



**BERGISCHE
UNIVERSITÄT
WUPPERTAL**

Standard Model @ Hadron Colliders

I. QCD

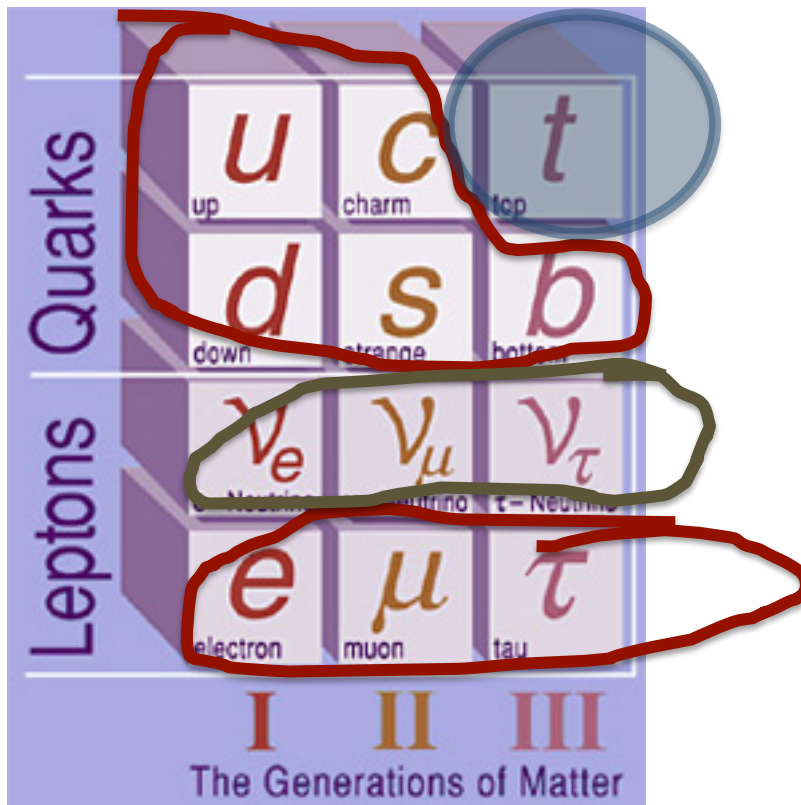
P.Mättig

Bergische Universität Wuppertal

Standar model pillar I: Matter



BERGISCHE
UNIVERSITÄT
WUPPERTAL



Unique topic for hadron colliders

Neutrinos not really testable @ hadron colliders

Most quarks/all charged leptons very deeply scrutinized

Standard Model pillar II: Forces



BERGISCHE
UNIVERSITÄT
WUPPERTAL



All interactions very precisely determined:

$$\alpha_s(M = M_Z) = 0.1184(7)$$

$$\alpha_{em} = 1/137.03499976(50)$$

$$G_F(M = m_\mu) = 1.16639(1) \cdot 10^{-5} \text{ GeV}^{-2}$$

$$M_Z = 91.1882(22) \text{ GeV}$$

Dynamics well tested at energies $\sim 100 \text{ GeV}$

e.g.: $g \rightarrow gg, (Z, \gamma) \rightarrow W^+W^-, \dots$

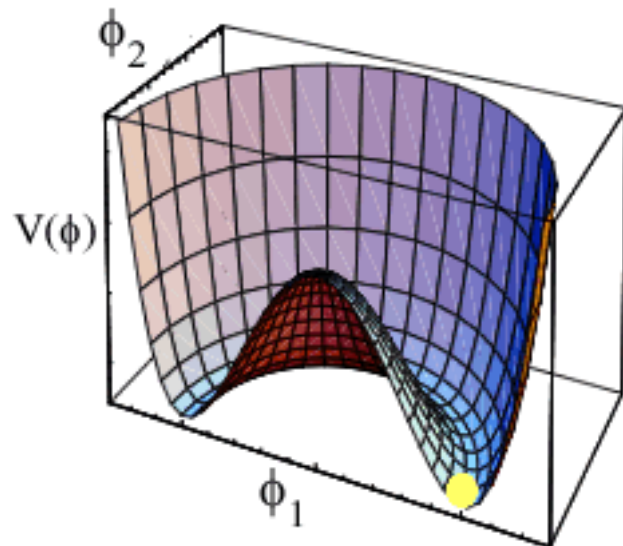
Standard Model Pillar III: Higgs



BERGISCHE
UNIVERSITÄT
WUPPERTAL

**Boson masses and fermion masses
break gauge symmetries**

→ Non – renormalisable theory



Standard Model way out:

Four Higgs fields

- Three give mass to W/Z bosons
- one is physical with well defined properties (except mass)

Until 20 days ago ???

THE ONLY MISSING PIECE OF THE STANDARD MODEL!



Why Standard Model @ Hadron Colliders?

- Explore phase space not determined from first principles
- Probe at highest energies
- More statistics → Top Quark
- Scrutinize the remaining piece → Higgs Boson

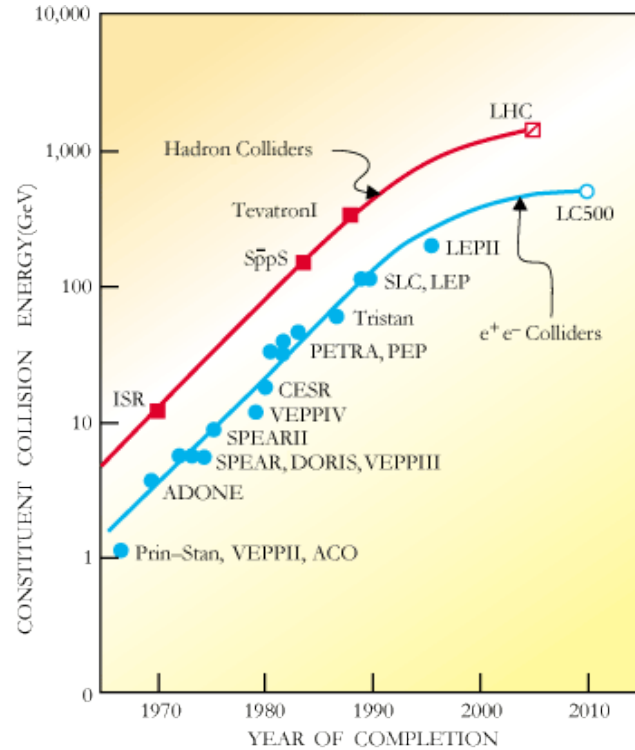
Standard model: the way towards establishing ‚New Physics‘?

- Standard Model processes background to ‚New Physics‘
- will provide tools for searches for new phenomena
- Testing Standard Model to the extreme →
may reveal a glimpse of ‚New Physics‘

Forerunners of LHC



BERGISCHE
UNIVERSITÄT
WUPPERTAL



**Tevatron (Fermilab): last 20 years:
Leading Proton – Antiproton collider
1.96 TeV c.m. energy**

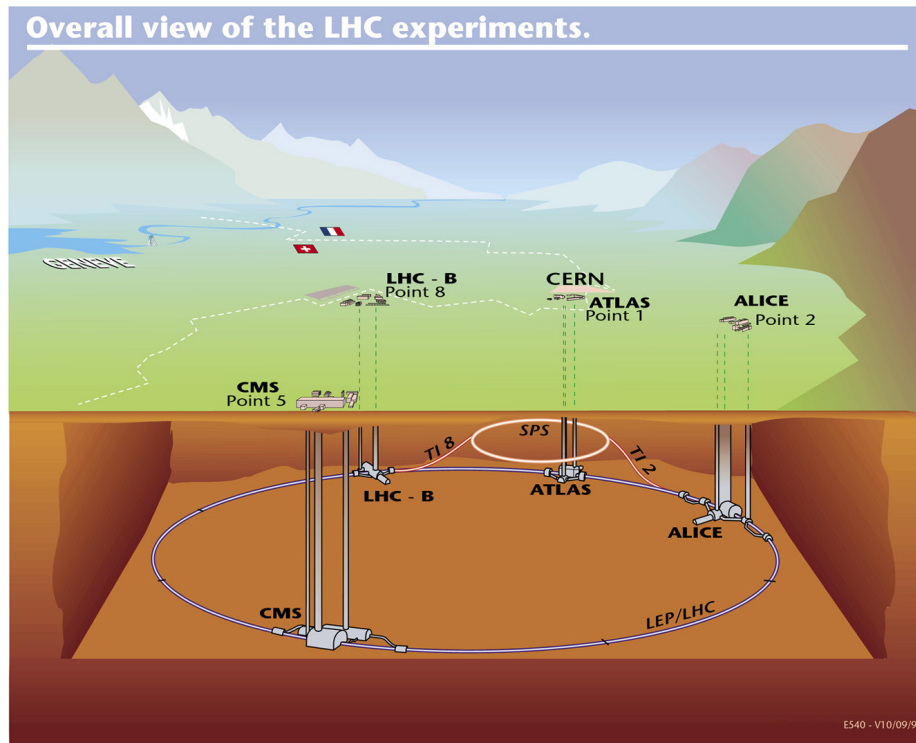


**Two experiments
CDF & D0**

Today's flagship LHC



BERGISCHE
UNIVERSITÄT
WUPPERTAL



**Proton – Proton Kollisionen
@ 14 TeV c.m. energy
(currently 8 TeV)**

4 Experiments

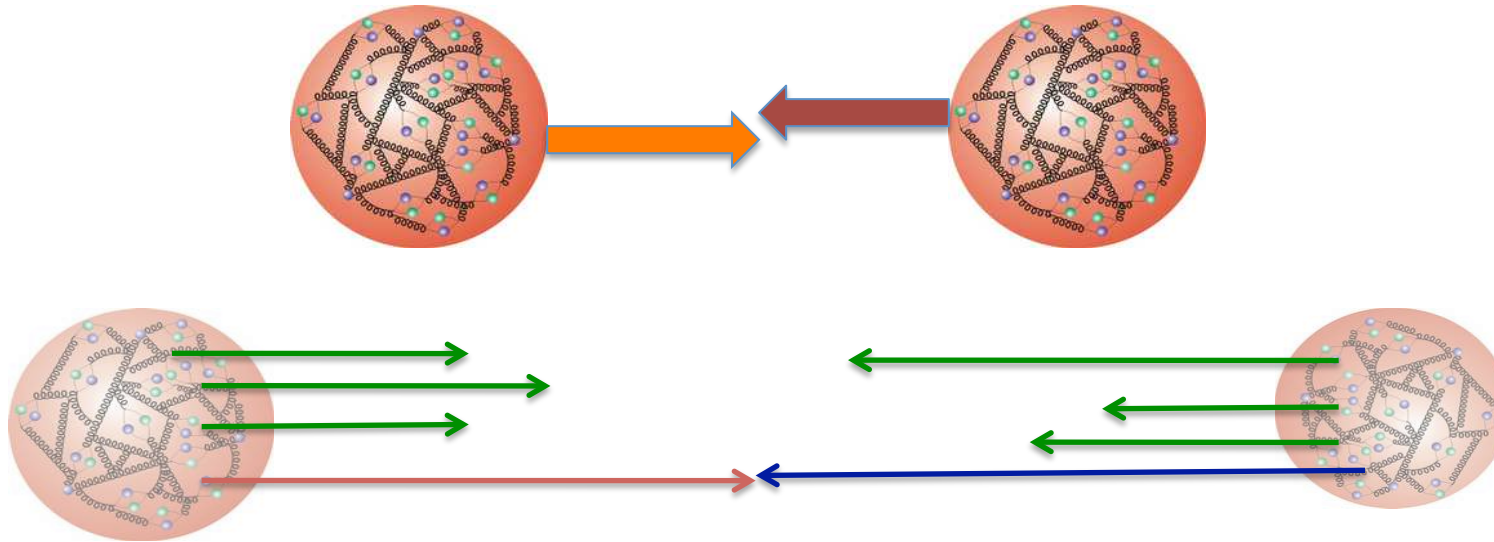
**Will focus on results from
ATLAS and CMS**

(LHCb → talk of G.Raven)

Reminder: how ,protons' interact



BERGISCHE
UNIVERSITÄT
WUPPERTAL

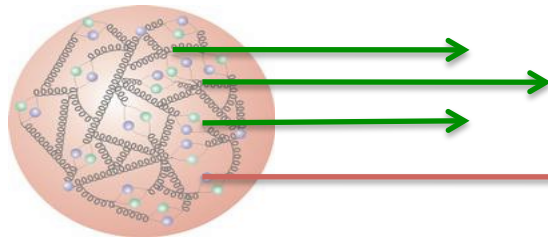


Proton scattering = scattering of quarks and gluons

$$\sigma(pp \rightarrow YX) = \int_0^1 dx_1 \int_0^1 dx_2 \sum_f f_f(x_1) f_{\bar{f}}(x_2) \cdot \sigma(q_f(x_1 P) + \bar{q}_f(x_2 P) \rightarrow Y)$$



Reminder: x, M



$$x = E_{\text{parton}} / M_{\text{proton}}$$

$$M_{\text{scatter}} = \sqrt{x_1 \cdot x_2} \cdot E_{pp}$$

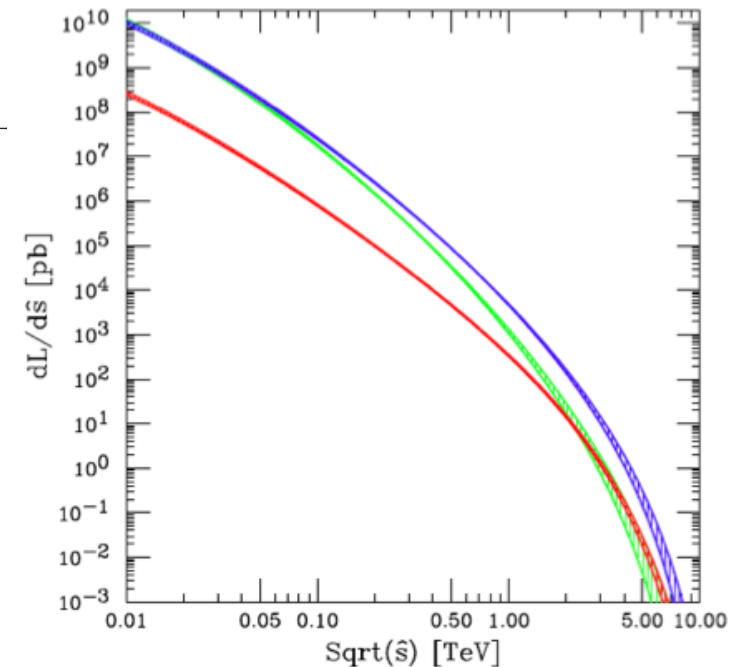
↑
„resolution power“

↑
for LHC: 8 TeV

**I.e. high masses requires
large x - values**

**LHC and Tevatron:
LHC has 4 (7)x higher energy,**

Note for $M \sim 400 - 1000$ TeV: Tevatron qq – LHC gg



Some basics: rapidity



BERGISCHE
UNIVERSITÄT
WUPPERTAL

Rapidity a ,natural' observable for consecutive branchings

$$\frac{d\sigma}{dy} = \text{const}$$
$$y = \frac{1}{2} \ln \left(\frac{E + p_{\parallel}}{E - p_{\parallel}} \right) = \frac{1}{2} \ln \left(\frac{E + p_{\parallel}}{\sqrt{m^2 + p_T^2}} \right)$$
$$y \implies y' = y + \frac{1}{2} \ln \left(\frac{1 + \beta}{1 - \beta} \right)$$

**Frequently used $y \rightarrow \eta$ assuming massless particles
,pseudo – rapidity'**

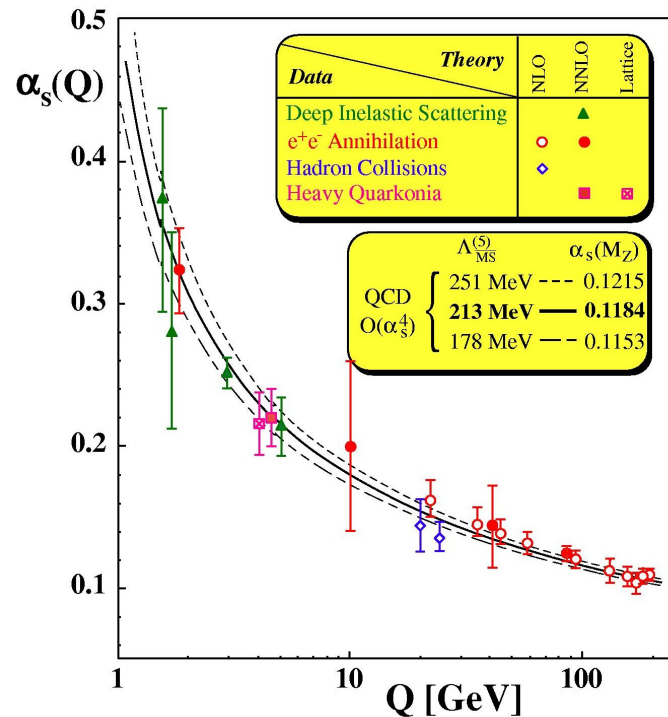
$$\eta = \frac{1}{2} \ln (\tan \theta / 2)$$

LHC a strong interaction collider



BERGISCHE
UNIVERSITÄT
WUPPERTAL

Remember: strong coupling rises with decreasing Q^2



Difficulty:
at around $Q \sim 1$ GeV
too strong to be calculable in
perturbation theory

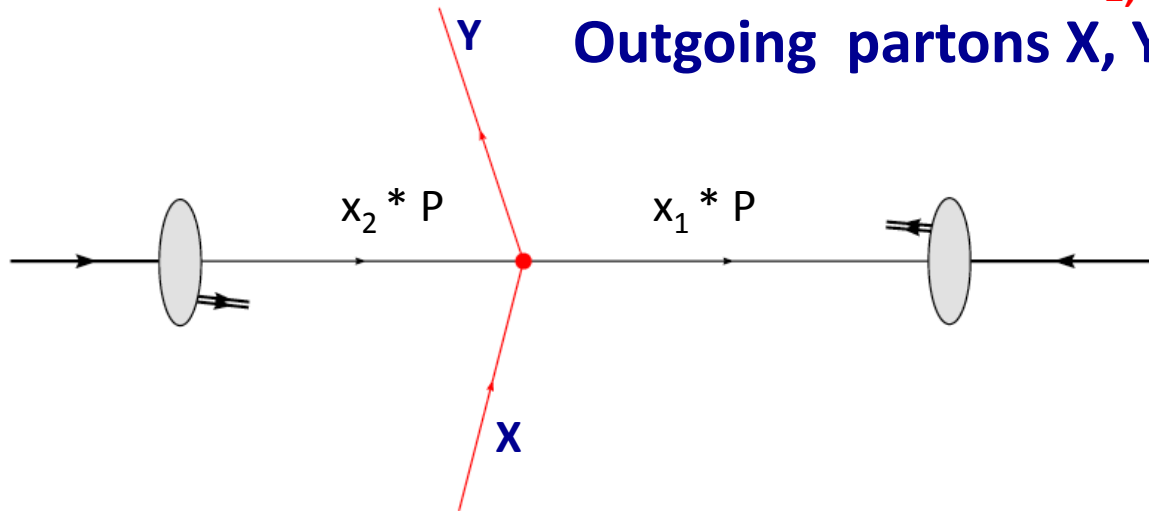
,too many gluons emitted'

Basic limitation of theoretical description

hard scatter: two in \rightarrow two out



This can be calculated:
 Incoming partons p_1, p_2 with momenta P_1, P_2
 Outgoing partons X, Y



Stefan Gieseke - DESY MC school 09

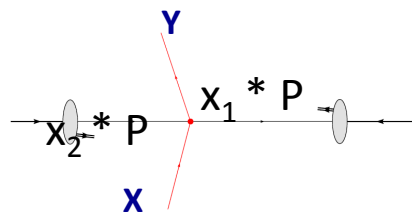
$$\sigma(p_1(P_1) + p_2(P_2) \rightarrow Y + X + \text{Rest})$$

$$= \int_0^1 dx_1 \int_0^1 dx_2 \sum_f F_f(x_1) F_{\bar{f}}(x_2) \sigma(q_1(x_1 P) + q_2(x_2 P) \rightarrow Y + X + \text{Rest})$$

Parton distribution function

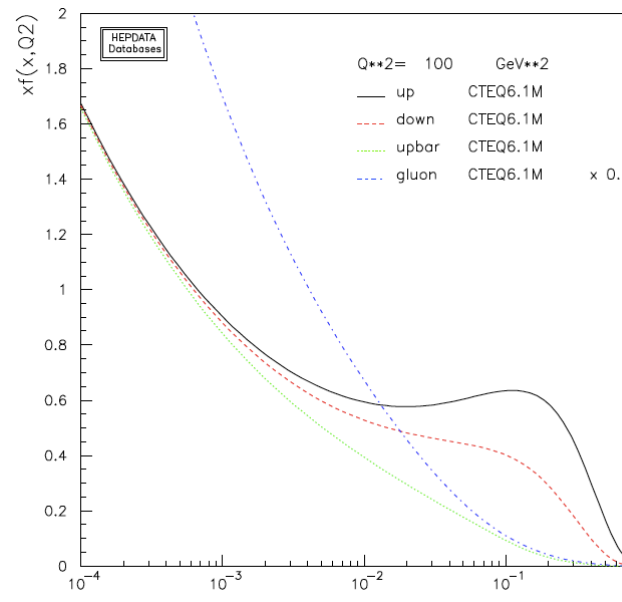


Parton momenta P_1, P_2 : fraction of proton momenta $\rightarrow x_1 P, x_2 P$
only probability distributions known



Stefan Greider - DESY MC school 09

TU/02



Interpolated from
previous data

Extrapolated to LHC
energies

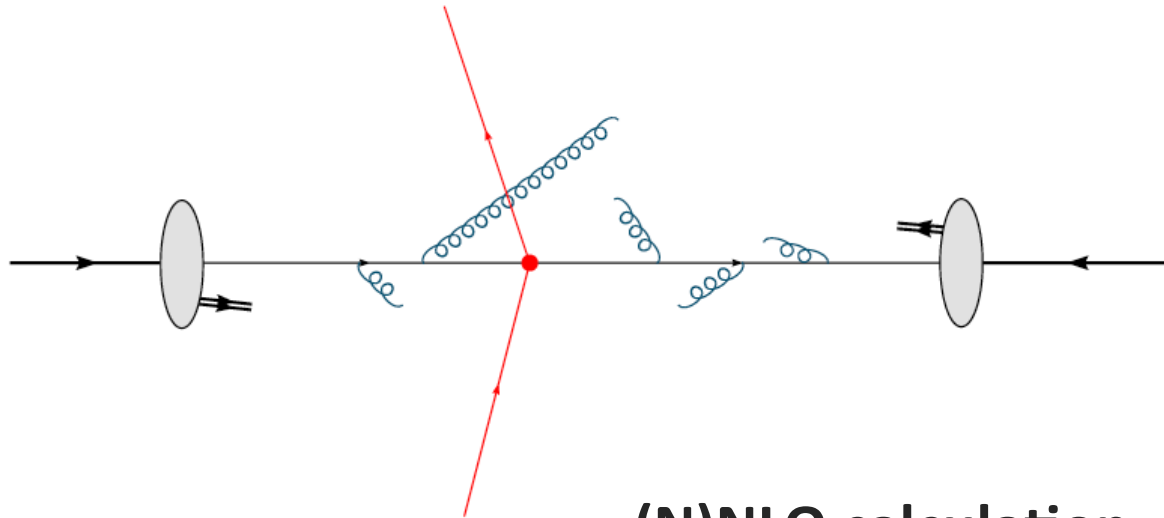
$$\sigma(p_1(P_1) + p_2(P_2) \rightarrow Y + X + \text{Rest})$$

$$= \int_0^1 dx_1 \int_0^1 dx_2 \sum_f F_f(x_1) F_{\bar{f}}(x_2) \sigma(q_1(x_1 P) + q_2(x_2 P) \rightarrow Y + X + \text{Rest})$$

Strong interaction: gluon radiation



BERGISCHE
UNIVERSITÄT
WUPPERTAL



**calculable
(although in
most cases not
completely)**

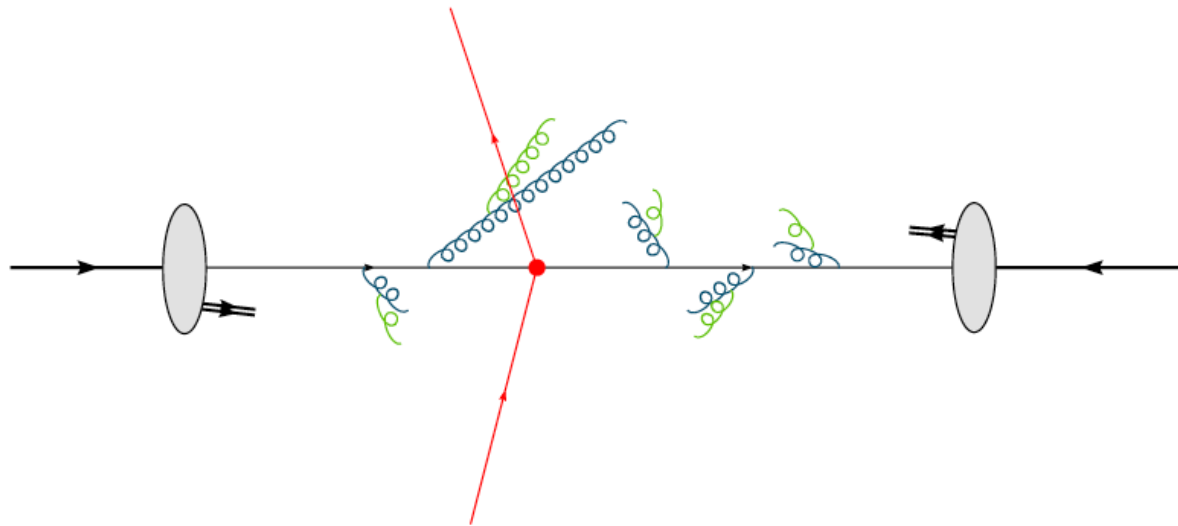
**(N)NLO calculation,
i.e. full matrix element with up to two
additional partons $\mathcal{O}(\alpha_s^3)$**

Stefan Gieseke · DESY MC school 09

A parton shower



BERGISCHE
UNIVERSITÄT
WUPPERTAL

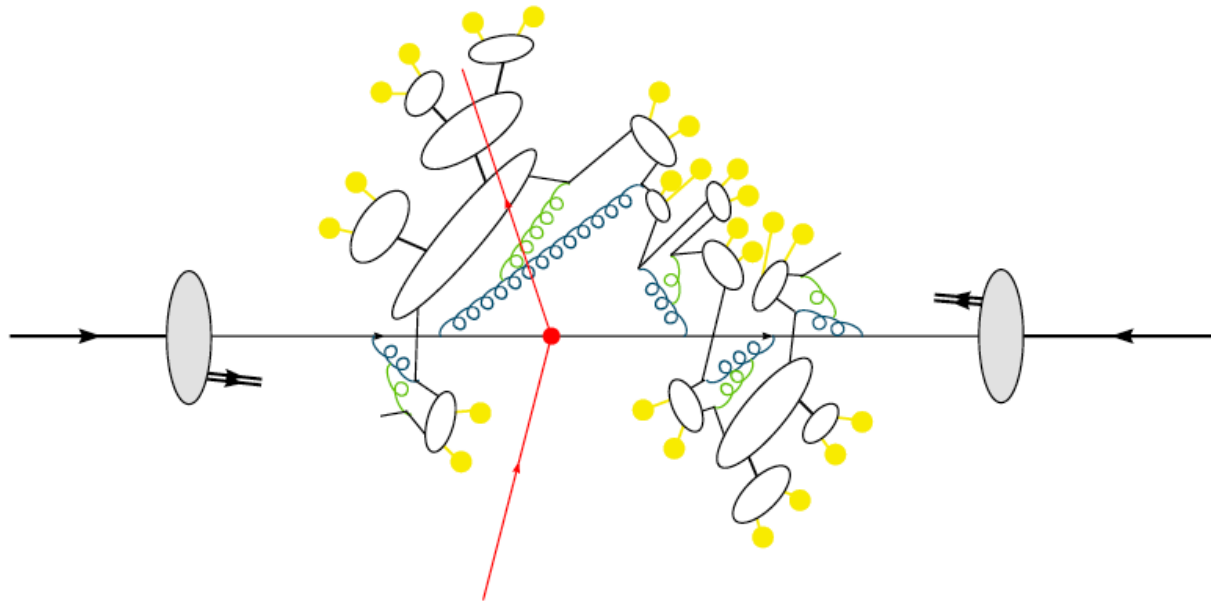


**Original hard
partons start to
,shower',
i.e. split in
gluons and
quarks**

Quarks and Gluons hadronize



BERGISCHE
UNIVERSITÄT
WUPPERTAL



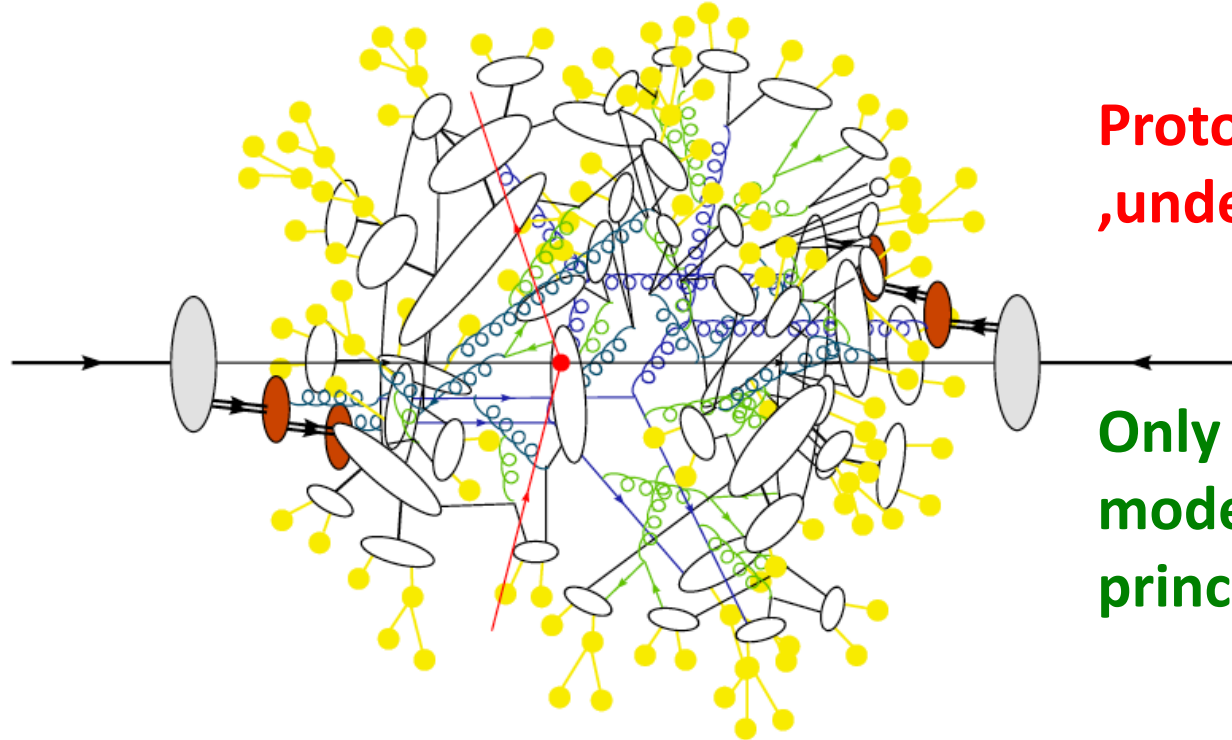
**Quarks and
Gluons turn into
pions, kaons,
protons:**

hadronisation

A more comprehensive picture



BERGISCHE
UNIVERSITÄT
WUPPERTAL



**Proton remnants interact:
,underlying event‘**

**Only QCD ,motivated‘
models – not from first
principles!**

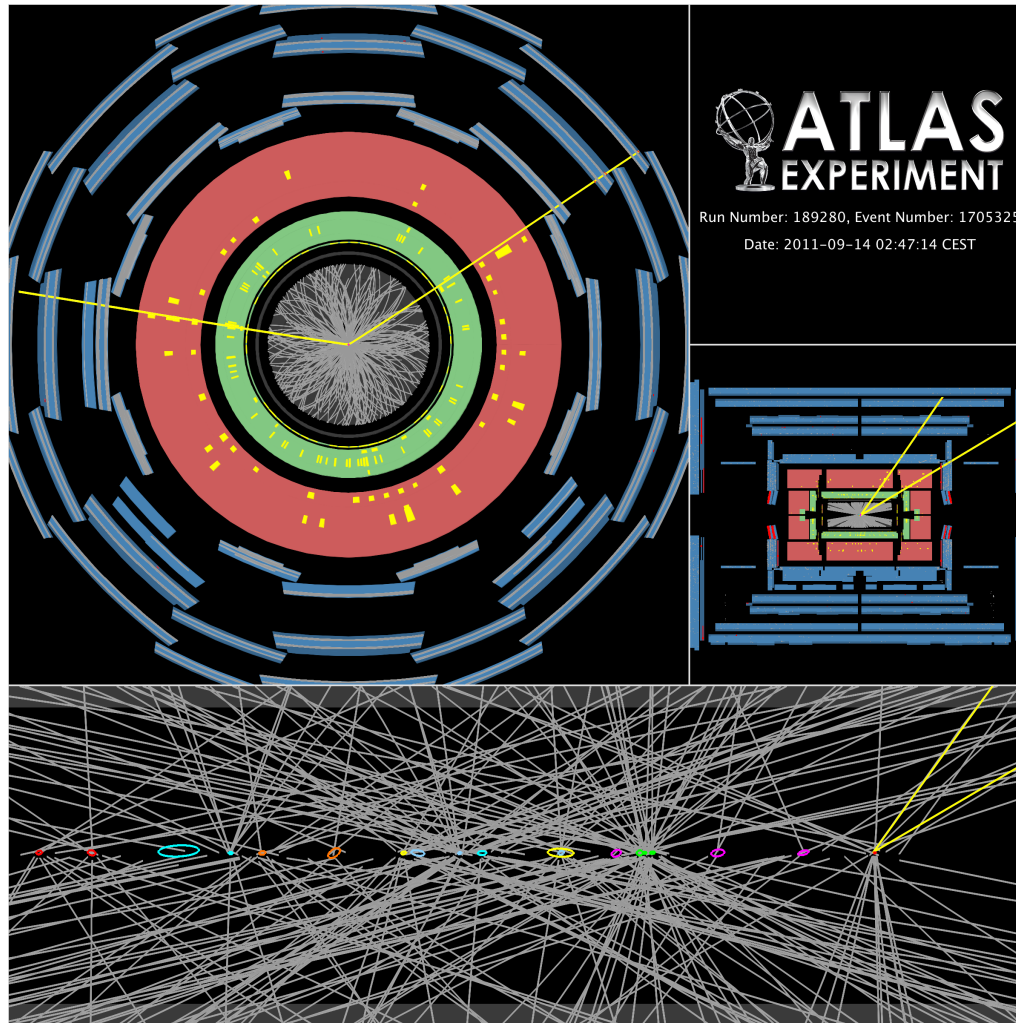
$$\sigma(p_1(\mathbf{P}_1) + p_2(\mathbf{P}_2) \rightarrow \mathbf{Y} + \mathbf{X} + \text{Rest})$$

$$= \int_0^1 dx_1 \int_0^1 dx_2 \sum_f F_f(x_1) F_{\bar{f}}(x_2) \sigma(q_1(x_1\mathbf{P}) + q_2(x_2\mathbf{P}) \rightarrow \mathbf{Y} + \mathbf{X} + \text{Rest})$$

QCD in the detector



BERGISCHE
UNIVERSITÄT
WUPPERTAL



A lot of ,isotropic' hadron production

**One bunch Xing:
Some 20 pp – interactions
,pile – up'**

**Started with
 $qq \rightarrow qq$
Result: 1000 hadrons**



Standard Model tests: Type I

Underlying event

$$= \int_0^1 dx_1 \int_0^1 dx_2 \sum_f F_f(x_1) F_{\bar{f}}(x_2) \sigma(q_1(x_1 P) + q_2(x_2 P) \rightarrow Y + X + \text{Rest})$$

$\sigma(p_1(P_1) + p_2(P_2) \rightarrow Y + X + \text{Rest})$

Take from previous measurements

Well known process

Measure underlying event



Standard Model tests: Type II

Parton distribution function

$$= \int_0^1 dx_1 \int_0^1 dx_2 \sum_f F_f(x_1) F_{\bar{f}}(x_2) \underbrace{\sigma(q_1(x_1 P) + q_2(x_2 P) \rightarrow Y + X + \text{Rest})}_{\text{Well known process}} \underbrace{\sigma(p_1(P_1) + p_2(P_2) \rightarrow Y + X + \text{Rest})}_{\text{Take from models}}$$

Measure parton
Distribution function

Standard Model tests: Type III

The hard scatter process



$$\begin{aligned}
 & \sigma(\mathbf{p}_1(\mathbf{P}_1) + \mathbf{p}_2(\mathbf{P}_2) \rightarrow \mathbf{Y} + \mathbf{X} + \text{Rest}) \\
 = & \int_0^1 dx_1 \int_0^1 dx_2 \underbrace{\sum_f F_f(x_1) F_{\bar{f}}(x_2)}_{\text{Take from previous measurements}} \sigma(\mathbf{q}_1(x_1\mathbf{P}) + \mathbf{q}_2(x_2\mathbf{P}) \rightarrow \underbrace{\mathbf{Y} + \mathbf{X} + \text{Rest}}_{\text{Take from models}}) \\
 & \quad \quad \quad \uparrow \\
 & \quad \quad \quad \text{Measure hard process}
 \end{aligned}$$



In a nutshell:

Hard process

= (data

- pile up events from simultaneous pp – collisions
- underlying event from proton remnants)

x (transfer from jets → partons)

x (unfolding of parton energies = parton distribution fct.)

Involved,

..... but with experimental knowledge feasible

Key ingredients to use data



BERGISCHE
UNIVERSITÄT
WUPPERTAL

- pile up events = multiple proton – proton interactions in one bunch crossing
- ‚underlying event‘
- transfer function (partons → hadrons)
- Parton distribution functions

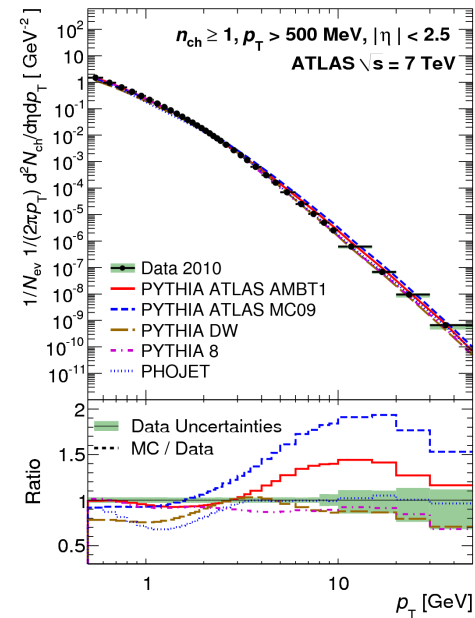
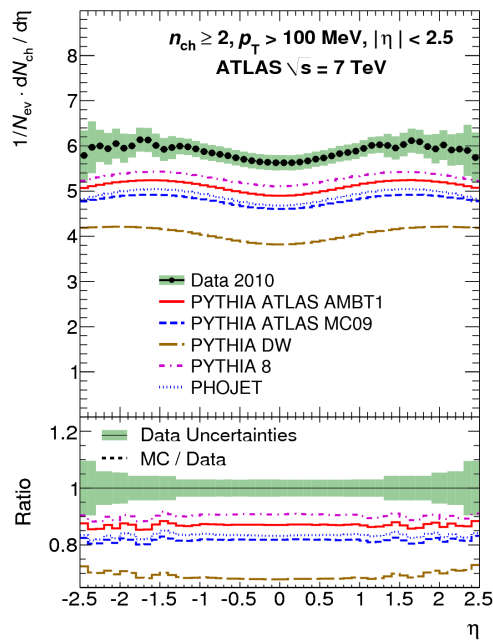
Pile up events



Pile – up events can be measured:

pp – interactions without trigger bias ,minimum bias events‘

At 7 TeV: 6 charged particles per $|\Delta\eta| = 1$, mostly low p_T



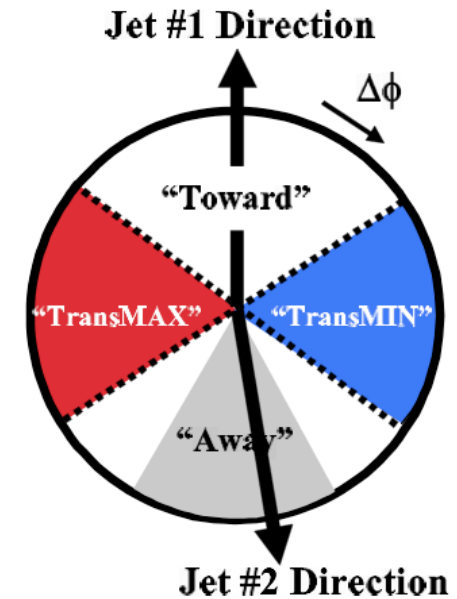
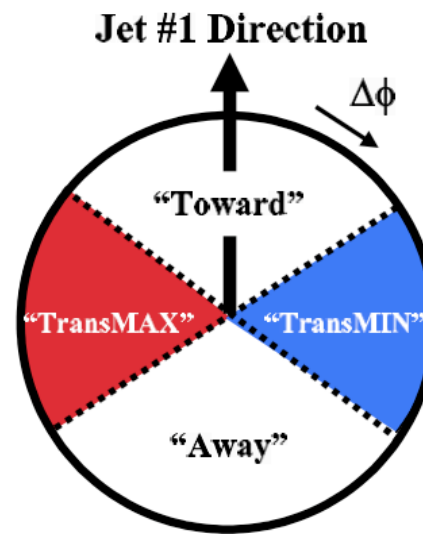
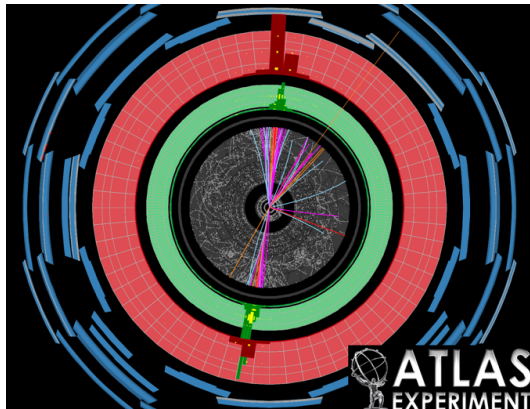
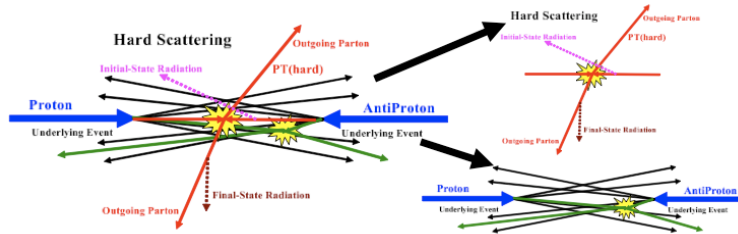
No good description by models

Note: per LHC bunch crossing \sim currently 20 of these events

Underlying events



BERGISCHE
UNIVERSITÄT
WUPPERTAL

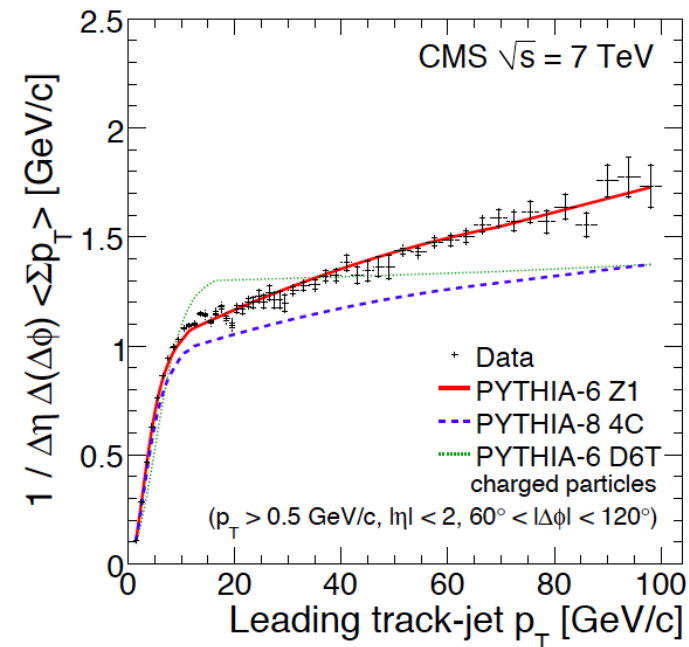
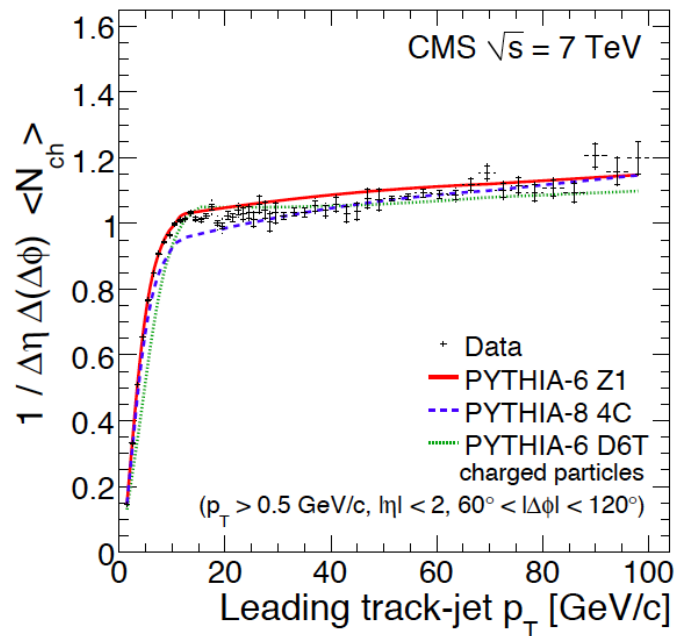


**Transverse regions little affected by hard process
→ properties like underlying event**

Particle distributions in UE events



BERGISCHE
UNIVERSITÄT
WUPPERTAL



Can be reasonably described by models

Modelling 'soft interactions'



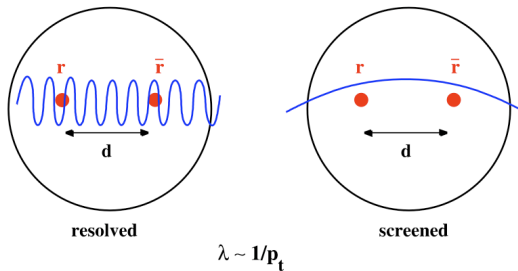
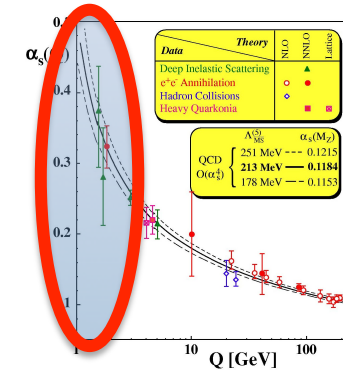
BERGISCHE
UNIVERSITÄT
WUPPERTAL

Minimum bias + underlying events:

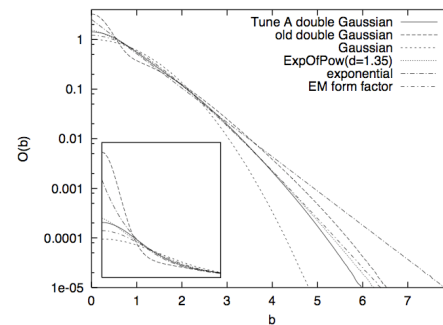
Measured in special environment

Extrapolate to all conditions:

try to model applying several ad – hoc concepts

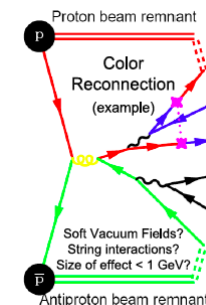


Colour screening



Colour reconnection

Overlap of protons



Challenging! Only an approximate description possible!

Parton distribution functions



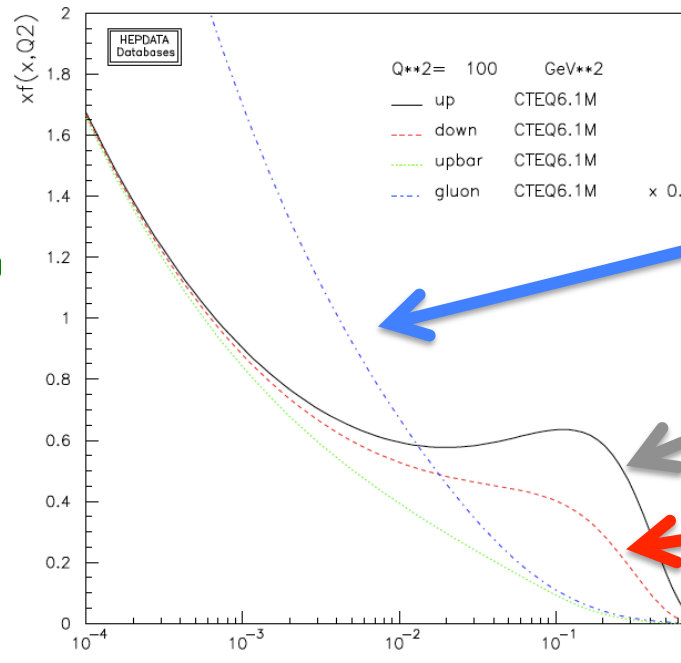
Energy fractions of different kinds of partons f in proton

$$\sigma(p_1(P_1) + p_2(P_2) \rightarrow Y + X + \text{Rest})$$

$$= \int_0^1 dx_1 \int_0^1 dx_2 \sum_f F_f(x_1) F_{\bar{f}}(x_2) \sigma(q_1(x_1 P) + q_2(x_2 P) \rightarrow Y + X + \text{Rest})$$

Various measurements
at M^2_1
theoretical evolution to
 $(M^2)_2$

Just one of several
pdf parametrisations



Gluons

Up quarks

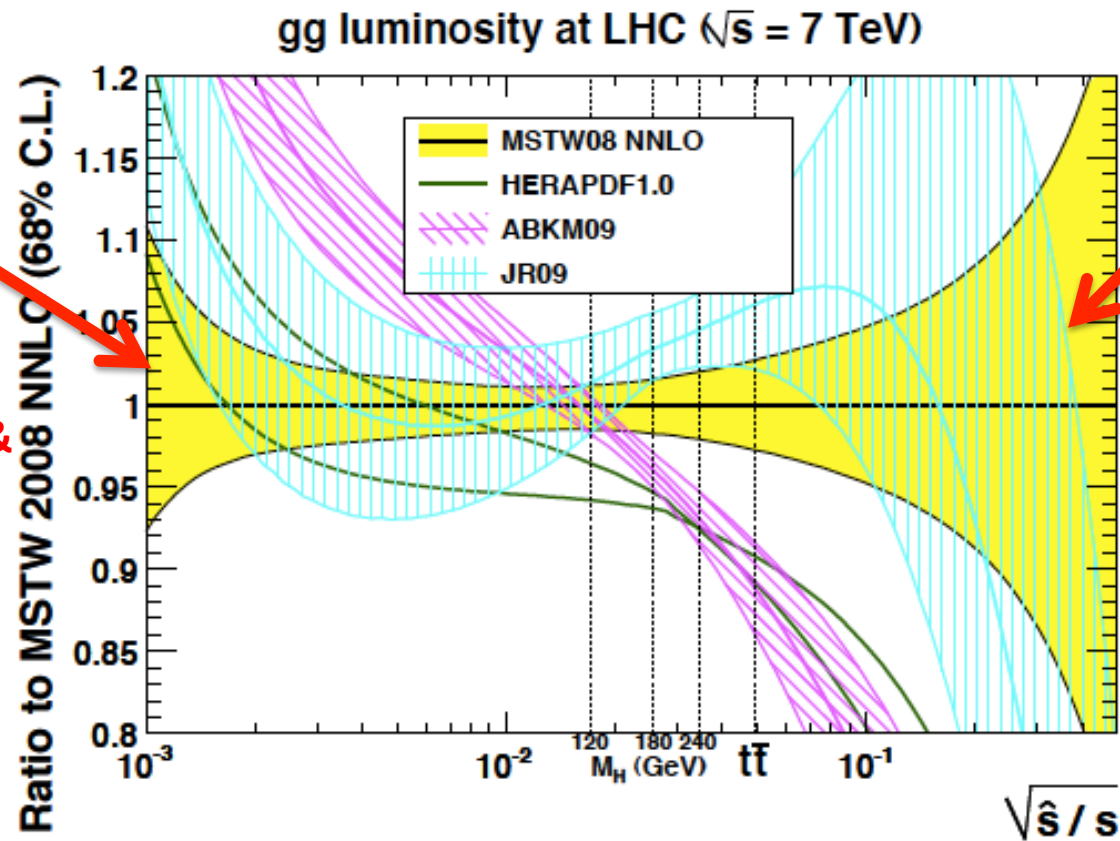
Down quarks

Significant uncertainties



G.Watt

low x:
many gluons
→ Theoretical &
experimental
uncertainties



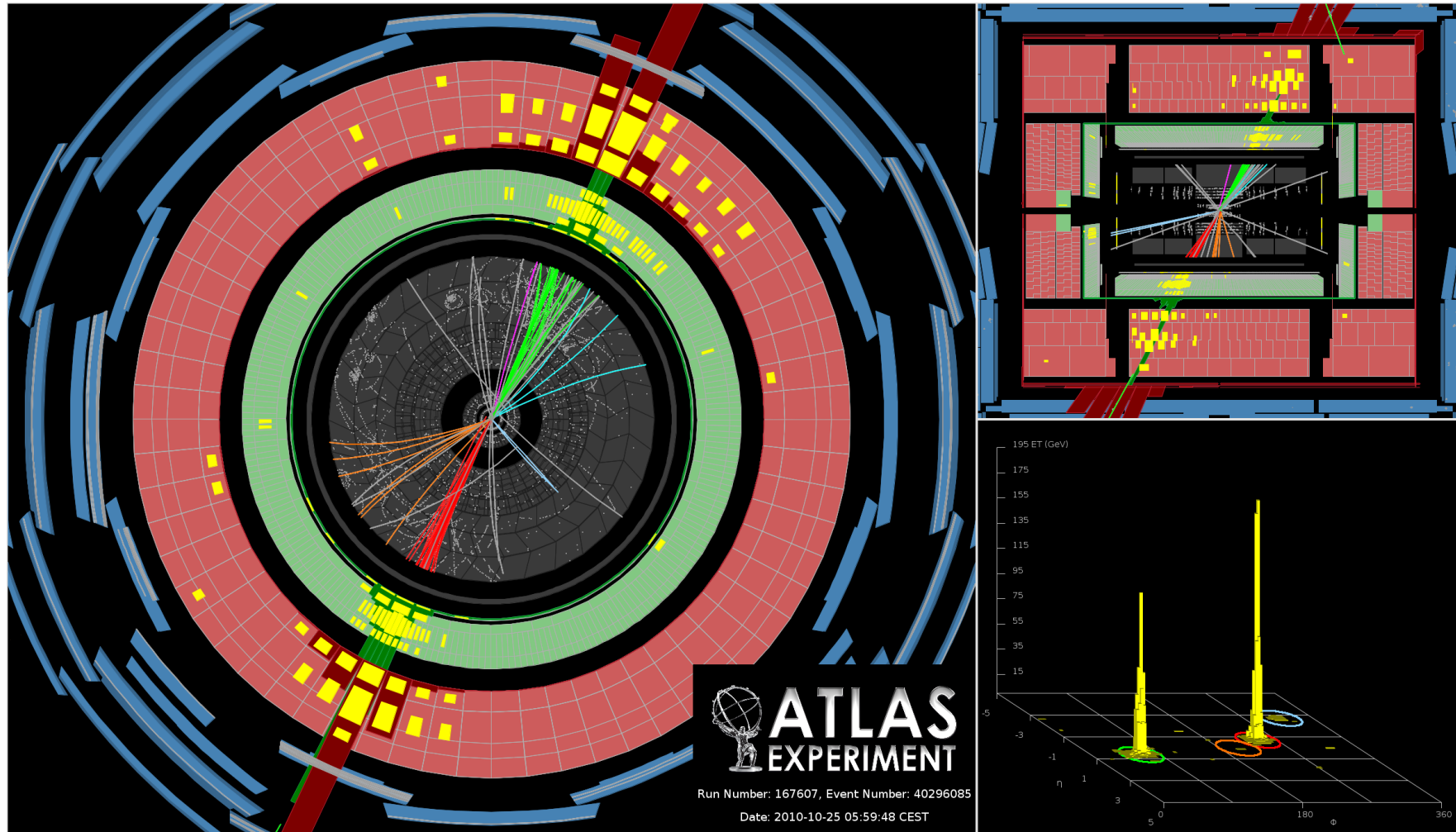
High x:
few gluons
→ Large
uncertainty

LHC will allow some self - calibration

Hard interaction: Jets



BERGISCHE
UNIVERSITÄT
WUPPERTAL

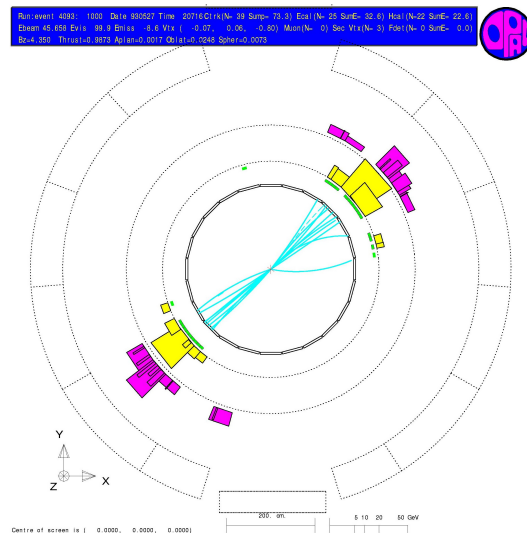


Jets are universal

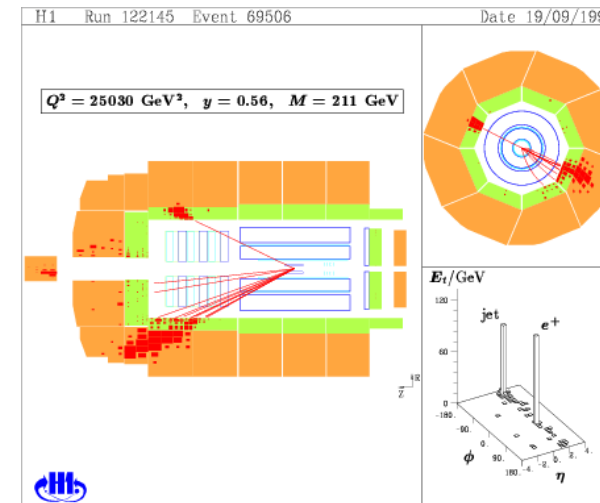


BERGISCHE
UNIVERSITÄT
WUPPERTAL

$e^+ e^-$ collisions



$e p$ collisions

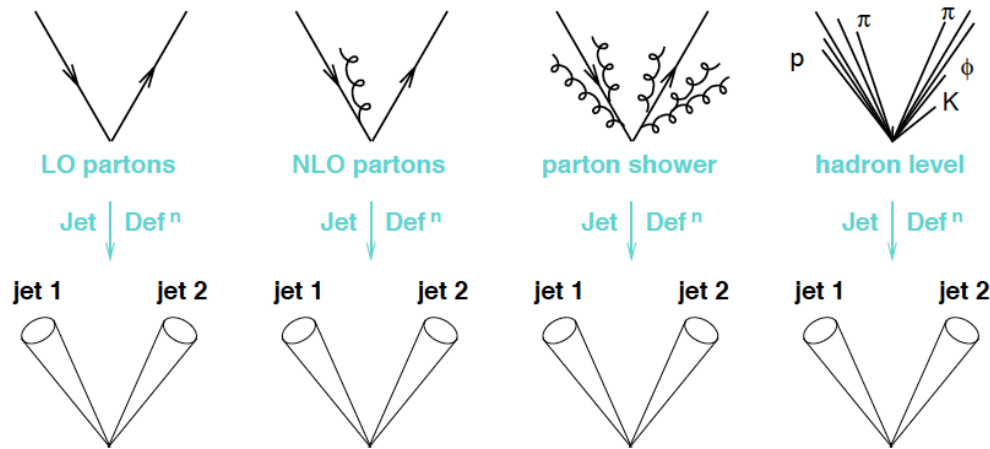


Jets: representative of quarks and gluons

- stringent test of theory**
- experimental challenge: extract partons from 1000 hadrons**
- experimentally attainable**
direction and energy + (sometimes) parton flavour

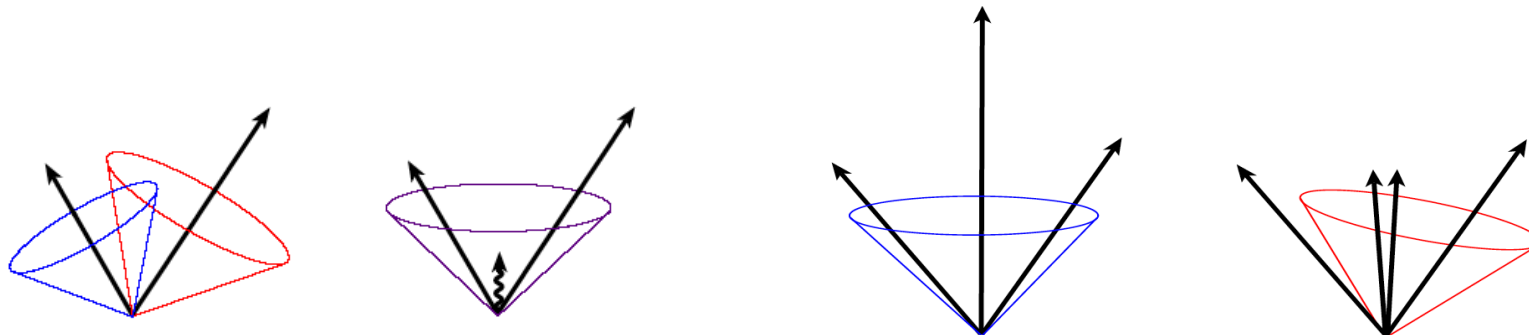


How to find a jet ?



**Unambiguous
connection to
underlying partons →
Comparison to theory**

Not so straight – forward: example cone – jet finder





Sequential jet finder

„Reverse evolution of event“

- 1 Select one particle (e.g. most energetic)**
- 2 Find ‚most similar‘ particle, (e.g. smallest angle, p_t)**
- 3 Is combination smaller than predefined ‚cut off‘ value (e.g. maximum angle, maximum mass)**

IF YES:

- 4 Combine to a new ‚pseudo – particle‘ (e.g. sum 4 – momenta)**
- 5 Go to 2**

IF NO:

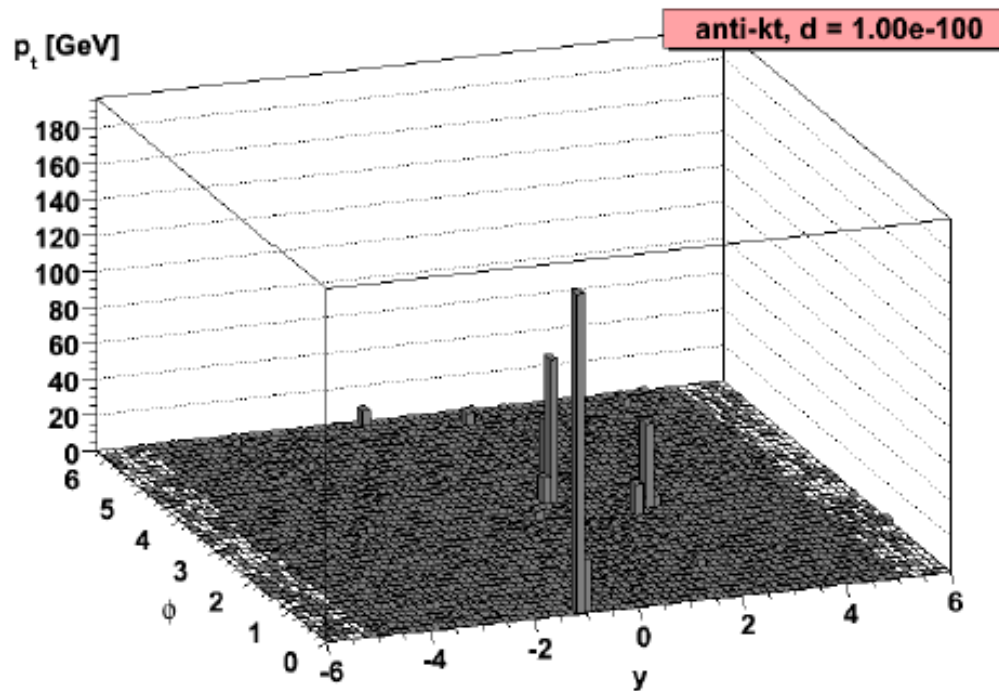
- 4 Jet found: sum of all associated particles**

Standard jet finding at LHC: ,Anti – kt‘

$$d_{ij} = \min(p_{ti}^{-2}, p_{tj}^{-2}) \frac{\Delta R_{ij}^2}{R^2}$$

© Gavin Salam

$$\Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$



Select hard particles as ,seeds‘ for jets: favoured by $\min(p_t^2)$

Hard particles separated in space are distinct seeds: large ΔR_{ij}

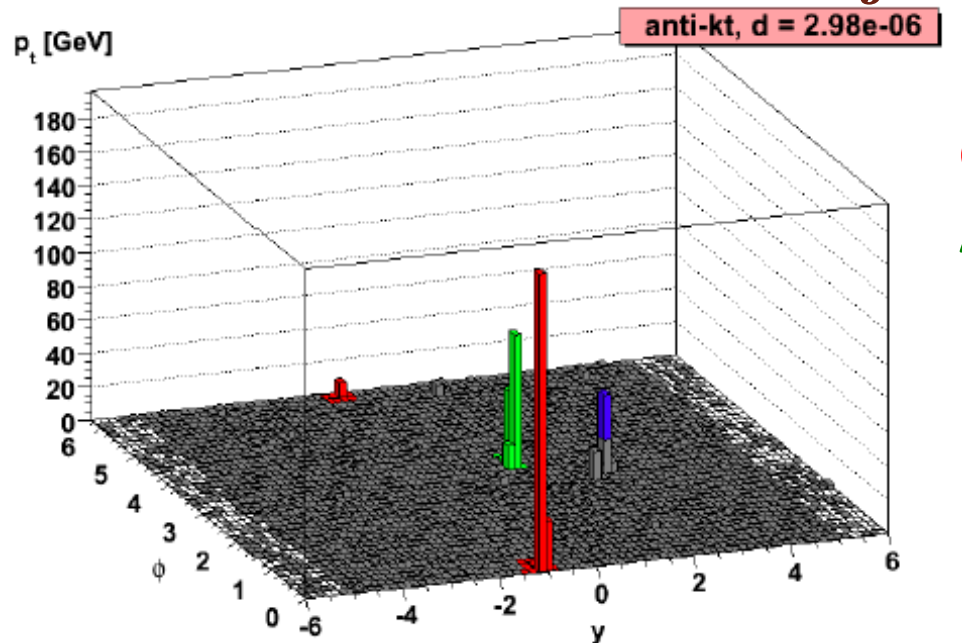
,cut off‘ given by d_{ij} (steered by R)

Standard jet finding at LHC: 'Anti - kt'

$$d_{ij} = \min(p_{ti}^{-2}, p_{tj}^{-2}) \frac{\Delta R_{ij}^2}{R^2}$$

$$\Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

© Gavin Salam

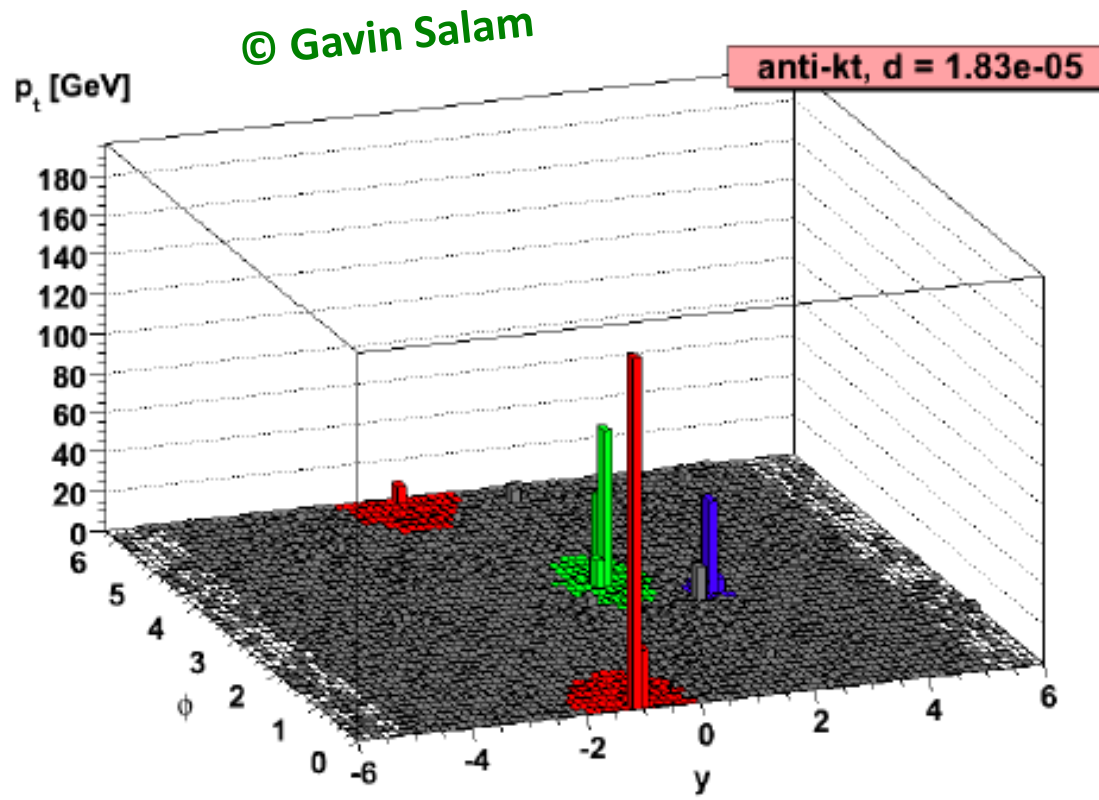


Gradual d_{ij} increase:
Associate close by particles:
mostly soft ones in
neighbourhood

(if no hard ones close by)

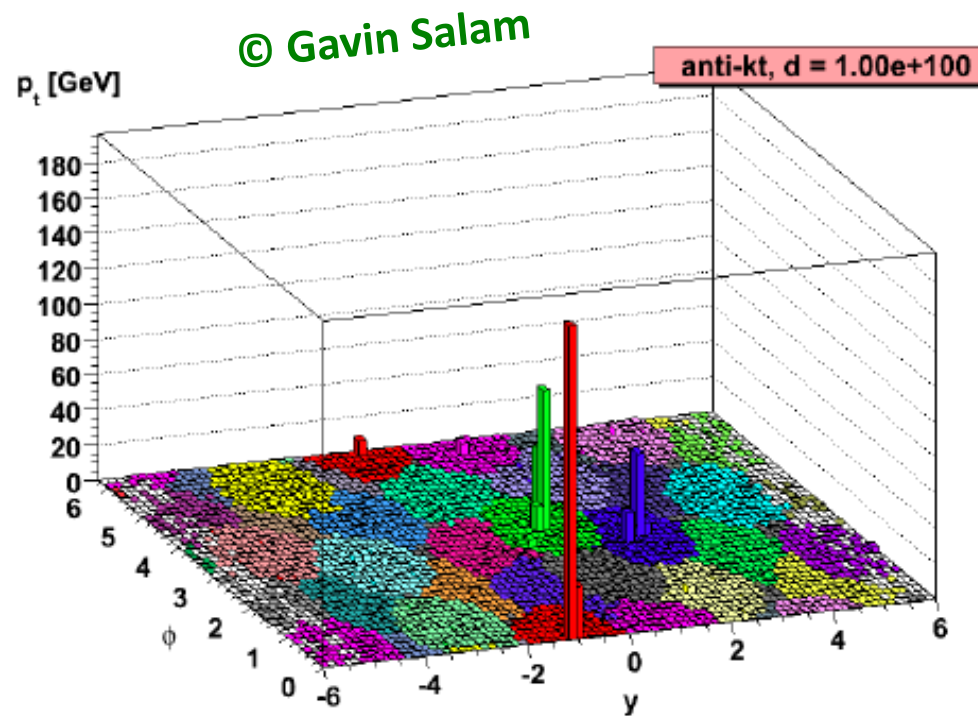
Standard jet finding at LHC: „Anti – kt“

Intermediate step: emerging jet cones





The final jets



All particles assigned to jets

Close to circular in space
good for experimental
corrections

Note: special treatment
of particles close to beam



Physics from Jet measurements @ hadron - colliders

- crucial for understanding background
- tests of QCD predictions at highest reachable energies (inclusive jets, jj – masses, multi – jets)
- will help sorting out parton distribution functions
- tests of physics beyond SM

The experimental challenge I

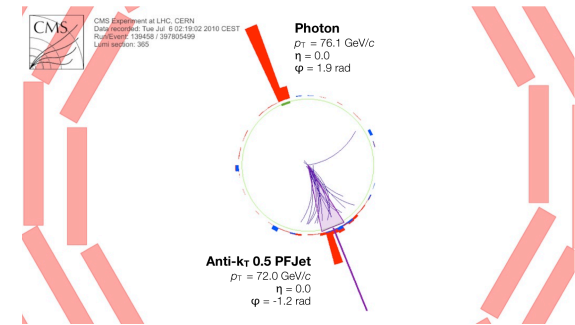
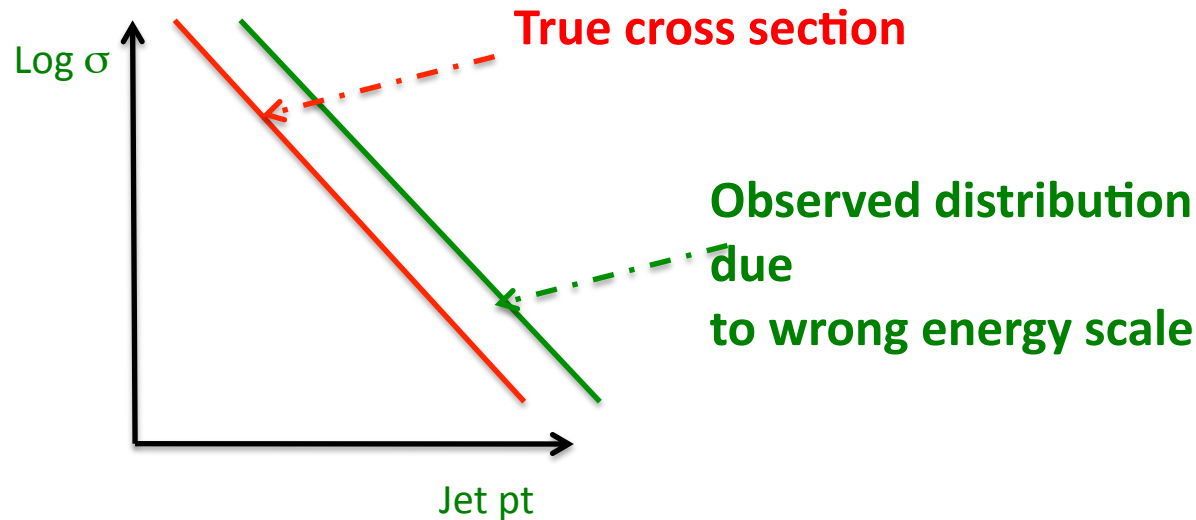


BERGISCHE
UNIVERSITÄT
WUPPERTAL

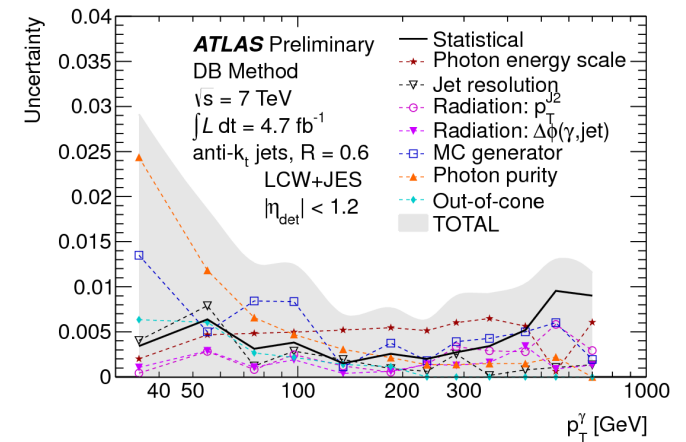
Steeply falling cross section → sensitivity to energy scale

Jet energy determined from calorimeter (+ tracking information)

Sophisticated calibration procedure



Use γ + jet events:
Jet energy scale known to 1 – 3%!

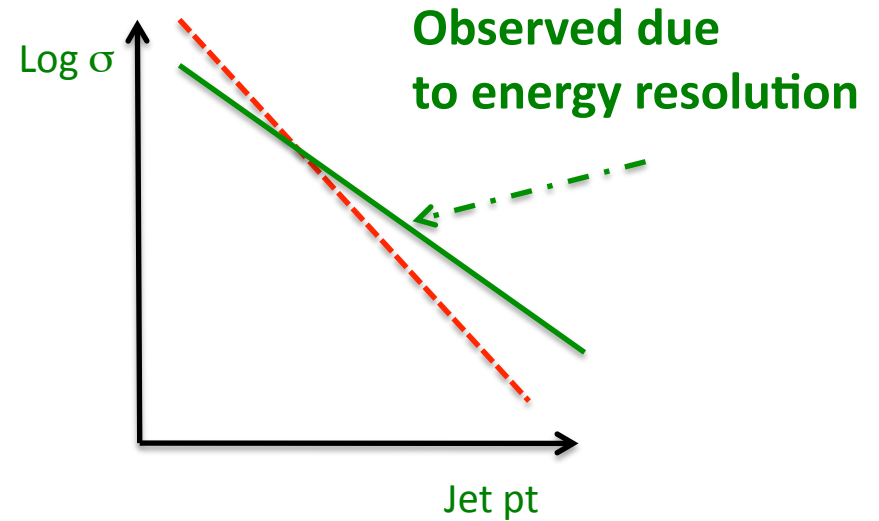
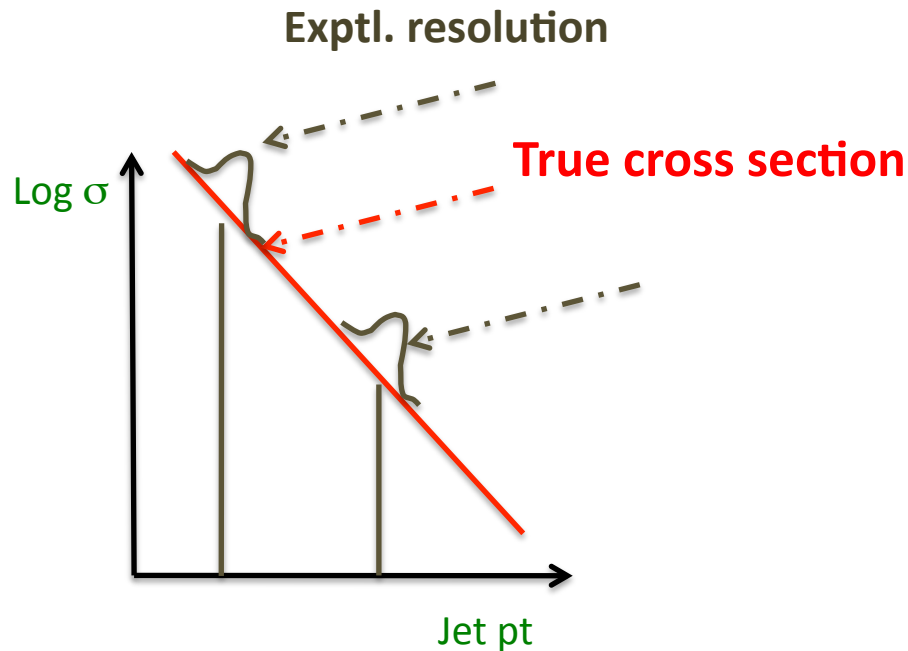
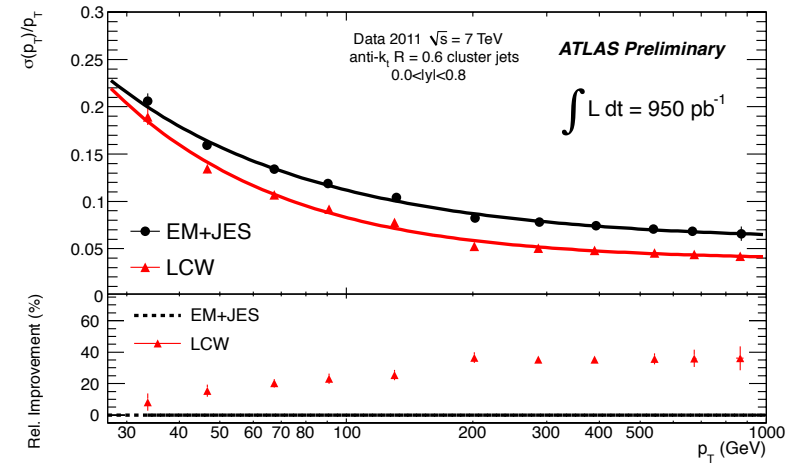


The experimental challenge II



BERGISCHE
UNIVERSITÄT
WUPPERTAL

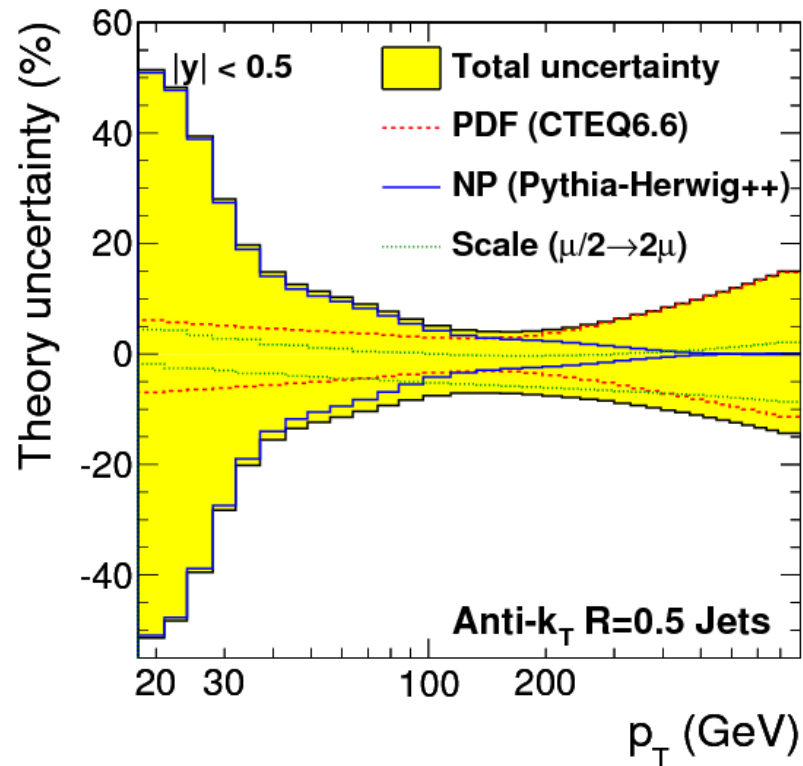
sensitivity to energy resolution



Uncertainties: summary



BERGISCHE
UNIVERSITÄT
WUPPERTAL



**Experimental uncertainties
dominate at low p_T**

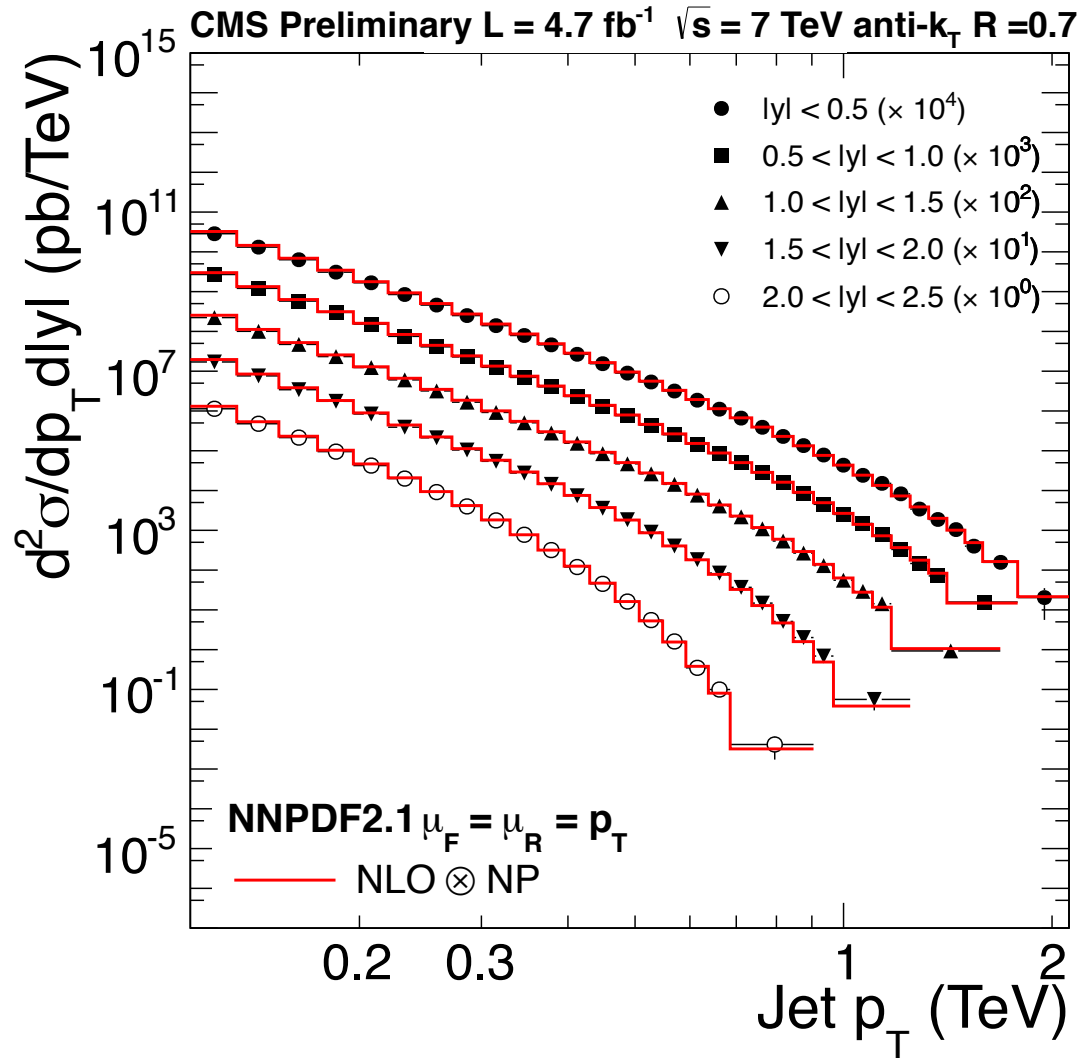
**pdf/theoretical uncertainties
dominate at high p_T**

**Note: loss of control of
uncertainties for $p_T < 20$ GeV**

Jet cross sections in rapidity and pT



BERGISCHE
UNIVERSITÄT
WUPPERTAL



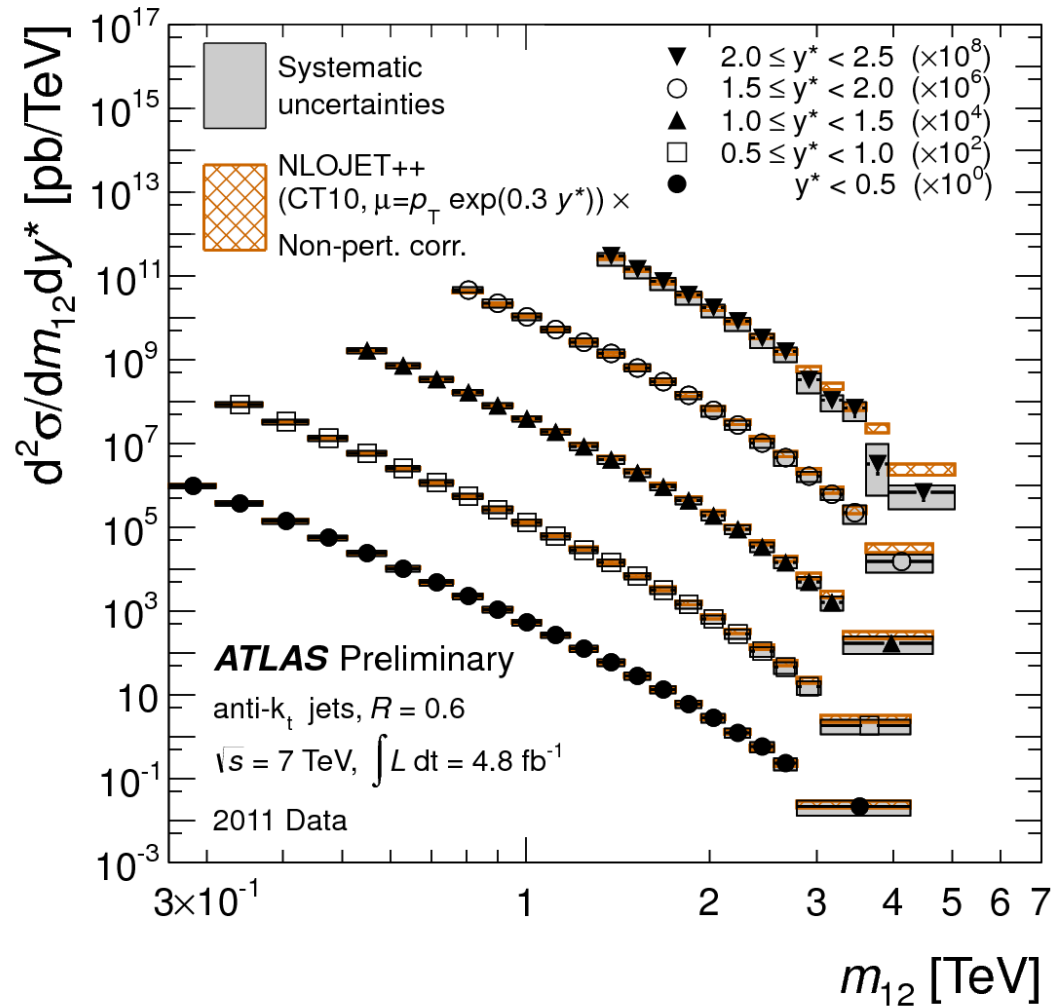
Excellent agreement
theory \leftrightarrow data

over huge range in
phase space

jet – jet mass



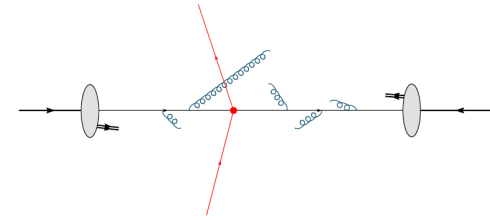
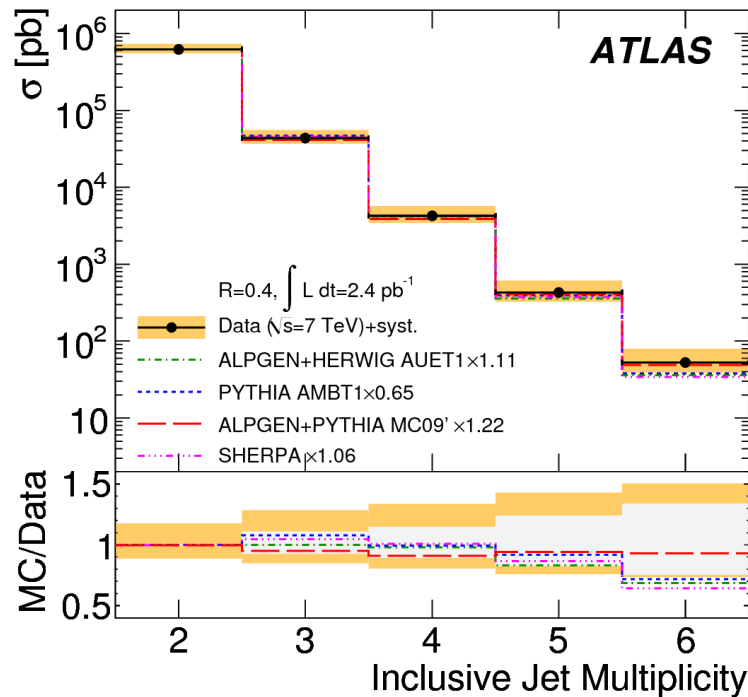
BERGISCHE
UNIVERSITÄT
WUPPERTAL



Excellent agreement
theory \leftrightarrow data

Probing masses up
to 5 TeV!

QCD effects: number of jets

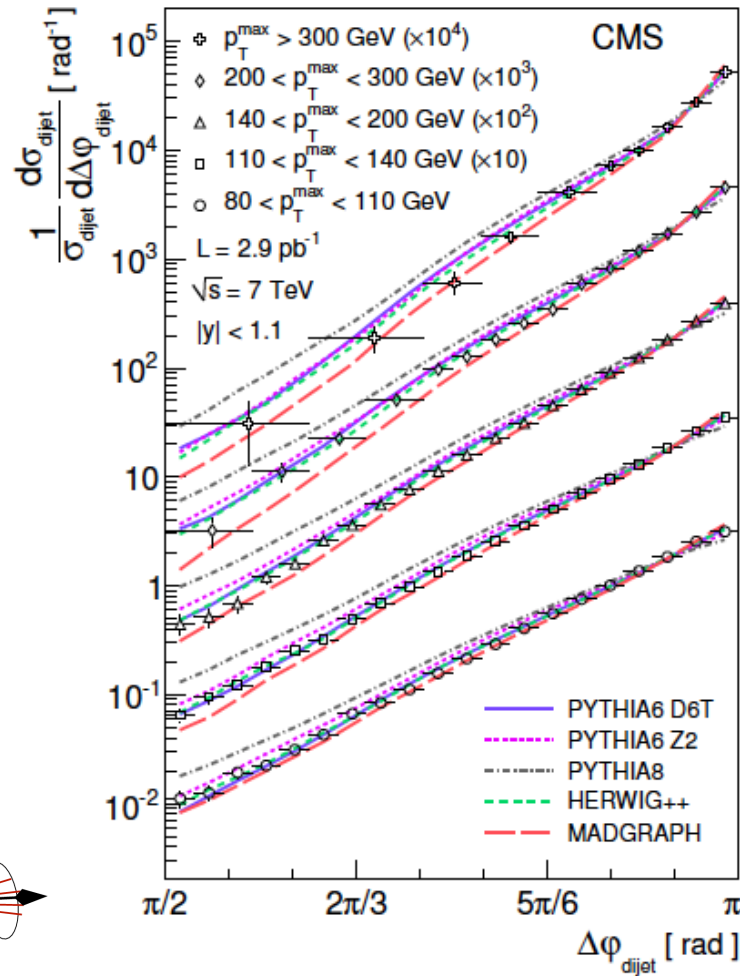


Stefan Gieseke - DESY MC school 09

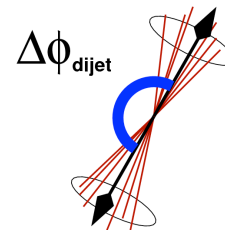
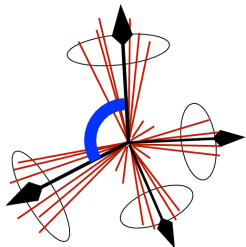
11/42

**Even though not exact
matrix element:
Good agreement on
jet multiplicity**

The effects of gluon radiation



Azimuthal angle between leading, i.e. highest p_T jets



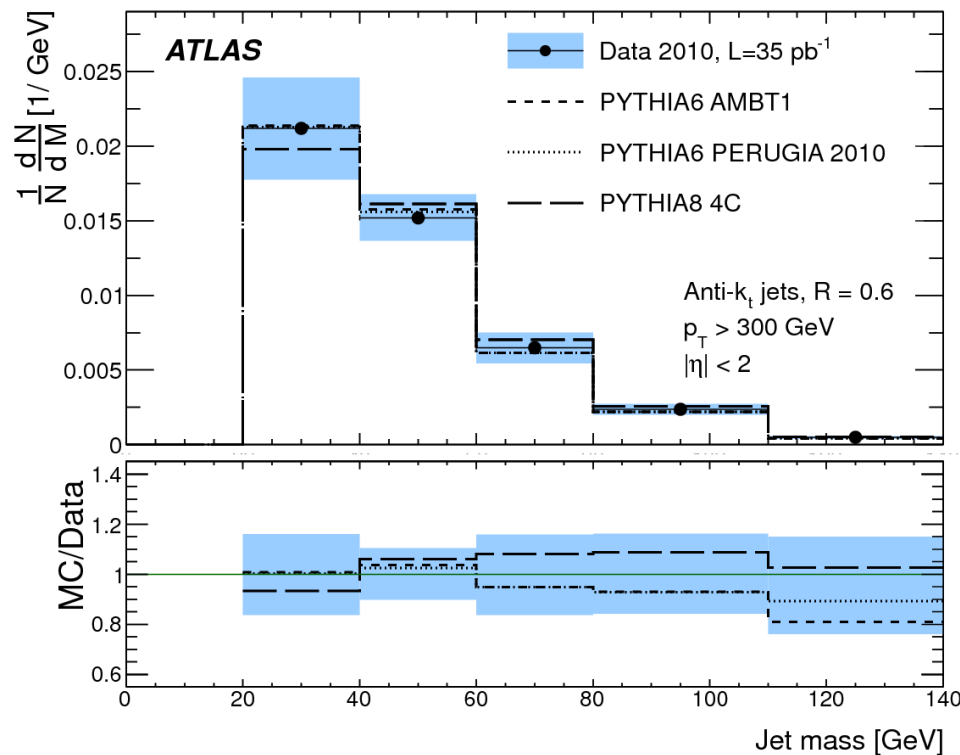
High p_T Jets



High p_T jets: important to explore TeV scale physics

May be due to boosted objects → substructure

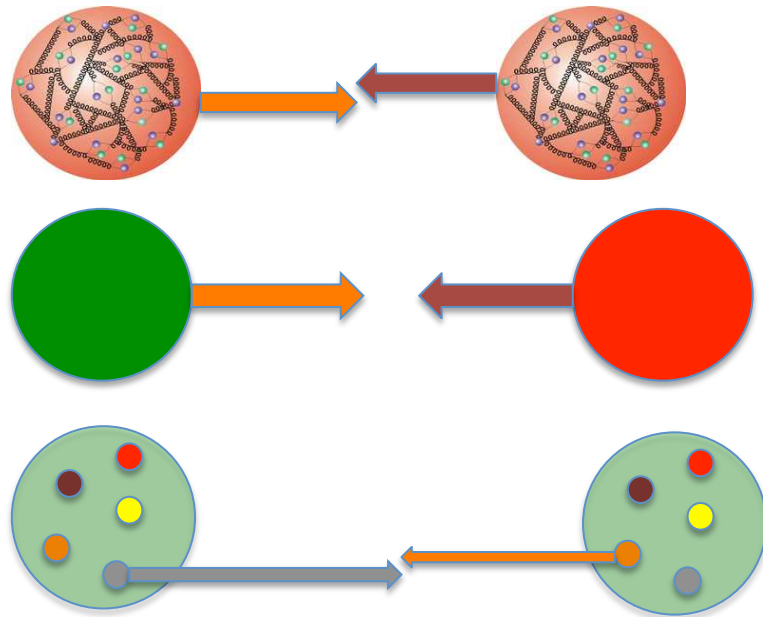
Important: does QCD describe the structure of boosted jets?



Measure mass of high p_T jet:

Good agreement with
expectation found

**Testing high p_T – jets = search for BSM:
Are partons composite?**



pp – interaction



qq – interaction



**interaction of quark
constituents ????**

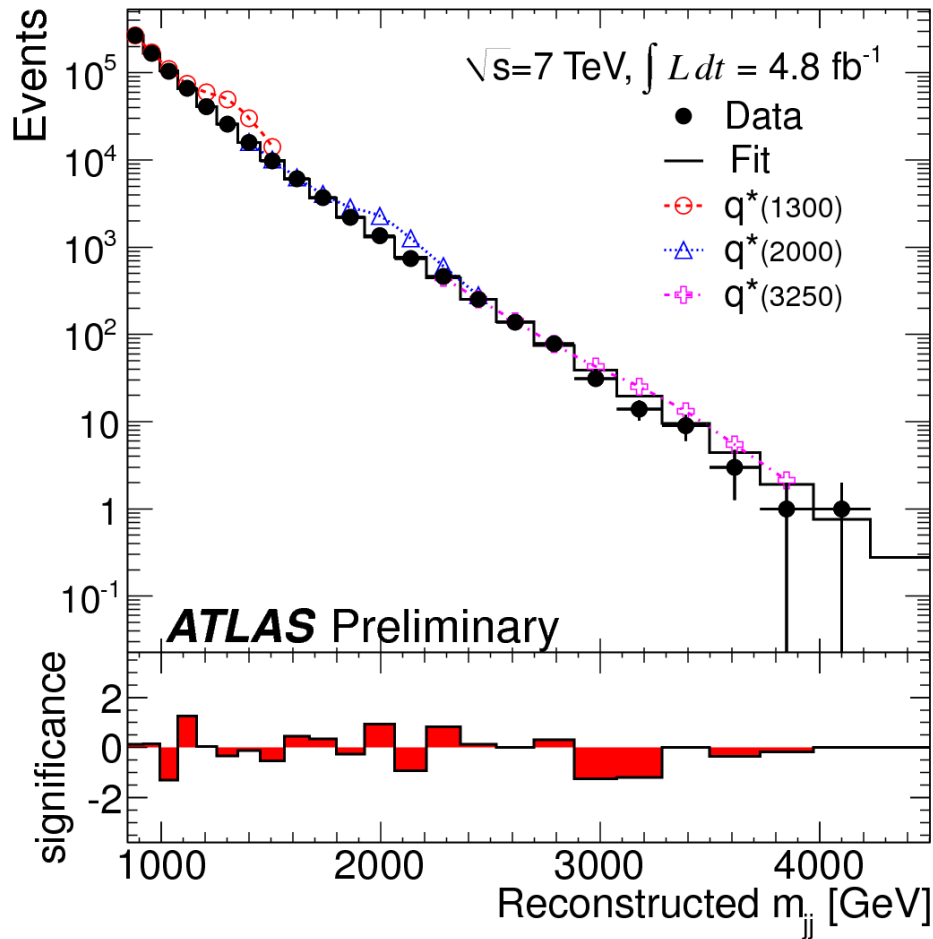
$$\mathcal{L}_{CI} = \frac{g^2}{\Lambda^2} \eta_{LL} (\bar{\psi}_L \gamma^\mu \psi_L) (\bar{\psi}_L \gamma_\mu \psi_L) + (RR, LR)$$

$$\sigma_{ff} = |\mathcal{M}_{SM}|^2 + 2 \frac{1}{\Lambda^2} \mathcal{RE}(\mathcal{M}_{SM} \cdot \mathcal{M}_{CI}) + \frac{1}{\Lambda^4} |\mathcal{M}_{CI}|^2$$

Jets and BSM: Search for di – jet resonances



BERGISCHE
UNIVERSITÄT
WUPPERTAL



An excited quark ?

$q^* \rightarrow q + g$

(Remember excited atom, nucleus)

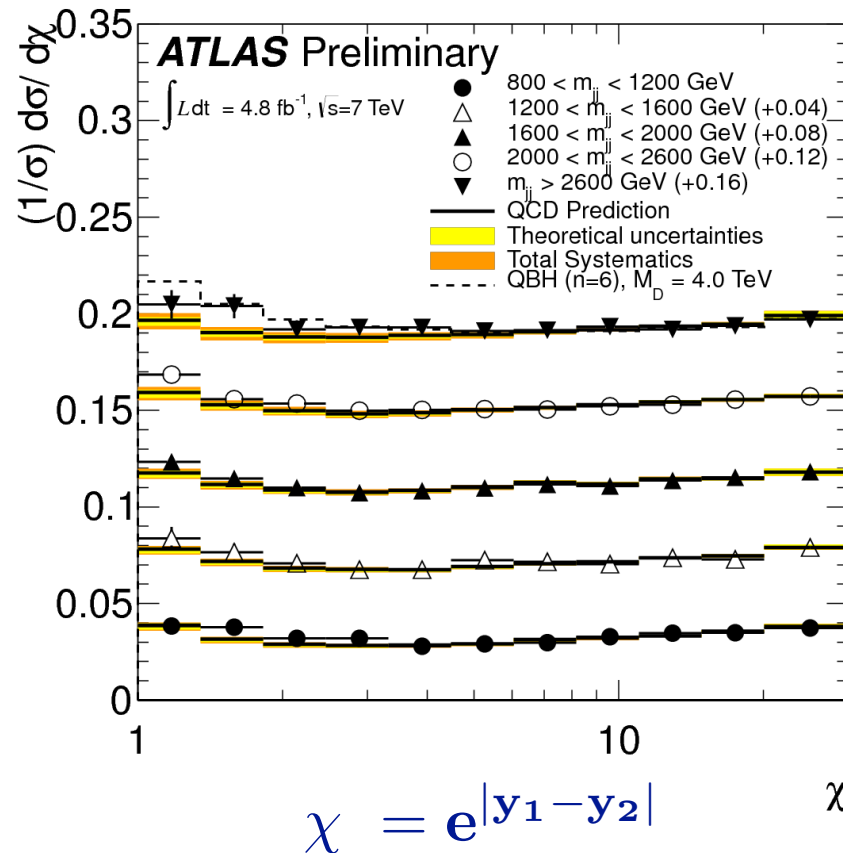
Would be strong signal for compositeness

Search for resonance: enhancement

Are quarks composite ?



BERGISCHE
UNIVERSITÄT
WUPPERTAL



Compositeness

→ modify angular distribution

**continuous change with higher
jet – jet mass**

**No deviation from SM observed:
 $\Lambda > 7.8 \text{ TeV}$**

**Note: results applicable to other exotic models:
black – holes, colour octet quarks,**

Strong interactions at core of pp –interactions

- **Multihadron events (soft interactions) measured**
- **Jet cross sections agree with predictions over a wide range**
- **Probing Multi - TeV range: no sign for physics Beyond Standard Model**