

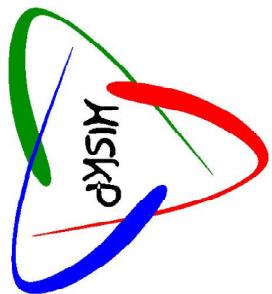
# Development of the Bonn-Gatchina partial wave analysis method and search for parity partners

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## Bonn-Gatchina partial wave analysis group:

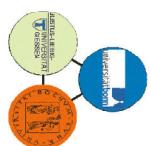
**A. Anisovich, E. Klemp, V. Nikonov, A. Sarantsev, U. Thoma**

**<http://pwa.hiskp.uni-bonn.de/>**



### Bonn-Gatchina Partial Wave Analysis

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Last changes: January 26<sup>th</sup>, 2010.

## Search for baryon states

1. Analysis of single and double meson photoproduction reactions.

$\gamma p \rightarrow \pi N, \eta N, K\Lambda, K\Sigma, \pi\pi N, \pi\eta N$ , CB-ELSA, CLAS, GRAAL, LEPS.

2. Analysis of single and double meson production in pion-induced reactions.

$\pi N \rightarrow \pi N, \eta N, K\Lambda, K\Sigma, \pi\pi N$ .

## Search for meson states

1. Analysis of the  $p\bar{p}$  annihilation at rest and  $\pi\pi$  interaction data.

2. Analysis of the  $p\bar{p}$  annihilation in flight into two and tree meson final state.

3. Analysis of the BES III data on  $J/\Psi$  decays (in collaboration with JINR Dubna).

## Analysis of $NN$ interaction

1. Analysis of single and double meson production  $NN \rightarrow \pi NN$  and  $\pi\pi NN$  (WASA, PNPI, HADES)

2. Analysis of hyperon production  $NN \rightarrow K\Lambda p$  (WASA, HADES)

## Energy dependent approach

In many cases an unambiguous partial wave decomposition at fixed energies is impossible. Then the energy and angular parts should be analyzed together:

$$A(s, t) = \sum_{\beta \beta' n} A_n^{\beta \beta'}(s) Q_{\mu_1 \dots \mu_n}^{(\beta)} F_{\nu_1 \dots \nu_n}^{\mu_1 \dots \mu_n} Q_{\nu_1 \dots \nu_n}^{(\beta')}$$

1. C. Zemach, Phys. Rev. **140**, B97 (1965); **140**, B109 (1965).
  2. S.U.Chung, Phys. Rev. D **57**, 431 (1998).
  3. B. S. Zou and D. V. Bugg, Eur. Phys. J. A **16**, 537 (2003)
- 1. Correlations between angular part and energy part are under control.
  - 2. Unitarity and analyticity can be introduced from the beginning.
  - 3. Parameters can be fixed from a combined fit of many reactions.
1. Anisovich:2001ra A. V. Anisovich, V. V. Anisovich, V. N. Markov, M. A. Matveev and A. V. Sarantsev, J. Phys. G **G 28**, 15 (2002)
  2. A. Anisovich, E. Klemp, A. Sarantsev and U. Thoma, Eur. Phys. J. A **24**, 111 (2005)
  3. A. V. Anisovich and A. V. Sarantsev, Eur. Phys. J. A **30**, 427 (2006)
  4. A. V. Anisovich, V. V. Anisovich, E. Klemp, V. A. Nikonorov and A. V. Sarantsev, Eur. Phys. J. A **34**, 129 (2007).

## $\pi N$ vertices

$$N_{\mu_1 \dots \mu_n}^+ = X_{\mu_1 \dots \mu_n}^{(n)} \quad N_{\mu_1 \dots \mu_n}^- = i \gamma_\nu \gamma_5 X_{\nu \mu_1 \dots \mu_n}^{(n+1)} \quad (1)$$

## $\gamma N$ vertices

$$\begin{aligned} Q_{\alpha_1 \dots \alpha_n}^{(1+) \mu} &= \gamma_\mu i \gamma_5 X_{\alpha_1 \dots \alpha_n}^{(n)} , \\ Q_{\alpha_1 \dots \alpha_n}^{(2+) \mu} &= \gamma_\nu i \gamma_5 X_{\mu \nu \alpha_1 \dots \alpha_n}^{(n+2)} , \\ Q_{\alpha_1 \dots \alpha_n}^{(3+) \mu} &= \gamma_\nu i \gamma_5 X_{\nu \alpha_1 \dots \alpha_n}^{(n+1)} g_{\mu \alpha_n}^\perp , \end{aligned}$$

## Fermion propagator for $J = N + \frac{1}{2}$

$$F_{\nu_1 \dots \nu_L}^{\mu_1 \dots \mu_L}(p) = (m + \hat{p}) O_{\alpha_1 \dots \alpha_L}^{\mu_1 \dots \mu_L} \frac{L+1}{2L+1} \left( g_{\alpha_1 \beta_1}^\perp - \frac{L}{L+1} \sigma_{\alpha_1 \beta_1} \right) \prod_{i=2}^L g_{\alpha_i \beta_i} O_{\nu_1 \dots \nu_L}^{\beta_1 \dots \beta_L}$$

$$\sigma_{\alpha_i \alpha_j} = \frac{1}{2} (\gamma_{\alpha_i} \gamma_{\alpha_j} - \gamma_{\alpha_j} \gamma_{\alpha_i})$$

# Parameterization of the partial wave amplitude

$$A_{1i} = K_{1j}(I - i\rho K)_{ji}^{-1}$$

and

$$K_{ij} = \sum_{\alpha} \frac{g_i^{\alpha} g_j^{\alpha}}{M_{\alpha}^2 - s} + f_{ij}(s) \quad f_{ij} = \frac{f_{ij}^{(1)} + f_{ij}^{(2)}}{s - s_0^{ij}} \sqrt{s}.$$

where  $f_{ij}$  is non-resonant transition part.

For the small coupled initial state, e.g. photoproduction:

$$A_k = P_j(I - i\rho K)_{jk}^{-1}$$

The vector of the initial interaction has the form:

$$P_j = \sum_{\alpha} \frac{\Lambda^{\alpha} g_j^{\alpha}}{M_{\alpha}^2 - s} + F_j(s)$$

Here  $F_j$  is non-resonant production of the final state  $j$ .

## N/D based (D-matrix) analysis of the data

$$\overline{\overline{J}} \overline{\overline{m}} = \overline{\overline{J}} \overline{\overline{K}} \stackrel{\pi\eta K}{\circ} \overline{\overline{m}} + \delta_{JK}$$

$$D_{jm} = D_{jk} \sum_{\alpha} B_{\alpha}^{km}(s) \frac{1}{M_m - s} + \frac{\delta_{jm}}{M_j^2 - s} \quad \hat{D} = \hat{\kappa}(I - \hat{B}\hat{\kappa})^{-1}$$

$$\hat{\kappa} = diag \left( \frac{1}{M_1^2 - s}, \frac{1}{M_2^2 - s}, \dots, \frac{1}{M_N^2 - s}, R_1, R_2 \dots \right)$$

$$\hat{B}_{ij} = \sum_{\alpha} B_{\alpha}^{ij} = \sum_{\alpha} \int \frac{ds'}{\pi} \frac{g_{\alpha}^{(R)i} \rho_{\alpha}(s', m_{1\alpha}, m_{2\alpha}) g_{\alpha}^{(L)j}}{s' - s - i0}$$

**In the present fits we calculate the elements of the  $B_\alpha^{ij}$  using one subtraction taken at the channel threshold  $M_\alpha = (m_{1\alpha} + m_{2\alpha})$ :**

$$B_\alpha^{ij}(s) = B_\alpha^{ij}(M_\alpha^2) + (s - M_\alpha^2) \int_{m_a^2}^{\infty} \frac{ds'}{\pi} \frac{g_\alpha^{(R)i} \rho_\alpha(s', m_{1\alpha}, m_{2\alpha}) g_\alpha^{(L)j}}{(s' - s - i0)(s' - M_\alpha^2)}.$$

**In this case the expression for elements of the  $\hat{B}$  matrix can be rewritten as:**

$$B_\alpha^{ij}(s) = g_a^{(R)i} \left( b^\alpha + (s - M_\alpha^2) \int_{m_a^2}^{\infty} \frac{ds'}{\pi} \frac{\rho_\alpha(s', m_{1\alpha}, m_{2\alpha})}{(s' - s - i0)(s' - M_\alpha^2)} \right) g_\beta^{(L)j} = g_a^{(R)i} B_\alpha g_\beta^{(L)j}$$

**and D-matrix method equivalent to the K-matrix method with loop diagram with real part taken into account:**

$$A = \hat{K}(I - \hat{B}\hat{K})^{-1}$$

$$B_{\alpha\beta} = \delta_{\alpha\beta} B_\alpha$$

### Meson spectroscopy. Two body reactions:

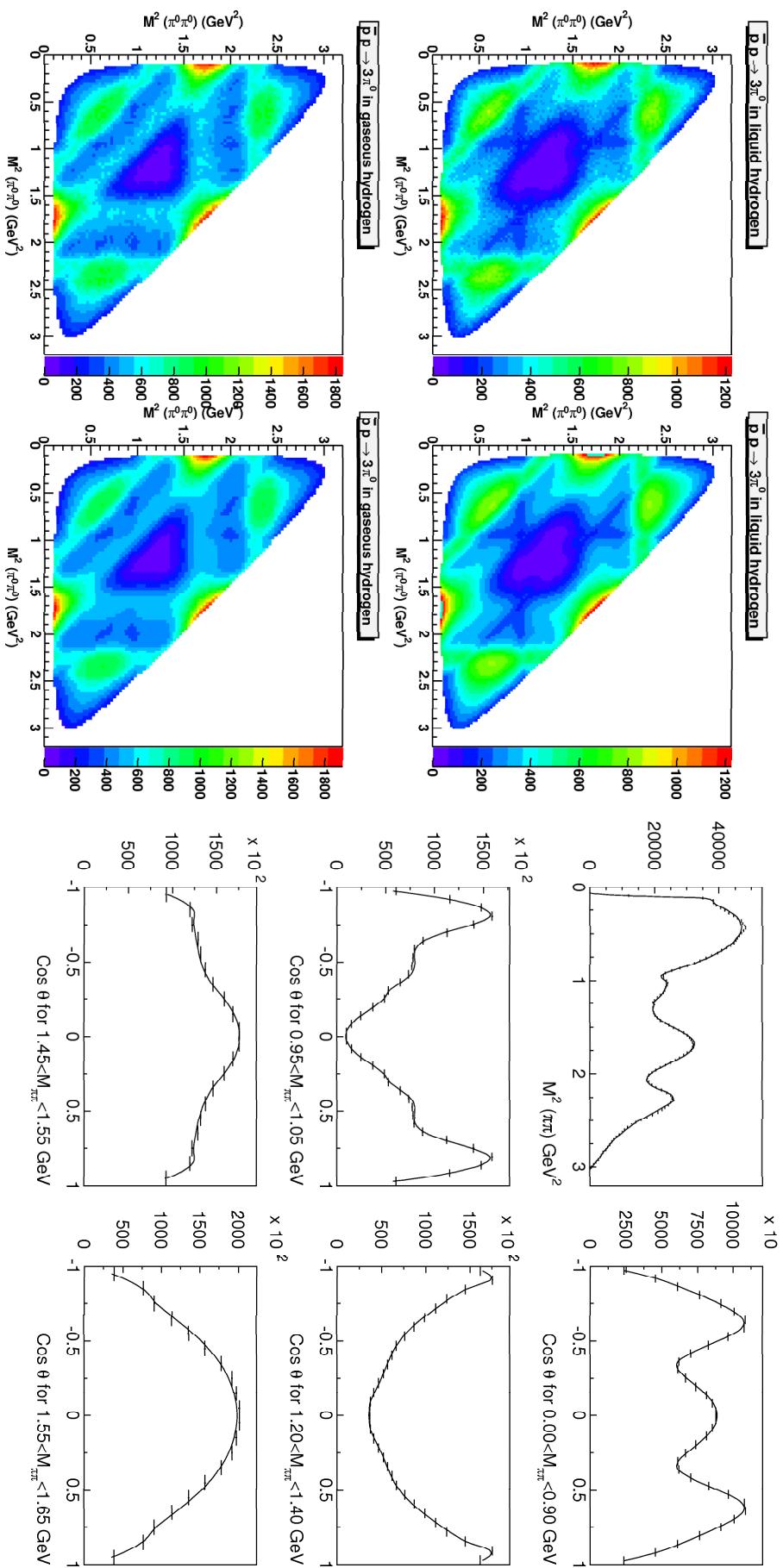
Reaction	Experiment	Reaction	Experiment
$\pi^+ \pi^- \rightarrow \pi^+ \pi^-$ (all waves)	CERN-Münich	$\pi\pi \rightarrow \pi^0 \pi^0$ (S-wave)	E852
$\pi\pi \rightarrow \pi^0 \pi^0$ ( <b>S-wave</b> )	GAMS	$\pi\pi \rightarrow \eta\eta'$ (S-wave)	GAMS
$\pi\pi \rightarrow K\bar{K}$ ( <b>S-wave</b> )	BNL	<b>S-wave</b> $\delta(\pi^+ \pi^-)$	Ke4

### Three body reactions from Crystal Barrel: (**L**-liquid, **G**-gaseous targets).

Reaction	Target	Reaction	Target	Reaction	Target
$\bar{p}p \rightarrow \pi^0 \pi^0 \pi^0$	( <b>L</b> ) $H_2$	$\bar{p}p \rightarrow \pi^+ \pi^0 \pi^-$	( <b>L</b> ) $H_2$	$\bar{p}p \rightarrow K_S K_S \pi^0$	( <b>L</b> ) $H_2$
$\bar{p}p \rightarrow \pi^0 \eta\eta$	( <b>L</b> ) $H_2$	$\bar{p}n \rightarrow \pi^0 \pi^0 \pi^-$	( <b>L</b> ) $D_2$	$\bar{p}p \rightarrow K^+ K^- \pi^0$	( <b>L</b> ) $H_2$
$\bar{p}p \rightarrow \pi^0 \pi^0 \eta$	( <b>L</b> ) $H_2$	$\bar{p}n \rightarrow \pi^- \pi^- \pi^+$	( <b>L</b> ) $D_2$	$\bar{p}p \rightarrow K_L K^\pm \pi^\mp$	( <b>L</b> ) $H_2$
$\bar{p}p \rightarrow \pi^0 \pi^0 \pi^0$	( <b>G</b> ) $H_2$			$\bar{p}n \rightarrow K_S K_S \pi^-$	( <b>L</b> ) $D_2$
$\bar{p}p \rightarrow \pi^0 \eta\eta$	( <b>G</b> ) $H_2$			$\bar{p}n \rightarrow K_S K^- \pi^0$	( <b>L</b> ) $D_2$
$\bar{p}p \rightarrow \pi^0 \pi^0 \eta$	( <b>G</b> ) $H_2$				

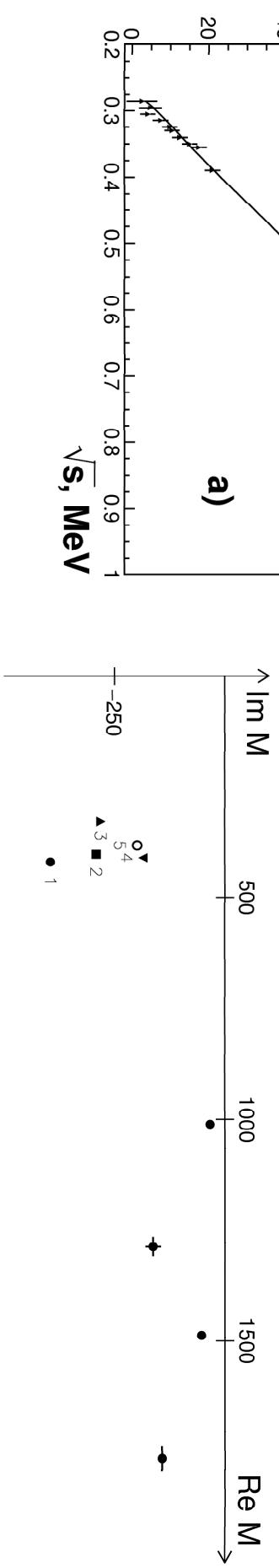
## Description of the $\bar{p}p \rightarrow 3\pi^0$ data (D-matrix method)

$p\bar{p} - 3\pi^0$  Liquid target



## Pole position of the resonances

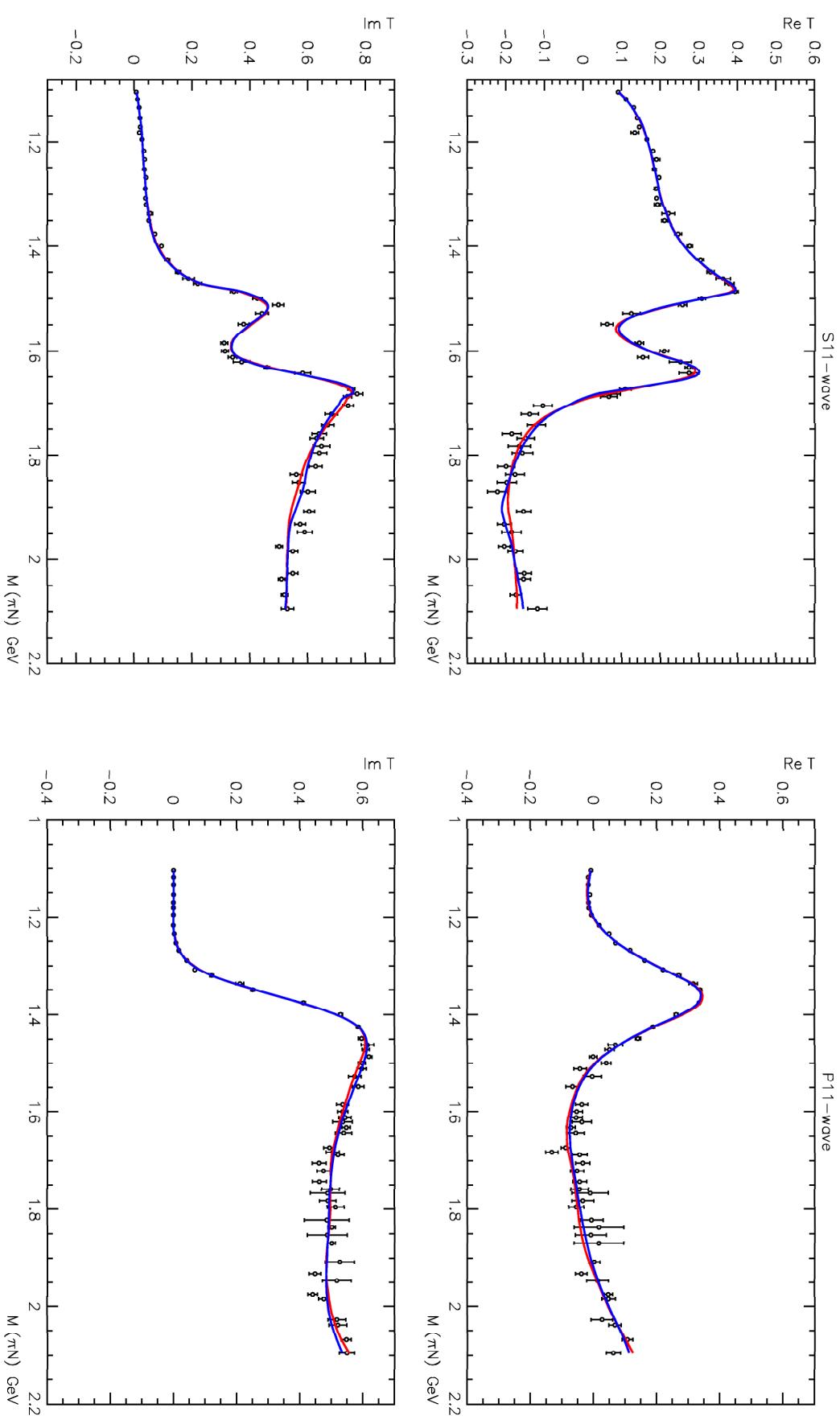
	K-matrix	D-matrix
$\sigma$ -meson		
$f_0(980)$	420-i 395	407-i 281
$f_0(1300)$	1014-i 31	1015-i 36
$f_0(1500)$	1302-i 140	1307-i 137
$f_0(1750)$	1487-i 58	1487-i 60
	1738-i 152	1781-i 140



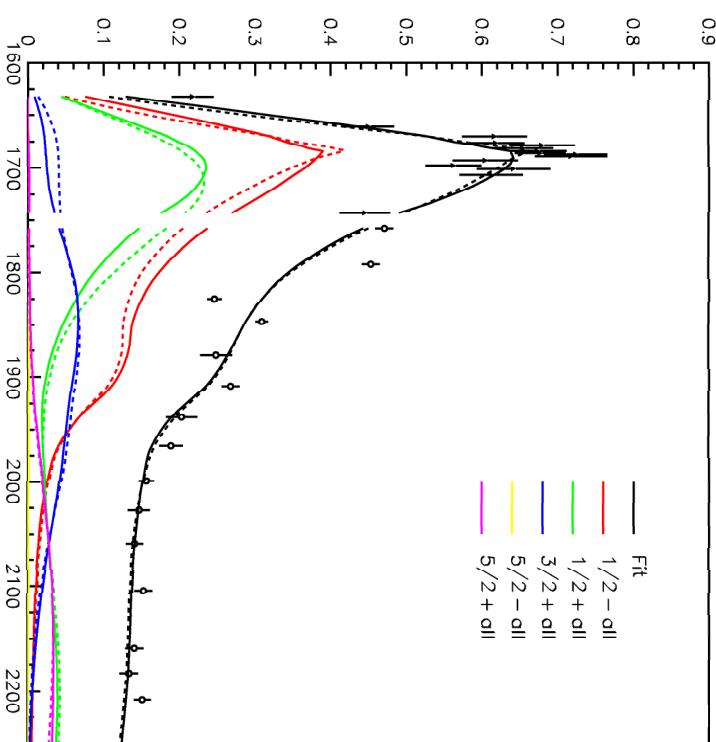
$445_{-8}^{+16} - i 272_{-13}^{+9}$  I.Caprini, G.Colangelo, and H.Leutwyler, Phys.Rev.Lett.96, 132001 (2006)

$457_{-15}^{+14} - i 279_{-7}^{+11}$  R.Garcia-Martin, R.Kaminski, J.R.Pelaez, J.Ruiz de Elvira, and F.J.Yndurain

## Description of the $\pi/N$ elastic amplitudes (GWU energy independent solution) with K-matrix and D-matrix solutions



## The fit of the $\pi^- p \rightarrow K\Lambda$ reaction

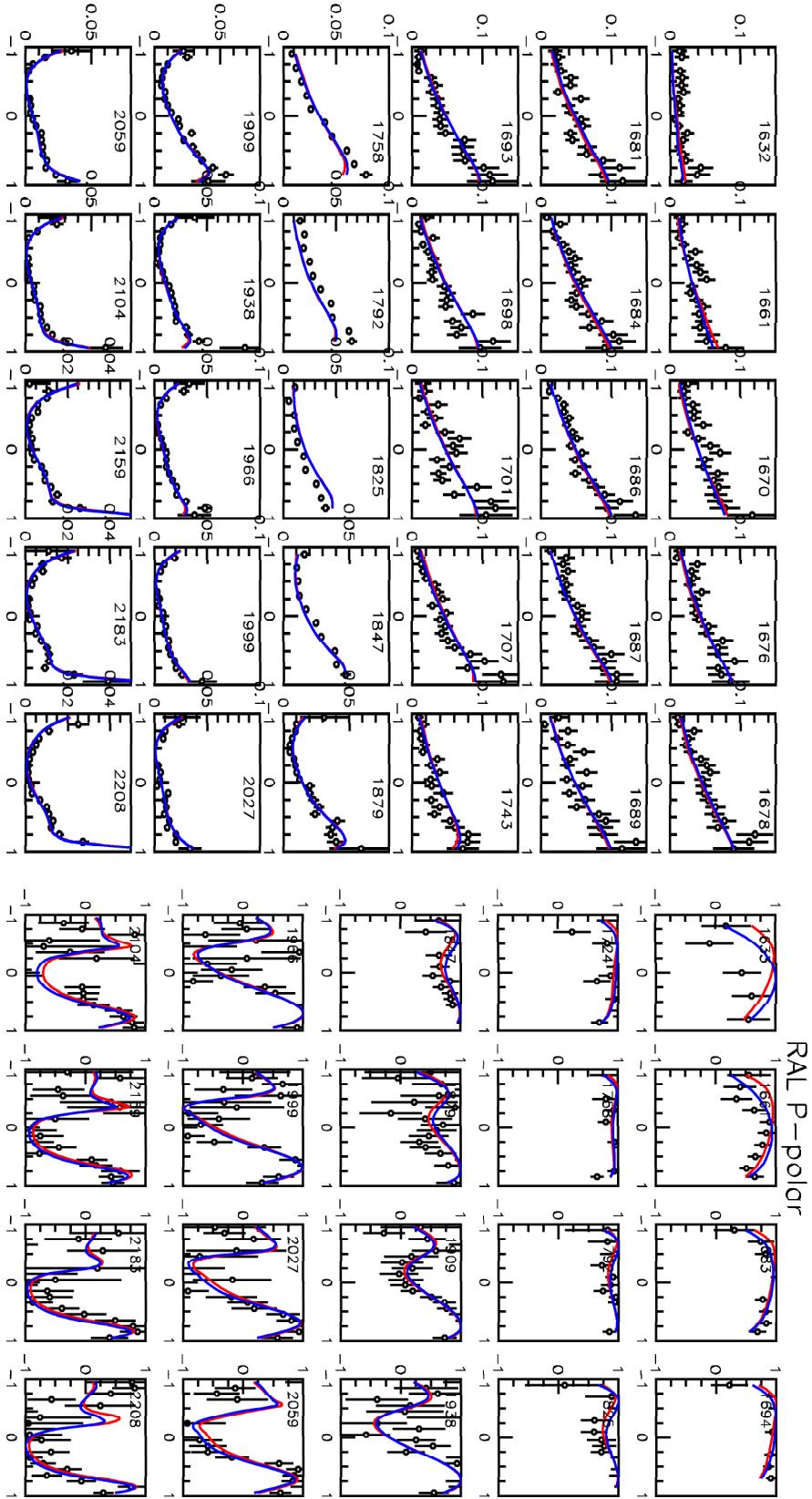


**Full experiment for  $\pi N \rightarrow K\Lambda$ :  
differential cross section, analyzing  
power, rotation parameter.**

**A clear evidence for resonances which  
are hardly seen (or not seen) in  
the elastic reactions:  $N(1710)P_{11}$ ,  
 $N(1900)P_{13}$ ,**

**The total cross section for the reaction  $\pi^- p \rightarrow K^0\Lambda$  and contributions from leading  
partial waves in K-matrix (full) and D-matrix (dashed) solutions.**

$$\pi^- p \rightarrow K\Lambda (d\sigma/d\Omega, P)$$



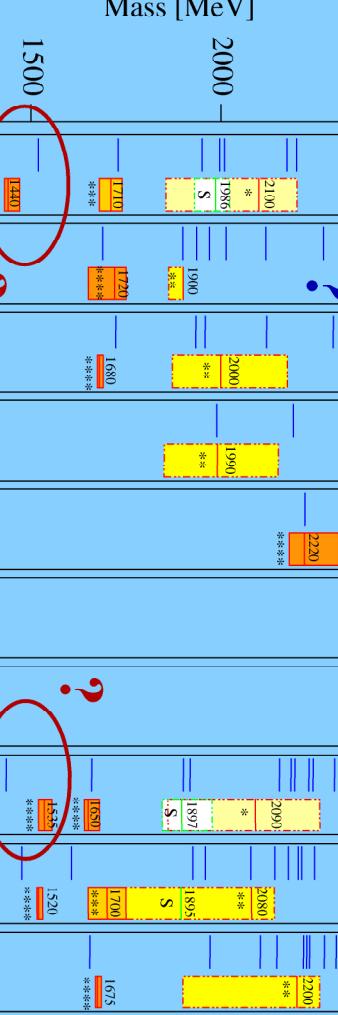
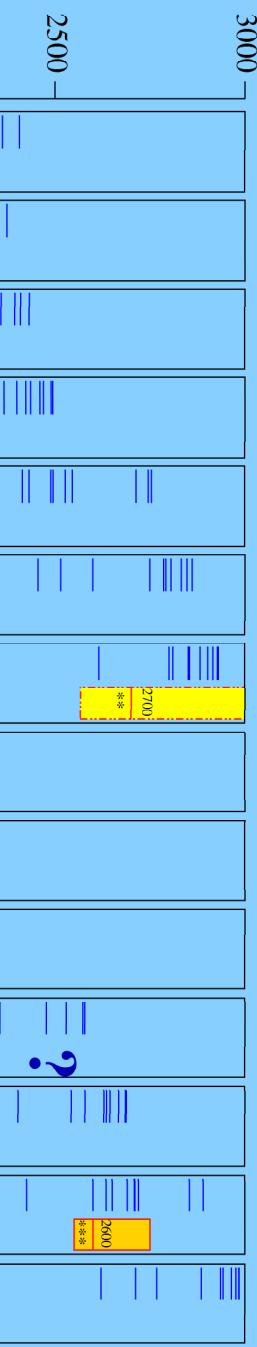
### Pole parameters of the $S_{11}$ states

	$N(1535)S_{11}$	$N(1650)S_{11}$	$N(1890)S_{11}$			
	K-matrix	D-matrix	K-matrix	D-matrix	K-matrix	D-matrix
$M_{\text{pole}}$	<b><math>1501 \pm 4</math></b>	<b><math>1494</math></b>	<b><math>1647 \pm 6</math></b>	<b><math>1651</math></b>	<b><math>1900 \pm 15</math></b>	<b><math>1905</math></b>
$\Gamma_{\text{pole}}$	<b><math>134 \pm 11</math></b>	<b><math>116</math></b>	<b><math>103 \pm 8</math></b>	<b><math>95</math></b>	$90^{+30}_{-15}$	<b><math>106</math></b>
<b>Elastic residue</b>	<b><math>31 \pm 4</math></b>	<b><math>25</math></b>	<b><math>24 \pm 3</math></b>	<b><math>23</math></b>	<b><math>1 \pm 1</math></b>	<b><math>1.5</math></b>
<b>Phase</b>	<b><math>-(29 \pm 5)^\circ</math></b>	<b><math>-38^\circ</math></b>	<b><math>-(75 \pm 12)^\circ</math></b>	<b><math>-62^\circ</math></b>	–	–
<b>Res<math>_{\pi N \rightarrow N\eta}</math></b>	<b><math>28 \pm 3</math></b>	<b><math>25</math></b>	<b><math>15 \pm 3</math></b>	<b><math>15</math></b>	<b><math>4 \pm 2</math></b>	<b><math>5</math></b>
<b>Phase</b>	<b><math>-(76 \pm 8)^\circ</math></b>	<b><math>-69^\circ</math></b>	<b><math>(132 \pm 10)^\circ</math></b>	<b><math>140</math></b>	<b><math>(40 \pm 20)^\circ</math></b>	<b><math>42^\circ</math></b>
<b>Res<math>_{\pi N \rightarrow \Delta\pi}</math></b>	<b><math>7 \pm 4</math></b>	<b><math>4</math></b>	<b><math>11 \pm 3</math></b>	<b><math>12</math></b>	–	–
<b>Phase</b>	<b><math>(147 \pm 17)^\circ</math></b>	<b><math>157^\circ</math></b>	<b><math>-(30 \pm 20)^\circ</math></b>	<b><math>-40</math></b>	–	–
<b><math>A^{1/2} (\text{GeV}^{-\frac{1}{2}})</math></b>	<b><math>0.116 \pm 0.010</math></b>	<b><math>0.107</math></b>	<b><math>0.033 \pm 0.007</math></b>	<b><math>0.029</math></b>	<b><math>0.012 \pm 0.006</math></b>	<b><math>0.010</math></b>
<b>Phase</b>	<b><math>(7 \pm 6)^\circ</math></b>	<b><math>1^\circ</math></b>	<b><math>-(9 \pm 15)^\circ</math></b>	<b><math>0^\circ</math></b>	<b><math>120 \pm 50^\circ</math></b>	<b><math>150^\circ</math></b>

## N\* - resonances in the quark model

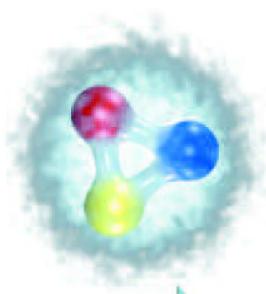
Nukleon  
10<sup>-15</sup> m

U. Loering, B. Metsch, H. Petry et al. (Bonn)



proton

Constituent  
quarks  
Confinement-  
potential  
Residual  
interaction



J π	L <sub>2T2J</sub>
1/2+	P <sub>11</sub>
3/2+	P <sub>13</sub>
5/2+	F <sub>15</sub>
7/2+	F <sub>17</sub>
9/2+	H <sub>19</sub>
11/2+	H <sub>111</sub>
13/2+	K <sub>113</sub>
1/2-	S <sub>11</sub>
3/2-	D <sub>13</sub>
5/2-	D <sub>15</sub>
7/2-	G <sub>17</sub>
9/2-	G <sub>19</sub>
11/2-	I <sub>111</sub>
13/2-	I <sub>113</sub>

## Baryon data base

<b>DATA</b>	<b>MAID</b>	<b>SAID</b>	<b>BnGa</b>
$\pi N \rightarrow \pi N$ ampl.	<b>SAID energy fixed</b>	<b>all data</b>	<b>SAID or Hoehler energy fixed</b>
$\gamma p \rightarrow \pi N$	$\frac{d\sigma}{d\Omega}, \Sigma, T, P, G, H, E$	$\frac{d\sigma}{d\Omega}, \Sigma, T, P$	$\frac{d\sigma}{d\Omega}, \Sigma, T, P$
$\gamma n \rightarrow \pi N$	$\frac{d\sigma}{d\Omega}, \Sigma, T, P$	$\frac{d\sigma}{d\Omega}, \Sigma, T, P$	$\frac{d\sigma}{d\Omega}, \Sigma, T, P$
$\gamma n \rightarrow \eta n$	$\frac{d\sigma}{d\Omega}, \Sigma, T$	$\frac{d\sigma}{d\Omega}, \Sigma$	$\frac{d\sigma}{d\Omega}, \Sigma$
$\gamma p \rightarrow \eta p$	$\frac{d\sigma}{d\Omega}, \Sigma, T$	$\frac{d\sigma}{d\Omega}, \Sigma$	$\frac{d\sigma}{d\Omega}, \Sigma$
$\gamma p \rightarrow K^+ \Lambda$	$\frac{d\sigma}{d\Omega}, P$	$\frac{d\sigma}{d\Omega}, \Sigma, P, T, C_x, C_z, O_{x'}, O_{z'}$	$\frac{d\sigma}{d\Omega}, \Sigma, P, T, C_x, C_z$
$\gamma p \rightarrow K^+ \Sigma^0$	$\frac{d\sigma}{d\Omega}, P$	$\frac{d\sigma}{d\Omega}, \Sigma, P, C_x, C_z$	$\frac{d\sigma}{d\Omega}, \Sigma, P$
$\gamma p \rightarrow K^0 \Sigma^+$	-	-	$\frac{d\sigma}{d\Omega}, \Sigma, P$
$\pi^- p \rightarrow \eta n$	-	$\frac{d\sigma}{d\Omega}$	$\frac{d\sigma}{d\Omega}$
$\pi^- p \rightarrow K^0 \Lambda$	-	$\frac{d\sigma}{d\Omega}$	$\frac{d\sigma}{d\Omega}, P, \beta$
$\pi^- p \rightarrow K^0 \Sigma^0$	-	$\frac{d\sigma}{d\Omega}$	$\frac{d\sigma}{d\Omega}, P$
$\pi^+ p \rightarrow K^+ \Sigma^+$	-	$\frac{d\sigma}{d\Omega}$	$\frac{d\sigma}{d\Omega}, P, \beta$
$\pi^- p \rightarrow \pi^0 \pi^0 n$	-	-	$\frac{d\sigma}{d\Omega}$
$\gamma p \rightarrow \pi^0 \pi^0 p$	-	-	$\frac{d\sigma}{d\Omega}, \Sigma, E, I_c, I_s$
$\gamma p \rightarrow \pi^0 \eta p$	-	-	$\frac{d\sigma}{d\Omega}, \Sigma, I_c, I_s$

## Nucleon spectrum

$N(1700)\frac{3}{2}^-$	or	$N(1700)D_{13}$	$N(1710)\frac{1}{2}^+$	or	$N(1710)P_{11}$
<hr/>					
$N(1700)\frac{3}{2}^-$ pole parameters (MeV)			$N(1710)\frac{1}{2}^+$ pole parameters (MeV)		
$M_{\text{pole}}$	$1770 \pm 40$	$\Gamma_{\text{pole}}$	$M_{\text{pole}}$	$1687 \pm 17$	$\Gamma_{\text{pole}}$
Elastic pole residue	$50 \pm 40$	Phase	- $(100 \pm 40)^\circ$	$6 \pm 4$	Phase
Residue $\pi N \rightarrow \Delta \pi_{L=0}$	$75 \pm 50$	Phase	- $(60 \pm 40)^\circ$	$11 \pm 4$	Phase
Residue $\pi N \rightarrow \Delta \pi_{L=2}$	$18 \pm 12$	Phase	$(90 \pm 35)^\circ$	$17 \pm 7$	Phase
$A^{1/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ )	$0.044 \pm 0.020$	Phase	$(85 \pm 45)^\circ$	$0.055 \pm 0.018$	Phase
$A^{3/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ )	$-0.037 \pm 0.012$	Phase	$(0 \pm 30)^\circ$		$-(10 \pm 65)^\circ$
<hr/>					
$N(1700)\frac{3}{2}^-$ Breit-Wigner parameters (MeV)			$N(1710)\frac{1}{2}^+$ Breit-Wigner parameters (MeV)		
$M_{\text{BW}}$	$1790 \pm 40$	$\Gamma_{\text{BW}}$	$M_{\text{BW}}$	$1710 \pm 20$	$\Gamma_{\text{BW}}$
$\text{Br}(\pi N)$	$12 \pm 5\%$		$\text{Br}(N\pi)$	$5 \pm 4\%$	$\text{Br}(N\eta)$
$\text{Br}(\Delta \pi_{L=0})$	$72 \pm 16\%$	$\text{Br}(\Delta \pi_{L=2})$		$23 \pm 7\%$	
$A_{BW}^{1/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ )	$0.041 \pm 0.017$	$A_{BW}^{3/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ )	$-0.034 \pm 0.013$	$A_{BW}^{1/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ )	$0.052 \pm 0.015$

**Confirmed, but ambiguous**

**Confirmed**

## Nucleon spectrum

$N(1720)\frac{3}{2}^+$	or	$N(1720)P_{13}$	$N(1860)\frac{5}{2}^+$	or	$N(1860)F_{15}$
<hr/>					
$N(1720)\frac{3}{2}^+$ pole parameters (MeV)			$N(1860)\frac{5}{2}^+$ pole parameters (MeV)		
$M_{\text{pole}}$	$1660 \pm 30$	$\Gamma_{\text{pole}}$	$M_{\text{pole}}$	$1830^{+120}_{-60}$	$\Gamma_{\text{pole}}$
Elastic pole residue	$22 \pm 8$	Phase	Elastic pole residue	$50 \pm 20$	Phase
Residue $\pi N \rightarrow N\eta$	$7 \pm 5$	Phase	not defined		
Residue $\pi N \rightarrow \Lambda K$	$14 \pm 10$	Phase	- $(150 \pm 45)^\circ$		
Residue $\pi N \rightarrow \Delta \pi_{L=1}$	$64 \pm 25$	Phase	$(80 \pm 40)^\circ$		
Residue $\pi N \rightarrow \Delta \pi_{L=3}$	$8 \pm 8$	Phase	not defined		
$A^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$0.110 \pm 0.045$	Phase	$A^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$0.020 \pm 0.012$	Phase
$A^{3/2} (\text{GeV}^{-\frac{1}{2}})$	$0.150 \pm 0.035$	Phase	$A^{3/2} (\text{GeV}^{-\frac{1}{2}})$	$0.050 \pm 0.020$	Phase
<hr/>					
$N(1720)\frac{3}{2}^+$ Breit-Wigner parameters (MeV)			$N(1860)\frac{5}{2}^+$ Breit-Wigner parameters (MeV)		
$M_{\text{BW}}$	$1690^{+70}_{-35}$	$\Gamma_{\text{BW}}$	$M_{\text{BW}}$	$1860^{+120}_{-60}$	$\Gamma_{\text{BW}}$
$\text{Br}(N\pi)$	$10 \pm 5\%$	$\text{Br}(N\eta)$	$\text{Br}(N\pi)$	$20 \pm 6\%$	
$\text{Br}(\Delta\pi_{L=1})$	$75 \pm 15\%$	$\text{Br}(\Delta\pi_{L=3})$			
$A_{BW}^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$0.110 \pm 0.045$	$A_{BW}^{3/2} (\text{GeV}^{-\frac{1}{2}})$	$0.150 \pm 0.030$	$A_{BW}^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$-0.019 \pm 0.011$
				$A_{BW}^{3/2} (\text{GeV}^{-\frac{1}{2}})$	$0.048 \pm 0.018$

**Needs confirmation**

## Nucleon spectrum

$N(1875)\frac{3}{2}^-$	or	$N(1875)D_{13}$	$N(1880)\frac{1}{2}^+$	or	$N(1880)P_{11}$
<hr/>					
$N(1875)\frac{3}{2}^-$ pole parameters (MeV)			$N(1880)\frac{1}{2}^+$ pole parameters (MeV)		
$M_{\text{pole}}$	$1860 \pm 25$	$\Gamma_{\text{pole}}$	$200 \pm 20$	$M_{\text{pole}}$	$1860 \pm 35$
Elastic pole residue	$2.5 \pm 1.0$	Phase	not defined	Elastic pole residue	$6 \pm 4$
Residue $\pi N \rightarrow \Lambda K$	$1.5 \pm 1.0$	Phase	not defined	Residue $\pi N \rightarrow \eta N$	$13 \pm 8$
Residue $\pi N \rightarrow \Sigma K$	$5 \pm 3$	Phase	not defined	Residue $\pi N \rightarrow K \Lambda$	$4 \pm 3$
Residue $\pi N \rightarrow N \sigma$	$8 \pm 3$	Phase	$-(170 \pm 65)^\circ$	Residue $\pi N \rightarrow K \Sigma$	$13 \pm 7$
$A^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$0.018 \pm 0.008$	Phase	$-(100 \pm 60)^\circ$	$A^{1/2} (\text{GeV}^{-\frac{1}{2}}) 0.014 \pm 0.004^{(01)}$	Phase
$A^{3/2} (\text{GeV}^{-\frac{1}{2}})$	$0.010 \pm 0.004$	Phase	$(180 \pm 30)^\circ$	$A^{1/2} (\text{GeV}^{-\frac{1}{2}}) 0.036 \pm 0.012^{(02)}$	Phase
<hr/>					
$N(1875)\frac{3}{2}^-$ Breit-Wigner parameters (MeV)			$N(1880)\frac{1}{2}^+$ Breit-Wigner parameters (MeV)		
$M_{\text{BW}}$	$1880 \pm 20$	$\Gamma_{\text{BW}}$	$200 \pm 25$	$M_{\text{BW}}$	$1870 \pm 35$
$\text{Br}(N\pi)$	$3 \pm 2\%$	$\text{Br}(N\eta)$	$5 \pm 2\%$	$\text{Br}(\pi N)$	$5 \pm 3\%$
$\text{Br}(\Lambda K)$	$4 \pm 2\%$	$\text{Br}(\Sigma K)$	$15 \pm 8\%$	$\text{Br}(K\Lambda)$	$2 \pm 1\%$
$\text{Br}(\Delta\pi)$	$20 \pm 12\%$	$\text{Br}(N\sigma)$	$60 \pm 12\%$	$\text{Br}(K\Sigma)$	$17 \pm 7\%$
$A_{\text{BW}}^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$0.018 \pm 0.010$	$A_{\text{BW}}^{3/2} (\text{GeV}^{-\frac{1}{2}})$	$-0.009 \pm 0.005$	$A_{\text{BW}}^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$-0.013 \pm 0.003^{(01)}$
$A_{\text{BW}}^{1/2} (\text{GeV}^{-\frac{1}{2}})$				$A_{\text{BW}}^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$0.034 \pm 0.011^{(02)}$

Observed by BG group (needs confirmation)

## Nucleon spectrum

$N(1895)\frac{1}{2}^-$	or	$N(1895)S_{11}$	$N(1900)\frac{3}{2}^+$	or	$N(1900)P_{13}$
<hr/>					
$N(1895)\frac{1}{2}^-$ pole parameters (MeV)			$N(1900)\frac{3}{2}^+$ pole parameters (MeV)		
$M_{\text{pole}}$	$1900 \pm 15$	$\Gamma_{\text{pole}}$	$M_{\text{pole}}$	$1900 \pm 30$	$\Gamma_{\text{pole}}$
Elastic pole residue	$1 \pm 1$	Phase	not defined	$3 \pm 2$	Phase
Residue $\pi N \rightarrow \eta N$	$3 \pm 2$	Phase	$(40 \pm 20)^\circ$	$6 \pm 3$	Phase
Residue $\pi N \rightarrow K\Lambda$	$2 \pm 1$	Phase	$-(90 \pm 30)^\circ$	$9 \pm 5$	Phase
Residue $\pi N \rightarrow K\Sigma$	$3 \pm 2$	Phase	$(40 \pm 30)^\circ$	$5 \pm 3$	Phase
$A^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$0.012 \pm 0.006$	Phase	$(120 \pm 50)^\circ$	$A^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$0.026 \pm 0.015$
				$A^{3/2} (\text{GeV}^{-\frac{1}{2}})$	$0.060 \pm 0.030$
<hr/>					
$N(1895)\frac{1}{2}^-$ Breit-Wigner parameters (MeV)			$N(1900)\frac{3}{2}^+$ Breit-Wigner parameters (MeV)		
$M_{\text{BW}}$	$1895 \pm 15$	$\Gamma_{\text{BW}}$	$M_{\text{BW}}$	$1905 \pm 30$	$\Gamma_{\text{BW}}$
$\text{Br}(\pi N)$	$2 \pm 1\%$	$\text{Br}(\eta N)$	$\text{Br}(\pi N)$	$3 \pm 2\%$	$\text{Br}(\eta N)$
$\text{Br}(K\Lambda)$	$18 \pm 5\%$	$\text{Br}(K\Sigma)$	$\text{Br}(K\Lambda)$	$16 \pm 5\%$	$\text{Br}(K\Sigma)$
			$\text{Br}(\Delta\pi_{L=1})$	$38 \pm 10\%$	$\text{Br}(\Delta\pi_{L=3})$
$A_{BW}^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$-0.011 \pm 0.006$		$A_{BW}^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$0.026 \pm 0.015$	$A_{BW}^{3/2} (\text{GeV}^{-\frac{1}{2}})$
					$-0.065 \pm 0.030$
<hr/>					

Observed by BG (needs confirmation)

Observed by BG (Confirmed)

## Nucleon spectrum

$N(1990)\frac{7}{2}^+$	or	$N(1990)F_{17}$	$N(2000)\frac{5}{2}^+$	or	$N(2000)F_{15}$
<hr/> <hr/>					
$N(1990)\frac{7}{2}^+$ pole parameters (MeV)			$N(2000)\frac{5}{2}^+$ pole parameters (MeV)		
$M_{\text{pole}}$	$2030 \pm 65$	$I_{\text{pole}}$	$M_{\text{pole}}$	$2030 \pm 110$	$I_{\text{pole}}$
Elastic pole residue	$2 \pm 1$	Phase	(125±65) $^\circ$	$35^{+80}_{-15}$	Phase
Residue $\pi N \rightarrow \Delta \pi_{L=3}$	$8 \pm 5$	Phase	(80±50) $^\circ$		
$A^{1/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ )	$0.042 \pm 0.014$	Phase	$A^{1/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ )	$0.035 \pm 0.015$	Phase
$A^{3/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ )	$0.058 \pm 0.014$	Phase	$A^{3/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ )	$0.050 \pm 0.014$	Phase
<hr/> <hr/>					
$N(1990)\frac{7}{2}^+$ Breit-Wigner parameters (MeV)			$N(2000)\frac{5}{2}^+$ Breit-Wigner parameters (MeV)		
$M_{\text{BW}}$	$2060 \pm 65$	$I_{\text{BW}}$	$M_{\text{BW}}$	$2090 \pm 120$	$I_{\text{BW}}$
$\text{Br}(\pi N)$	$2 \pm 1\%$	$\text{Br}(\Delta \pi_{L=3})$	$\text{Br}(\pi N)$	$9 \pm 4\%$	$\text{Br}(\Delta N)$
$A_{BW}^{1/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ )	$0.040 \pm 0.012$	$A_{BW}^{3/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ )	$A_{BW}^{1/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ )	$0.057 \pm 0.012$	$A_{BW}^{3/2}$ ( $\text{GeV}^{-\frac{1}{2}}$ ) $0.048 \pm 0.014$
<hr/> <hr/>					

Two solutions

## Nucleon spectrum

$N(2060)\frac{5}{2}^-$	or	$N(2060)D_{15}$	$N(2150)\frac{3}{2}^-$	or	$N(2150)D_{13}$
<hr/>					
$N(2060)\frac{5}{2}^-$ pole parameters (MeV)			$N(2150)\frac{3}{2}^-$ pole parameters (MeV)		
$M_{\text{pole}}$	$2040 \pm 15$	$\Gamma_{\text{pole}}$	$M_{\text{pole}}$	$2110 \pm 50$	$\Gamma_{\text{pole}}$
Elastic pole residue	$19 \pm 5$	Phase	Elastic pole residue	$13 \pm 3$	Phase
Residue $\pi N \rightarrow \eta N$	$15 \pm 8$	Phase	Residue $\pi N \rightarrow K\Lambda$	$5 \pm 2$	Phase
Residue $\pi N \rightarrow K\Lambda$	$1 \pm 0.5$	Phase	Residue $\pi N \rightarrow K\Sigma$	$3 \pm 2$	Phase
Residue $\pi N \rightarrow K\Sigma$	$7 \pm 4$	Phase	$-(70 \pm 30)^\circ$		
$A^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$0.065 \pm 0.015$	Phase	$A^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$0.125 \pm 0.045$	Phase
$A^{3/2} (\text{GeV}^{-\frac{1}{2}})$	$0.055^{+15}_{-35}$	Phase	$A^{3/2} (\text{GeV}^{-\frac{1}{2}})$	$0.150 \pm 0.060$	Phase
<hr/>					
$N(2060)\frac{5}{2}^-$ Breit-Wigner parameters (MeV)			$N(2150)\frac{3}{2}^-$ Breit-Wigner parameters (MeV)		
$M_{\text{BW}}$	$2060 \pm 15$	$\Gamma_{\text{BW}}$	$M_{\text{BW}}$	$2150 \pm 60$	$\Gamma_{\text{BW}}$
$\text{Br}(\pi N)$	$8 \pm 2\%$	$\text{Br}(\eta N)$	$\text{Br}(\pi N)$	$6 \pm 2\%$	$\text{Br}(\Delta\pi)$
$\text{Br}(K\Sigma)$	$3 \pm 2\%$				
$A_{BW}^{1/2} (\text{GeV}^{-\frac{1}{2}})$	$0.067 \pm 0.015$	$A_{BW}^{3/2} (\text{GeV}^{-\frac{1}{2}}) 0.055 \pm 0.020$	$A_{BW}^{1/2} (\text{GeV}^{-\frac{1}{2}}) 0.130 \pm 0.045$	$A_{BW}^{3/2} (\text{GeV}^{-\frac{1}{2}}) 0.150 \pm 0.055$	

Observed by BG (Confirmed)

Observed by BG (needs confirmation)

# Parity doublets of $N$ and $\Delta$ resonances at high mass region

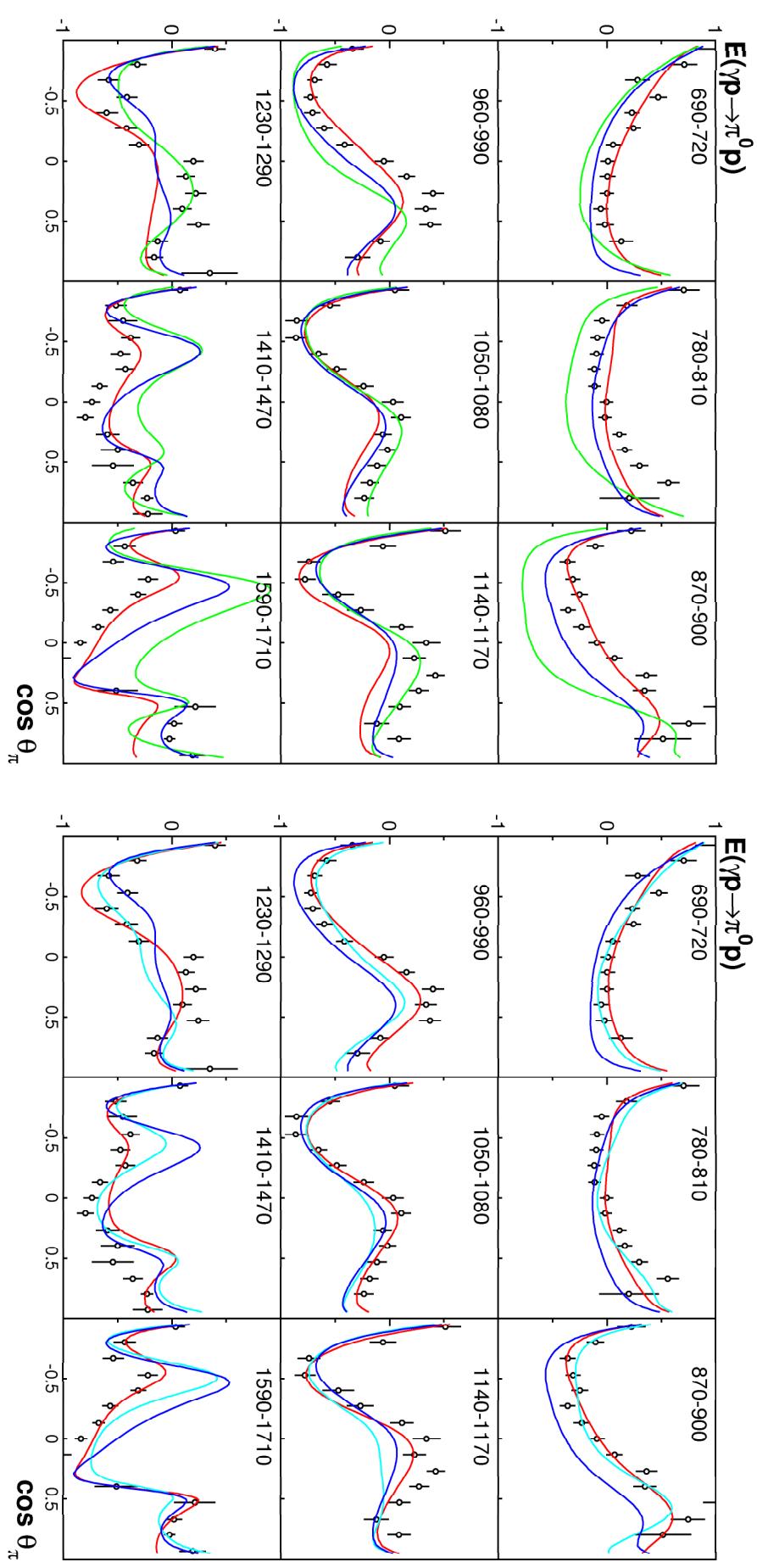
Parity doublets must not interact by pion emission

and could have a small coupling to  $\pi N$ .

$J = \frac{1}{2}$	<b>N</b> <sub>1/2+</sub> (1880) **	<b>N</b> <sub>1/2-</sub> (1890) **	$\Delta$ <sub>1/2+</sub> (1910) ****	$\Delta$ <sub>1/2-</sub> (1900) **
$J = \frac{3}{2}$	<b>N</b> <sub>3/2+</sub> (1900) ***	<b>N</b> <sub>3/2-</sub> (1875) **	$\Delta$ <sub>3/2+</sub> (1940) ***	$\Delta$ <sub>3/2-</sub> (1990) **
$J = \frac{5}{2}$	<b>N</b> <sub>5/2+</sub> (1880) **	<b>N</b> <sub>5/2-</sub> (2060) **	$\Delta$ <sub>5/2+</sub> (1940) ****	$\Delta$ <sub>5/2-</sub> (1930) ***
$J = \frac{7}{2}$	<b>N</b> <sub>7/2+</sub> (1980) ***	<b>N</b> <sub>7/2-</sub> (2170) *****	$\Delta$ <sub>7/2+</sub> (1920) *****	<b>Δ</b> <sub>7/2-</sub> (2200) *
$J = \frac{9}{2}$	<b>N</b> <sub>9/2+</sub> (2220) *****	<b>N</b> <sub>9/2-</sub> (2250) *****	$\Delta$ <sub>9/2+</sub> (2300) **	$\Delta$ <sub>9/2-</sub> (2400) **

$J = \frac{5}{2}$	<b>N</b> <sub>5/2+</sub> (2090) **	<b>N</b> <sub>5/2-</sub> (2060) **	$\Delta$ <sub>5/2+</sub> (1940) ****	$\Delta$ <sub>5/2-</sub> (1930) ***
$J = \frac{7}{2}$	<b>N</b> <sub>7/2+</sub> (2100) **	<b>N</b> <sub>7/2-</sub> (2150) ****	$\Delta$ <sub>7/2+</sub> (1920) ****	<b>Δ</b> <sub>7/2-</sub> (2200) *
$J = \frac{9}{2}$	<b>N</b> <sub>9/2+</sub> (2220) *****	<b>N</b> <sub>9/2-</sub> (2250) *****	$\Delta$ <sub>9/2+</sub> (2300) **	$\Delta$ <sub>9/2-</sub> (2400) <sup>a</sup> **

# First double polarization data: helicity asymmetry in $\gamma p \rightarrow \pi^0 p$



**Bonn-Gatchina, SAID (SN11), MAID      Bonn-Gatchina (fitted), SAID (SN11), SAID(CM12)**

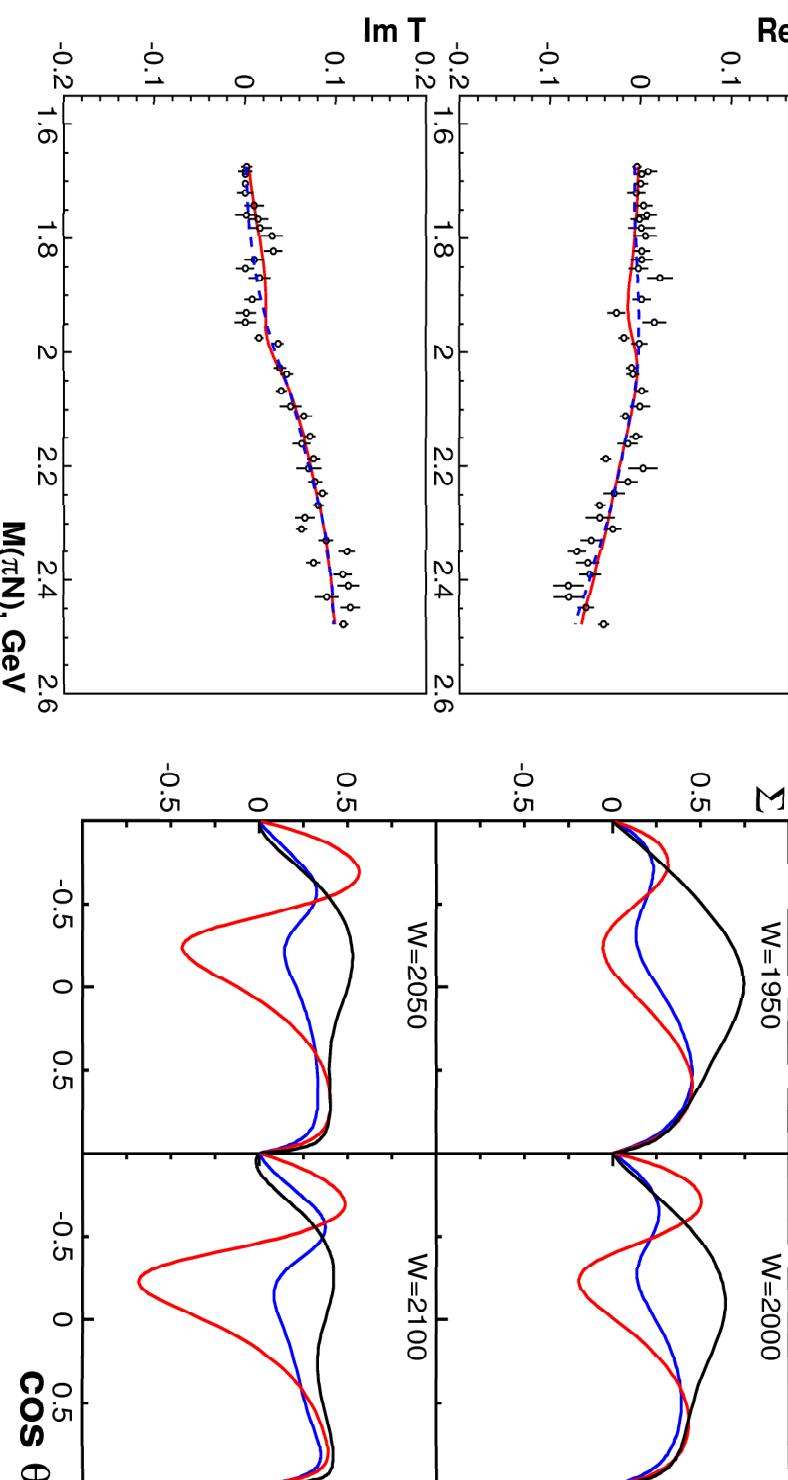
## Pole position of $N(1990)7/2^+$

$N(2190)7/2^- : M_{pole} = 2150 \pm 25, \quad \Gamma_{pole} = 330 \pm 30$

State	Solution 1	$A(\frac{1}{2})/A(\frac{3}{2})$	Solution 2	$A(\frac{1}{2})/A(\frac{3}{2})$
$N(1990)\frac{7}{2}^+$	Re $1980 \pm 25$	$15/14^\circ$	$2100 \pm 30$	$76/50^\circ$
*	-2Im $180 \pm 30$	$28/3^\circ$	$300 \pm 60$	$78/45^\circ$

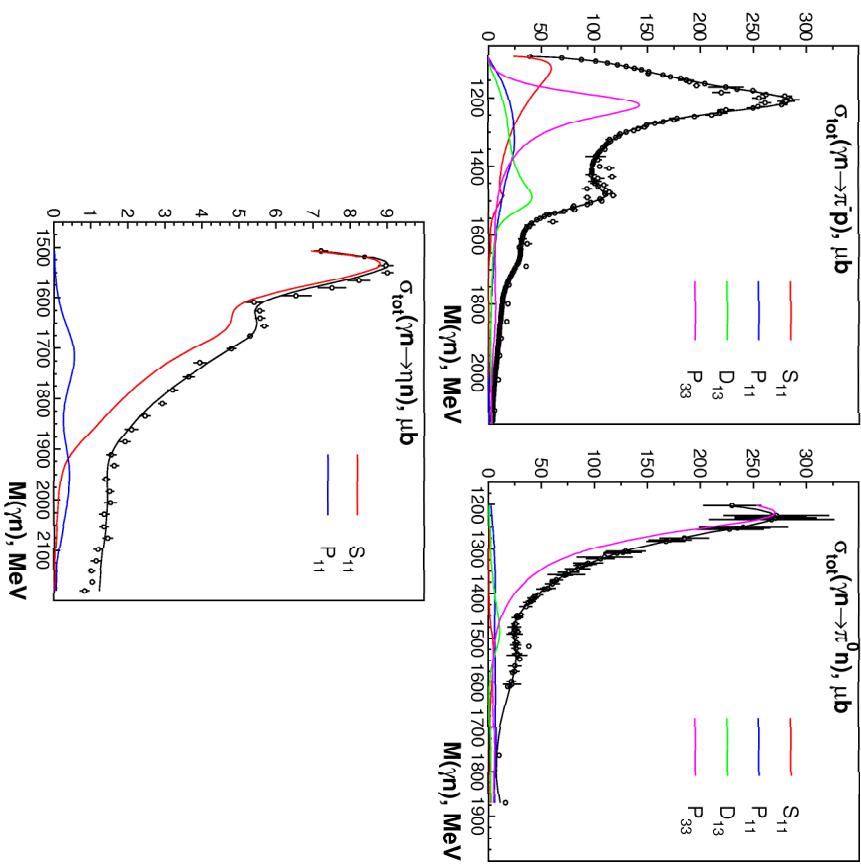
Can be resolved by fitting the beam asymmetry data on  $\gamma p \rightarrow K\Lambda$

**BG2011-01** **BG2011-02** **KAON-MAID**



# Analysis of $\pi^0$ and $\eta$ photoproduction off neutron

$\gamma n \rightarrow \pi^- p$	$N_{\text{data}}$	$\chi^2_0$	$\chi^2_f$
$d\sigma/d\Omega$	<b>1298</b>	<b>2.84</b>	<b>2.32</b>
$d\sigma/d\Omega$	<b>529</b>	<b>3.16</b>	<b>3.08</b>
$P$	<b>20</b>	<b>3.22</b>	<b>3.17</b>
$\Sigma$	<b>316</b>	<b>3.74</b>	<b>3.08</b>
$T$	<b>105</b>	<b>4.96</b>	<b>3.18</b>
<hr/>			
$\pi^- p \rightarrow \gamma n$			
$d\sigma/d\Omega$	<b>495</b>	<b>1.65</b>	<b>1.53</b>
$P$	<b>55</b>	<b>4.59</b>	<b>3.11</b>
<hr/>			
$\gamma d \rightarrow \pi^0 n(p)$			
$d\sigma/d\Omega$	<b>147</b>	<b>3.14</b>	<b>2.98</b>
$\Sigma$	<b>216</b>	<b>2.82</b>	<b>1.90</b>
<hr/>			
$\gamma d \rightarrow \eta n(p)$	$N_{\text{data}}$	$\chi^2_0$	$\chi^2_f$
$d\sigma/d\Omega$	<b>330</b>	<b>1.57</b>	<b>1.40</b>
$\Sigma$	<b>88</b>	<b>2.42</b>	<b>2.17</b>



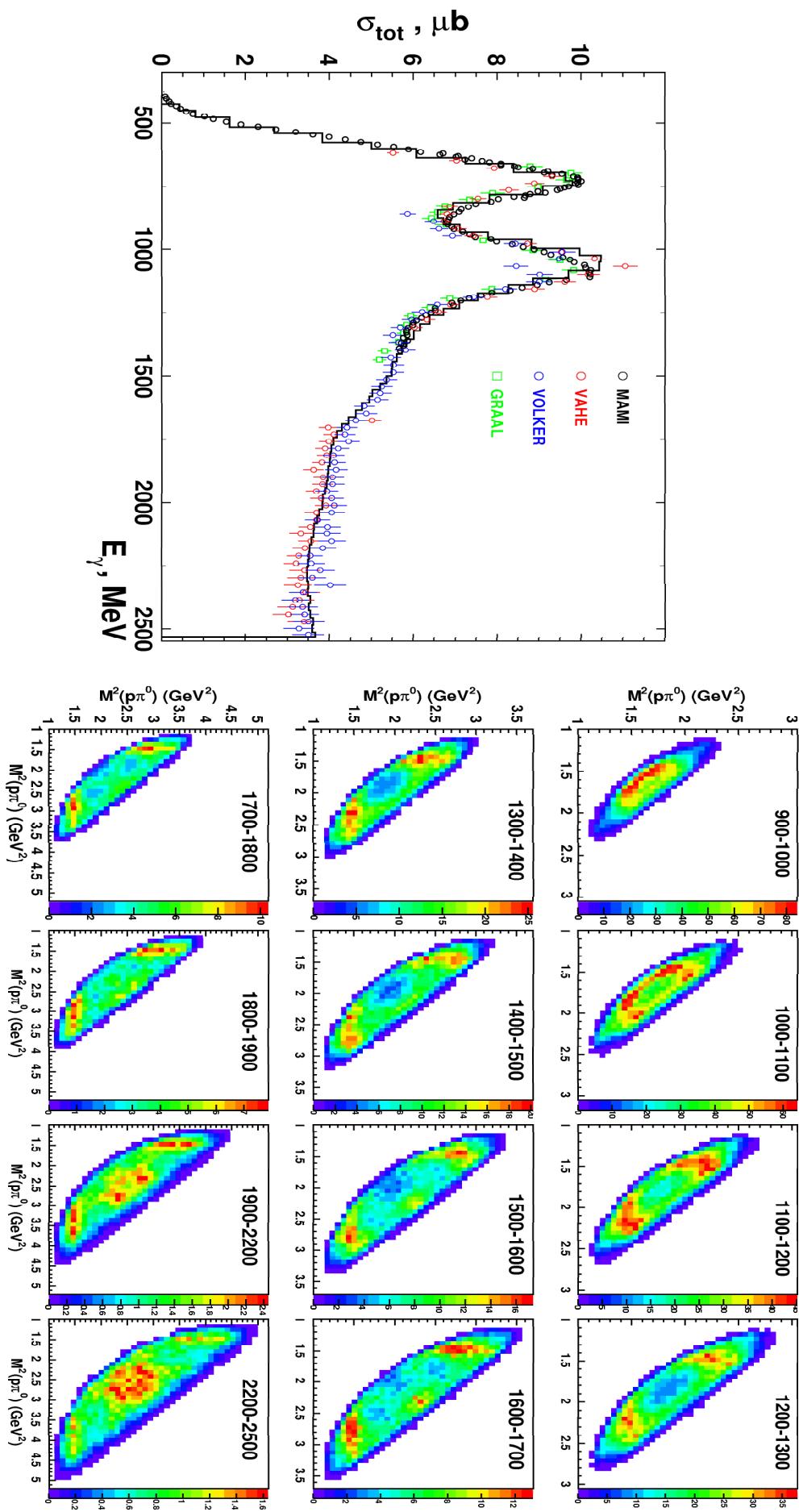
### $\gamma n$ BW helicity couplings (GeV $^{-1/2}$ 10 $^{-3}$ )

	$ A_{BW}^{1/2} $	$ A_{BW}^{3/2} $		$ A_{BW}^{1/2} $	$ A_{BW}^{3/2} $
$N(1535)1/2^-$	<b>-93±11</b>		$N(1440)1/2^+$	<b>43±12</b>	
<b>GB12</b>	<b>-58±6</b>	<b>(-85±15)</b>	<b>GB12</b>	<b>48±4</b>	
<b>SN11</b>	<b>-60±3</b>		<b>SN11</b>	<b>45±15</b>	
<b>MAID</b>	<b>-51</b>		<b>MAID</b>	<b>54</b>	
<b>PDG12</b>	<b>-46±27</b>		<b>PDG12</b>	<b>40±10</b>	
$N(1650)1/2^-$	<b>25±20</b>		$N(1710)1/2^+$	<b>-40±20</b>	
<b>GB12</b>	<b>-40±10</b>	<b>(?±?)</b>	<b>GB12</b>		
<b>SN11</b>	<b>-26±8</b>		<b>SN11</b>		
<b>MAID</b>	<b>9</b>		<b>MAID</b>		
<b>PDG12</b>	<b>-15±21</b>		<b>PDG12</b>	<b>2±14</b>	
$N(1520)3/2^-$	<b>-49±8</b>	<b>-113±12</b>	$N(1720)3/2^+$	<b>-80±50</b>	<b>-140±65</b>
<b>GB12</b>	<b>-46±6</b>	<b>-115±5</b>	<b>GB12</b>		
<b>SN11</b>	<b>-47±2</b>	<b>-125±2</b>	<b>SN11</b>	<b>ambiguous</b>	<b>ambiguous</b>
<b>MAID</b>	<b>-77</b>	<b>-154</b>	<b>MAID</b>	<b>-21±4</b>	<b>-38±7</b>
<b>PDG12</b>	<b>-59±9</b>	<b>-139±11</b>	<b>PDG12</b>	<b>-3</b>	<b>-31</b>
<b>PDG12</b>			<b>PDG12</b>	<b>4±15</b>	<b>-10±20</b>
$N(1675)5/2^-$	<b>-60±7</b>	<b>-88±10</b>	$N(1680)5/2^+$	<b>34±6</b>	<b>-44±9</b>
<b>GB12</b>	<b>-58±2</b>	<b>-80±5</b>	<b>GB12</b>	<b>26±4</b>	<b>-29±2</b>
<b>SN11</b>	<b>-42±2</b>	<b>-60±2</b>	<b>SN11</b>	<b>50±4</b>	<b>-47±2</b>
<b>MAID</b>	<b>-62</b>	<b>-84</b>	<b>MAID</b>	<b>28</b>	<b>-38</b>
<b>PDG12</b>	<b>-43±12</b>	<b>-58±13</b>	<b>PDG12</b>	<b>29±10</b>	<b>-33±9</b>

**Solution BG2011-02 with  $N(1990)7/2^+$  at a mass around 2100 MeV provides a notably better**

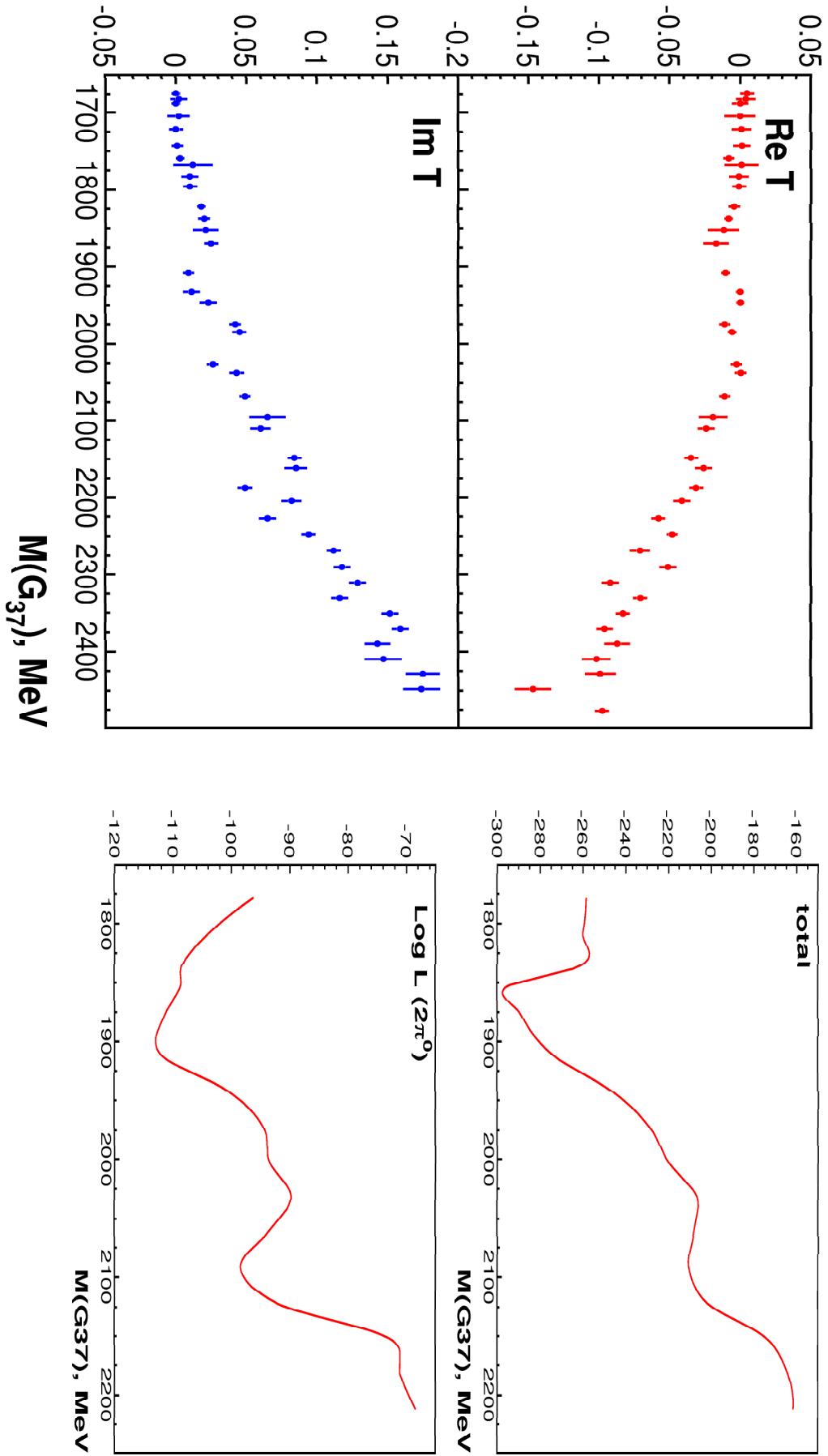
**description of the data**

# New data on $\gamma p \rightarrow \pi^0 \pi^0 p$



## $\Delta(2200)(7/2^-)$ state

$\Delta(1950)7/2^+: M = 1915 \pm 6, \quad \Gamma_{pole} = 246 \pm 10$



## Summary

- The new N/D-based method is developed and applied to the analysis of the high statistic data on production of meson and baryon resonances.
  - The new analysis confirmed the result of the K-matrix analysis for high mass states and provides a better description of low energy part.
  - The new data on  $\gamma\eta$  initial state, double polarization data from CB-ELSA and new data on  $2\pi^0$  and  $\eta\pi^0$  photoproduction are included in the data base.
  - The  $\gamma\eta$  data favor solution BG2011-02 with mass of  $N(1990)^7/2^+$  at 2100 MeV. The new data on  $\gamma p \rightarrow 2\pi^0 p$  provide an indication for  $\Delta(7/2^-)$  with the mass around 1900 MeV.
- Both results support parity doublet idea.