

(N)NLL+(N)NLO QCD predictions and QED FSR
for a novel variable which probes the low p_T^Z domain

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- 3 Preparation for ϕ_η^* measurement using 2011 ATLAS data
 - (N)NLL+(N)NLO QCD predictions for ϕ_η^* at $\sqrt{s} = 7$ TeV
 - QED FSR - one of the main systematic uncertainties
 - ϕ_η^* measurement in ATLAS 2011 will be available soon!

(Data analysis is in the official ATLAS procedure for the approval of results and is not allowed to present in public.)

p_T^Z theoretical predictions (1/2)

- High p_T^Z ($> \sim 30$ GeV)
 - Fixed order perturbative QCD predictions (like FEWZ)
 - Test pQCD
- Low p_T^Z ($< \sim 30$ GeV):
 - Resummation of leading logarithms to all orders in α_S (like RESBOS).
 - OR modeling by parton shower generators (like PYTHIA).
 - Tune Monte Carlo models

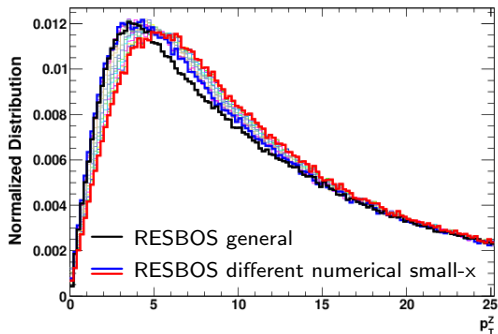
→ This measurement helps to improve the modelling of W boson production needed for a precise measurement of the W mass.

p_T^Z theoretical predictions (2/2)

The small- x broadening effect was studied in [Phys.Rev.D72:033015,2005](#):
The resummed form factor may need to be modified for processes involving a small- x parton in the initial state.

→ Lead to a wider p_T^Z distribution of Z bosons with large rapidity.

→ Interesting to be tested at LHC 7 TeV.



2010 ATLAS data at $\sqrt{s} = 7$ TeV proton-proton collisions

- p_T^Z distribution was measured using:

$$Z/\gamma^* \rightarrow e^+e^-$$

$$Z/\gamma^* \rightarrow \mu^+\mu^-$$

$$\int L dt = 35 - 40 \text{ pb}^{-1}$$

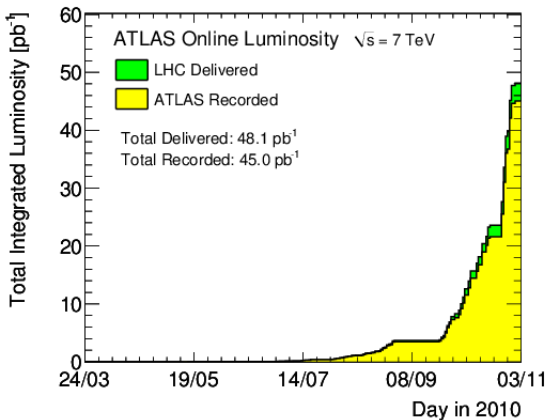
- Fiducial region:

$$|\eta^I| < 2.4$$

$$p_T^I > 20 \text{ GeV}$$

(In electron channel -
Energy by calorimetry,
direction by tracker)

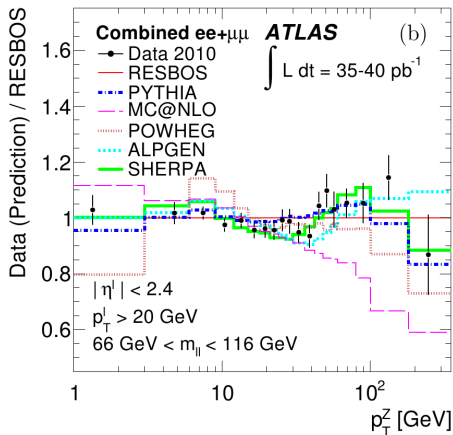
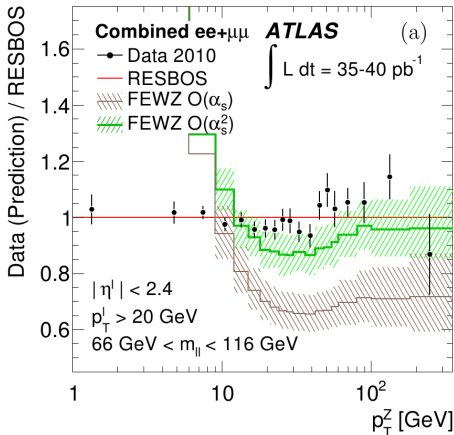
$$66 \text{ GeV} < m_{ll} < 116 \text{ GeV}$$



→ 8923 $Z/\gamma^* \rightarrow e^+e^-$ and 15060 $Z/\gamma^* \rightarrow \mu^+\mu^-$ candidates

Comparison with theoretical predictions and MC generators

Phys.Lett.B 705 (2011) 415-434



Main systematic uncertainties

ρ_T^Z (GeV)	stat. (%)	syst. (%)
0 - 3	3.3	4.7
3 - 6	2.4	3.3
6 - 9	2.7	2.3
9 - 12	3.1	2.4
12 - 15	3.3	2.7
15 - 18	3.9	3.0
18 - 21	4.4	3.3
21 - 24	4.8	3.6
24 - 27	5.5	3.8
27 - 30	6.5	4.0

Phys.Lett.B 705 (2011) 415-434

Systematic uncertainties in electron channel:

- Energy scale: 0.2% – 4.4%.
- Unfolding: 2.0% – 4.2%.
- Efficiencies: 1.0% – 3.2%.
- Background: 1.4%
- Pileup: 0.3%
- MC statistics: 0.4% – 3.6%
- QED final state radiation: 0.6%

Why new variables?

Phys.Lett.B 705 (2011) 415-434

Main systematic uncertainties of the p_T^Z measurement:

- Energy scale: 0.2% – 4.4%.
- Unfolding: 2.0% – 4.2%.



Optimize new variables which:

- is less susceptible to the effects of experimental resolution.

- probes the same physical effects as p_T^Z .

A novel variable definition

p_T Eur.Phys.J.C71:1600,2011

↓

a_T

$$\downarrow \frac{\Delta a_T/M}{a_T/M} = \left(\frac{\Delta a_T}{a_T} - \frac{1}{2} \right) \frac{\Delta p_T^{(1)}}{p_T^{(1)}}$$

a_T/M

$$\downarrow (p_T^{(1)} \approx p_T^{(2)})$$

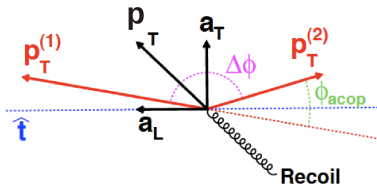
$$a_T/M \approx \tan(\phi_{acop}/2) \sin(\theta^*)$$

↓

$$\phi^* \equiv \tan(\phi_{acop}/2) \sin(\theta^*)$$

$$\downarrow \cos(\theta_\eta^*) = \tanh\left(\frac{\eta^- - \eta^+}{2}\right)$$

$$\phi_\eta^* \equiv \tan(\phi_{acop}/2) \sin(\theta_\eta^*)$$



$$\hat{t} = (p_T^{(1)} - p_T^{(2)}) / |p_T^{(1)} - p_T^{(2)}|$$

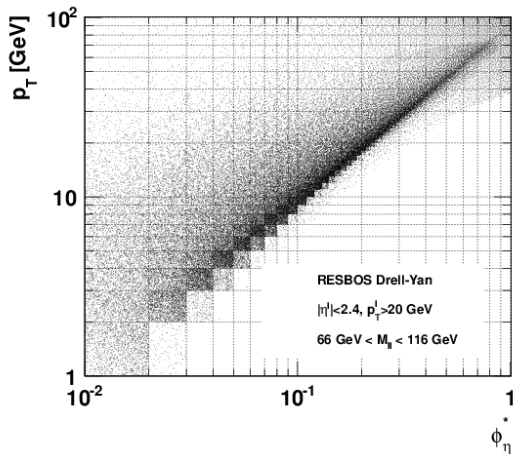
- θ^* is the scattering angle of the leptons relative to the beam direction in the dilepton rest frame.

- θ^* is commonly evaluated in the Collins Soper frame and susceptible to the effects of lepton momentum resolution.

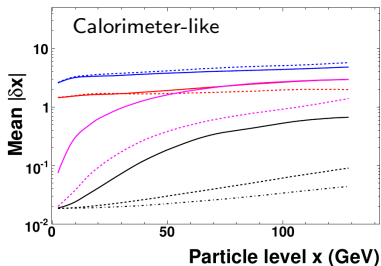
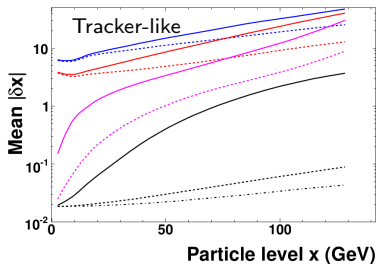
- θ_η^* is an alternative way to measure of the scattering angle that is based entirely on the measured track directions.

Correlation

Evident correlation between p_T^Z and ϕ_η^*

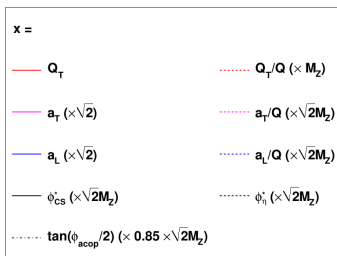


Resolution



Eur.Phys.J.C71:1600,2011

Mean resolution of each candidate variable for the optimization as a function of that candidate using PYTHIA re-weighted to RESBOS for $D\bar{0}$.



Purity

Phys.Lett.B 705 (2011) 415-434

ATLAS ρ_T^Z purity $\sim 60\% - 90\%$ with 19 bins in $[0 - 350]$ GeV

Phys.Rev.Lett.106:122001,2011

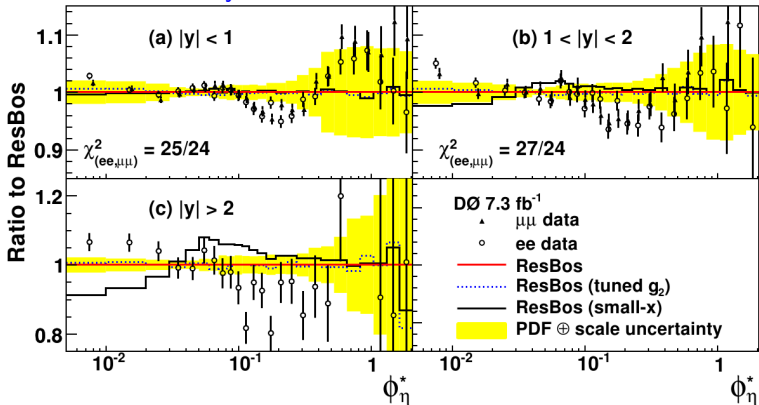
$D\emptyset$ ϕ_η^* purity $\sim 92\% - 98\%$ with 29 bins in $[0 - 4.749]$

→ simplify unfolding procedure

→ smaller systematic uncertainty due to unfolding is expected

D0 results

Phys.Rev.Lett.106:122001,2011



Conclusion:

1. A QCD prediction is unable to describe the detailed shape of the ϕ_η^* distribution.
2. The small-x broadening effect is strongly disfavored.

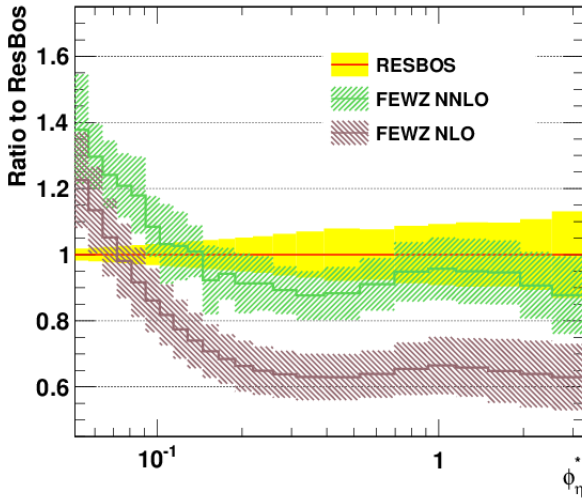
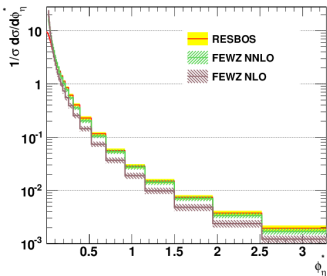
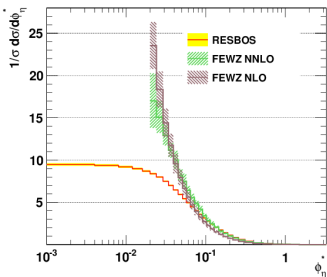
FEWZ

- FEWZ program:
 - QCD calculation at NLO ($\mathcal{O}(\alpha_S)$) or NNLO ($\mathcal{O}(\alpha_S^2)$) for high p_T^Z predictions.
 - **No resummation** for the emission of soft and collinear gluons in the low p_T^Z region.
 - PDF and α_S uncertainties calculated automatically.
 - QCD renormalization (μ_R) and factorization (μ_F) scales initialized independently.
- The ϕ_{η}^* prediction using FEWZ:
 - The prediction with $\mu_R = \mu_F = M_Z$, NNLO PDF MSTW2008.
 - The theoretical uncertainty: $\sigma = \sqrt{\sigma_{PDF,\alpha_S}^2 + \sigma_{QCDscale}^2}$.
 - QCD scale uncertainty from scale variations by a factor of 2 with $1/2 \leq \mu_R/\mu_F \leq 2$.

RESBOS

- RESBOS program:
 - QCD calculation at NNLO for high p_T^Z predictions.
 - **NNLL Resummation** for the emission of soft and collinear gluons in the low p_T^Z region.
 - PDF uncertainties calculable.
 - Input grid with fixed QCD renormalization (μ_R) and factorization (μ_F) scales.
- The ϕ_{η}^* prediction using RESBOS:
 - NLO PDF CTEQ6.6.
 - The theoretical uncertainty: $\sigma = \sqrt{\sigma_{PDF}^2 + \sigma_{QCDscale}^2}$.
 - **No input grid for different choices of QCD scale \rightarrow QCD scale uncertainty is extrapolated from FEWZ.**

FEWZ and RESBOS comparison



Systematic uncertainties of ϕ_η^* measurement

- Energy scale and resolution (**negligible**)
- Unfolding
- Efficiencies
- Background
- Pileup
- MC statistics
- PDF
- Tracking
- QED final state radiation (studied by Z. WAS, L. DI CIACCIO):
expected to give one of the highest contribution
(0.6% in [Phys.Lett.B 705 \(2011\) 415-434](#))

Monte Carlo generators used for QED FSR study

- PHOTOS 2.5 - interfaced with the ATLAS simulation
(approximations for the calculations of the first and second order matrix elements to describe QED FSR)
- KKMC
(a second order QED matrix element)
- SANC
(one loop electroweak and QCD radiative corrections to high energy processes)

QED FSR systematic uncertainty: Methodology

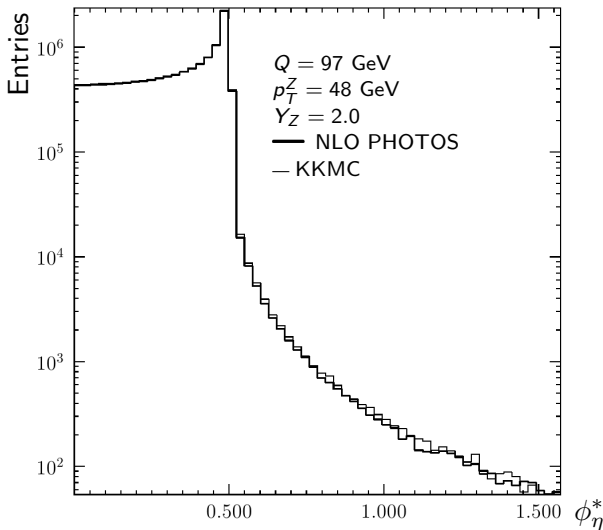
QED final state radiation can change the true level (or generated) fiducial cross section in the electron channel by about -5% and in the muon channel by about -3%.

The systematic uncertainty due to QED FSR is estimated by comparing:

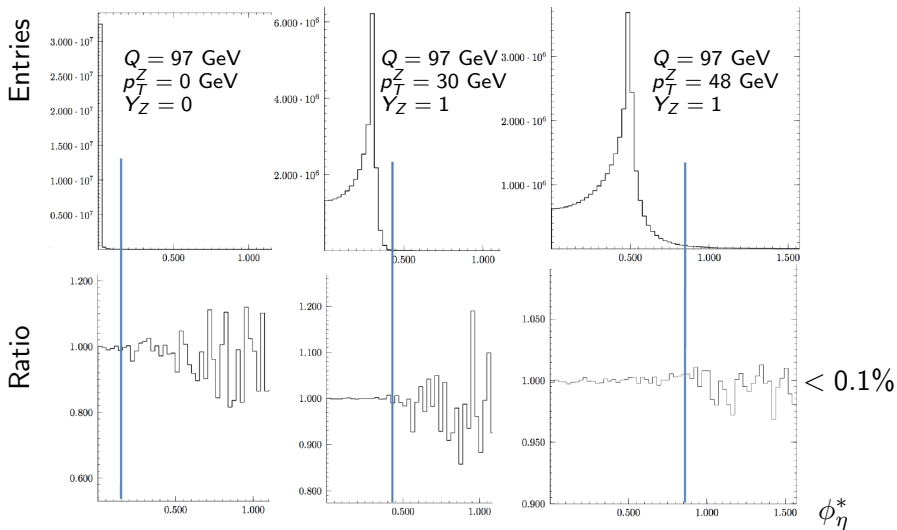
- ϕ_{η}^* differential distributions for fixed values of:
 Q, p_{τ}^Z, Y_Z for $Z \rightarrow ee$ and $Z \rightarrow \mu\mu$
- Integrated cross-sections in each Q, p_{τ}^Z, Y_Z bin

in PHOTOS with KKMC and SANC.

Examples of PHOTOS and KKMC comparison (1/2)



Examples of PHOTOS and KKMC comparison (2/2)

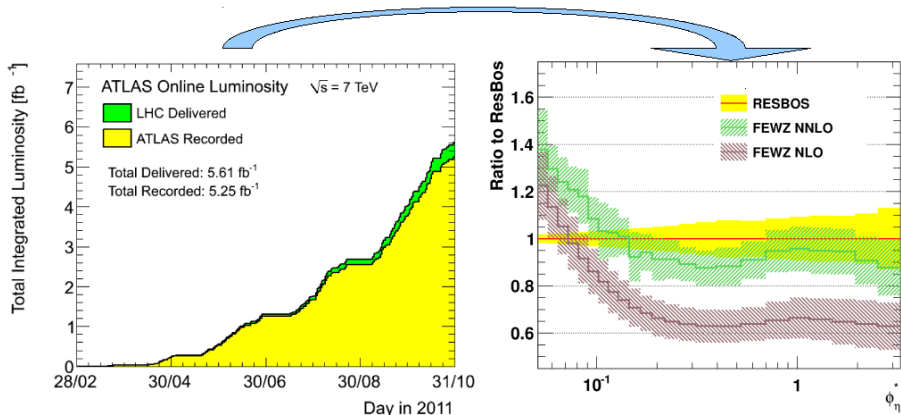


QED FSR systematic uncertainty study: First results

Comparison of PHOTOS with KKMC and SANC:

- PHOTOS and KKMC: $\sim 0.1\%$
- PHOTOS and SANC (multiple-photon mode):
 - Charged current ($\sim 0.1\%$)
 - Neutral current (is going on...)

2011 ATLAS data at $\sqrt{s} = 7$ TeV proton-proton collisions



Expected statistic uncertainty: $\sim 0.5\%$

Conclusion

- Theoretical predictions for ϕ_{η}^* measurement at $\sqrt{s} = 7$ TeV are presented.
- QED FSR systematic uncertainty estimation is going on and will be finalized in near future.
- Analysis of ϕ_{η}^* measurement using 2011 ATLAS data is being finalized and will be ready soon.

References

① FEWZ:

Comput.Phys.Commun.182:2388-2403,2011

arXiv:1201.5896v1

www.hep.anl.gov/fpetriello/FEWZ_2.1.tar.gz

② RESBOS:

Phys.Rev.D56:5558-5583,1997

<http://hep.pa.msu.edu/resum/>

③ PHOTOS:

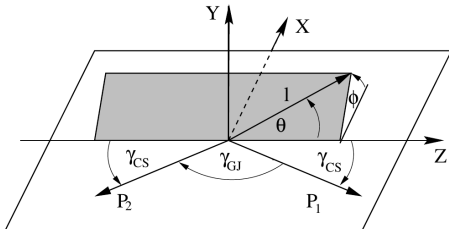
<http://annapurna.ifj.edu.pl/wasm/phi-star.html>

Thank you for your attention!

Backup

Collins Soper frame (CS)

Nucl.Phys.B582:537-570,2000



The Collins-Soper frame (in the dilepton rest frame):

When we boost from the hadron center-of-mass frame to the dilepton rest frame, the collinearity of the hadron momenta \mathbf{P}_1 and \mathbf{P}_2 is lost and they span a plane which we identify with the \mathbf{X} - \mathbf{Z} -plane.

We are still free to fix \mathbf{Z} within this plane. In the Collins-Soper frame \mathbf{Z} is chosen to bisect the angle between \mathbf{P}_1 and $-\mathbf{P}_2$. The angle between \mathbf{Z} and \mathbf{P}_1 and between \mathbf{Z} and \mathbf{P}_2 is called γ_{CS} .

θ and ϕ define the lepton direction in CS frame.

RESBOS resummation with non-perturbative functions

1. No small-x: The resummed cross section for the process AB->VX is calculated as:

$$\frac{d\sigma_{AB}}{dQ^2 dy dQ_T^2} \approx \int \frac{d^2b}{(2\pi)^2} e^{i\vec{q}_T \cdot \vec{b}} \tilde{W}_{AB}(b, \dots) + Y$$

$$\tilde{W}_{AB}(b, Q, x_A, x_B) = \tilde{W}_{AB}^{pert}(b_*, Q, x_A, x_B) e^{-S_{NP}^{BLNY}(b, Q, b_*)}$$

Where the non-perturbative Sudakov function has the BLNY (Brock-Landry-Nadolsky-Yuan) parametrization:

$$S_{NP}^{BLNY}(b, Q, b_*) = \left[0.21 + 0.68 \ln\left(\frac{Q}{3.2 \text{ GeV}}\right) - 0.126 \ln(100 x_A x_B) \right] b^2$$

2. Small-x: The new form of resummed form factor:

$$\tilde{W}_{AB}(b) = \tilde{W}_{AB}^{pert}(b_*, Q, x_A, x_B) e^{-S_{NP}^{BLNY}(b, Q, b_*)} e^{-\rho(x_A)b^2 - \rho(x_B)b^2}$$

One choice of $\rho(x)$:

$$\rho(x) = c_0 \left(\sqrt{\frac{1}{x^2} + \frac{1}{x_0^2}} - \frac{1}{x_0} \right)$$

c_0 controls the magnitude of the broadening for a given x ,

x_0 is a characteristic value of x below which $\rho(x)$ becomes non-negligible.

MC generators

- PYTHIA: the hard scattering process is calculated in leading order approximation and the higher order corrections are approximated with a parton shower approach.
- ALPGEN: LO MC generator which implements the exact matrix element LO calculation for multi-partonic final states.
- SHERPA: account for multijet production through multi-parton tree-level matrix elements merged with the parton shower.
- MC@NLO: full NLO calculations of rates for QCD processes during the hard scattering.
- POWHEG: a prescription for interfacing NLO QCD calculations with parton shower generators, can be interfaced with any modern shower generator such as HERWIG and PYTHIA.