

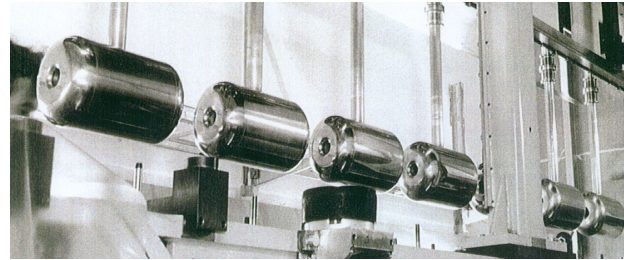
# *Introduction to Accelerator Physics*

*Bernhard Holzer,  
CERN-LHC*

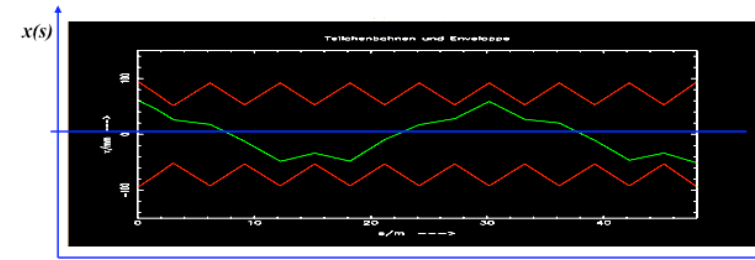
## *I.) The First Steps*



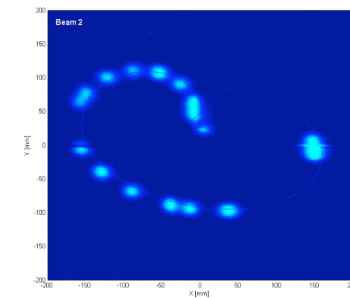
# *A Bit of History*



# *A Bit of Theory*



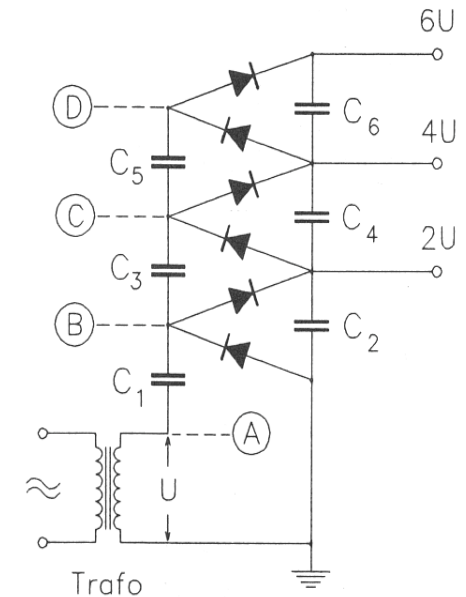
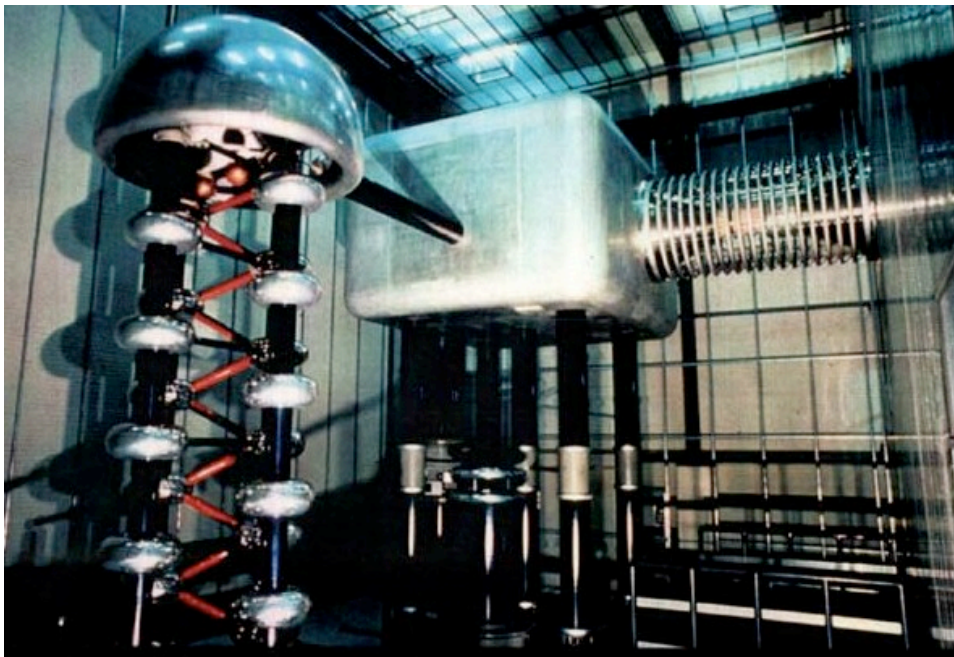
# *A Bit of Reality*



# 1.) Electrostatic Machines: The Cockcroft-Walton Generator

**1928:** Encouraged by Rutherford Cockcroft and Walton start the design & construction of a high voltage generator to accelerate a proton beam

**1932:** First particle beam (protons) produced for nuclear reactions: splitting of Li-nuclei with a proton beam of 400 keV



**Particle source:** Hydrogen discharge tube on 400 kV level

**Accelerator:** evacuated glass tube

**Target:** Li-Foil on earth potential

**Technically:** rectifier circuit, built of capacitors and diodes (Greinacher)

*robust, simple, on-knob machines*

*largely used in history as pre-accelerators for proton and ion beams*

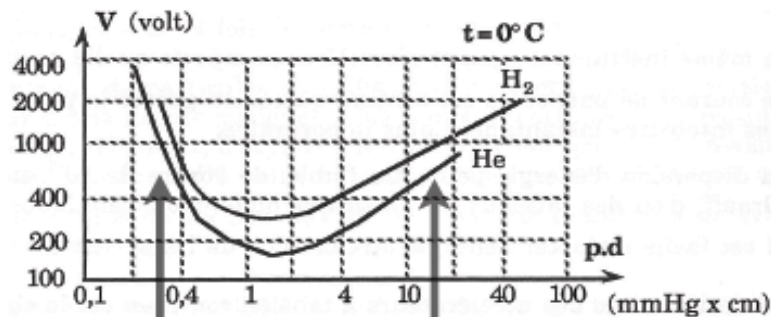
*recently replaced by modern structures (RFQ)*

# Main limitation

Main limitation:  
electric discharge due to too high Voltage.  
Maximum limit: 1 MV

## Limit set by Paschen law:

the breaking Voltage between two parallel electrodes depends only on the pressure of the gas between the electrodes and their distance



Low pressure: gas not too dense, long mean average path of electrons

High pressure: dense gas, large Voltage needed for gas ionisation

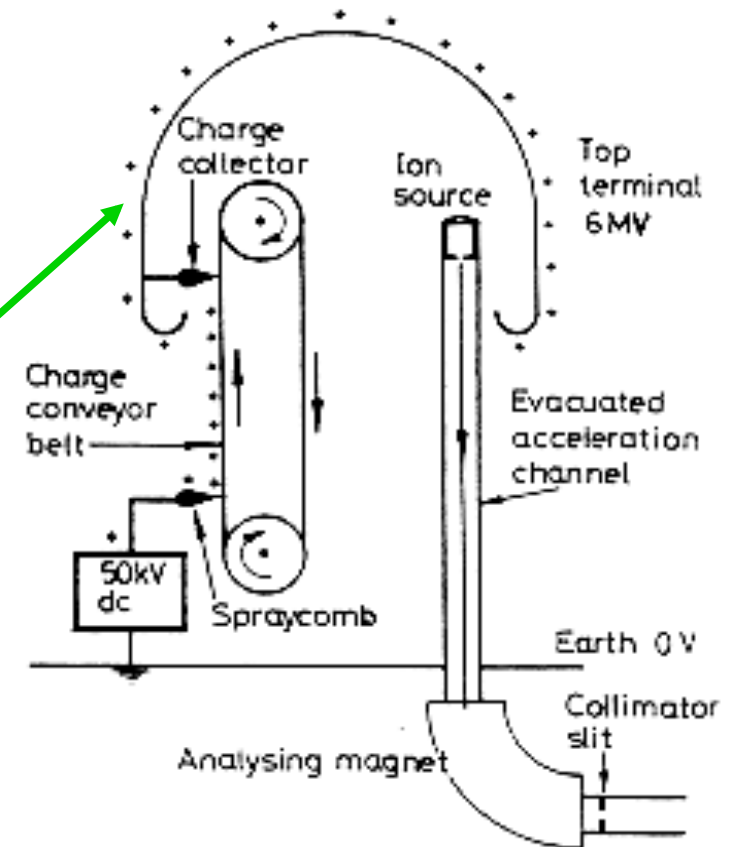


## 2.) Electrostatic Machines: (Tandem -) van de Graaff Accelerator (1930 ...)

*creating high voltages by mechanical transport of charges*

\* *Terminal Potential:  $U \approx 12 \dots 28 \text{ MV}$   
using high pressure gas to suppress discharge ( $\text{SF}_6$ )*

**Problems:** \* *Particle energy limited by high voltage discharges*  
\* *high voltage can only be applied once per particle ...  
... or twice ?*



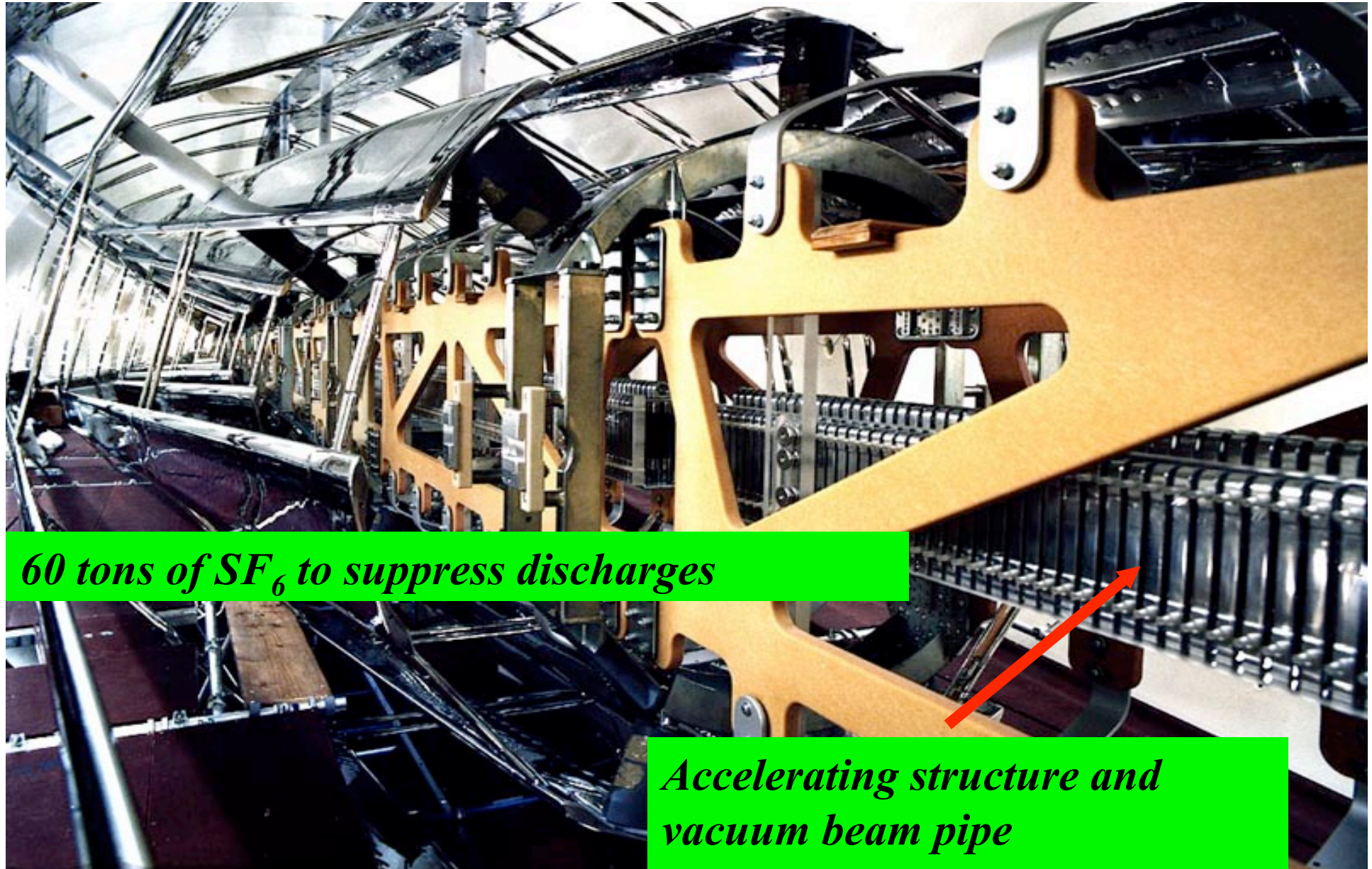
*The „Tandem principle“: Apply the accelerating voltage twice ...  
... by working with **negative ions** (e.g.  $H^-$ ) and  
**stripping the electrons** in the centre of the  
structure*

*Example for such a „steam engine“: 12 MV-Tandem van de Graaff  
Accelerator at MPI Heidelberg*



*... and how it looks inside*

*“Vivitron” Strassbourg*



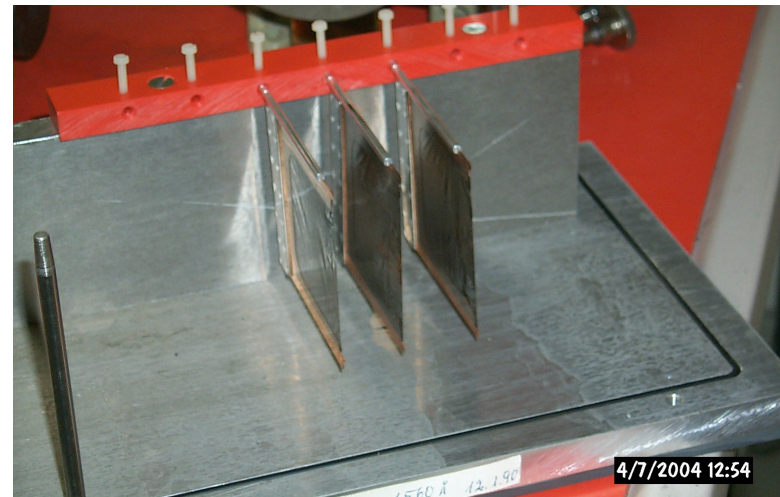
*60 tons of SF<sub>6</sub> to suppress discharges*

*Accelerating structure and  
vacuum beam pipe*

*The Principle of the “Steam Engine”:  
Mechanical Transport of Charge via a rotating  
chain or belt*



*stripping foils: 1500 Å*

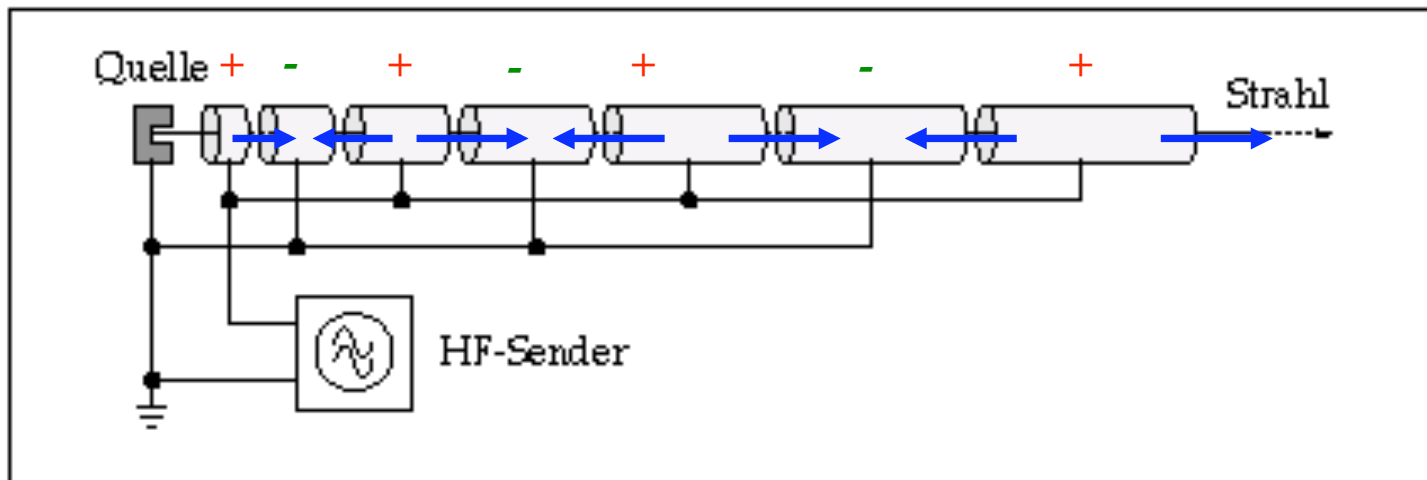




### 3.) The first RF-Accelerator: „Linac“

*1928, Wideroe: how can the acceleration voltage be applied several times to the particle beam*

*schematic Layout:*



*Energy gained after  $n$  acceleration gaps*

$$E_n = n * q * U_0 * \sin \psi_s$$

*$n$  number of gaps between the drift tubes*

*$q$  charge of the particle*

*$U_0$  Peak voltage of the RF System*

*$\Psi_s$  synchronous phase of the particle*

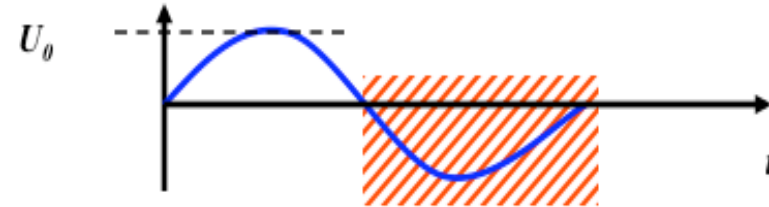
*\* acceleration of the proton in the first gap*

*\* voltage has to be „flipped“ to get the right sign in the second gap → RF voltage*

*→ shield the particle in drift tubes during the negative half wave of the RF voltage*

# Wideroe-Structure: the drift tubes

*shielding of the particles during the negative half wave of the RF*



*Time span of the negative half wave:*  $\tau_{RF}/2$

*Length of the Drift Tube:*

$$l_i = v_i * \frac{\tau_{rf}}{2}$$

*Kinetic Energy of the Particles*

$$E_i = \frac{1}{2} m v^2$$

$$\rightarrow v_i = \sqrt{2E_i/m}$$

$$l_i = \frac{1}{v_{rf}} * \sqrt{\frac{i * q * U_{0 * \sin \psi_s}}{2m}}$$

*valid for non relativistic particles ...*

*Alvarez-Structure: 1946, surround the whole structure by a rf vessel*

*Energy:  $\approx 20$  MeV per Nucleon  $\beta \approx 0.04 \dots 0.6$ , Particles: Protons/Ions*

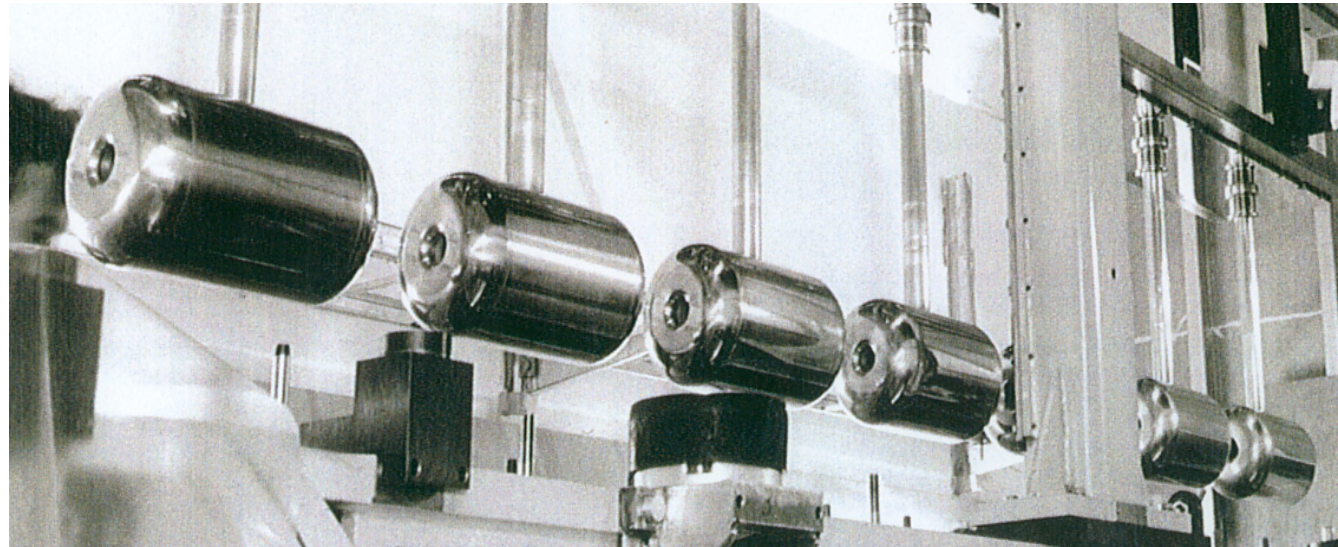
*Example: DESY Accelerating structure of the Proton Linac*

$$E_{total} = 988 \text{ M eV}$$

$$m_0 c^2 = 938 \text{ M eV}$$

$$p = 310 \text{ M eV} / c$$

$$E_{kin} = 50 \text{ M eV}$$



*Beam energies*

*1.) reminder of some relativistic formula*

*rest energy*       $E_0 = m_0 c^2$

*total energy*       $E = \gamma * E_0 = \gamma * m_0 c^2$

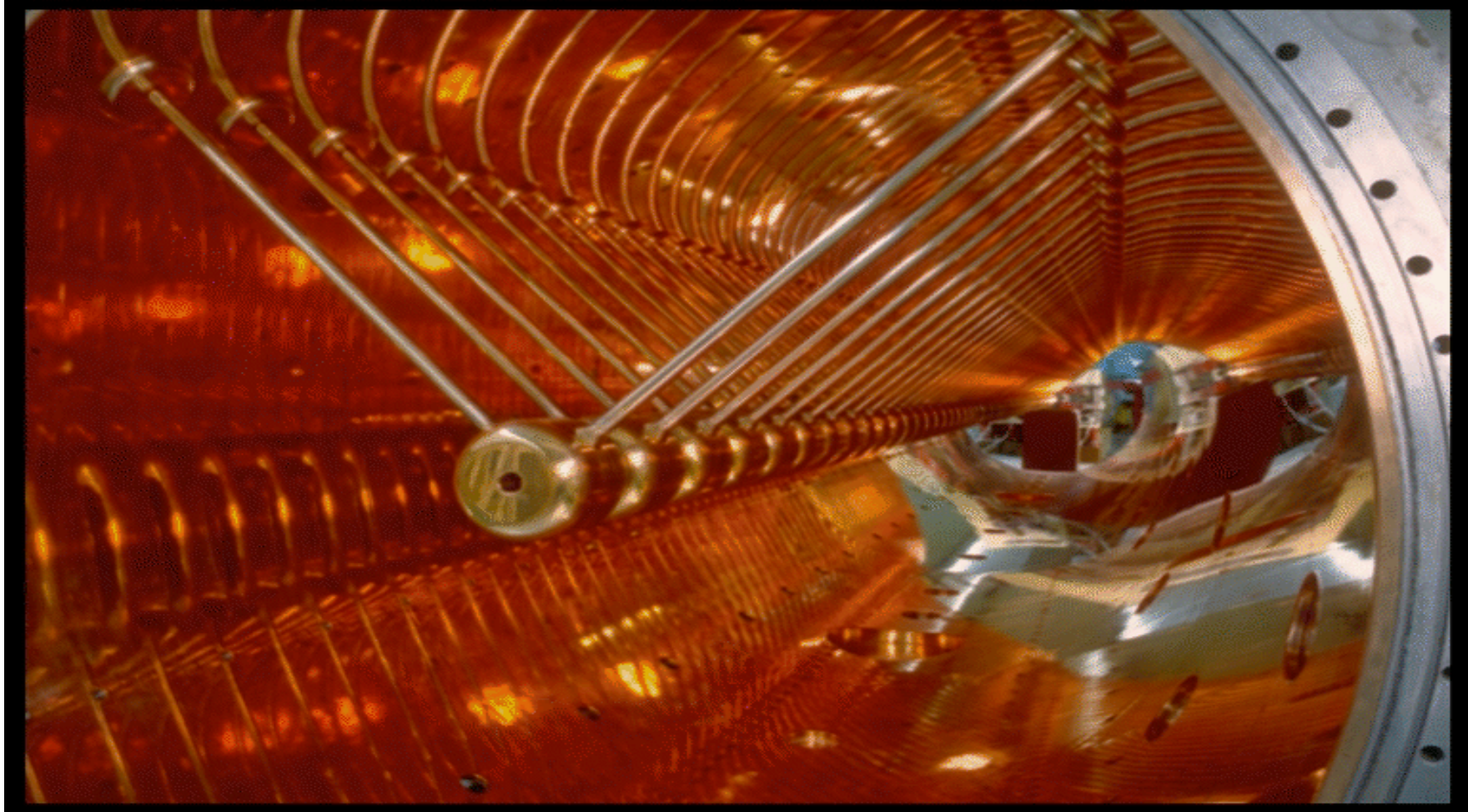
*kinetic energy*       $E_{kin} = E_{total} - m_0 c^2$

*momentum*       $E^2 = c^2 p^2 + m_0^2 c^4$

*GSI: Unilac, typical Energie  $\approx 20$  MeV per  
Nukleon,  $\beta \approx 0.04 \dots 0.6$ ,  
Protons/Ions,  $\nu = 110$  MHz*

**Energy Gain per „Gap“:**

$$W = q U_0 \sin \omega_{RF} t$$



***Application:** until today THE standard proton / ion pre-accelerator  
CERN Linac 4 is being built at the moment*

## 4.) The Cyclotron: (Livingston / Lawrence ~1930)

*Idea: Bend a Linac on a Spiral*  
*Application of a constant magnetic field*  
*keep  $B = \text{const}$ ,  $RF = \text{const}$*

→ *Lorentzforce*

$$\vec{F} = q * (\vec{v} \times \vec{B}) = q * v * B$$

*circular orbit*

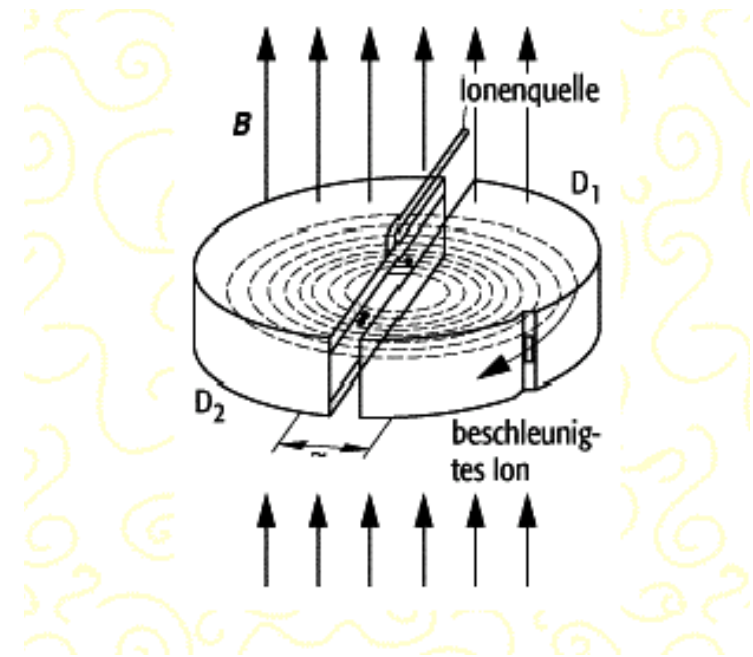
$$q * v * B = \frac{m * v^2}{R} \quad \rightarrow \quad B * R = p / q$$

*increasing radius for  
increasing momentum*  
→ *Spiral Trajectory*

*revolution frequency*

$$\omega_z = \frac{q}{m} * B_z$$

*the cyclotron (rf-) frequency  
is independent of the momentum*

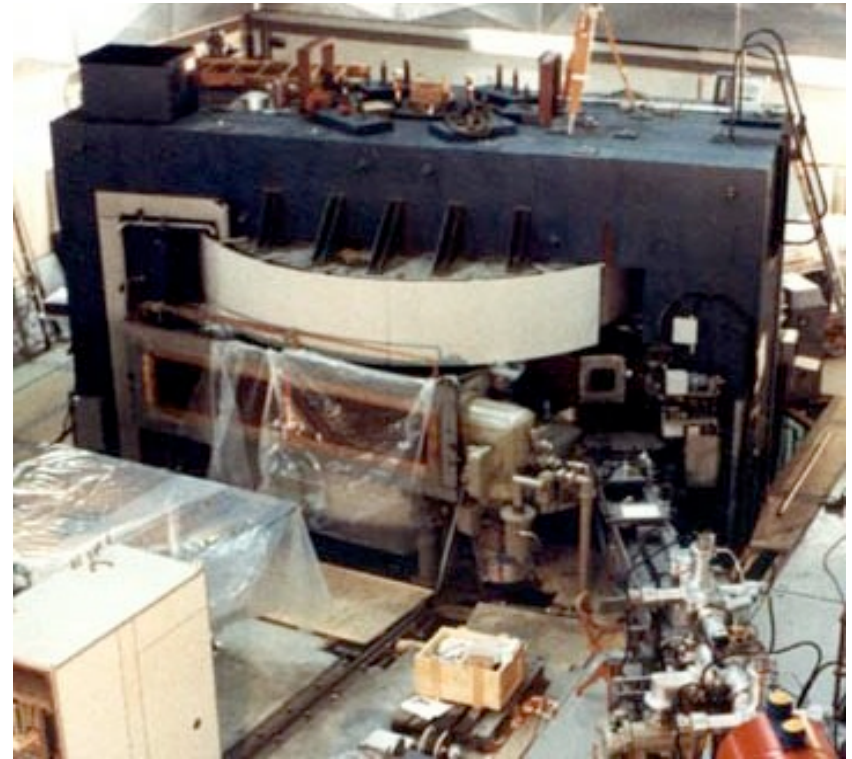


## Cyclotron:

**!**  $\omega$  is constant for a given  $q$  &  $B$

**!!**  $B \cdot R = p/q$   
large momentum  $\rightarrow$  huge magnet

**!!!!**  $\omega \sim 1/m \neq \text{const}$  works properly only for  
non relativistic particles



*PSI Zurich*

### **Application:**

**Work horses for medium energy protons**

**Proton / Ion Acceleration up to  $\approx 60$  MeV (proton energy)**

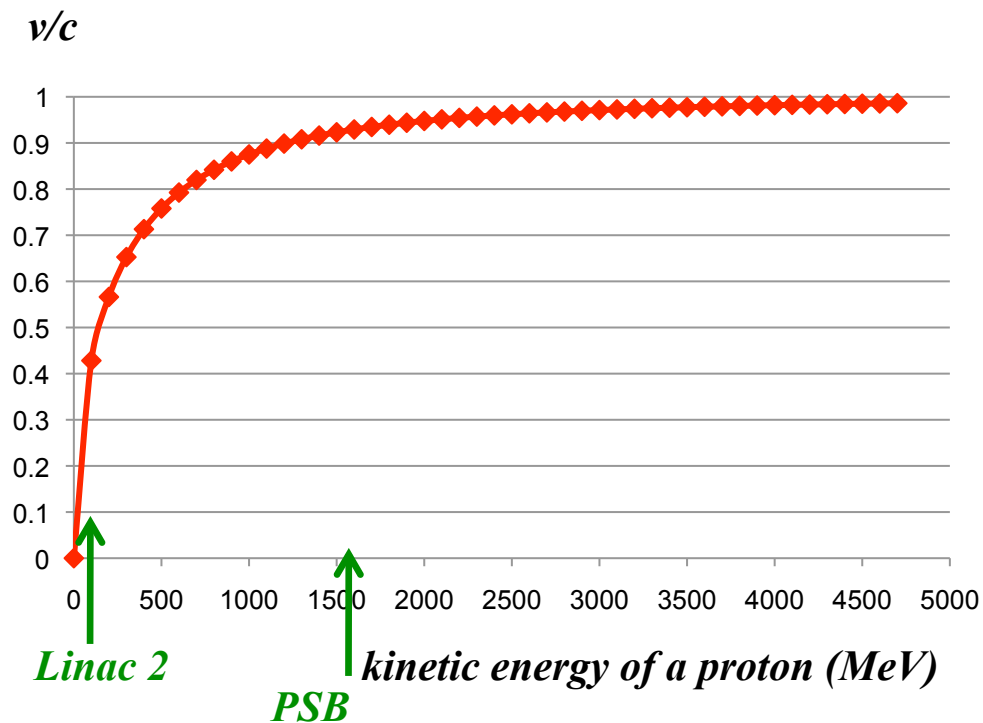
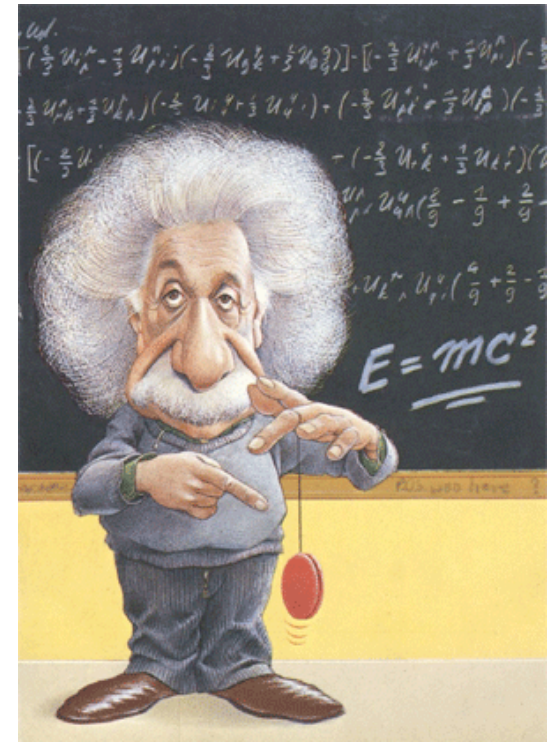
**nuclear physics**

**radio isotope production, proton / ion therapy**

## Beam Energy

... so sorry, here we need help from Albert:

$$\gamma = \frac{E_{total}}{mc^2} = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} \quad \frac{v}{c} = \sqrt{1 - \frac{mc^2}{E^2}}$$



### CERN Accelerators

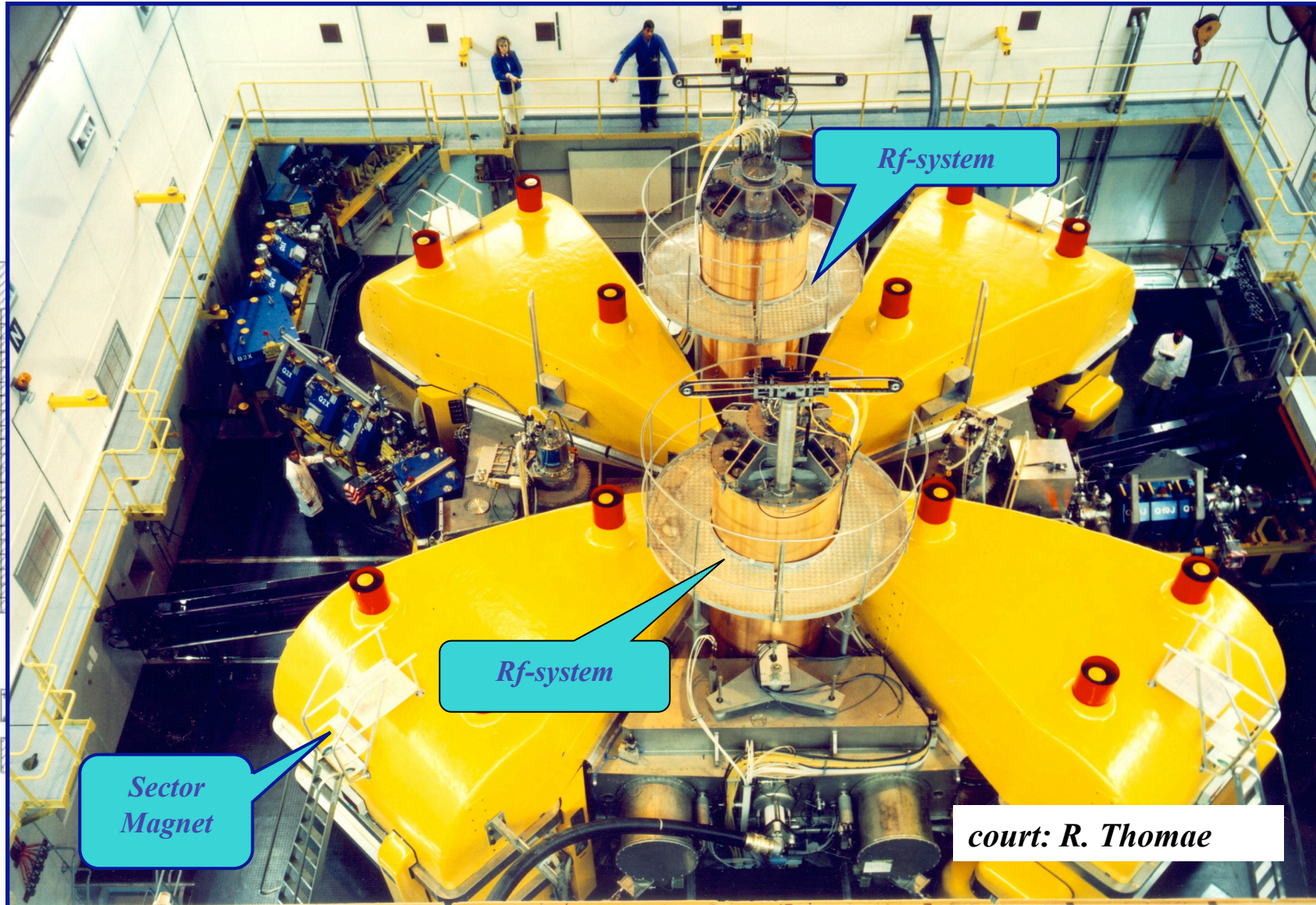
	kin. Energy	$\gamma$
<i>Linac 2</i>	60 MeV	1.06
<i>PS</i>	26 GeV	27
<i>SPS</i>	450 GeV	480
<i>LHC</i>	7 TeV	7460

remember: proton mass = 938 MeV

# Cyclotron:

modern trends: Problem:  $m \neq \text{const.}$   
→ non relativistic machine

$$\omega_z = \frac{e * B_z}{\gamma * m m_0}$$



Rf-system

Rf-system

Sector Magnet

court: R. Thomae

MeV

ons



## 5.) The Betatron: Wideroe 1928/ Kerst 1940

...apply the transformer principle to an electron beam: *no RF system needed, changing magnetic B field*

Idea: a time varying magnetic field induces a voltage that will accelerate the particles

Farady induction law

$$\oint \vec{E} d\vec{s} = - \int_A \dot{B} df = - \dot{\Phi}$$

circular orbit

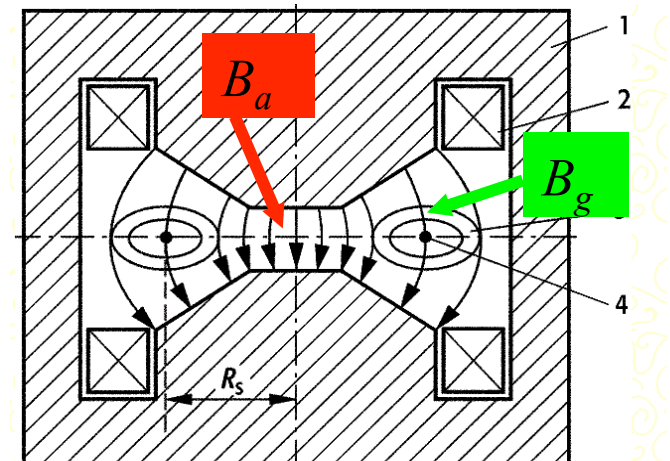
$$\frac{mv^2}{r} = e * v * B$$

$$\rightarrow p = e * B * r$$

magnetic flux through this orbit area

$$\Phi = \int B df = \pi r^2 * B_a$$

schematic design



*induced electric field*

$$\oint \vec{E} ds = \vec{E} * 2\pi r = -\dot{\Phi} \Rightarrow \vec{E} = \frac{-\pi r^2 * \dot{B}_a}{2\pi r} = -\frac{1}{2} \dot{B}_a r$$

*force acting on the particle:*

$$\dot{p} = -|\vec{E}|e = \frac{1}{2} \dot{B}_a r$$

*The increasing momentum of the particle has to be accompanied by a rising magnetic guide field:*

$$\dot{p} = e * \dot{B}_g r$$

$$B_g = \frac{1}{2} B_a$$



*robust, compact machines,  
Energy  $\leq$  300...500 MeV,  
limit: Synchrotron radiation*

## 6.) Synchrotrons / Storage Rings / Colliders:

*Wideroe 1943, McMillan, Veksler 1944,  
Courant, Livingston, Snyder 1952*

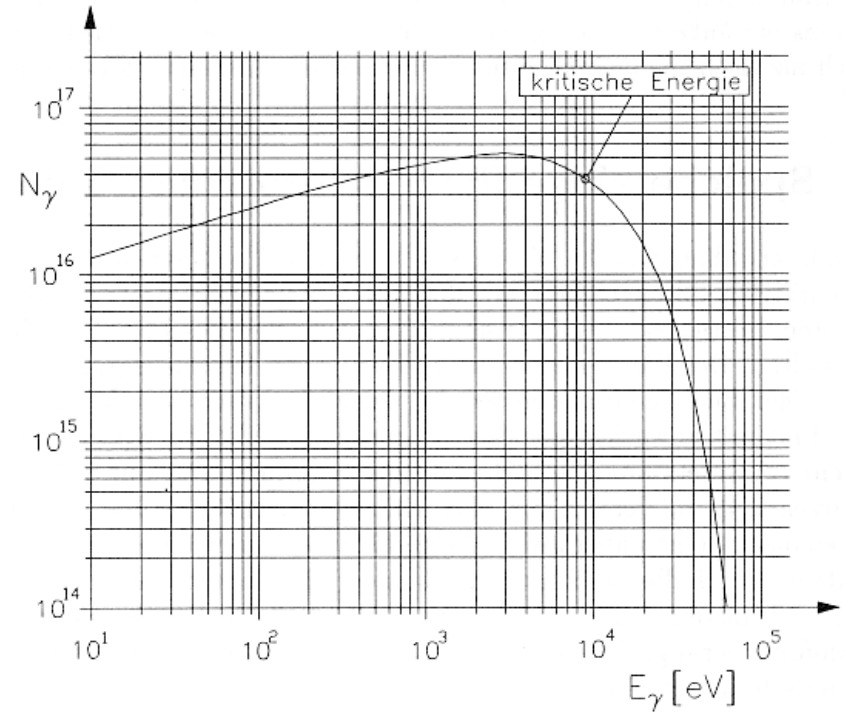
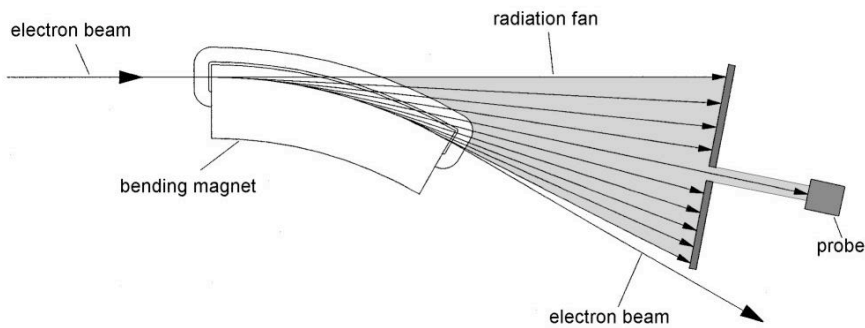
*Idea: define a circular orbit of the particles,  
keep the beam there during acceleration,  
put magnets at this orbit to **guide and focus***



*Advanced Photon Source,  
Berkley*

# 7.) Electron Storage Rings

## Production of Synchrotron Light



$$P_s = \frac{e^2 c}{6\pi\epsilon_0} * \frac{1}{(m_0 c^2)^4} \frac{E^4}{R^4}$$

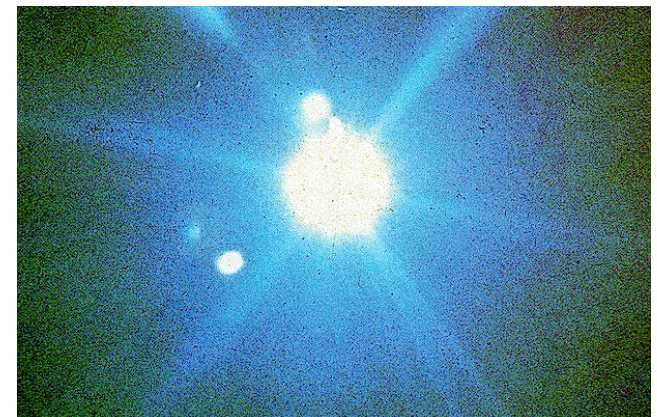
**Radiation Power**

$$\Delta E = \frac{e^2}{3\epsilon_0 (m_0 c^2)^4} \frac{E^4}{R}$$

**Energy Loss per turn**

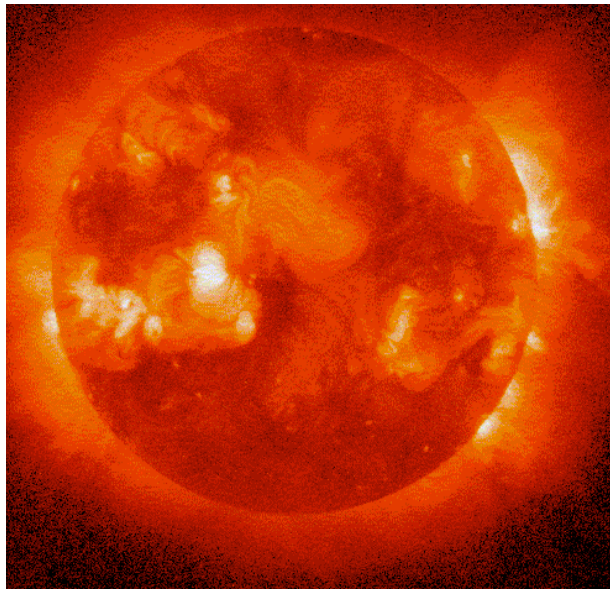
$$\omega_c = \frac{3c\gamma^3}{2R}$$

**„typical Frequency“  
of emitted light**



# Application of Synchrotron Light Analysis at Atoms & Molecules

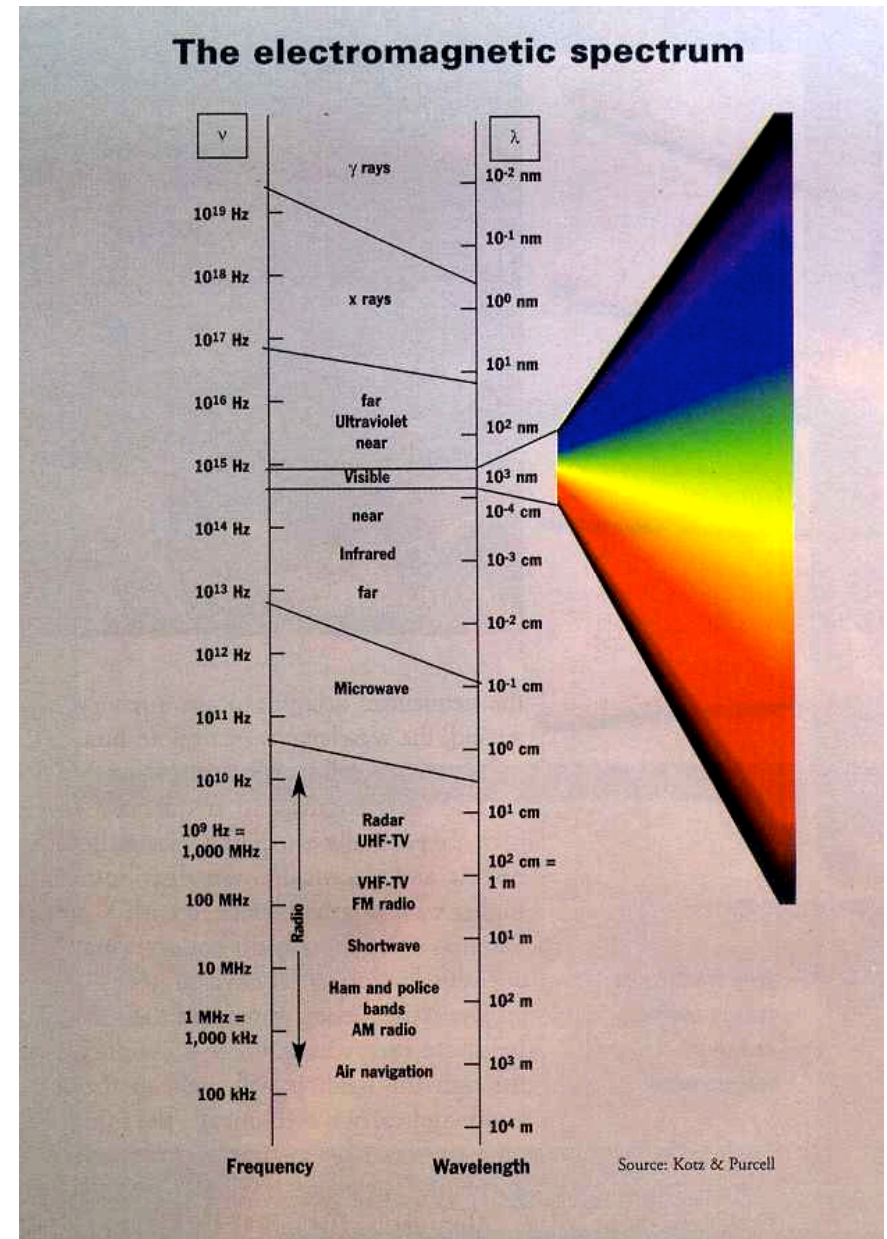
*The electromagnetic Spectrum:*



*having a closer look at the sun ...*

**Light:**

$\lambda \approx 400 \text{ nm} \dots 800 \text{ nm}$   
*1 Oktave*



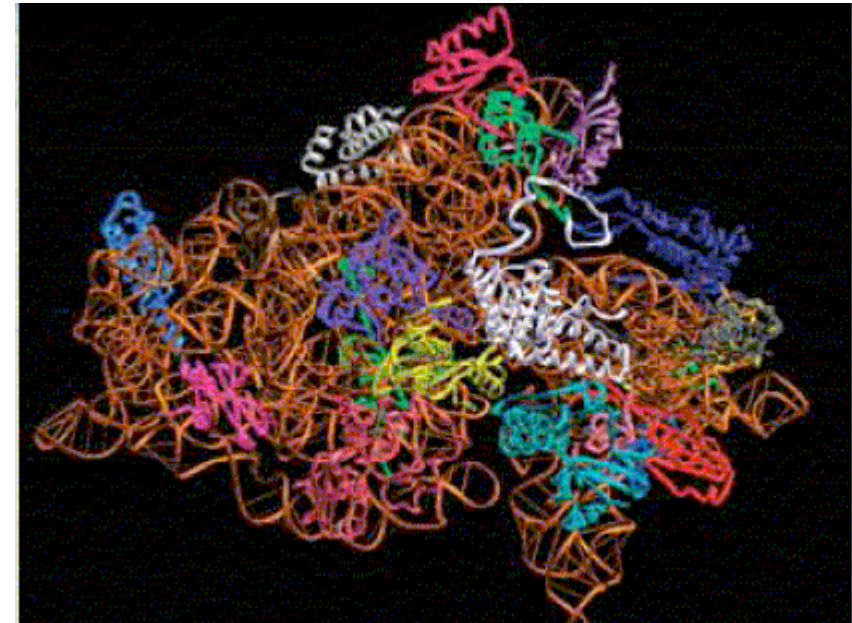
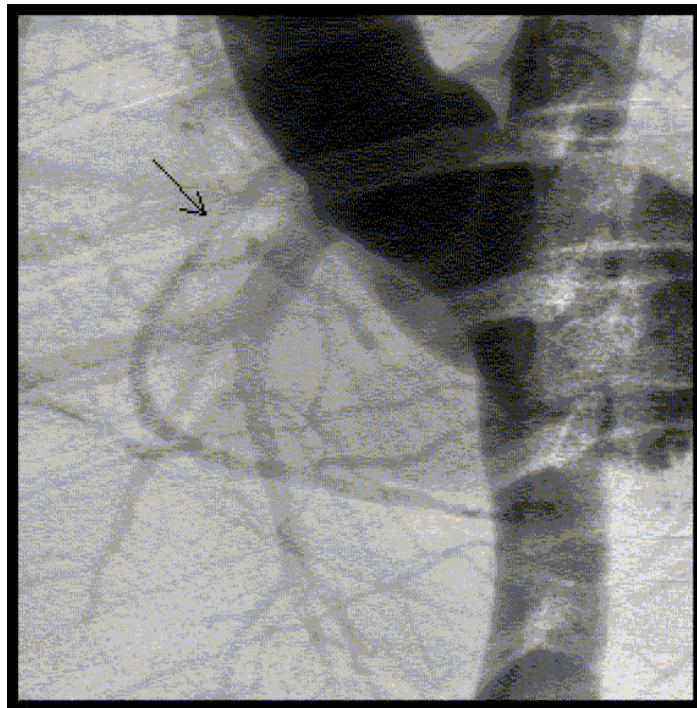
## *Analysis of Cell structures*

### **Structure of a Ribosom**

Ribosomen are responsible for the protein production in living cells.

The structure of these Ribosom molecules can be analysed using brilliant synchrotron light from electron storage rings

(Quelle: Max-Planck-Arbeitsgruppen für Strukturelle Molekularbiologie)



Structure of the ribosome, the "protein factory" in living cells

## *Angiographie*

x-ray method applicable for the imaging of coronar heart arteria

## 8.) Synchrotrons as Collider Rings (1960 ... ):

### Beam energies

#### 1.) reminder of some relativistic formula

total energy  $E^2 = p^2 c^2 + m_0^2 c^4$

→  $cp = \sqrt{E^2 - m_0^2 c^4} = \sqrt{(\gamma m_0 c^2)^2 - (m_0 c^2)^2} = \sqrt{\gamma^2 - 1} m_0 c^2$

→  $cp = \gamma \beta * m_0 c^2$

#### 2.) energy balance of colliding particles

rest energy of a particle  $E_0^2 = (m_0 c^2)^2 = E^2 - p^2 c^2$

in exactly the same way we define a center of mass energy of a system of particles:

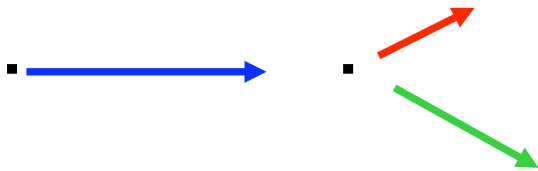
$$E_{cm}^2 = \left( \sum_i E_i \right)^2 - \left( \sum_i cp_i \right)^2$$

two colliding particles

$$E_{cm}^2 = (\gamma_1 m_1 + \gamma_2 m_2)^2 c^4 - (cp_1 + cp_2)^2$$

$$E_{cm}^2 = (\gamma_1 m_1 + \gamma_2 m_2)^2 c^4 - (\gamma_1 \beta_1 m_1 + \gamma_2 \beta_2 m_2)^2 c^4$$

**Example 1): proton beam on fixed proton**



$$m_1 = m_2 = m_p$$

$$\gamma_2 = 1$$

$$\beta_2 = 0$$

$$E_{cm}^2 = (\gamma_1 + 1)^2 m_p^2 c^4 - (\gamma_1 \beta_1 m_p)^2 c^4$$

remember:

$$\beta\gamma = \sqrt{\gamma^2 - 1}$$

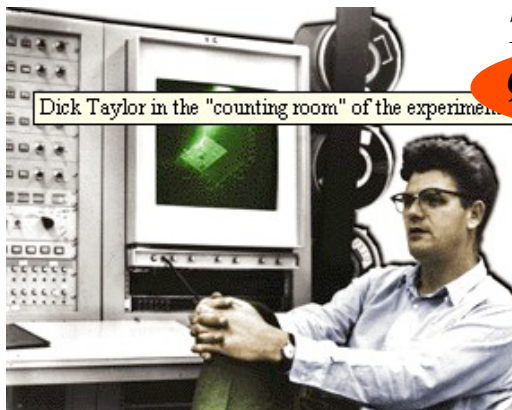


$$E_{cm}^2 = (\gamma_1 + 1)^2 m_p^2 c^4 - (\gamma_1^2 - 1) m_p^2 c^4$$

$$E_{cm}^2 = 2(\gamma_1 - 1) m_p^2 c^4$$

$$E_{cm} = \sqrt{2(\gamma_1 - 1)} m_p c^2$$

*Discovery of the Quarks: electron beam on fixed proton / neutron target*



*Taylor/Kendall/Friedman: Discovery of the  
Quark structure of protons and neutrons  
1966-1978 ..... 1990 Nobel Prize*



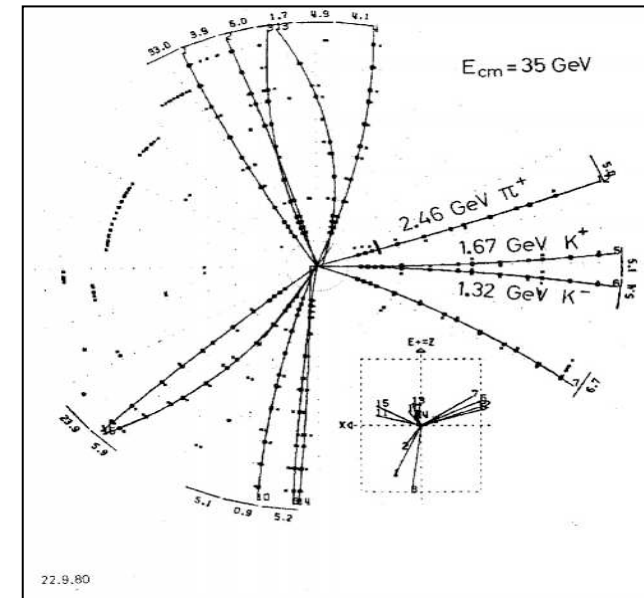
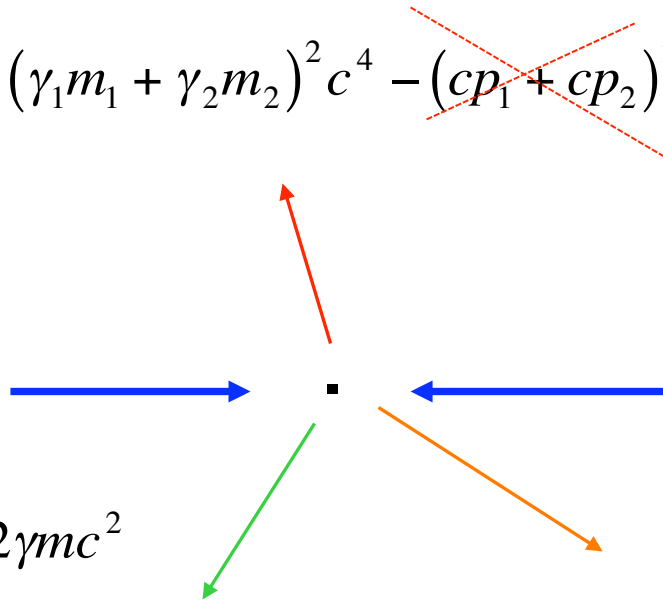
**Example 2 : particle anti-particle collider**

$e^+ / e^-$  ,  $p / \bar{p}$  ,  $m^+ / m^-$

- \* store both **counter rotating** particle beams in the same magnet lattice
- \* no conservation of quantum numbers required

$$E_{cm}^2 = (\gamma_1 m_1 + \gamma_2 m_2)^2 c^4 - (\cancel{cp_1} + \cancel{cp_2})^2$$

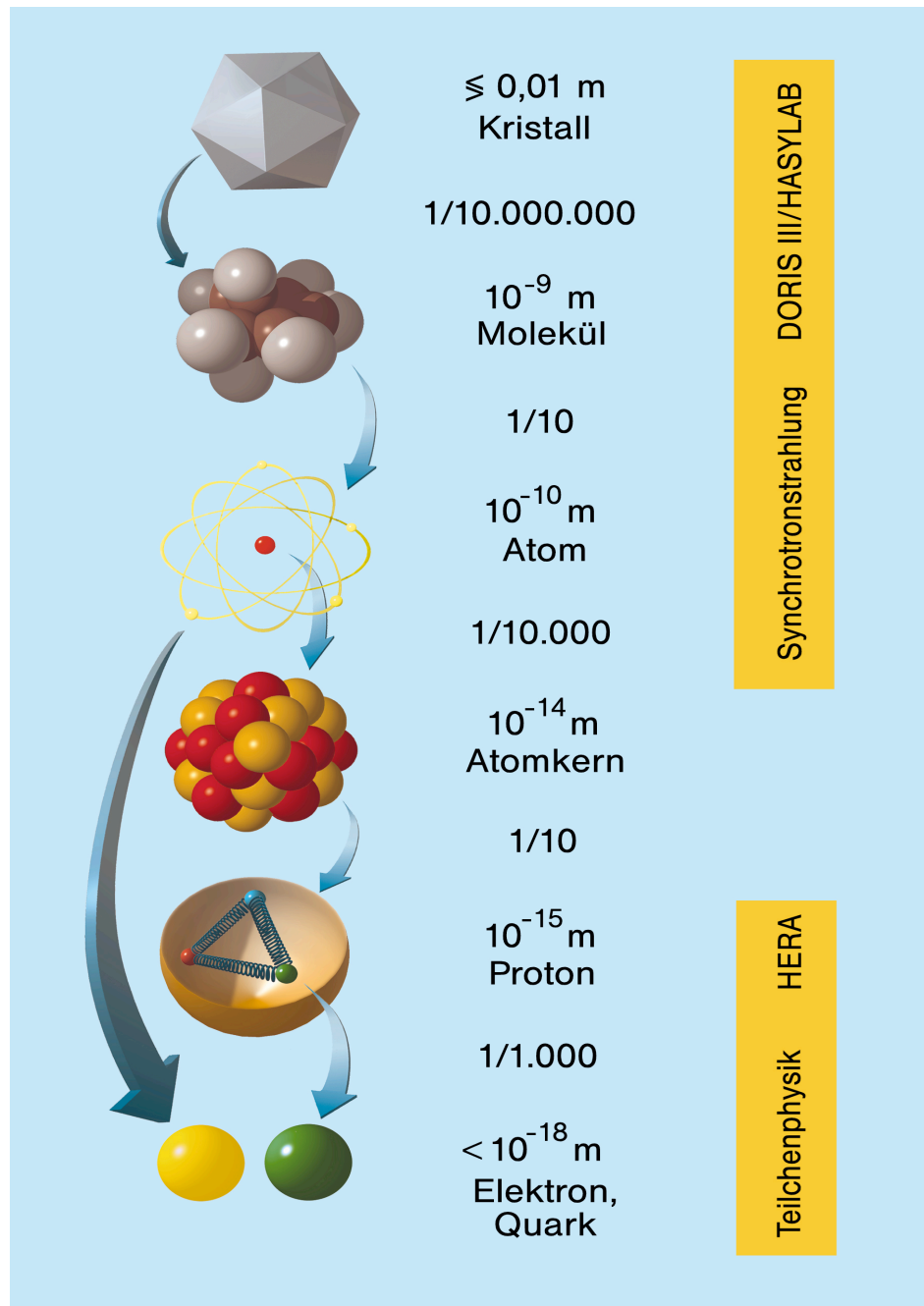
$$E_{cm} = 2\gamma mc^2$$



**1979 PETRA Collider at DESY  
discovery of the gluon**

- Colliders:**
- \* working at highest energies (“cm”)
  - \* store the particles for long time in an accelerator
  - \* bring two beams into collision
  - \* particle density !!
  - \* preparation / technical design / field qualities are extreme

## Structure of Matter



## 9.) Storage Rings for Structure Analysis

*synchrotron light: nm*

*electron scattering: Å ...  $10^{-18}$  m*

*de Broglie:*

$$\lambda = \frac{h}{p} = \frac{ch}{E}$$

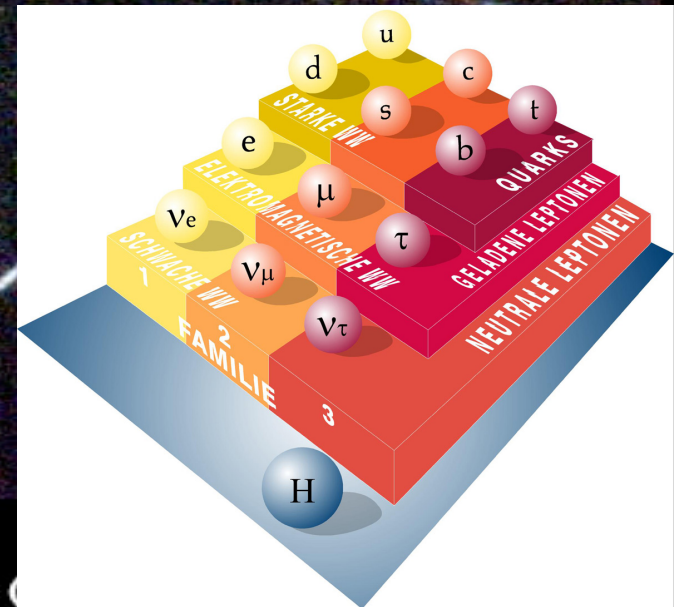
$$E \approx pc$$

## 10.) Storage Rings to Explain the Universe

*Precision Measurements of the Standard Model,  
Search for Higgs, Supersymmetry, Dark Matter  
Physics beyond the Standard Model*

**Hubble Deep Field**

PRC96-01a · ST ScI OPO · January 15, 1996 · R. Williams



# *Introduction to Accelerator Physics* *Beam Dynamics for „Summer Students“*

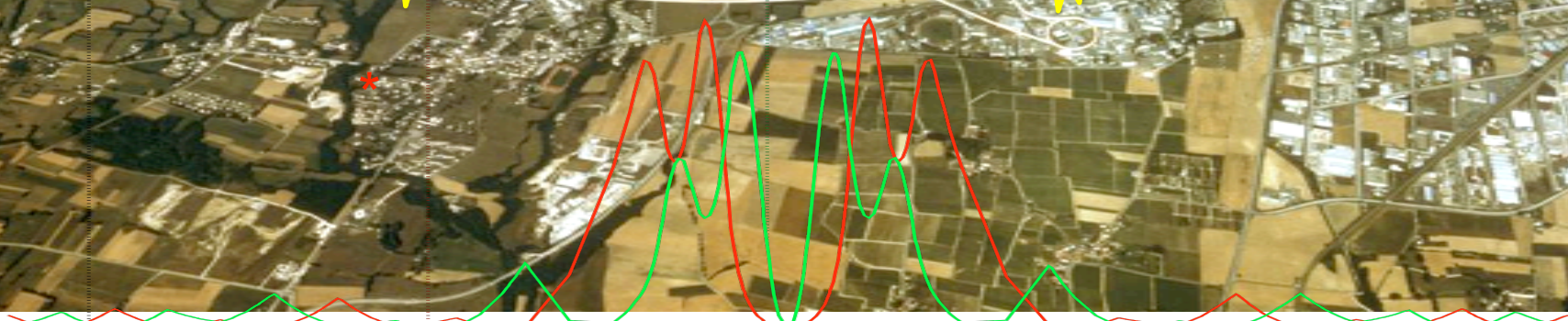
*Bernhard Holzer,  
CERN-LHC*

## *IP5 The Ideal World* *I.) Magnetic Fields and Particle Trajectories*

**IP2**

**IP1**

**IP8**



## *Luminosity Run of a typical storage ring:*

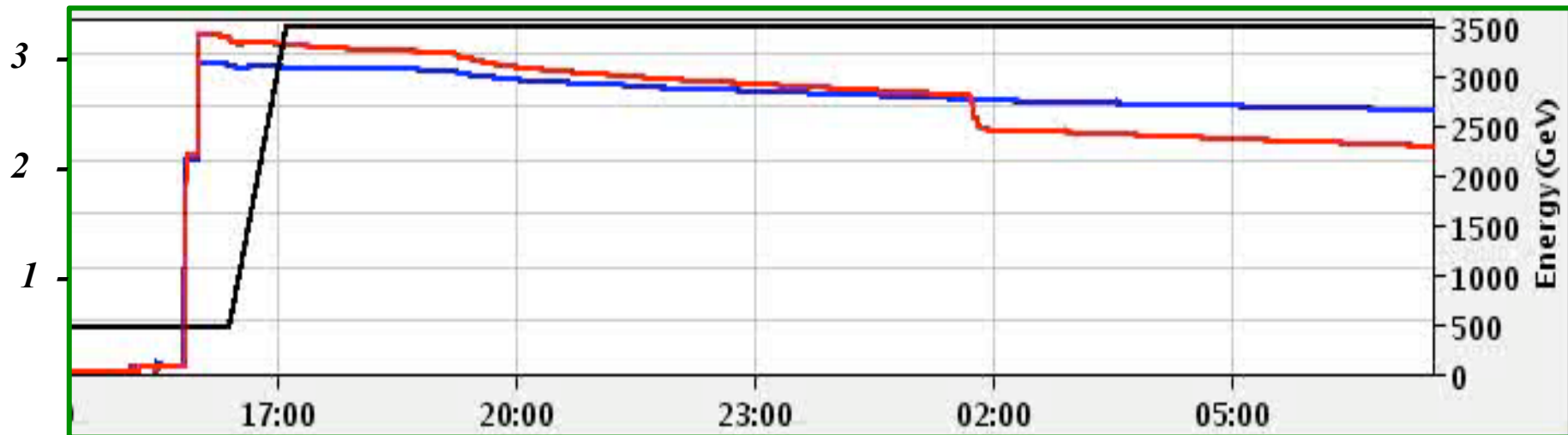
*LHC Storage Ring: Protons accelerated and stored for 12 hours*

*distance of particles travelling at about  $v \approx c$*

*$L = 10^{10}$ - $10^{11}$  km*

*... several times Sun - Pluto and back ♪*

*intensity ( $10^{11}$ )*



- *guide the particles on a well defined orbit („design orbit“)*
- *focus the particles to keep each single particle trajectory within the vacuum chamber of the storage ring, i.e. close to the design orbit.*

# 1.) Introduction and Basic Ideas

„ ... in the end and after all it should be a kind of circular machine“

→ need transverse deflecting force

Lorentz force  $\vec{F} = q * (\vec{E} + \vec{v} \times \vec{B})$

typical velocity in high energy machines:

$$v \approx c \approx 3 * 10^8 \text{ m/s}$$

Example:♪

$$B = 1 \text{ T} \quad \rightarrow \quad F = q * 3 * 10^8 \frac{\text{m}}{\text{s}} * 1 \frac{\text{Vs}}{\text{m}^2}$$

$$F = q * 300 \frac{\text{MV}}{\text{m}}$$

equivalent el. field ...♪  $E$

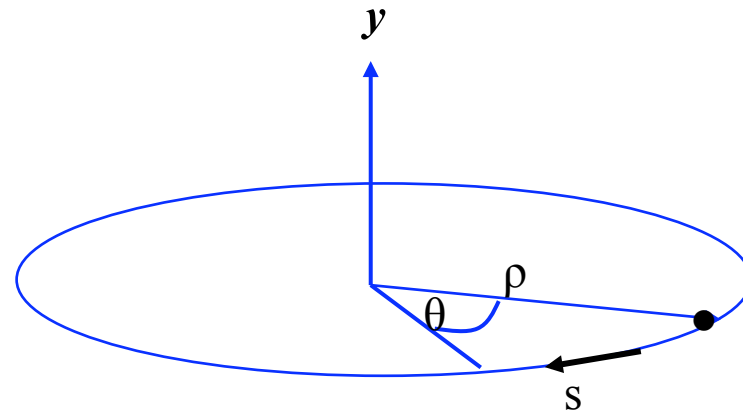
technical limit for el. field:♪

$$E \leq 1 \frac{\text{MV}}{\text{m}}$$

*old greek dictum of wisdom:*

*if you are clever, you use magnetic fields in an accelerator wherever it is possible.*

*The ideal circular orbit*



*circular coordinate system*

*condition for circular orbit:*

*Lorentz force*

$$F_L = e v B$$

*centrifugal force*

$$F_{centr} = \frac{\gamma m_0 v^2}{\rho}$$

$$\frac{\gamma m_0 v^2}{\rho} = e v B$$

$$\frac{p}{e} = B \rho$$

*B ρ = "beam rigidity"*

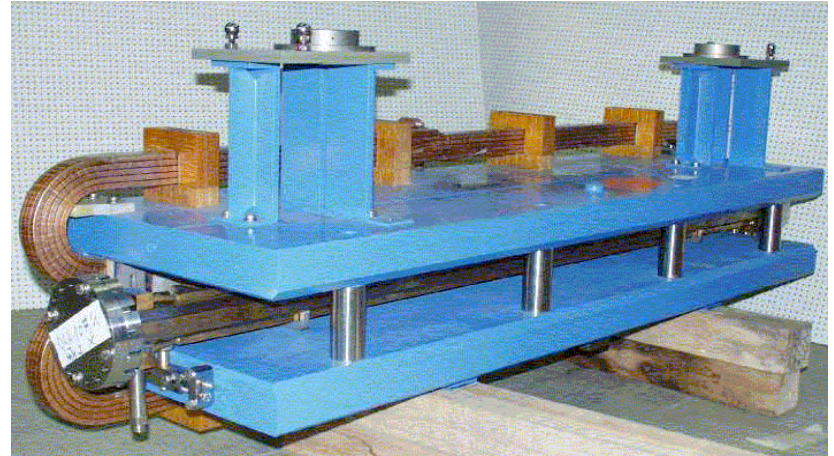


## 2.) The Magnetic Guide Field

### Dipole Magnets:

define the ideal orbit  
**homogeneous field** created  
 by two flat pole shoes

$$B = \frac{\mu_0 n I}{h}$$



Normalise magnetic field to momentum:

$$\frac{p}{e} = B \rho \quad \longrightarrow \quad \frac{1}{\rho} = \frac{e B}{p}$$

convenient units:

$$B = [T] = \left[ \frac{Vs}{m^2} \right] \quad p = \left[ \frac{GeV}{c} \right]$$

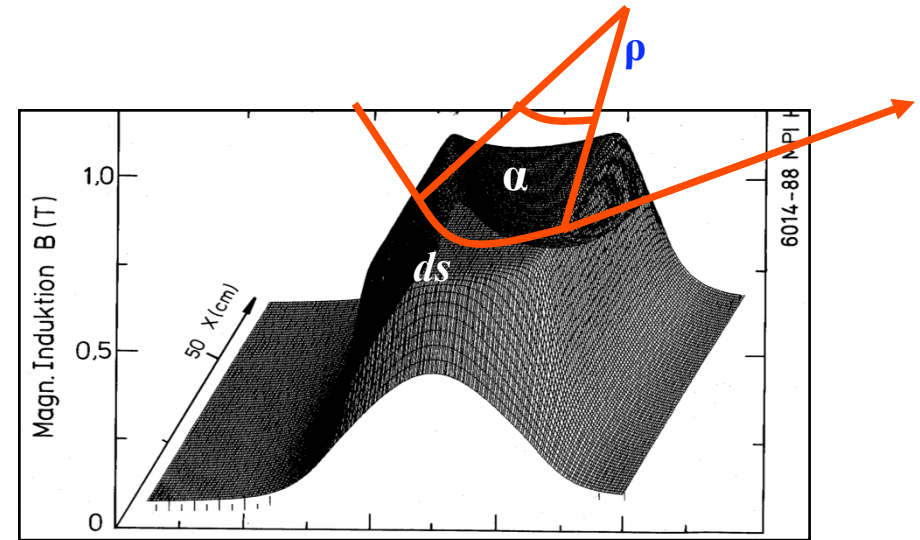
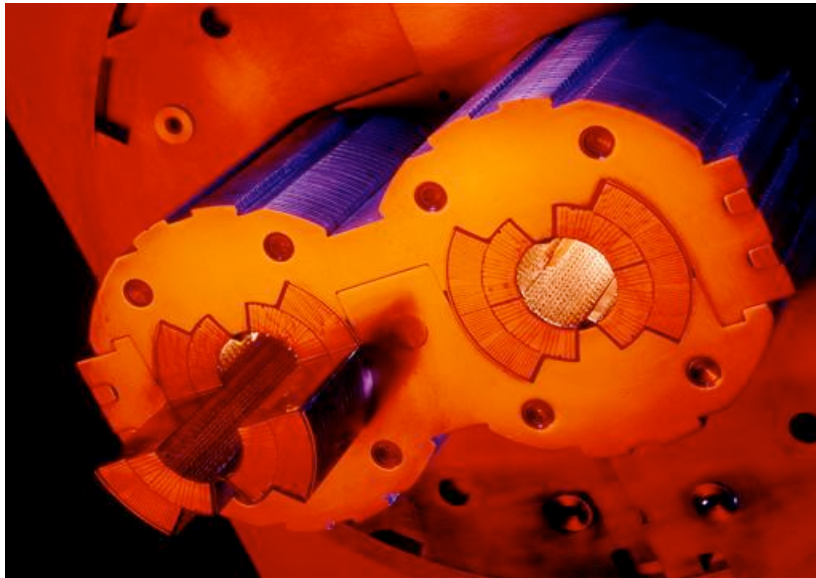
Example LHC:

$$\left. \begin{aligned} B &= 8.3 T \\ p &= 7000 \frac{GeV}{c} \end{aligned} \right\}$$

$$\frac{1}{\rho} = e \frac{8.3 \frac{Vs}{m^2}}{7000 * 10^9 \frac{eV}{c}} = \frac{8.3 s * 3 * 10^8 \frac{m}{s}}{7000 * 10^9 m^2}$$

$$\frac{1}{\rho} = 0.333 \frac{8.3}{7000} \frac{1}{m}$$

# The Magnetic Guide Field



field map of a storage ring dipole magnet

$$\rho = 2.53 \text{ km} \quad \longrightarrow \quad 2\pi\rho = 17.6 \text{ km} \approx 66\%$$

$$B \approx 1 \dots 8 \text{ T}$$

rule of thumb:

$$\frac{1}{\rho} \approx 0.3 \frac{B [T]}{p [\text{GeV}/c]}$$

„normalised bending strength“

## *The Problem:*

*LHC Design Magnet current:  $I=11850\text{ A}$*

*and the machine is 27 km long !!!*

*Ohm's law:  $U = R * I$ ,  $P = R * I^2$*

*Problem:*

*reduce ohmic losses to the absolute minimum*

Georg Simon Ohm

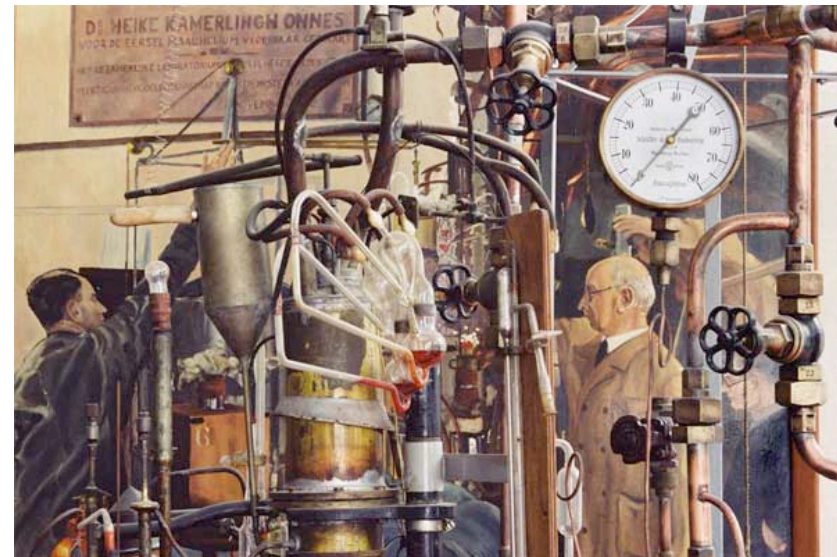


Born

17 March 1789  
Erlangen, Germany

## *The Solution:*

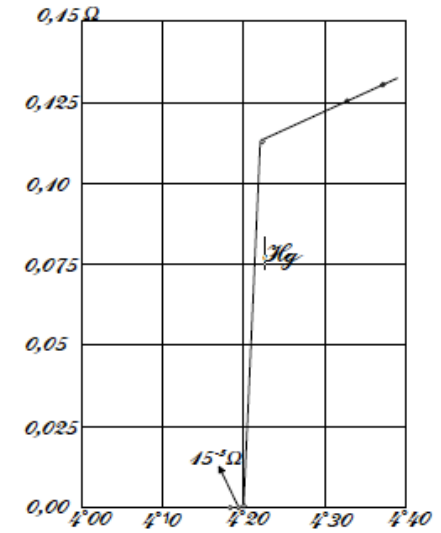
*super conductivity*



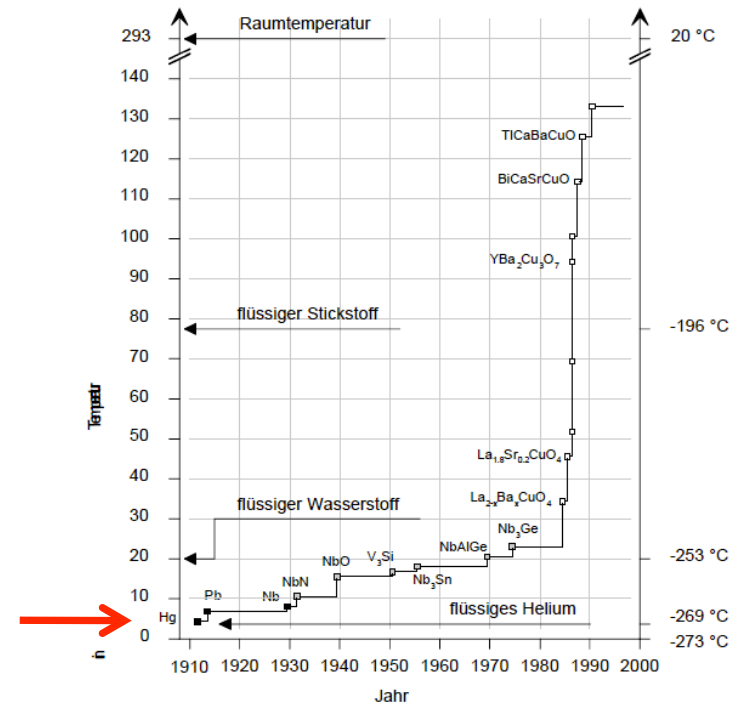
# Super Conductivity



discovery of sc. by  
H. Kamerling Onnes,  
Leiden 1911

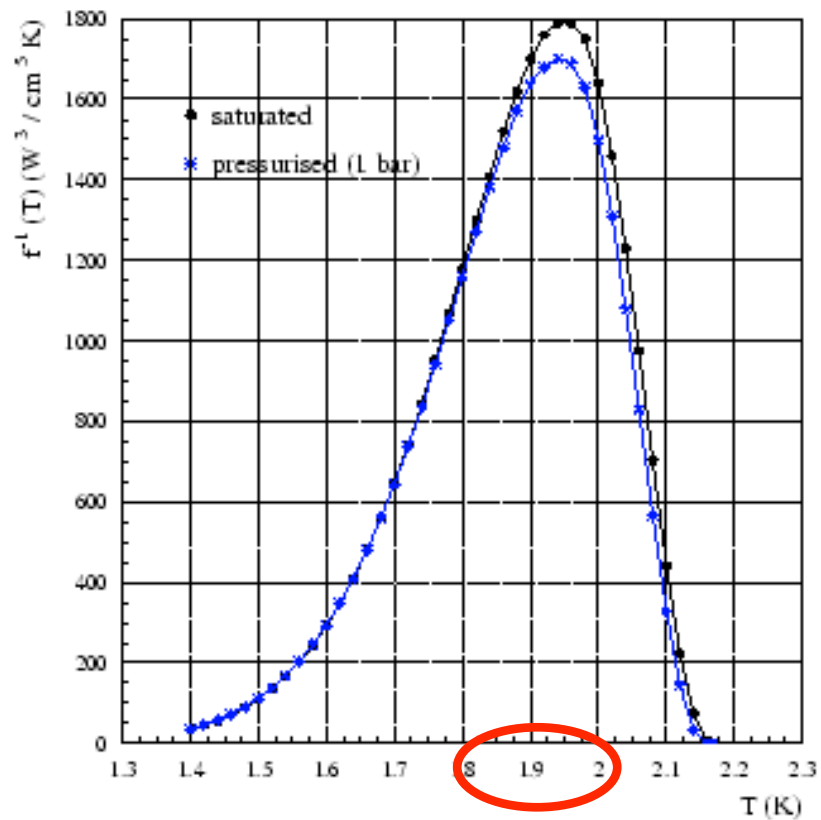
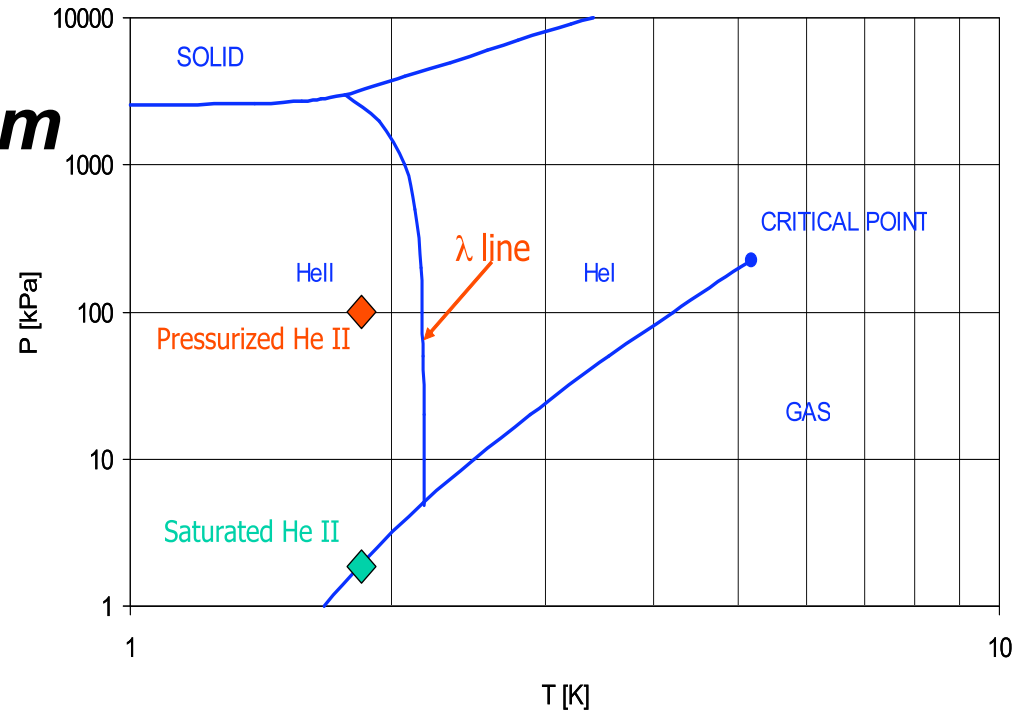


LHC 1.9 K cryo plant



# Superfluid helium: 1.9 K cryo system

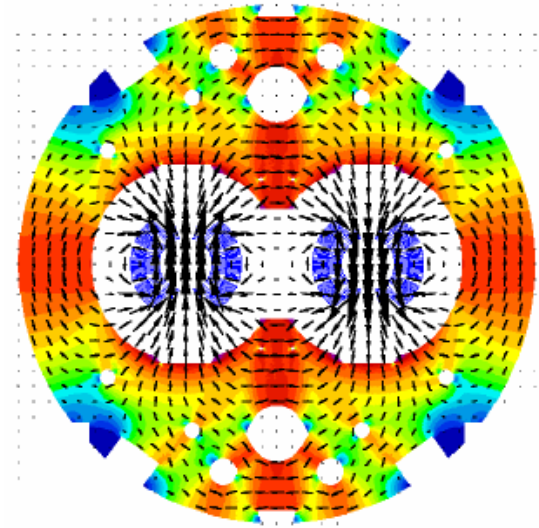
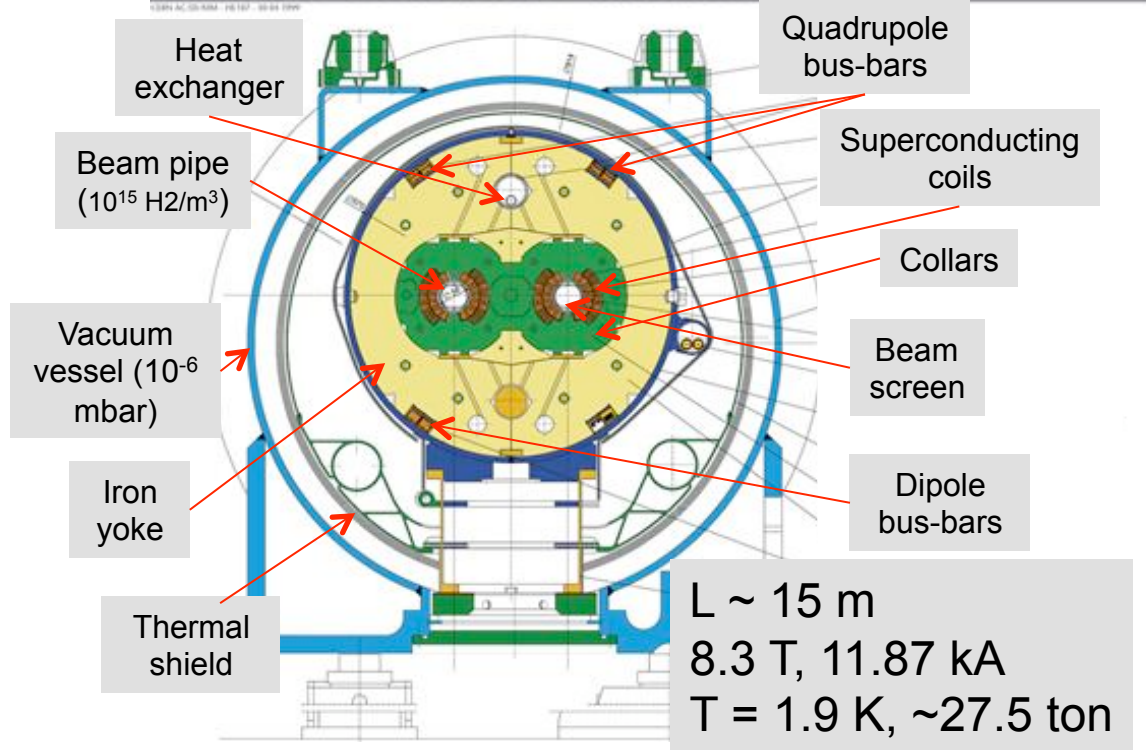
*Phase diagramm of Helium*



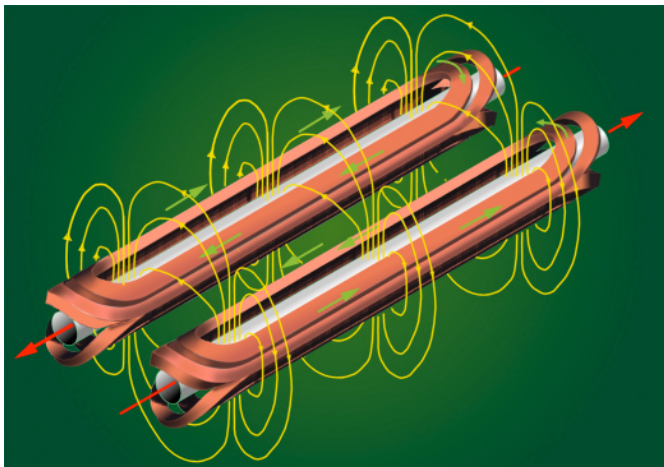
*thermal conductivity of fl. Helium  
in supra fluid state*

# LHC: The -1232- Main Dipole Magnets

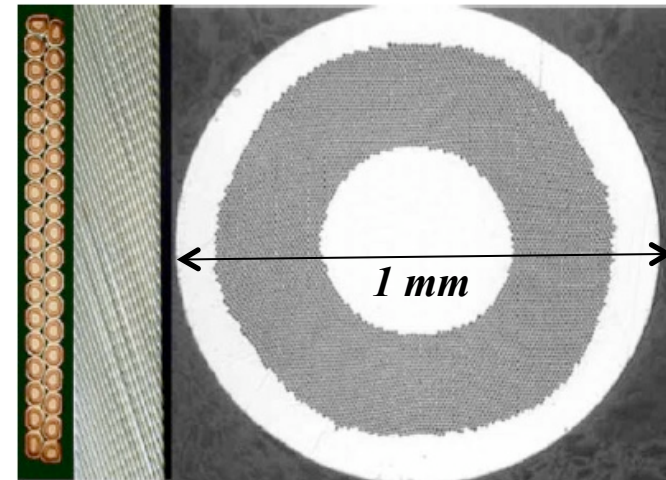
LHC DIPOLE : STANDARD CROSS-SECTION



required field quality:  
 $\Delta B/B = 10^{-4}$



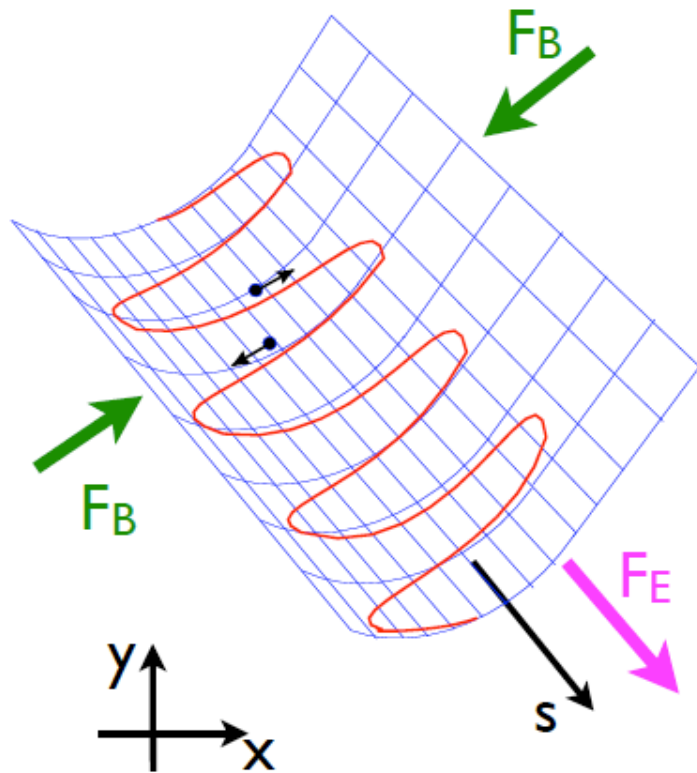
$6 \mu\text{m}$  Ni-Ti filament



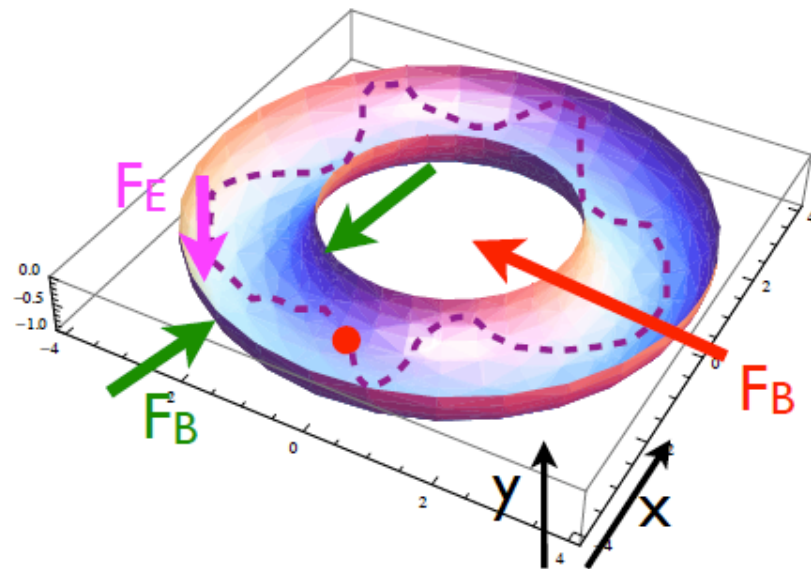
## 2.) Focusing Properties - Transverse Beam Optics

$$\overline{F}(t) = q \left( \underbrace{\overline{E}(t)}_{F_E} + \underbrace{\overline{v}(t) \otimes \overline{B}(t)}_{F_B} \right)$$

Linear Accelerator

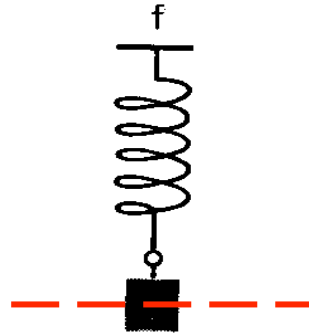


Circular Accelerator



## 2.) Focusing Properties - Transverse Beam Optics

*classical mechanics:  
pendulum*



*there is a **restoring force**, proportional to the elongation  $x$ :*

$$m^* \frac{d^2 x}{dt^2} = -c^* x$$

*general solution: free harmonic oscillation*

$$x(t) = A^* \cos(\omega t + \varphi)$$

**Storage Ring:** we need a **Lorentz force** that rises as a function of the **distance to .....** ?

**..... the design orbit**

$$F(x) = q^* v^* B(x)$$



# Quadrupole Magnets:

required: *focusing forces* to keep trajectories in vicinity of the ideal orbit

*linear increasing Lorentz force*

*linear increasing magnetic field*

$$B_y = g x \quad B_x = g y$$

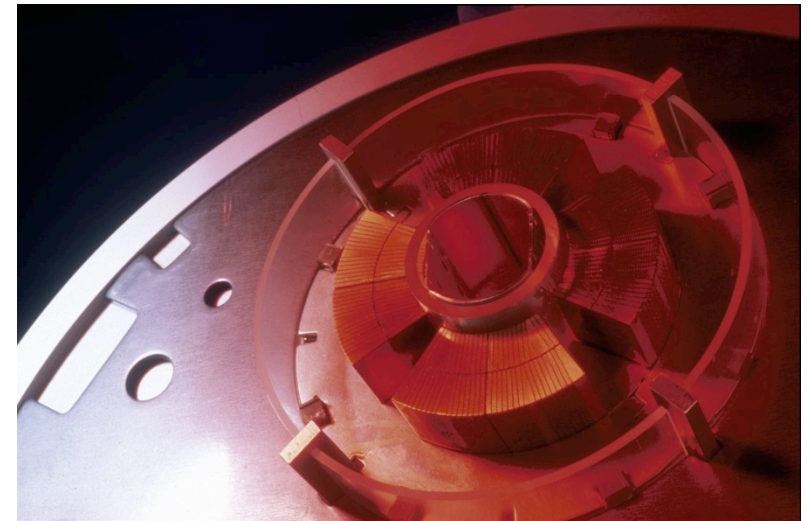
normalised quadrupole field:



$$k = \frac{g}{p/e}$$

simple rule:

$$k = 0.3 \frac{g(T/m)}{p(GeV/c)}$$



LHC main quadrupole magnet

$$g \approx 25 \dots 220 \text{ T/m}$$

what about the vertical plane:  
... Maxwell

$$\vec{\nabla} \times \vec{B} = \cancel{\vec{j}} + \cancel{\frac{\partial \vec{E}}{\partial t}} = 0$$

$$\Rightarrow \frac{\partial B_y}{\partial x} = \frac{\partial B_x}{\partial y} = g$$

## *Focusing forces and particle trajectories:*

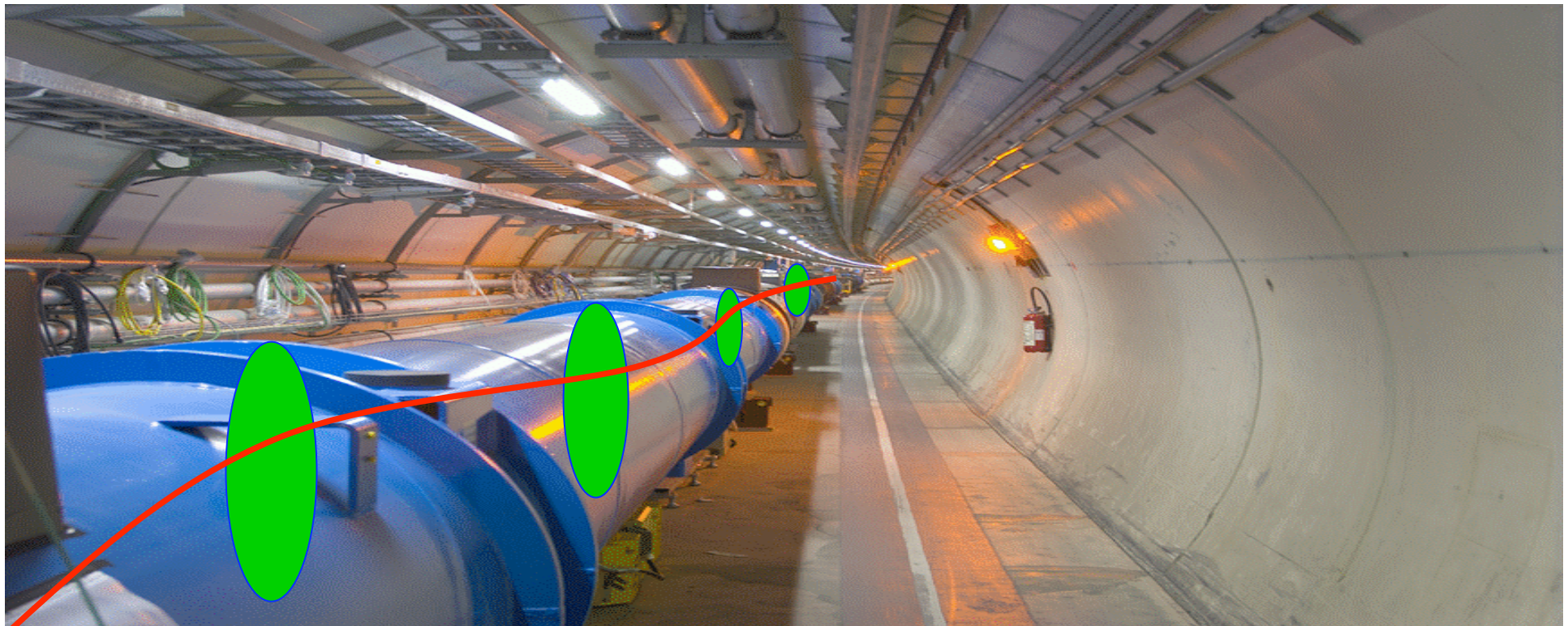
*normalise magnet fields to momentum  
(remember:  $\mathbf{B}^*\rho = \mathbf{p} / q$ )*

*Dipole Magnet*

$$\frac{B}{p/q} = \frac{B}{B\rho} = \frac{1}{\rho}$$

*Quadrupole Magnet*

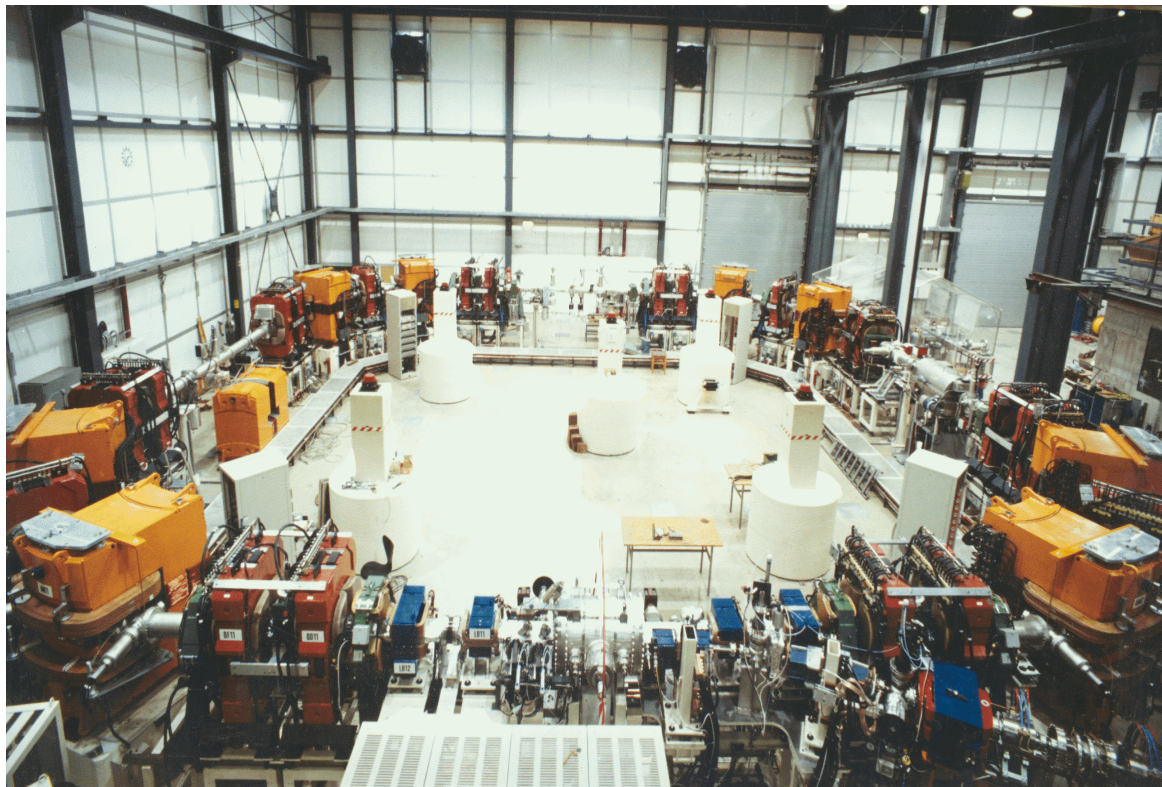
$$k := \frac{g}{p/q}$$



### 3.) *The Equation of Motion:*

$$\frac{B(x)}{p/e} = \frac{1}{\rho} + kx + \frac{1}{2!} \cancel{m} x^2 + \frac{1}{3!} \cancel{n} x^3 + \dots$$

*only terms linear in x, y taken into account* **dipole fields**  
**quadrupole fields**



**Separate Function Machines:**

*Split the magnets and optimise them according to their job:*

*bending, focusing etc*

*Example:  
heavy ion storage ring TSR*

\* *man sieht nur  
dipole und quads → linear*

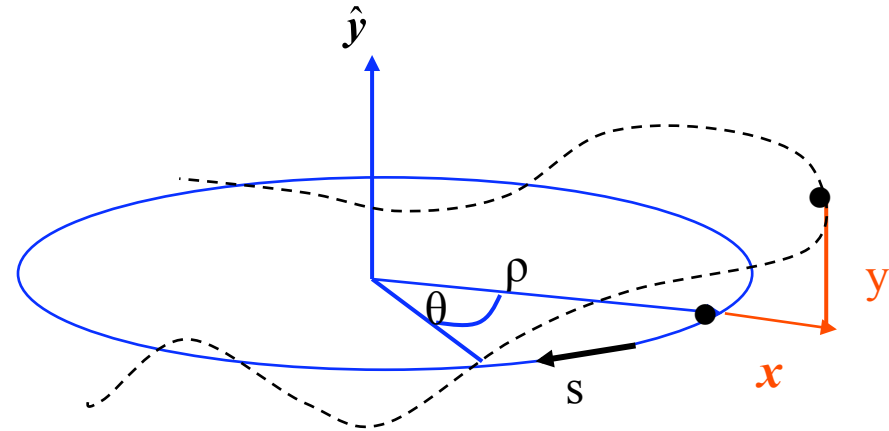
## The Equation of Motion:

- \* Equation for the *horizontal motion*:

$$x'' + x \left( \frac{1}{\rho^2} + k \right) = 0$$

$x =$  particle amplitude

$x' =$  angle of particle trajectory (wrt ideal path line)

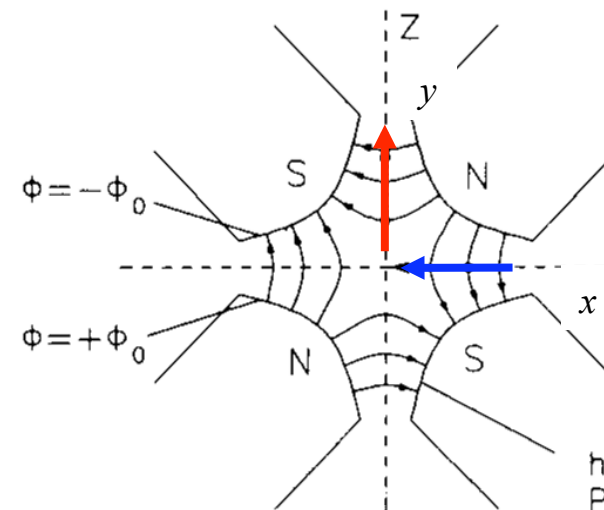


- \* Equation for the *vertical motion*:

$$\frac{1}{\rho^2} = 0 \quad \text{no dipoles ... in general ...}$$

$$k \leftrightarrow -k \quad \text{quadrupole field changes sign}$$

$$y'' - k y = 0$$



## 4.) Solution of Trajectory Equations

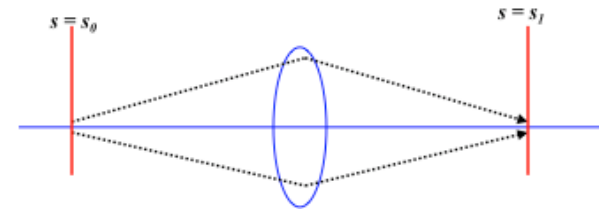
$$\left. \begin{array}{l} \text{Define ... hor. plane: } K = 1/\rho^2 + k \\ \text{... vert. Plane: } K = -k \end{array} \right\} x'' + K x = 0$$

Differential Equation of harmonic oscillator ... with spring constant  $K$

Ansatz: **Hor. Focusing Quadrupole**  $K > 0$ :

$$x(s) = x_0 \cdot \cos(\sqrt{|K|}s) + x'_0 \cdot \frac{1}{\sqrt{|K|}} \sin(\sqrt{|K|}s)$$

$$x'(s) = -x_0 \cdot \sqrt{|K|} \cdot \sin(\sqrt{|K|}s) + x'_0 \cdot \cos(\sqrt{|K|}s)$$



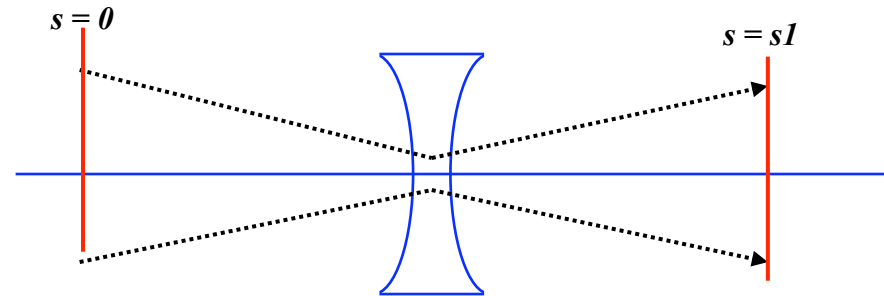
For convenience expressed in matrix formalism:

$$\begin{pmatrix} x \\ x' \end{pmatrix}_{s_1} = M_{foc} * \begin{pmatrix} x \\ x' \end{pmatrix}_{s_0}$$

$$M_{foc} = \begin{pmatrix} \cos(\sqrt{|K|}l) & \frac{1}{\sqrt{|K|}} \sin(\sqrt{|K|}l) \\ -\sqrt{|K|} \sin(\sqrt{|K|}l) & \cos(\sqrt{|K|}l) \end{pmatrix}$$

*hor. defocusing quadrupole:*

$$x'' - K x = 0$$



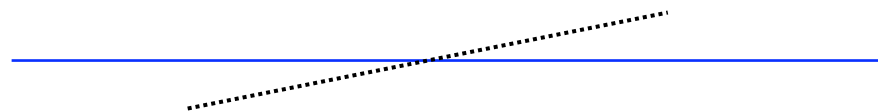
*Ansatz: Remember from school*

$$x(s) = a_1 \cdot \cosh(\omega s) + a_2 \cdot \sinh(\omega s)$$

$$M_{defoc} = \begin{pmatrix} \cosh \sqrt{|K|} l & \frac{1}{\sqrt{|K|}} \sinh \sqrt{|K|} l \\ \sqrt{|K|} \sinh \sqrt{|K|} l & \cosh \sqrt{|K|} l \end{pmatrix}$$

*drift space:*

$$K = 0$$



$$x(s) = x'_0 * s$$

$$M_{drift} = \begin{pmatrix} 1 & l \\ 0 & 1 \end{pmatrix}$$

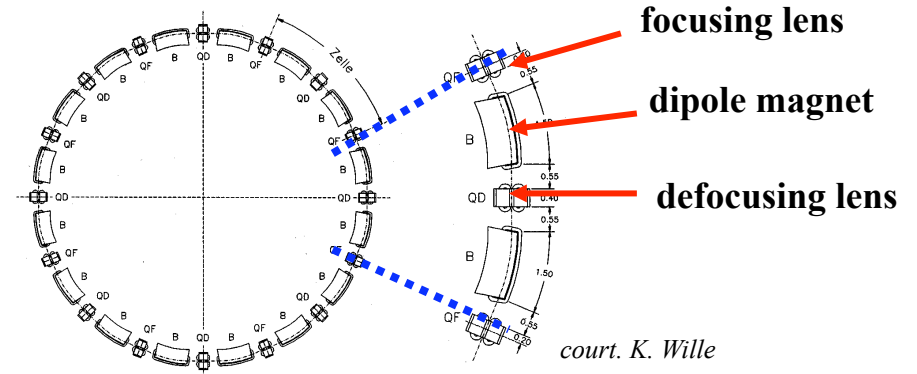
**!** *with the assumptions made, the motion in the horizontal and vertical planes are independent „ ... the particle motion in x & y is uncoupled“*

## Transformation through a system of lattice elements

combine the single element solutions by multiplication of the matrices

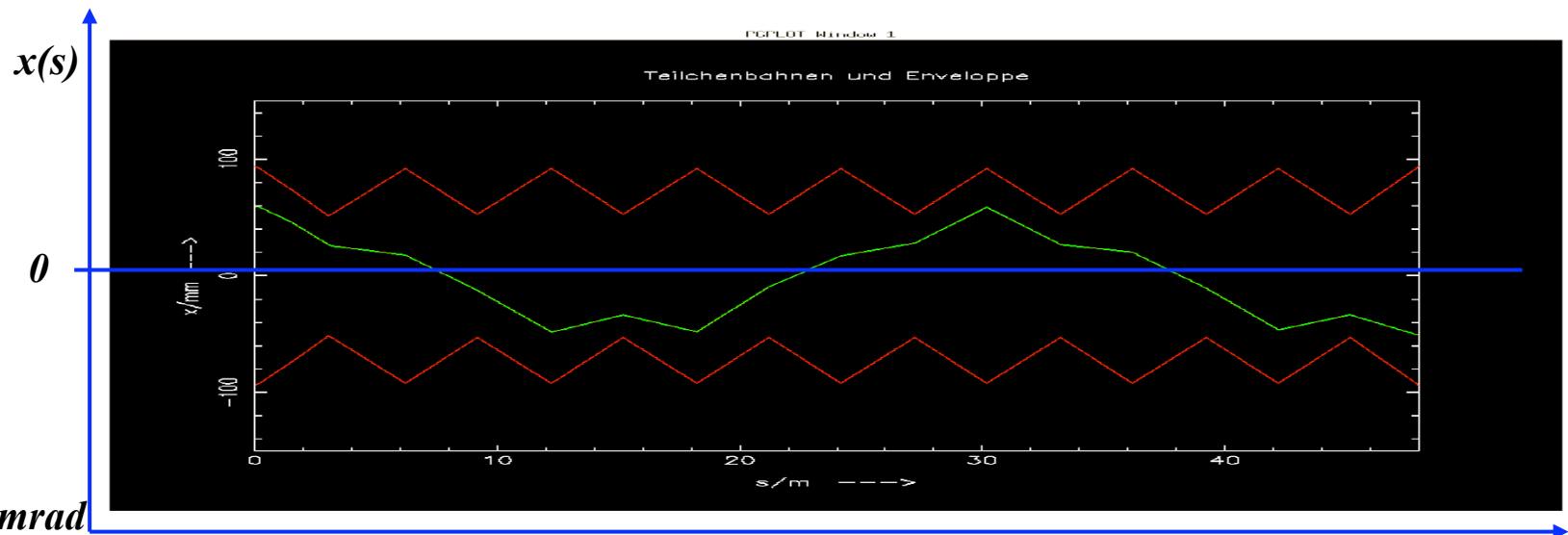
$$M_{total} = M_{QF} * M_D * M_{QD} * M_{Bend} * M_D * \dots$$

$$\begin{pmatrix} x \\ x' \end{pmatrix}_{s_2} = M(s_2, s_1) * \begin{pmatrix} x \\ x' \end{pmatrix}_{s_1}$$



in each accelerator element the particle trajectory corresponds to the movement of a harmonic oscillator ,,

typical values  
in a strong  
foc. machine:  
 $x \approx \text{mm}$ ,  $x' \leq \text{mrad}$



## 5.) Orbit & Tune:

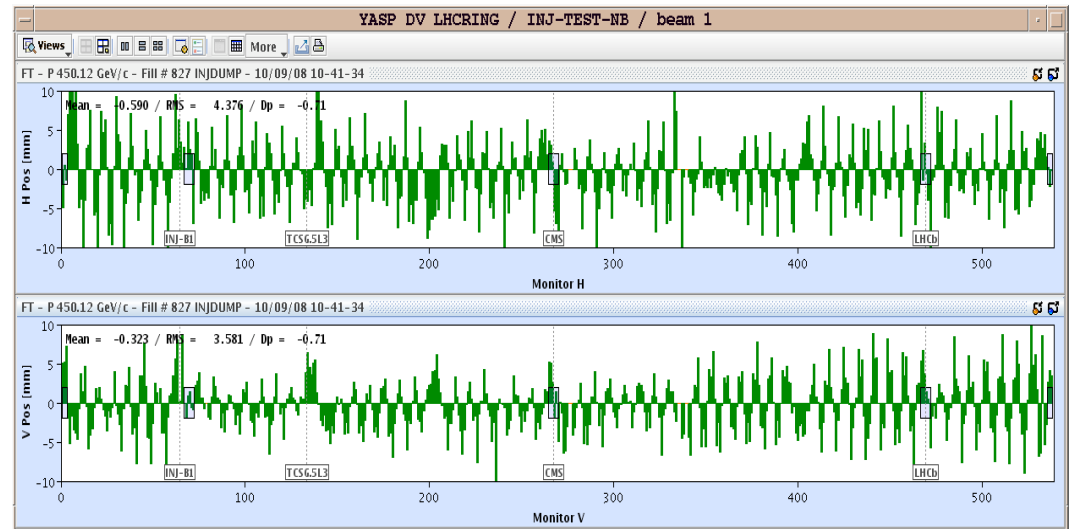
*Tune: number of oscillations per turn*

**64.31**

**59.32**

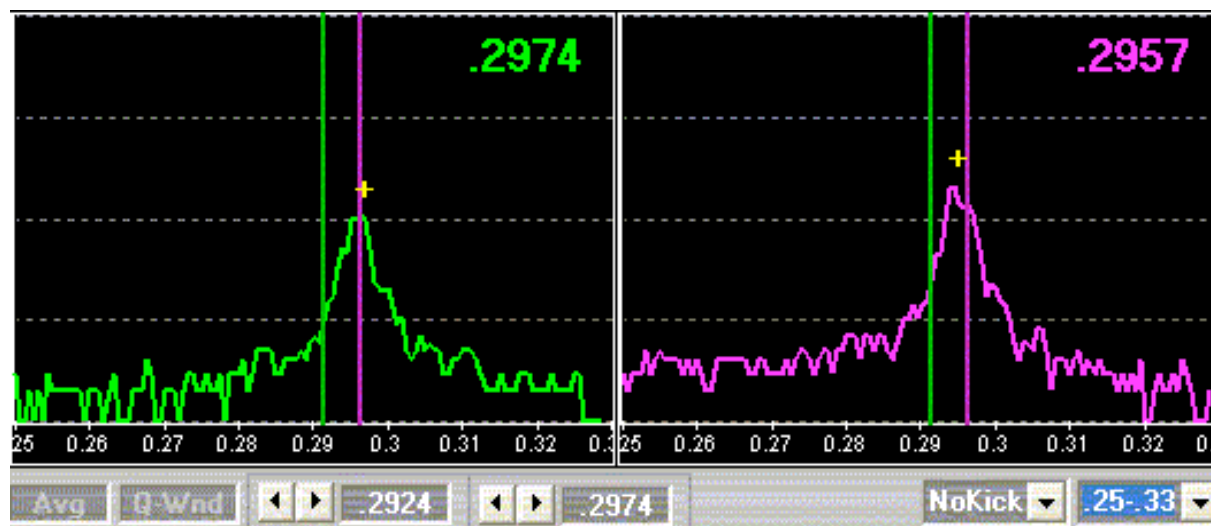
*Relevant for beam stability:*

*non integer part*



*LHC revolution frequency: 11.3 kHz*

$$0.31 * 11.3 = 3.5 \text{ kHz}$$

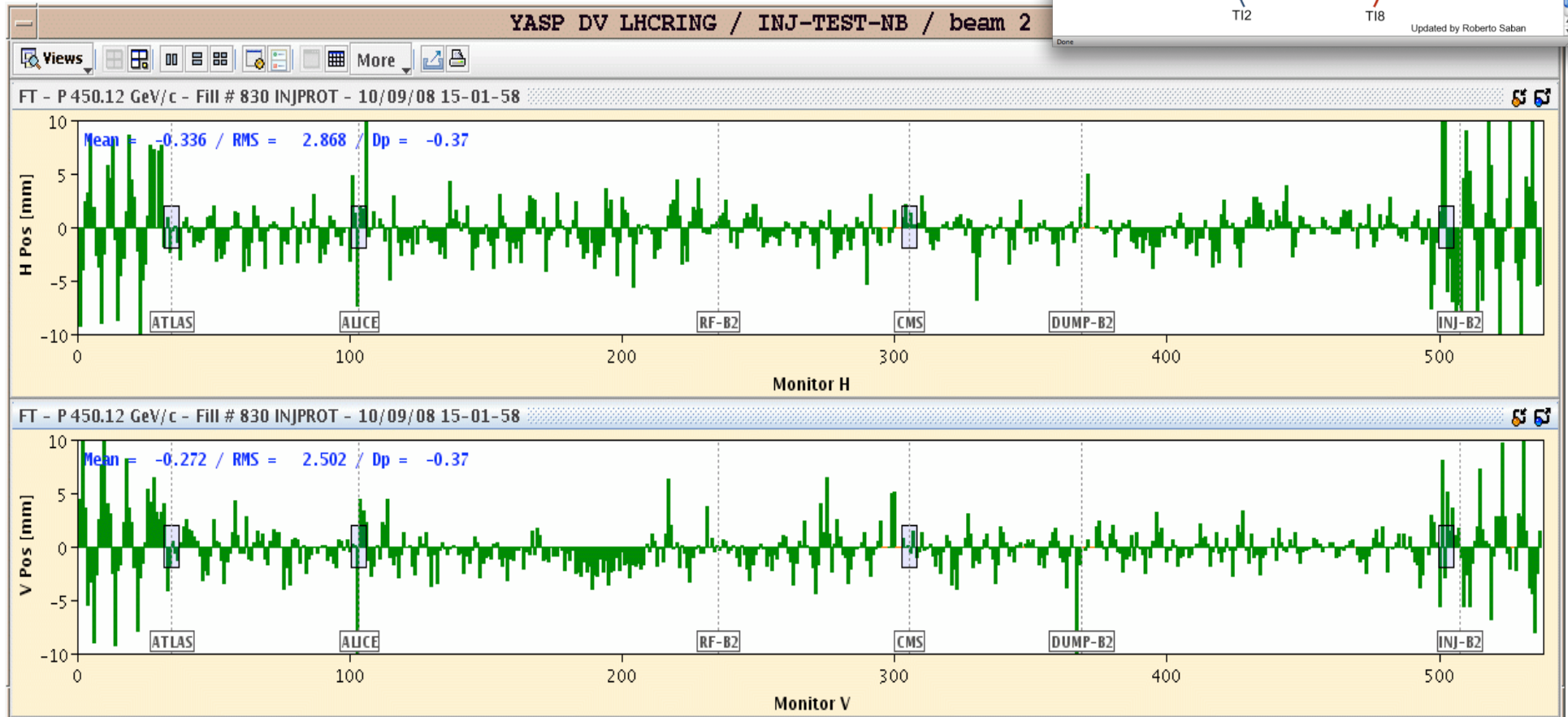
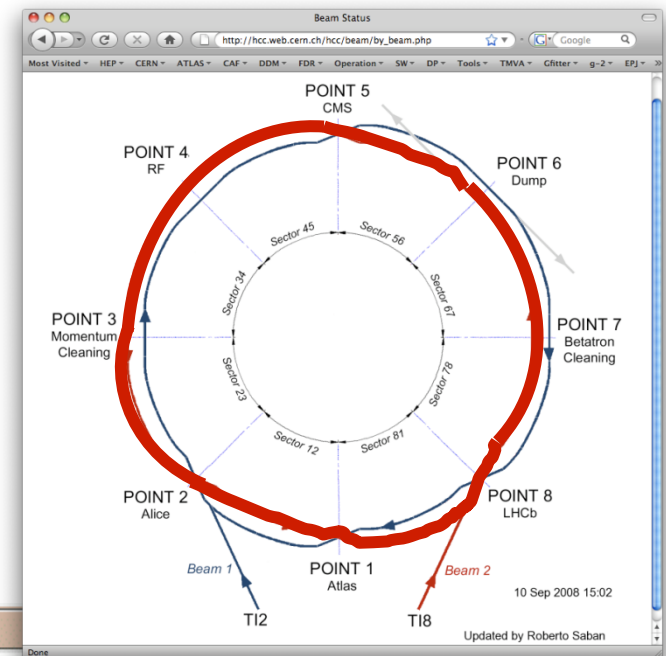




# LHC Operation: Beam Commissioning

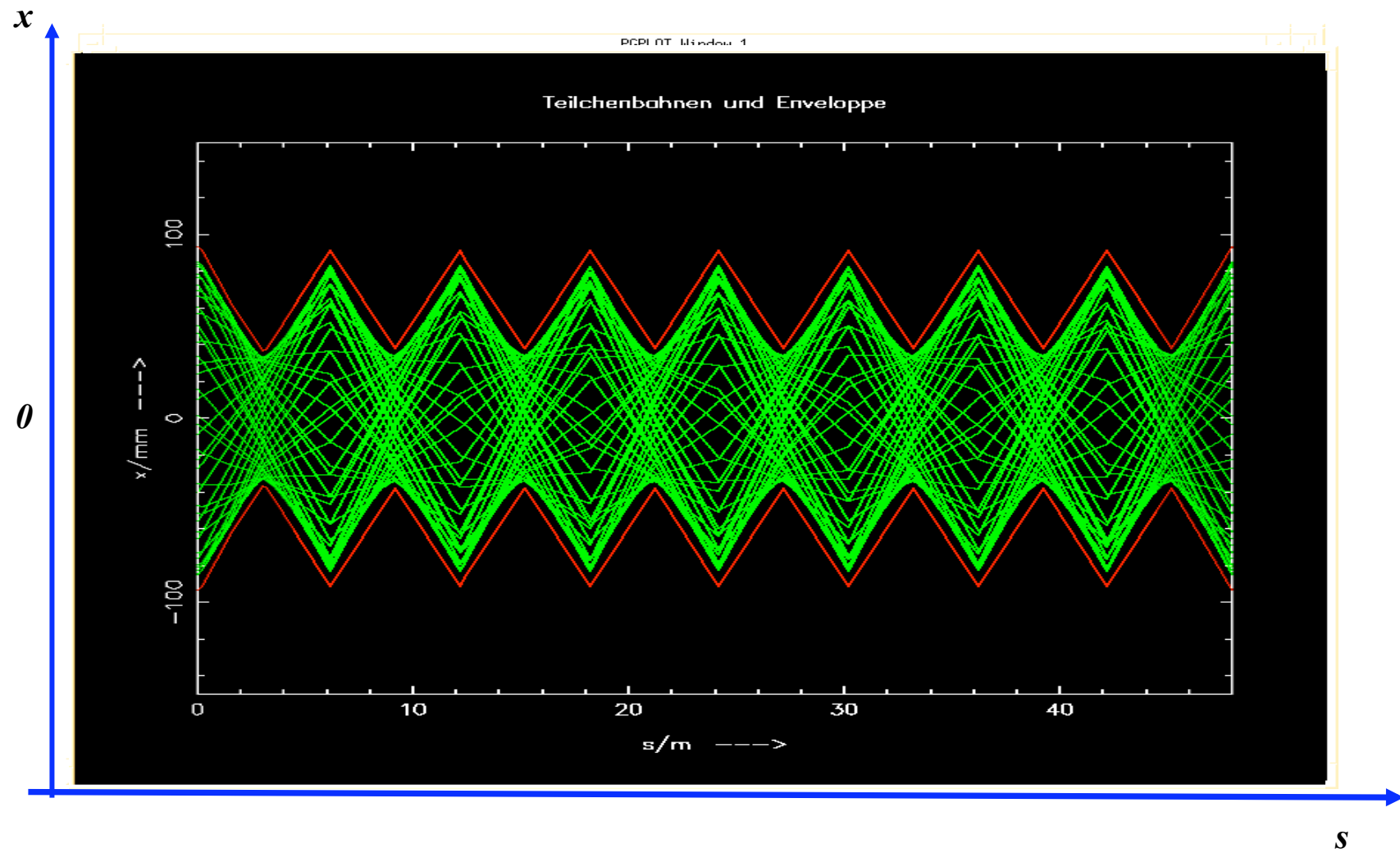
## First turn steering "by sector:"

- One beam at the time
- Beam through 1 sector (1/8 ring), correct trajectory, open collimator and move on.



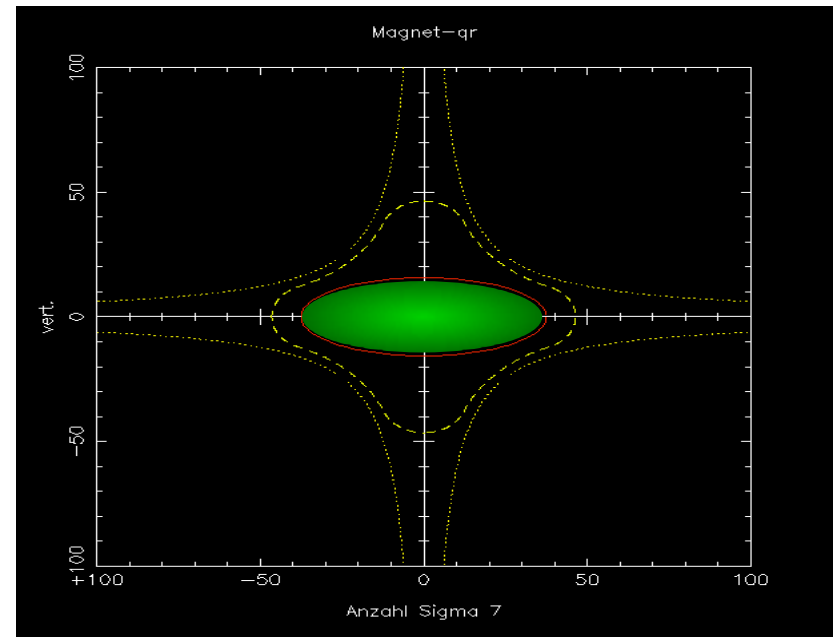
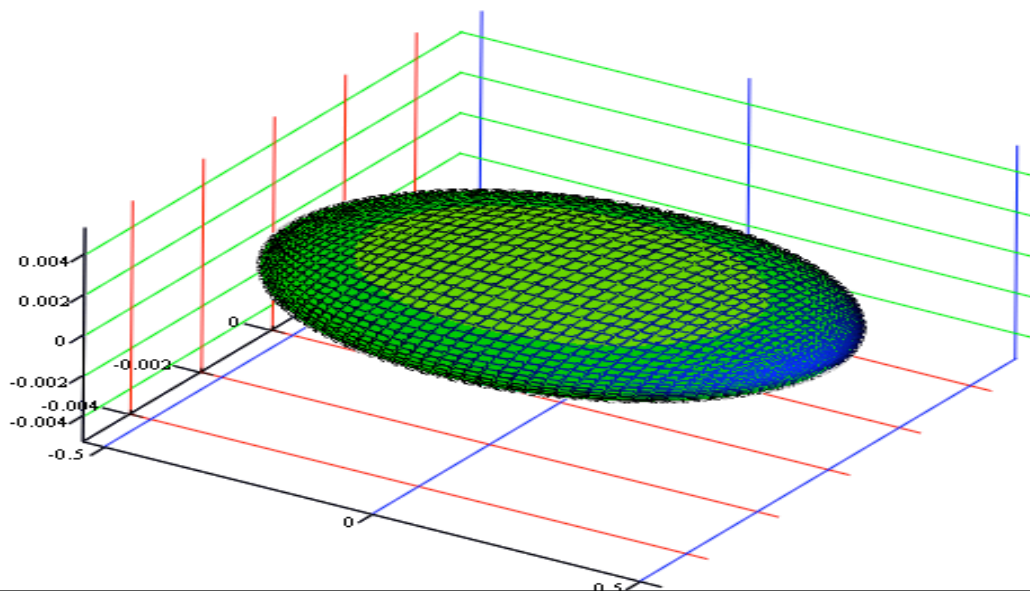
*Question: what will happen, if the particle performs a second turn ?*

*... or a third one or ...  $10^{10}$  turns*



## II.) *The Ideal World:*

### *Particle Trajectories, Beams & Bunches*



*Bunch in a Storage Ring*

(Z, X, Y)

## *Astronomer Hill:*

*differential equation for motions with periodic focusing properties  
„Hill's equation“*

*Example: particle motion with  
periodic coefficient*



*equation of motion:*  $x''(s) - k(s)x(s) = 0$

*restoring force  $\neq$  const,  
 $k(s)$  = depending on the position  $s$   
 $k(s+L) = k(s)$ , periodic function*

*we expect a kind of quasi harmonic  
oscillation: amplitude & phase will depend  
on the position  $s$  in the ring.*

## 6.) The Beta Function

„it is convenient to see“

... *after some beer* ... general solution of Mr Hill  
can be written in the form:

*Ansatz:*

$$x(s) = \sqrt{\varepsilon} * \sqrt{\beta(s)} * \cos(\psi(s) + \phi)$$

$\varepsilon, \Phi =$  integration *constants*  
determined by initial conditions

$\beta(s)$  *periodic function* given by *focusing properties* of the lattice  $\leftrightarrow$  quadrupoles

$$\beta(s + L) = \beta(s)$$

$\varepsilon$  *beam emittance* = *woozilycity* of the particle ensemble, *intrinsic beam parameter*,  
cannot be changed by the foc. properties.

*scientifically spoken: area covered in transverse  $x, x'$  phase space ... and it is constant !!!*

$\Psi(s) =$  „*phase advance*“ of the oscillation between point „0“ and „s“ in the lattice.  
For one complete revolution: number of oscillations per turn „*Tune*“

$$Q_y = \frac{1}{2\pi} \cdot \int \frac{ds}{\beta(s)}$$

## 6.) The Beta Function

*Amplitude of a particle trajectory:*

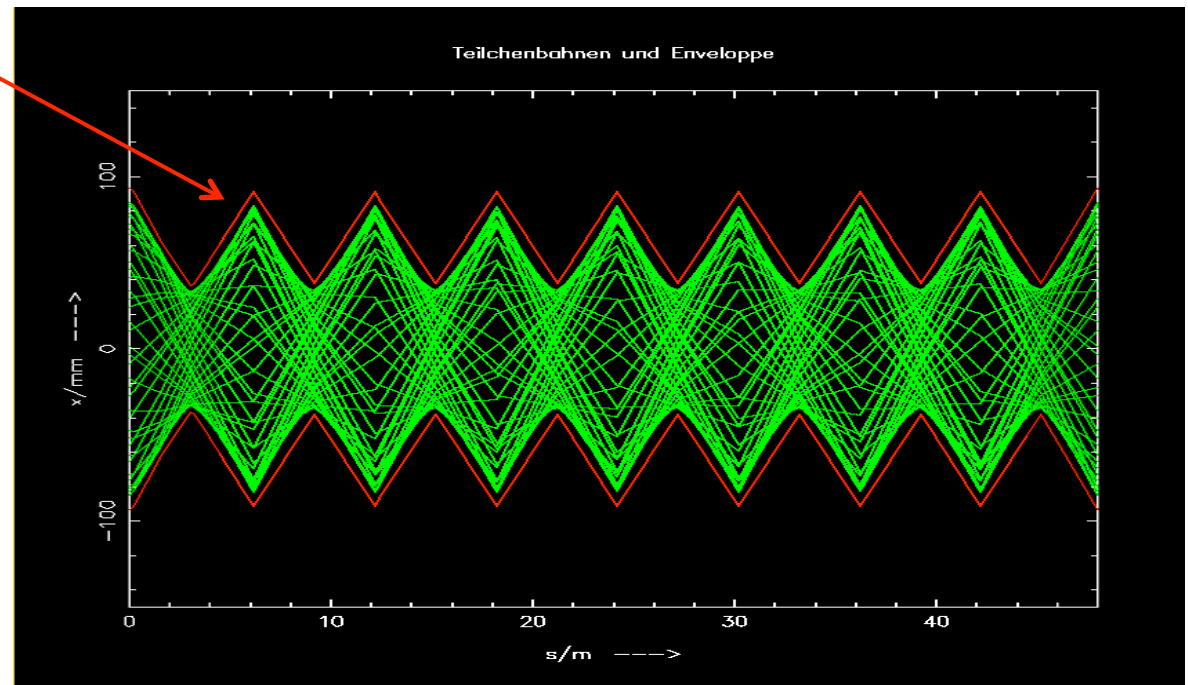
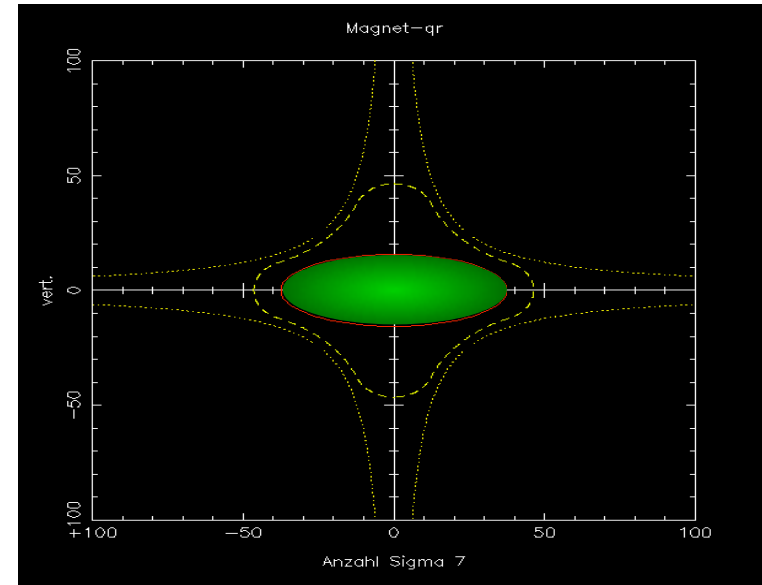
$$x(s) = \sqrt{\varepsilon} * \sqrt{\beta(s)} * \cos(\psi(s) + \varphi)$$

*Maximum size of a particle amplitude*

$$\hat{x}(s) = \sqrt{\varepsilon} \sqrt{\beta(s)}$$

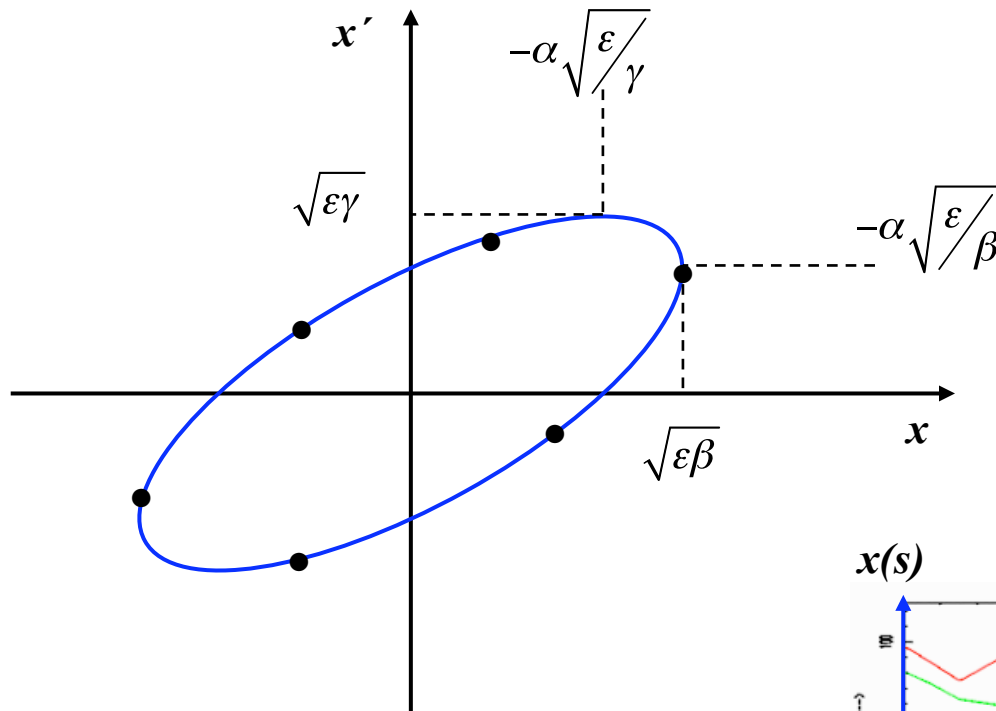
*$\beta$  determines the beam size  
(... the envelope of all particle  
trajectories at a given position  
“s” in the storage ring.*

*It **reflects the periodicity** of the  
magnet structure.*



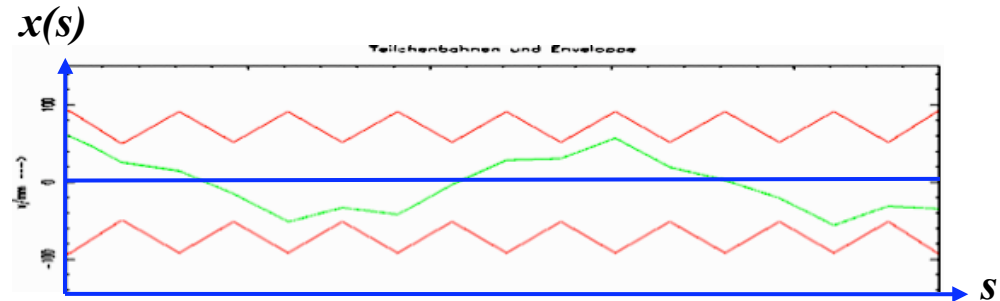
## 7.) Beam Emittance and Phase Space Ellipse

$$\varepsilon = \gamma(s) * x^2(s) + 2\alpha(s)x(s)x'(s) + \beta(s)x'(s)^2$$



**Liouville:** in reasonable storage rings  
area in phase space is constant.

$$A = \pi * \varepsilon = \text{const}$$



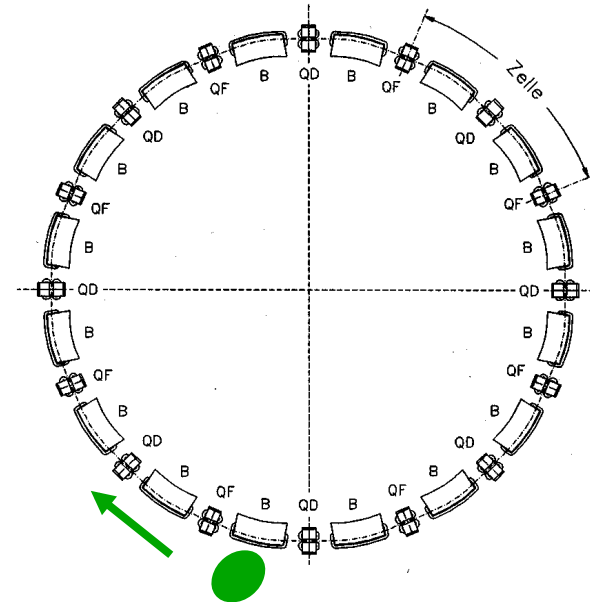
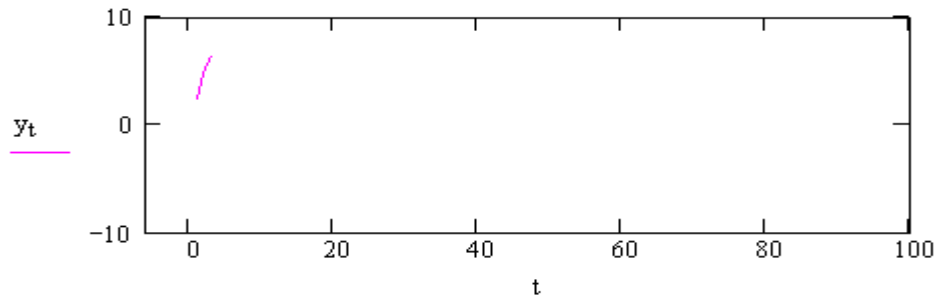
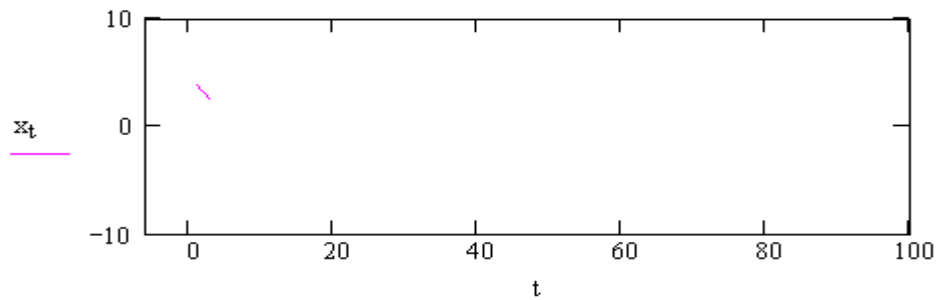
$\varepsilon$  beam emittance = **woozilycity** of the particle ensemble, **intrinsic beam parameter**,  
cannot be changed by the foc. properties.

**Scientificquely spoken:** area covered in transverse  $x, x'$  phase space ... and it is constant !!!

# Particle Tracking in a Storage Ring

Calculate  $x, x'$  for each linear accelerator element according to matrix formalism

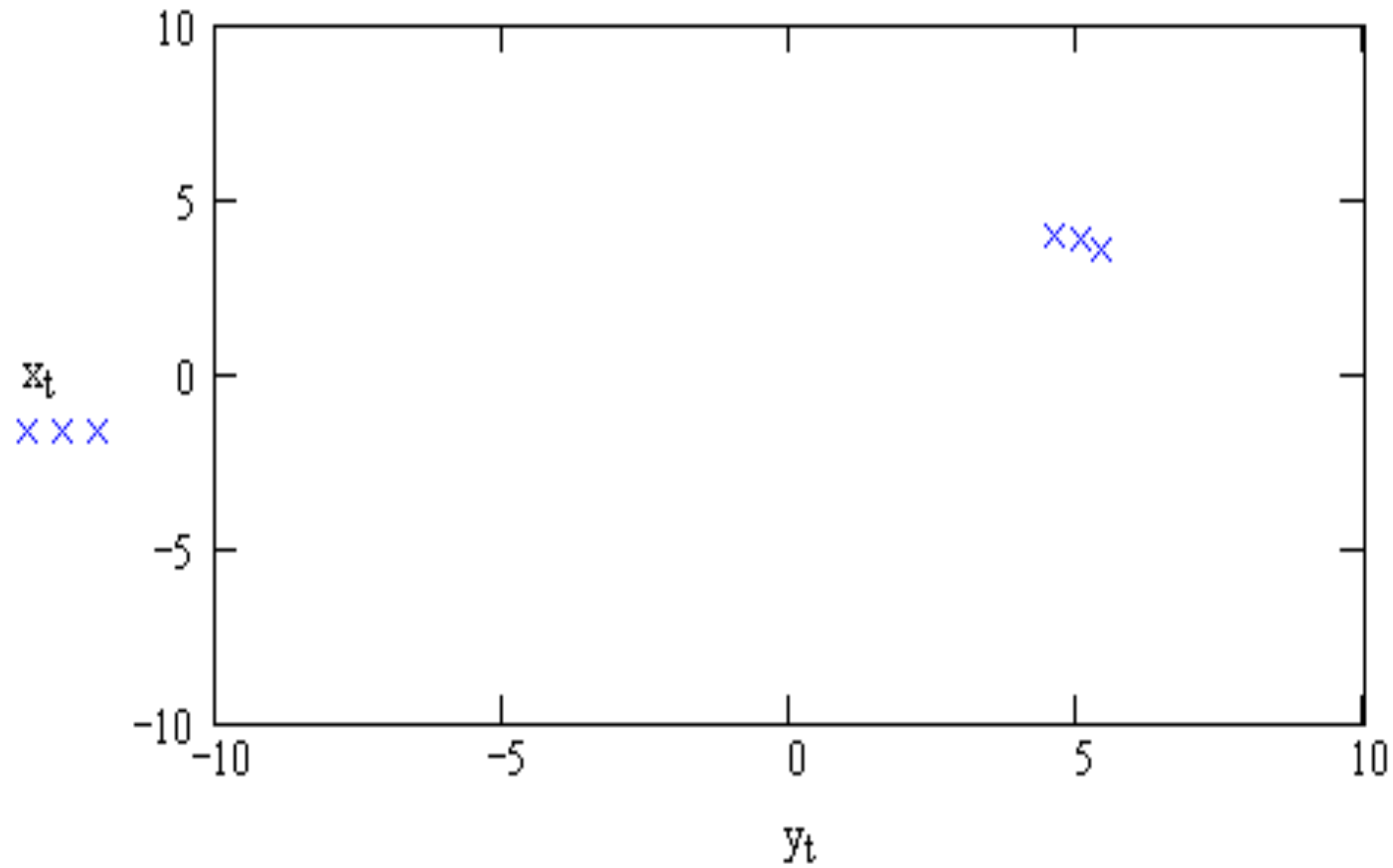
plot  $x, x'$  as a function of „s“



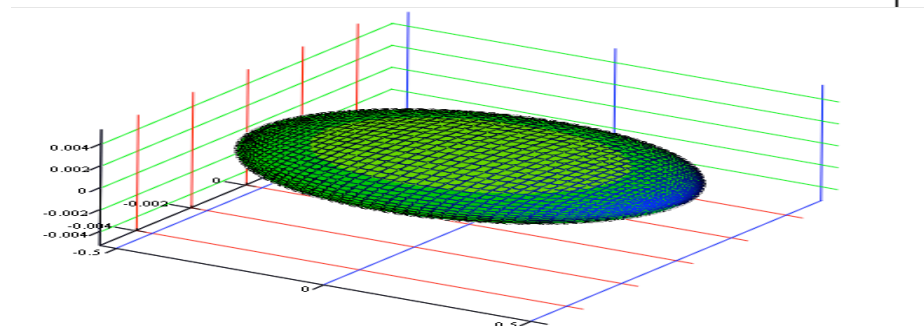
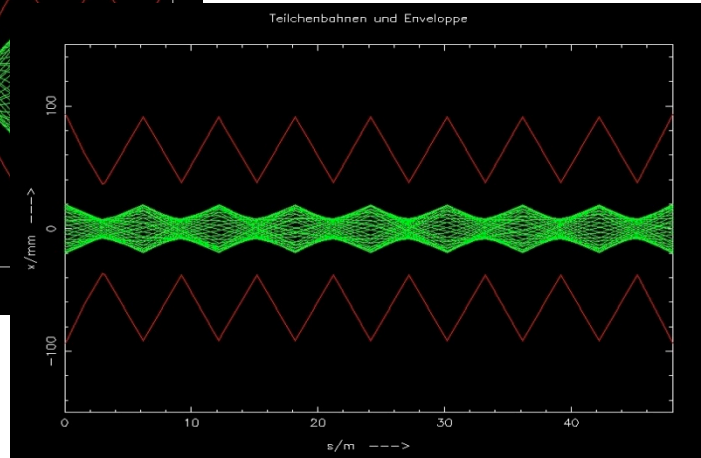
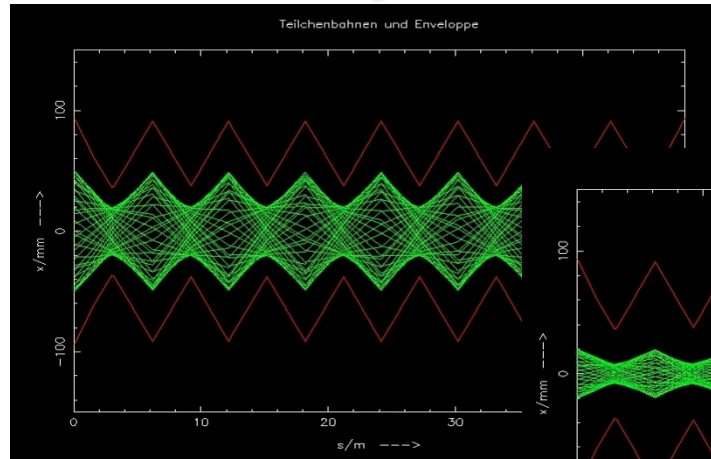


*... and now the ellipse:*

*note for each turn  $x$ ,  $x'$  at a given position „ $s_1$ “ and plot in the phase space diagram*

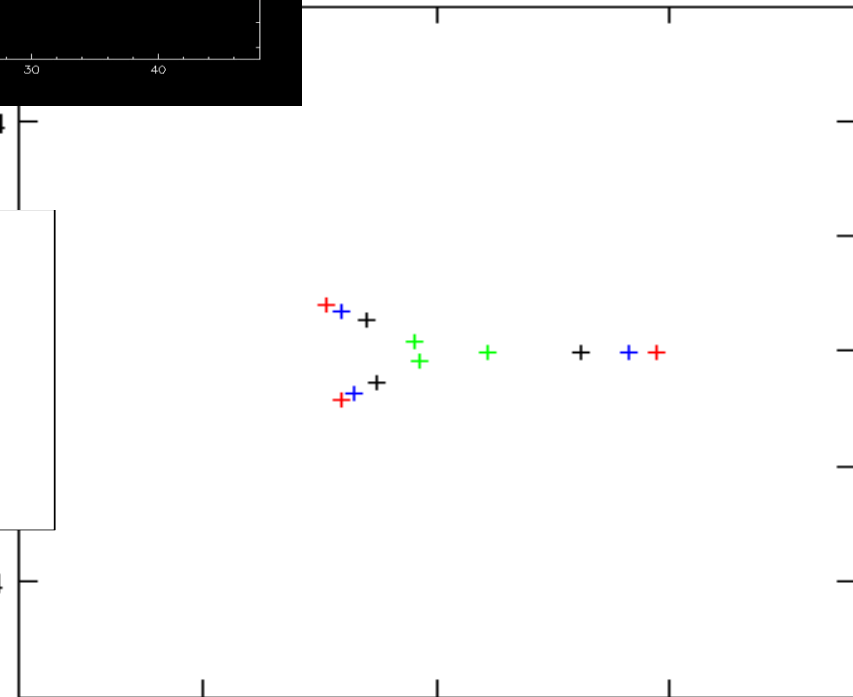


# *Emittance of the Particle Ensemble:*



0.04

-0.04

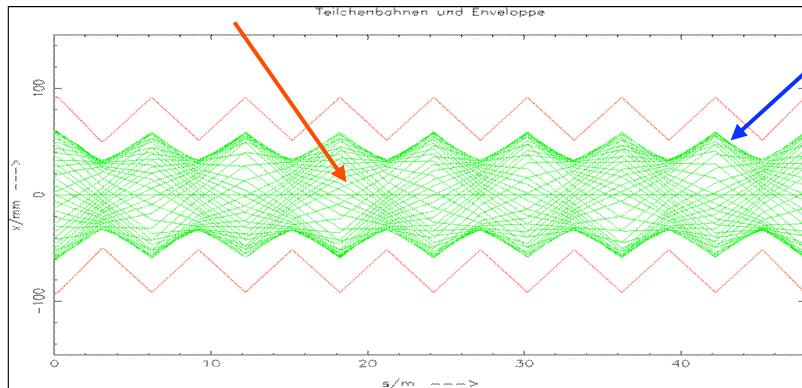


$x_{n,1}, x_{n,2}, x_{n,3}, x_{n,4}$

# Emittance of the Particle Ensemble:

$$x(s) = \sqrt{\varepsilon} \sqrt{\beta(s)} \cdot \cos(\Psi(s) + \phi)$$

$$\hat{x}(s) = \sqrt{\varepsilon} \sqrt{\beta(s)}$$

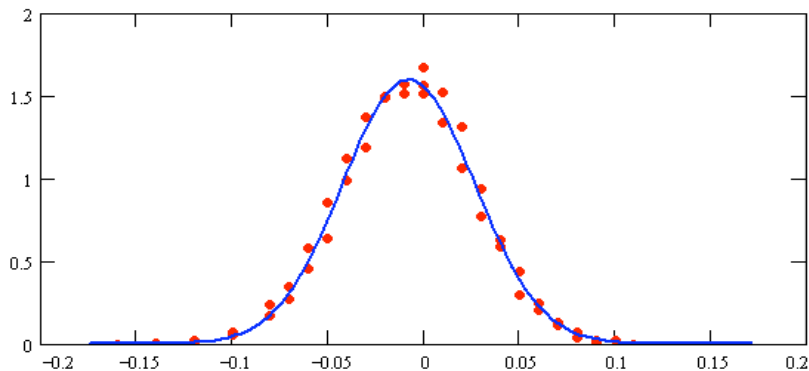


single particle trajectories,  $N \approx 10^{11}$  per bunch

**LHC:**  $\beta = 180\text{ m}$

$\varepsilon = 5 * 10^{-10}\text{ m rad}$

$$\sigma = \sqrt{\varepsilon * \beta} = \sqrt{5 * 10^{-10}\text{ m} * 180\text{ m}} = 0.3\text{ mm}$$

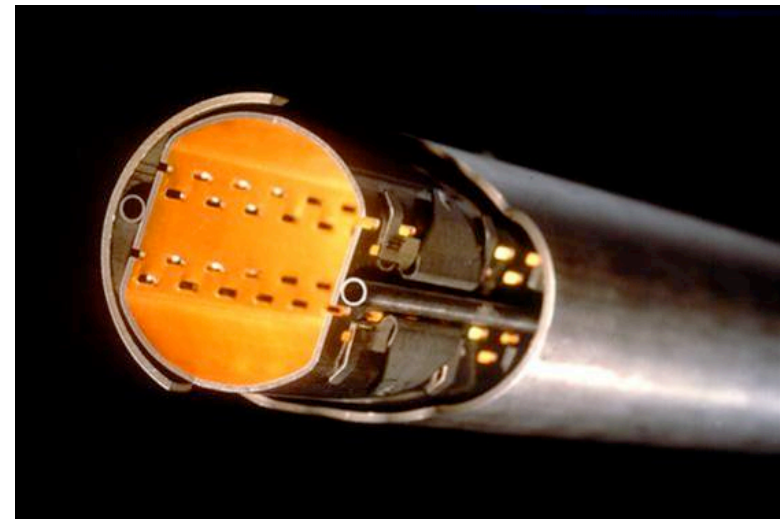


**Gauß  
Particle Distribution:**

$$\rho(x) = \frac{N \cdot e}{\sqrt{2\pi} \sigma_x} \cdot e^{-\frac{1}{2} \frac{x^2}{\sigma_x^2}}$$

particle at distance  $1 \sigma$  from centre

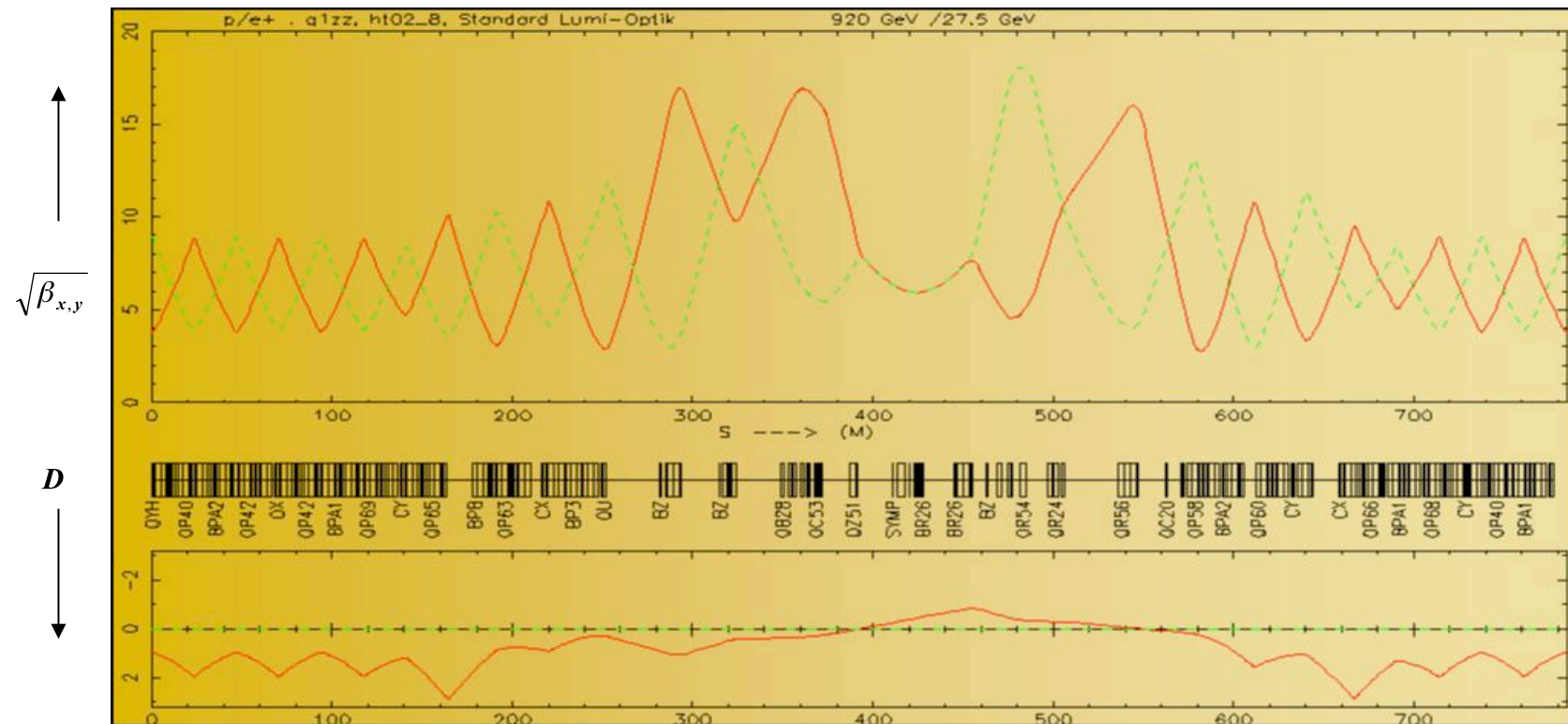
$\leftrightarrow$  68.3 % of all beam particles



aperture requirements:  $r_0 = 12 * \sigma$

### III.) The „not so ideal“ World

## Lattice Design in Particle Accelerators



1952: Courant, Livingston, Snyder:

*Theory of strong focusing in particle beams*

# Recapitulation: ...the story with the matrices !!!

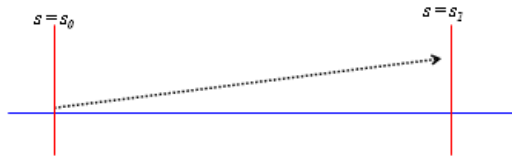
## Equation of Motion:

$$x'' + K x = 0 \quad K = 1/\rho^2 - k \quad \dots \text{ hor. plane:}$$

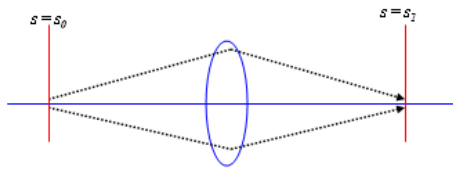
$$K = k \quad \dots \text{ vert. Plane:}$$

## Solution of Trajectory Equations

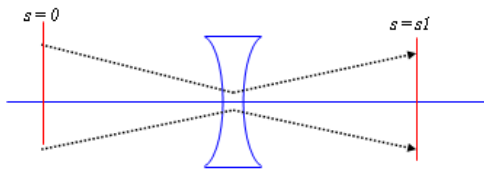
$$\begin{pmatrix} x \\ x' \end{pmatrix}_{s_1} = M * \begin{pmatrix} x \\ x' \end{pmatrix}_{s_0}$$



$$M_{drift} = \begin{pmatrix} 1 & l \\ 0 & 1 \end{pmatrix}$$



$$M_{foc} = \begin{pmatrix} \cos(\sqrt{|K|}l) & \frac{1}{\sqrt{|K|}} \sin(\sqrt{|K|}l) \\ -\sqrt{|K|} \sin(\sqrt{|K|}l) & \cos(\sqrt{|K|}l) \end{pmatrix}$$



$$M_{defoc} = \begin{pmatrix} \cosh(\sqrt{|K|}l) & \frac{1}{\sqrt{|K|}} \sinh(\sqrt{|K|}l) \\ \sqrt{|K|} \sinh(\sqrt{|K|}l) & \cosh(\sqrt{|K|}l) \end{pmatrix}$$

$$M_{total} = M_{QF} * M_D * M_B * M_D * M_{QD} * M_D * \dots$$

## 8.) *Lattice Design: „... how to build a storage ring“*

*Geometry of the ring:  $B^* \rho = p / e$*

*$p$  = momentum of the particle,  
 $\rho$  = curvature radius*

*$B\rho$  = beam rigidity*

*Circular Orbit: bending angle of one dipole*

$$\alpha = \frac{ds}{\rho} \approx \frac{dl}{\rho} = \frac{Bdl}{B\rho}$$

*The angle run out in one revolution must be  $2\pi$ , so for a full circle*

$$\alpha = \frac{\int Bdl}{B\rho} = 2\pi$$

$$\int Bdl = 2\pi \frac{p}{q}$$

*... defines the integrated dipole field around the machine.*



*Example LHC:*



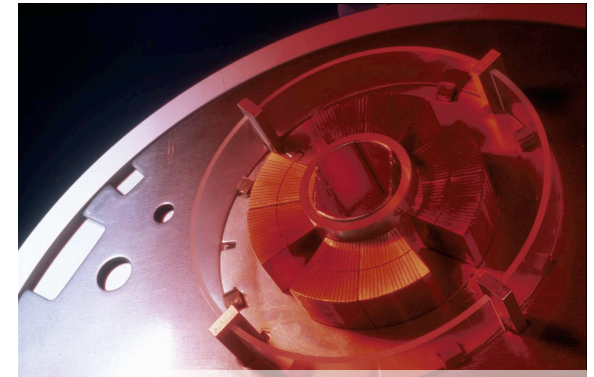
7000 GeV Proton storage ring  
dipole magnets  $N = 1232$   
 $l = 15 \text{ m}$   
 $q = +1 e$

$$\int \mathbf{B} \, dl \approx N l B = 2\pi p / e$$

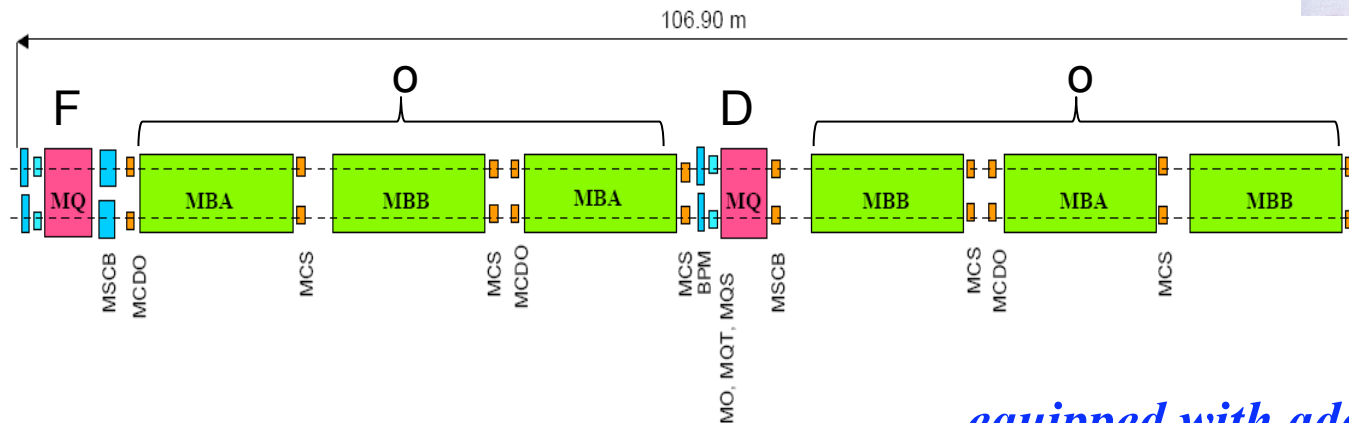
$$B \approx \frac{2\pi \cdot 7000 \cdot 10^9 \text{ eV}}{1232 \cdot 15 \text{ m} \cdot 3 \cdot 10^8 \frac{\text{m}}{\text{s}} \cdot e} = \underline{\underline{8.3 \text{ Tesla}}}$$

# *LHC: Lattice Design*

## *the ARC 90° FoDo in both planes*



*MQ: main quadrupole*



*equipped with additional corrector coils*



*MB: main dipole*

*MQ: main quadrupole*

*MQT: Trim quadrupole*

*MQS: Skew trim quadrupole*

*MO: Lattice octupole (Landau damping)*

*MSCB: Skew sextupole*

*Orbit corrector dipoles*

*MCS: Spool piece sextupole*

*MCDO: Spool piece 8 / 10 pole*

*BPM: Beam position monitor + diagnostics*



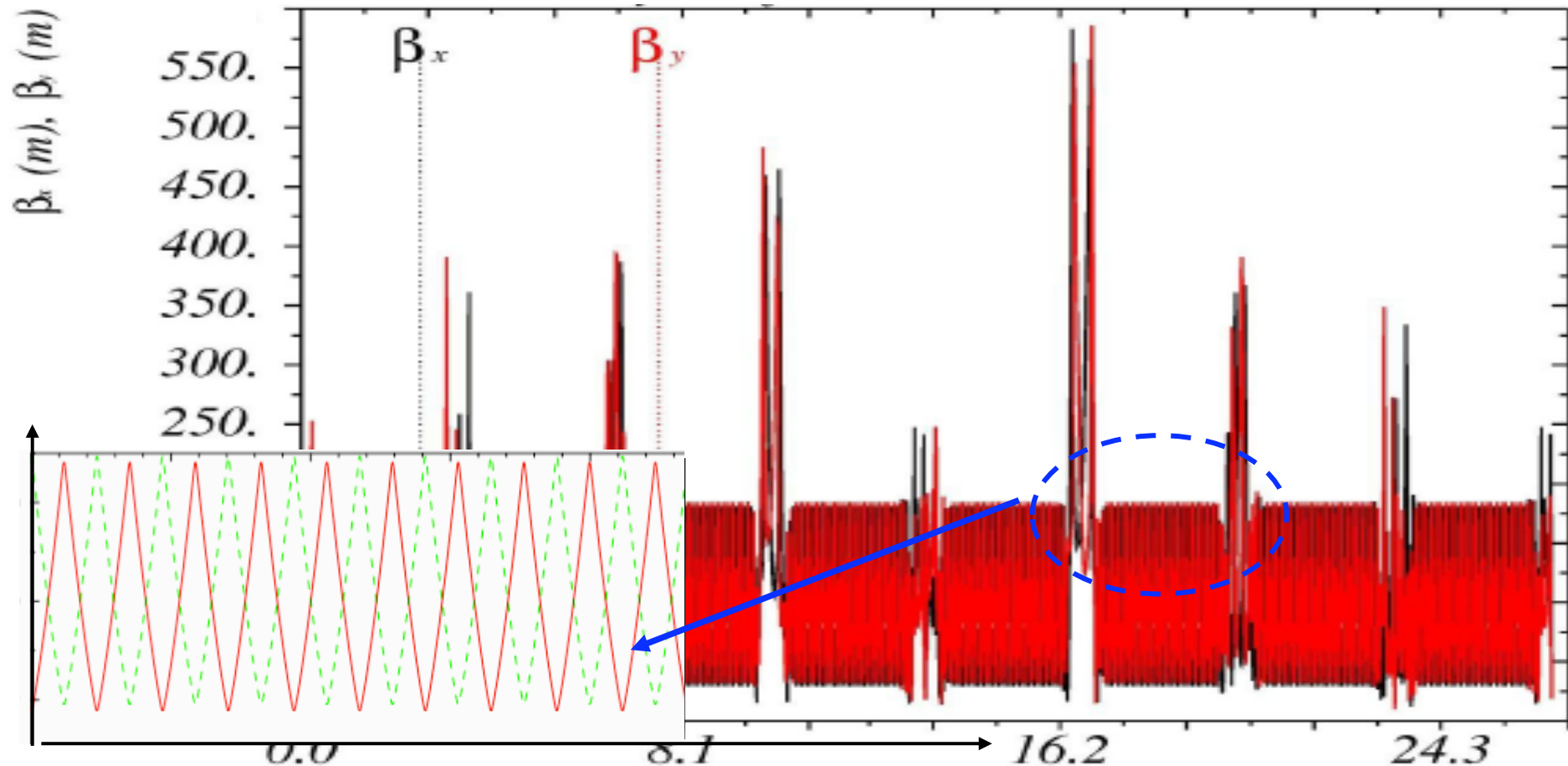
Magnets for the LHC, total budget, every magnet has a role in the optics design

Name	Quantity	Purpose
MB	1232	Main dipoles
MQ	400	Main lattice quadrupoles
MSCB	376	Combined chromaticity/ closed orbit correctors
MCS	2464	Dipole spool sextupole for persistent currents at injection
MCDO	1232	Dipole spool octupole/decapole for persistent currents
MO	336	Landau octupole for instability control
MQT	256	Trim quad for lattice correction
MCB	266	Orbit correction dipoles
MQM	100	Dispersion suppressor quadrupoles
MQY	20	Enlarged aperture quadrupoles

In total 6628 cold magnets ...

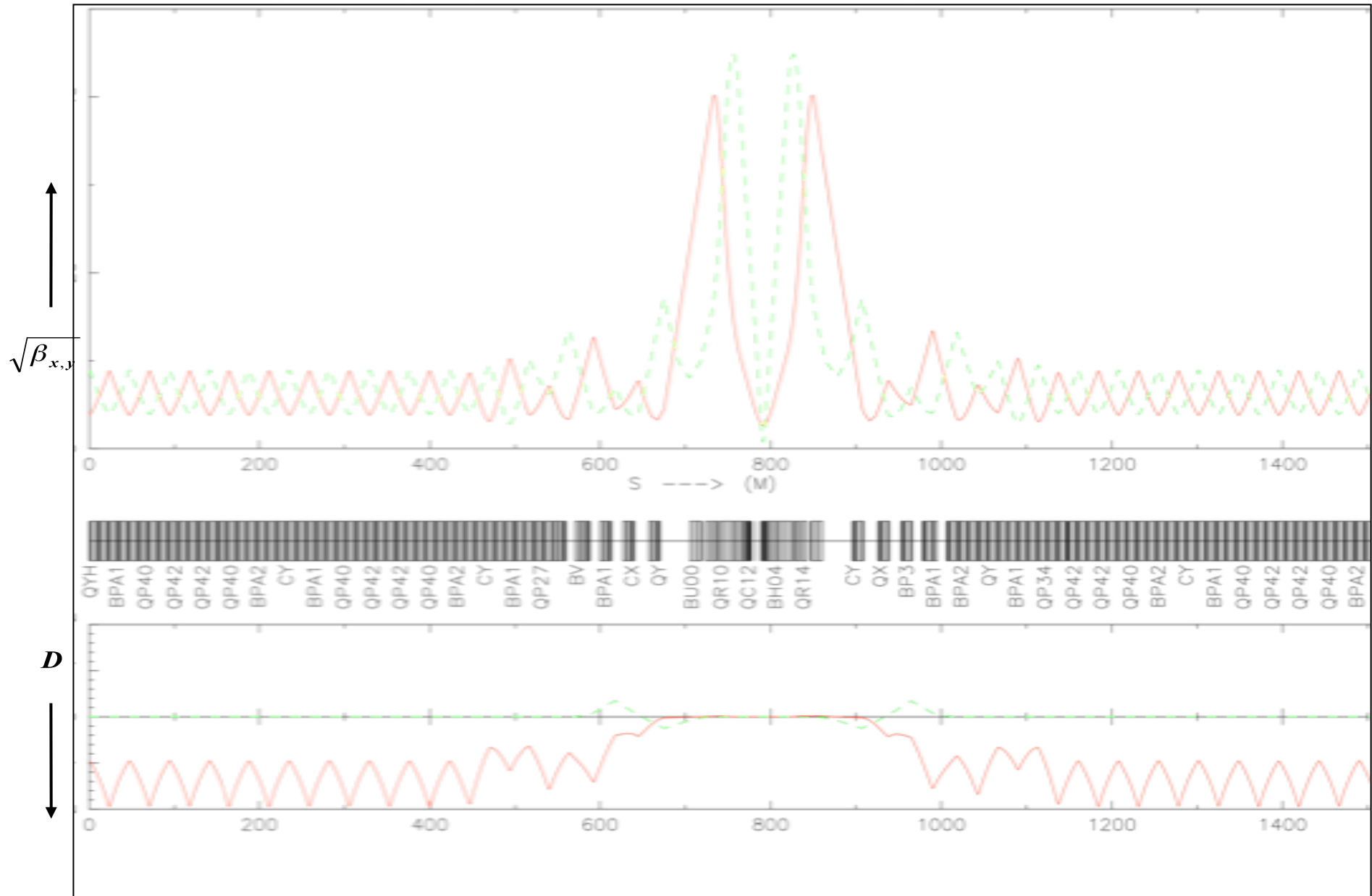
## FoDo-Lattice

A magnet structure consisting of focusing and defocusing quadrupole lenses in alternating order with **nothing** in between.  
(**Nothing** = elements that can be neglected on first sight: drift, bending magnets, RF structures ... **and especially experiments...**)



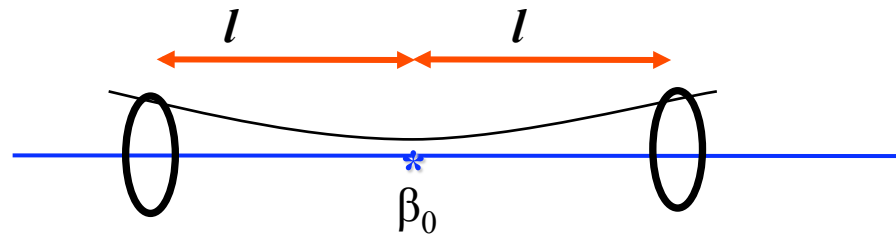
Starting point for the calculation: in the middle of a focusing quadrupole  
Phase advance per cell  $\mu = 45^\circ$ ,  
→ calculate the twiss parameters for a periodic solution

## 9.) Insertions



## $\beta$ -Function in a Drift:

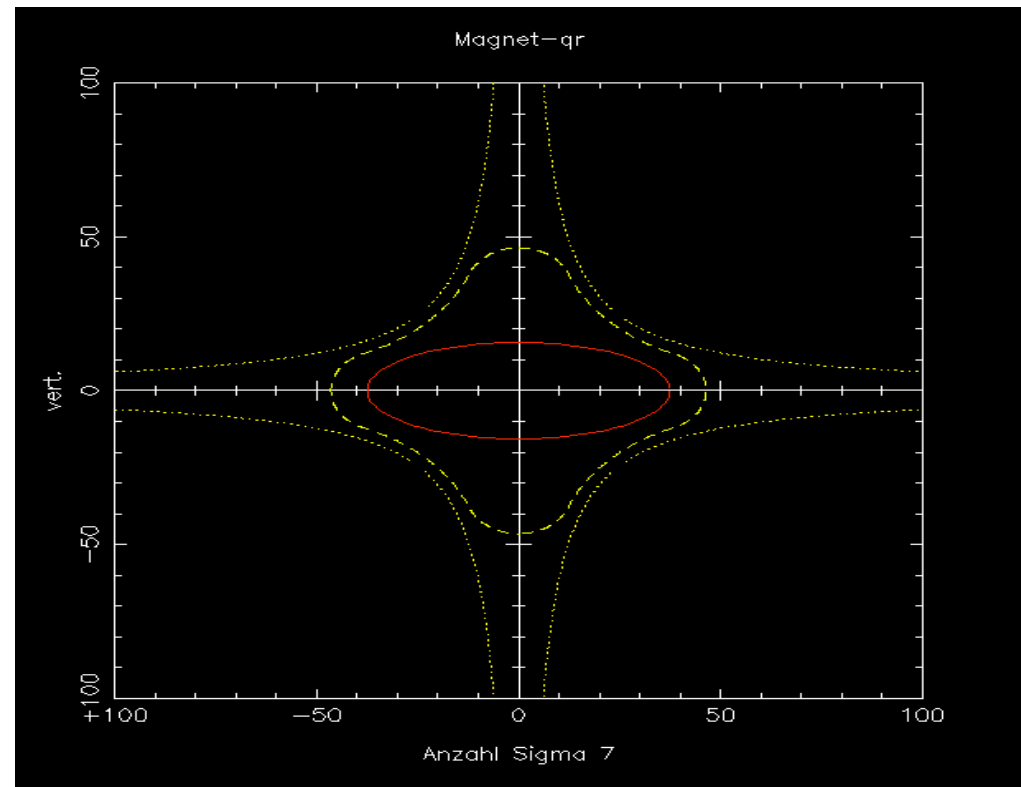
$$\beta(\ell) = \beta_0 + \frac{\ell^2}{\beta_0}$$



*At the end of a long symmetric drift space the beta function reaches its maximum value in the complete lattice.*

*-> here we get the largest beam dimension.*

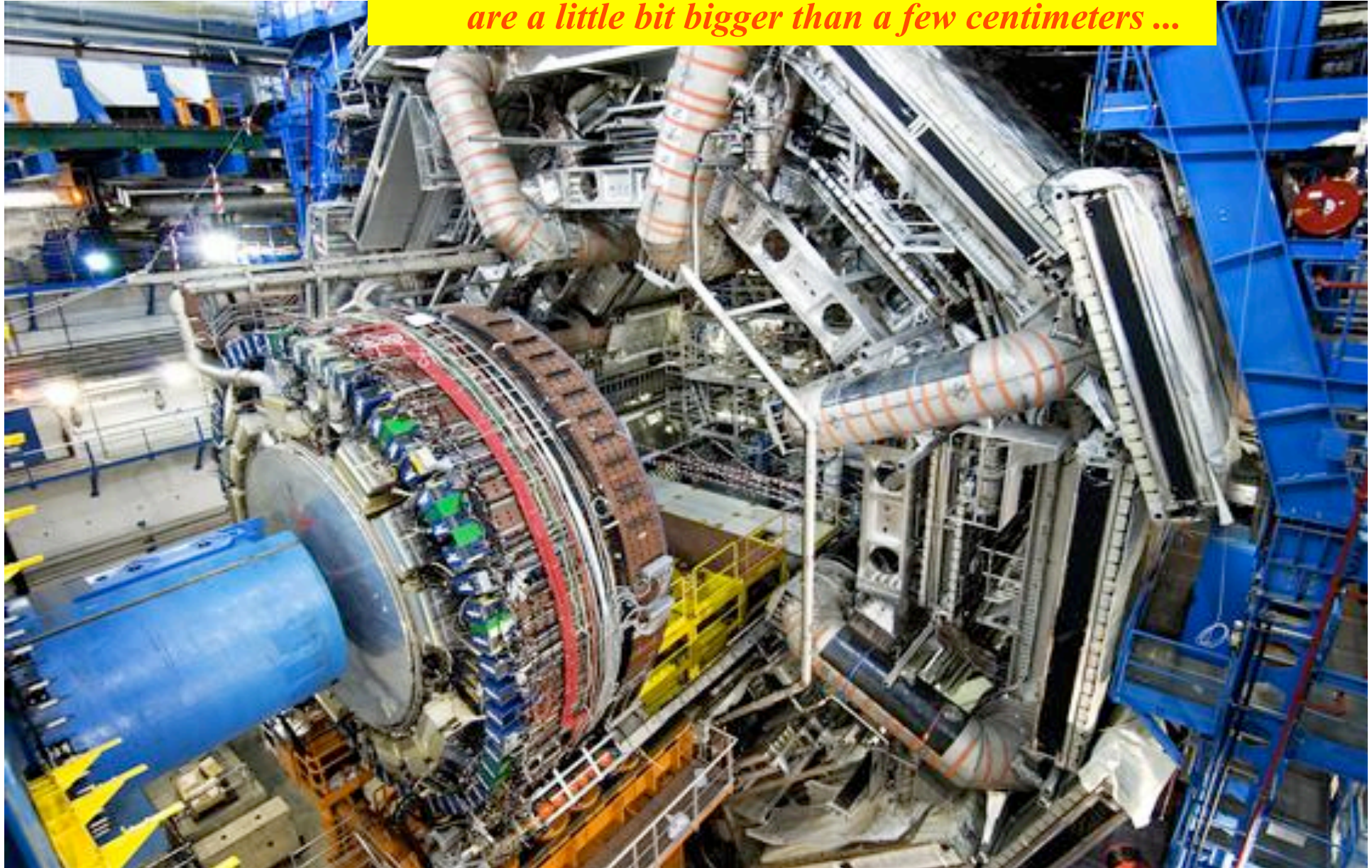
*-> keep  $l$  as small as possible*



*7 sigma beam size inside a mini beta quadrupole*

... clearly there is an

*... unfortunately ... in general  
high energy detectors that are  
installed in that drift spaces  
are a little bit bigger than a few centimeters ...*

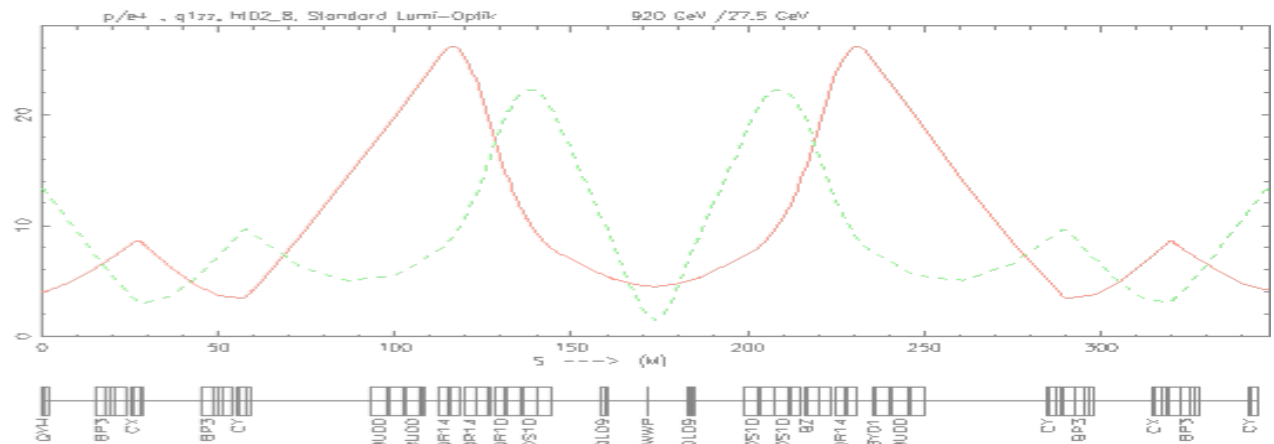
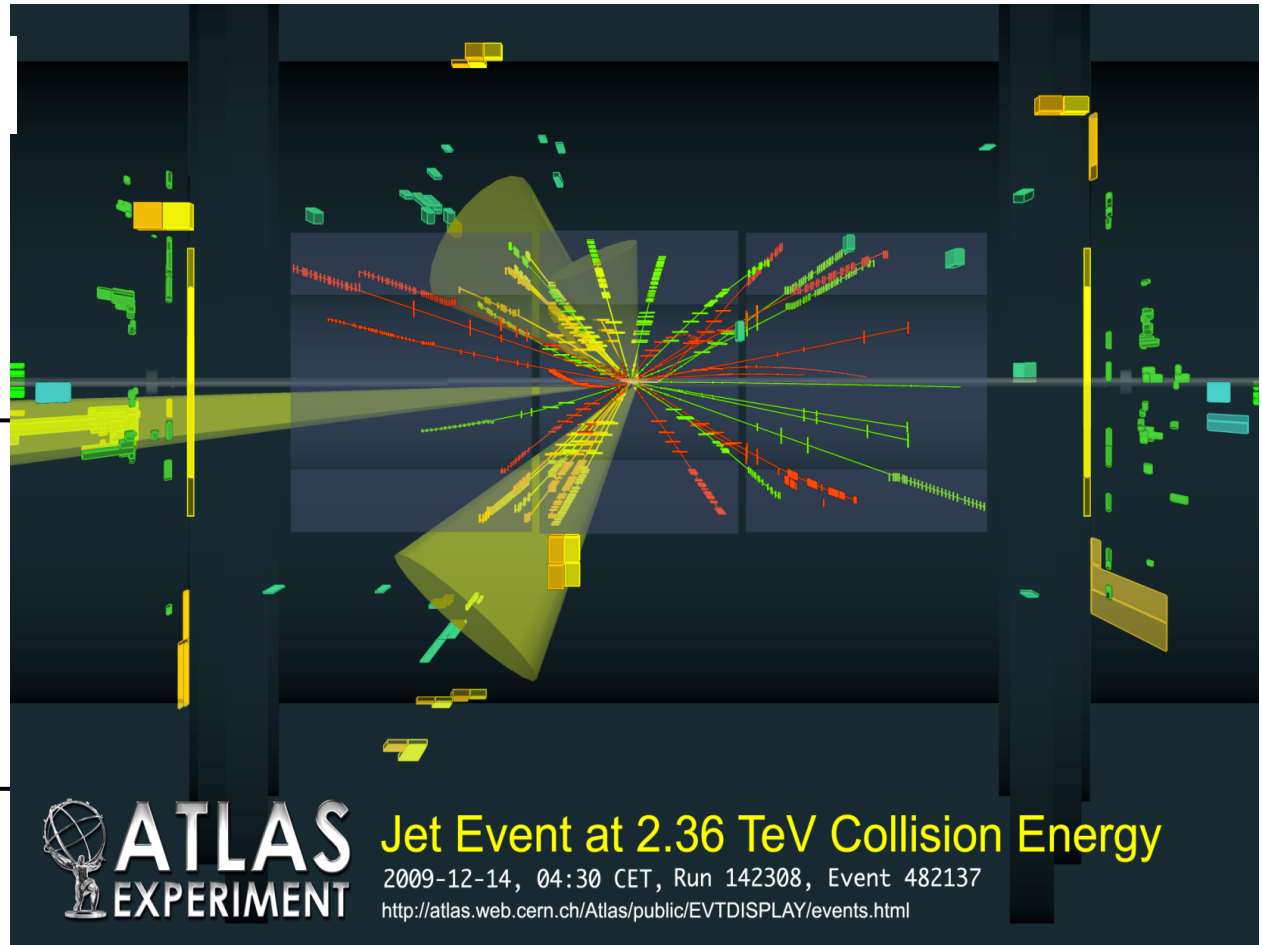


## The Mini-β Insertion:

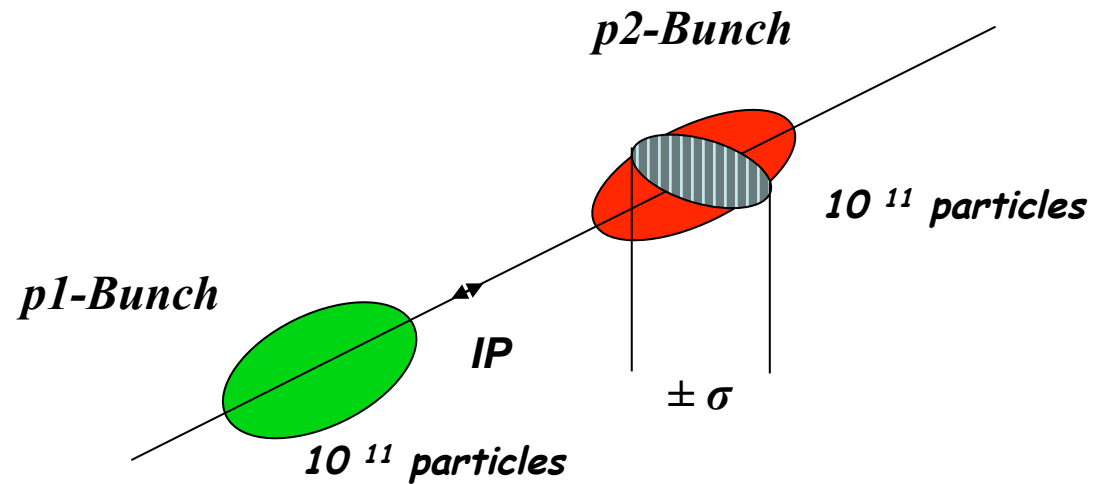
$$R = L * \Sigma_{react}$$

production rate of events  
is determined by the  
cross section  $\Sigma_{react}$   
and a parameter L that is given  
by the design of the accelerator:  
... the luminosity

$$L = \frac{1}{4\pi e^2 f_0 b} * \frac{I_1 * I_2}{\sigma_x^* * \sigma_y^*}$$



# 10.) Luminosity



*Example: Luminosity run at LHC*

$$\beta_{x,y} = 0.55 \text{ m}$$

$$f_0 = 11.245 \text{ kHz}$$

$$\varepsilon_{x,y} = 5 * 10^{-10} \text{ rad m}$$

$$n_b = 2808$$

$$\sigma_{x,y} = 17 \text{ } \mu\text{m}$$

$$L = \frac{1}{4\pi e^2 f_0 n_b} * \frac{I_{p1} I_{p2}}{\sigma_x \sigma_y}$$

$$I_p = 584 \text{ mA}$$

---

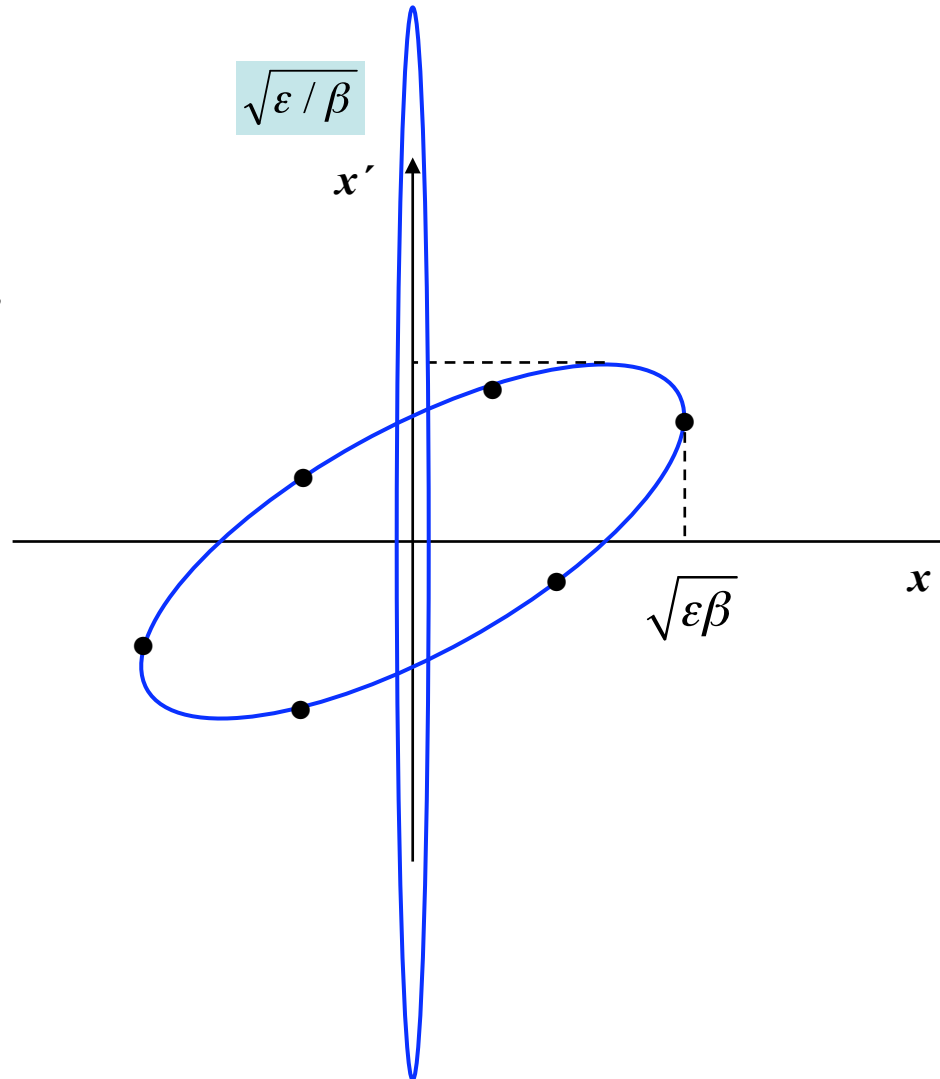
$$L = 1.0 * 10^{34} \text{ } 1/\text{cm}^2 \text{ s}$$

# Mini- $\beta$ Insertions: Betafunctions

A mini- $\beta$  insertion is always a kind of **special symmetric drift space**.

$\rightarrow$  greetings from Liouville

*the smaller the beam size  
the larger the beam divergence*





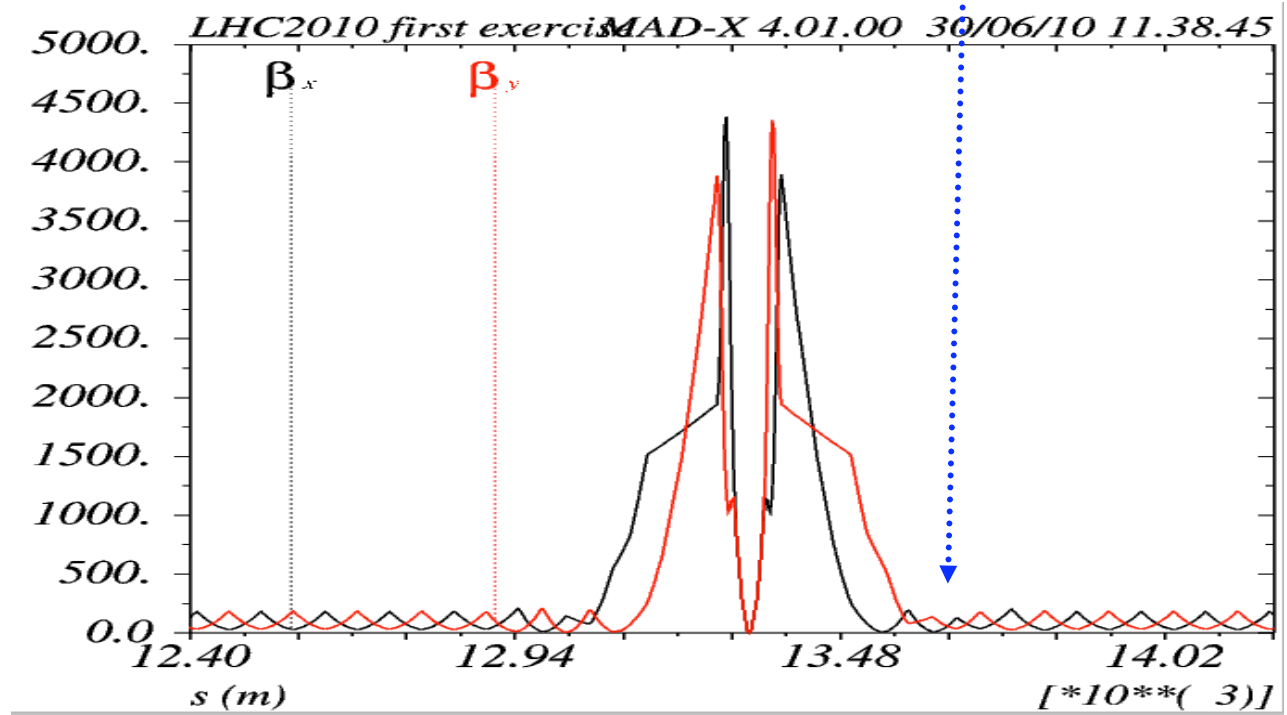
## Mini- $\beta$ Insertions: some guide lines

- \* calculate the *periodic solution in the arc*
- \* *introduce the drift space* needed for the insertion device (detector ...)
- \* put a *quadrupole doublet* (triplet ?) *as close as possible*
- \* introduce *additional quadrupole lenses* to match the beam parameters to the values at the beginning of the arc structure

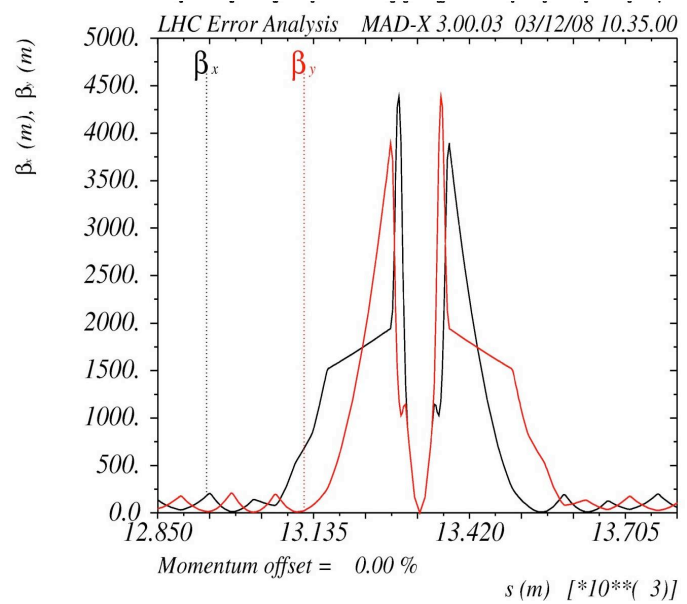
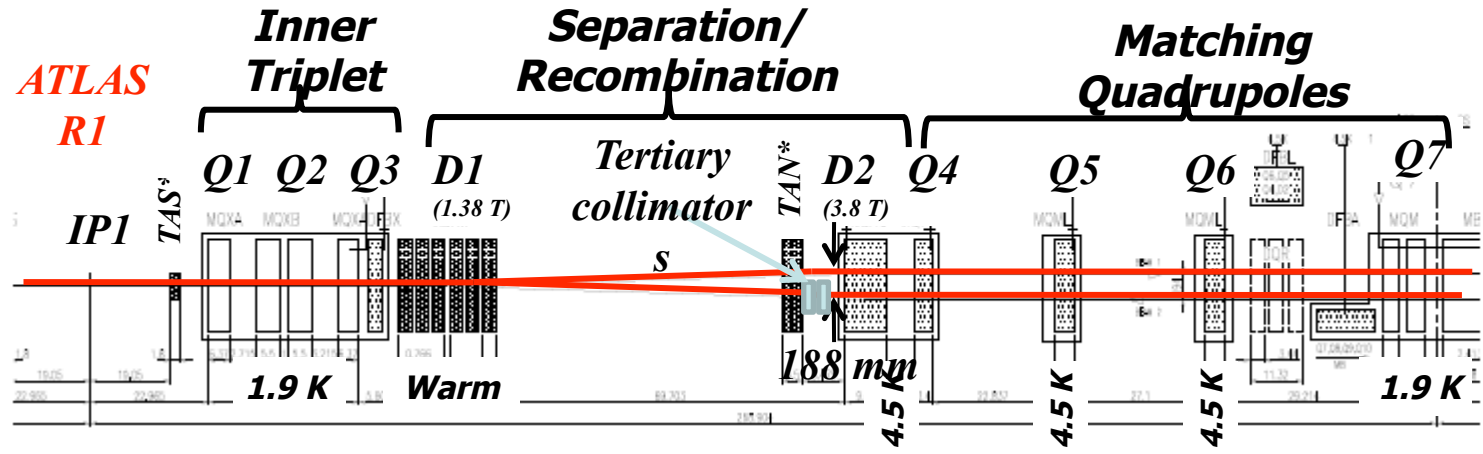
parameters to be optimised & matched to the periodic solution:

$$\begin{array}{ll} \alpha_x, \beta_x & D_x, D_x' \\ \alpha_y, \beta_y & Q_x, Q_y \end{array}$$

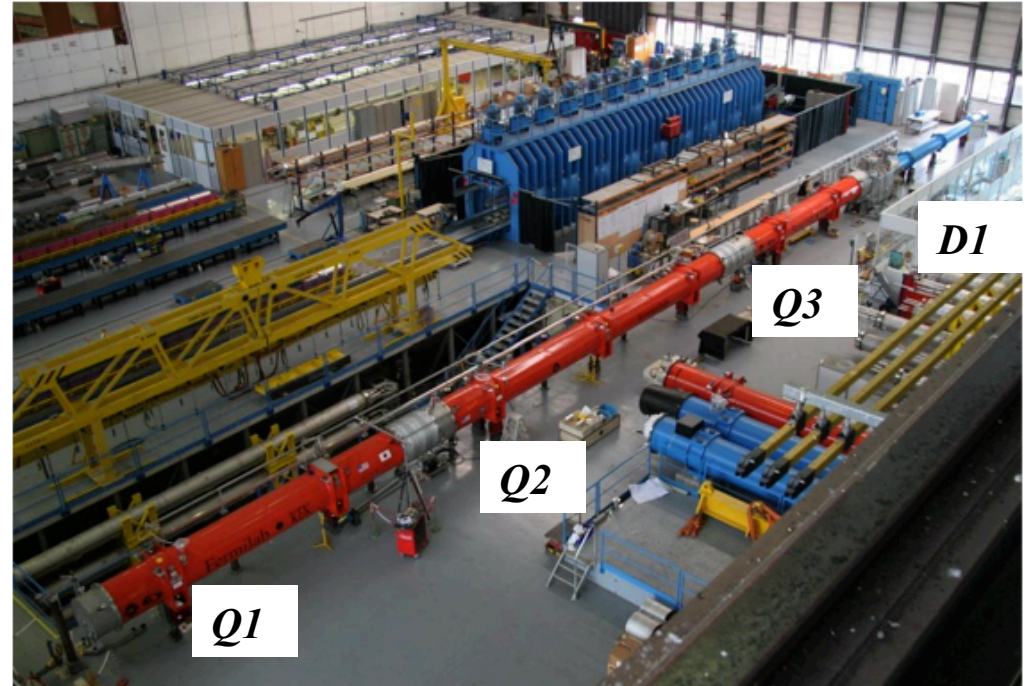
8 individually  
powered quad  
magnets are  
needed to match  
the insertion  
( ... at least)



# The LHC Insertions



mini  $\beta$  optics



# Acceleration: Energy Gain

... we have to start again from the basics

*Lorentz force*

$$\vec{F} = q * (\vec{E} + \vec{v} \times \vec{B})$$

*in long. direction the  
B-field creates no force*

$\vec{v} \parallel \vec{B}$

$$\vec{F} = \frac{d\vec{p}}{dt} = e\vec{E}$$

*acc. force is given by the electr. Field*

*In relativistic dynamics, energy and momentum satisfy the relation:*

$$E^2 = E_0^2 + p^2 c^2 \quad (E = E_0 + W)$$

*Hence:*

$$dE = \int F ds = v dp$$

*and the kinetic energy gained from the field along the z path is:*

$$dW = dE = eE_z ds \quad \Rightarrow \quad W = e \int E_z ds = eV$$

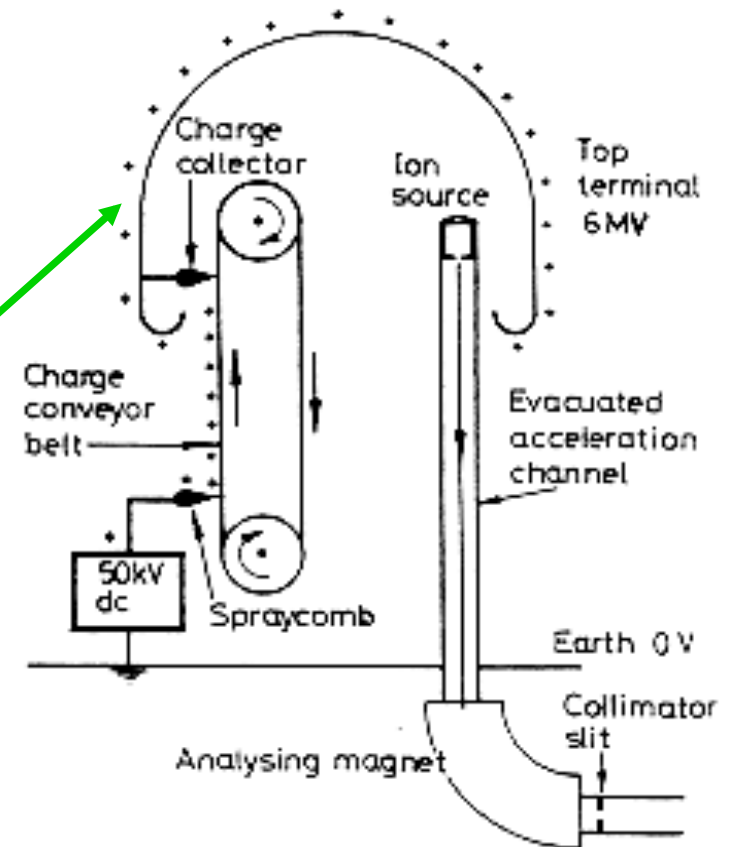
# 11.) Electrostatic Machines

## (Tandem -) van de Graaff Accelerator

creating high voltages by *mechanical* transport of charges

\* *Terminal Potential:  $U \approx 12 \dots 28 \text{ MV}$*   
using high pressure gas to suppress discharge ( $\text{SF}_6$ )

**Problems:** \* *Particle energy limited by high voltage discharges*  
\* *high voltage can only be applied once per particle ...*  
*... or twice ?*



The „Tandem principle“: Apply the accelerating voltage twice ...  
... by working with *negative ions* (e.g.  $H^-$ ) and  
*stripping the electrons* in the centre of the  
structure

$$dW = dE = eE_z ds \quad \Rightarrow \quad W = e \int E_z ds = eV$$

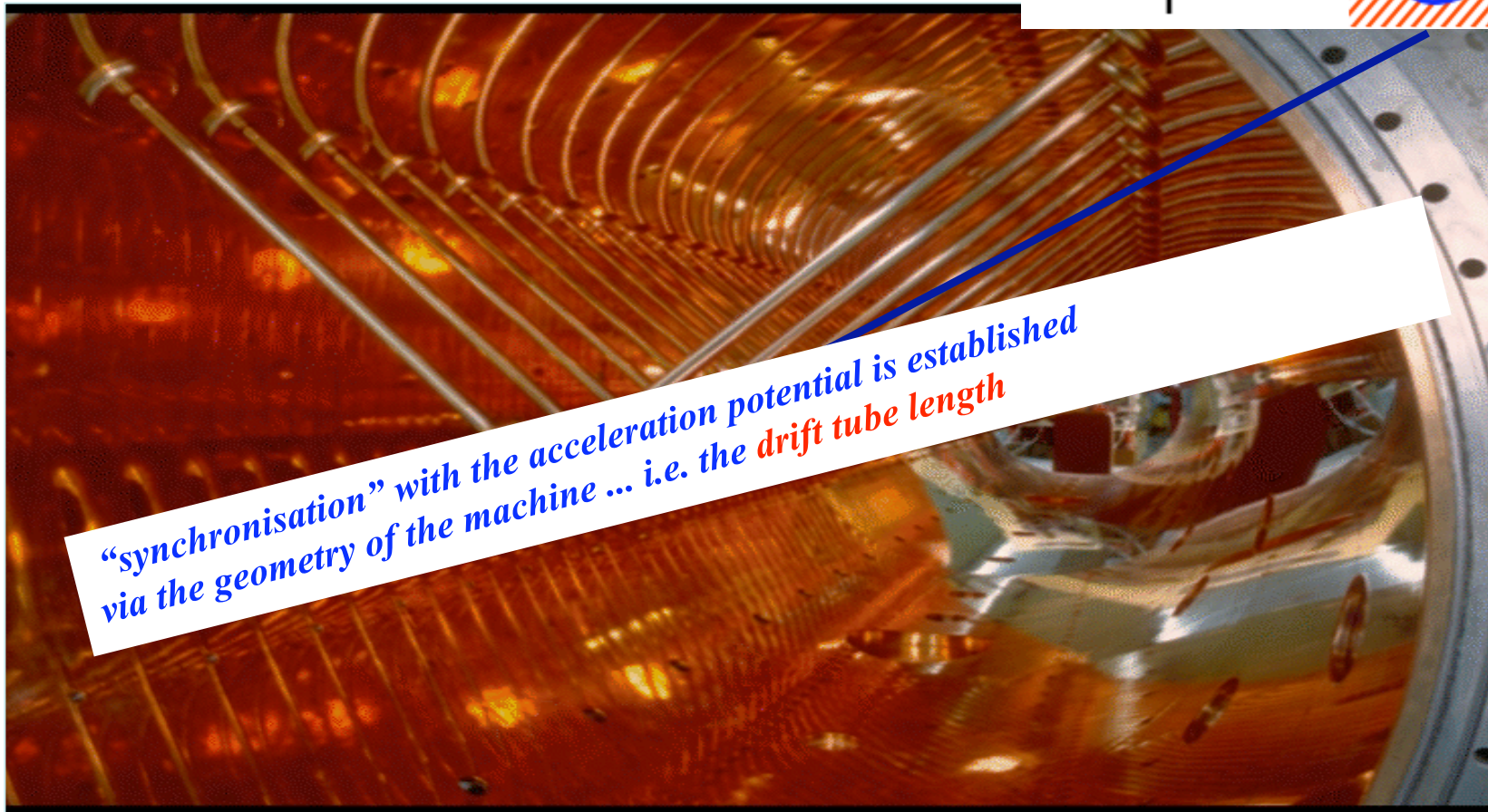
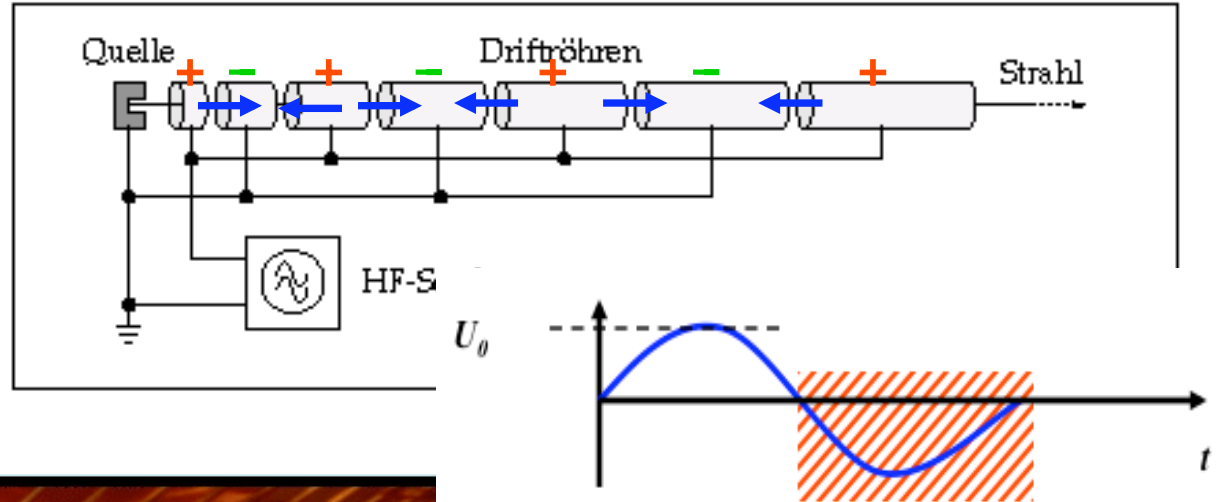
nota bene: all particles are “synchron” with the acceleration potential

*Electro Static Accelerator: 12 MV-Tandem van de Graaff  
Accelerator at MPI Heidelberg*

# 12.) Linear Accelerator 1928, Wideroe

Energy Gain per „Gap“:

$$W = q U_0 \sin \omega_{RF} t$$



“synchronisation” with the acceleration potential is established via the geometry of the machine ... i.e. the drift tube length

drift tube structure at a proton linac (GSI Unilac)

# Cyclotron:

*exact equation for revolution frequency:*

$$\omega_z = \frac{v}{R} = \frac{q}{\gamma * m} * B_z$$

1.) if  $v \ll c \Rightarrow \gamma \cong 1$

2.)  $\gamma$  increases with the energy  
 $\Rightarrow$  no exact synchronism

Syn *on*

*“synchronisation” with the acceleration potential is established via the spiraling orbit length*

$B = \text{constant}$

$\gamma \omega_{RF} = \text{constant}$

$\omega_{RF}$  decreases with time

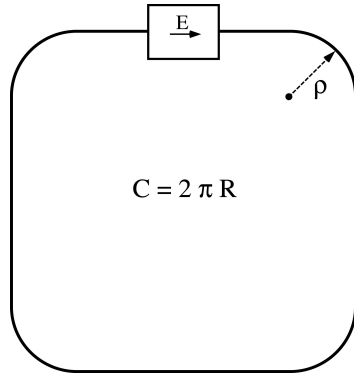
$$\omega_s(t) = \omega_{rf}(t) = \frac{q}{\gamma(t) * m_0} * B$$

*keep the synchronisation condition by varying the rf frequency*



*Cyclotron SPIRAL at GANIL*

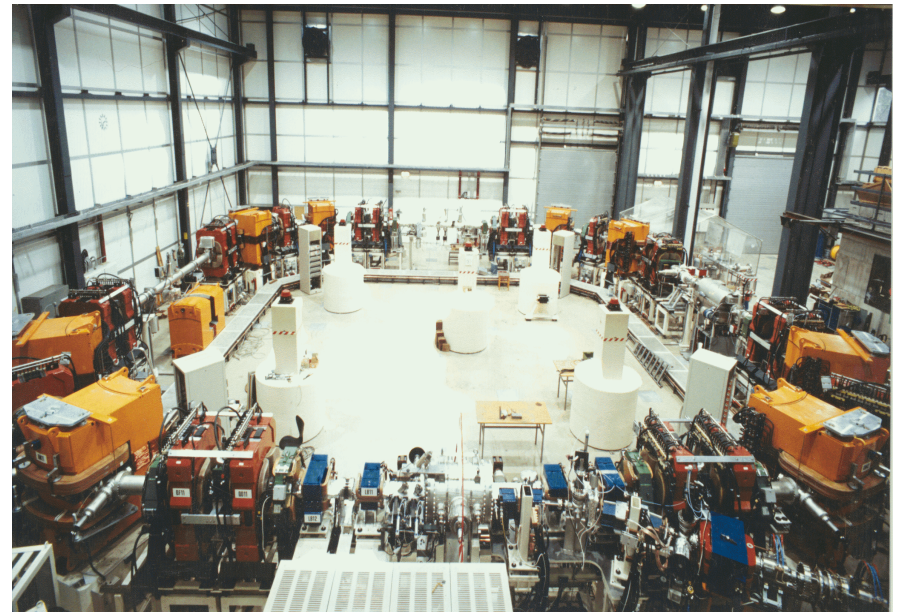
# The Synchrotron (Mac Millan, Veksler, 1945)



The synchrotron: *Ring Accelerator of const. R* where the *increase in momentum* (i.e. B-field) is *automatically synchronised* with the correct synchronous *phase of the particle in the rf cavities*

**“synchronisation” as basic principle of the particle dynamics**

- $eV$  → *Energy gain per turn*
- $\Phi = \Psi_s = cte$  → *Synchronous particle*
- $\omega_{RF} = h\omega_r$  → *RF synchronism*
- $\rho = cte \quad R = cte$  → *Constant orbit*
- $B\rho = P/e \Rightarrow B$  → *Variable magnetic field*

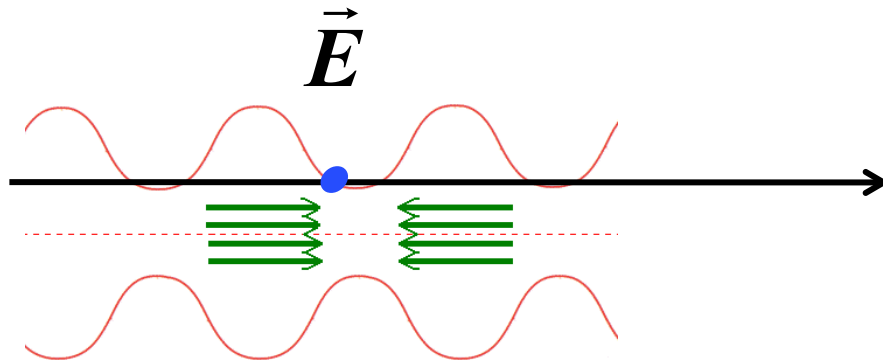




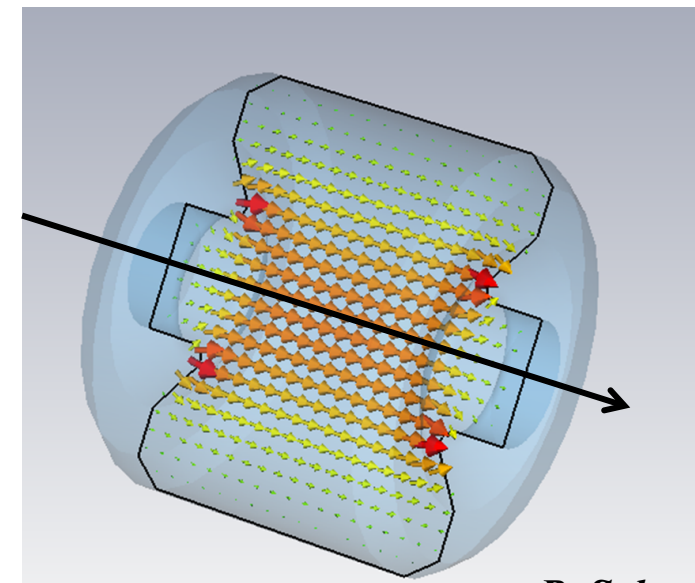
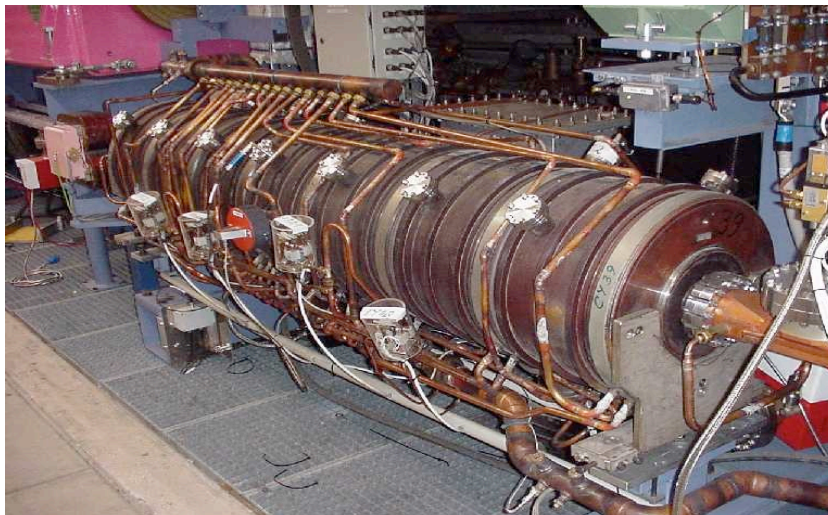
# 13.) The Acceleration

*Where is the acceleration?*

*Install an RF accelerating structure in the ring and adjust the phase (the timing) between particle and RF-Voltage in the right way: “Synchronisation”*



*500 MHz cavities in an electron storage ring*



*B. Salvant  
N. Biancacci*

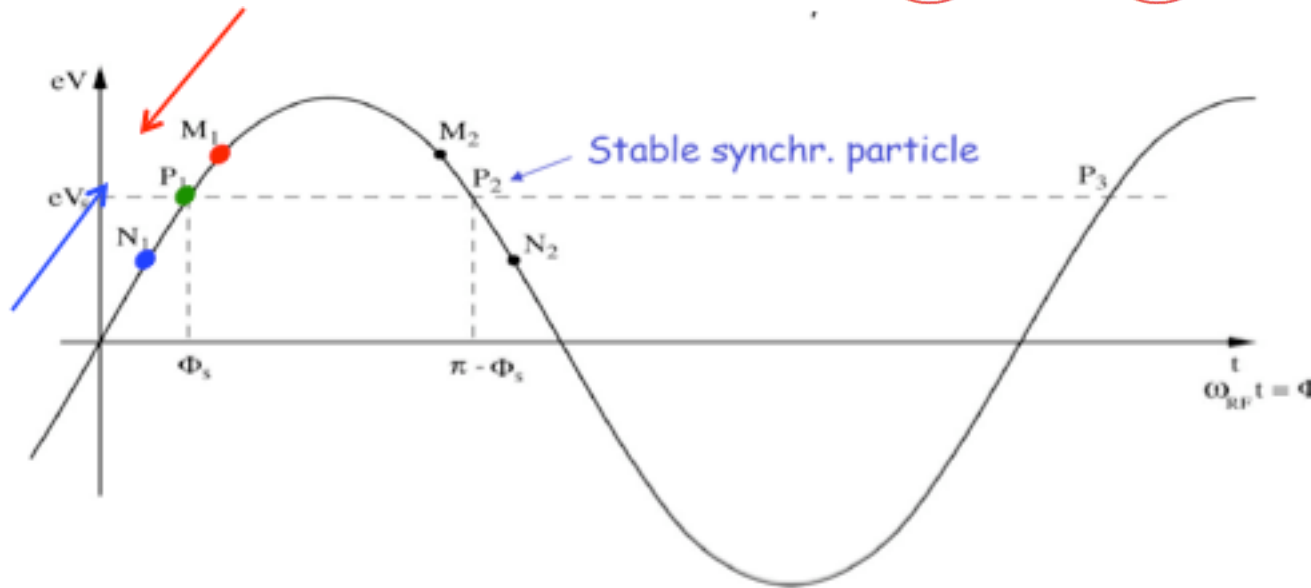
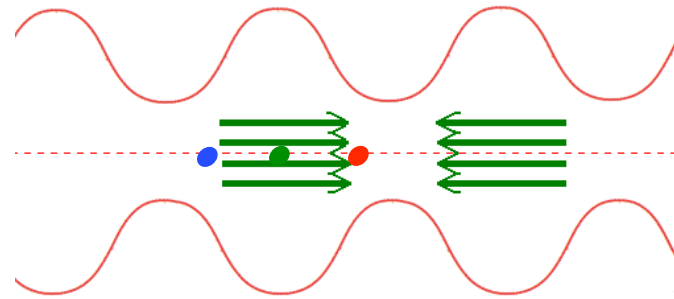
# 14.) The Acceleration for $\Delta p/p \neq 0$

*"Phase Focusing" below transition*

*ideal particle* •

*particle with  $\Delta p/p > 0$*  • *faster*

*particle with  $\Delta p/p < 0$*  • *slower*

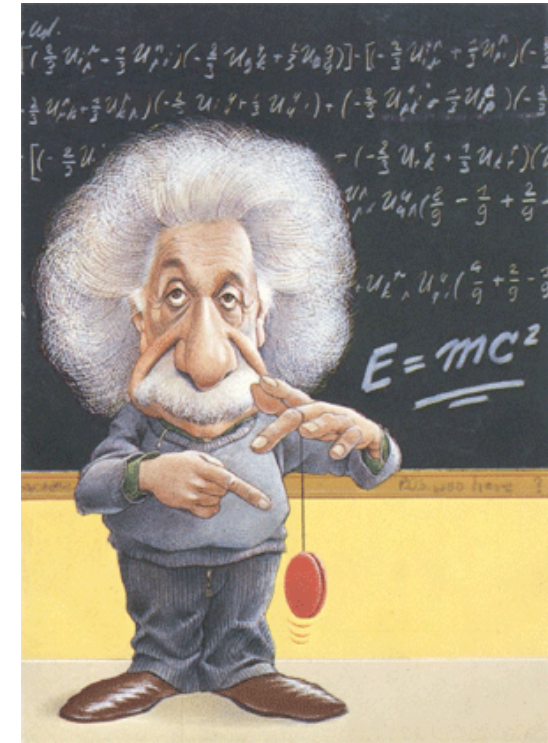
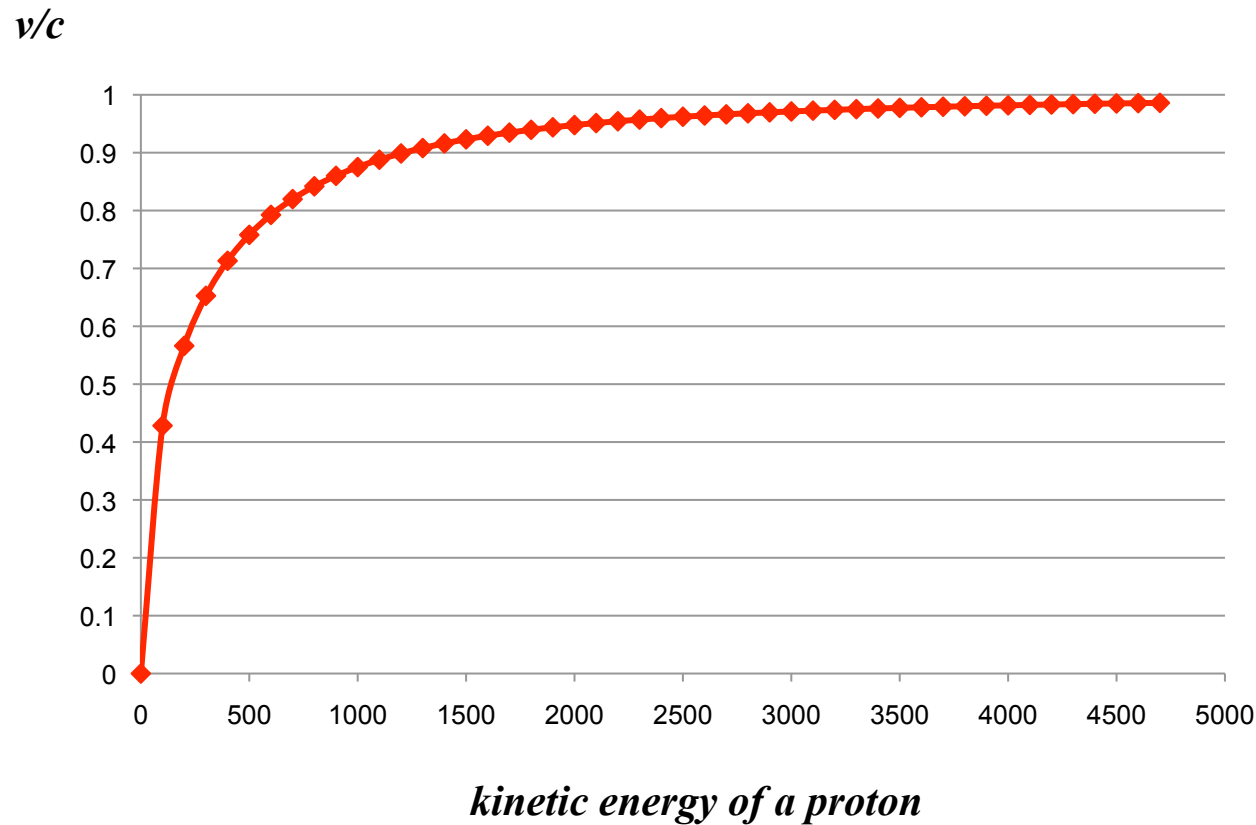


*Focussing effect in the longitudinal direction keeping the particles close together ... forming a "bunch"*

*oscillation frequency:*  $f_s = f_{rev} \sqrt{-\frac{h\alpha_s * qU_0 \cos \phi_s}{2\pi E_s}} \approx \text{some Hz}$

*... so sorry, here we need help from Albert:*

$$\gamma = \frac{E_{total}}{mc^2} = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} \quad \longrightarrow \quad \frac{v}{c} = \sqrt{1 - \frac{mc^2}{E^2}}$$



*... some when the particles do not get faster anymore*

*.... but heavier !*

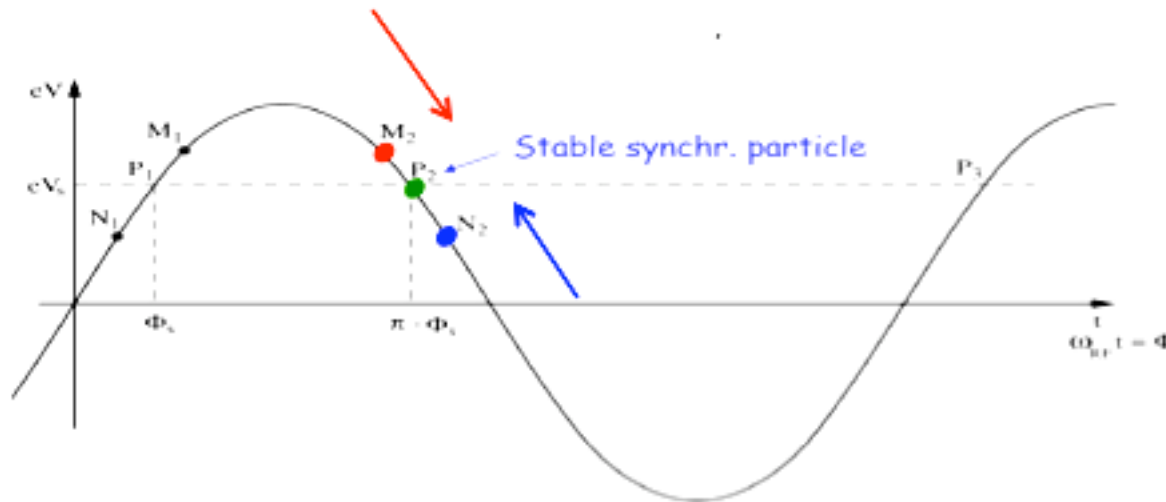
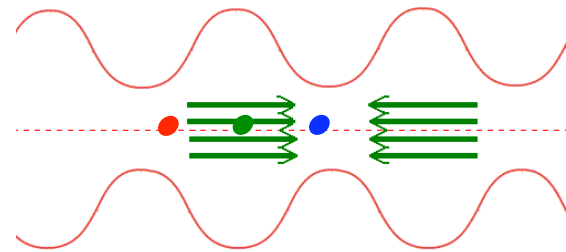
# 15.) The Acceleration for $\Delta p/p \neq 0$

*"Phase Focusing" above transition*

*ideal particle* •

*particle with  $\Delta p/p > 0$*  • *heavier*

*particle with  $\Delta p/p < 0$*  • *lighter*



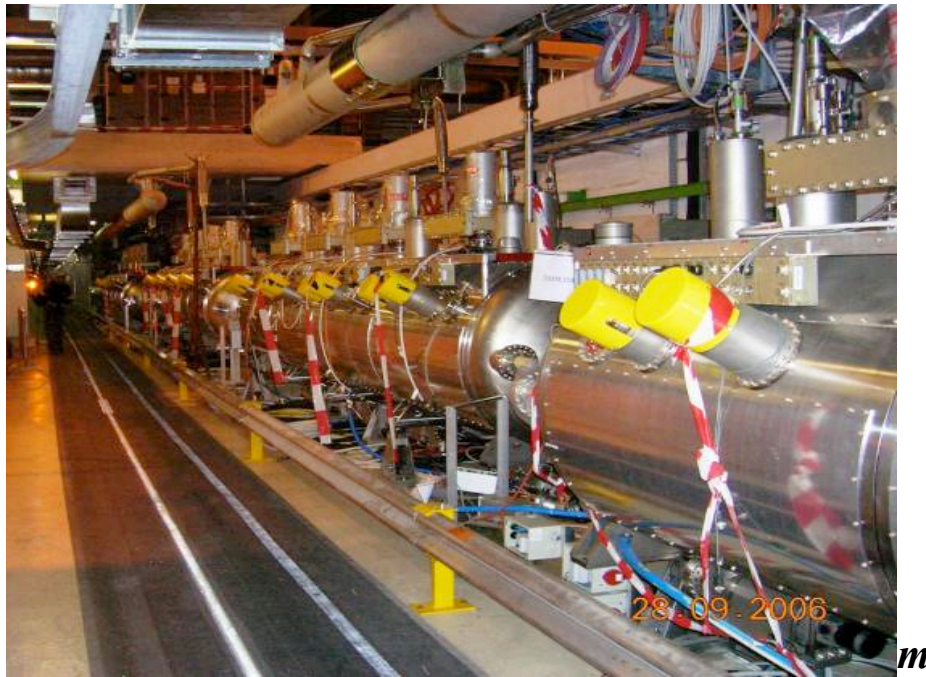
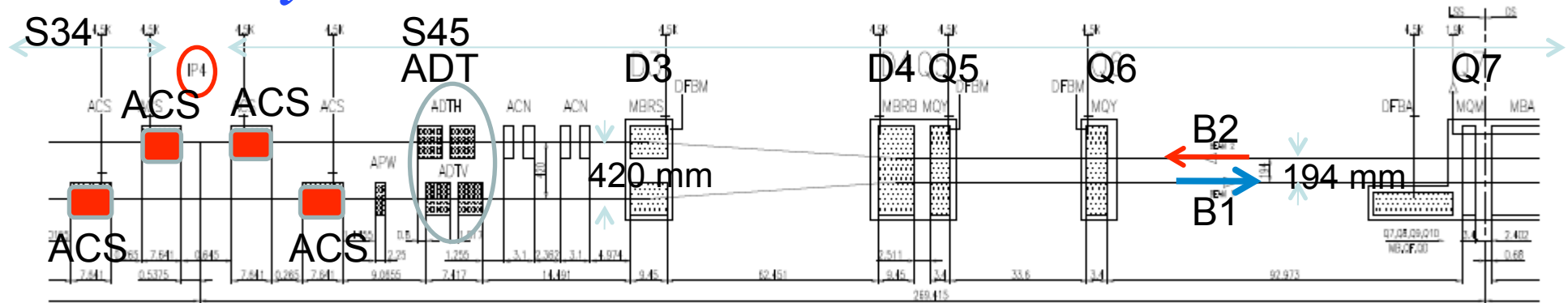
*Focussing effect in the longitudinal direction*

*keeping the particles close together ... forming a "bunch"*

*... and how do we accelerate now ???*

*with the dipole magnets !*

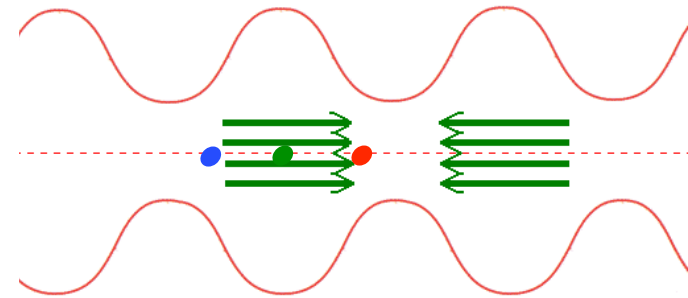
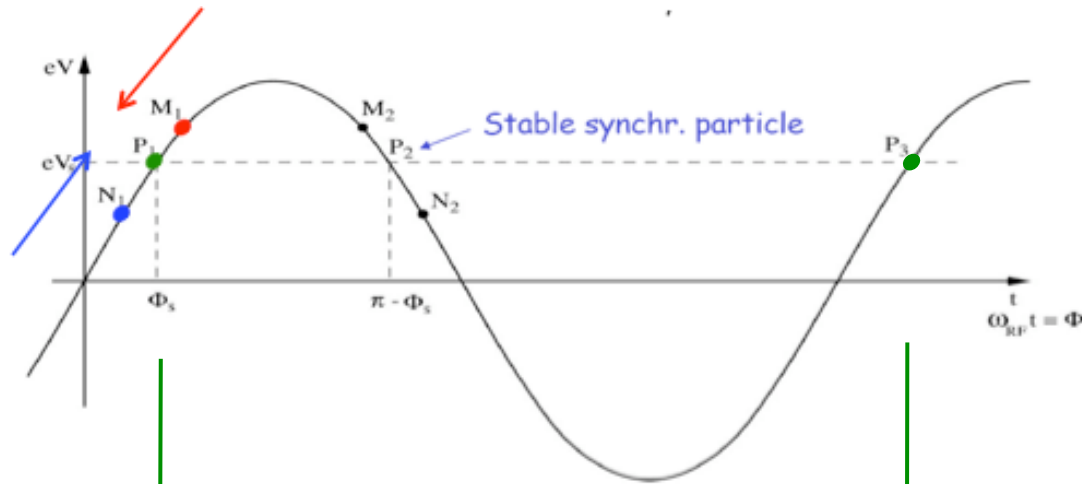
# The RF system: IR4



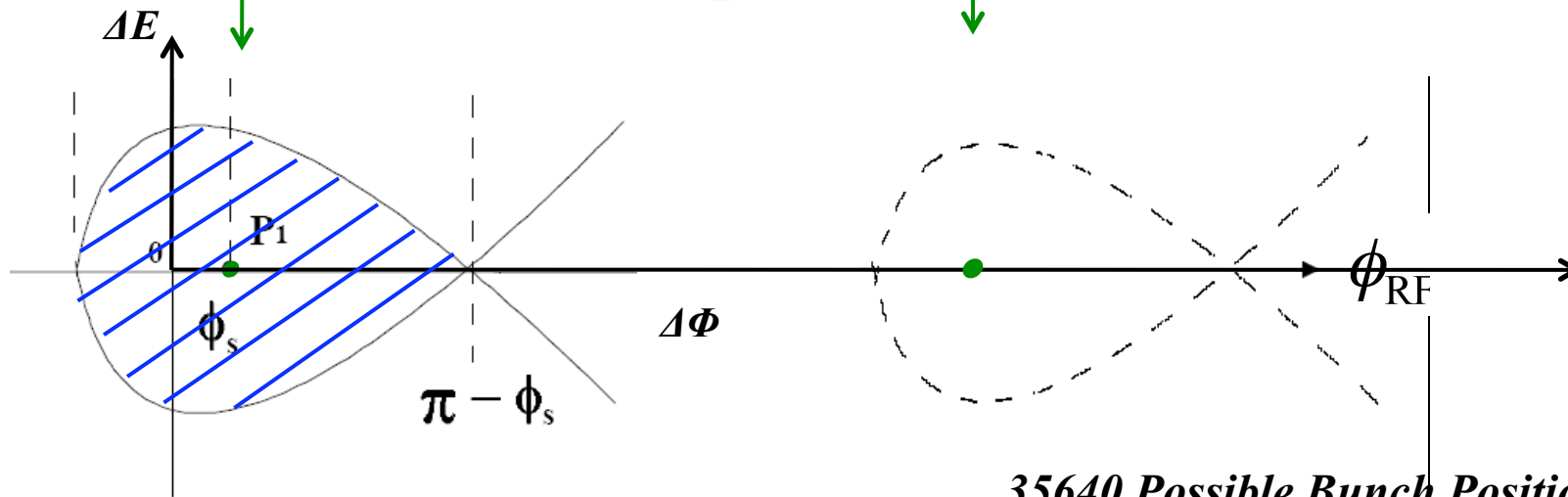
*Nb on Cu cavities @4.5 K (=LEP2)  
Beam pipe diam.=300mm*

<i>Bunch length (<math>4\sigma</math>)</i>	<i>ns</i>	<i>1.06</i>
<i>Energy spread (<math>2\sigma</math>)</i>	<i><math>10^{-3}</math></i>	<i>0.22</i>
<i>Synchr. rad. loss/turn</i>	<i>keV</i>	<i>7</i>
<i>Synchr. rad. power</i>	<i>kW</i>	<i>3.6</i>
<i>RF frequency</i>	<i>M</i>	<i>400</i>
	<i>Hz</i>	
<i>Harmonic number</i>		<i>35640</i>
<i>RF voltage/beam</i>	<i>MV</i>	<i>16</i>
<i>Energy gain/turn</i>	<i>keV</i>	<i>485</i>
<i>Synchrotron frequency</i>	<i>Hz</i>	<i>23.0</i>

# RF Buckets & long. dynamics in phase space

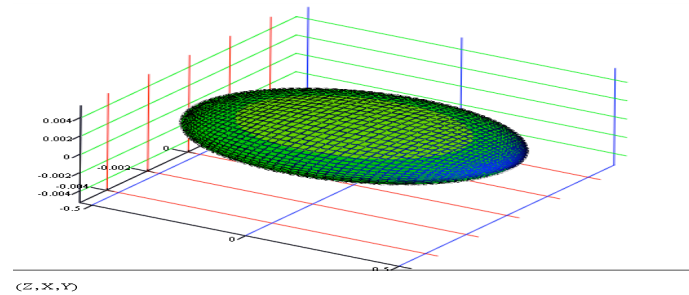


*Oscillations in Energy and Phase*

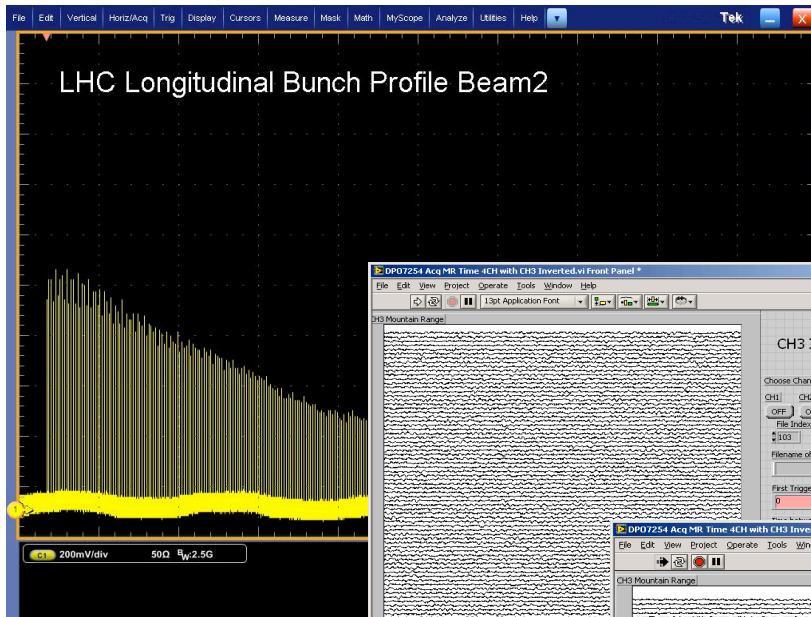


**35640 Possible Bunch Positions ("buckets")**  
**2808 Bunches**

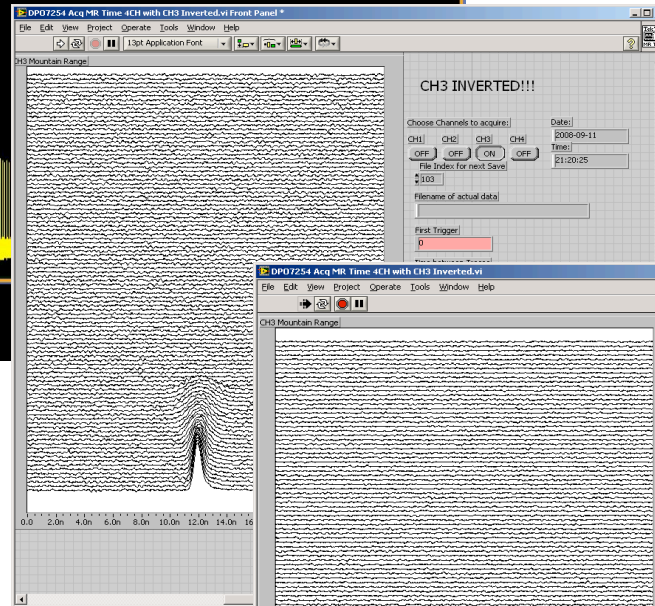
# LHC Commissioning: RF



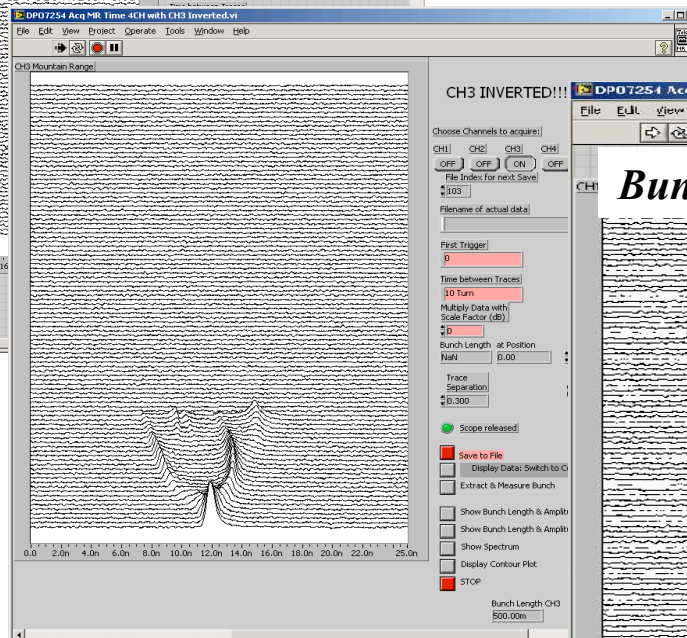
*a proton bunch: focused longitudinal by the RF field*



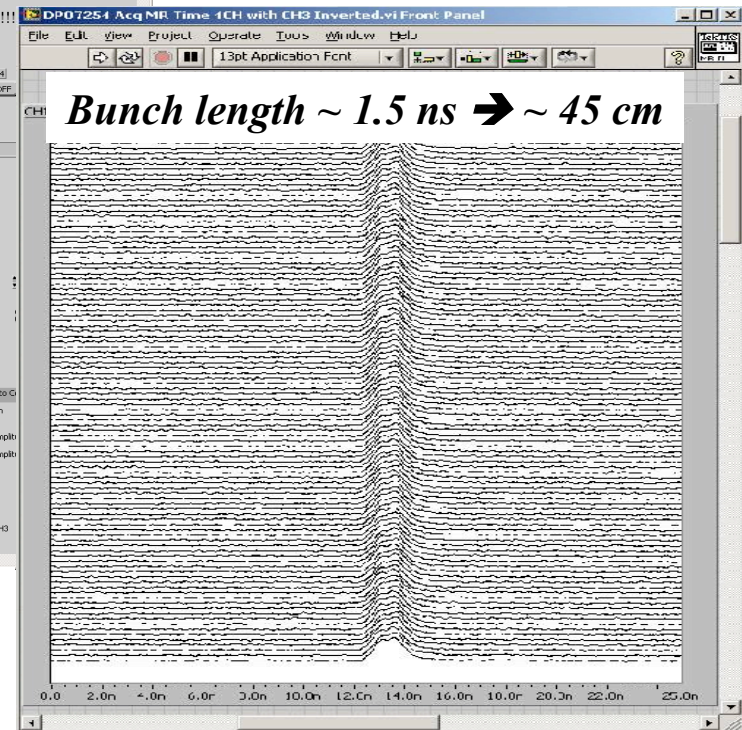
*RF off*



*RF on,  
phase optimisation*



*RF on, phase adjusted,  
beam captured*



*IV.) Are there Any Problems ???*

*sure there are*

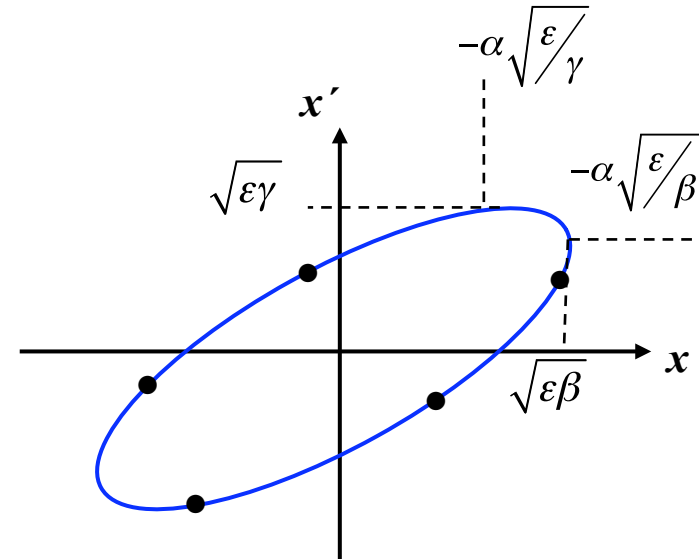


## Liouville during Acceleration

$$\varepsilon = \gamma(s) x^2(s) + 2\alpha(s)x(s)x'(s) + \beta(s) x'^2(s)$$

*Beam Emittance* corresponds to the area covered in the  $x, x'$  Phase Space Ellipse

*Liouville: Area in phase space is constant.*



**But so sorry ...  $\varepsilon \neq \text{const}$  !**

*Classical Mechanics:*

*phase space = diagram of the two canonical variables  
position & momentum*

$x$                        $p_x$

$$p_j = \frac{\partial L}{\partial \dot{q}_j} \quad ; \quad L = T - V = \text{kin. Energy} - \text{pot. Energy}$$

According to Hamiltonian mechanics:  
 phase space diagram relates the variables  $q$  and  $p$

$$q = \text{position} = x$$

$$p = \text{momentum} = \gamma m v = mc \gamma \beta_x$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} \quad ; \quad \beta_x = \frac{\dot{x}}{c}$$

Liouville's Theorem:  $\int p dq = \text{const}$

for convenience (i.e. *because we are lazy bones*) we use in accelerator theory:

$$x' = \frac{dx}{ds} = \frac{dx}{dt} \frac{dt}{ds} = \frac{\beta_x}{\beta} \quad \text{where } \beta_x = v_x / c$$

$$\int p dq = mc \int \gamma \beta_x dx$$

$$\int p dq = mc \gamma \beta \underbrace{\int x' dx}_{\varepsilon}$$

$$\Rightarrow \varepsilon = \int x' dx \propto \frac{1}{\beta \gamma}$$

*the beam emittance  
 shrinks during  
 acceleration  $\varepsilon \sim 1/\gamma$*

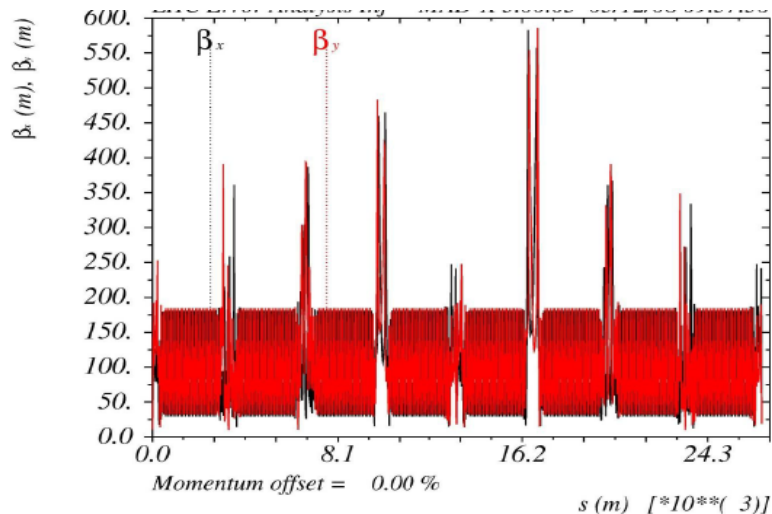
*Nota bene:*

1.) A proton machine ... or an electron linac ... needs the highest aperture at injection energy !!!  
 as soon as we start to accelerate the *beam size shrinks as  $\gamma^{-1/2}$*  in both planes.

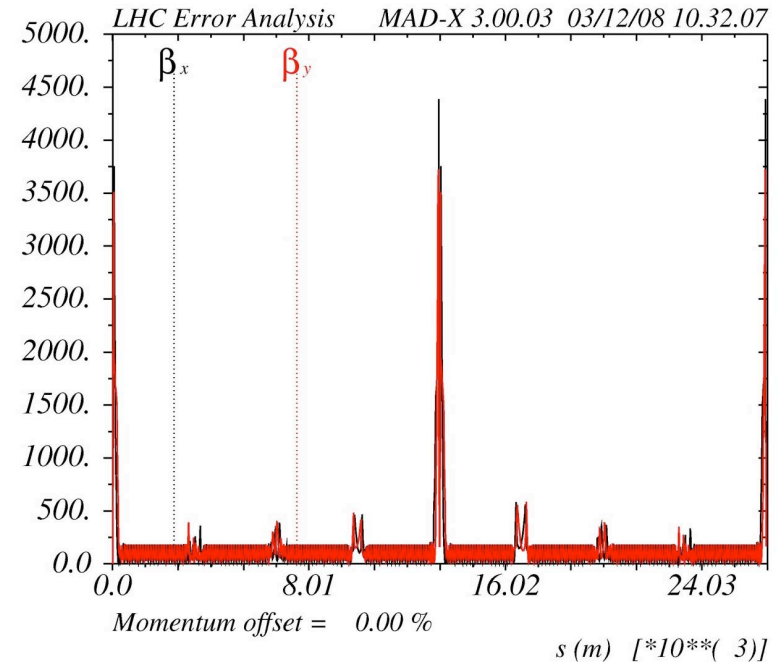
$$\sigma = \sqrt{\epsilon\beta}$$

2.) At lowest energy the machine will have the major aperture problems,  
 → here we have to *minimise  $\hat{\beta}$*

3.) we need *different beam optics* adopted to the energy:  
*A Mini Beta concept will only be adequate at flat top.*



*LHC injection optics at 450 GeV*

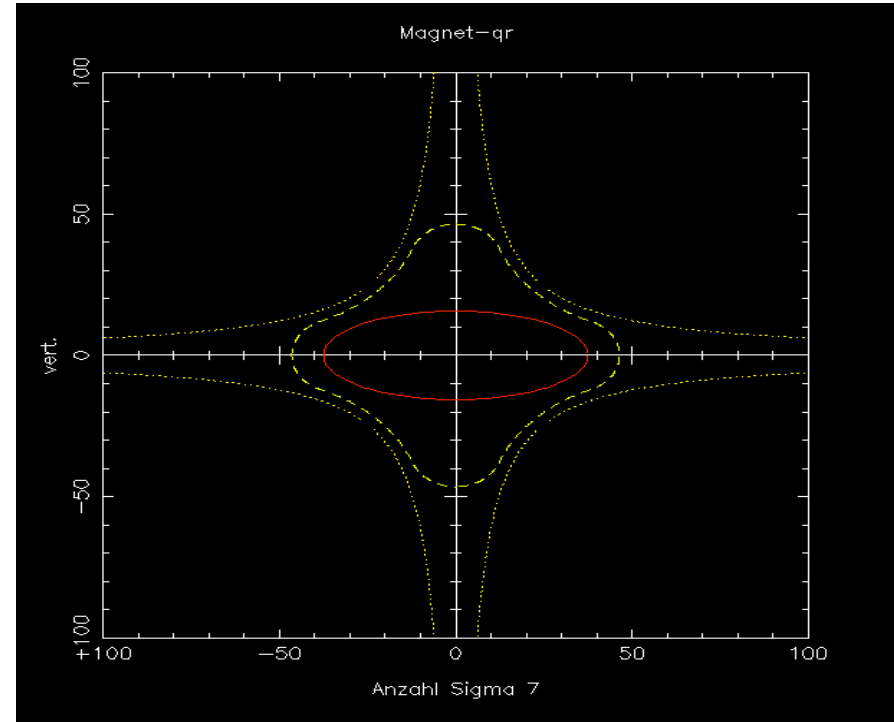
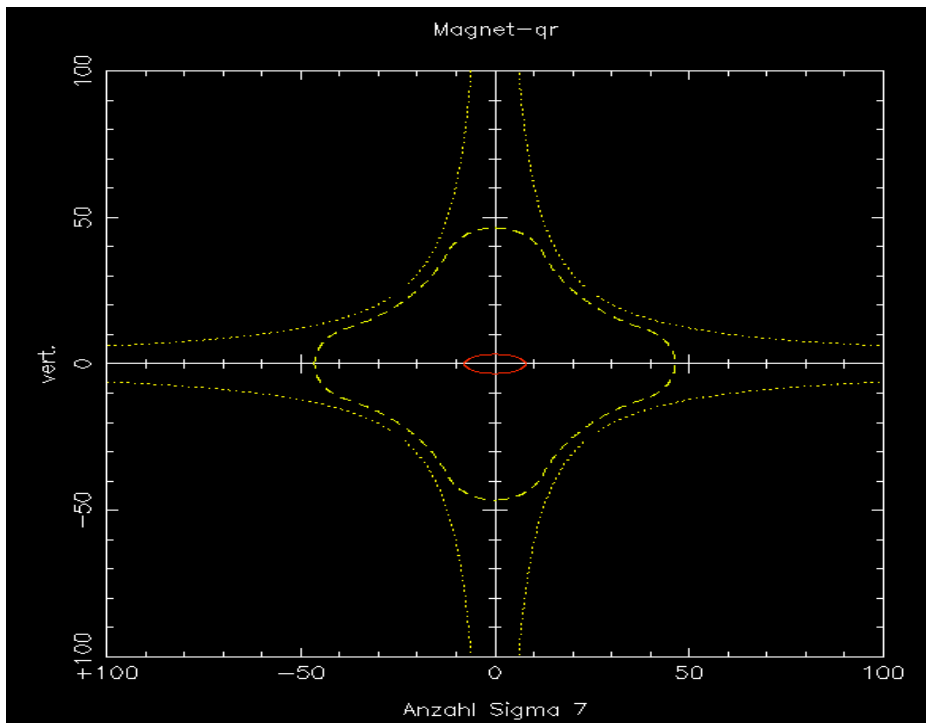


*LHC mini beta optics at 7000 GeV*

*Example: HERA proton ring*

*injection energy: 40 GeV     $\gamma = 43$   
flat top energy: 920 GeV     $\gamma = 980$*

*emittance  $\varepsilon$  (40GeV) =  $1.2 * 10^{-7}$   
 $\varepsilon$  (920GeV) =  $5.1 * 10^{-9}$*



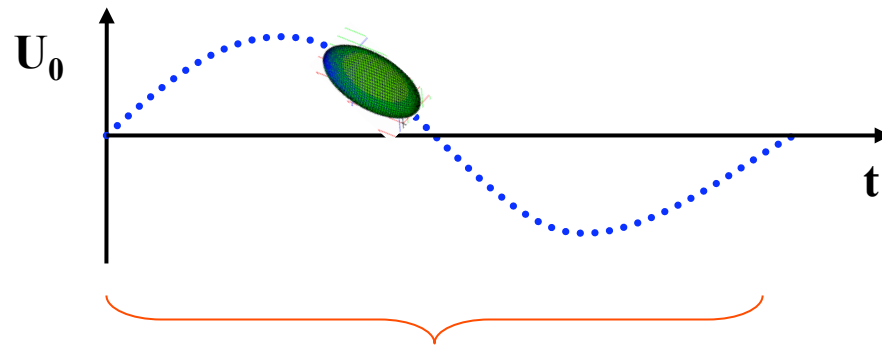
*7  $\sigma$  beam envelope at E = 40 GeV*

*... and at E = 920 GeV*

# RF Acceleration-Problem: panta rhei !!!

(Heraklit: 540-480 v. Chr.)

just a stupid (and nearly wrong) example)

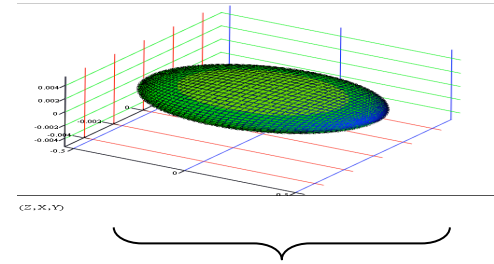


$$\lambda = 75 \text{ cm}$$

$$\sin(90^\circ) = 1$$

$$\sin(84^\circ) = 0.994$$

$$\frac{\Delta U}{U} = 6.0 \cdot 10^{-3}$$



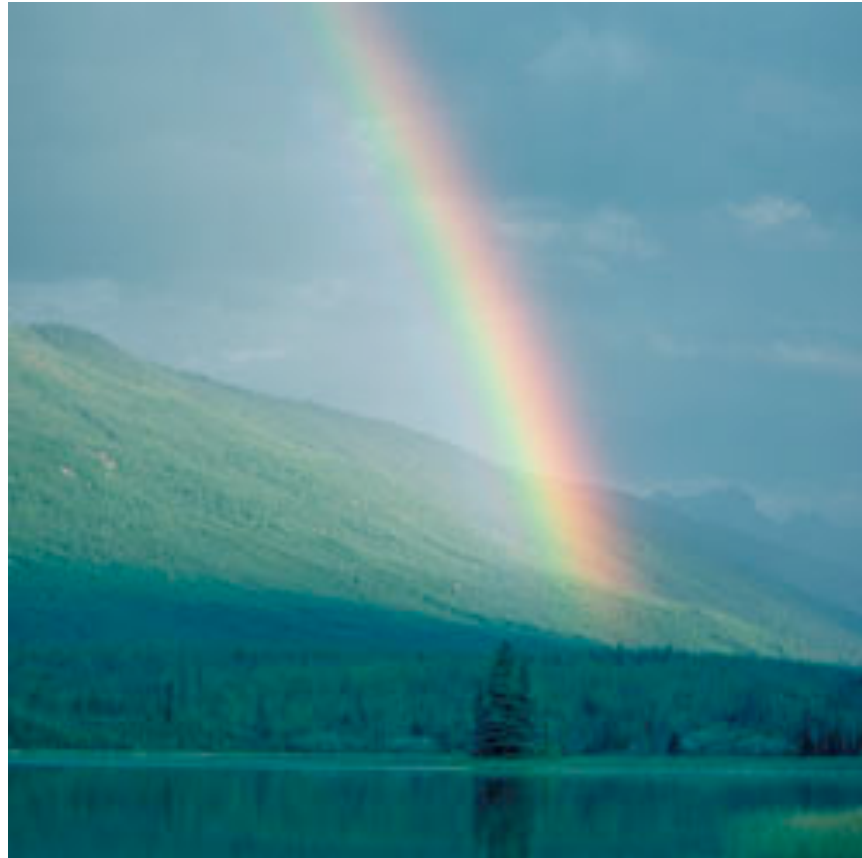
Bunch length of Electrons  $\approx 1 \text{ cm}$

$$\left. \begin{array}{l} \nu = 400 \text{ MHz} \\ c = \lambda \nu \end{array} \right\} \lambda = 75 \text{ cm}$$

typical momentum spread of an electron bunch:

$$\frac{\Delta p}{p} \approx 1.0 \cdot 10^{-3}$$

## *Dispersive and Chromatic Effects: $\Delta p/p \neq 0$*



*Are there any Problems ???*

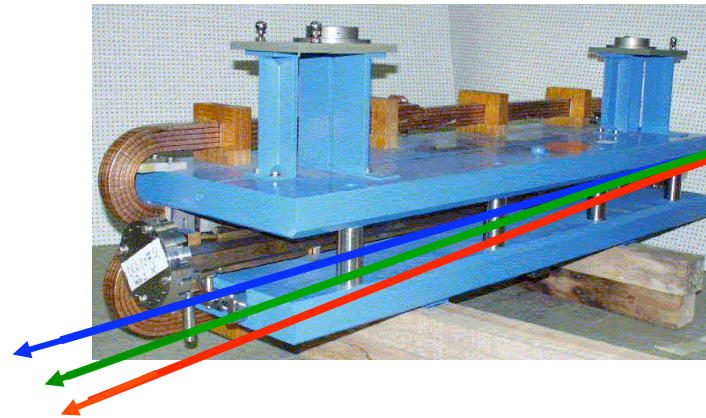
*Sure there are !!!*

*font colors due to  
pedagogical reasons*

# 17.) Dispersion and Chromaticity: Magnet Errors for $\Delta p/p \neq 0$

Influence of external fields on the beam: *prop. to magn. field & prop. zu  $1/p$*

dipole magnet  $\alpha = \frac{\int B dl}{p/e}$



$$x_D(s) = D(s) \frac{\Delta p}{p}$$

focusing lens  $k = \frac{g}{p/e}$

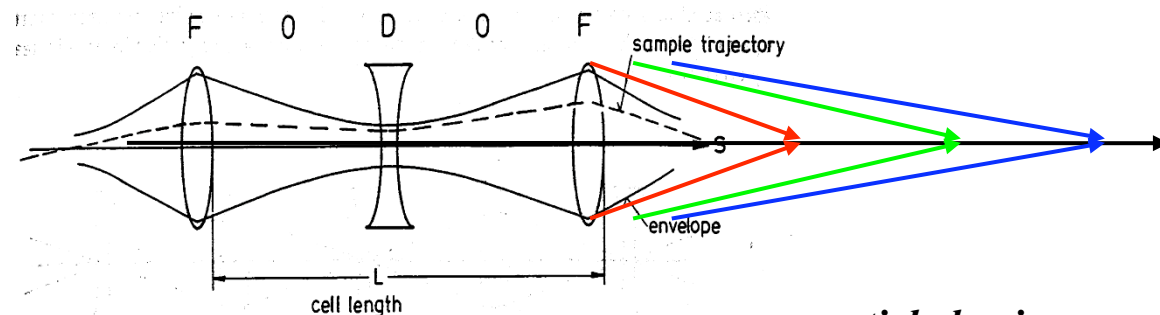
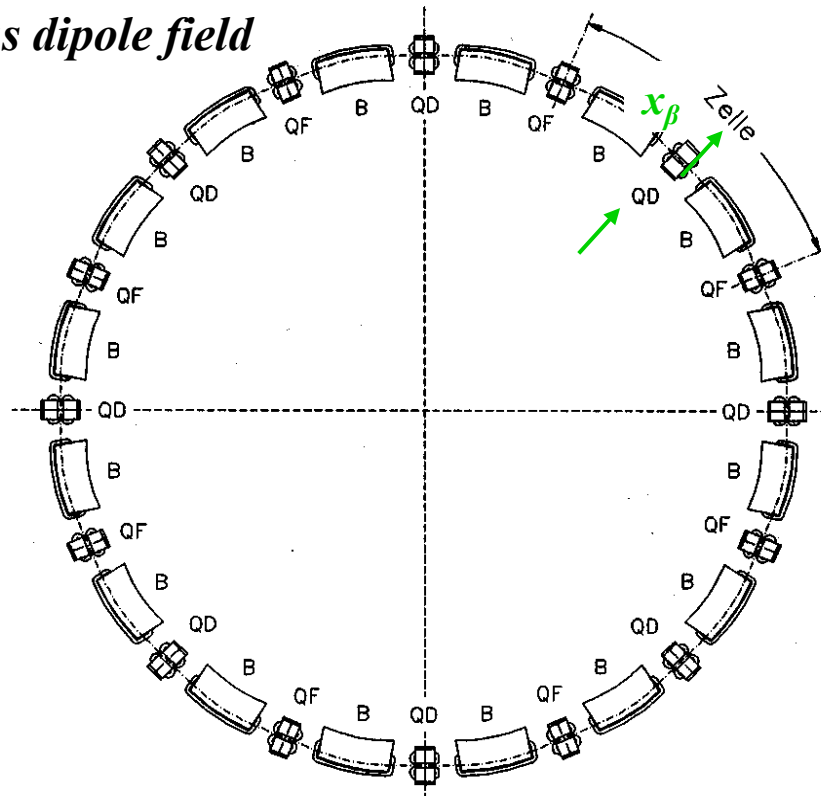


Figure 29: FODO cell

particle having ...  
to high energy  
to low energy  
ideal energy

# Dispersion

Example: homogeneous dipole field



valid for  $\Delta p/p > 0$

$$: D(s) \cdot \frac{\Delta p}{p}$$

## Matrix formalism:

$$x(s) = x_\beta(s) + D(s) \cdot \frac{\Delta p}{p}$$

$$x(s) = C(s) \cdot x_0 + S(s) \cdot x'_0 + D(s) \cdot \frac{\Delta p}{p}$$

$$\begin{pmatrix} x \\ x' \end{pmatrix}_s = \begin{pmatrix} C & S \\ C' & S' \end{pmatrix} \begin{pmatrix} x \\ x' \end{pmatrix}_0 + \frac{\Delta p}{p} \begin{pmatrix} D \\ D' \end{pmatrix}_0$$



or expressed as 3x3 matrix

$$\begin{pmatrix} x \\ x' \\ \Delta p/p \end{pmatrix}_s = \begin{pmatrix} C & S & D \\ C' & S' & D' \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} x \\ x' \\ \Delta p/p \end{pmatrix}_0$$

Example

$$x_\beta = 1 \dots 2 \text{ mm}$$

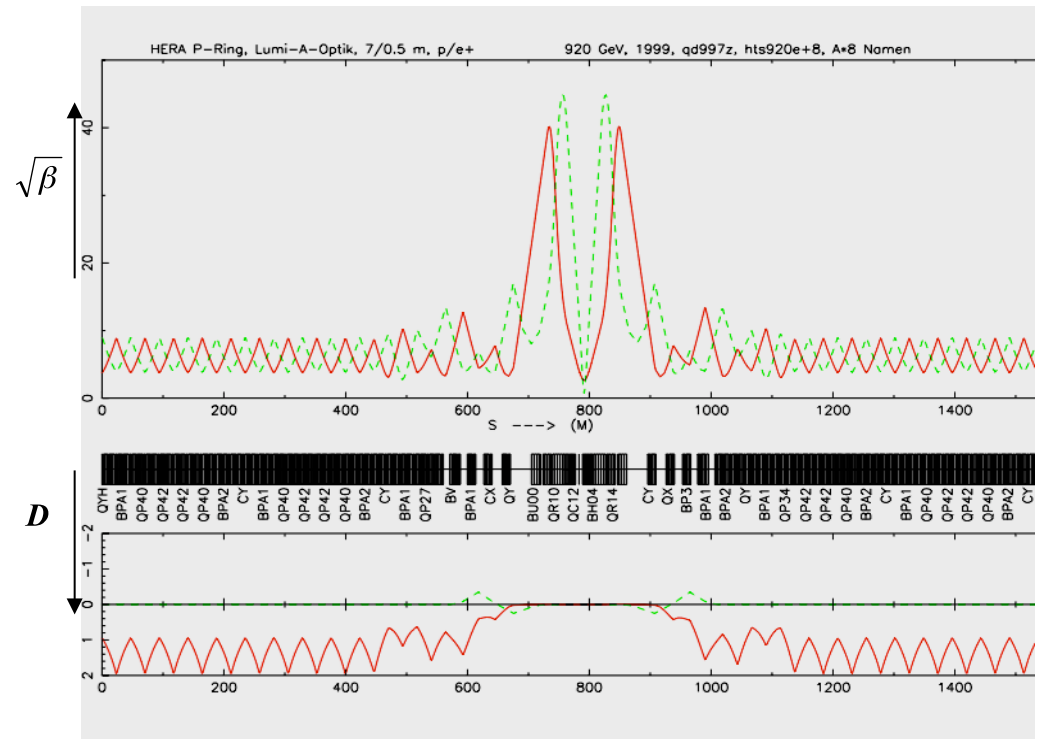
$$D(s) \approx 1 \dots 2 \text{ m}$$

$$\frac{\Delta p}{p} \approx 1 \cdot 10^{-3}$$

Amplitude of Orbit oscillation

contribution due to Dispersion  $\approx$  beam size

$\rightarrow$  Dispersion must vanish at the collision point



Calculate  $D, D'$ : ... takes a couple of sunny Sunday evenings !

## 26.) Chromaticity:

### A Quadrupole Error for $\Delta p/p \neq 0$

Influence of external fields on the beam: *prop. to magn. field & prop. zu  $1/p$*

focusing lens

$$k = \frac{g}{p/e}$$

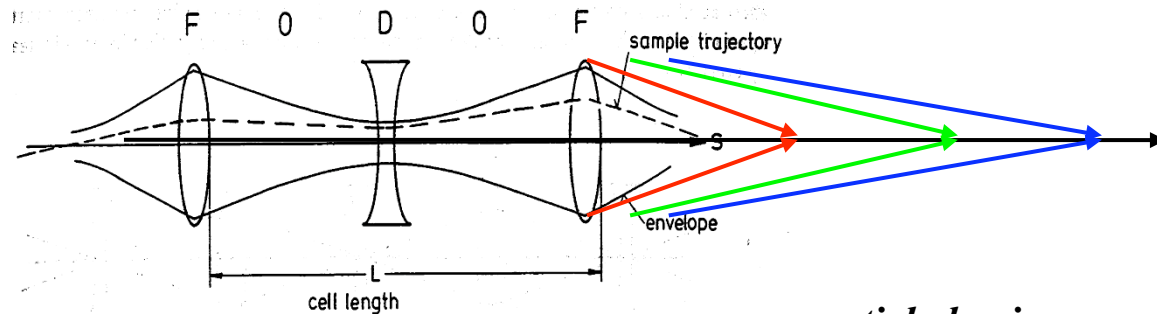


Figure 29: FODO cell

particle having ...  
*to high energy*  
*to low energy*  
*ideal energy*

... which *acts like a quadrupole error in the machine*  
 and *leads to a tune spread:*

$$\Delta Q = -\frac{1}{4\pi} \frac{\Delta p}{p_0} k_0 \beta(s) ds$$

definition of chromaticity:

$$\Delta Q = Q' * \frac{\Delta p}{p}$$

... what is wrong about Chromaticity:

**Problem: chromaticity is generated by the lattice itself !!**

$Q'$  is a number indicating the size of the tune spot in the working diagram,

$Q'$  is always created if the beam is focussed

→ it is determined by the focusing strength  $k$  of all quadrupoles

$$Q' = -\frac{1}{4\pi} \oint k(s) \beta(s) ds$$

$k$  = quadrupole strength

$\beta$  = **betafunction** indicates the beam size ... and even more the **sensitivity of the beam to external fields**

Example: LHC

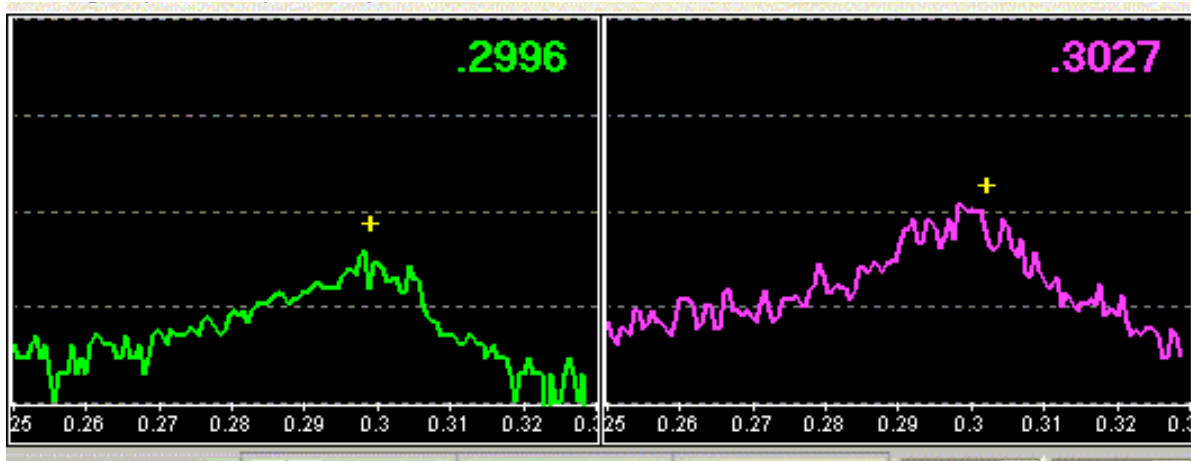
$$Q' = 250$$

$$\Delta p/p = \pm 0.2 \cdot 10^{-3}$$

$$\Delta Q = 0.256 \dots 0.36$$

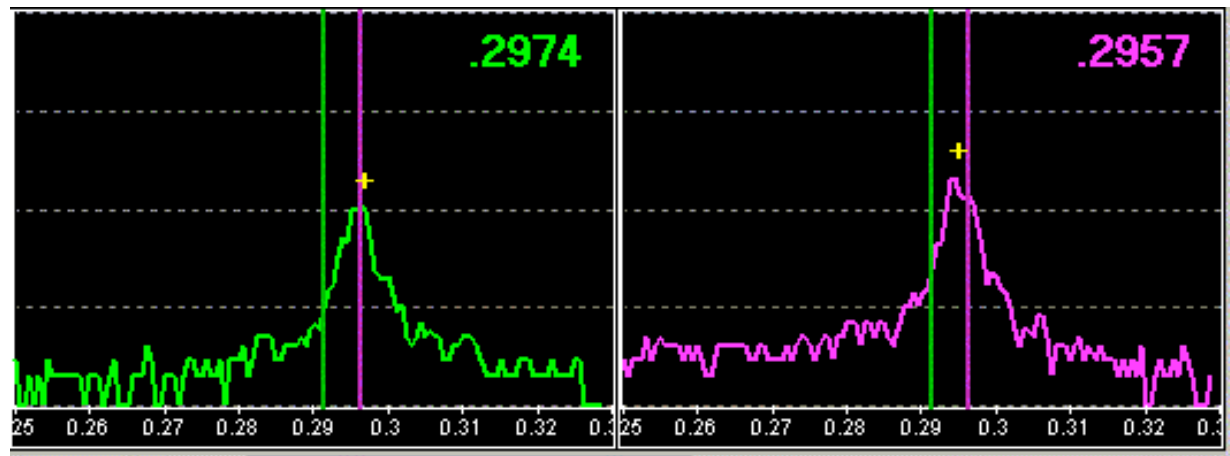
→ Some particles get very close to resonances and are lost

in other words: the tune is not a point  
it is a **pancake**



*Tune signal for a nearly uncompensated chromaticity ( $Q' \approx 20$ )*

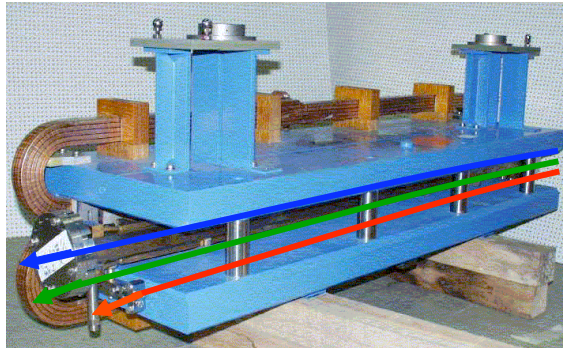
*Ideal situation: chromaticity well corrected, ( $Q' \approx 1$ )*



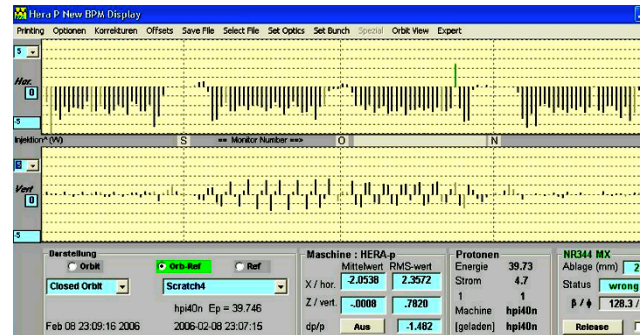
## Correction of $Q'$ :

*Need: additional quadrupole strength for each momentum deviation  $\Delta p/p$*

1.) *sort the particles according to their momentum*  $x_D(s) = D(s) \frac{\Delta p}{p}$



*... using the dispersion function*



2.) *apply a magnetic field that rises quadratically with  $x$  (sextupole field)*

$$B_x = \tilde{g}xz$$

$$B_z = \frac{1}{2} \tilde{g}(x^2 - z^2)$$

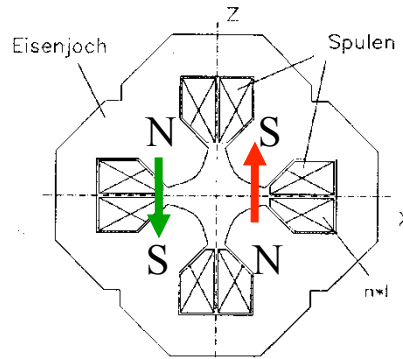
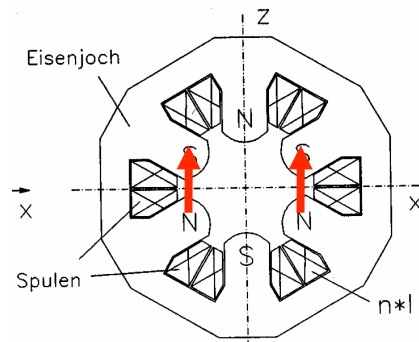
}

$$\frac{\partial B_x}{\partial z} = \frac{\partial B_z}{\partial x} = \tilde{g}x$$

*linear rising  
„gradient“:*

# Correction of $Q'$ :

## Sextupole Magnets:

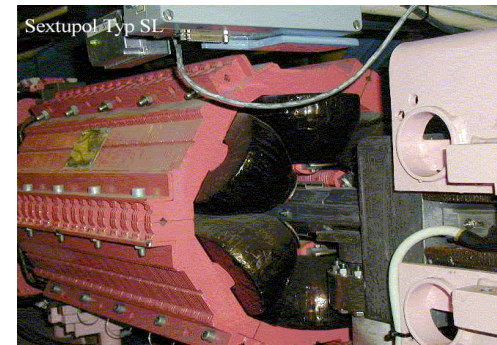


$k_1$  normalised quadrupole strength

$k_2$  normalised sextupole strength

$$k_1(\text{sext}) = \frac{\tilde{g} x}{p/e} = k_2 * x$$

$$k_1(\text{sext}) = k_2 * D * \frac{\Delta p}{p}$$



corrected chromaticity

considering a single cell:

$$Q'_{\text{cell}_x} = -\frac{1}{4\pi} \left\{ k_{qf} \hat{\beta}_x l_{qf} - k_{qd} \check{\beta}_x l_{qd} \right\} + \frac{1}{4\pi} \sum_{F \text{ sext}} k_2^F l_{\text{sext}} D_x^F \beta_x^F - \frac{1}{4\pi} \sum_{D \text{ sext}} k_2^D l_{\text{sext}} D_x^D \beta_x^D$$

$$Q'_{\text{cell}_y} = -\frac{1}{4\pi} \left\{ -k_{qf} \check{\beta}_y l_{qf} + k_{qd} \hat{\beta}_y l_{qd} \right\} + \frac{1}{4\pi} \sum_{F \text{ sext}} k_2^F l_{\text{sext}} D_x^F \beta_x^F - \frac{1}{4\pi} \sum_{D \text{ sext}} k_2^D l_{\text{sext}} D_x^D \beta_x^D$$

## *Some Golden Rules to Avoid Trouble*

**I.) Golden Rule number one:  
do not focus the beam !**

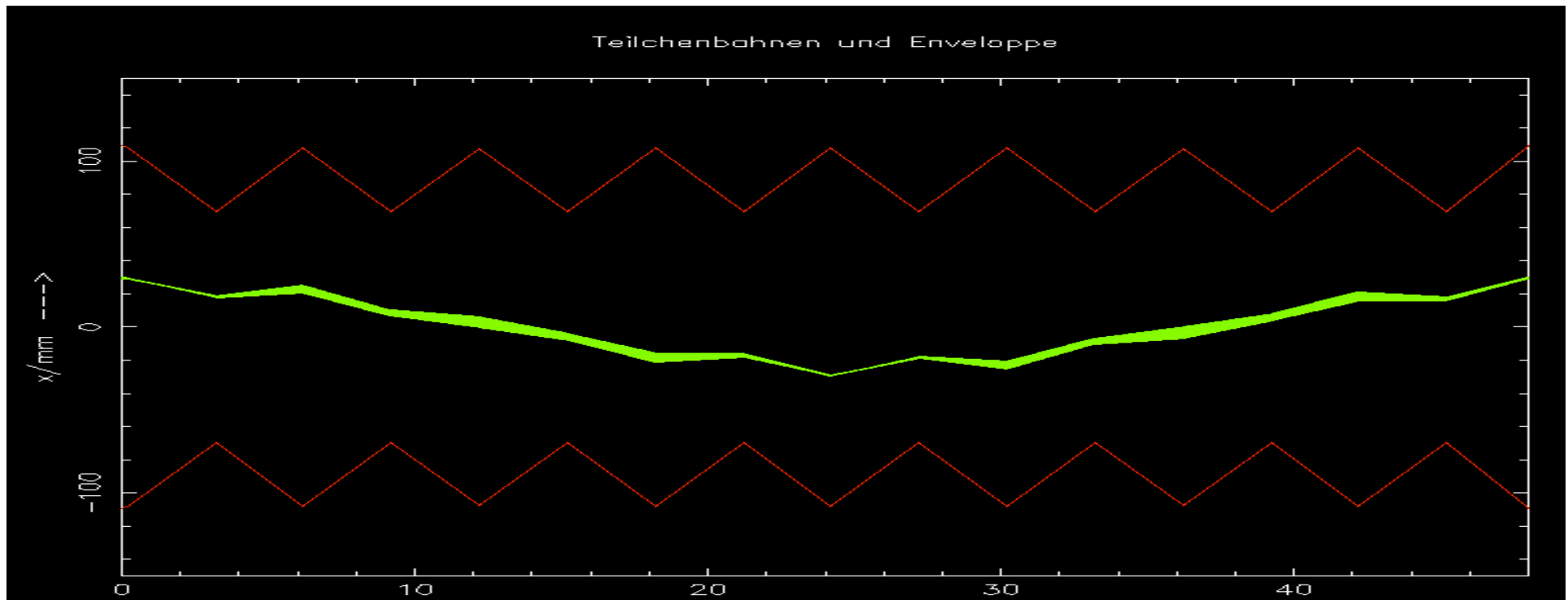
**Problem: Resonances**

$$x_{co}(s) = \frac{\sqrt{\beta(s)} * \int \frac{1}{\rho_{s1}} \sqrt{\beta_{s1}} * \cos(\psi_{s1} - \psi_s - \pi Q) ds}{2 \sin \pi Q}$$

Assume: Tune = integer     $Q = 1 \rightarrow 0$

Qualitatively spoken:

Integer tunes lead to a resonant increase of the closed orbit amplitude in presence of the smallest dipole field error.

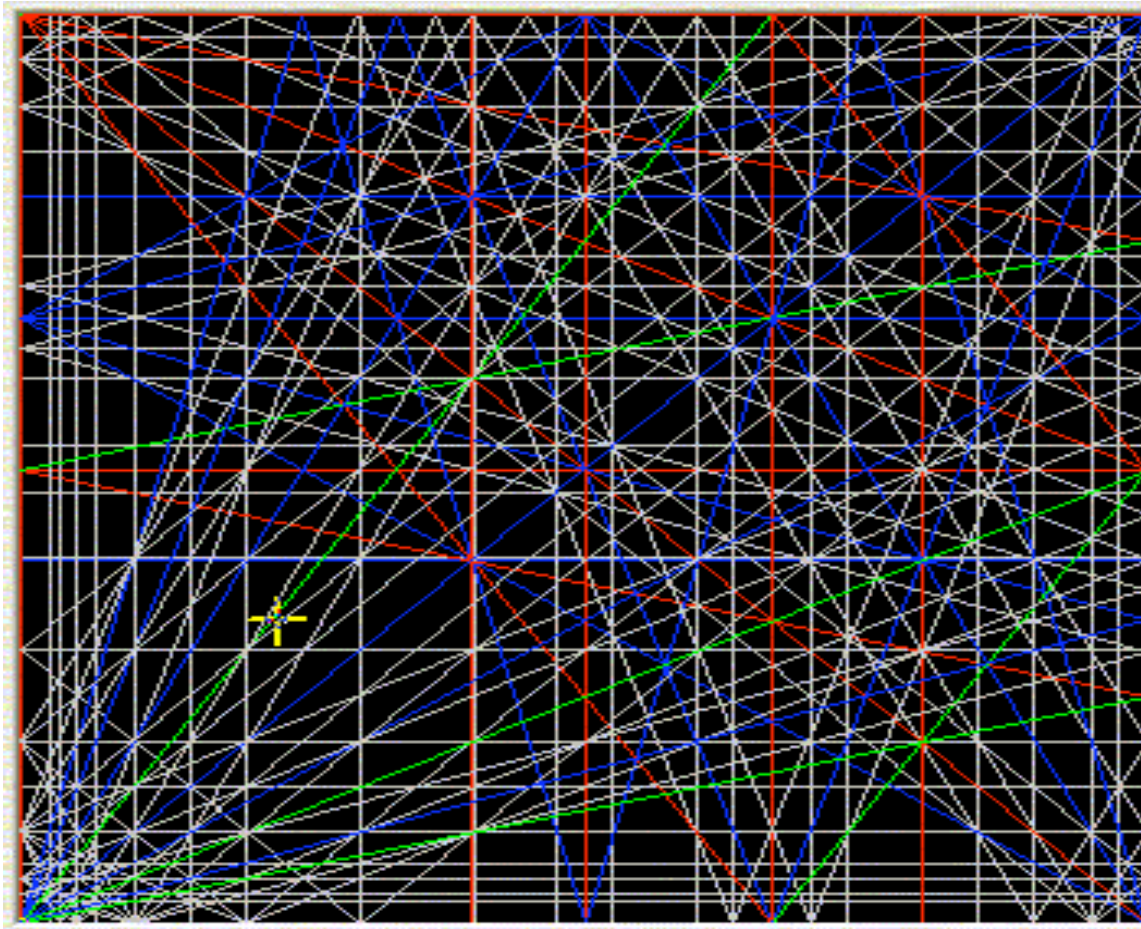




## *Tune and Resonances*

$$m*Q_x+n*Q_y+l*Q_s = \text{integer}$$

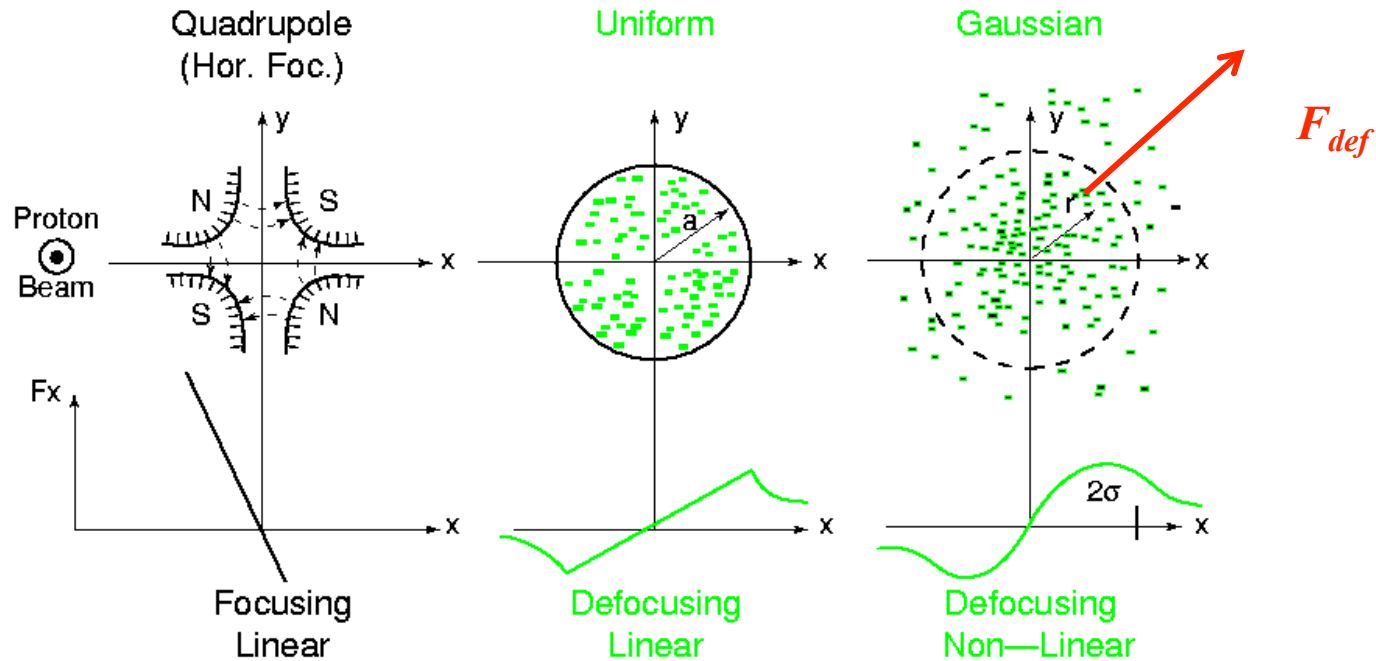
*Tune diagram up to 3rd order*



*... and up to 7th order*

*Homework for the operateurs:  
find a nice place for the tune  
where against all probability  
the beam will survive*

## II.) Golden Rule number two: *Never accelerate **charged** particles !*



*Transport line with quadrupoles*

$$x'' + K(s)x = 0$$

*Transport line with quadrupoles and **space charge***

$$x'' + (K(s) + K_{SC}(s))x = 0$$

$$x'' + \left( K(s) - \frac{2r_0 I}{ea^2 \beta^3 \gamma^3 c} \right) x = 0$$

$K_{SC}$

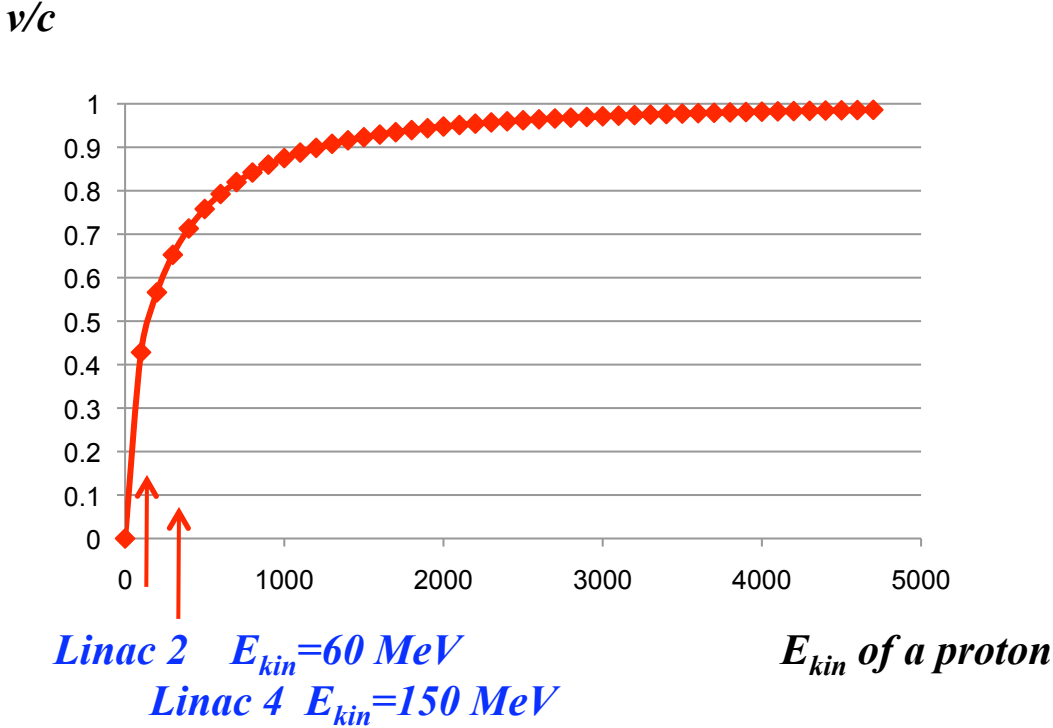
**Golden Rule number two:**

*Never accelerate **charged** particles !*

*Tune Shift due to Space Charge Effect  
Problem at low energies*

$$\Delta Q_{x,y} = -\frac{r_0 N}{2\pi\epsilon_{x,y} \beta \gamma^2}$$

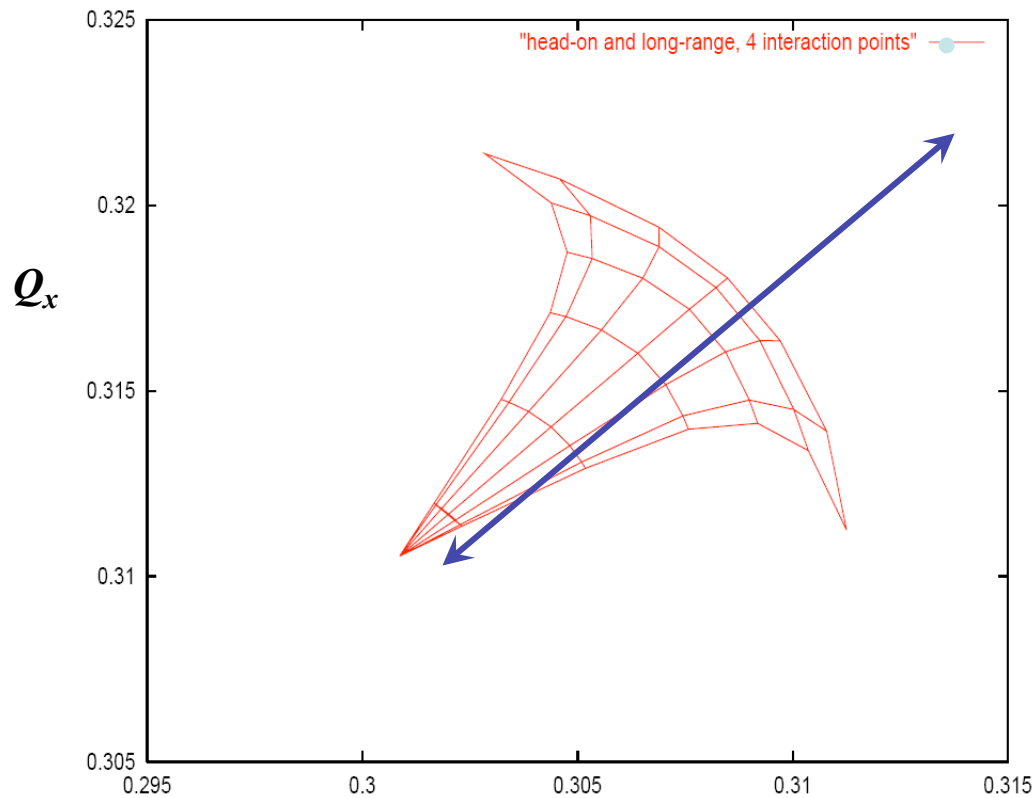
*... at low speed the particles  
repel each other*



### III.) Golden Rule number three:

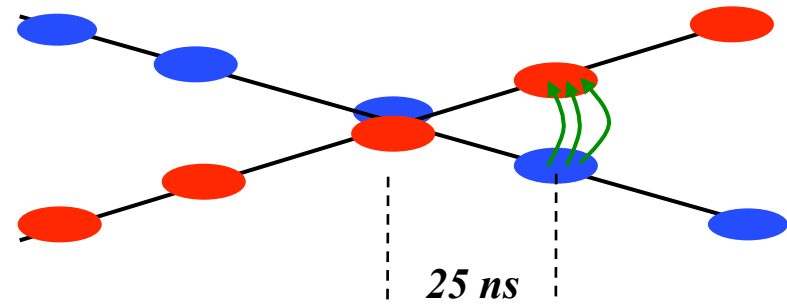
*Never Collide the Beams !*

*the colliding bunches influence each other  
 → change the focusing properties of the ring !!*



Courtesy W. Herr

$Q_x$

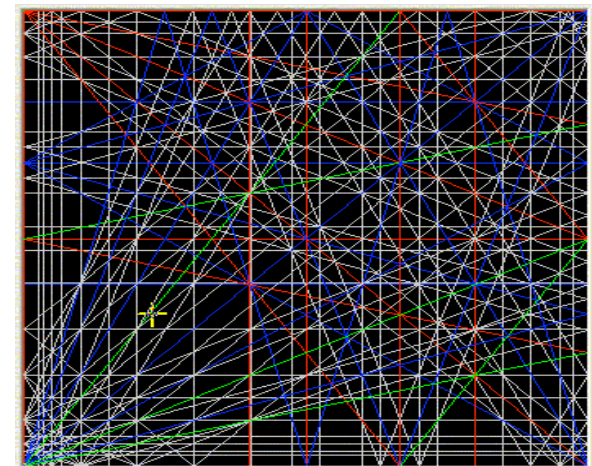


*most simple case:*

*linear beam beam tune shift*

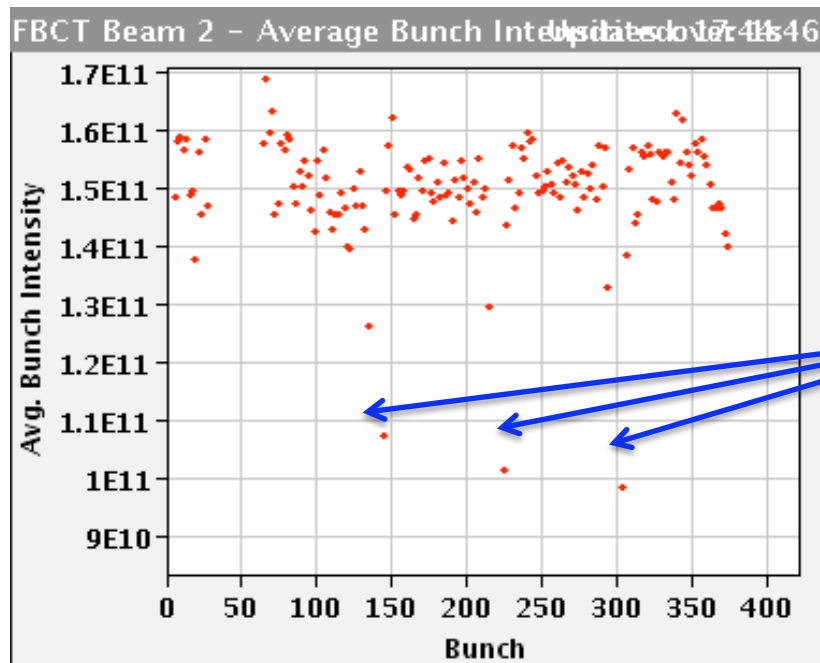
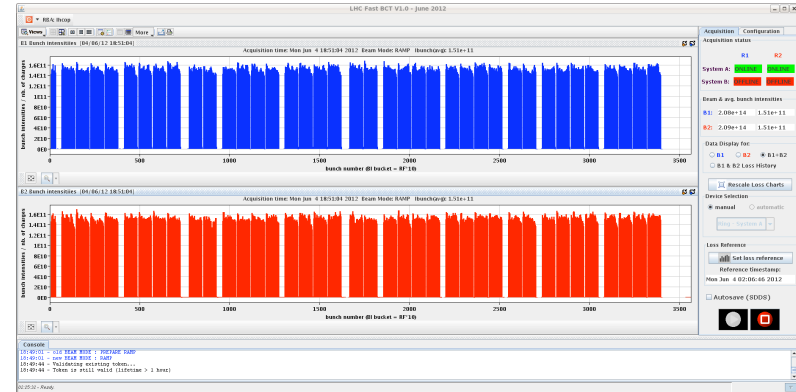
$$\Delta Q_x = \frac{\beta_x^* * r_p * N_p}{2\pi \gamma_p (\sigma_x + \sigma_y) * \sigma_x}$$

*and again the resonances !!!*



# LHC logbook: Sat 9-June "Late-Shift"

*18:18h injection for physics  
clean injection !*



*but particle losses when beams  
are brought into collision*

# IV.) Golden Rule Number 4: Never use Magnets

\*\*\*\*\*

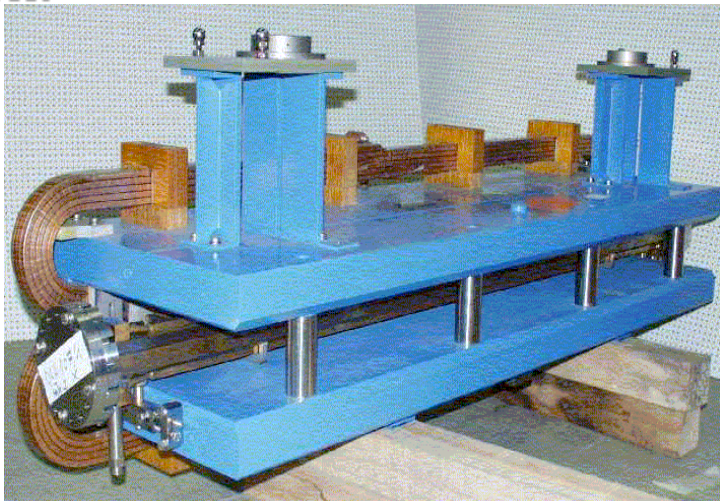
```

bn at injection
b1M_MQXCD_inj := 0.0000 ; b1U_MQXCD_inj :=
b2M_MQXCD_inj := 0.0000 ; b2U_MQXCD_inj :=
b3M_MQXCD_inj := 0.0000 ; b3U_MQXCD_inj :=
b4M_MQXCD_inj := 0.0000 ; b4U_MQXCD_inj :=
b5M_MQXCD_inj := 0.0000 ; b5U_MQXCD_inj :=
b6M_MQXCD_inj := 0.0000 ; b6U_MQXCD_inj :=
b7M_MQXCD_inj := 0.0000 ; b7U_MQXCD_inj :=
b8M_MQXCD_inj := 0.0000 ; b8U_MQXCD_inj :=
b9M_MQXCD_inj := 0.0000 ; b9U_MQXCD_inj :=
b10M_MQXCD_inj := 0.5000 ; b10U_MQXCD_inj :=
b11M_MQXCD_inj := 0.0000 ; b11U_MQXCD_inj :=
b12M_MQXCD_inj := 0.0000 ; b12U_MQXCD_inj :=
b13M_MQXCD_inj := 0.0000 ; b13U_MQXCD_inj :=
b14M_MQXCD_inj := -0.2700 ; b14U_MQXCD_inj := 0.0300 ; b14R_MQXCD_inj := 0.0100
b15M_MQXCD_inj := 0.0000 ; b15U_MQXCD_inj := 0.0000 ; b15R_MQXCD_inj := 0.0000
  
```

$$B_y + iB_x = B_{ref} * \sum_{n=1}^{\infty} (b_n + ia_n) \left( \frac{x + iy}{r_0} \right)^{n-1}$$

“effective magnetic length”

$$B * l_{eff} = \int_0^{l_{mag}} B ds$$

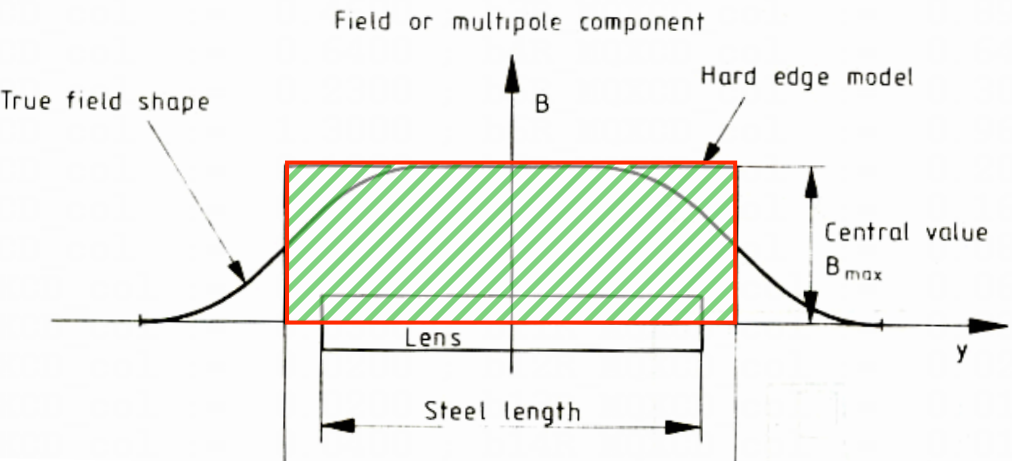
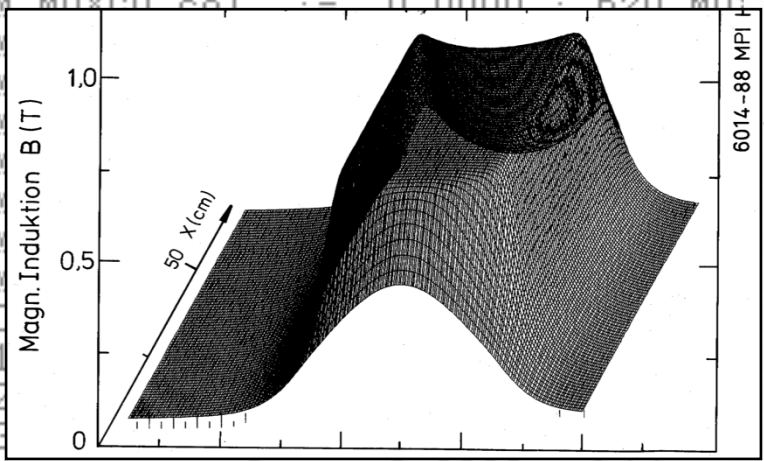


```

0000
0000
8900
6400
4600
2800
2100
1600
0800
0600
0300
0200
0100
0.0000 ; b15L_MQXCD_inj := 0.0100
0.0300 ; b14R_MQXCD_inj := 0.0100
0.0000 ; b15R_MQXCD_inj := 0.0000
  
```

```

bn in collision
b1M_MQXCD_col := 0.0000 ; b1U_MQXCD_col := 0.0000 ; b1R_MQXCD_col := 0.0000
b2M_MQXCD_col := 0.0000 ; b2U_MQXCD_col := 0.0000 ; b2R_MQXCD_col := 0.0000
b3M_MQXCD_col := 0.0000 ; b3U_MQXCD_col := 0.0000 ; b3R_MQXCD_col := 0.0000
b4M_MQXCD_col := 0.0000 ; b4U_MQXCD_col := 0.0000 ; b4R_MQXCD_col := 0.0000
b5M_MQXCD_col := 0.0000 ; b5U_MQXCD_col := 0.0000 ; b5R_MQXCD_col := 0.0000
b6M_MQXCD_col := 0.0000 ; b6U_MQXCD_col := 0.0000 ; b6R_MQXCD_col := 0.0000
b7M_MQXCD_col := 0.0000 ; b7U_MQXCD_col := 0.0000 ; b7R_MQXCD_col := 0.0000
b8M_MQXCD_col := 0.0000 ; b8U_MQXCD_col := 0.0000 ; b8R_MQXCD_col := 0.0000
b9M_MQXCD_col := 0.0000 ; b9U_MQXCD_col := 0.0000 ; b9R_MQXCD_col := 0.0000
b10M_MQXCD_col := 0.0000 ; b10U_MQXCD_col := 0.0000 ; b10R_MQXCD_col := 0.0000
b11M_MQXCD_col := 0.0000 ; b11U_MQXCD_col := 0.0000 ; b11R_MQXCD_col := 0.0000
b12M_MQXCD_col := 0.0000 ; b12U_MQXCD_col := 0.0000 ; b12R_MQXCD_col := 0.0000
b13M_MQXCD_col := 0.0000 ; b13U_MQXCD_col := 0.0000 ; b13R_MQXCD_col := 0.0000
b14M_MQXCD_col := 0.0000 ; b14U_MQXCD_col := 0.0000 ; b14R_MQXCD_col := 0.0000
b15M_MQXCD_col := 0.0000 ; b15U_MQXCD_col := 0.0000 ; b15R_MQXCD_col := 0.0000
  
```



```

b14M_MQXCD_col := 0.0000 ; b14U_MQXCD_col := 0.0000 ; b14R_MQXCD_col := 0.0000
b15M_MQXCD_col := 0.0000 ; b15U_MQXCD_col := 0.0000 ; b15R_MQXCD_col := 0.0000
  
```

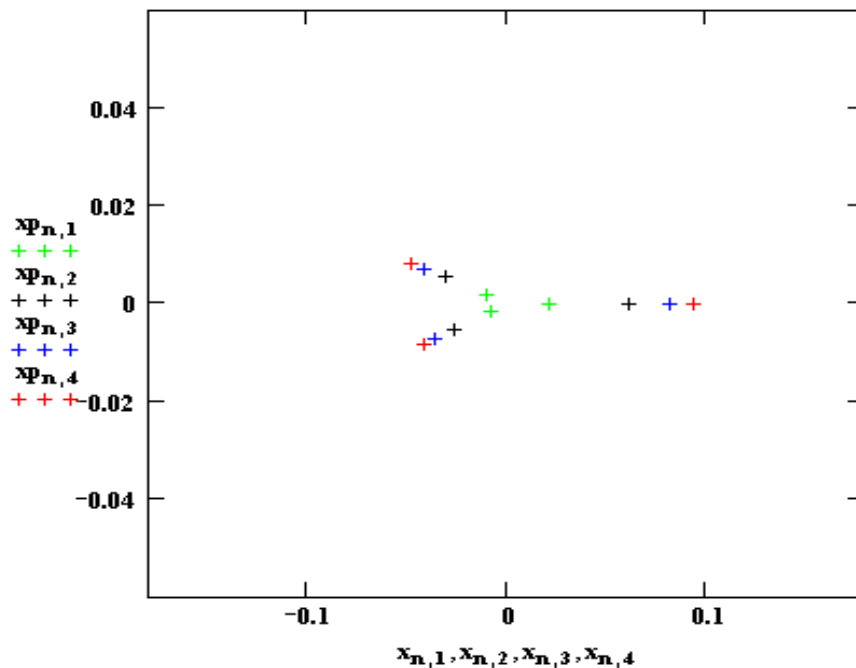
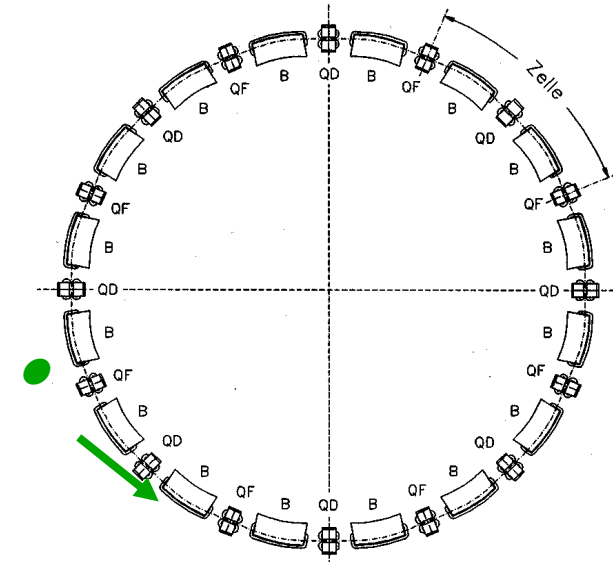
Clearly there is another problem ...

... if it were easy everybody could do it

Again: the phase space ellipse

for each turn write down - at a given position „s“ in the ring - the single particle amplitude  $x$

and the angle  $x'$  ... and plot it.  $\begin{pmatrix} x \\ x' \end{pmatrix}_{s1} = M_{turn} * \begin{pmatrix} x \\ x' \end{pmatrix}_{s0}$



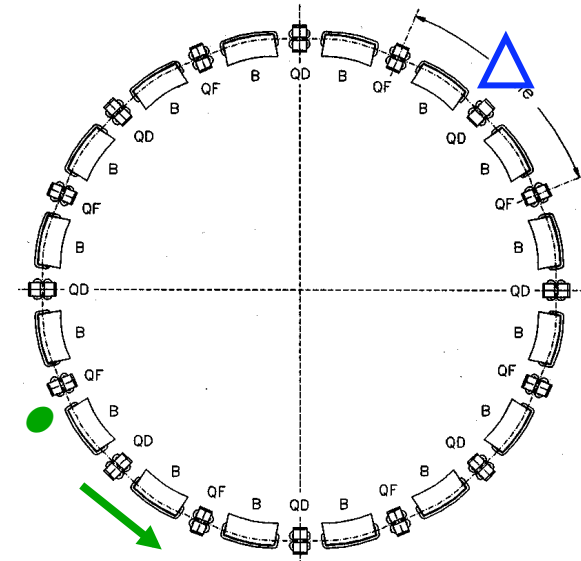
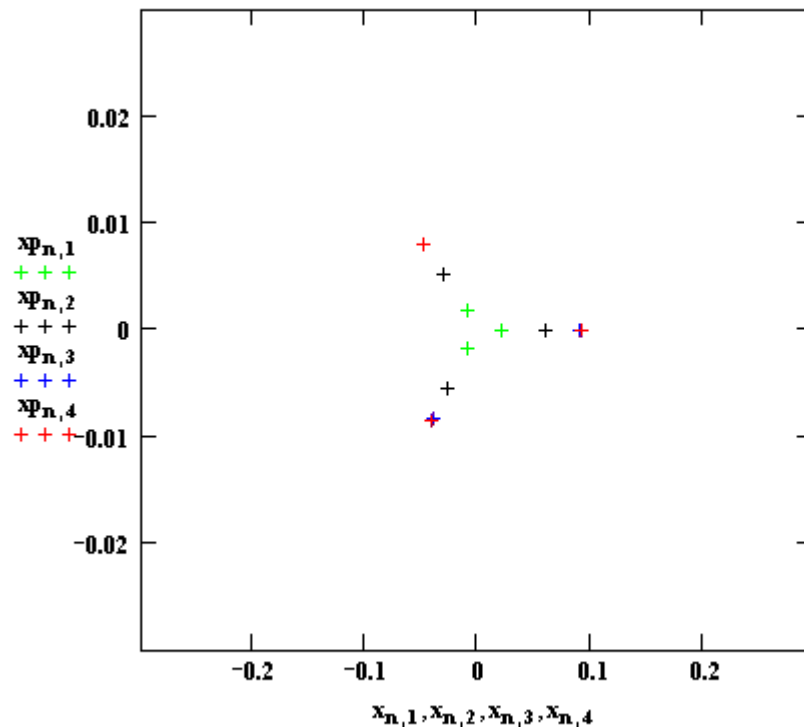
A beam of 4 particles

– each having a slightly different emittance:

## Installation of a weak ( !!! ) sextupole magnet

The good news: sextupole fields in accelerators cannot be treated analytically anymore.

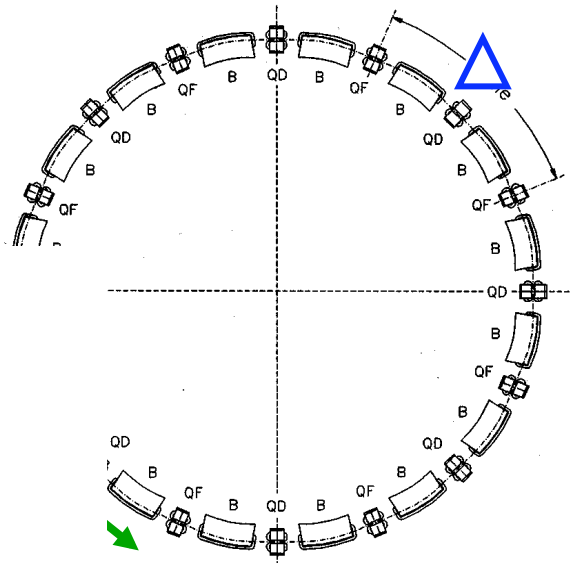
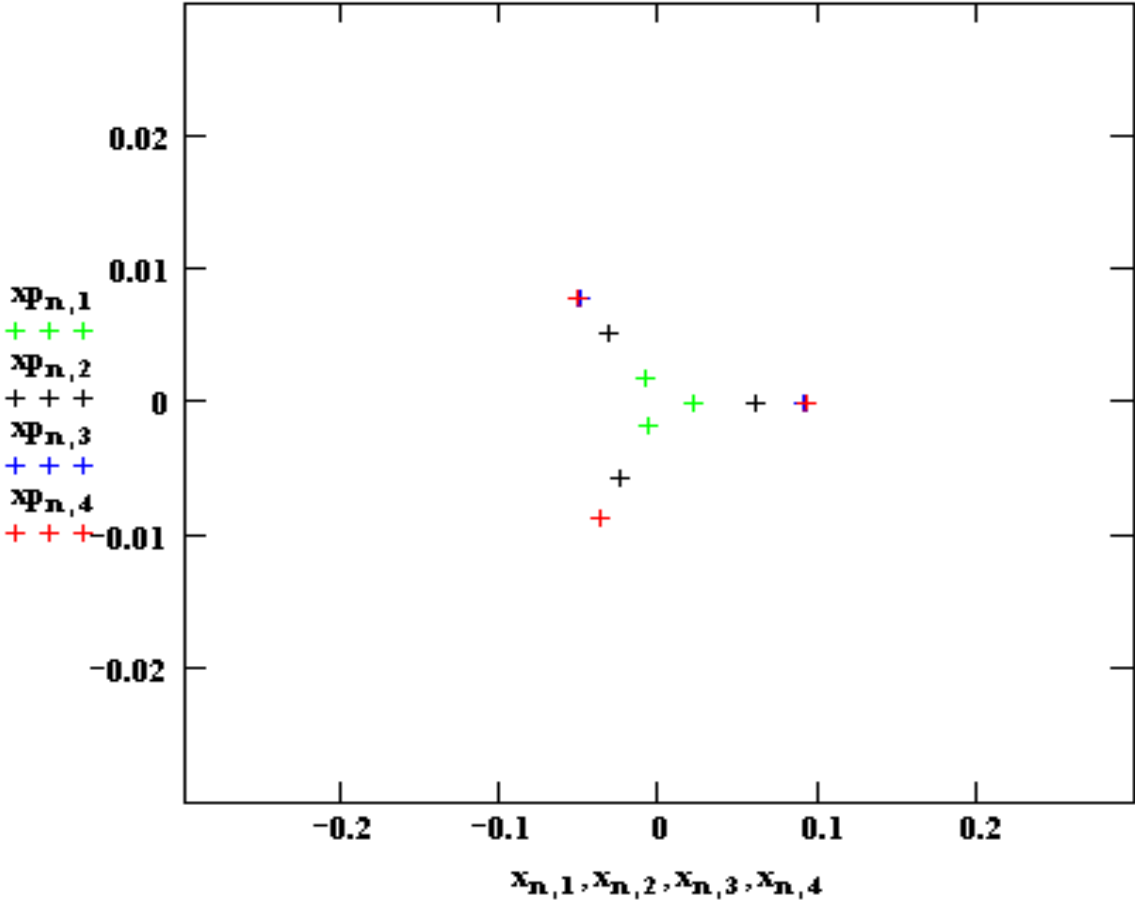
→ no equations; instead: Computer simulation  
„ particle tracking “





# Effect of a strong ( !!! ) Sextupole ...

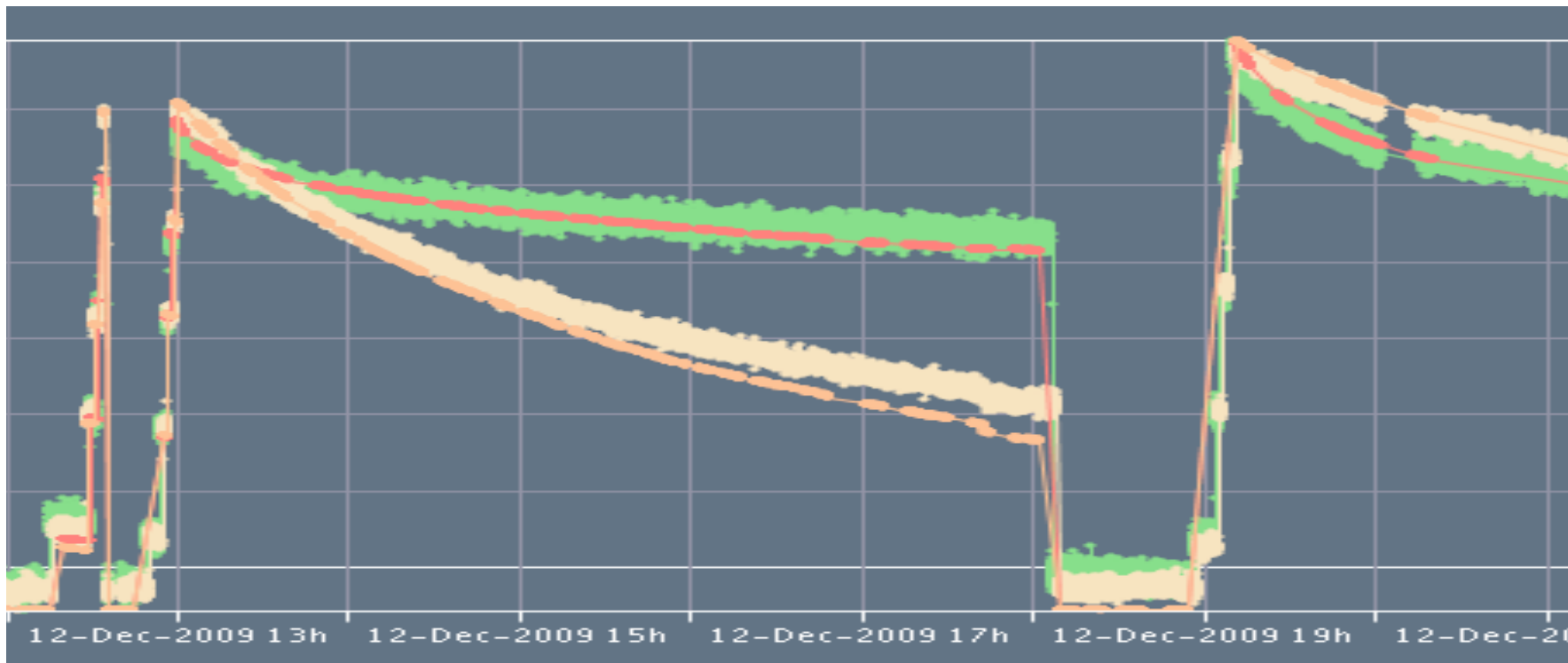
→ Catastrophy !



„dynamic aperture“

***Golden Rule XXL: COURAGE***

*and with a lot of effort from Bachelor / Master / Diploma / PhD  
and **Summer-Students** the machine is running !!!*



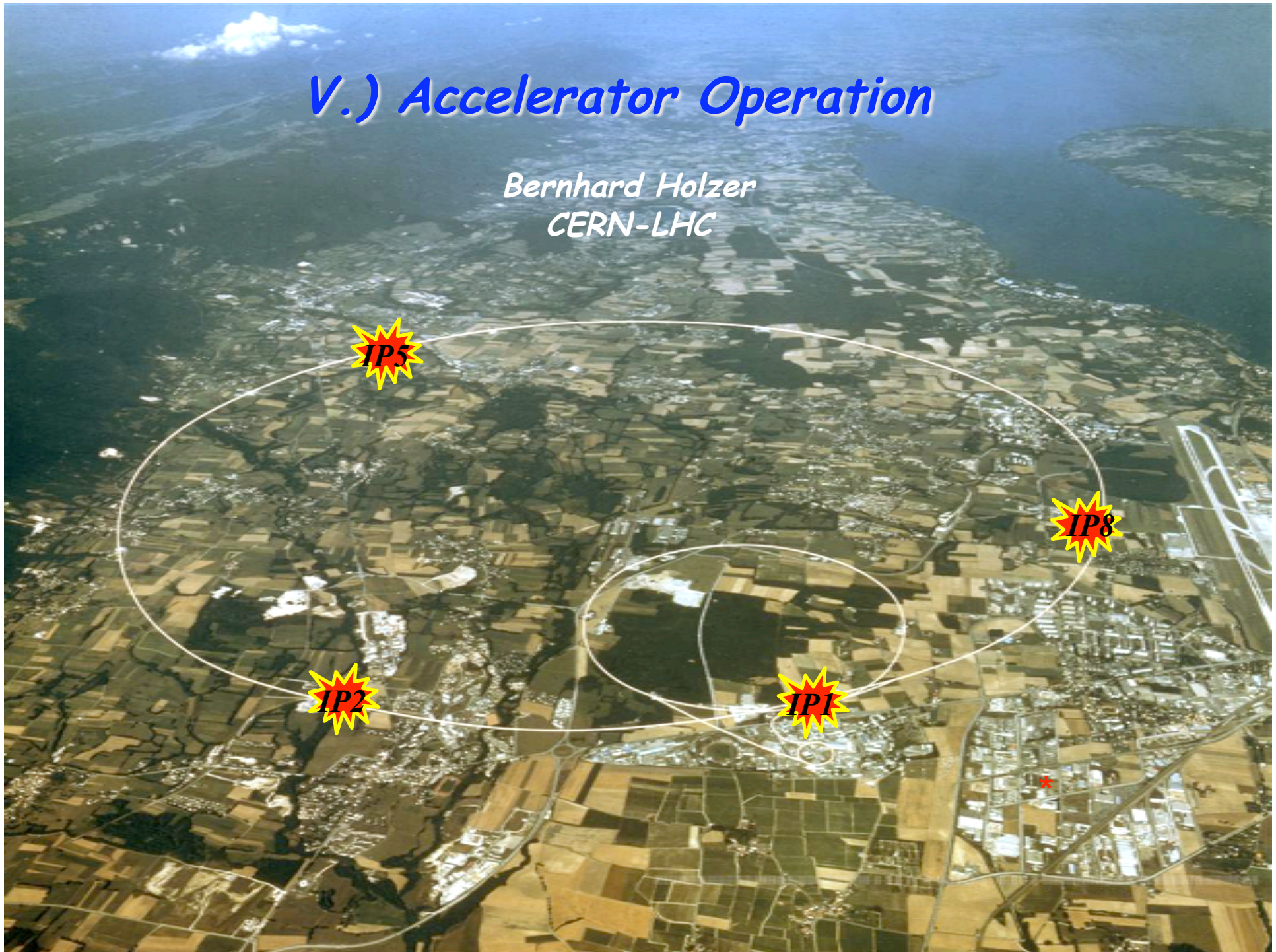
*thank'x for your help and have a lot of fun*

## *Bibliography:*

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Oxford Press, 2001*
- 2.) *Klaus Wille: Physics of Particle Accelerators and Synchrotron  
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- 3.) *Peter Schmüser: Basic Course on Accelerator Optics, CERN Acc.  
School: 5<sup>th</sup> general acc. phys. course CERN 94-01*
- 4.) *Bernhard Holzer: Lattice Design, CERN Acc. School: Interm. Acc. phys course,  
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- 5.) *Herni Bruck: Accelérateurs Circulaires des Particules,  
presse Universitaires de France, Paris 1966 (english / francais)*
- 6.) *M.S. Livingston, J.P. Blewett: Particle Accelerators,  
Mc Graw-Hill, New York, 1962*
- 7.) *Frank Hinterberger: Physik der Teilchenbeschleuniger, Springer Verlag 1997*
- 8.) *Mathew Sands: The Physics of  $e^+ e^-$  Storage Rings, SLAC report 121, 1970*
- 9.) *D. Edwards, M. Syphers : An Introduction to the Physics of Particle  
Accelerators, SSC Lab 1990*

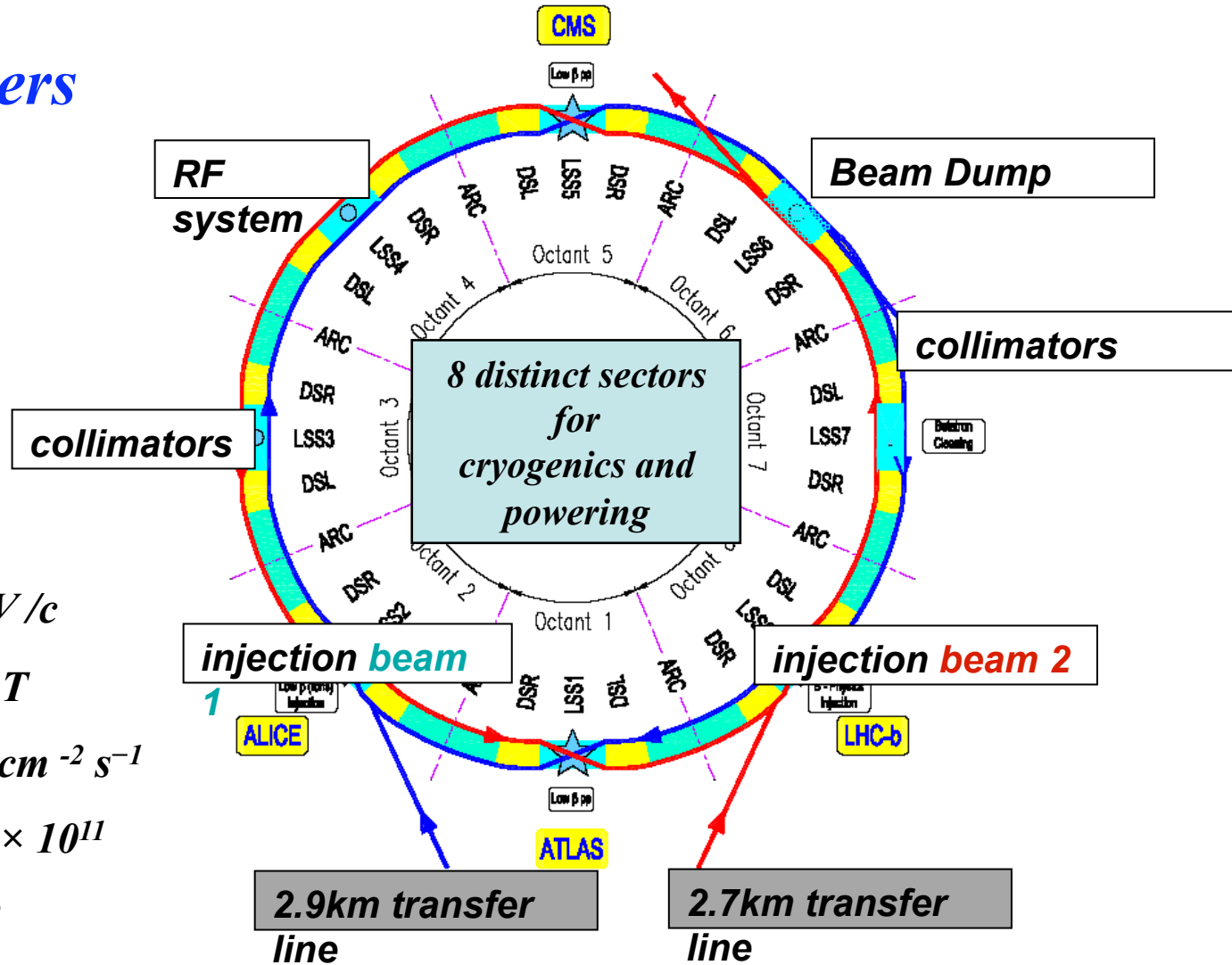
# V.) Accelerator Operation

Bernhard Holzer  
CERN-LHC



# LHC Main Parameters

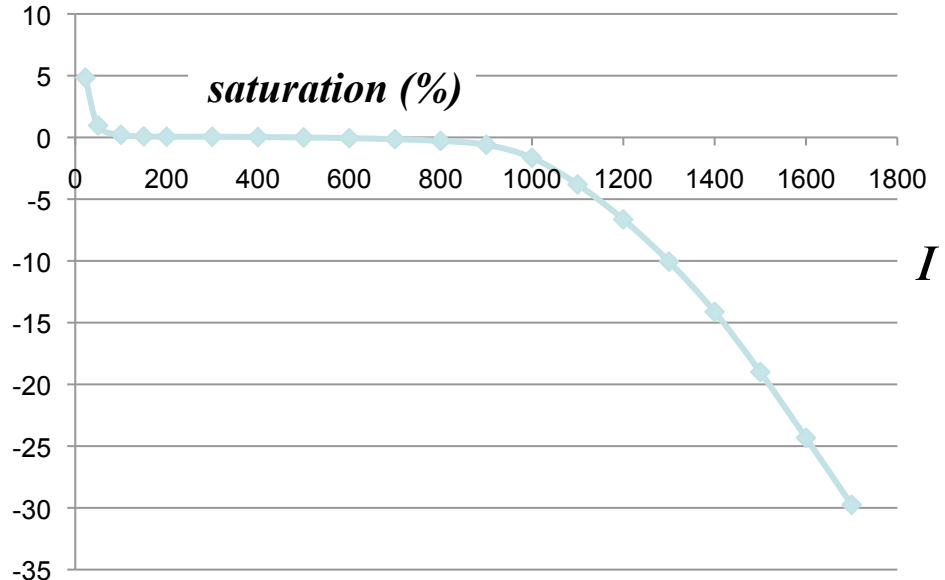
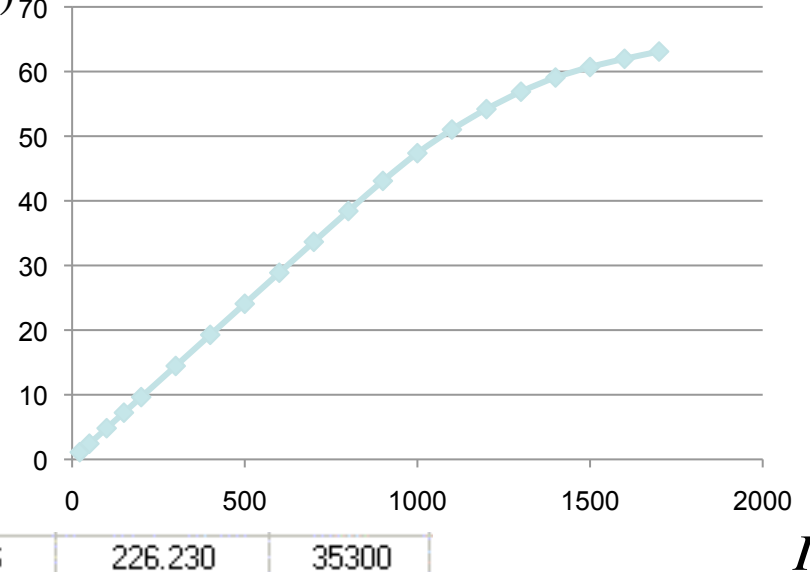
<i>Momentum at collision</i>	<i>7 TeV /c</i>
<i>Dipole field for 7 TeV</i>	<i>8.33 T</i>
<i>Luminosity</i>	<i><math>10^{34} \text{ cm}^{-2} \text{ s}^{-1}</math></i>
<i>Protons per bunch</i>	<i><math>1.15 \times 10^{11}</math></i>
<i>Number of bunches/beam</i>	<i>2808</i>
<i>Nominal bunch spacing</i>	<i>25 ns</i>
<i>Normalized emittance</i>	<i><math>3.75 \mu\text{m}</math></i>
<i>rms beam size (7TeV, arc)</i>	<i><math>300 \mu\text{m}</math></i>
<i>beam pipe diameter</i>	<i>56 mm</i>



# Magnet Currents

$$\int gdl(I)$$

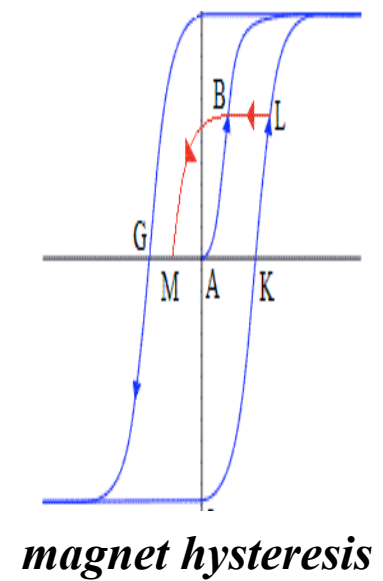
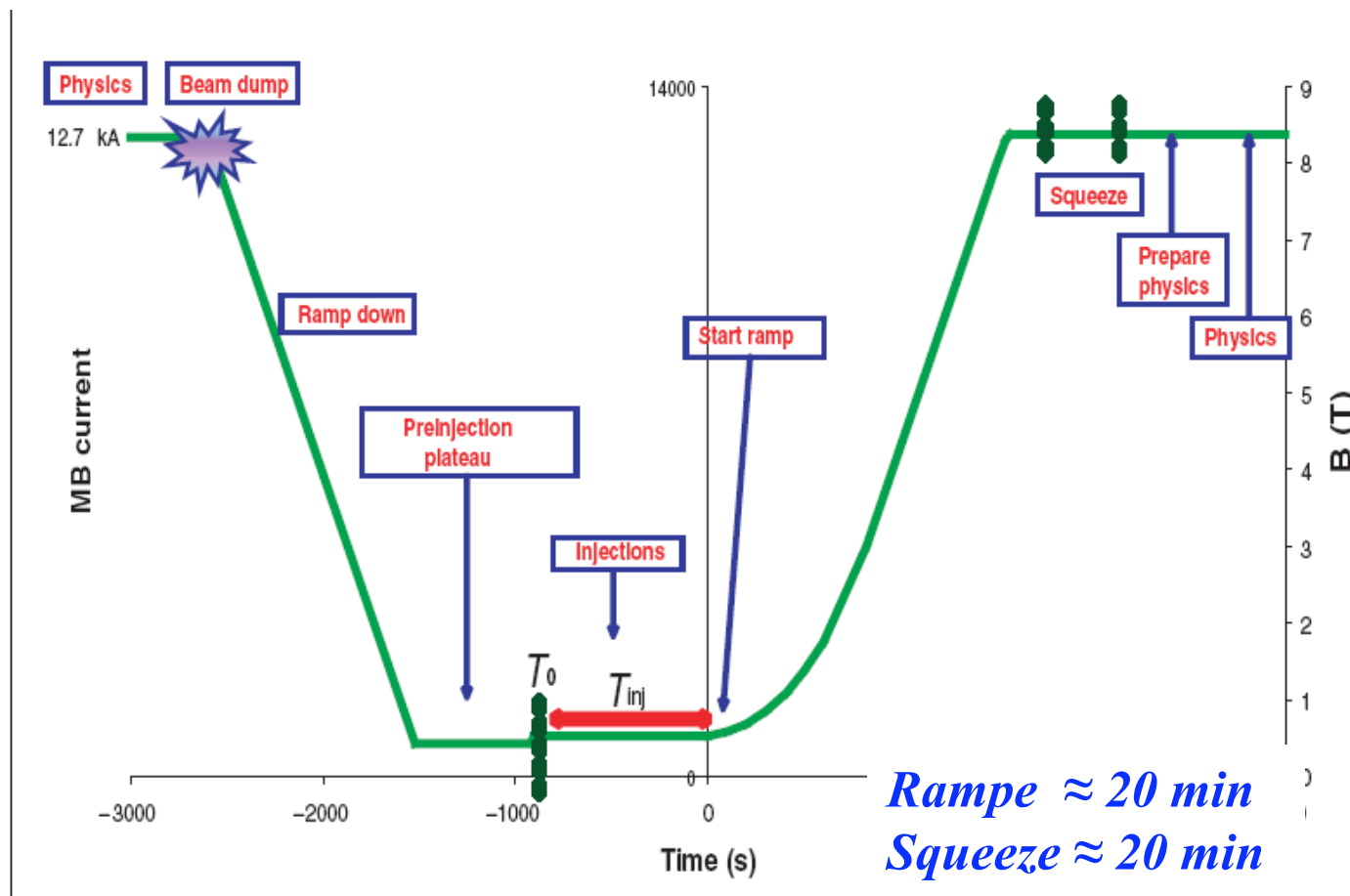
Nummer	Gruppe	Name	aktiv	Sollwerte File1 [A]	Sollwert [A]		
1	HPDIPOL	BPA1	True	4138.993	5646		
2	HPMAINW	QZ51 WL	True	235.462	326.		
3	HPMAINW	QR52 WR	True	258.724	377.		
4	HPMAINW	QC53 WL	True	237.933	327.		
5	HPMAINW	QB28 WL	True	625.429	849.		
6	HPMAINW	QR54 WR	True	291.486	405.		
7	HPMAINW	QR24 WR	True	139.139	185.		
8	HPMAINW	QR50 WL	True	305.348	419.		
9	HPMAINW	QC22 WR	True	75.816	302.046	226.230	35300
10	HPMAINW	QR57 WL	True	260.769	354.833	94.064	12329
11	HPMAINW	QR56 WR	True	190.123	263.722	73.599	11484
12	HPMAINW	QC20 WR	True	91.056	-13.587	-104.643	-16328
13	HPMAINW	QP58 WR	True	-5.517	19.		
14	HPMAINW	QP59 WL	True	-10.401	-11.		
15	HPMAINW	QP60 WR	True	73.600	98.		
16	HPMAINW	QP61 WL	True	69.504	90.		
17	HPMAINW	QP62 WR	True	40.163	58.		
18	HPMAINW	QP63 WL	True	47.489	63.		
19	HPMAINW	QP64 WR	True	-47.780	-71.		



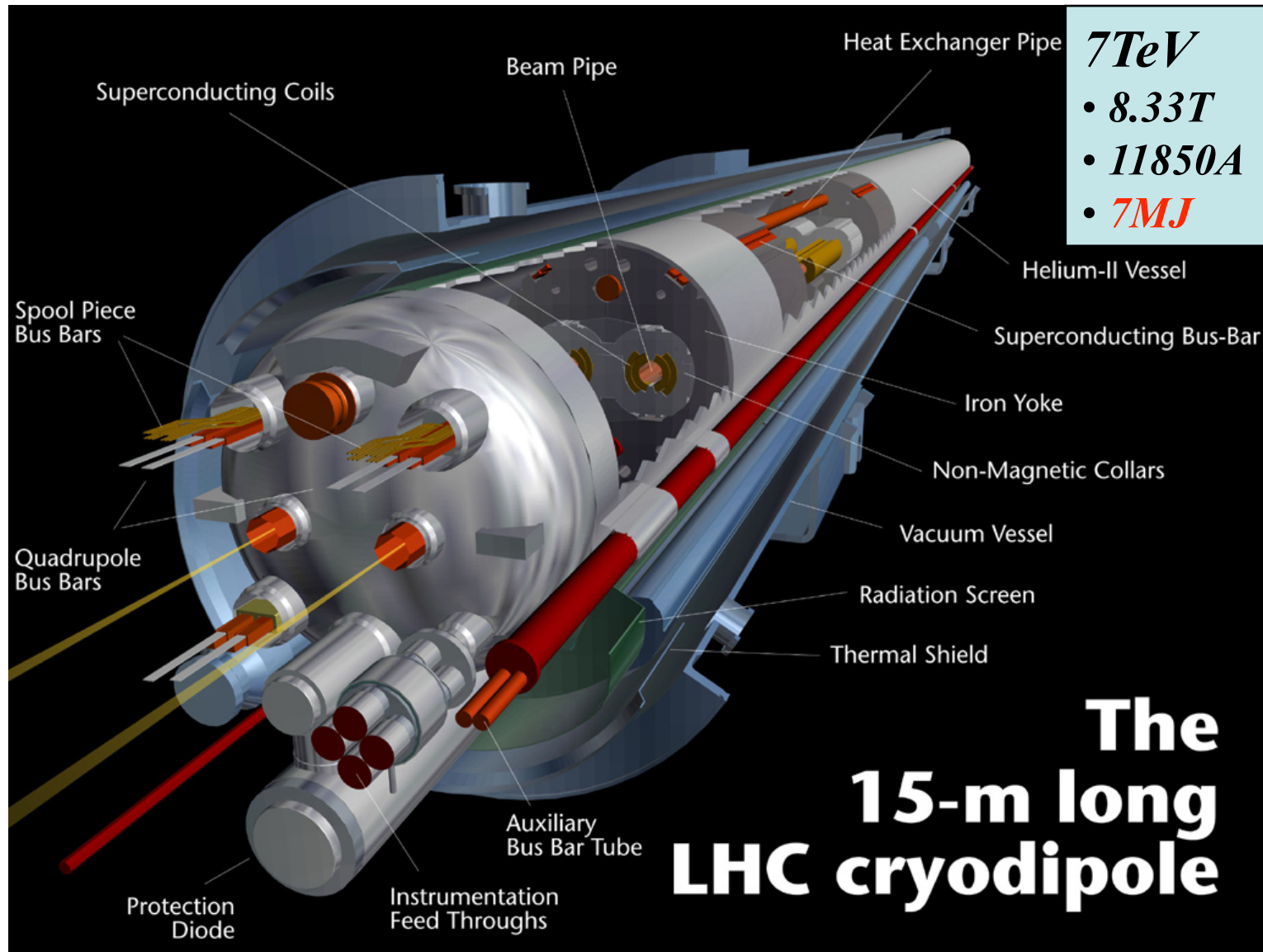
remember:  $\Delta B/B \approx 10^{-4}$

# LHC Operation: Magnet Preparation Cycle & Ramp

*8 independent sectors, hysteresis effects, saturation & remanence in nc and sc magnets, synchronisation of the power converters, magnet model to describe the transfer functions of every element*



# *LHC dipoles (1232 of them)*

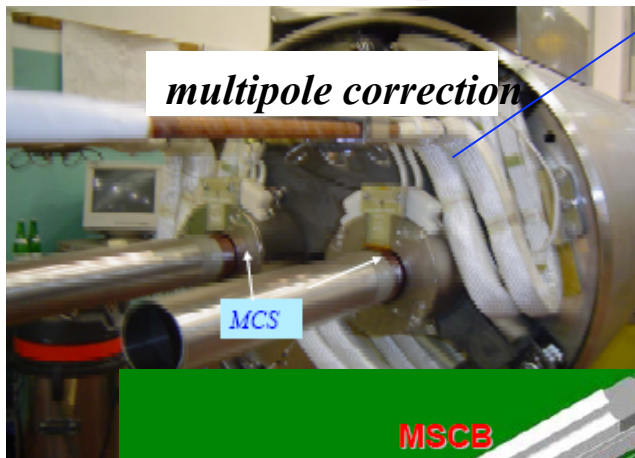
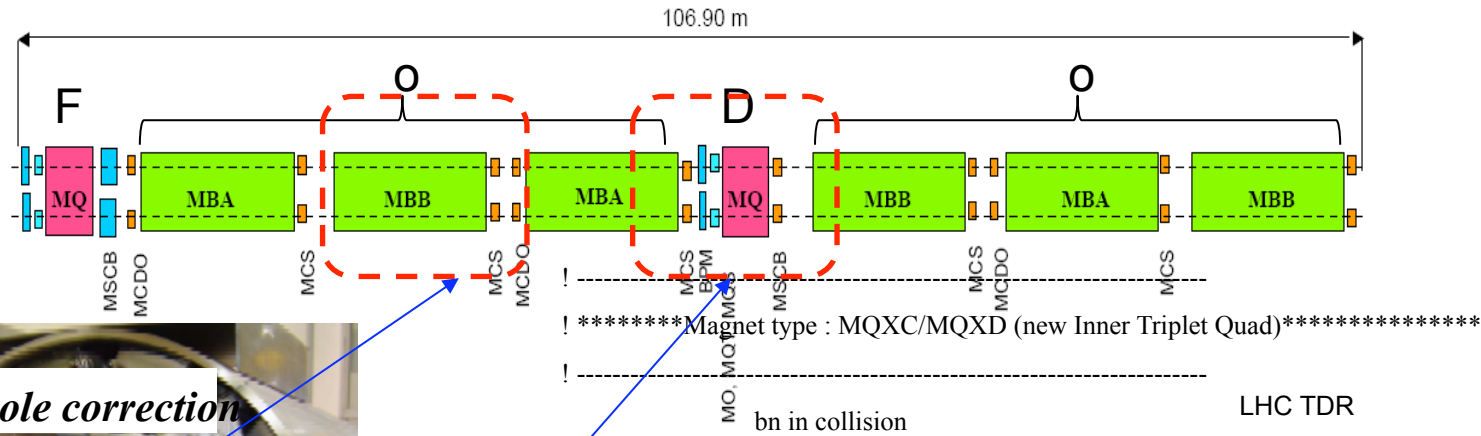




# LHC: Basic Layout of the Machine

## multipole corrector magnets

2, 6, 8, 10, 12 pol  
skew & trim quad, chroma 6pol  
landau 8 pole



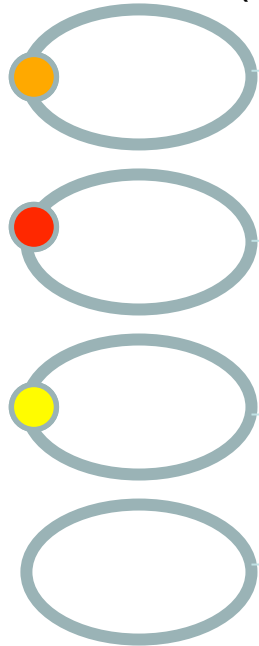
- b1M\_MQXCD\_col := 0.0000 ; b1U\_MQXCD\_col := 0.0000 ; b1R\_MQXCD\_col := 0.0000 ;
- b2M\_MQXCD\_col := 0.0000 ; b2U\_MQXCD\_col := 0.0000 ; b2R\_MQXCD\_col := 0.0000 ;
- b3M\_MQXCD\_col := 0.0000 ; b3U\_MQXCD\_col := 0.4600 ; b3R\_MQXCD\_col := 0.8900 ;
- b4M\_MQXCD\_col := 0.0000 ; b4U\_MQXCD\_col := 0.6400 ; b4R\_MQXCD\_col := 0.6400 ;
- b5M\_MQXCD\_col := 0.0000 ; b5U\_MQXCD\_col := 0.4600 ; b5R\_MQXCD\_col := 0.4600 ;
- b6M\_MQXCD\_col := 0.0000 ; b6U\_MQXCD\_col := 1.7700 ; b6R\_MQXCD\_col := 1.2800 ;
- b7M\_MQXCD\_col := 0.0000 ; b7U\_MQXCD\_col := 0.2100 ; b7R\_MQXCD\_col := 0.2100 ;
- b8M\_MQXCD\_col := 0.0000 ; b8U\_MQXCD\_col := 0.1600 ; b8R\_MQXCD\_col := 0.1600 ;
- b9M\_MQXCD\_col := 0.0000 ; b9U\_MQXCD\_col := 0.0800 ; b9R\_MQXCD\_col := 0.0800 ;
- b10M\_MQXCD\_col := 0.0000 ; b10U\_MQXCD\_col := 0.2000 ; b10R\_MQXCD\_col := 0.0600 ;
- b11M\_MQXCD\_col := 0.0000 ; b11U\_MQXCD\_col := 0.0300 ; b11R\_MQXCD\_col := 0.0300 ;
- b12M\_MQXCD\_col := 0.0000 ; b12U\_MQXCD\_col := 0.0200 ; b12R\_MQXCD\_col := 0.0200 ;
- b13M\_MQXCD\_col := 0.0000 ; b13U\_MQXCD\_col := 0.0200 ; b13R\_MQXCD\_col := 0.0100 ;
- b14M\_MQXCD\_col := 0.0000 ; b14U\_MQXCD\_col := 0.0400 ; b14R\_MQXCD\_col := 0.0100 ;
- b15M\_MQXCD\_col := 0.0000 ; b15U\_MQXCD\_col := 0.0000 ; b15R\_MQXCD\_col := 0.0000 ;

**MB:** main dipole  
**MQ:** main quadrupole  
**MQT:** Trim quadrupole  
**MQS:** Skew trim quadrupole  
**MO:** Lattice octupole (Landau damping)  
**MSCB:** Normal & Skew sextupole  
**Orbit corrector dipoles**  
**MCS:** Spool piece sextupole  
**MCDO:** Spool piece 8 / 10 pole  
**BPM:** Beam position monitor + diagnostics

# LHC Operation: Pre-Accelerators and Injection

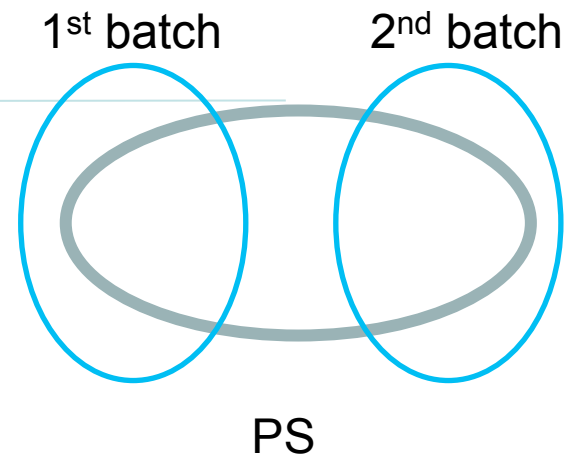
BOOSTER (1.4 GeV) → PS (26 GeV) → SPS (450 GeV) → LHC

BOOSTER (4 rings)



$h=1$

13/01/2010

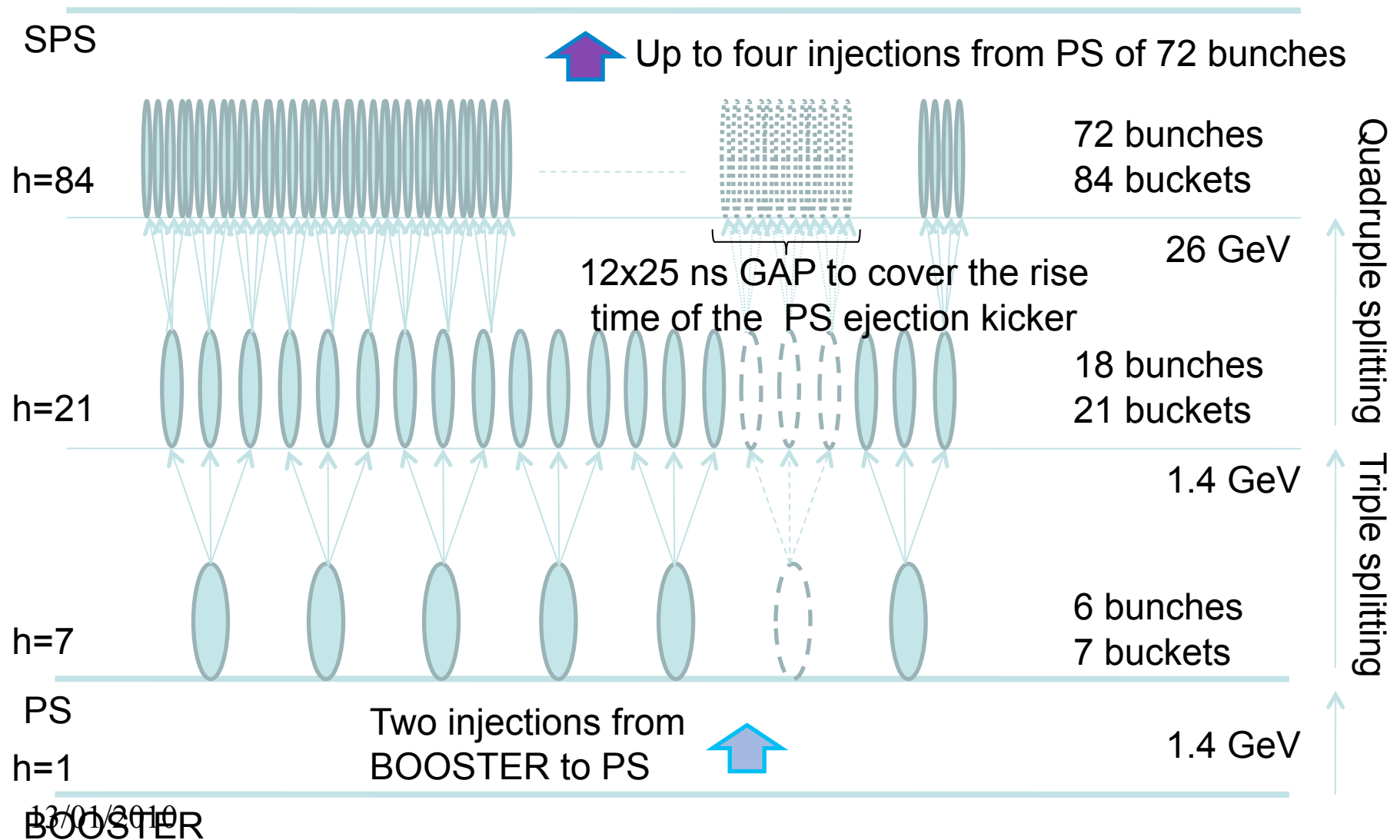


Two injections from  
BOOSTER to PS

$h=7$  (6 buckets filled +  
1 empty)

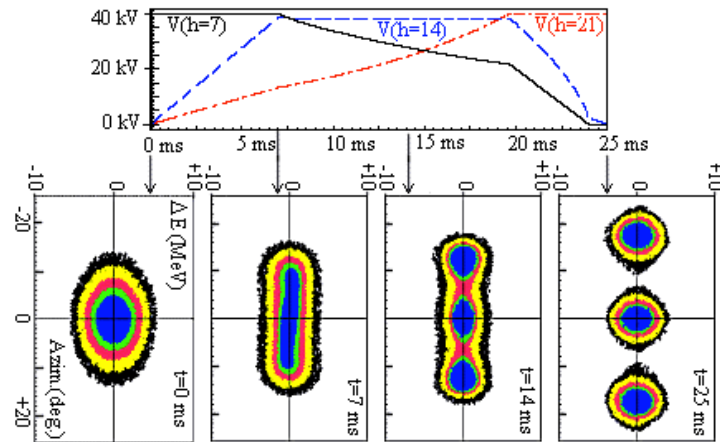
*court. R. Alemany*

# LHC Injection: Preparing the Bunch Trains



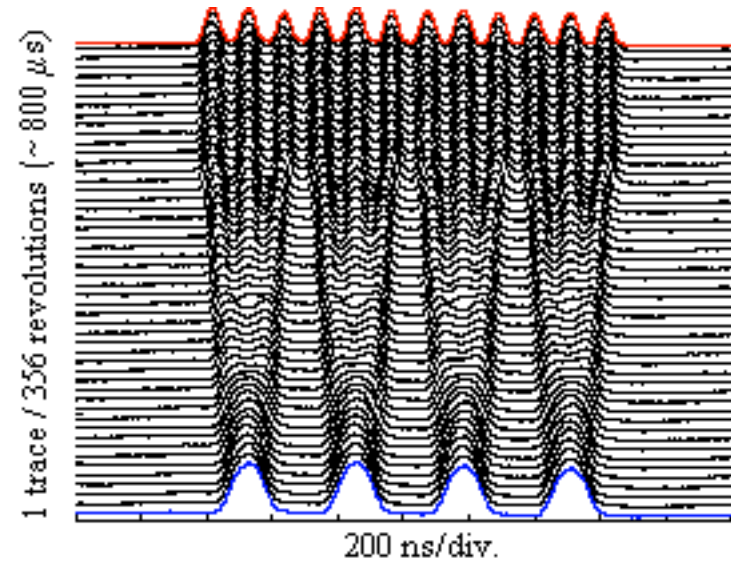
# Beam Injection

## Bunch Splitting in the PS

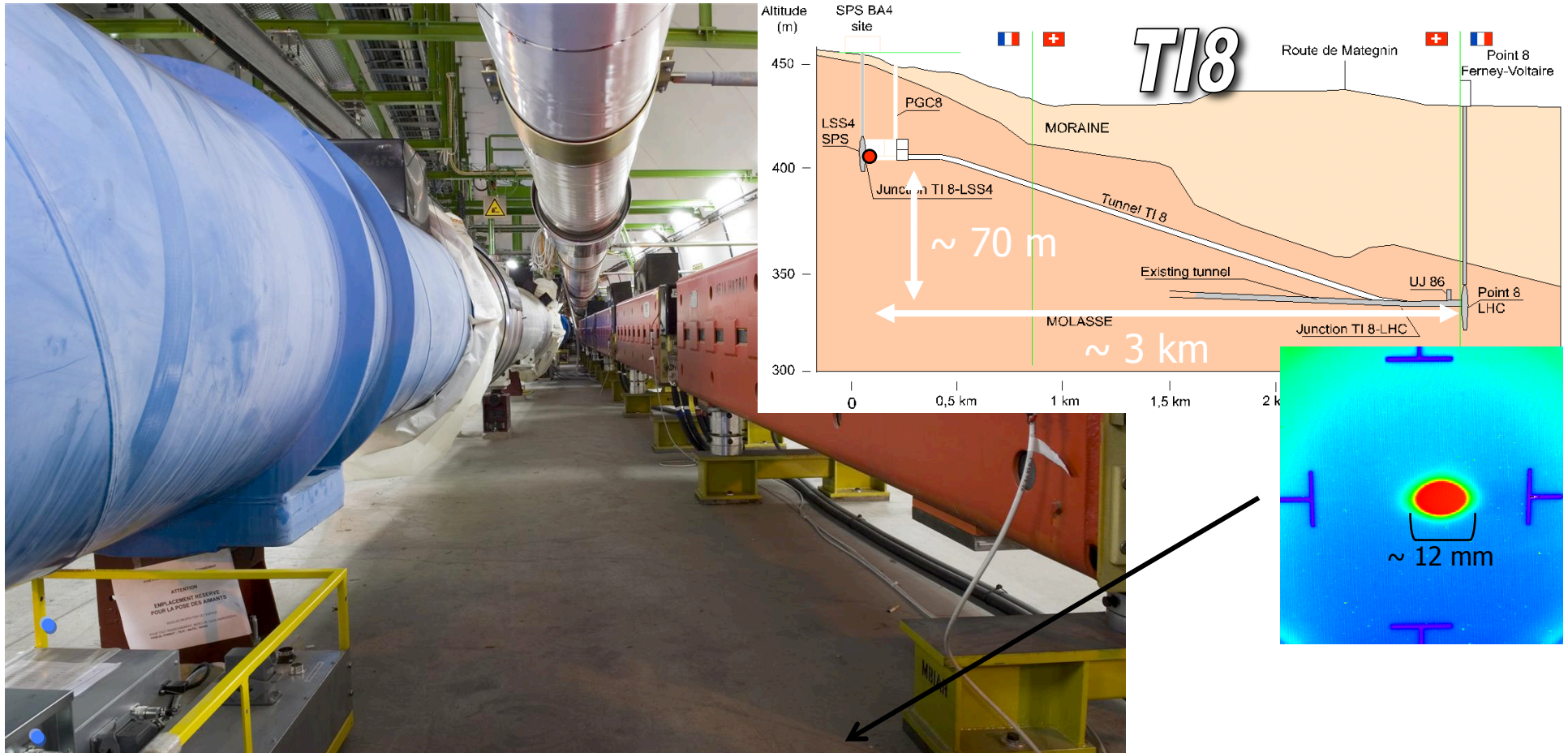


**CERN: Linac 2 injection into PSB**

$$N_p \approx 1.5 \cdot 10^{13} \text{ protons per bunch, } E_{inj} = 50 \text{ MeV}$$
$$\beta = 0.31$$
$$\gamma = 1.05$$



# Injection mechanism: the transfer lines



13/01/2010

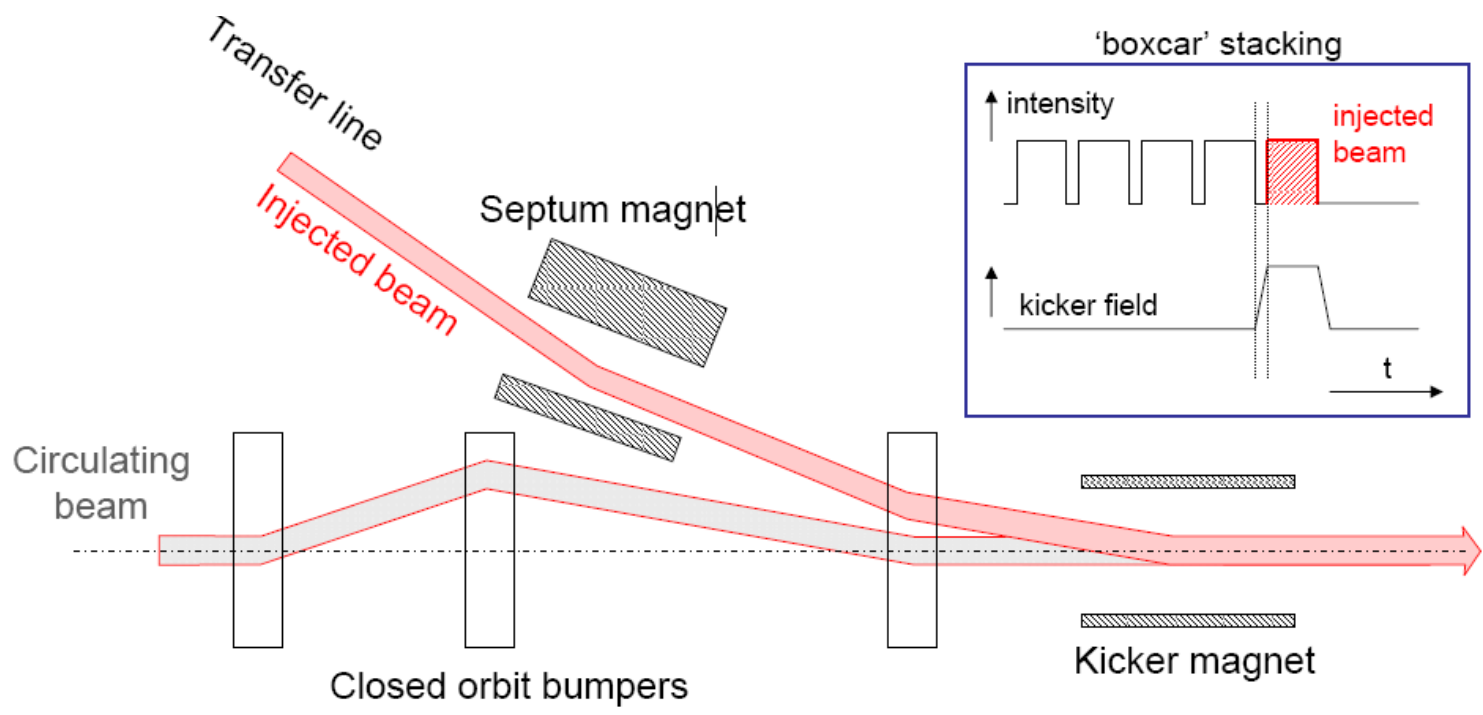
*court. R. Alemany*

# Injection schemes:

- Standard Proton Beam ... single turn Injection
- Electron Beam ..... "off axis" Injection
- Ion Beam ..... "multi turn" injection

## Single Turn Injection

Example: LHC, HERA-P



## Transferlines & Injection: Errors & Tolerances

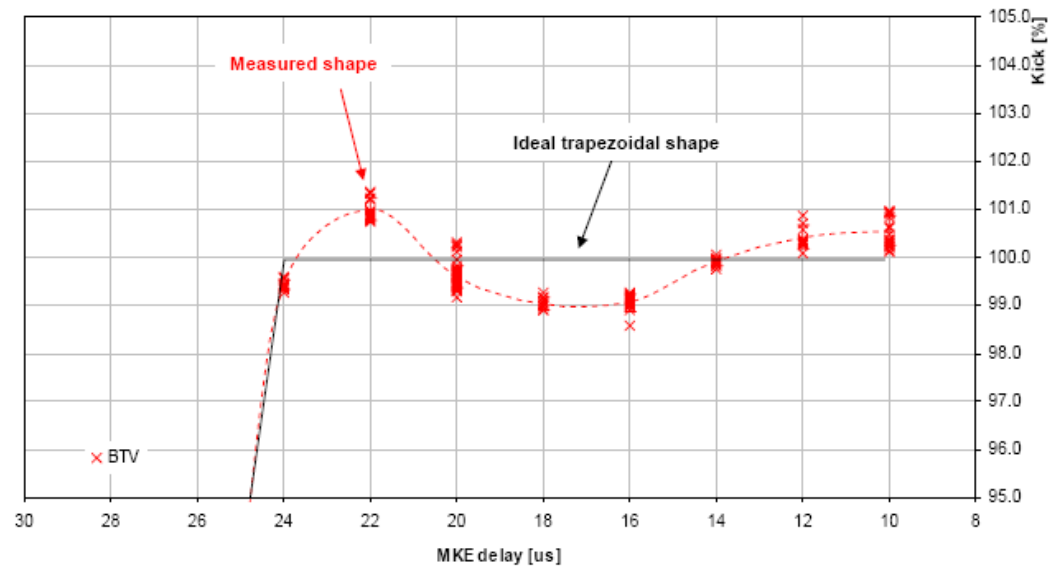
- \* *quadrupole strengths* --> "beta beat"  $\Delta\beta / \beta$
- \* *alignment of magnets* --> orbit distortion in transferline & storage ring
- \* *septum & kicker pulses* --> orbit distortion & emittance dilution in storage ring

*Example: Error in position  $\Delta a$ :*

$$\varepsilon_{new} = \varepsilon_0 * \left(1 + \frac{\Delta a^2}{2}\right)$$

$$\Delta a = 0.5 \sigma$$

$$\rightarrow \varepsilon_{new} = 1.125 * \varepsilon_0$$



*Kicker "plateau" at the end of the PS - SPS transferline measured via injection - oscillations*

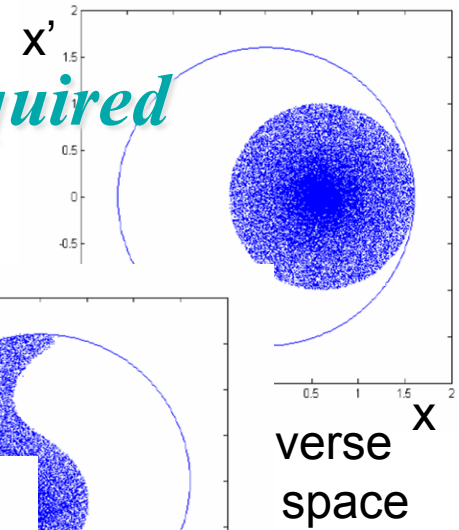
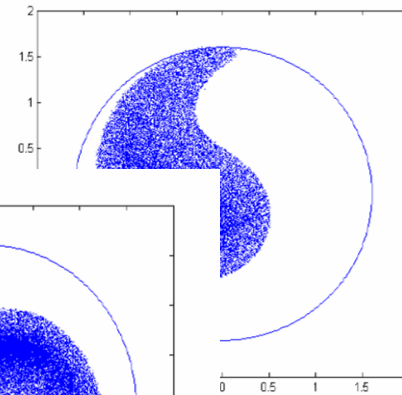
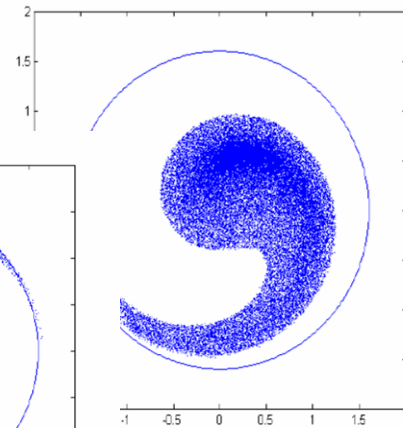
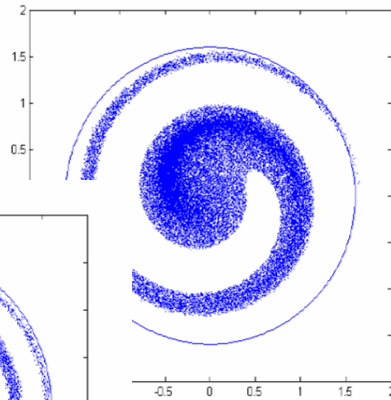
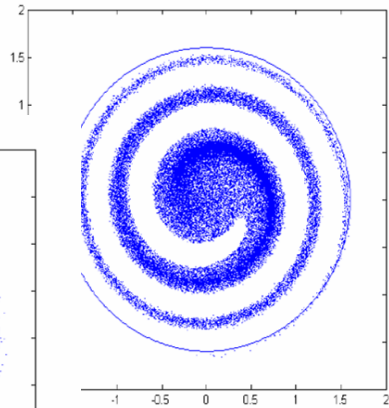
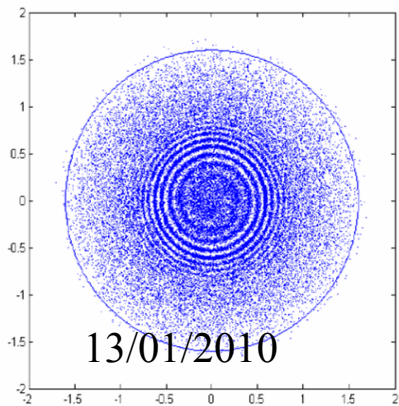
# LHC Injection: Again ... high accuracy required

## Filamentation

Injection errors (position or angle) dilute the beam emittance

Non-linear effects (e.g. magnetic field multipoles) introduce distort the harmonic oscillation and lead to amplitude dependent effects into parti

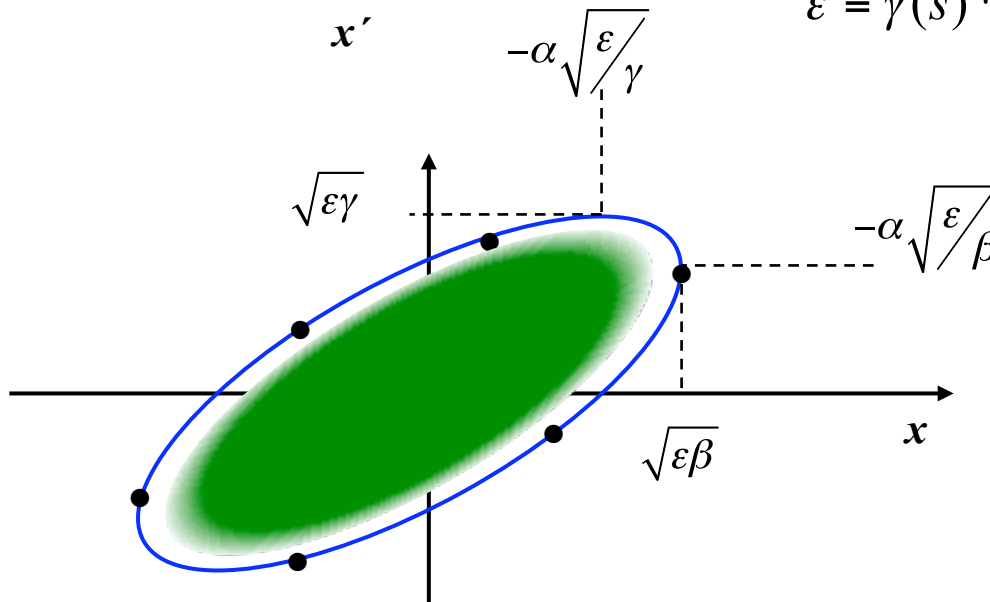
Over many turns oscillation is 1 increase.



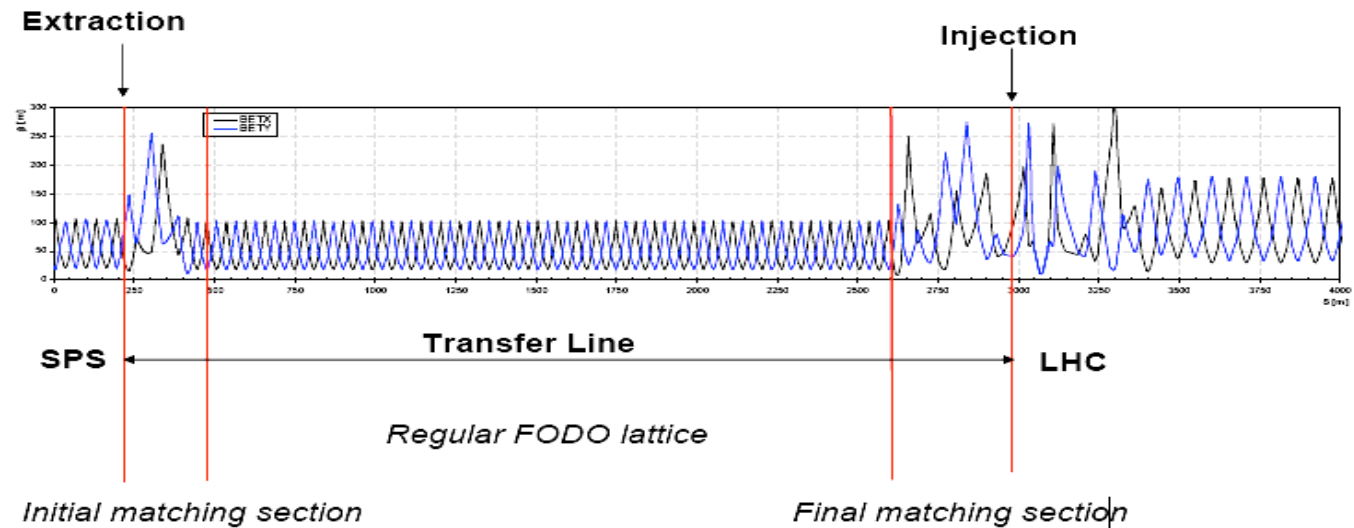


# LHC Injection: remember the phase space

$$\varepsilon = \gamma(s) * x^2(s) + 2\alpha(s)x(s)x'(s) + \beta(s)x'(s)^2$$



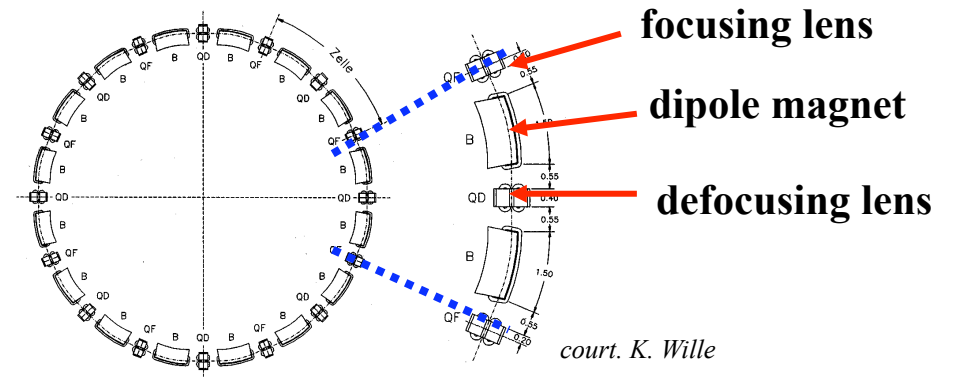
**Injected Beam has to be matched to the optics of the storage ring**



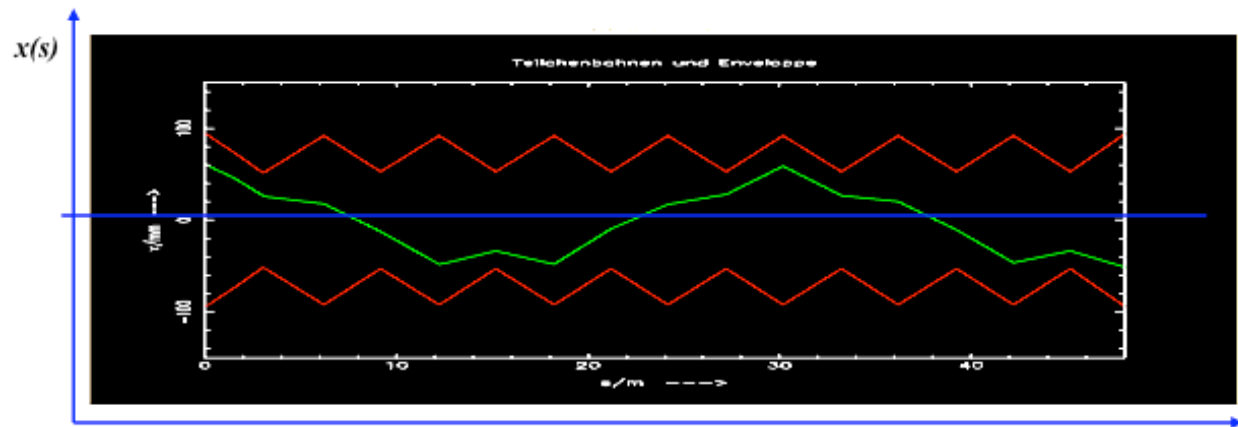
# LHC First Turn Steering

$$M_{total} = M_{QF} * M_D * M_{QD} * M_{Bend} * M_{D^*} * \dots$$

$$\begin{pmatrix} x \\ x' \end{pmatrix}_{s_2} = M(s_2, s_1) * \begin{pmatrix} x \\ x' \end{pmatrix}_{s_1}$$

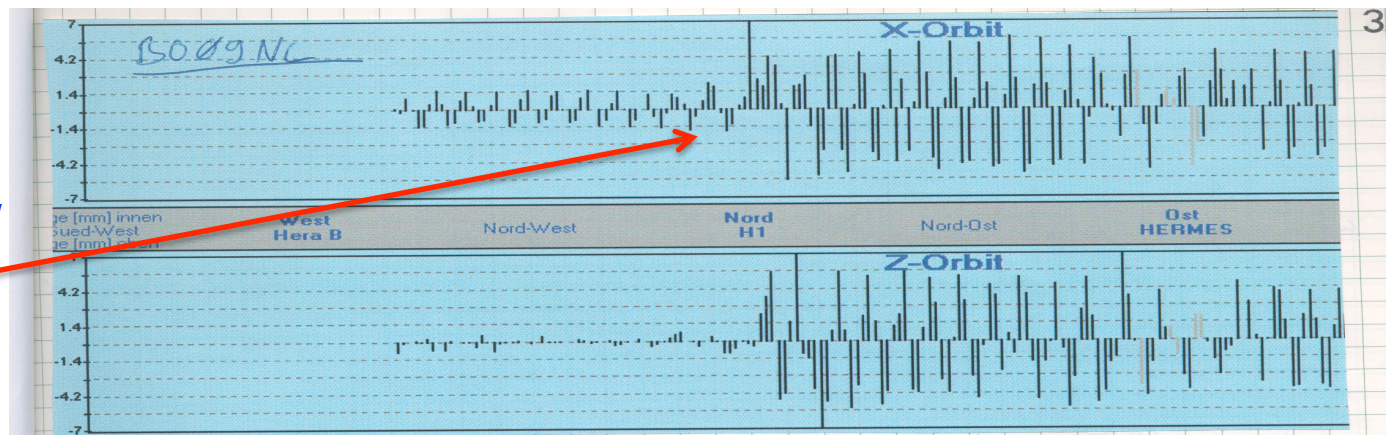


*in theory*  
*nice harmonic oscillation*



*in reality:*  
*effect of many localised orbit distortions*

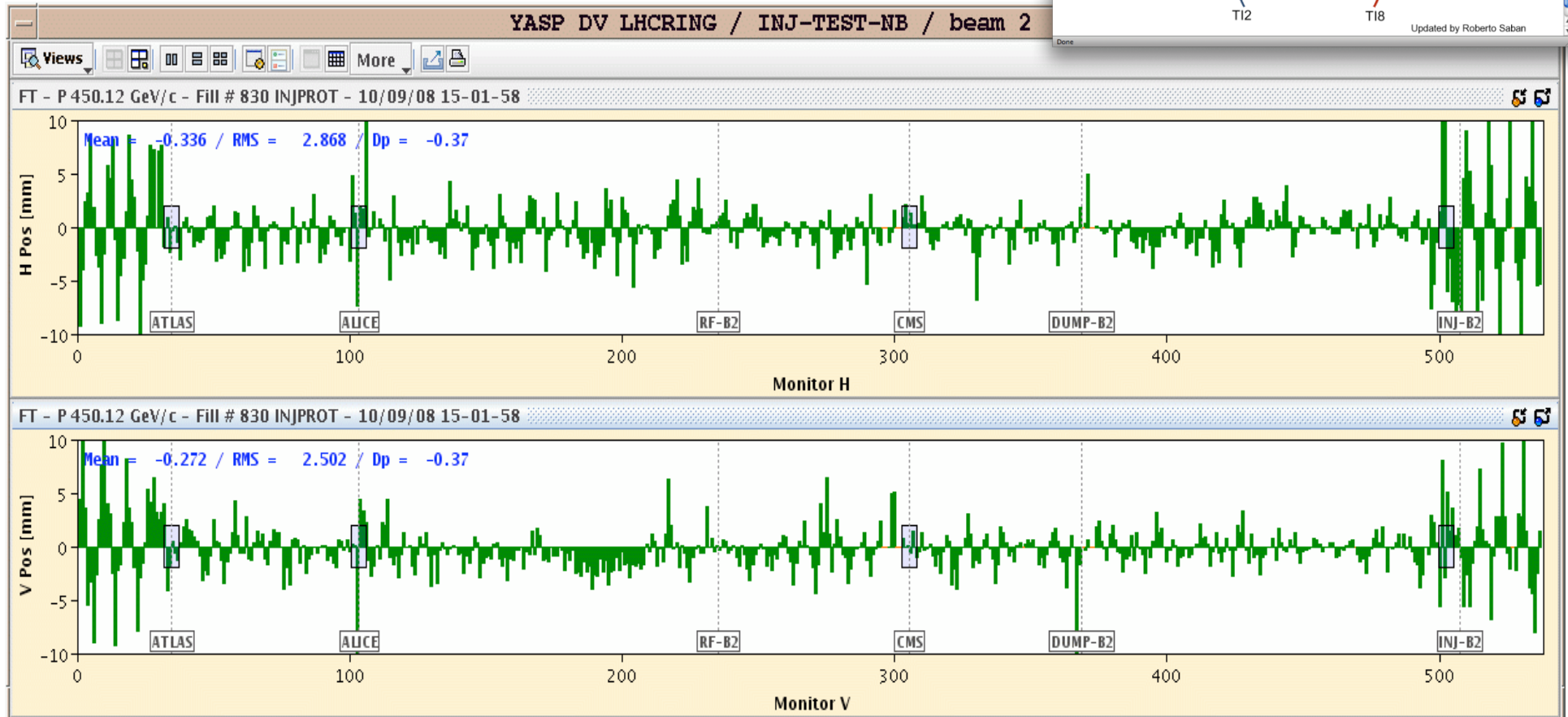
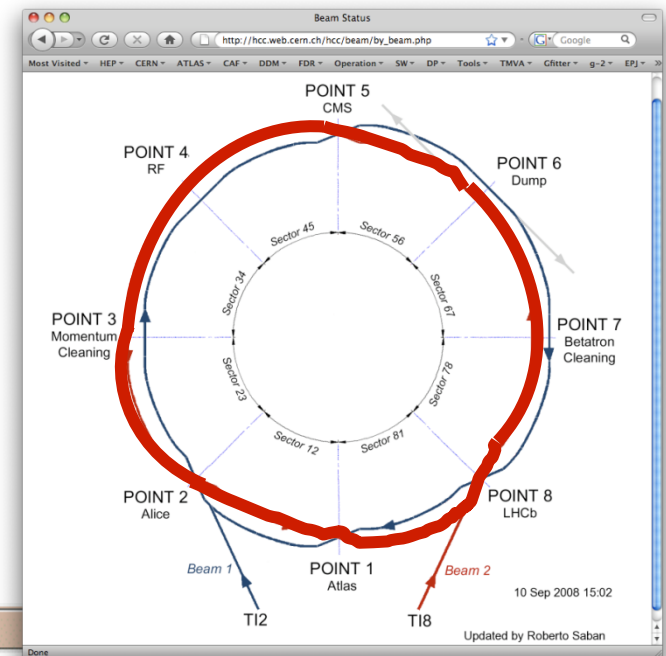
*-> correct*



# LHC Operation: Beam Commissioning

## First turn steering "by sector:"

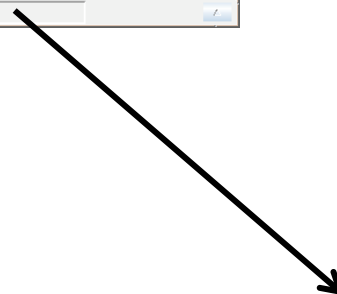
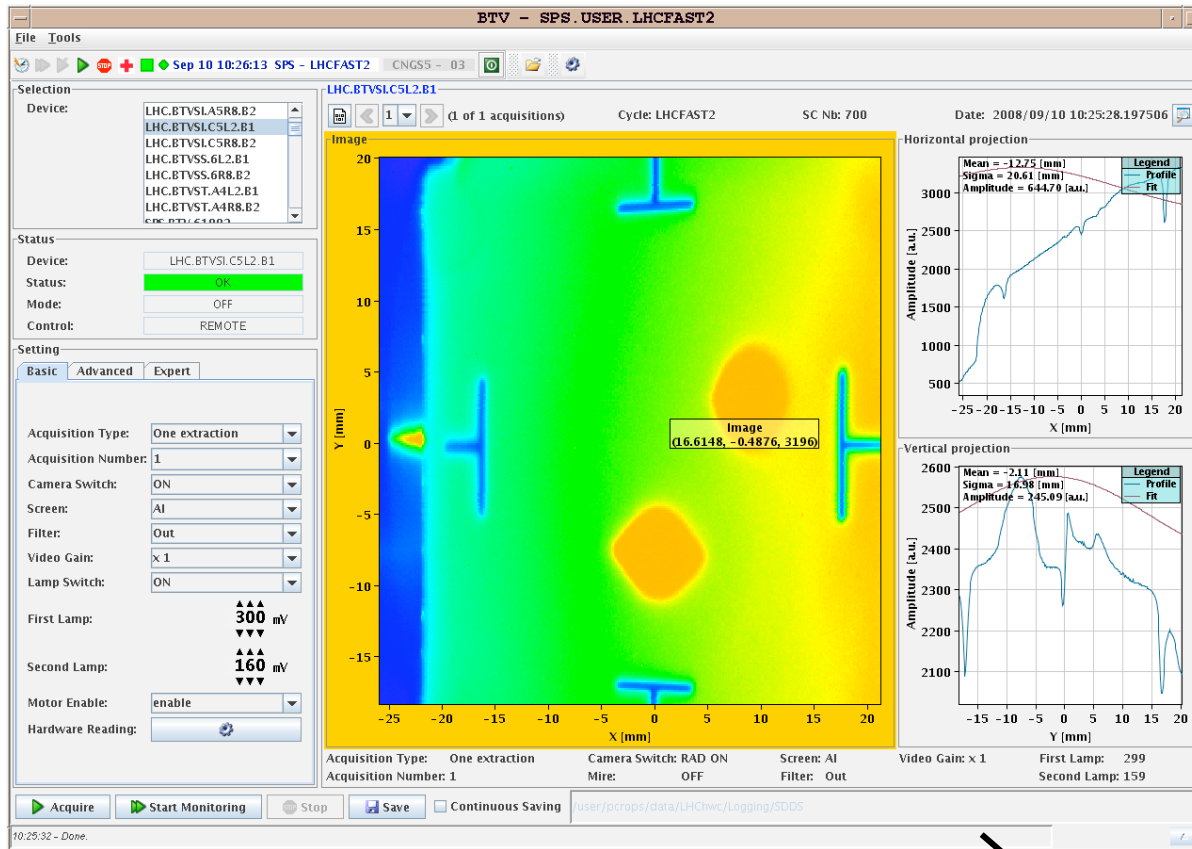
- One beam at the time
- Beam through 1 sector (1/8 ring), correct trajectory, open collimator and move on.



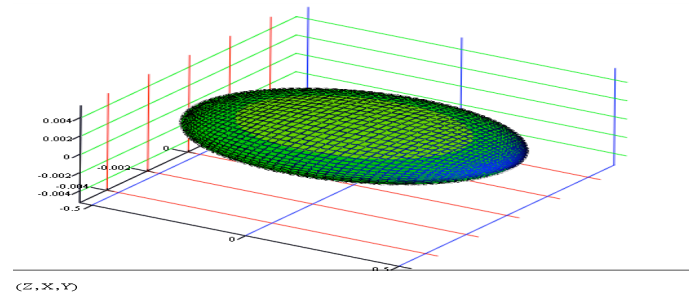
# LHC Operation: the First Turn

*Beam 1 on OTR screen  
1st and 2nd turn*

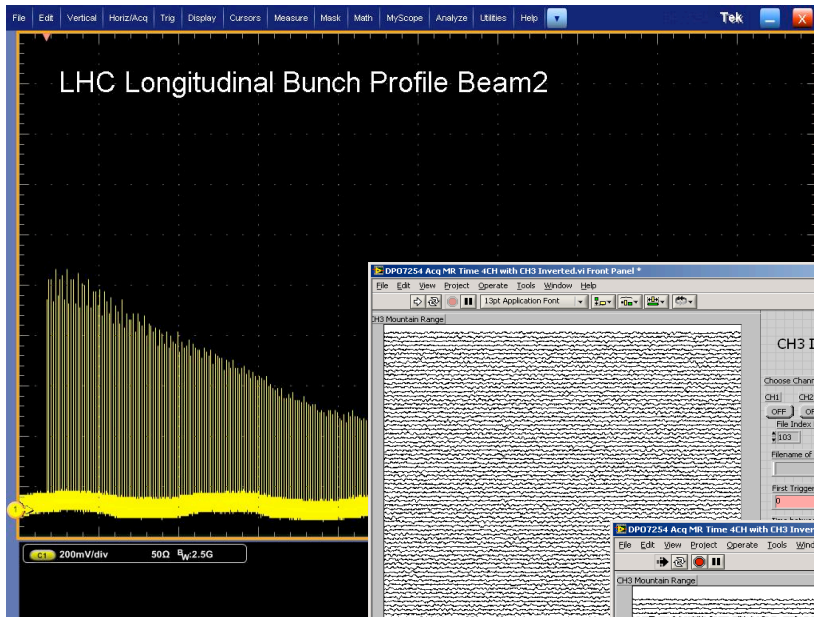
*Correct  $x, x'$ ,  
 $y, y'$   
to obtain the **Closed Orbit***



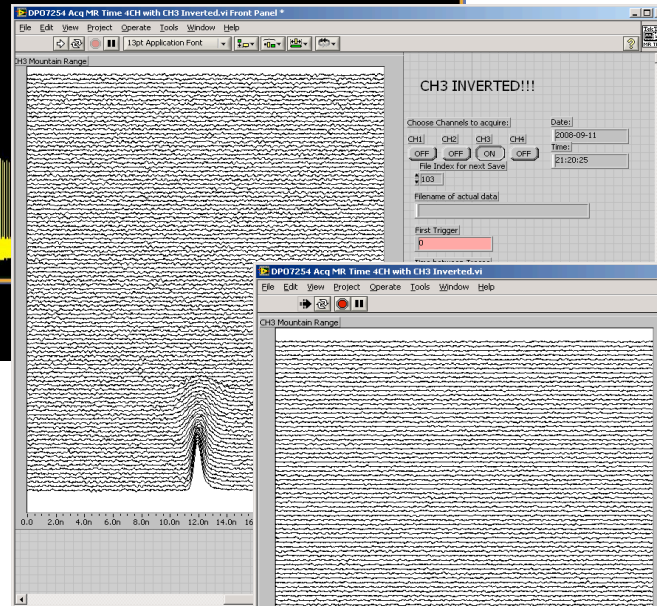
# LHC Commissioning: RF



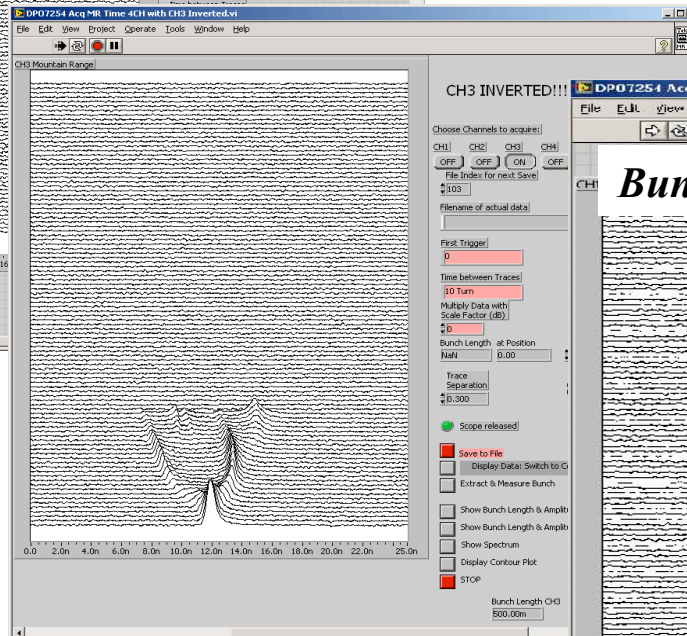
*a proton bunch: focused longitudinal by the RF field*



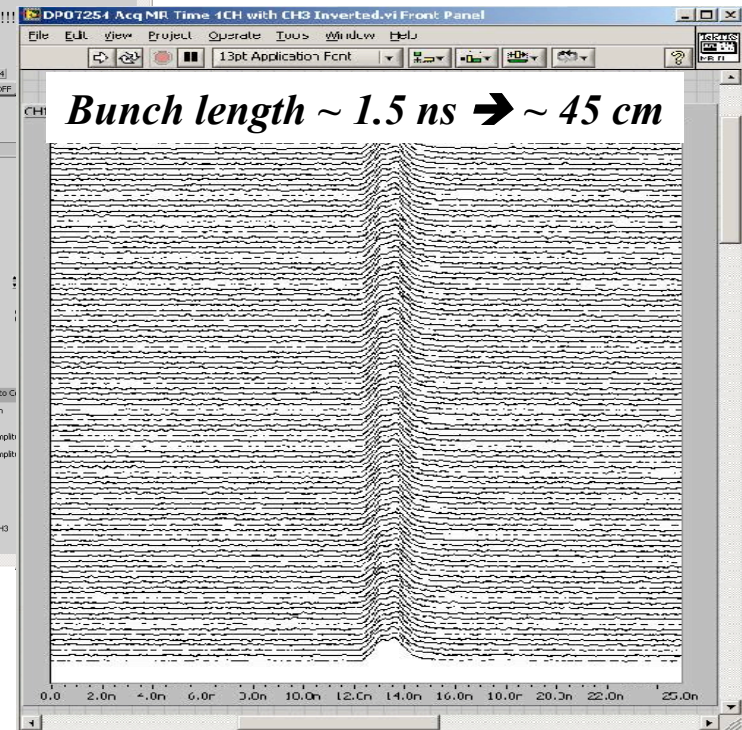
*RF off*



*RF on,  
phase optimisation*



*RF on, phase adjusted,  
beam captured*



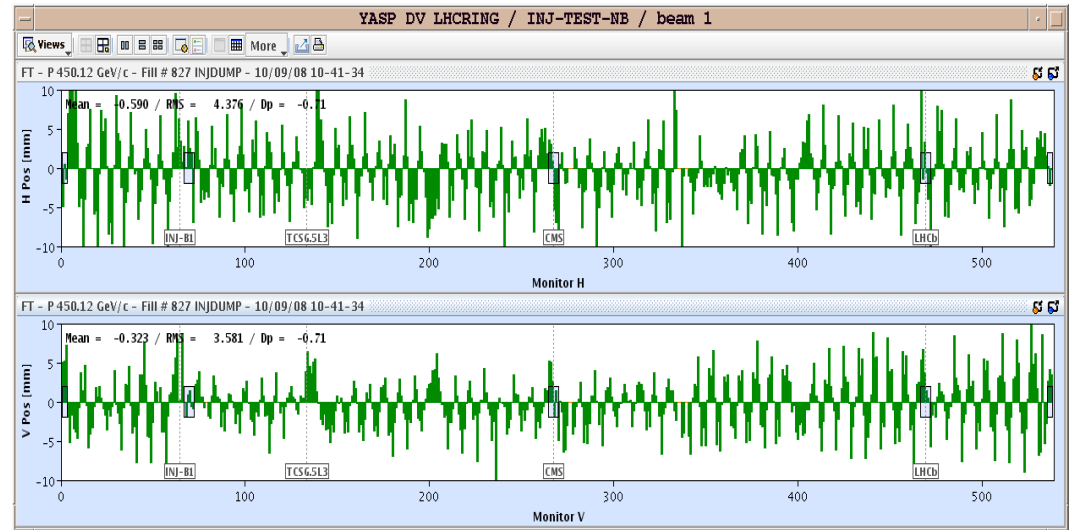
# Orbit & Tune:

*Tune: number of oscillations per turn*

**64.31**  
**59.32**

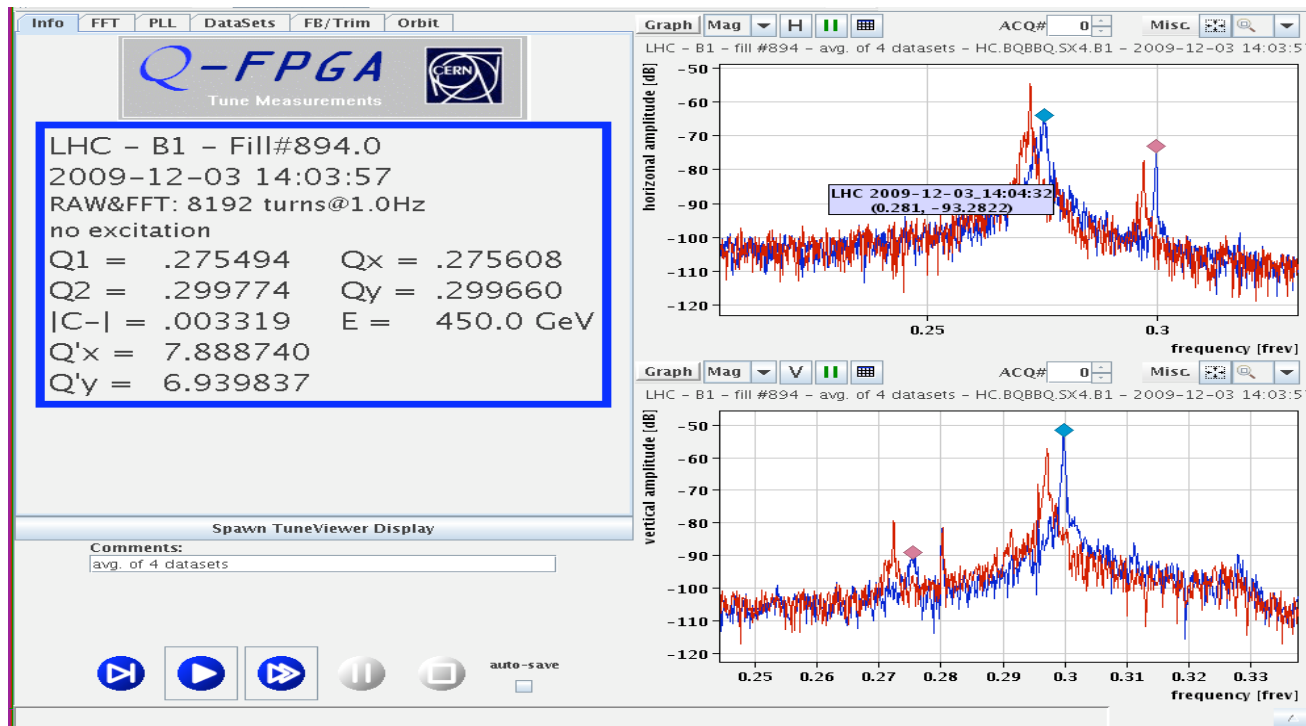
*Relevant for beam stability:*

*non integer part*



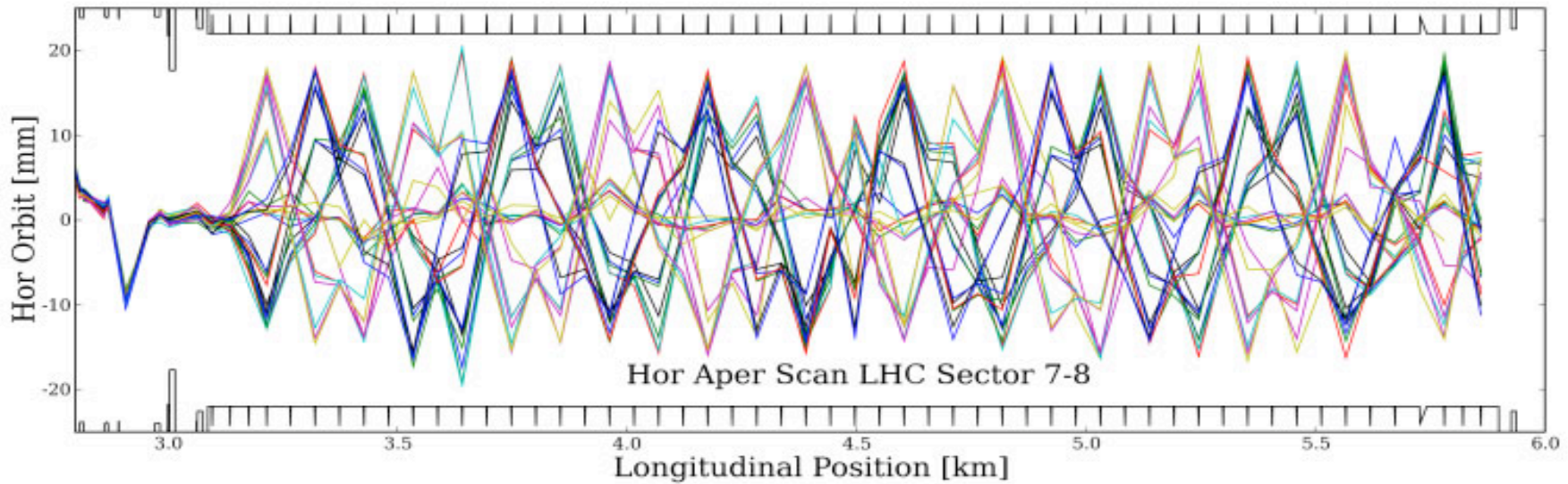
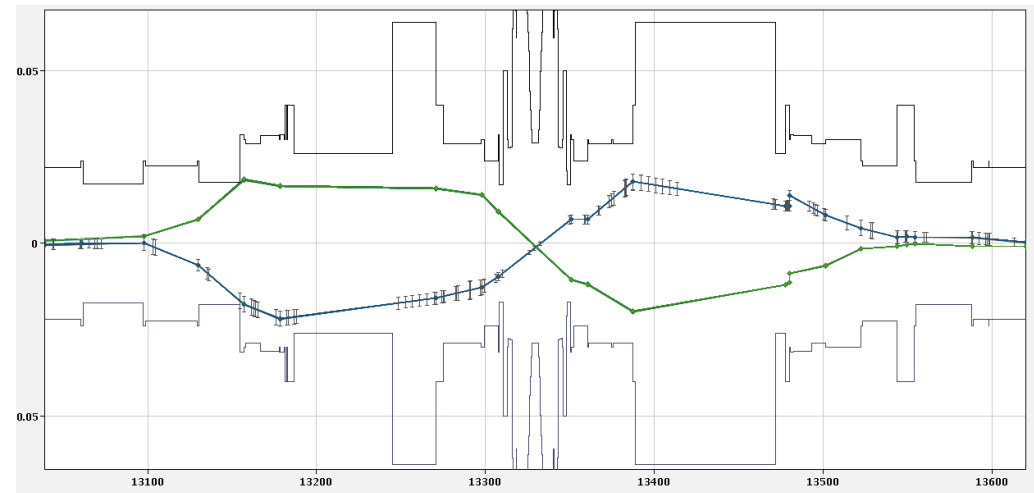
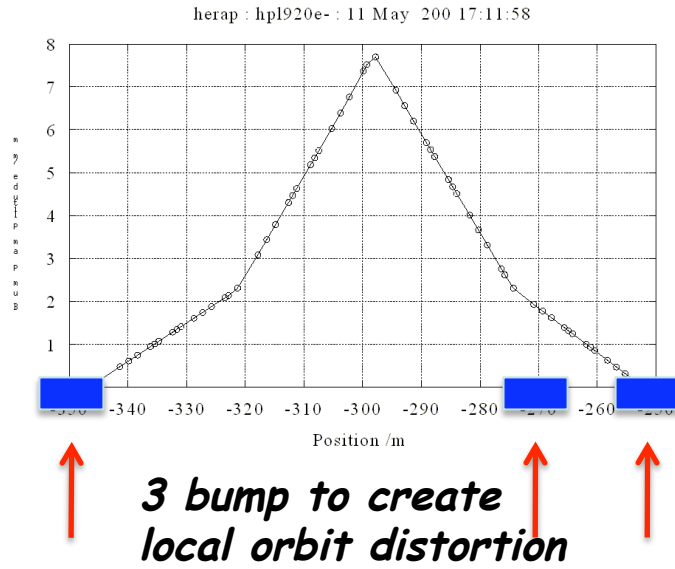
*LHC revolution frequency: 11.3 kHz*

$$0.31 * 11.3 = 3.5 \text{ kHz}$$



# LHC Operation: Aperture Scans

Apply closed orbit bumps until losses indicate the aperture limit  
... what about the *beam size* ?



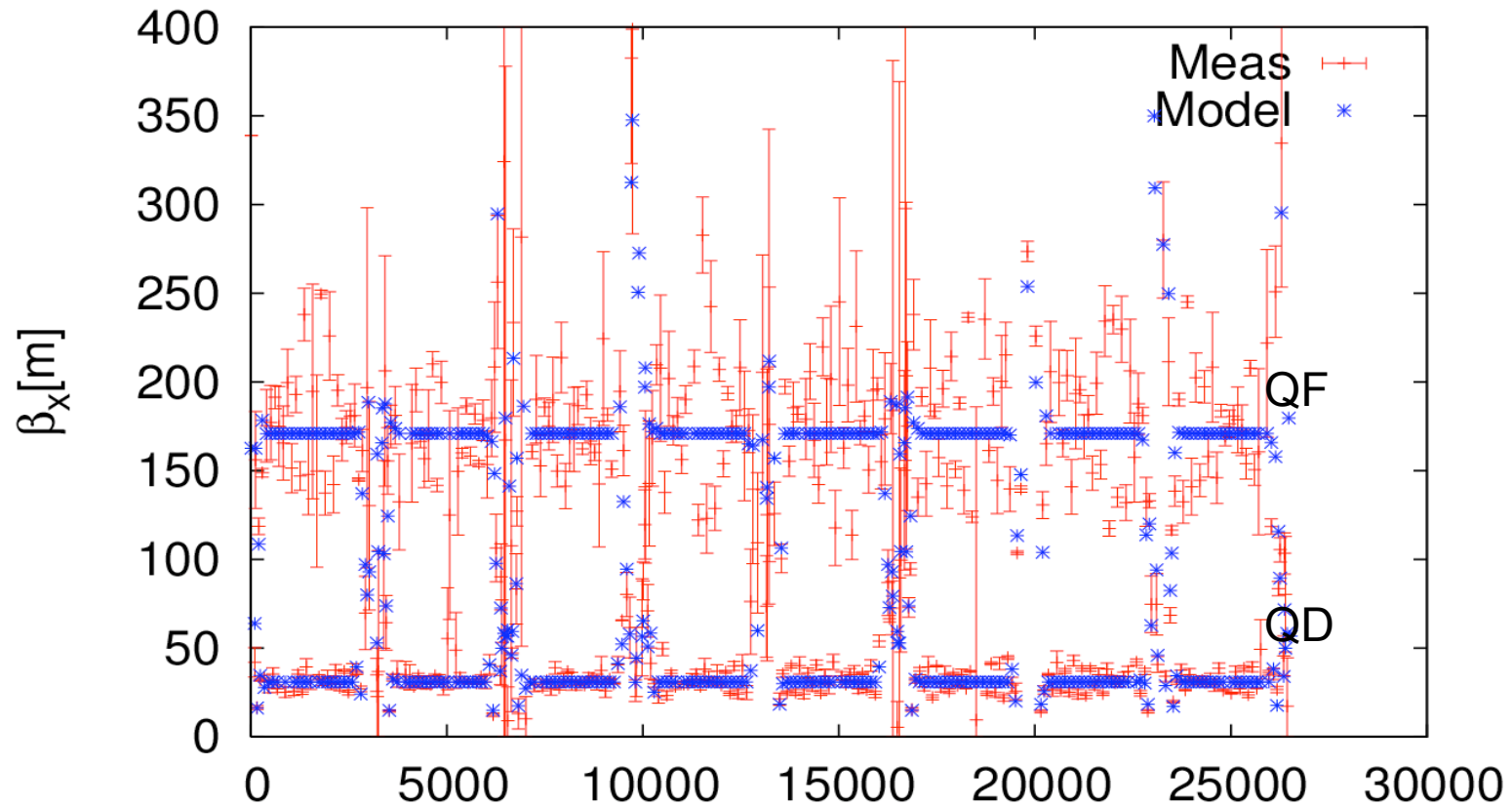
# LHC Operation: the First Beam

## Measurement of $\beta$ :

$$\Delta\beta(s_0) = \frac{\beta_0}{2 \sin 2\pi Q} \int_{s_1}^{s_1+l} \beta(s_1) \Delta K \cos(2|\psi_{s_1} - \psi_{s_0}| - 2\pi Q) ds$$

$\Delta\beta / \beta = 50 \%$

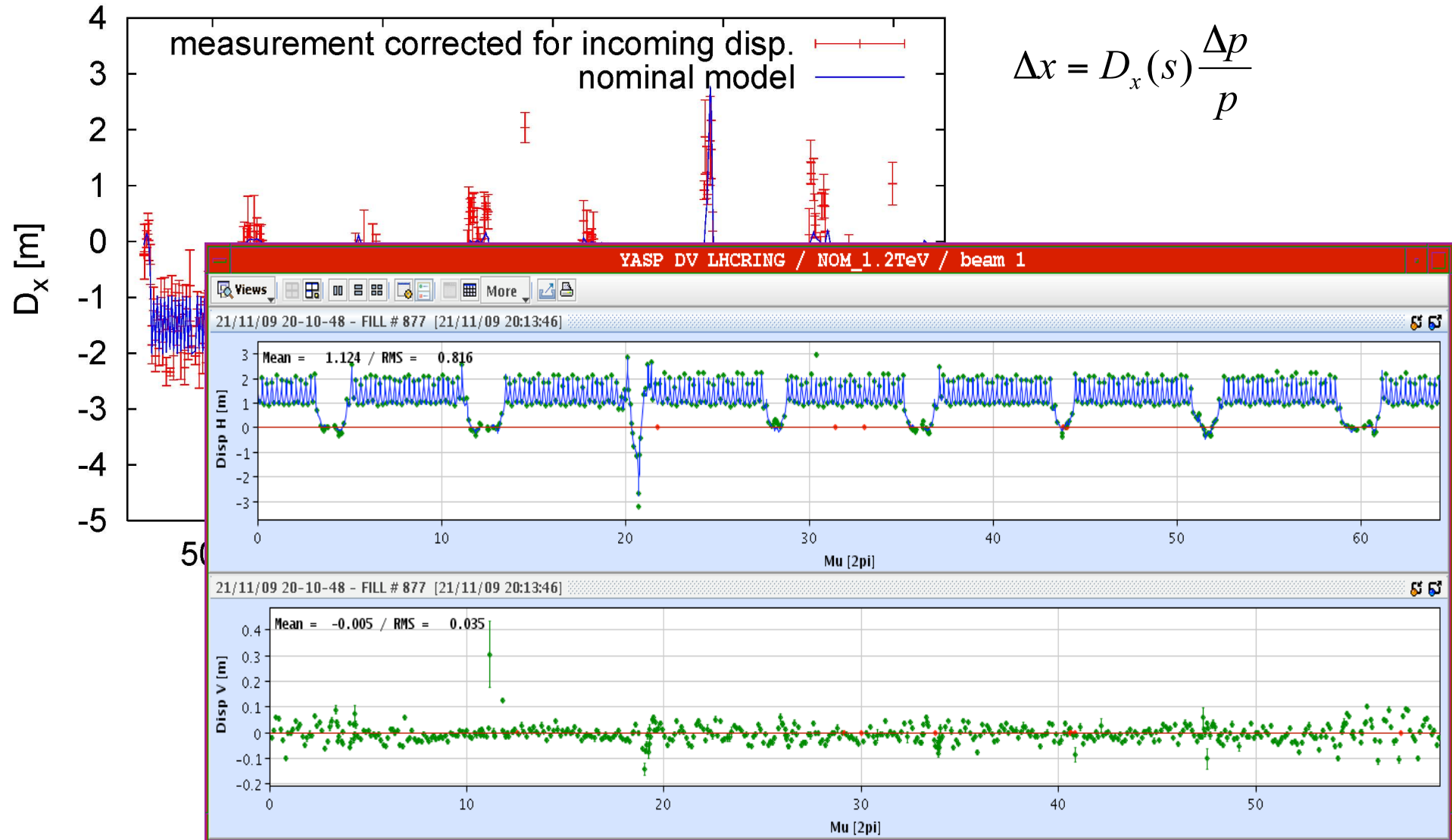
LHCB2, 90 turns (12/09/08 12:38:16)





# LHC Operation: the First Beam

## Dispersion Measurement



# Luminosity optimization

$$L = \frac{N_1 N_2 f_{rev} N_b}{2\pi \sqrt{\sigma_{1x}^2 + \sigma_{2x}^2} \sqrt{\sigma_{1y}^2 + \sigma_{2y}^2}} F \cdot W$$

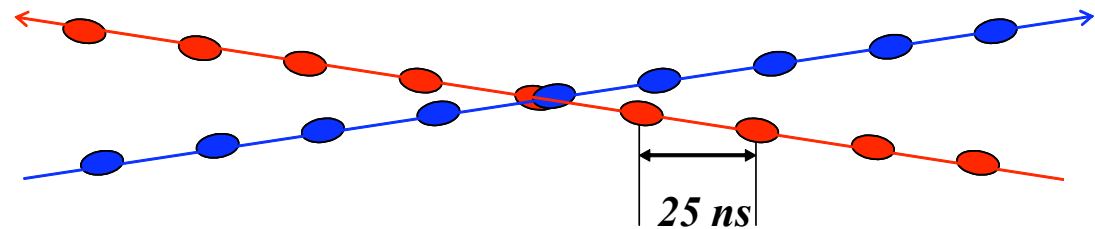
$N_i$  = number of protons/bunch  
 $N_b$  = number of bunches  
 $f_{rev}$  = revolution frequency  
 $\sigma_{ix}$  = beam size along x for beam i  
 $\sigma_{iy}$  = beam size along y for beam i

F is a pure **crossing angle ( $\Phi$ )** contribution:

$$F = \frac{1}{\sqrt{1 + 2 \frac{\sigma_s^2}{\sigma_{1x}^2 + \sigma_{2x}^2} \tan^2 \frac{\phi}{2}}}$$

←  $F_{LHC} = 0.836$

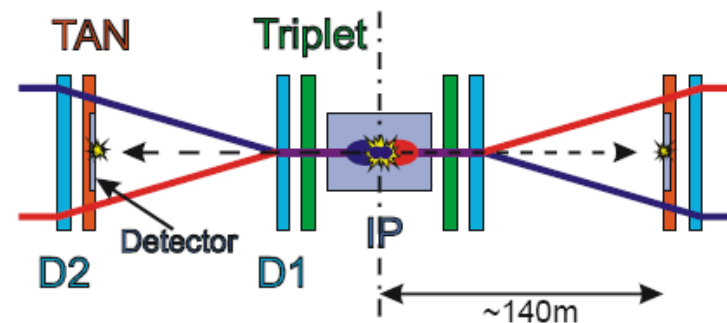
*... cannot be avoided*



W is a pure beam offset contribution.

*... can be avoided by careful tuning*

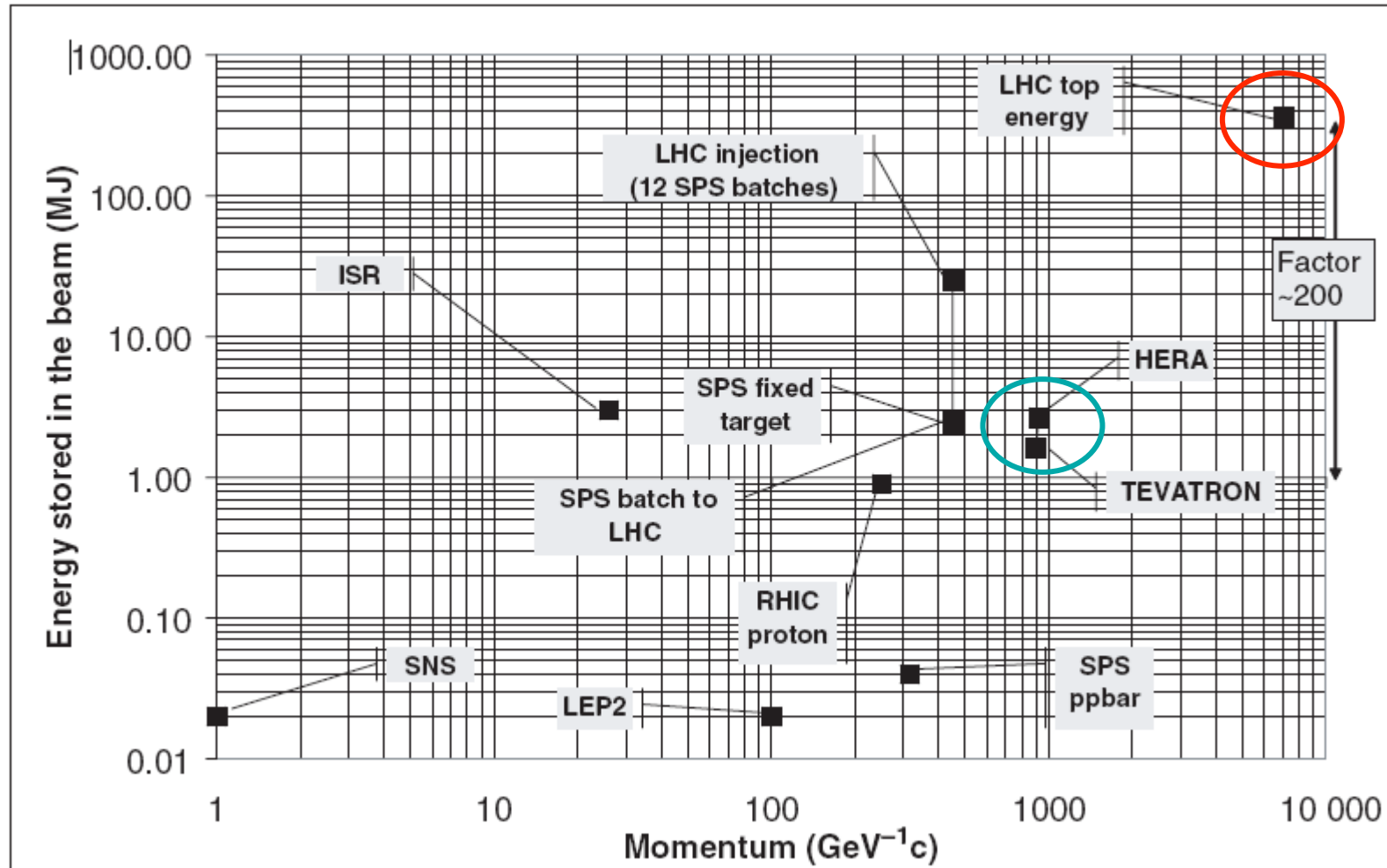
$$W = e^{-\frac{(d_2 - d_1)^2}{2(\sigma_{x1}^2 + \sigma_{x2}^2)}}$$



# LHC Operation:

## Machine Protection & Safety

### Energy Stored in the Beam of different Storage Rings

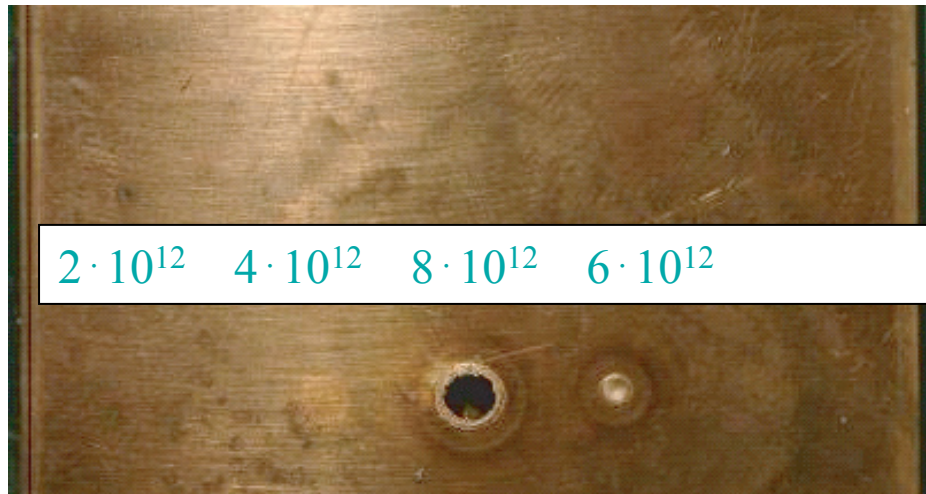


## LHC Operation:

### Machine Protection & Safety

Energy stored in magnet system	10	GJ
Energy stored in one main dipole circuit	1.1	GJ
Energy stored in one beam	362	MJ

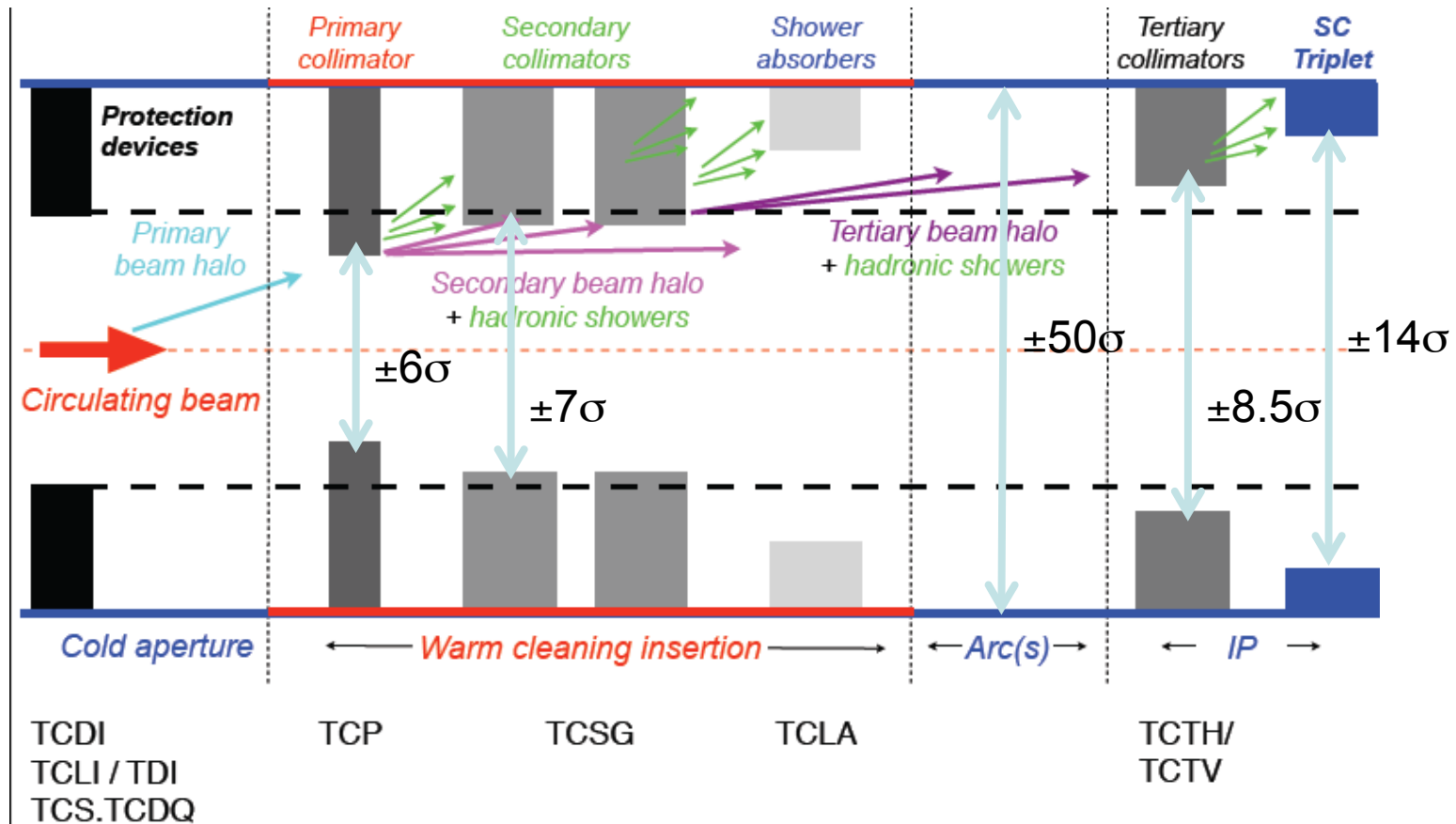
*Enough to melt 500 kg of copper*



$2 \cdot 10^{12}$     $4 \cdot 10^{12}$     $8 \cdot 10^{12}$     $6 \cdot 10^{12}$

450 GeV p Strahl

# LHC Aperture and Collimation

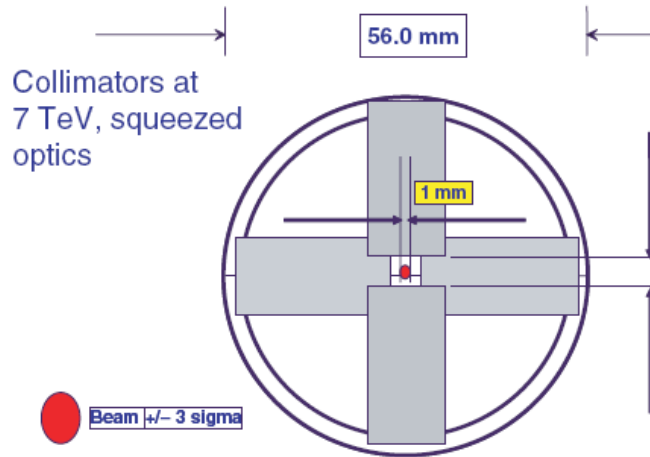


S. Redaelli, OP WG on Checkout, 08-11-2007

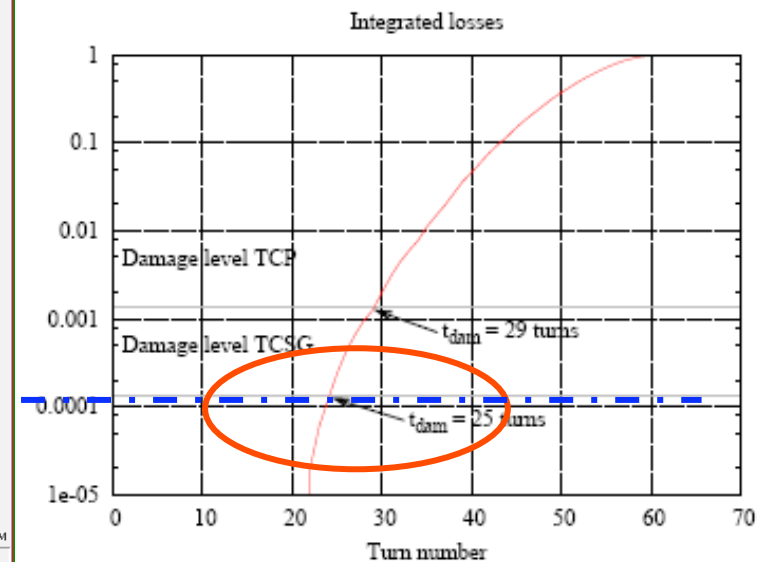
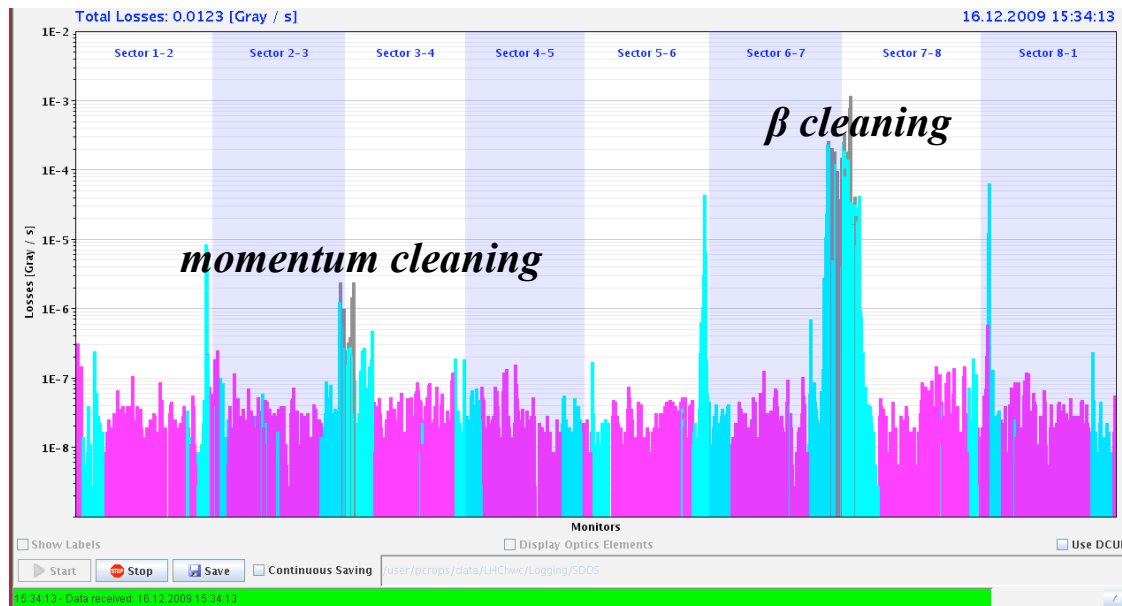
*Settings @7TeV and  $\beta^*=0.55$  m*  
*Beam size ( $\sigma$ ) = 300  $\mu$ m (@arc)*  
*Beam size ( $\sigma$ ) = 17  $\mu$ m (@IR1, IR5)*

# LHC Operation: Machine Protection & Safety

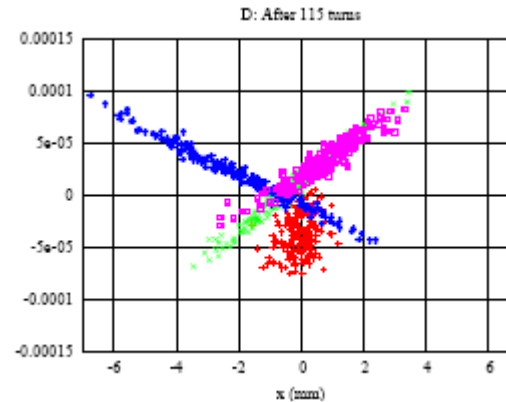
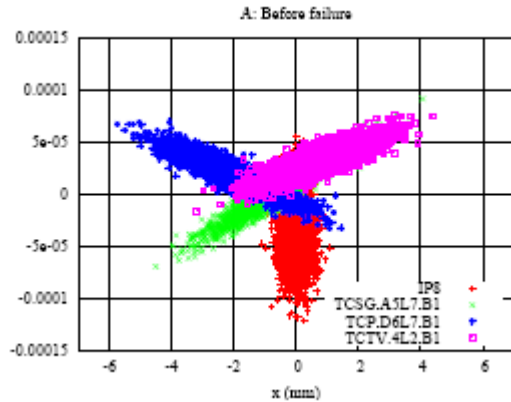
... *Komponenten des Machine Protection Systems* :



- beam loss monitors*
- QPS*
- permit server*
- orbit control*
- power supply control*
- collimators*
- online on beam check of all (?)*
- hardware components*
- a fast dump*
- the gaussian beam profile*



# LHC Operation: Machine Protection & Safety



*What will happen in case of **Hardware Failure***

*Phase space deformation in case of failure of RQ4.LR7  
(A. Gómez)*

*Short Summary of the studies:*

*quench in sc. arc dipoles:  $\tau_{loss} = 20 - 30 \text{ ms}$*

*BLM system reacts in time, QPS is not fast enough*

*quench in sc. arc quadrupoles:  $\tau_{loss} = 200 \text{ ms}$*

*BLM & QPS react in time*

*failure of nc. quadrupoles:  $\tau_{det} = 6 \text{ ms}$*

*$\tau_{damage} = 6.4 \text{ ms}$*

*failure of nc. dipole:*

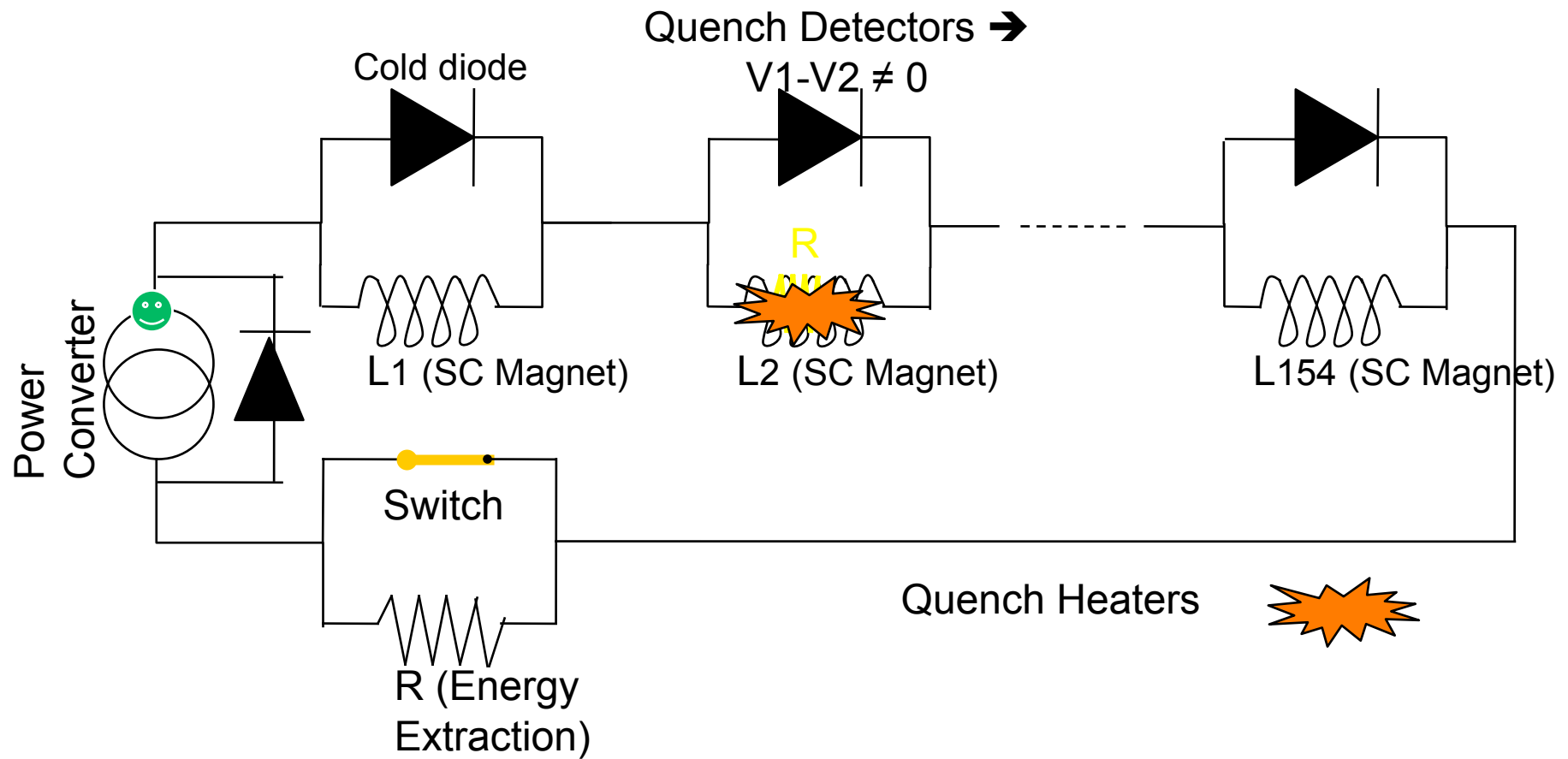
*$\tau_{damage} = 2 \text{ ms}$*

*→ FMCM installed*

# Energy stored in the magnets: 10 GJ

## Quench Protection System

*Schematics of the QPS in the main dipoles of a sector*





# *Energy stored in the magnets: quench*

If not fast and safe ...

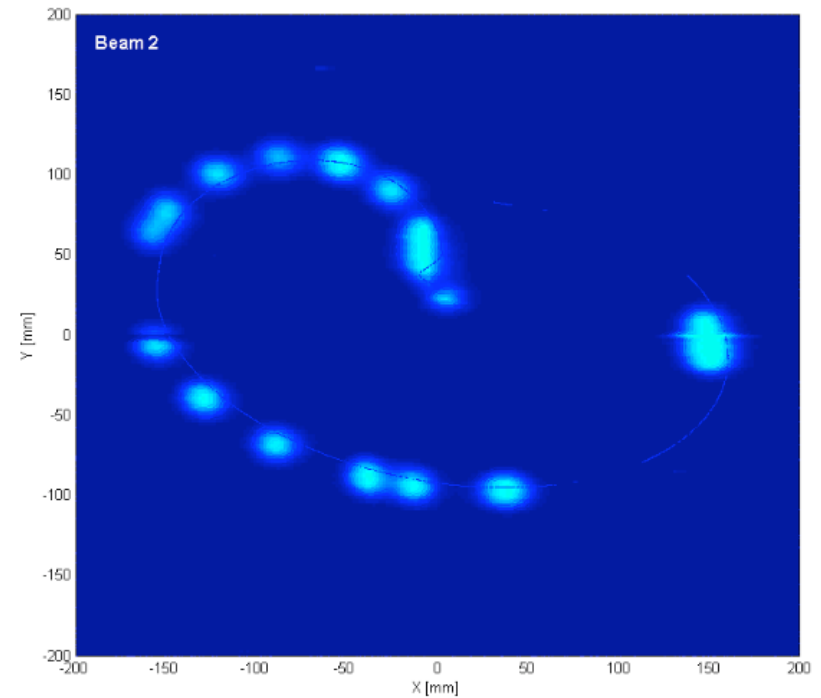
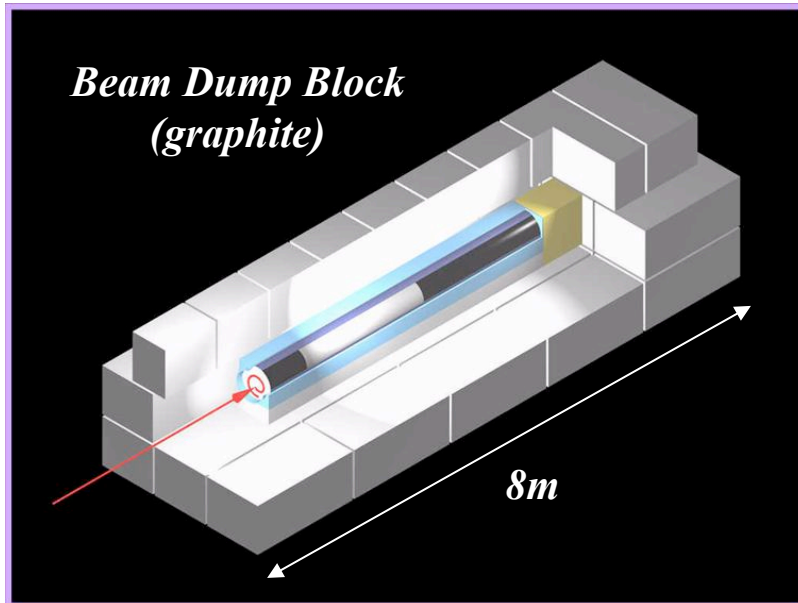
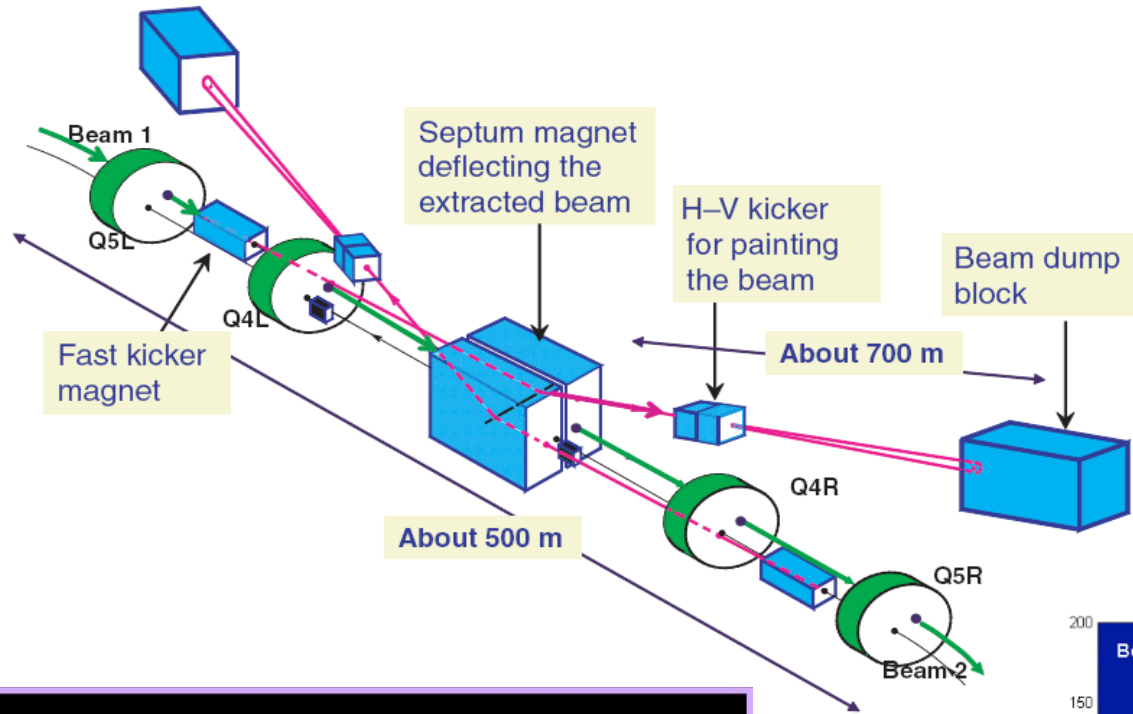
Quench in a magnet



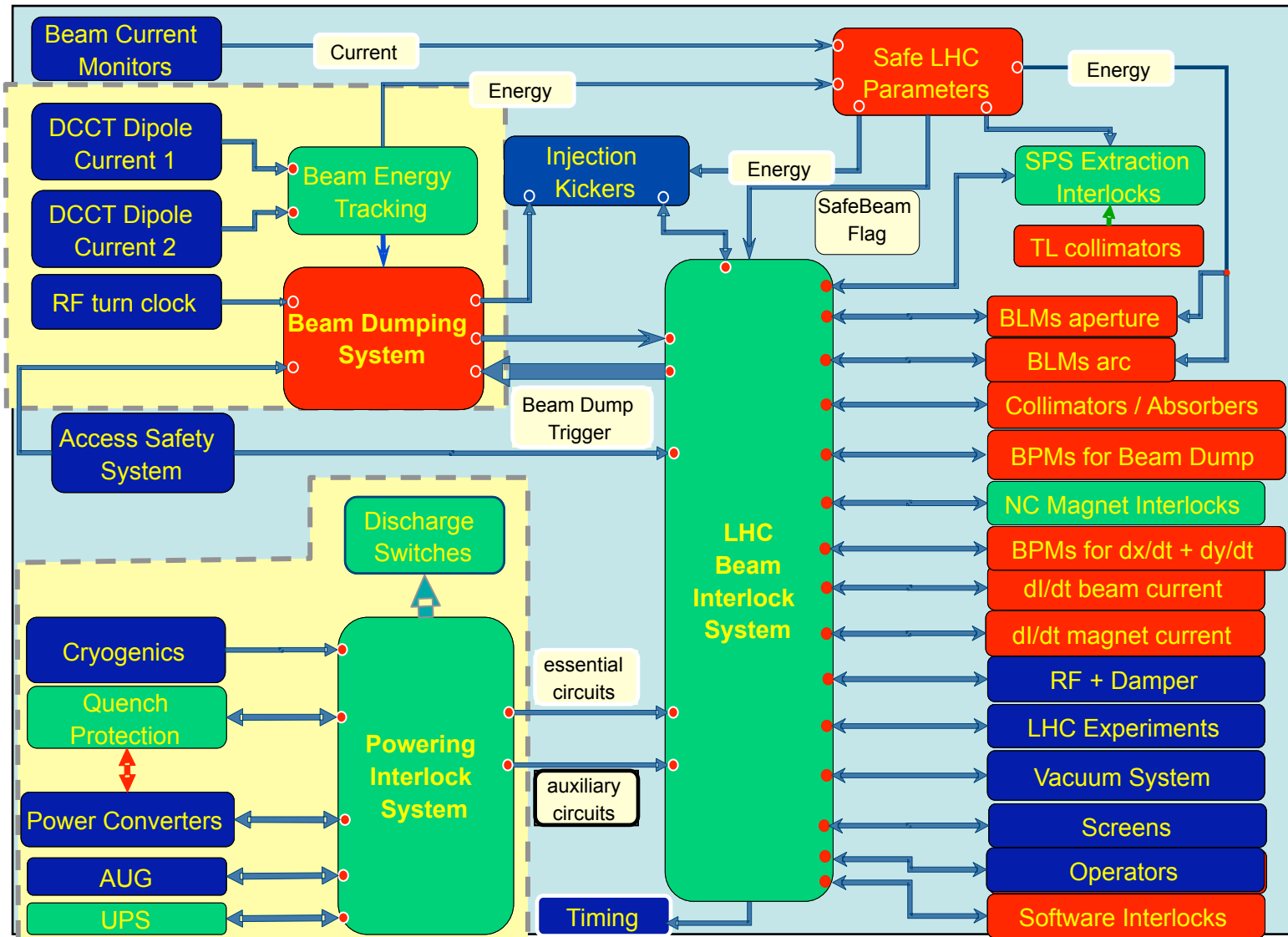
During magnet test campaign, the **7 MJ** stored in one magnet were released into one spot of the coil (inter-turn short)

P. Pugnati

# LHC Operation: Dump System



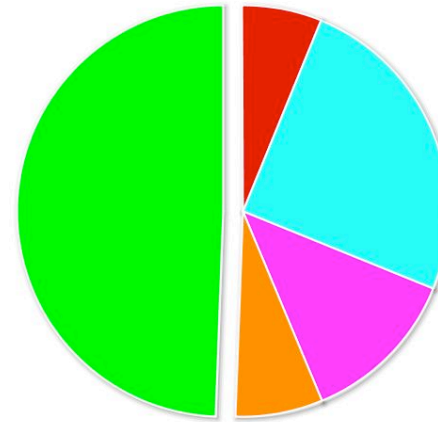
# LHC Operation: Machine Protection & Safety



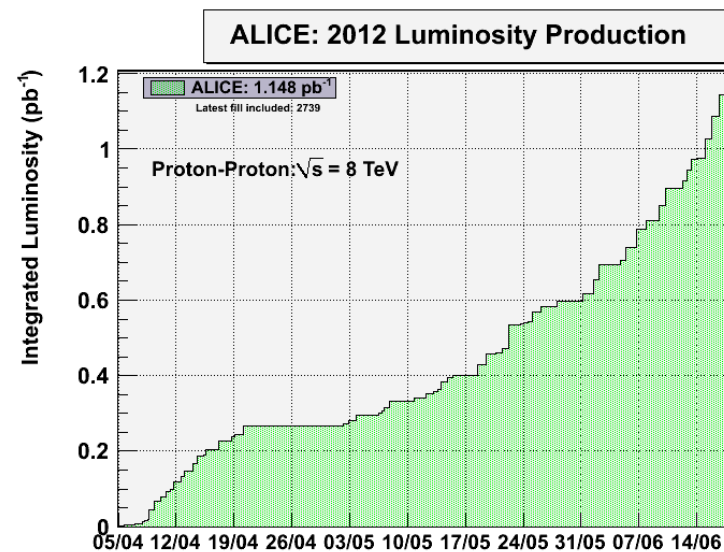
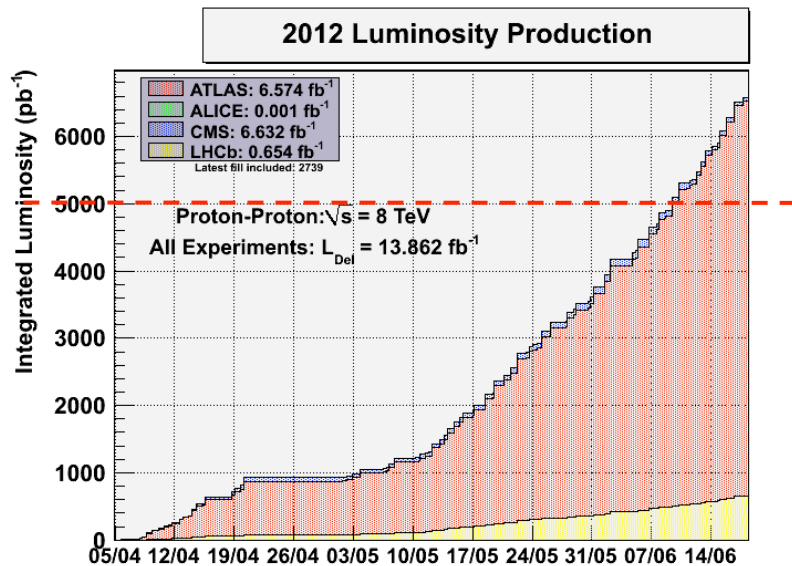
... no comment

# LHC Operation where are we ?

*Luminosity Efficiency:*  
*time spent in collisions / overall time*

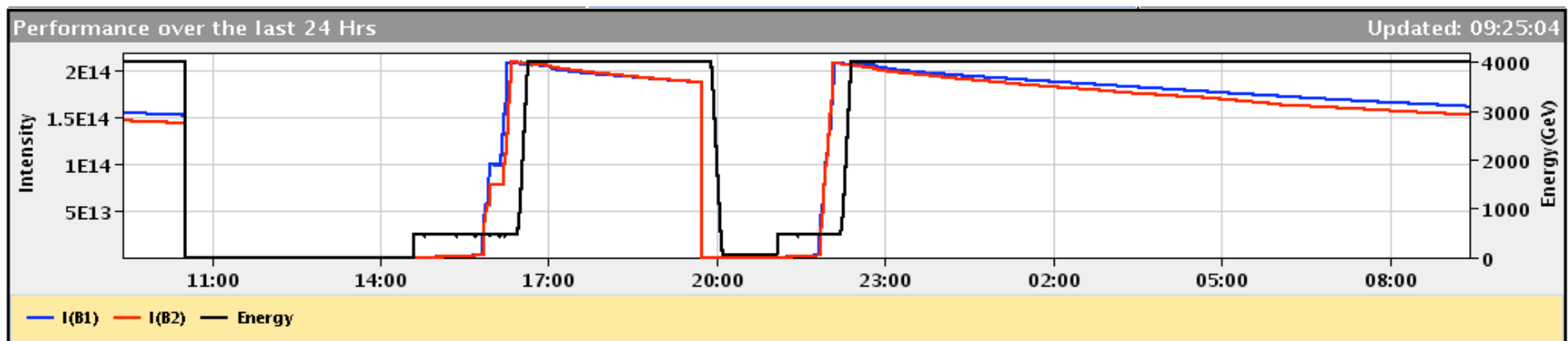


- Access - No beam : 6.24%
- Machine setup : 24.89%
- Beam in : 12.59%
- Ramp + squeeze : 6.85%
- Stable beams: 49.42%



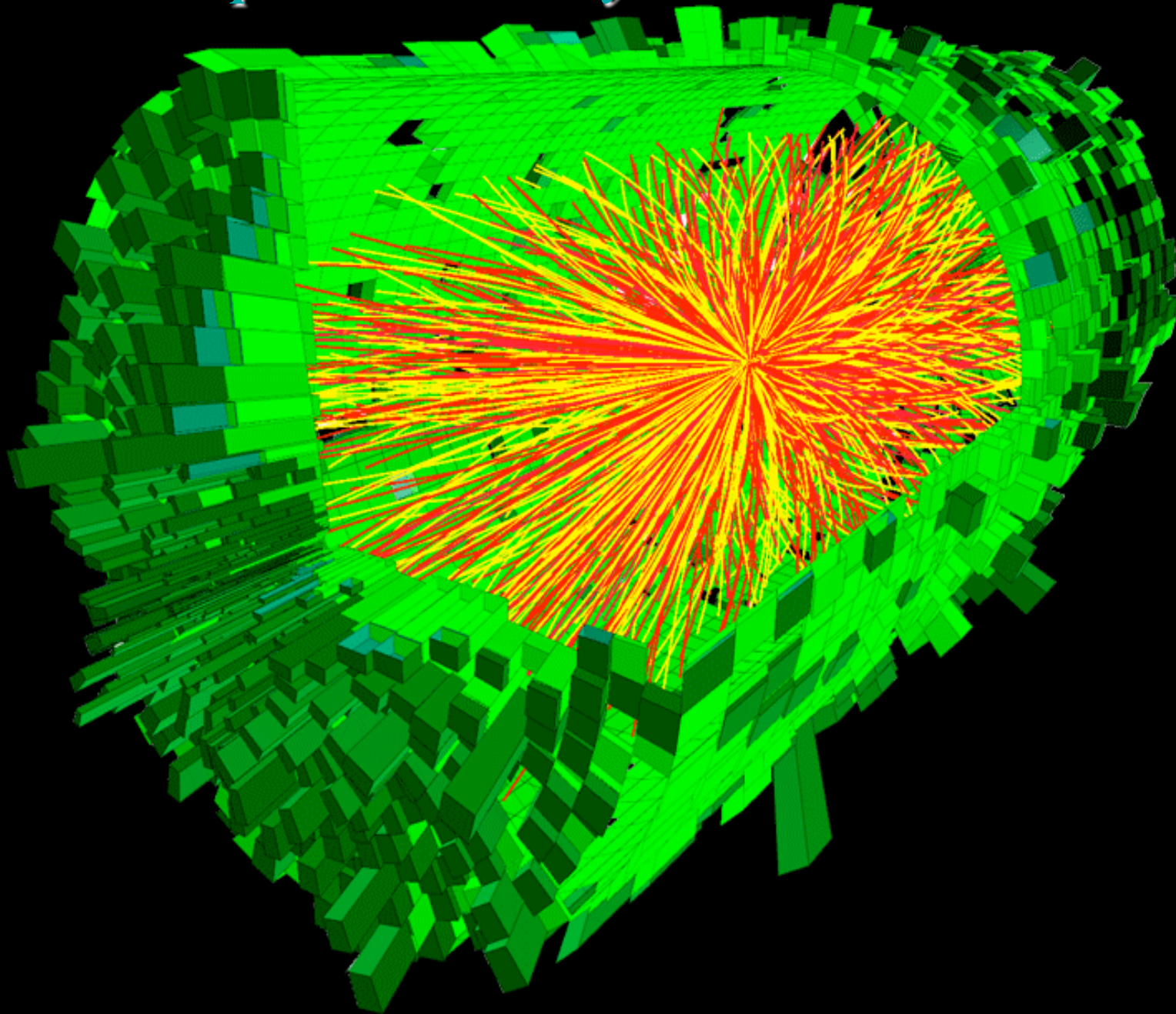
# LHC Operation where are we ?

	<i>LHC Design</i>	<i>LHC 2012</i>
<i>Momentum at collision</i>	7 TeV /c	3.5 TeV
<i>Dipole field</i>	8.33 T	4.16 T
<i>Protons per bunch</i>	$1.15 \times 10^{11}$	$1.5 \times 10^{11}$
<i>Number of bunches/beam</i>	2808	1380
<i>Nominal bunch spacing</i>	25 ns	50 ns
<i>Normalized emittance</i>	3.75 $\mu\text{m}$	2.2 $\mu\text{m}$
<i>Absolute Emittance</i>	$5 \times 10^{-10}$	$6.7 \times 10^{-10}$
<i>Beta Function</i>	0.5 m	0.6 m
<i>rms beam size (IP)</i>	16 $\mu\text{m}$	18 $\mu\text{m}$
<i>Luminosity</i>	$1.0 \times 10^{34}$	$6.7 \times 10^{33}$





# *LHC Operation: Heavy Ion Collisions*



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