

# Exotic Atoms



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Paolo Crivelli

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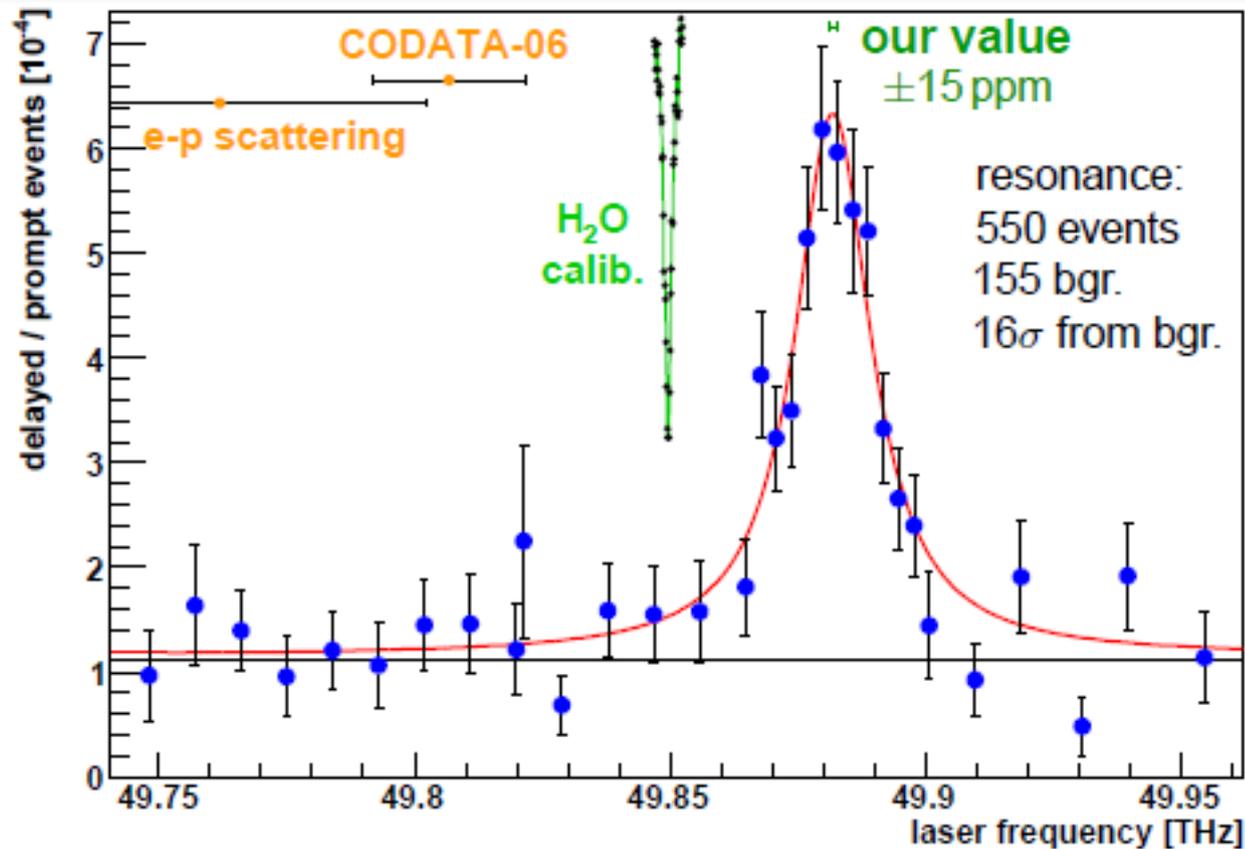
CHIPP plenary meeting, Kartause-Ittingen, 13.09.2012

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My work is supported by the Swiss National Science Foundation  
(Ambizione grant PZ00P2\_132059) and by the ETH Research Grant ETH-47 12-1

# Muonic Hydrogen- Results (2010)

F. Kottmann, CHIPP, Gersau 24.08.2010



## Reference:

R. Pohl, A. Antognini,  
F. Nez, D. Taqqu, et al.,  
Nature **466**, 213 (2010)

## Collaboration:

- MPQ Garching
- LKB Paris
- Coimbra and Aveiro
- Stuttgart
- Fribourg
- Yale
- PSI - ETHZ - ...

Statistics:  $\pm 0.70$  GHz  
Systematics:  $\pm 0.30$  GHz (laser calibration)

Discrepancy (to CODATA-06):  
 $\sim 75$  GHz  $\leftrightarrow 5.0\sigma \leftrightarrow \delta\nu/\nu = 1.5 \times 10^{-3}$



## The proton radius puzzle (2012)

$7\sigma$  discrepancy between  $r_p$  from muonic hydrogen and CODATA-10

- Re-analysis and new e-p scattering data consistent with previous results
- Muonic hydrogen QED theory confirmed (Antognini et al., arXiv:1208.2637)
- Second transition in muonic-H (measured also in 2009) confirms previous results (see next slide)



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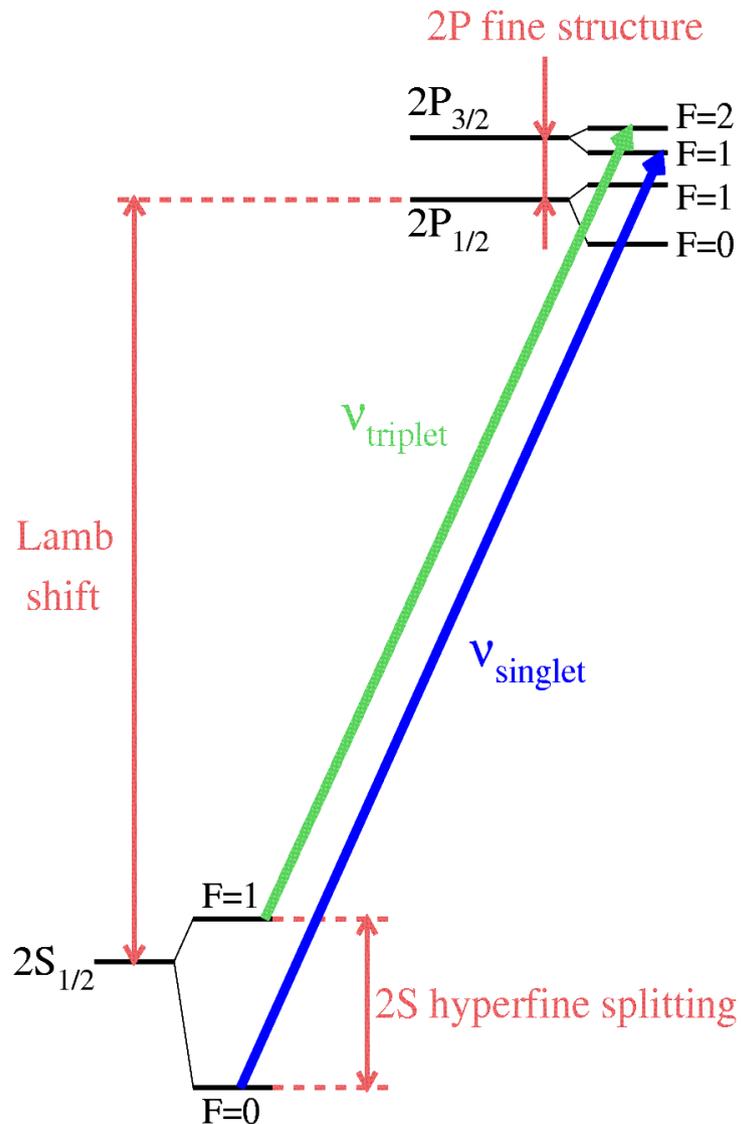
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What is the origin?

- Alternative analysis of scattering data consistent results with muonic hydrogen
- New physics?
- Value of the Rydberg constant? Several experiments are ongoing in H to check it.

# New results from muonic hydrogen

Antognini et al., submitted (2012)



Second transition confirms previous muonic-H results

- Combining the two transitions:
  - pure 2S-2P Lamb shift
  - 2S HFS
- Improved  $r_p$  value to  $u_r = 5 \times 10^{-4}$ 
  - Deuteron radius to  $u_r = 1 \times 10^{-4}$
  - Rydberg constant to  $u_r = 1 \times 10^{-12}$
- From HFS
  - Zemach and magnetic radius of the proton (in agreement with other results)

# Muonic Helium

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CREMA (Charged Radius Experiment with Muonic Atoms) collaboration

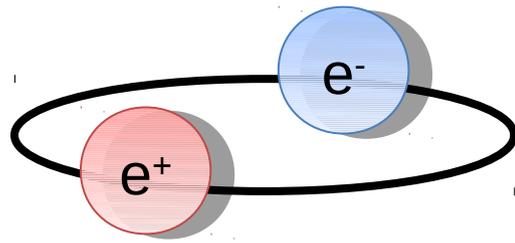
- Goal: measure several 2S-2P transitions in muonic helium ions  $\mu\text{He}^+$ 
  - Determine alpha and helion charge radius to  $u_r = 10^{-4}$  (0.0004 fm)
- Aims
  - help to solve the proton radius puzzle
  - absolute nuclear charge radii  $^3\text{He}$ ,  $^4\text{He}$ ,  $^6\text{He}$
  - low energy effective nuclear theories
  - “improved” bound-state QED test when combined with  $\text{He}^+$  spectroscopy
- Proposal approved at PSI in 2010

**1<sup>st</sup> BEAM TIME EXPECTED IN 2013**

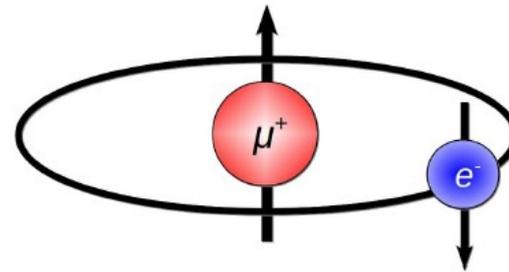
# Leptonic atoms

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Positronium (Ps)



Muonium (Mu)

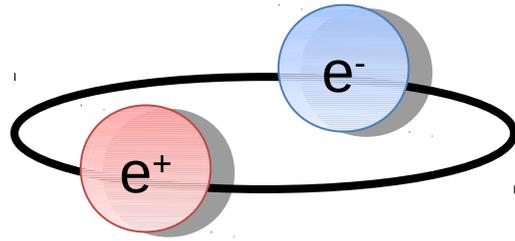


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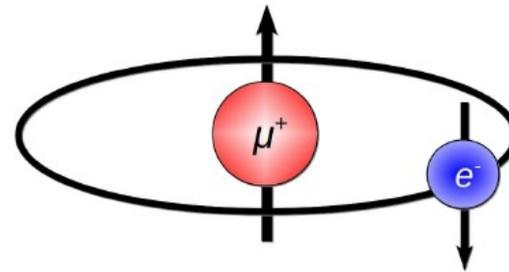
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Precise test of  
bound state QED  
free from finite size effects

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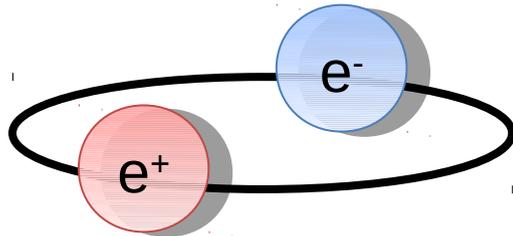


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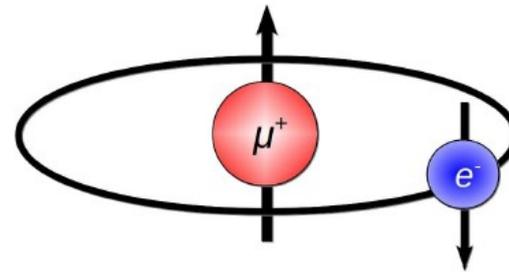
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Fundamental  
constants  
( $m_{e^+}/m_{e^-}$ ,  $m_{\mu}$ ,  $q_{e^-}/q_{\mu^+}$  ..)

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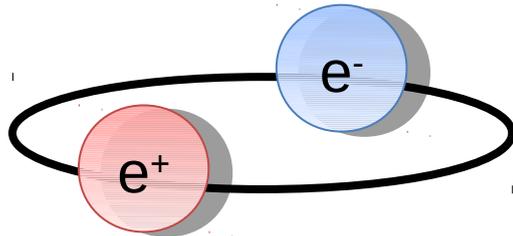


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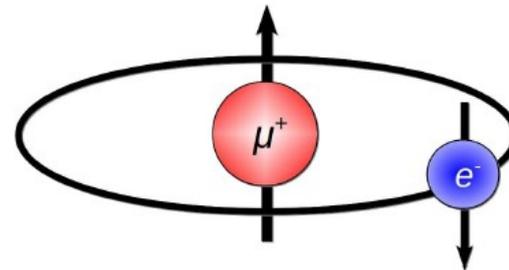
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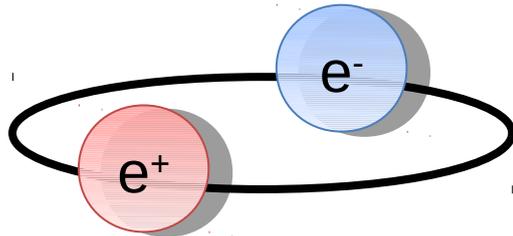
Test of the fundamental  
symmetries

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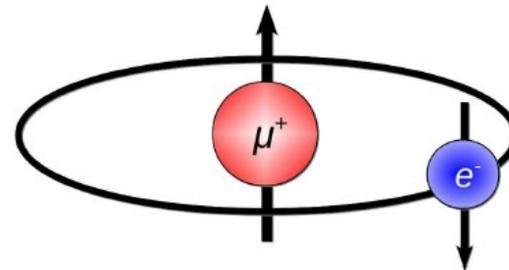
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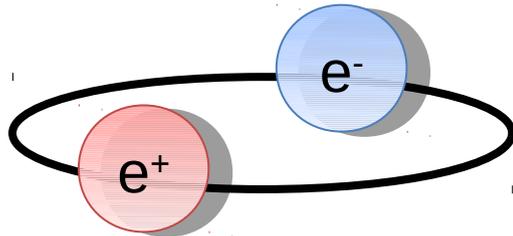
Search for new physics

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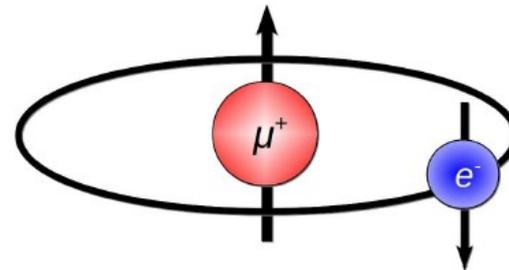
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Positronium (Ps)



Muonium (Mu)



Test of the fundamental  
symmetries

Test the effect of gravity  
on  
anti-matter

Search for new physics

# Ps and Mu sources

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Quality of the Ps and Mu sources: main limitation to improve the current experiments.

High vacuum yield

Small emission velocities

Long term stability

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C. M. Surko and R. G. Greaves, Phys. Plasmas 11, 2333 (2004)

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- Muons: efforts undertaken at PSI and J-PARC.

D. Taqqu, Phys. Rev. Lett. 97, 194801 (2006) and e.g. A. Toyoda et al., arXiv:1110.1125.



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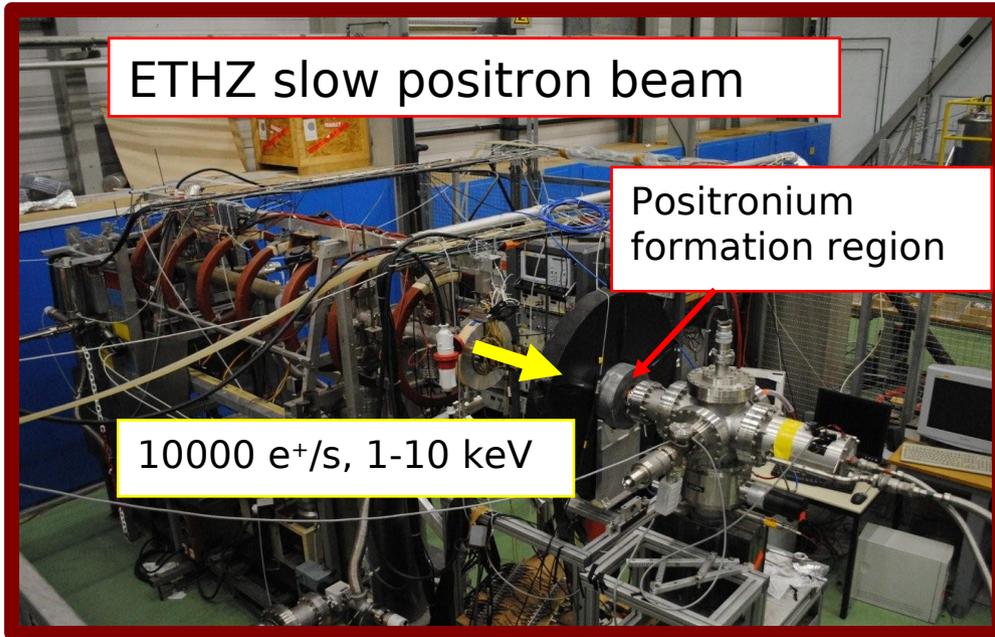
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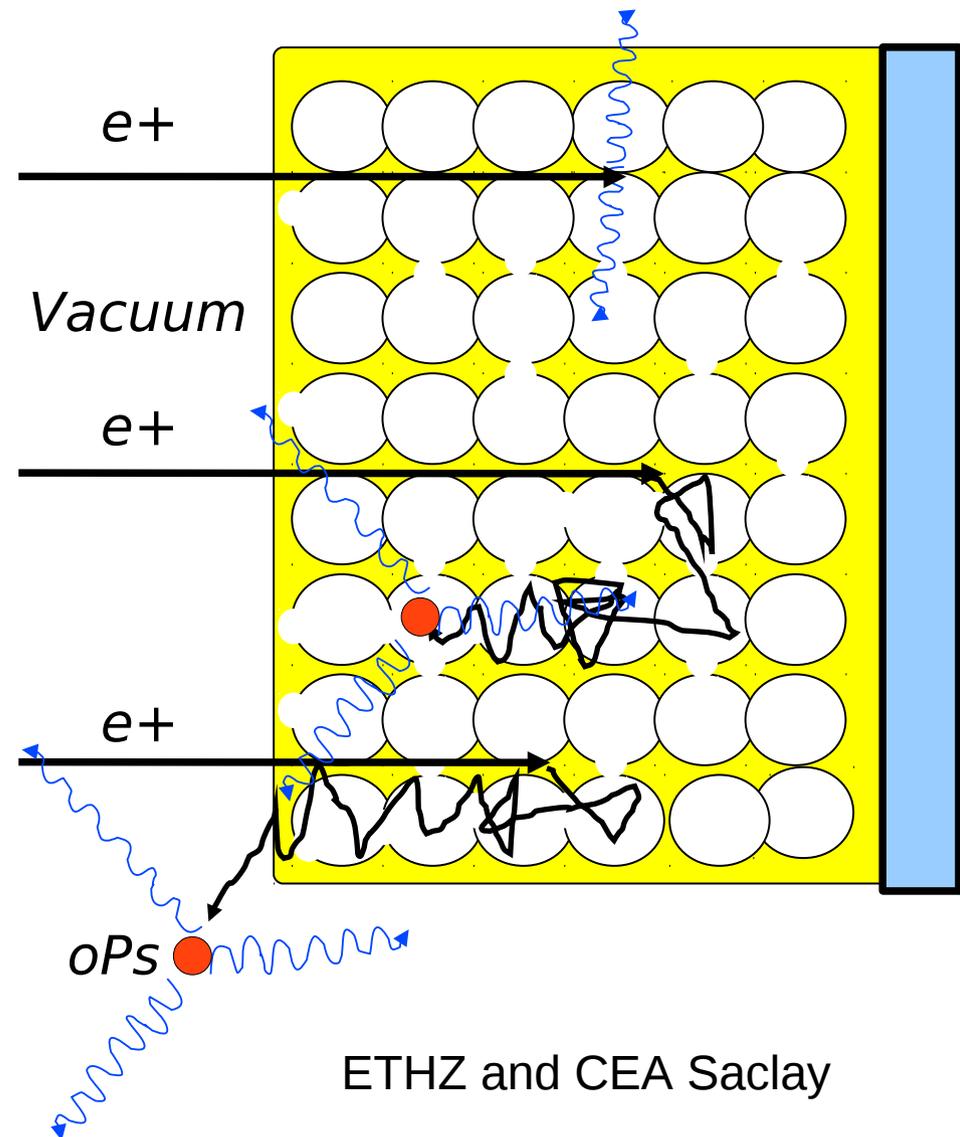
2) Improve the  $e^+ \rightarrow \text{Ps}$  and  $\mu^+ \rightarrow \text{Mu}$  conversion targets (this talk).

# Ps production in porous SiO<sub>2</sub> thin films



- e<sup>+</sup> implanted with few keV (range of 300 nm for 5 keV energy)
- e<sup>+</sup> slow down and stop in the bulk material
- Ps formation in the bulk material (~60% in SiO<sub>2</sub>)
- Ps ejection in the pores (work energy ~1 eV)
- Thermalization and diffusion in the pores
- A fraction of Ps 30-40 % exits into vacuum

Porous Silica thin film  
~500 -1000nm and 3-5 nm pore size

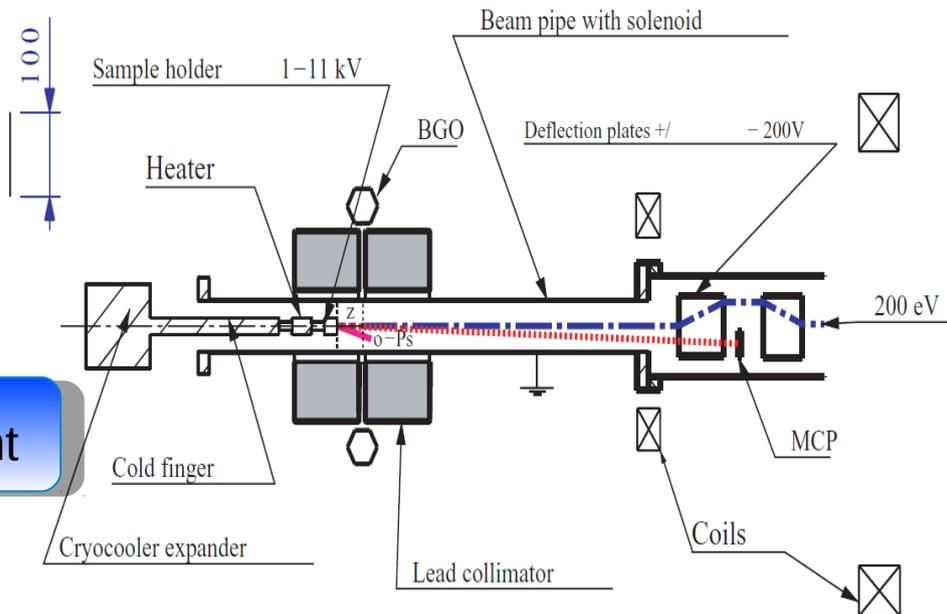
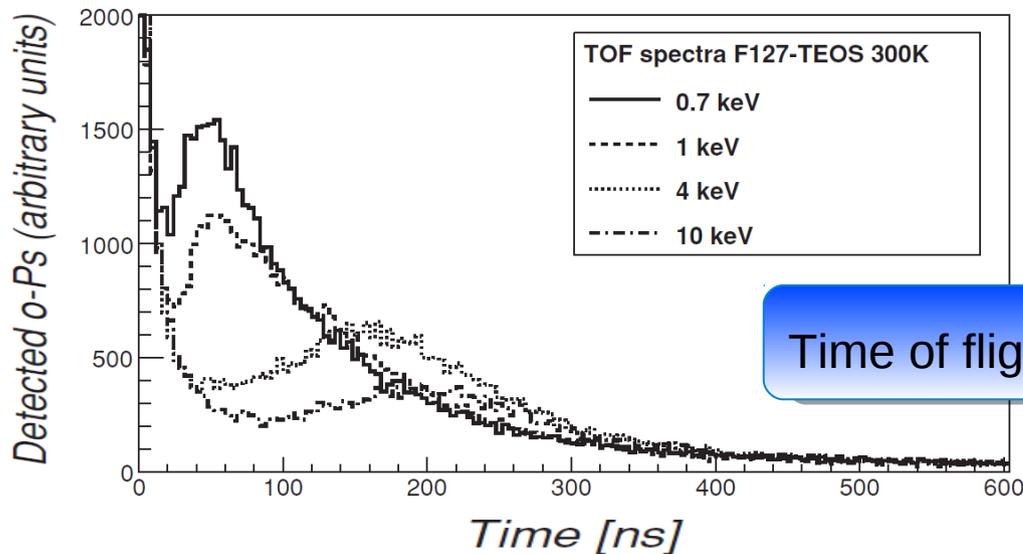


ETHZ and CEA Saclay

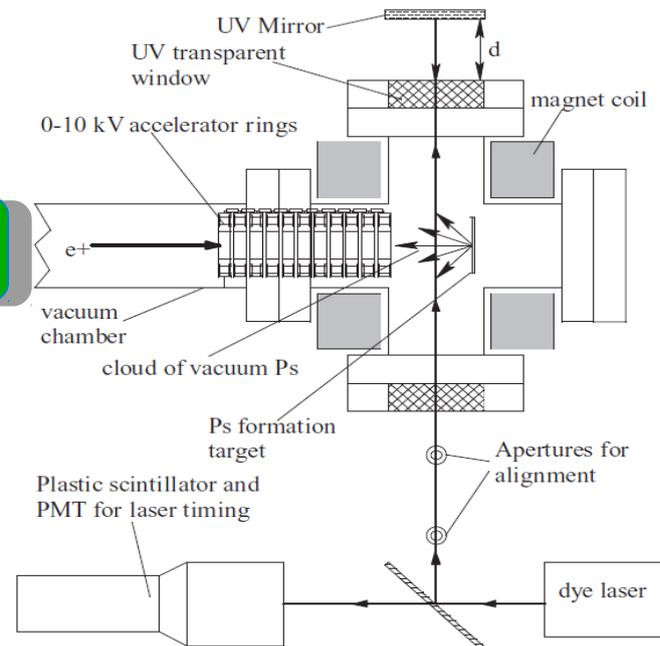
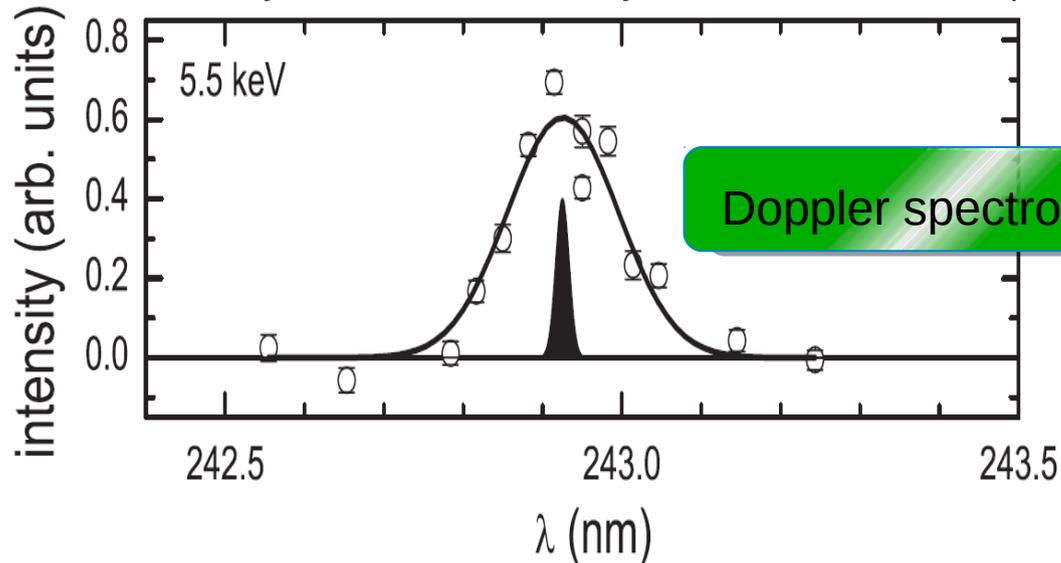
P. Crivelli et al. , Phys. Rev. A81, 052703 (2010)

# Measurement of Ps energy

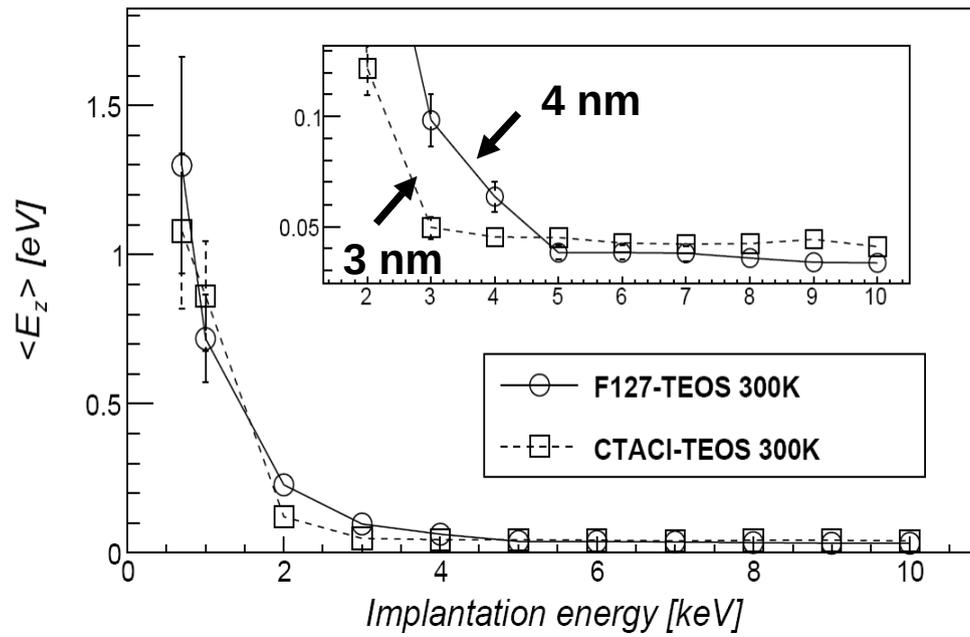
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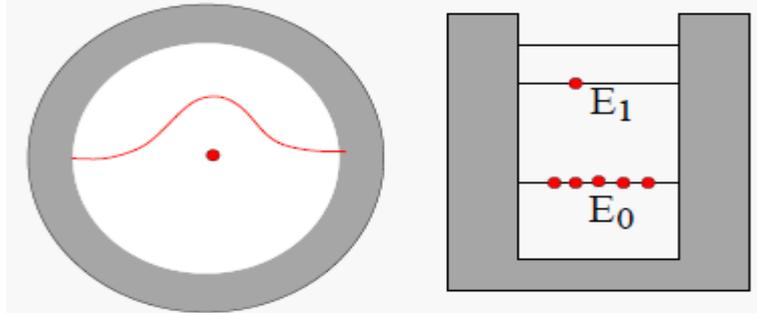
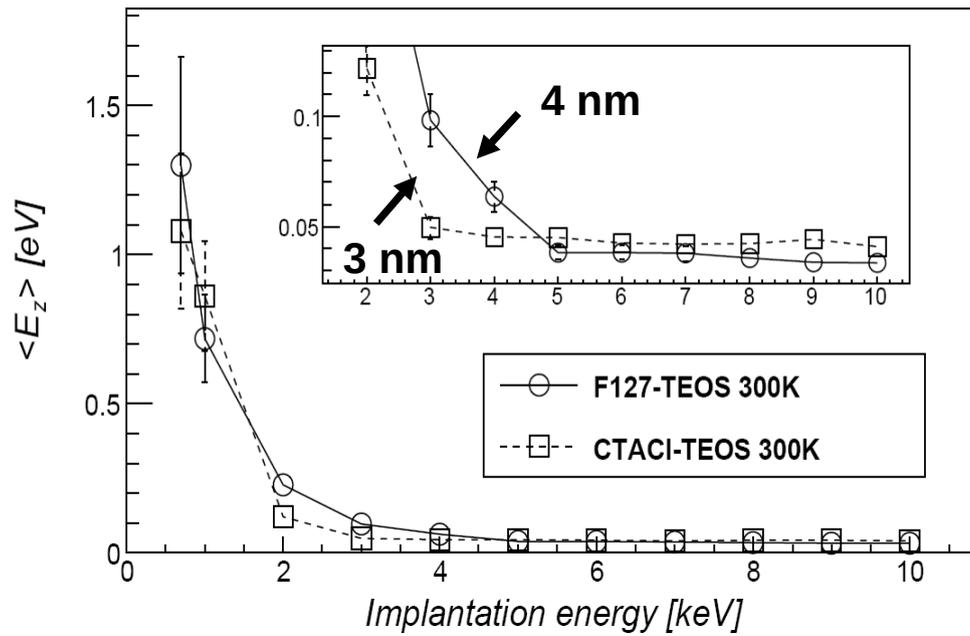
D. Cassidy, P. Crivelli et al., Phys. Rev. A 81, 012715 (2010)



# Ps as a particle in a box

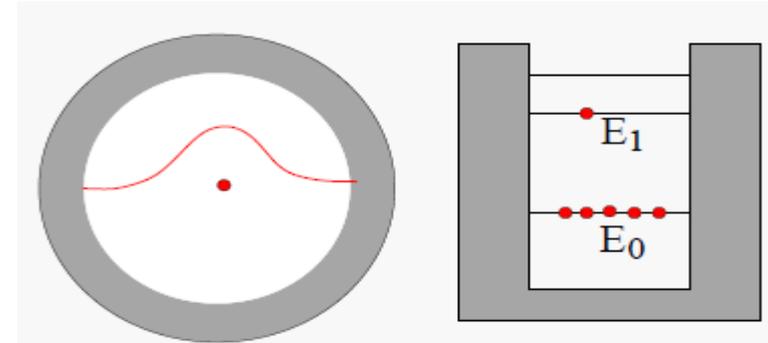
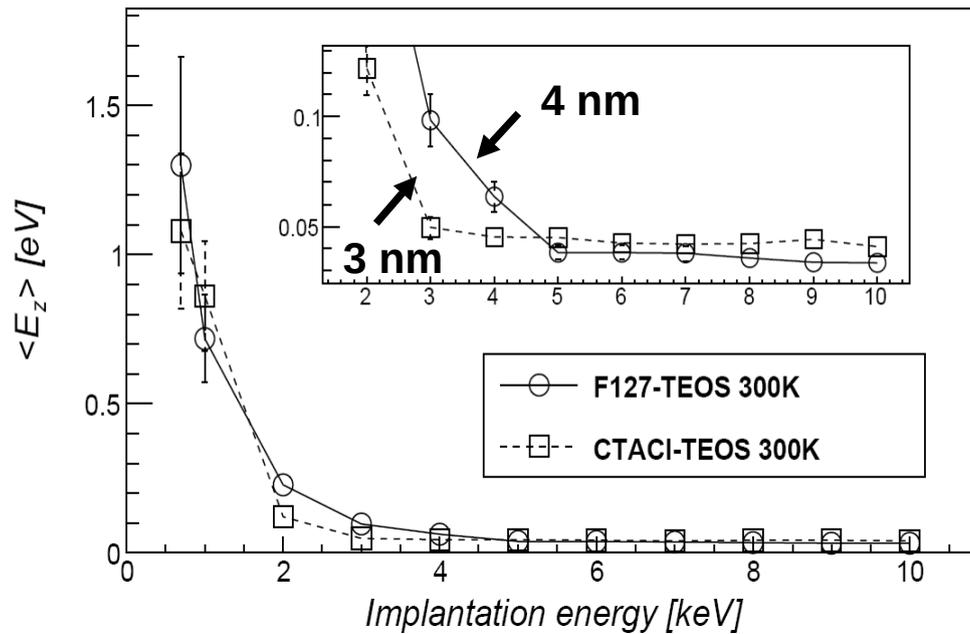


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$$E_{Ps} = \frac{h^2}{2m d^2} \approx 0.8 \text{ eV} (1 \text{ nm}/d)^2$$

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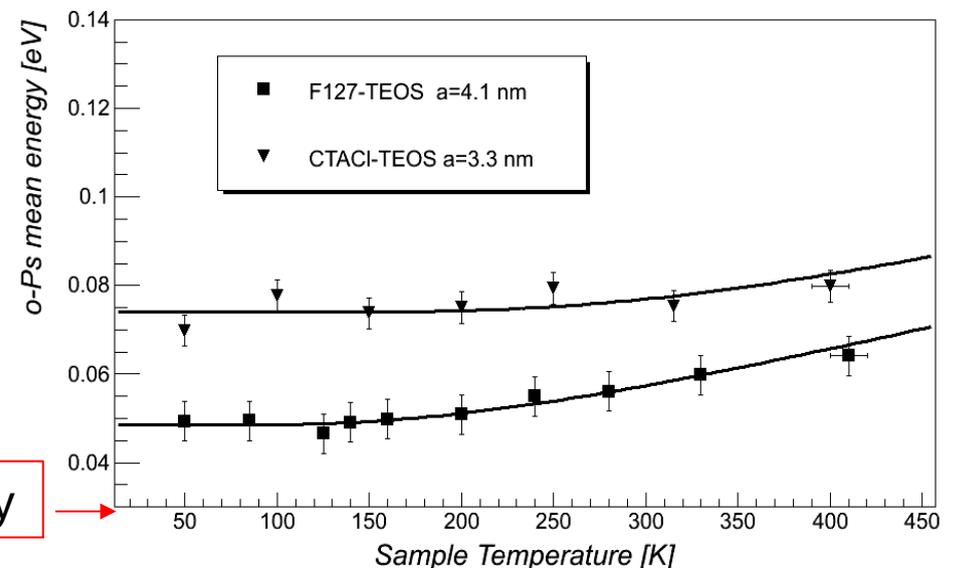
## Model Ps as a particle in a box

$$\langle H \rangle = kT^2 \left( \frac{1}{Z(a)} \frac{dZ(a)}{dT} + \frac{1}{Z(b)} \frac{dZ(b)}{dT} + \frac{1}{Z(c)} \frac{dZ(c)}{dT} \right)$$

Z is the partition function defined as

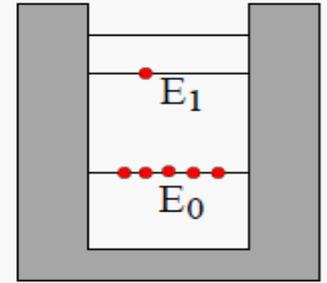
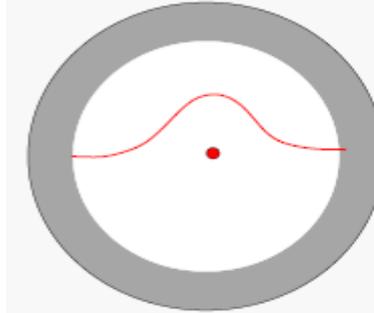
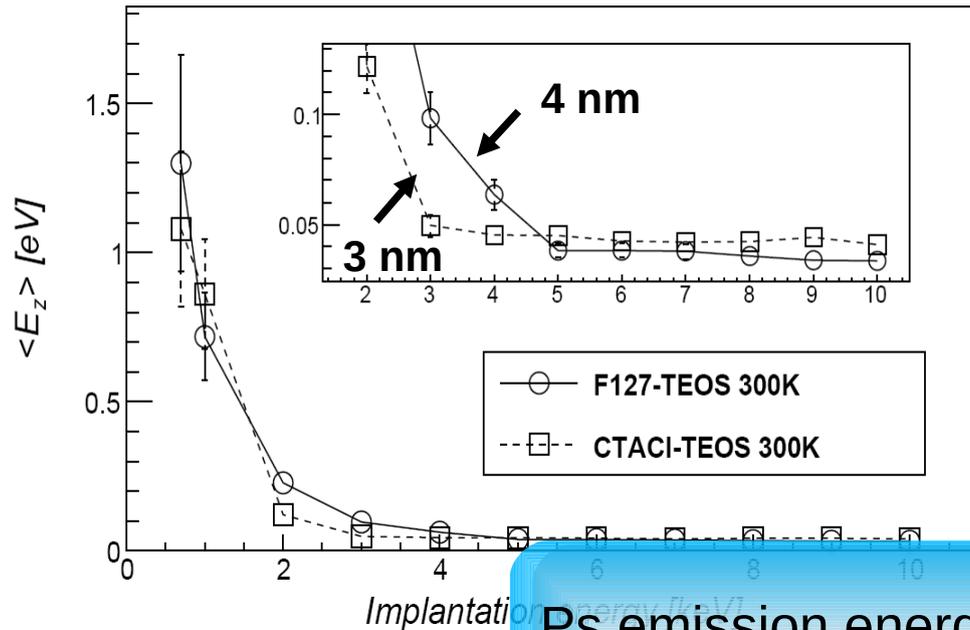
$$Z(a) = \sum_{n=1}^{\infty} e^{-\frac{h^2 n^2}{8ma^2} / kT},$$

Thermal energy



P. Crivelli et al., Phys. Rev. A81, 052703 (2010)

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Ps emission energy into vacuum defined by ground state energy in the pores

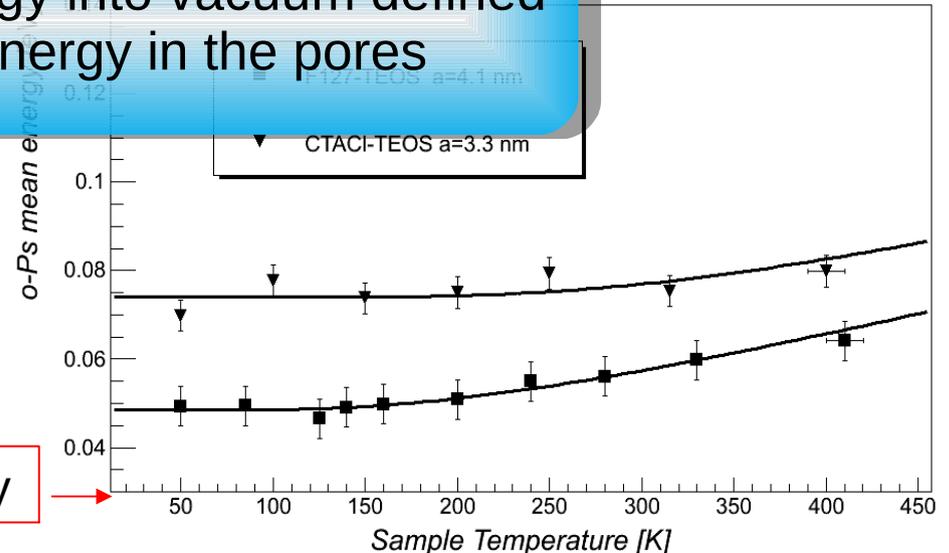
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# Mu production in SiO<sub>2</sub> thin films

Ps and Mu have similar formation mechanisms and yields in vacuum in silica powders ( used for Mu production in previous experiments).

→ Test the targets developed for Ps at the low energy muon beam line at PSI

We were confident that those would be promising candidate for:

- 1) Higher Mu vacuum yield
- 2) Low Mu emission velocity ( $\lambda_{\text{Mu}} \sim 1/10 \lambda_{\text{Ps}}$ )
- 3) Stable source (Ps vacuum yield constant in a time scale of months while powders degradation in few hours).

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PRL 108, 143401 (2012)

PHYSICAL REVIEW LETTERS

week ending  
6 APRIL 2012

## Muonium Emission into Vacuum from Mesoporous Thin Films at Cryogenic Temperatures

A. Antognini,<sup>1,\*</sup> P. Crivelli,<sup>1,†</sup> T. Prokscha,<sup>2,‡</sup> K. S. Khaw,<sup>1</sup> B. Barbiellini,<sup>3</sup> L. Liskay,<sup>4</sup> K. Kirch,<sup>1,2</sup>  
K. Kwuida,<sup>1</sup> E. Morenzoni,<sup>2</sup> F. M. Piegsa,<sup>1</sup> Z. Salman,<sup>2</sup> and A. Suter<sup>2</sup>

<sup>1</sup>*Institute for Particle Physics, ETH Zurich, Switzerland*

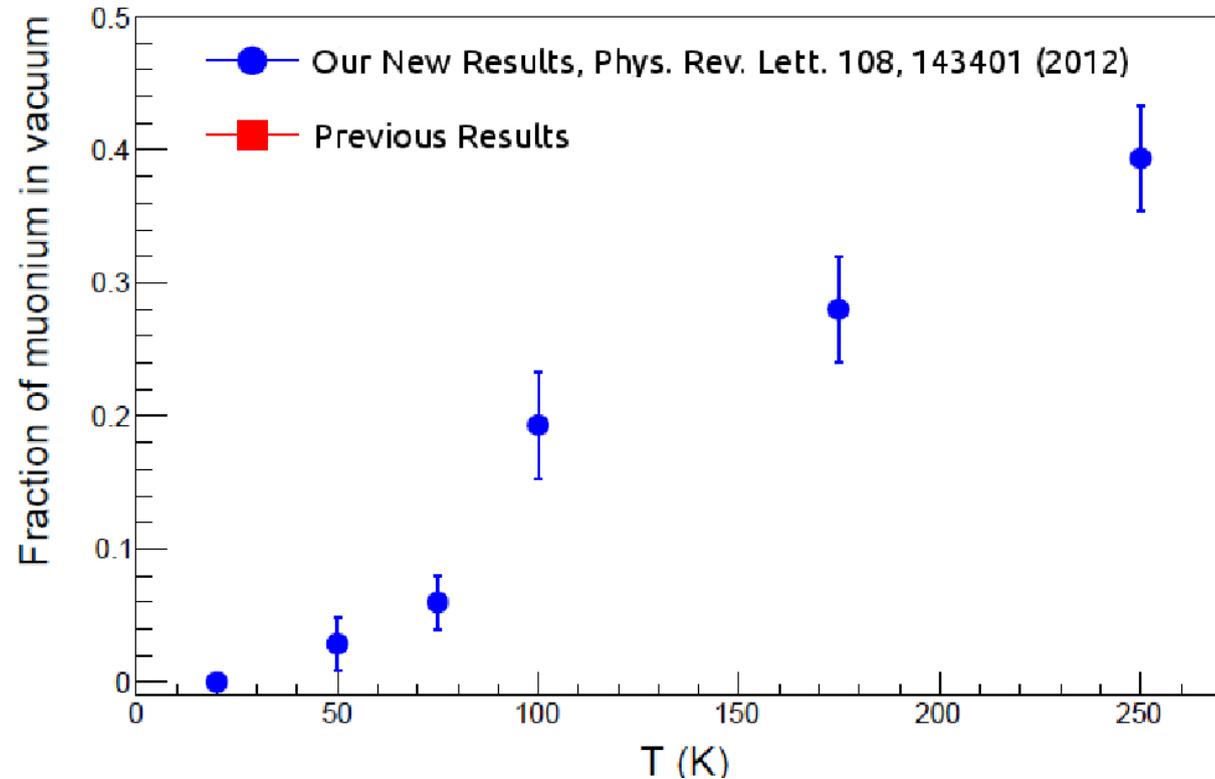
<sup>2</sup>*Paul Scherrer Institute, Villigen, Switzerland*

<sup>3</sup>*Department of Physics, Northeastern University, Boston, Massachusetts 02115, USA*

<sup>4</sup>*CEA, Irfu, Sédi, Centre de Saclay, F-91191 Gif-sur-Yvette, France*

(Received 23 December 2011; published 3 April 2012)

# Results of Mu production into vacuum

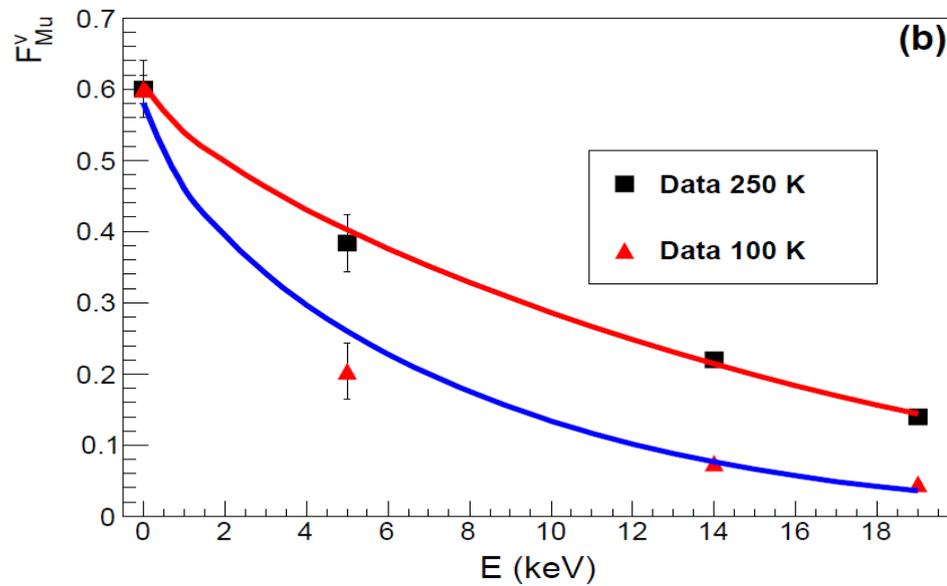


Sizeable fraction of thermalized muonium emitted into vacuum from SiO<sub>2</sub> thin film at 5 keV implantation energy:

- At 250 K, the yield (38%) is more than a factor of two higher than previously found in SiO<sub>2</sub> powders at room temperature (RT).
- At 100 K, the yield (20%) is still as large as previously found at RT.

# Mu diffusion

$$F_{\text{Mu}}^v(E) = F_{\text{Mu}}^0(E)J(E)$$



Solution of 1D diffusion model

$$J(E) = \int_0^l e^{-\beta x} P(x, E) dx$$

$\mu^+$  implantation profile  $P(x, E)$

Inverse of diffusion length

$$\beta = 1/\sqrt{D_{\text{Mu}}\tau}$$

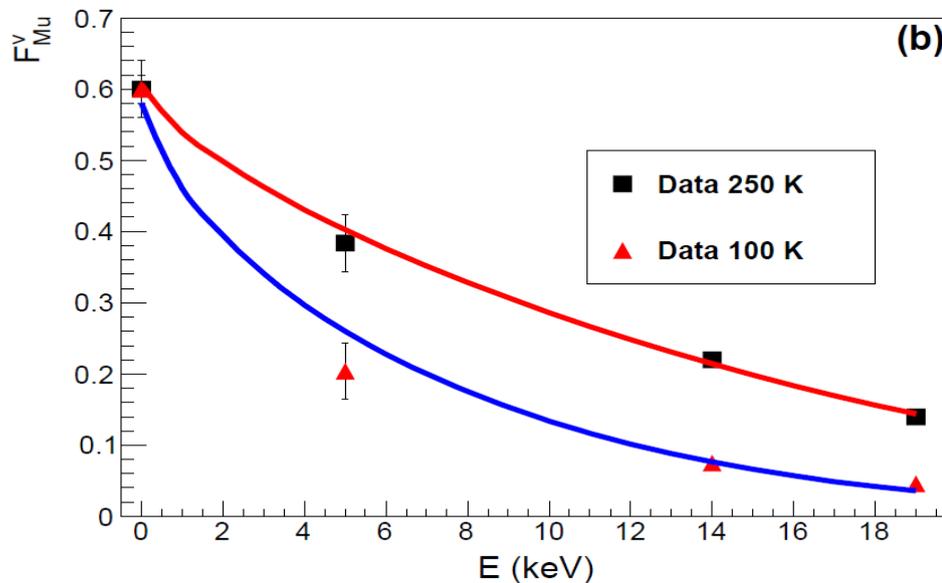
Model developed for Ps:

A. Mills and C. Murray, Appl. Phys. 21, 323 (1980)

K. Lynn and H. Lutz, Phys. Rev. B22, 4143 (1980)

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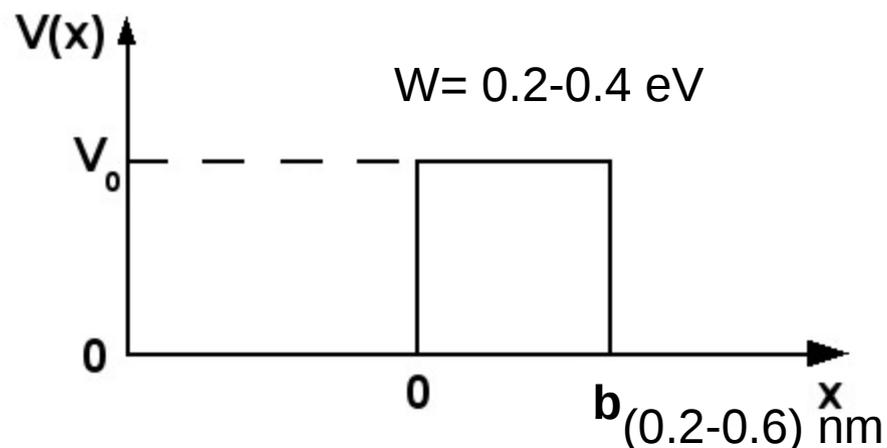
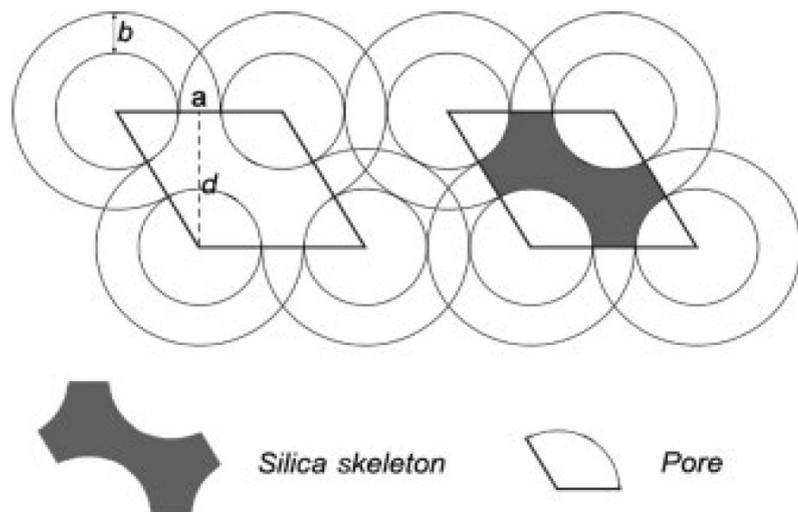
$$D_{\text{Mu}}^{250\text{K}} = (1.6 \pm 0.1) \times 10^{-4} \text{ cm}^2/\text{s}$$

$$D_{\text{Mu}}^{100\text{K}} = (4.2 \pm 0.5) \times 10^{-5} \text{ cm}^2/\text{s}$$

3 orders of magnitude smaller than expected from a classical diffusion model as used to for SiO<sub>2</sub> powders ( $D_{\text{mu}} \sim \text{meanfreepath} \cdot v_{\text{Mu}}$ )!

G. Marshall et al. Phys. Rev. D25 1174 (1982)

# Pore-to-pore QM tunneling



Our model: diffusion of Mu as quantum mechanical tunneling from pore-to-pore.  
Tunneling probability at a potential barrier for  $E < V_0$ :

$$P_t = \frac{1}{1 + \frac{V_0^2 \sinh^2(b\sqrt{2m_{\text{Mu}}/h^2}(V_0 - E))}{4E(V_0 - E)}}$$

Since in our regime the tunneling probability scales approximately linearly with  $T$ :

$$D_{\text{Mu}}(T) \propto P_t \sqrt{E_{\text{Mu}}} \propto T \sqrt{T} \propto T^{3/2}$$

Measured ratio  $D_{\text{Mu}}^{250\text{K}} / D_{\text{Mu}}^{100\text{K}} \approx 3.8 \pm 0.5$ .

Expected value from the  $T^{3/2}$  dependence of  $(250\text{K}/100\text{K})^{3/2} \approx 4$

# 1S-2S spectroscopy of Ps and Mu

Our results on Ps and Mu formation open the way to improve the accuracy of the 1S-2S frequency interval measurements of leptonic atoms.

The 1S-2S signal rate is proportional to

$$R \sim N_{\text{Mu}} \cdot I^2 \cdot t^2$$

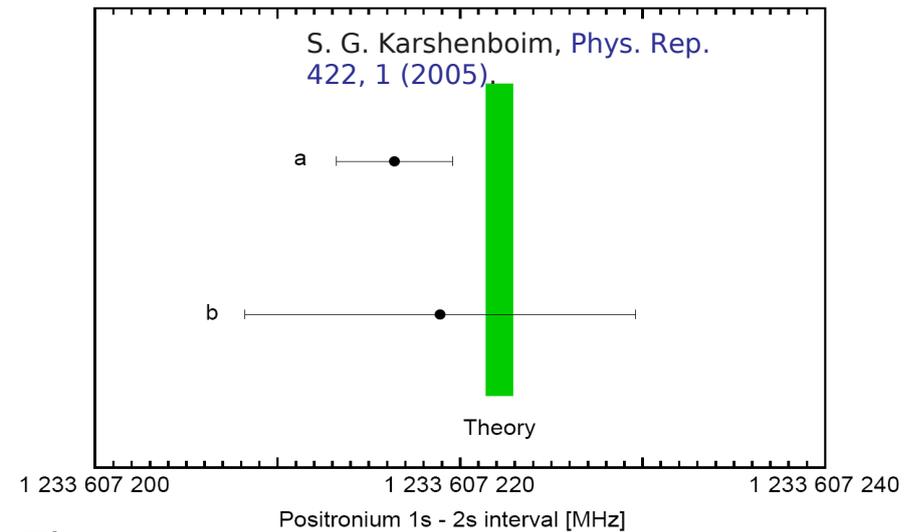
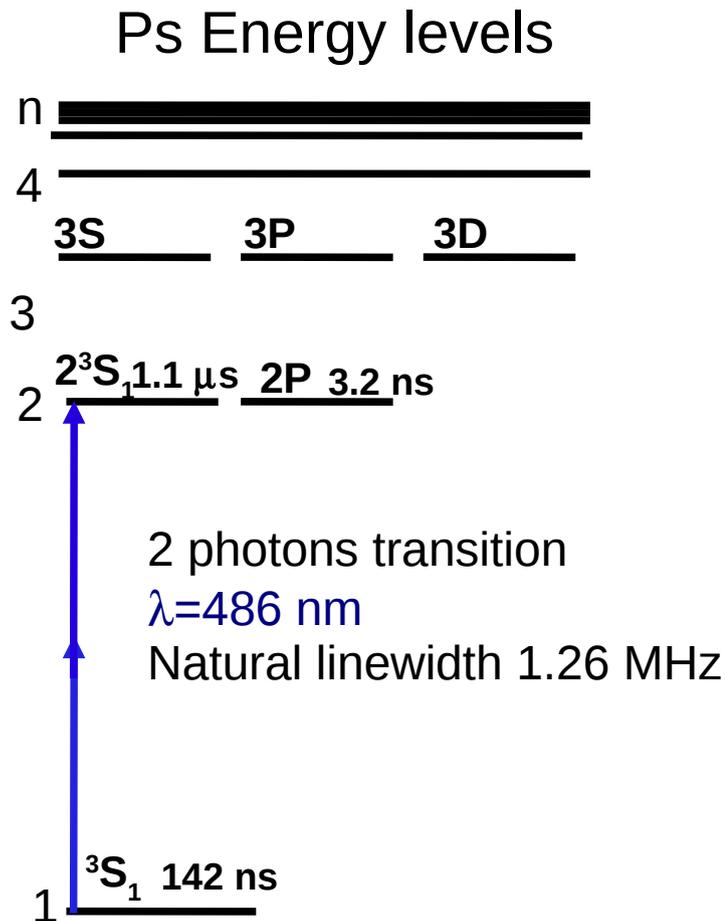
where

$$\left\{ \begin{array}{ll} N : & \text{Ps/Mu production rate} \\ I : & \text{Laser intensity} \\ t \sim v^{-1} : & \text{Interaction time} \end{array} \right.$$

Ps/Mu source with **high yield** and **low energy**

- Decrease requirements of laser intensity
- Decrease systematical effects
- Increase statistical significance

# Positronium 1S-2S transition



Theory

$$\nu^{theory} = 1233607222.2(6) \text{ MHz}$$

K. Pachucki and S. G. Karshenboim, Phys. Rev. A60, 2792 (1999),  
 K. Melnikov and A. Yelkhovsky, Phys. Lett. B458, 143 (1999).

Experiment

$$\nu^a = 1233607216.4(3.2) \text{ MHz}$$

M. S. Fee et al., Phys. Rev. Lett. 70, 1397 (1993)

$$\nu^b = 1233607218.9(10.7) \text{ MHz}$$

S. Chu, A. P. Mills, Jr. and J. Hall, Phys. Rev. Lett. 52, 1689 (1984)

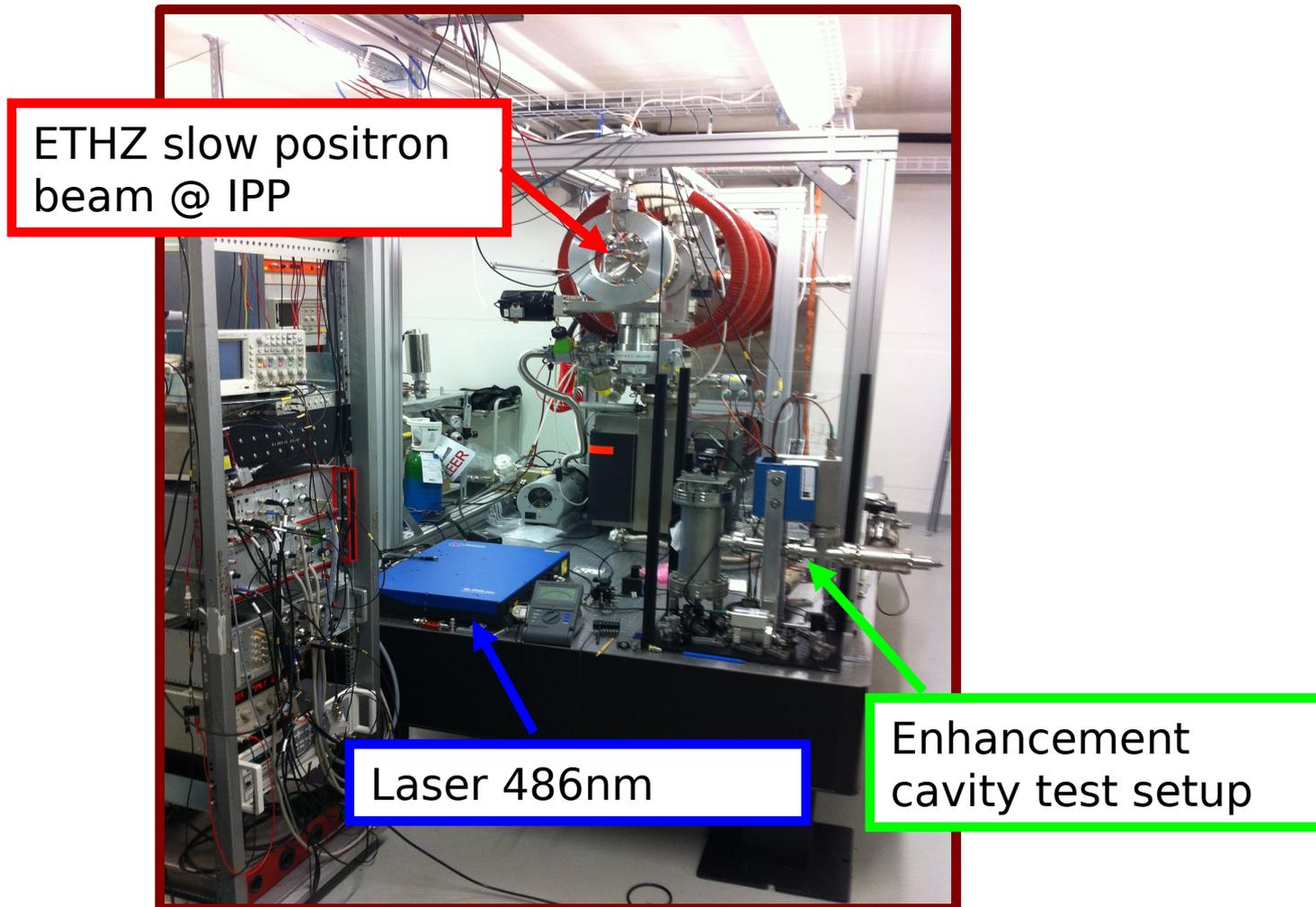


Measurement of 1S-2S of Ps at a level about  $5 \times 10^{-10}$  => check QED calculations at the order  $\alpha^7 m$  and provide the best determination of  $m_{e^+}/m_{e^-}$ .

# New measurement @ ETH

P. Crivelli (ETHZ), D. Cooke (ETHZ), A. Antognini (ETHZ), K. Kirch (ETHZ/PSI),  
J. Alnis (MPQ), T. Haensch (MPQ), B. Brown (MU, USA)

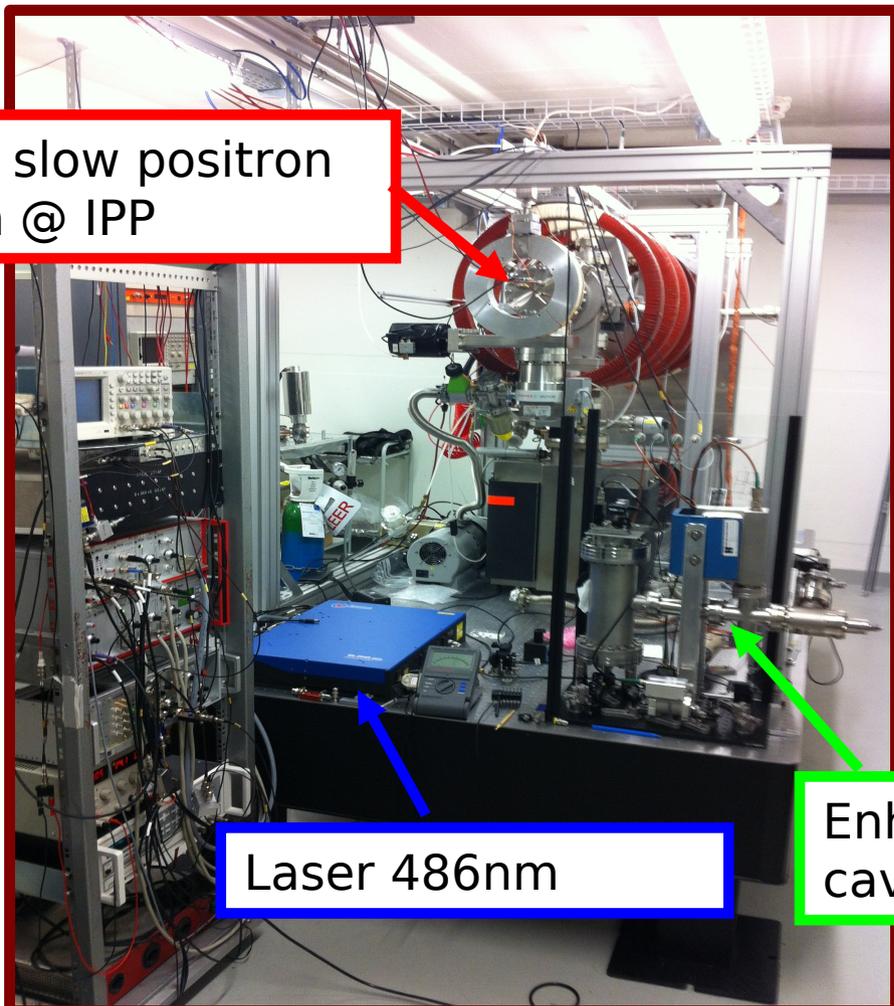
Project supported by the SNSF and ETH started in April 2011.



# New measurement @ ETH

P. Crivelli (ETHZ), D. Cooke (ETHZ), A. Antognini (ETHZ), K. Kirch (ETHZ/PSI), J. Alnis (MPQ), T. Haensch (MPQ), B. Brown (MU, USA)

Project supported by the SNSF and ETH started in April 2011.

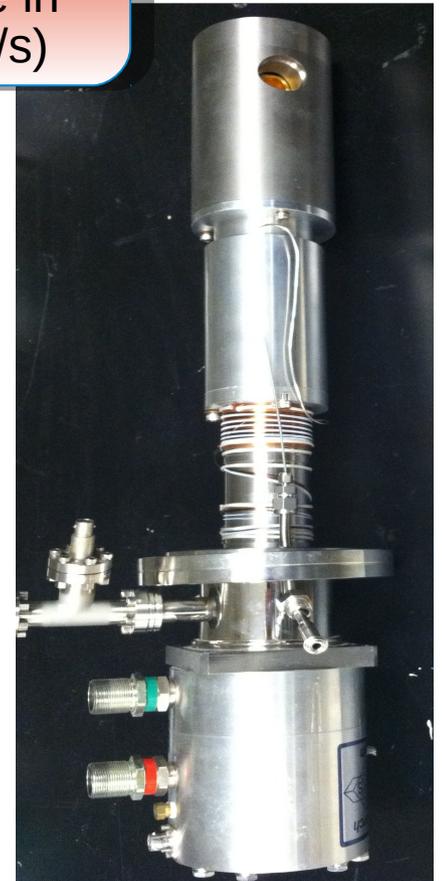


ETHZ slow positron beam @ IPP

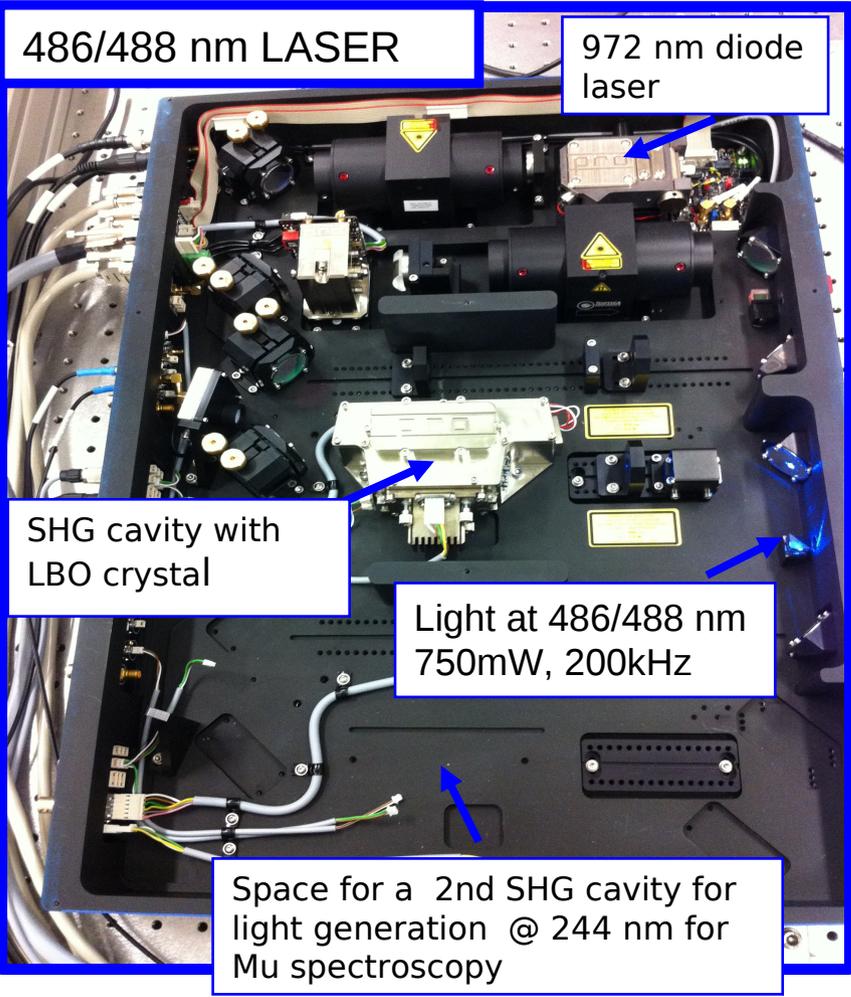
W moderator replaced with solid Ne:  
-> Factor 20 increase in  $e^+$  flux ( $2 \times 10^5 e^+/s$ )

Laser 486nm

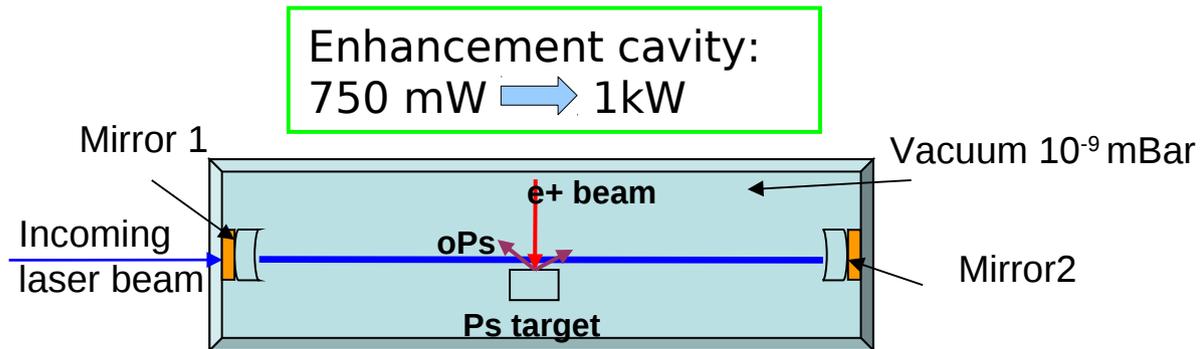
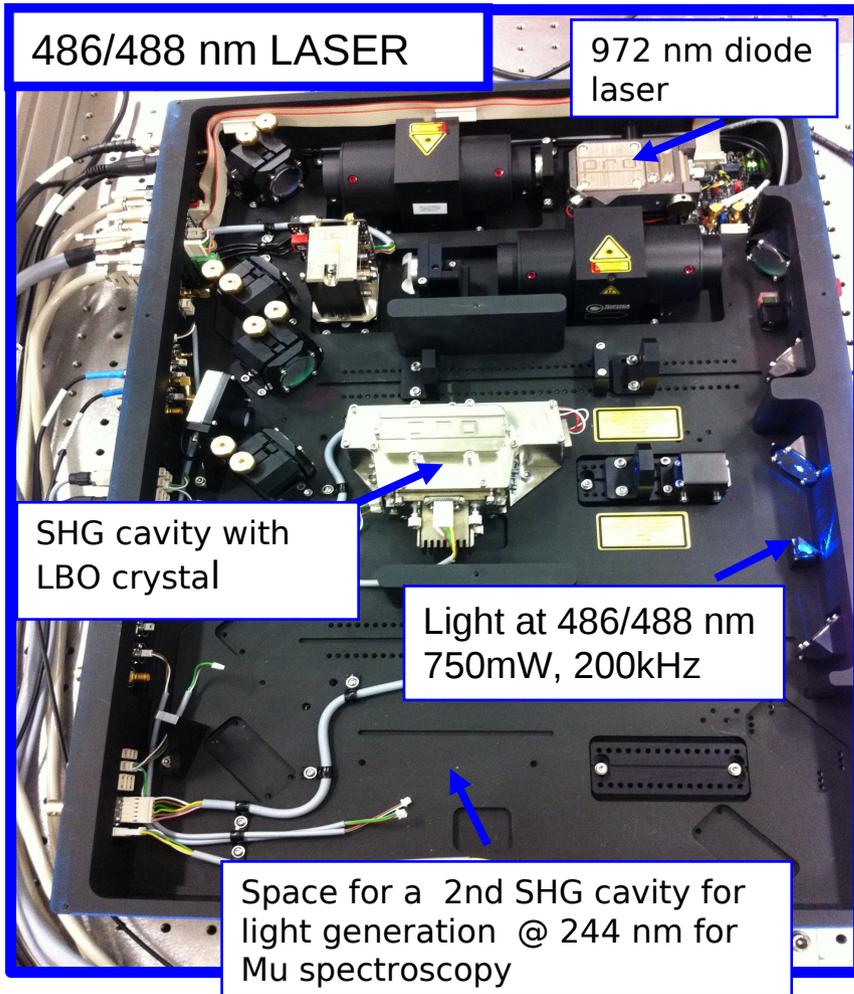
Enhancement cavity test setup



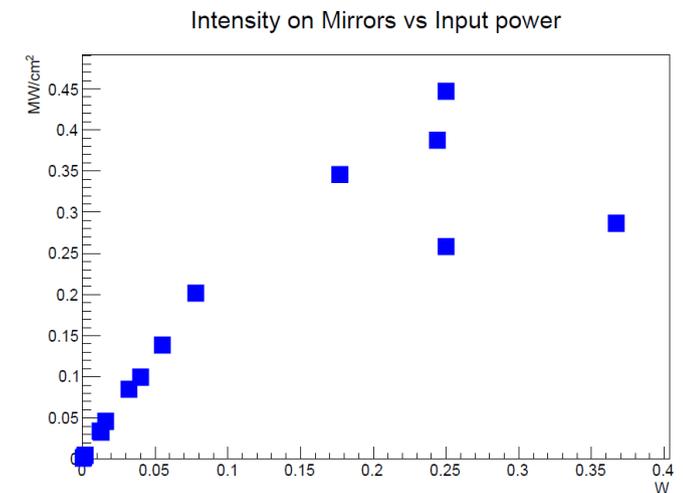
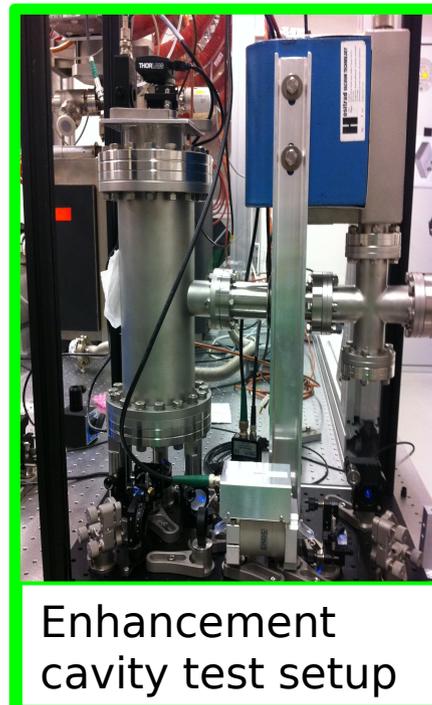
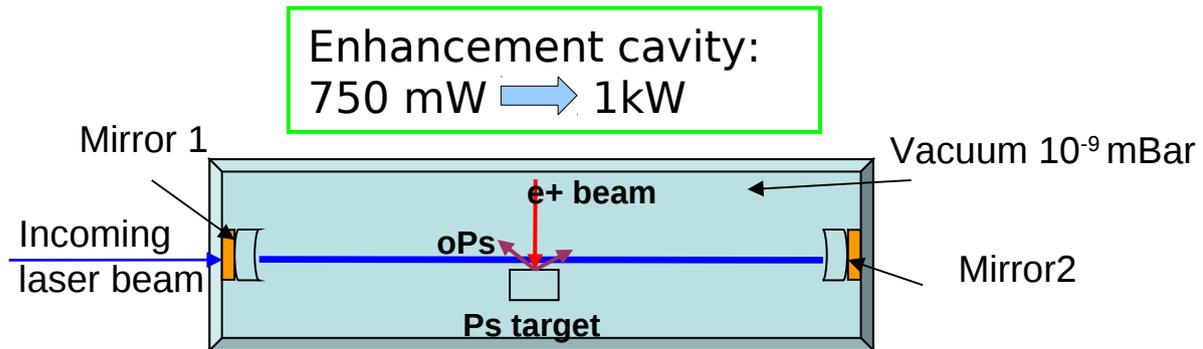
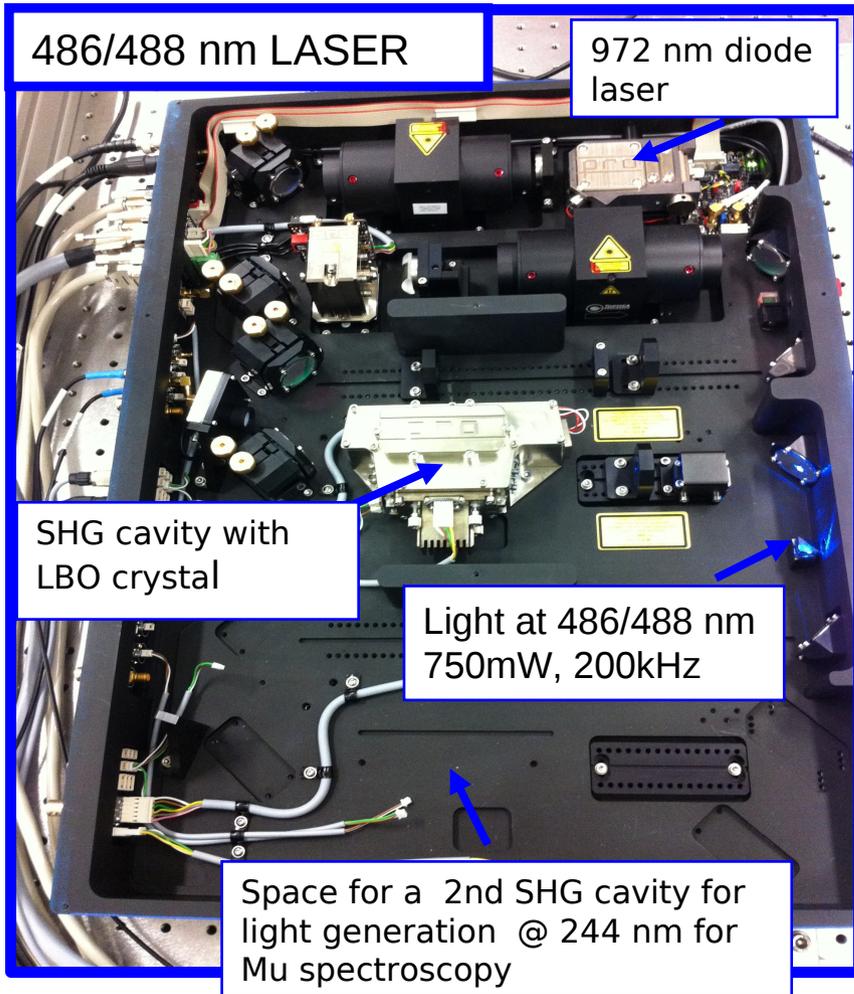
# The laser (Ps and Mu)



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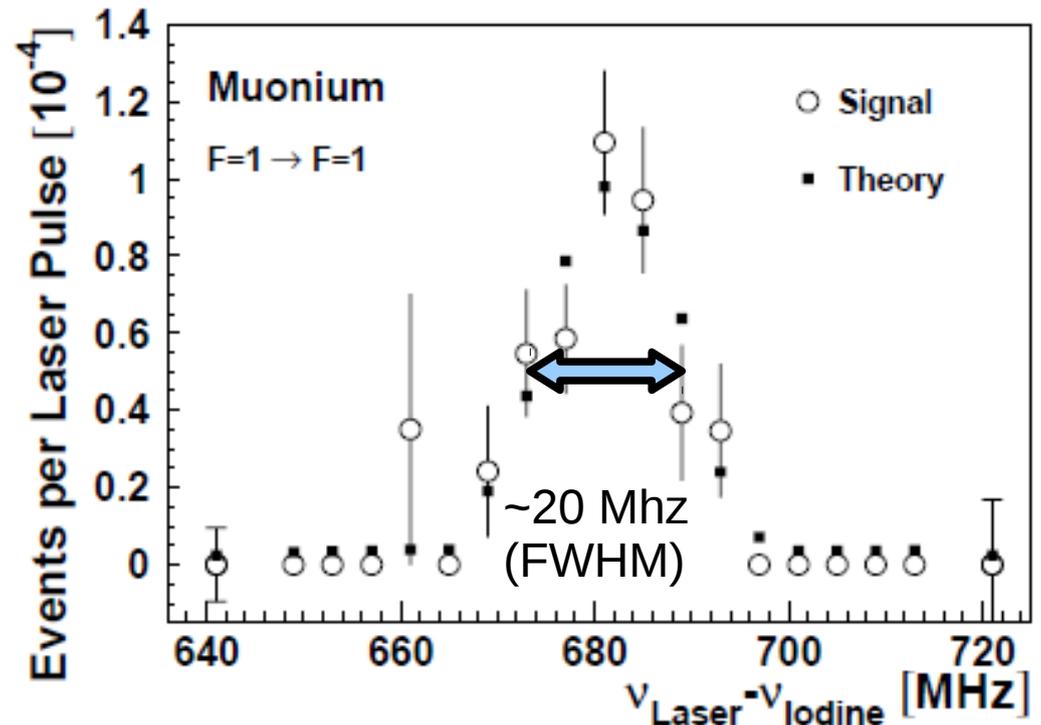
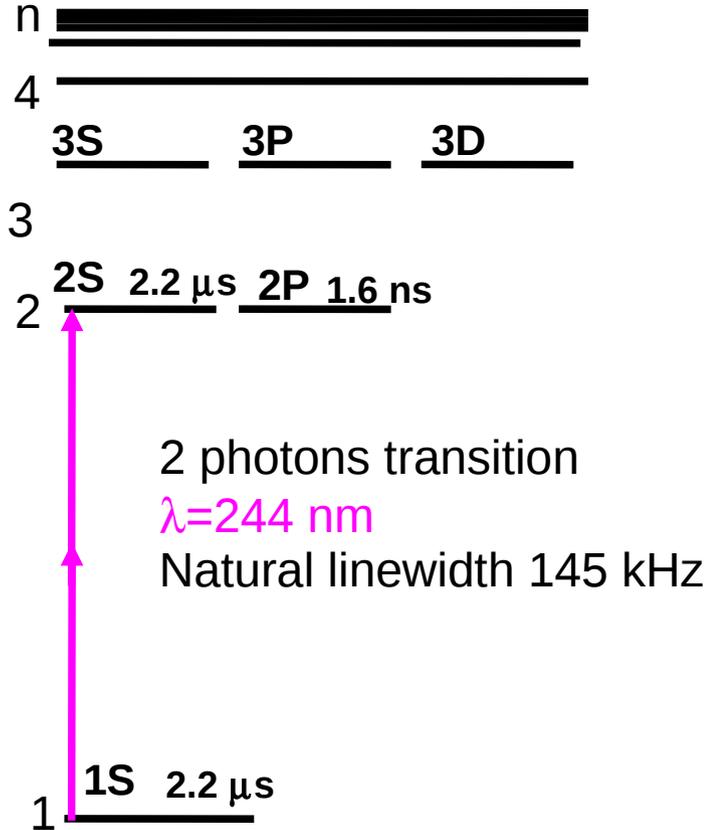
# The laser (Ps and Mu)



More than 1 kW circulating power before mirror degradation  
 -> **Excitation rate = 0.01 \* (Number of Ps in vacuum)**

# Status of Muonium 1S-2S

## Mu Energy levels



$$\Delta\nu_{1s2s}(\text{expt.}) = 2\,455\,528\,941.0(9.8) \text{ MHz}$$

V. Meyer et al., Phys. Rev. Lett. 84, 1136 (2000).

$$\Delta\nu_{1s2s}(\text{theory}) = 2\,455\,528\,935.4(1.4) \text{ MHz}$$

J. R. Sapirstein and D. R. Yermie, in: QED, T. Kinoshita (ed.), World Scientific, Singapore, p.560

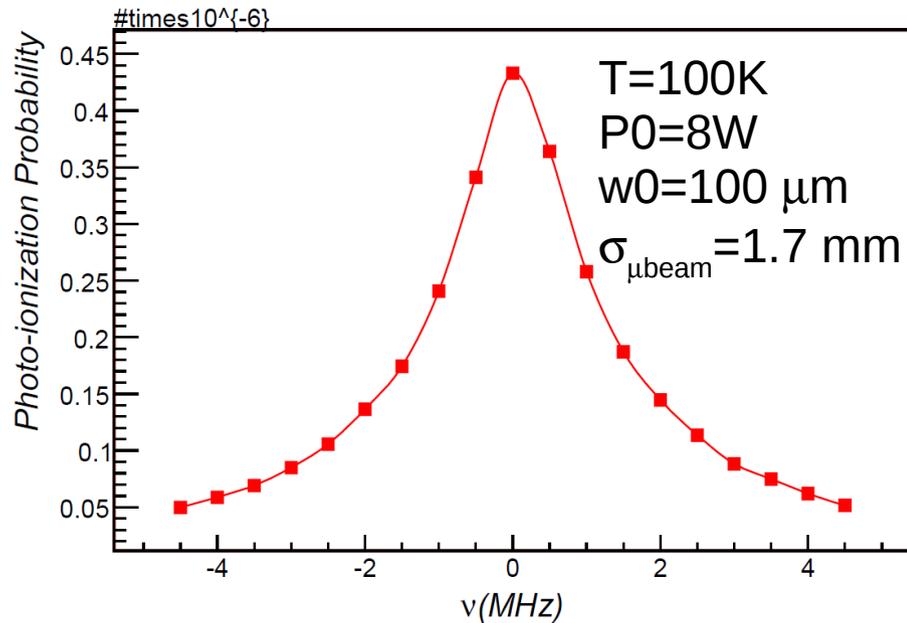


$$m_{\mu^+}/m_{e^-} = 206.768\,38(17)$$

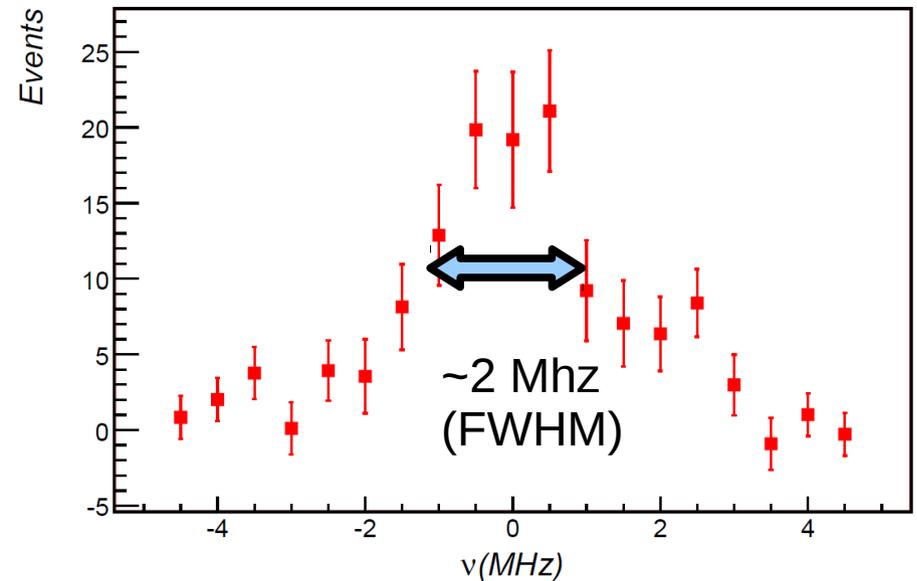
$$q_{\mu^+}/q_{e^-} = -1 - 1.1(2.1) \cdot 10^{-9}$$

# Expected signal rate and accuracy

Simulated lineshape



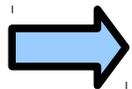
Expected resonance curve



With a similar setup as the existing LEM beam @PSI 4000  $\mu^+$  /s

-> On resonance 27 events/day expected and 2.5 background/events per day.

-> Such a measurement would take 2 weeks time



Measurement of 1S-2S of Mu at a level about  $1 \times 10^{-9}$  => check QED calculations and provide best determination of  $m_{\mu^+}/m_{e^-}$  and  $q_{\mu^+}/q_{e^-}$ .

# Summary & Outlook

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## Positronium

- The beam intensity has been increased by a factor of 20.
- The laser power necessary for the measurement has been produced.
- The stabilization of the laser to 1 kHz is in progress.
- Promising targets for Ps production at cryogenic temperature have been prepared and will be tested soon.
- Results expected for 2014.

# Summary & Outlook

---

## Positronium

- The beam intensity has been increased by a factor of 20.
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## Muonium

- Our results on Mu formation open the way to the first continuous wave spectroscopy of the 1S-2S transition -> an improvement in the accuracy of a factor of 10 is possible (result limited by statistical uncertainty)
- We were granted 5 days beam time at the end of July 2012 at the LEM facility (PSI). Analysis of the data is in progress.
- The laser system is under development for the Ps experiment.

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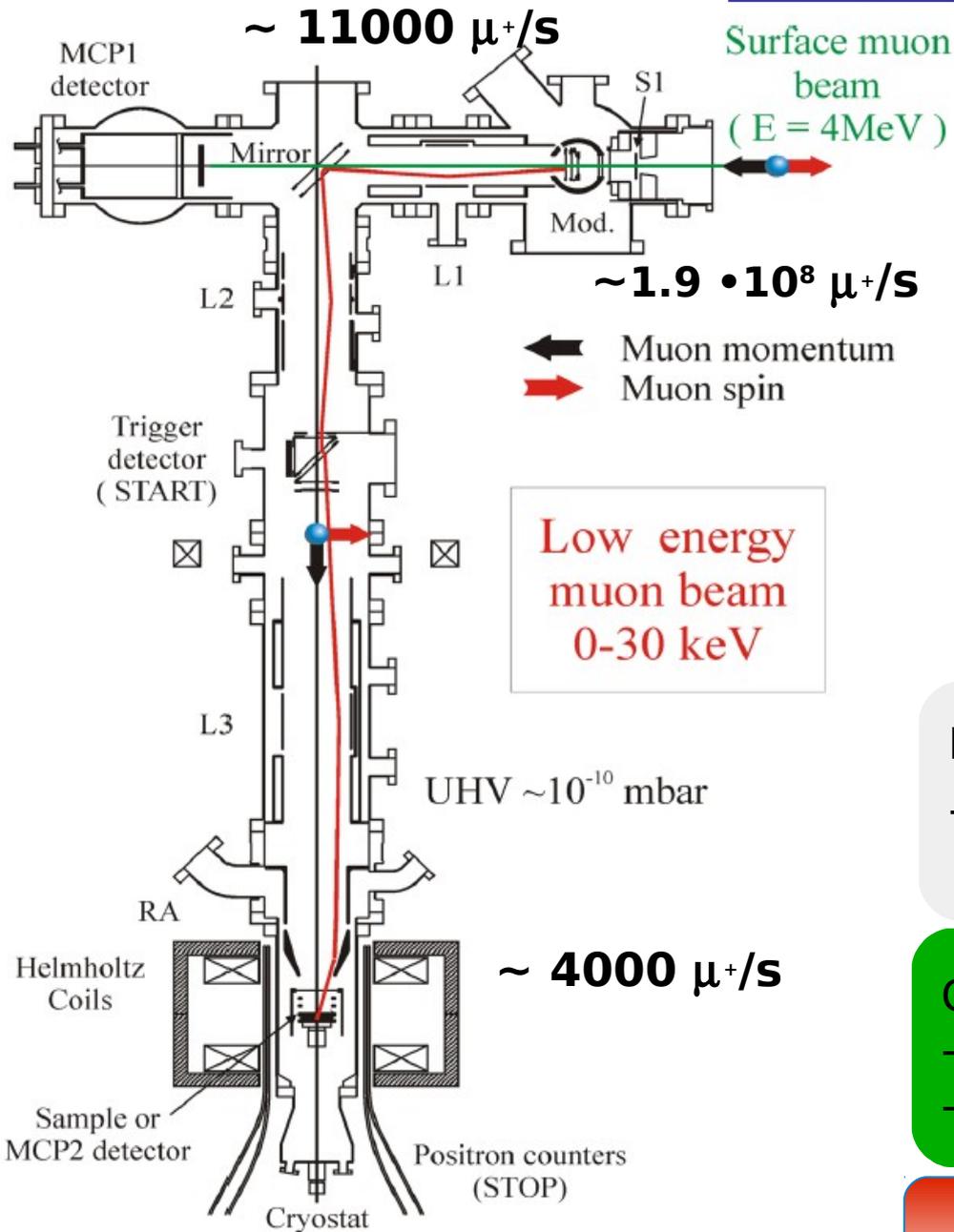
Thank you very much for your attention!

# Backup slides

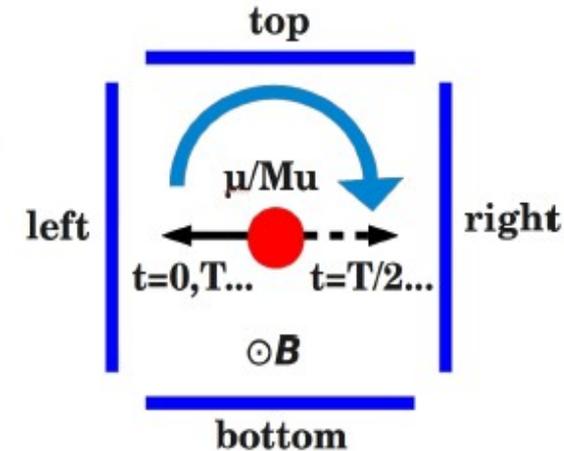
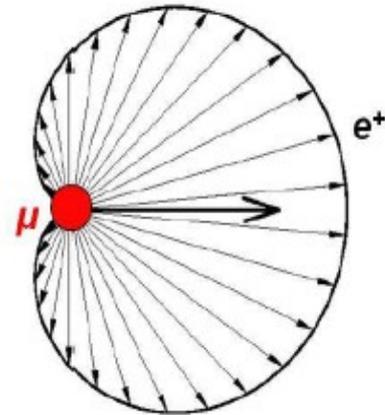
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# Low energy muon (LEM) beam @PSI

T. Prokscha, et al., NIM. A 595, 317 (2008)



## Muon spin rotation technique (muSR)

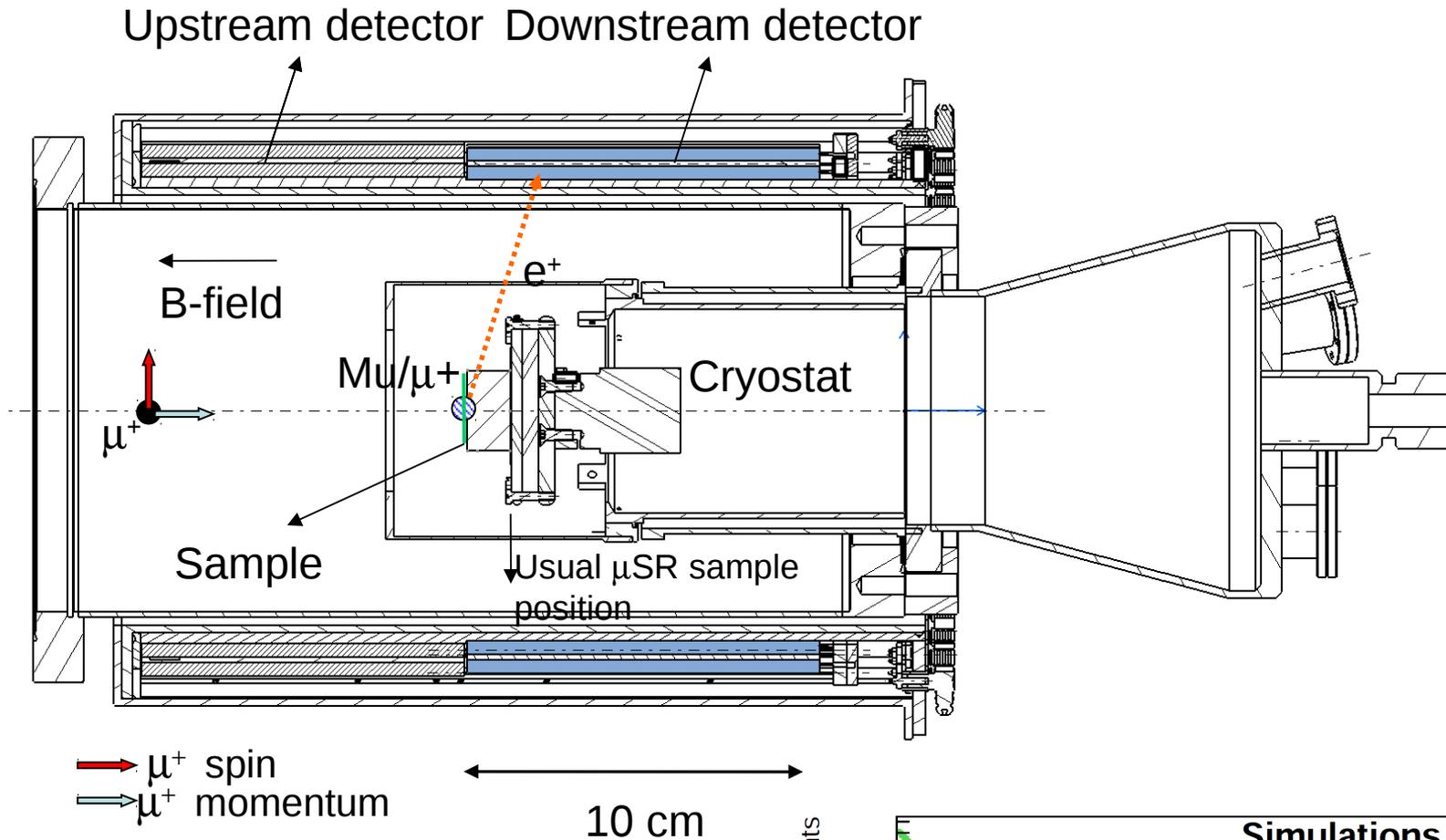


Larmor precession:  $\omega_{\text{Mu}} = 103 \omega_{\mu^+}$   
 -> possible to distinguish if an implanted  $\mu^+$  remains unbound or forms Mu

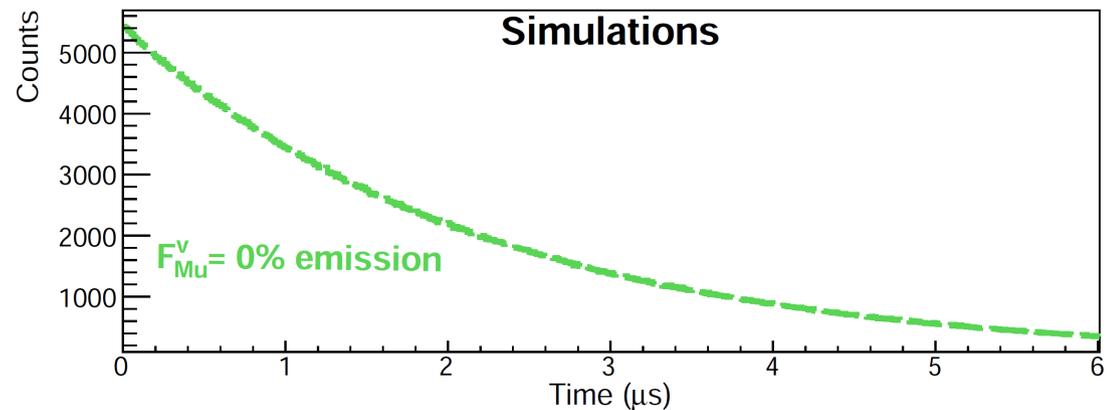
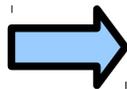
Our muSR results:  
 -> 60% of  $\mu^+$  converts to Mu  
 -> 25% of Mu retain their polarization

Fraction of Mu emitted into vacuum ?

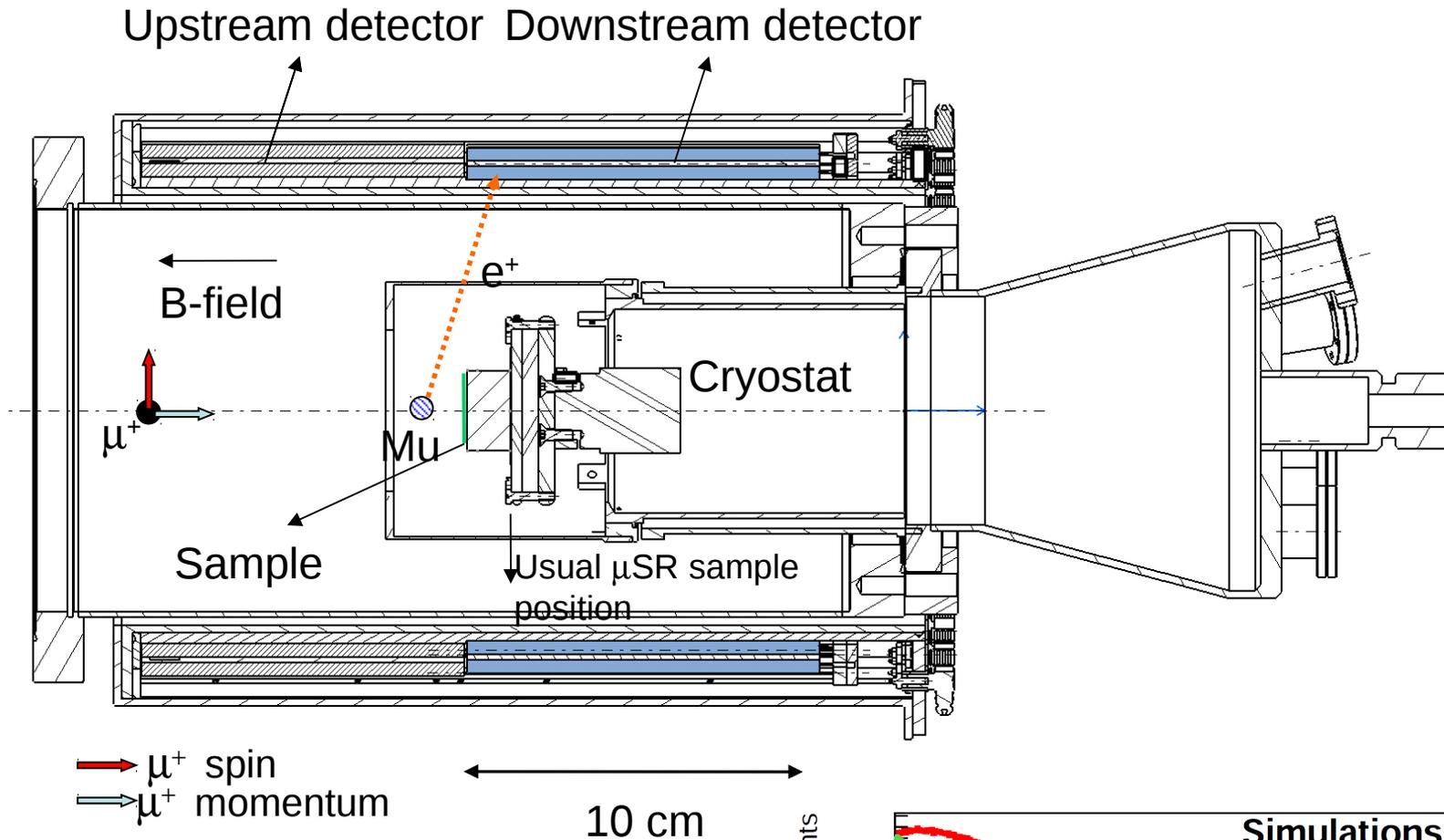
# Positron shielding technique (PST)



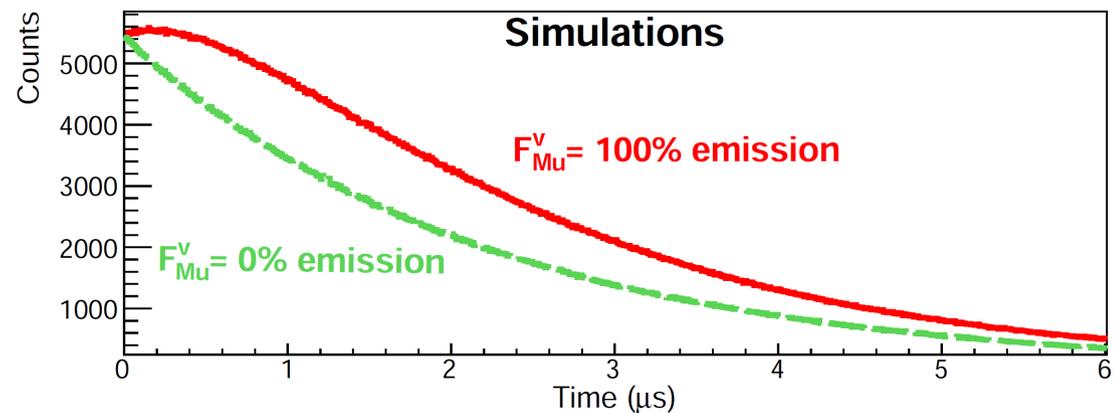
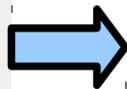
No emission in vacuum  
Exponential decay distribution  
From Mu and  $\mu^+$  decays



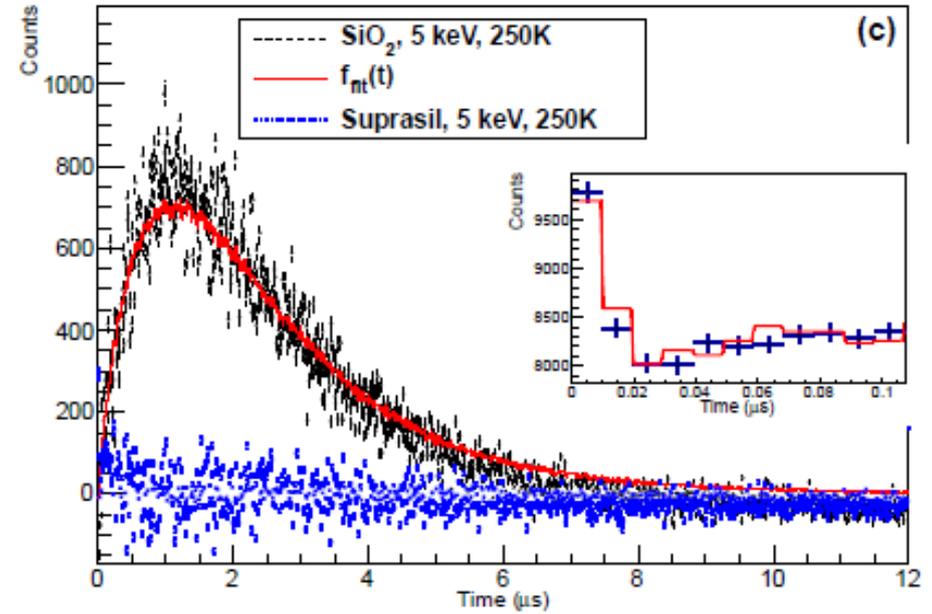
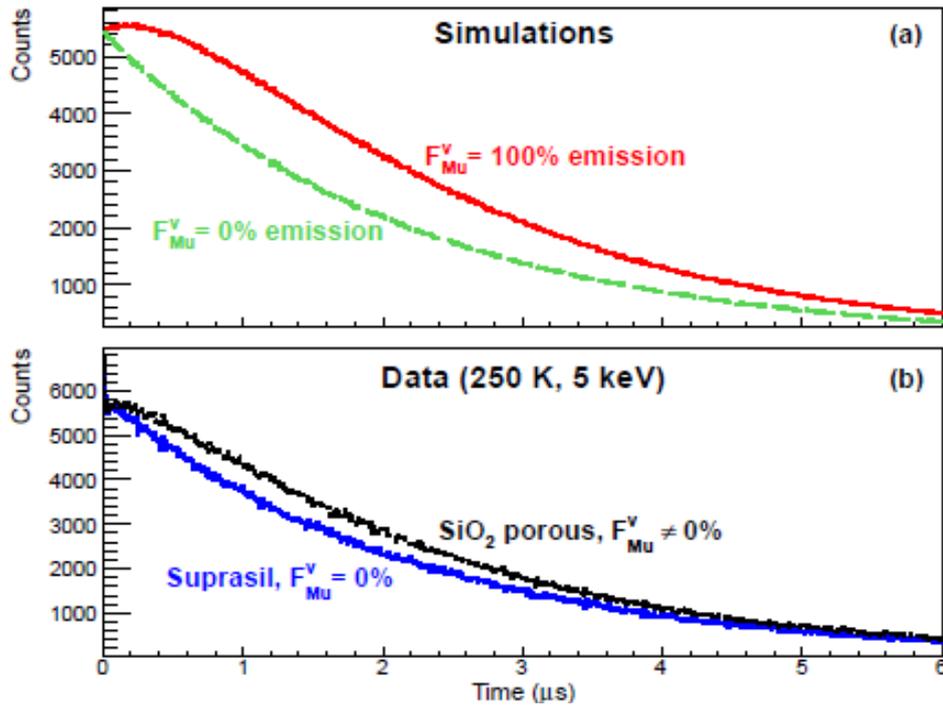
# Positron shielding technique (PST)



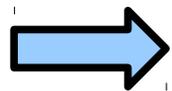
Mu emission in vacuum  
detection efficiency in downstream  
detector is time dependent ->  
deviation from exponential decay



# PST results

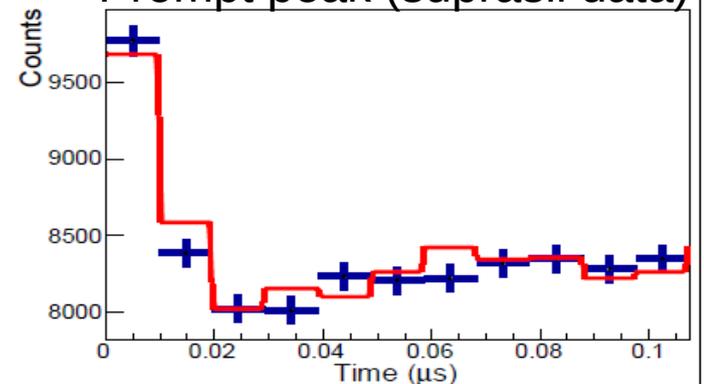


$$f_{\text{fit}}(t) = n[(1 - F_{Mu}^v)f_0(t) + F_{Mu}^vf_{100}(t)] + n_{pp}f_{pp}(t)$$

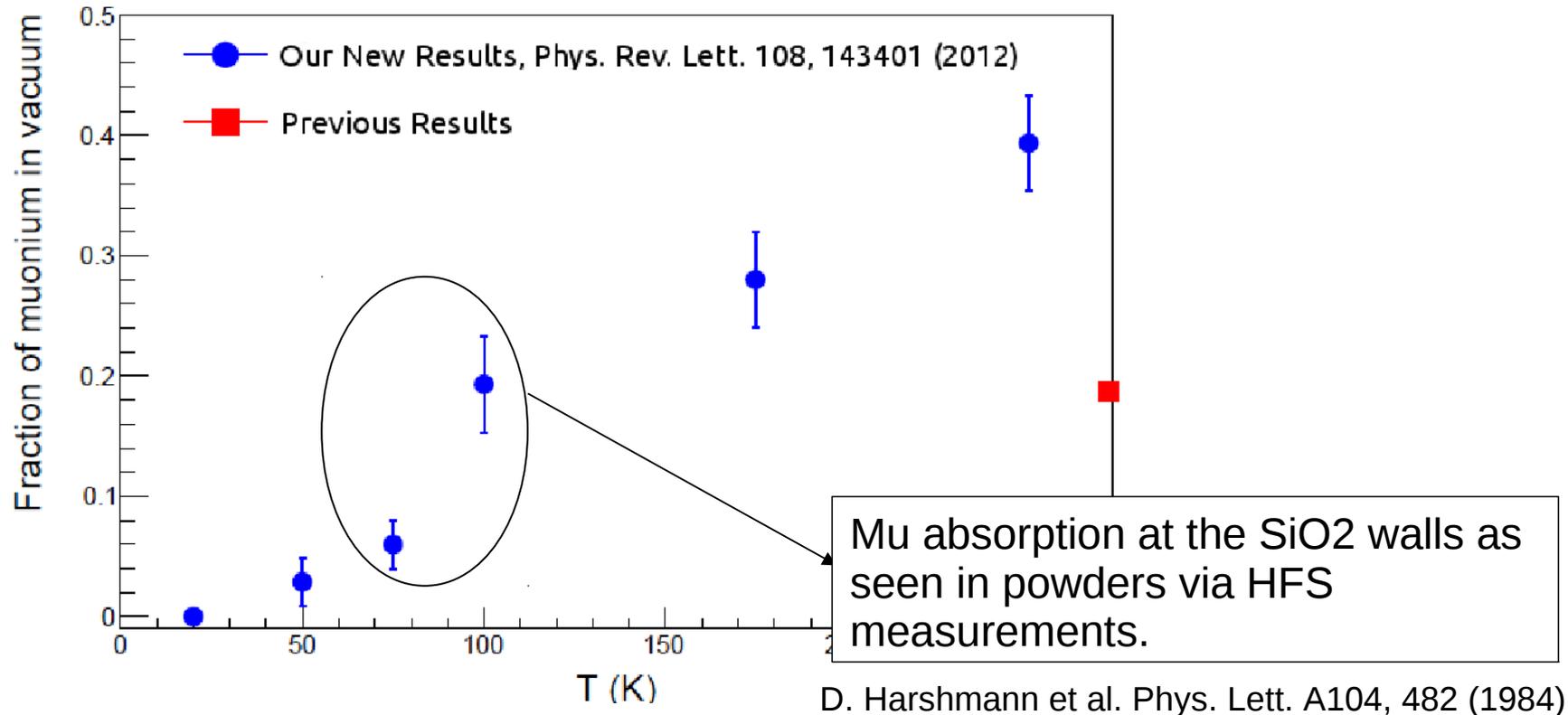


Vacuum yield  $F_{Mu}^v$

Prompt peak (suprasil data)



# PST results



Mu absorption at the SiO<sub>2</sub> walls as seen in powders via HFS measurements.

D. Harshmann et al. Phys. Lett. A104, 482 (1984)

Sizeable fraction of thermalized muonium emitted into vacuum from SiO<sub>2</sub> thin film at 5 keV implantation energy:

- At 250 K, the yield (38%) is more than a factor of two higher than previously found in SiO<sub>2</sub> powders at room temperature (RT).
- At 100 K, the yield (20%) is still as large as previously found at RT.

# Expected accuracy

---

With available source of Ps (30% @ 40 meV)

1) Uncertainty from statistics 1.8 MHz -> 0.3 MHz.

-Better positron beam

-Higher detection efficiency based on the lifetime method

-Long term stability of the laser system

2) Systematic uncertainty 1.9 MHz -> 0.4 MHz.

- Main contribution of 1993 exp. unknown parameters in photoionization laser  
→ proposed method free of this systematic.

- Main systematic 2<sup>nd</sup> order Dopplershift ~0.4 MHz

- No restriction of beam time (careful study the systematics)

Measurement of 1S-2S of Ps at a level about  $5 \times 10^{-10}$  => check QED



Colder (100K) Ps → higher precision  
(new porous films being prepared, CEA Saclay)

# Hydrogen spectroscopy

