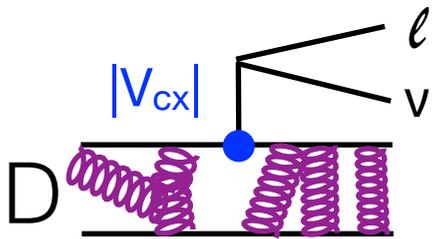


# Semileptonic Charm Decays

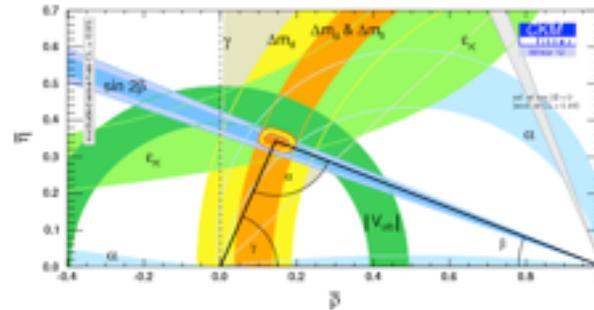
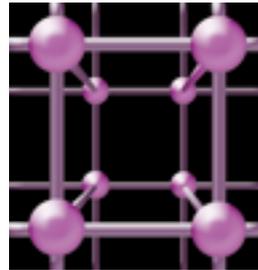
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Jonas Rademacker on behalf of CLEO

# Semileptonic Charm Decays



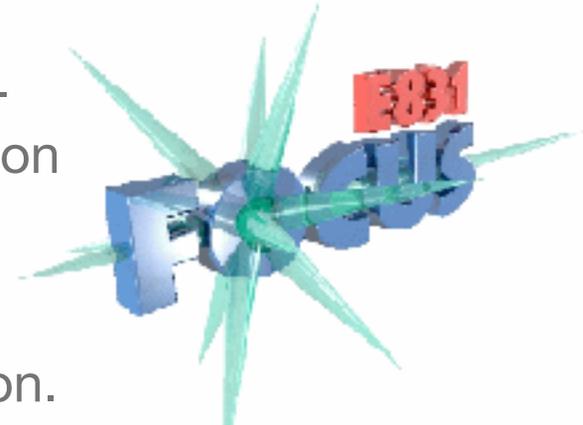
- Measure  $|V_{cx}| \times (\text{QCD-form factor(s)})$ . Take  $|V_{cx}|$  from CKM unitarity to extract form factors, test LQCD. Or input LQCD and test CKM-unitarity.



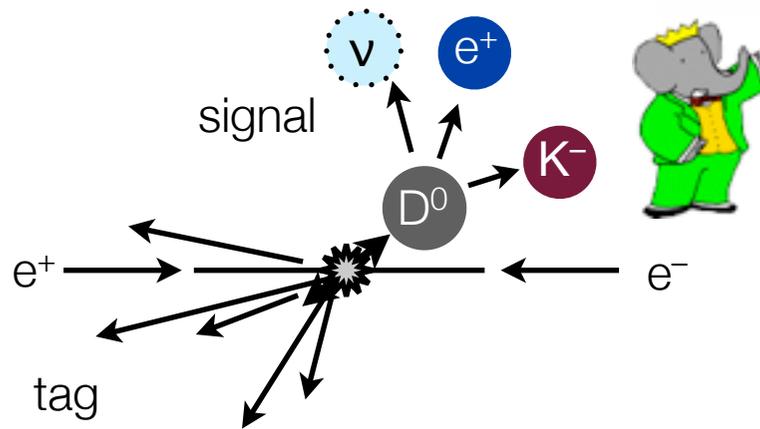
- Study S-wave in  $D \rightarrow K\pi\ell\nu$ ,  $D \rightarrow \pi\pi\ell\nu$ ,  $D_s \rightarrow K\ell\nu$
- Search for rare/forbidden modes like  $D_s \rightarrow \omega\ell\nu$  to study the structure of the  $D_s$  and long-distance effects.
- Input to B physics
  - Validate LQCD form factor calculations, relied upon in extracting  $|V_{ub}|$
  - Combine  $D \rightarrow \rho\ell\nu$ ,  $D \rightarrow K^*\ell\nu$ ,  $B \rightarrow V \ell \ell$  to improve  $|V_{ub}|$  (Phys.Rev. D70 (2004) 114005)
  - S-waves in  $D \rightarrow \pi\pi\ell\nu$  helped motivate use of  $B_s \rightarrow J/\psi f_0$  for  $\phi_s$ .

# Experimental Challenge: Find the $\nu$ in $D \rightarrow h \ell \nu$

- FOCUS: Get direction of D from vertex information, and 4-momenta of charged decay products  $\Rightarrow$  enough information to reconstruct  $\nu$ .
- BaBar: Get direction of the D from momentum conservation.



$$\vec{p}_D \propto - \sum_{\text{all except } e, K \text{ from } D} \vec{p}_i$$



**BABAR**

- BELLE: Fully reconstruct tag side as  $D^* X$ . Better resolution than BaBar's method, but less statistics.

(see also Andrzej Bozek's talk on Tue)



- All much cleaner at threshold...



Semileptonic Charm Decays

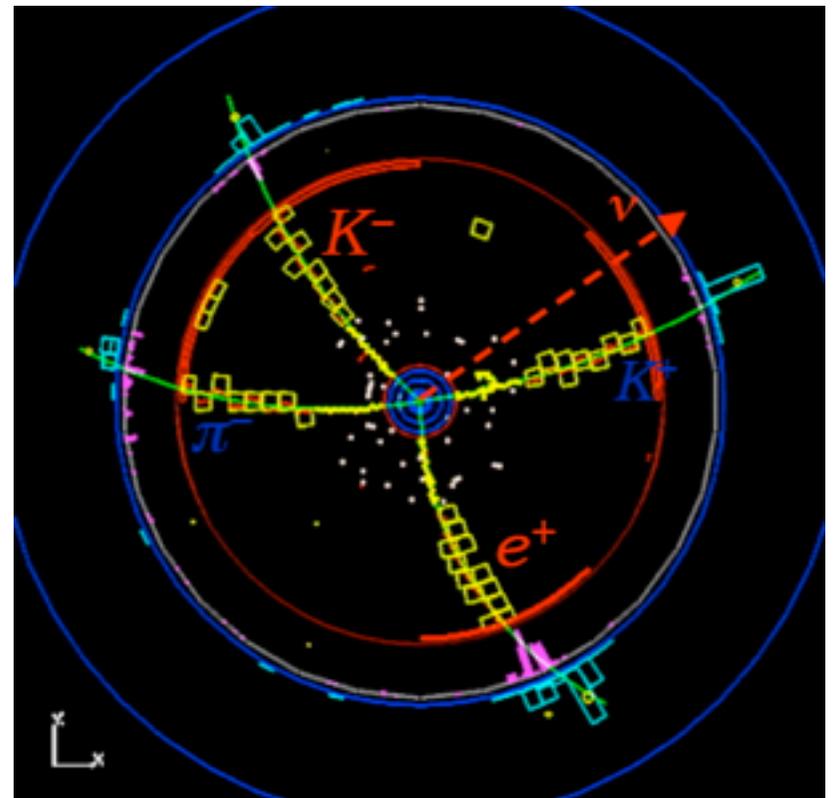
# D → h ℓ ν @ charm threshold (CLEO-c/BES III)

$$e^+ e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$$

CLEAN-c

- 100% of beam energy converted to DD pair ⇒ very clean. Kinematic constraints allow reconstruction of ν.
- Always generate D-mesons in pairs. One D provides the normalisation for the other ⇒ absolute branching fractions.
- These features let CLEO-c, and now BES III, perform competitive leptonic & semileptonic measurements with each only ca 0.3%\* of the D mesons produced the B-factories.

\*) For BES III this corresponds roughly to what has been analysed; there is 3x as much data on tape.



$$\psi(3770) \rightarrow \bar{D}^0(K^+\pi^-)D^0(K^-e^+\nu_e)$$

# Form factor in decays to pseudoscalars

- $D \rightarrow h \ell \nu$ ,  $h = K, \pi, \dots$

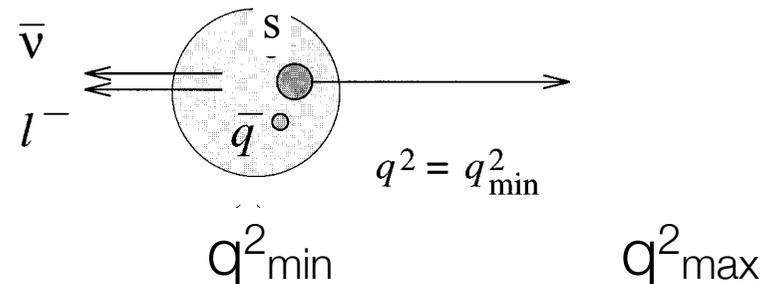
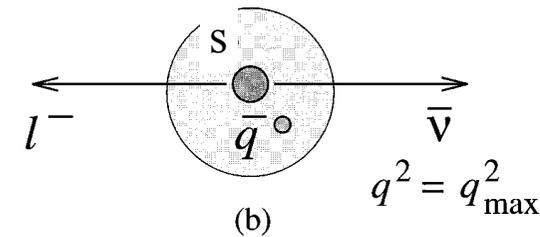
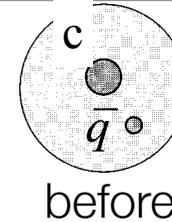
$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{cx}| |\vec{p}_h|^3 |f_+^{D \rightarrow h}(q^2)|^2$$

(neglecting fermion masses)

- $q^2 = (p_\ell + p_\nu)^2 =$  invariant mass-squared of lepton pair.

- $f_+(q^2)$  = form factor - the QCD bit.

- Measure  $|V_{cx}| \cdot f_+(q^2)$ . Get  $|V_{cx}|$  from CKM-unitarity to measure  $f_+(q^2)$  as a test of LQCD - or reverse the logic and test CKM-unitarity.



See review by [Richman & Burchat](#), *Rev.Mod.Phys.* 67 (1995) 893-976

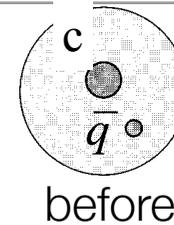
# Form factor in decays to pseudoscalars

- $D \rightarrow h \ell \nu$ ,  $h = K, \pi, \dots$

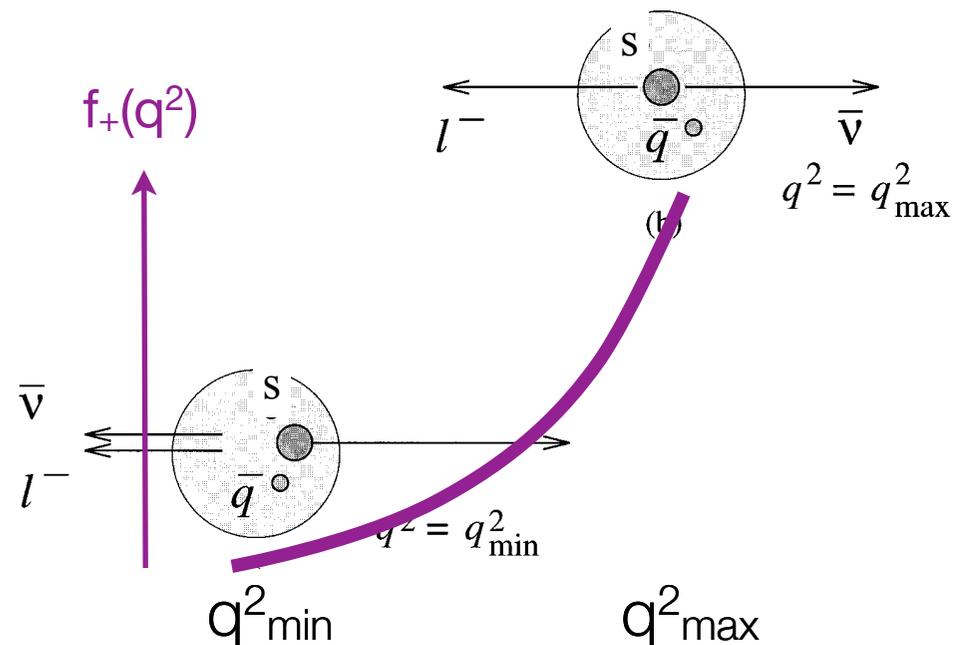
$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{cx}| |\vec{p}_h|^3 |f_+^{D \rightarrow h}(q^2)|^2$$

(neglecting fermion masses)

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- Measure  $|V_{cx}| \cdot f_+(q^2)$ . Get  $|V_{cx}|$  from CKM-unitarity to measure  $f_+(q^2)$  as a test of LQCD - or reverse the logic and test CKM-unitarity.



QCD likes this, weak doesn't  
(heavily helicity suppressed)



See review by [Richman & Burchat, Rev.Mod.Phys. 67 \(1995\) 893-976](#)

# $D^0 \rightarrow \{K, \pi\} e^+ \nu$ Form factor parameterisations

- Simple pole model:

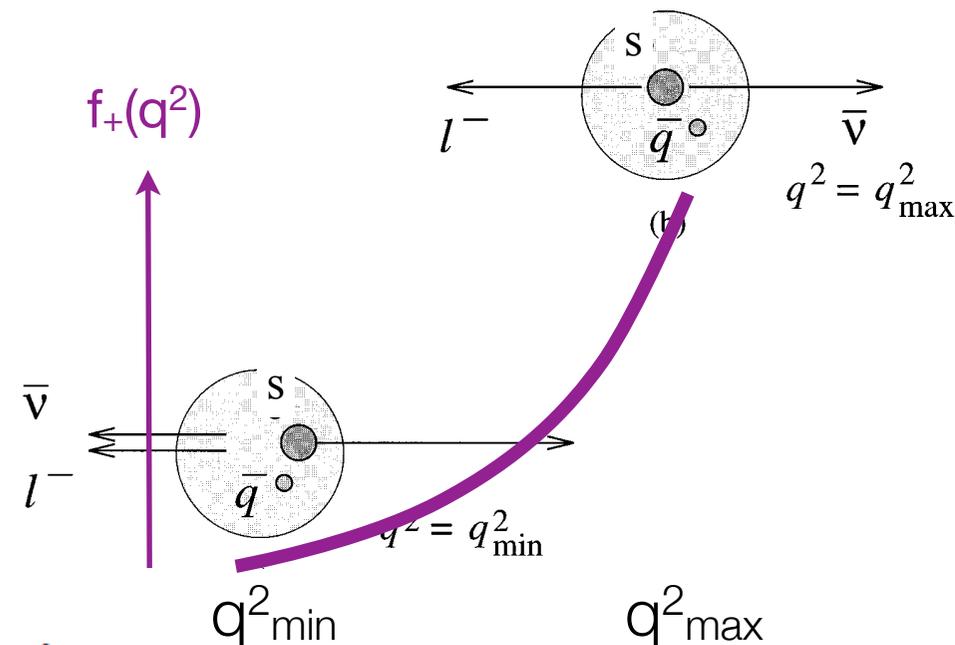
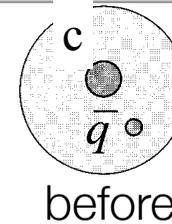
$$f_+(q^2) = \frac{f_+(0)}{1 - q^2/m_{pole}^2}$$

- Modified Pole Model (Becirevic and Kaidalov, PLB 478, 417)

$$f_+(q^2) = \frac{f_+(0)}{\left(1 - \frac{q^2}{m_{pole}^2}\right) \left(1 - \alpha \frac{q^2}{m_{pole}^2}\right)}$$

- Series expansion (CLEO-c/BES III both explored 2nd and 3rd order):

$$f_+(q^2) = \frac{1}{P(q^2) \phi(q^2, t_0)} \sum_{k=0}^{\infty} a_k(t_0) [z(q^2, t_0)]^k$$



See review by [Richman & Burchat, Rev.Mod.Phys. 67 \(1995\) 893-976](#)

# $D \rightarrow K e \nu$ , $D \rightarrow \pi e \nu$

---

- Recent results
  - BaBar 2007 and 2010,  $D^0$
  - CLEO-c 2009, 0.8/fb,  $D^0$  and  $D^\pm$ .
  - BES III May 2012: New result (so far,  $D^0$  only)  
2.9 /fb data taken  
0.9/fb analysed

**BaBar: Phys.Rev. D76 (2007) 052005**

**CLEO: Phys.Rev. D80 (2009) 032005**

**BES III: New result, shown first at  
CHARM 2012 by Cunlei Liu**



# $D \rightarrow K e \nu$ , $D \rightarrow \pi e \nu$

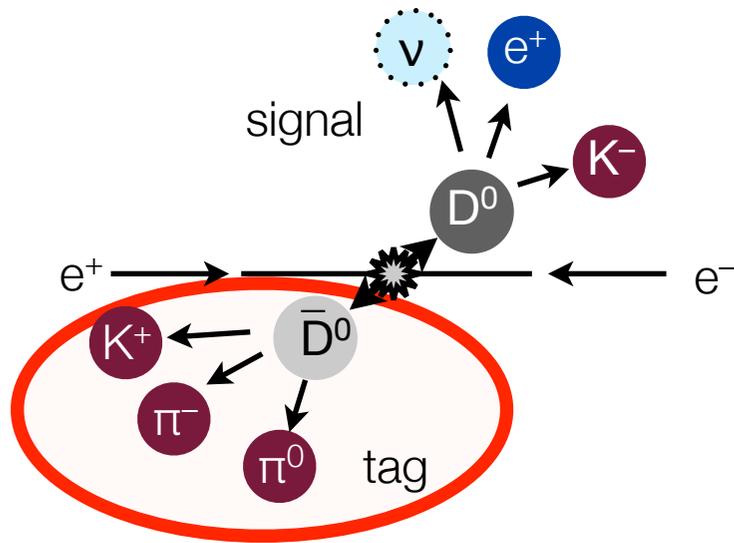
- Recent results
  - BaBar 2007 and 2010,  $D^0$
  - CLEO-c 2009, 0.8/fb,  $D^0$  and  $D^\pm$ .
  - **BES III May 2012: New result (so far,  $D^0$  only)**  
2.9 /fb data taken  
0.9/fb analysed

**BaBar: Phys.Rev. D76 (2007) 052005**  
**CLEO: Phys.Rev. D80 (2009) 032005**  
**BES III: New result, shown first at**  
**CHARM 2012 by Cunlei Liu**



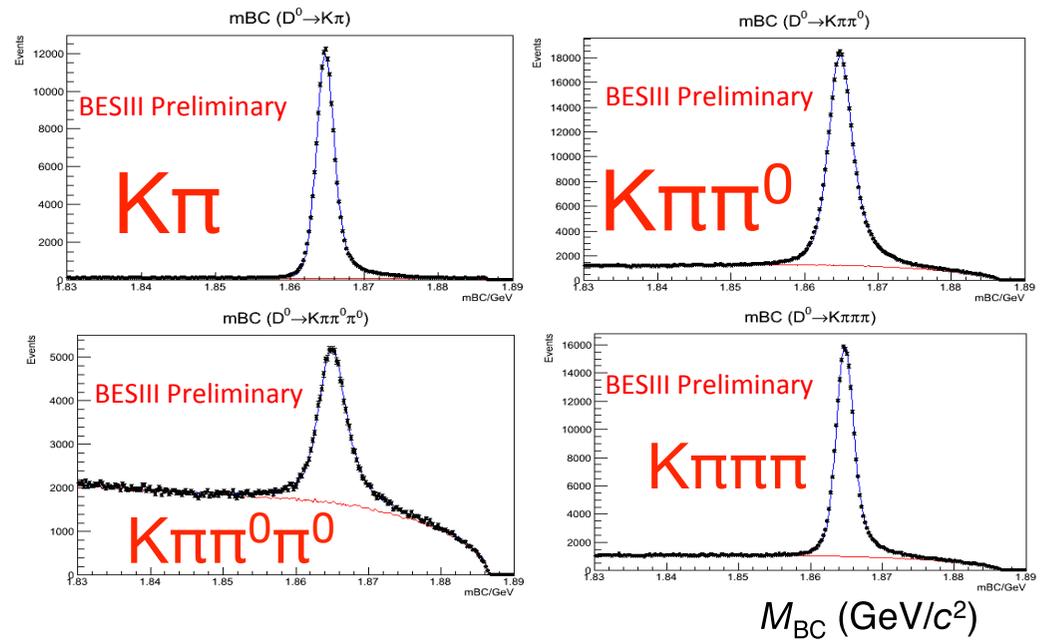
# $D^0 \rightarrow \{K, \pi\} e^+ \nu$ new BES III result

BES III 2012 (prelim)



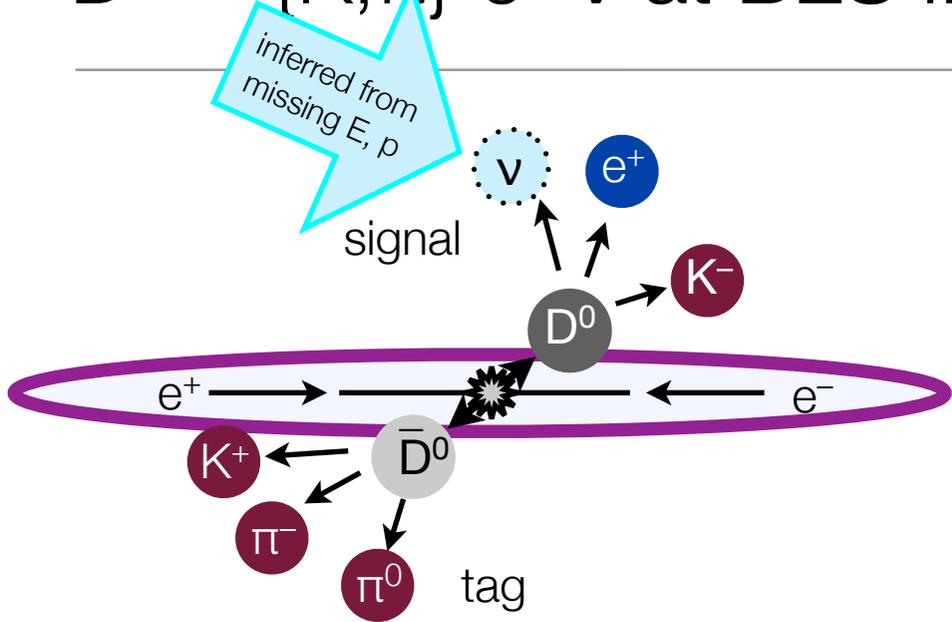
beam-constrained mass of tag D

- Step 1: Reconstruct  $\sim 3/4$  M tag D (provides normalisation)

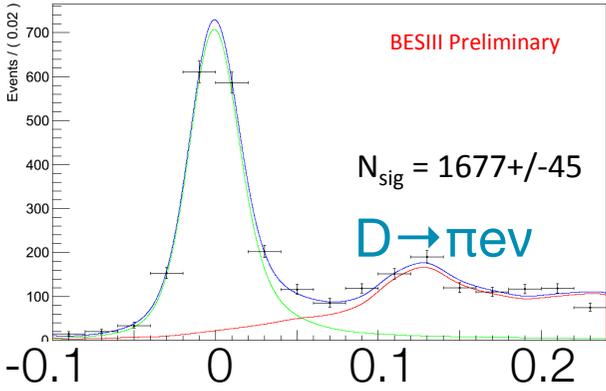
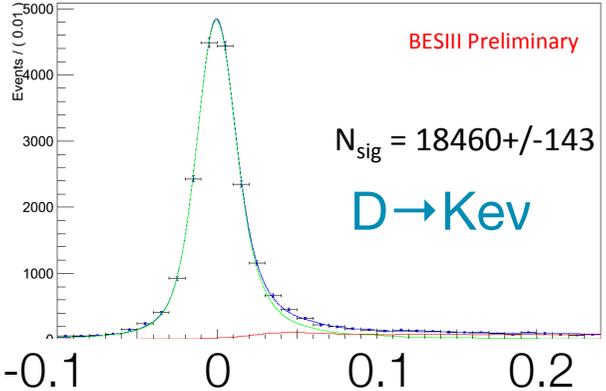


**BES III: CHARM 2012 by Chunlei Liu**

$D^0 \rightarrow \{K, \pi\} e^+ \nu$  at BES III



$$U \equiv E_{\text{miss}} - |\vec{p}_{\text{miss}}| \text{ (GeV)}$$



- Step 1: Reconstruct Tag D
- Step 2: Find U (~ missing mass) from beam constraint and e and  $\eta, \eta', \phi$ .

# $D^0 \rightarrow \{K, \pi\} e^+ \nu$ Branching Fractions

BES III 2012 (prelim)

BESIII Preliminary

BES III prelim (0.9/fb)

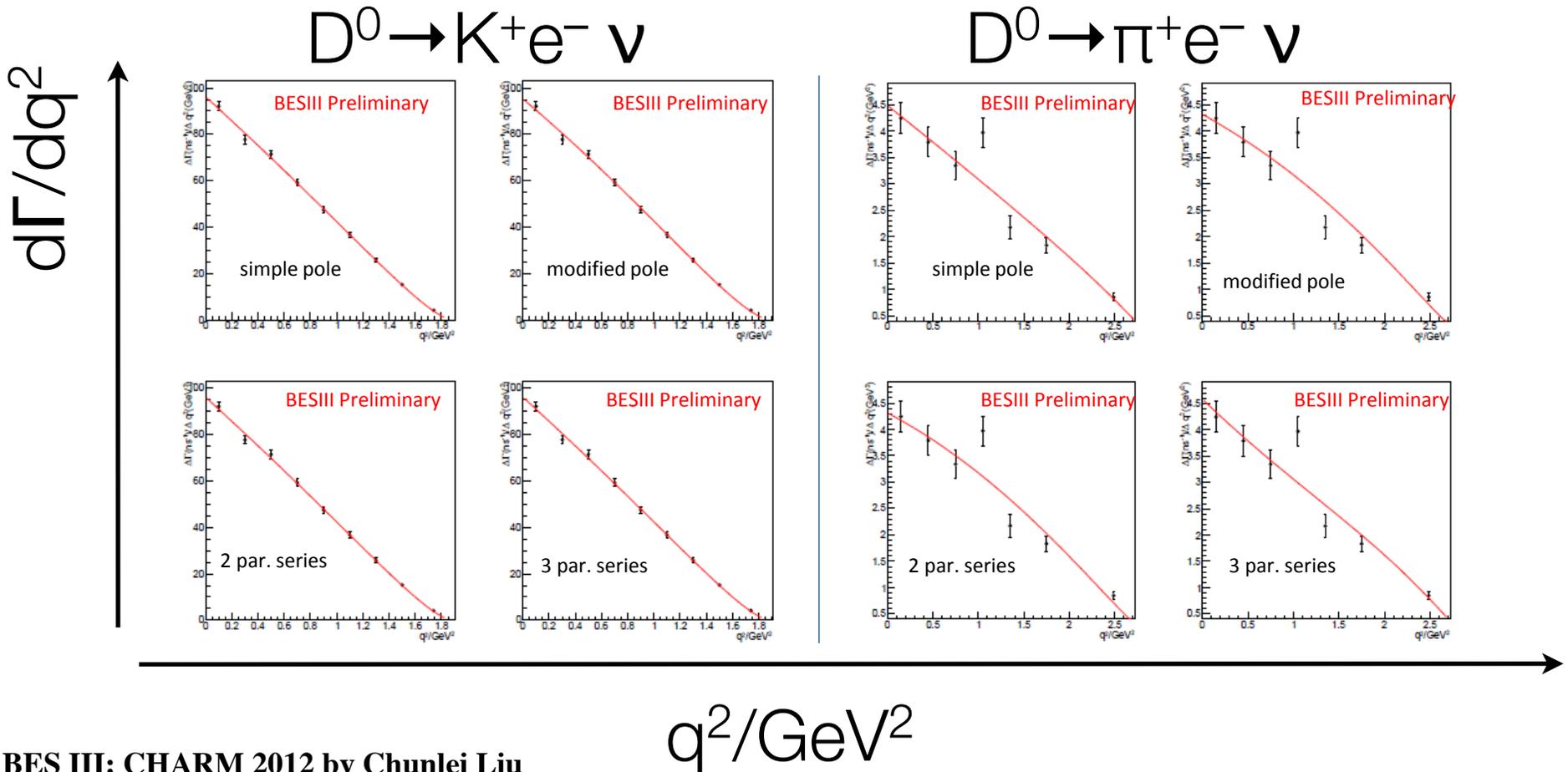
Mode	measured branching fraction(%)	PDG	CLEOc
$\bar{D}^0 \rightarrow K^+ e^- \bar{\nu}$	$3.542 \pm 0.030 \pm 0.067$	$3.55 \pm 0.04$	$3.50 \pm 0.03 \pm 0.04$
$\bar{D}^0 \rightarrow \pi^+ e^- \bar{\nu}$	$0.288 \pm 0.008 \pm 0.005$	$0.289 \pm 0.008$	$0.288 \pm 0.008 \pm 0.003$

**BES III: CHARM 2012 by Chunlei Liu**

# $D^0 \rightarrow \{K, \pi\} e^+ \nu$ fits to decay rates

BES III 2012 (prelim)

$d\Gamma/dq^2$ : BES III data with fits using different form factor models



BES III: CHARM 2012 by Chunlei Liu

# BES III form factor fit results

BES III 2012 (prelim)

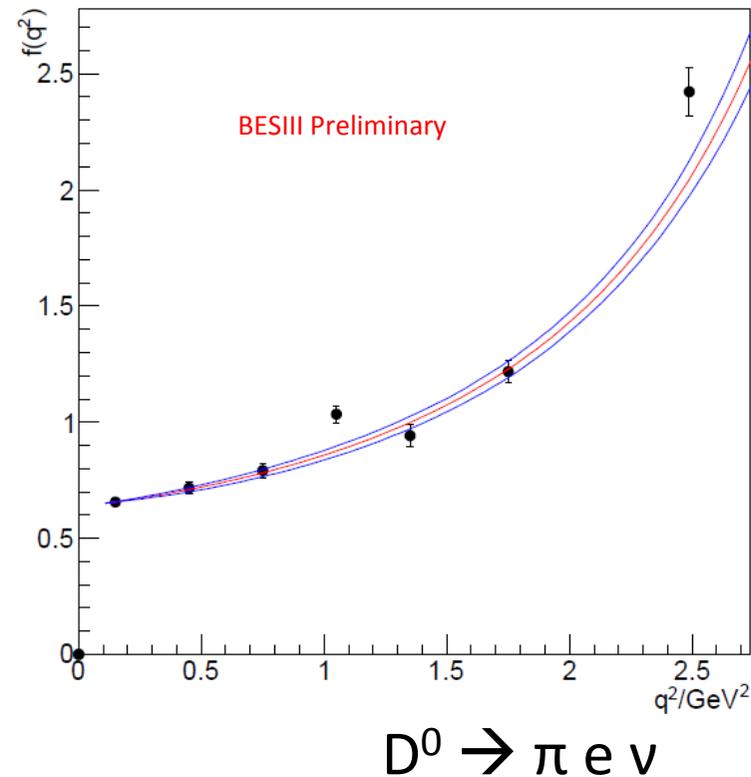
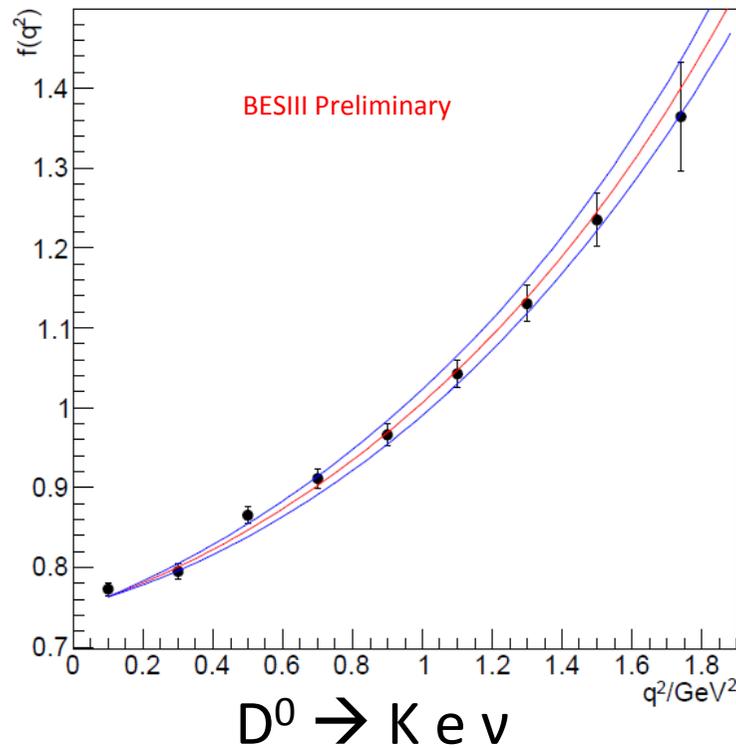
BESIII Preliminary

Simple Pole	$f_+(0) V_{cd(s)} $	$m_{pole}$	
$D^0 \rightarrow Ke\nu$	$0.729 \pm 0.005 \pm 0.007$	$1.943 \pm 0.025 \pm 0.003$	
$D^0 \rightarrow \pi e\nu$	$0.142 \pm 0.003 \pm 0.001$	$1.876 \pm 0.023 \pm 0.004$	
Modified Pole	$f_+(0) V_{cd(s)} $	$\alpha$	
$D^0 \rightarrow Ke\nu$	$0.725 \pm 0.006 \pm 0.007$	$0.265 \pm 0.045 \pm 0.006$	
$D^0 \rightarrow \pi e\nu$	$0.140 \pm 0.003 \pm 0.002$	$0.315 \pm 0.071 \pm 0.012$	
2 par. series	$f_+(0) V_{cd(s)} $	$r_1$	
$D^0 \rightarrow Ke\nu$	$0.726 \pm 0.006 \pm 0.007$	$-2.034 \pm 0.196 \pm 0.022$	
$D^0 \rightarrow \pi e\nu$	$0.140 \pm 0.004 \pm 0.002$	$-2.117 \pm 0.163 \pm 0.027$	
3 par. series	$f_+(0) V_{cd(s)} $	$r_1$	$r_2$
$D^0 \rightarrow Ke\nu$	$0.729 \pm 0.008 \pm 0.007$	$-2.179 \pm 0.355 \pm 0.053$	$4.539 \pm 8.927 \pm 1.103$
$D^0 \rightarrow \pi e\nu$	$0.144 \pm 0.005 \pm 0.002$	$-2.728 \pm 0.482 \pm 0.076$	$4.194 \pm 3.122 \pm 0.448$

**BES III: CHARM 2012 by Chunlei Liu**

# Form factor shapes: BES III / LQCD

note: these compare shape-only, no absolute scale.



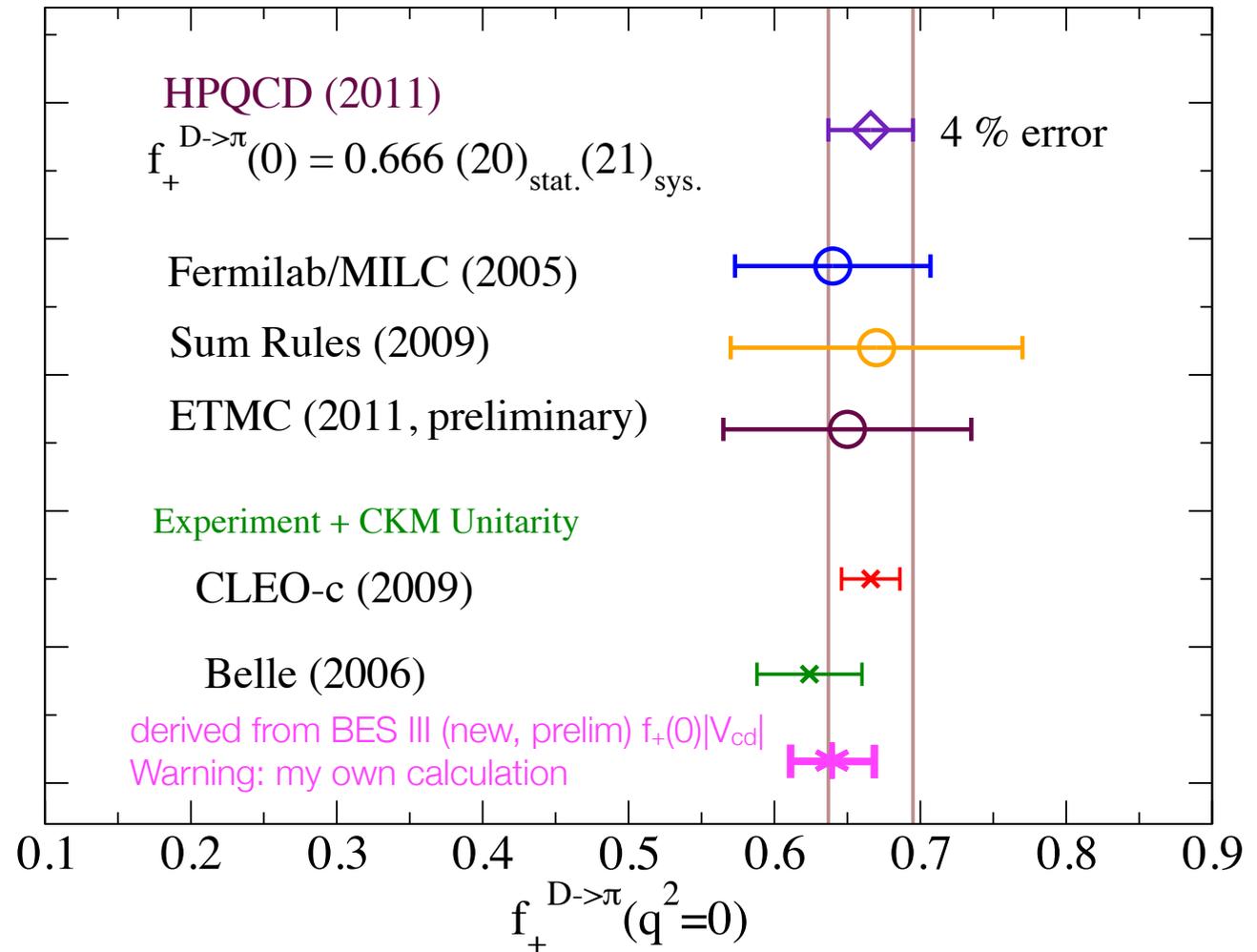
Points: BES III preliminary with stat errors

Curves: Fermilab/The Lattice/MILC with  $1\sigma$  stat error band, arXiv:1111.5471 (Nov 2011)

**BES III: CHARM 2012 by Chunlei Liu**

# $f_+^{D \rightarrow \pi}(0)$ from experiment and theory

Taken from Na, Davies, Follana, Koponen, Lepage and Shigemitsu, Phys.Rev. D84 (2011) 114505 and modified (added BES III)

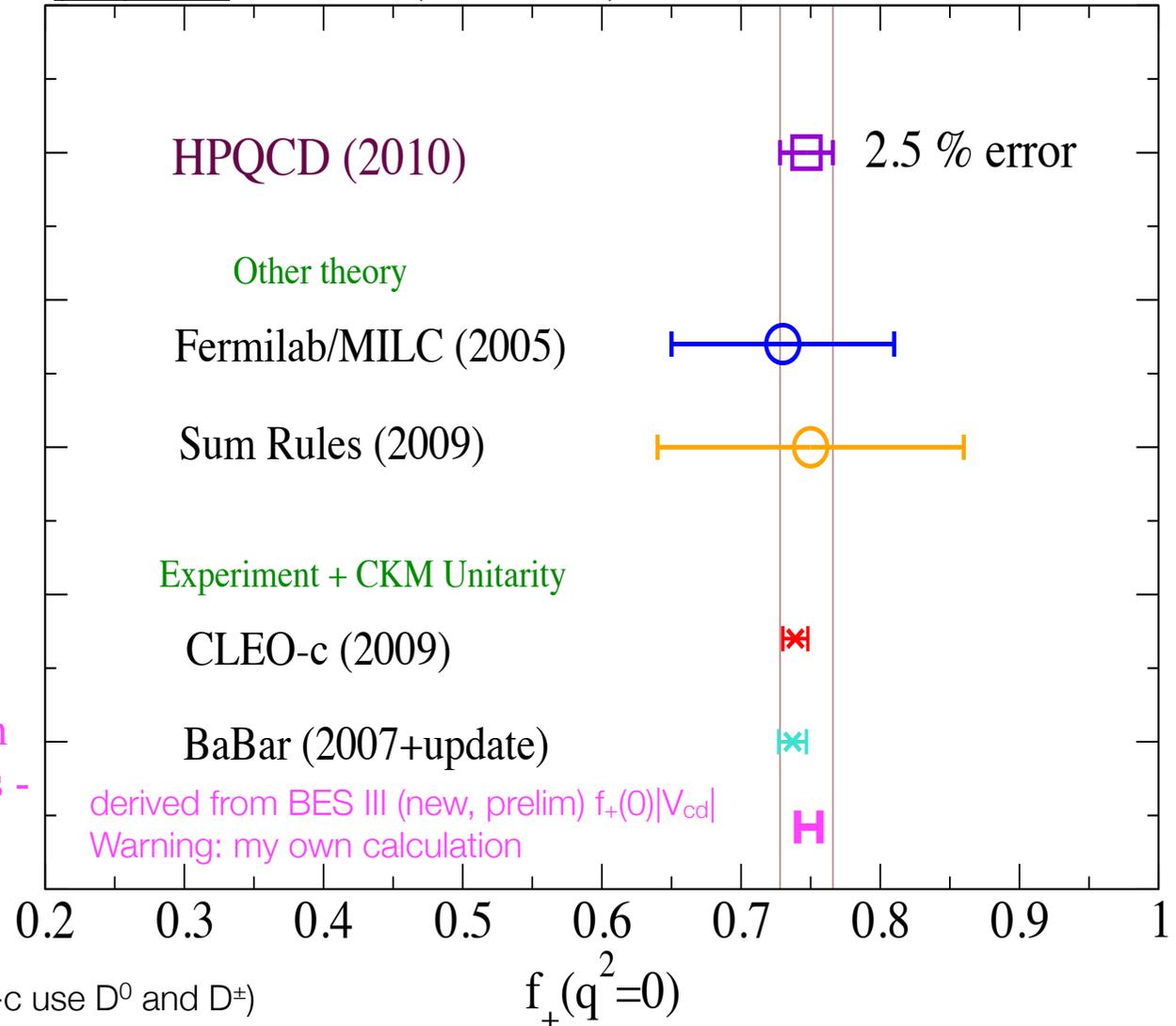


With  $|V_{cd}| = 0.2252 \pm 0.0007$ , I get from BES III new result (3 par series - as used by CLEO-c):

(note: BES III result from  $D^0$  only, CLEO-c use  $D^0$  and  $D^\pm$ )

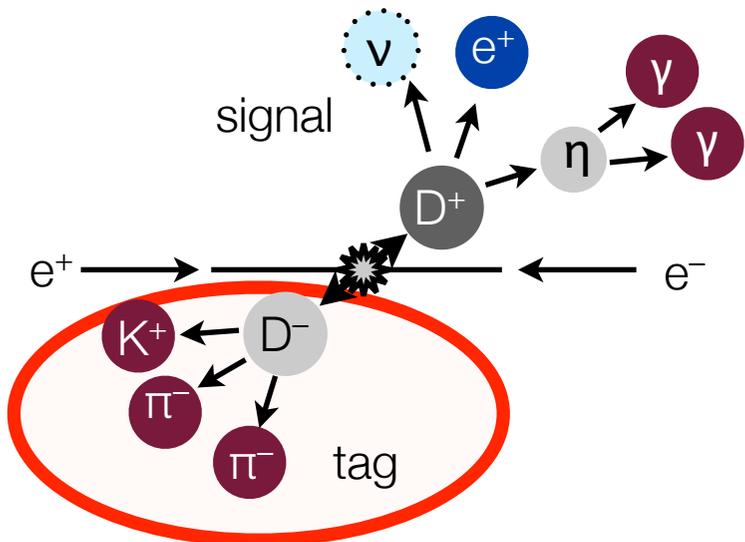
# $f_+^{D \rightarrow K}(0)$ from experiment and theory

Taken from [Na, Davies, Follana, Koponen, Lepage and Shigemitsu, Phys.Rev. D82 \(2010\) 114506](#) and modified (added BES III)



(note: BES III result from  $D^0$  only, CLEO-c use  $D^0$  and  $D^\pm$ )

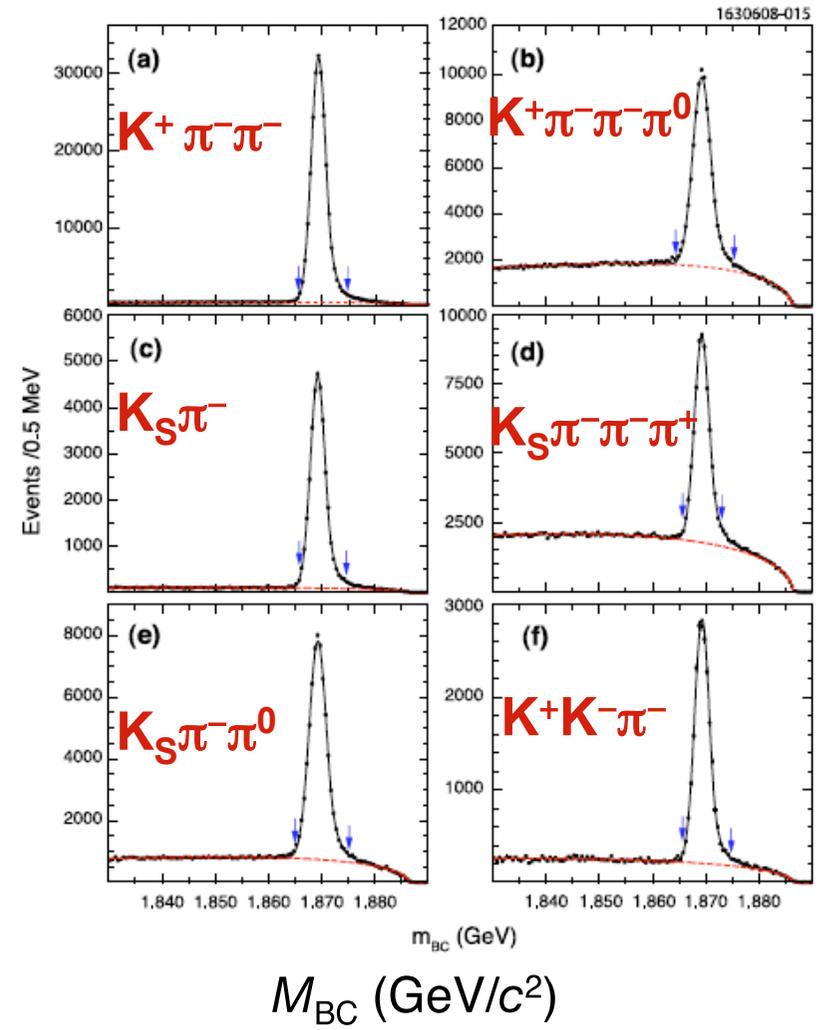
# CLEO-c: $D^+ \rightarrow \{\eta, \eta' \text{ or } \varphi\} e^+ \nu$ (tagged)



beam-constrained mass of tag D

- Step 1: Reconstruct Tag D (provides normalisation)

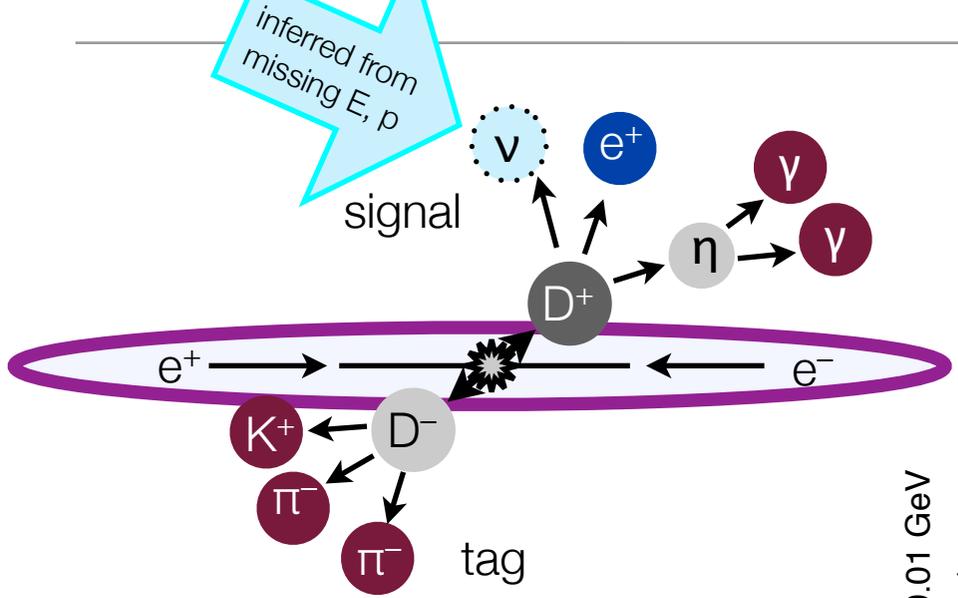
481k tags



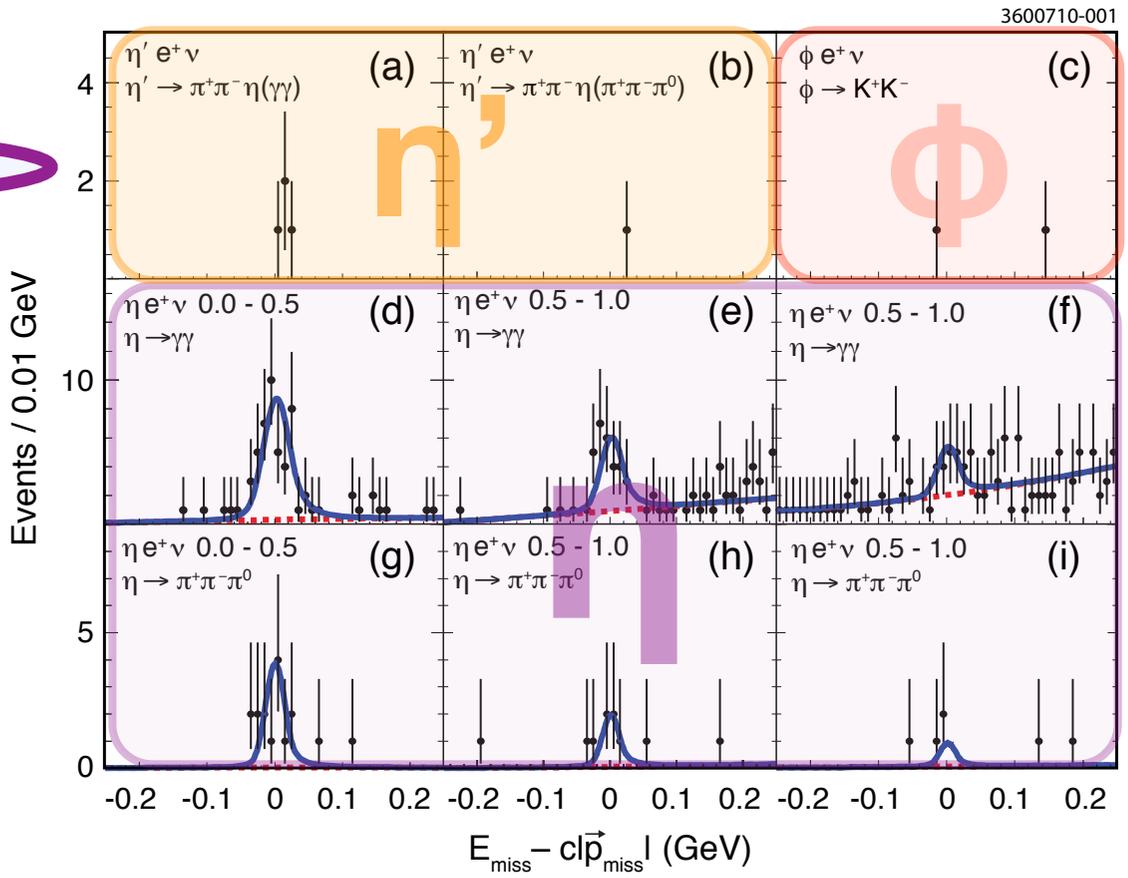
plots from different CLEO-c paper (using same technique): PRD 78, 052003 (2008)

CLEO: Phys.Rev. D84 (2011) 032001

# CLEO-c: $D^+ \rightarrow \{\eta, \eta' \text{ or } \phi\} e^+ \nu$ (tagged)



$$U \equiv E_{\text{miss}} - |\vec{p}_{\text{miss}}|$$

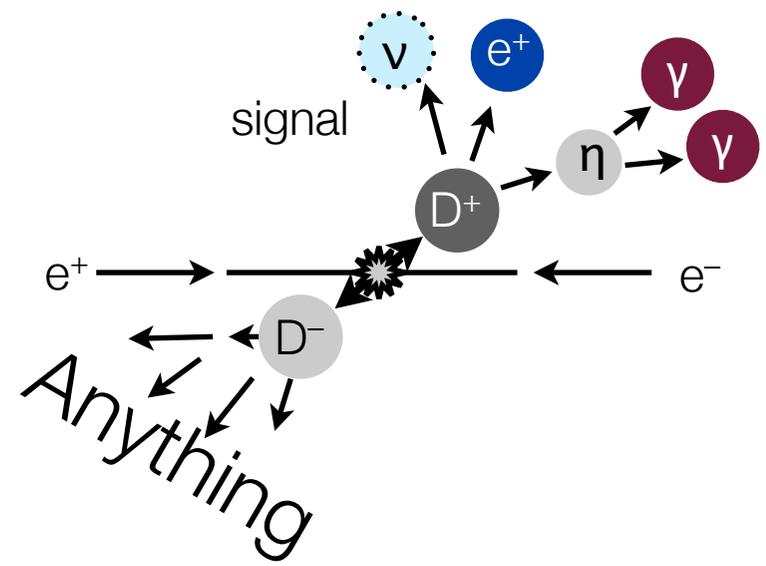


- Step 1: Reconstruct Tag D
- Step 2: Find U (~ missing mass) from beam constraint and e and  $\eta, \eta', \phi$ .

CLEO: Phys.Rev. D84 (2011) 032001

# Generic Reconstruction of $D^+ \rightarrow \{\eta, \eta' \text{ or } \varphi\} e^+ \nu$

- We have 2.4M  $D^+D^-$  events, but only 0.5M tags - the generic reconstruction is an attempt to make use of the other 1.9M.
- Instead of fully reconstructing a tag D in specific decay modes, the generic reconstruction adds up all momenta & energies in the event to identify the neutrino.
- Several cuts (eg exactly one electron in the decay), plus the specific reconstruction of  $\eta$ ,  $\pi^0$  and  $K_S$  help clean up the sample.
- Signal yield normalised to  $D \rightarrow K\pi\pi$  - normalisation mode reconstructed in the same manner as signal.



**CLEO: Phys.Rev. D84 (2011) 032001**

# Combined CLEO-c $D^+ \rightarrow \{\eta, \eta' \text{ or } \phi\} e^+ \nu$ results

## $D^+ \rightarrow \{\eta, \eta', \phi\} e^+ \nu$ Branching Fractions & Limits

- First observation of  $D^+ \rightarrow \eta' e^+ \nu$  ( $5.8\sigma$ )  
 $\mathcal{B}(D^+ \rightarrow \eta' e^+ \nu_e) = (2.16 \pm 0.53 \pm 0.07) \times 10^{-4}$
- Improved  $D^+ \rightarrow \eta e^+ \nu$  BR:  
 $\mathcal{B}(D^+ \rightarrow \eta e^+ \nu_e) = (11.4 \pm 0.9 \pm 0.4) \times 10^{-4}$
- Limit on  $D^+ \rightarrow \phi e^+ \nu$  ~twice as stringent as previous CLEO-c limit:  
 $\mathcal{B}(D^+ \rightarrow \phi e^+ \nu_e) < 0.9 \times 10^{-4}$  (90% C.L.).

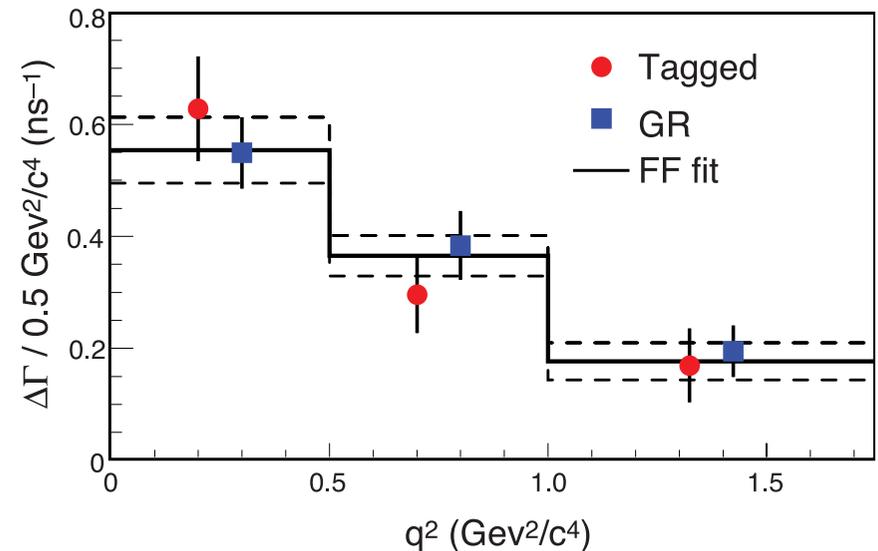
## Precision dominated by Generic Reconstruction sample

Results consistent with both ISGW2 [1] and Fajfer-Kamenic [2] models.

[1] D. Scora and N. Isgur, Phys. Rev. D 52, 2783 (1995)

[2] S. Fajfer and J. Kamenik, Phys. Rev. D 71, 014020 (2005).

## First $D^+ \rightarrow \eta e^+ \nu$ form factor measurement



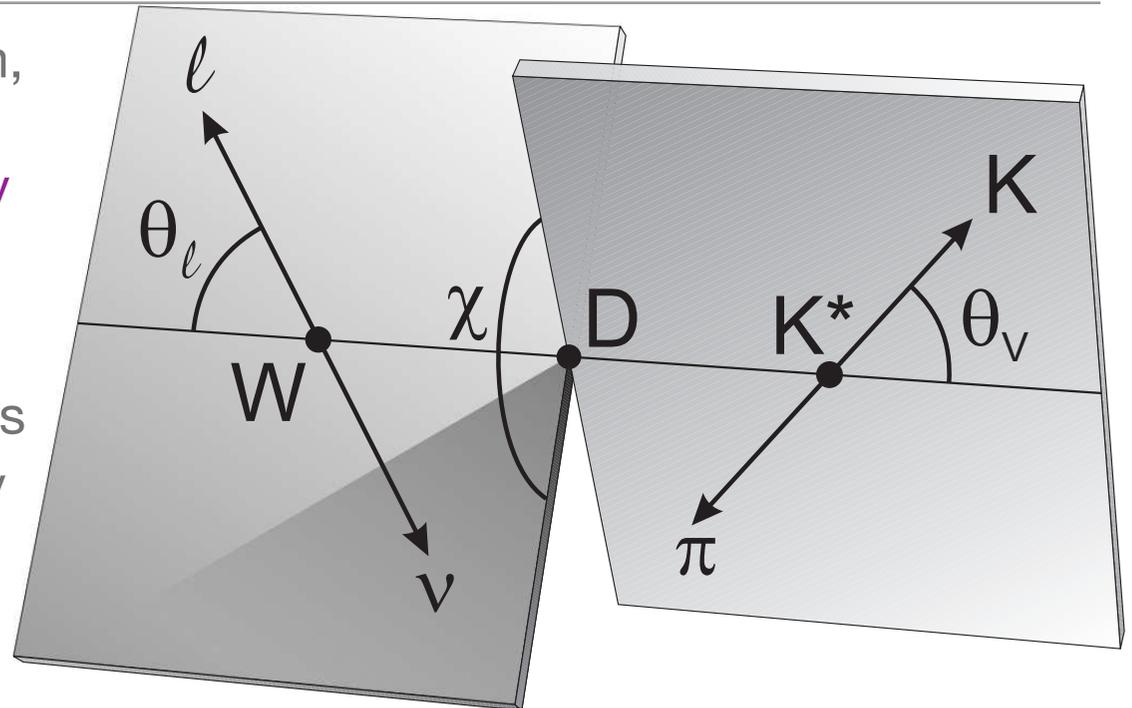
$$f_+(0) |V_{cd}| = 0.086 (6)_{(stat)} (1)_{(sys)}$$

(results identical for simple pole or modified pole parameterisation)

**CLEO: Phys.Rev. D84 (2011) 032001**

# $D \rightarrow V \ell \nu$

- Need 5 variables,  $m^2$  of  $V$  system,  $q^2$  of  $e\nu$  system, plus 3 angular variables to disentangle 3 helicity states.
- Need 3 form factors (for massless  $\ell$ ) 2 axial and one vector. Usually parameterised with simple pole.



- Frequently experiments measure the ratios  $r_V$ ,  $r_A$ .

$$V(q^2) = \frac{V(0)}{1 - q^2/m_V^2}; \quad A_{1,2}(q^2) = \frac{A_{1,2}(0)}{1 - q^2/m_A^2}$$

- Combine  $D \rightarrow \rho e \nu$   $D \rightarrow K^* e \nu$  and  $B \rightarrow V \ell \ell$  to improve  $|V_{ub}|$  (see [Phys.Rev. D70 \(2004\) 114005](#))

$$r_V \equiv \frac{V(0)}{A_1(0)} \quad r_A \equiv \frac{A_2(0)}{A_1(0)}$$

# $D \rightarrow K^* e \nu$ , $D \rightarrow K \pi e \nu$

- BaBar (2011) measure the  $D \rightarrow K^* e \nu$  form-factors, using 1/4 M  $D \rightarrow K \pi e \nu$  signal events. Amongst the result:

$$m_A = (2.63 \pm 0.10 \pm 0.13) \text{ GeV}$$

$$r_V = (1.463 \pm 0.017 \pm 0.032) \text{ GeV}$$

$$r_2 = (0.801 \pm 0.020 \pm 0.020) \text{ GeV}$$

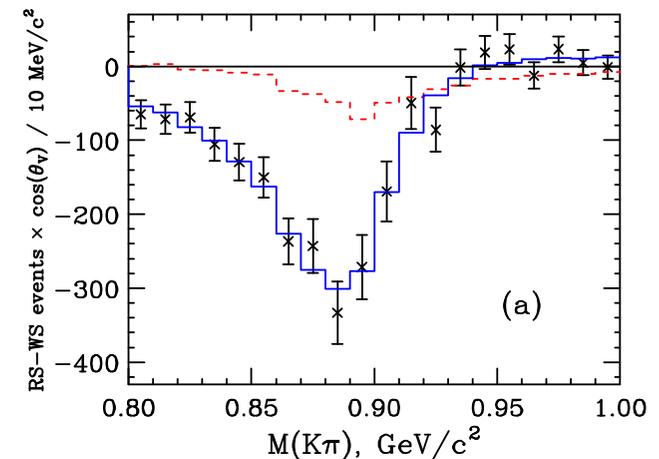
- The decay also has a significant  $D \rightarrow \{K \pi\text{-S-wave}\} e \nu$ , component, first observed by FOCUS in 2002. BaBar (2011) find and S-wave fraction in  $D \rightarrow K \pi e \nu$ :

$$(5.78 \pm 0.16 \pm 0.15)\%$$

**BaBar:** [Phys.Rev. D83 \(2011\) 072001](#)

S-wave in this channel was first seen by FOCUS (2002).

The plot shows the  $\cos(\theta_V)$  - weighted distribution in  $M(K\pi)$ . S - P wave interference results in an asymmetry in  $\cos(\theta_V)$ .



blue: fit with S-wave  
red: without

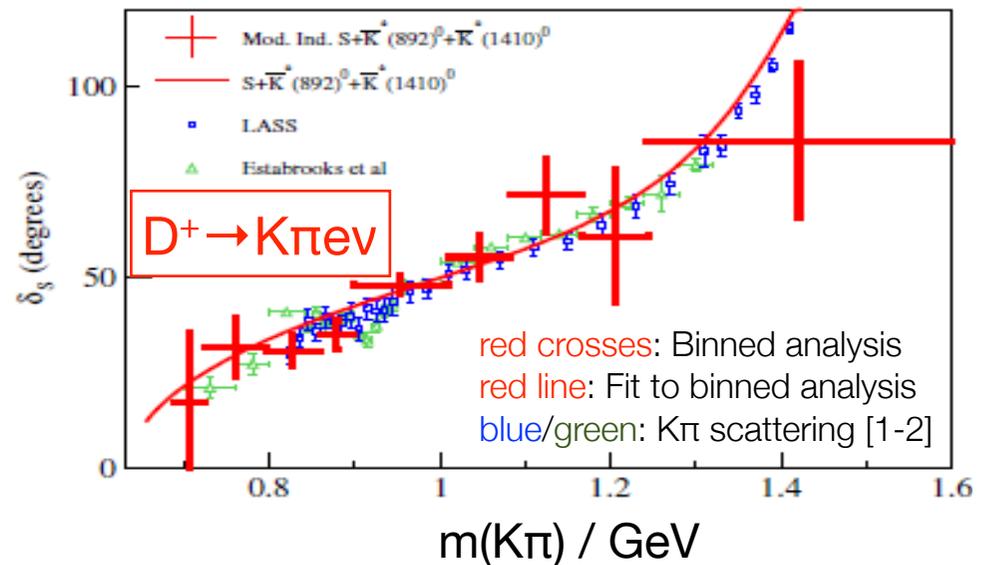
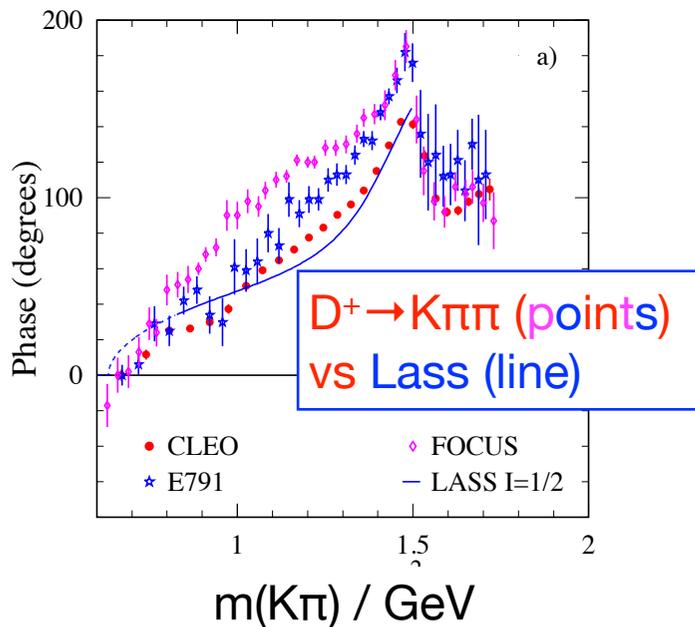
**FOCUS:** [Phys.Lett. B535 \(2002\) 43-51](#)

FOCUS: Phys.Lett. B535 (2002) 43-51

# Using $D \rightarrow K^* e \nu$ as interferometer to measure $D \rightarrow K\pi e \nu$ S-wave

BaBar 2011

- **BaBar (2011)** performed a detailed analysis of the  $K\pi$  S-wave using its interference with  $K^*$  to extract both magnitude and phase.
- Model-independent measurement of the phase is in much better agreement with scattering data (**LASS [1]**, **Estabrooks et al [2]**) than S-wave contributions measured in  $D^+ \rightarrow K^- \pi^+ \pi^-$  [3-6].



[1] D. Aston et al., Nucl. Phys. B 296, 493 (1988). (LASS)

[2] P. Estabrooks et al., Nucl. Phys. B 133, 490 (1978).

[3] E.M. Aitala et al. (Fermilab E791 Collaboration), Phys. Rev. D 73, 032004 (2006). [4] J.M. Link et al. (FOCUS Collaboration), Phys. Lett. B 653, 1 (2007).

[5] J.M. Link et al. (FOCUS Collaboration), Phys. Lett. B 681, 14 (2009). [6] A. Bonvicini et al. (CLEO Collaboration), Phys. Rev. D 78, 052001 (2008).

# Non-parametric $D \rightarrow K\pi$ $e/\mu$ $\nu$ form factors

CLEO-c 2010

- CLEO-c (2010) use a projective reweighting technique pioneered by FOCUS (2006).

- Basic idea: rates (after integrating over  $\chi$ ) can be expressed as

$$\begin{aligned} \frac{d^4 \Gamma(\theta_\ell, \theta_V, m_{K\pi}^2, q^2)}{d\theta_\ell, d\theta_V, dm_{K\pi}^2, dq^2} &= F_0(\theta_\ell, \theta_V) |\text{BW}(m_{K\pi}^2)|^2 q^2 |H_0(q^2)|^2 \\ &+ F_+(\theta_\ell, \theta_V) |\text{BW}(m_{K\pi}^2)|^2 q^2 |H_+(q^2)|^2 \\ &+ F_-(\theta_\ell, \theta_V) |\text{BW}(m_{K\pi}^2)|^2 q^2 |H_-(q^2)|^2 \\ &+ \dots \end{aligned}$$

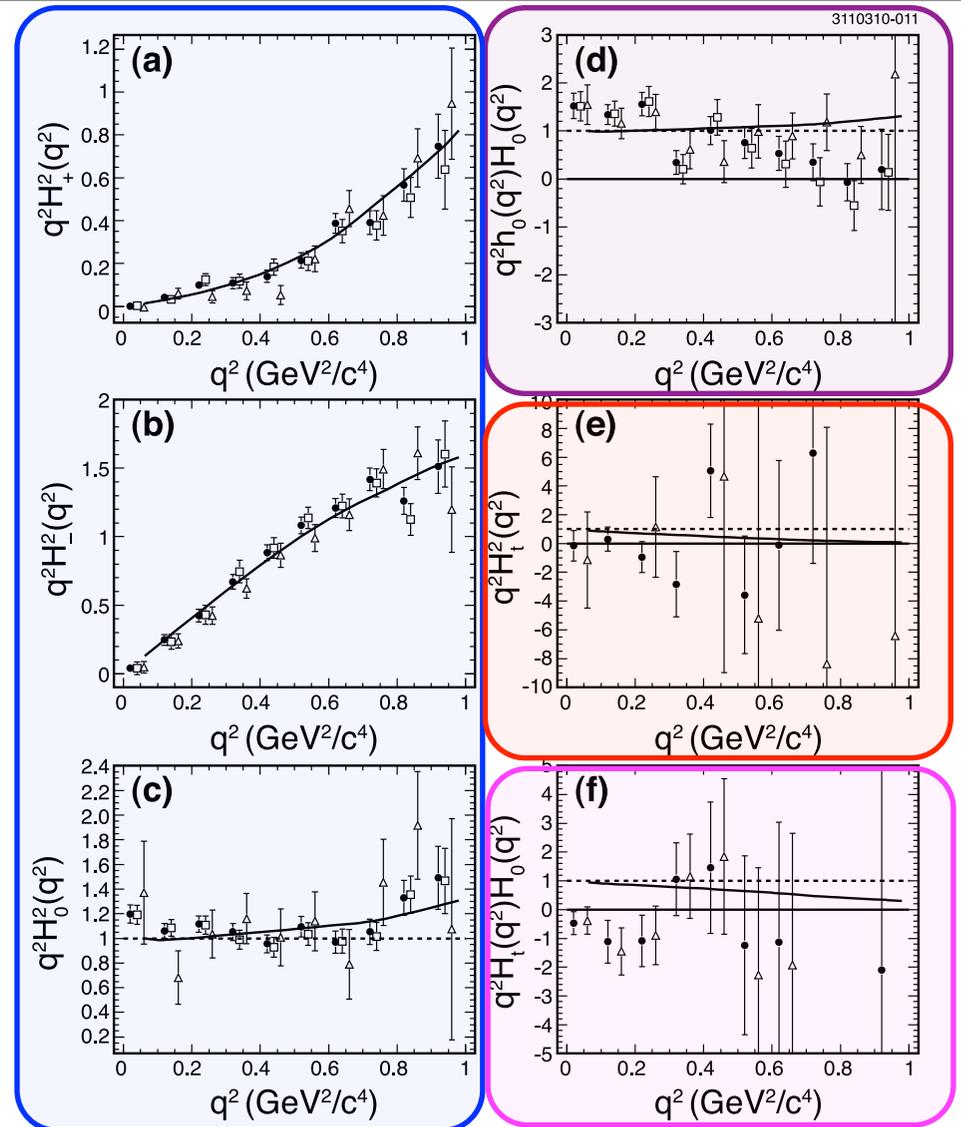
- .... histogram in  $q^2$  = integrate over  $\theta_\ell, \theta_V$ . Find functions  $F^\pm_i(\theta_\ell, \theta_V)$  orthogonal to the  $F_i(\theta_\ell, \theta_V)$ . **Weighting** events by  $F^\pm_i(\theta_\ell, \theta_V)$  removes the corresponding terms from the  $q^2$  projection.

**CLEO: Phys.Rev. D81 (2010) 112001; FOCUS: Phys. Lett. B 633, 183 (2006)**

# Non-parametric $D \rightarrow K\pi e/\mu \nu$ form factors

CLEO-c 2010

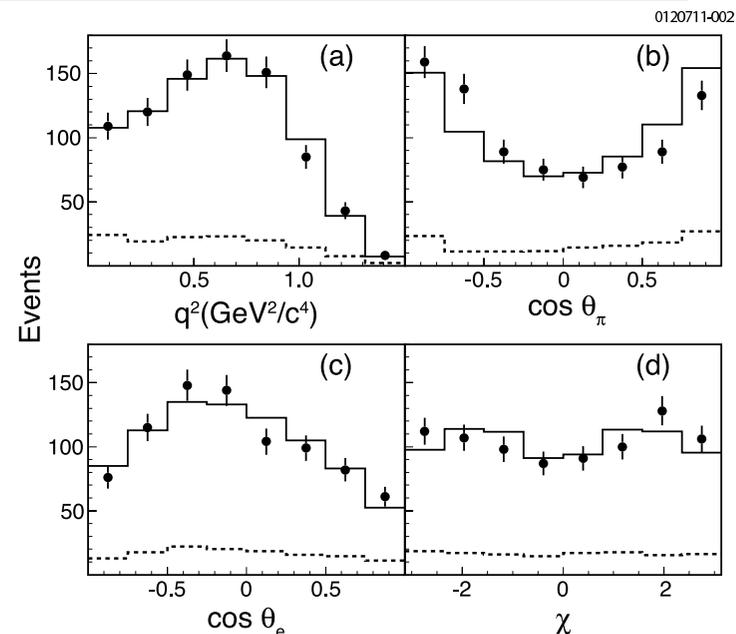
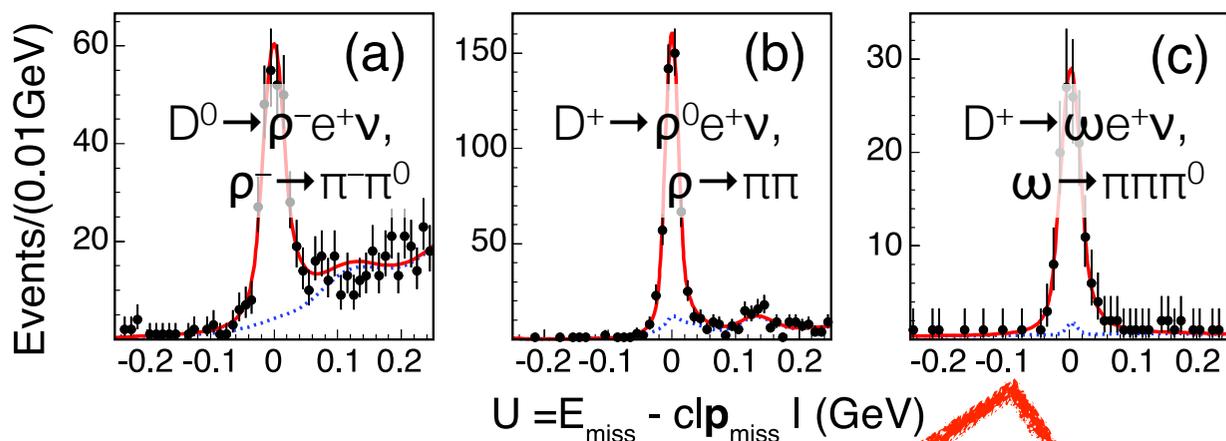
- Plots on left compare model-independent measurements with simple pole model - generally good agreement.
- Confirms evidence for S-wave.
- Cleo-c's analysis considers highly-suppressed amplitudes with right-handed  $e/\mu$  (adds a helicity,  $H_T$ , and a form factor,  $A_3$ )
- $H_T H_0$  interference less than LQCD prediction.



CLEO: Phys.Rev. D81 (2010) 112001

# Form factors for $D^0 \rightarrow \rho^- e^+ \nu$ , $D^+ \rightarrow \rho^0 e^+ \nu$

CLEO-c 2011



$$A_1(0) = 0.56 \pm 0.01^{+0.02}_{-0.03}$$

$$A_2(0) = 0.47 \pm 0.06 \pm 0.04$$

$$V(0) = 0.84 \pm 0.09^{+0.05}_{-0.06}$$

First measurement.

Decay Mode	$\epsilon$ (%)	$N_{\text{tag, SL}}$	$\mathcal{B}_{\text{SL}}$	$\mathcal{B}_{\text{SL}}(\text{prev})$	$\mathcal{B}_{\text{SL}}(\text{ISGW2})$	$\mathcal{B}_{\text{SL}}(\text{FK})$
$D^0 \rightarrow \rho^- e^+ \nu_e$	$26.03 \pm 0.02$	$304.6 \pm 20.9$	$1.77 \pm 0.12 \pm 0.10$	$1.94 \pm 0.39 \pm 0.13$	1.0	2.0
$D^+ \rightarrow \rho^0 e^+ \nu_e$	$42.84 \pm 0.03$	$447.4 \pm 24.5$	$2.17 \pm 0.12^{+0.12}_{-0.22}$	$2.1 \pm 0.4 \pm 0.1$	1.3	2.5
$D^+ \rightarrow \omega e^+ \nu_e$	$14.67 \pm 0.03$	$128.5 \pm 12.6$	$1.82 \pm 0.18 \pm 0.07$	$1.6^{+0.7}_{-0.6} \pm 0.1$	1.3	2.5

$$\frac{\Gamma(D^0 \rightarrow \rho^- e^+ \nu_e)}{2\Gamma(D^+ \rightarrow \rho^0 e^+ \nu_e)} = 1.03 \pm 0.09^{+0.08}_{-0.02}$$

CLEO: arXiv:1112.2884 [hep-ex] (Dec 2011)

# $D_s \rightarrow \phi \mu \nu$ form factors: Experiment & Lattice

---

- Due to higher mass of spectator quark, expect more reliable lattice QCD form factor calculations than for  $D^+$ .
- Recent results for  $D_s \rightarrow \phi e \nu$  show good agreement:

	HPQCD 2011	BaBar 2008 [3]	UKQCD 2001 [2]
$A_1(0)$	0.594(22)	0.607(11)(19)(18)	0.63(2)
Local $A_1(0)$	0.603(20)	–	–
$V(0)$	0.903(67)	1.122(85)*	0.85(4)
$A_0(0)$	0.686(17)	–	0.63(2)
$A_2(0)$	0.401(80)	0.463(61)*	0.62(5)
$r_V$	1.52(12)	1.849(60)(95)	1.35(7)*
$r_2$	0.62(12)	0.763(71)(65)	0.98(8)*

**Table and HPQCD results from: Donald, Davies, Koponen: arXiv:1111.0254 [hep-lat], Nov 2011**  
**BaBar: Phys.Rev. D78 (2008) 051101**

# $D_s \rightarrow KK e \nu$ and the $f_0$ at BaBar

BaBar 2008

- $D_s \rightarrow KK e \nu$  at BaBar:  
 KK system **dominated by  $\phi$** , but there is a significant **S-wave** component (first observed by BaBar), evident in as an **asymmetry in  $\cos(\theta_\nu)$** .

- BaBar measure an  $f_0$  BR:

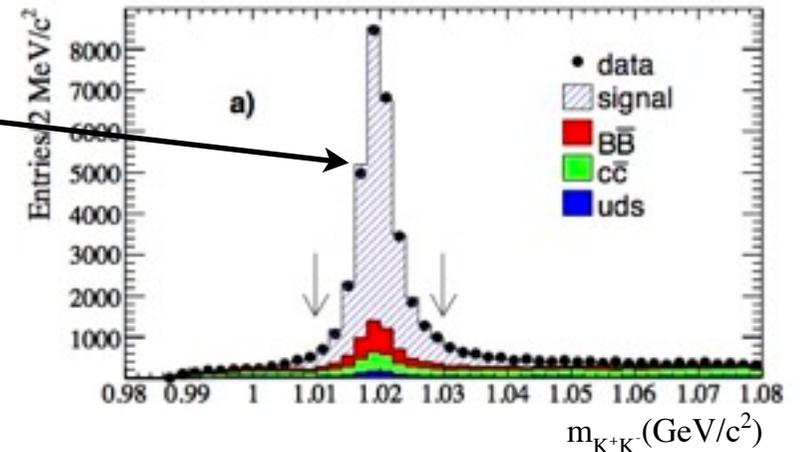
$$\frac{BR(D_s \rightarrow f_0 e^+ \nu)}{BR(D_s \rightarrow \phi e^+ \nu)} = (4.5^{+2.5}_{-1.6} \pm 0.6)\%$$

- Which is similar to the  $D^+$  system:

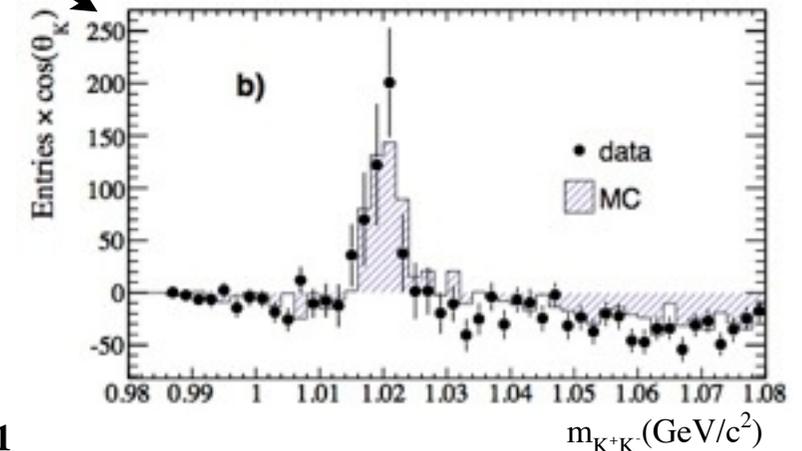
$$\frac{BR(D^+ \rightarrow K^- \pi^+ e^+ \nu)_S}{BR(D^+ \rightarrow K^- \pi^+ e^+ \nu)_{total}} = (5.79 \pm 0.16 \pm 0.15)\%$$

BaBar: Phys.Rev. D78 (2008) 051101

KK mass distribution



$\cos(\theta_\nu)$ -weighted KK mass distribution

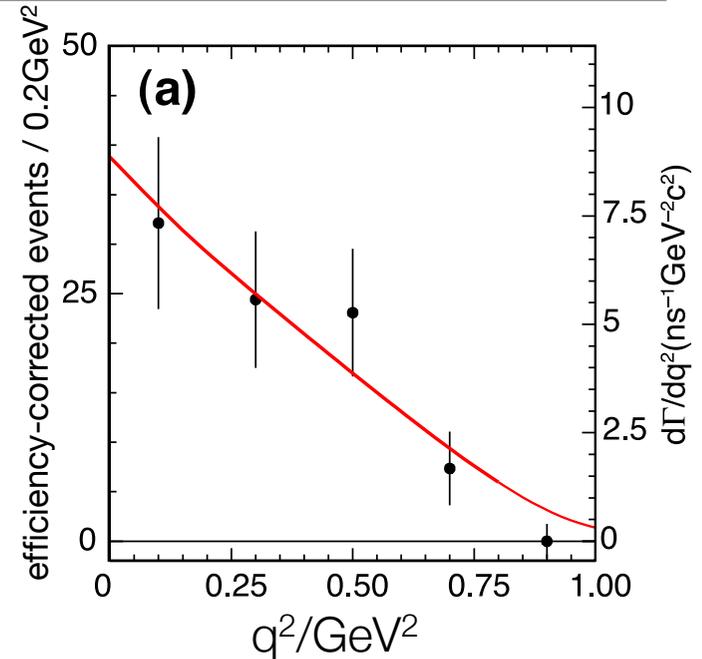


# $D_s^+ \rightarrow f_0 \mu^+ \nu$ at CLEO-c

CLEO-c 2009  
+ LHCb 2012

- $D_s \rightarrow f_0 e \nu$  was subsequently analysed by CLEO-c (2009) with  $f_0 \rightarrow \pi\pi$ .
- CLEO-c performed a full form-factor analysis.
- The result was used to evaluate the form-factor ratio at  $q^2 = 0$ .

$$R_{f/\phi} \equiv \frac{\frac{d\Gamma}{dq^2}(D_s^+ \rightarrow f_0(980)e^+\nu, f_0 \rightarrow \pi^+\pi^-) |_{q^2=0}}{\frac{d\Gamma}{dq^2}(D_s^+ \rightarrow \phi e^+\nu, \phi \rightarrow K^+K^-) |_{q^2=0}} = (42 \pm 11)\%$$



CLEO: **Phys.Rev. D80 (2009) 052009**

- This provided further evidence that  $\mathcal{B}(B_s \rightarrow J/\psi f_0) / \mathcal{B}(B_s \rightarrow J/\psi \phi)$  could be large enough to make a significant contribution to measuring  $\sin(\phi_s)$ . Recently, LHCb found:

$$\frac{\mathcal{B}(\bar{B}_s^0 \rightarrow J/\psi \pi^+ \pi^-)}{\mathcal{B}(\bar{B}_s^0 \rightarrow J/\psi \phi)} = (21.28 \pm 0.51 \pm 0.56)\%$$

(see also [Yuehong Xie](#) and [Liming Zhang's talks](#), yesterday)

LHCb: **arXiv:1204.5643 [hep-ex] (2012)**

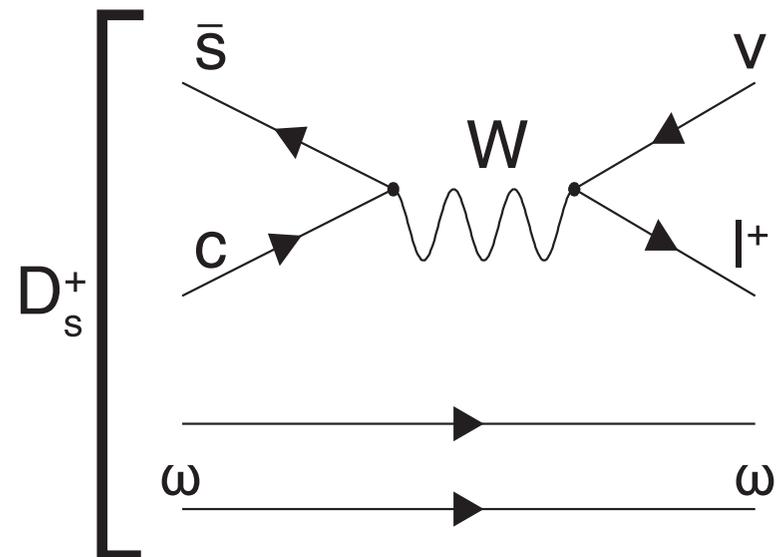
# CLEO-c search for $D_s \rightarrow \omega e \nu$

CLEO-c 2011

- Highly suppressed. Potential processes (Gronau & Rosner *Phys.Rev. D79* (2009) 074006):

- Via  $\omega$ - $\phi$  mixing ( $\omega$  has  $s\bar{s}$  component)?  $BR < 2 \cdot 10^{-4}$
- Via weak annihilation (radiate an  $\omega$  in a non-perturbative process before annihilating)?  $BR \sim (0.13 \pm 0.05)\%$
- Anything larger might hint at a **four-quark content** of the  $D_s$  (4-quark systems have been suggested to explain several exotic charmonium states).

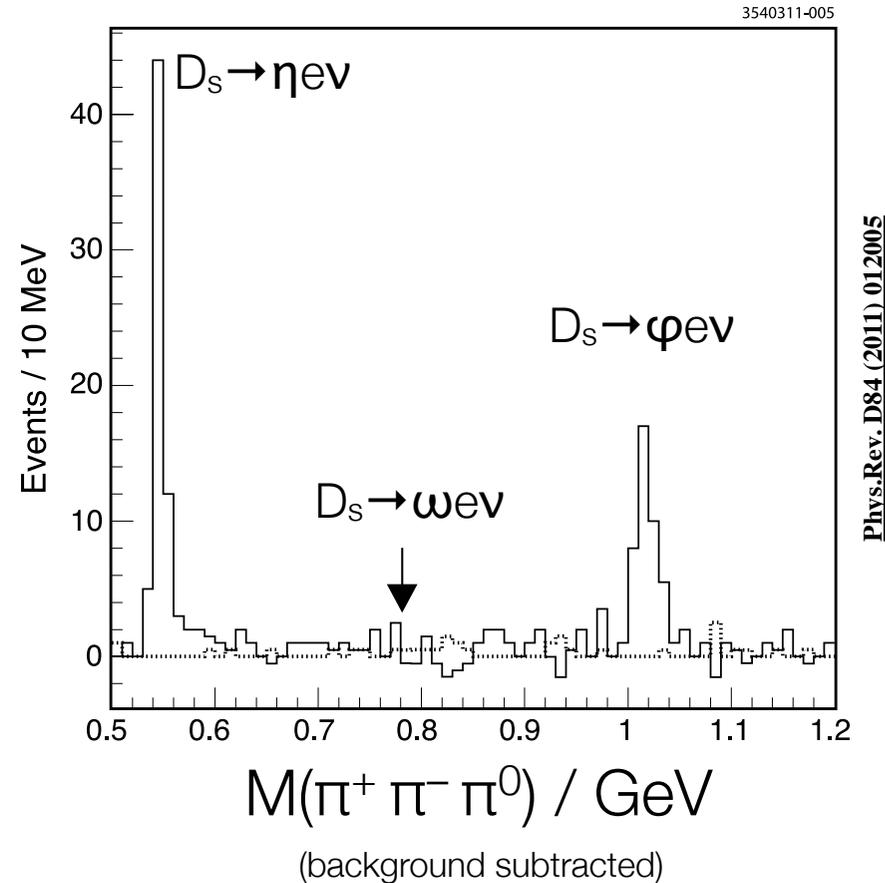
$D_s \rightarrow \omega e \nu$  as a probe for a 4-quark contribution to the  $D_s$



# CLEO-c search for $D_s \rightarrow \omega e \nu$

CLEO-c 2011

- Analysis makes careful use of control channels  $D_s \rightarrow \eta e \nu$  and  $D_s \rightarrow \phi e \nu$ .
- No evidence for  $D_s \rightarrow \omega e \nu$ .
- At 90% CL:  
 $\mathcal{B}(D_s^+ \rightarrow \omega e^+ \nu) < 0.20\%$   
(compatible with Gronau & Rosner's estimate of  $(0.13 \pm 0.05)\%$ , no evidence of 4-quark content of  $D_s$ .)



**CLEO: Phys.Rev. D84 (2011) 012005**

# Calculate $\Lambda_c \rightarrow \Lambda \ell \nu$

---

- $\Lambda_c$  branching fractions are normalised to  $\Lambda_c \rightarrow pK\pi$ , which has a 26% uncertainty.
- This in turn dominates many uncertainties -  $\Lambda_c$  BF,  $\Lambda_b \rightarrow \Lambda_c X$  BF,  $\Lambda_b$  production fractions

$$\frac{\Lambda_b}{f_u + f_d} = [0.404 \pm 0.017(\text{stat}) \pm 0.027(\text{syst}) \pm 0.105(\text{Br})] \\ \times [1 - (0.031 \pm 0.004(\text{stat}) \pm 0.003(\text{syst}))p_T(\text{GeV})] .$$

- Rosner suggests to use a calculated  $\Lambda_c \rightarrow \Lambda e \nu$  BF for normalisation instead. Currently measured as  $\mathcal{B}(\Lambda_c \rightarrow \Lambda e \nu) = (2.1 \pm 0.6)\%$ .
- Requires a challenging calculation of 4 form factors on lattice. But a precision of better than 25% would already help!

**Jonathan Rosner: [arXiv:1205.4964 \[hep-ph\]](https://arxiv.org/abs/1205.4964) (23 May 2012)**

# Summary

---

- Many new and improved form factor measurements. Where LQCD exist, they are generally in good agreement with data. Time to tackle baryons?
- Beyond the form factor: innovative ways of using semileptonic charm decays include rare decays to learn about the structure of  $D_s$ ;  $D \rightarrow V \ell \nu$  as interferometer to measure S-wave phases.

# Summary

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- Most results are from experiments that have stopped data taking, and most are statistics limited



# Summary

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- Most results are from experiments that have stopped data taking, and most are statistics limited, but there is a future:

BES III have shown first results, from 1/3 of their data - there is much more to come.

# Backup

---

# Quark content of $f_0$

- If  $|f_0\rangle = \cos\theta |\bar{s}s\rangle + \frac{\sin\theta}{\sqrt{2}} |(\bar{u}u + \bar{d}d)\rangle$  (Aliev & Savci)
- From BES:  $\frac{\mathcal{B}(f_0 \rightarrow K^+K^-)}{\mathcal{B}(f_0 \rightarrow \pi^+\pi^-)} = (25_{-11}^{+17})\%$ . Assuming KK,  $\pi\pi$  dominate:  $\mathcal{B}(f_0 \rightarrow \pi^+\pi^-) = (50_{-9}^{+7})\%$   
and thus from CLEO-c:  $\mathcal{B}(D_s^+ \rightarrow f_0 e^+ \nu) = (0.40 \pm 0.06 \pm 0.06)\%$
- Using  $\mathcal{B}(D_s^+ \rightarrow f_0 e^+ \nu) = \cos^2\theta \times (0.41)\%$  (Aliev & Savci)  
CLEO-c get:  $\cos^2\theta = 0.98_{-0.21}^{+0.02}$
- Intriguing: If  $f_0$  is predominantly s-sbar, why does it predominantly decay to  $\pi\pi$ ?  
4-quark content?

[17] T. M. Aliev and M. Savci, “Semileptonic decays of pseudoscalar mesons to scalar  $f_0$  meson,” arXiv:hep-ph/0701108. A previous work, I. Bediaga, F. S. Navarra and M. Nielsen, Phys. Lett. B **579**, 59 (2006), predicts a smaller width with a 50% error, which leads to a smaller value of  $\cos^2\theta$  with a large error.

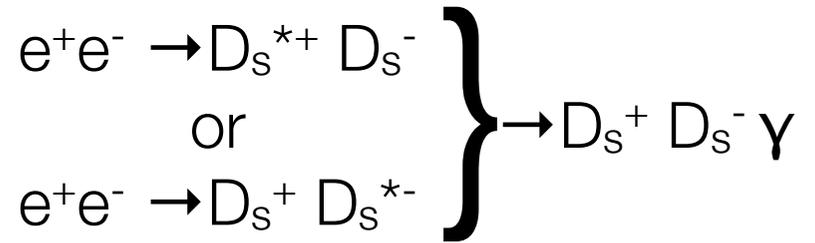
[18] M. Ablikim et al. (BES), Phys. Rev. D **70**, 092002 (2004); M. Ablikim et al. (BES), Phys. Rev. D **72**, 092002 (2005)

[2] A. H. Fariborz, R. Jora, and J. Schechter, “Global Aspects of the Scalar Meson Puzzle,” arXiv:0902.2825v1 [hep-ph]; A. V. Anisovich *et al.*, “The Riddle of the  $f_0(980)$  and  $a_0(980)$ : Are They the Quark-Antiquark States?” arXiv:hep-ph/0508260 and references contained therein; T. Branz, T. Gutsche, V. E. Lyubovitskij, Phys. Rev. D **79**, 014035 (2009) arXiv:0812.094 [hep-ph]; V. Baru, J. Haidenbauer, C. Hanhart, Yu. Kalashnikova, A. Kudryavtsev, Phys. Lett. B **586**, 53 (2004) arXiv:hep-ph/0308129.

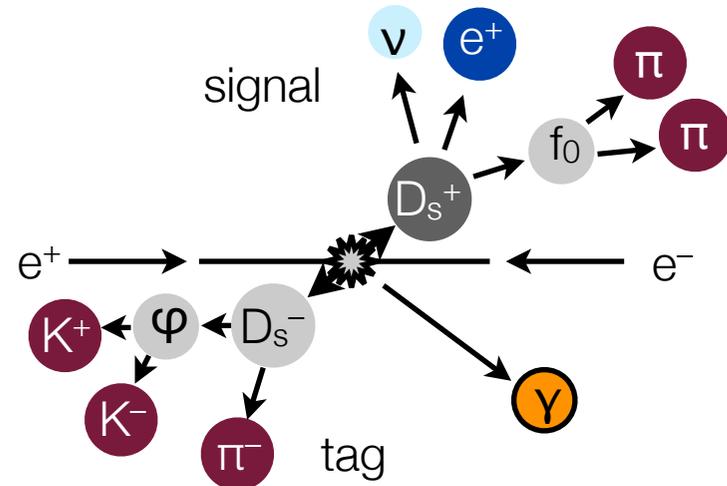
**CLEO: Phys.Rev. D80 (2009) 052009**

# $D_s^+ \rightarrow f_0 \mu^+ \nu$ and $D_s^+ \rightarrow \varphi \mu^+ \nu$ at CLEO-c

- CLEO produces  $D_s^* D_s \rightarrow D_s D_s \gamma$  (giving an additional photon).



- Step 1: Fully reconstruct “tag  $D_s$ ”
- Step 2: Identify photon and use beam constraint to reconstruct signal  $D_s$  mass:  
 $(p_{\text{beam}} - p_{\text{tag}} - p_{\gamma})^2 = \text{consistent with } D_s \text{ mass for signal.}$
- Step 3: Find missing mass from beam constraints and reconstructed signal.



# $D_s^+ \rightarrow f_0 \mu^+ \nu$ and $D_s^+ \rightarrow \phi \mu^+ \nu$ at CLEO-c

- Motivation: Relationship to  $B \rightarrow J/\psi f_0$ . originally related to  $D_s \rightarrow f_0 \pi$ :

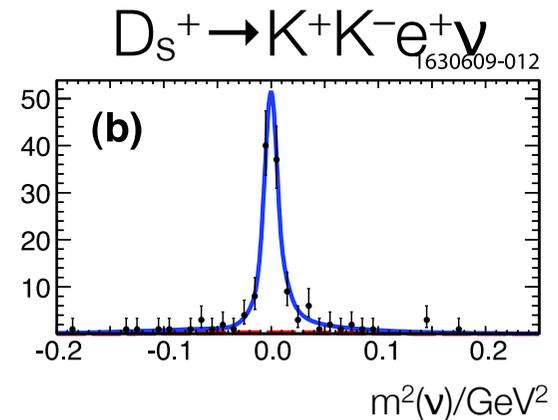
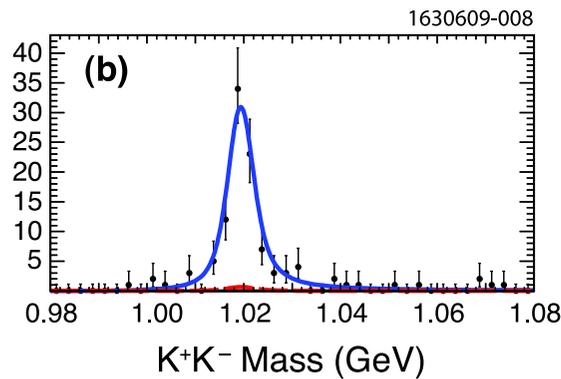
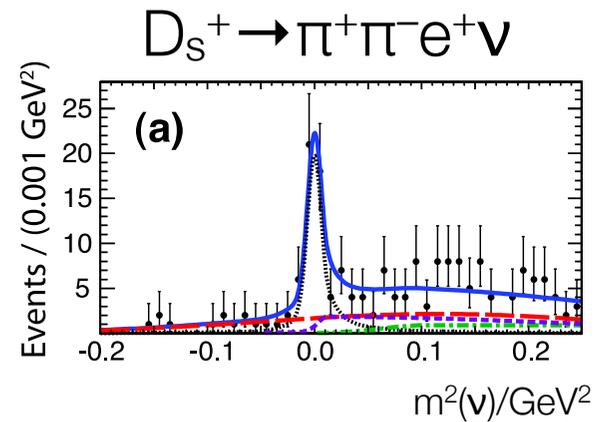
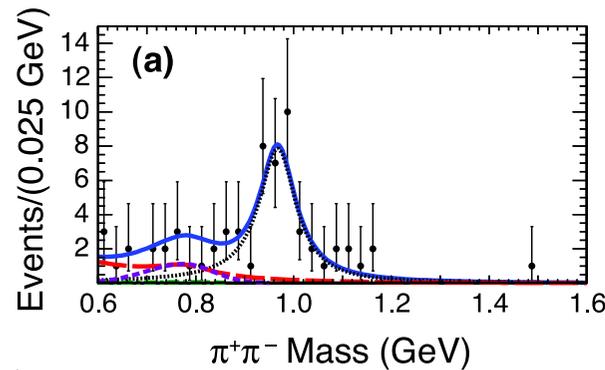
$$R_{f/\phi} \equiv \frac{\Gamma(B_s^0 \rightarrow J/\psi f_0, f_0 \rightarrow \pi^+ \pi^-)}{\Gamma(B_s^0 \rightarrow J/\psi \phi, \phi \rightarrow K^+ K^-)} = \frac{\Gamma(D_s^+ \rightarrow f_0 \pi^+, f_0 \rightarrow \pi^+ \pi^-)}{\Gamma(D_s^+ \rightarrow \phi \pi^+, \phi \rightarrow K^+ K^-)} \approx (20-30)\%$$

- But:  $J/\psi$  is spin 1, while  $\pi^+$  is spin 0. Hence, it might be better to use the ratio of rates at  $q^2 = 0$  (maximising the phase space, thus making it more similar to the B decay):

$$R_{f/\phi} = \frac{\frac{d\Gamma}{dq^2}(D_s^+ \rightarrow f_0(980)e^+ \nu, f_0 \rightarrow \pi^+ \pi^-) |_{q^2=0}}{\frac{d\Gamma}{dq^2}(D_s^+ \rightarrow \phi e^+ \nu, \phi \rightarrow K^+ K^-) |_{q^2=0}}$$

# $D_s^+ \rightarrow f_0 \mu^+ \nu$ and $D_s^+ \rightarrow \varphi \mu^+ \nu$ at CLEO-c

reconstructed  $\nu$  mass-squared  $(p_{\text{beam}} - \Sigma p_{\text{reco}})^2$



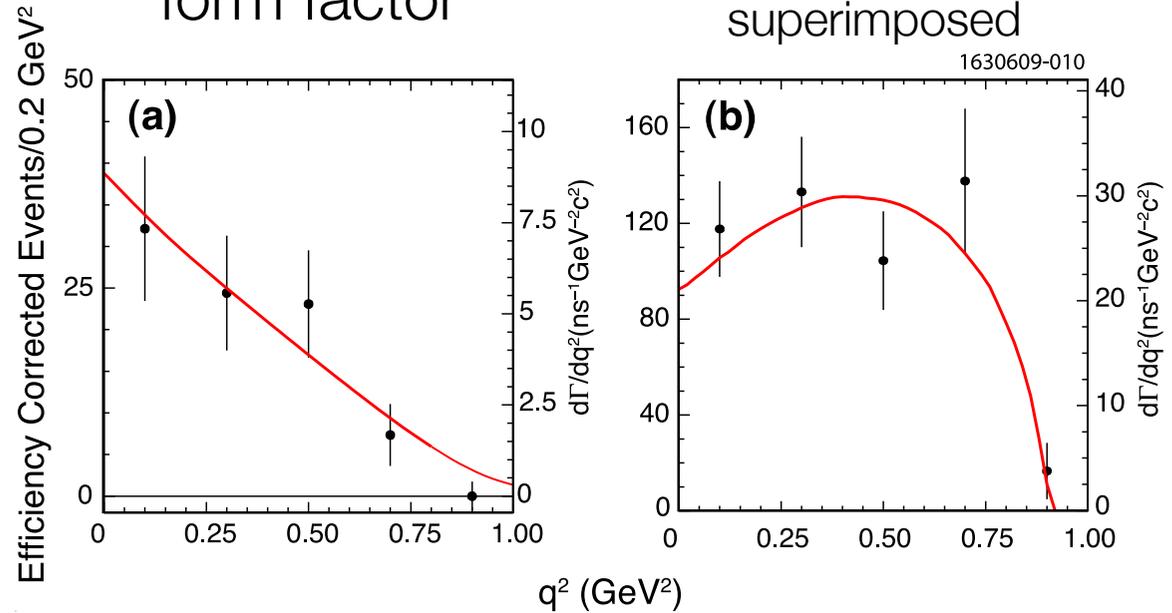
# $D_s^+ \rightarrow f_0 \mu^+ \nu$ and $D_s^+ \rightarrow \phi \mu^+ \nu$ at CLEO-c

$$B(D_s^+ \rightarrow f_0(980)e^+\nu)B(f_0 \rightarrow \pi^+\pi^-) = (0.20 \pm 0.03 \pm 0.01)\%.$$

CLEO-c data for  $\phi$   
form factor with  
BaBar result  
superimposed

CLEO-c fit for  $f_0$   
form factor

$$B(D_s^+ \rightarrow \phi e^+\nu) = (2.36 \pm 0.23 \pm 0.13)\%$$



$$R_{f/\phi} \equiv \frac{\frac{d\Gamma}{dq^2}(D_s^+ \rightarrow f_0(980)e^+\nu, f_0 \rightarrow \pi^+\pi^-) |_{q^2=0}}{\frac{d\Gamma}{dq^2}(D_s^+ \rightarrow \phi e^+\nu, \phi \rightarrow K^+K^-) |_{q^2=0}} = (42 \pm 11)\%$$

LHCb found:  $R$  for the  $f_0(980)$ ,  $0.149 \pm 0.006^{+0.028}_{-0.003}$ ,

# $D_s^+ \rightarrow f_0 \mu^+ \nu$ and $D_s^+ \rightarrow \varphi \mu^+ \nu$ at CLEO-c

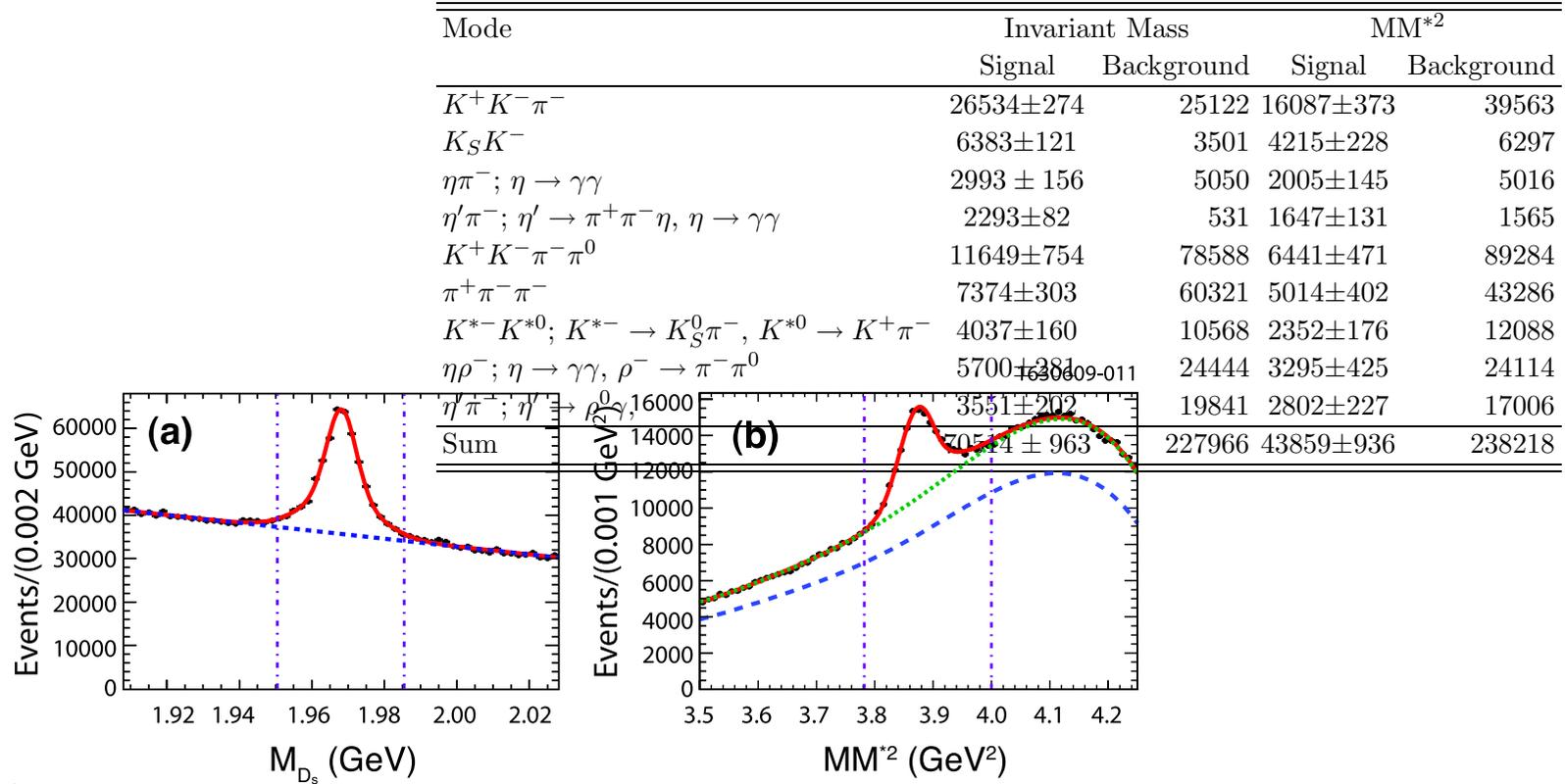
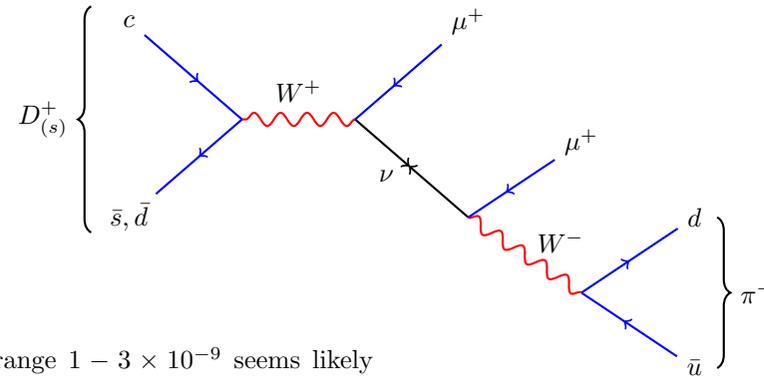
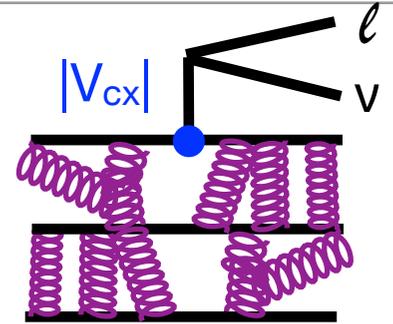
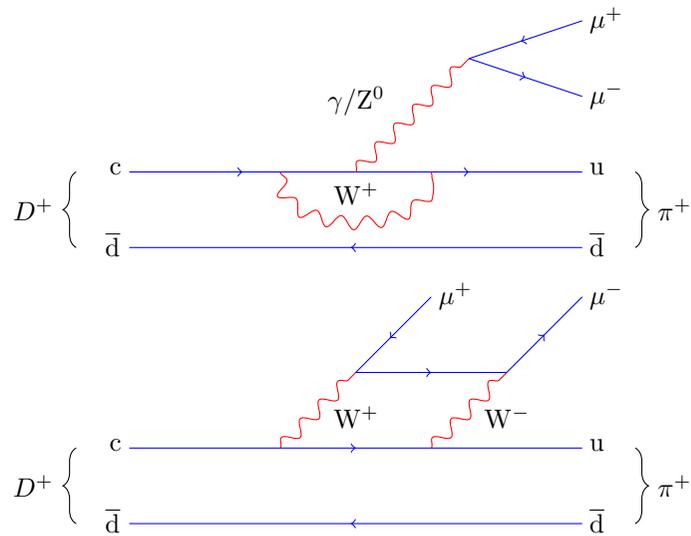


FIG. 2: (a) Invariant mass of  $D_s^-$  candidates summed over all decay modes and fit to a two-Gaussian signal shape plus a straight line for the background. The vertical dot-dashed lines indicate the  $\pm 17.5$  MeV definition of the signal region. (b) The  $MM^{*2}$  distribution summed over all modes. The curves are fits to the number of signal events using the Crystal Ball function and two 5th order Chebychev background functions; the dashed curve shows the background from fake  $D_s^-$  tags, while the dotted curve in (b) shows the sum of the backgrounds from multiple photon combinations and fake  $D_s^-$  tags. The vertical dashed lines show the region of events selected for further analysis.

# Rare Semileptonic D decays



Predictions of the rate of these processes are sparse though something in the range  $1 - 3 \times 10^{-9}$  seems likely for the FCNC decay [3, 4, 5] though it is noted that great care should be taken when avoiding pollution from the long-distance resonance contributions. The LFV mode is forbidden in the SM.

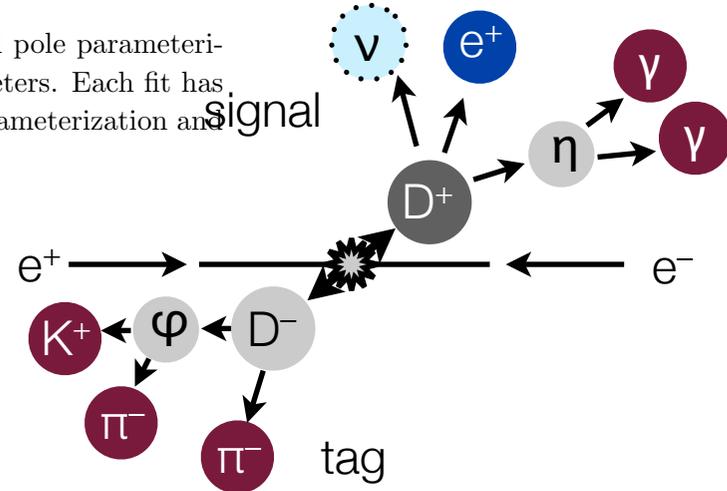
- [3] S. Fajfer, S. Prelovsek, and P. Singer, *Rare charm meson decays  $D \rightarrow Pl^+l^-$  and  $c \rightarrow ul^+l^-$  in SM and MSSM*, Phys. Rev. **D64** (2001) 114009, [arXiv:hep-ph/0106333](#).
- [4] S. Fajfer, N. Kosnik, and S. Prelovsek, *Updated constraints on new physics in rare charm decays*, Phys. Rev. **D76** (2007) 074010, [arXiv:0706.1133](#).
- [5] A. Paul, I. I. Bigi, and S. Recksiegel, *On  $D \rightarrow X_u l^+l^-$  within the Standard Model and Frameworks like the Littlest Higgs Model with  $T$  Parity*, Phys. Rev. **D83** (2011) 114006, [arXiv:1101.6053](#).

# Combine

Analysis	$f_+(0) V_{cd} $	$r_1$	$\rho$	$\chi^2/\text{d.o.f.}$
Tagged	0.094(9)(3)	2.17(4.50)(1.12)	0.83	0.7/(3 - 2)
GR	0.085(6)(1)	-2.89(2.24)(32)	0.81	0.0/(3 - 2)
Combined	0.086(6)(1)	-1.83(2.23)(28)	0.81	2.5/(6 - 2)

TABLE VI.  $D^+ \rightarrow \eta e^+ \nu_e$  form factor fit results using the simple and modified pole parameterizations. The quantity  $\rho$  is the correlation coefficient between the two fit parameters. Each fit has  $(6 - 2)$  degrees of freedom. The shape parameter is  $m_{\text{pole}}$  for the simple pole parameterization and  $\alpha$  for the modified pole parameterization.

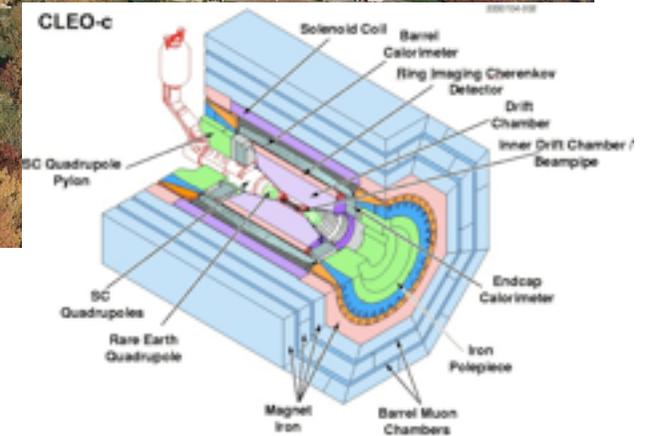
	Simple Pole	Modified Pole
$f_+(0) V_{cd} $	$0.086 \pm 0.005 \pm 0.001$	$0.086 \pm 0.005 \pm 0.001$
shape parameter	$1.87 \pm 0.24 \pm 0.00$	$0.21 \pm 0.44 \pm 0.05$
$\rho$	0.75	-0.80
$\chi^2$	2.5	2.5



These measurements are consistent with our previous results [6], which they supersede, and with the particle data group's upper limits [10]. They are also consistent with predictions from both the ISGW2 [2] and Fajfer-Kamenic [21] models. The upper limit for  $D^+ \rightarrow \phi e^+ \nu_e$  is about twice as restrictive as our previous limit [6].

# CLEO-c at CESR

- CLEO-c at the CESR  $e^+ e^-$  collider on the Cornell campus.
- CLEO-c run now complete, with
  - $818 \text{ pb}^{-1}$  at  $\psi(3770)$ , corresponding to  $3.0\text{M } D^0\bar{D}^0$  and  $2.4\text{M } D^+D^-$  events
  - $600 \text{ pb}^{-1}$  at  $4170 \text{ MeV}$ , corresponding to  $600\text{k } D_s D_s^*$  events



# BES results

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BESIII Preliminary

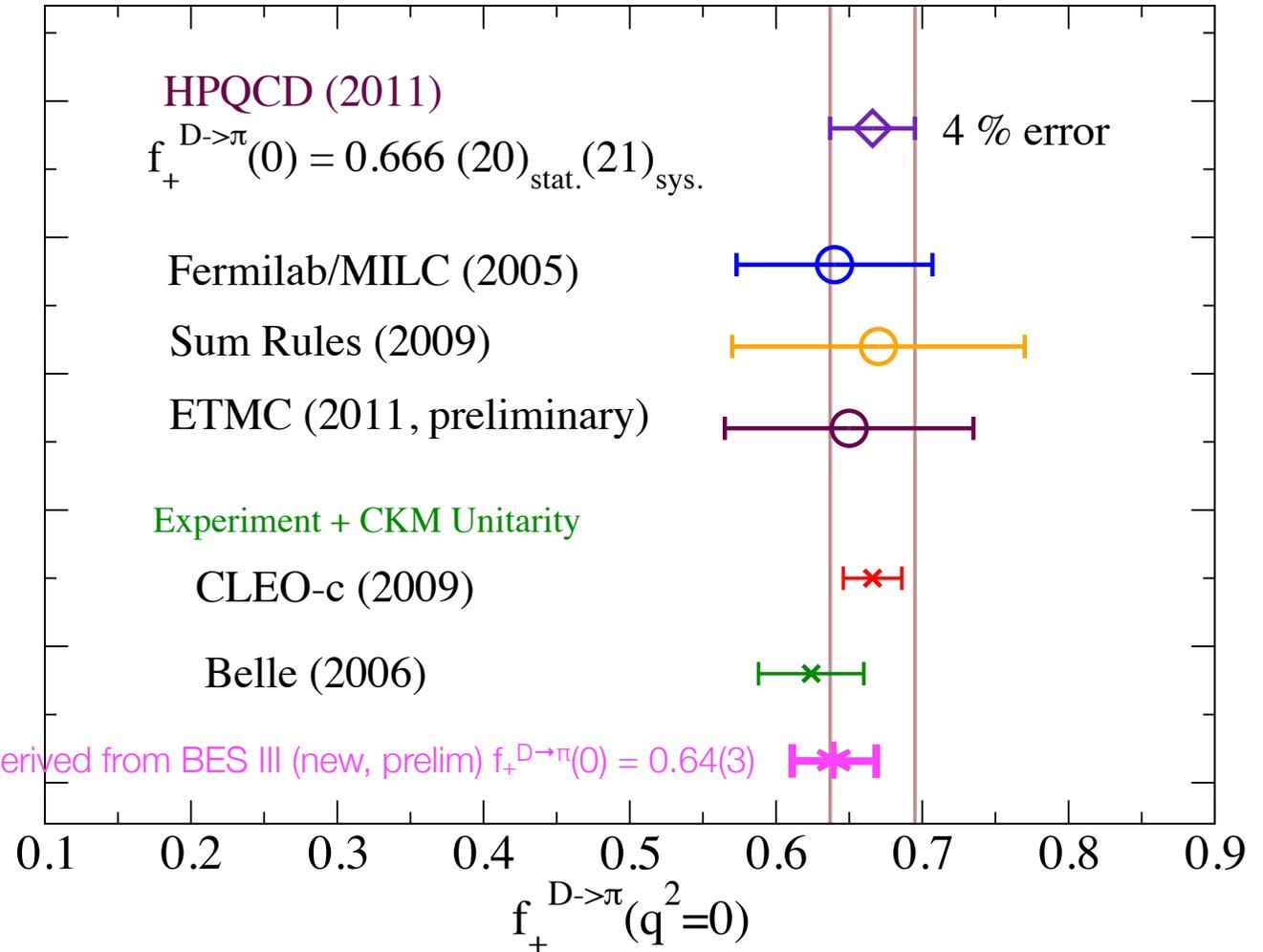
Mode	Data Yield	Fraction of All Tags (%)	Tag Efficiency(%)
$D^0 \rightarrow K^- \pi^+$	$159,929 \pm 413$	20.7	$62.08 \pm 0.07$
$D^0 \rightarrow K^- \pi^+ \pi^0$	$323,348 \pm 667$	41.8	$33.56 \pm 0.03$
$D^0 \rightarrow K^- \pi^+ \pi^0 \pi^0$	$78,467 \pm 480$	10.1	$14.93 \pm 0.04$
$D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$	$211,910 \pm 550$	27.4	$36.80 \pm 0.04$

# $f_+^{D \rightarrow \pi}(0)$ from experiment and theory

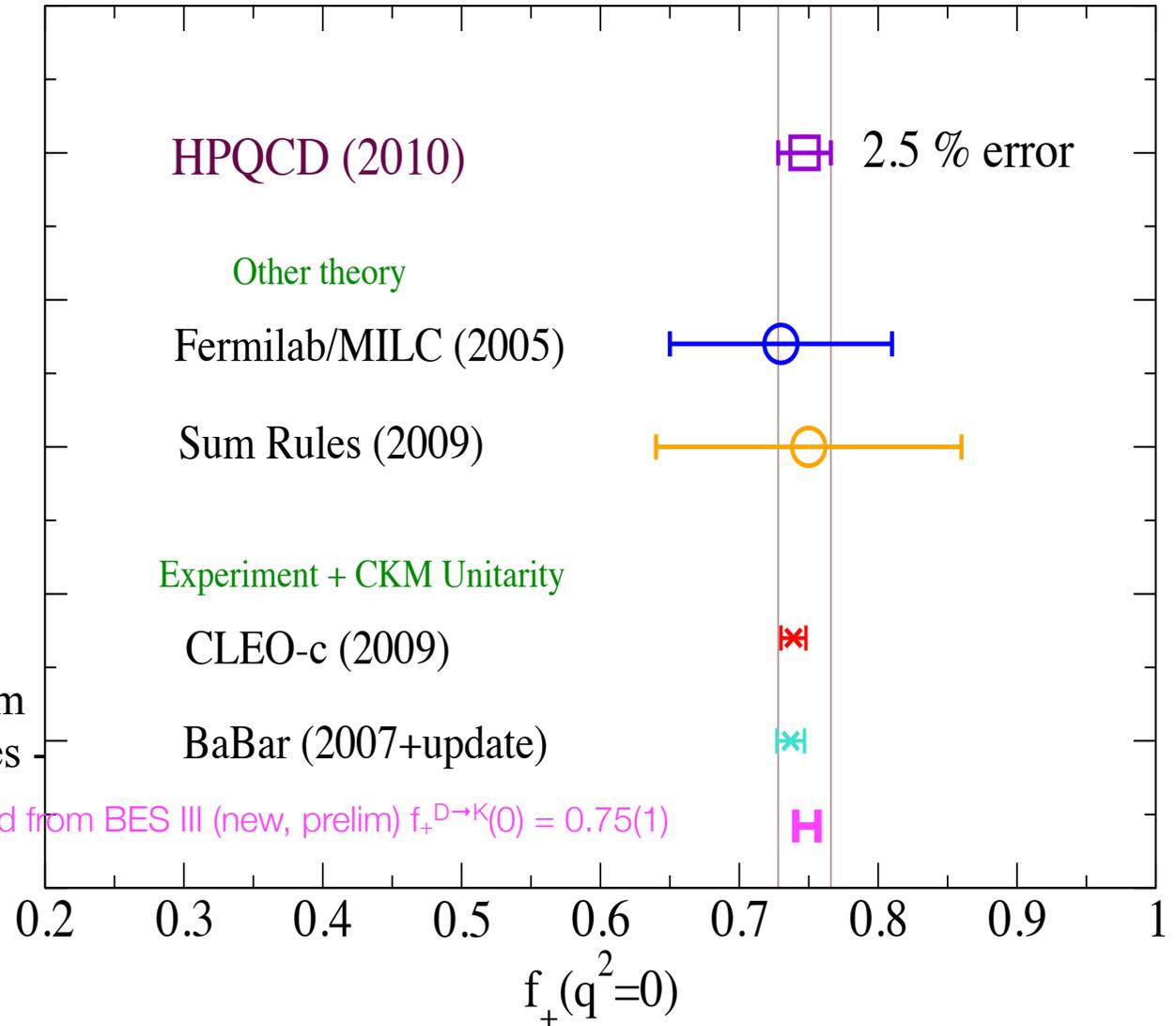
Note: CLEO-c result from combination of  $D^+$  and  $D^0$  decays, which explains the better stat error - for individual channels, uncertainties are virtually identical

With  $|V_{cd}| = 0.2252 \pm 0.0007$ , I get from BES III new result (3 par series - as used by CLEO-c):

Taken from Phys.Rev. D84 (2011) 114505 and modified (added BES III)



Taken from Phys.Rev. D82 (2010) 114506 and modified (added BES III)

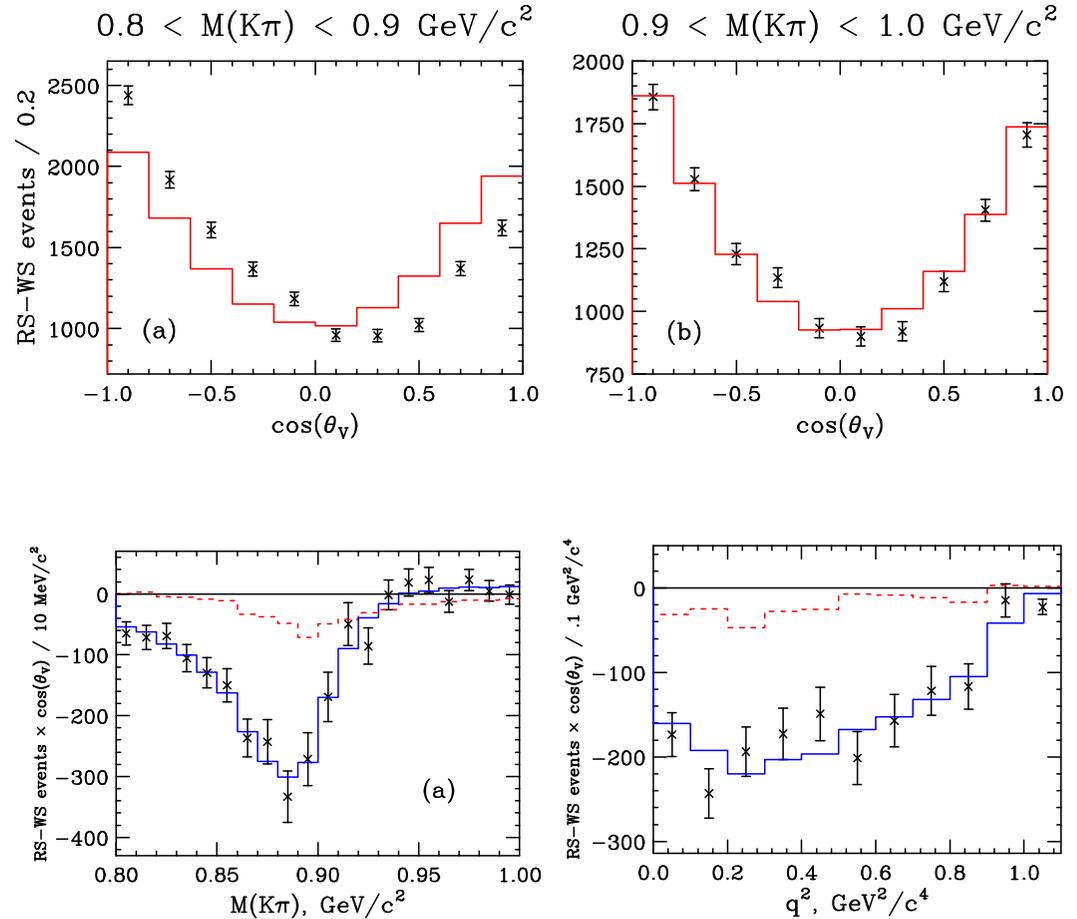


With  $|V_{cs}| = 0.97345$ , I get from BES III new result (3 par series as used by CLEO-c):

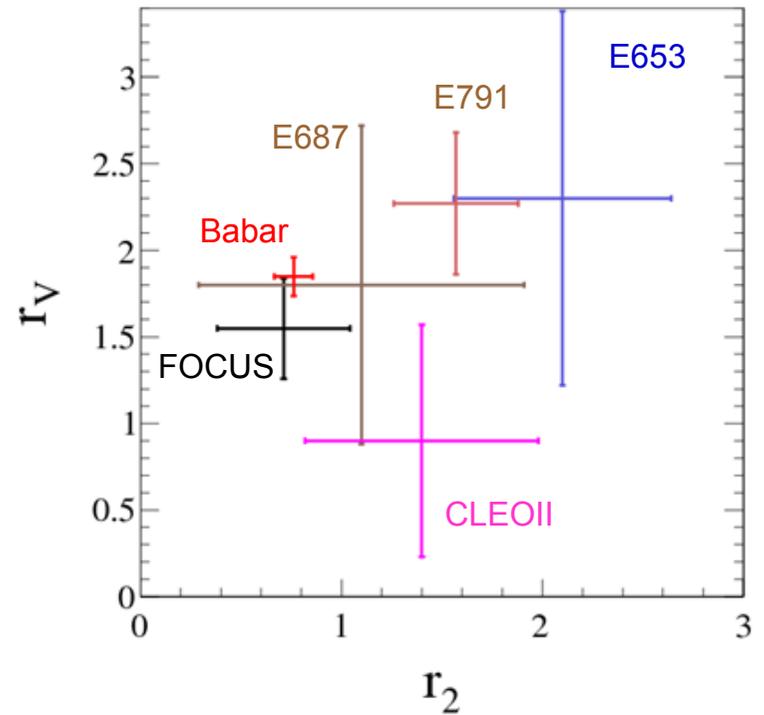
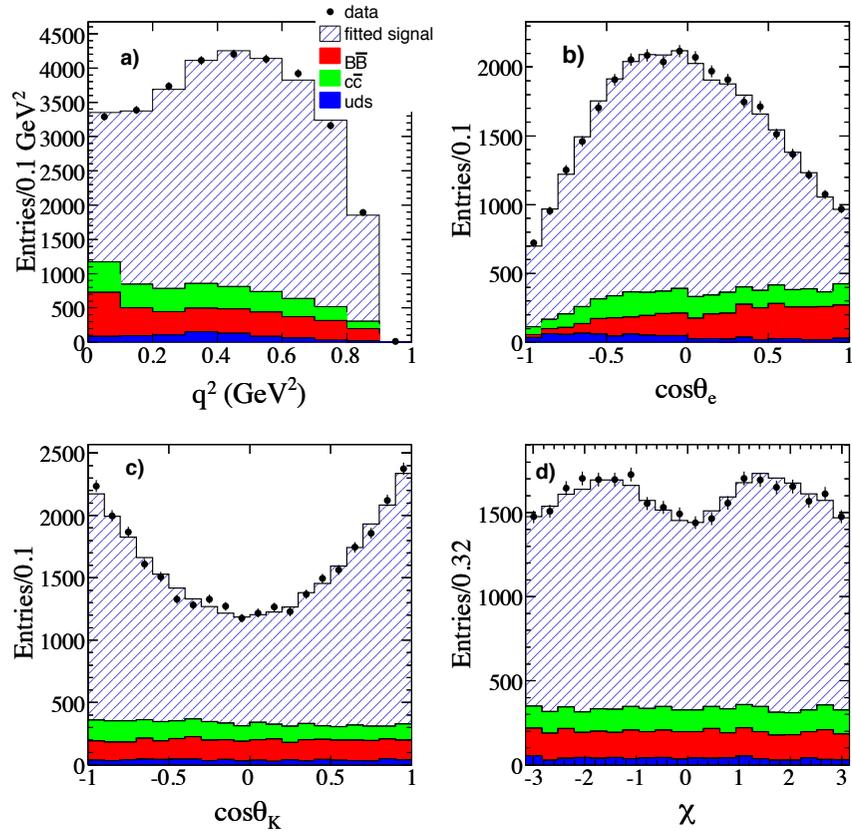
derived from BES III (new, prelim)  $f_+^{D \rightarrow K}(0) = 0.75(1)$

# FOCUS - evidence for $K\pi$ S-wave in $D \rightarrow K\pi \mu\nu$

- FOCUS find discrepancies between data (black) and  $D \rightarrow K^* \mu\nu$  MC (red) in  $\cos(\theta_V)$  distribution below pole.
- S wave – P wave interference results in asymmetry in  $\cos(\theta_V)$ .
- Plots below show  $\cos(\theta_V)$  - weighted distributions in  $M(K\pi)$  and  $q^2$ .
- Discrepancies get resolved by adding a constant S-wave term  $Ae^{i\delta} = 0.36 \cdot e^{(i\pi/4)} \text{GeV}^{-1}$  (blue).

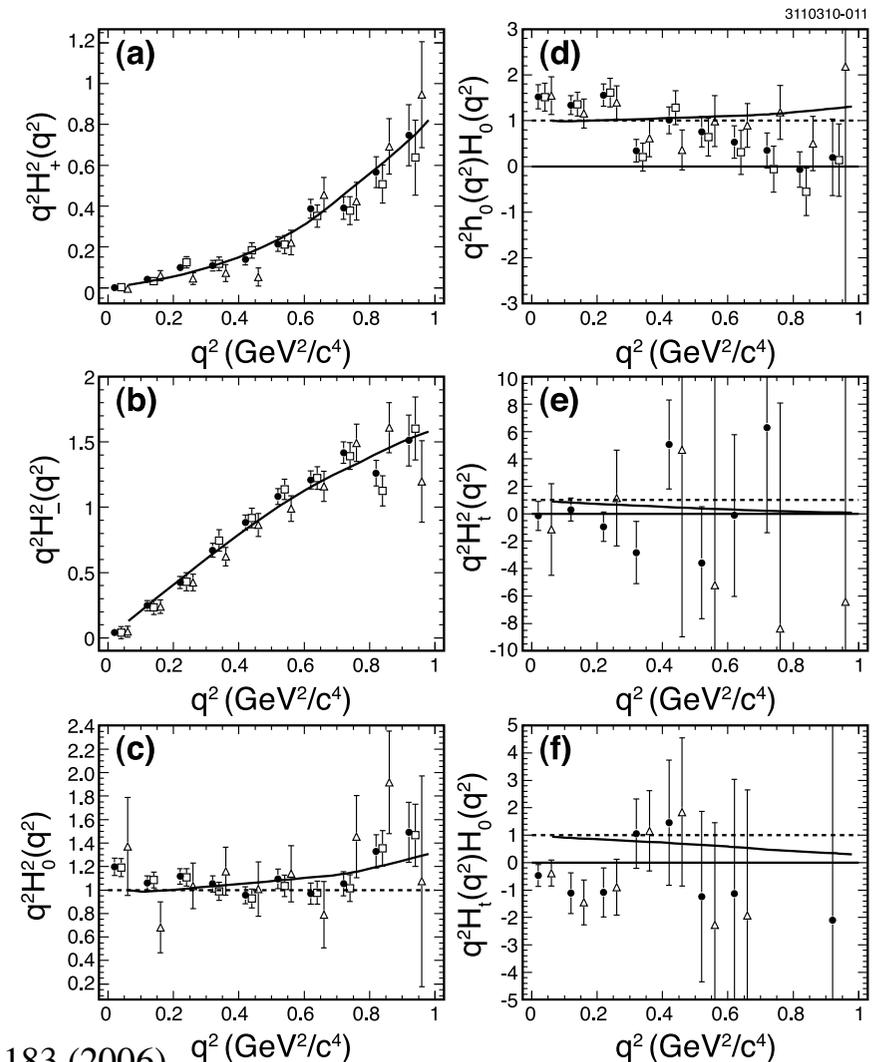


# $D_s \rightarrow KK e \nu$ at BaBar (2008)



# Non-parametric form factors

- CLEO-c (2010) use a projective reweighting technique pioneered by FOCUS (2006).
- Includes parameterisation for highly-suppressed right-handed lepton (adds a helicity  $H_T$ , and form factor,  $A_3$ )
- Projection = integration over all but one variable. Weights are chosen such that this integral is zero for all terms, except for the terms of interest.

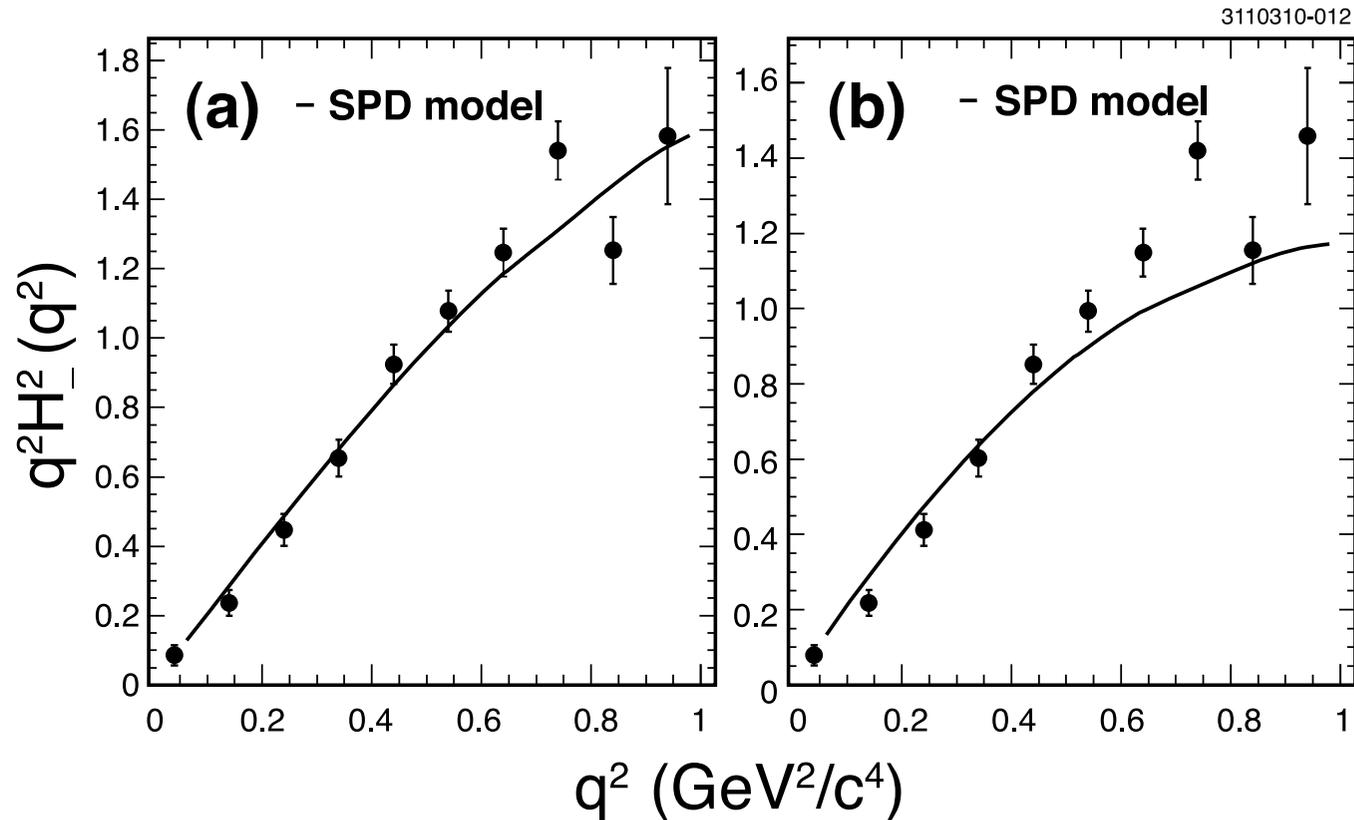


CLEO: Phys.Rev. D81 (2010) 112001; FOCUS: Phys. Lett. B 633, 183 (2006)

# Non-parametric vs simple pole

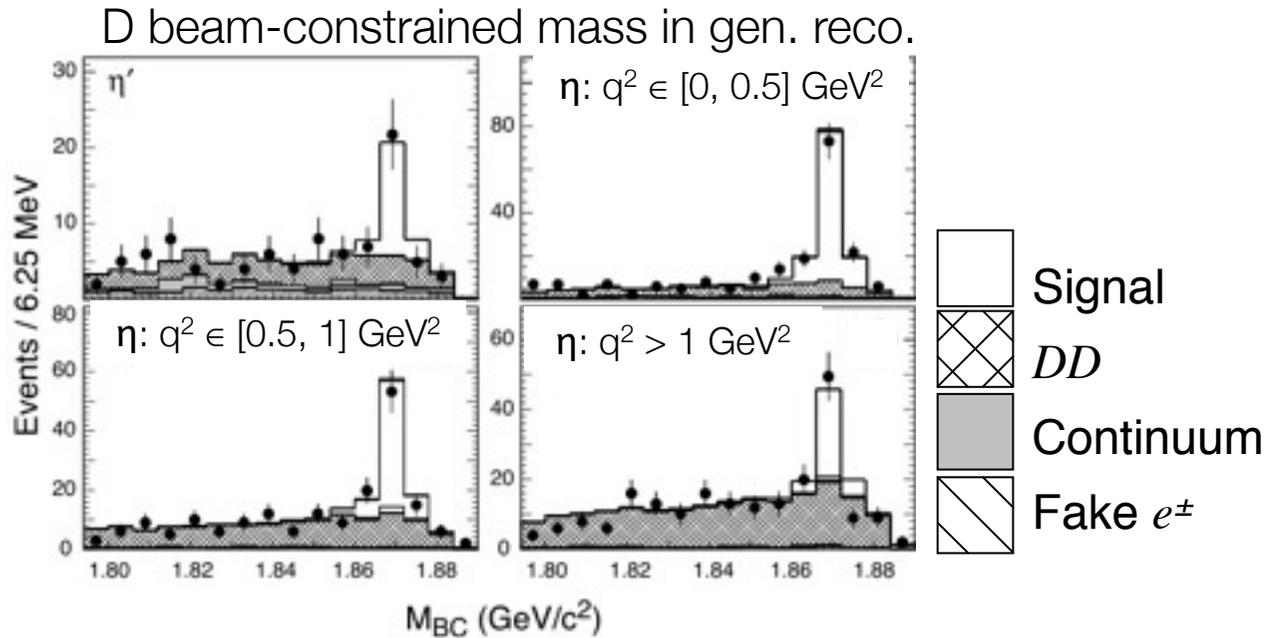
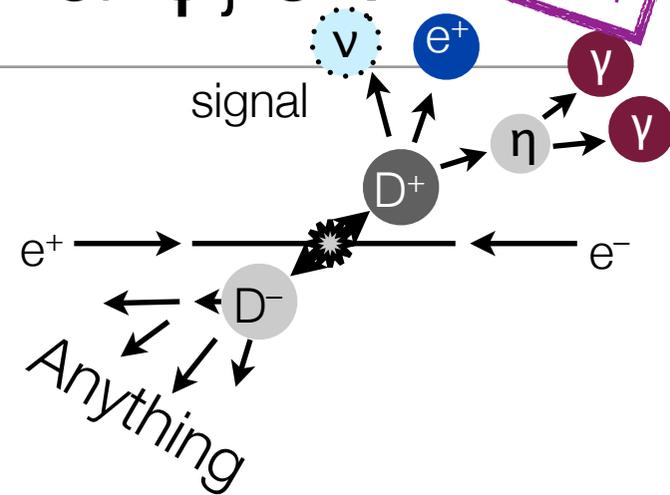
finite pole mass

infinite pole mass



# Generic Reconstruction of $D^+ \rightarrow \{\eta, \eta' \text{ or } \phi\} e^+ \nu$

CLEO-c 2011



- Leads to first observation of  $D^+ \rightarrow \eta' e^+ \nu$ , CL:  $5.8\sigma$
- GR dominates precision on  $D^+ \rightarrow \eta e^+ \nu$  form factor.

CLEO: Phys.Rev. D84 (2011) 032001

Mode	$\mathcal{B}_{\text{tag}} [10^{-4}]$	$R_{\text{GR}} [\%]$	$\mathcal{B}_{\text{GR}} [10^{-4}]$
$\eta' e^+ \nu_e$	$2.5^{+1.6}_{-1.0} (0.1)$	0.237(58)(5)	2.16(53)(7)
$\phi e^+ \nu_e$	< 0.9 @ 90% confidence level (C.L.)		
$\eta e^+ \nu_e$	11.1(1.3)(0.4)	1.28(11)(4)	11.7(1.0)(0.4)
$\eta e^+ \nu_{e,0-0.5}$	6.53(94)(26)	0.625(69)(18)	5.71(63)(20)
$\eta e^+ \nu_{e,0.5-1.0}$	3.08(71)(13)	0.437(68)(13)	3.99(62)(15)
$\eta e^+ \nu_{e,\geq 1.0}$	1.77(67)(16)	0.223(52)(10)	2.03(47)(10)