

STUDIES OF MULTI-PARTON INTERACTIONS AT DØ

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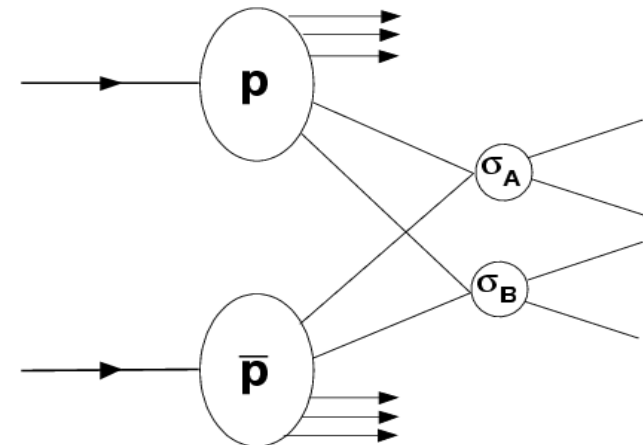
Florida State University

MPI at TAU

October 16, 2012, Tel Aviv University

Outline

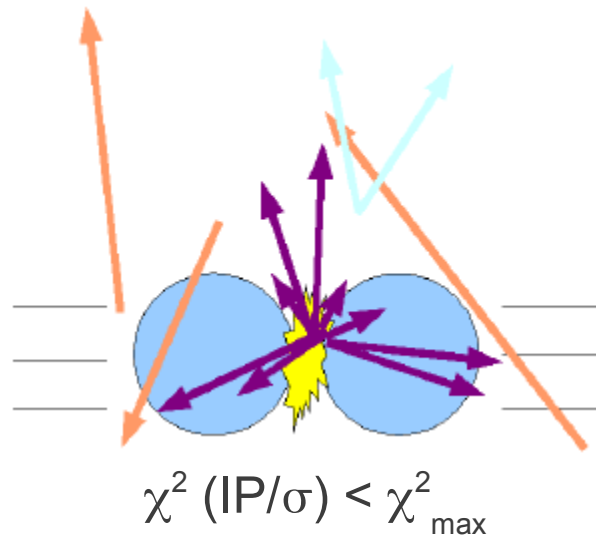
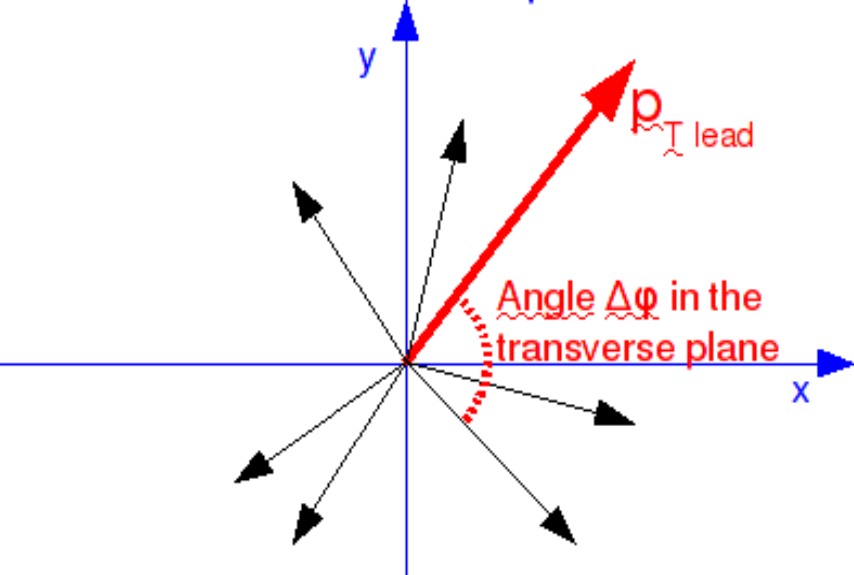
- Study of Underlying Events with low p_T tracks
- Study of Multiple Parton Interactions using photon+n-jet events
 - Fraction of the events with Double Parton interactions
 - Effective cross-section measurement
 - Comparison/tuning to MPI models
- Summary



Track angular correlations in minbias events

- Use correlations in $\Delta\phi$ to characterize Minimum Bias Events
- Compare data to various Monte Carlo tunes and models

Detector transverse plane



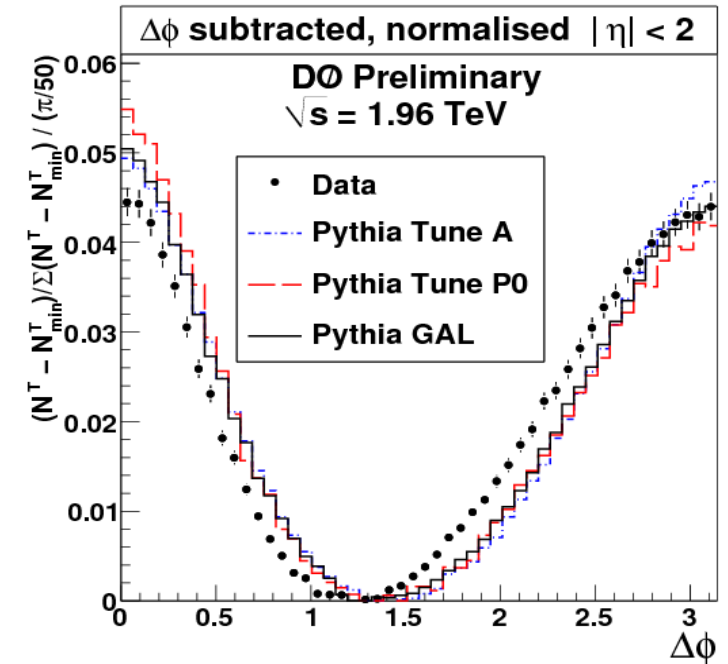
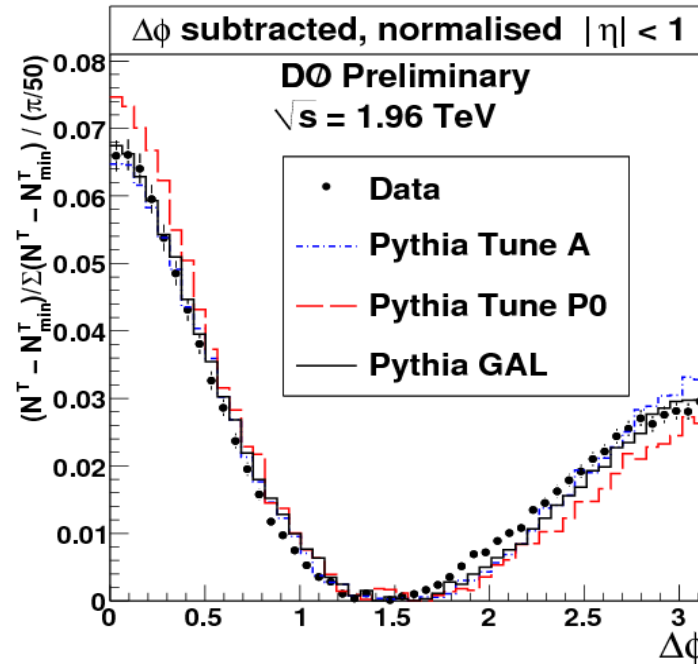
Strategy: Associate all tracks to PVs and then select good quality tracks associated to minbias PVs. Minimize fakes, cosmics, conversions, long-lived resonances, vertex mis-associations

- Trigger on dimuon events
- Require exactly 2 muons w/ $p_T > 2$ GeV associated with the main primary vertex (PV) (not considered in the analysis)
- Then require one or more Minimum Bias PVs
 - At least 5 tracks
 - At least 0.5cm from triggered PV
 - Within 20cm of center of detector
 - $p_T > 0.5$ GeV, $|\eta| < 2$
- Choose track with max p_T for each MB PV as a reference point

Comparison to MPI models

$$(N^T - N_{\min}^T) / \sum_{\phi} (N^T - N_{\min}^T)$$

N^T – total number of tracks in a bin
 N_{\min}^T – combinatorial background

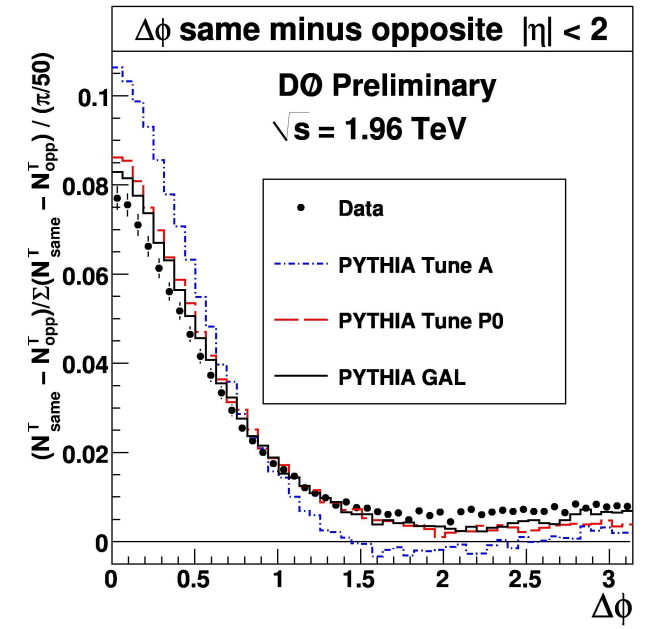
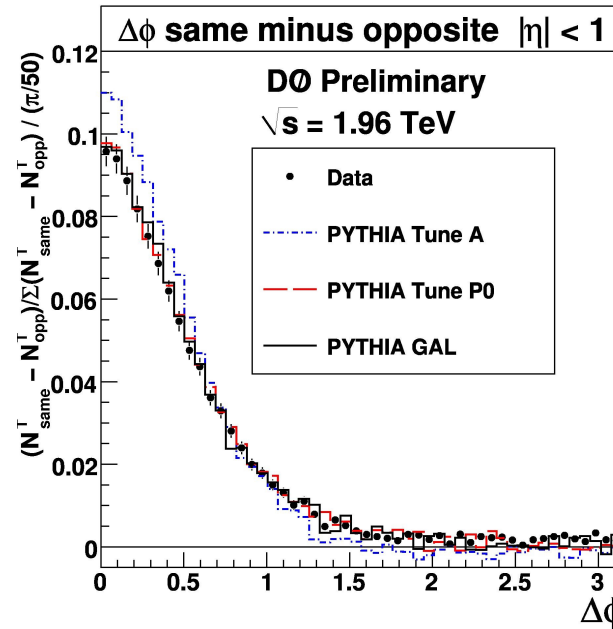
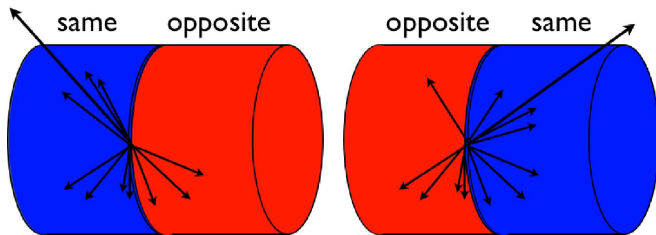


- Combinatorial (flat) background is subtracted
- Due to subtraction and normalization, dependence on tracking efficiency, background becomes negligible.
- Almost same distribution at reconstruction (detector) and particle level
 => very small acceptance corrections
- The peak at π (recoil) is softer by construction and wider to keep p_T balance
- The height of peaks depend on track rapidity: only a fraction of the recoil tracks are in the same $|\eta|$ range. When the η range is extended, more tracks from the recoil side are included in the measurement, enhancing the peak at π .

Comparison to MPI models

$$(N_{\text{same}}^T - N_{\text{opp}}^T) / \sum_{\phi} (N_{\text{same}}^T - N_{\text{opp}}^T)$$

$N_{\text{same (opp)}}^T$ – total number of tracks with same (opposite) η sign as the leading track



- Study of correlations in rapidity in addition to the azimuthal angle
- Distribution has a rather broad and high same side peak, and a flatter tail closer to π with $N_{\text{same}}^T \approx N_{\text{opp}}^T$
- After subtraction, peak is lower with $|\eta| < 2$

Double Parton Interactions
in $\gamma+3$ (and 2) jet events:
from low p_T to high p_T in MPI studies

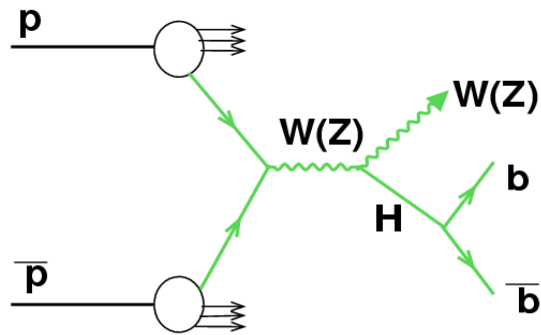
- New motivations and prospects
- New effects

Motivations

- Most of the processes that cause MPI production are non-perturbative and implemented in some phenomenological models of a hadron structure and parton-to-hadron fragmentation.
=> Being phenomenological, the models strongly need experimental inputs.
- The provided experimental inputs have been based so far mainly on the minbias Tevatron (0.63, 1.8, 1.96 TeV), SPS (0.2, 0.54, 0.9 TeV), Tevatron DY and similar LHC data.
- However, there is a quite small amount of tests of MPI events in high p_T regime, specifically with events having jet $p_T > 15$ GeV,
=> i.e. right in the region used in many measurements (e.g. top-quark mass) and most important for searches of rare processes, especially with multi-jet final state.
=> MPI events can mimic a signature of a new physics processes and thus be a significant background to them.
=> in the energy regime of pQCD

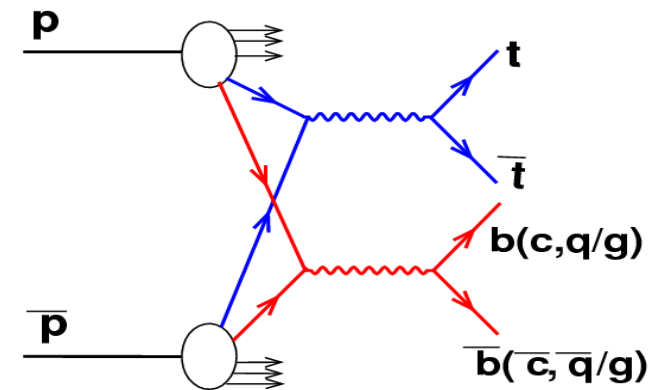
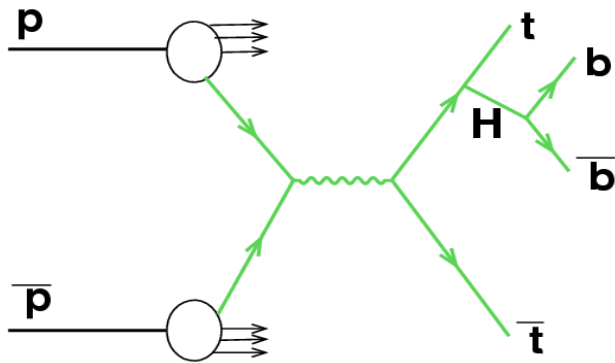
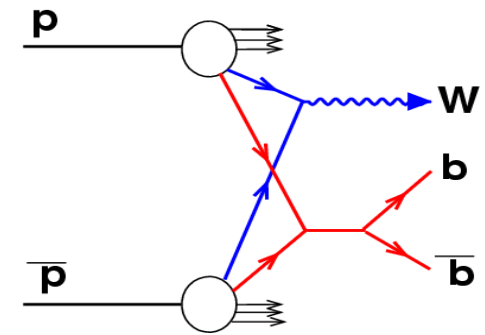
Double Parton events as a background to Higgs production

Signal



$$\sigma_{DP} = \frac{\sigma_A \sigma_B}{\sigma_{eff}}$$

Double Parton background

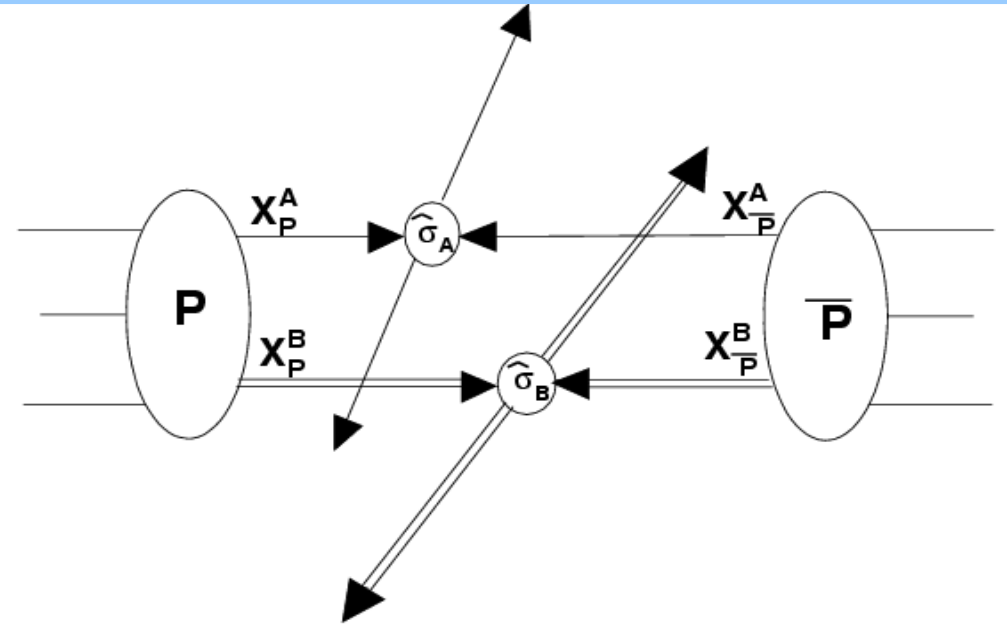


Estimates for Tevatron [JHEP 1104:054\(2011\)](#), LHC [PRD61,077502\(2000\)](#), [PRD81,014014\(2010\)](#)

- Many Higgs production channels can be mimicked by Double Parton events!
- Some of them can be significant even after signal selections.
- Dedicated cuts are required to increase sensitivity to the Higgs signal (same is true for many other rare processes)!

Double parton and effective cross sections

$$\sigma_{DP} = \frac{\sigma_A \sigma_B}{\sigma_{eff}}$$



σ_{DP} - double parton cross section for processes A and B

σ_{eff} - factor characterizing a size of effective interaction region

→ can be directly related to the spatial distribution of partons $f(b)$.

Uniform: σ_{eff} is large and σ_{DP} is small

Clumpy: σ_{eff} is small and σ_{DP} is large

⇒ Having σ_{eff} measured we can estimate $f(b)$

→ Should be measured in experiment !!

Just 4 measurements existed up to recent time : AFS, UA2, 2 CDF [Run 1]

History of the measurements

Experiment	\sqrt{s} (GeV)	Final state	p_T^{min} (GeV)	η range	σ_{eff}
AFS (pp), 1986	63	4 jets	$p_T^{jet} > 4$	$ \eta^{jet} < 1$	~ 5 mb
UA2 ($p\bar{p}$), 1991	630	4 jets	$p_T^{jet} > 15$	$ \eta^{jet} < 2$	> 8.3 mb (95% C.L.)
CDF ($p\bar{p}$), 1993	1800	4 jets	$p_T^{jet} > 25$	$ \eta^{jet} < 3.5$	$12.1^{+10.7}_{-5.4}$ mb
CDF ($p\bar{p}$), 1997	1800	$\gamma + 3$ jets	$p_T^{jet} > 6$ $p_T^\gamma > 16$	$ \eta^{jet} < 3.5$ $ \eta^\gamma < 0.9$	$14.5 \pm 1.7^{+1.7}_{-2.3}$ mb
DØ ($p\bar{p}$), 2010	1960	$\gamma + 3$ jets	$60 < p_T^\gamma < 80$ $15 < p_T^{jet2} < 30$	$ \eta^\gamma < 1.0$ $1.5 < \eta^\gamma < 2.5$ $ \eta^{jet} < 3.0$	$\sigma_{eff} = 16.4 \pm 0.3(\text{stat}) \pm 2.3(\text{syst})$ mb

AFS'86, UA2'91 and CDF'93

4-jet samples, motivated by a large dijet cross section (but low DP fractions)

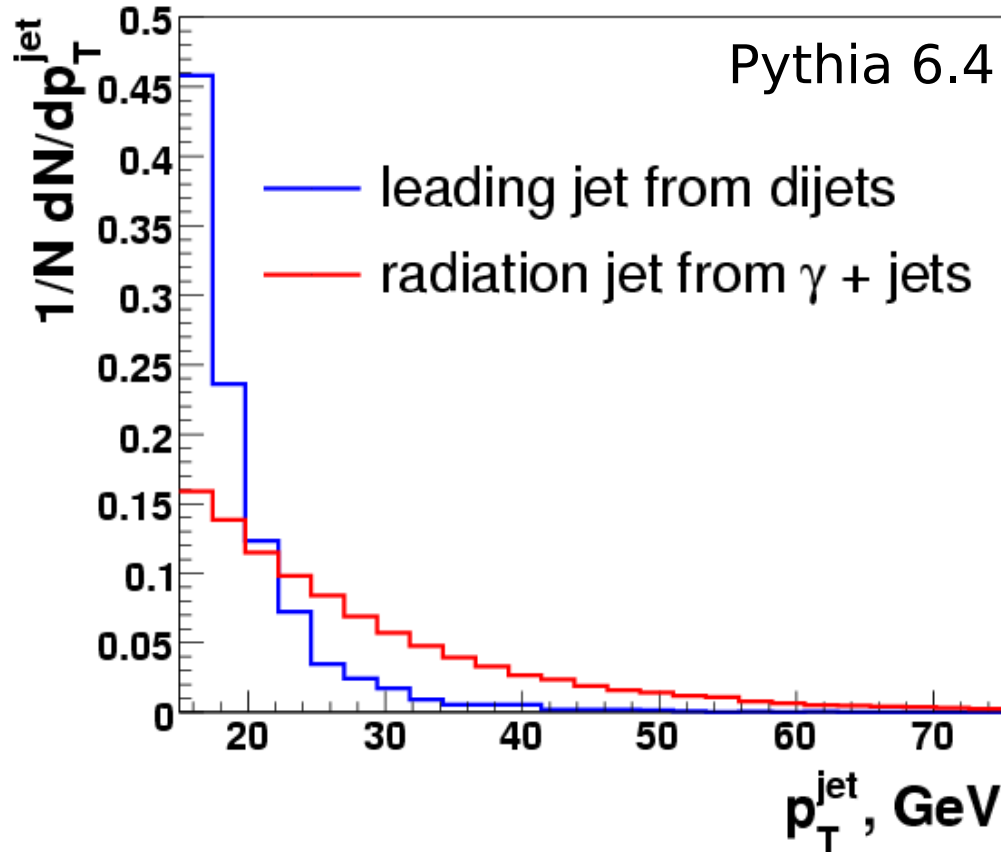
CDF'97, D0'10

$\gamma + 3$ jets events, **data-driven method**: use rates of Double Interaction events (two separate $p\bar{p}$ collisions) and Double Parton (single $p\bar{p}$ collision) events to extract σ_{eff} from their ratio.

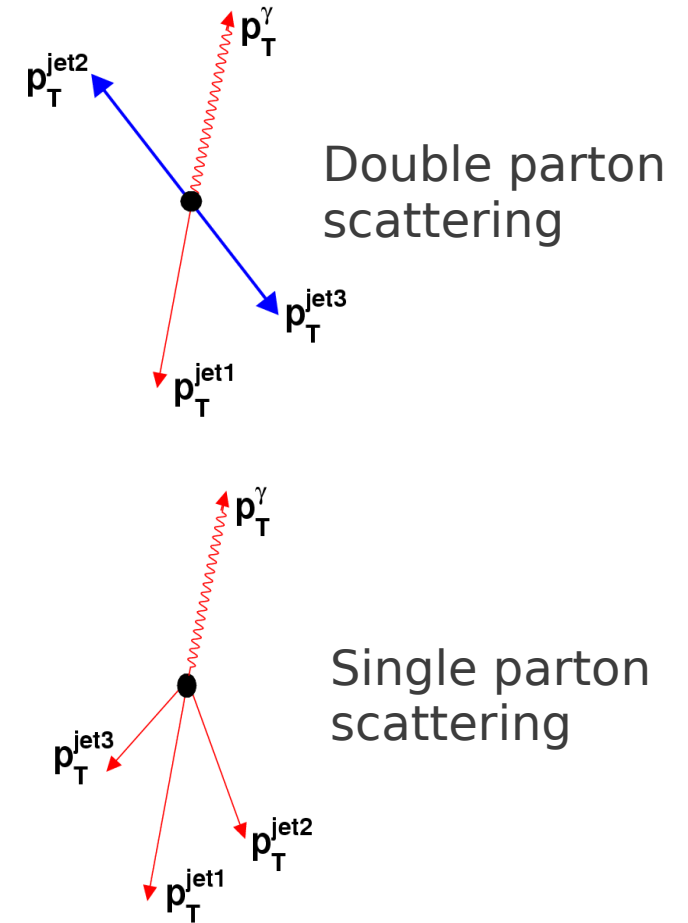
=> reduces dependence on Monte-Carlo and NLO QCD theory predictions.

Motivation for jet pT binning

Jet pT: jet from **dijets** vs. **radiation** jet from γ +jet events



$$\sim 1/p_T^4$$
$$\sim 1/p_T^2$$

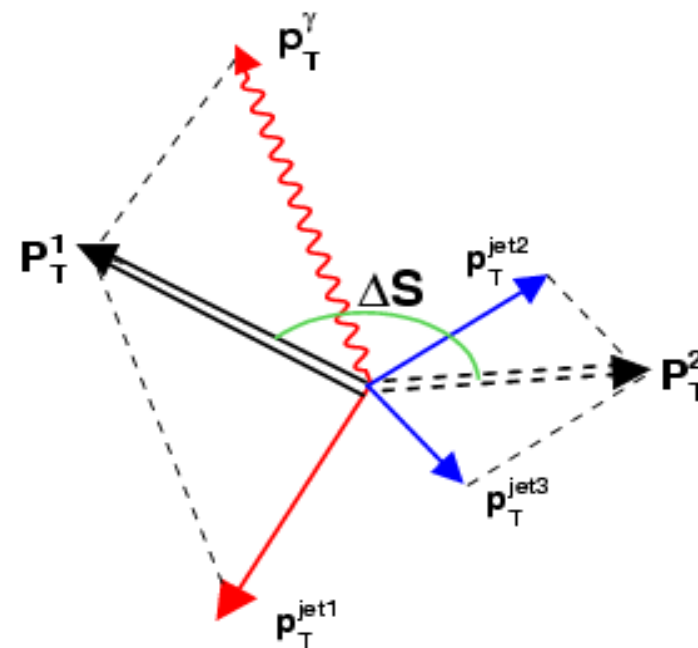
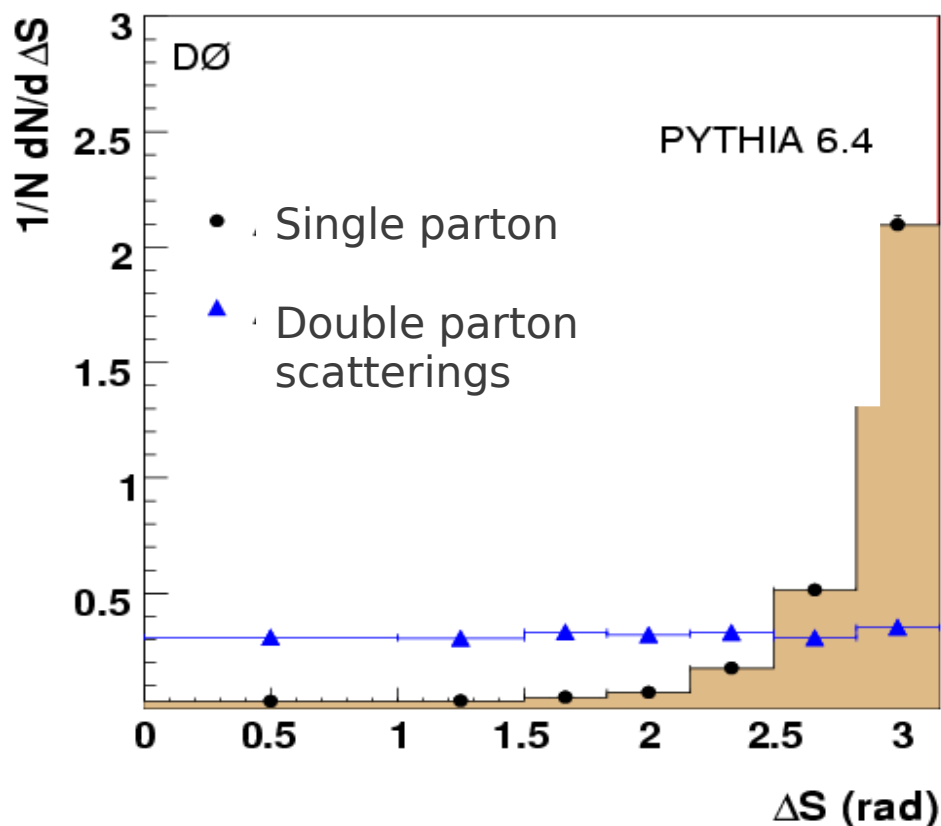


- ▶ Jet pT from dijets falls much faster than that for a radiation jet, i.e. Fraction of dijet (Double Parton) events should drop with increasing jet pT
=> Measurement is done in three bins of 2nd jet pT: 15-20, 20-25, 25-30 GeV

Discriminating variables

- ▶ Main one is $\Delta\phi$ angle between two best pT-balancing pairs

$$\Delta S = \Delta\phi(p_T^{\gamma, \text{jet}}, p_T^{\text{jet}_i, \text{jet}_k})$$



For “ $\gamma+3$ -jet” events from Single Parton scattering we expect ΔS to peak at π , while it should be flat for “ideal” Double Parton interaction (2nd and 3rd jets are both from dijet production) due to a pairwise pT balance.

Double Parton interaction model

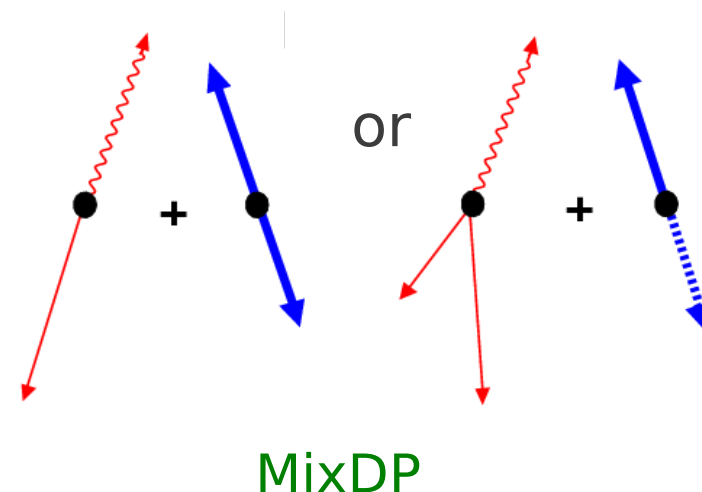
Built from D0 data. Samples:

A: photon + ≥ 1 jet from γ +jets data events:

- 1 VTX events
- photon p_T : 60-80 GeV
- leading jet $p_T > 25$ GeV, $|\eta| < 3.0$.

B: ≥ 1 jets from MinBias events:

- 1 VTX events
- jets with p_T 's recalculated to the primary vertex of sample A have $p_T > 15$ GeV and $|\eta| < 3.0$.



- ▶ **A** & **B** samples have been (randomly) mixed with jets p_T re-ordering
- ▶ Events should satisfy photon + ≥ 3 jets requirement.
- ▶ $\Delta R(\text{photon}, \text{jet1}, \text{jet2}, \text{jet3}) > 0.7$

⇒ Two scatterings are independent by construction !

The fraction of DP events: the two datasets method

Since dijet pT cross section drops faster than that of radiation jets the different DP fractions in various (2nd) jet pT intervals are expected. The larger 2nd jet pT the smaller DP fraction.

Dataset 1 - "DP-rich", smaller 2nd jet pT bin, e.g. 15-20 GeV

Dataset 2 - "DP-poor", larger 2nd jet pT bin, e.g. 20-25 GeV

Each distribution can be expressed as a sum of DP and SP :

$$D_1 = f_1 M_1 + (1 - f_1) B_1$$

$$D_2 = f_2 M_2 + (1 - f_2) B_2$$

$$D_1 - f_1 M_1 = (1 - f_1) B_1$$

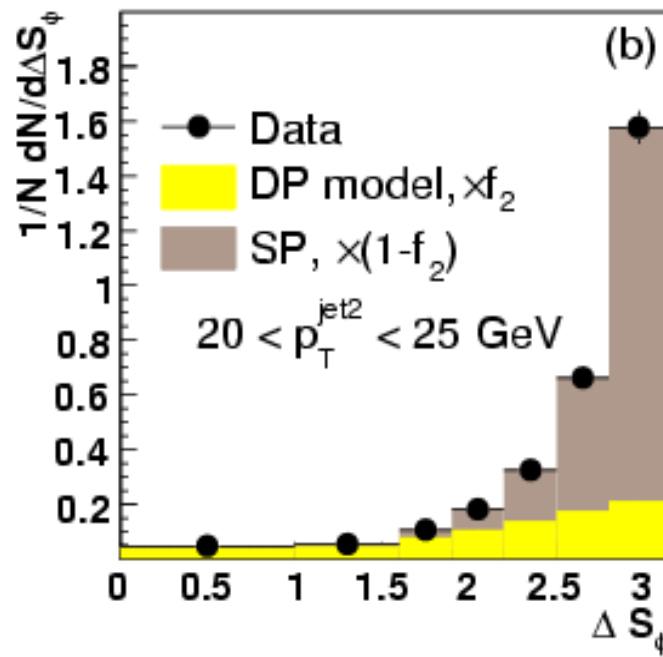
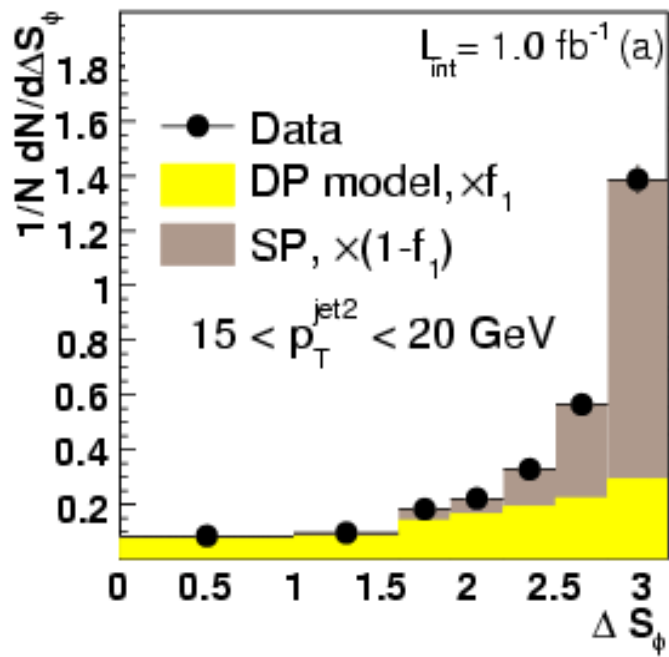
$$D_2 - f_2 M_2 = (1 - f_2) B_2$$

- D_i - data distribution
- M_i - MIXDP distribution
- B_i - background distribution
- f_i - fraction of DP events
- $(1 - f_i)$ - fraction of SP events

$$D_1 - \lambda K D_2 = f_1 M_1 - \lambda K C f_1 M_2 \quad \text{where} \quad \lambda = \frac{B_1}{B_2} \quad K = \frac{(1 - f_1)}{(1 - f_2)} \quad C = \frac{f_2}{f_1}$$

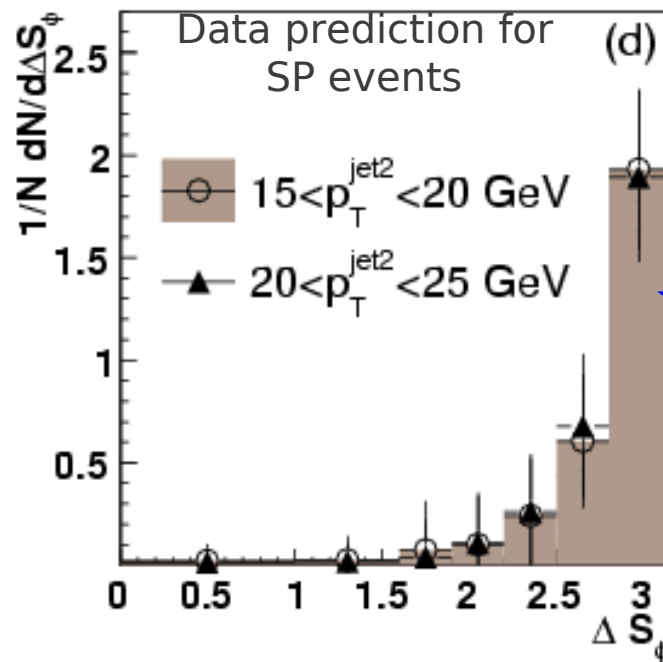
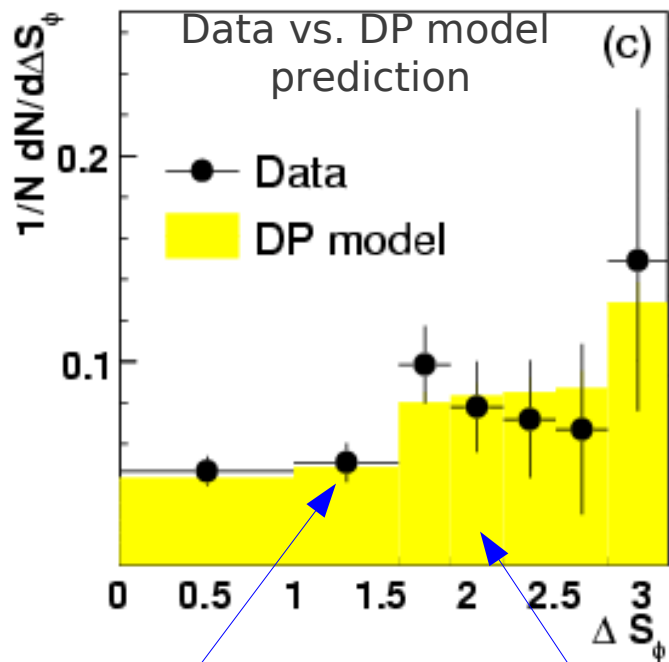
f₁ is the only unknown --> get from minimization

The two datasets method



Dataset 1: 2nd jet pT: 15-20 GeV
 Dataset 2: 2nd jet pT: 20-25 GeV

✓ Fraction of Double Parton in bin 15-20 GeV (f_1) is the only unknown
 → get from minimization.

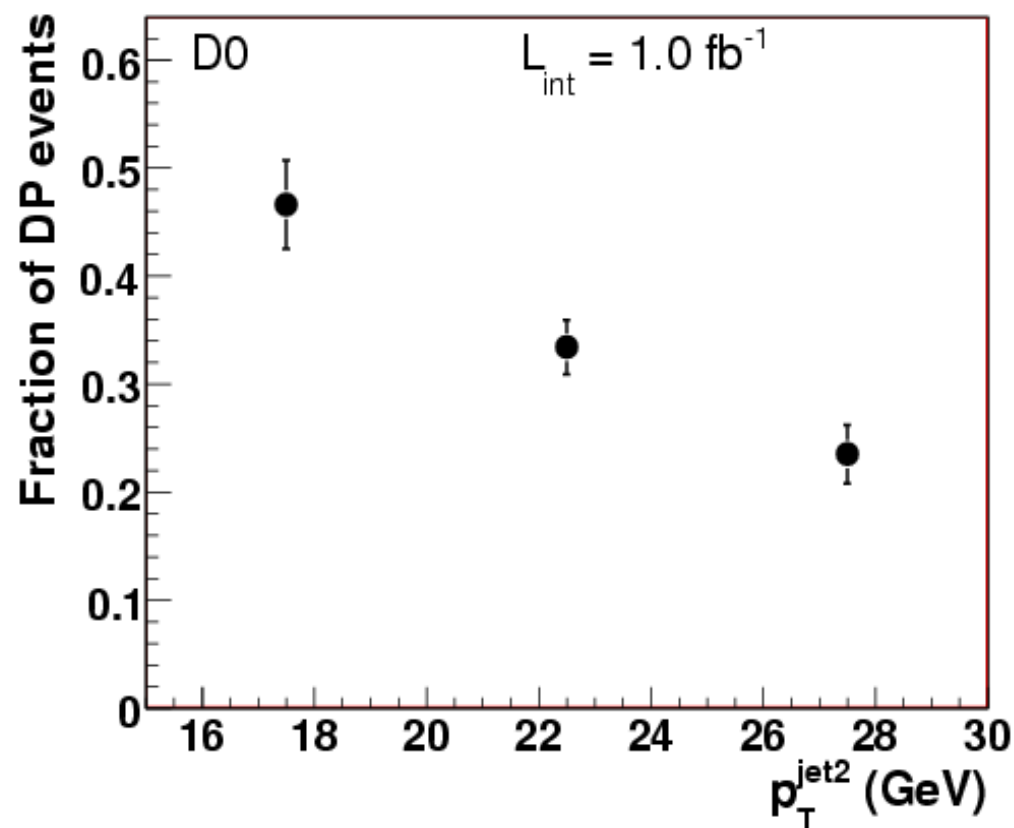


Good agreement of the ΔS Single Parton distribution extracted in data and in MC (see previous slide)
 → another confirmation for the found DP fractions.

Data are corrected for the DP fractions

Good agreement of Data and DP model

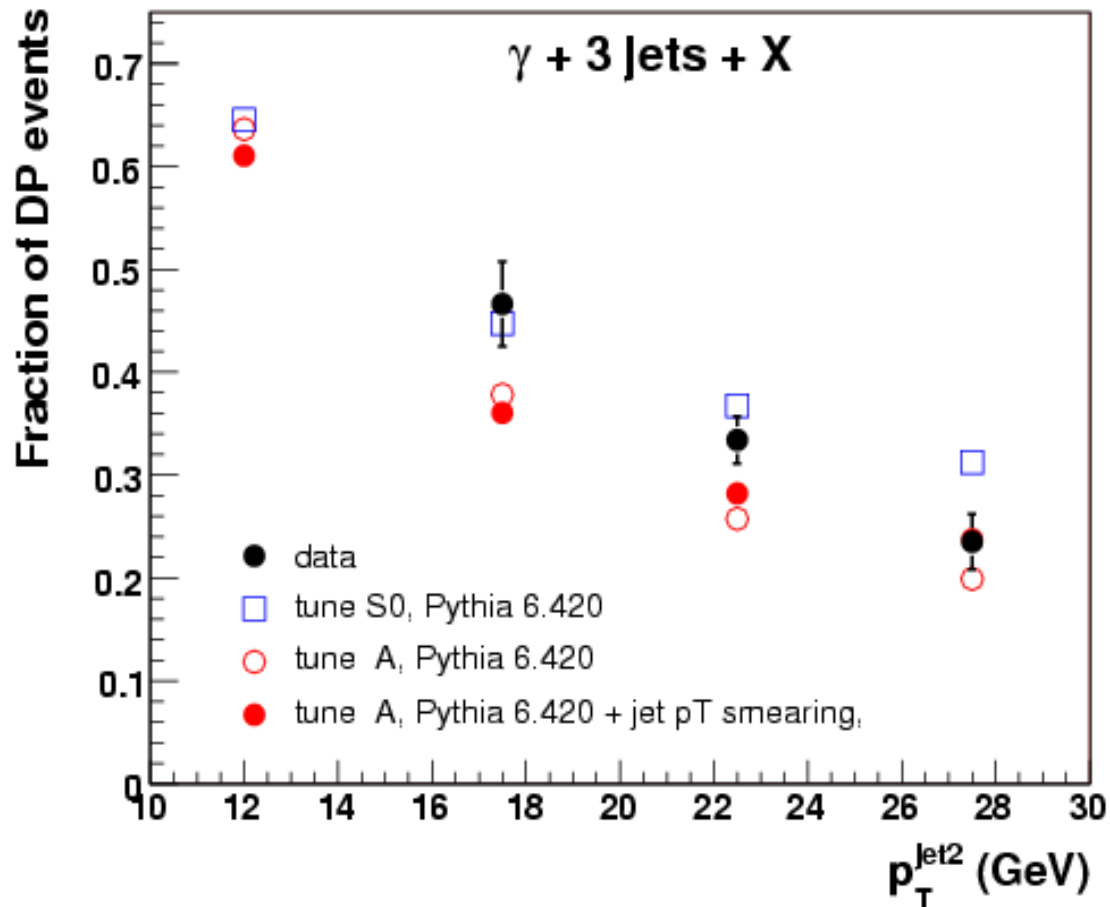
Fractions of Double Parton $\gamma+3$ -jet events



Found DP fractions are pretty sizable: they drop from $\sim 46\text{-}48\%$ at 2^{nd} jet p_T 15-20 GeV to $\sim 22\text{-}23\%$ at 2^{nd} jet 25-30 GeV with relative uncertainties $\sim 7\text{-}12\%$.

CDF Run I: $53 \pm 3\%$ at 5-7 GeV of uncorr. jet p_T .

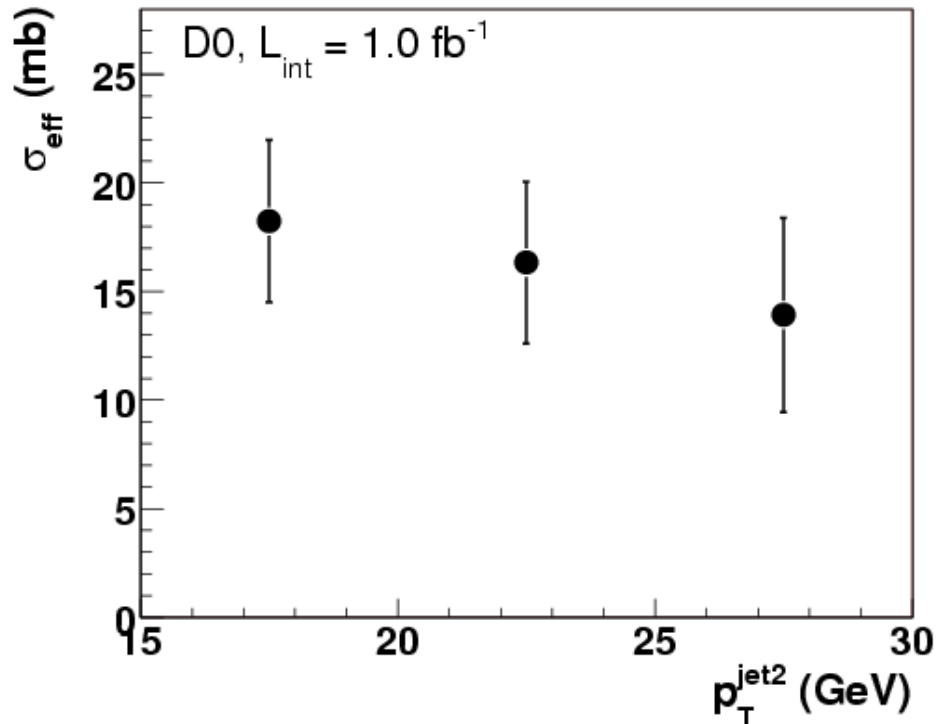
Fractions of Double Parton events : MPI models and D0 data



- Pythia MPI tunes A and S0 are considered.
- Data are in between the model predictions.

Calculation of σ_{eff}

Phys.Rev.D81,052012(2010)



- σ_{eff} values in different jet p_T bins agree with each other within their uncertainties (also compatible with a slow decrease with p_T).
- Uncertainties have very small correlations between 2nd jet p_T bins.
- One can calculate the averaged (weighted by uncertainties) values over the p_T bins:

$$\sigma_{\text{eff}}^{\text{ave}} = 16.4 \pm 0.3(\text{stat}) \pm 2.3(\text{syst}) \text{ mb}$$

CDF Run I: $14.5 \pm 1.7_{-2.3}^{+1.7} \text{ mb}$

Main systematic and statistical uncertainties (in %) for σ_{eff} .

$p_T^{\text{jet}2}$ (GeV)	Systematic uncertainty sources					δ_{syst} (%)	δ_{stat} (%)	δ_{total} (%)
	f_{DP}	f_{DI}	$\epsilon_{\text{DP}}/\epsilon_{\text{DI}}$	JES	$R_c\sigma_{\text{hard}}$			
15 - 20	7.9	17.1	5.6	5.5	2.0	20.5	3.1	20.7
20 - 25	6.0	20.9	6.2	2.0	2.0	22.8	2.5	22.9
25 - 30	10.9	29.4	6.5	3.0	2.0	32.2	2.7	32.3

Models of parton spatial density and σ_{eff}

- σ_{eff} is directly related with parameters of models of parton spatial density
- Three models have been considered: Solid sphere, Gaussian and Exponential.

TABLE VI: Parameters of parton spatial density models calculated from measured σ_{eff} .

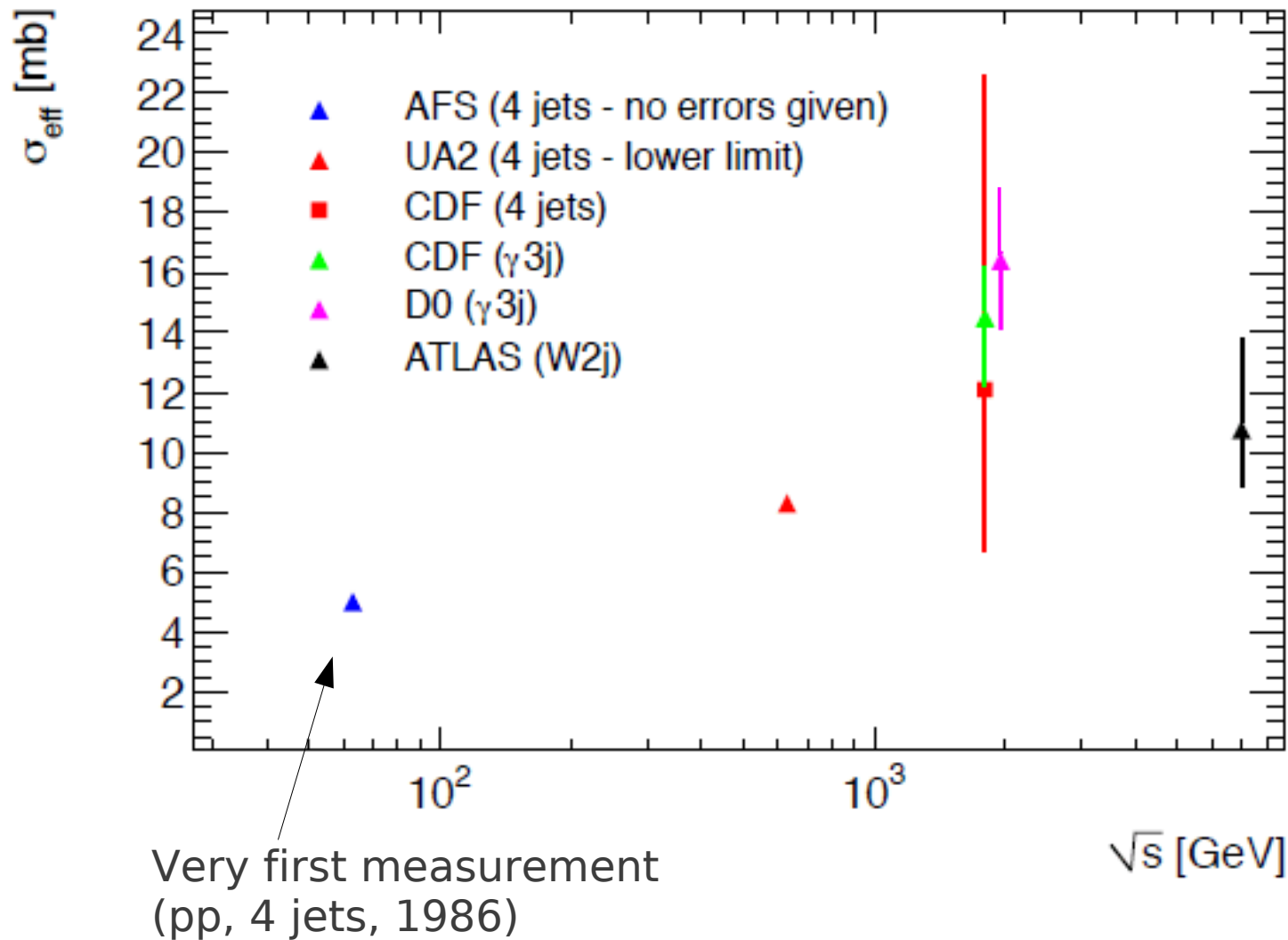
Model for density	$\rho(r)$	σ_{eff}	R_{rms}	Parameter (fm)	R_{rms} (fm)
Solid Sphere	Constant, $r < r_p$	$4\pi r_p^2/2.2$	$\sqrt{3/5}r_p$	0.53 ± 0.06	0.41 ± 0.05
Gaussian	$e^{-r^2/2a^2}$	$8\pi a^2$	$\sqrt{3}a$	0.26 ± 0.03	0.44 ± 0.05
Exponential	$e^{-r/b}$	$28\pi b^2$	$\sqrt{12}b$	0.14 ± 0.02	0.47 ± 0.06

- The rms-radii above are calculated w/o account of possible parton spatial correlations. For example, for the Gaussian model one can write [Trelelani, Galucci, 0901.3089, hep-ph]:

$$\frac{1}{\sigma_{\text{eff}}} = \frac{3}{8\pi R_{\text{rms}}^2} (1 + \text{Corr.})$$

- If we have rms-radii from some other source, one can estimate the size of the spatial correlations (larger corr. \leftrightarrow larger rms-radius with a fixed σ_{eff})

Experimental results on σ_{eff}



from Atlas talk
at MPI workshop,
DESY, 2011

=> No clear energy dependence so far...
=> More measurements are needed!

Angular decorrelations in $\gamma+2$ and $\gamma+3$ jet events

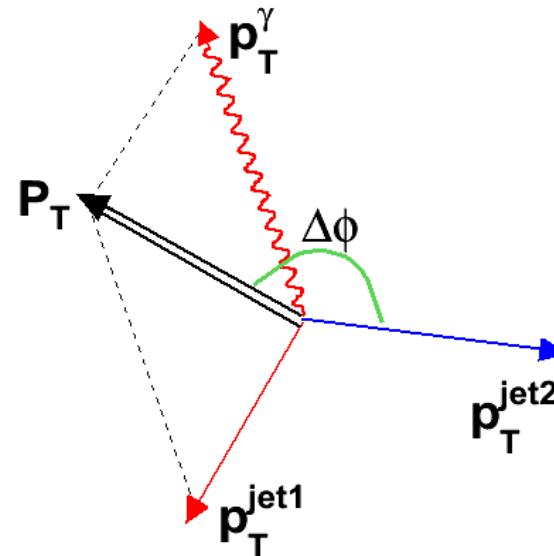
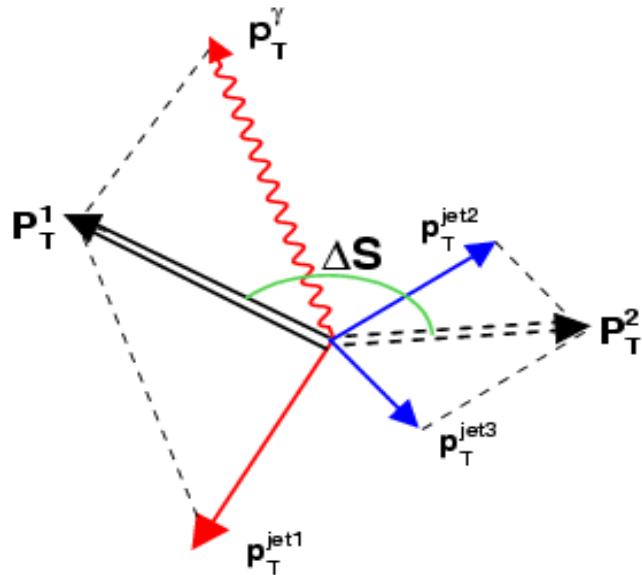
Phys.Rev.D83, 052008 (2011)

Motivations:

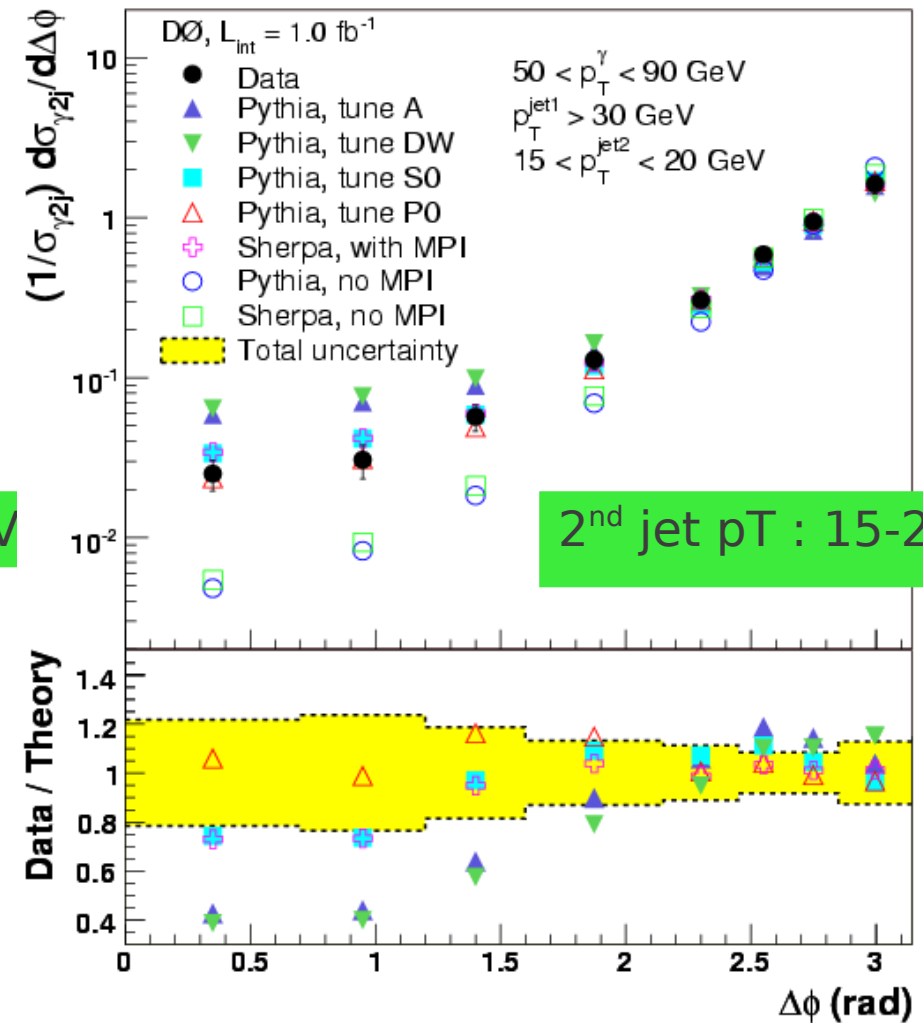
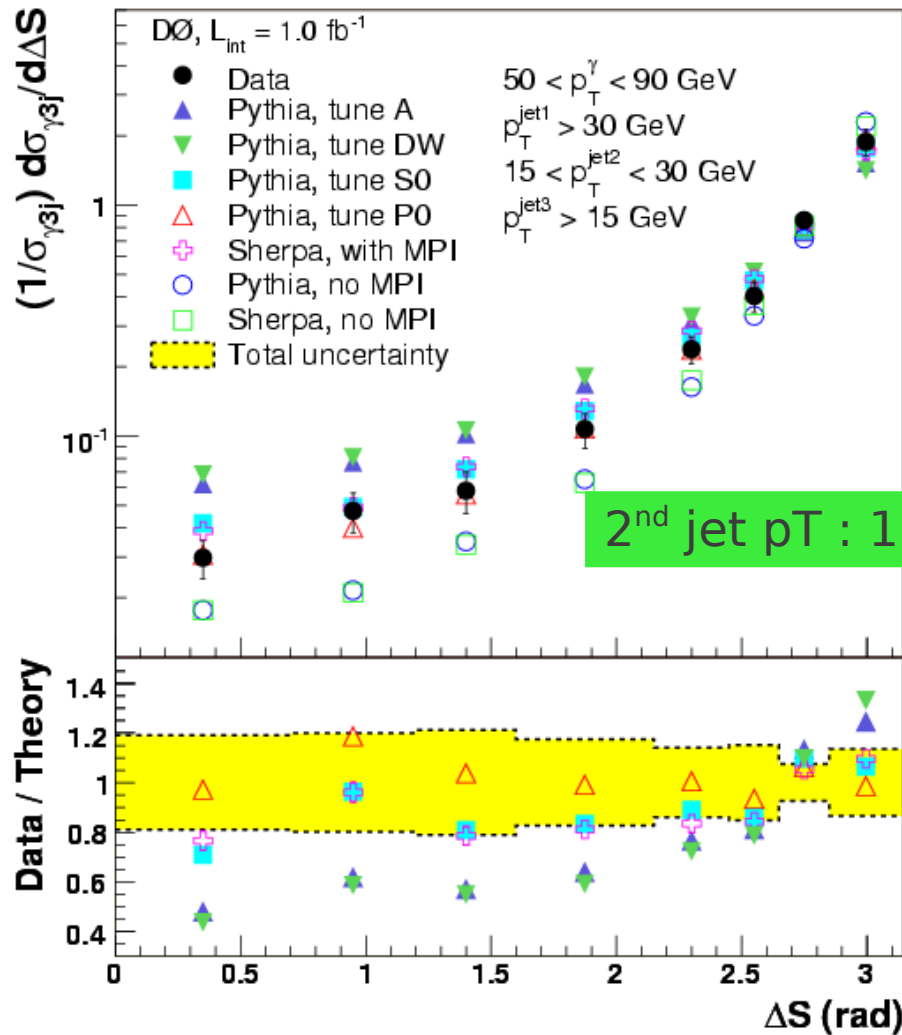
- By measuring **differential** cross sections vs. the azimuthal angles in $\gamma+3(2)$ jet events we can better tune (or even exclude some) MPI models in events with high p_T jets.
- Differentiation in jet p_T increases sensitivity to the models even further.

Four normalized differential cross sections are measured:

- $\Delta\phi(\gamma+\text{jet1}, \text{jet2})$ in 3 bins of 2nd jet p_T : 15-20, 20-25 and 25-30 GeV
- $\Delta S(\gamma+\text{jet1}, \text{jet2}+\text{jet3})$ for 2nd jet p_T 15-30 GeV (larger for stat. reasons but still has good sensitivity to MPI models)



ΔS and $\Delta\phi$ cross sections



- MPI models substantially differ from any SP (=single parton scattering) prediction.
- Large difference between SP models and data confirms presence of DP events in data.
- MPI models differ noticeably, especially at small angles
 => we can tune the models or just choose the best one(s)
- Data are close to Perugia (P0), S0 and Sherpa MPI tunes.
 N.B.: the conclusion is valid for both the considered variables and 3 jet p_T intervals!

$\Delta\phi$ cross sections

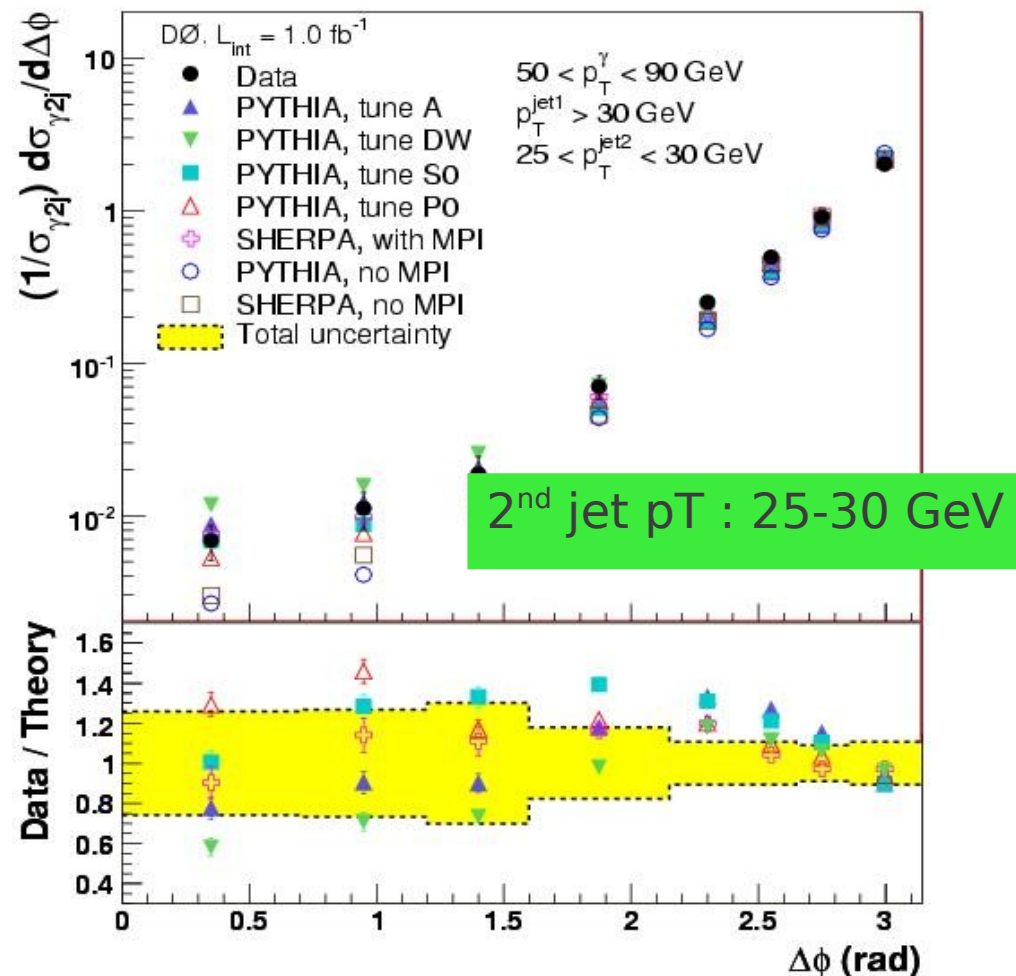
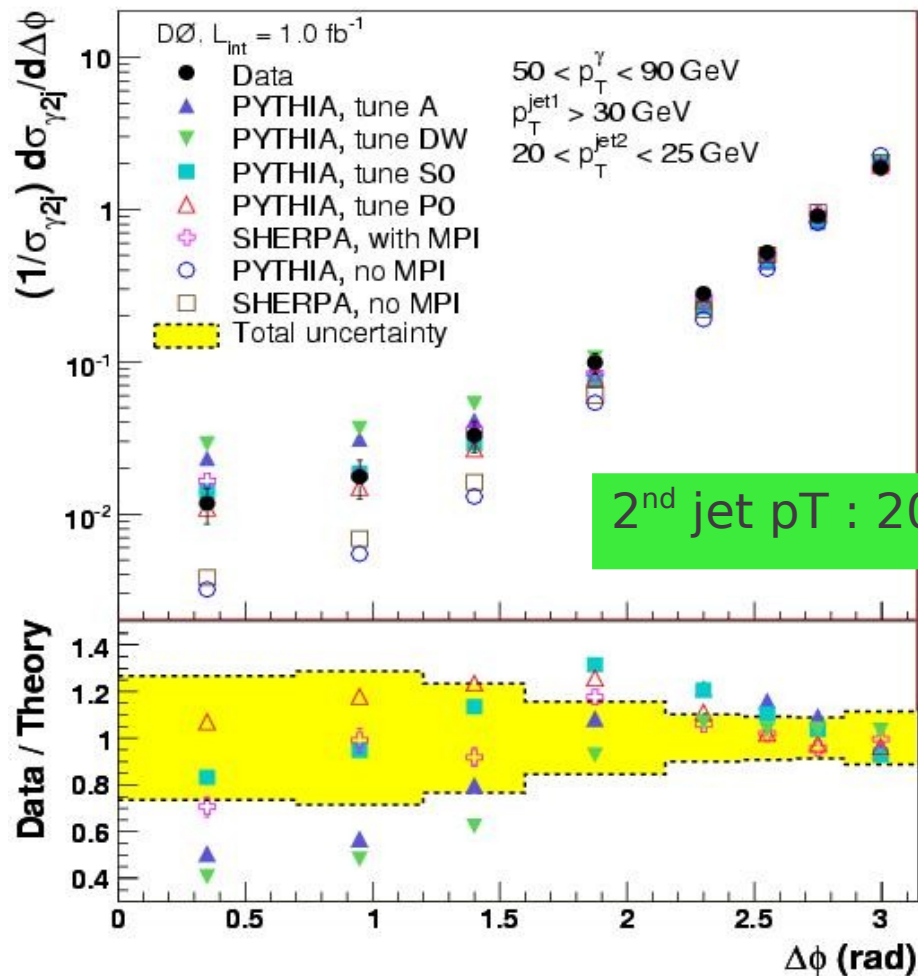


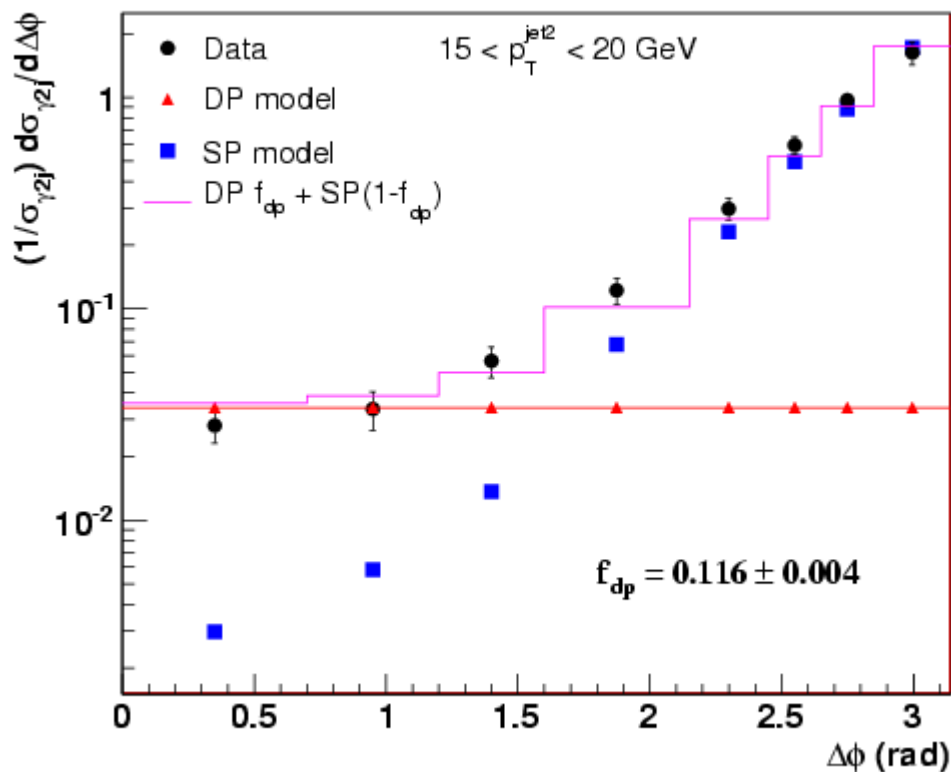
TABLE V: The results of a χ^2 test of the agreement between data points and theory predictions for the ΔS ($\gamma + 3$ jet) and $\Delta\phi$ ($\gamma + 2$ jet) distributions for $0.0 \leq \Delta S(\Delta\phi) \leq \pi$ rad. Values are χ^2/ndf .

Variable	p_T^{jet2} (GeV)	SP model					MPI model						
		PYTHIA	SHERPA	A	DW	S0	P0	P-nocr	P-soft	P-hard	P-6	P-X	SHERPA
ΔS	15 – 30	7.7	6.0	15.6	21.4	2.2	0.4	0.5	2.9	0.5	0.4	0.5	1.9
$\Delta\phi$	15 – 20	16.6	11.7	19.6	27.7	1.6	0.5	0.9	1.6	0.9	0.6	0.8	1.2
$\Delta\phi$	20 – 25	10.2	5.9	4.0	7.9	1.1	0.9	1.4	2.1	1.1	1.3	1.5	0.4
$\Delta\phi$	25 – 30	7.2	3.5	2.8	3.0	2.4	1.1	1.1	3.7	0.2	1.3	1.9	0.7

DP fractions in $\gamma+2$ jet events

- In $\gamma+2$ jet events in which 2nd jet is produced in the 2nd parton interaction, $\Delta\phi(\gamma+\text{jet1}, \text{jet2})$ distribution should be flat.
- Using this fact and also SP prediction for $\Delta\phi(\gamma+\text{jet1}, \text{jet2})$ one can get DP fraction from a maximal likelihood fit to data.

Example of the fit for 2nd jet pT
bin 15 – 20 GeV



DP fractions f_{DP} in $\gamma+2$ jet events

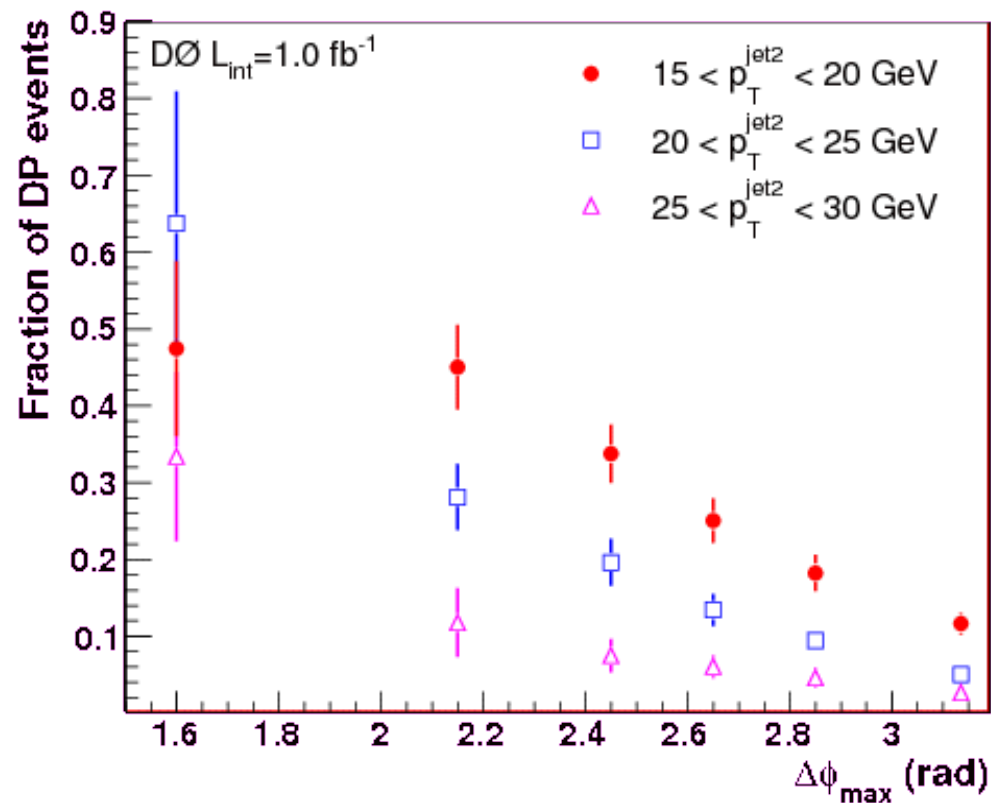
p_T^{jet2} (GeV)	$\langle p_T^{\text{jet2}} \rangle$ (GeV)	$f_{\text{dp}}^{\gamma+2j}$ (%)	Uncertainties (in %)		
			Fit	δ_{tot}	SP model
15 – 20	17.6	11.6 ± 1.0	5.2	8.3	6.7
20 – 25	22.3	5.0 ± 1.2	4.0	20.3	11.0
25 – 30	27.3	2.2 ± 0.8	27.8	21.0	17.9

CDF Run I: 14_{-7}^{+8} % at jet pT > 8 GeV and
photon pT > 16 GeV

DP fractions in $\gamma+2$ jet events vs. $\Delta\phi$

- DP fractions should depend on $\Delta\phi(\gamma+\text{jet1}, \text{jet2})$: the smaller $\Delta\phi$ angle the larger DP fraction (see, for example, plot on the previous slide).
- We can find this dependence by repeating the same fits at smaller $\Delta\phi$ angles.

DP fractions vs $\Delta\phi$ bin for 3 bins of 2nd jet pT



=> DP fractions are larger at smaller angles and smaller 2nd jet pT

TP fractions

$\gamma+3\text{jet}$ final state also can be produced by Tripple Parton interaction (TP).
 In $\gamma+3\text{jet}$ TP events all 3 jets should stem from 3 different parton scatterings.
 To estimate the TP fraction we used results on DP+TP fractions and fractions of Type I(II) events found in our previous measurement.
 TP in $\gamma+3\text{jet}$ data is calculated as:

$$f_{tp}^{\gamma 3j} = f_{dp+tp}^{tp} \cdot f_{dp+tp}^{\gamma 3j}$$

The fraction of TP in MixDP can be found as:

$$f_{dp+tp}^{tp} = F_{typeII} \cdot f_{dp}^{\gamma 2j} + F_{typeI} \cdot f_{dp}^{jj}$$

$f_{dp+tp}^{\gamma 3j}$ - measured in previous DP analysis;

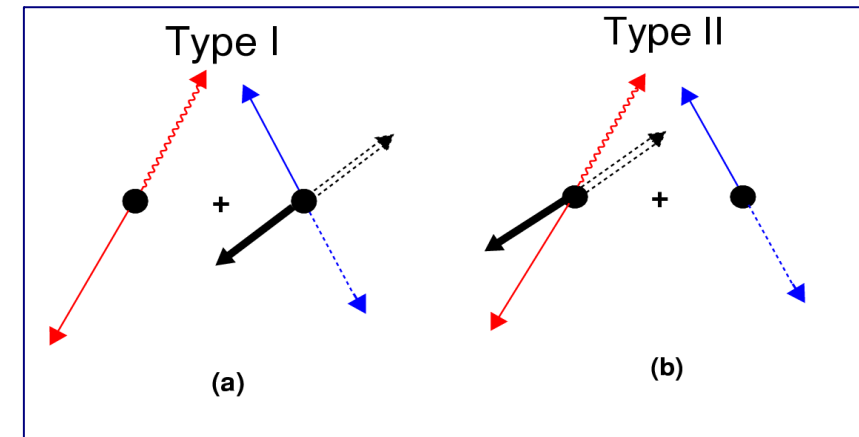
f_{dp}^{jj} - estimated using dijet cross section;

$f_{dp}^{\gamma 2j}$ - measured;

$F_{typeI(II)}$ - found from the model (MixDP).

Probability to produce another parton scattering is proportional to $R = \sigma_{ij} / \sigma_{eff}$, ratio $f_{tp}^{\gamma 3j} / f_{dp}^{\gamma 3j}$ should be proportional to R .

Types in MixDP model



TP fractions

$p_T^{\text{jet}2}$ (GeV)	$f_{tp}^{\gamma 3j}$ (%)	$f_{tp}^{\gamma 3j} / f_{dp}^{\gamma 3j}$ (%)
15 – 20	5.5 ± 1.1	13.5 ± 3.0
20 – 25	2.1 ± 0.6	6.6 ± 2.0
25 – 30	0.9 ± 0.3	3.8 ± 1.4

Summary

➤ In D0 we have been studying DP production events and measured recently:

- **Fraction of DP events in $\gamma+3$ -jet events** in three pT bins of 2nd jet :
15-20, 20-25, 25-30 GeV. It varies from $\sim 47\%$ at 15-20 GeV to $\sim 23\%$ at 25-30 GeV

- **Effective cross section** (process-independent, defines rate of DP events)
 σ_{eff} in the same jet pT bins with average value:

$$\sigma_{\text{eff}}^{\text{ave}} = 16.4 \pm 0.3(\text{stat}) \pm 2.3(\text{syst}) \text{ mb}$$

- **The DP in $\gamma+2$ jets: 11.6% at 15-20 GeV to 2.2% at 25-30 GeV.**
 - **The TP fractions in $\gamma+3$ -jet events** are determined for the first time. As a function of 2nd jet pT, they drop from $\sim 5.5\%$ at 15-20 GeV, to $\sim 0.9\%$ at 25-30 GeV.
 - **The ΔS and $\Delta\phi$ cross sections.** They allow to better tune MPI models: Data prefer the Sherpa and Pythia MPI models (P0, P0-X, P0-hard) with pT-ordered showers.
- DP production can be a significant background to many rare processes, especially with multi-jet final state. A set of variables allowing to reduce the DP background is suggested.

BACK-UP SLIDES

Parton spatial density and σ_{eff}

Double parton cross section

$$\sigma_{\text{dp}} = \sum_{q/g} \int \frac{\sigma_{12}\sigma_{34}}{2\sigma_{\text{eff}}} D_p(x_1, x_3) D_{\bar{p}}(x_2, x_4) dx_1 dx_2 dx_3 dx_4$$

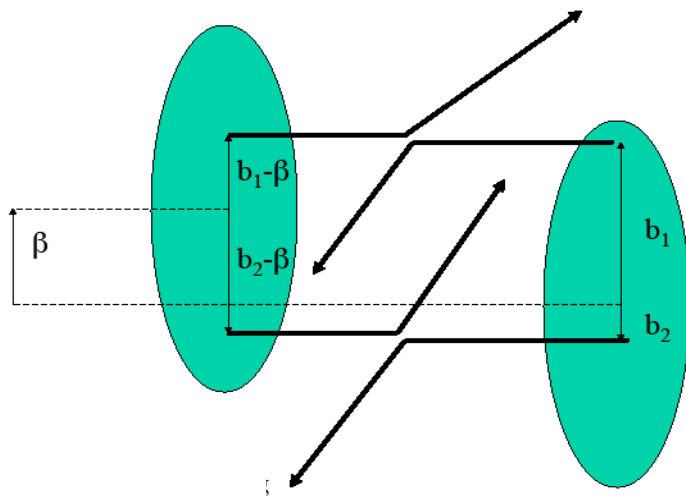
Effective cross section σ_{eff} is directly related with parton spatial density:

$$\sigma_{\text{eff}}^{-1} = \int d^2\beta [F(\beta)]^2, \quad \beta \text{ is impact parameter}$$

$$F(\beta) = \int f(b) f(b - \beta) d^2b,$$

where $f(b)$ is the density of partons in transverse space.

=> Having σ_{eff} measured we can estimate $f(b)$



Double parton scattering

Double parton interactions and dPDF evolution

From Phys.Rev.D81,065014(2010)(arXiv:1001.0104)
as an interpretation of the D0 measurement

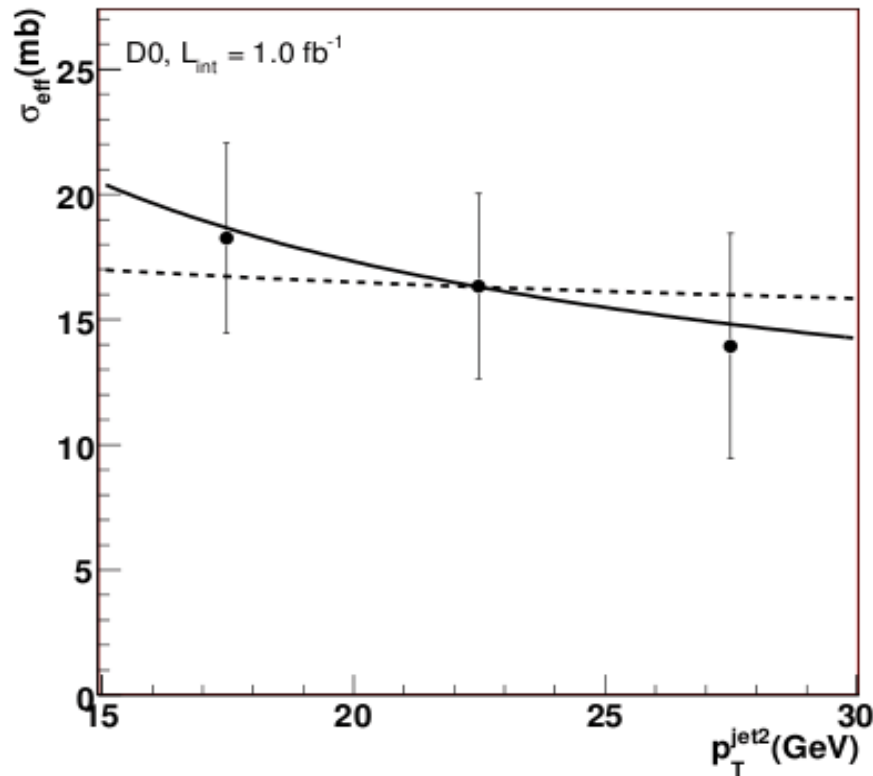


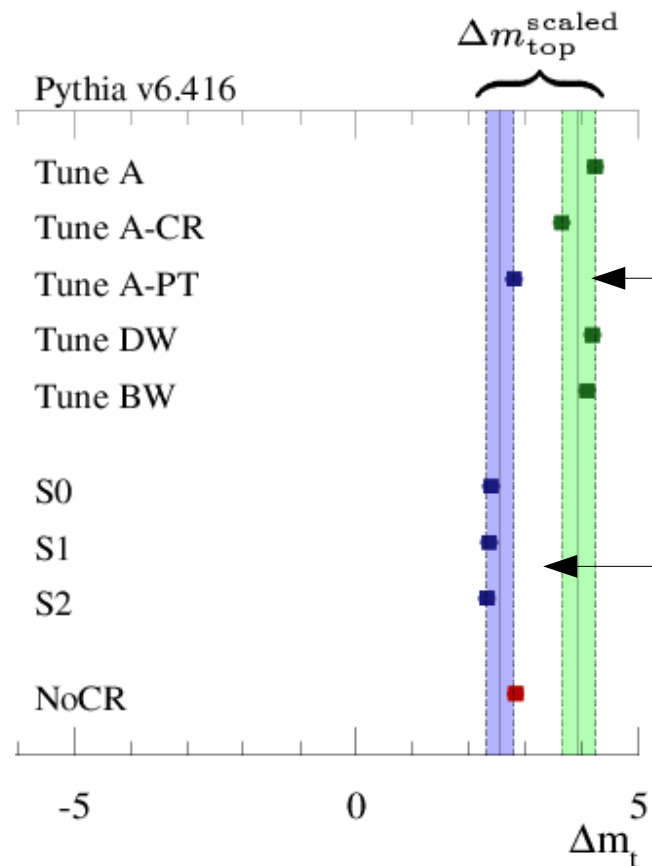
FIG. 1: Effective cross section $\sigma_{\text{eff}}^{\text{exp}}$ measured in the three $p_T^{\text{jet}2}$ bins at the D0 experiment [5]. The solid ($k = 0.5$) and dashed ($k = 0.1$) lines are the results from Eq. (11) at $p_{T0}^{\text{jet}2} = 22.5$ GeV and $\sigma_{\text{eff}}^0 = 16.3$ mb.

- If at any given scale μ_0 :
 $D(x_1, x_2, \mu_0) = D(x_1, \mu_0) * D(x_2, \mu_0) \theta(1-x_1-x_2)$
the dPDF evolution violates this factorization inevitably at any different scale $\mu \neq \mu_0$:
 $D(x_1, x_2, \mu) = D(x_1, \mu) * D(x_2, \mu) + R(x_1, x_2, \mu)$,
where $R(x_1, x_2, \mu)$ is a correlation term.

- Direct account of double PDFs: J.Gaunt and J.Stirling, JHEP 1003:005,2010.
First software implemented evolution equations and solutions for dPDF
To the large extent, being encouraged by the D0 measurement.

Motivations

Comparison of the top-quark mass offset corrections with a few MPI models



Plot from: D.Wicke, P.Z.Skands, Nuovo Cim. 123B, s1 (2008), arXiv:0807.3248v1 [hep-ph]

Models with virtuality-ordered parton shower

Models with pT-ordered parton shower

Difference between the two sets of the models leads to about 0.5-1.0 GeV uncertainty to the offset corrections for the top-quark mass.