

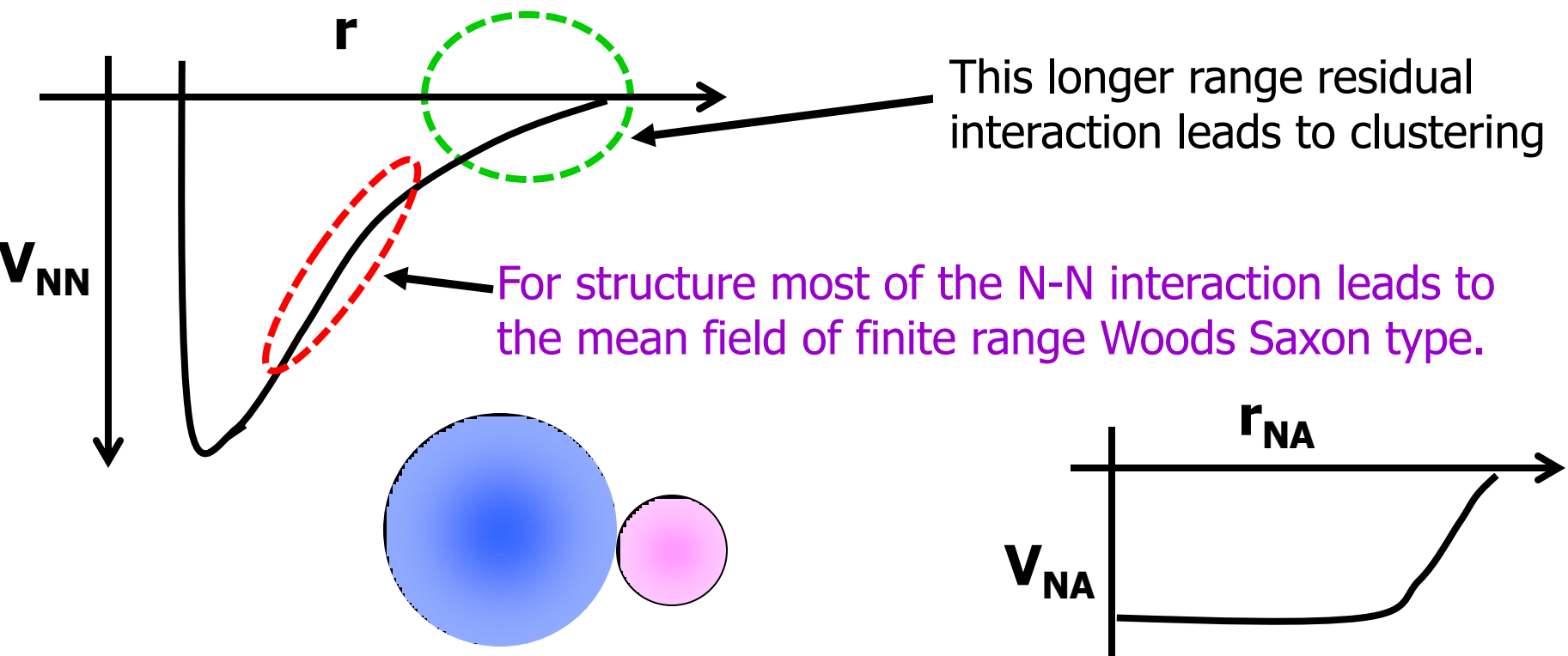
# Nuclear Surface Unveiled by Knockout Reactions.

**Arun K Jain**

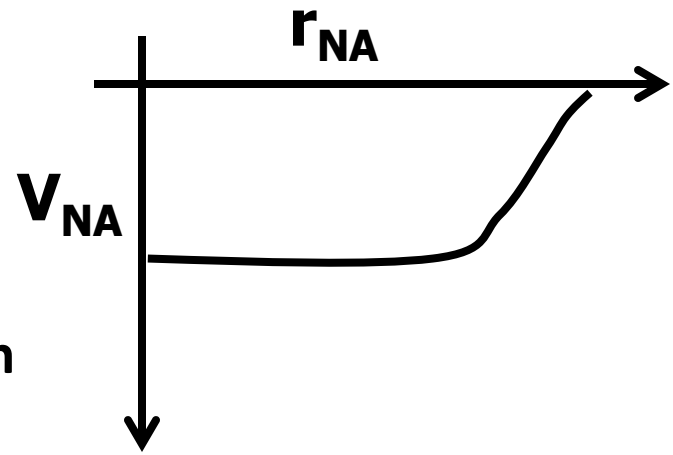
**Nuclear Physics Division, B.A.R.C., Mumbai.**



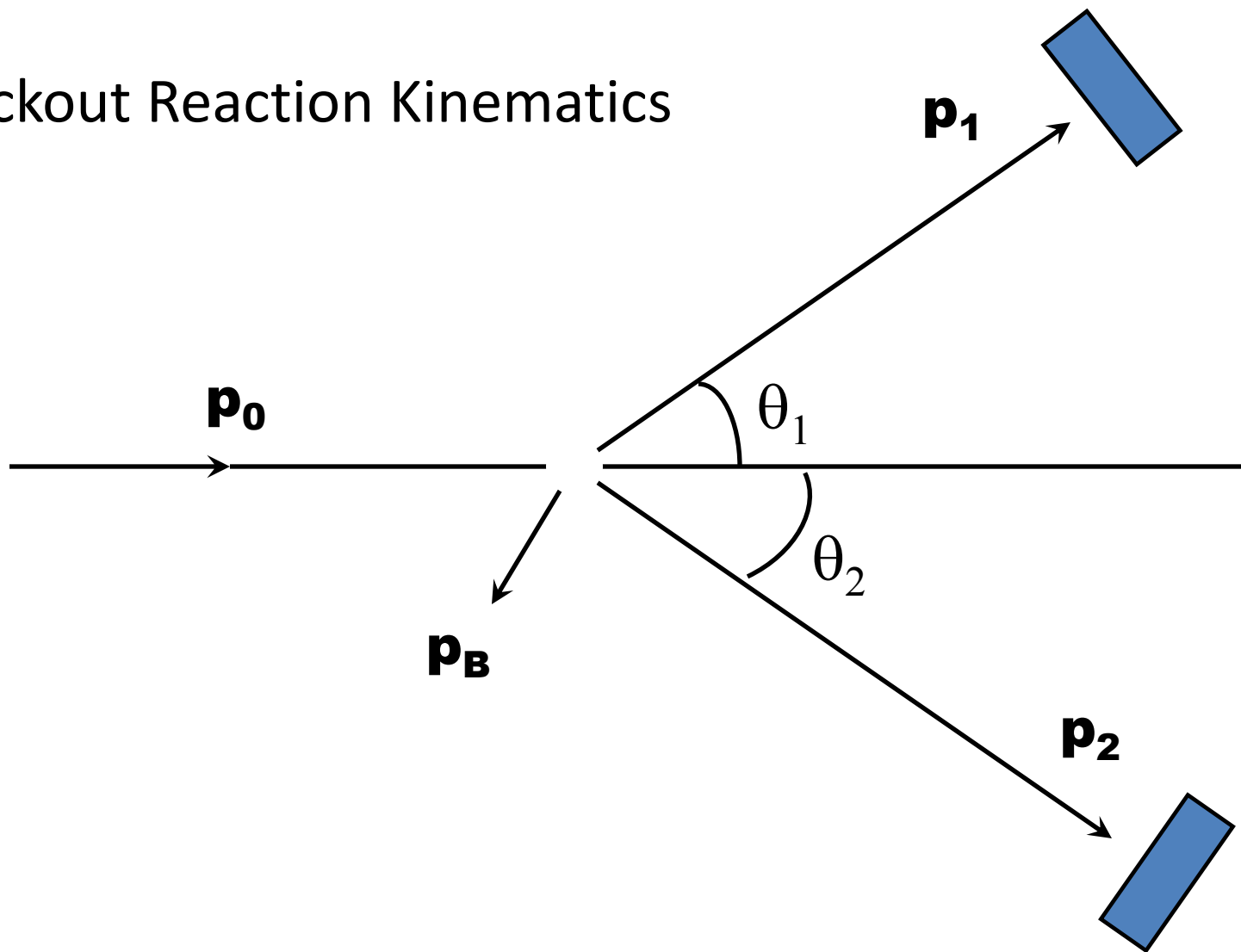
N-N Interaction has a complicated nature ( provided to it by the strong coupling finite mass mesons), it has strong **short range repulsion** (almost a **hard core** of  $\sim 0.5$  to  $0.6$  fm) and a finite short range, but a comparatively longer range,  $\sim 2$  fm **strong attraction**.

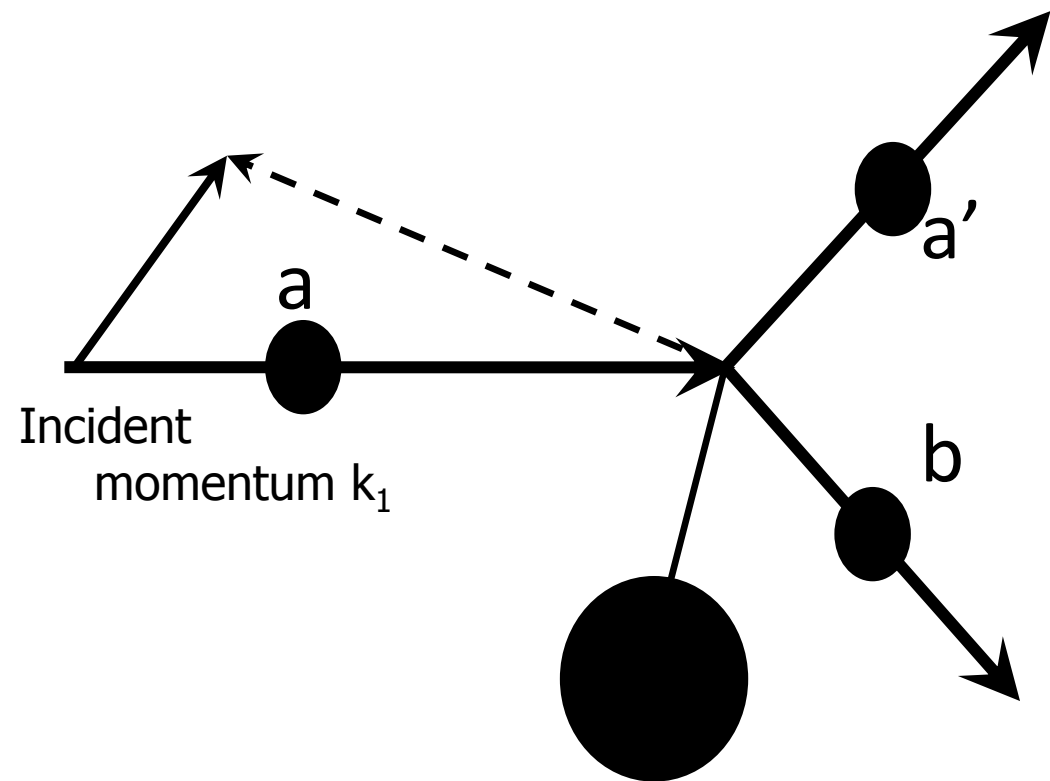


Clustering due to long range residual interaction



# Knockout Reaction Kinematics

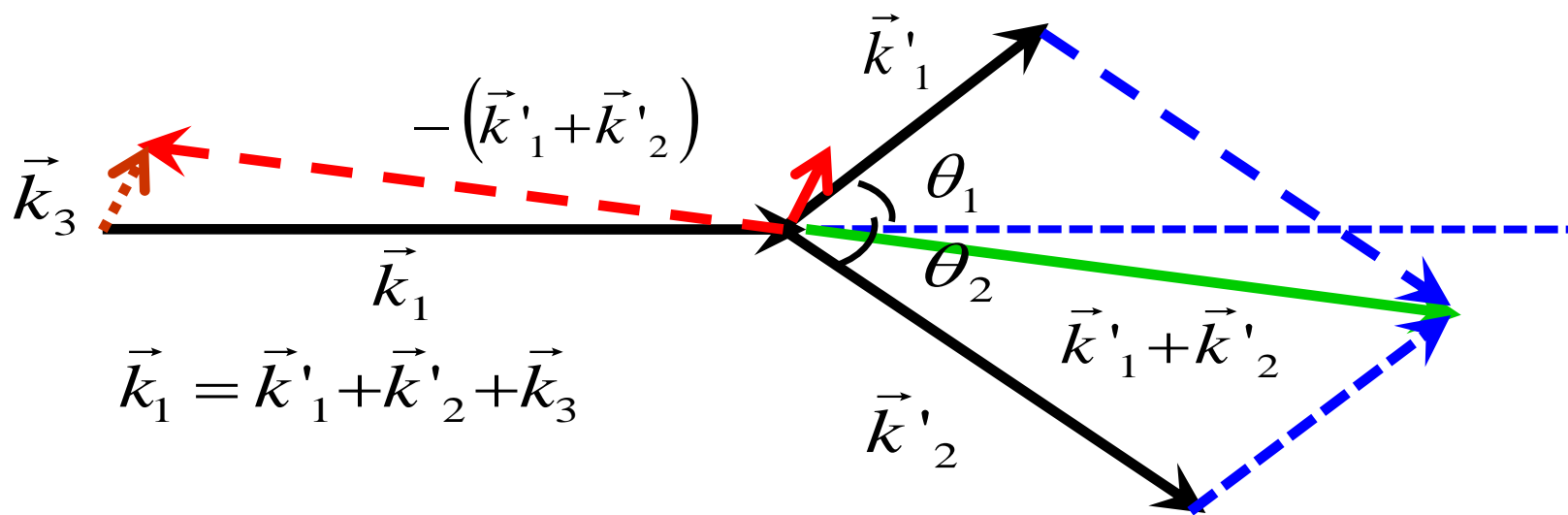




## Knockout Reaction

$A(a, a'b)B$

$$\vec{k}_1 \quad \vec{k}'_1 \quad \vec{k}'_2$$



If  $b$  were free then

$$\mathbf{k}_3 = -\mathbf{k}_3 = 0 \quad \vec{k}_1 = \vec{k}'_1 + \vec{k}'_2 \quad E_1 = E'_1 + E'_2$$

If the particle is bound by a few  $MeV$ , then

$$E_0 = E'_1 + E'_2 + Q$$

as the  $Q$  is ( $-ve$ )

$E'_1$  and  $E'_2$  are  $<$   $E_1$  and  $E_2$  respectively.

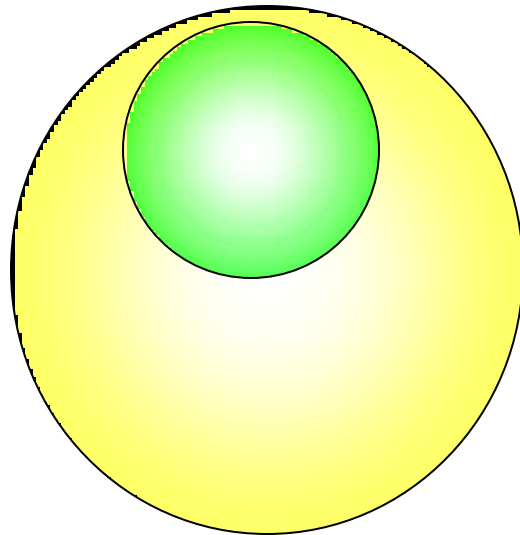
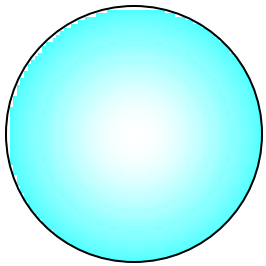
Hence  $k'_1$  and  $k'_2$  are  $<$   $k_1$  and  $k_2$  respectively.

and  $\theta_1$  and  $\theta_2$  of  $\mathbf{k}'_1$  and  $\mathbf{k}'_2$  will be

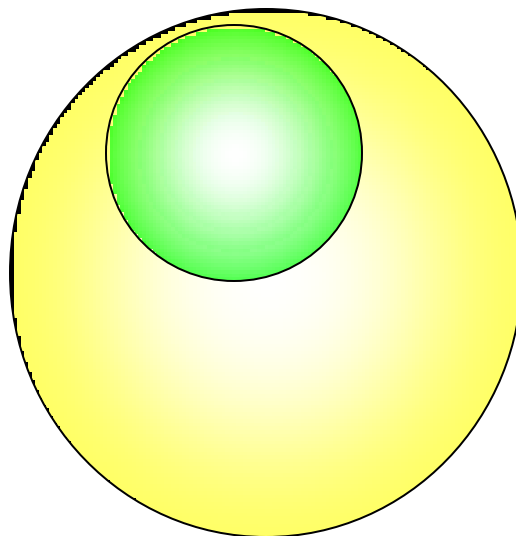
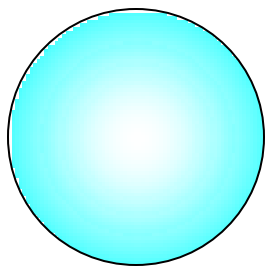
slightly  $<$  that of free scattering.

# Zero Range Knockout

# Zero Range Knockout

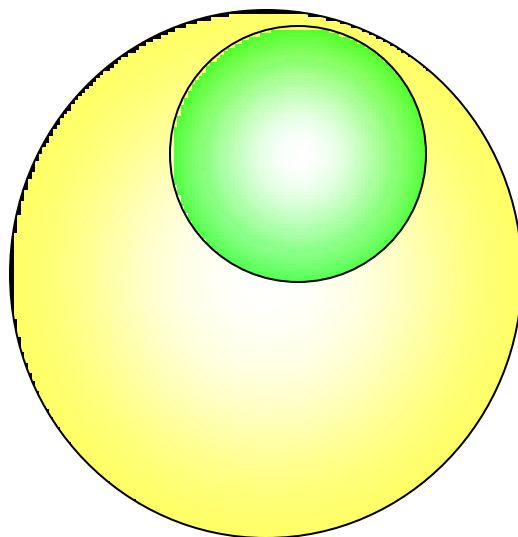
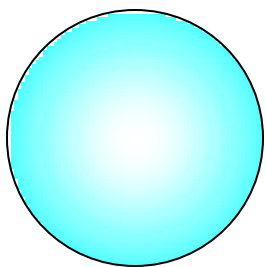


# Zero Range Knockout

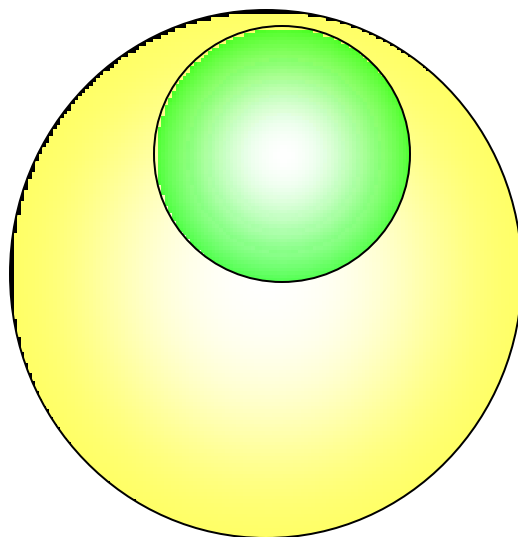
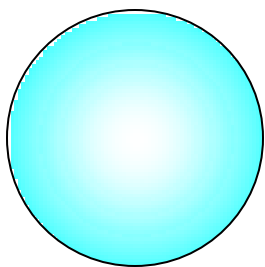




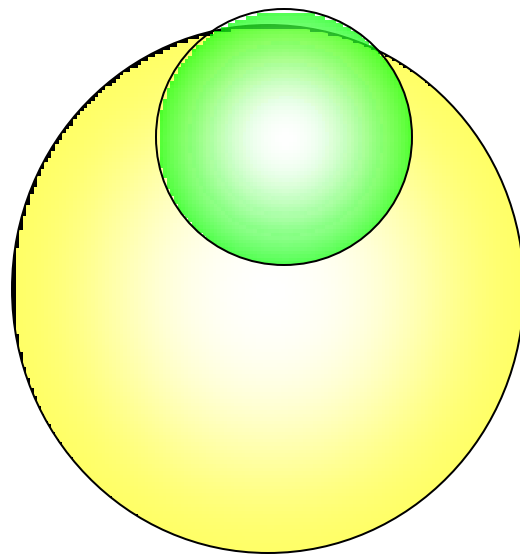
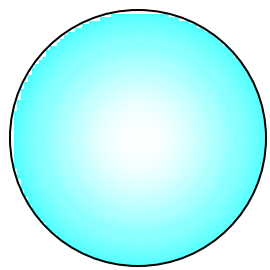
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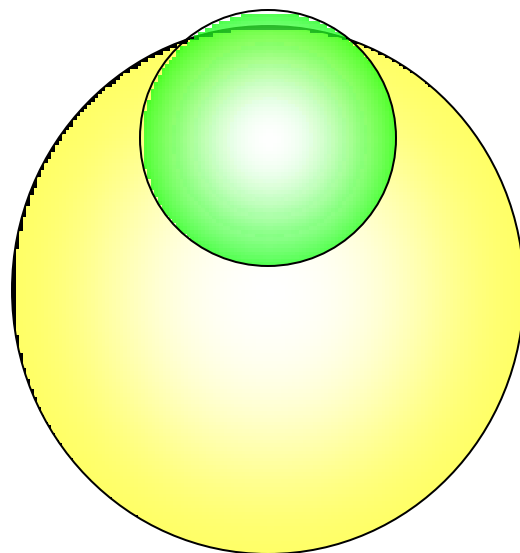
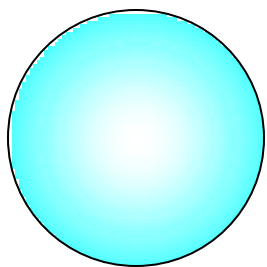
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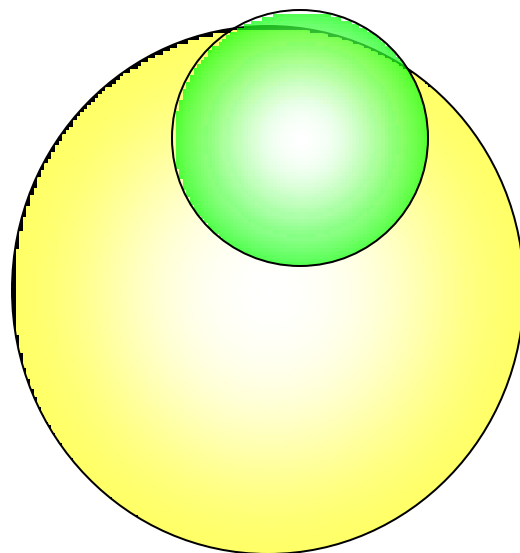
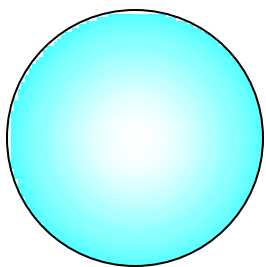
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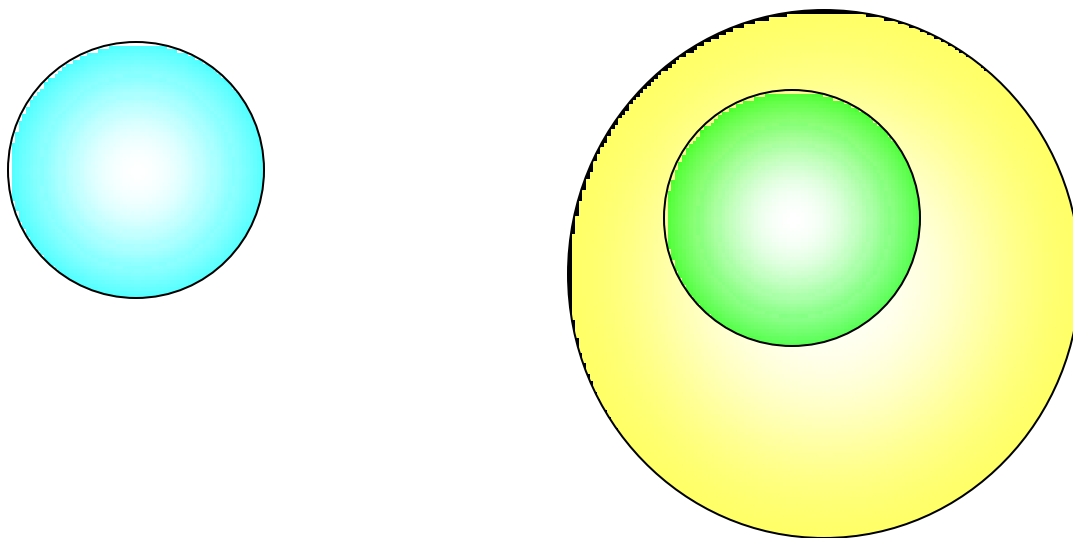
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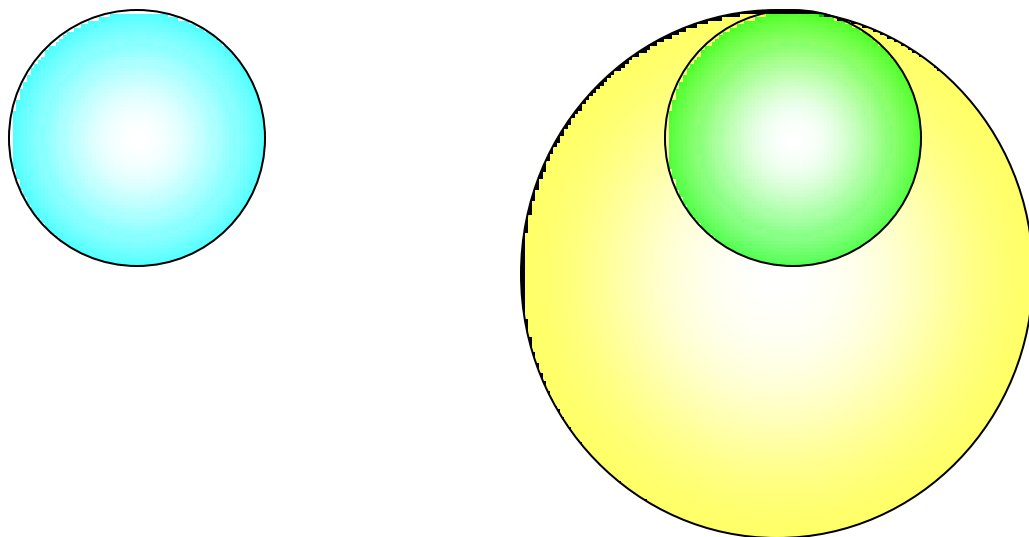
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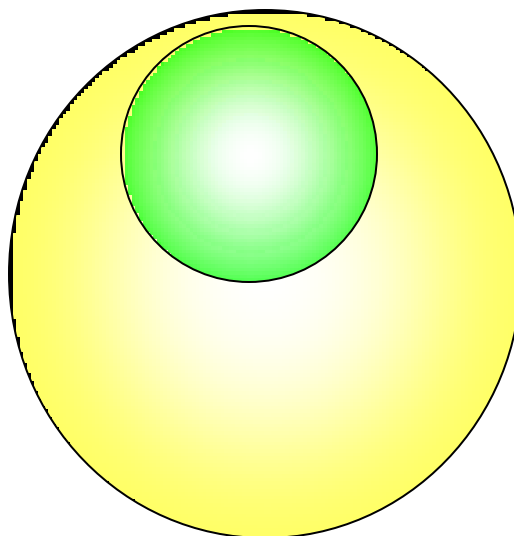
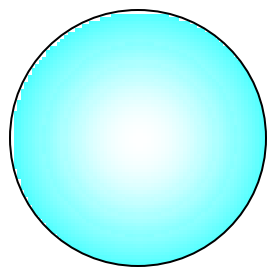
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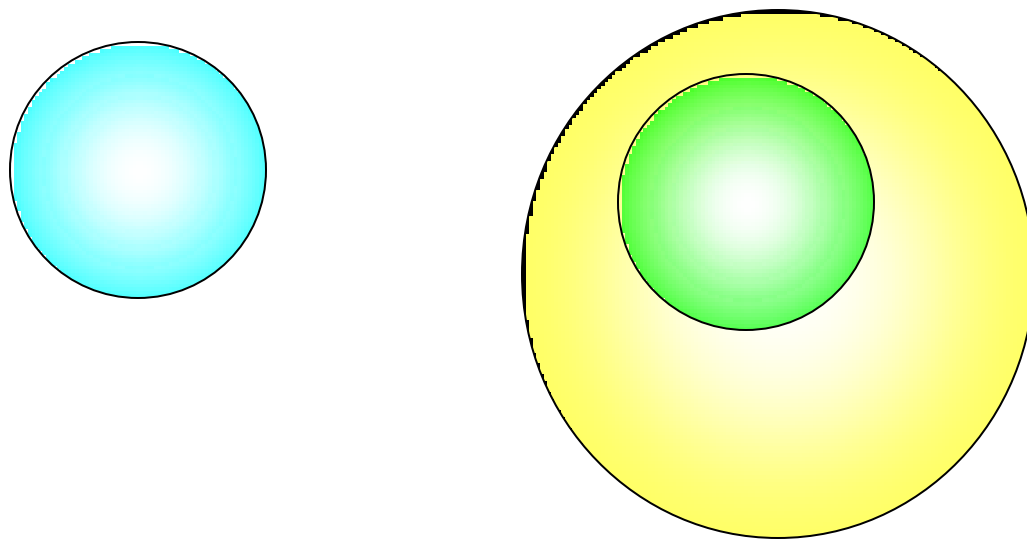


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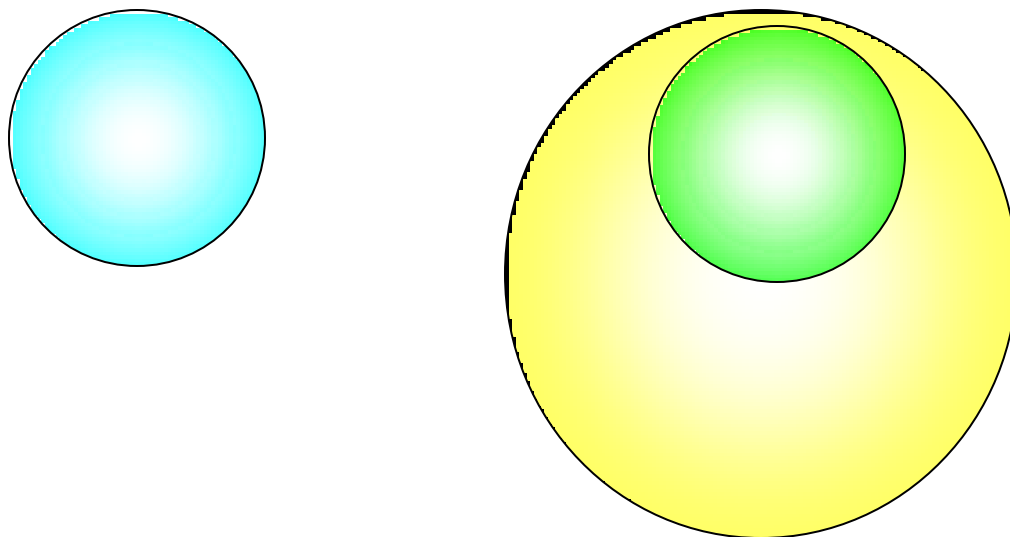




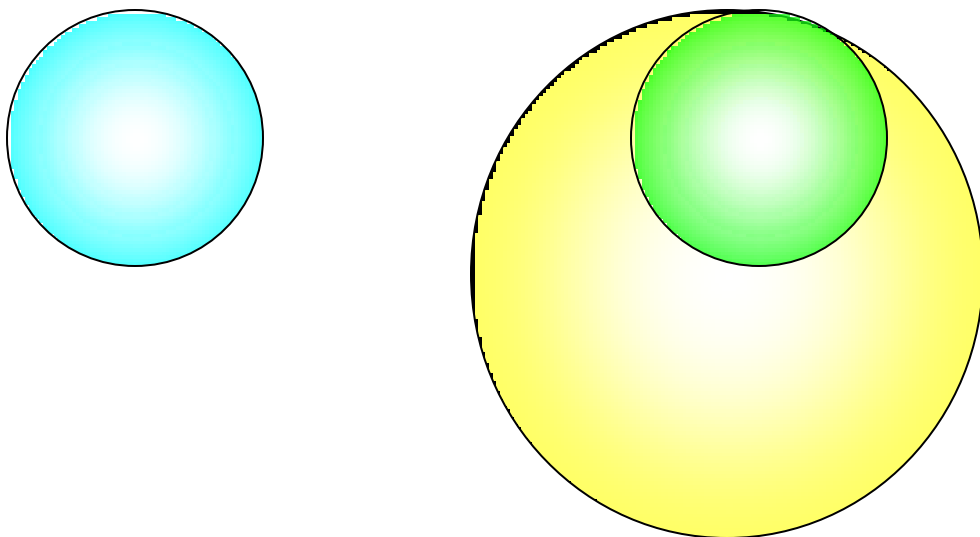
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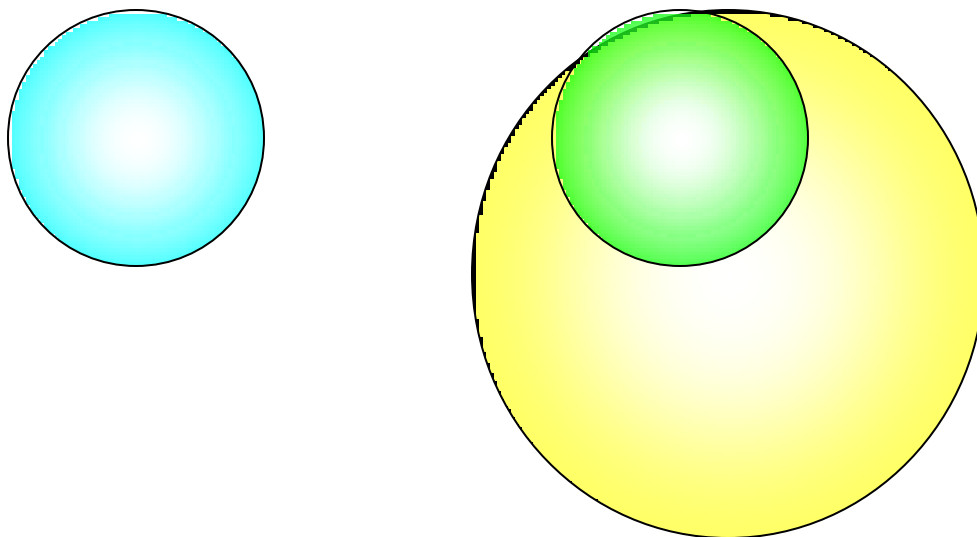
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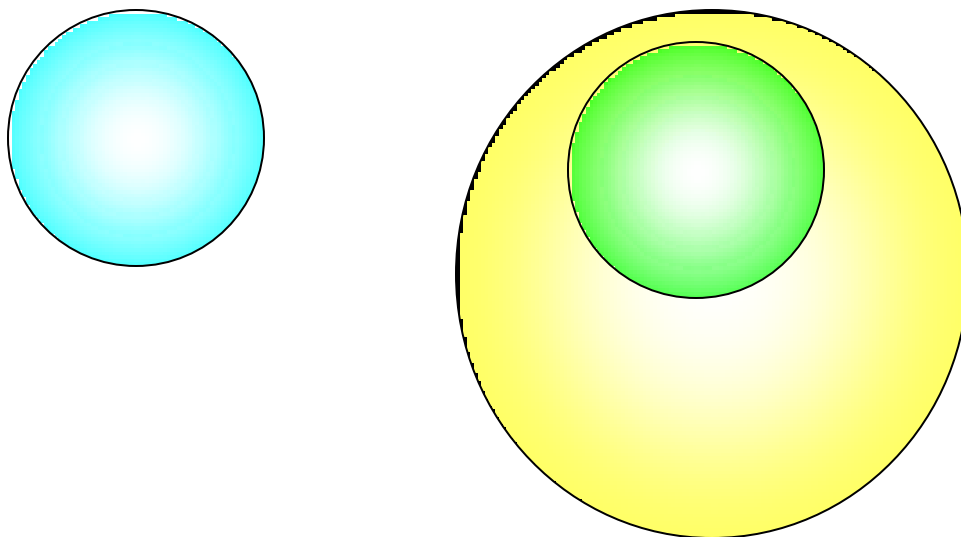
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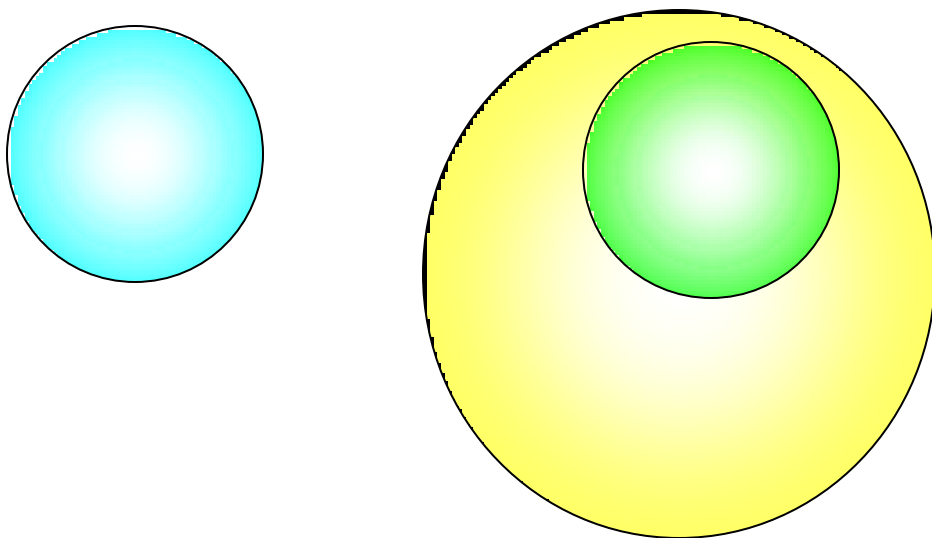
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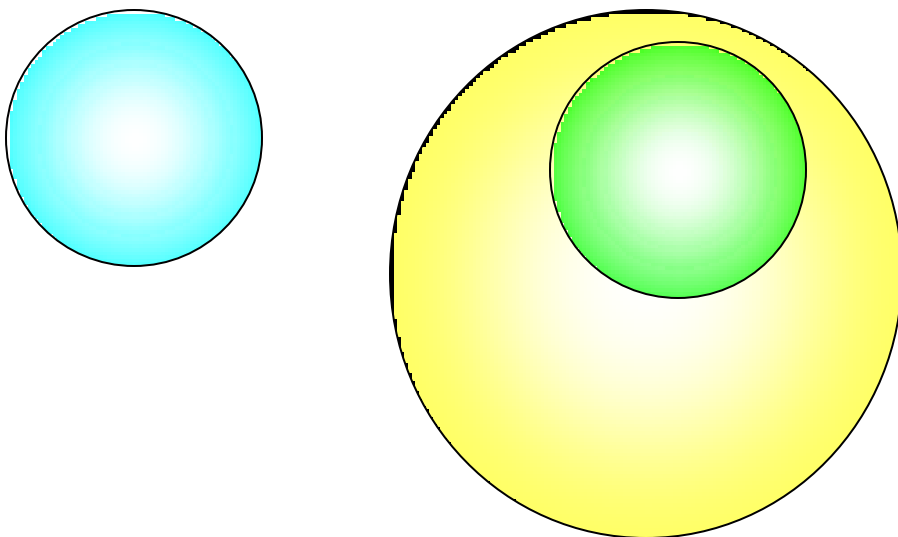
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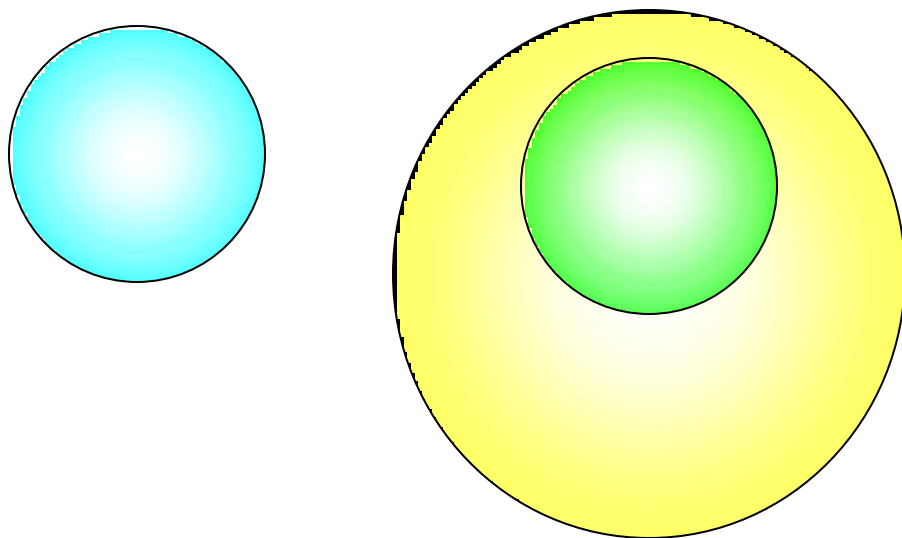
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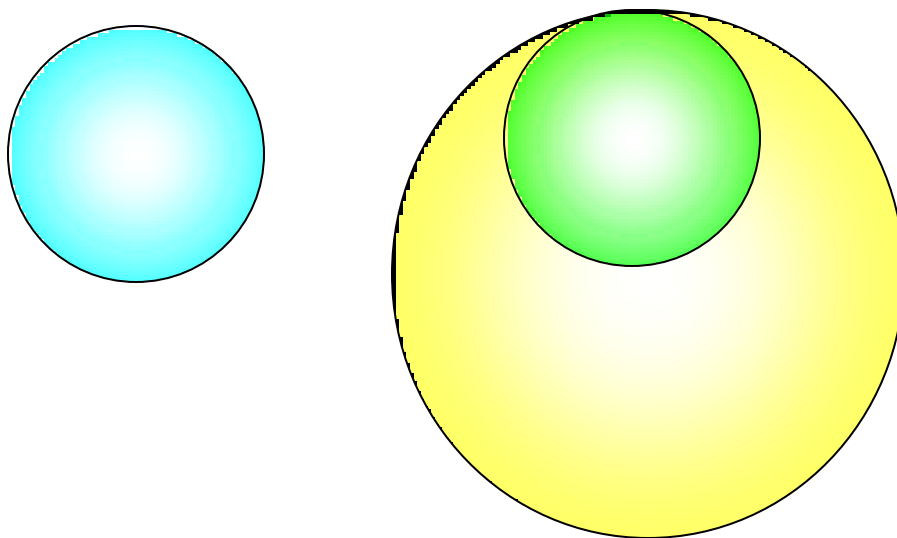


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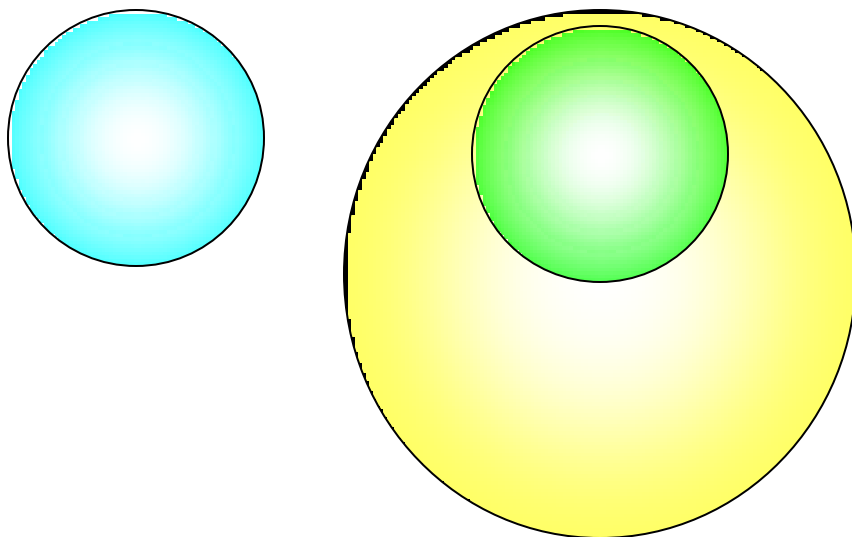




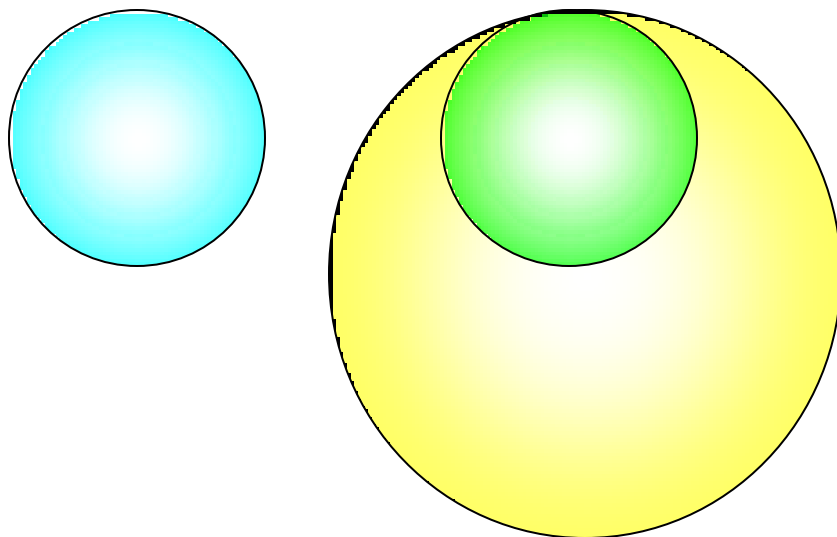
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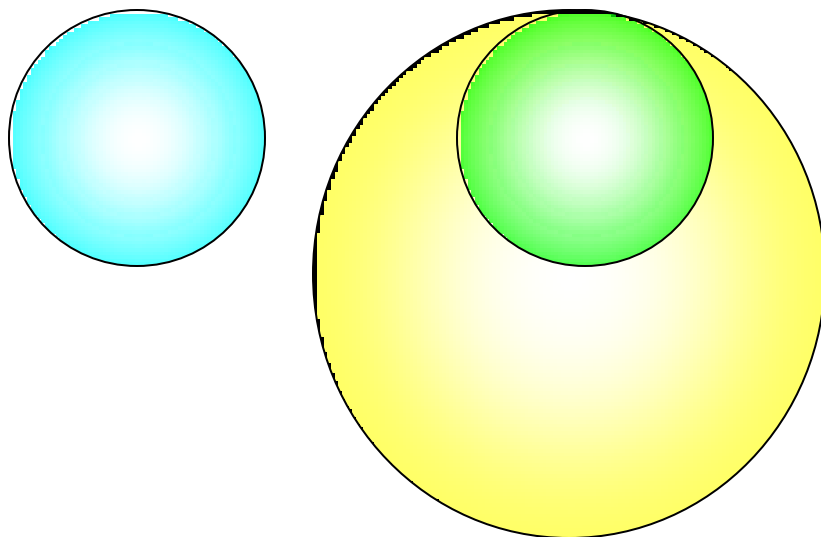
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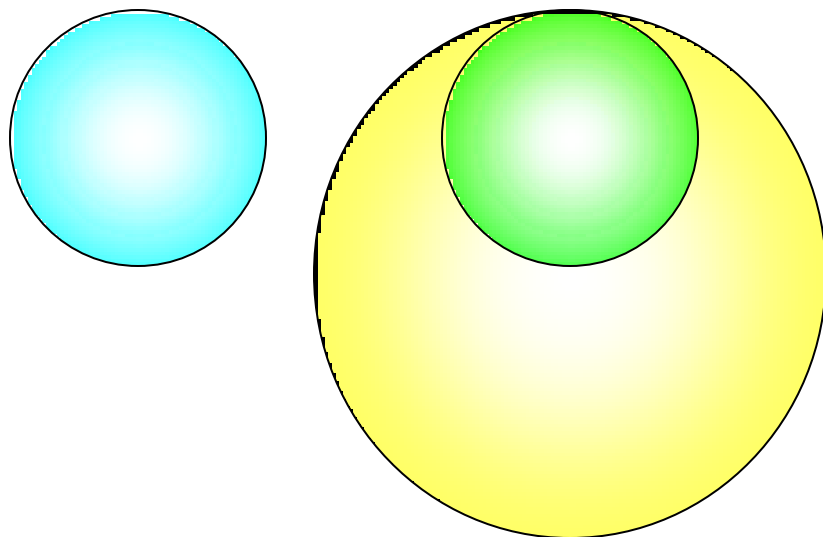
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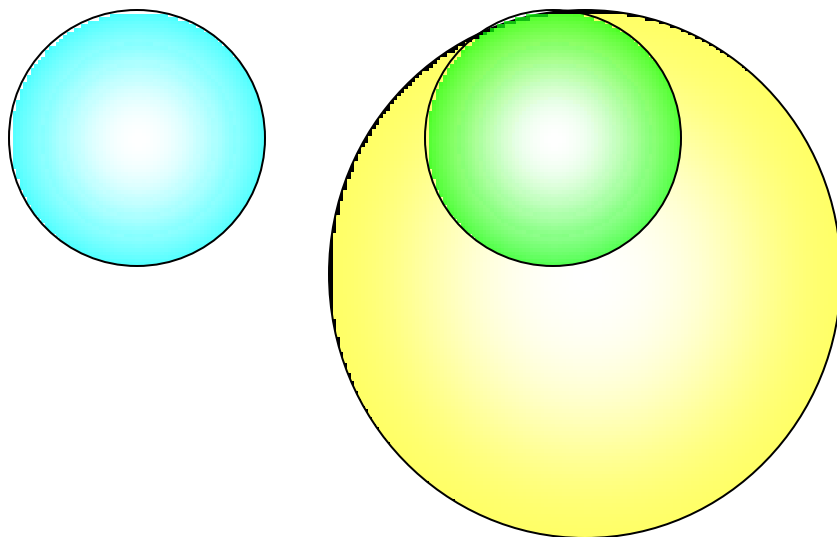
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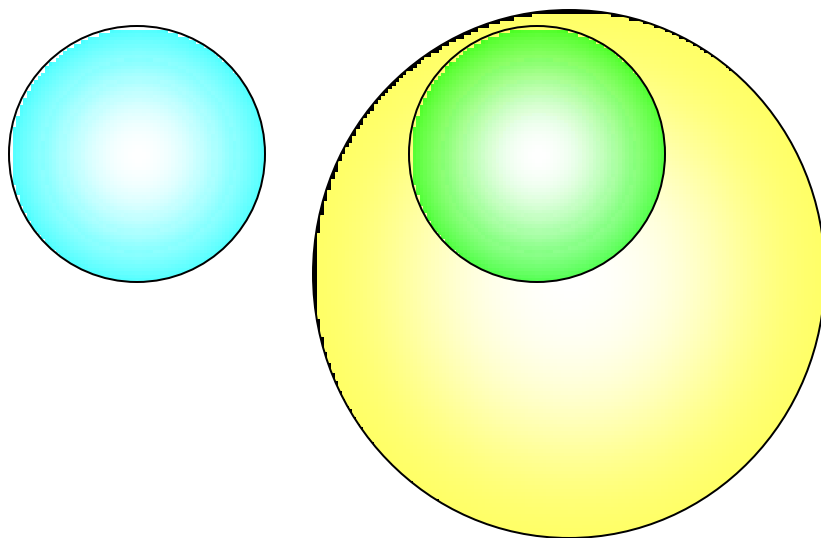
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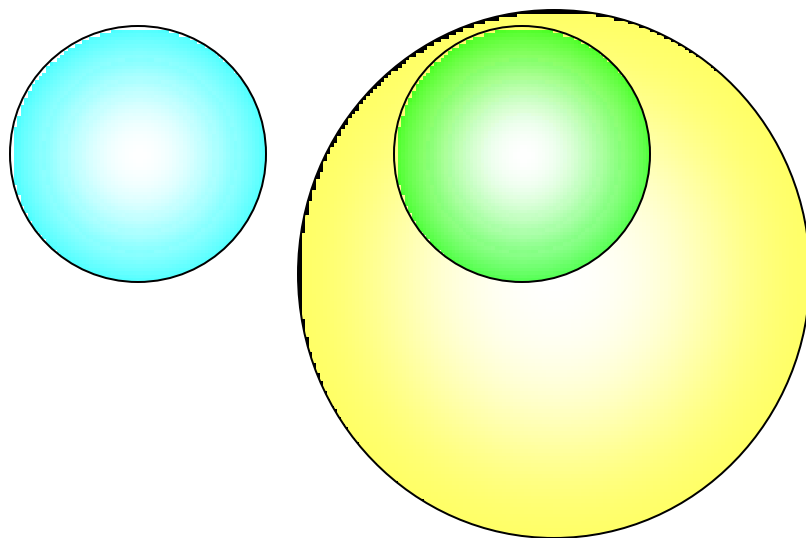
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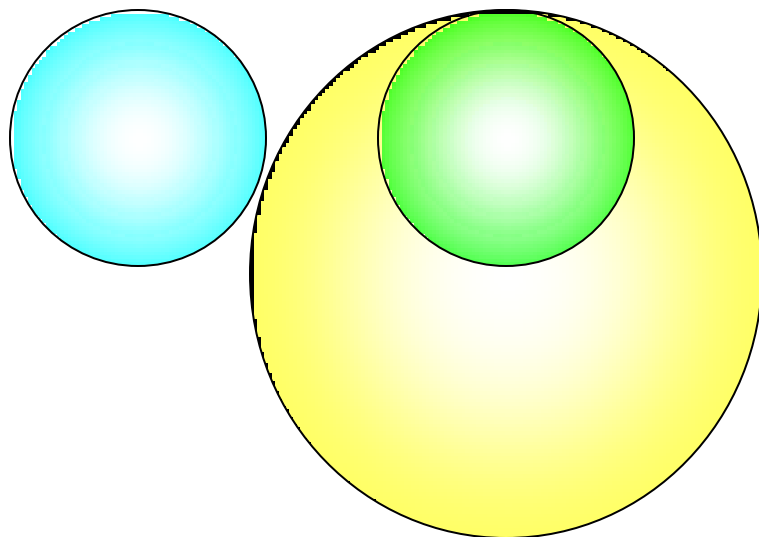


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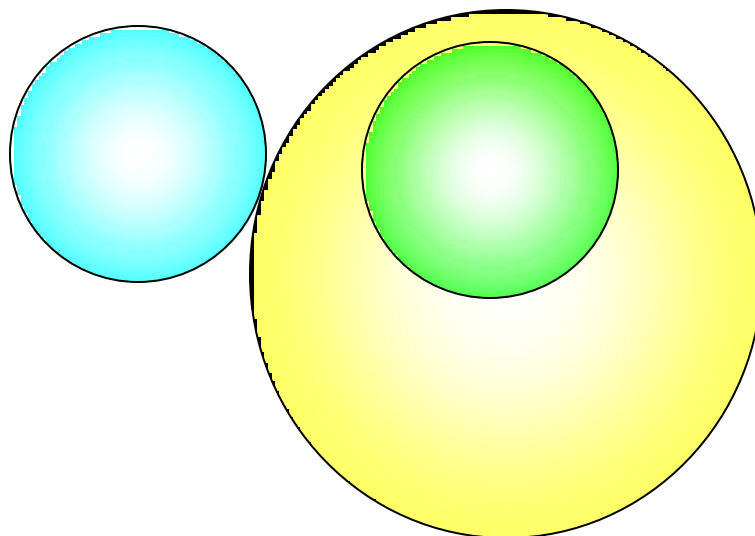




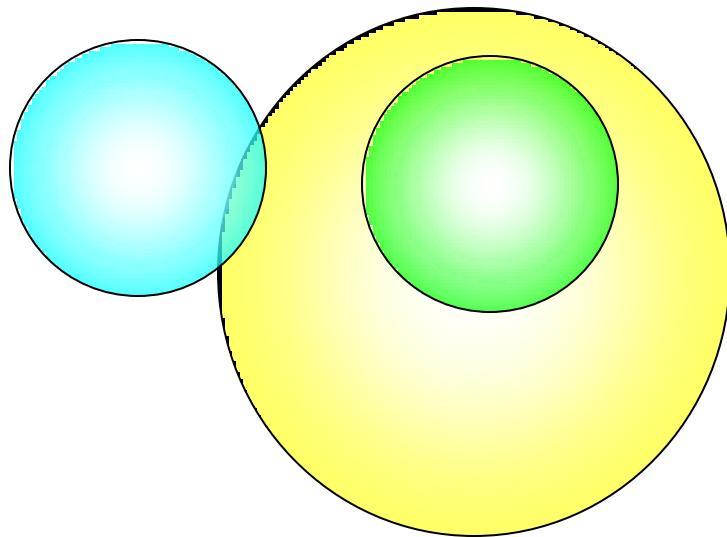
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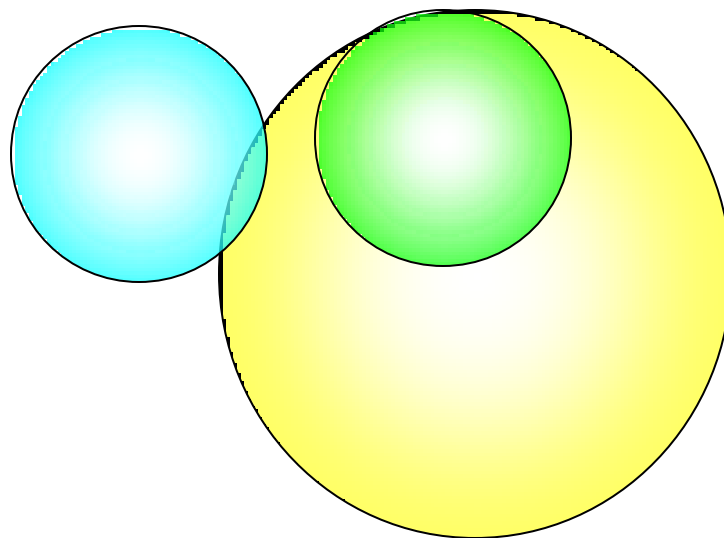
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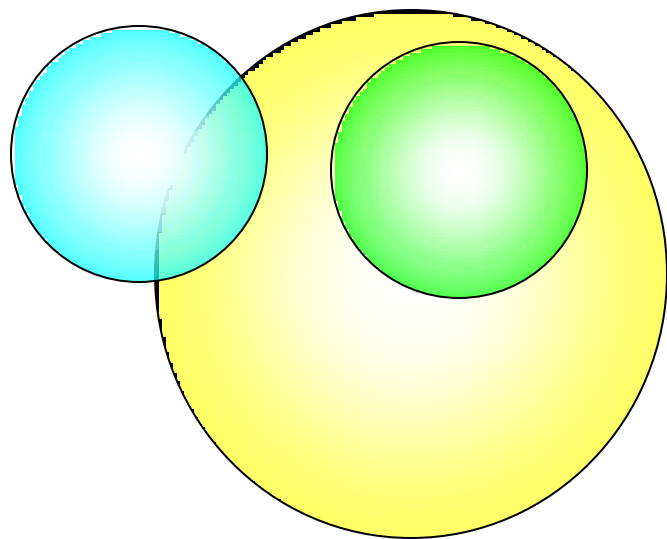
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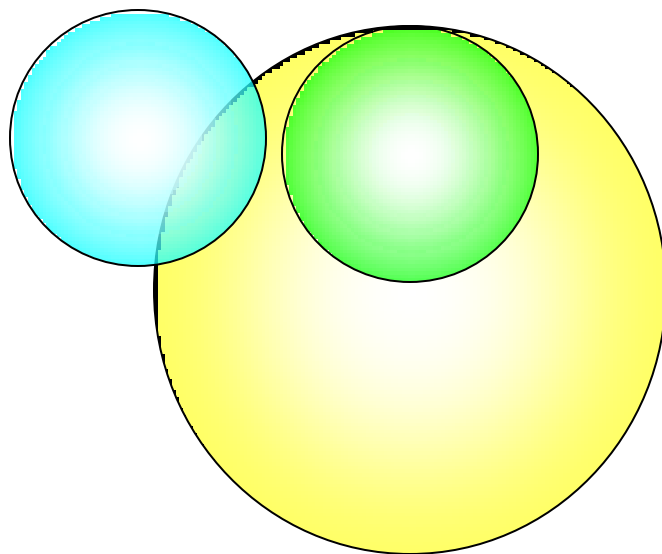
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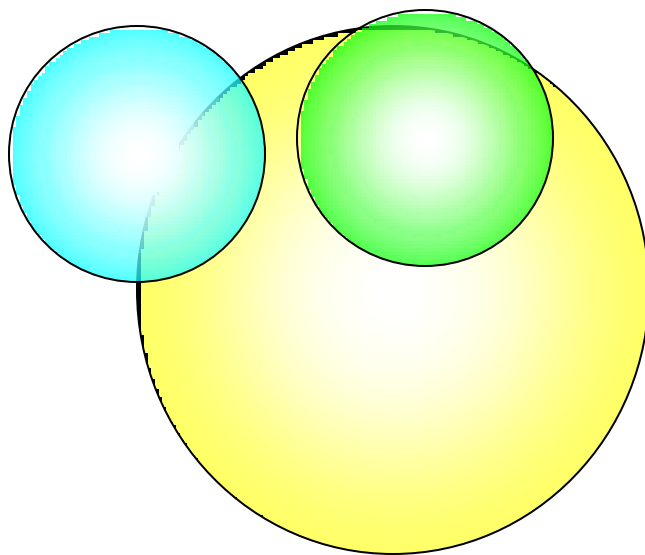
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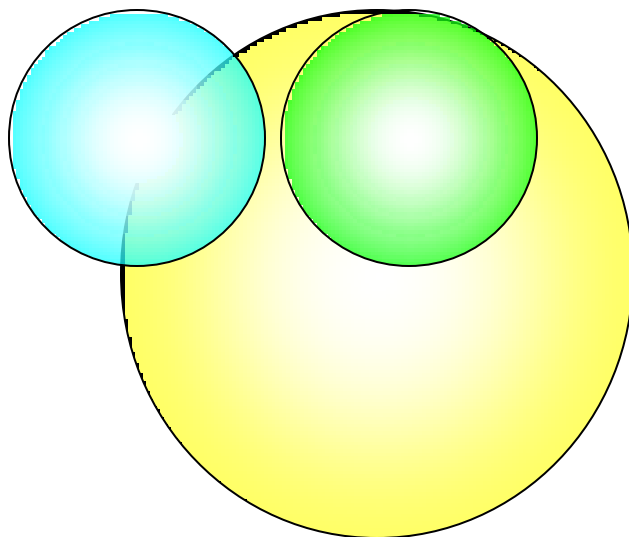
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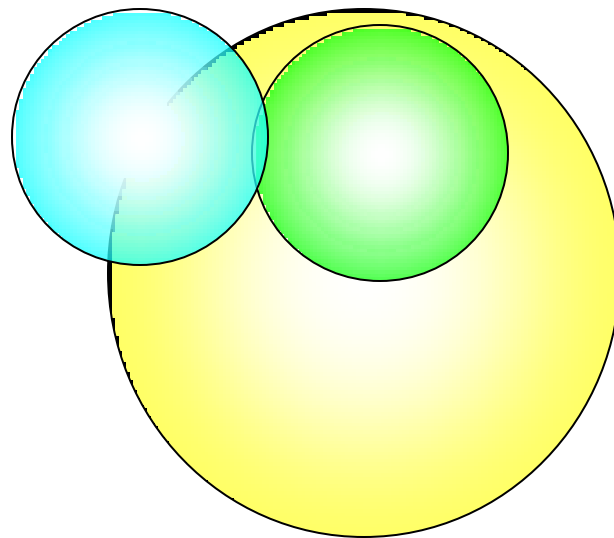


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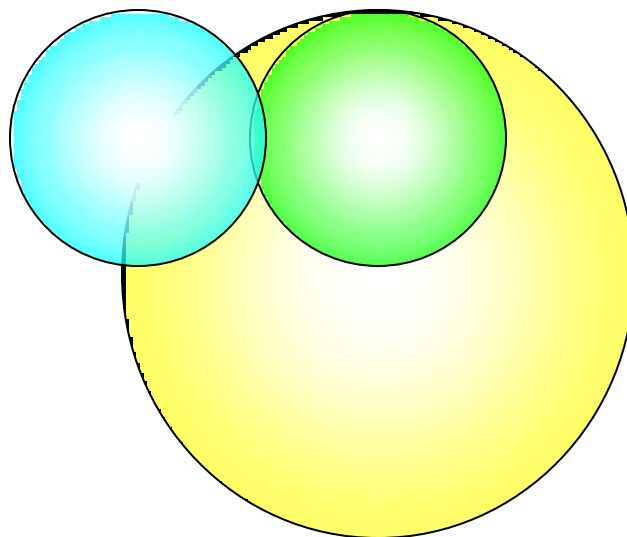




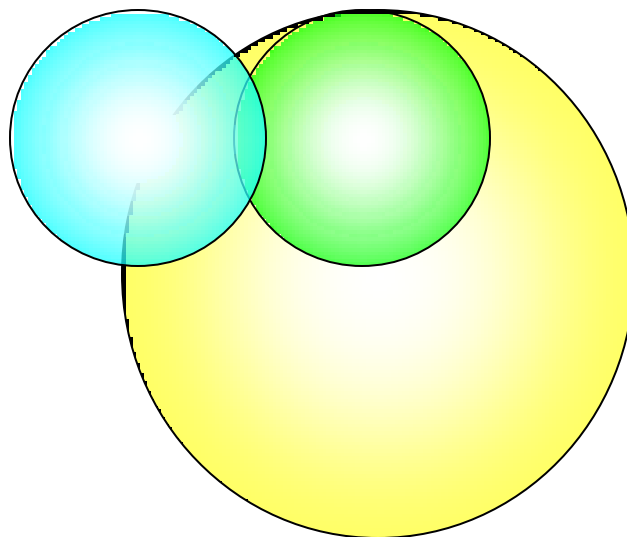
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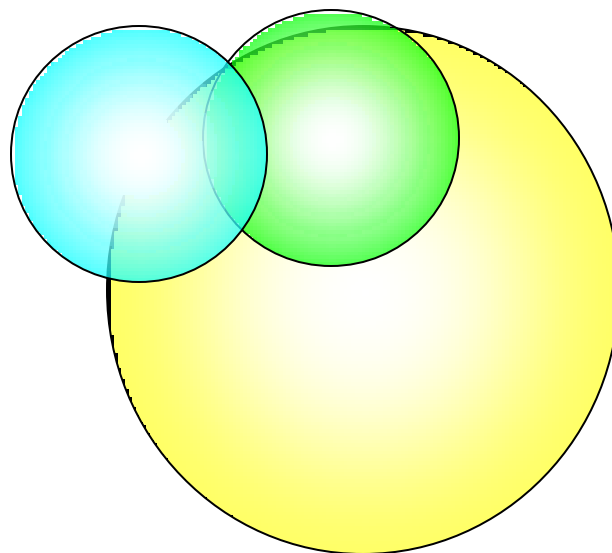
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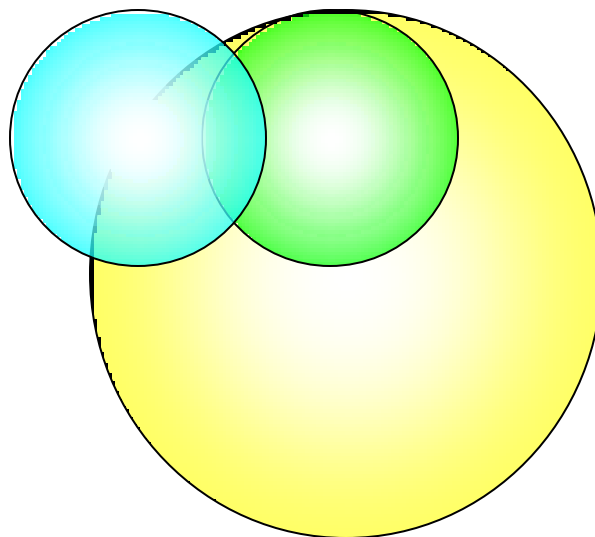
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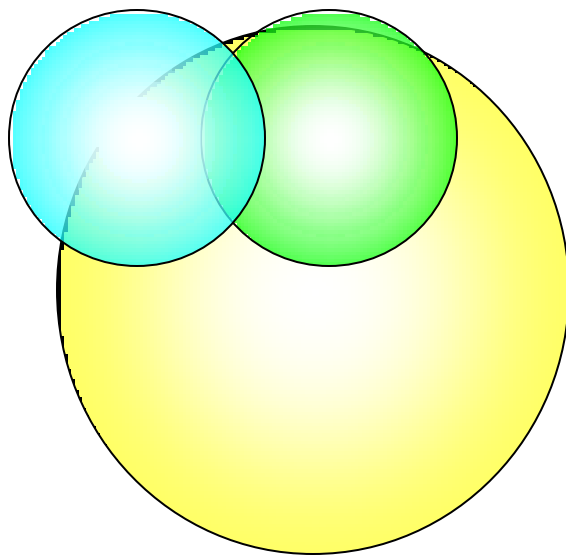
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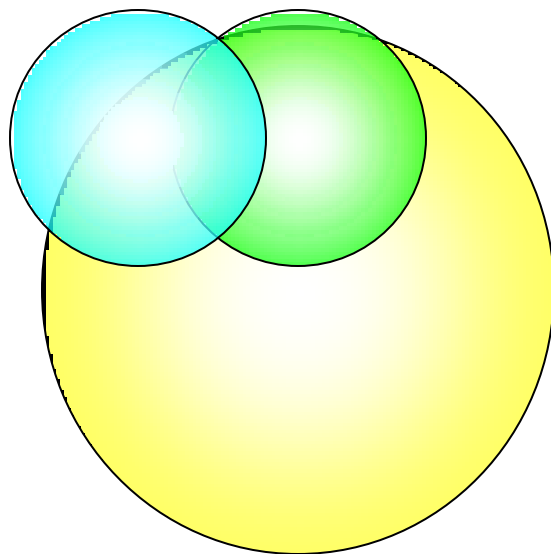
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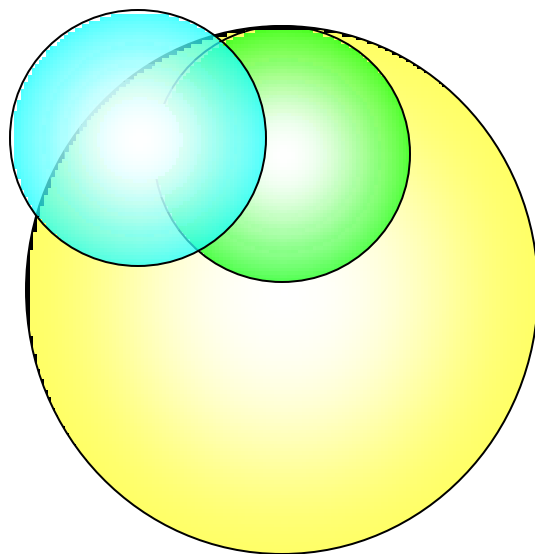
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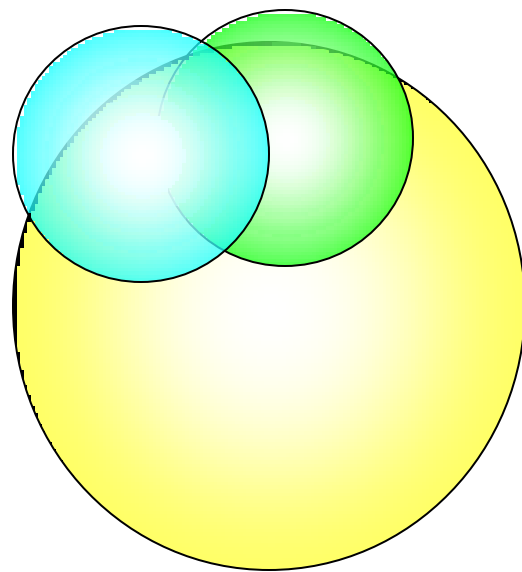


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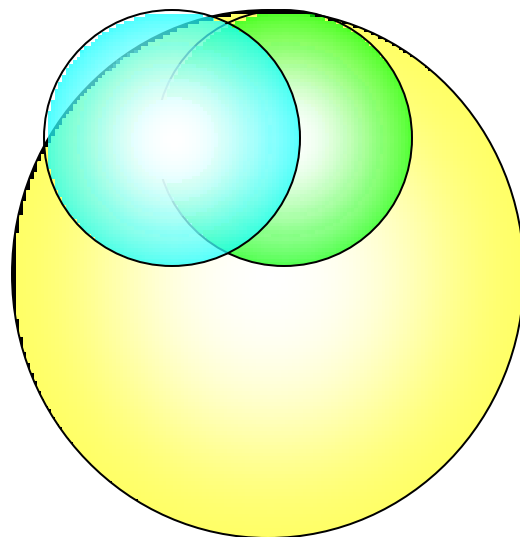




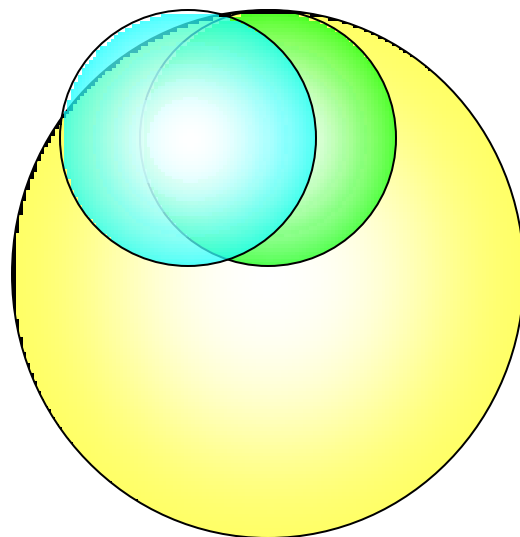
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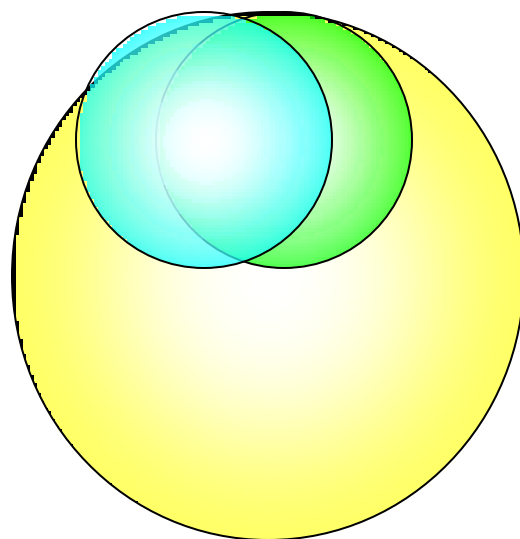
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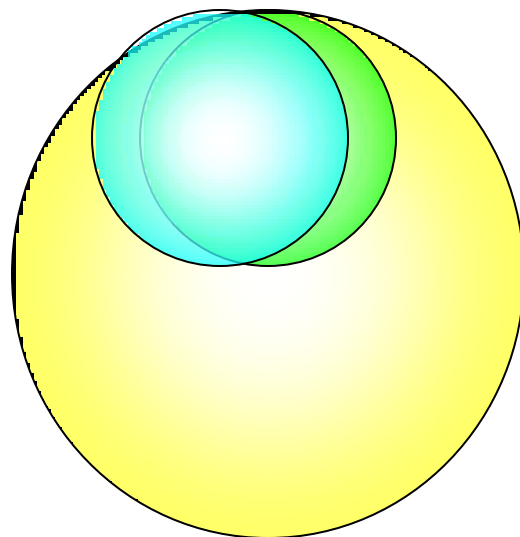
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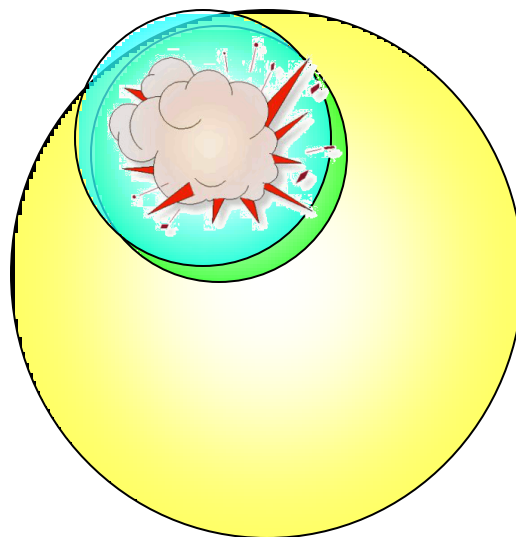
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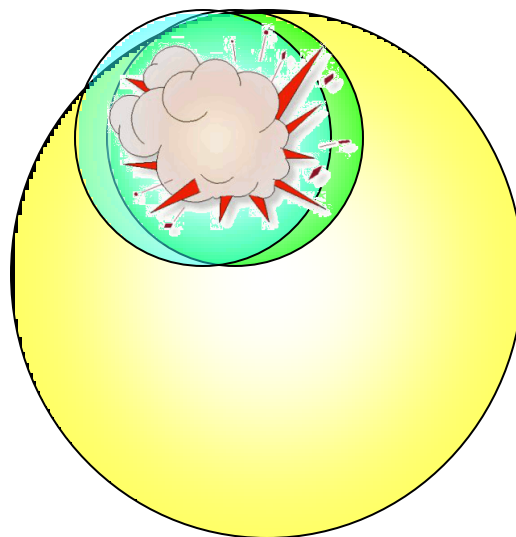
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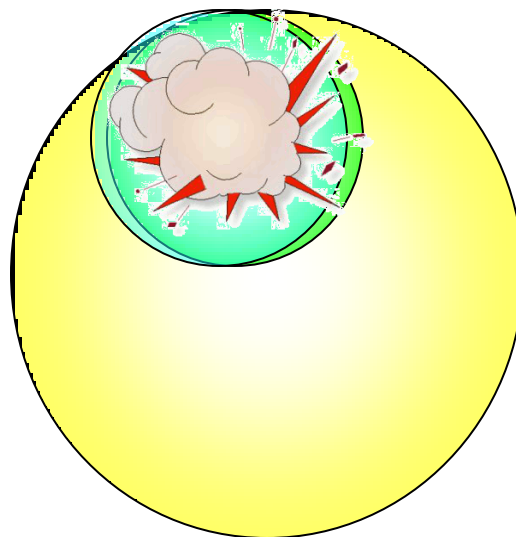
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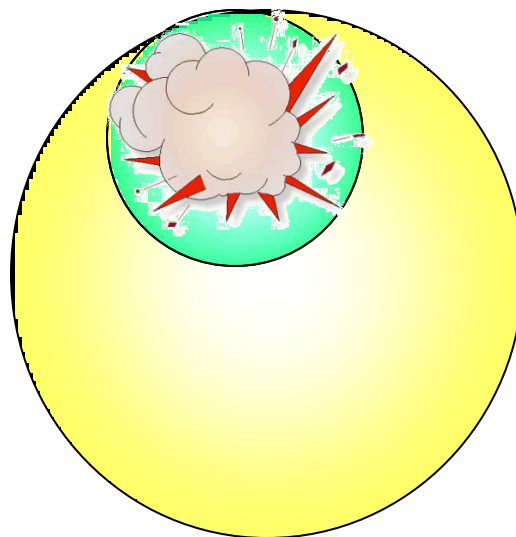


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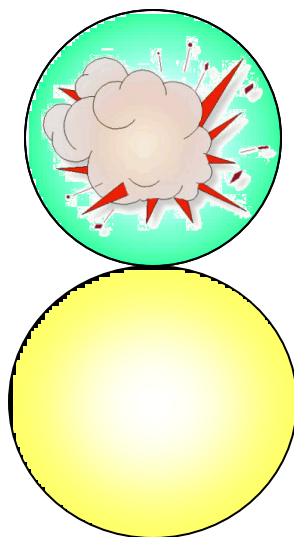




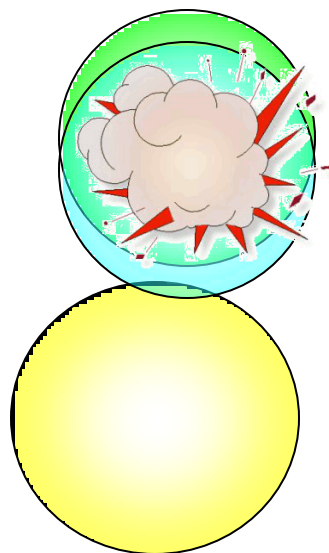
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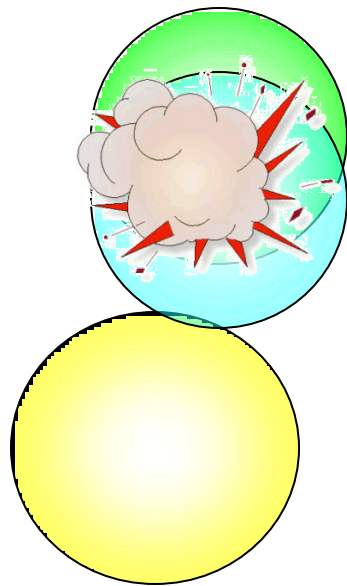
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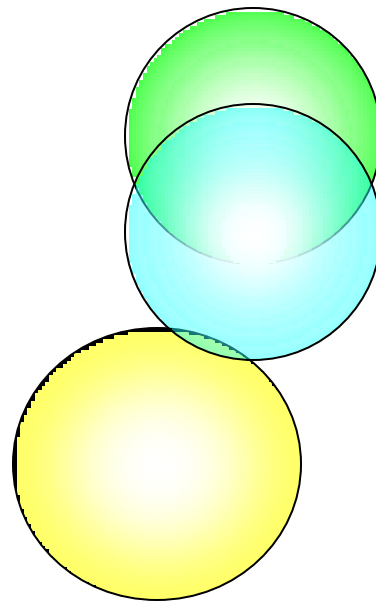
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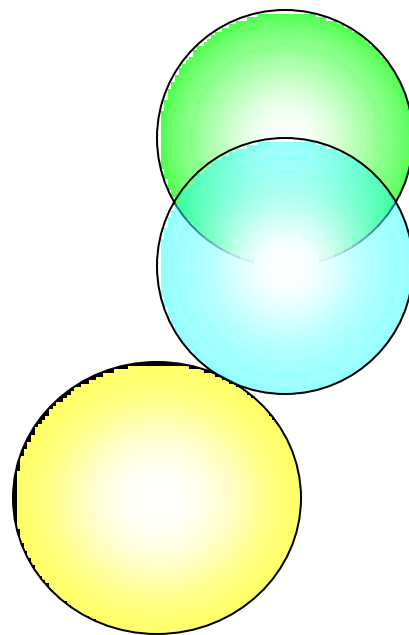
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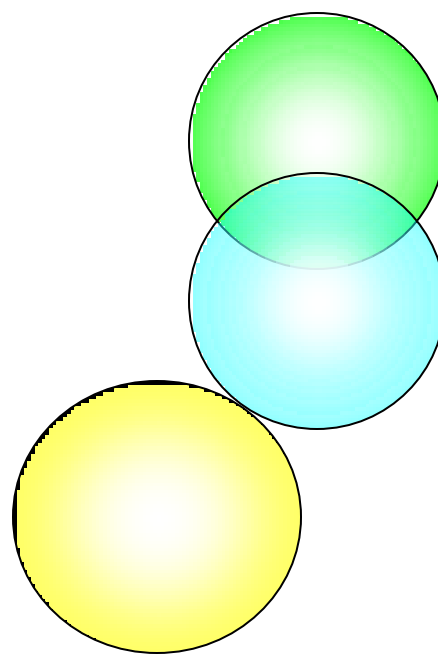
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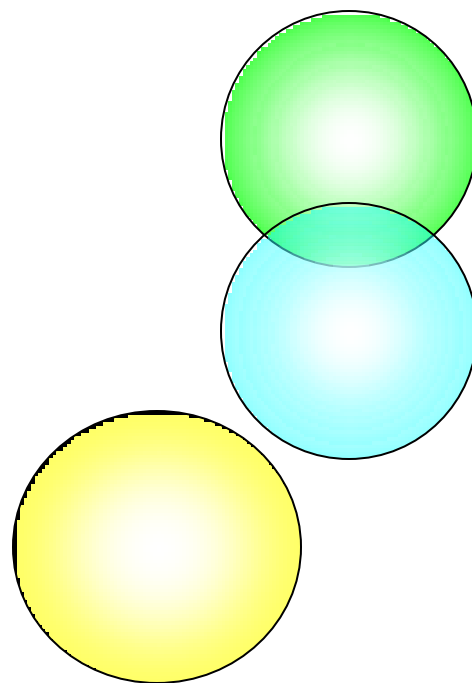
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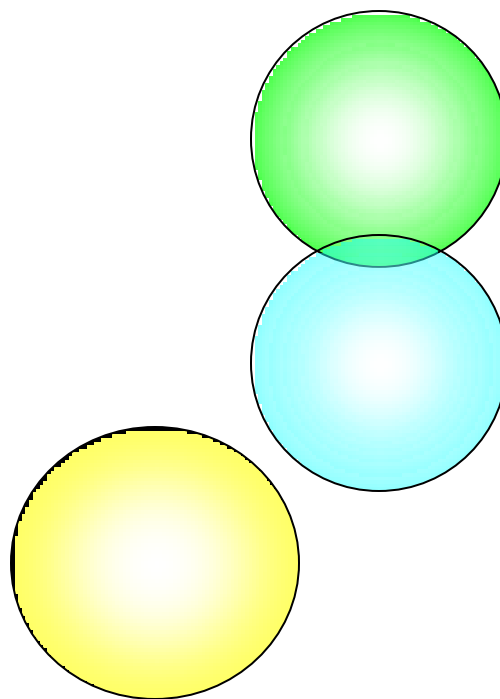


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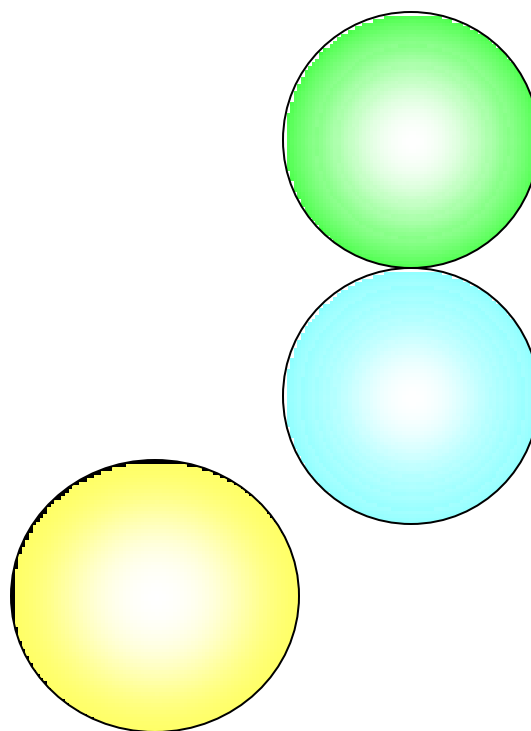




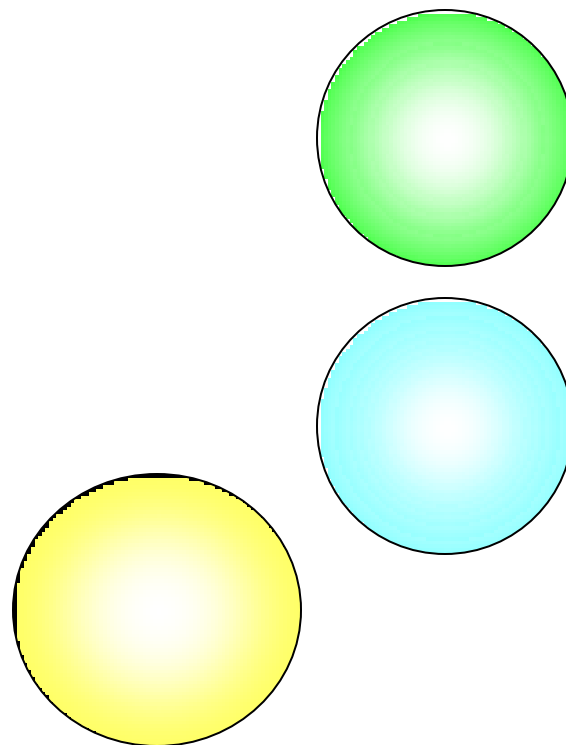
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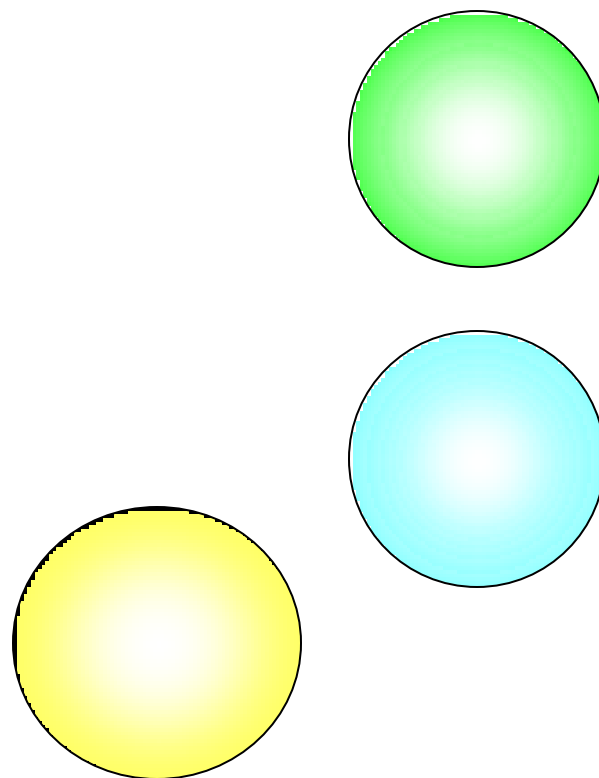
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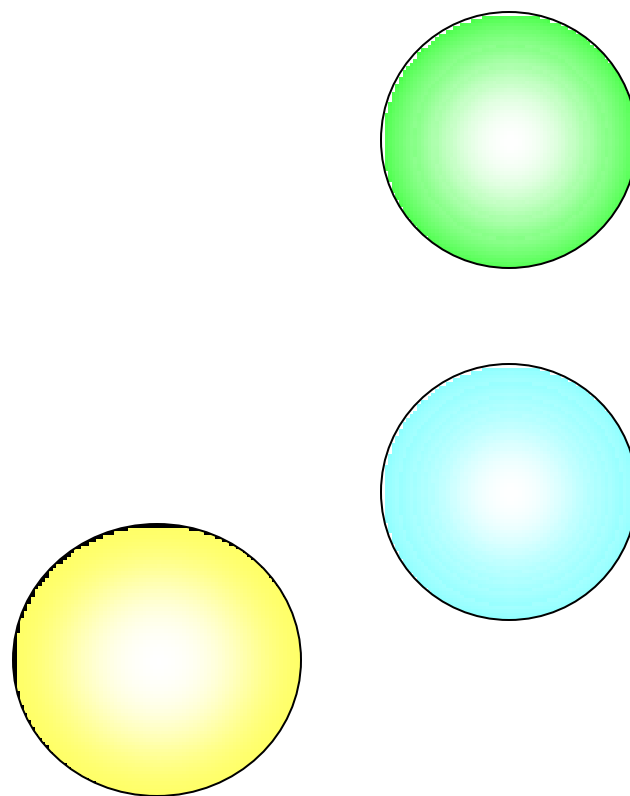
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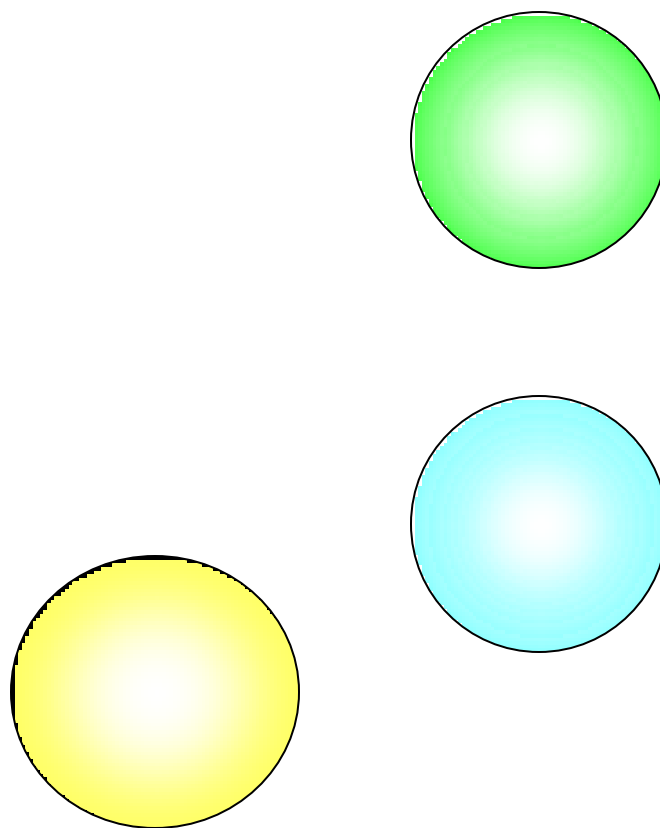
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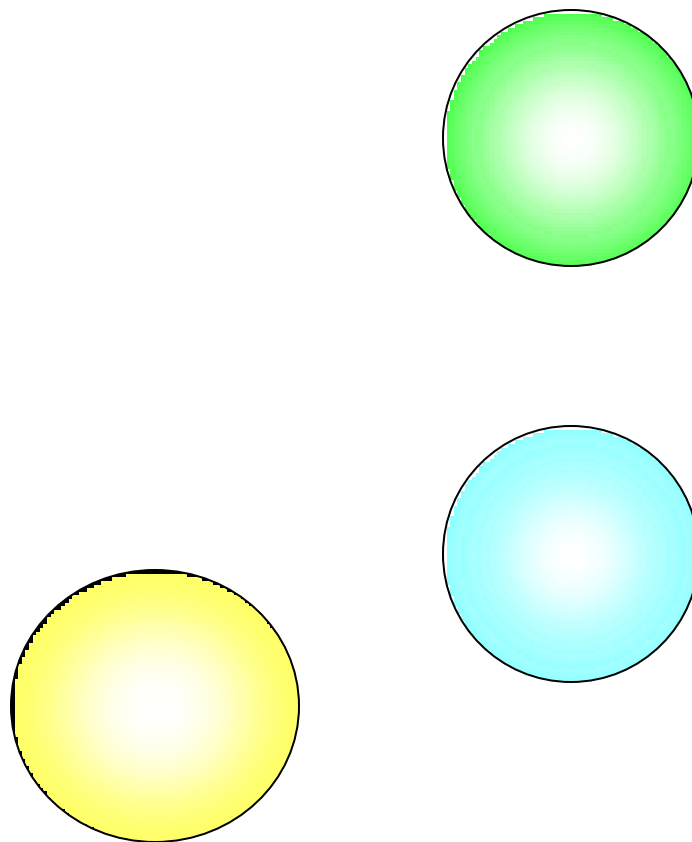
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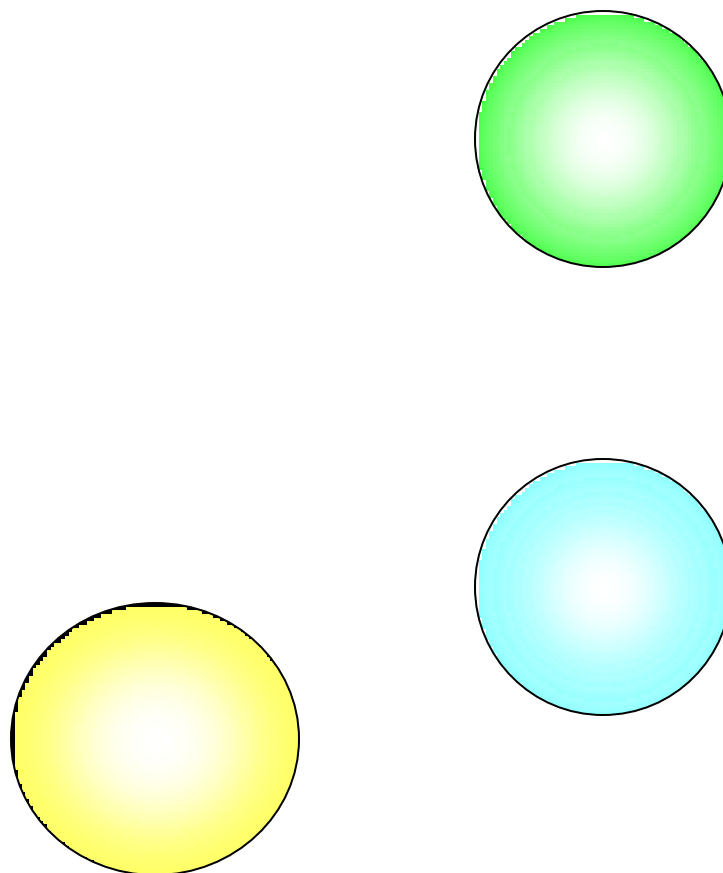
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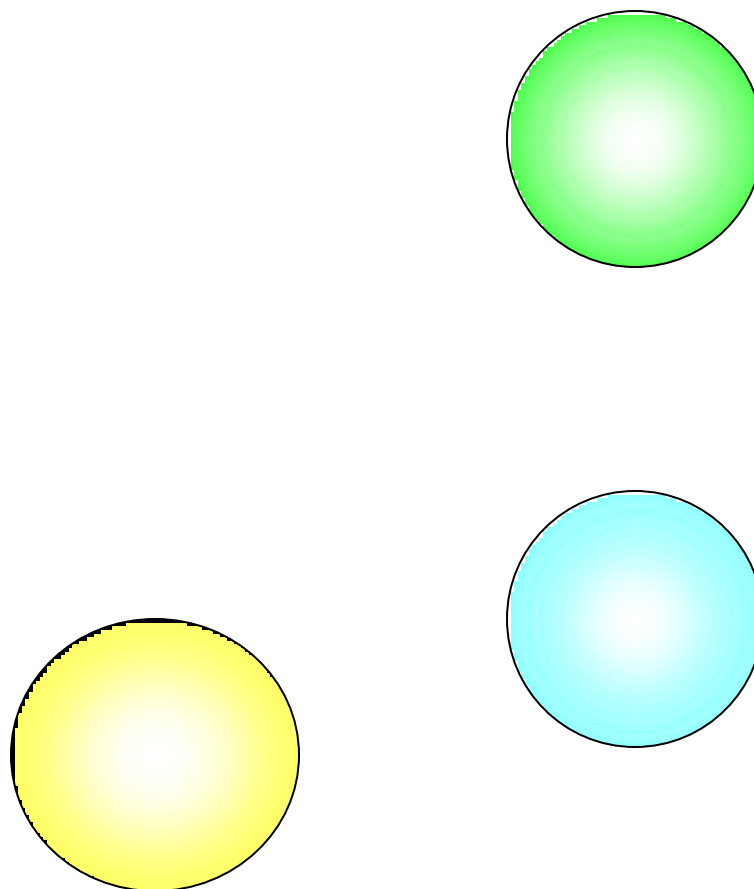


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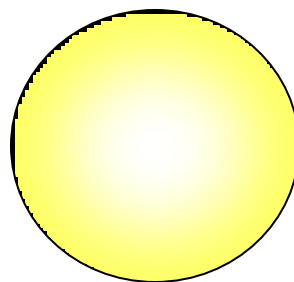
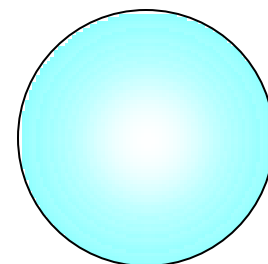
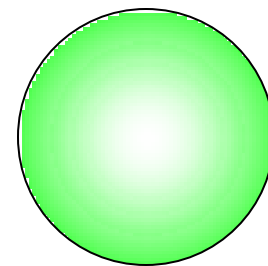




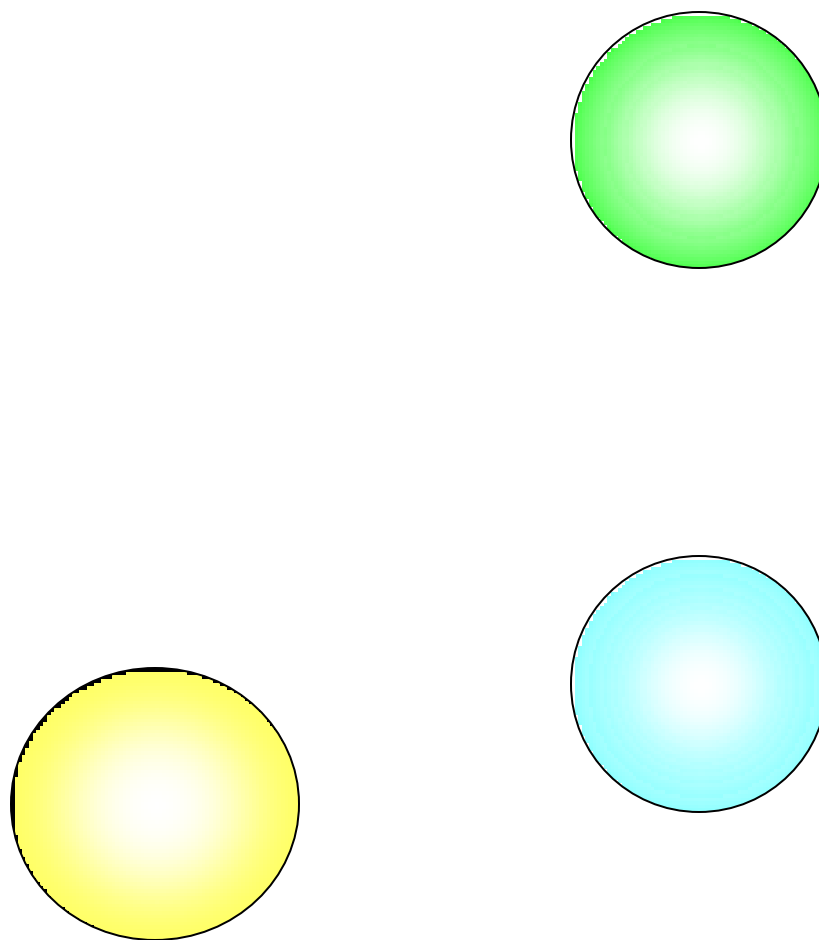
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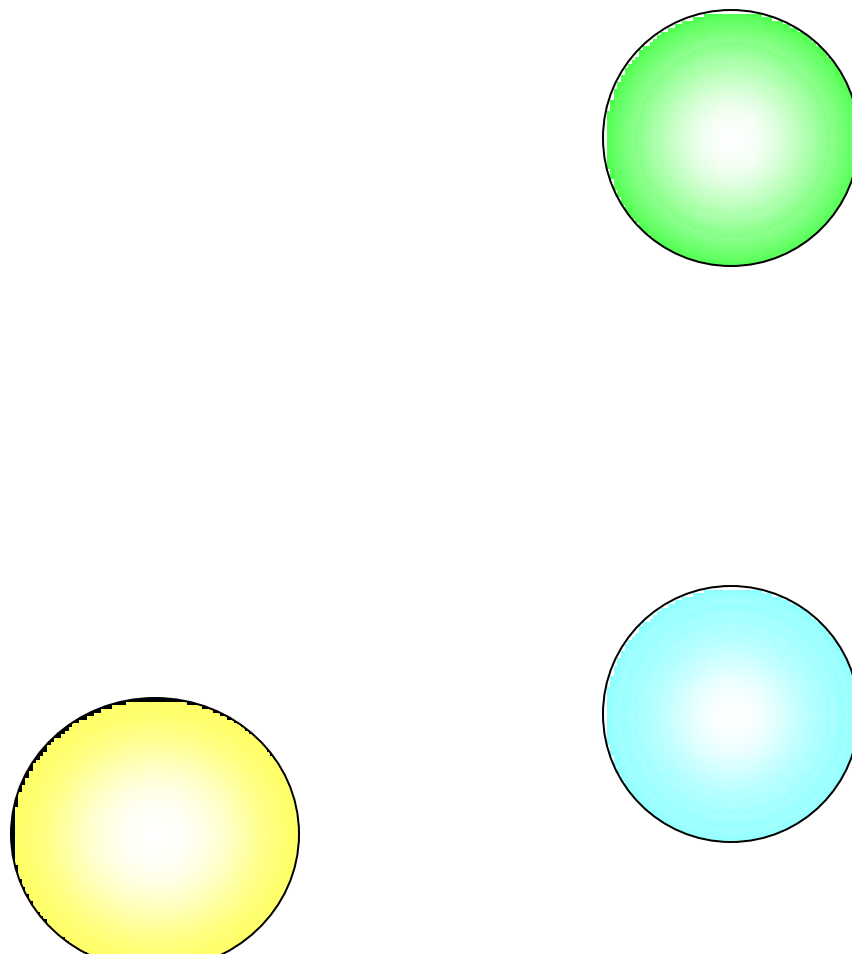
# Zero Range Knockout



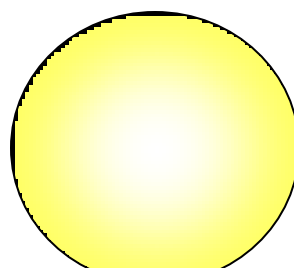
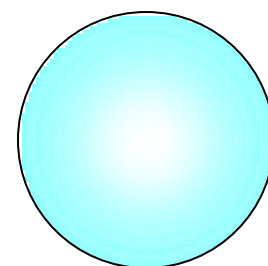
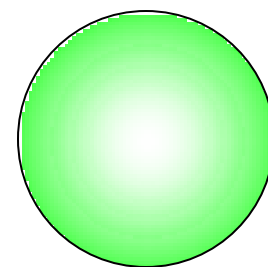
# Zero Range Knockout



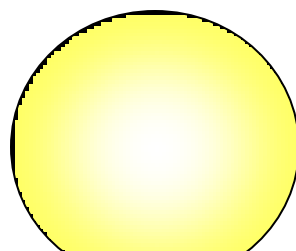
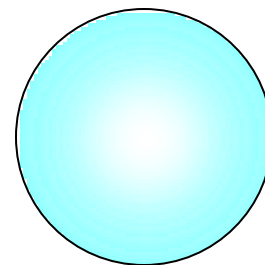
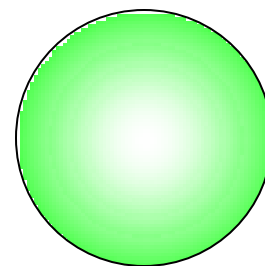
# Zero Range Knockout



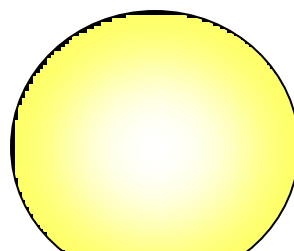
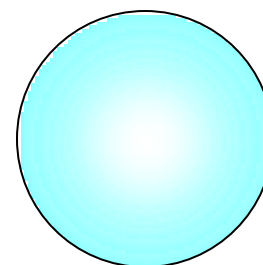
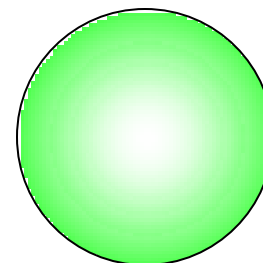
# Zero Range Knockout



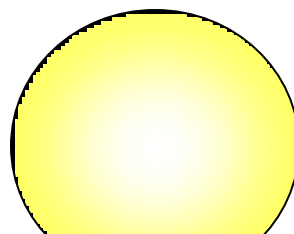
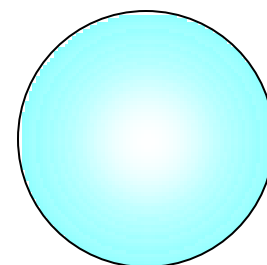
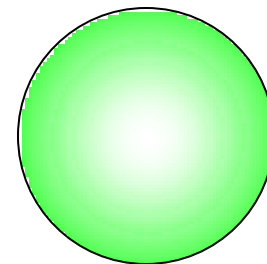
# Zero Range Knockout



# Zero Range Knockout

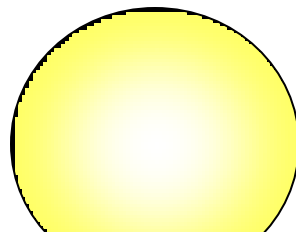
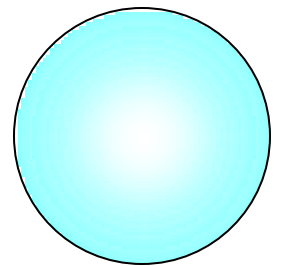
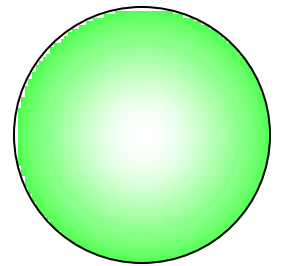


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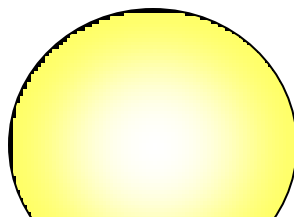
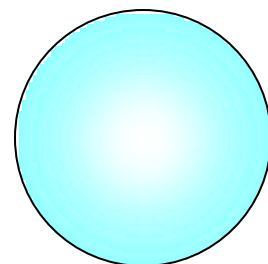
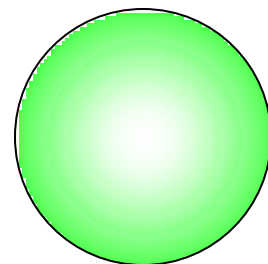




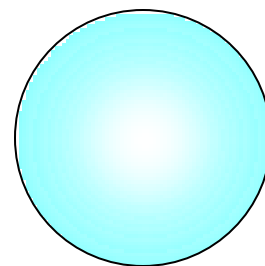
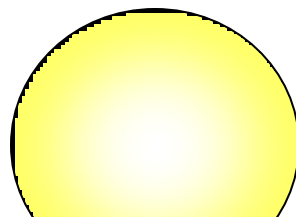
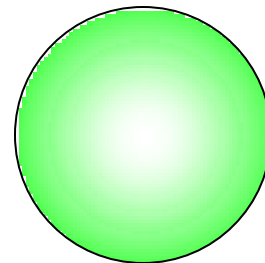
# Zero Range Knockout



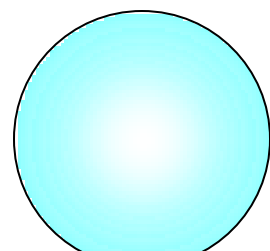
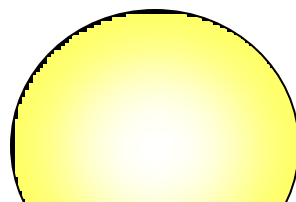
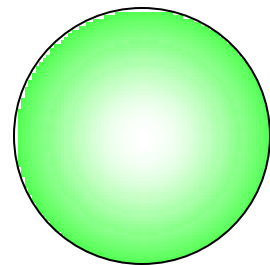
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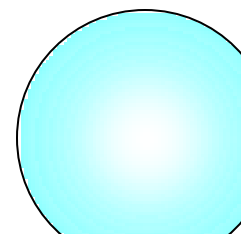
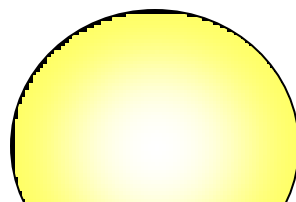
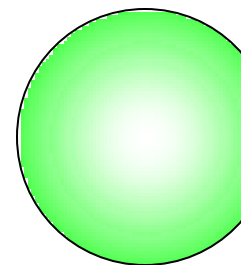
# Zero Range Knockout



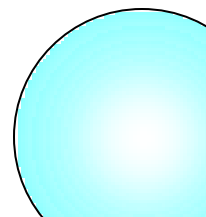
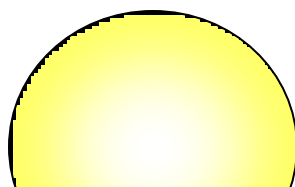
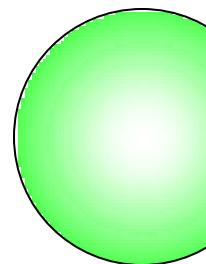
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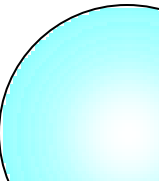
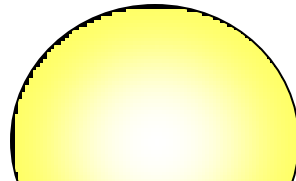
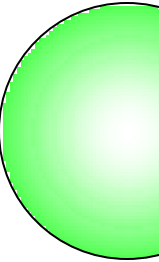
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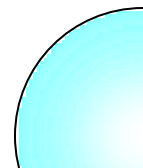
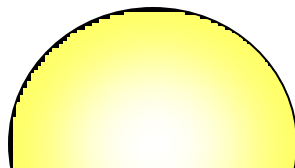
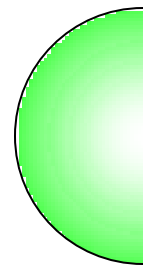
# Zero Range Knockout



# Zero Range Knockout

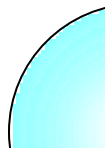
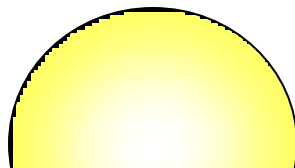
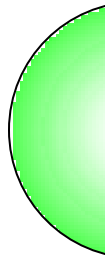


# Zero Range Knockout

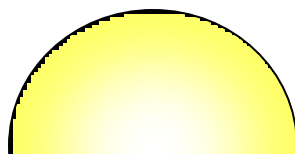




# Zero Range Knockout



# Zero Range Knockout



**From Transfer Reactions one obtains reasonable relative spectroscopic factors.**

**For Knockout Reactions one uses quasi free scattering approx. or Distorted Wave Impulse Approximation (DWIA).**

**$(\alpha, 2\alpha)$ , knockout reaction cross section**

**= product of kinematic factor,  
 $\alpha$ - $\alpha$  Cross section and**

**Distorted wave form factor,  
( $\sim$ Fourier transform of Wfn).**

$$\frac{d^3\sigma}{d\Omega_1 d\Omega_2 dE_1} = KF \cdot S_{LJ} \cdot \left( \frac{d\sigma}{d\Omega} \right)_{ab} \sum_{\Lambda} \left| T_{BA}^{LJ}(Q) \right|^2.$$

$S_{LJ}$  is the cluster spectroscopic factor for specific L and J.

The transition amplitude may be written as :

$$T_{BA}^{LJ}(Q) = (2L+1)^{-1/2} \int \chi_{aB}^{(-)*}(\vec{k}_{aB}, \vec{R}) \cdot \chi_{bB}^{(-)*}(\vec{k}_{bB}, \vec{R}) \cdot \chi_{aA}^{(+)}(\vec{k}_{aA}, \epsilon\vec{R}) \cdot \phi_{LJ}(\vec{R}) d\vec{R}.$$

Here  $\epsilon = B/A$ .

Ground State spectroscopic factors  $S_a$  for  $^{16}\text{O}(\alpha, 2\alpha)^{12}\text{C}$

$E\alpha$	$S_{o+}$	$\sigma_{PW} / \sigma_{DW}$
<b>Theory</b>	<b>0.23</b>	-
<b>850 MeV</b>	<b>&lt; 1.8</b>	5.4
<b>90 MeV</b>	<b>15</b>	$\sim 1500$
<b>52.5 MeV</b>	<b>150</b>	$\sim 3200$

Ground State spectroscopic factors  $S_a$  for  $^{12}\text{C}(\alpha, 2\alpha)^8\text{Be}$   
at **139 MeV** and **200 MeV**

	<b>139 MeV</b>	<b>200 MeV</b>	<b>Ratio</b>
	17	<b>0.48</b>	35
<b>Theory</b>	<b>0.55</b>	<b>0.55</b>	

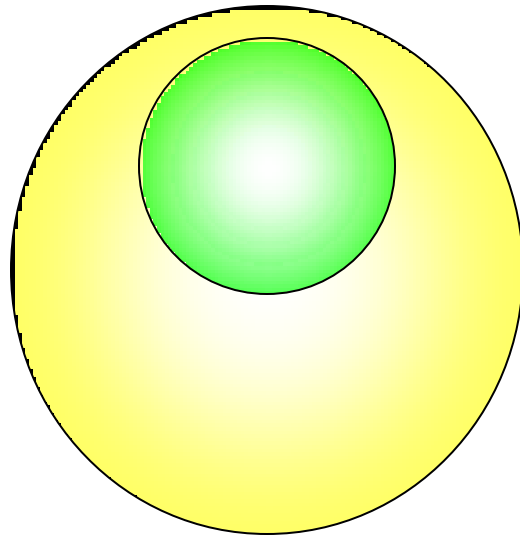
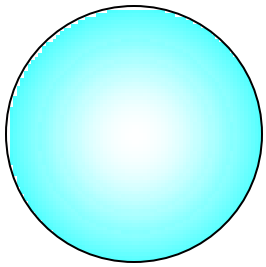
# Discrepancy between Proton and Alpha induced Cluster Knockout Reactions

**Here Spectroscopic Factor  $S_\alpha$  is seen to be almost  
 $\sim 2$ -orders of magnitude too large**

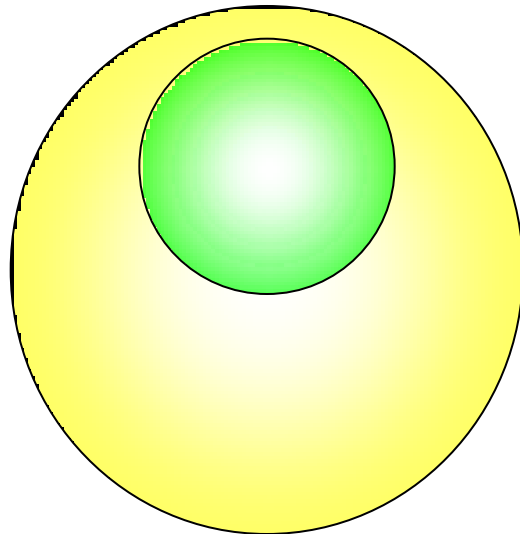
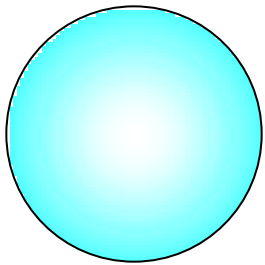
Reaction	$\theta_1$ - $\theta_2$	P3 (MeV/c)	Spectroscopic factor ( $S_\alpha$ )
$^{16}\text{O}(p, pd)^{14}\text{N}$	$40.1^\circ$ - $40.0^\circ$	$\sim 41$	0.43
$^{16}\text{O}(p, pt)^{13}\text{N}$	$40.1^\circ$ - $40.0^\circ$	$\sim 51$	3.4
$^{16}\text{O}(\alpha, ad)^{14}\text{N}$	$9.0^\circ$ - $43.99^\circ$	$\sim 4$	55
$^{16}\text{O}(\alpha, at)^{13}\text{N}$	$25.81^\circ$ - $43.99^\circ$	$\sim 13$	53
$^{16}\text{O}(\alpha, at)^{13}\text{C}$	$25.81^\circ$ - $43.99^\circ$	$\sim 2$	55

# Finite Range Knockout

# Knockout using Short Finite Range Repulsion

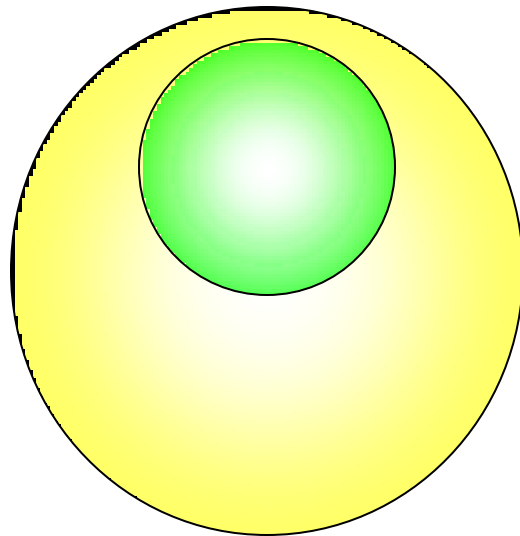
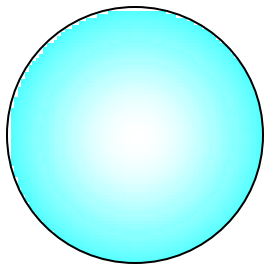


# Knockout using Short Finite Range Repulsion

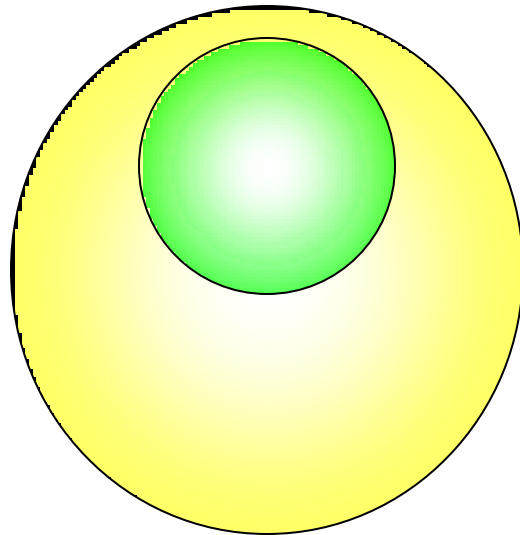
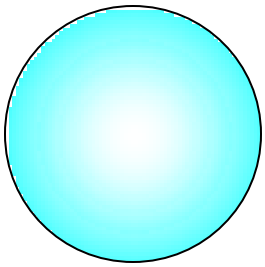




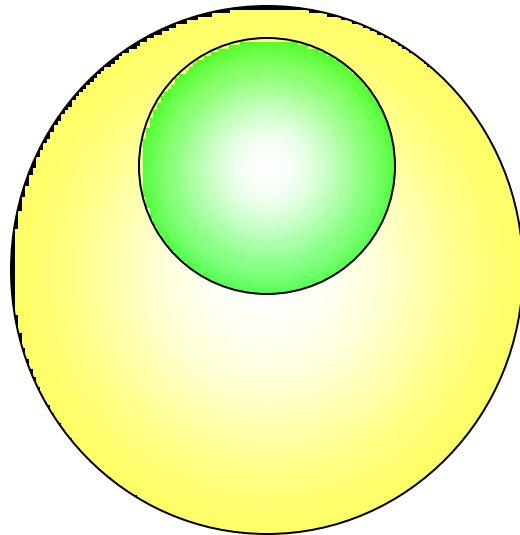
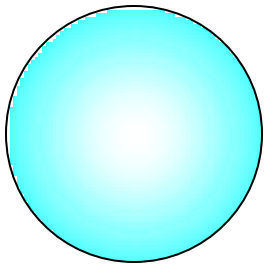
# Knockout using Short Finite Range Repulsion



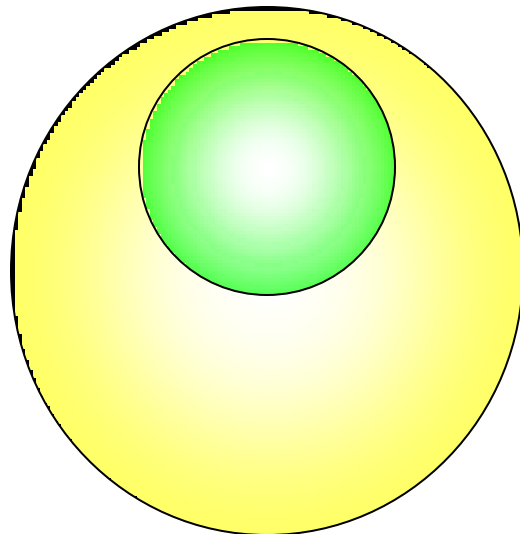
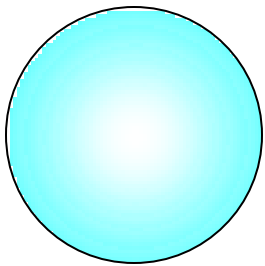
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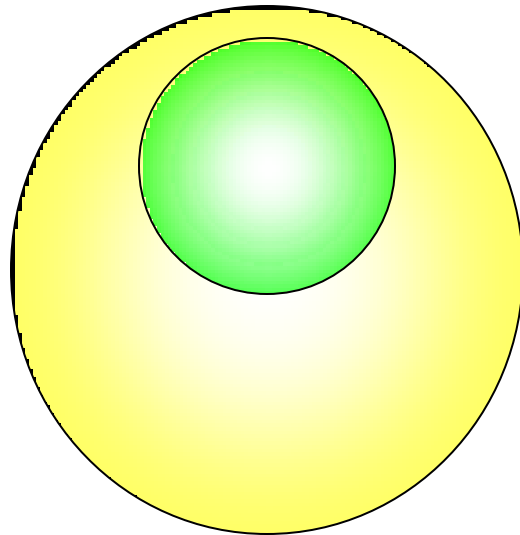
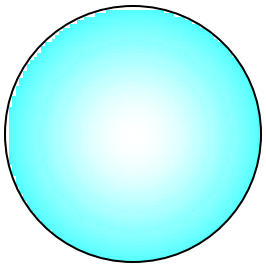
# Knockout using Short Finite Range Repulsion



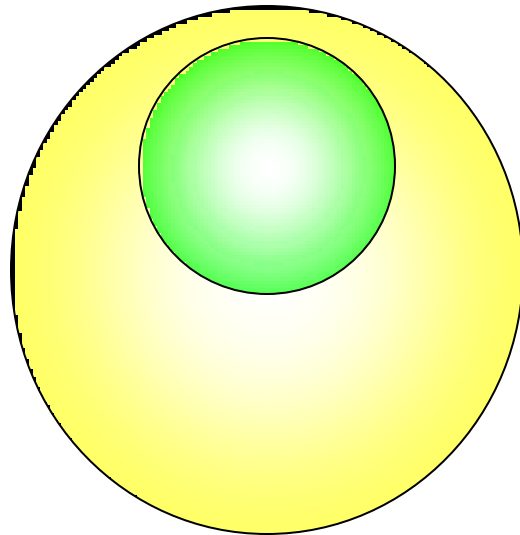
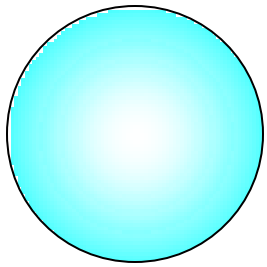
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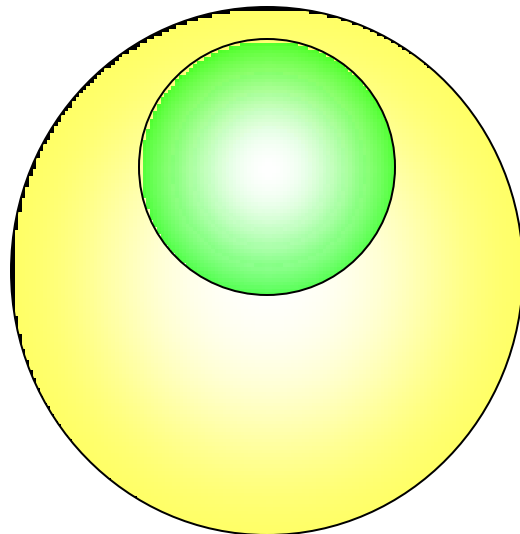
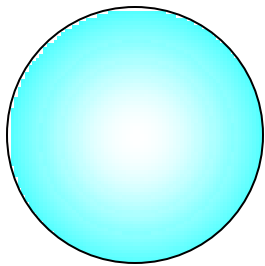
# Knockout using Short Finite Range Repulsion



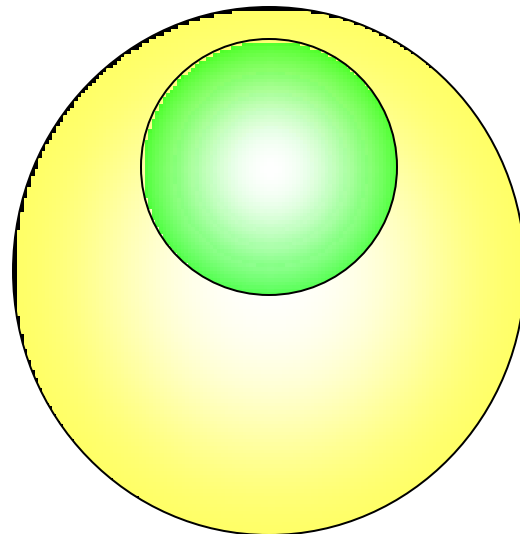
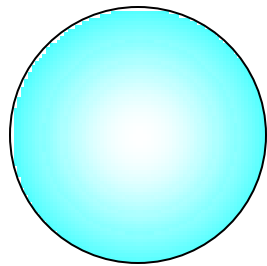
# Knockout using Short Finite Range Repulsion



# Knockout using Short Finite Range Repulsion

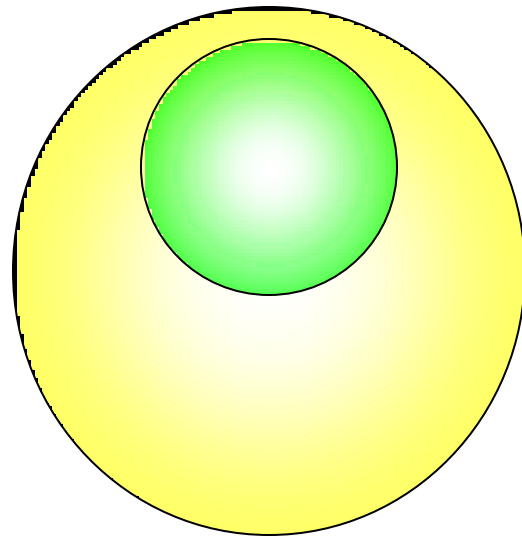
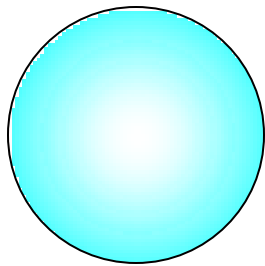


# Knockout using Short Finite Range Repulsion

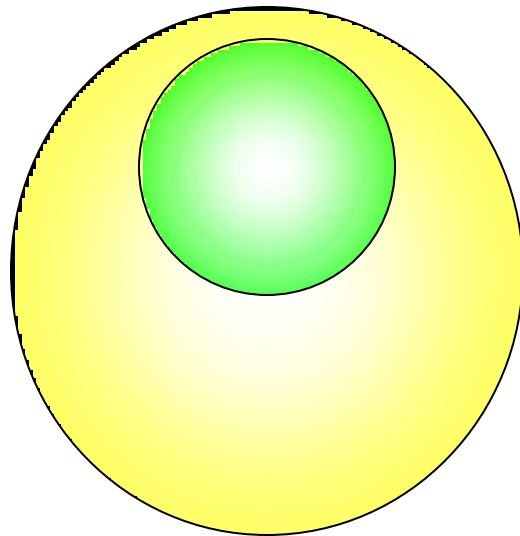
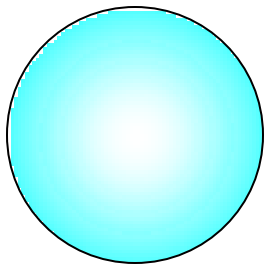




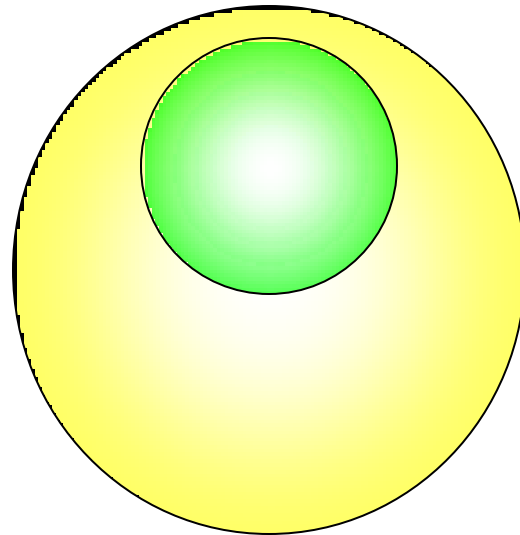
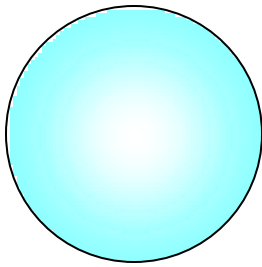
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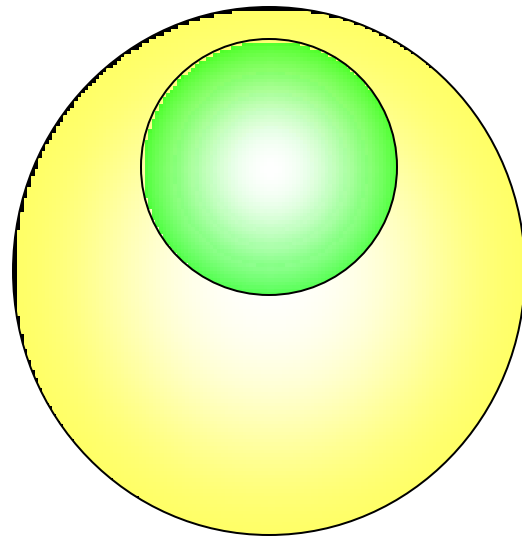
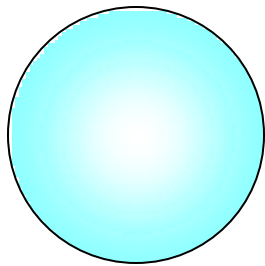
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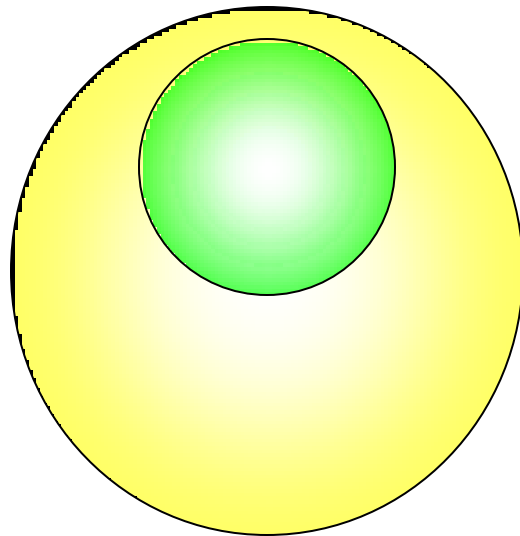
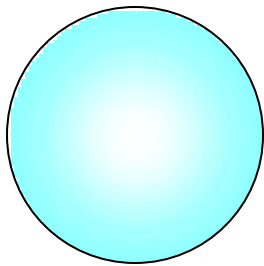
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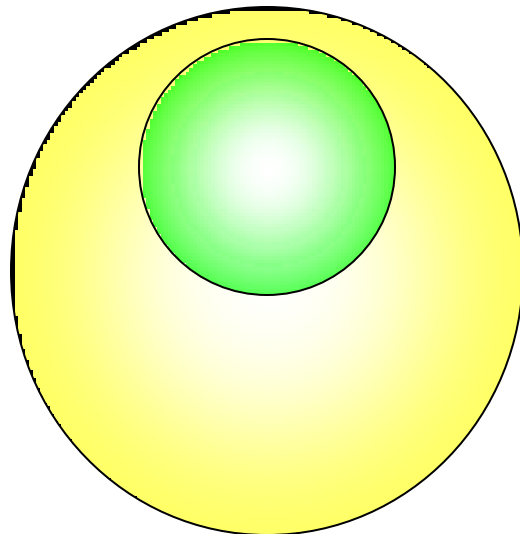
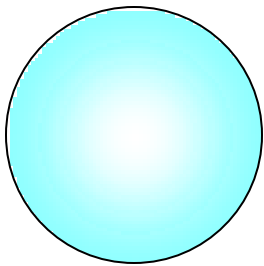
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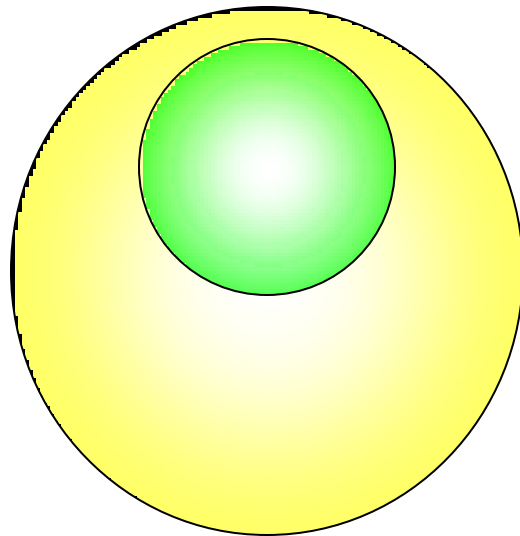
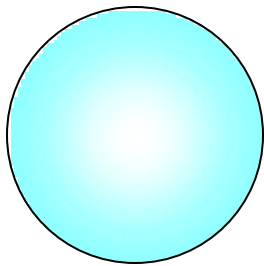
# Knockout using Short Finite Range Repulsion



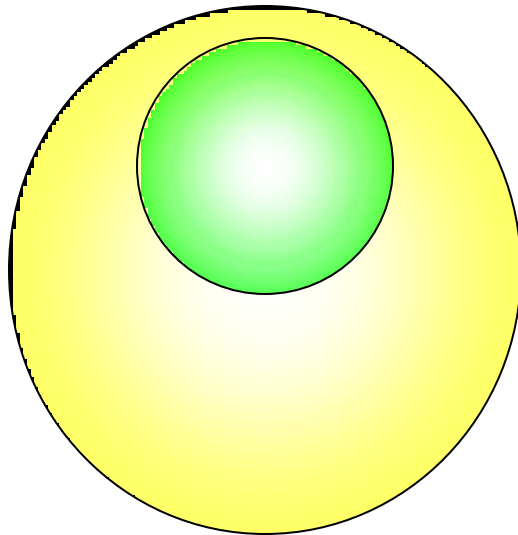
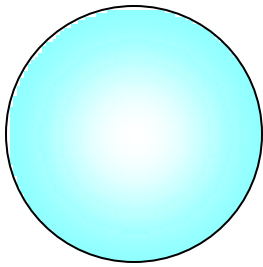
# Knockout using Short Finite Range Repulsion



# Knockout using Short Finite Range Repulsion

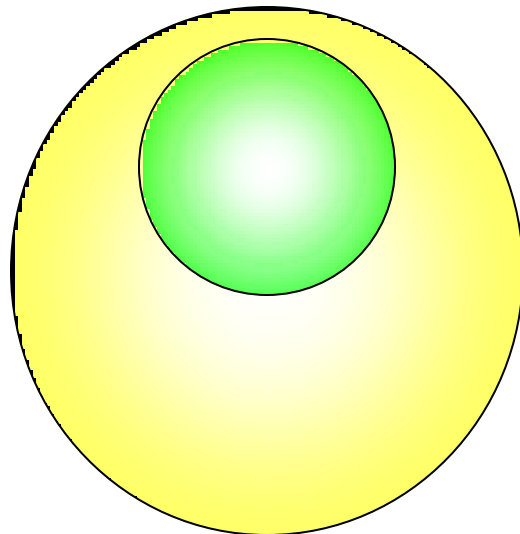
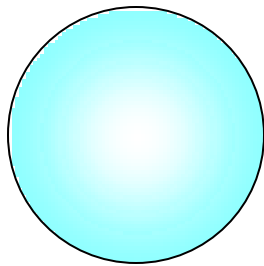


# Knockout using Short Finite Range Repulsion

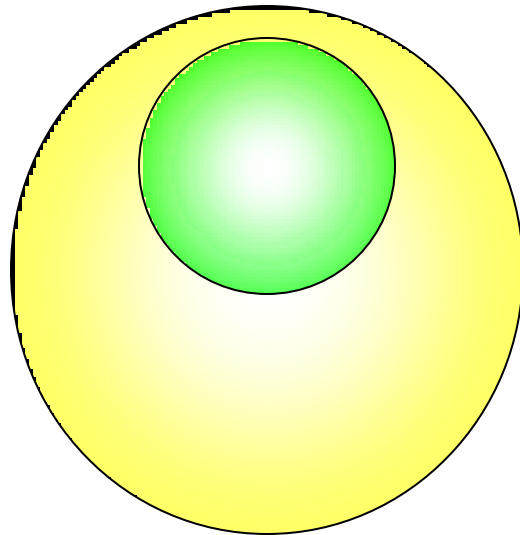
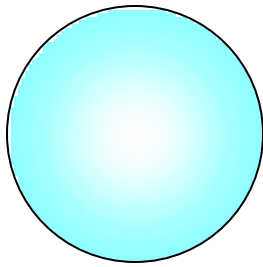




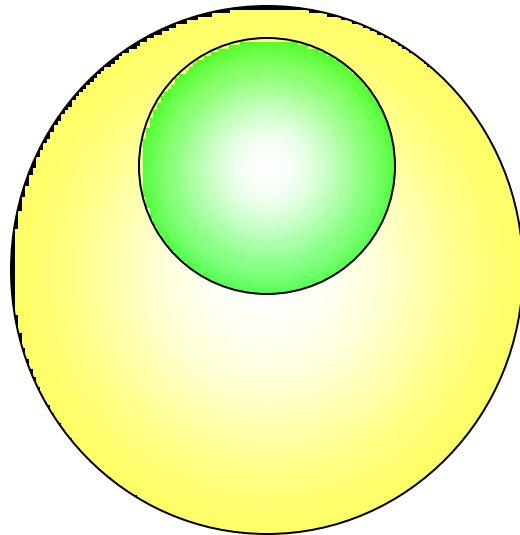
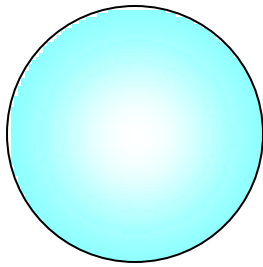
# Knockout using Short Finite Range Repulsion



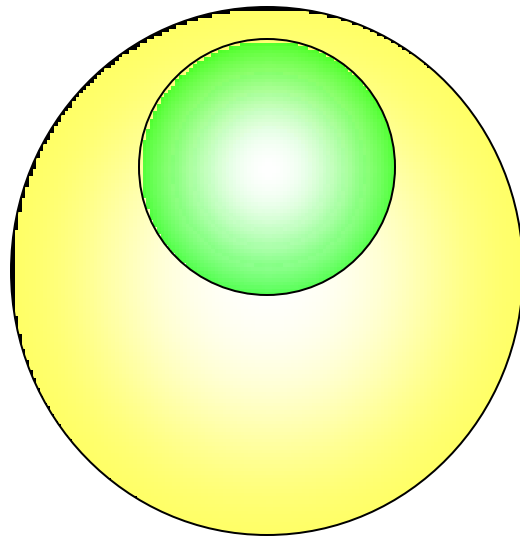
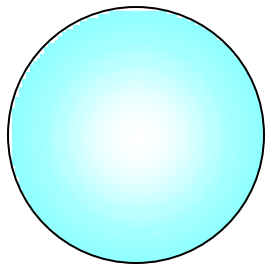
# Knockout using Short Finite Range Repulsion



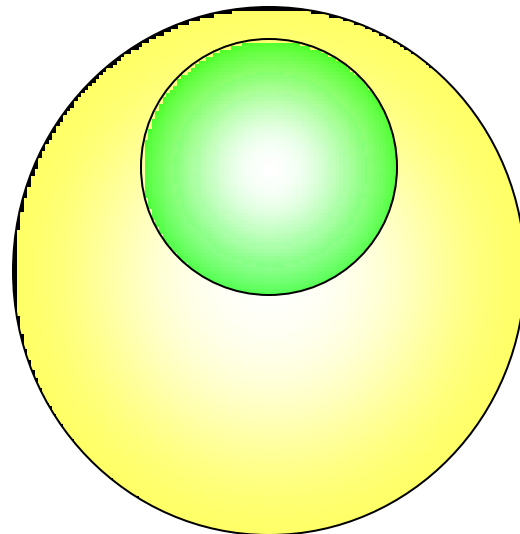
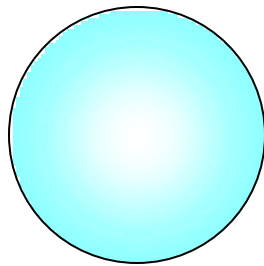
# Knockout using Short Finite Range Repulsion



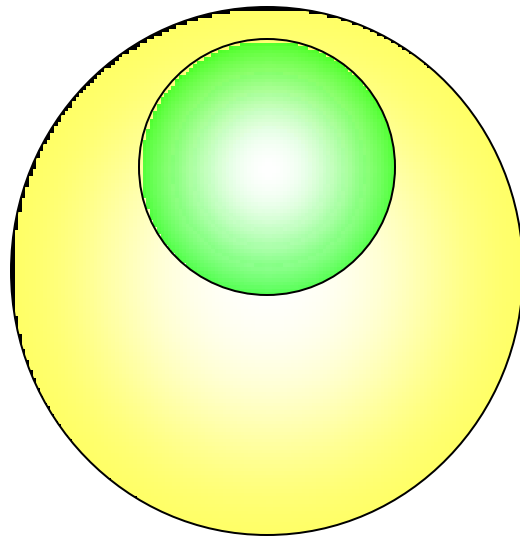
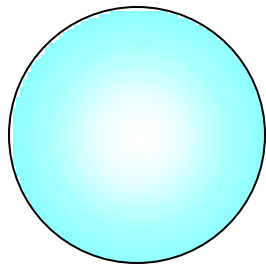
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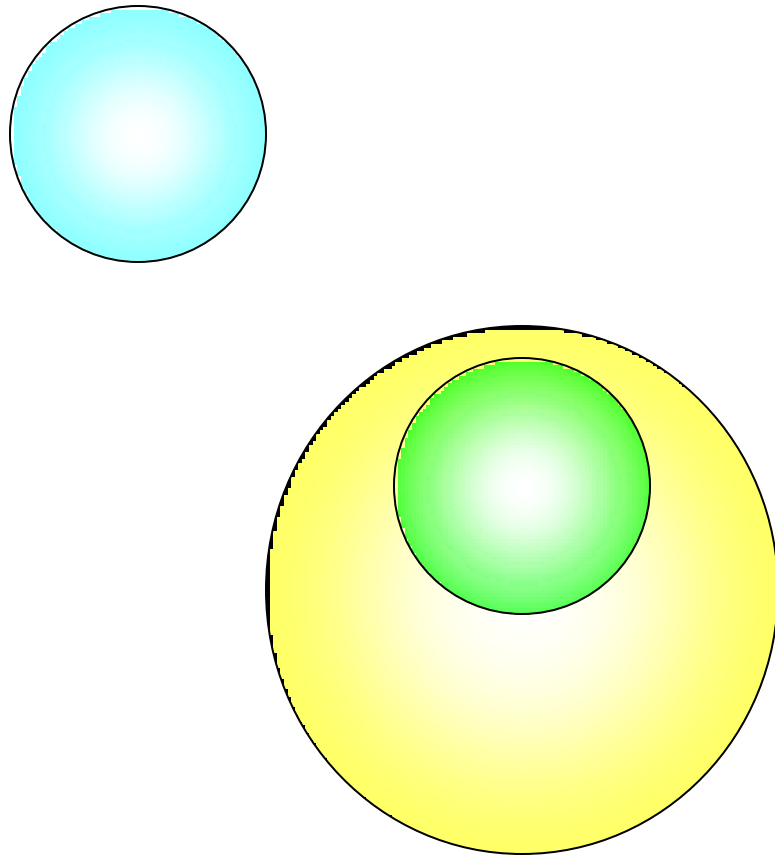
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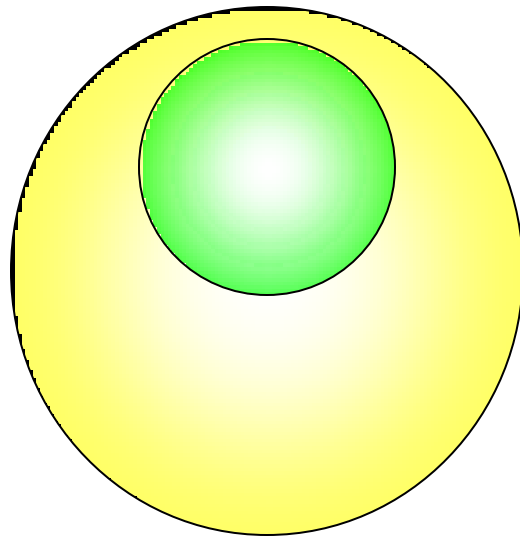
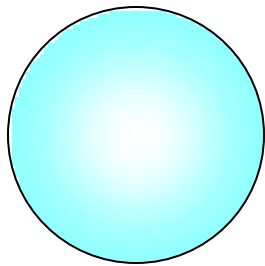
# Knockout using Short Finite Range Repulsion



# Knockout using Short Finite Range Repulsion

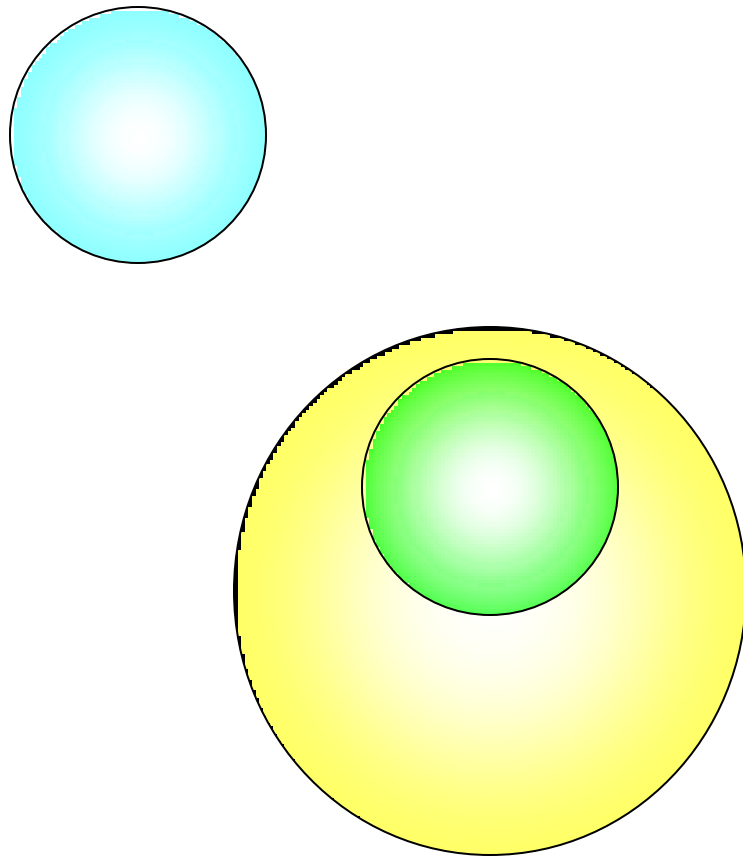


# Knockout using Short Finite Range Repulsion

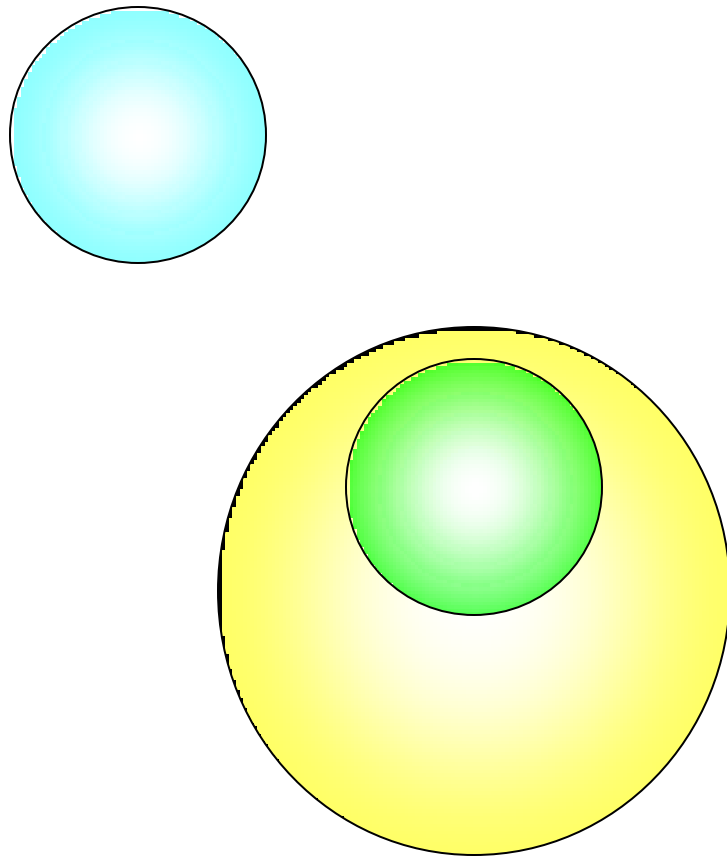




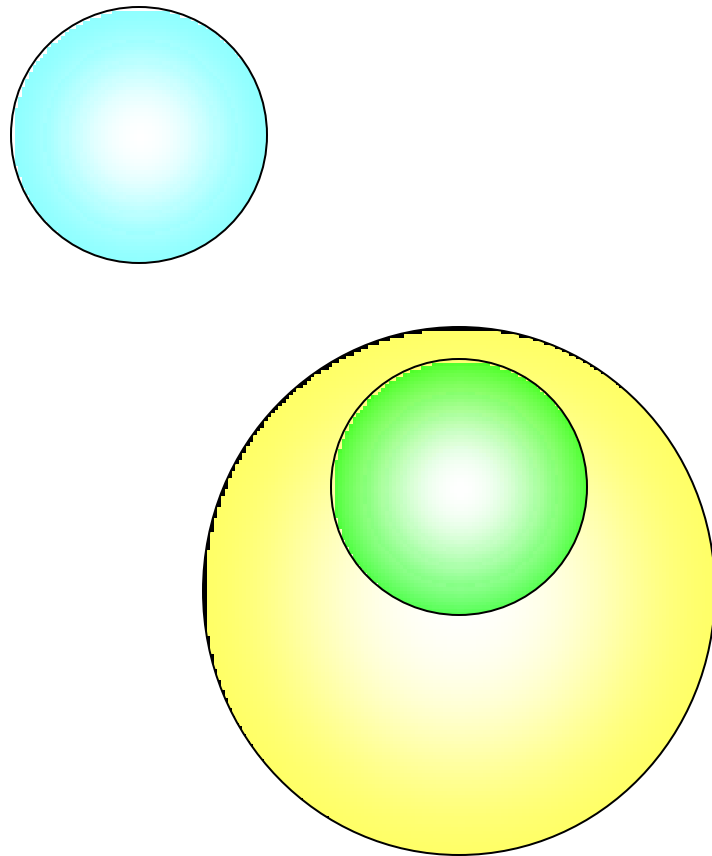
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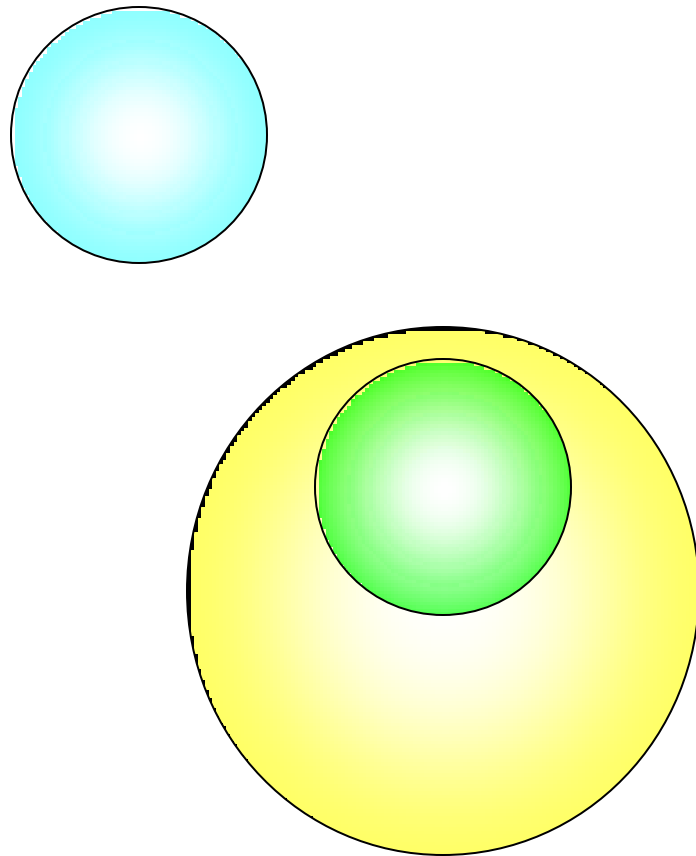
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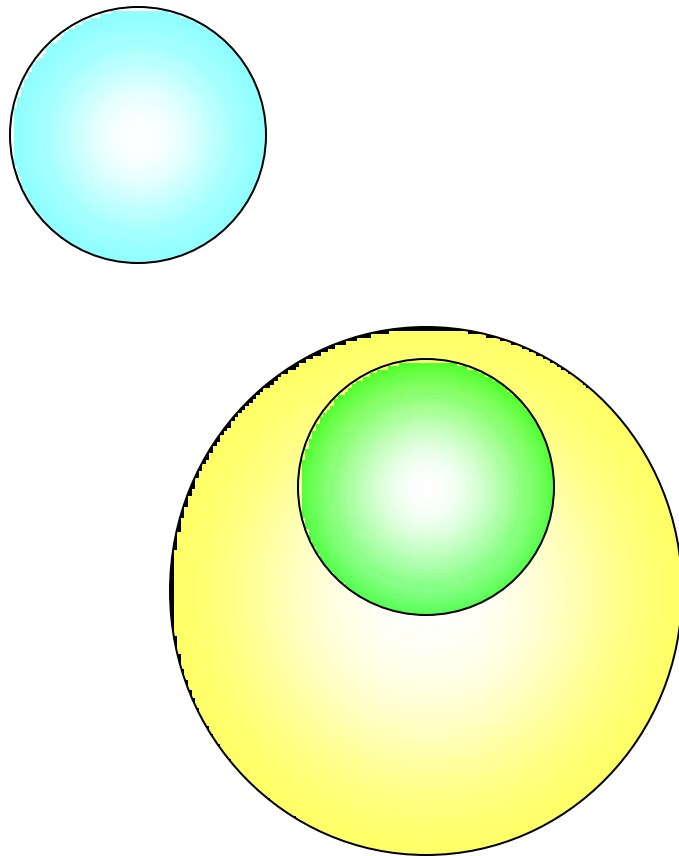
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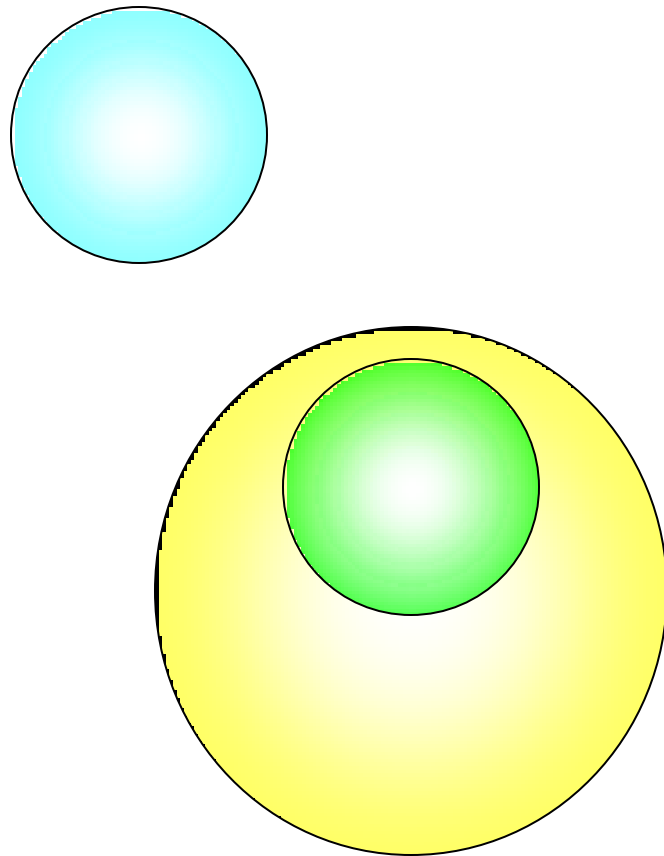
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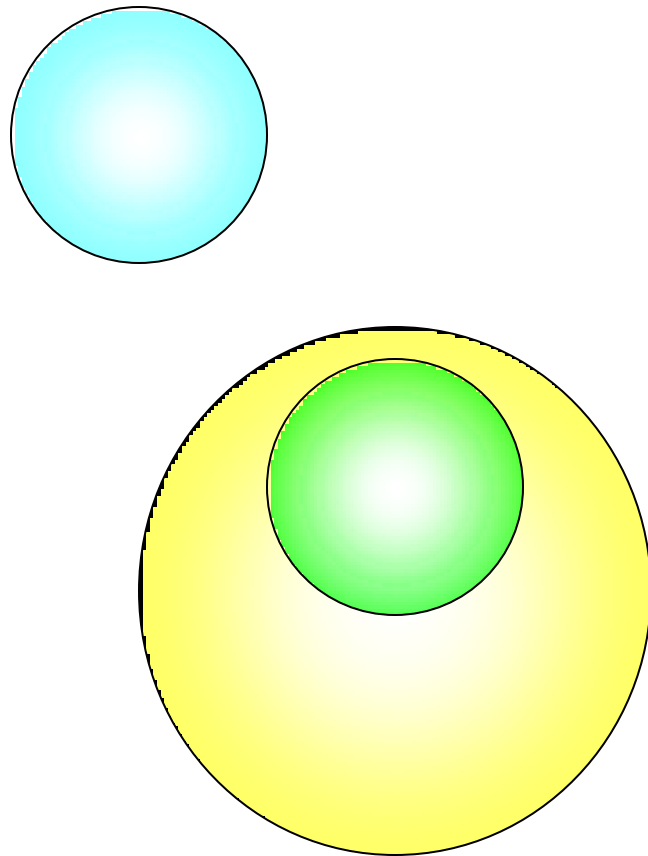
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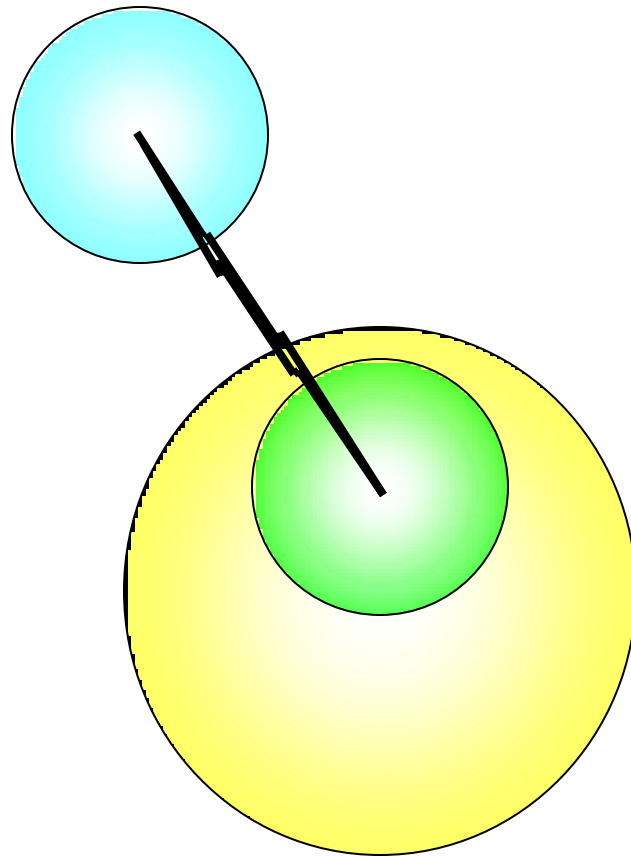
# Knockout using Short Finite Range Repulsion



# Knockout using Short Finite Range Repulsion

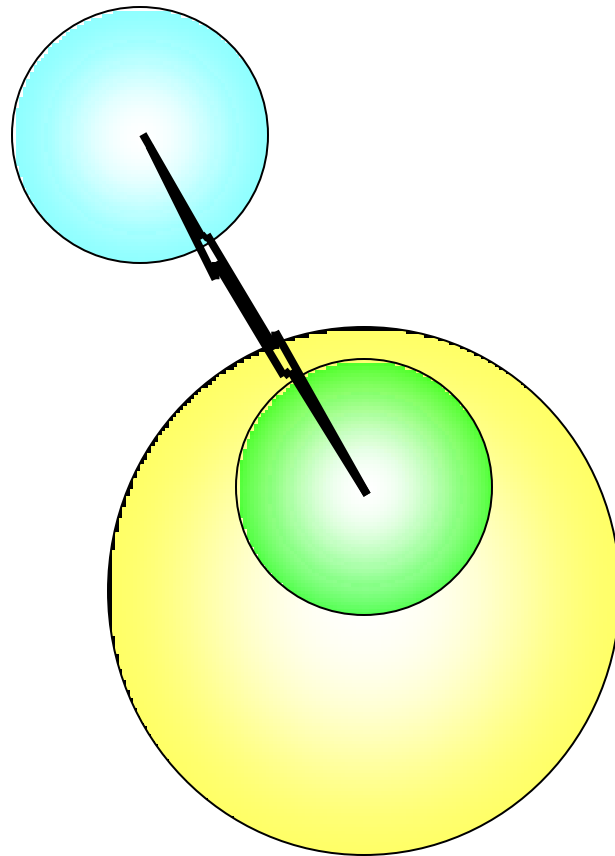


# Knockout using Short Finite Range Repulsion

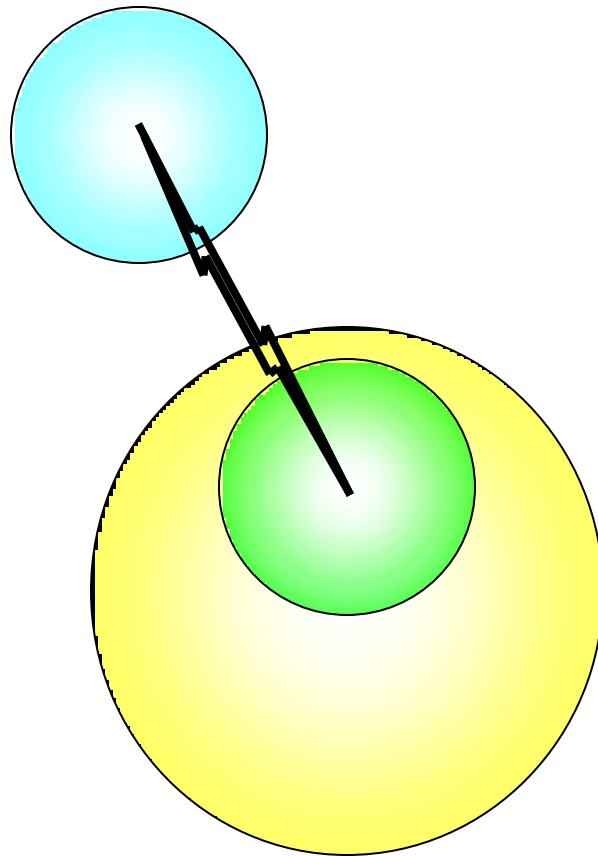




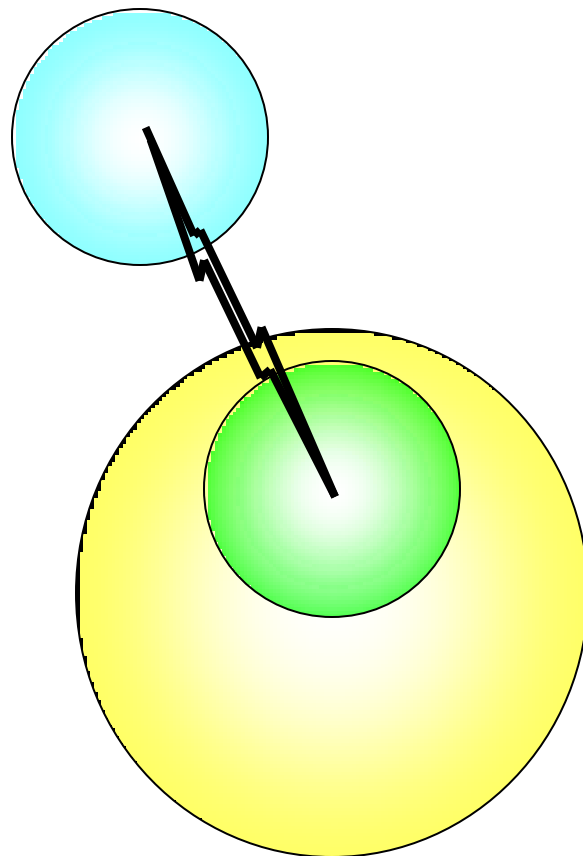
# Knockout using Short Finite Range Repulsion



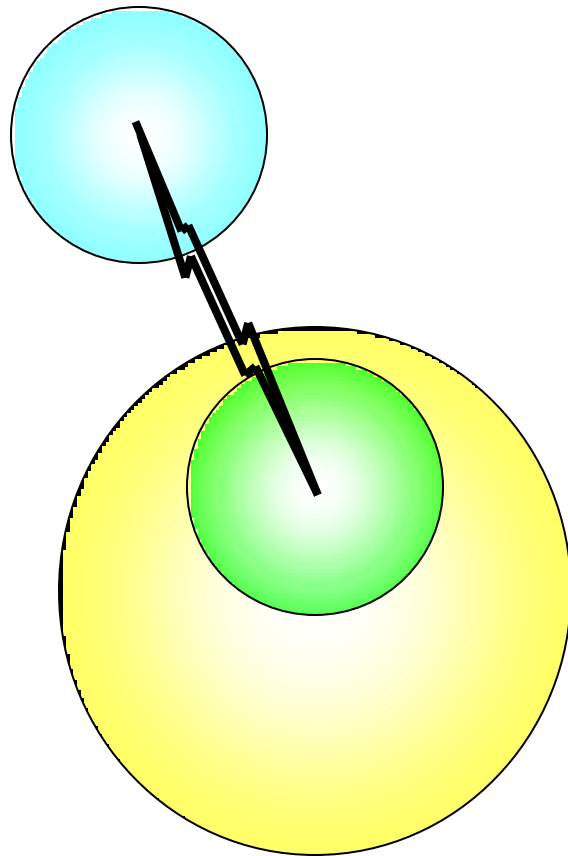
# Knockout using Short Finite Range Repulsion



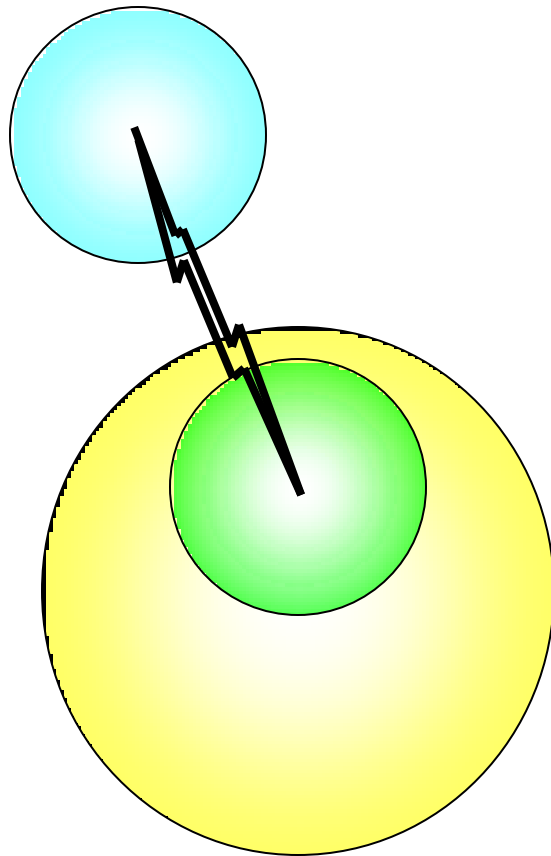
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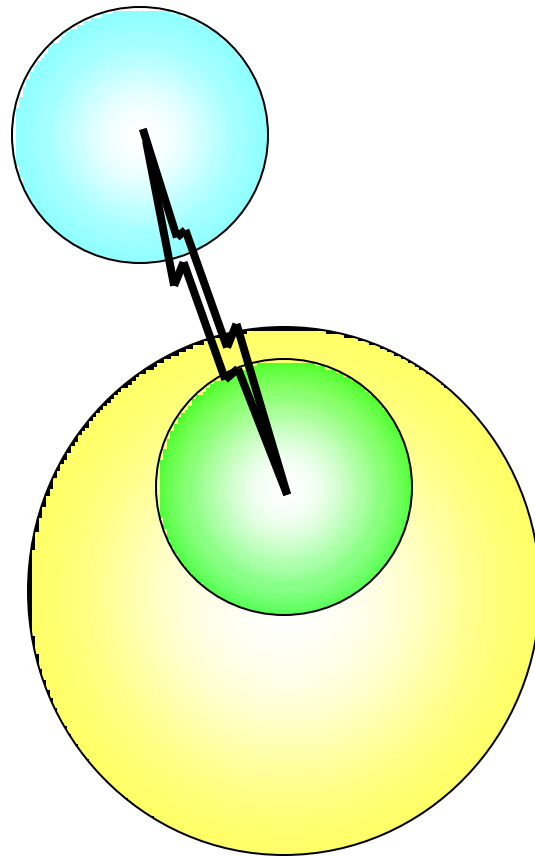
# Knockout using Short Finite Range Repulsion



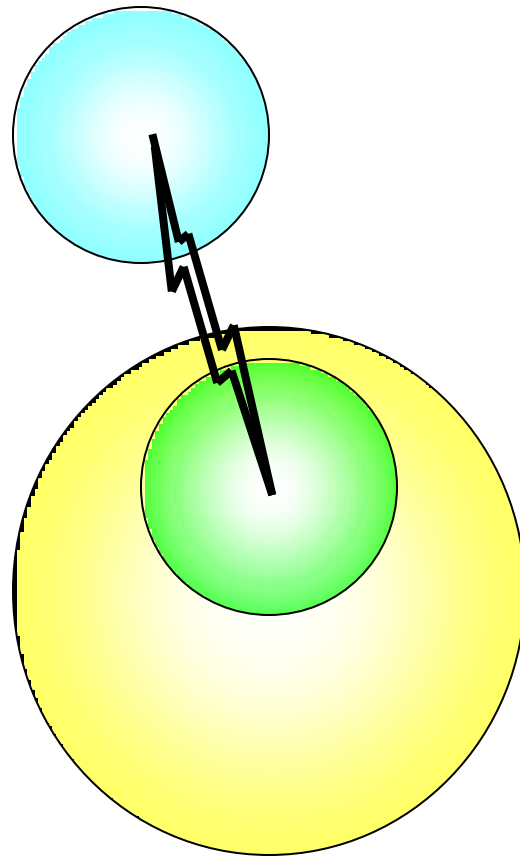
# Knockout using Short Finite Range Repulsion



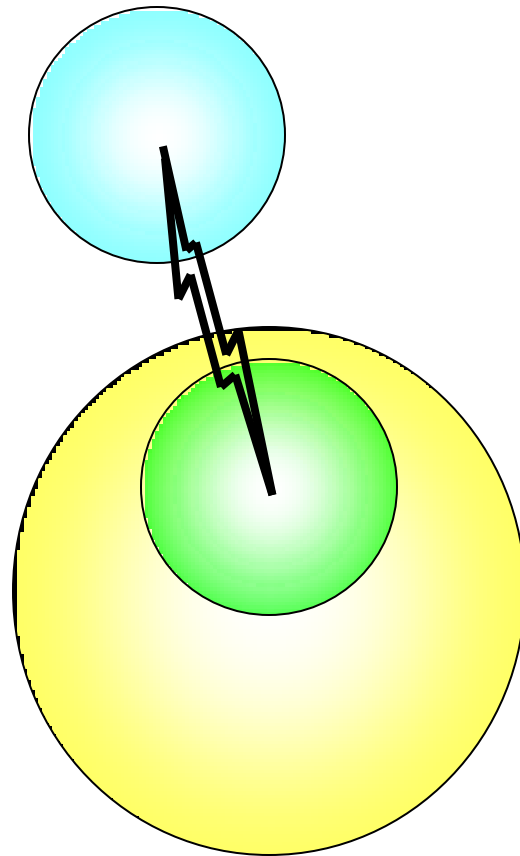
# Knockout using Short Finite Range Repulsion



# Knockout using Short Finite Range Repulsion

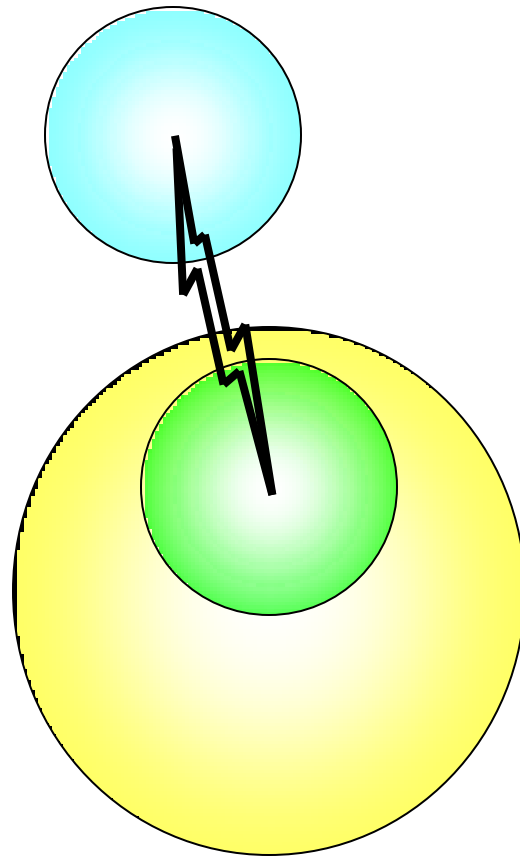


# Knockout using Short Finite Range Repulsion

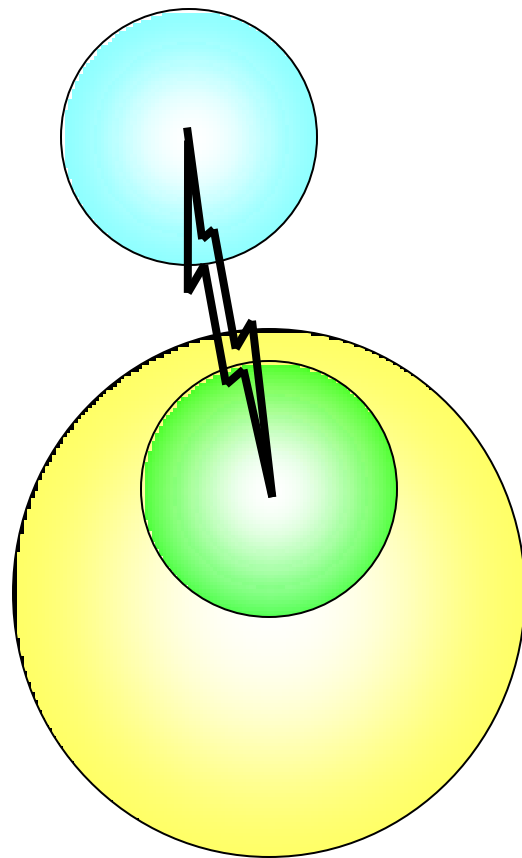




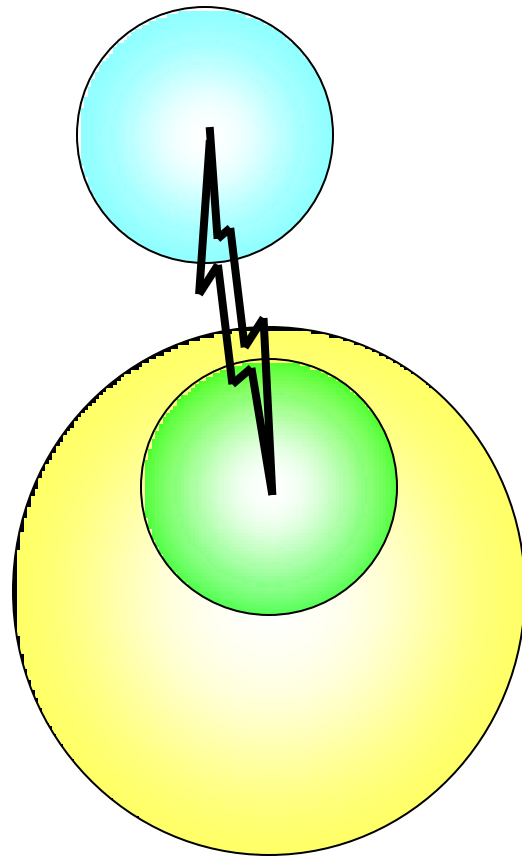
# Knockout using Short Finite Range Repulsion



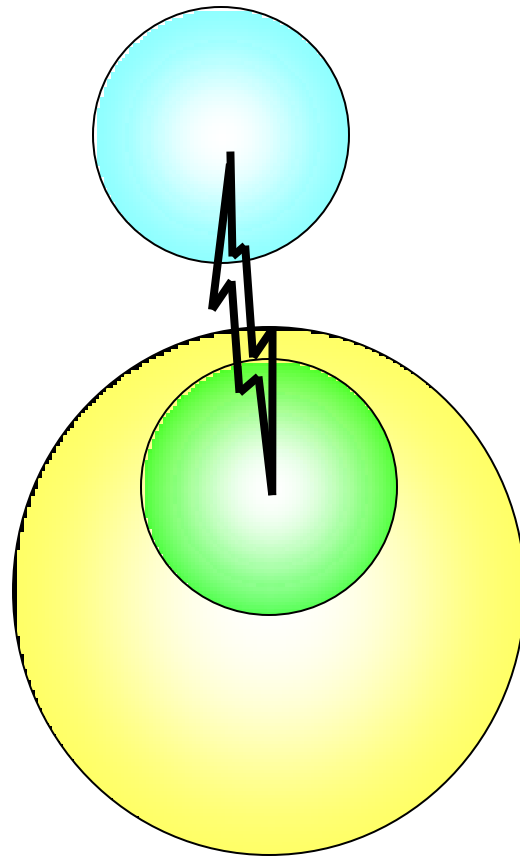
# Knockout using Short Finite Range Repulsion



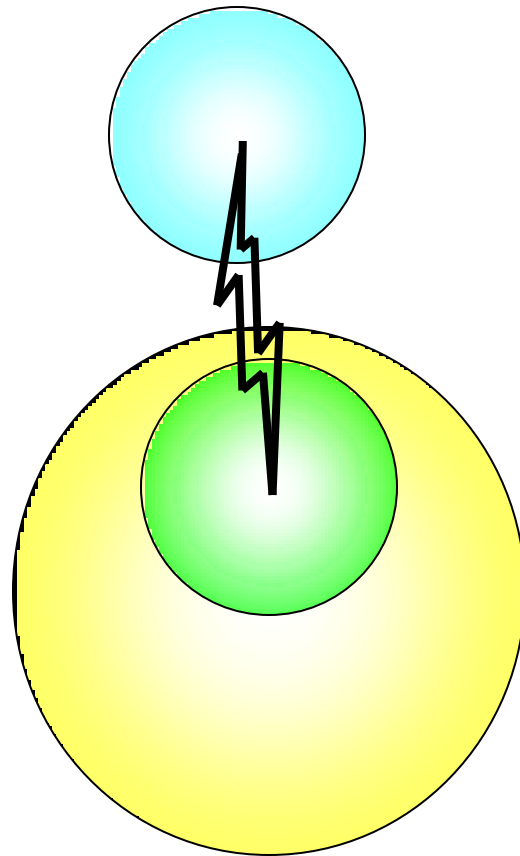
# Knockout using Short Finite Range Repulsion



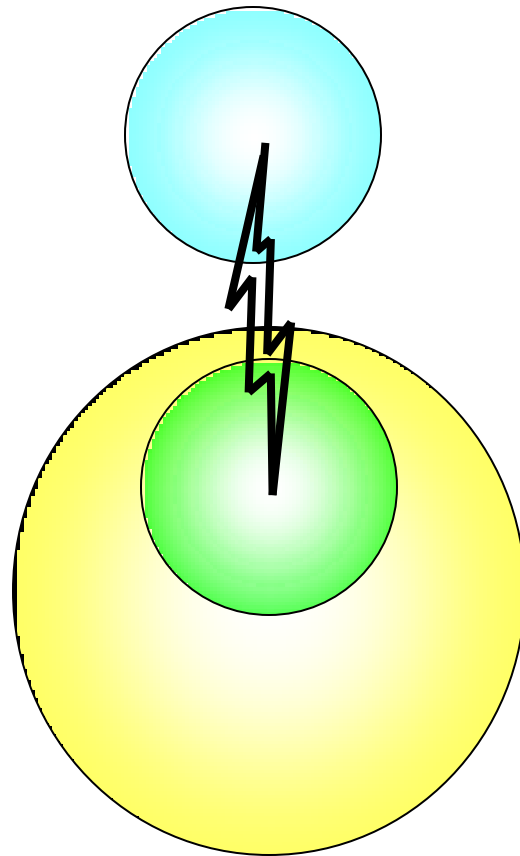
# Knockout using Short Finite Range Repulsion



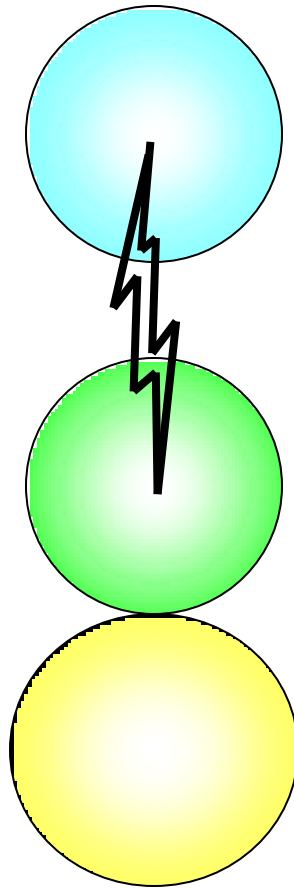
# Knockout using Short Finite Range Repulsion



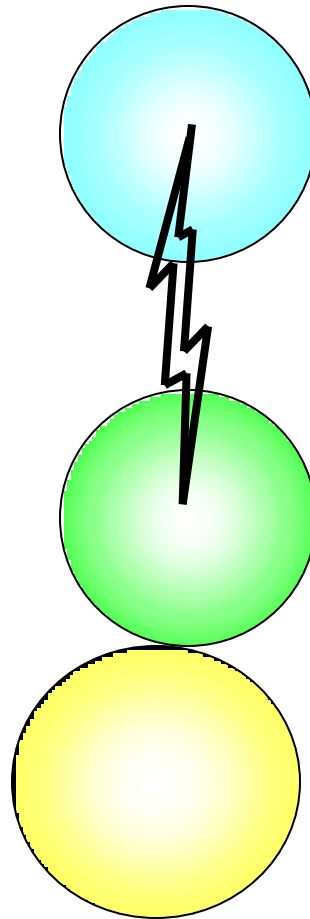
# Knockout using Short Finite Range Repulsion



# Knockout using Short Finite Range Repulsion

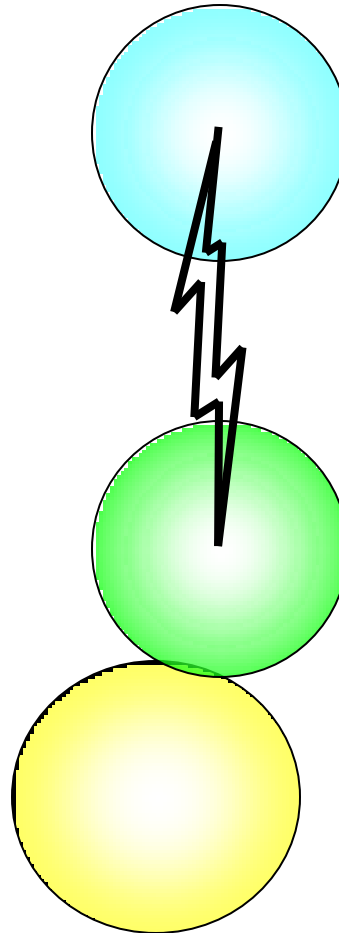


# Knockout using Short Finite Range Repulsion

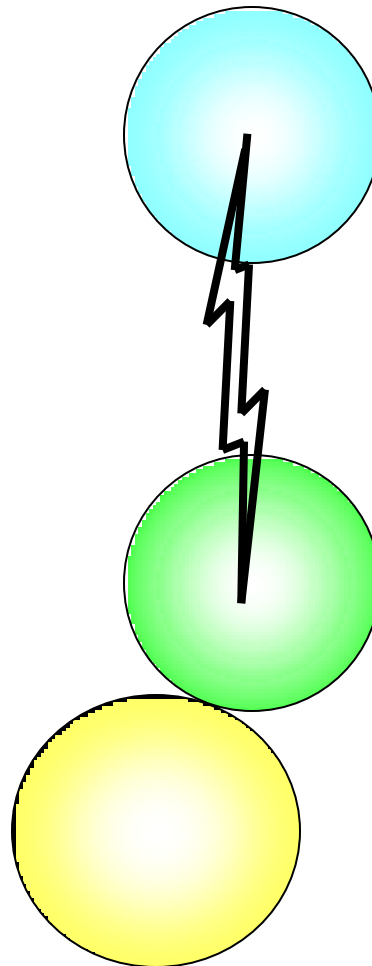




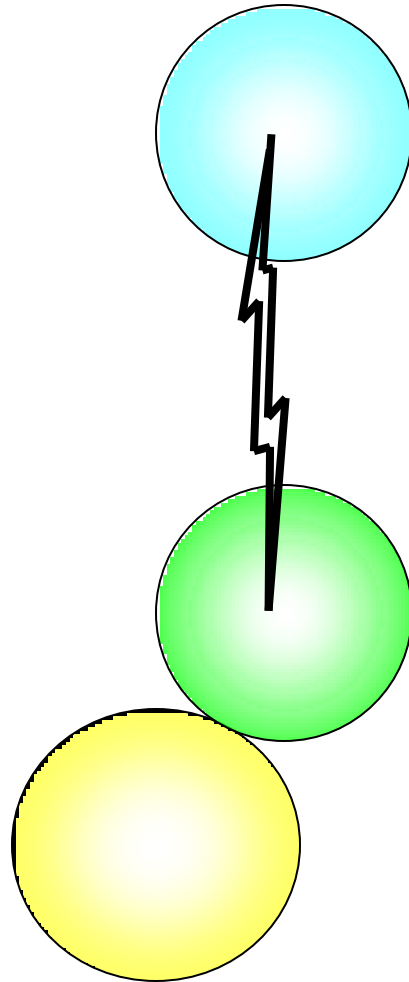
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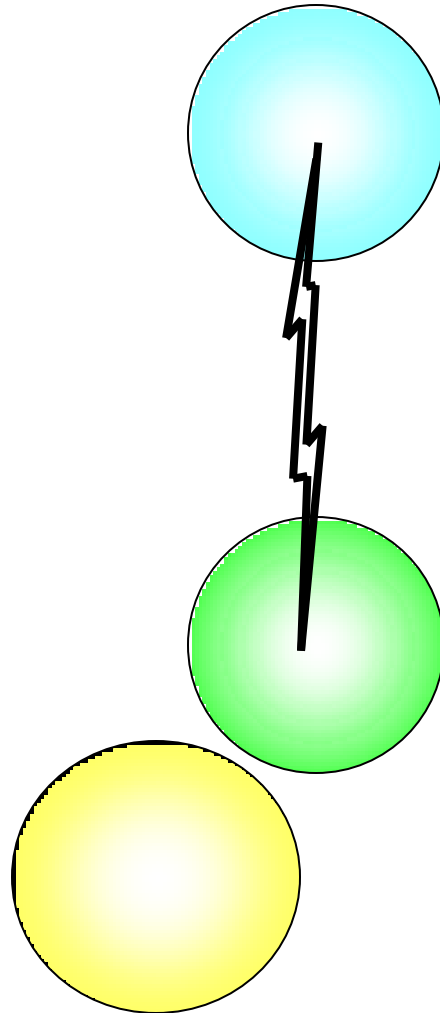
# Knockout using Short Finite Range Repulsion



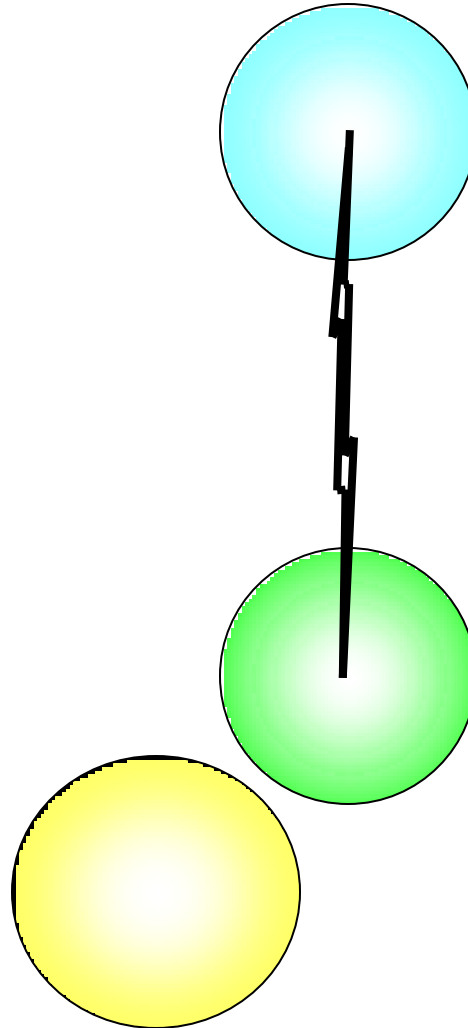
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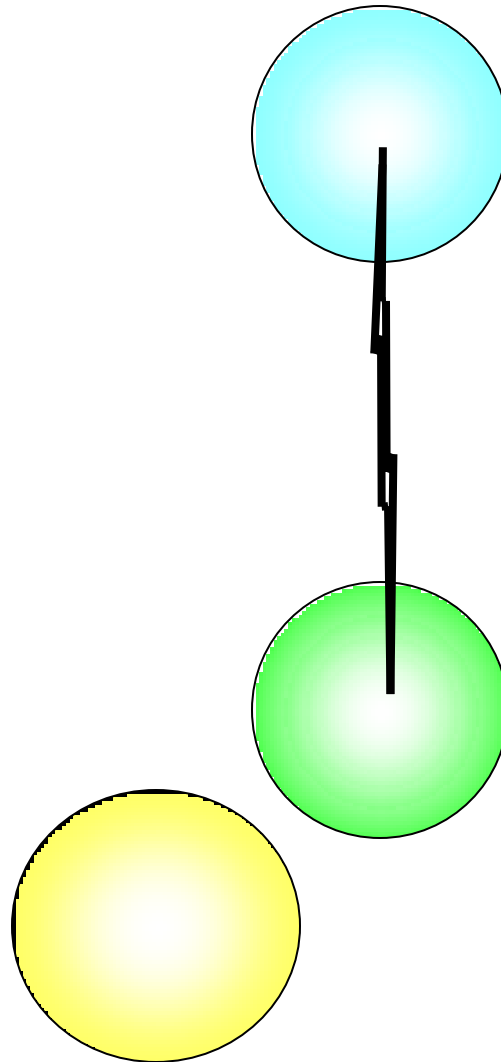
# Knockout using Short Finite Range Repulsion



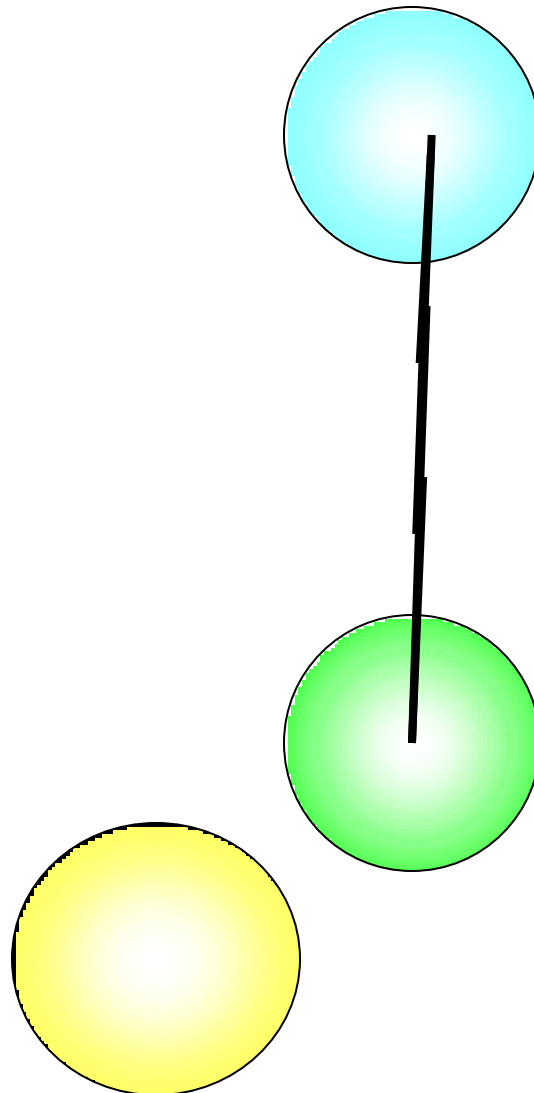
# Knockout using Short Finite Range Repulsion



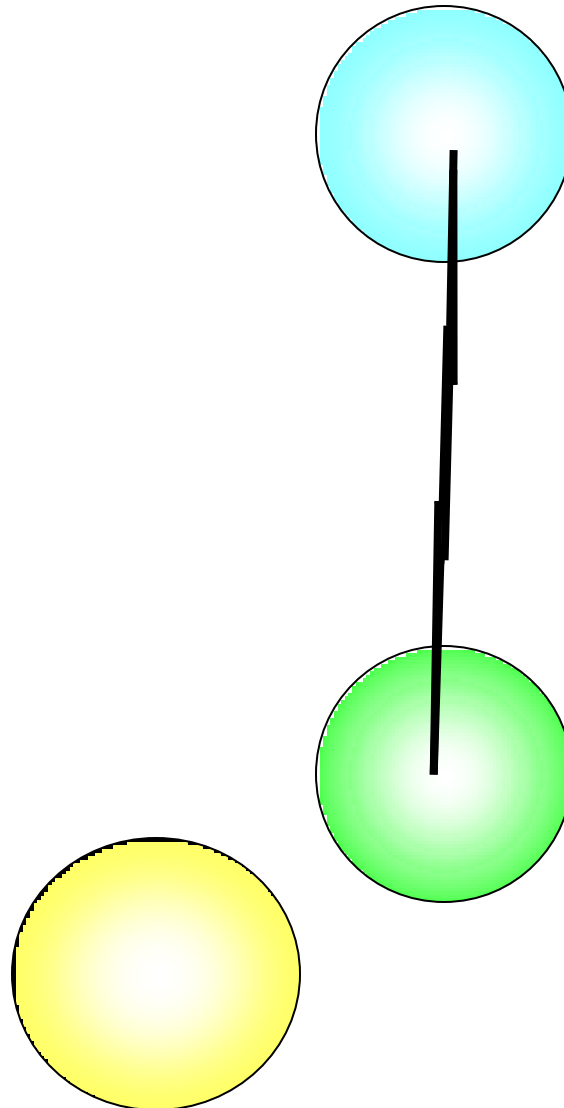
# Knockout using Short Finite Range Repulsion



# Knockout using Short Finite Range Repulsion

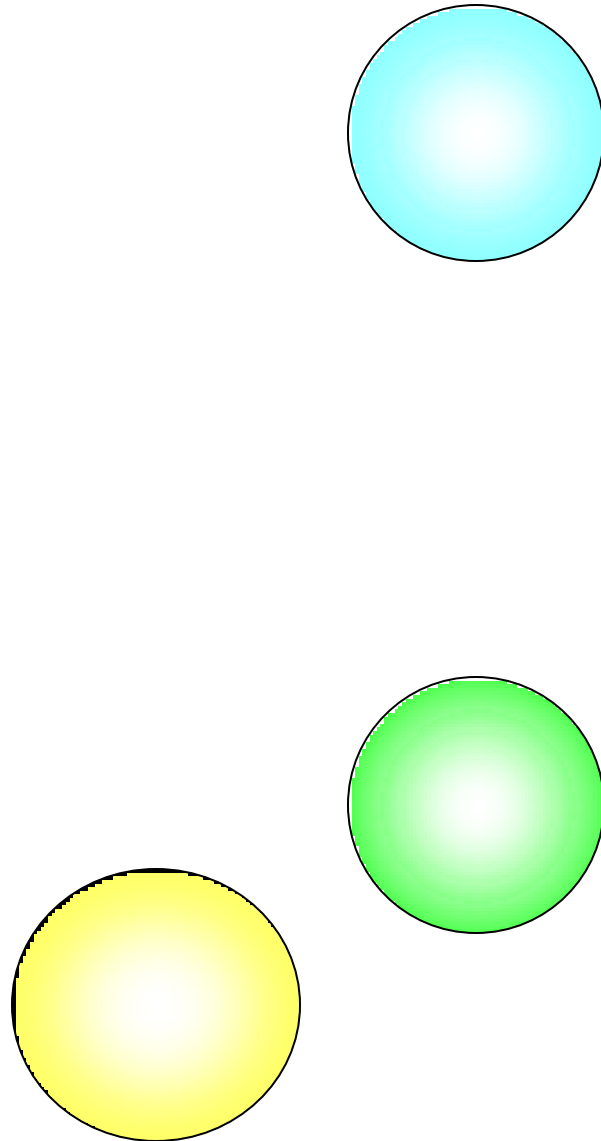


# Knockout using Short Finite Range Repulsion

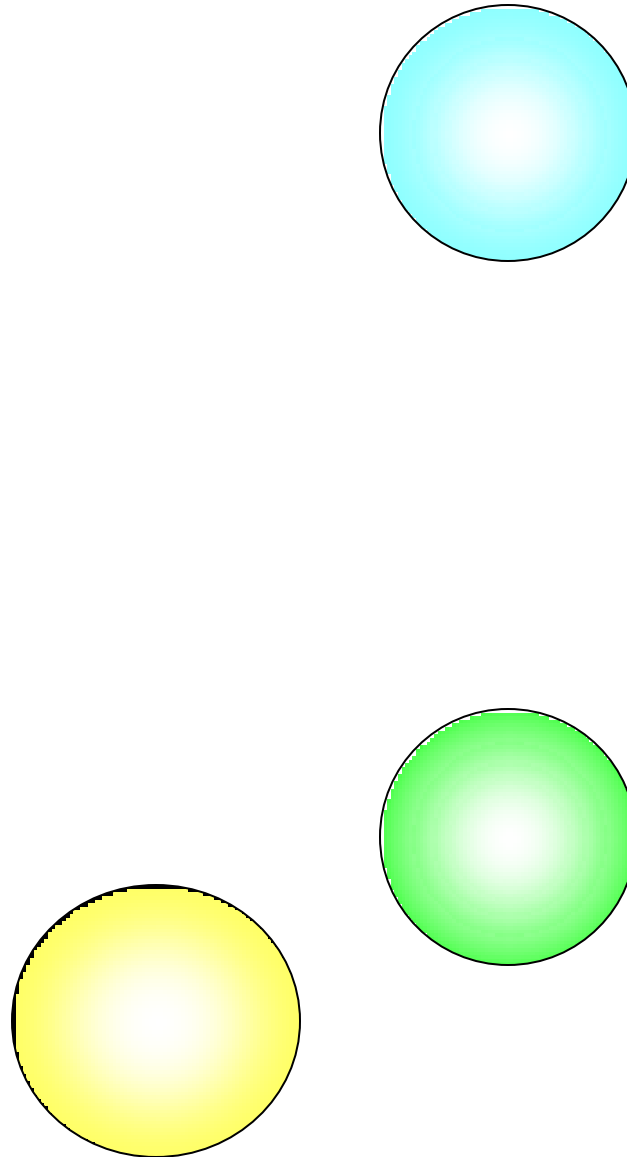




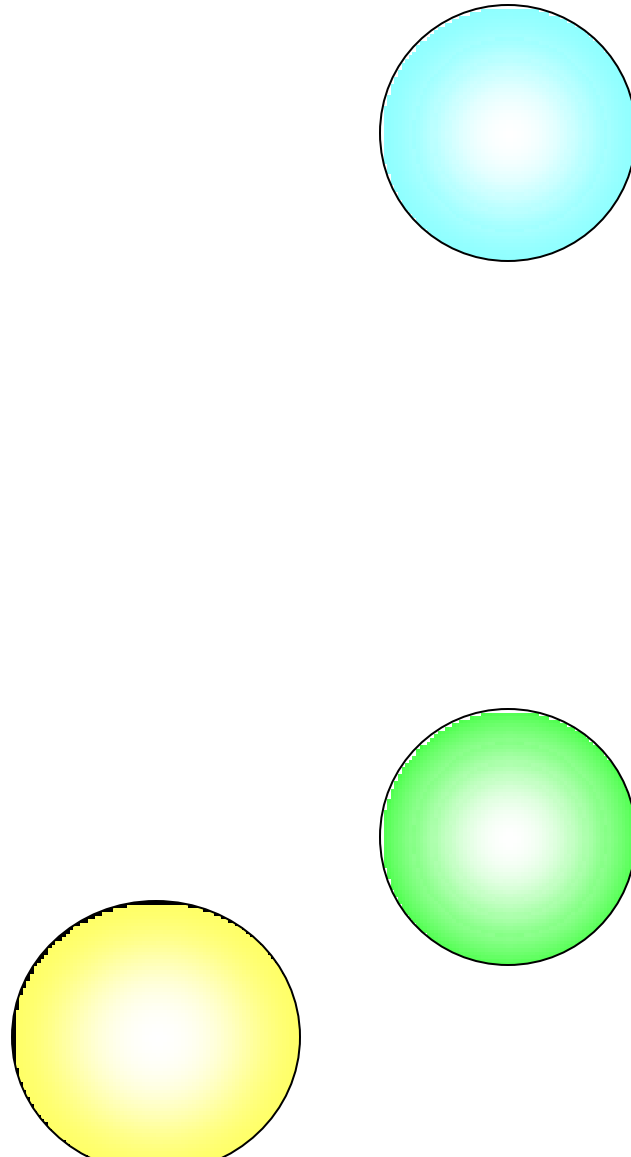
# Knockout using Short Finite Range Repulsion



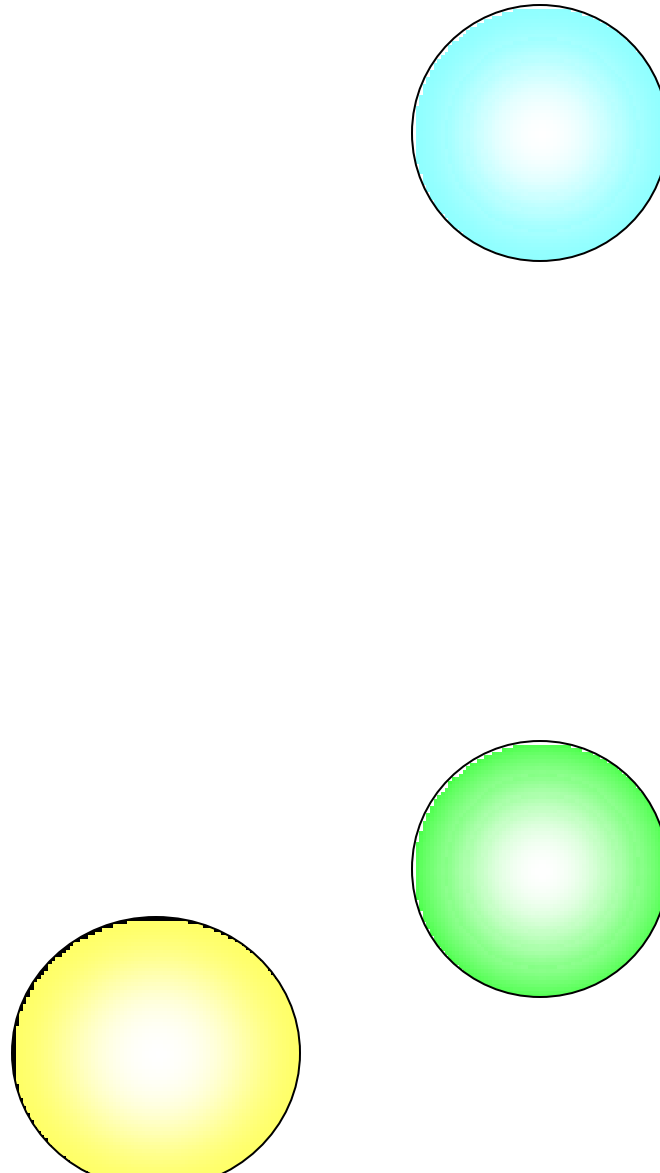
# Knockout using Short Finite Range Repulsion



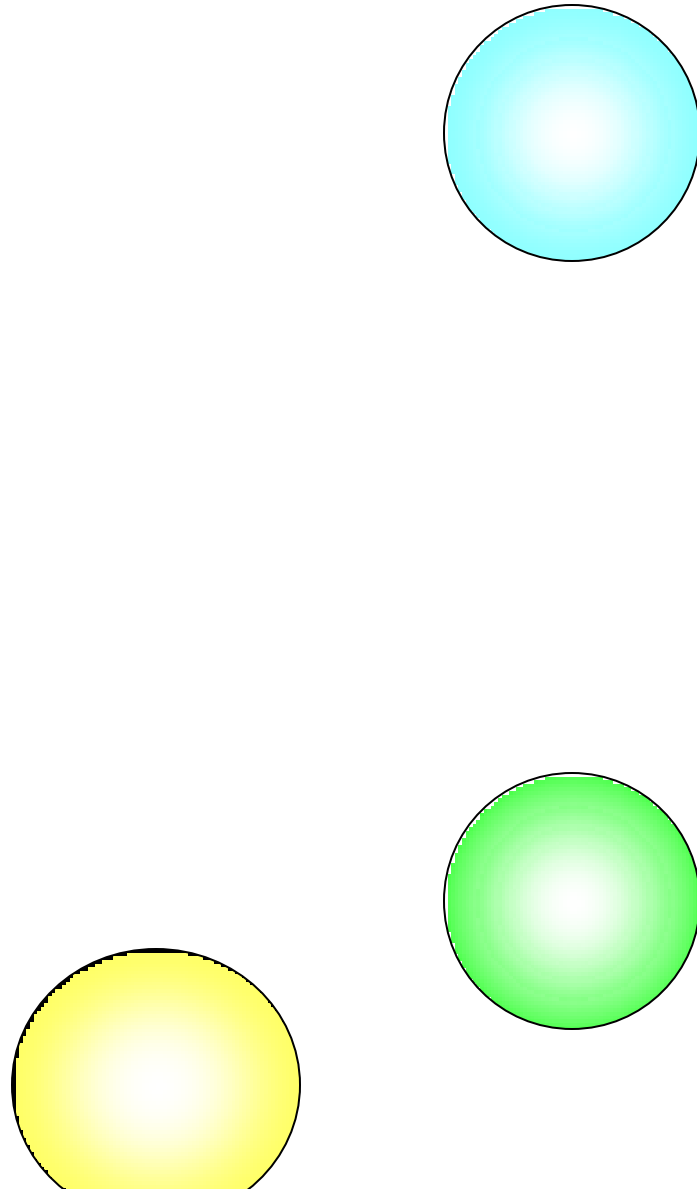
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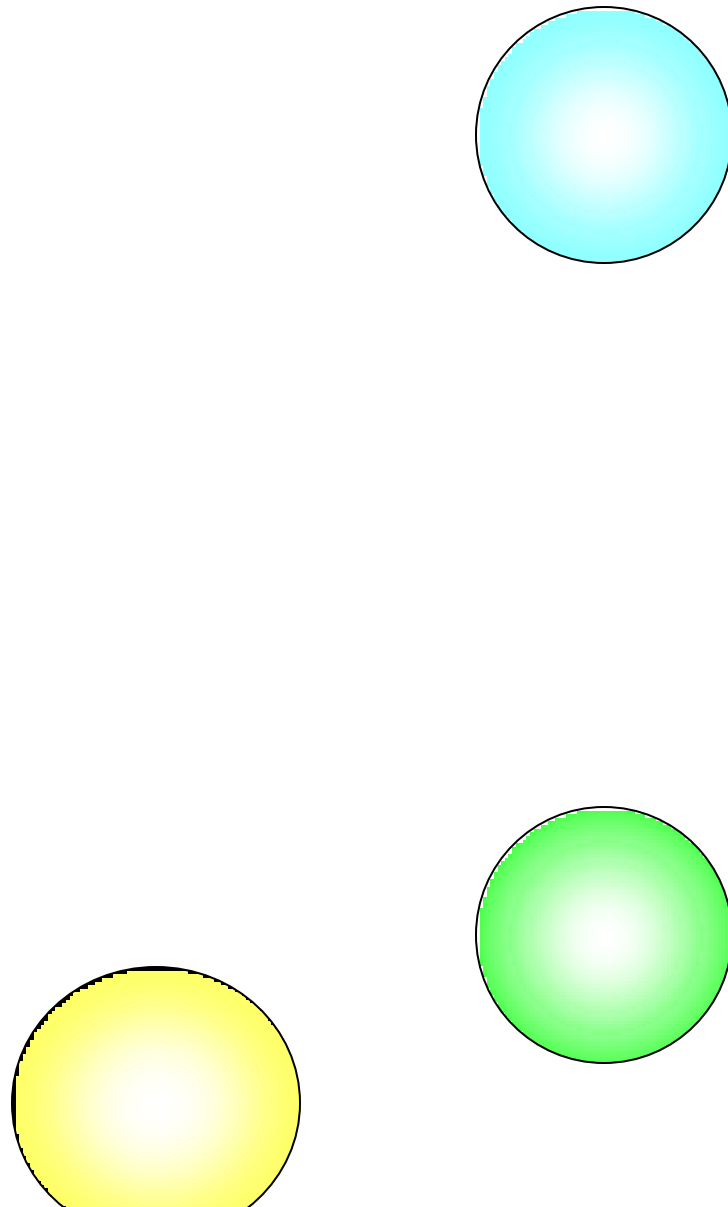
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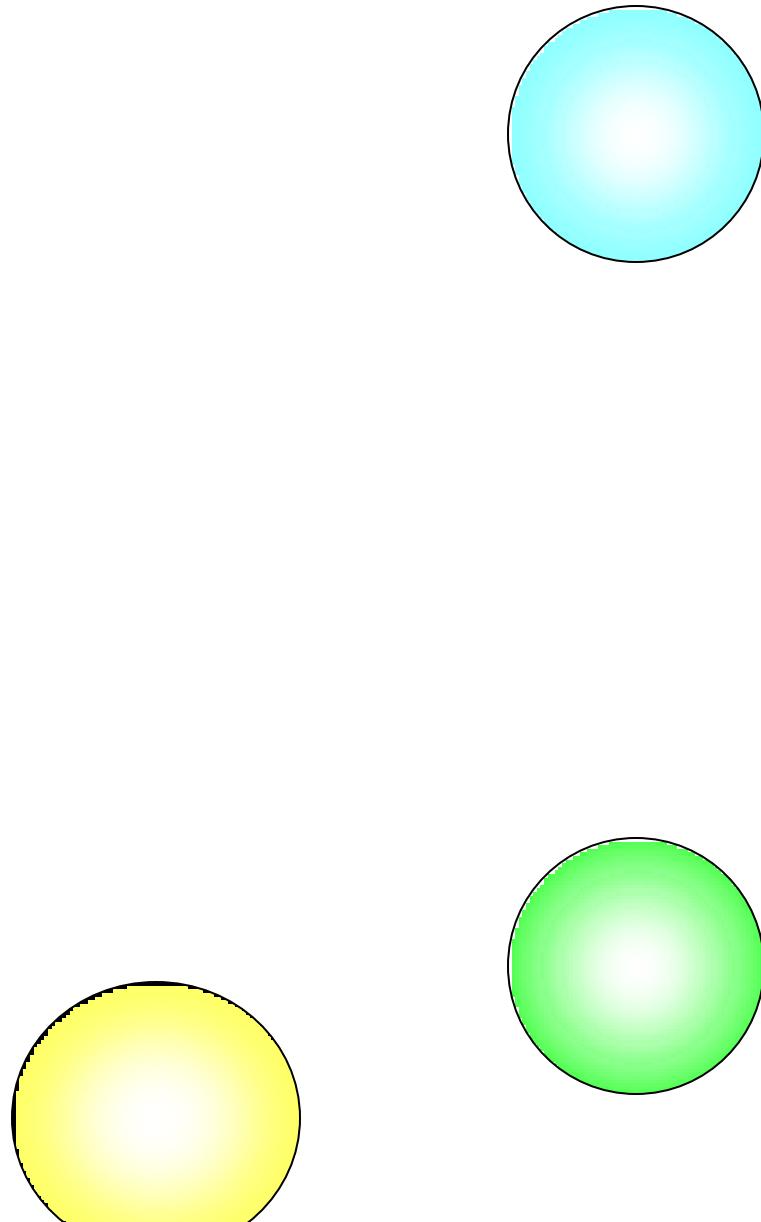
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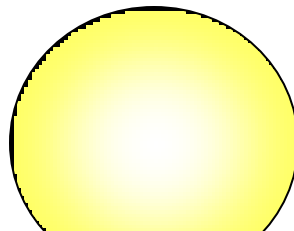
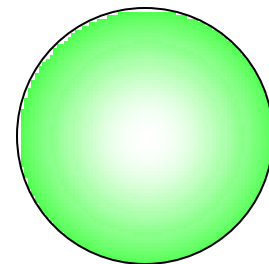
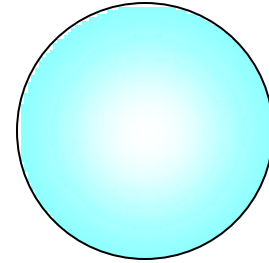
# Knockout using Short Finite Range Repulsion



# Knockout using Short Finite Range Repulsion

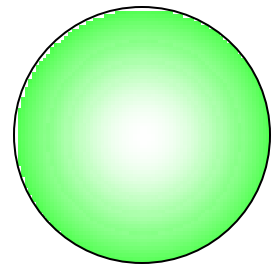
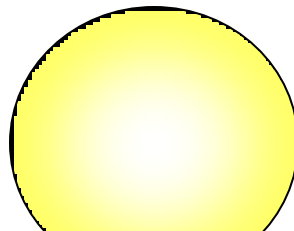
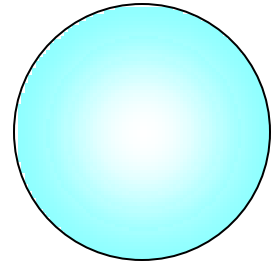


# Knockout using Short Finite Range Repulsion

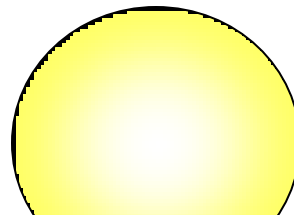
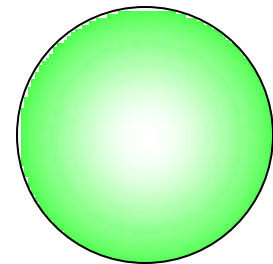
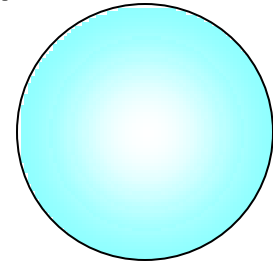




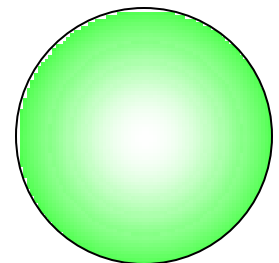
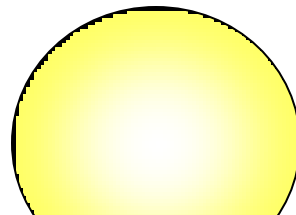
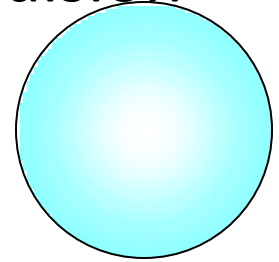
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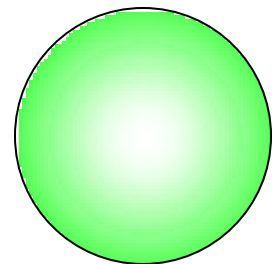
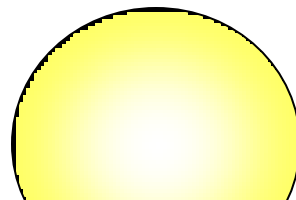
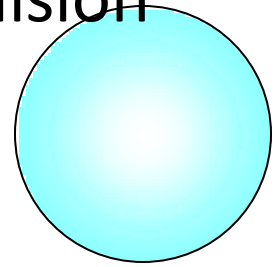
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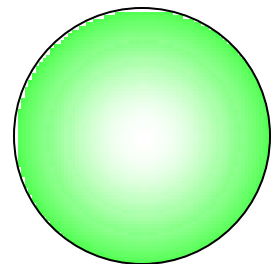
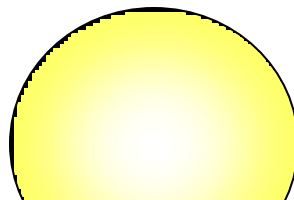
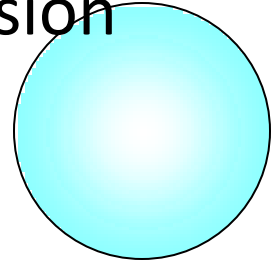
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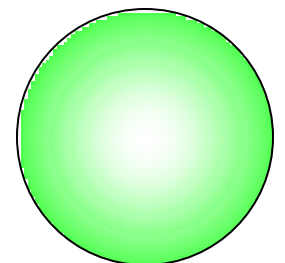
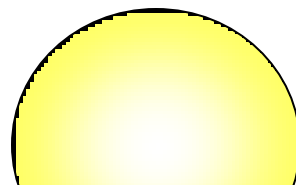
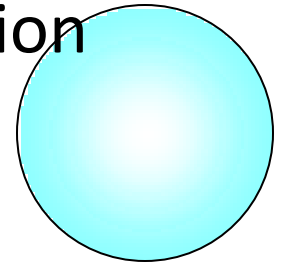
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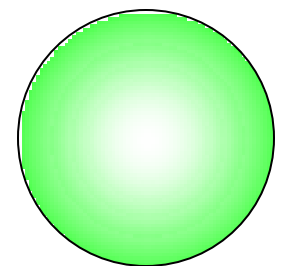
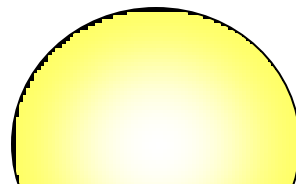
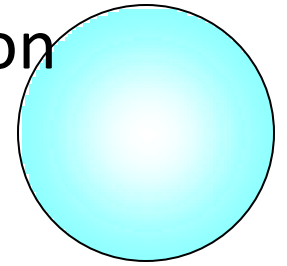
# Knockout using Short Finite Range Repulsion



# Knockout using Short Finite Range Repulsion



# Knockout using Short Finite Range Repulsion



Zero Range Approximation for the knockout vertex is hidden in the conventional language of the factorization approximation of the knockout vertex matrix element.

Actually the transition matrix element and the double differential cross section are written as,

$$\frac{d^3\sigma^{L,J}}{d\Omega_1 d\Omega_2 dE_1} = F_{kin} \cdot S_\alpha^{LJ} \cdot \sum_{\Lambda} \left| T_{fi}^{\alpha L \Lambda}(\vec{k}_f, \vec{k}_i) \right|^2$$

$$T_{fi}^{\alpha L \Lambda}(\vec{k}_f, \vec{k}_i) = \int g(r) dr$$

$$= \int \chi_1^{(-)*}(\vec{k}_{aB}, \vec{r}_{aB}) \chi_2^{(-)*}(\vec{k}_{2B}, \vec{R}_{2B}) t_{12}(\vec{r}_{12}) \chi_0^{(+)}(\vec{k}_{1A}, \vec{r}_{1A}) \varphi_{L\Lambda}(\vec{R}_{2B}) d\vec{r}_{12} d\vec{R}_{2B}$$

**Which includes the finite range effects, which we have worked for the first time.**



t- matrix effective Interaction

## t-matrix:-

$$t^{\pm} = V\Omega^{\pm}$$

The Moller wave  $\Omega^{\pm}$  operator is such that it transforms the plane wave states,  $\Phi$  into scattering states,  $\psi^{\pm}$  is defined in terms of radial scattering solutions  $u_l(kr)$  as:

$$\psi_{\alpha\alpha}^{\pm}(\vec{r}) = \sum_{l=0,2,4} i^l (2l+1) \frac{u_l(kr)}{kr} e^{i\sigma_l} P_l(\hat{r})$$

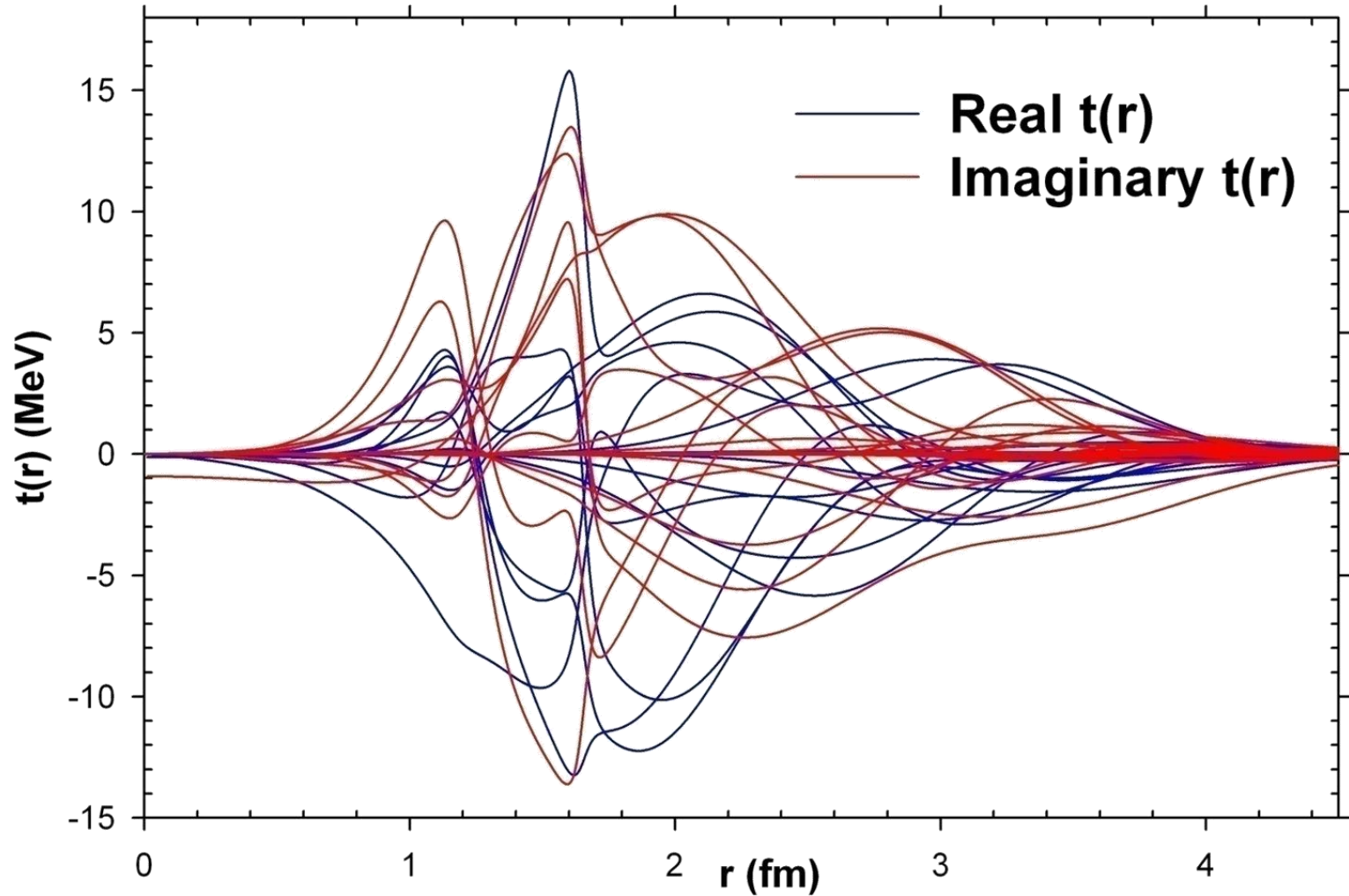
$$t_{\alpha\alpha}^+(E, \vec{r}) = e^{-ikz} \sum_{l=0,2,4\dots} V_l(r) i^l (2l+1) \frac{u_l(kr)}{kr} e^{i\sigma_l} P_l(\hat{r})$$

$$t_L(E, r) = \frac{2L+1}{2} \sum_{l,m} V_l(r) i^l (2L+1) \frac{\mu_l(kr)}{kr} j_m(kr) (-i)^m (2m+1) e^{i\sigma_l} \int_{-1}^{+1} P_L^*(\cos\theta) P_l(\cos\theta) P_m(\cos\theta) d(\cos\theta)$$

**Arun K Jain & Bhushan N. Joshi, Prog. Theor. Phys. 120 (2008) 1193**

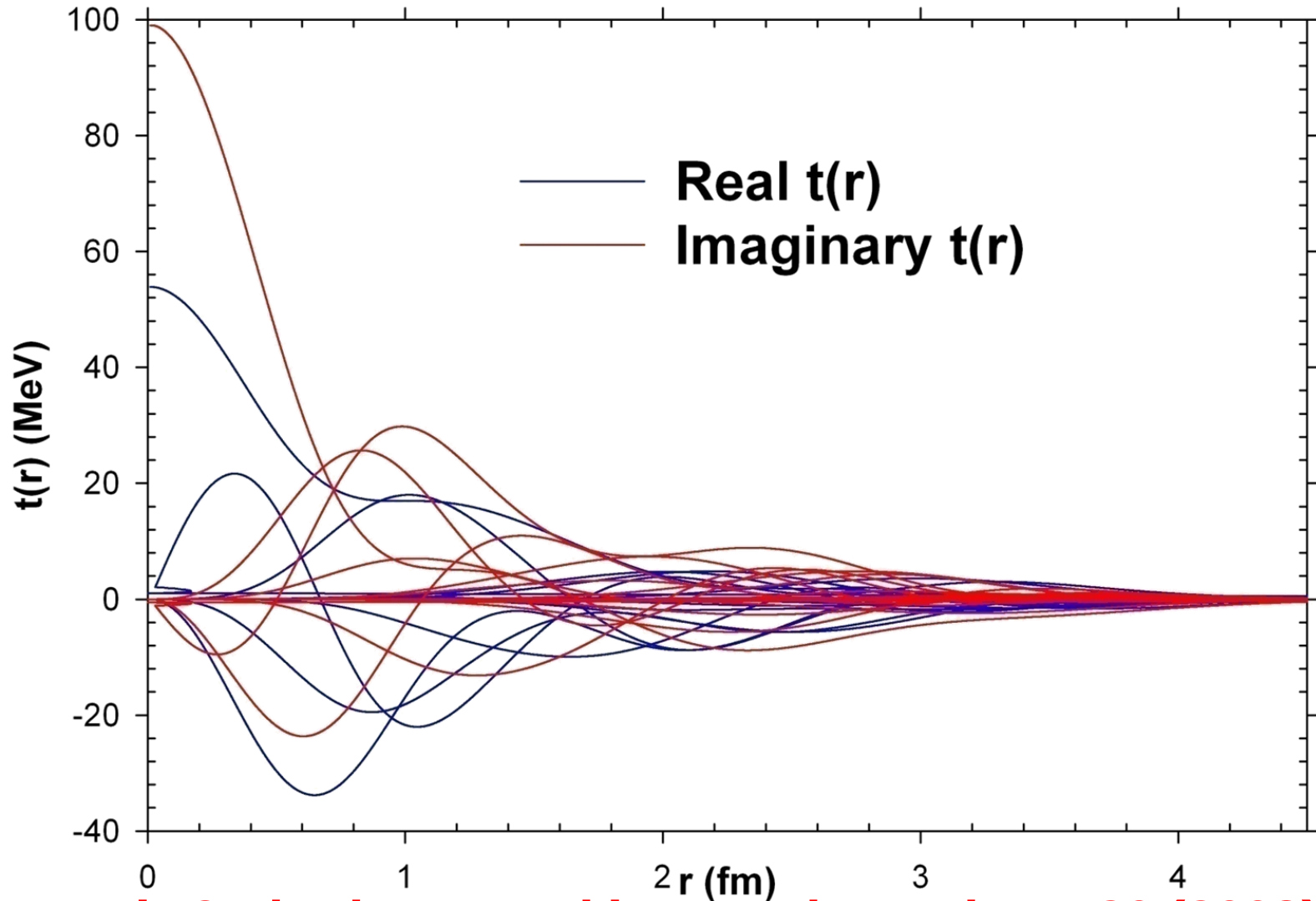
# Repulsive core + Attractive $\alpha$ - $\alpha$ t-matrix, $t\psi=V\Phi$

69 MeV (Repulsive+Attractive) t-matrix

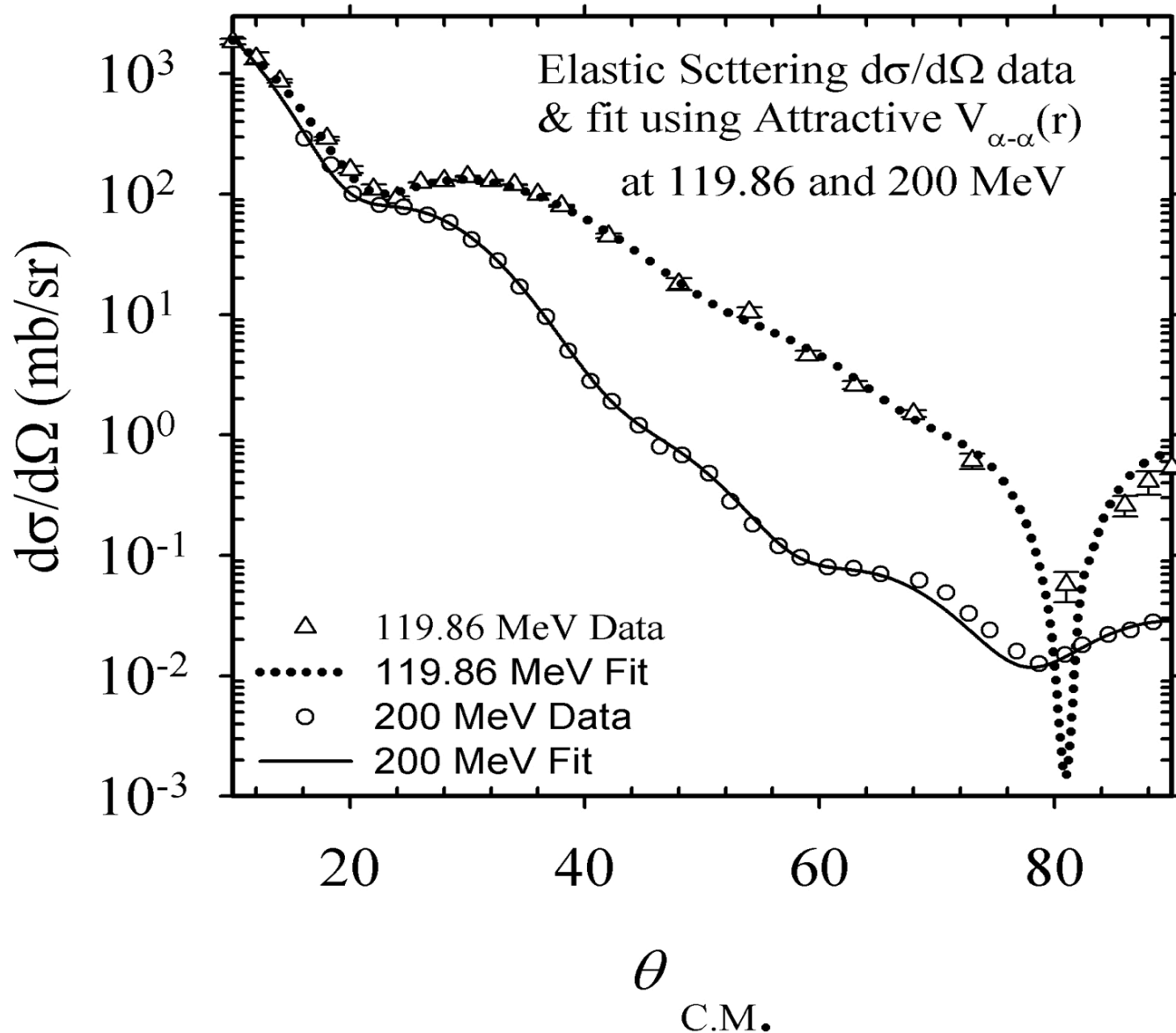


# Attractive $\alpha$ - $\alpha$ t-matrix, $t\psi=V\phi$

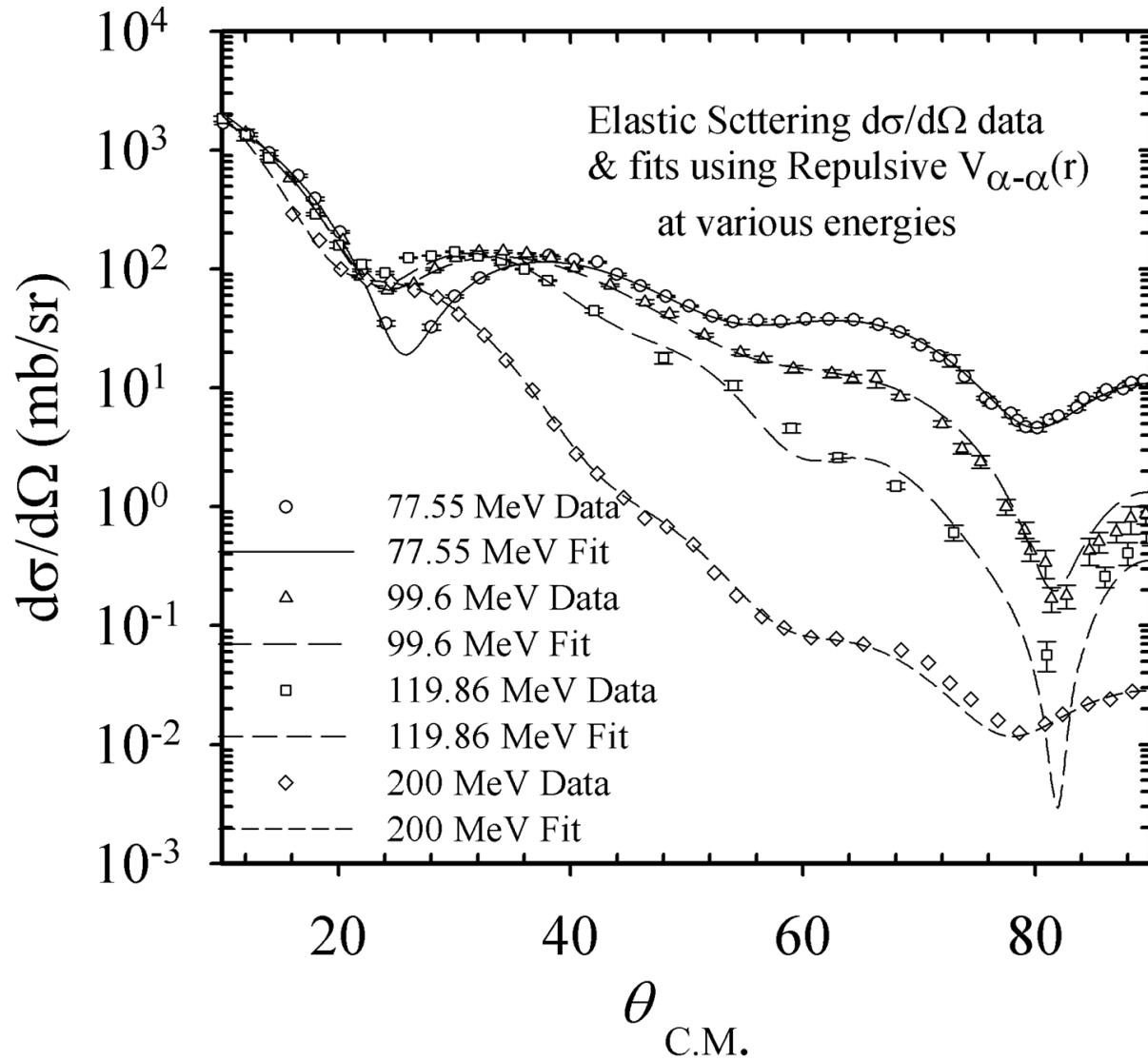
69 MeV attractive t-matrix



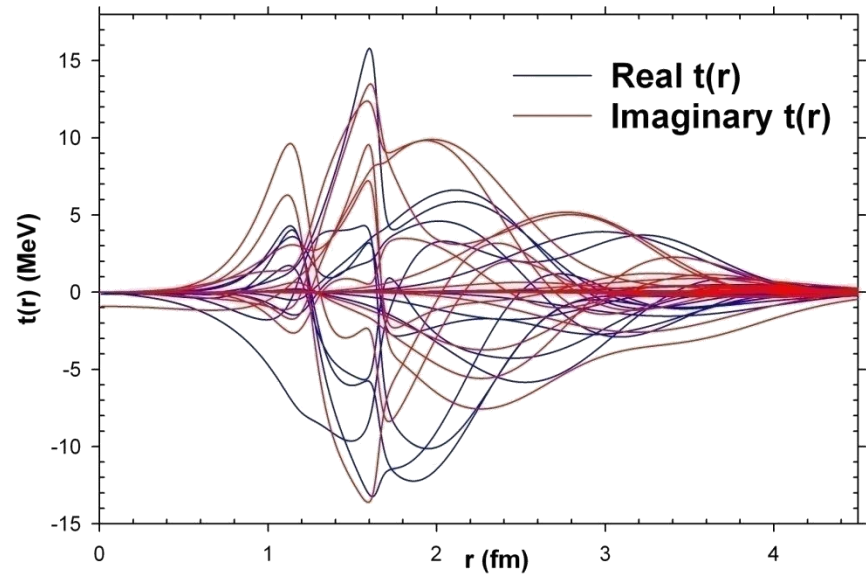
# $d\sigma/d\Omega$ from Attractive $\alpha$ - $\alpha$ potential



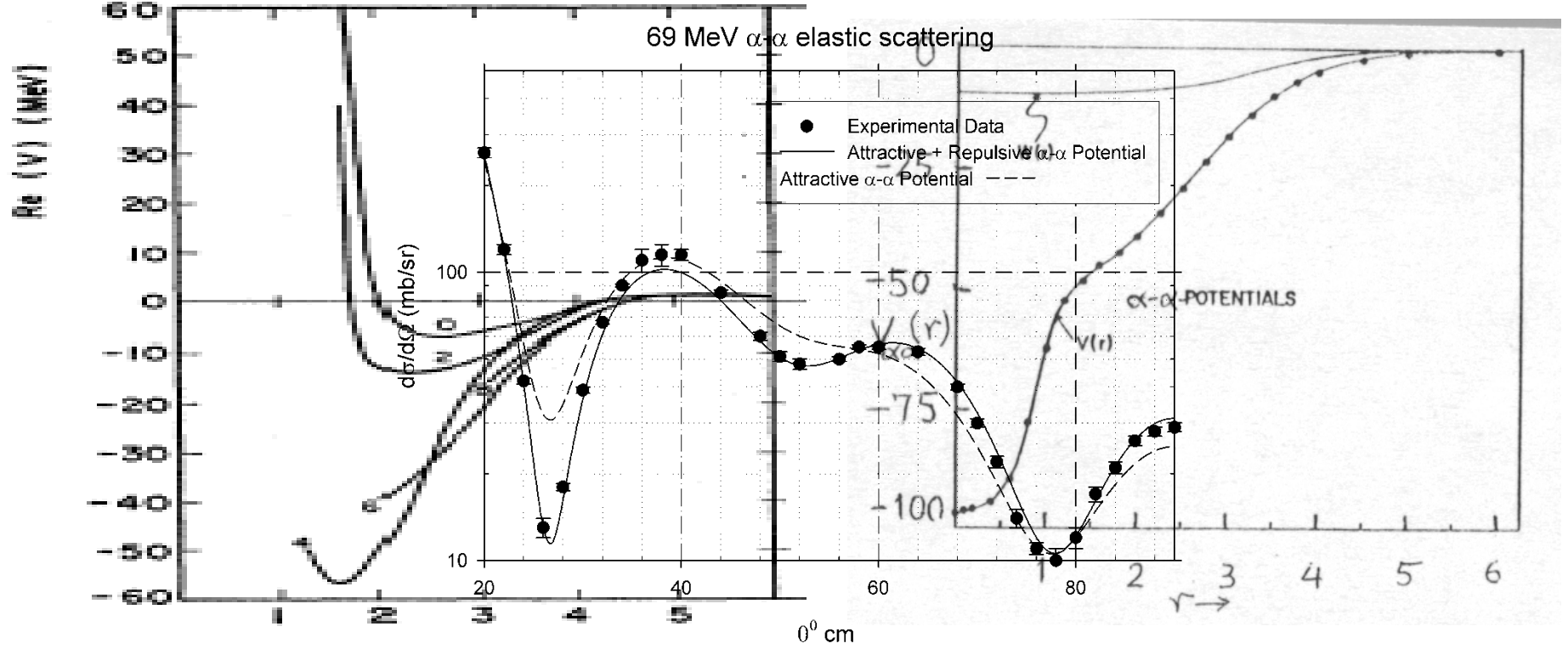
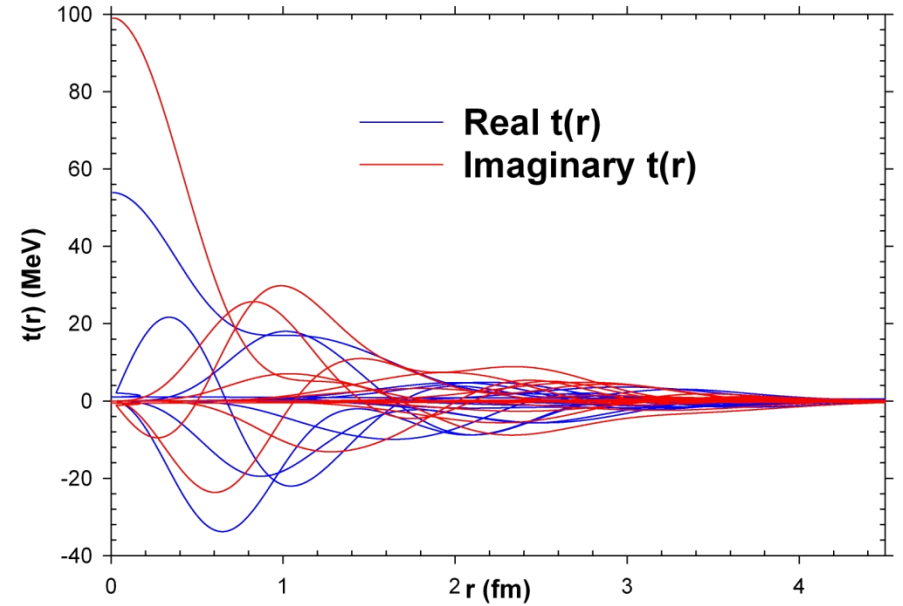
# $d\sigma/d\Omega$ from Attractive + Repulsive Core $\alpha$ - $\alpha$ Potential



69 MeV (Repulsive+Attractive) t-matrix



69 MeV attractive t-matrix



## FR DWIA A2A CODE

$$\chi_0 \longrightarrow \ell \quad (r, \theta, \varphi, R, \Theta, \Phi)$$

$$60 \quad 90, 64, 64, 22, 22, 22$$

$$\chi_1 \longrightarrow \ell \quad m \quad (r, \theta, \varphi, R, \Theta, \Phi)$$

$$60, 121 \quad 90, 64, 64, 22, 22, 22$$

$$\chi_2 \longrightarrow \ell \quad m \quad (R, \Theta, \Phi)$$

$$60, 121 \quad 22, 22, 22$$

$$\Psi(\mathbf{R}) \longrightarrow (R, \Theta, \Phi)$$

$$22, 22, 22$$

$$t_\ell(r) \longrightarrow \ell \quad (r, \theta, \varphi)$$

$$60 \quad 90, 64, 64$$

$$D_{\ell m}(\beta) \longrightarrow \ell \quad m$$

$$60, 121$$

$$64*64*90*22*22*22 = 3.9*10^9 \text{ Multiplications}$$

$$60*60*121*60*121*60*60*121 = 1.38*10^{15} \text{ Sums}$$

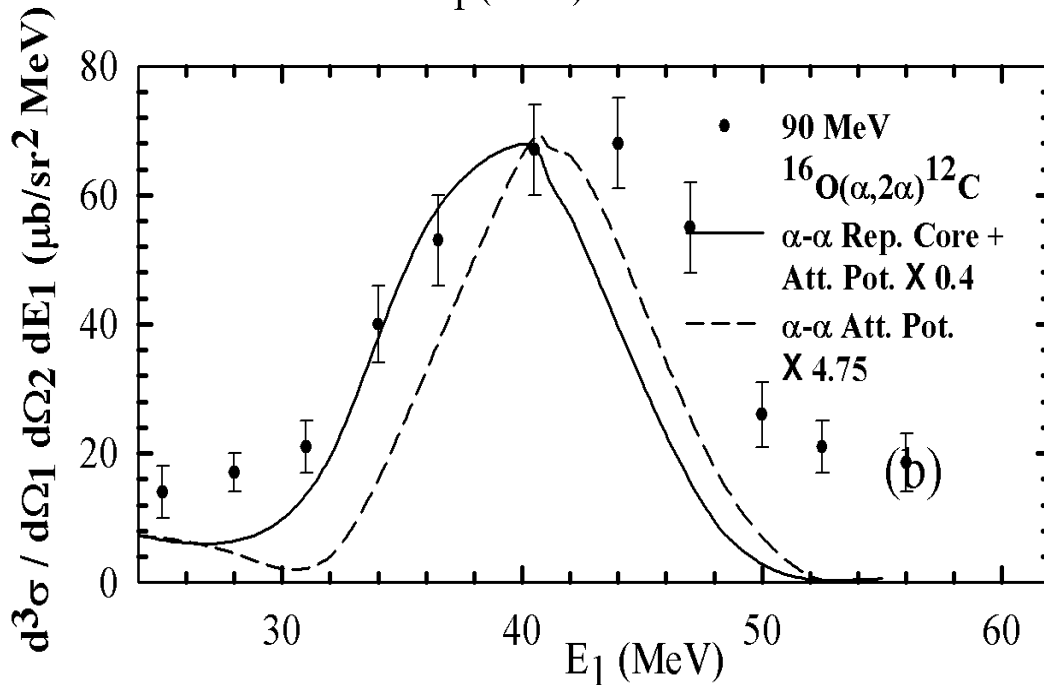
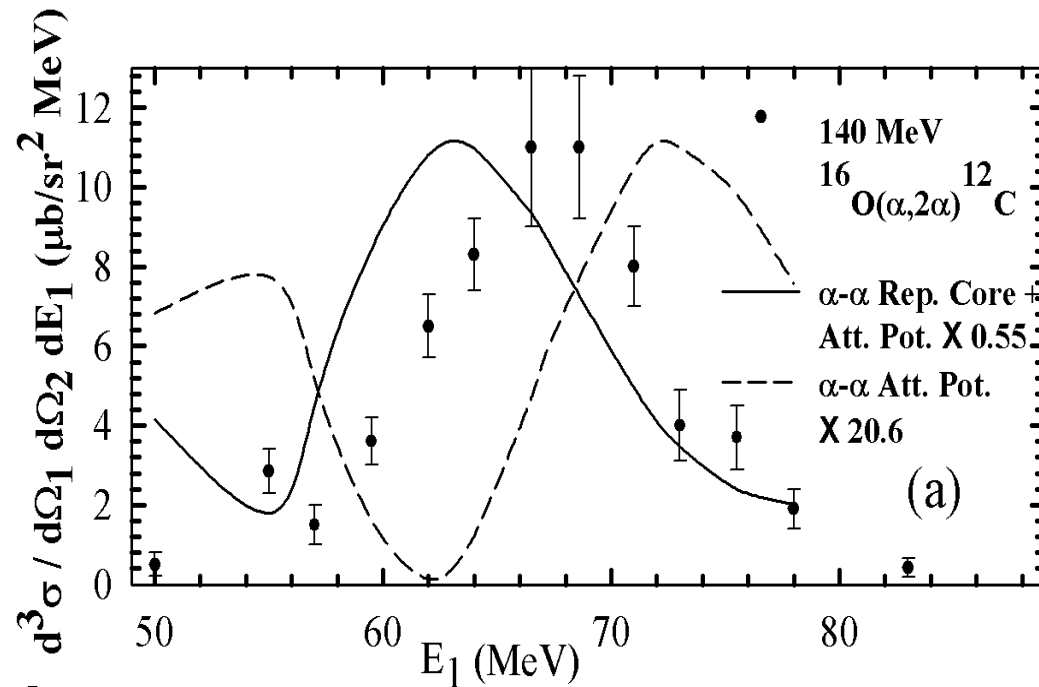


$(\alpha, 2\alpha)$  results

Arun Jain & Bhushan Joshi

**P R L, 103 (2009)132503**

140 MeV  $^{16}\text{O}(\alpha, 2\alpha)^{12}\text{C}$   
Repulsive  $\alpha$ - $\alpha$  potential  
explains the spectroscopic  
factor



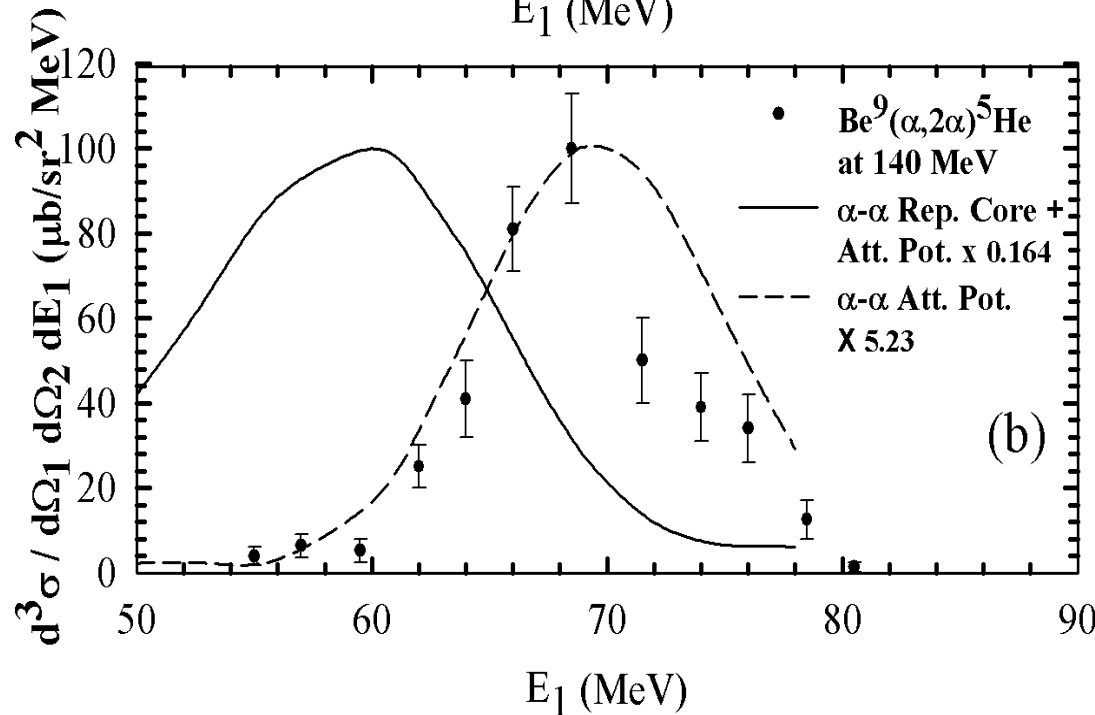
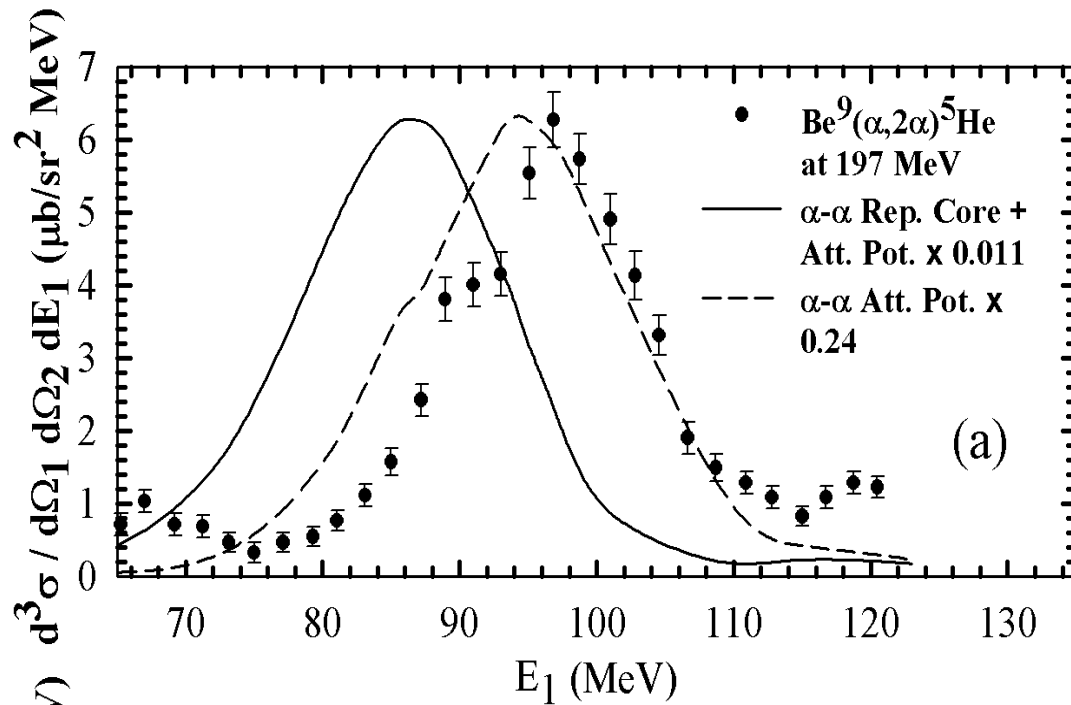
90 MeV  $^{16}\text{O}(\alpha, 2\alpha)^{12}\text{C}$   
Repulsive  $\alpha$ - $\alpha$  potential  
explains the spectroscopic  
factor

Arun Jain & Bhushan Joshi

**P R L, 103 (2009)132503**

197 MeV  ${}^9\text{Be}(\alpha, 2\alpha){}^5\text{He}$

Attractive  $\alpha$ - $\alpha$  potential  
explains the spectroscopic  
factor



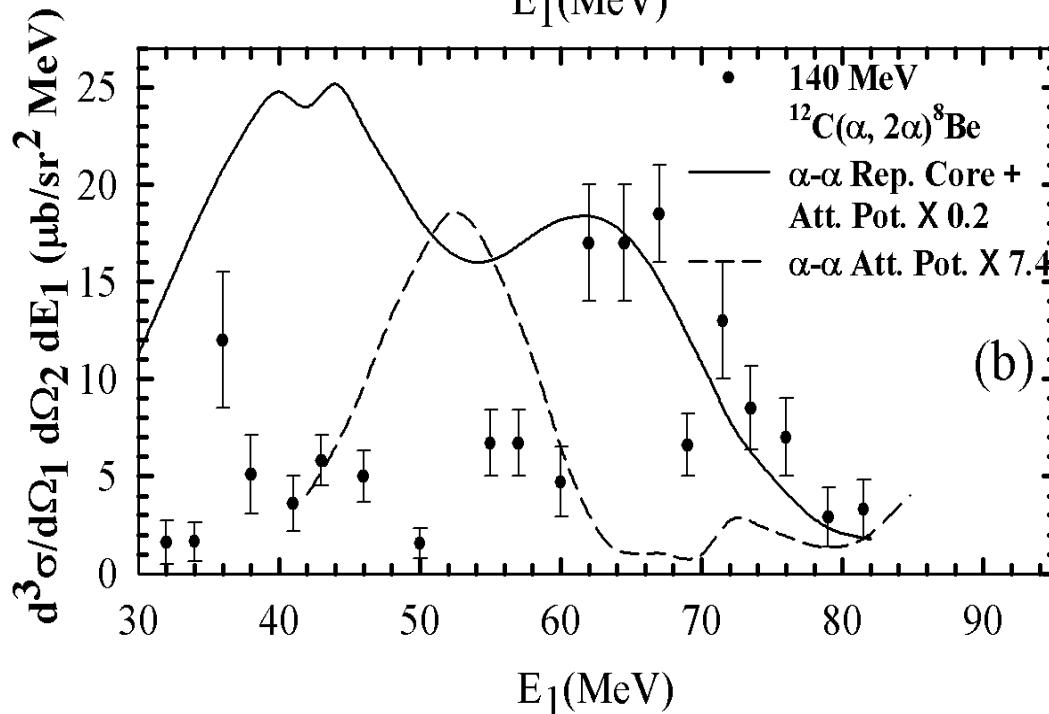
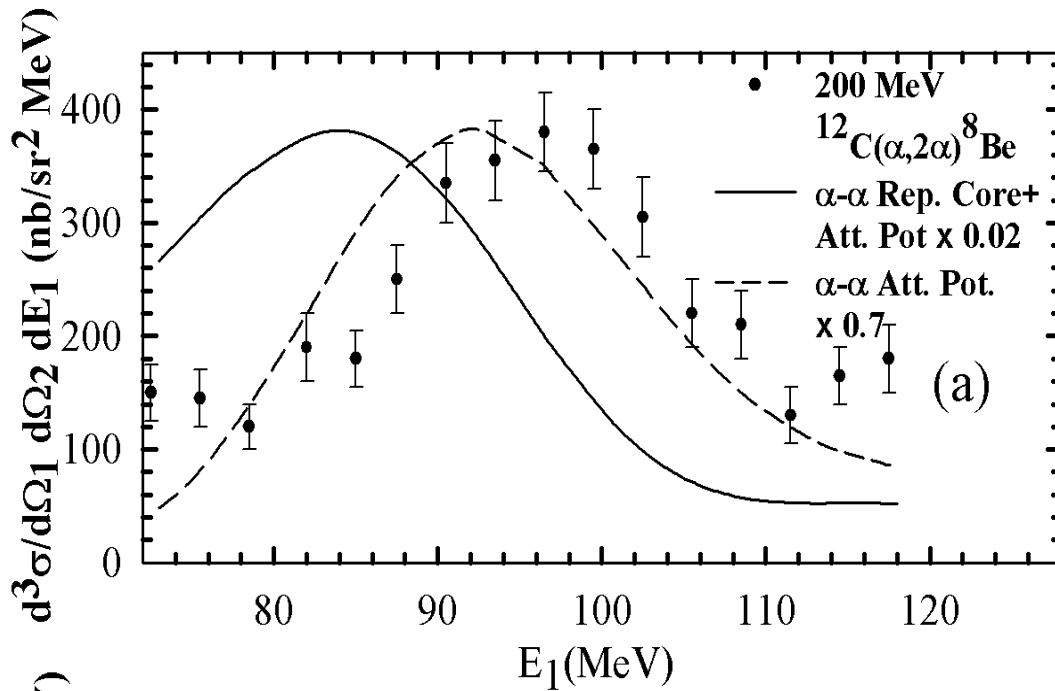
90 MeV  ${}^9\text{Be}(\alpha, 2\alpha){}^5\text{He}$

Repulsive  $\alpha$ - $\alpha$  potential  
explains the spectroscopic  
factor

Arun Jain & Bhushan Joshi

**P R L, 103 (2009)132503**

200 MeV  $^{12}\text{C}(\alpha, 2\alpha)^8\text{Be}$   
Attractive  $\alpha$ - $\alpha$  potential  
explains the spectroscopic  
factor



140 MeV  $^{12}\text{C}(\alpha, 2\alpha)^8\text{Be}$   
Repulsive  $\alpha$ - $\alpha$  potential  
explains the spectroscopic  
factor

Comparison of ( $\alpha$ , 2 $\alpha$ ) Spectroscopic factors from FR-DWIA calculations on  $^9\text{Be}$ ,  $^{12}\text{C}$ ,  $^{16}\text{O}$  nuclei at various energies

Reaction	E $\alpha$ (MeV)	S $\alpha$		
		(R+A)	(A)	Theory
$^9\text{Be}(\alpha, 2\alpha)^5\text{He}$	197	0.011	0.24	0.57
	140	0.164	5.23	
$^{12}\text{C}(\alpha, 2\alpha)^8\text{Be}$	200	0.02	0.7	0.55, 0.29
	140	0.2	7.4	
$^{16}\text{O}(\alpha, 2\alpha)^{12}\text{C}$	140	0.55	20.6	0.23, 0.3
	90	0.4	4.75	

**Arun Jain & Bhushan Joshi, P R L, 103 (2009) 132503**

## Understanding:-

In the shell model picture the two  $\alpha$ 's can not physically overlap unless their nucleonic wave functions satisfy Pauli Principle.

Which means that their shell model single particle orbitals are to be occupied by the second set of 2-neutrons and 2-protons with their single particle 1s -1p energy gap. Which can be seen in the excitation of  $\alpha$  -particle at  $\sim 20$  MeV.

4-particles of the other alpha to be promoted to this level require an excitation of  $\sim 80$  MeV.

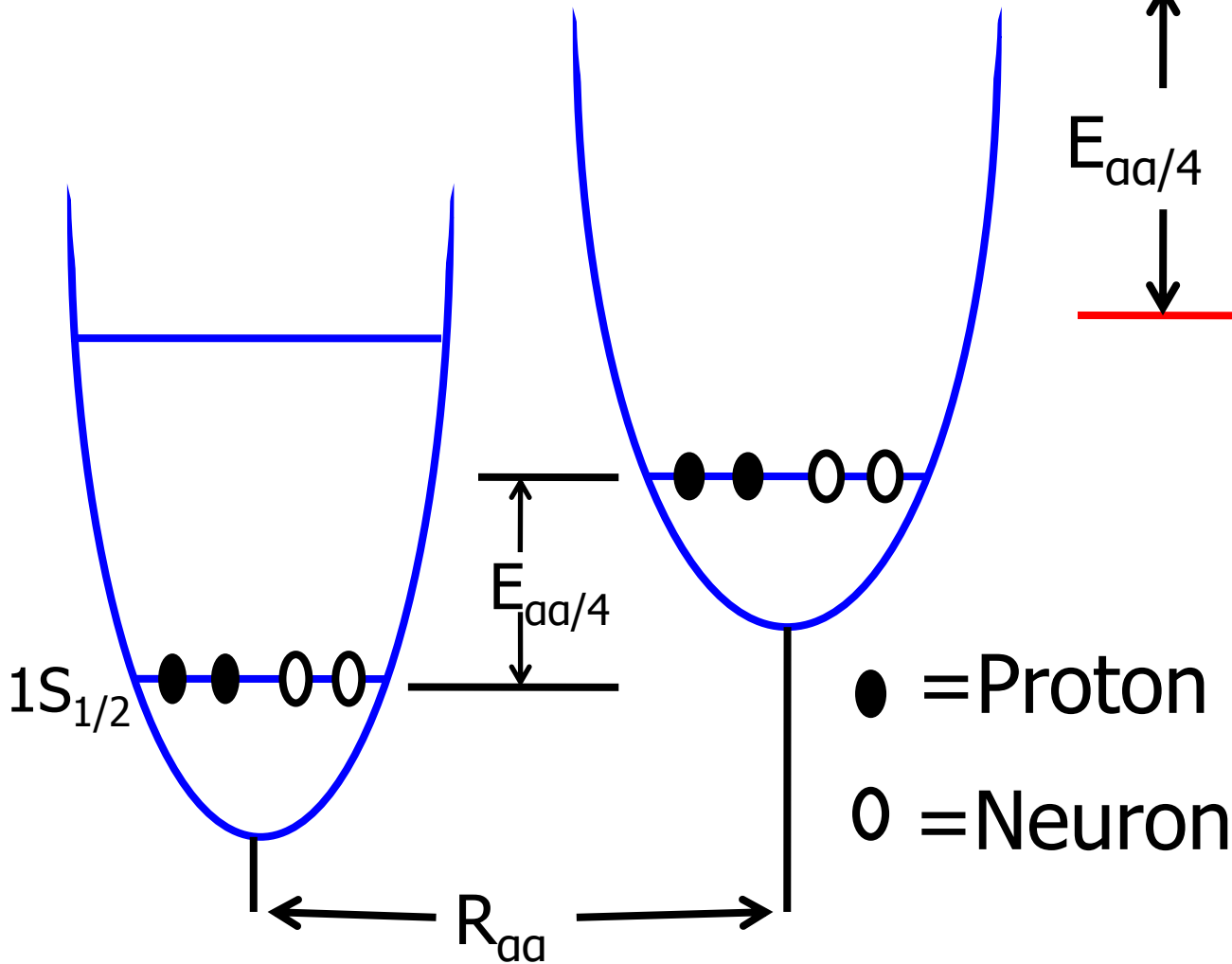
In the  $\alpha$  -  $\alpha$  lab system it will be  $\sim 160$  MeV.

Thus the two  $\alpha$ 's repel each other below this lab energy.

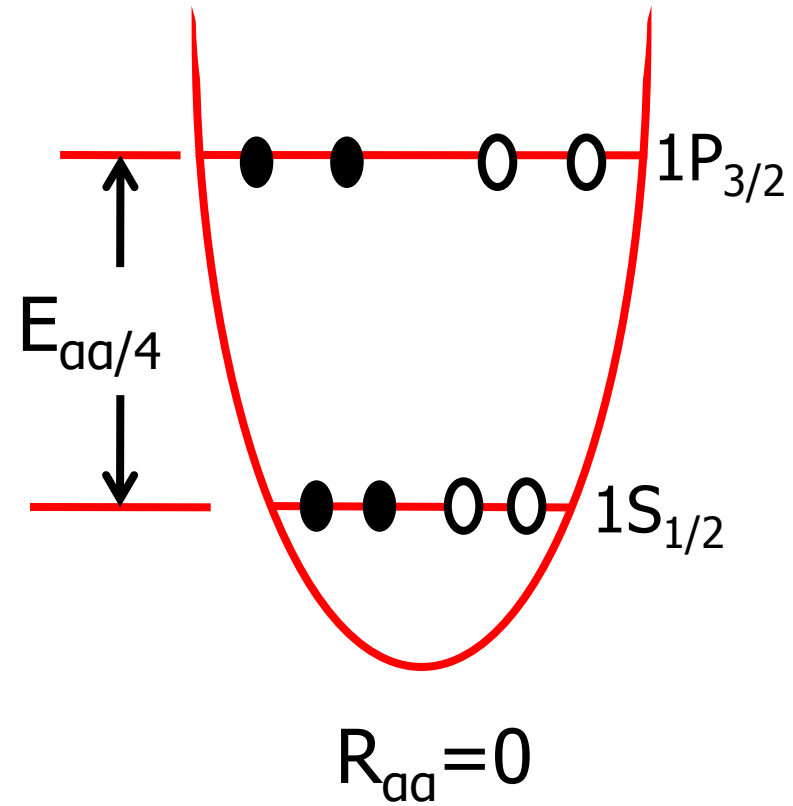
❖ ***Thus we have achieved an explanation of most of the puzzling features of the Direct Nuclear Reactions.***

# Explanation of $\alpha$ - $\alpha$ potential in RGM - Shell Model picture

$\alpha$ - $\alpha$  Repulsive Core + Attractive Potential



$\alpha$ - $\alpha$  Attractive Potential



# Heavy Cluster Knockout



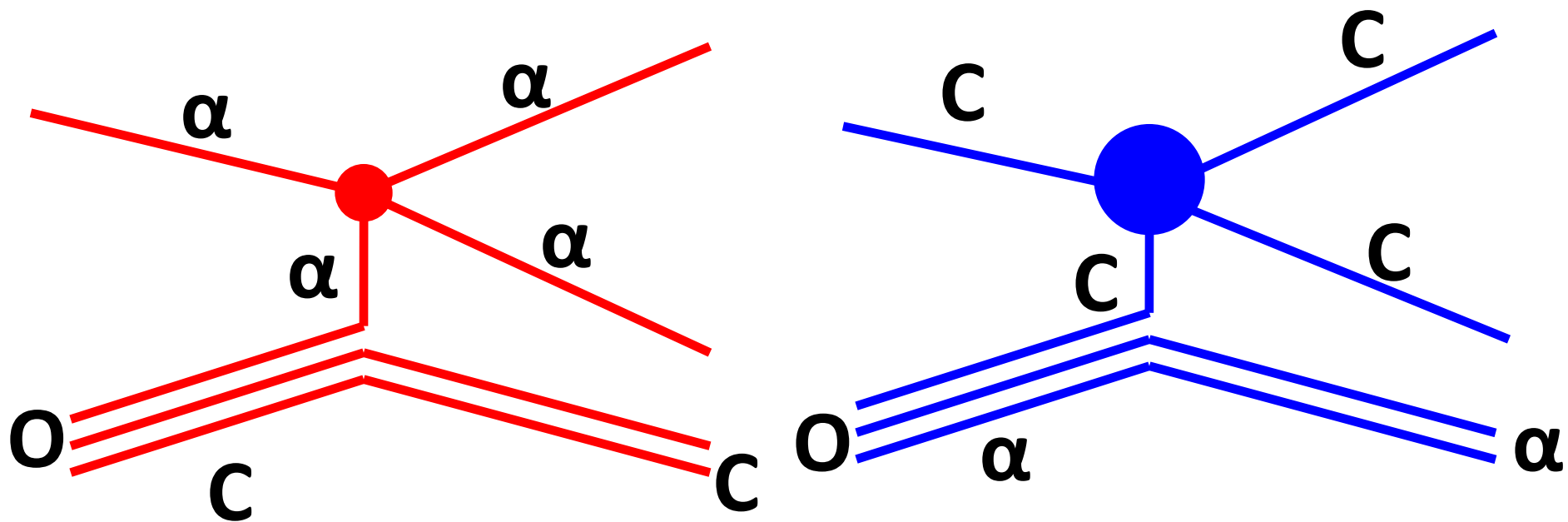
$(\alpha, 2\alpha)$



$(C, 2C)$



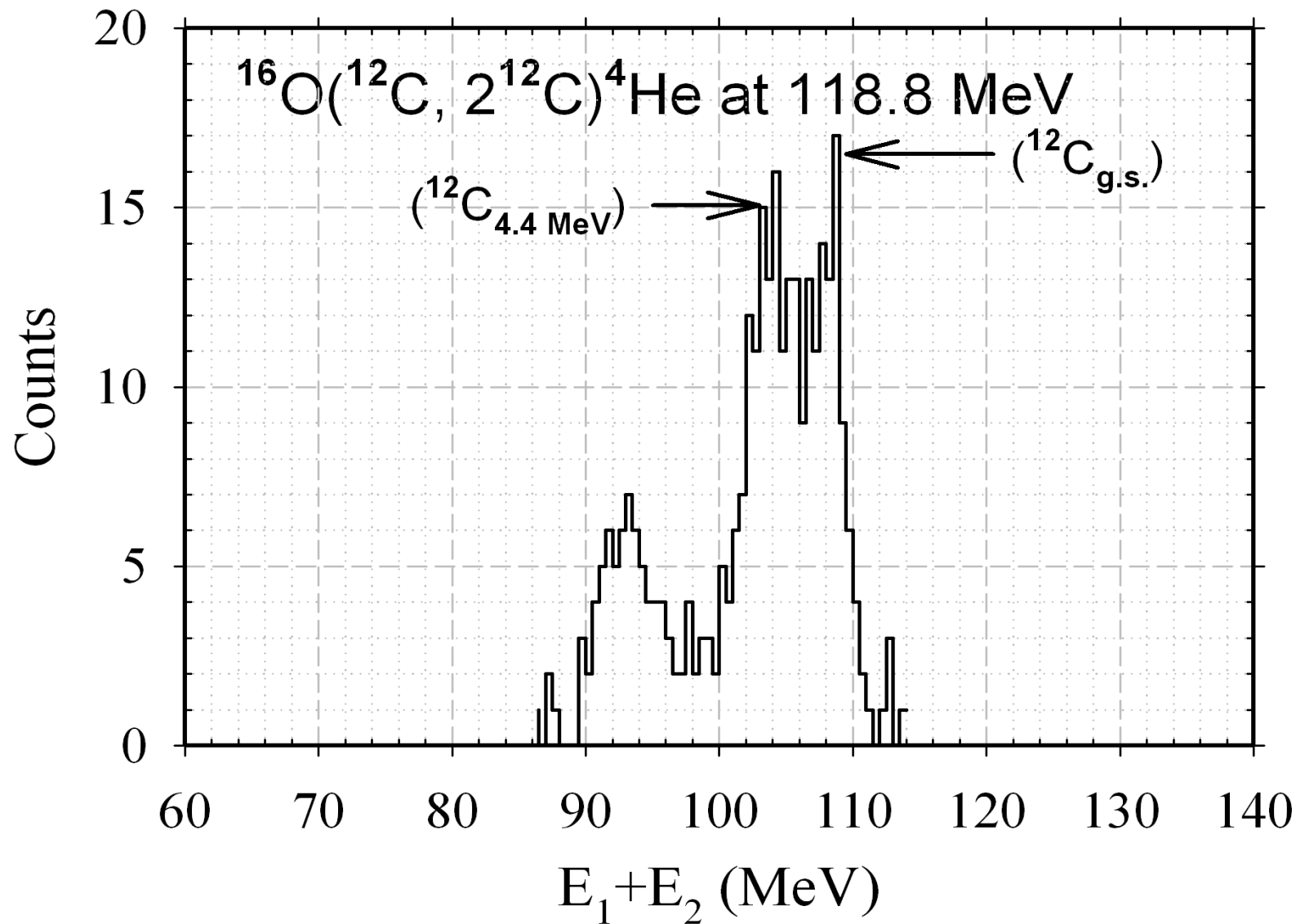
Comparison of  
 $^{16}\text{O} (\alpha, 2\alpha) ^{12}\text{C}$  and  $^{16}\text{O} (^{12}\text{C}, 2^{12}\text{C}) ^4\text{He}$



$^{16}\text{O}(\text{C}, 2\text{C})\alpha$  was performed at Mumbai LINAC-Pelletron at  $E_C=119$  MeV

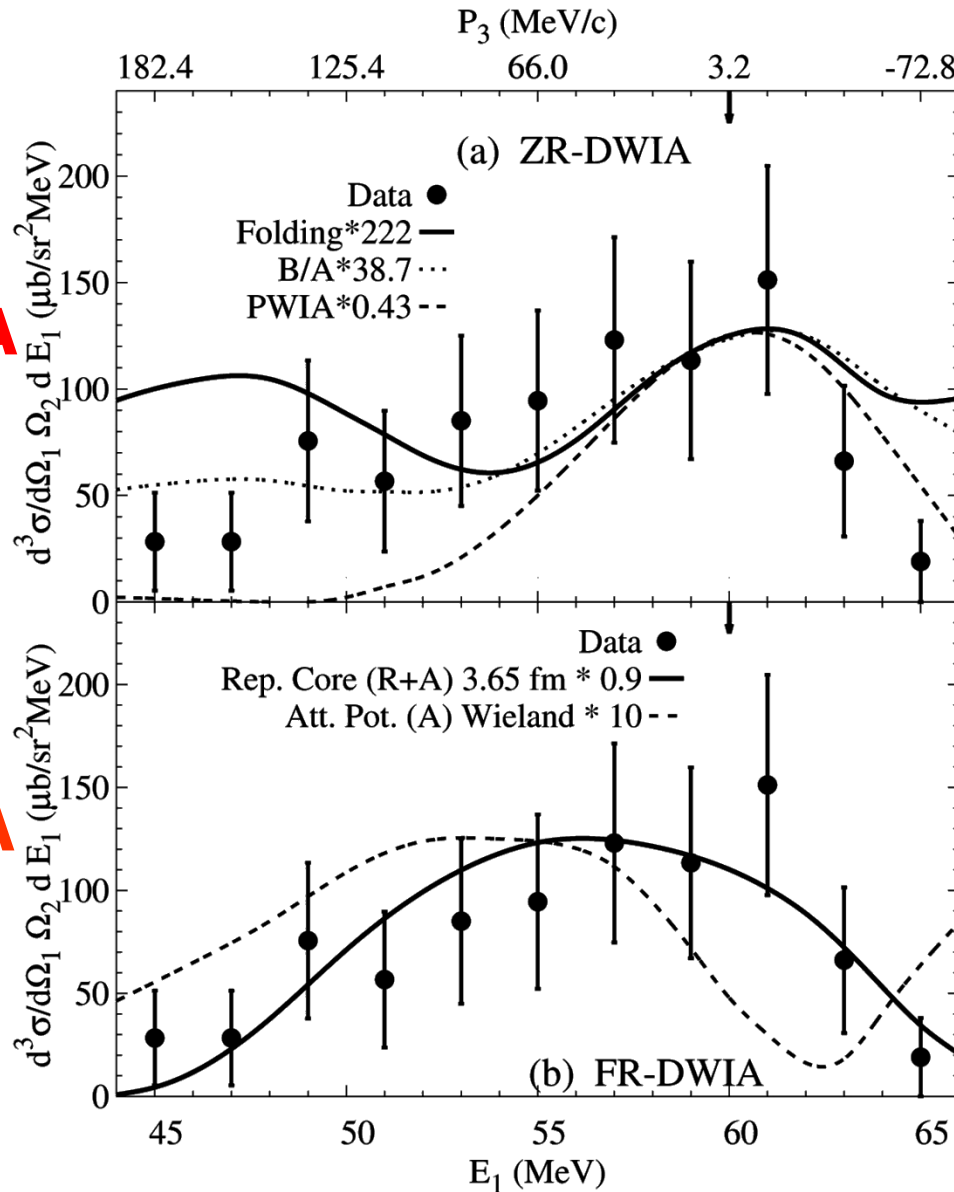
# Summed energy spectrum for the $^{16}\text{O}(^{12}\text{C}, 2^{12}\text{C})^4\text{He}$ Reaction

**Bhushan Joshi *et al*, P R L 106 (2011) 022501**



# Comparison of Theory and Experiment: energy sharing distribution for 119 MeV $^{16}\text{O}(\text{C}, 2\text{C})^4\text{He}$ Reaction:-

**ZR-DWIA**



**FR-DWIA**

Bhushan Joshi,  
 Arun Jain, Y. K. Gupta,  
 D. C. Biswas, A. Saxena  
 B. V. John, L. S. Danu,  
 R. P. Vind and  
 R. K. Choudhury

**P R L 106 (2011)**

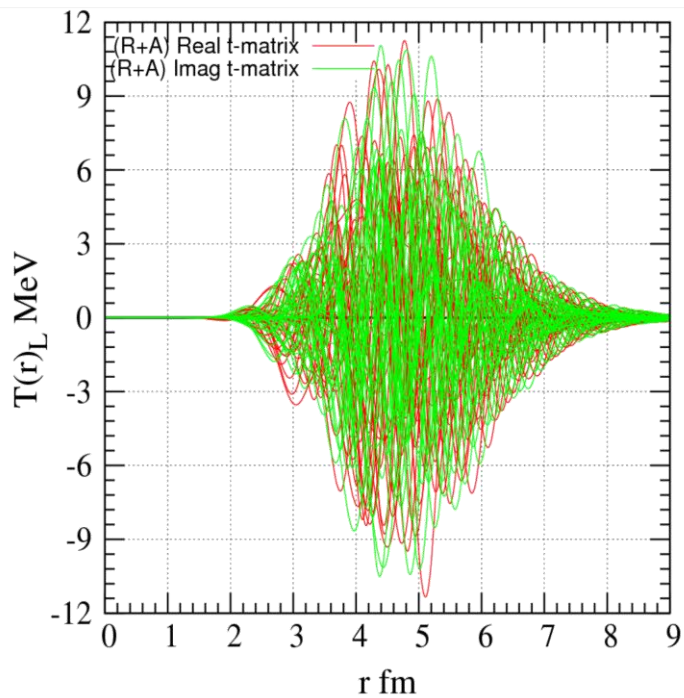
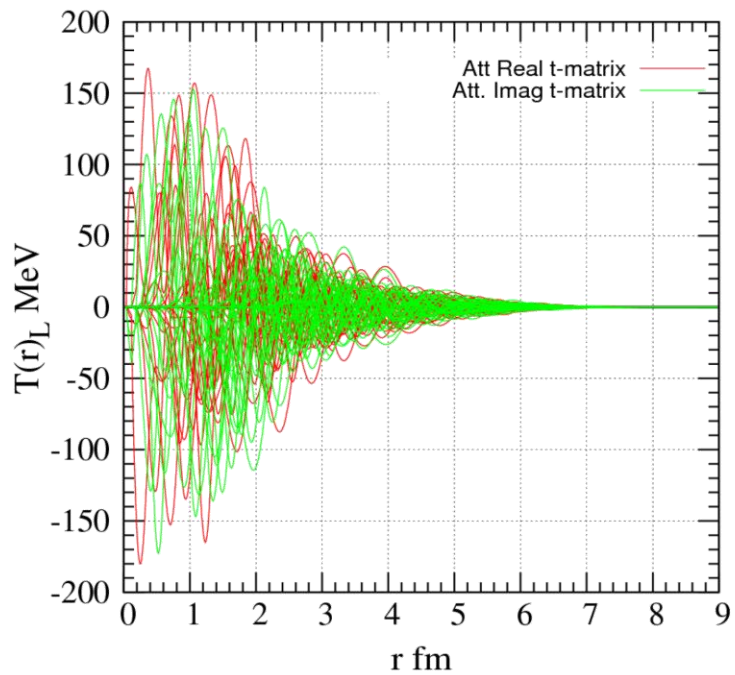
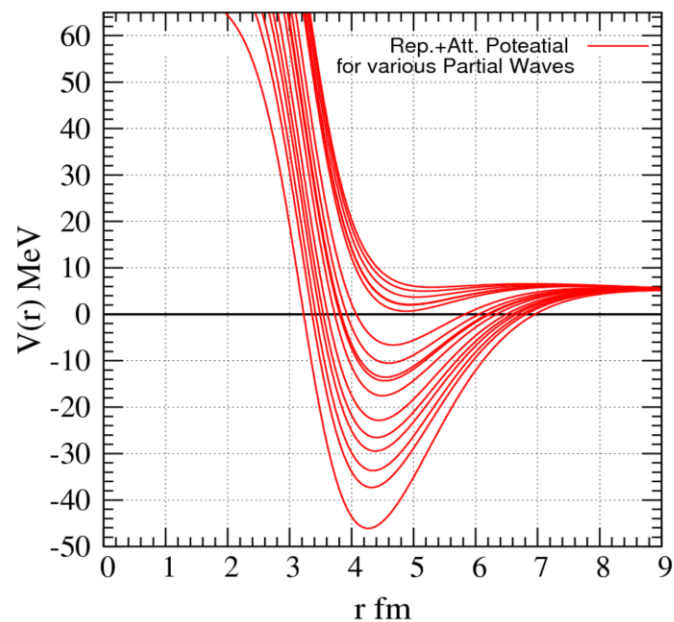
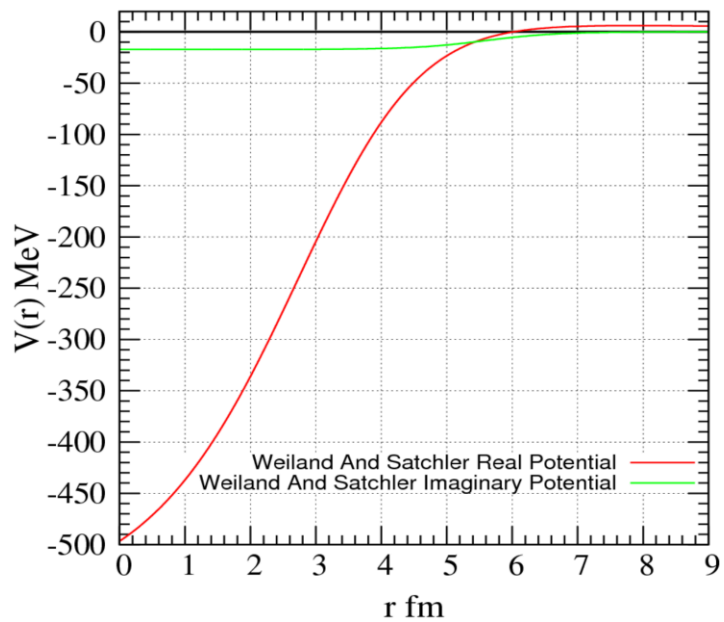
**022501**

# Comparison of the $(\alpha, 2\alpha)$ and $(C, 2C)$ reactions on $^{16}\text{O}$

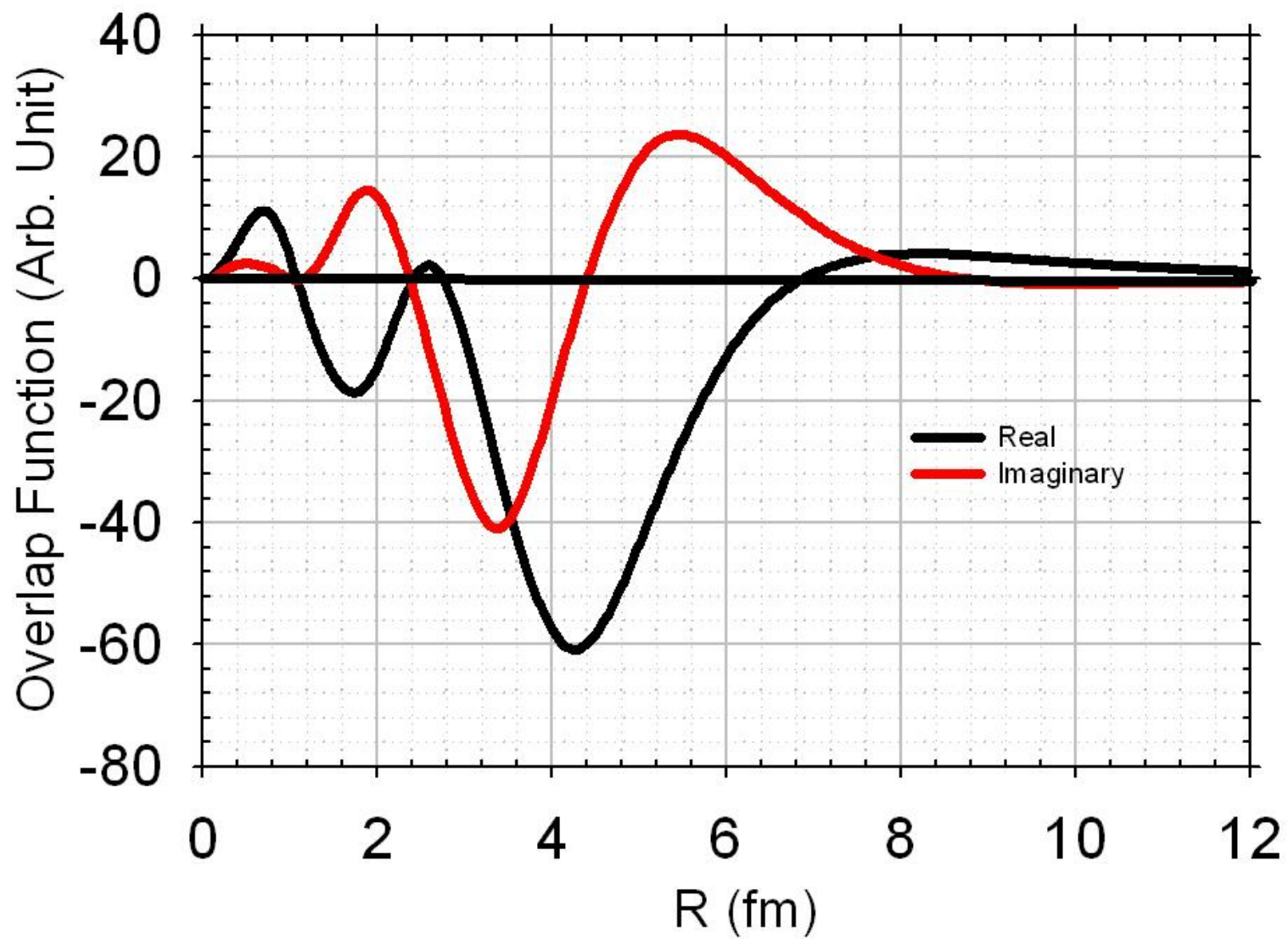
Projectile Energy (MeV)	Reaction	Exptl. X-Section $\mu\text{b}/\text{sr}^2 \text{ MeV}$	ZR-DWIA X-Section $\mu\text{b}/\text{sr}^2 \text{ MeV}$	$S_\alpha$ ZR-DWIA	FR-DWIA X-Section $\mu\text{b}/\text{sr}^2 \text{ MeV}$		$S_\alpha$ FR-DWIA		Theory
					A	R+A	A	R+A	
140	$^{16}\text{O}(\alpha, 2\alpha)^{12}\text{C}$	10.5	0.96	11	0.51	19.1	20.6	0.55	0.23
119	$^{16}\text{O}(\text{C}, 2\text{C})\alpha$	125±50	0.56	222	12.5	138	10	0.9	0.23

Comparison of  $S_\alpha$  (ZR-DWIA) indicates an enhancement of **20** times more in  $(\text{C}, 2\text{C})$  case as compared to  $(\alpha, 2\alpha)$  case

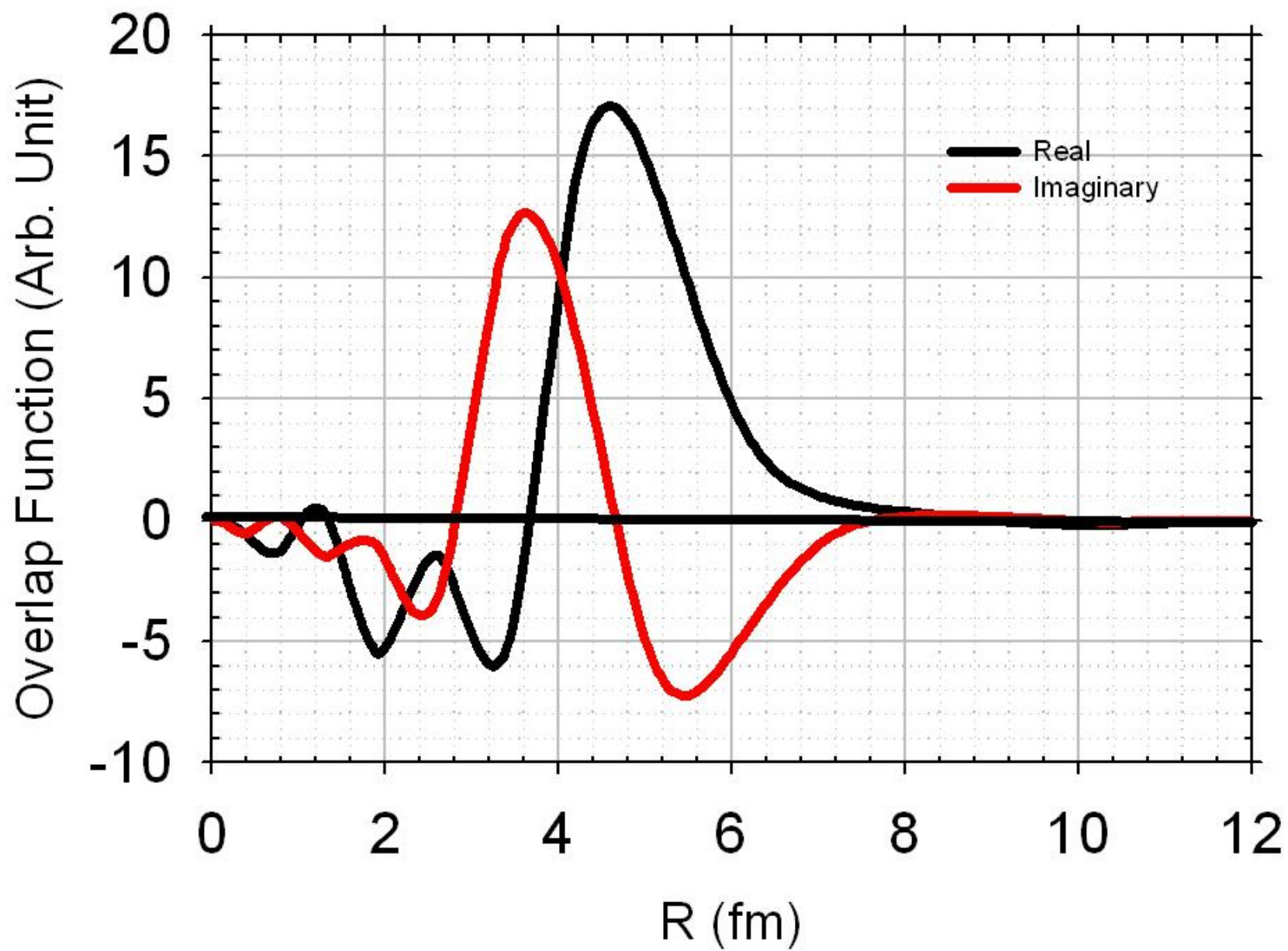
A comparison of  $S_\alpha$  (ZR-DWIA) with theory indicates an enhancement of **965** times in the  $(\text{C}, 2\text{C})$  case



${}^9\text{Be}(\alpha, 2\alpha){}^5\text{He}$  at 140 MeV

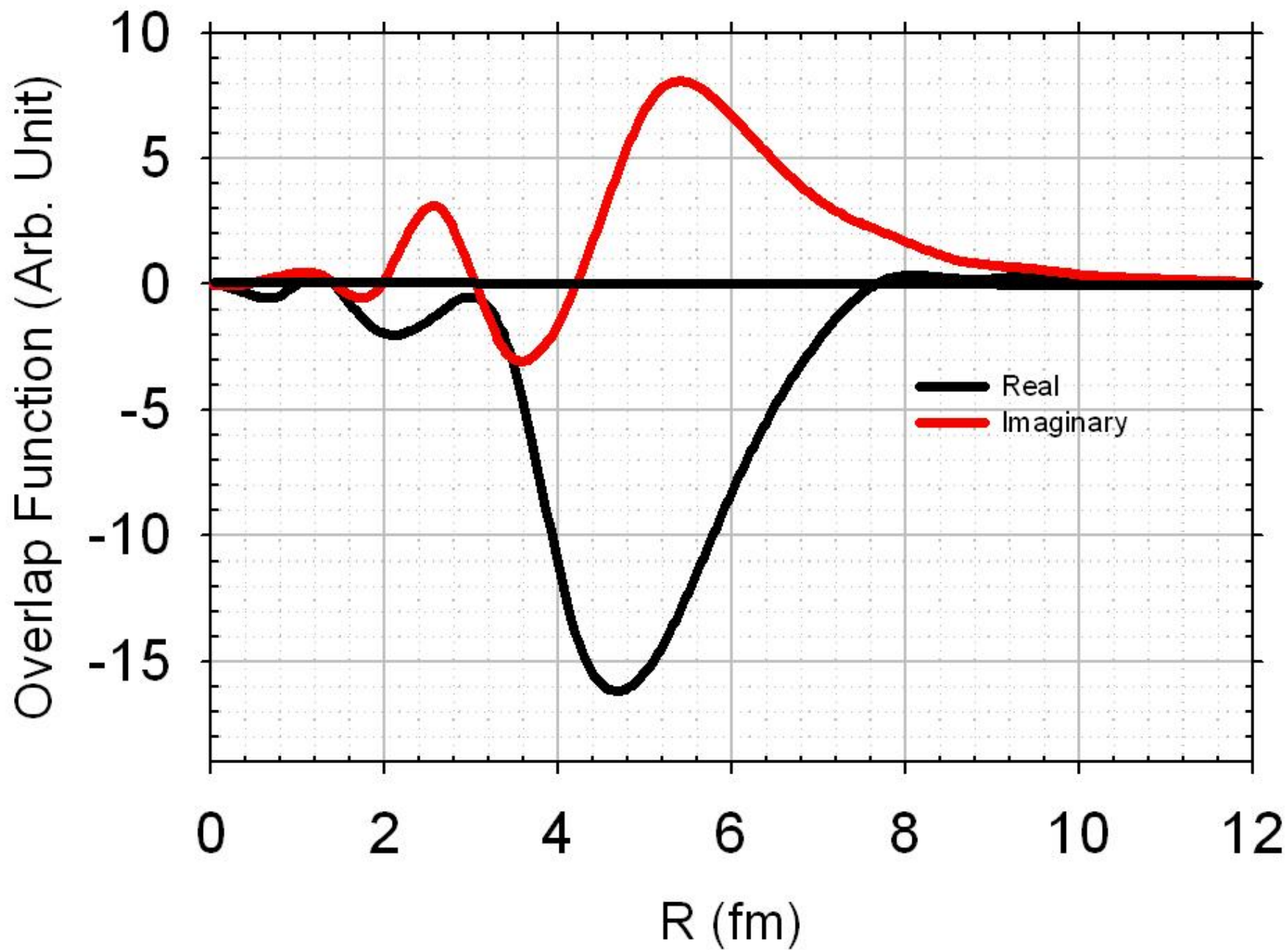


$^{16}\text{O}(\alpha, 2\alpha)^{12}\text{C}$  at 140 MeV



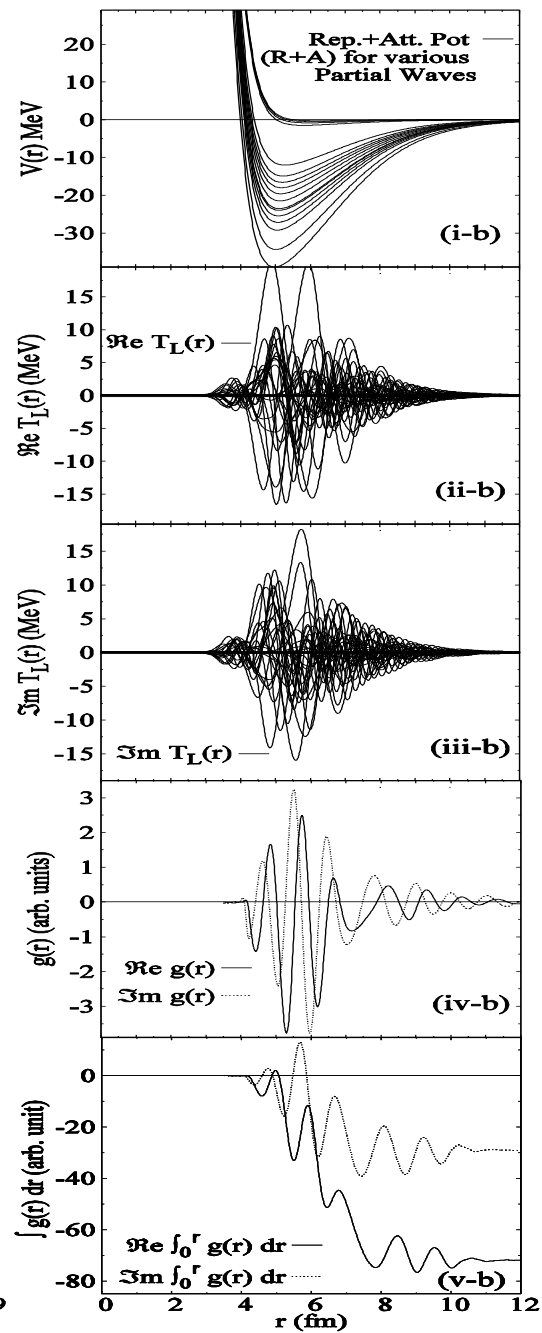
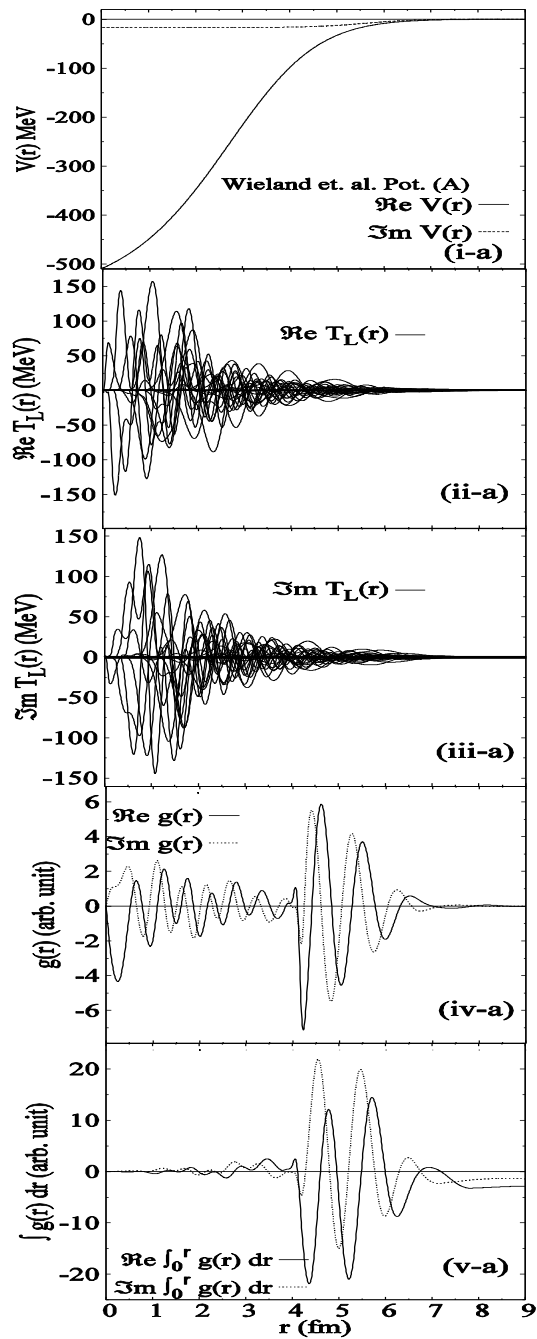


$^{16}\text{O}(\text{C}, 2\text{C})^4\text{He}$  at 118 MeV

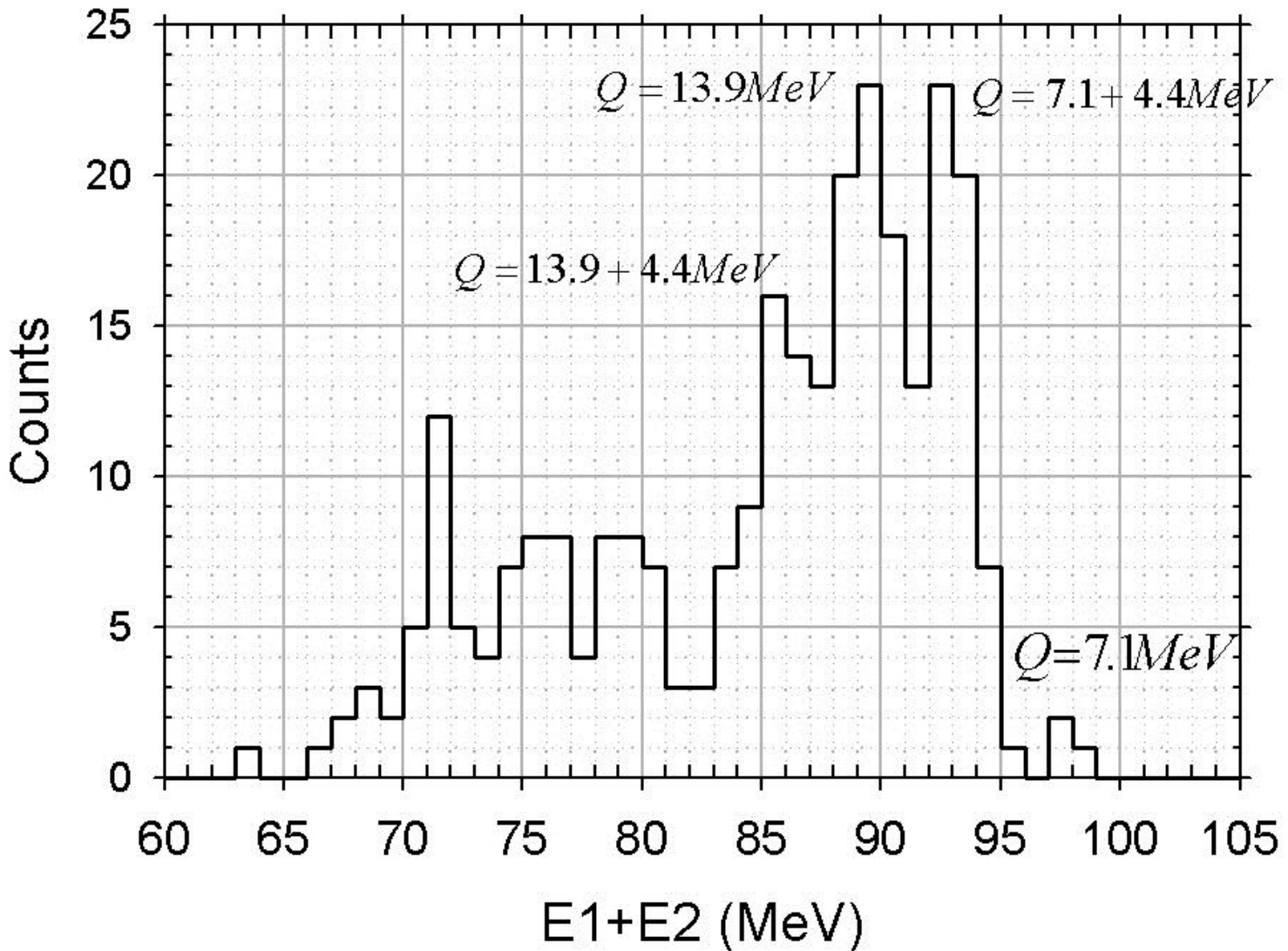


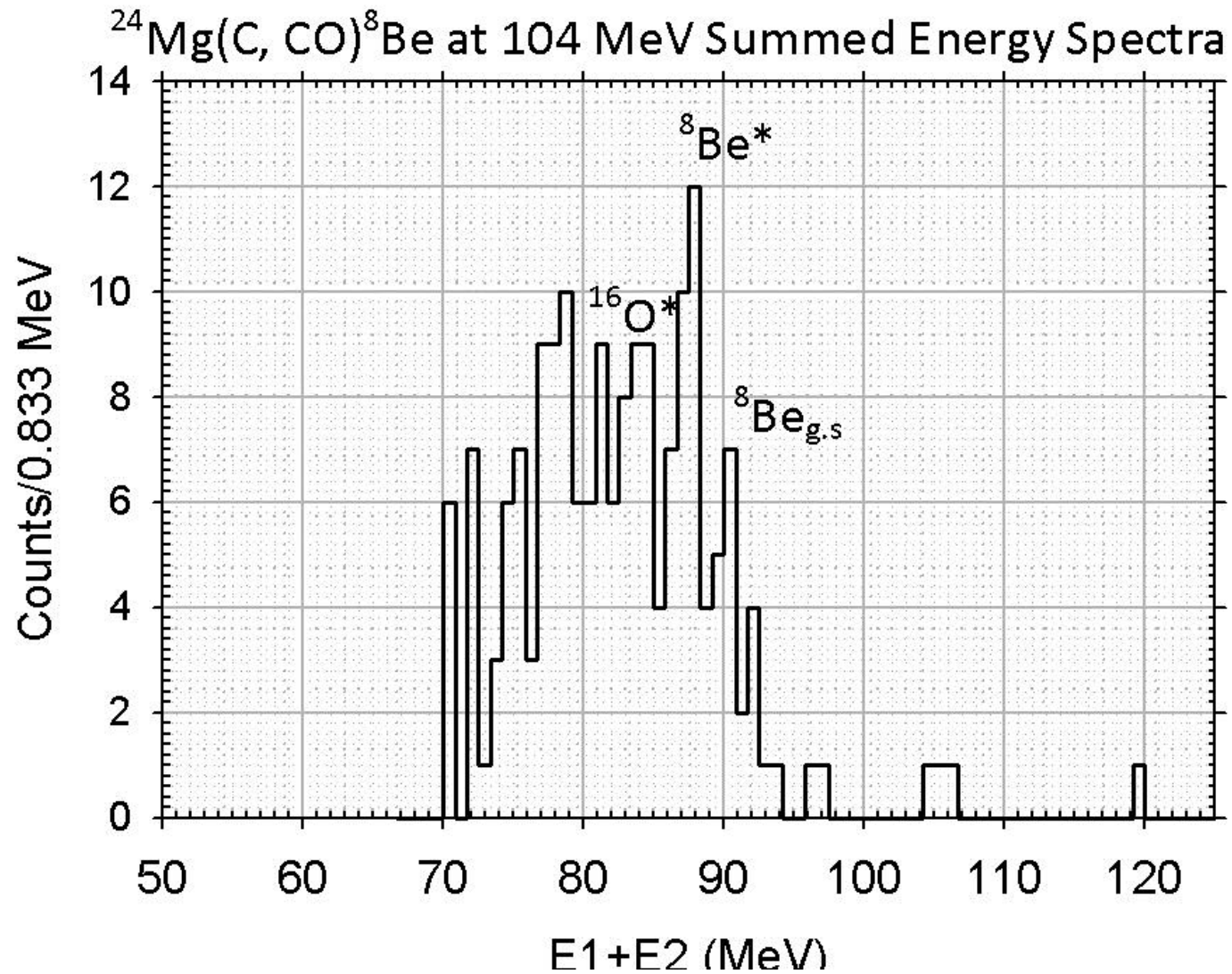
$$T_{fi}^{\alpha L\Lambda}(\vec{k}_f, \vec{k}_i) = \int g(r) dr$$

$$= \int \chi_1^{(-)*}(\vec{k}_{aB}, \vec{r}_{aB}) \chi_2^{(-)*}(\vec{k}_{2B}, \vec{R}_{2B}) t_{12}(\vec{r}_{12}) \chi_0^{(+)}(\vec{k}_{1A}, \vec{r}_{1A}) \varphi_{L\Lambda}(\vec{R}_{2B}) d\vec{r}_{12} d\vec{R}_{2B}$$

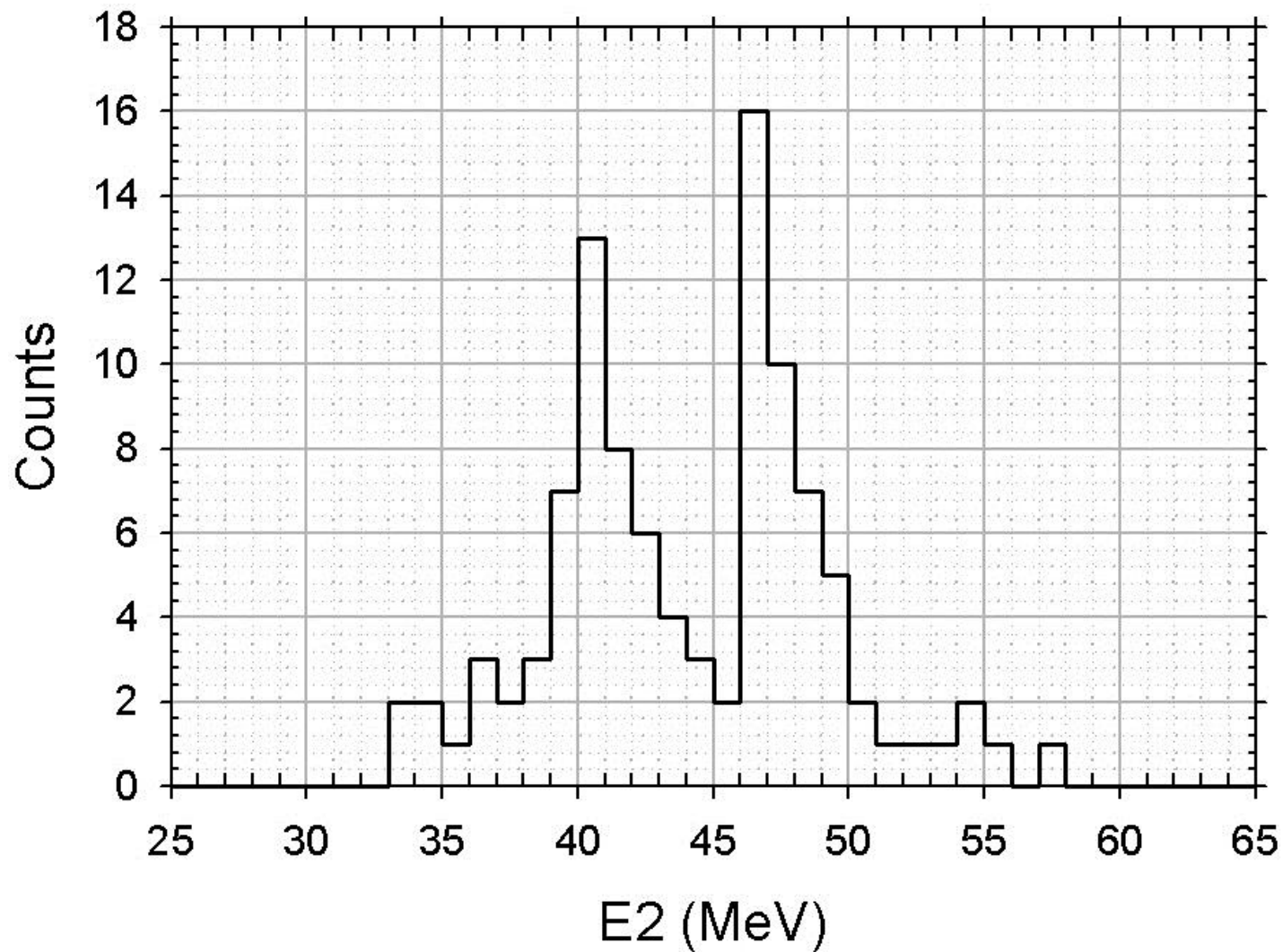


Summed Energy Spectrum of  $^{24}\text{Mg}(^{12}\text{C}, 2^{12}\text{C})^{12}\text{C}$  at 104 MeV.  
 $Q=13.9$  MeV at coplanar symmetric angle of  $40.5^\circ$

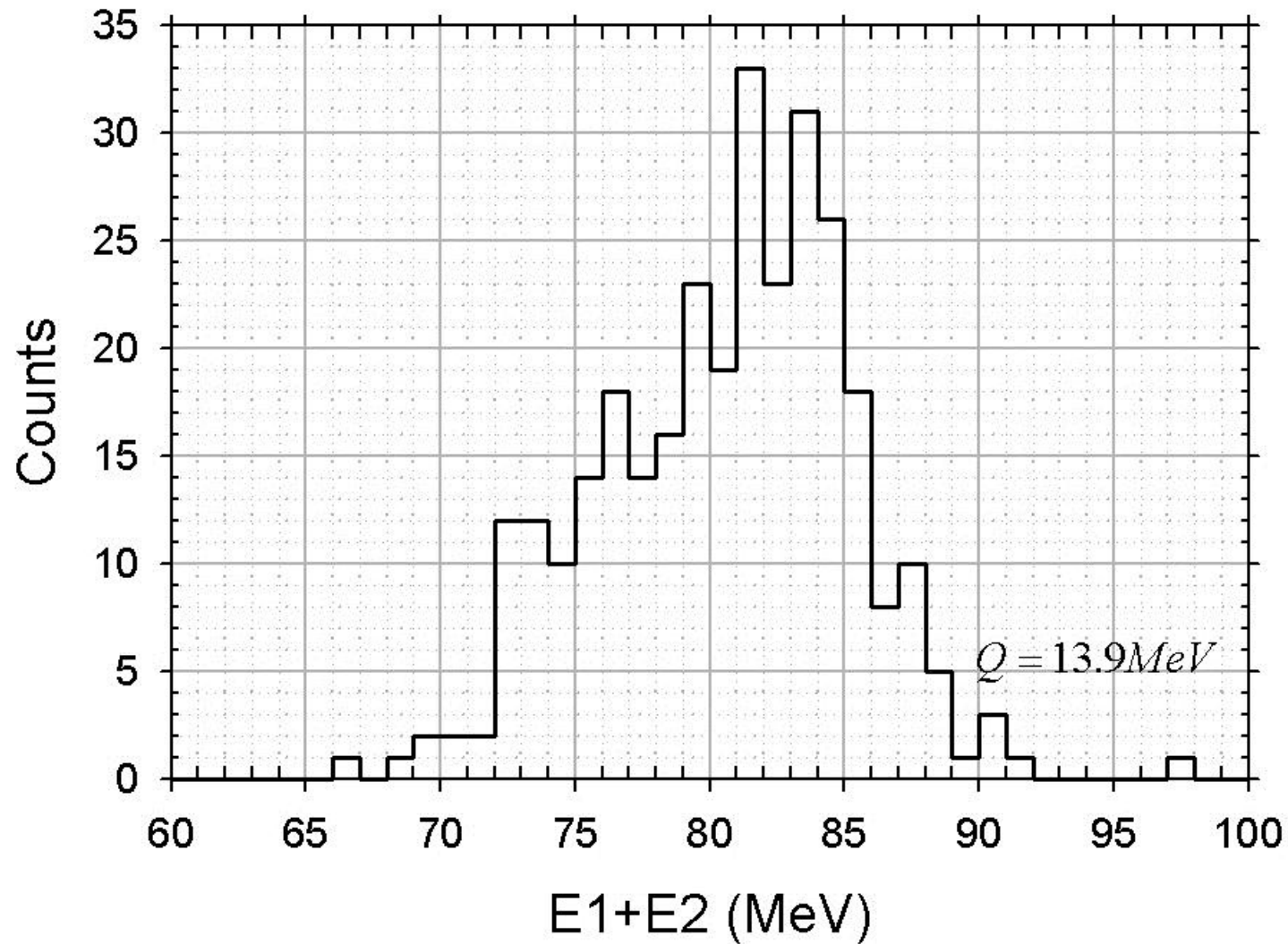




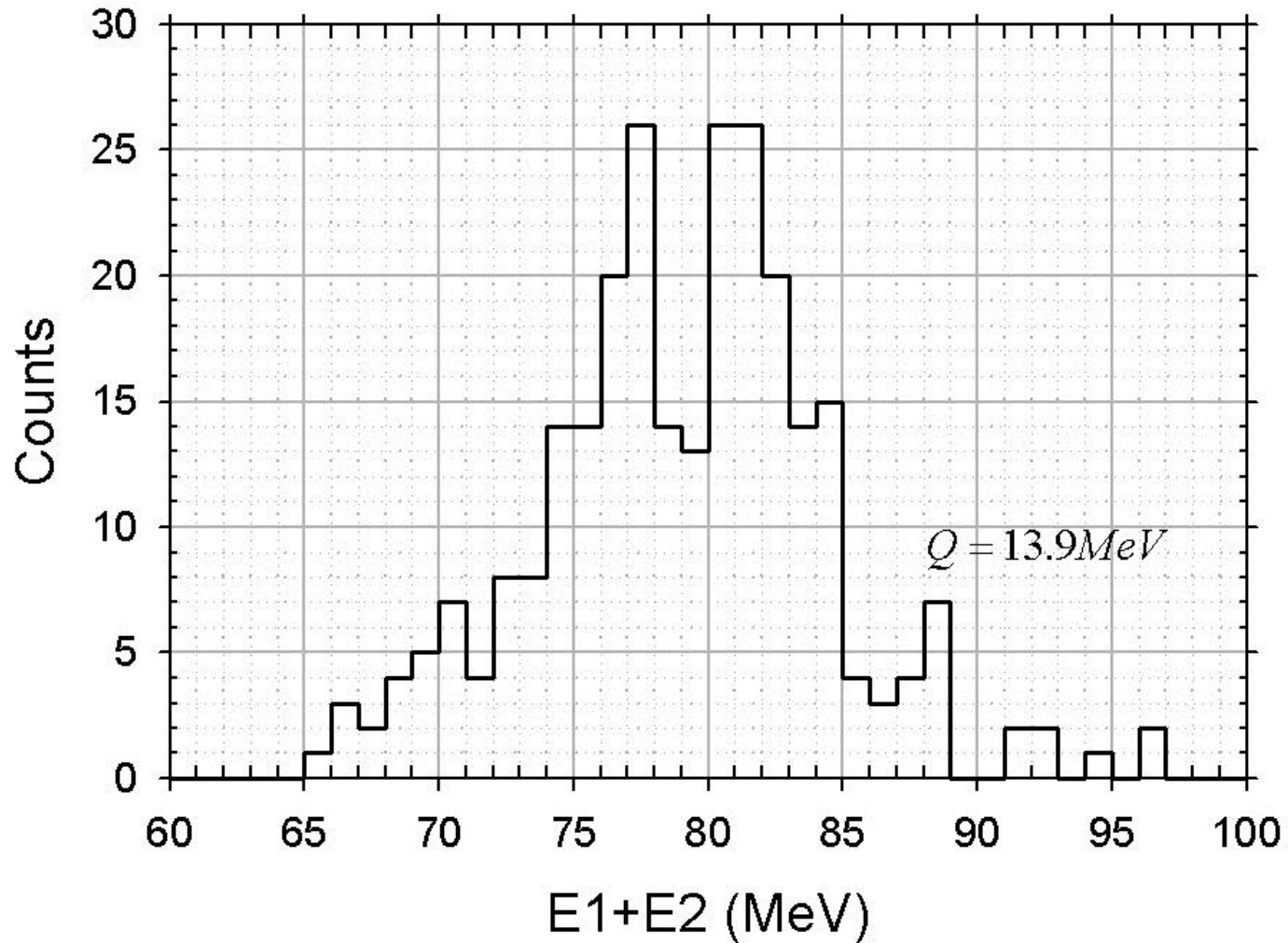
Energy sharing spectra of  $^{24}\text{Mg}(^{12}\text{C}, 2^{12}\text{C})^{12}\text{C}$  at 104 MeV with  $Q=13.9$  MeV  
at coplanar symmetric angle of  $40.5^\circ$



Summed Energy Spectrum of  $^{24}\text{Mg}(^{12}\text{C}, 2^{12}\text{C})^{12}\text{C}$  at 104 MeV.  
 $Q=13.9$  MeV at coplanar symmetric angle of  $36.7^\circ$



Summed Energy Spectrum of  $^{24}\text{Mg}(^{12}\text{C}, 2^{12}\text{C})^{12}\text{C}$  at 104 MeV.  
 $Q=13.9$  MeV at coplanar symmetric angle of  $33.9^\circ$

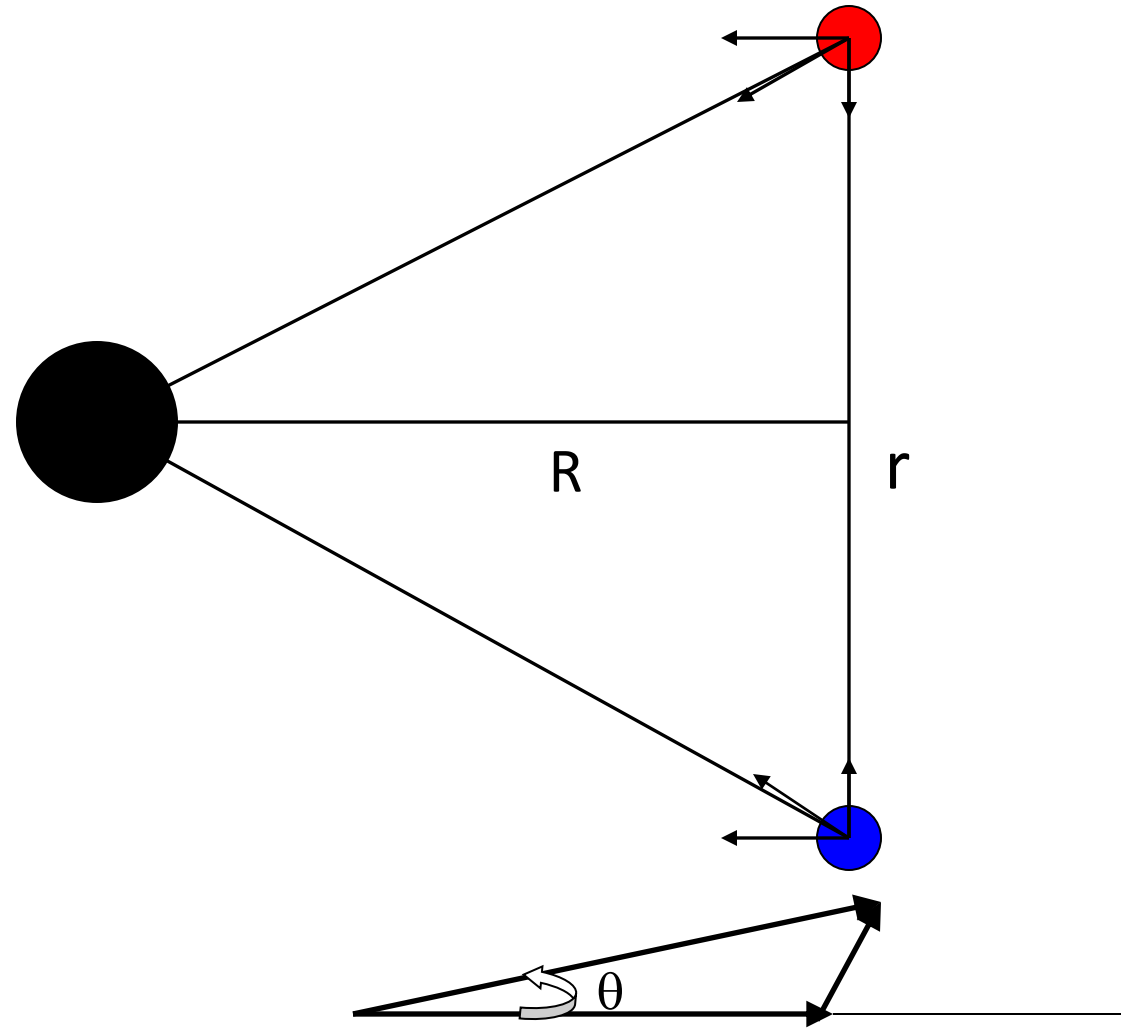




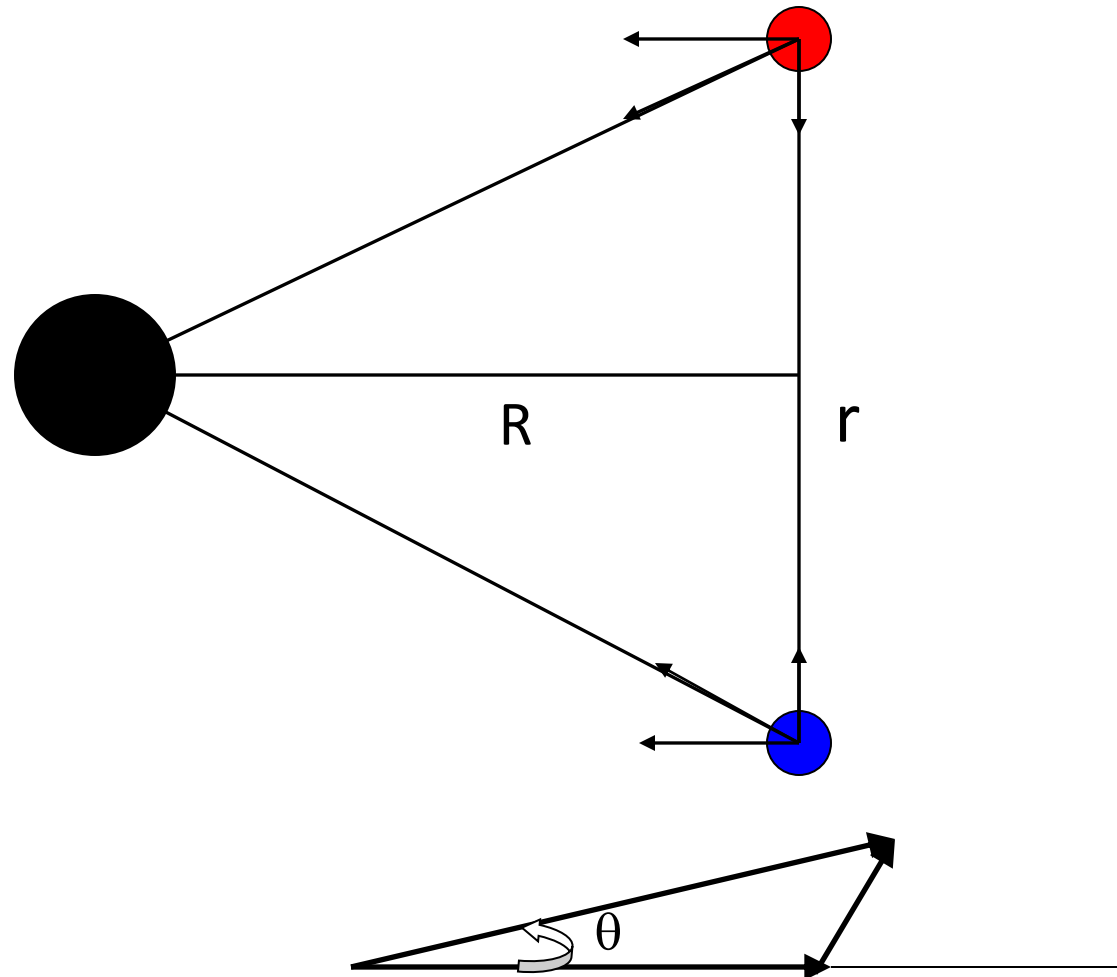
- Finite Range with distortions explain elastic as well as knockout data.
- One can do heavy cluster knockout similar to (C,2C) reaction to study the short distance behaviour of the heavy clusters vertex (Repulsive core radius).
- The repulsion arises from the antisymmetrization of the many fermions system.
- Distortions due to the residual nucleus can be used as an observer (not just a spectator) of the knockout vertex.
- Knockout reactions are very sensitive to the interaction at the knockout vertex. Which has never been imagined by earlier workers.
- Heavy cluster knockout is possible to analyze because of our Finite Range Formalism and program.

Shrinkage of Deuteron in  ${}^6\text{Li}$

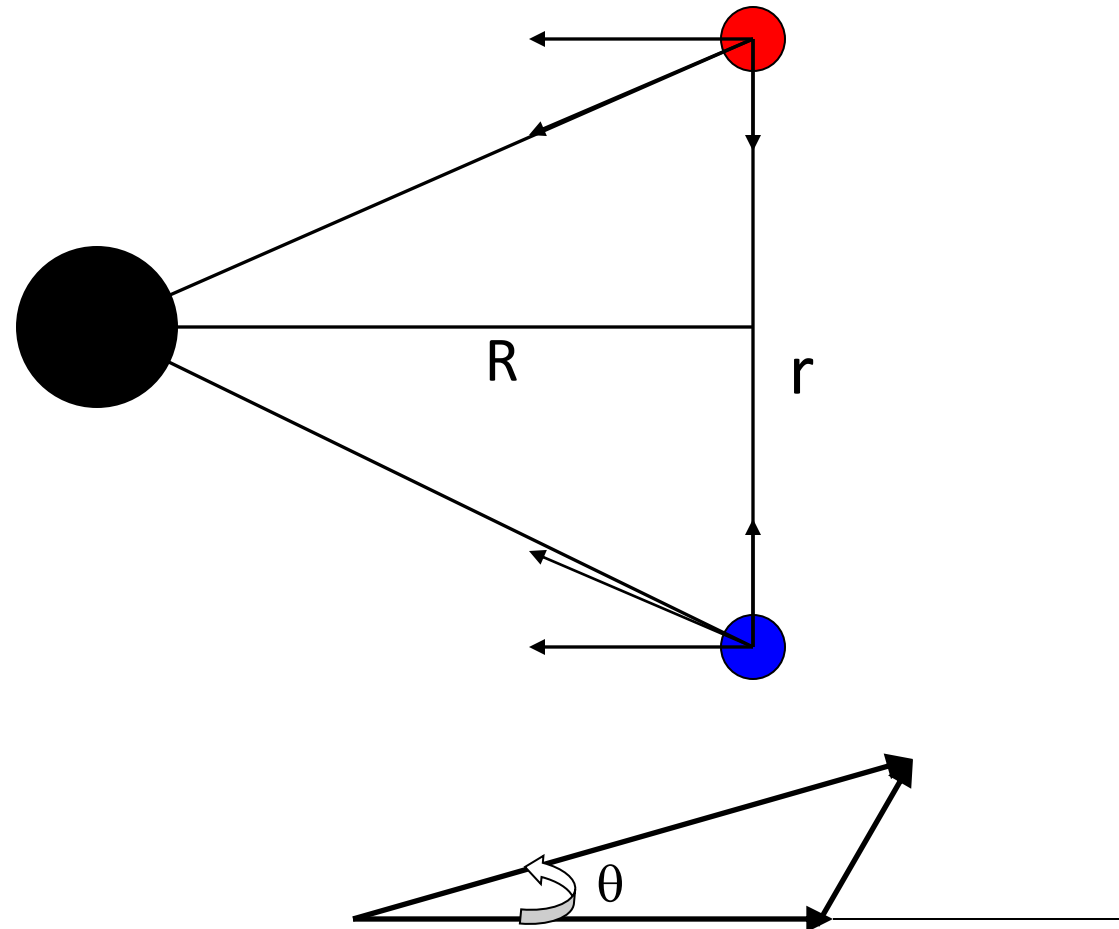
# Surface Clustering in Light Nuclei



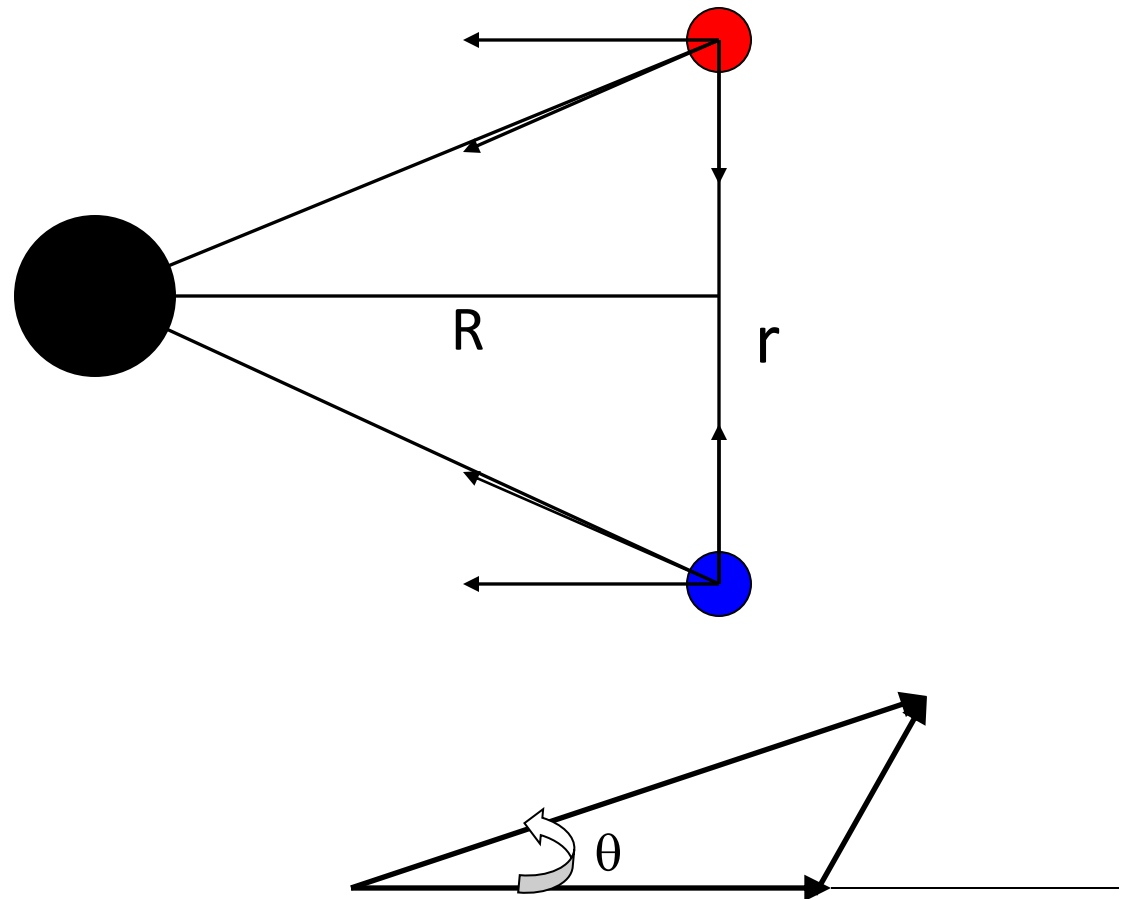
# Surface Clustering in Light Nuclei



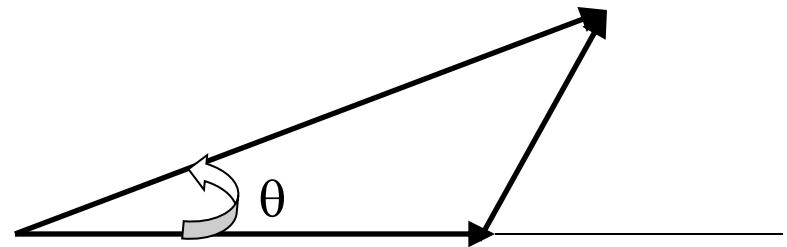
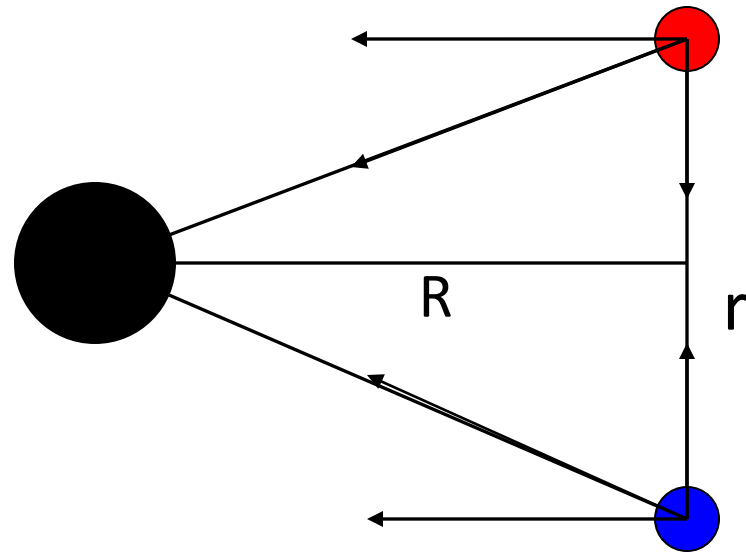
# Surface Clustering in Light Nuclei



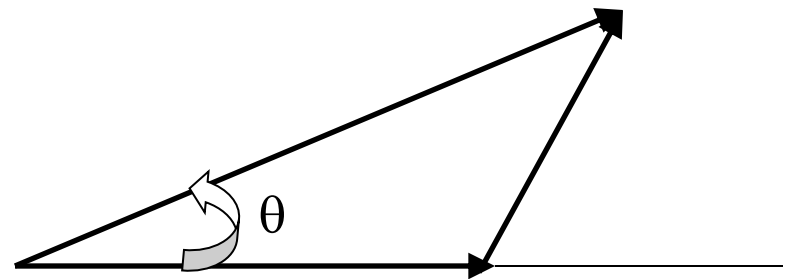
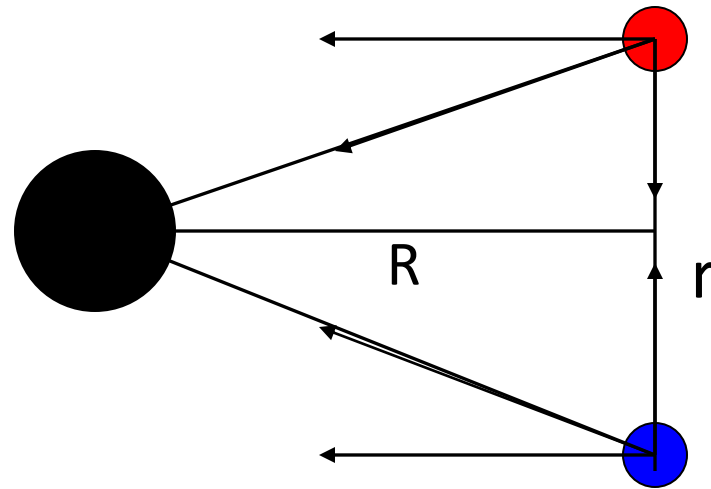
# Surface Clustering in Light Nuclei



# Surface Clustering in Light Nuclei

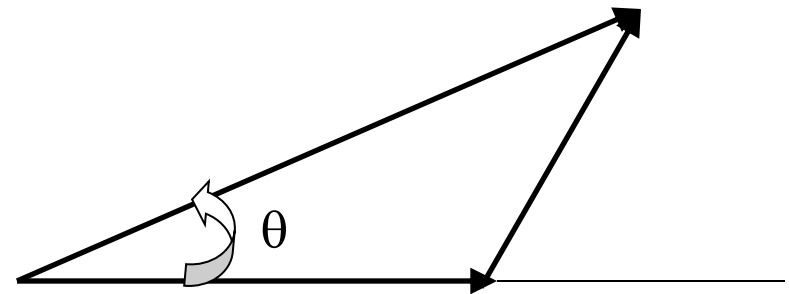
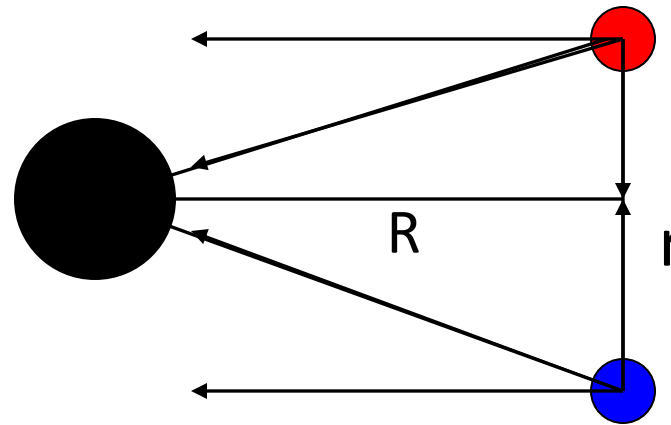


# Surface Clustering in Light Nuclei

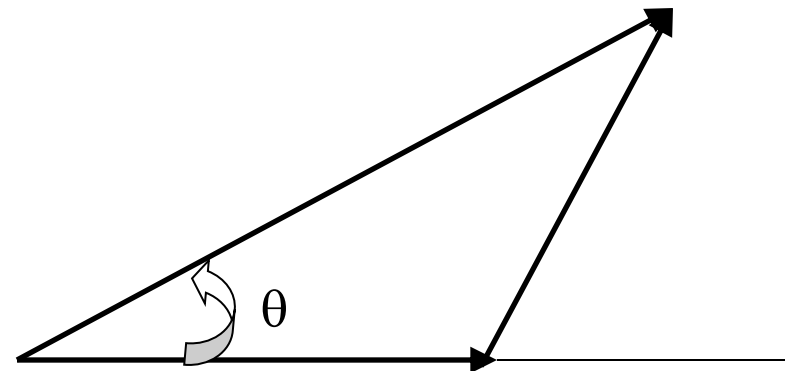
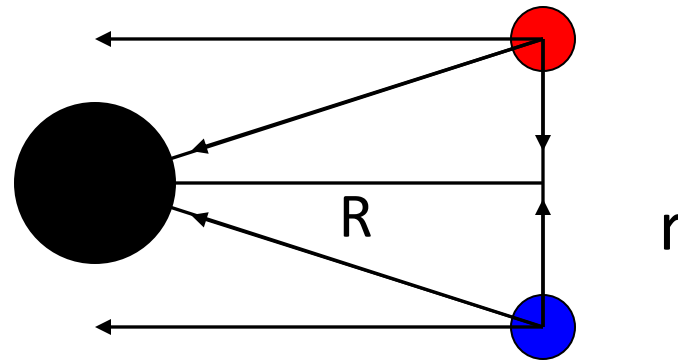




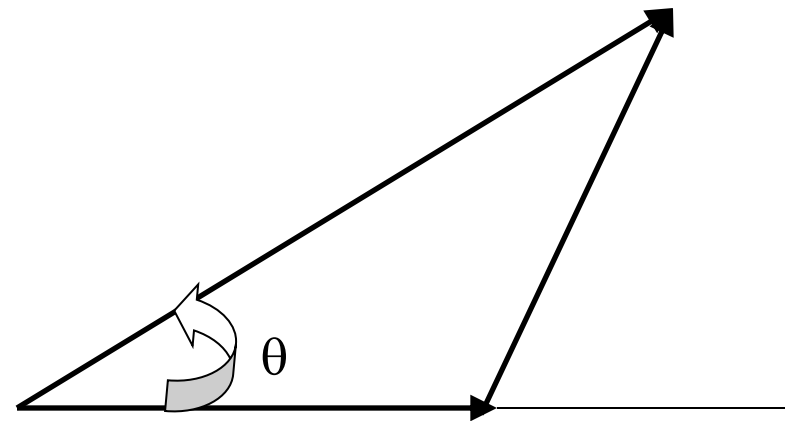
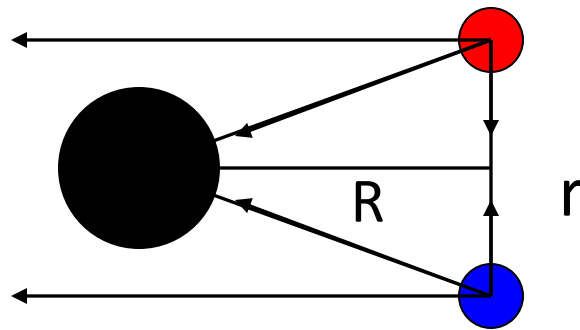
# Surface Clustering in Light Nuclei



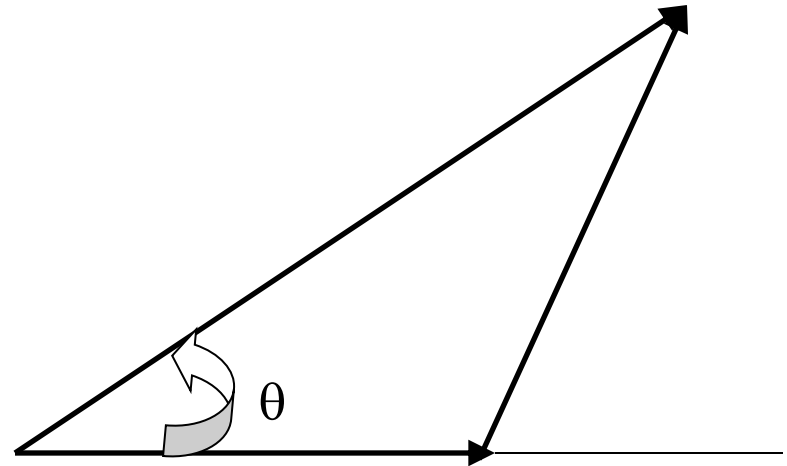
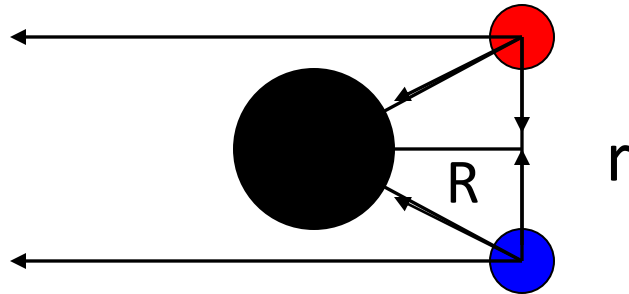
# Surface Clustering in Light Nuclei



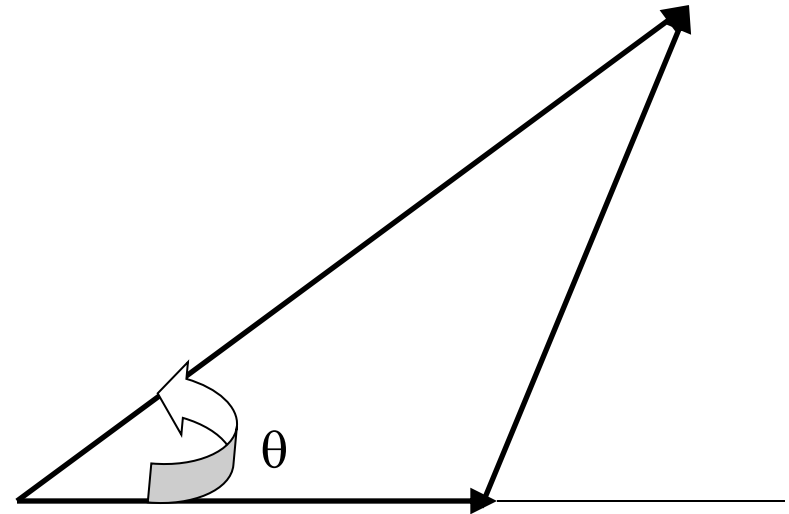
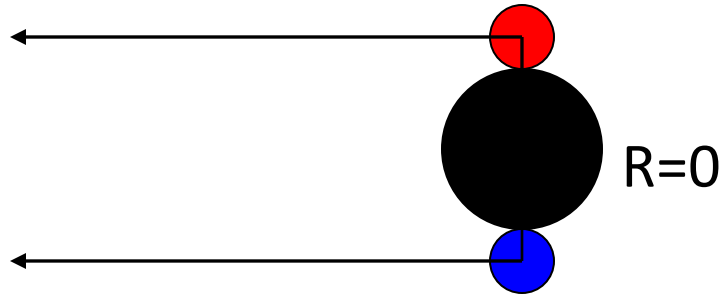
# Surface Clustering in Light Nuclei



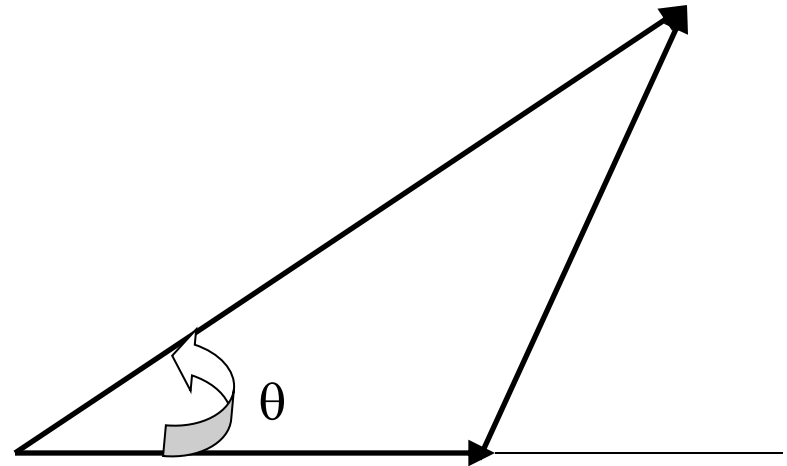
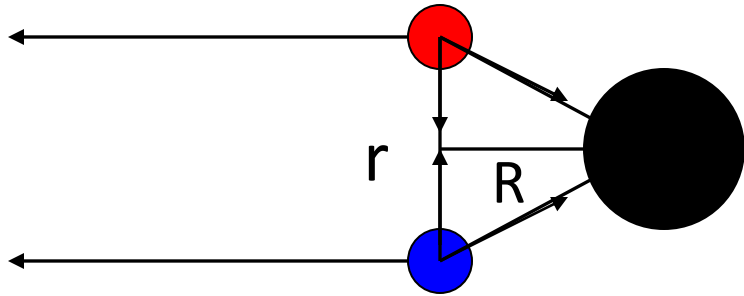
# Surface Clustering in Light Nuclei



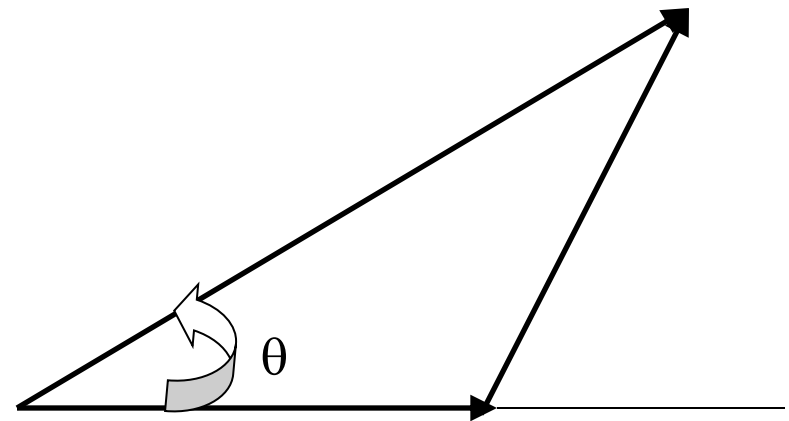
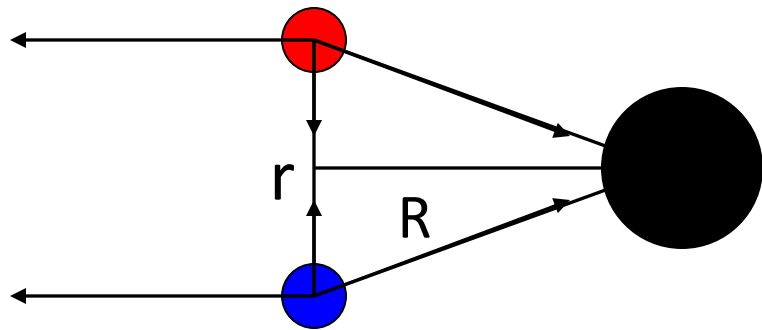
# Surface Clustering in Light Nuclei



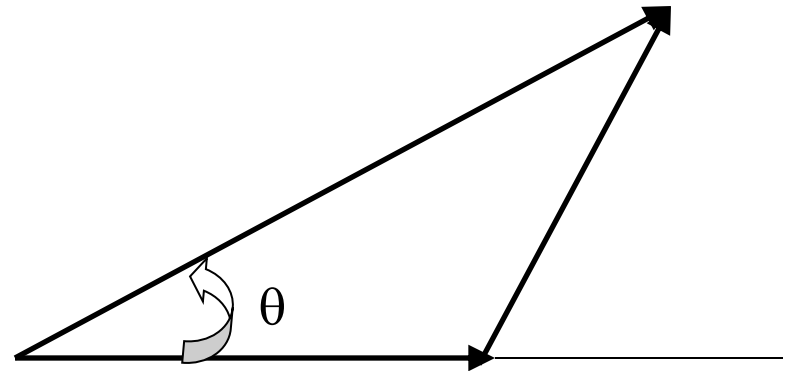
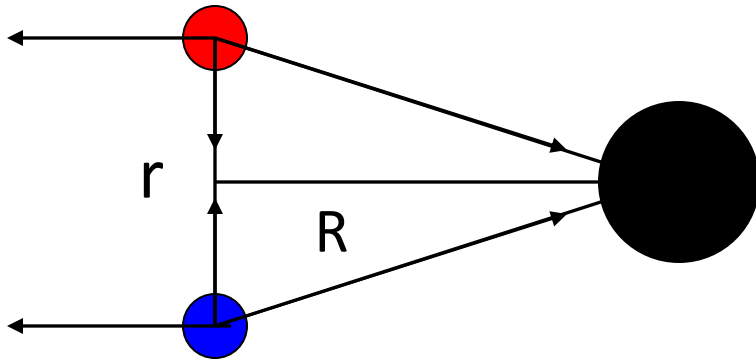
# Surface Clustering in Light Nuclei



# Surface Clustering in Light Nuclei

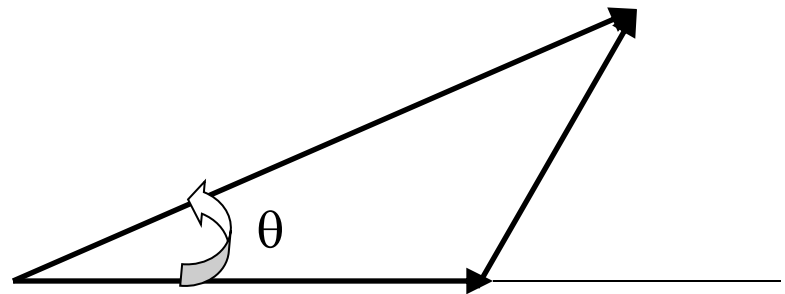
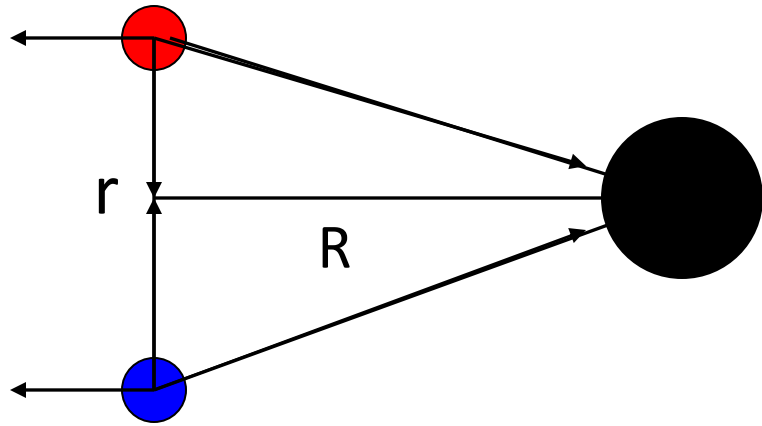


# Surface Clustering in Light Nuclei

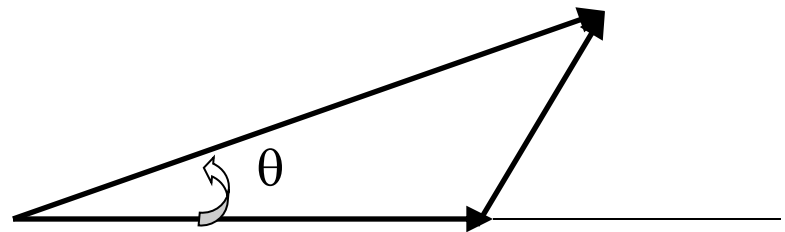
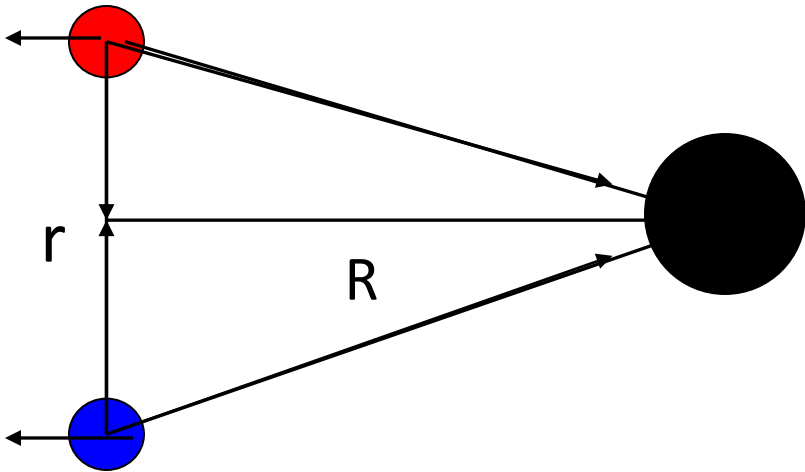




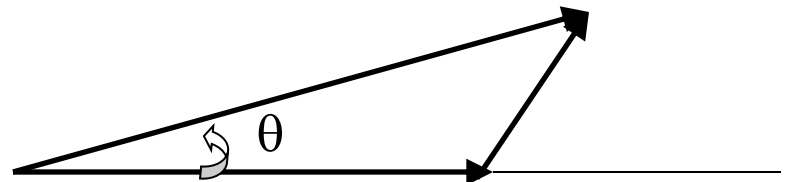
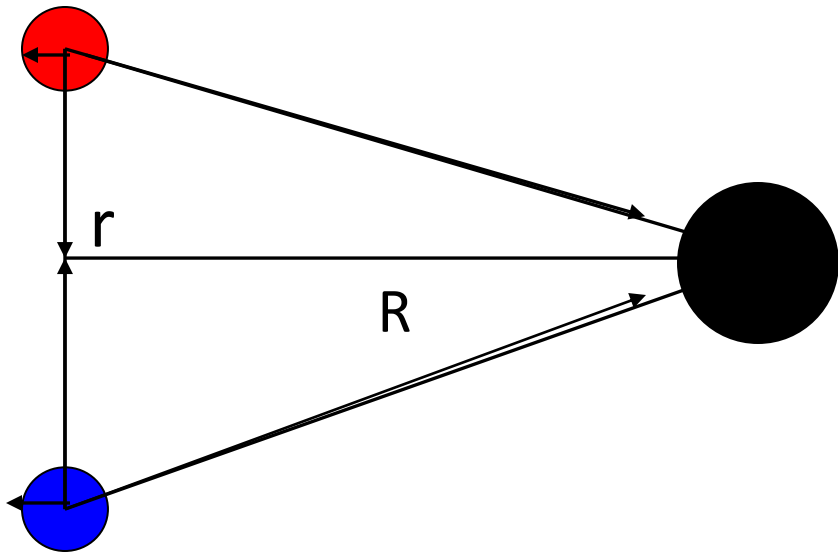
# Surface Clustering in Light Nuclei



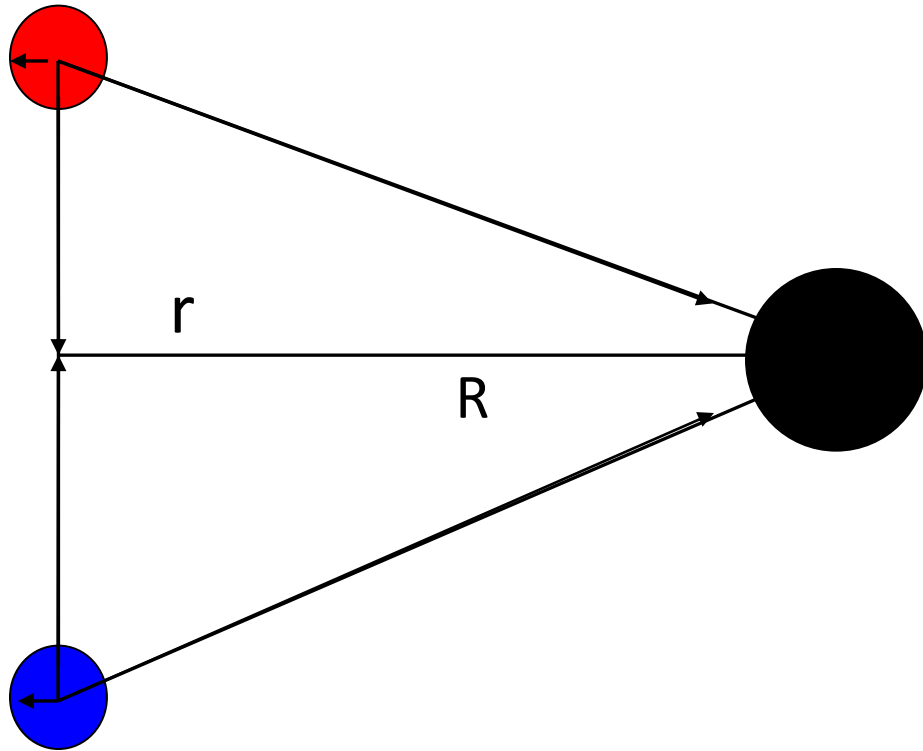
# Surface Clustering in Light Nuclei

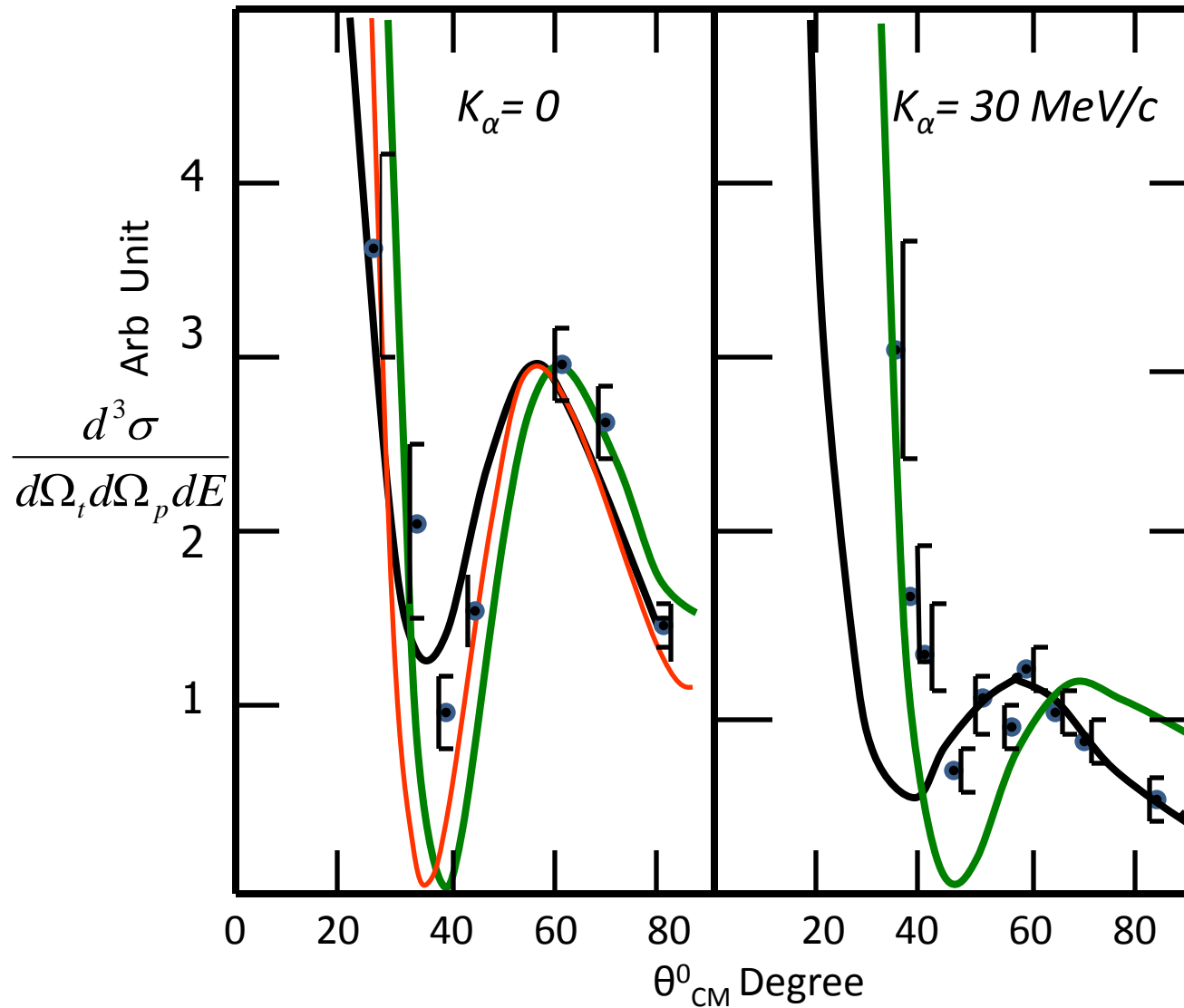


# Surface Clustering in Light Nuclei



# Surface Clustering in Light Nuclei

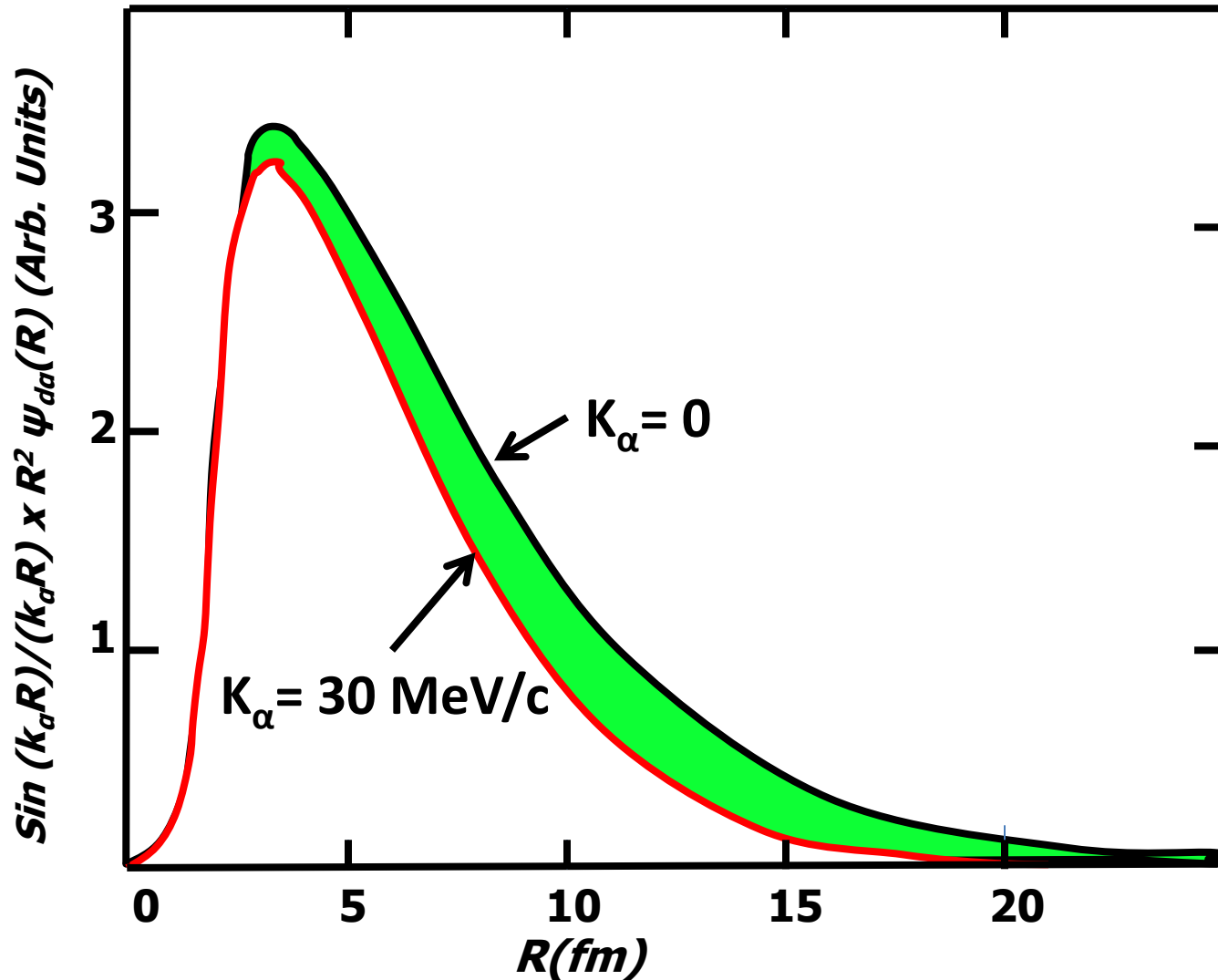




Shift of the Angular distribution of  $\text{Li}^6(d, tp)\text{He}^4$  reaction to larger angles for  $k_\alpha = 30 \text{ MeV}/c$  exhibiting shrinkage of d - cluster in  ${}^6\text{Li}$  as it approaches  $\alpha$  - cluster

Plane wave overlap function for  $\text{Li}^6(d, tp)\text{He}^4$  Reaction  $\sim 28$  MeV

*PRL. 32 (1974) 173*



➤ As seen in the previous figure, when the Deuteron cluster goes farther away from the  $\alpha$  cluster (when  $K_\alpha = 0$  MeV/c) the transition amplitude has relatively more contribution from larger  $R_{d-\alpha}$ .

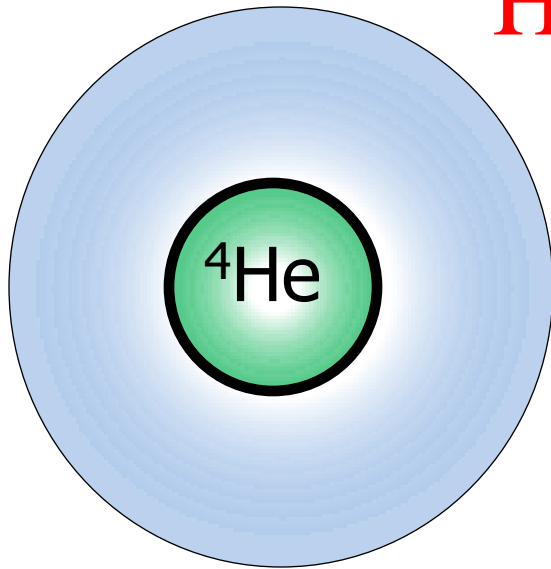
➤ Otherwise, corresponding to  $K_\alpha = -30$  MeV/c the  ${}^6\text{Li}(d, t p){}^4\text{He}$  is expected to display more contribution from the distorted deuteron and if the  $n-p$  residual interaction in Deuteron cluster is long range type then we will see shrinkage.

➤ It is clear from next slide; as compared to the free  $d(d, t)p$  distribution (free Deuteron cluster), the c.m.  $t-p$  angular distribution of the  ${}^6\text{Li}(d, t p){}^4\text{He}$  reaction shifts outwards. Which means that the relative momentum between *the  $n - p$  of the deuteron cluster* in  ${}^6\text{Li}$  increased.

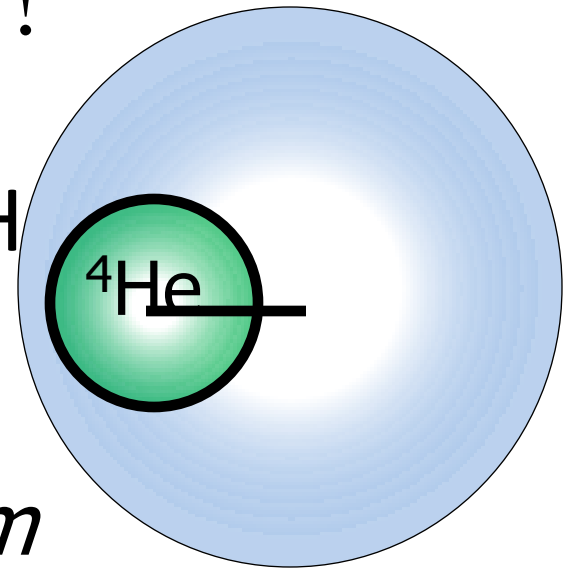
from **Halo** to **Hollow!!!**



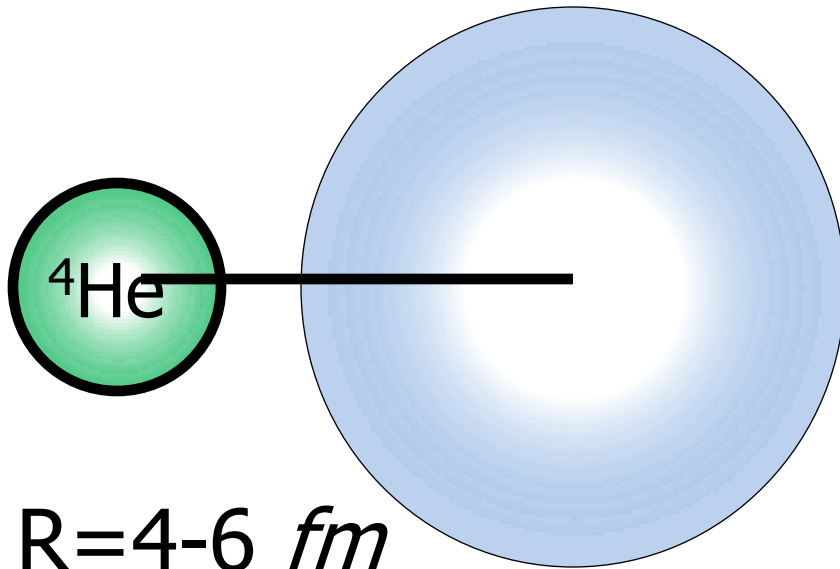
# Halo to Hollow !!



$R=0$



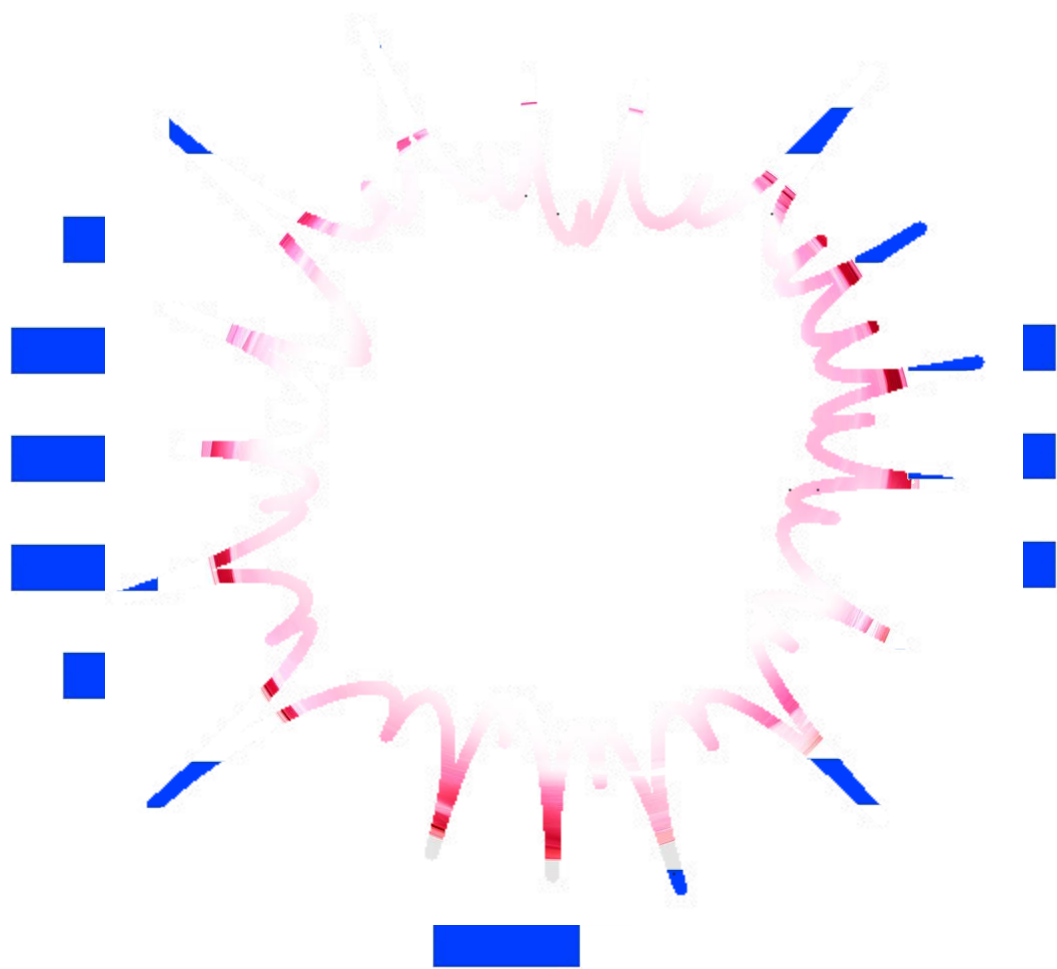
$R=1-2 \text{ fm}$



$R=4-6 \text{ fm}$



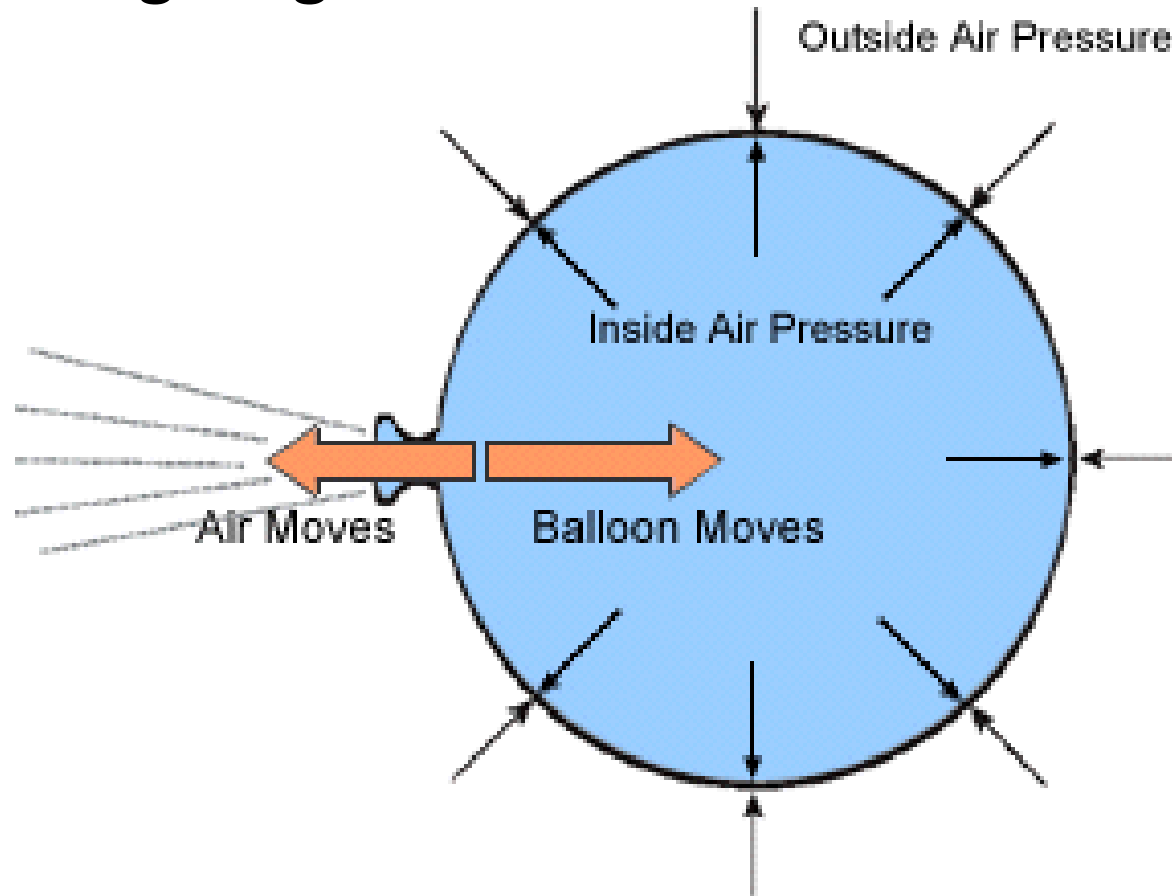




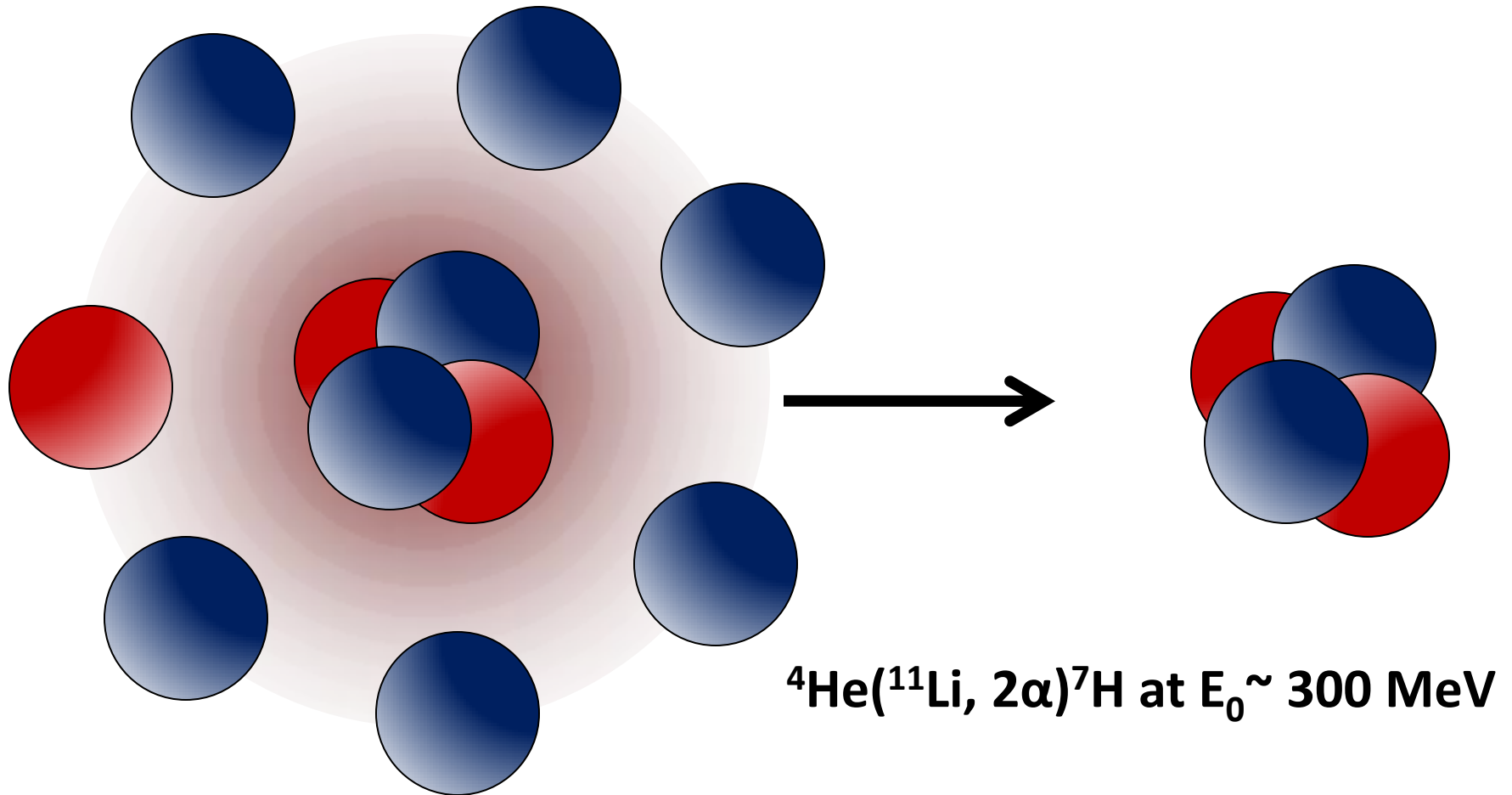
# Otherwise

**Deflation of a balloon when the surface tension is larger than the pressure inside the balloon.**

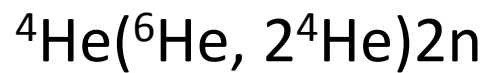
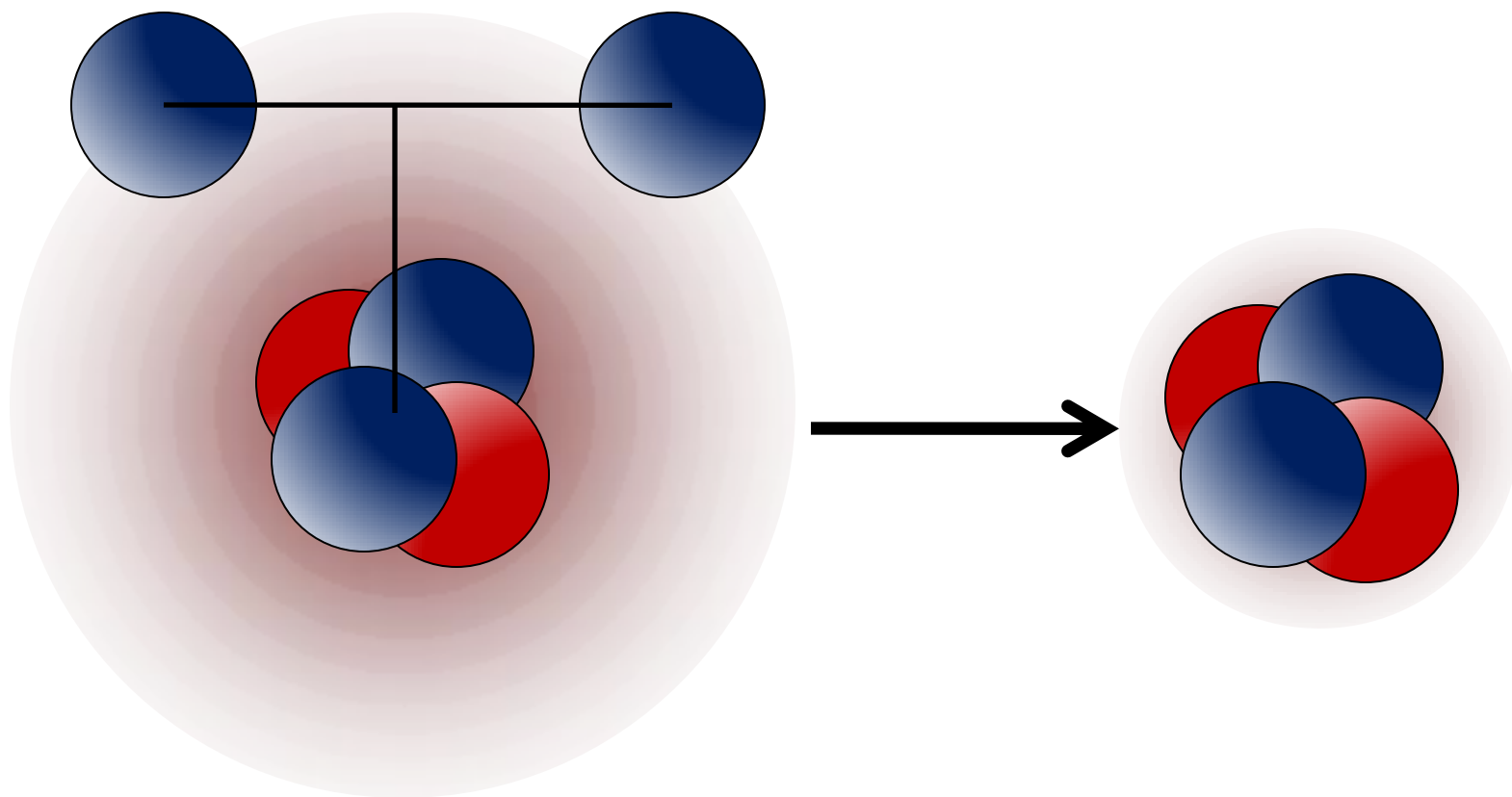
**It nicely represent the decay of a cluster to a compact shape when the long range  $N-N$  residual interaction is strong.**



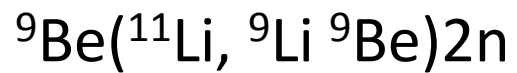
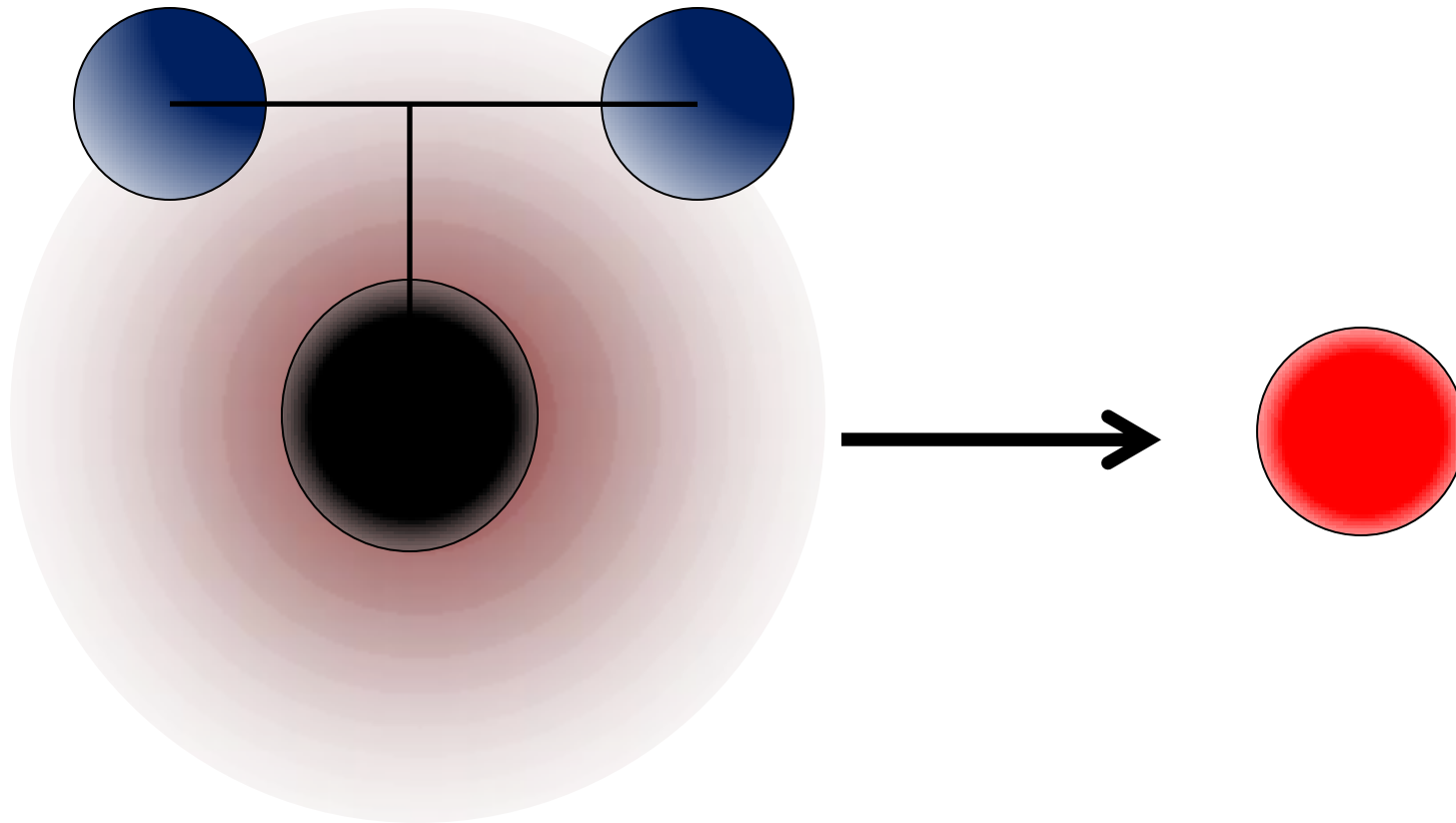
## Core Knockout Reaction of a Halo Nuclues:-



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## Conclusions:-

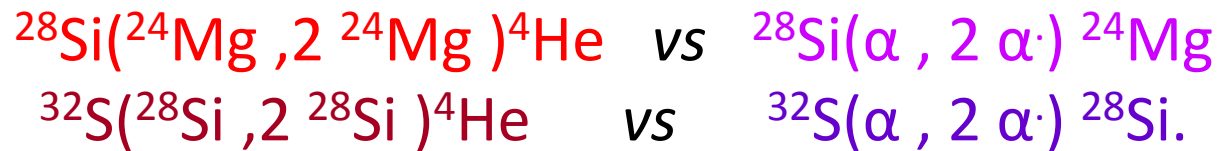
1. In case of ( $\alpha$ ,  $2\alpha$ ) knockout reactions there is a transition from 160 MeV to 200 MeV, where the  $\alpha$ - $\alpha$  interaction changes from repulsive to attractive potential.
- 2 One can explain the sudden change in reaction cross sections considering the strong interaction vertex.
- 3 One can do heavy cluster knockout similar to (C,2C) reaction to study the short distance behaviour of the heavy clusters vertex (Repulsive core radius).
- 4 Preliminary data analysis and understanding of the  $^{24}\text{Mg}(^{12}\text{C}, 2^{12}\text{C})^{12}\text{C}$  Reactions at 104 MeV suggest that  $^{24}\text{Mg}(\text{g.s})$  can not be described in terms of two Carbon-12 (g.s) clusters.
- 5 Data also indicated that  $^{16}\text{O}$  knockout from  $^{24}\text{Mg}$  is very significant leading to  $^{24}\text{Mg}$  as  $^{16}\text{O}+^8\text{Be}$
- 6 This also can be used to study the very weakly bound nuclei such as  $^{11}\text{Li}$ ,  $^8\text{He}$ ,  $^6\text{He}$  etc by core knockout reaction etc.
- 7 This way one can probably arrive at "HOLLOW" nuclei.







In the present project we would like to study the **heavy ion knockout on  $^{28}\text{Si}$  and  $^{32}\text{S}$  using  $^{24}\text{Mg}$  and  $^{28}\text{Si}$  Beams** respectively at the Mumbai LINAC in order to compare these reactions with the corresponding  **$(\alpha, 2\alpha)$  reactions.**



This way we will be able to observe the influence of bigger and bigger knockout vertices on the knockout reactions.

