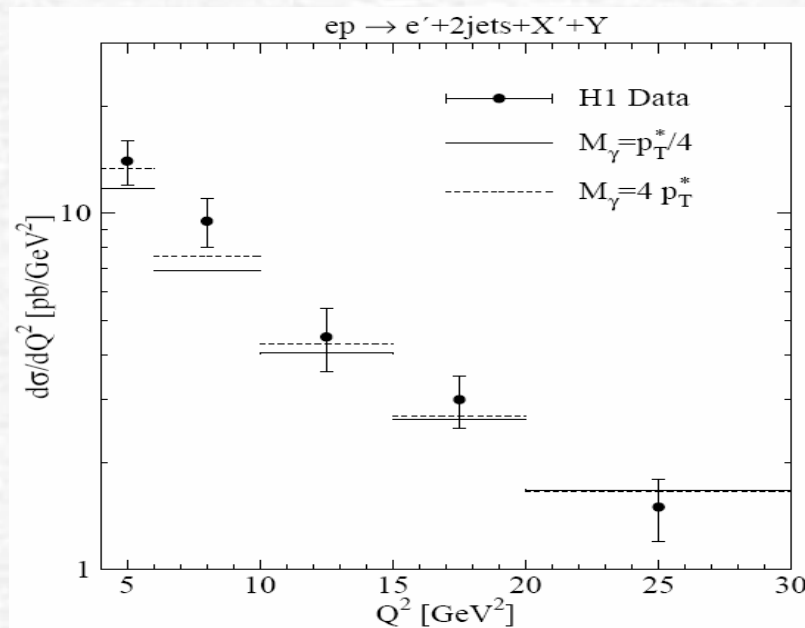


MK, G. Kramer, JPG 31 (2005) 1391

Factorization Scale Dependence (2)

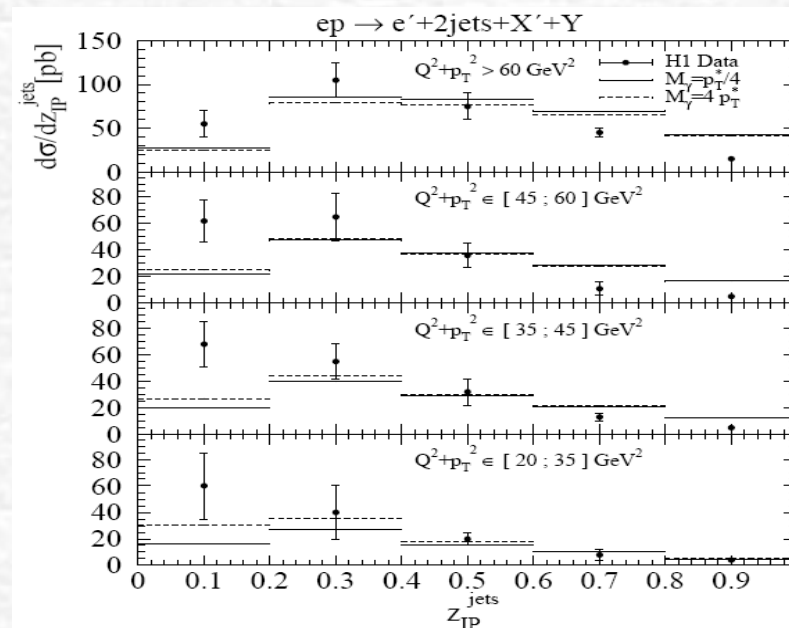
$$M(P^2)_{\overline{MS}} = -\frac{1}{2N_c} P_{q_i \leftarrow \gamma}(z_a) \ln \left(\frac{M_\gamma^2 z_a}{(z_a P^2 + y_s s)(1 - z_a)} \right) + \frac{Q_i^2}{2}$$

Q^2 -dependence:



MK, G. Kramer, JPG 31 (2005) 1391

z_{1P} -dependence:

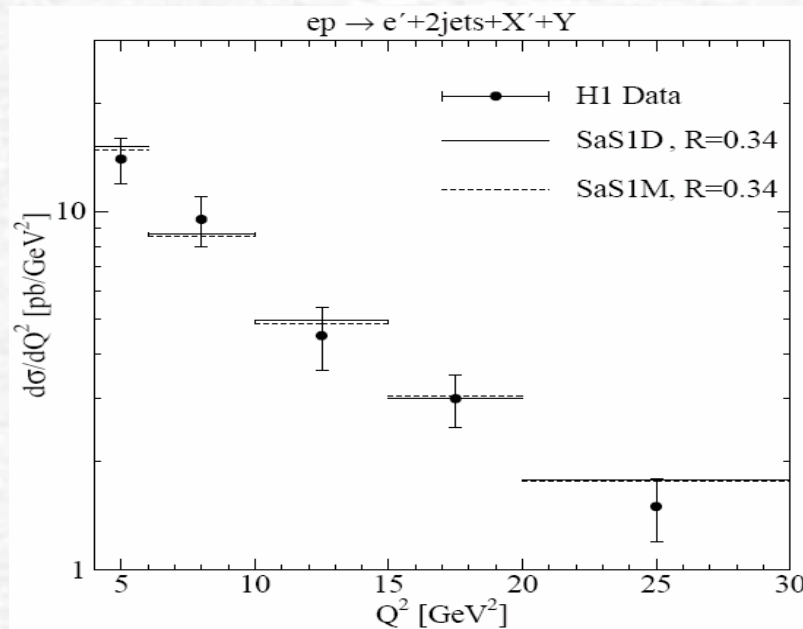


MK, G. Kramer, JPG 31 (2005) 1391

Factorization Scheme Dependence

$$F_2^\gamma(Q^2) = \sum_q 2xe_q^2 \left\{ f_{q/\gamma}(Q^2) + \frac{\alpha_s(Q^2)}{2\pi} [C_q \otimes f_{q/\gamma}(Q^2) + C_g \otimes f_{g/\gamma}(Q^2)] + \frac{\alpha}{2\pi} e_q^2 C_\gamma \right\}.$$

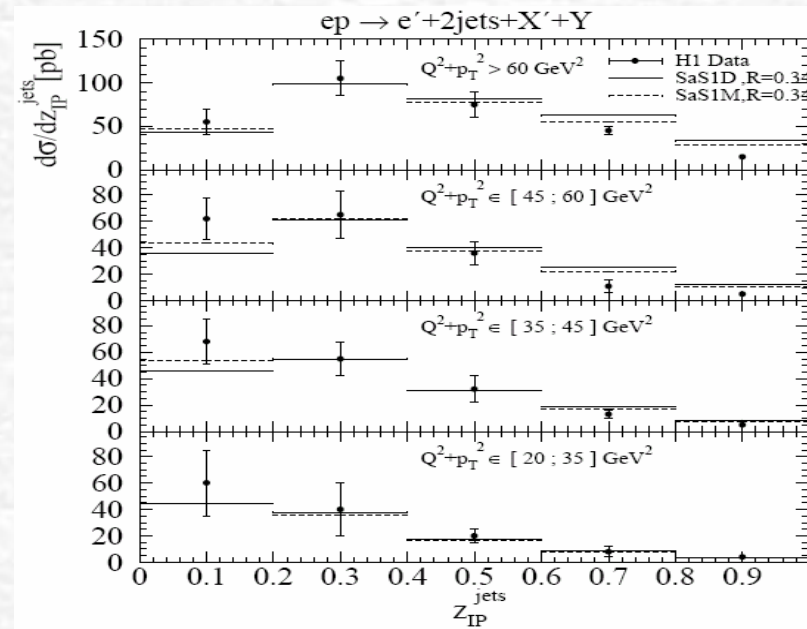
Q^2 -dependence:



MK, G. Kramer, JPG 31 (2005) 1391

$$C_\gamma(x) = 2N_C C_g(x) = 3 \left[(x^2 + (1-x)^2) \ln \frac{1-x}{x} + 8x(1-x) - 1 \right],$$

z_{IP} -dependence:



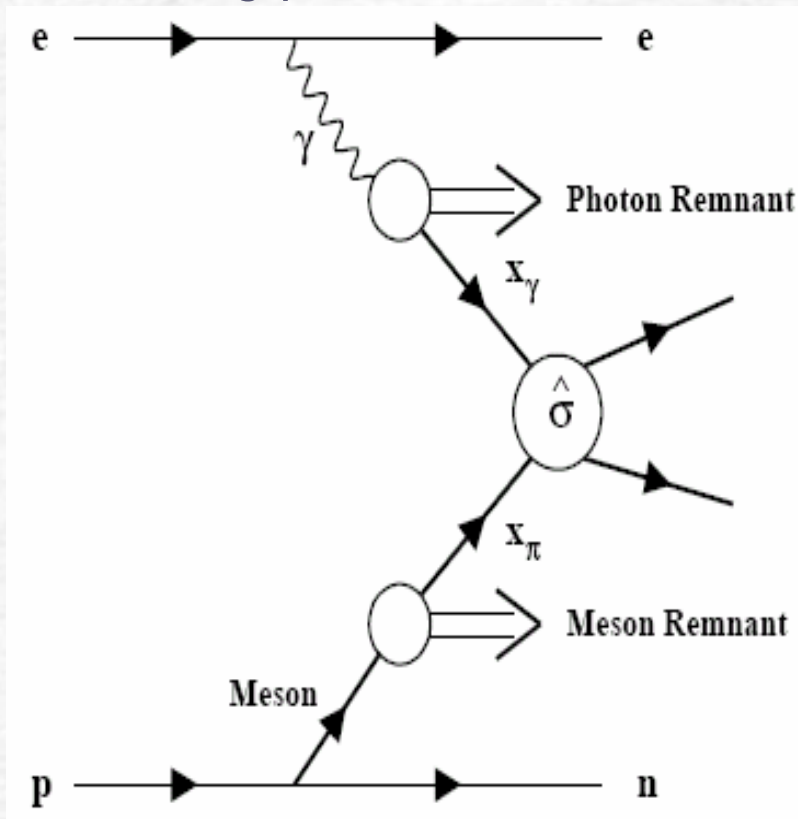
MK, G. Kramer, JPG 31 (2005) 1391

Components of Parton Densities in Photon

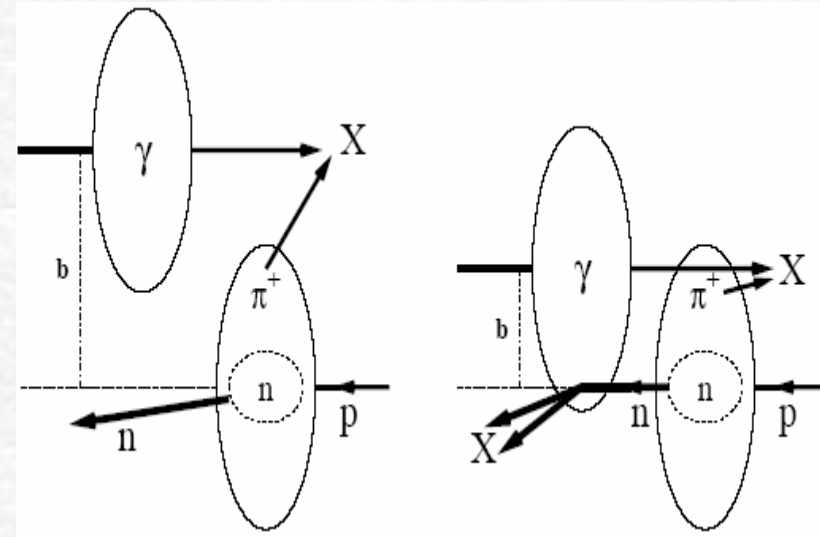
- ☞ SaS parameterizations allow for separation:
 - Anomalous component: Resummation of IS singularity
 - Hadronic component: Vector meson dominance model
- ☞ VMD component suppressed:
 - 10^{-4} for $Q^2 \approx 70 \text{ GeV}^2$
 - 10^{-2} for $Q^2 \approx 5 \text{ GeV}^2$
- ☞ Anomalous component dominates:
 - Direct higher order contributions
- ☞ Known from inclusive low- Q^2 production

Leading Neutron Production (1)

Scattering process:



Meson cloud model:



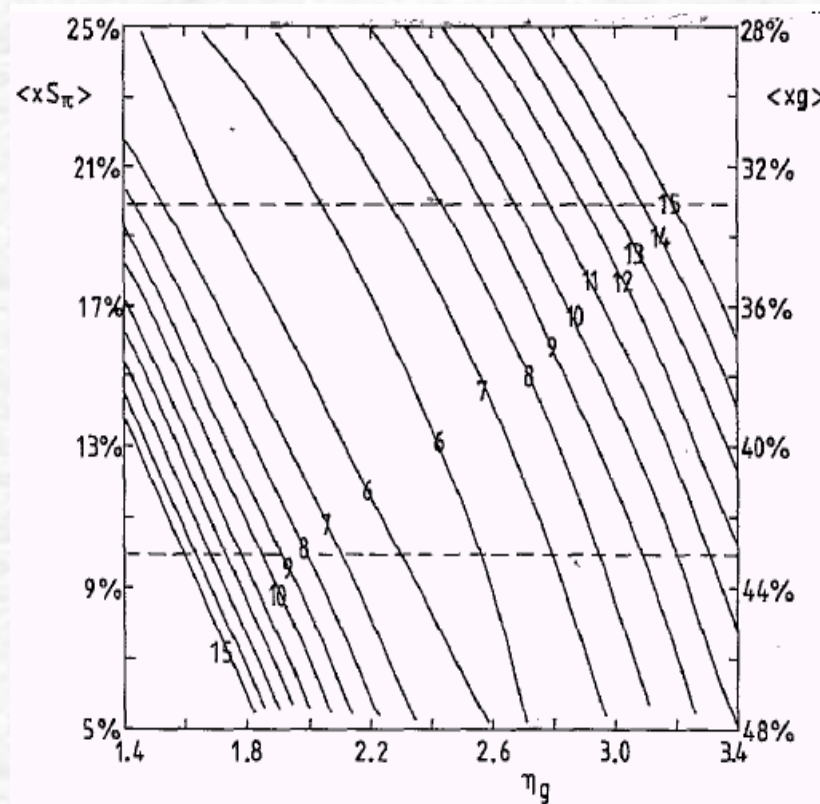
Pion flux factor:

$$f_{\pi/p}(1-x_n, t') = \int d^2 p_T |\phi_{\pi/p}(x_n, p_T)|^2 \delta(t' - f(p_T))$$

$$= \frac{3C_n}{4\pi} \frac{g_{n\pi p}^2}{4\pi} \frac{-t'}{(m_\pi^2 - t')^2} (1-x_n)^{1-2\alpha'_\pi(t'-m_\pi^2)} [F(x_n, t')]^2$$

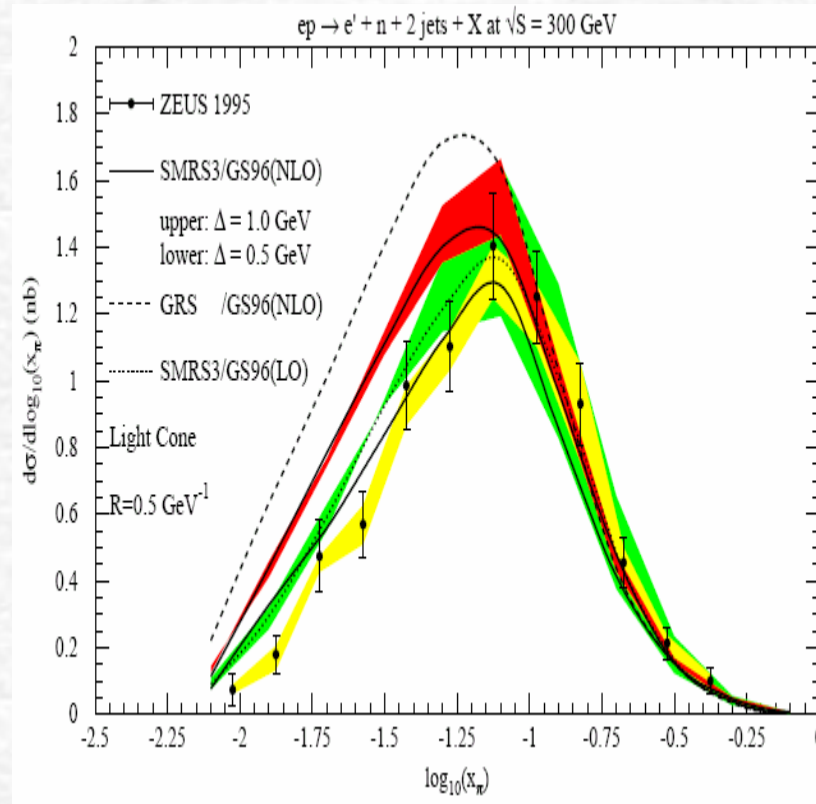
Leading Neutron Production (2)

Sea-quark and gluon density in pions:



Sutton, Martin, Roberts, Stirling, PRD 45

Dijet production with a leading neutron:



MK, G. Kramer, PLB 508 (2001) 259

Conclusions

Hard diffraction: **Factorizable or not?**

- ☞ Deep inelastic scattering: Yes → Diffractive parton densities
- ☞ Hadronic scattering: No → Multipomeron exchanges
- ☞ Important application: Diffractive Higgs production at LHC

Diffractive photoproduction of dijets: **Initial state singularity at NLO**

- ☞ Direct / resolved photoproduction: x_γ and M_γ dependence
- ☞ (Non-) factorizable multipomeron exchanges

Two-channel eikonal model:

- ☞ Generalized vector meson dominance: $\gamma \rightarrow \rho, \omega, \dots$
- ☞ Rapidity gap survival probability: **$R = 0.34$**

Related process:

- ☞ Leading neutron with π -exchange (NB: $f_{q/\pi}$, not $f_{g/IP}$!)