

# Multiple Parton Interactions in Sherpa

Multiple parton interactions @ the LHC”  
Tel Aviv October 2012

Frank Krauss    IPPP Durham



[www.ippp.dur.ac.uk](http://www.ippp.dur.ac.uk)



# Khoze-Martin-Ryskin model

- Eikonal as convolution of "two" parton densities"

$$\Omega(\vec{b}_\perp) = \frac{1}{2\beta_0^2} \int d^2b_\perp^{(1)} d^2b_\perp^{(2)} \delta^2(\vec{b}_\perp - \vec{b}_\perp^{(1)} - \vec{b}_\perp^{(2)}) \cdot \Omega_{i(k)}(\vec{b}_\perp^{(1)}, \vec{b}_\perp^{(2)}, y) \Omega_{(i)k}(\vec{b}_\perp^{(1)}, \vec{b}_\perp^{(2)}, y) ;$$

- Two channel eikonal, with two evolution equations

$$\frac{d \ln \Omega_{i(k)}(y)}{dy} = + \exp \left\{ -\frac{\lambda}{2} [\Omega_{i(k)}(y) + \Omega_{(i)k}(y)] \right\} \Delta$$
$$\frac{d \ln \Omega_{(i)k}(y)}{dy} = - \exp \left\{ -\frac{\lambda}{2} [\Omega_{i(k)}(y) + \Omega_{(i)k}(y)] \right\} \Delta$$

# Khoze-Martin-Ryskin model (cont'd)

- Boundary conditions involve form factors

$$\Omega_{i(k)}(\vec{b}_{\perp}^{(1)}, \vec{b}_{\perp}^{(2)}, -Y/2) = F_i(b_{\perp}(1)^2)$$

$$\Omega_{(i)k}(\vec{b}_{\perp}^{(1)}, \vec{b}_{\perp}^{(2)}, +Y/2) = F_k(b_{\perp}(2)^2)$$

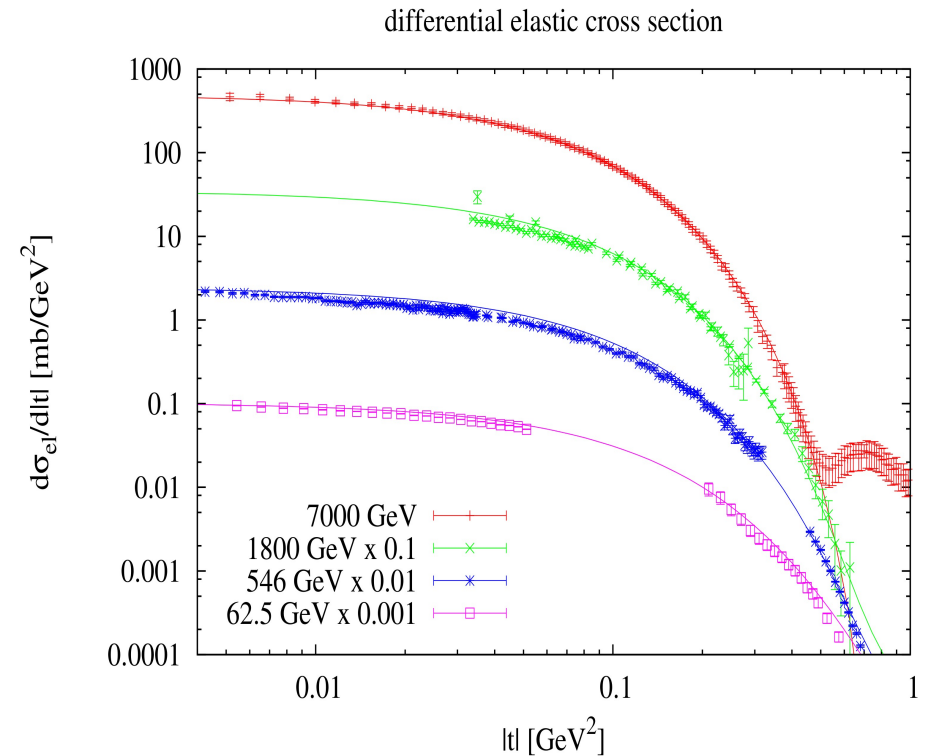
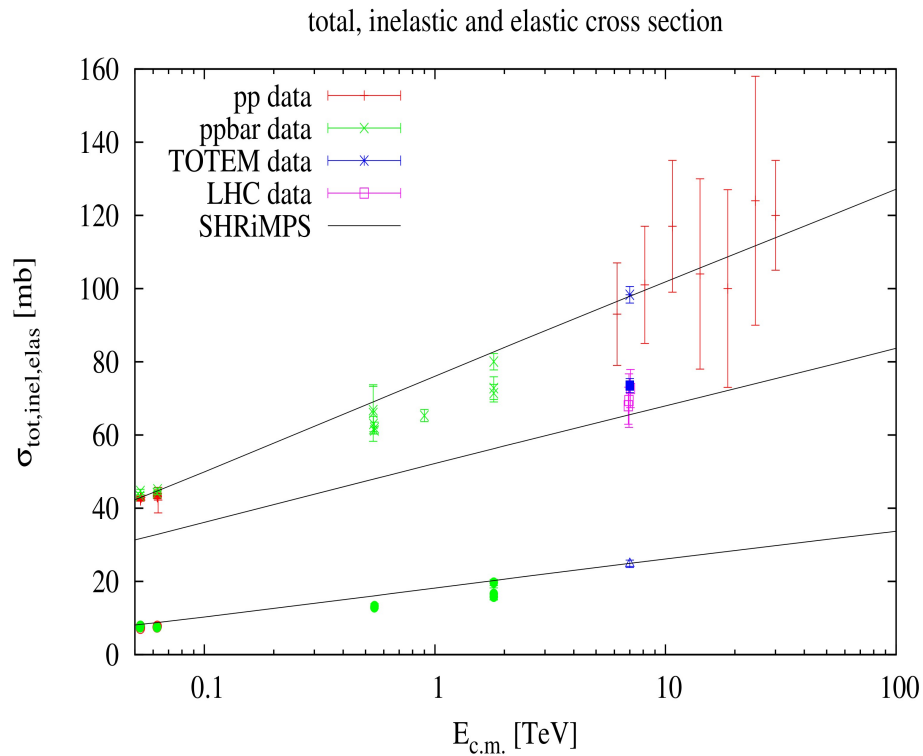
- Form factor as Fourier transforms of (dipole form with extra dampening)

$$F_{1,2}(q_{\perp}) = \beta_0^2(1 \pm \kappa) \frac{\exp\left[-\frac{(1 \pm \kappa)\xi q_{\perp}^2}{\Lambda^2}\right]}{\left[1 + \frac{(1 \pm \kappa)q_{\perp}^2}{\Lambda^2}\right]^2}$$

- Parameters:  $\Delta = 0.3$ ,  $\lambda = 0.25$ ,  $\beta_0^2 = 30 \text{ mb}$ ,  $\kappa = 0.5$ ,  $\Lambda^2 = 1.5 \text{ GeV}^2$ ,  $\xi = 0.225$

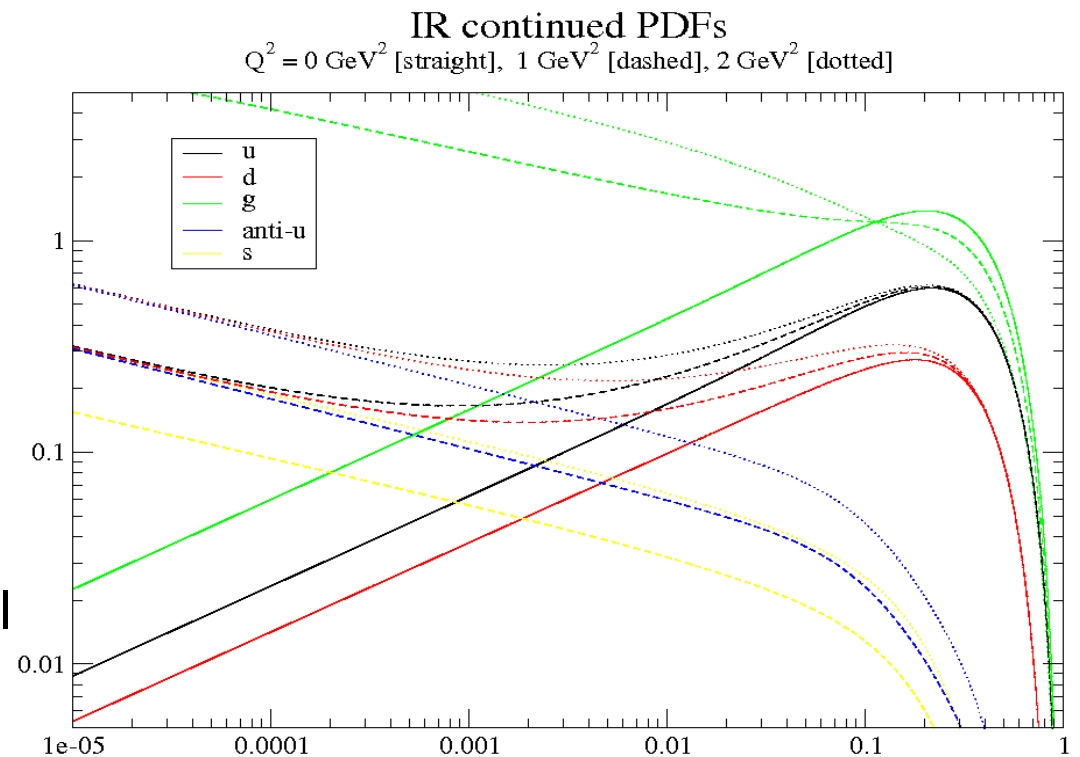
# Inclusive results

- Total and elastic cross sections vs. data at various energies



# Initialising the (primary) ladders

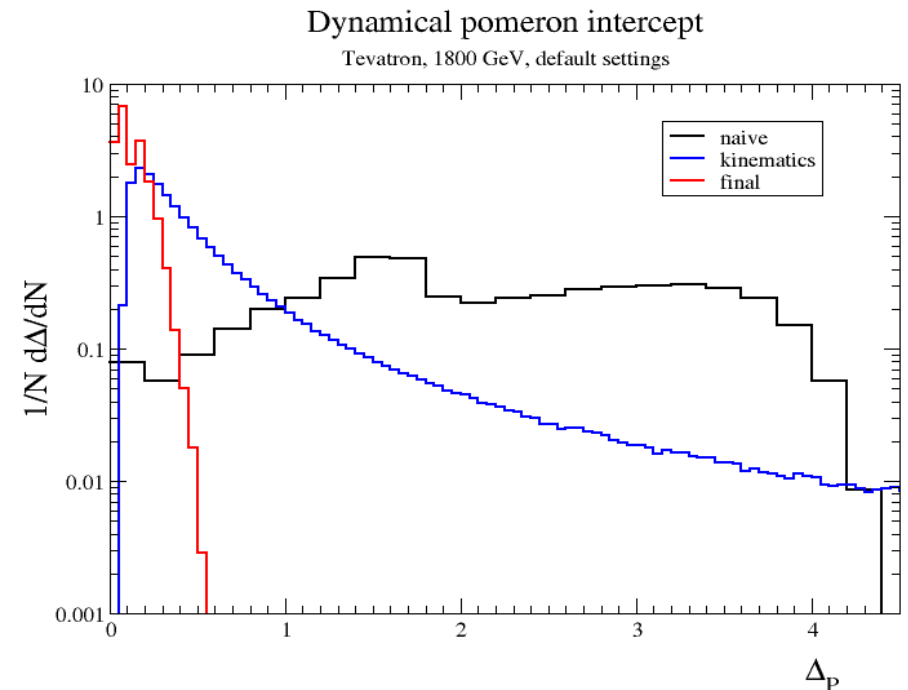
- Select flavours and (collinear) momenta according to IR-continued PDFs and Regge-motivated cross-section  $(s/s_0)^{1+\eta}$ , where
  - $s_0$  is fixed to reproduce inelastic cross section in this channel  $ik$ ,  $s > s_0$
  - Exponent  $\eta = \Delta \exp[-\lambda/2(\Omega_{ik}(b,0) + \Omega_{ki}(b,0))] = \text{“effective intercept”}$
- IR-continued PDFs:
  - assume  $f(x,0) = \text{valence only}$
  - keep norm of valence quarks, renormalise “valence” gluons to satisfy momentum sum rule
  - switch off sea with  $Q$
- Produce  $N_{\text{ladders}}$  pairs of incoming partons (one valence quark, rest will be gluons)
- Weight for each pair given by Regge expression times the PDFs



# Filling the ladders

- Generate emissions in between, according to “Sudakov form factor”

$$\begin{aligned}
 S(y_0, y_1) = \exp & \left\{ - \int_{y_0}^{y_1} dy \int dk_{\perp}^2 \frac{\alpha_s(k_{\perp}^2 + K_0^2)}{(k_{\perp}^2 + K_0^2)} \right. \\
 & \times \left[ \frac{K_0^2}{q^2 + K_0^2} \right]^{\frac{3\alpha_s(q^2 + K_0^2)}{\pi} |y - y_0|} \\
 & \left. \times \exp \left[ - \frac{\lambda}{2} \left( \Omega_{i(k)}(y) + \Omega_{(i)k}(y) \right) \right] \right\}
 \end{aligned}$$



- dynamical pomeron intercept
- Reweight ladder with ME for hardest emission
- Note: At this point strictly t-channel, filling stops when either no more  $y$  can be “squeezed” in, or when “active”  $y$ -interval goes to singlet colour config.

# Rescattering

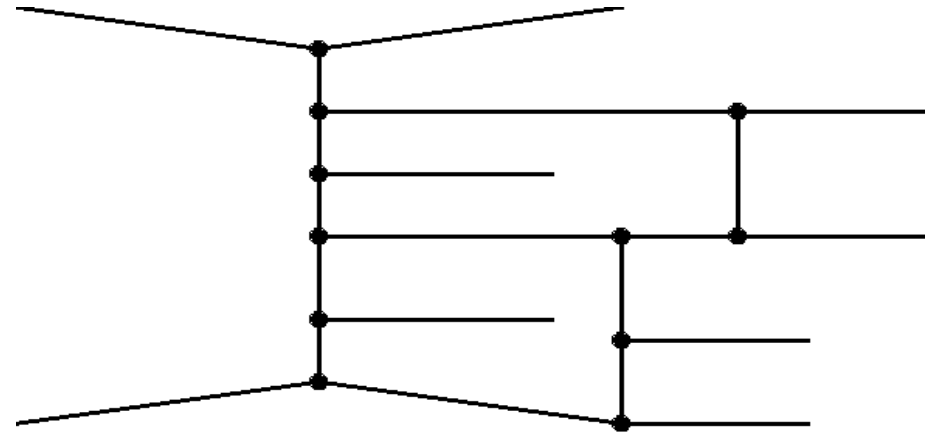
- Consider configurations like
- Partons from ladder may rescatter
- Additional feature (not shown):

FS parton shower attached to ladders ...

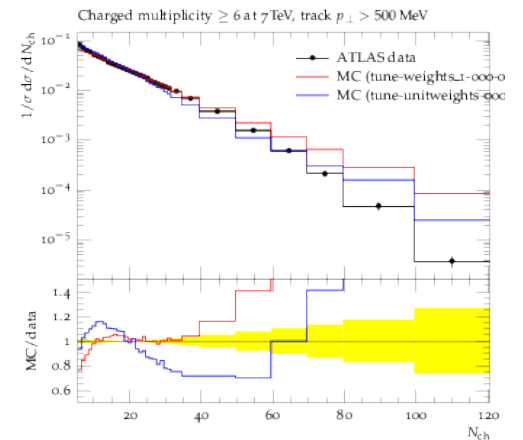
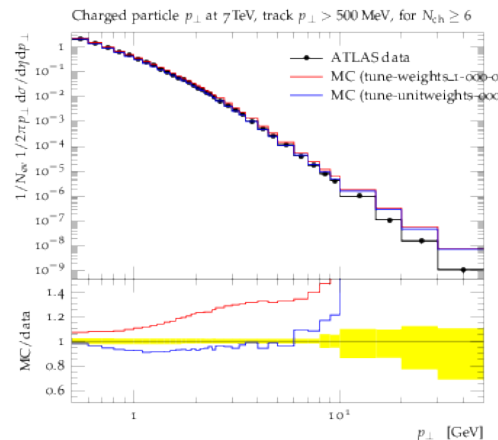
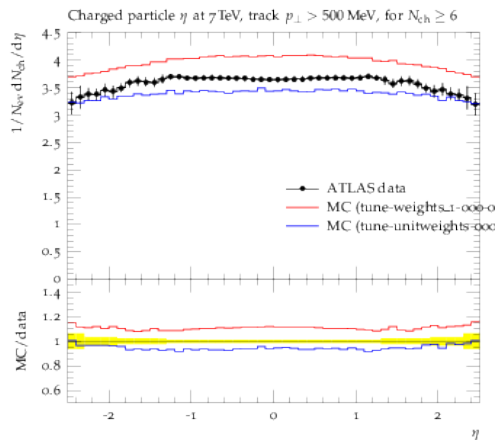
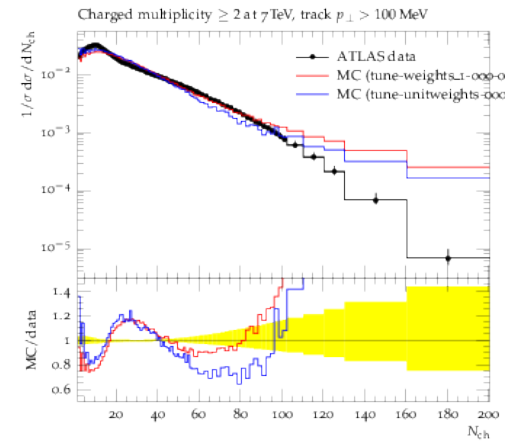
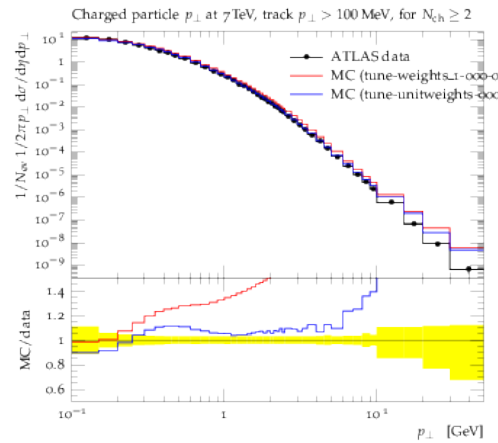
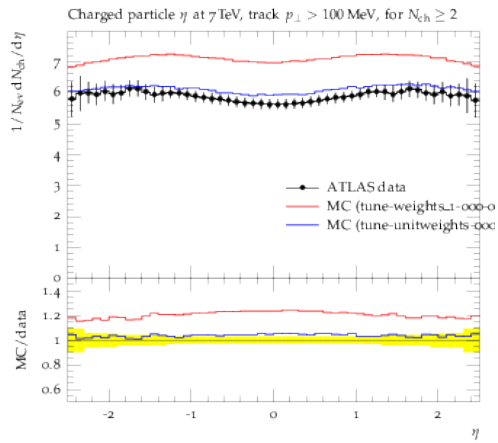
- Question: How to decide if rescattering or not?
- Answer: Same as before
  - Iterate over all pairs of partons at some place in transverse plane
  - Construct rescattering probability for each pair as

$$P_{\text{rescatter}} = 1 - \exp\{-\lambda/2 [\Omega(y_1) - \Omega(y_2)] / (\Omega(y_1))\}$$

- Check each pair (compare with random number)
- Open question: Is this consistent with AGK cutting rules? (Ryskin says yes)

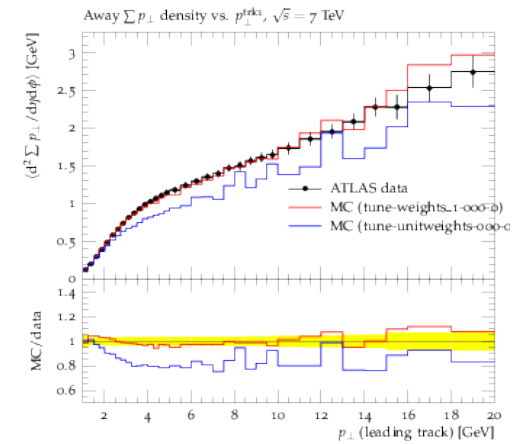
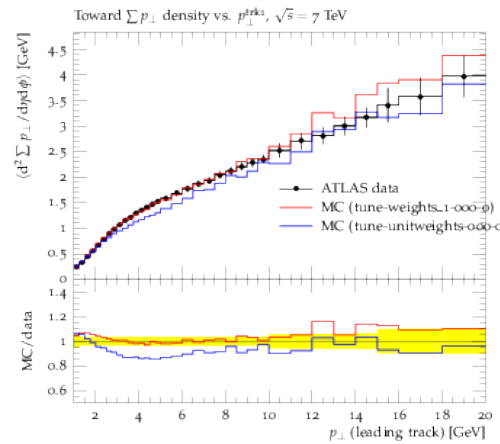
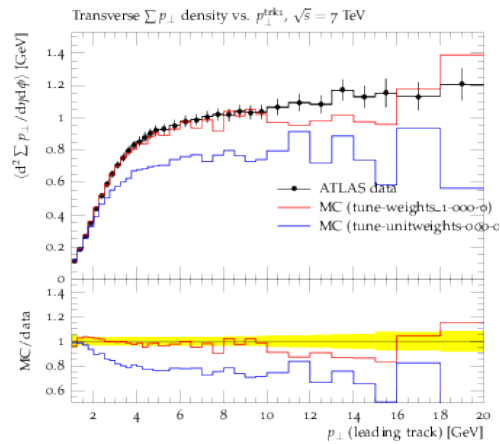
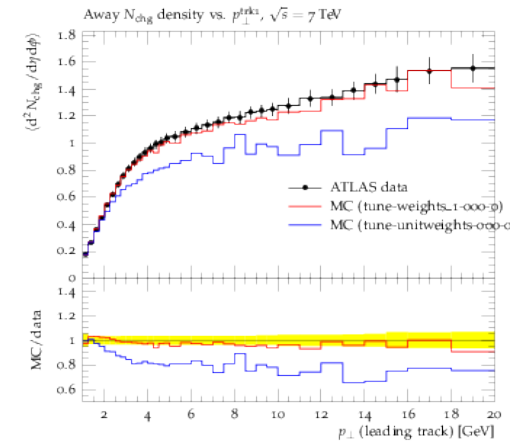
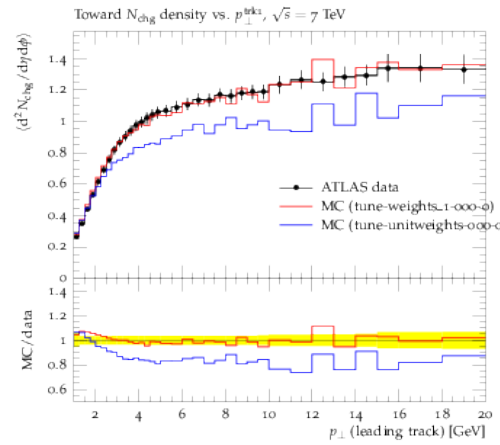
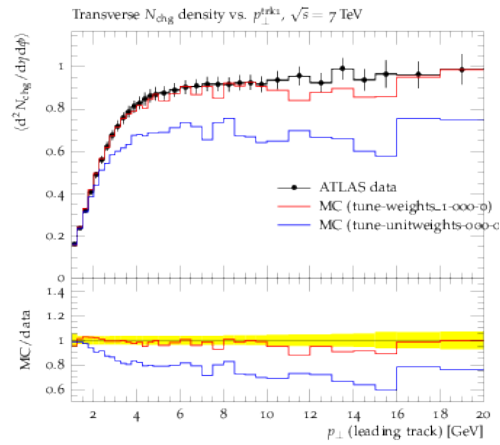


# Some example results

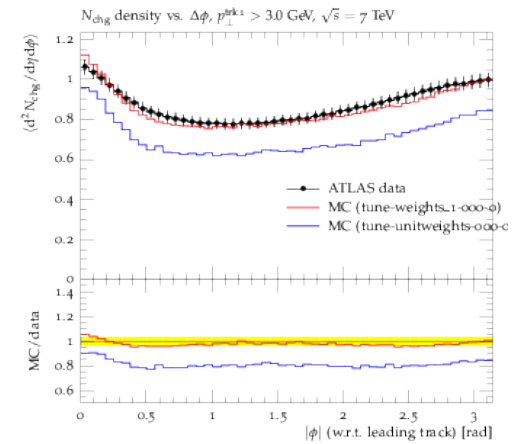
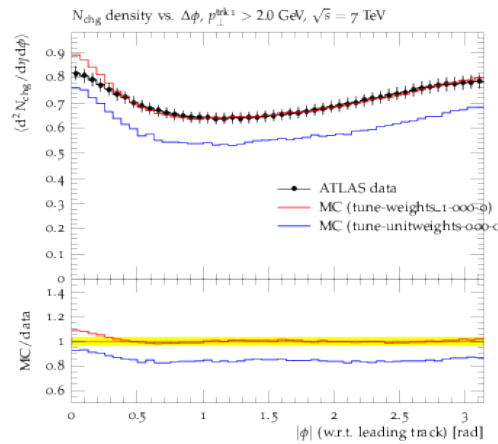
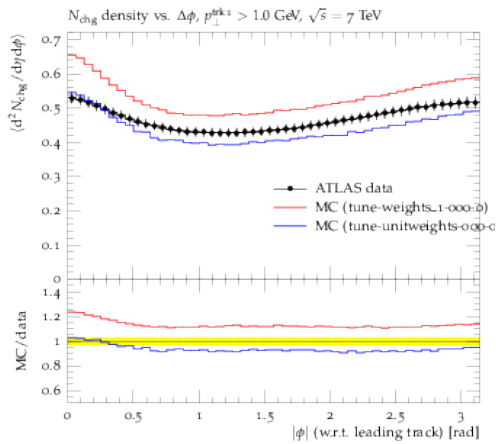
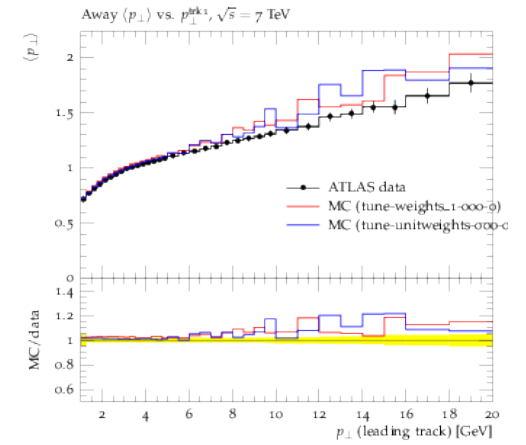
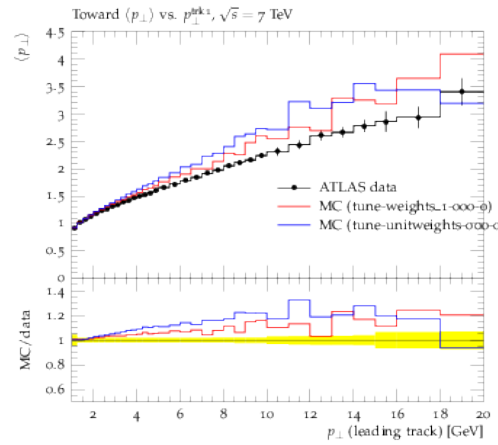
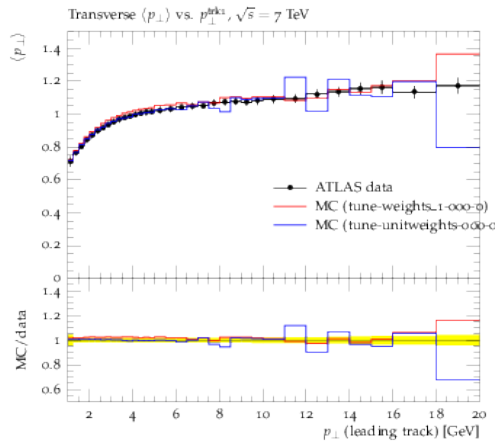




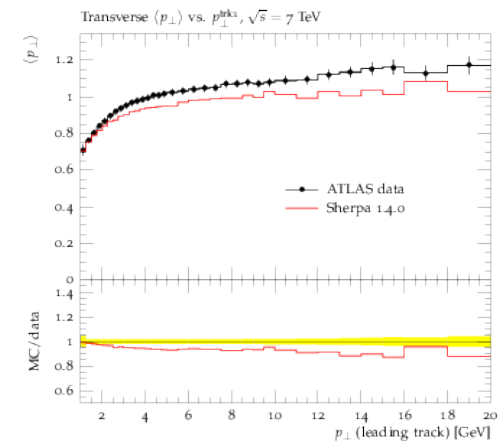
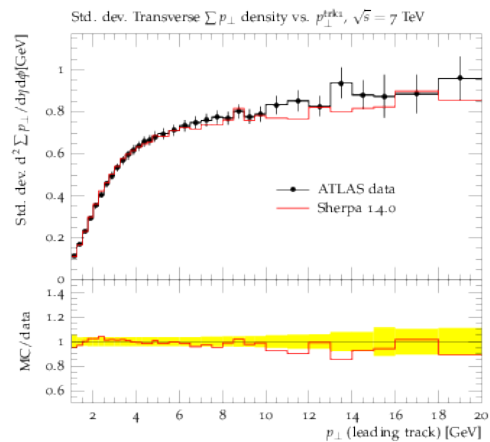
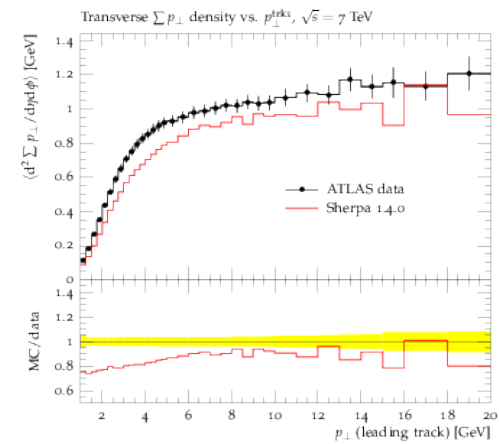
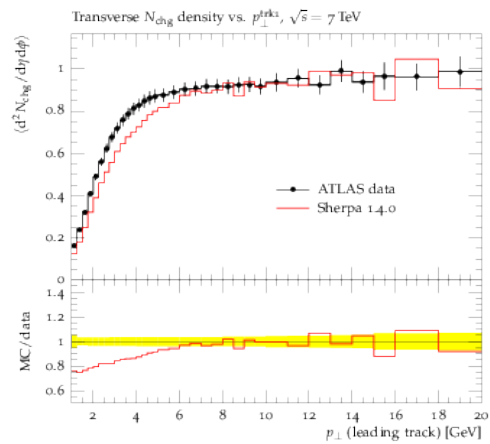
# Some example results



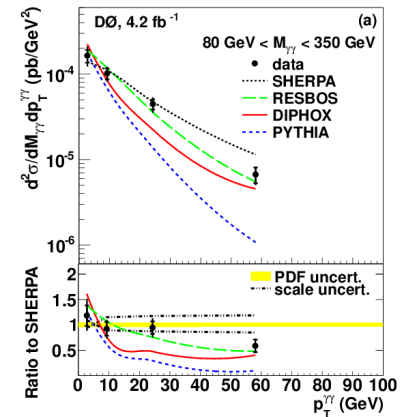
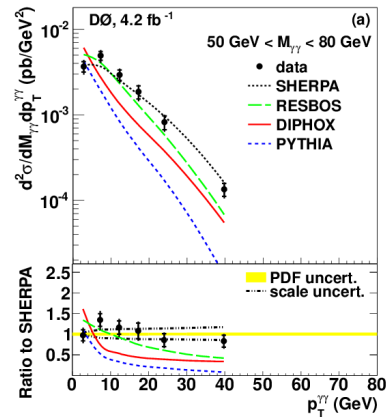
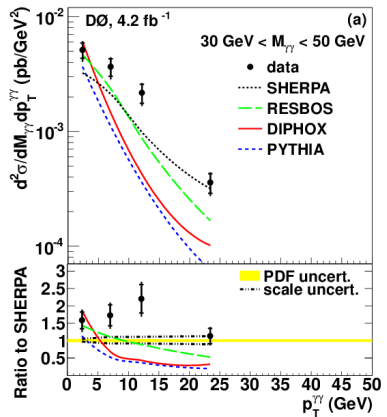
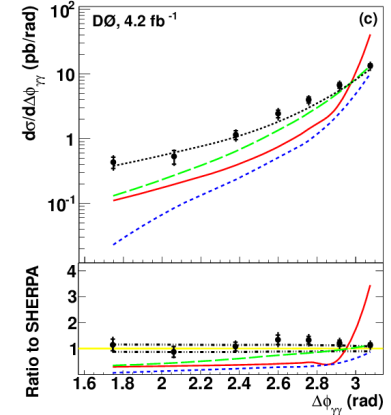
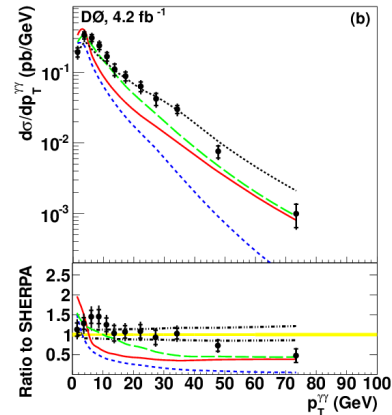
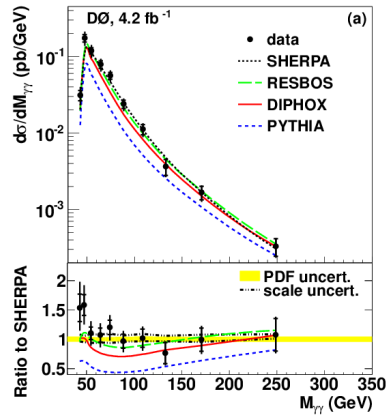
# Some example results



# Sherpa's standard UE model



# Sherpa's standard UE model



# Summary

- In SHERPA's standard MPI/UE model: Include photons, etc.. This will happen in release Sherpa2.0, due end of November (together with many other features, mainly NLO)
- Also: A new model for soft interactions (SHRiMPS), together with Hendrik Hoeth, Valery Khoze, Alan Martin, Misha Ryskin, and Korinna Zapp.
- At the moment we iron out a few more features that we didn't like so much, will need retuning.
- Once done, we'll promote the soft model to a full UE model.