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**Indirect Searches for
New Physics**

a personal perspective

Outline:

■ Introduction

- Indirect searches for New Physics
- Flavour violation in the Standard Model and the determination of the CKM matrix.
- Hints for NP?

■ Two Higgs Doublet Models

- Tauonic B decays in a 2HDM III

■ Minimal Supersymmetric Standard Model (MSSM)

- Constraints on the flavour structure and the “SUSY_FLAVOR” code
- Flavour violation from SUSY-breaking

■ Conclusions

Introduction

Indirect searches for New Physics

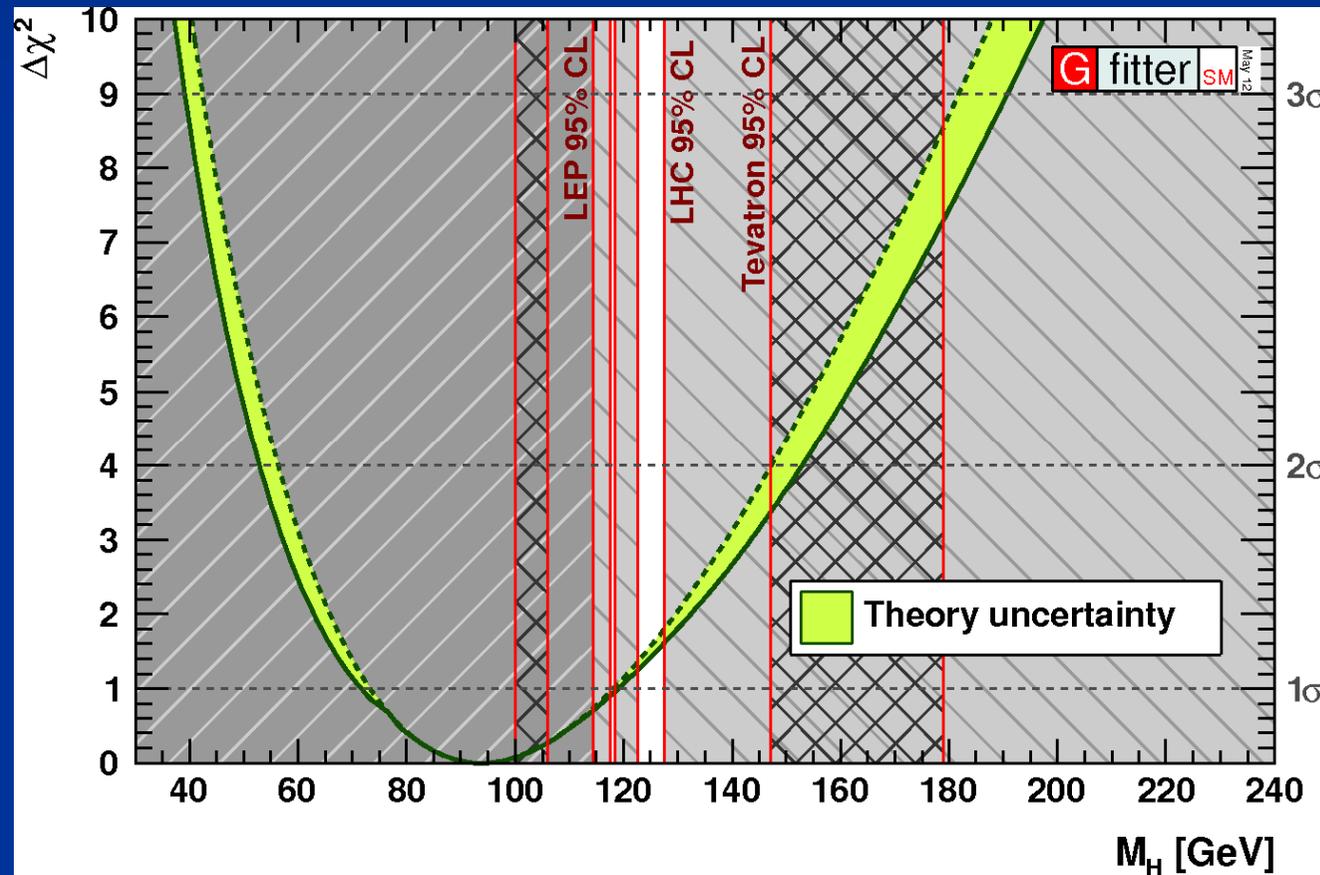
Indirect Searches for New Physics

Do low-energy observables which are sensitive to new (virtual) particles agree with the SM predictions?

- Tests of conservation laws
 - Proton decay (Baryon/Lepton number violation)
 - CPT violation
 - Neutrinoless double beta decay (lepton number violation)
- Electroweak precision observables
- Flavour observables
 - Anomalous Magnetic Moments
 - Electric dipole moments
 - Flavour-changing processes

Electroweak precision observables

- Higgs mass of 125 GeV fits well with the EW-precision data



Flavour-observables

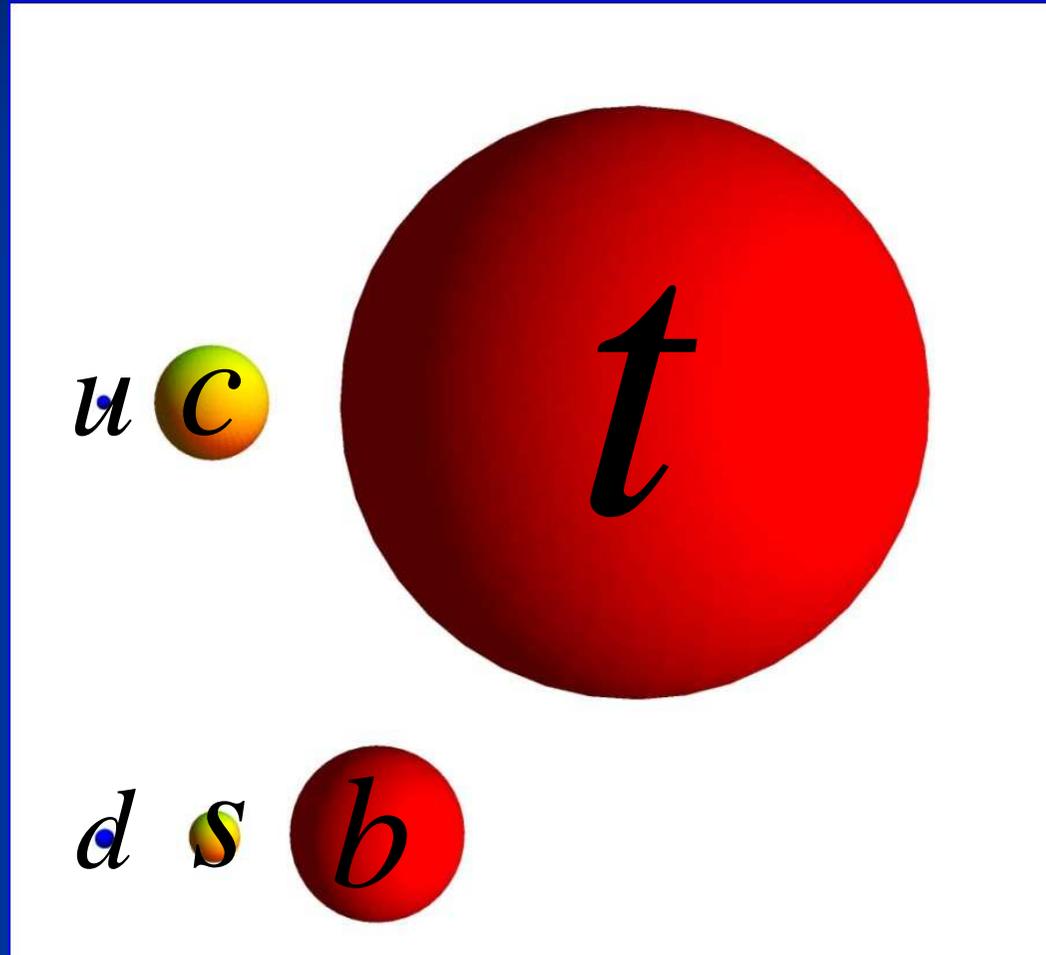
- Anomalous magnetic moments (g-2) sensitive to chirality violating New Physics
- Electric dipole moments (test flavour-blind CP violation)
- Lepton flavour violation
 - Neutrino oscillations
 - ➔ SM+ (with massive neutrinos)
 - Charged lepton flavour-violation
 $\mu \rightarrow e\gamma$, $\tau \rightarrow \mu\gamma$, $\tau \rightarrow e\gamma$, $\mu \rightarrow e$ conversion (forbidden in the SM)
- Quark flavour violation and CP violation
 - (Semi-) leptonic B and Kaon decays
 - Indirect determinations of the CKM matrix $\Delta F = 2$ processes
 - Rare decays $B_{d,s} \rightarrow \mu^+\mu^-$, $B_{d,s} \rightarrow \tau^+\tau^-$, $B \rightarrow \tau\nu$, $K \rightarrow \pi\nu\nu$
 $B \rightarrow X_{s,d}\gamma$

Quark flavour violation and the CKM matrix

Quark masses

- Coupling to the Higgs proportional to the mass.
- Bottom quark rather light, but Y^b can be big at large $\tan(\beta)$ in the MSSM or a 2HDM
- All other quark masses are very small

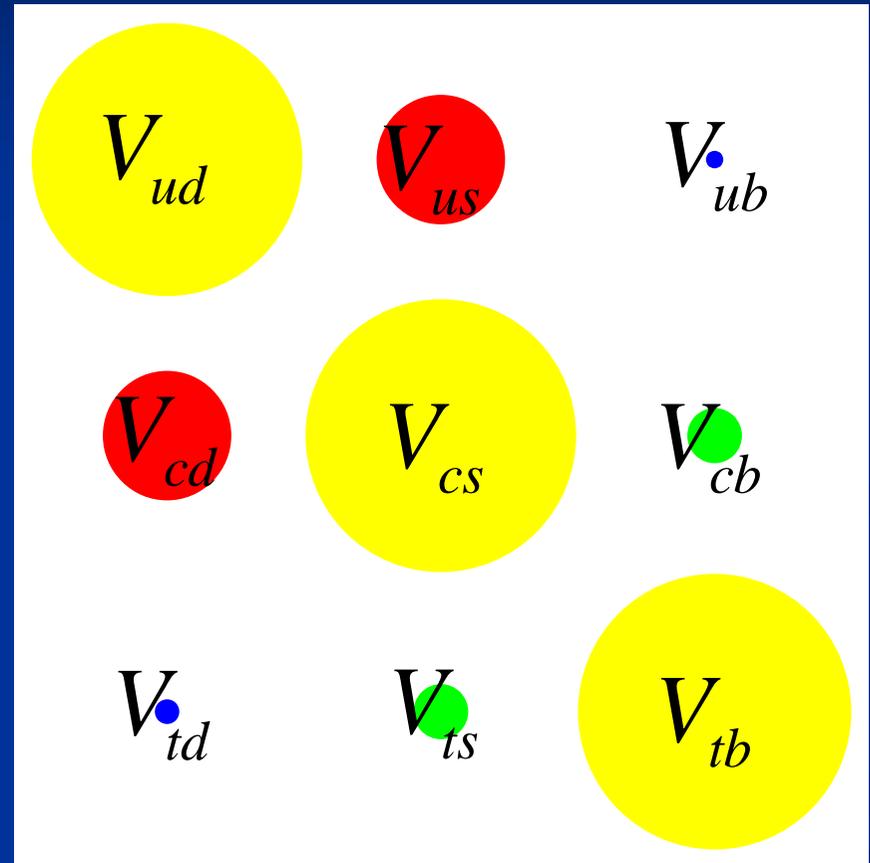
➔ sensitive to radiative corrections



CKM matrix

- CKM matrix is the only source of flavour and CP violation in the SM.
- No tree-level FCNCs
- Off-diagonal CKM elements are small
→ Flavour-violation is suppressed in the Standard Model.

$$V_{\text{CKM}} =$$



The Unitary Triangle

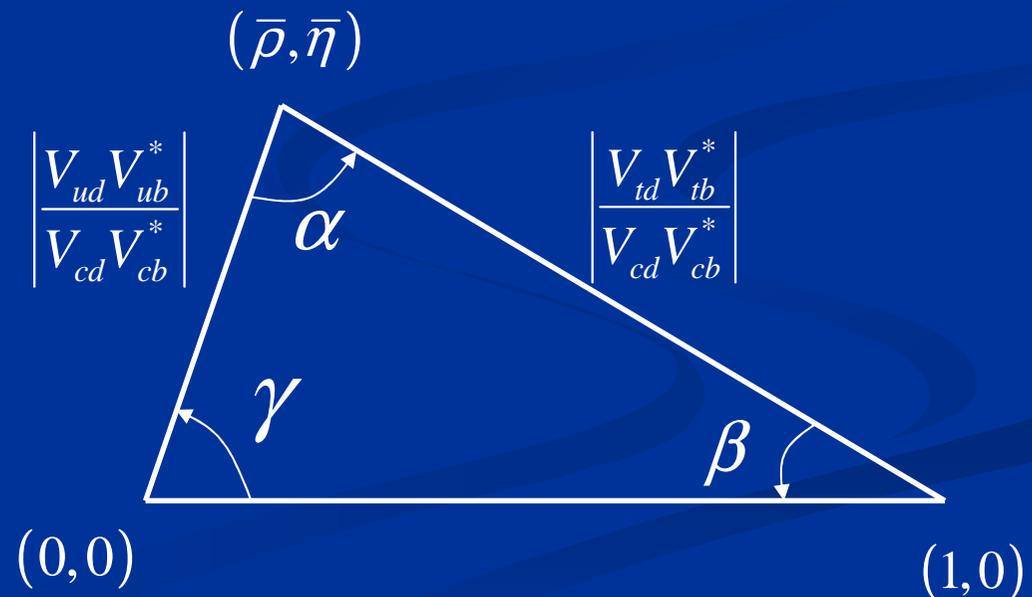
- 4 free parameter: 3 angles and 1 complex phase

$$V_{\text{CKM}} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

Unitary relation

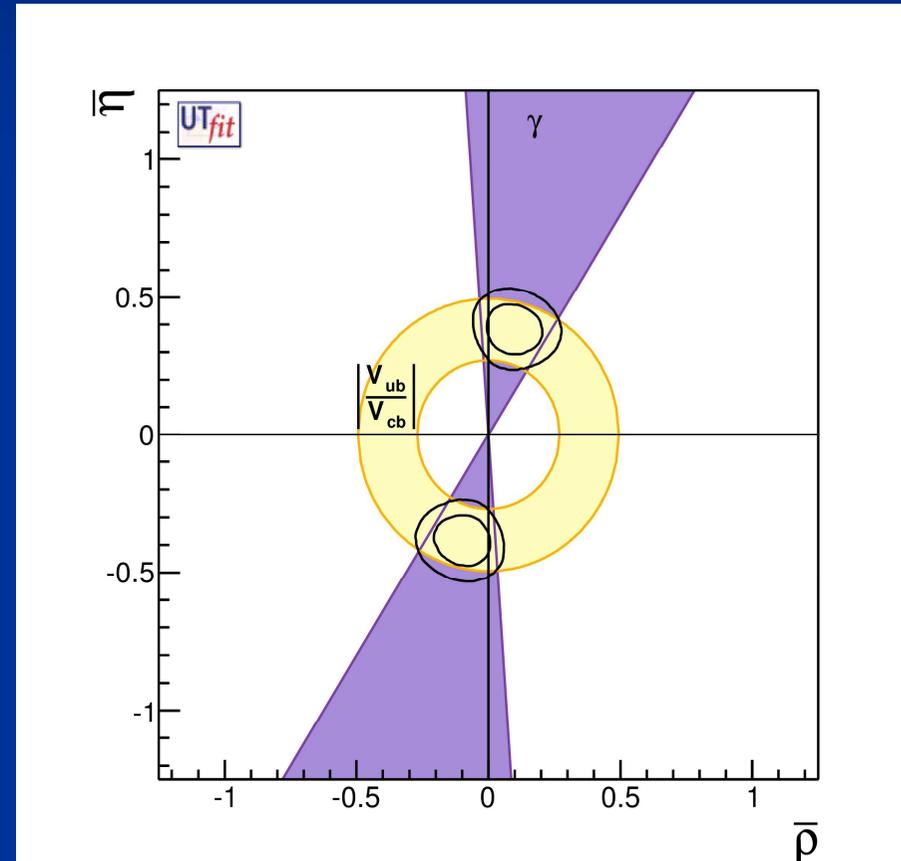
$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

$$\Rightarrow -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} - \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} = 1$$



Determination of the CKM elements from tree-level decays

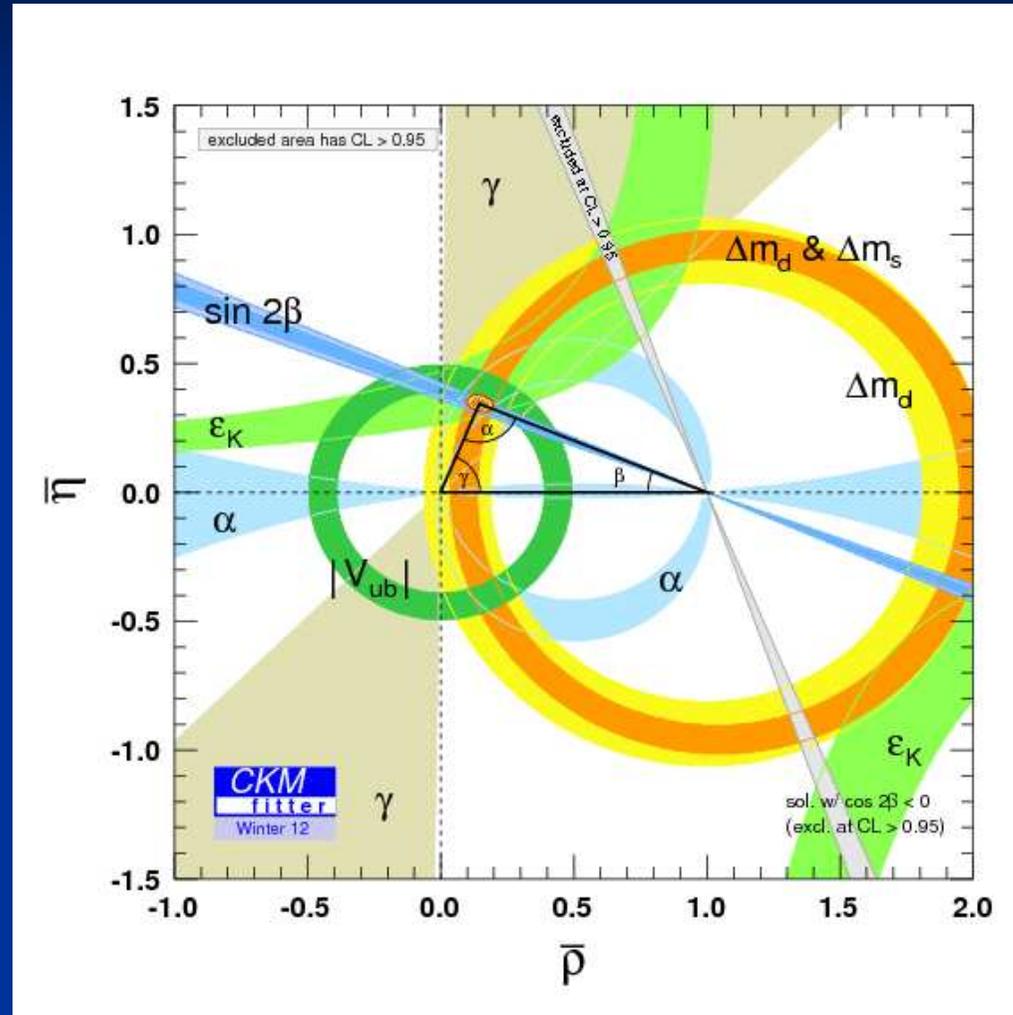
- Direct determination of $|V_{cb}|$ and $|V_{ub}|$ ($|V_{us}|$) from inclusive and exclusive semileptonic B (Kaon) decays.
 - In- and exclusive determinations of $|V_{cb}|$ agree reasonably (2.1σ)
 - New Belle result makes the $|V_{ub}|$ -problem from $B \rightarrow \tau \nu$ less severe. [arxiv:1208.4678](https://arxiv.org/abs/1208.4678)
- Determination of γ from $B^- \rightarrow D^0 K^-$, $B^- \rightarrow \bar{D}^0 K^-$



Global fit to the CKM matrix

- Determine UT including in addition constraints from loop-observables:
 - B_s mixing
 - B_d mixing
 - Kaon mixing
 - CP violation in B decays
- All determinations agree rather well

➔ CKM mechanism of flavour violation works very well

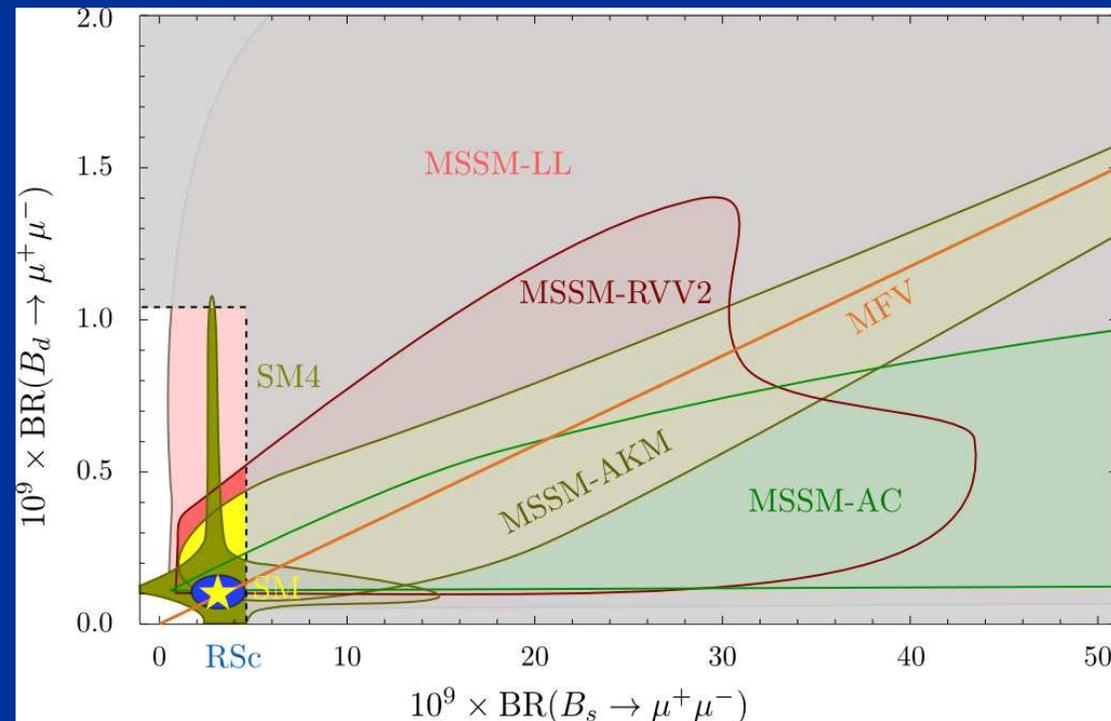


Rare decays

- $B \rightarrow X_s \gamma$ perfectly compatible with the SM
- $B_s \rightarrow \mu^+ \mu^-$ CDF found an excess but LHCb and CMS didn't confirm this. New upper bound close to the SM expectation.
- $B_d \rightarrow \mu^+ \mu^-$
new LHCb bound
- $K \rightarrow \pi \nu \nu$
waiting for Na62
- $B_d \rightarrow \tau^+ \tau^-$, $B \rightarrow K \nu \nu$
SuperB, Belle II

➔ No sign
of NP (yet)

Constraints on NP models



Plot from David Straub's talk at Moriond EW 2012

Hints for New Physics?

- CP violation in $D \rightarrow K^+K^-$, $D \rightarrow \pi^+\pi^-$
3.8 σ but large hadronic uncertainties.
- Anomalous magnetic moment of the muon
 $\sim 3.6 \sigma$ above the SM prediction
- Tauonic B decays

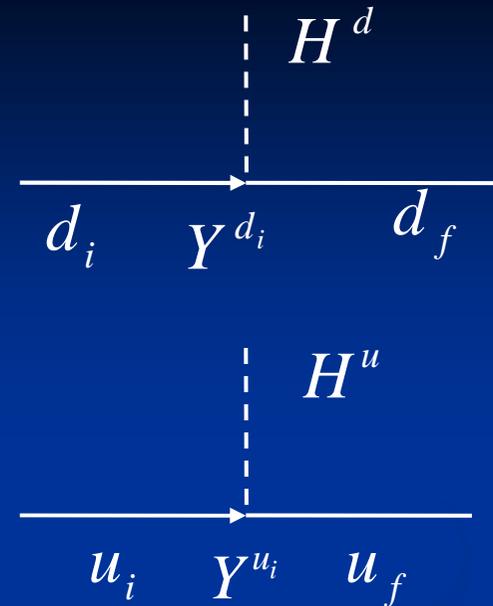
Observable	SM	Experiment	Significance
$\text{Br}[B \rightarrow \tau\nu]$	$(0.757^{+0.098}_{-0.061}) \times 10^{-4}$	$(1.15 \pm 0.23) \times 10^{-4}$	1.3 σ
$\text{Br}[B \rightarrow D\tau\nu]/\text{Br}[B \rightarrow D\ell\nu]$	0.297 ± 0.017	0.440 ± 0.072	2.0 σ
$\text{Br}[B \rightarrow D^*\tau\nu]/\text{Br}[B \rightarrow D^*\ell\nu]$	0.252 ± 0.003	0.332 ± 0.030	2.7 σ

 All three observables are above the SM prediction

Two Higgs Doublet Models (2HDMs)

2HDM of type II

- One Higgs doublet couples only to down-quarks the other Higgs doublet only to up-quarks.
 - 2 additional free parameters: $\tan(\beta)=v_u/v_d$ and the heavy Higgs mass M_H
 - Neutral Higgs-quark couplings are flavour-conserving.
 - Charged Higgs contribution to $b \rightarrow s\gamma$ requires $m_H > 380 \text{ GeV}$ T. Hermann, M. Misiak and M. Steinhauser 1208.2788
 - Contribution to $B \rightarrow \tau\nu$ necessarily destructive.
 - Cannot explain $B \rightarrow D^{(*)}\tau\nu$ and $B \rightarrow D\tau\nu$ simultaneously. BaBar collaboration 1205.5442
- ➔ **Disfavored by current data**



2HDM of type III

- Both Higgs doublets couple simultaneously to up and down quarks

→ Flavour-changing neutral Higgs couplings



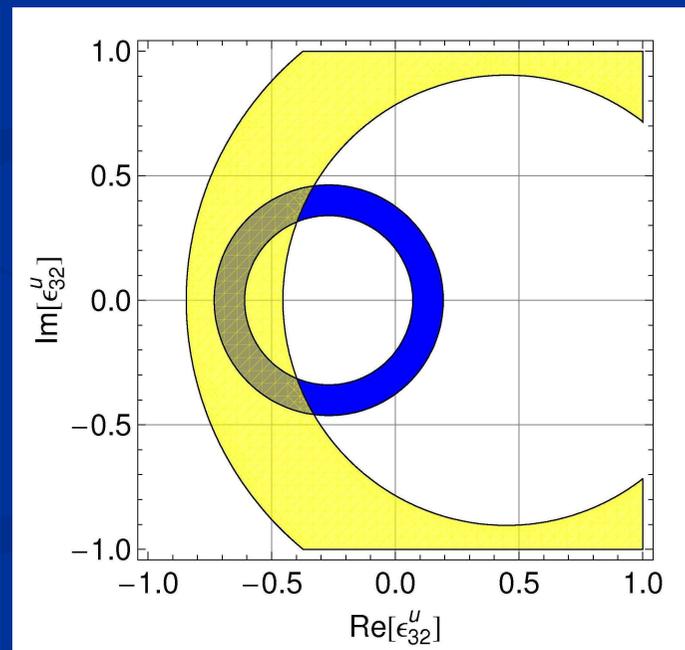
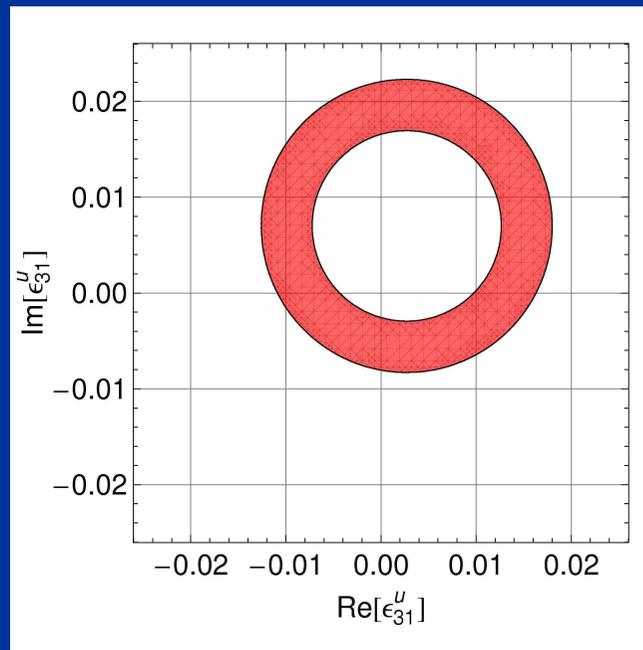
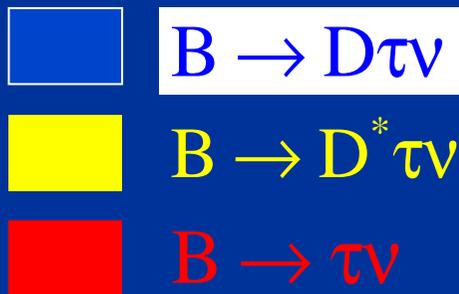
- All flavour-changing elements ϵ_{fi}^d and $\epsilon_{12,21}^u$ are constrained from FCNCs processes.
- Also $\epsilon_{13,23}^u$ constrained from charged Higgs diagrams, but $\epsilon_{31,32}^u$ is unconstrained.
- 2HDM III with MFV cannot explain $B \rightarrow \tau \nu$, $B \rightarrow D^{(*)} \tau \nu$ and $B \rightarrow D \tau \nu$

2HDM of type III with flavour-violation in the up-sector

A.C., C. Greub, A. Kokulu 1208.2788

- Constructive contribution to $B \rightarrow \tau \nu$ using ϵ_{31}^u is possible.
- $B \rightarrow D^{(*)} \tau \nu$ and $B \rightarrow D \tau \nu$ can be explained simultaneously using ϵ_{32}^u . **→** Check model via $H^0, A^0 \rightarrow \bar{t} c$

Allowed regions from:



Constraints on the MSSM Flavour Structure

SUSY flavour (CP) problem

- The squark mass matrices are not necessarily diagonal (and real) in the same basis as the quark mass matrices.
- Especially the trilinear A-terms can induce dangerously large flavour-mixing (and complex phases) since they don't necessarily respect hierarchy of the SM.
- The MSSM possesses two Higgs-doublets: Flavour-changing charged and (loop-induced) neutral Higgs interactions.

 **Why is the observed flavour violation so small?**

- Possible solutions:
 - MFV [D'Ambrosio, Giudice, Isidori, Strumia hep-ph/0207036](#)
 - Flavour-symmetries
 - effective SUSY [Barbieri et al hep-ph/10110730](#)
 - Radiative flavour violation

Squark mass matrix

$$M_{\tilde{q}}^2 = \begin{pmatrix} M_{LL}^{\tilde{q}2} & \Delta^{\tilde{q}LR} \\ \Delta^{\tilde{q}LR\dagger} & M_{RR}^{\tilde{q}2} \end{pmatrix}$$

$M_{LL,RR}^{\tilde{q}2}$ and Δ_{ij}^{qLR} are 3x3 matrices in flavour-space

$M_{LL,RR}^{\tilde{q}2}$ are chirality conserving

Δ_{ij}^{qLR} chirality changing

$$\Delta_{ij}^{dLR} = -v_d \left(\mu \tan(\beta) Y_i^d \delta_{ij} + A_{ij}^d \right)$$

$$\Delta_{ij}^{uLR} = -v_u \left(\mu \cot(\beta) Y_i^u \delta_{ij} + A_{ij}^u \right)$$

$$\tan(\beta) = \frac{v_u}{v_d}$$

$$\delta_{ij}^q = \frac{\Delta_{ij}^q}{\tilde{m}_{\tilde{q}}^2}$$

Constraints on the off-diagonal elements of the sfermion mass matrices

Except $\delta_{23,13}^{u,RR,RL}$ all elements are stringently constrained.

SUSY_FLAVOUR 2.0

A.C., J. Rosiek et al, arXiv:1203.5023

can calculate these observables including the numerically important resummation of all chirally enhanced corrections.

L. Hall, R. Rattazzi, U. Sarid hep-ph/9306309,
A.C., L. Hofer, J. Rosiek, arXiv:1103.4272

Observable	Most stringent constraints on	Experiment
$\Delta F = 0$		
$\frac{1}{2}(g-2)_e$	$\text{Re} \left[\delta_{11}^{\ell LR,RL} \right]$	$(1159652188.4 \pm 4.3) \times 10^{-12}$
$\frac{1}{2}(g-2)_\mu$	$\text{Re} \left[\delta_{22}^{\ell LR,RL} \right]$	$(11659208.7 \pm 8.7) \times 10^{-10}$
$\frac{1}{2}(g-2)_\tau$	$\text{Re} \left[\delta_{33}^{\ell LR,RL} \right]$	$< 1.1 \times 10^{-3}$
$ d_e (\text{ecm})$	$\text{Im} \left[\delta_{11}^{\ell LR,RL} \right]$	$< 1.6 \times 10^{-27}$
$ d_\mu (\text{ecm})$	$\text{Im} \left[\delta_{22}^{\ell LR,RL} \right]$	$< 2.8 \times 10^{-19}$
$ d_\tau (\text{ecm})$	$\text{Im} \left[\delta_{33}^{\ell LR,RL} \right]$	$< 1.1 \times 10^{-17}$
$ d_n (\text{ecm})$	$\text{Im} \left[\delta_{11}^{d LR,RL} \right], \text{Im} \left[\delta_{11}^{u LR,RL} \right]$	$< 2.9 \times 10^{-26}$
$\Delta F = 1$		
$\text{Br}(\mu \rightarrow e\gamma)$	$\delta_{12,21}^{\ell LR,RL}, \delta_{12}^{\ell LL,RR}$	$< 2.8 \times 10^{-11}$
$\text{Br}(\tau \rightarrow e\gamma)$	$\delta_{13,31}^{\ell LR,RL}, \delta_{13}^{\ell LL,RR}$	$< 3.3 \times 10^{-8}$
$\text{Br}(\tau \rightarrow \mu\gamma)$	$\delta_{23,32}^{\ell LR,RL}, \delta_{23}^{\ell LL,RR}$	$< 4.4 \times 10^{-8}$
$\text{Br}(K_L \rightarrow \pi^0 \nu\nu)$	$\delta_{23}^{u LR}, \delta_{13}^{u LR} \times \delta_{23}^{u LR}$	$< 6.7 \times 10^{-8}$
$\text{Br}(K^+ \rightarrow \pi^+ \nu\nu)$	sensitive to $\delta_{13}^{u LR} \times \delta_{23}^{u LR}$	$17.3_{-10.5}^{+11.5} \times 10^{-11}$
$\text{Br}(B_d \rightarrow ee)$	$\delta_{13}^{d LL,RR}$	$< 1.13 \times 10^{-7}$
$\text{Br}(B_d \rightarrow \mu\mu)$	$\delta_{13}^{d LL,RR}$	$< 1.8 \times 10^{-8}$
$\text{Br}(B_d \rightarrow \tau\tau)$	$\delta_{13}^{d LL,RR}$	$< 4.1 \times 10^{-3}$
$\text{Br}(B_s \rightarrow ee)$	$\delta_{23}^{d LL,RR}$	$< 7.0 \times 10^{-5}$
$\text{Br}(B_s \rightarrow \mu\mu)$	$\delta_{23}^{d LL,RR}$	$< 1.08 \times 10^{-8}$
$\text{Br}(B_s \rightarrow \tau\tau)$	$\delta_{23}^{d LL,RR}$	---
$\text{Br}(B_s \rightarrow \mu e)$	$\delta_{23}^{d LL,RR} \times \delta_{12}^{\ell LL,RR}$	$< 2.0 \times 10^{-7}$
$\text{Br}(B_s \rightarrow \tau e)$	$\delta_{23}^{d LL,RR} \times \delta_{13}^{\ell LL,RR}$	$< 2.8 \times 10^{-5}$
$\text{Br}(B_s \rightarrow \mu\tau)$	$\delta_{23}^{d LL,RR} \times \delta_{23}^{\ell LL,RR}$	$< 2.2 \times 10^{-5}$
$\text{Br}(B^+ \rightarrow \tau^+ \nu)$	—	$(1.65 \pm 0.34) \times 10^{-4}$
$\text{Br}(B_d \rightarrow D\tau\nu)/\text{Br}(B_d \rightarrow D\nu)$	—	$(0.407 \pm 0.12 \pm 0.049)$
$\text{Br}(B \rightarrow X_s \gamma)$	$\delta_{23}^{d LL,RR}$ for large $\tan\beta$, $\delta_{23,32}^{d LR}$	$(3.52 \pm 0.25) \times 10^{-4}$
$\Delta F = 2$		
$ \epsilon_K $	$\text{Im} \left[(\delta_{12}^{d LL,RR})^2 \right], \text{Im} \left[(\delta_{12,21}^{d LR})^2 \right]$	$(2.229 \pm 0.010) \times 10^{-3}$
ΔM_K	$\delta_{12}^{d LL,RR}, \delta_{12,21}^{d LR}$	$(5.292 \pm 0.009) \times 10^{-3} \text{ ps}^{-1}$
ΔM_D	$\delta_{12}^{u LL,RR}, \delta_{12,21}^{u LR}$	$(2.37_{-0.71}^{+0.66}) \times 10^{-2} \text{ ps}^{-1}$
ΔM_{B_d}	$\delta_{13}^{d LL,RR}, \delta_{13,31}^{d LR}$	$(0.507 \pm 0.005) \text{ ps}^{-1}$
ΔM_{B_s}	$\delta_{23}^{d LL,RR}, \delta_{23,32}^{d LR}$	$(17.77 \pm 0.12) \text{ ps}^{-1}$

Radiative Flavour Violation in the MSSM

Radiative Flavour Violation (RFV)

$SU(2)^3$ flavour-symmetry in the MSSM superpotential:

- CKM matrix is the unit matrix.
- Only the third generation Yukawa coupling is different from zero.

$$V_{\text{CKM}}^{(0)} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$Y^q = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & Y^{q_3} \end{pmatrix}$$

All other elements are generated radiatively using the trilinear A-terms!

Features of the model

- Additional flavour symmetries in the superpotential.
- Explains small masses and mixing angles via a loop-suppression.
- Deviations from MFV if the third generation is involved.
- Solves the SUSY CP problem via a mandatory phase alignment. (Phase of μ enters only at two loops)Borzumati, Farrar, Polonsky, Thomas 1999.
- The SUSY flavour problem reduces to the elements $\delta_{32}^{q LR}$, $\delta_{31}^{q LR}$

CKM generation in the down-sector:

CKM elements
generate by the
self-energies:

$$\Sigma_{13}^{dLR} = m_b V_{ub}$$

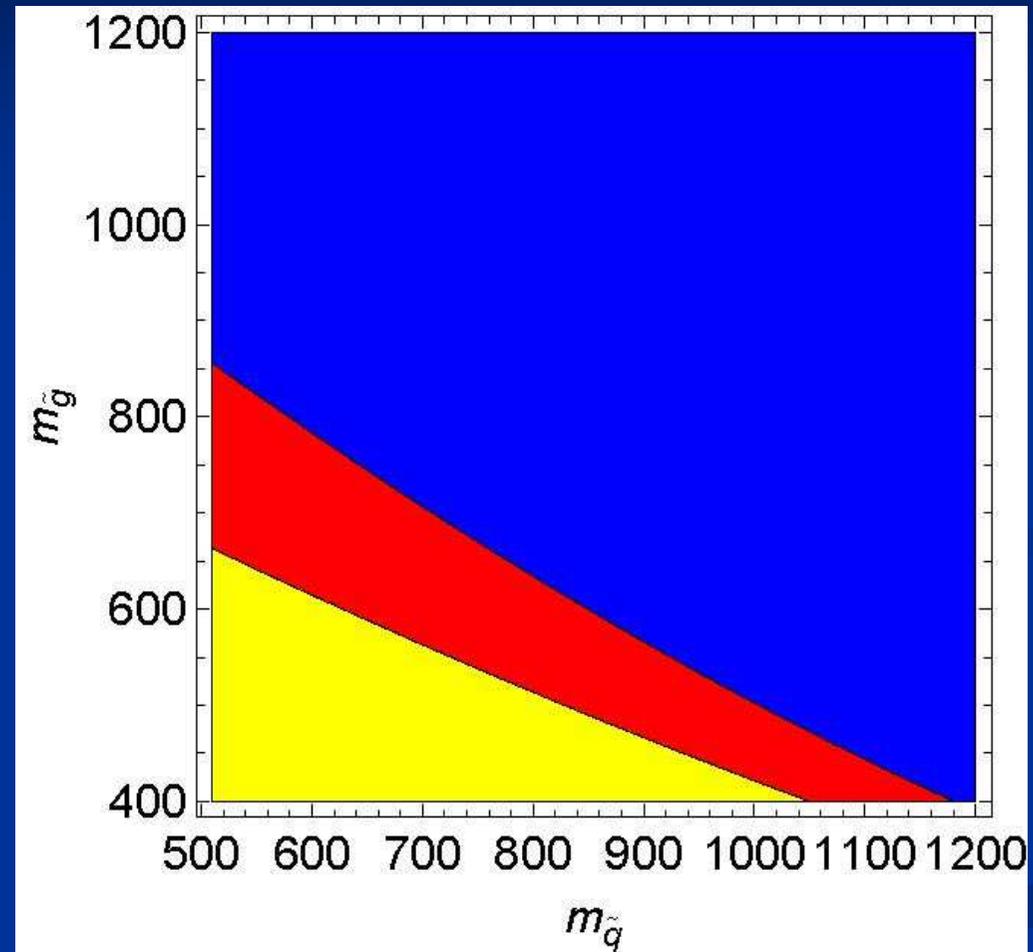
$$\Sigma_{23}^{dLR} = m_b V_{cb}$$

Allowed regions
from $b \rightarrow s\gamma$

 $m_b \mu \tan(\beta) = 0.12 \text{ TeV}^2$

 $m_b \mu \tan(\beta) = 0 \text{ TeV}^2$

 $m_b \mu \tan(\beta) = 0.12 \text{ TeV}^2$



Higgs effects: $B_s \rightarrow \mu^+ \mu^-$

- Constructive and destructive contribution depending on the sign of μ



$$\varepsilon_b = 0.005$$



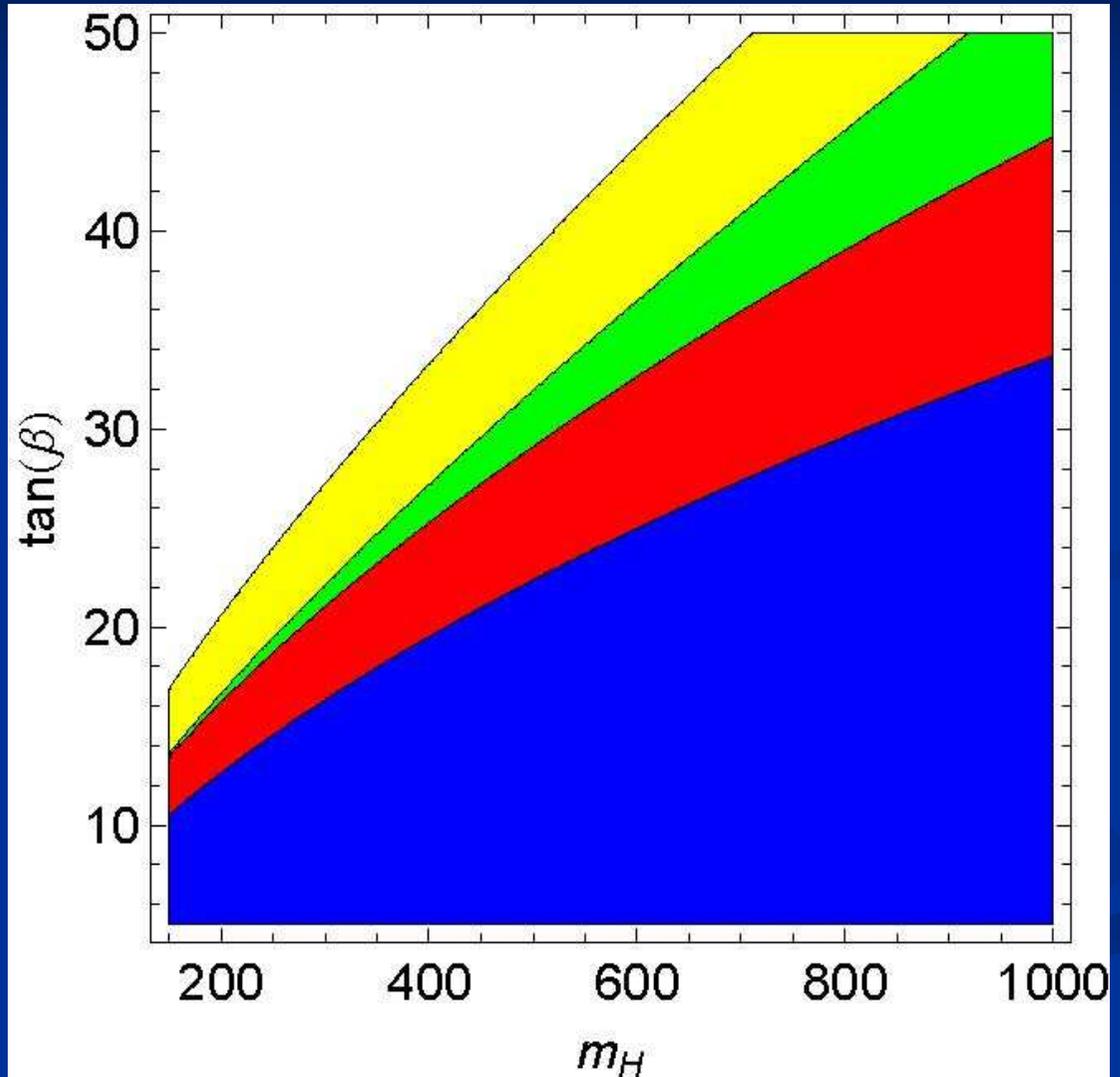
$$\varepsilon_b = 0.01$$



$$\varepsilon_b = -0.005$$



$$\varepsilon_b = -0.01$$

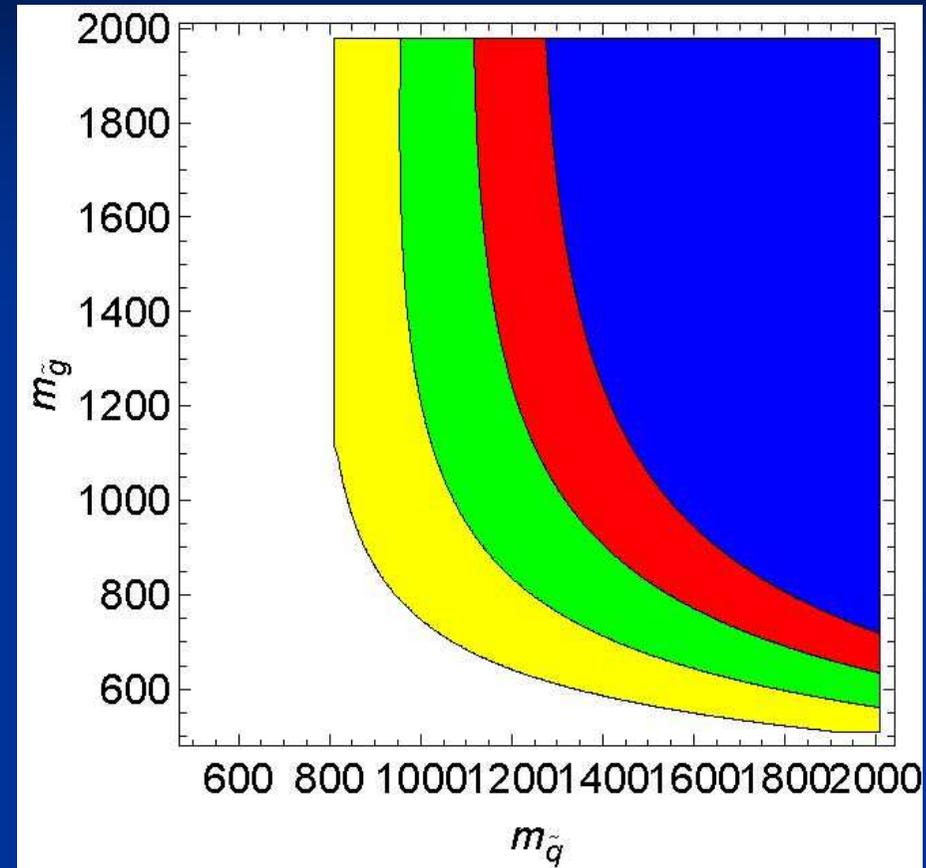


CKM generation in the up-sector:

$$\Sigma_{13}^{u LR} \stackrel{!}{=} m_t V_{td}^*$$

$$\Sigma_{23}^{u LR} \stackrel{!}{=} m_t V_{cb}^*$$

- Constraints from Kaon mixing.
- $\delta_{31}^{u LR}, \delta_{32}^{u LR}$ unconstrained from FCNC processes.
- $\delta_{31}^{u LR}$ can induce a sizable right-handed W-coupling.



■ $M_2 = 200\text{GeV}$

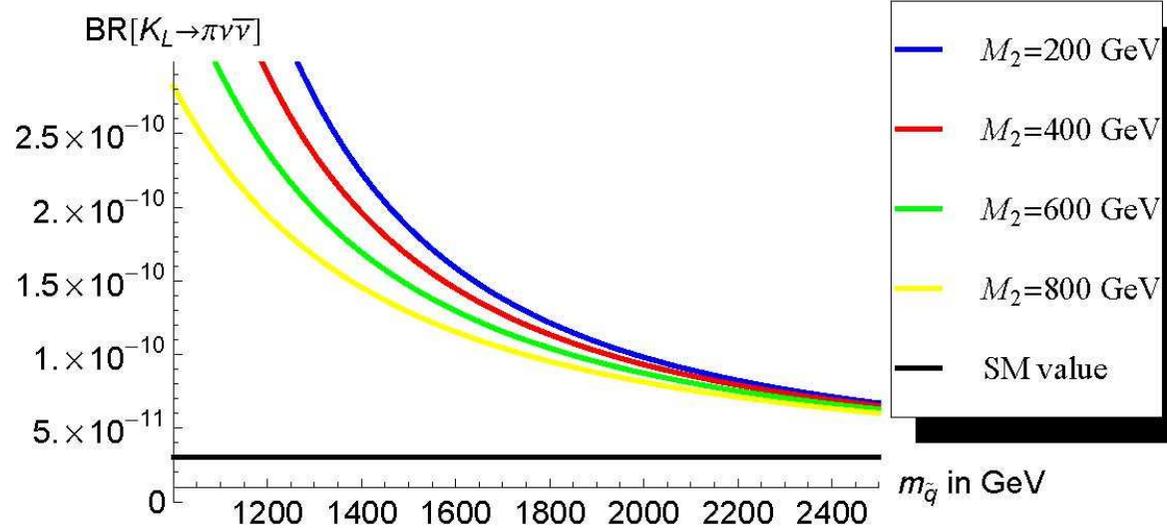
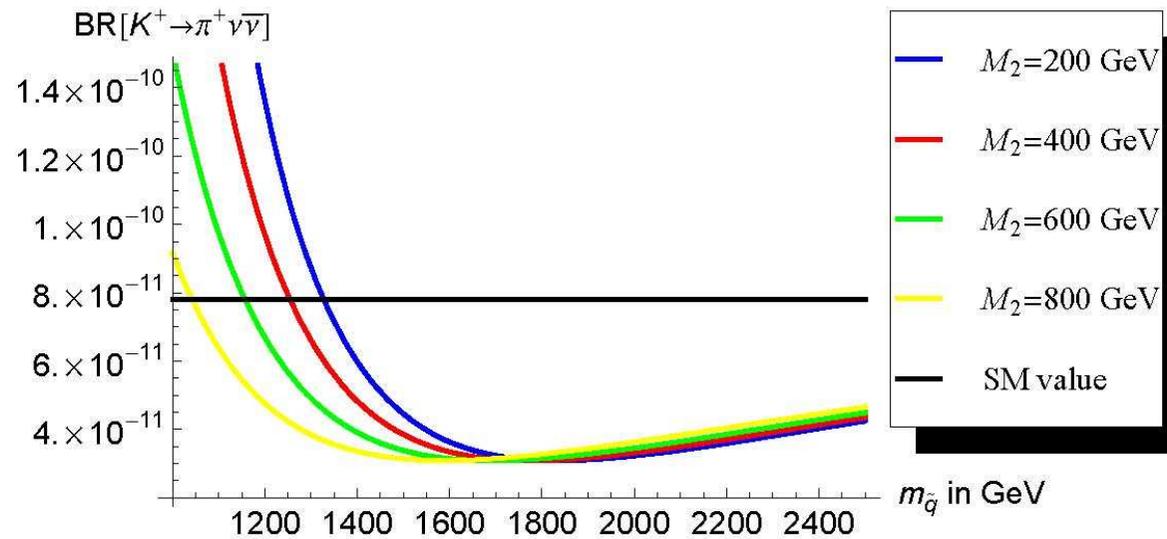
■ $M_2 = 400\text{GeV}$

■ $M_2 = 400\text{GeV}$

■ $M_2 = 800\text{GeV}$

- Effects in $K \rightarrow \pi \nu \bar{\nu}$

- Verifiable predictions for NA62



Radiative Lepton Mass Generation

- Contribution to the anomalous magnetic moment of the muon is necessarily constructive

Borzumati, Farrar, Polonsky, Thomas 1999.

- Difficulties with vacuum stability



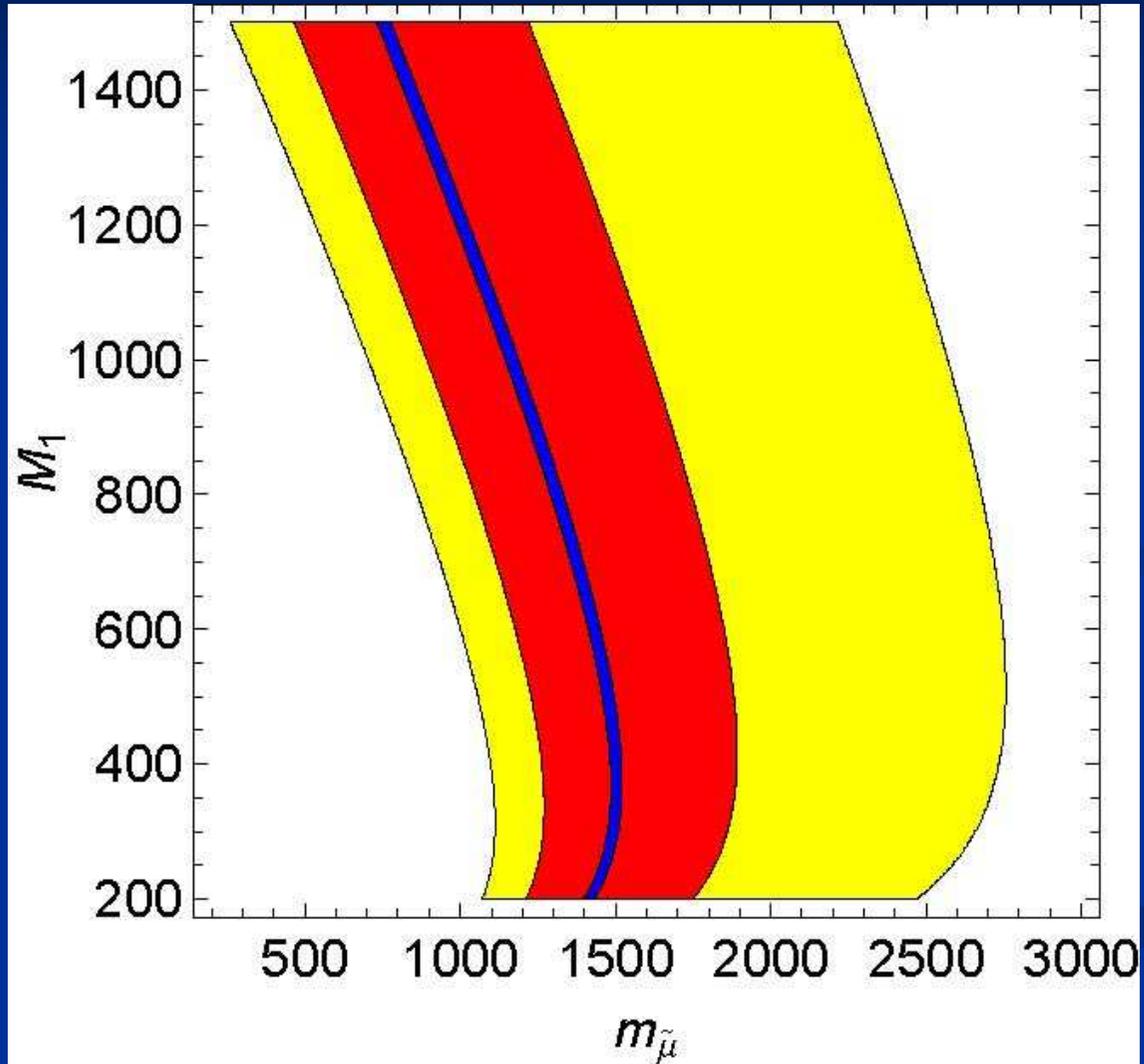
central value



1σ



2σ



Conclusions

- Indirect searches for NP probe energy scales much higher than the one of the LHC.
- The CKM mechanism of flavour-violation in the SM works very well.  Stringent constraints on physics beyond the SM.
- Hints for new physics: The anomalous magnetic moment of the muon and tauonic B decays?
- 2HDM of type III with flavour-violation in the up-sector can explain the $B \rightarrow \tau \nu$, $B \rightarrow D^{(*)} \tau \nu$ and $B \rightarrow D \tau \nu$.
- Flavour structure of the MSSM stringently constrained from flavour observables.
- RFV solves the SUSY flavour and the SUSY CP problem and can explain the anomalous magnetic moment of the muon.