



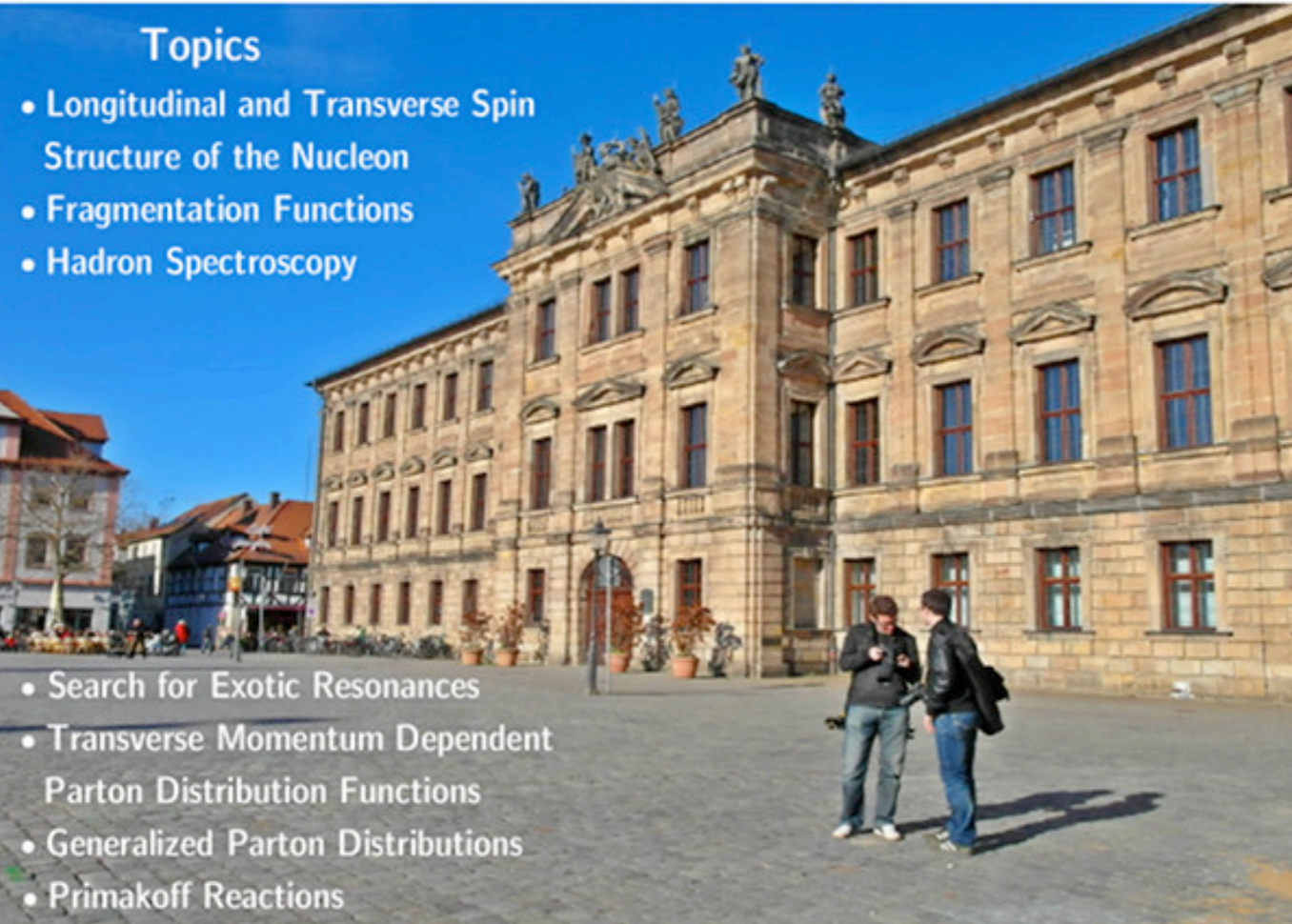
# IWHSS 2013

International Workshop on Hadron  
Structure and Spectroscopy 2013,  
Erlangen, Germany, 22-24 July



## Topics

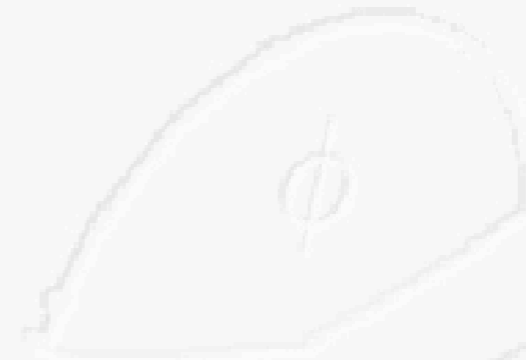
- Longitudinal and Transverse Spin  
Structure of the Nucleon
- Fragmentation Functions
- Hadron Spectroscopy
- Search for Exotic Resonances
- Transverse Momentum Dependent  
Parton Distribution Functions
- Generalized Parton Distributions
- Primakoff Reactions



# Experimental review of transverse-spin physics

# Transverse spin - a bumpy road

- largely neglected

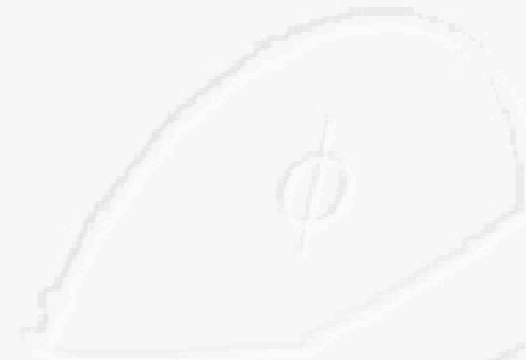


# Transverse spin - a bumpy road

- largely neglected
- "transverse spin" structure function  $g_2$  small (vanishing in parton model)



$\vec{p}_{had}$



1977

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$$A_N \propto \alpha_S \frac{m_q}{Q^2}$$

VOLUME 41, NUMBER 25

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18 DECEMBER 1978

**Transverse Quark Polarization in Large- $p_T$  Reactions,  $e^+e^-$  Jets,  
and Leptoproduction: A Test of Quantum Chromodynamics**

G. L. Kane

*Physics Department, University of Michigan, Ann Arbor, Michigan 48109*

and

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*Physics Department, Michigan State University, East Lansing, Michigan 48823*

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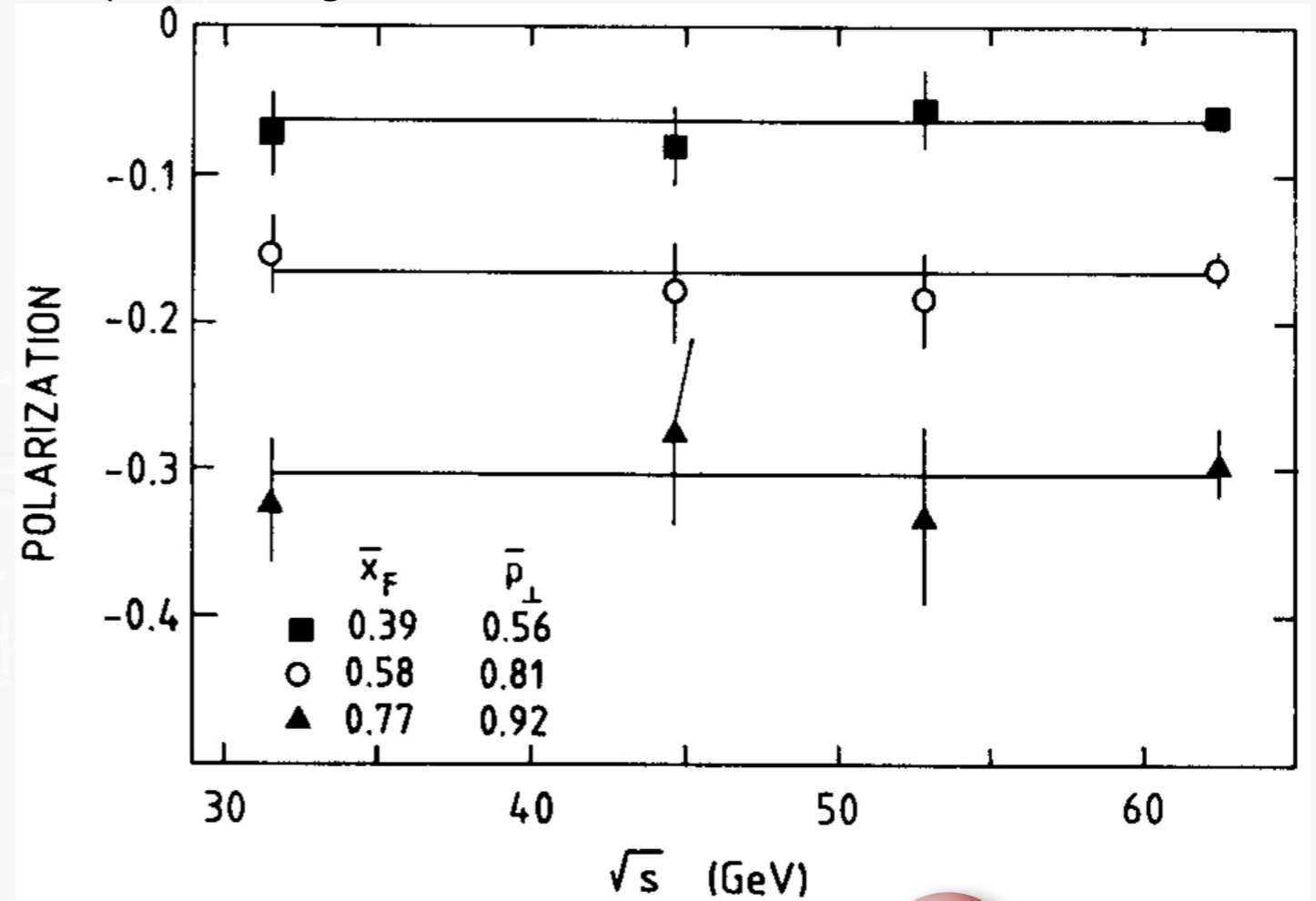
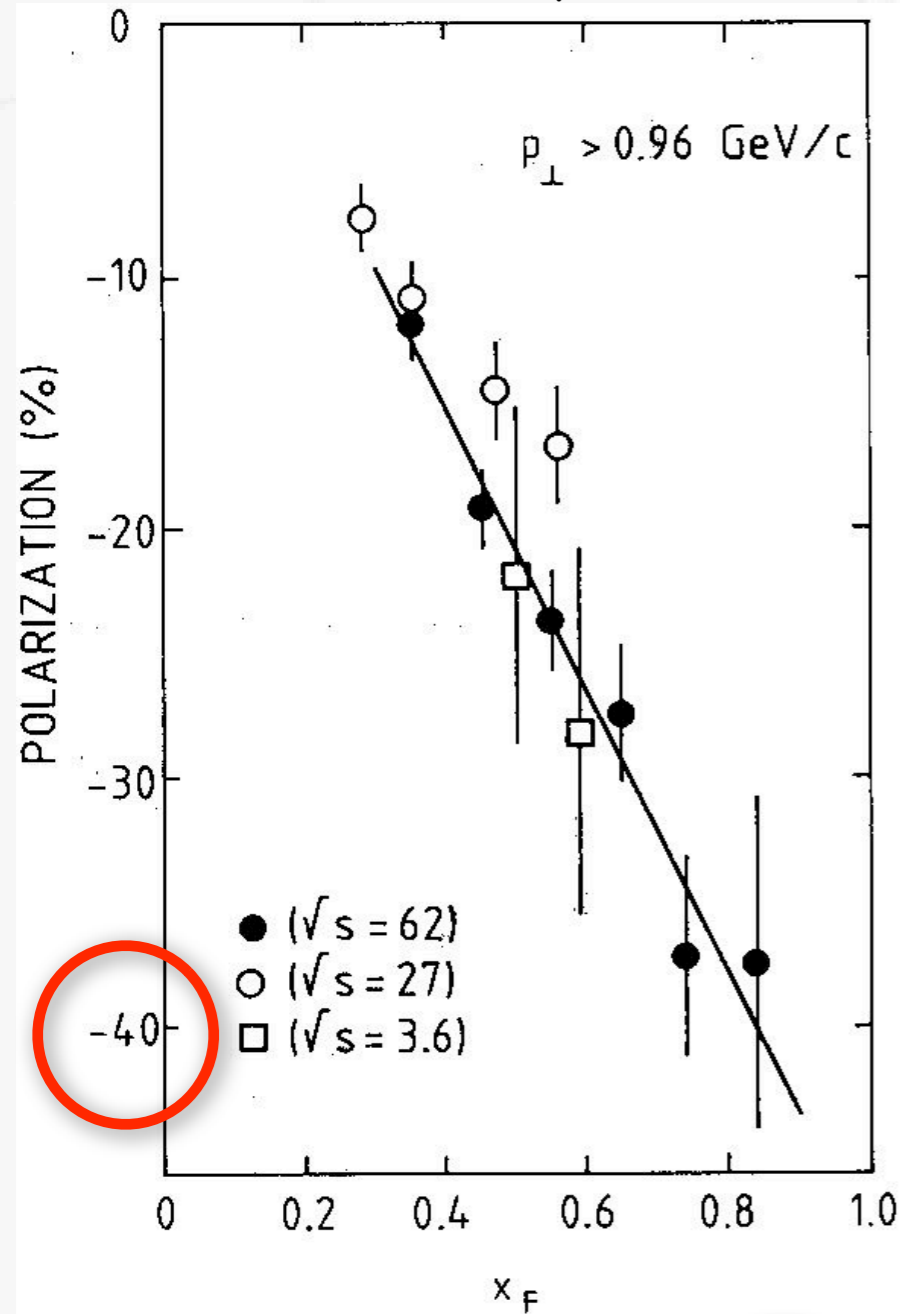
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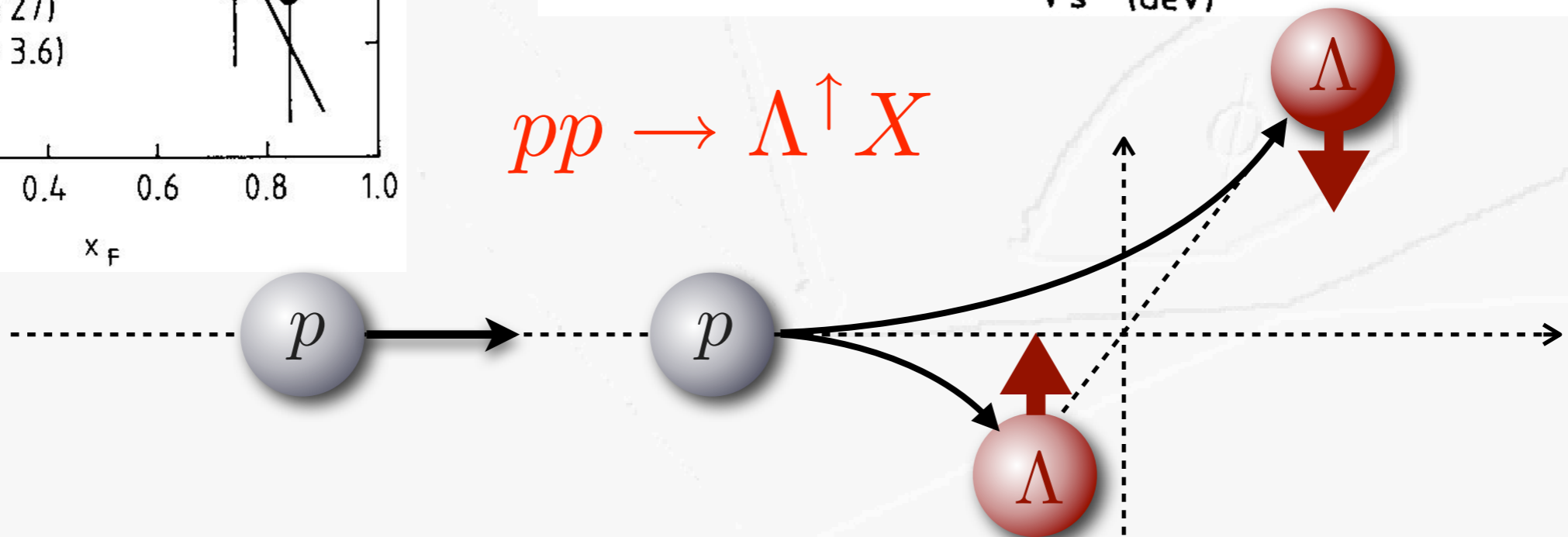
*Physics Department, Michigan State University, East Lansing, Michigan 48823*

# Nature does not seem to cooperate

Comprehensive review of data by A.D. Panagiotou (Int. J. Mod. Phys. A5 (1990) 1197)



$$pp \rightarrow \Lambda^{\uparrow} X$$

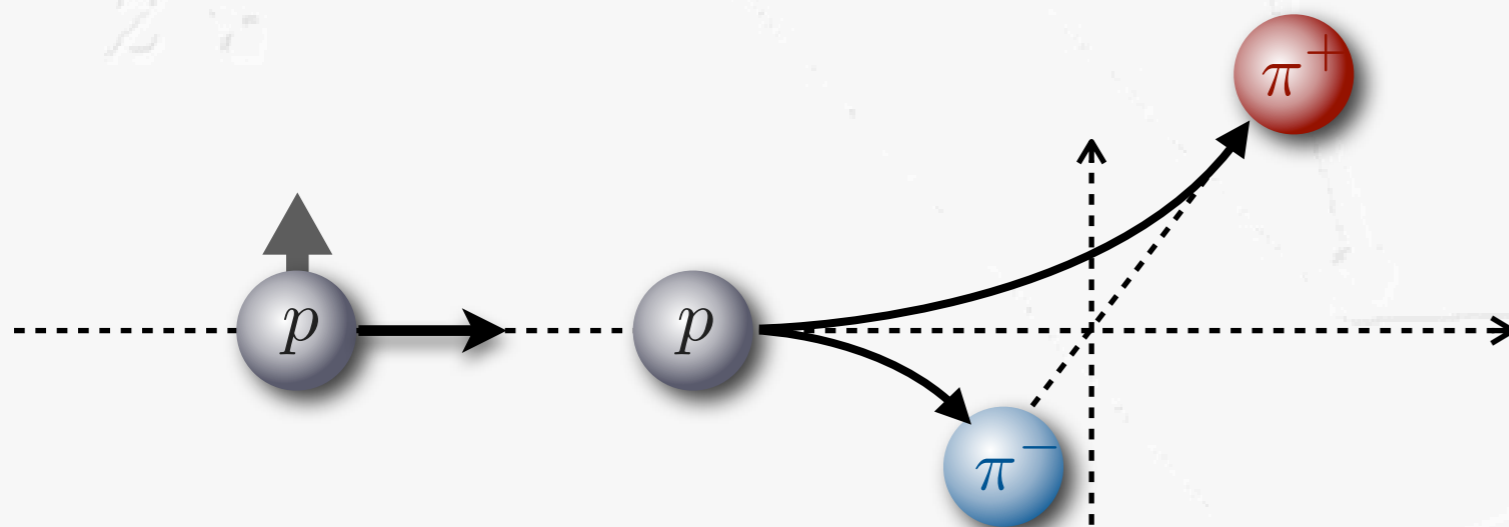
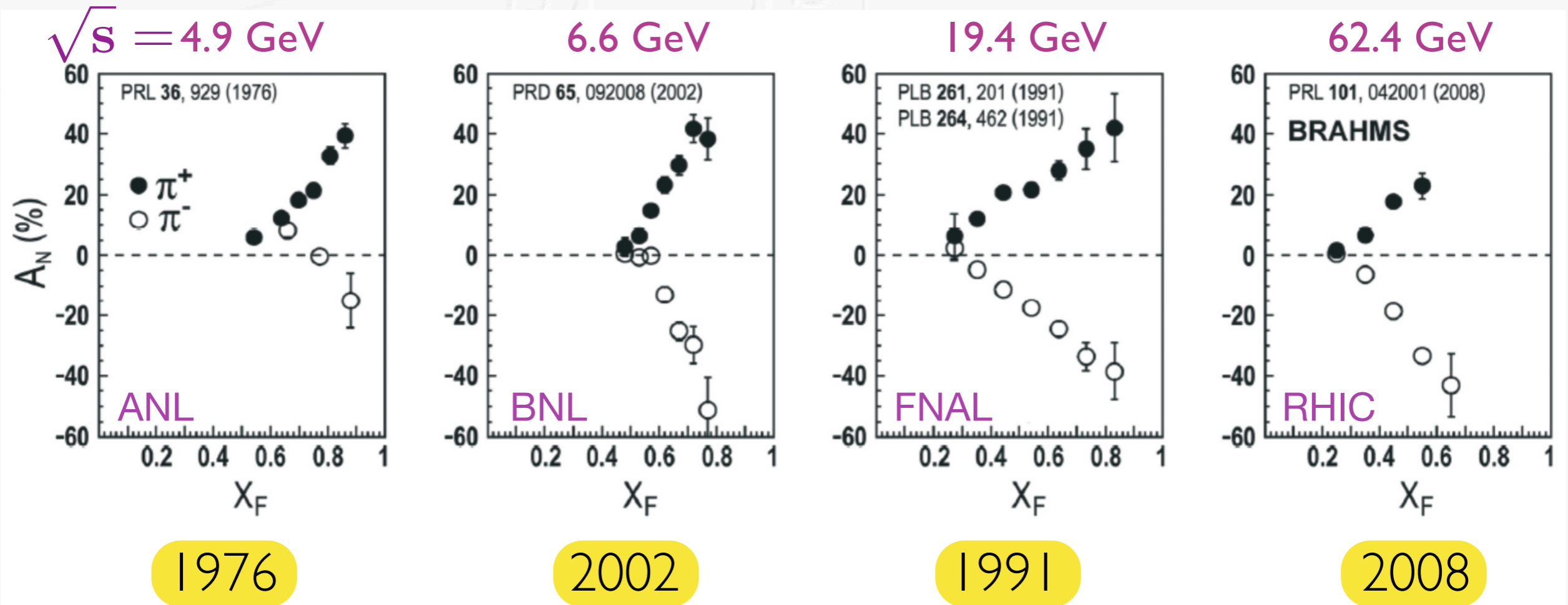


... also not for pion production ...

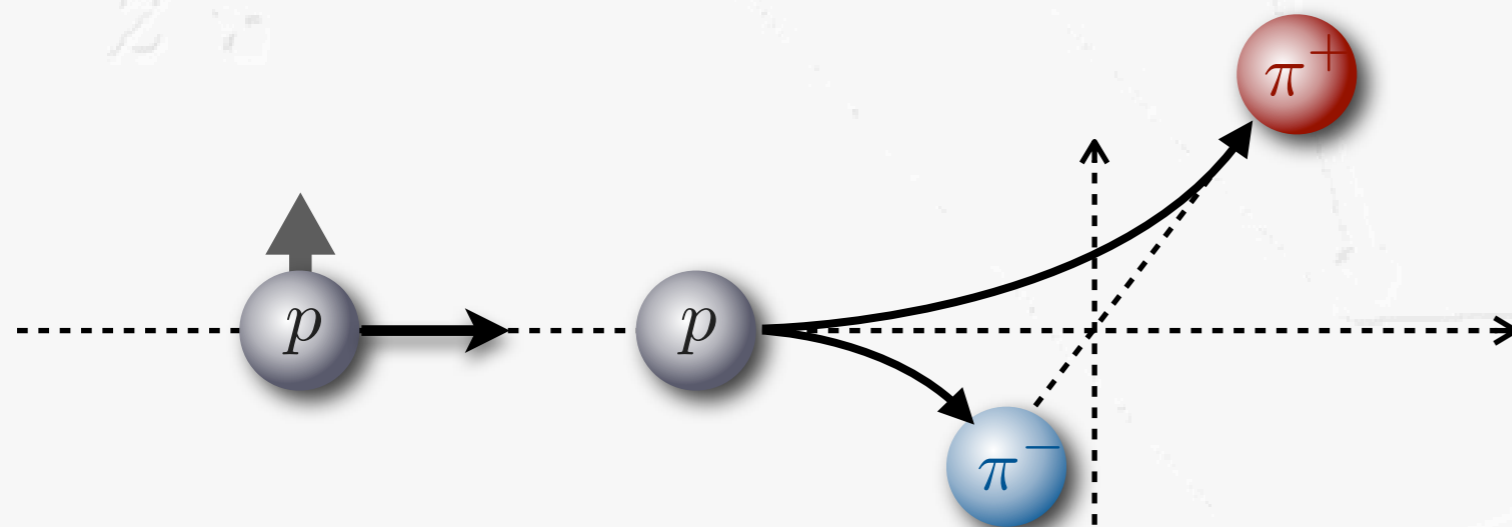
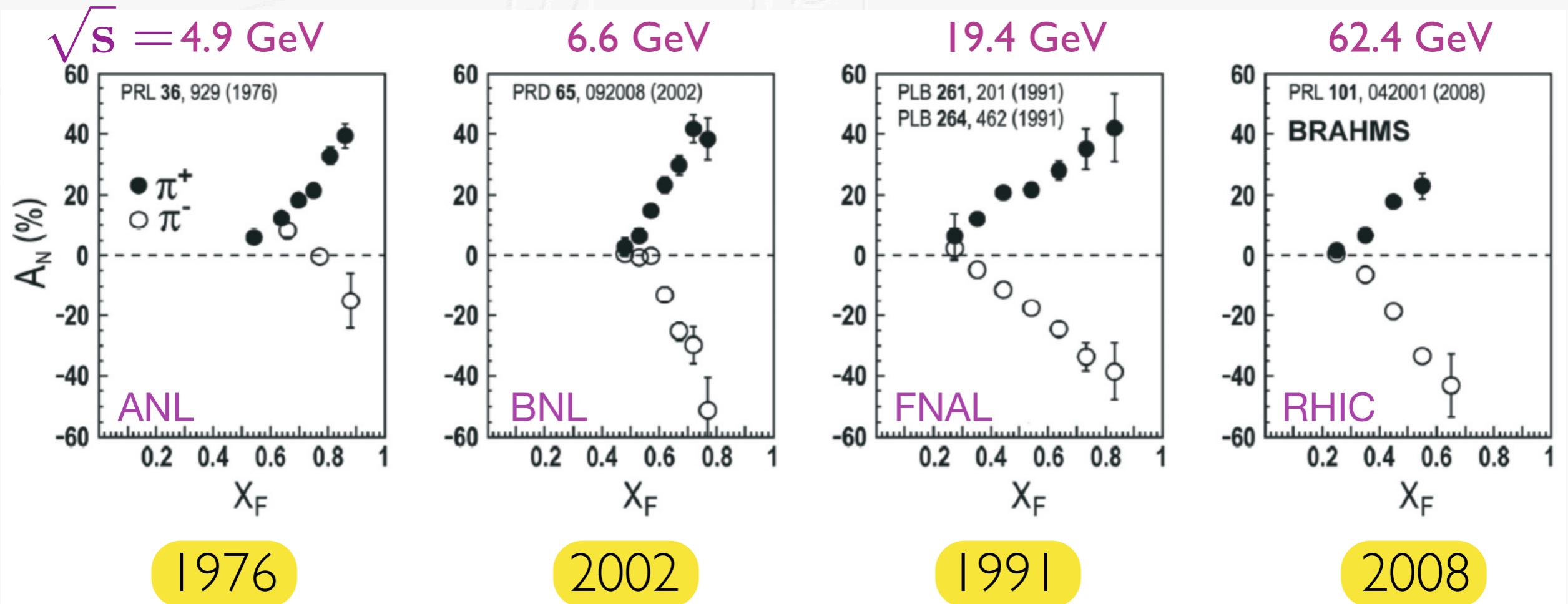




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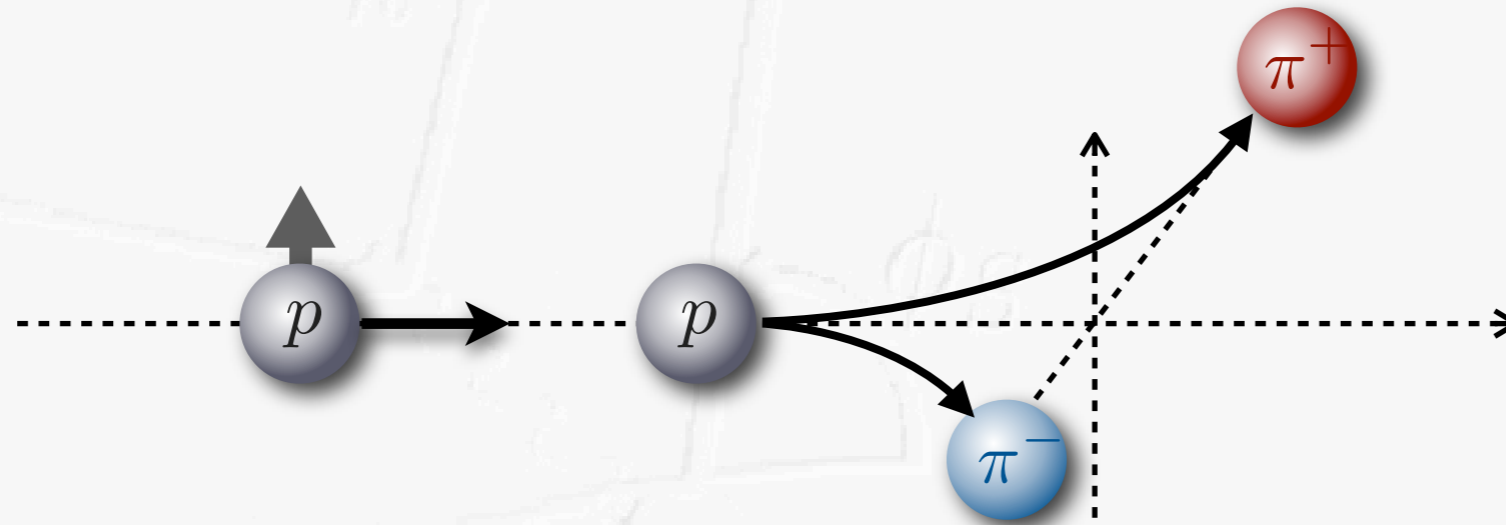


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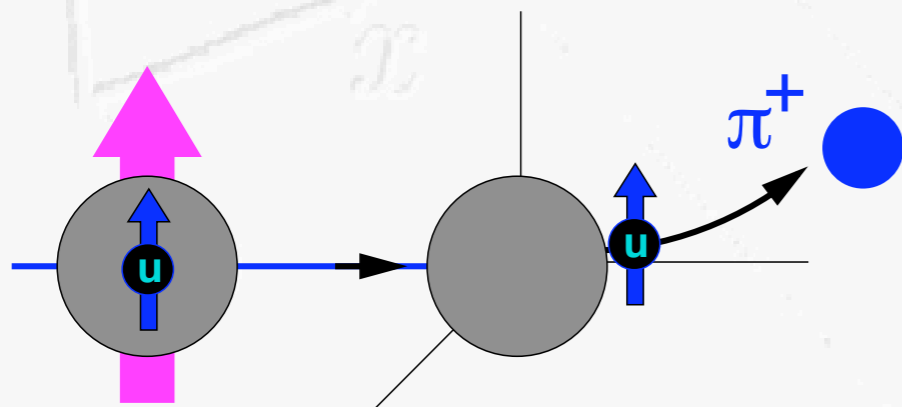


- large left-right asymmetries persist even at RHIC energies

# What's the origin of these SSA?



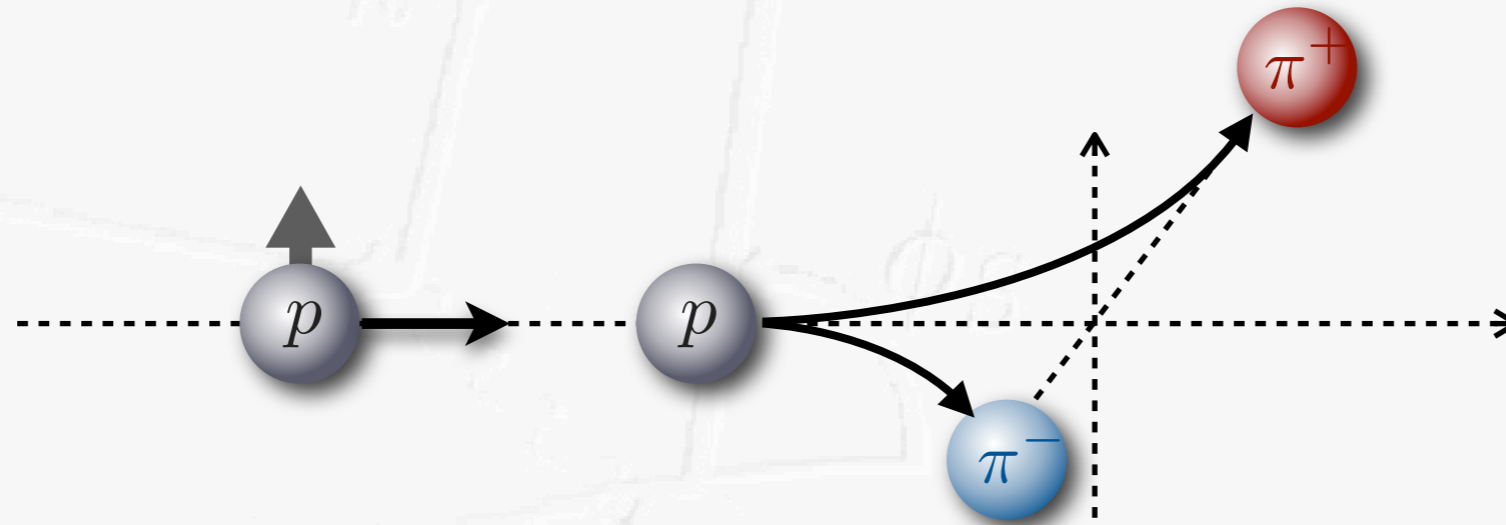
- fragmentation effect?



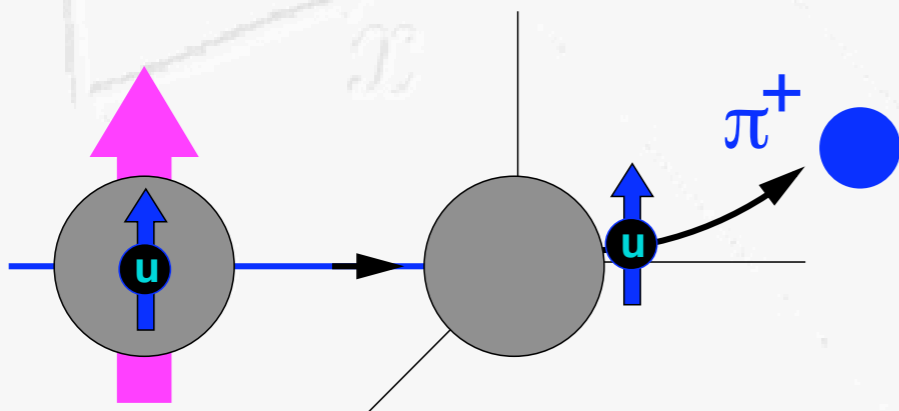
[J.C. Collins, NPB 396 (1993) 161]

- correlating transverse quark spin with transverse momentum

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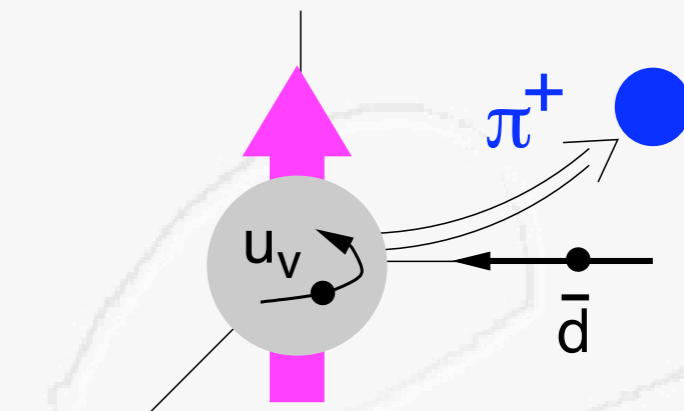


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[J.C. Collins, NPB 396 (1993) 161]

- quark-distribution effect?

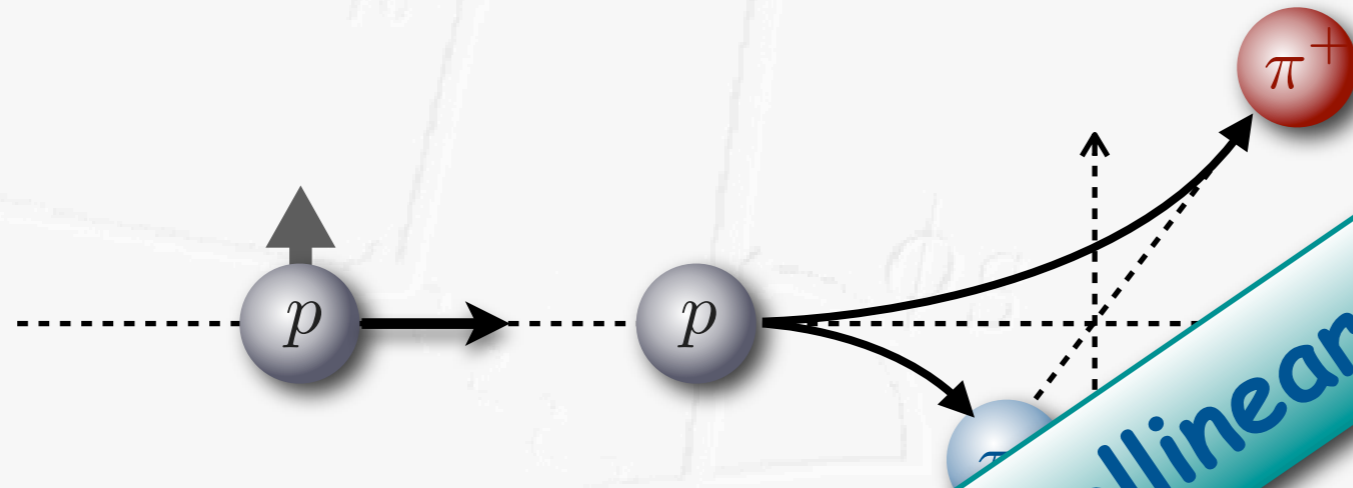


[D.W. Sivers, PRD 41 (1990) 83]

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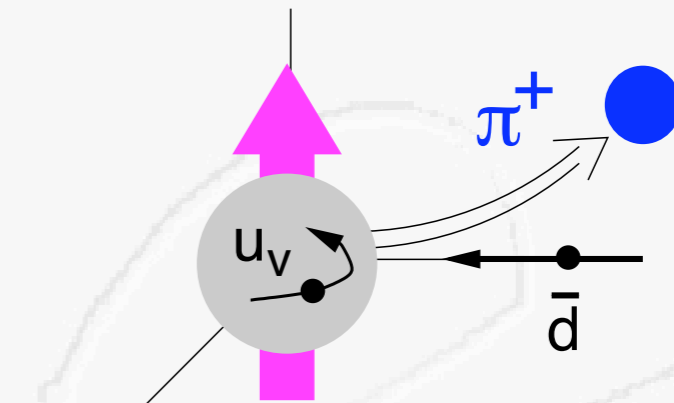
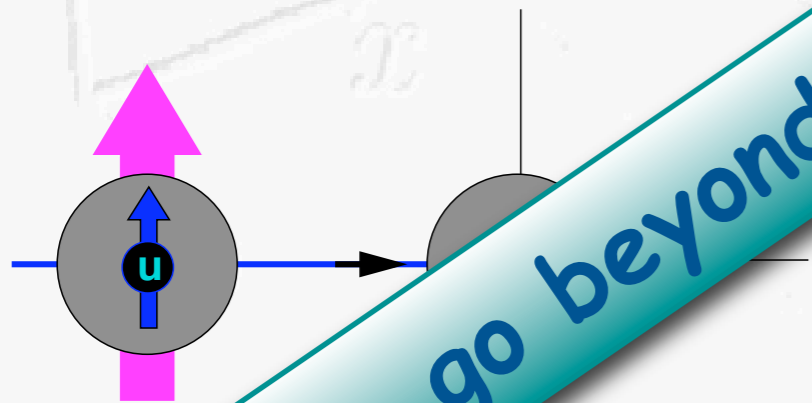
- correlating transverse quark momentum with transverse spin of nucleon

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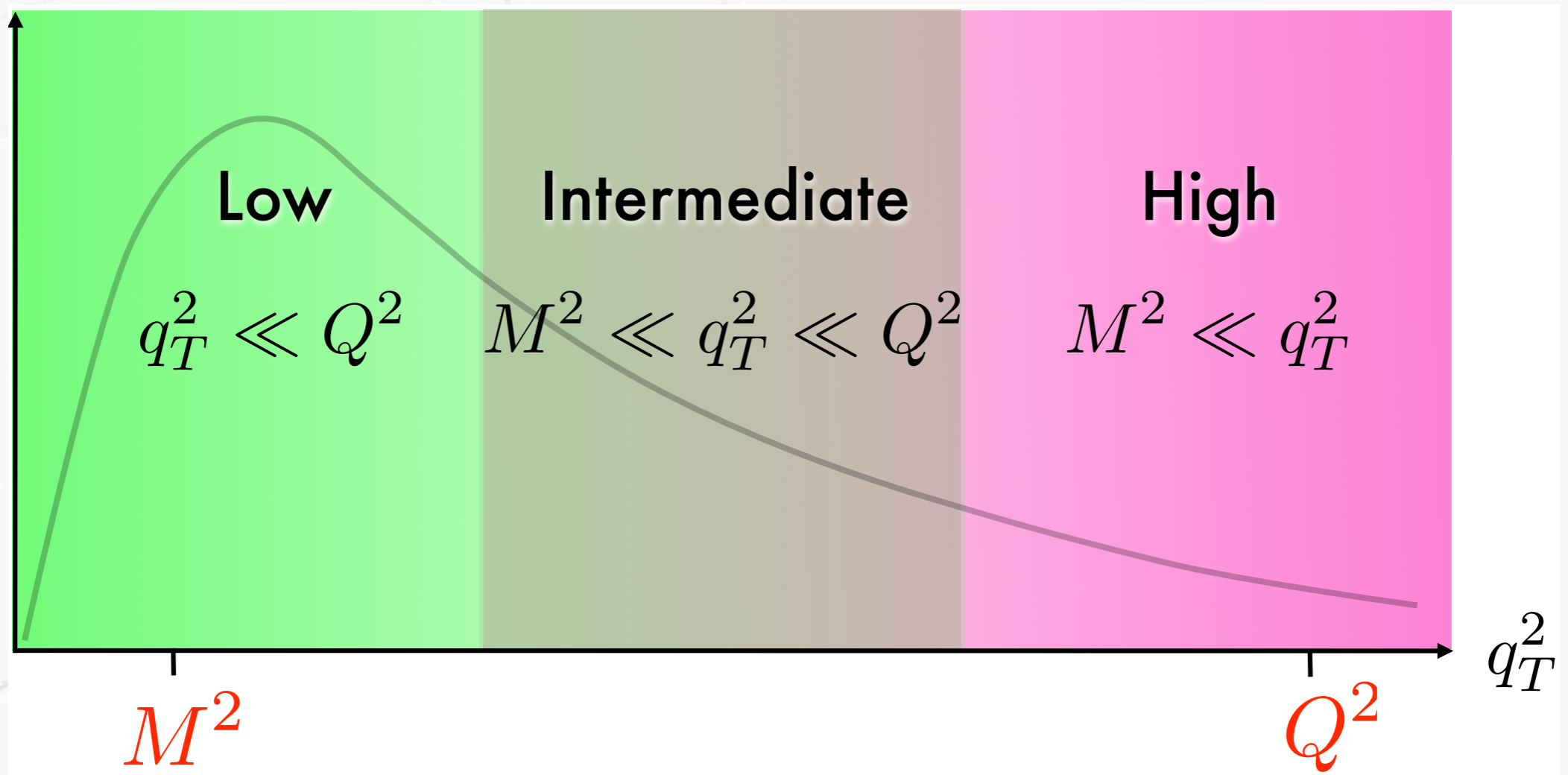
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relating transverse quark spin  
with transverse momentum

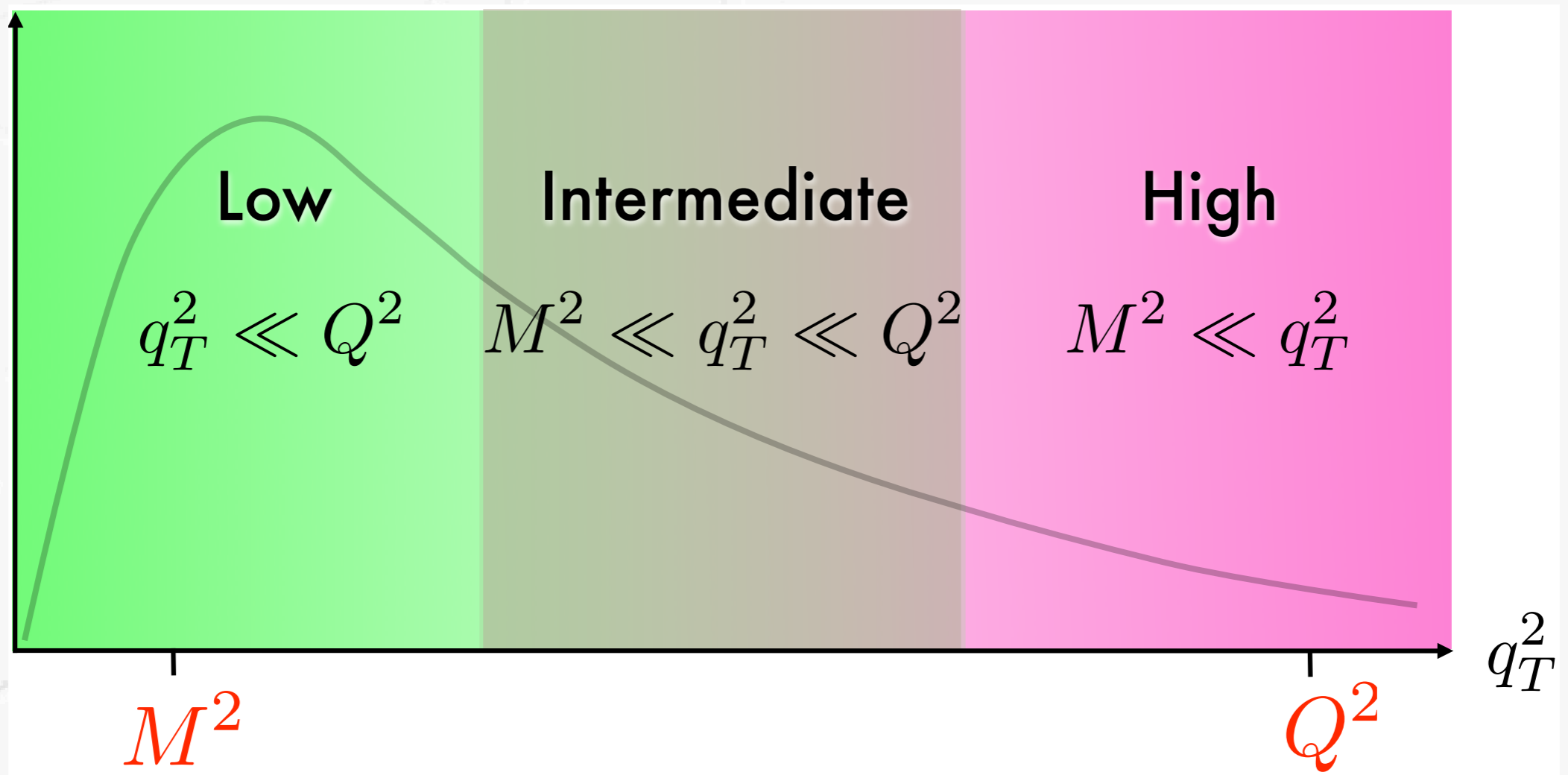
- correlating transverse quark momentum with transverse spin of nucleon

need to go beyond leading-twist collinear factorization

# going beyond leading-twist collinear approach



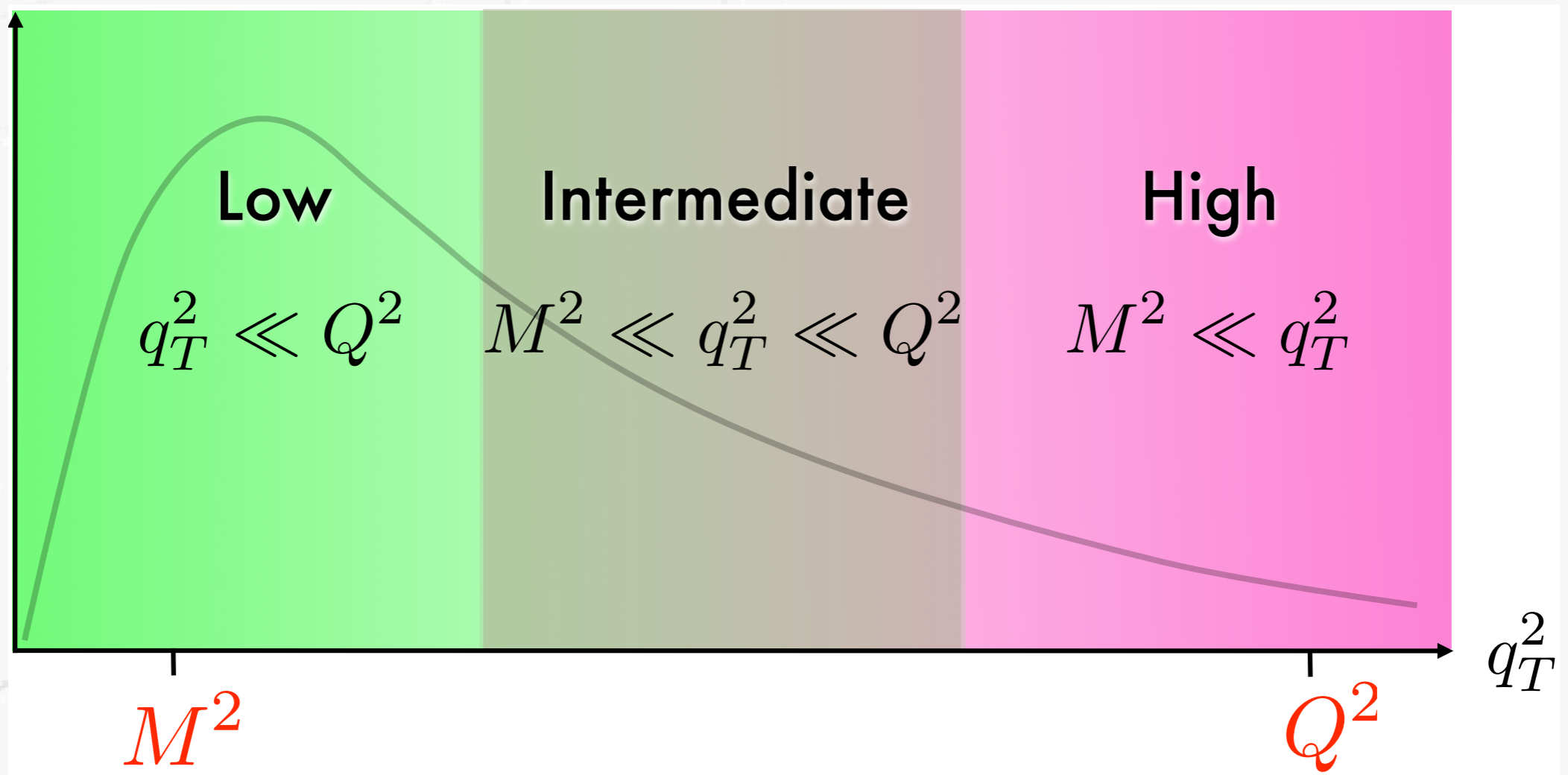
# going beyond leading-twist collinear approach



TMD  
factorization

TMD: transverse-momentum-dependent distributions

# going beyond leading-twist collinear approach



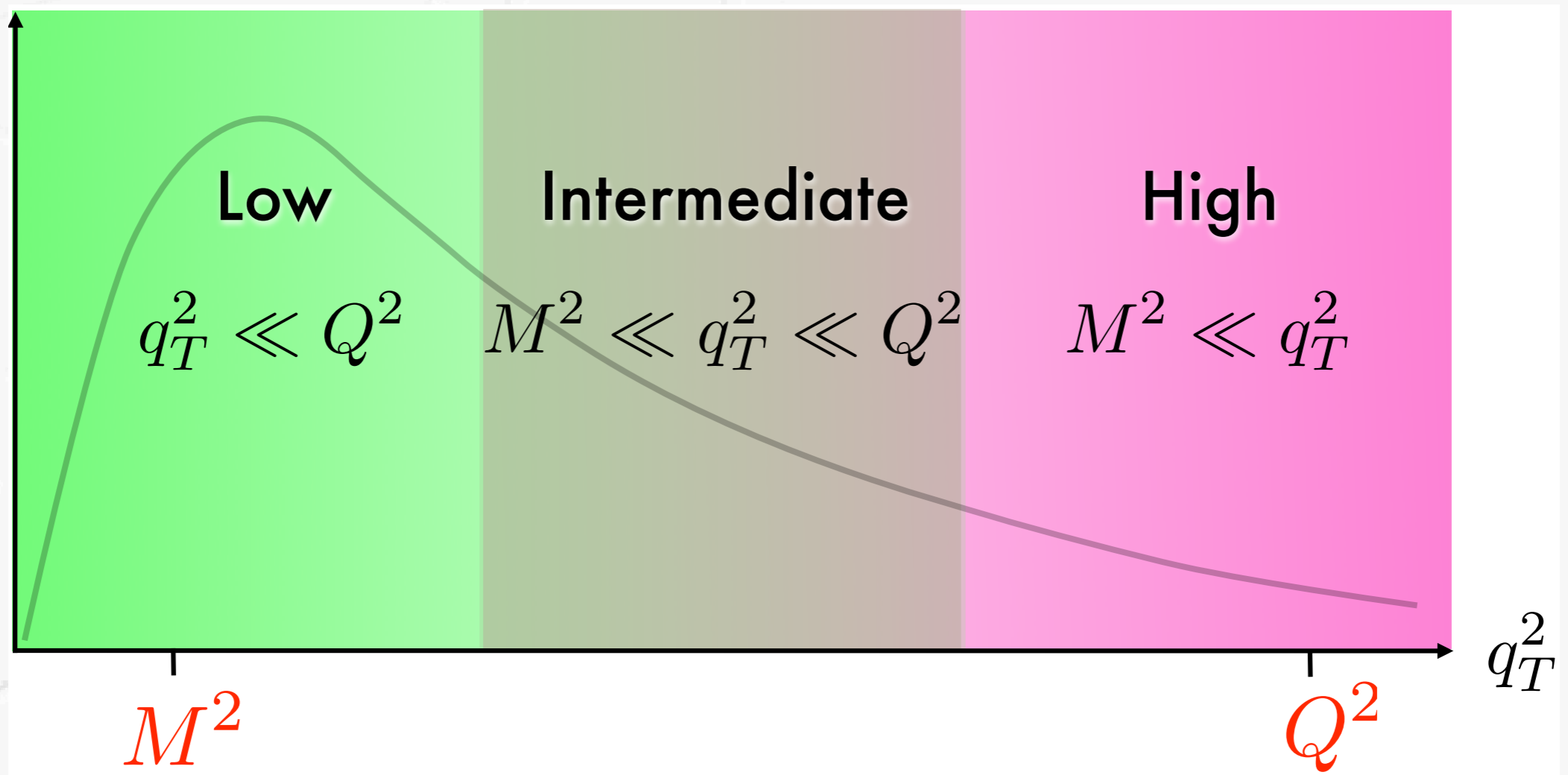
TMD  
factorization

twist-3 collinear  
factorization

TMD: transverse-momentum-dependent distributions



# going beyond leading-twist collinear approach



TMD  
factorization

overlap  
region

twist-3 collinear  
factorization

TMD: transverse-momentum-dependent distributions

# Spin-momentum structure of the nucleon

$$\frac{1}{2} \text{Tr} \left[ (\gamma^+ + \lambda \gamma^+ \gamma_5) \Phi \right] = \frac{1}{2} \left[ f_1 + S^i \epsilon^{ij} k^j \frac{1}{m} f_{1T}^\perp + \lambda \Lambda g_1 + \lambda S^i k^i \frac{1}{m} g_{1T} \right]$$

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quark pol.

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

nucleon pol.

- each TMD describes a particular spin-momentum correlation
- functions in black survive integration over transverse momentum
- functions in green box are chirally odd
- functions in red are naive T-odd

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**Boer-Mulders**

**pretzelosity**

**Sivers**

**worm-gear**

**transversity**

details M. Radici, M. Boglione

Transverse spin  $|\uparrow\downarrow\rangle = \frac{1}{2} (|+\rangle \pm |-\rangle)$

$$\langle\uparrow|\hat{O}|\uparrow\rangle - \langle\downarrow|\hat{O}|\downarrow\rangle \propto \langle+|\hat{O}|-\rangle - \langle-|\hat{O}|+\rangle$$

**transverse-spin asymmetries involve helicity flip**



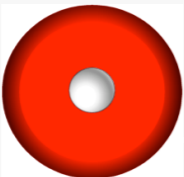
$\vec{p}_{had}$

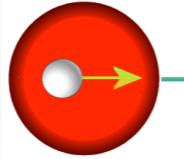
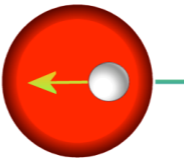


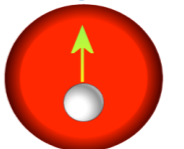
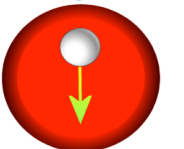
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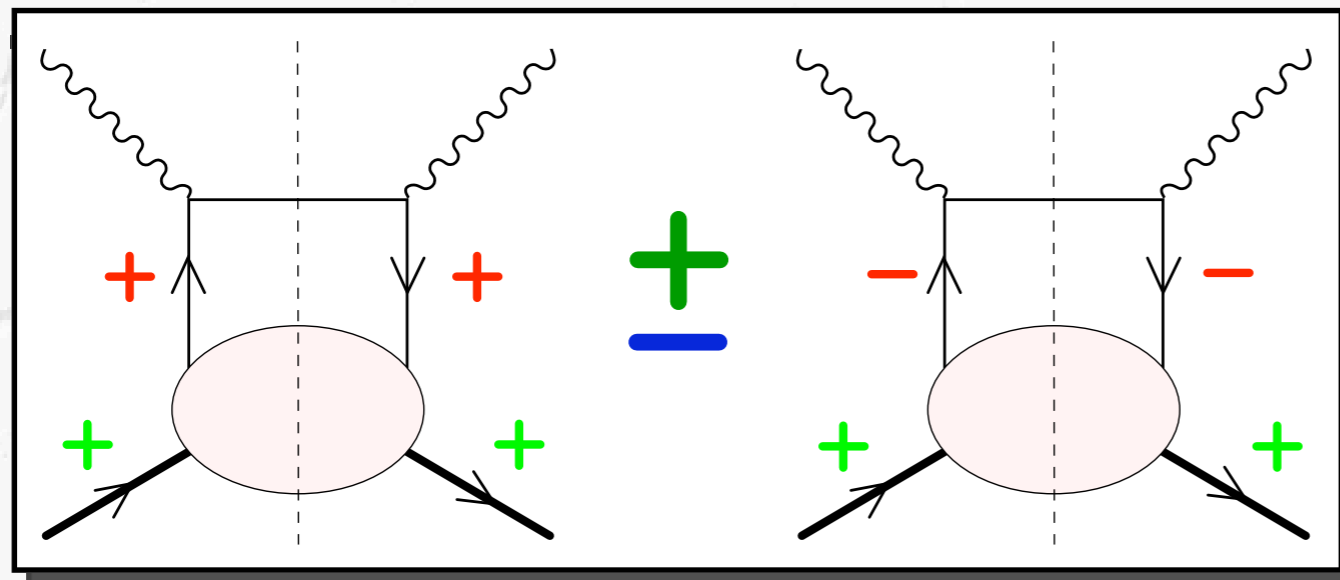
$$\langle \uparrow | \hat{O} | \uparrow \rangle - \langle \downarrow | \hat{O} | \downarrow \rangle \propto \langle + | \hat{O} | - \rangle - \langle - | \hat{O} | + \rangle$$

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PDFs:  $f_1^q =$  

$g_1^q =$    $-$  

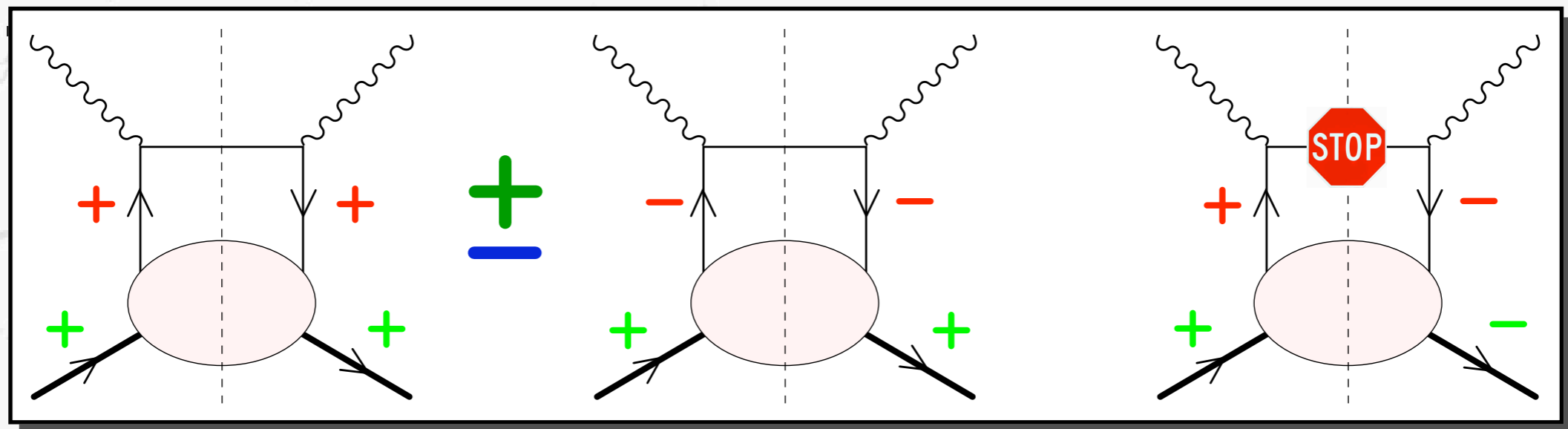
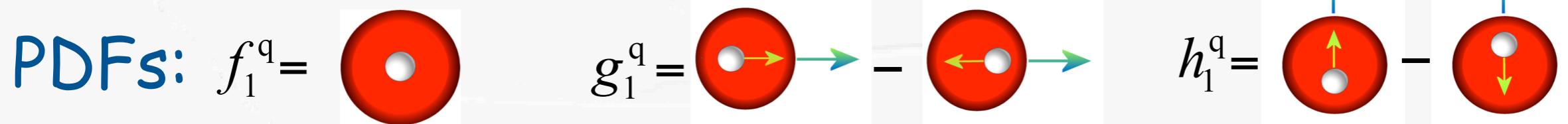
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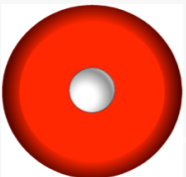
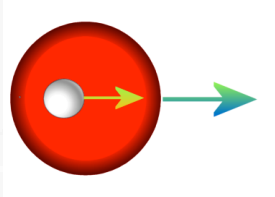
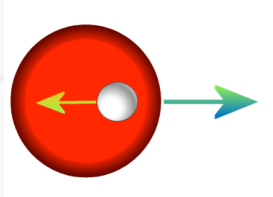
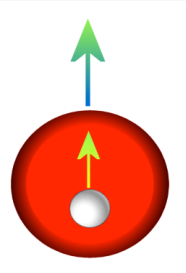
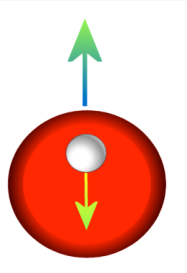
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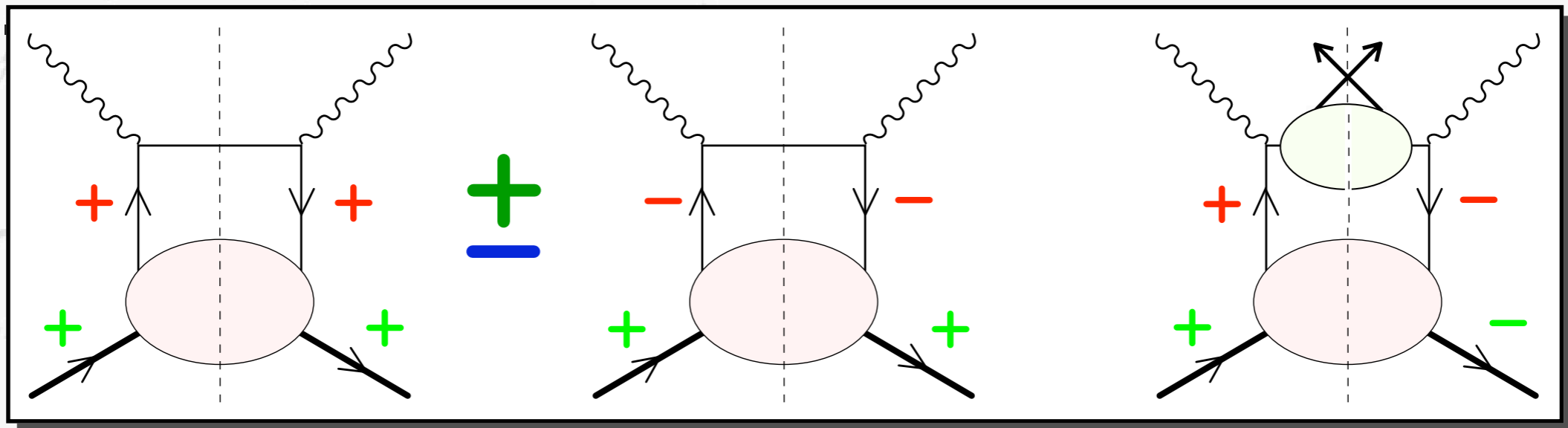


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transverse-spin asymmetries involve helicity flip

PDFs:  $f_1^q =$    $g_1^q =$    $-$    $h_1^q =$    $-$  



need to couple to chiral-odd fragmentation function:

- transverse spin transfer (polarized final-state hadron)
- 2-hadron fragmentation
- Collins fragmentation

# TMD fragmentation functions

quark pol.

	U	L	T
U	$D_1$		$H_1^\perp$
L		$G_1$	$H_{1L}^\perp$
T	$D_{1T}^\perp$	$G_{1T}^\perp$	$H_1 H_{1T}^\perp$

hadron pol.



# TMD fragmentation functions

hadron pol.

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→ relevant for unpolarized final state

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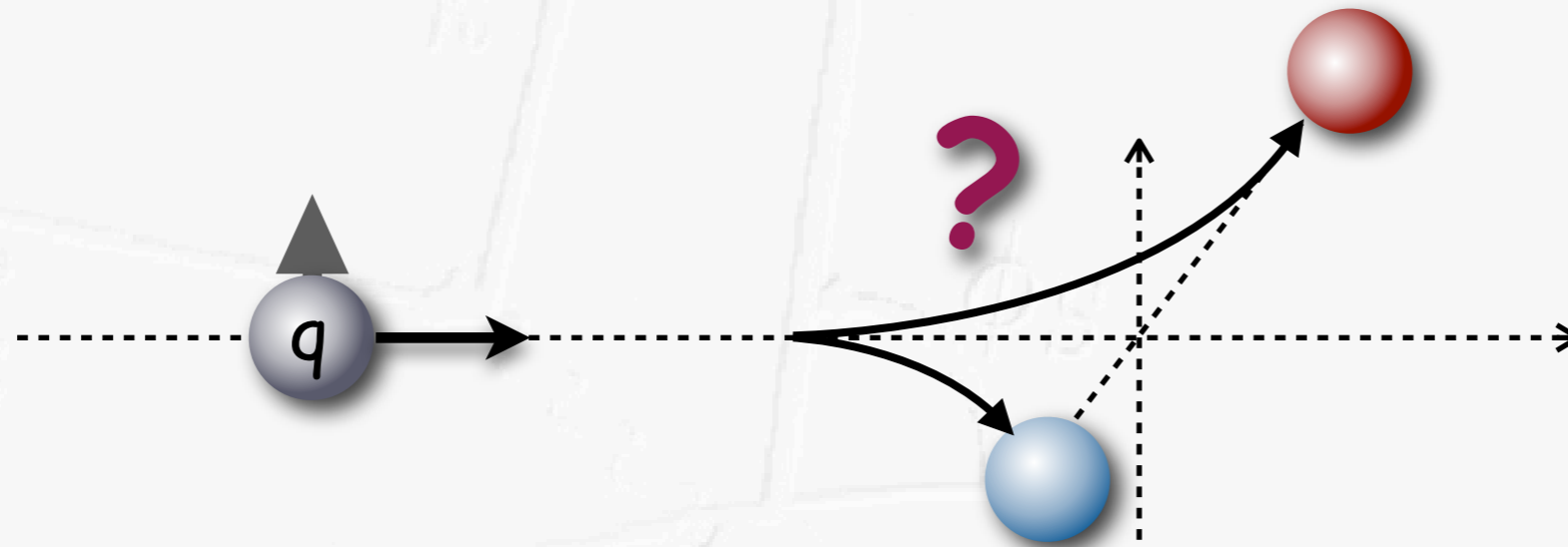
hadron pol.

👉 relevant for unpolarized final state

Collins FF:  $H_1^\perp, q \rightarrow h$

ordinary FF:  $D_1^{q \rightarrow h}$

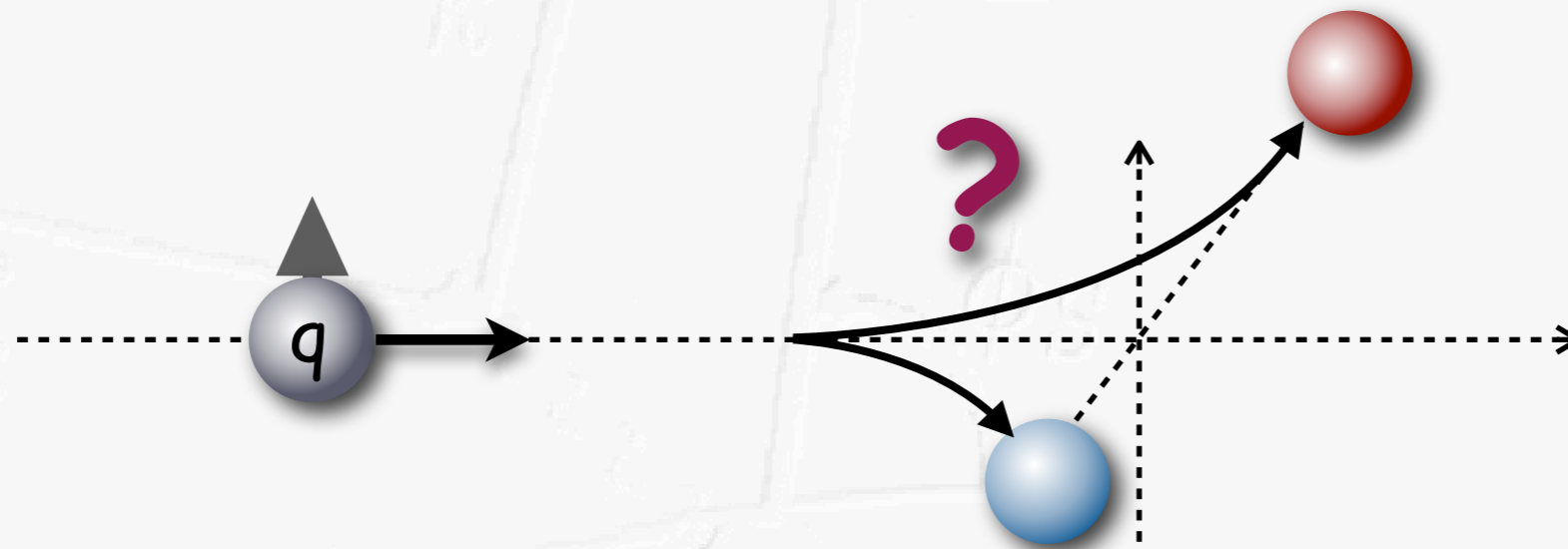
# Collins fctn. - chiral-odd fragmentation



- spin-dependence in fragmentation into unpolarized final state:

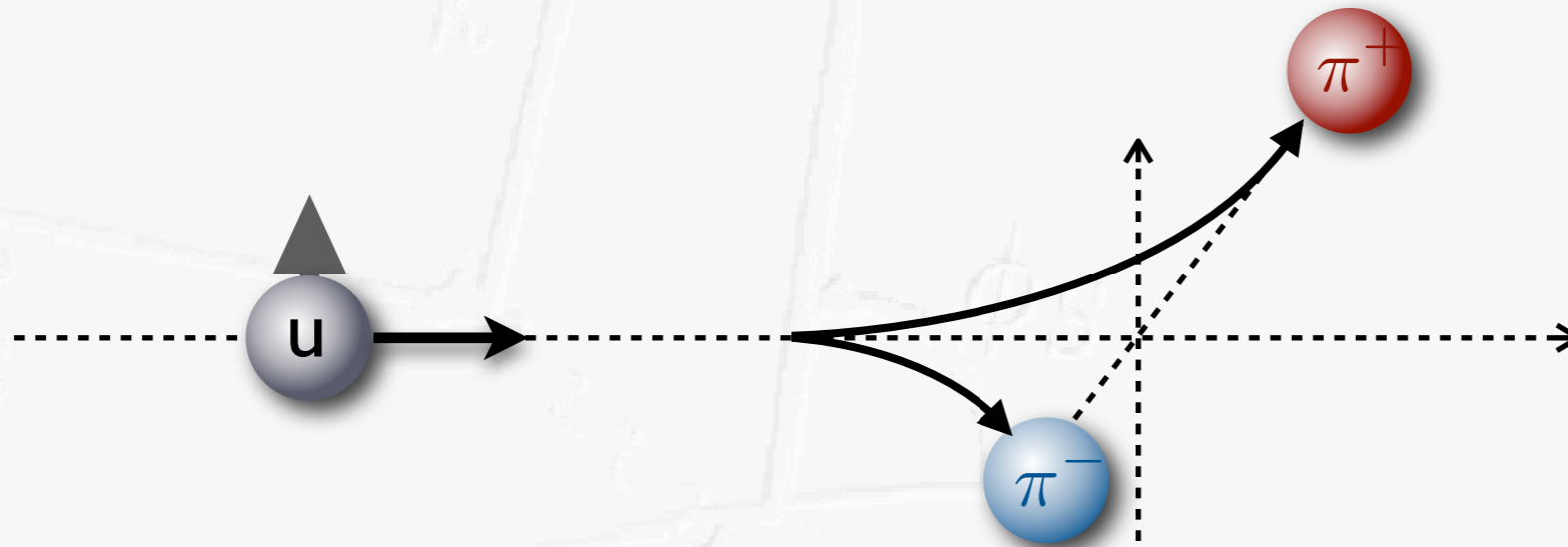
left-right asymmetry in hadron direction transverse to both quark spin and momentum

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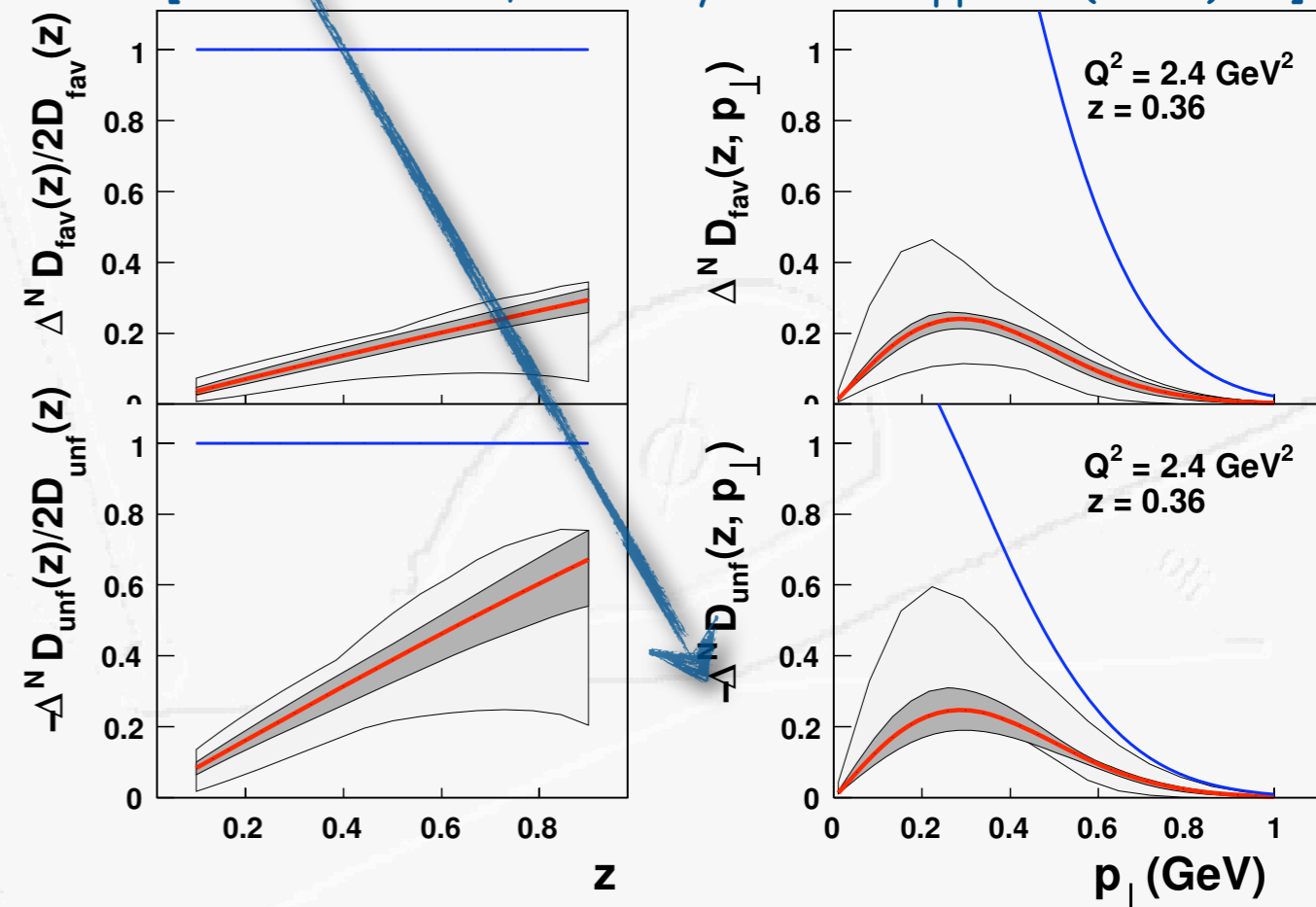
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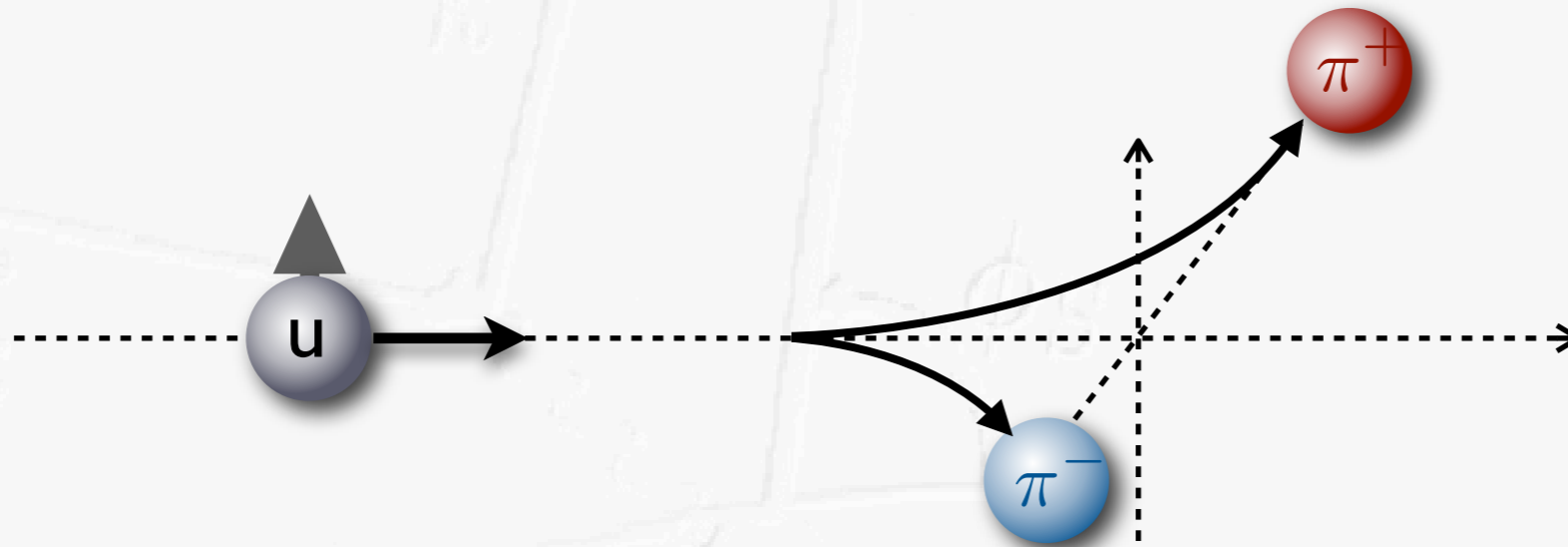


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[Anselmino et al., Nucl. Phys. Proc. Suppl.191 (2009) 98]

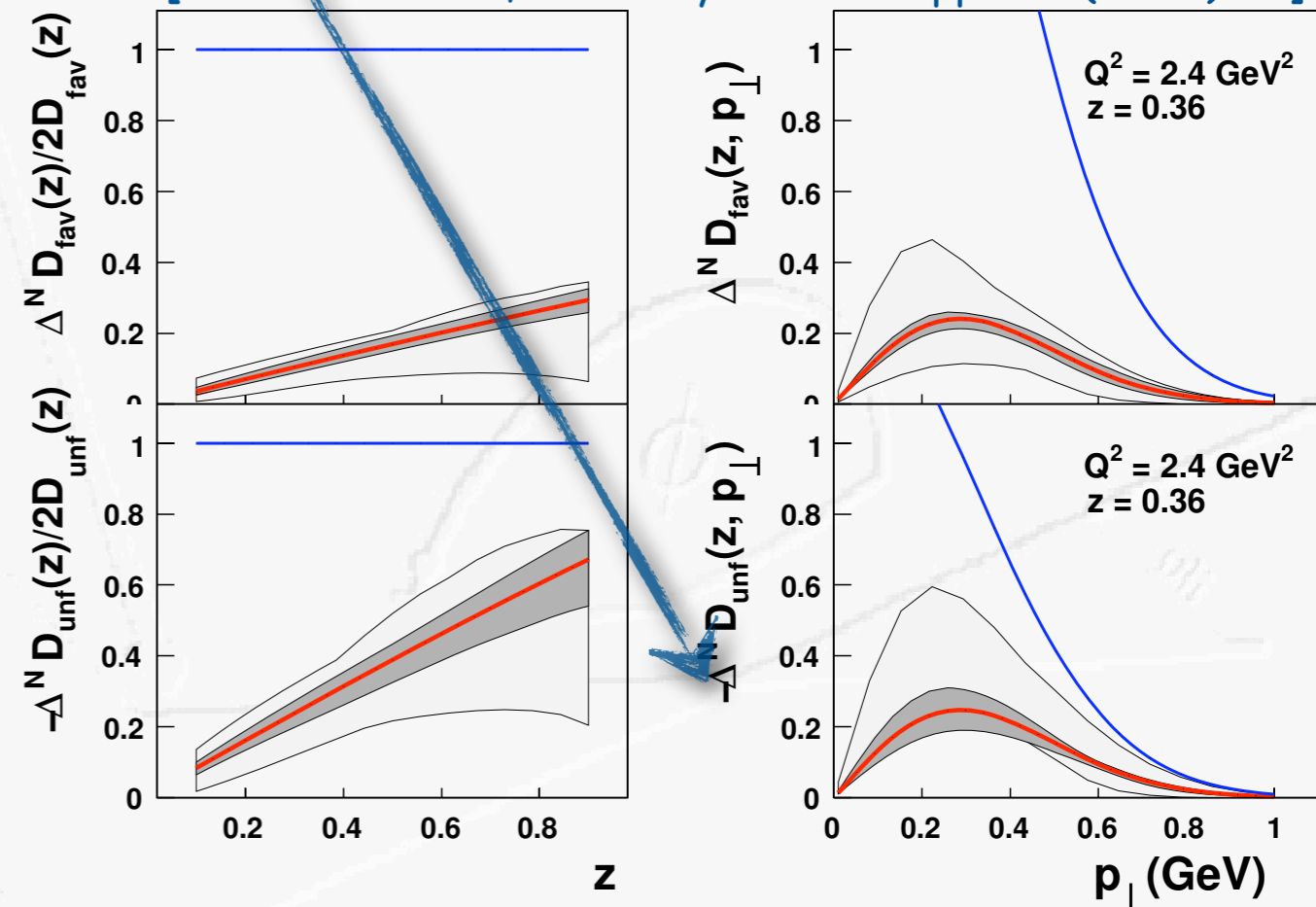


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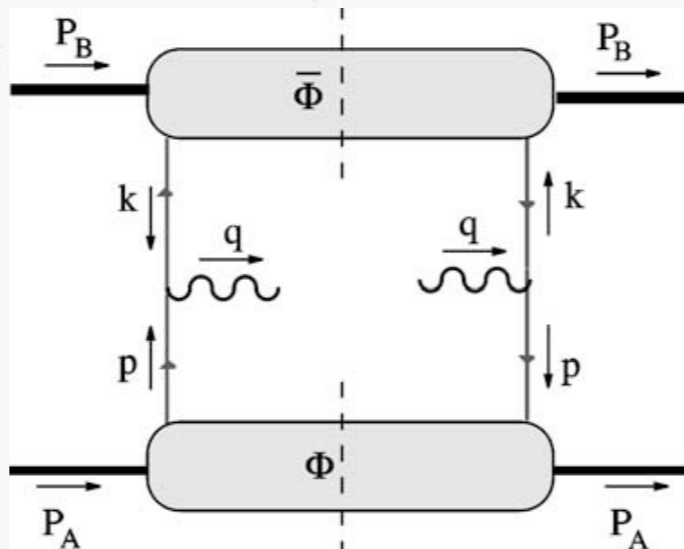
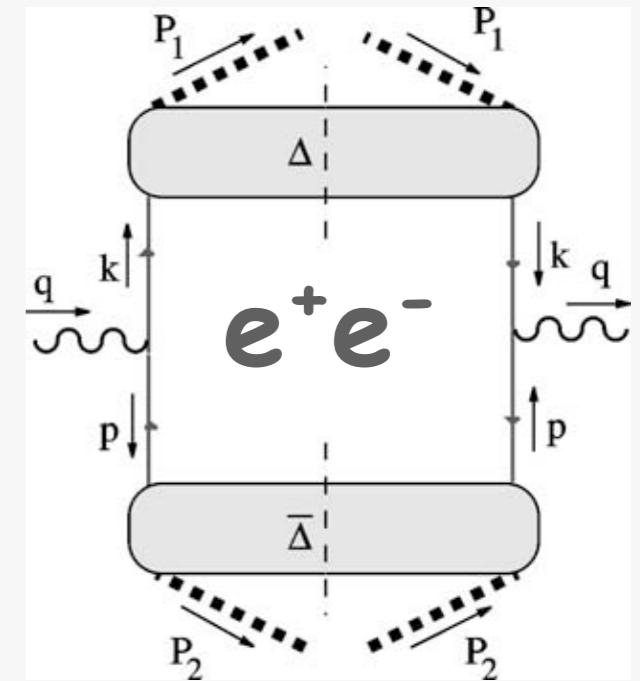
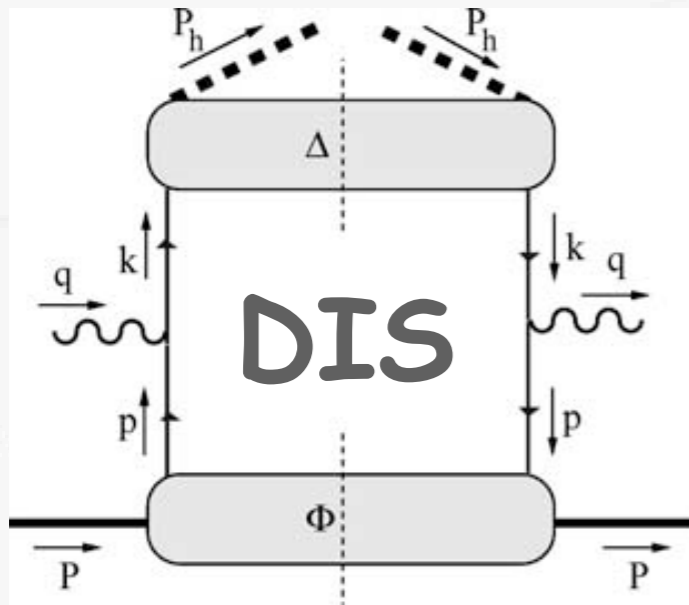


- spin-dependence in fragmentation into unpolarized final state:  
left-right asymmetry in hadron direction transverse to both quark spin and momentum
- extracted from SIDIS and  $e^+e^-$  annihilation data
- spin average gives "ordinary"  $D_1$

[Anselmino et al., Nucl. Phys. Proc. Suppl.191 (2009) 98]

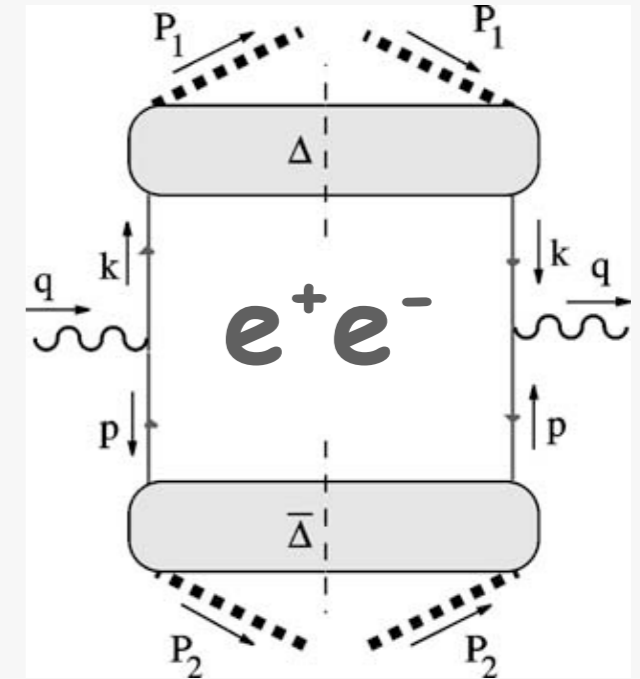
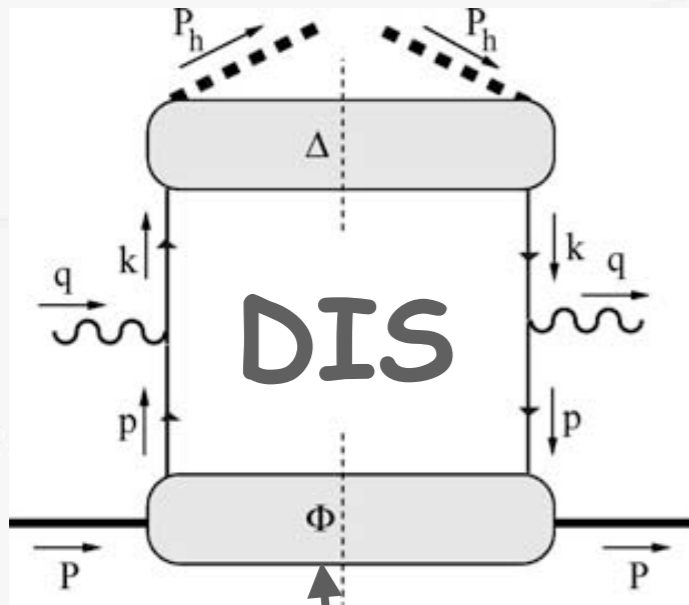


# a QCD laboratory



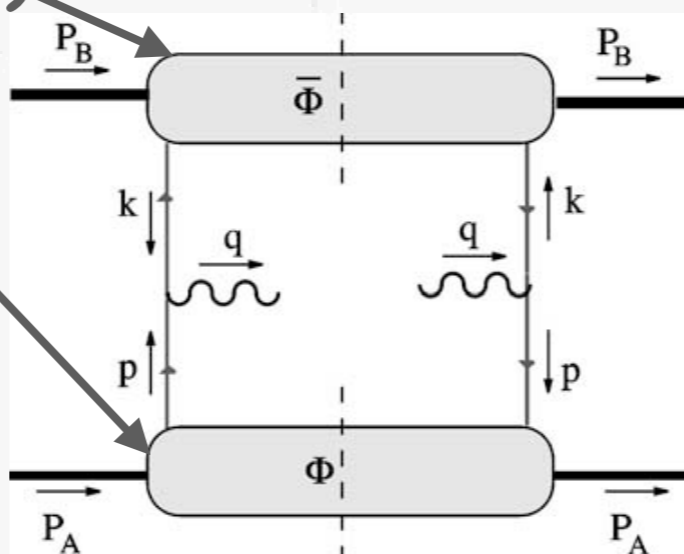
Drell-Yan

# a QCD laboratory



hadron structure

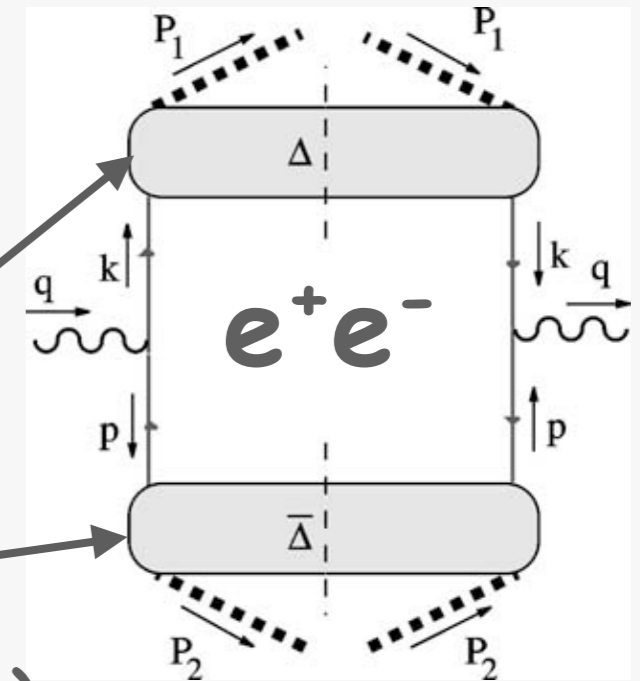
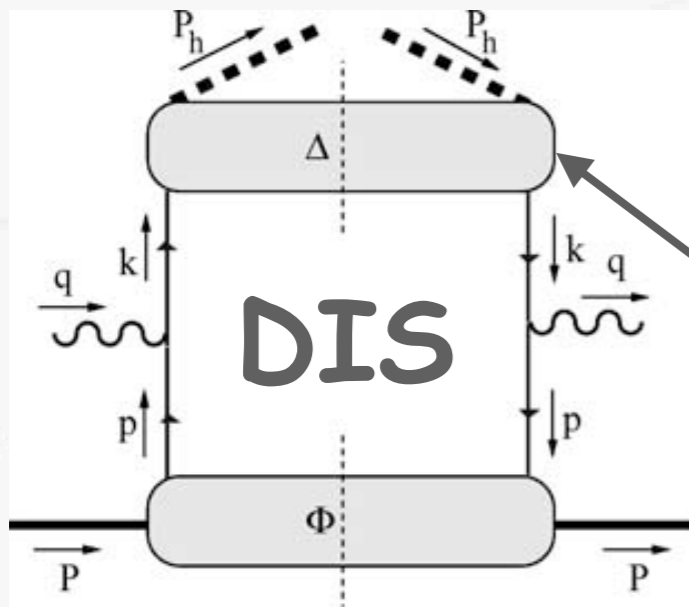
(distribution functions)



Drell-Yan

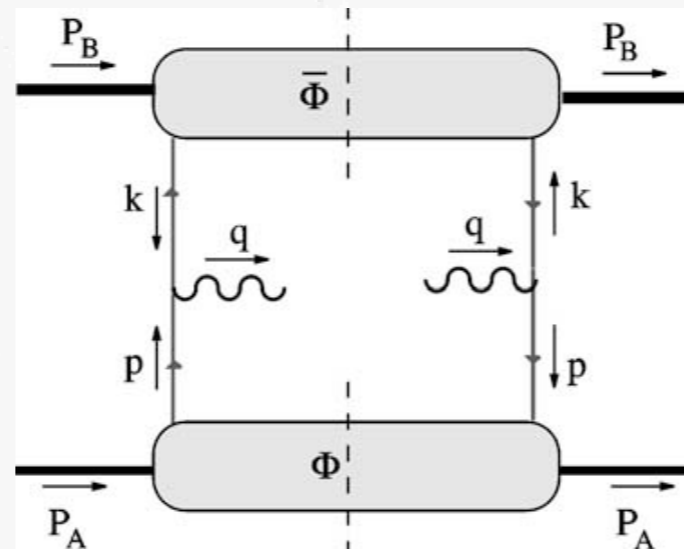


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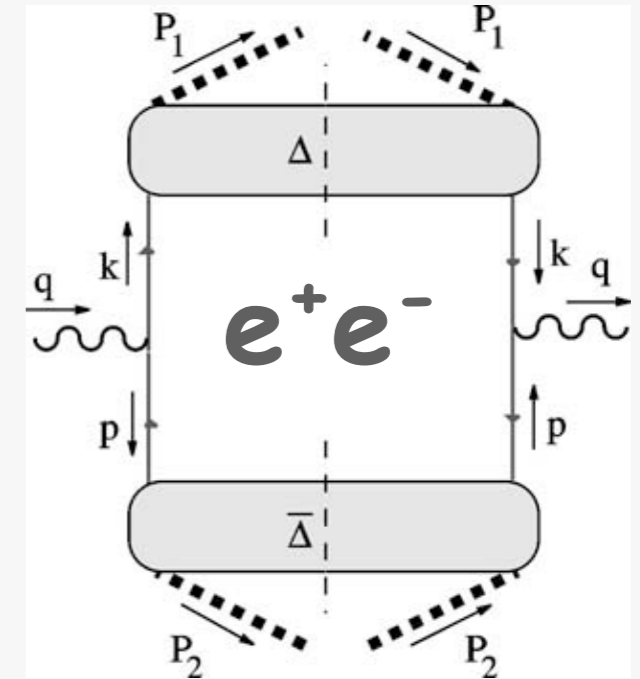
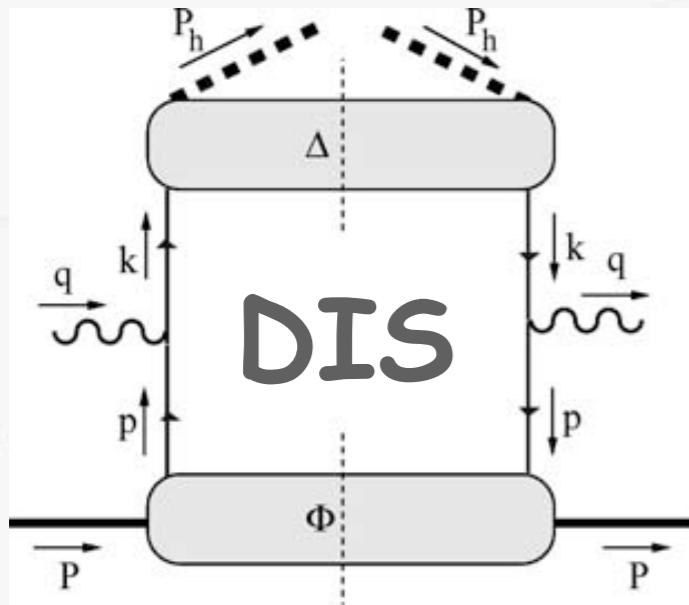
hadronization

(fragmentation functions)

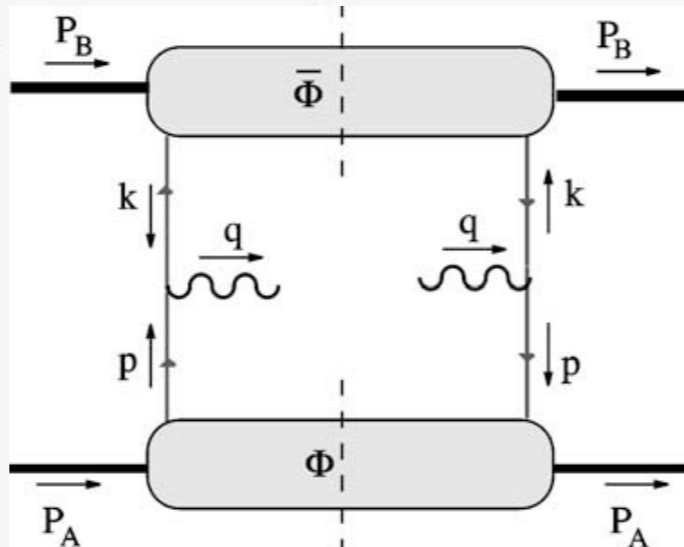


Drell-Yan

# a QCD laboratory

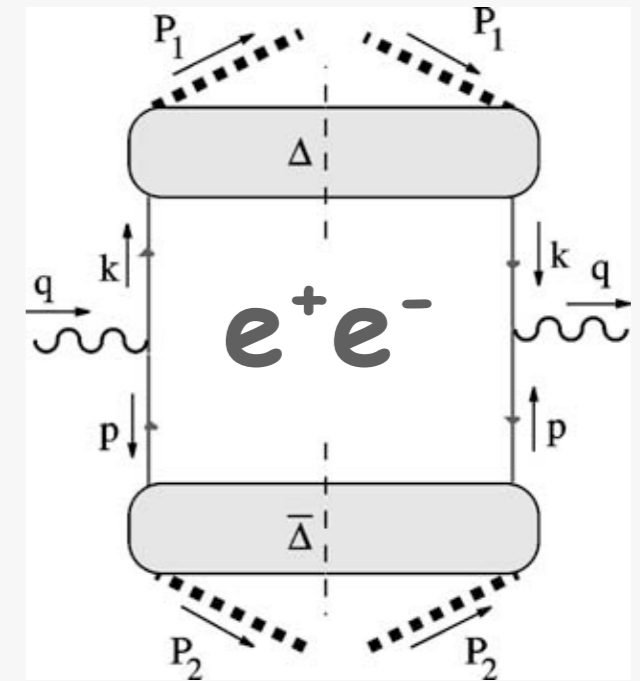
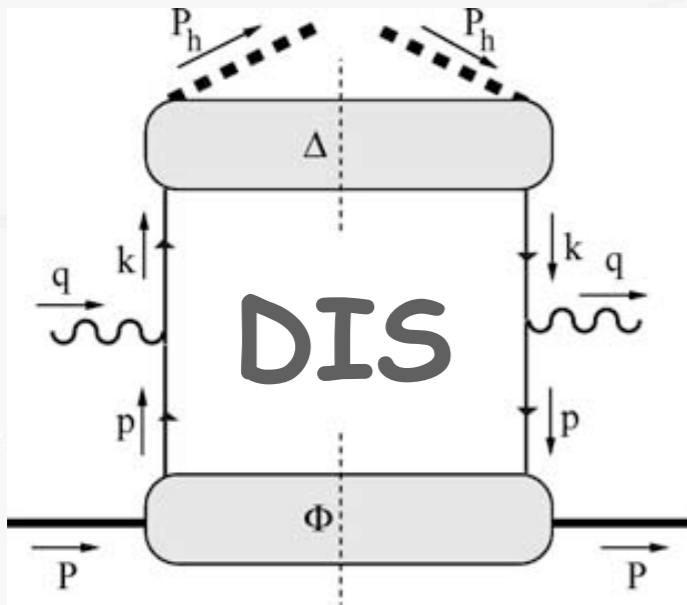


- data from COMPASS, HERMES, and JLab; planned for future EIC
- convolutes parton distribution ( $\Phi$ ) and fragmentation ( $\Delta$ ) functions  $\Phi \otimes \Delta$
- need fragmentation function to extract distribution functions



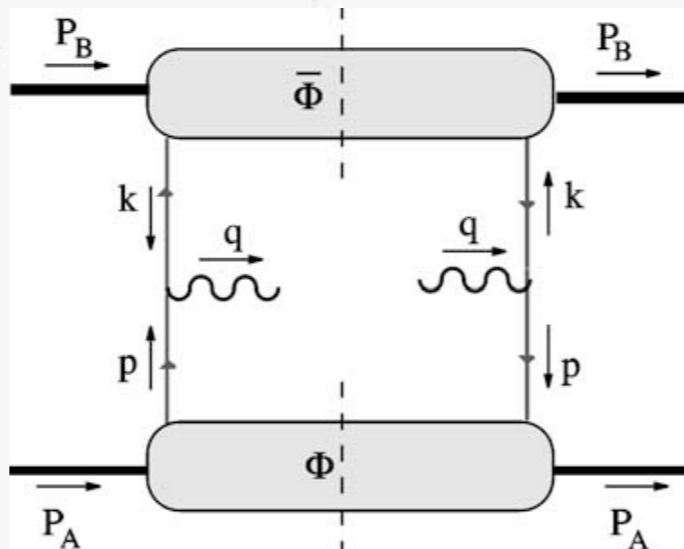
Drell-Yan

# a QCD laboratory



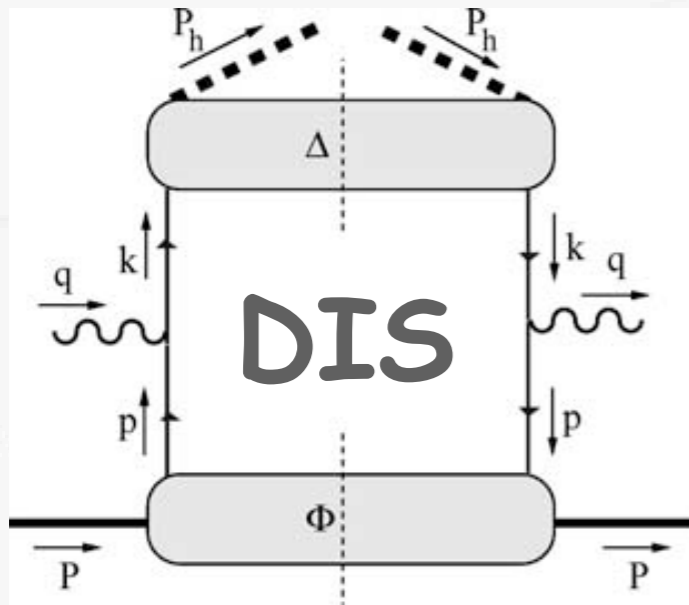
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- ideal place to study hadronization
- convolutes parton fragmentation functions  $\Delta \otimes \Delta$
- wealth of ("raw") data from Belle and BaBar



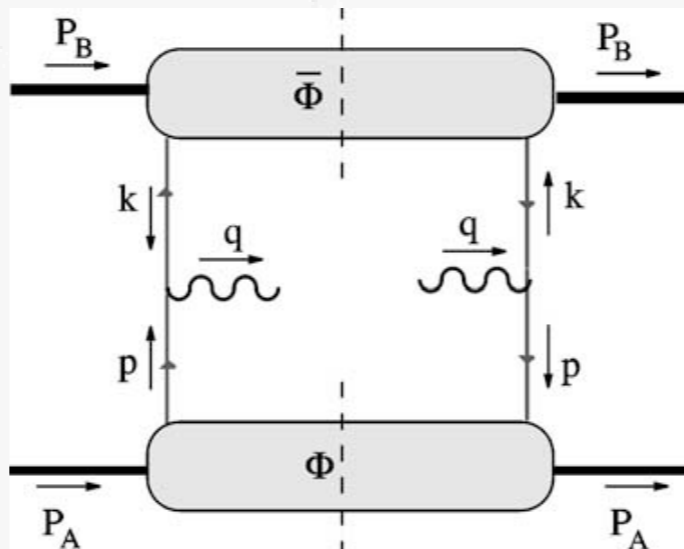
Drell-Yan

# a QCD laboratory

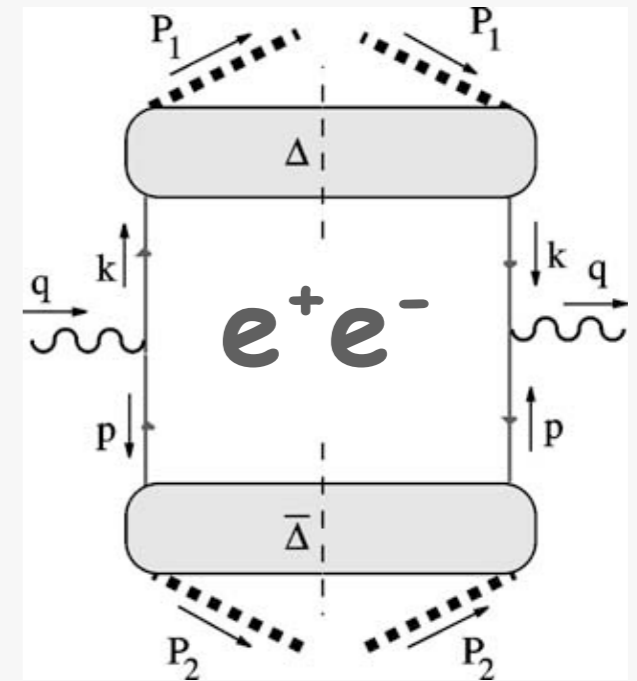


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- convolutes parton distribution functions  $\Phi \otimes \Phi$
- testing ground for sign reversal of naive-T-odd distributions
- hardly any data



Drell-Yan



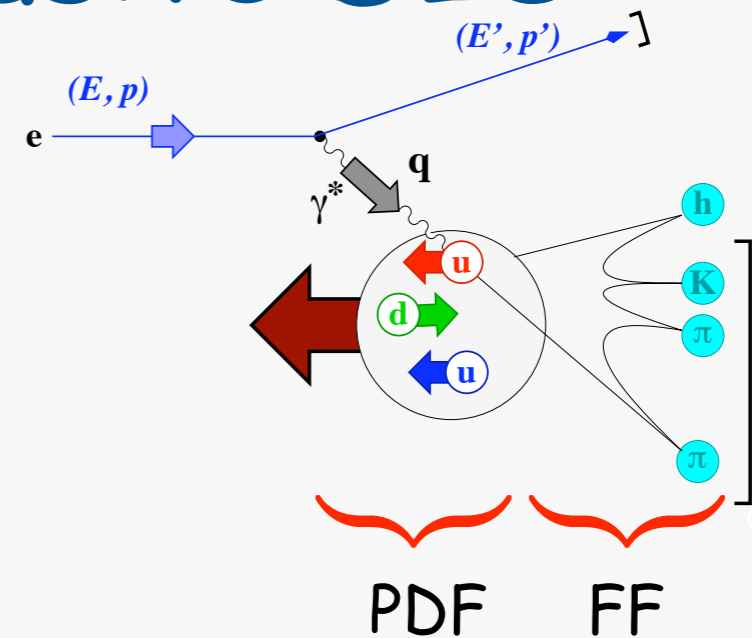
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# Probing TMDs in semi-inclusive DIS

quark pol.

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

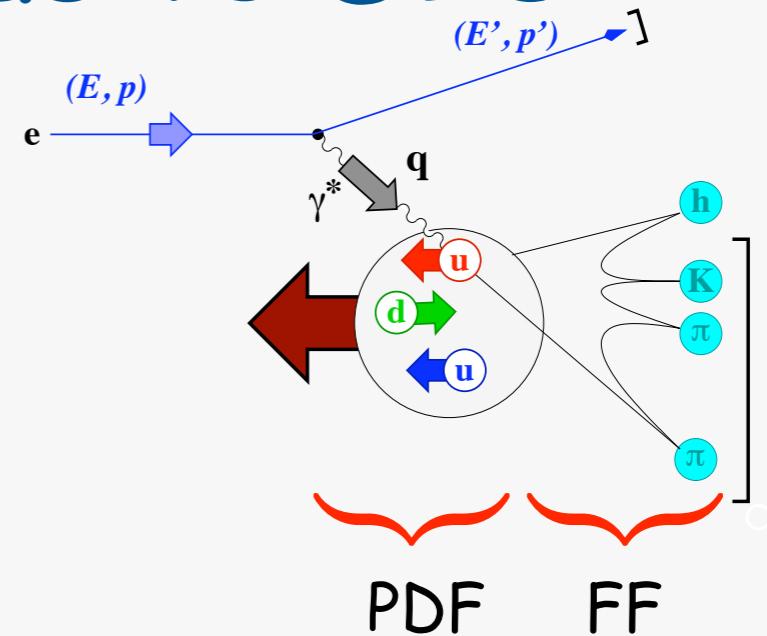
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in SIDIS\*) couple PDFs to:

\*) semi-inclusive DIS with unpolarized final state

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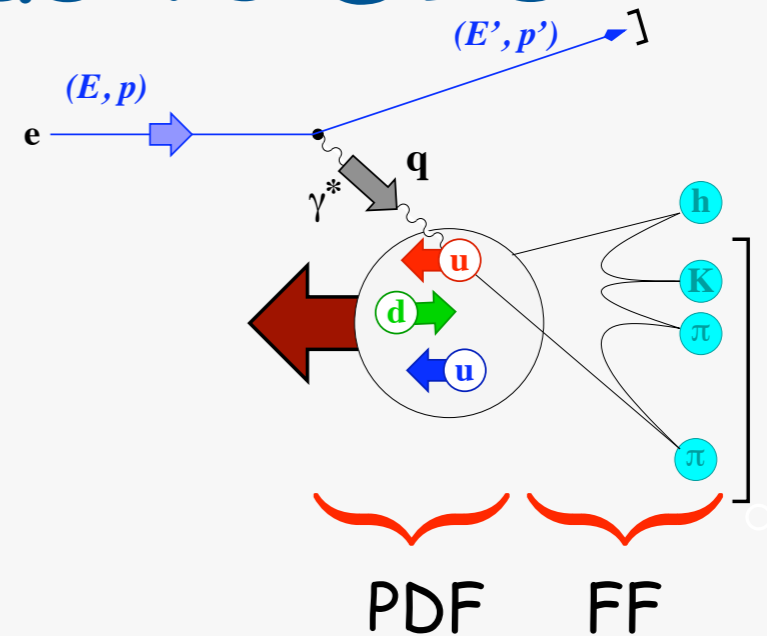
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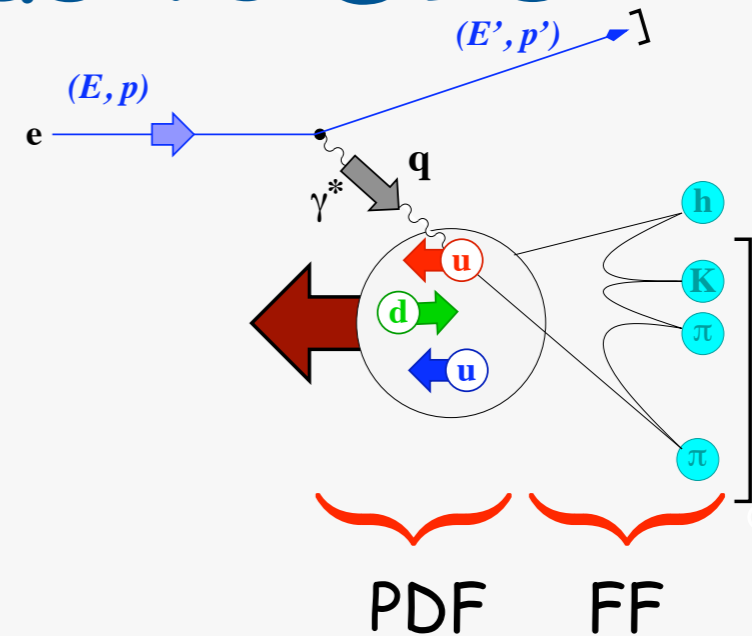
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nucleon pol.

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Collins FF:  $H_1^{\perp, q \rightarrow h}$

ordinary FF:  $D_1^{q \rightarrow h}$

⇒ give rise to characteristic azimuthal dependences

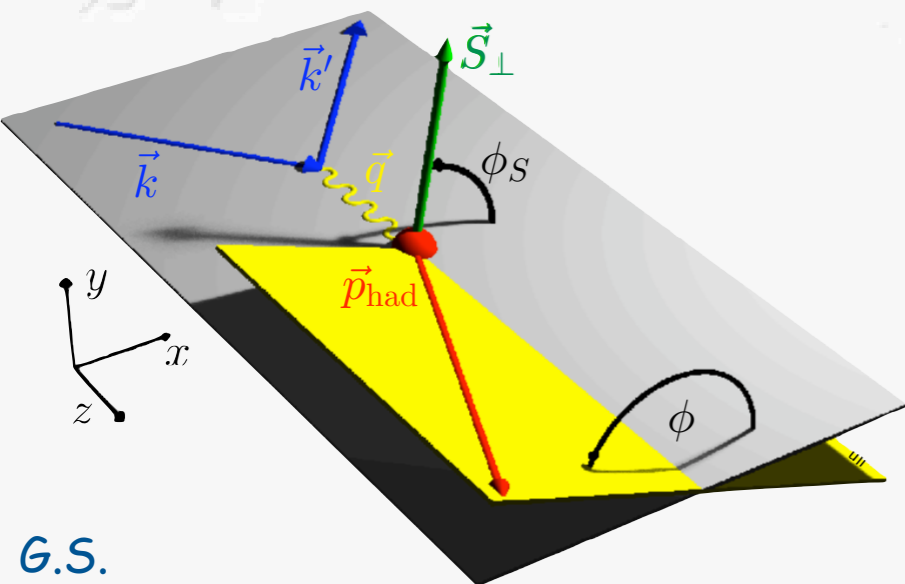
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# 1-hadron production ( $ep \rightarrow ehX$ )

$$\begin{aligned}
 d\sigma = & d\sigma_{UU}^0 + \cos 2\phi d\sigma_{UU}^1 + \frac{1}{Q} \cos \phi d\sigma_{UU}^2 + \lambda_e \frac{1}{Q} \sin \phi d\sigma_{LU}^3 \\
 & + S_L \left\{ \sin 2\phi d\sigma_{UL}^4 + \frac{1}{Q} \sin \phi d\sigma_{UL}^5 + \lambda_e \left[ d\sigma_{LL}^6 + \frac{1}{Q} \cos \phi d\sigma_{LL}^7 \right] \right\} \\
 & + S_T \left\{ \sin(\phi - \phi_S) d\sigma_{UT}^8 + \sin(\phi + \phi_S) d\sigma_{UT}^9 + \sin(3\phi - \phi_S) d\sigma_{UT}^{10} \frac{1}{Q} \right. \\
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 \end{aligned}$$

$\sigma_{XY}$   
 ↙ ↘  
**Beam Target**  
**Polarization**



Mulders and Tangermann, Nucl. Phys. B 461 (1996) 197

Boer and Mulders, Phys. Rev. D 57 (1998) 5780

Bacchetta et al., Phys. Lett. B 595 (2004) 309

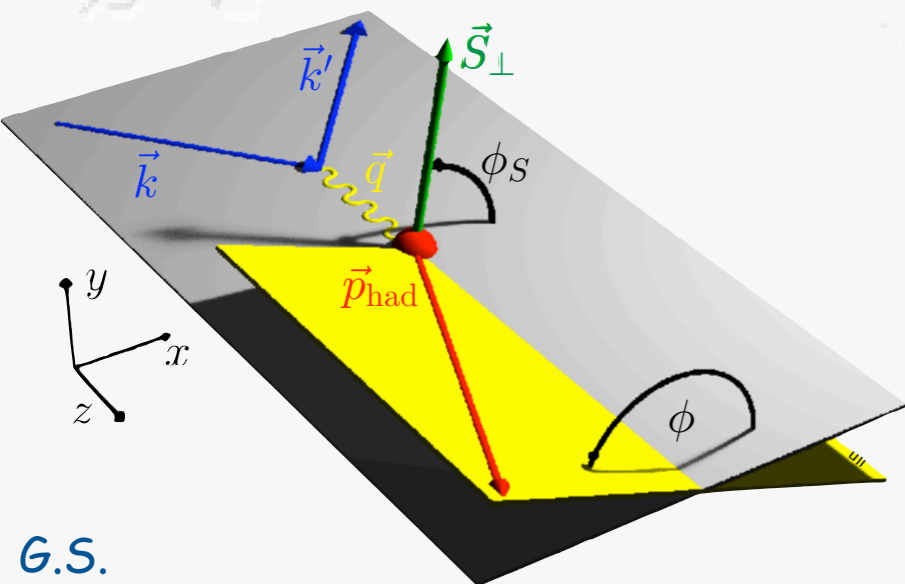
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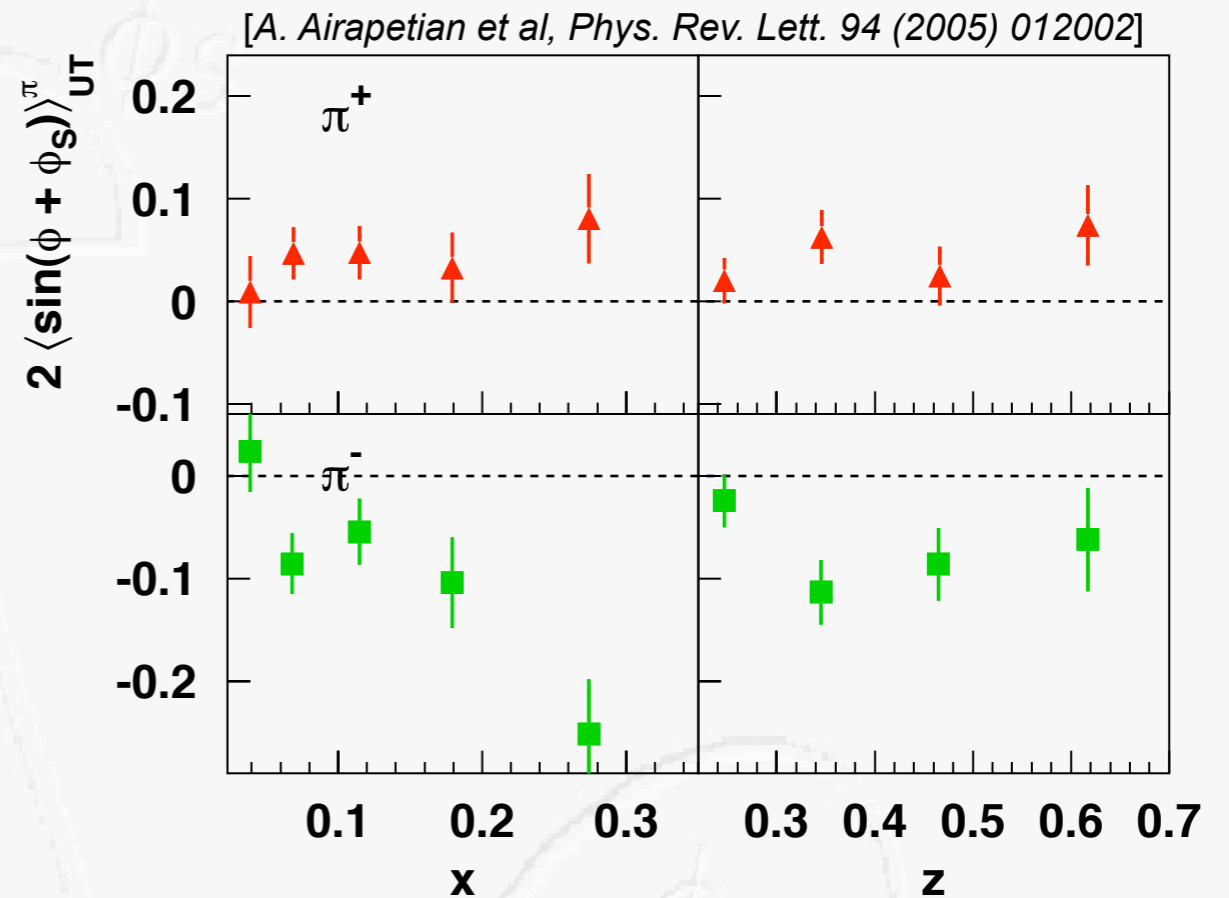
"Trento Conventions", Phys. Rev. D 70 (2004) 117504

**The quest for transversity**

# Transversity distribution (Collins fragmentation)

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

- significant in size and opposite in sign for charged pions



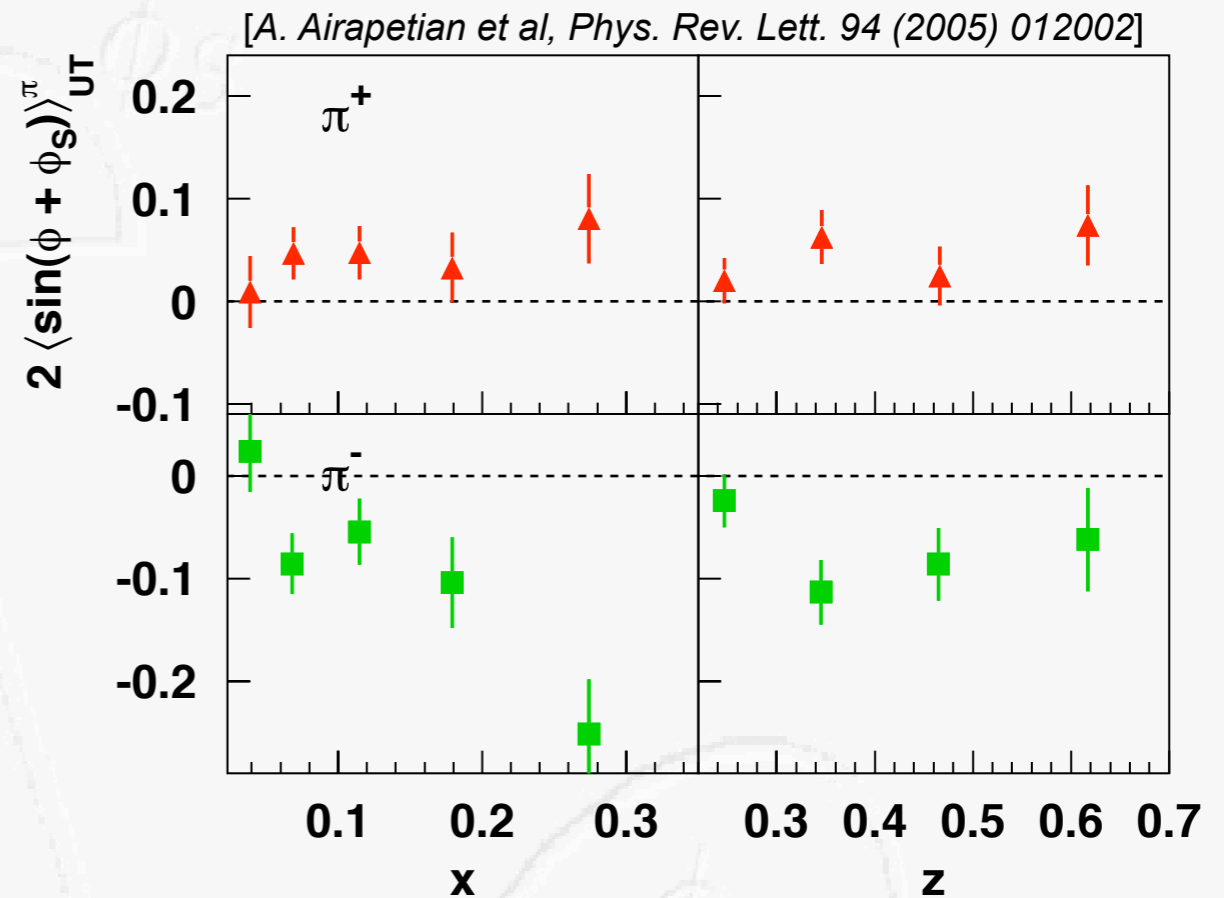
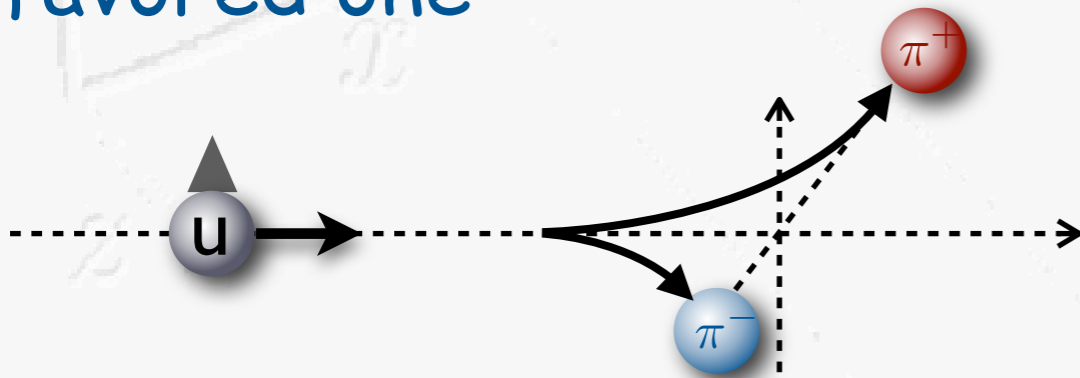
2005: First evidence from HERMES  
SIDIS on proton

Non-zero transversity  
Non-zero Collins function

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- significant in size and opposite in sign for charged pions
- disfavored Collins FF large and opposite in sign to favored one



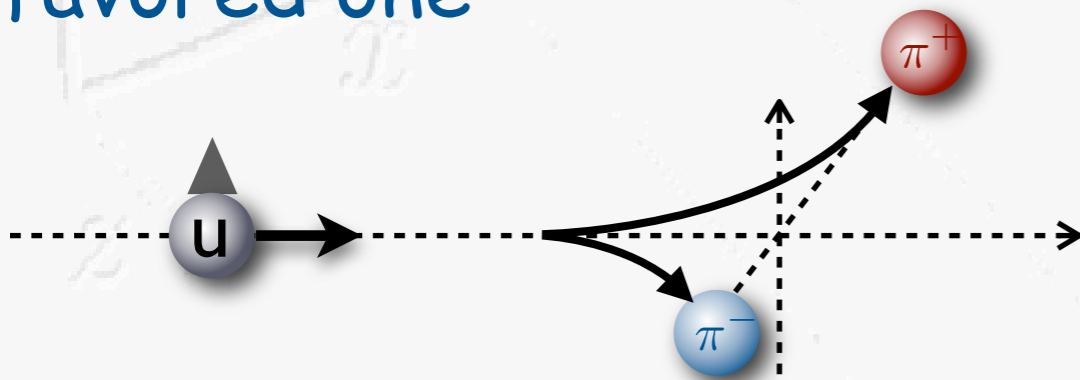
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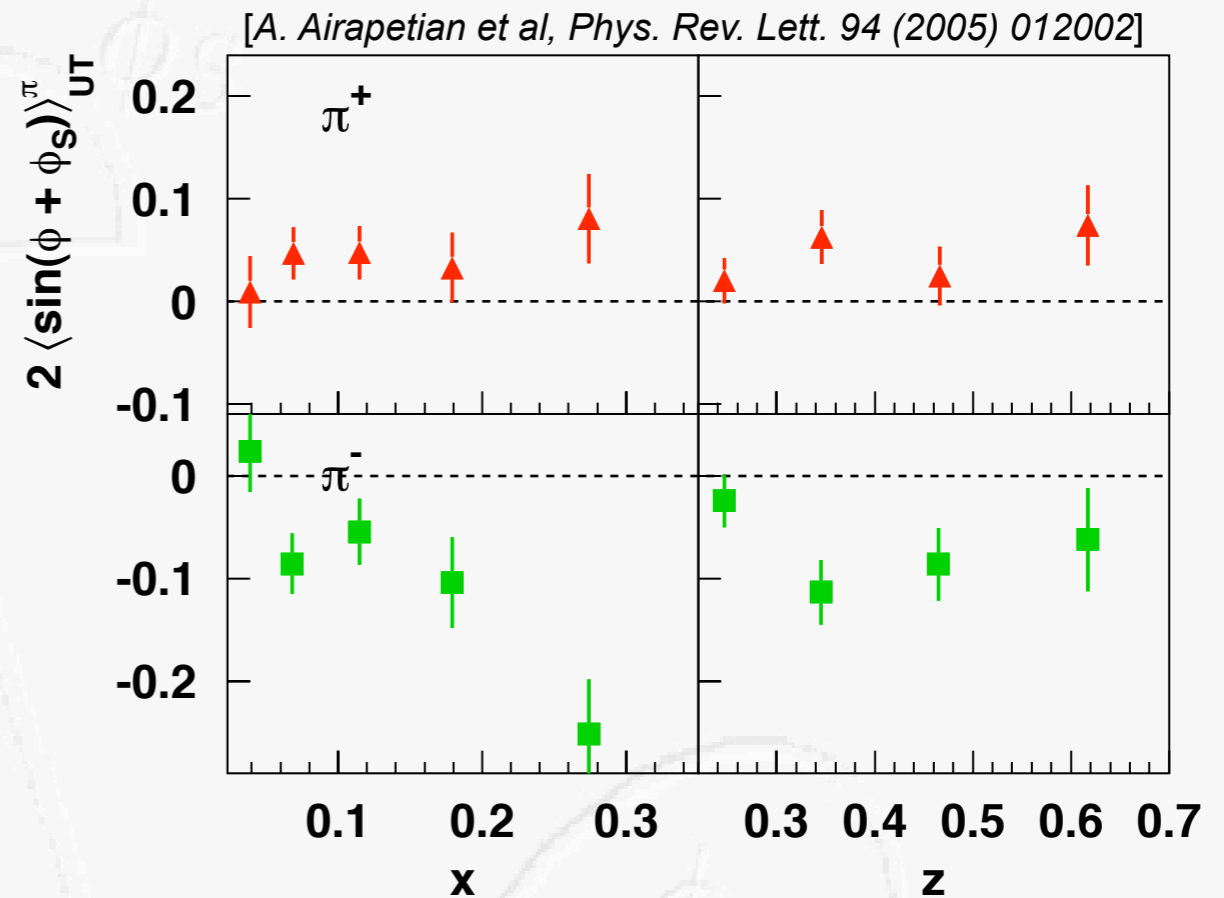
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- leads to various cancellations in SSA observables



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Non-zero transversity  
Non-zero Collins function

# Collins amplitudes

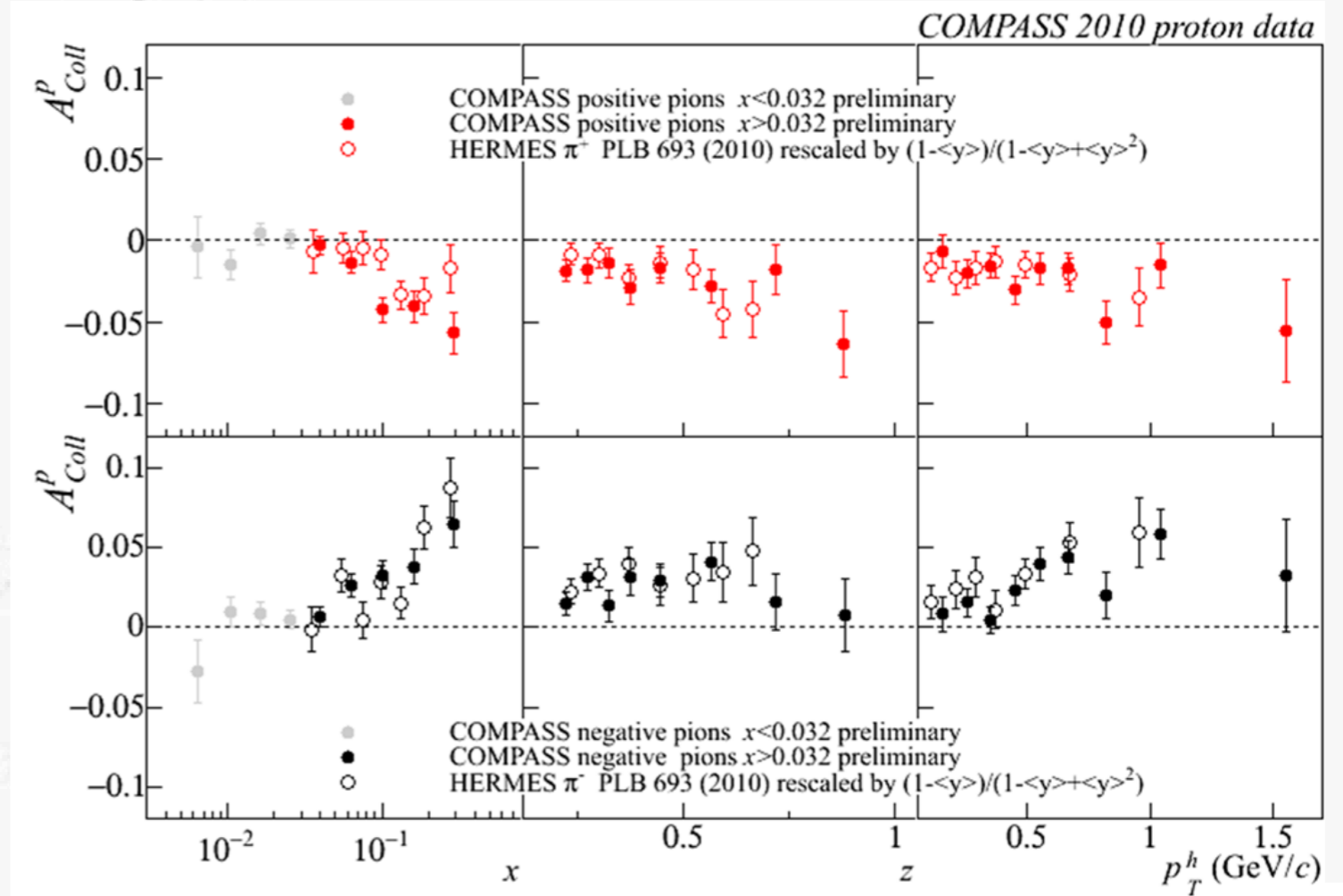
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● **wealth of new results:**

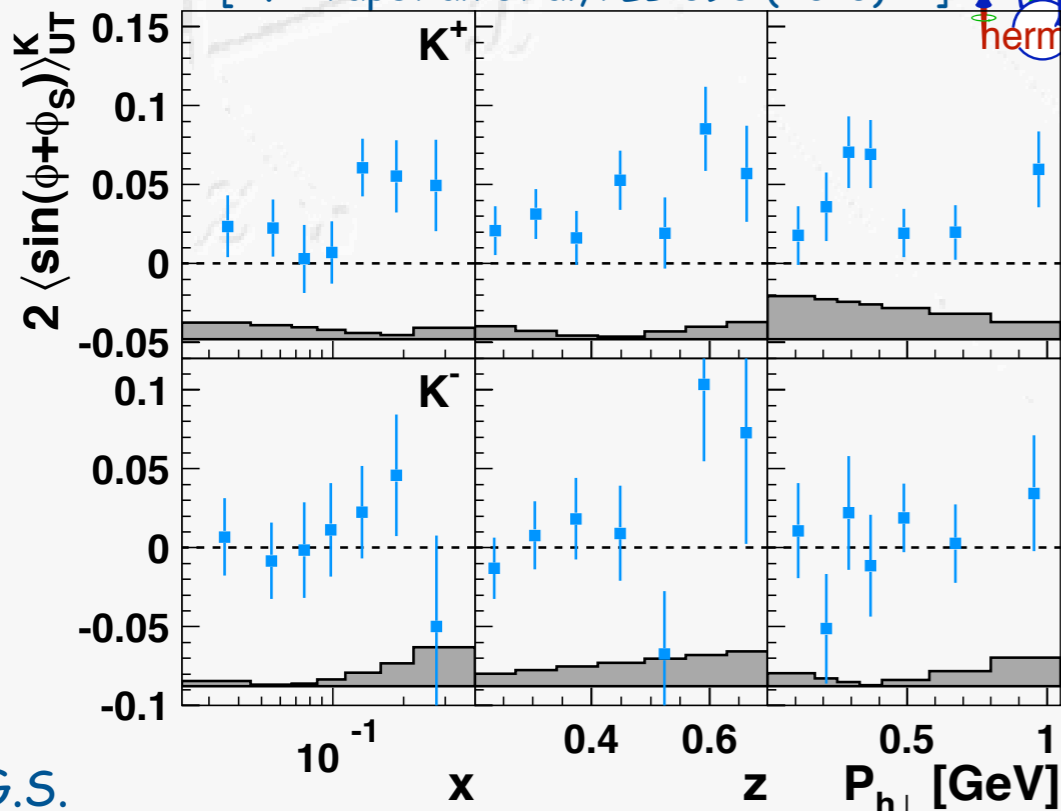
● **COMPASS**  
[PLB 692 (2010) 240,  
PLB 717 (2012) 376]

● **HERMES**  
[PLB 693 (2010) 11]

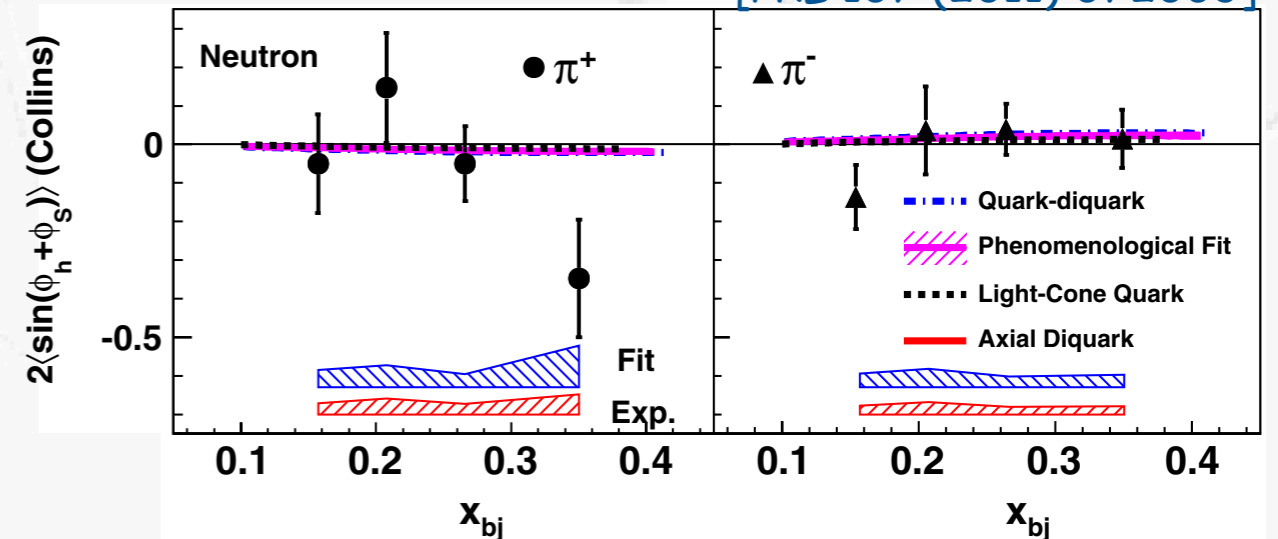
● **Jefferson Lab**  
[PRL 107 (2011) 072003]



[A. Airapetian et al, PLB 693 (2010) 11]



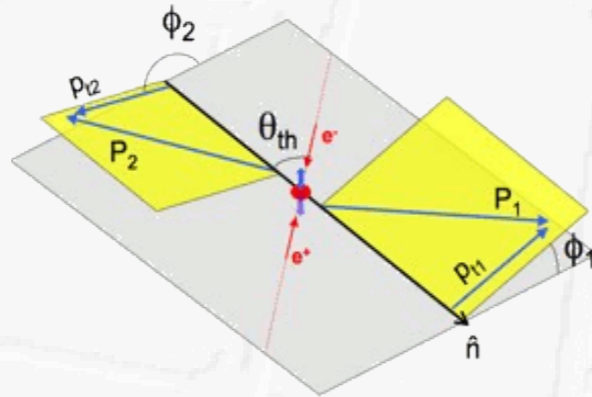
[PRL 107 (2011) 072003]



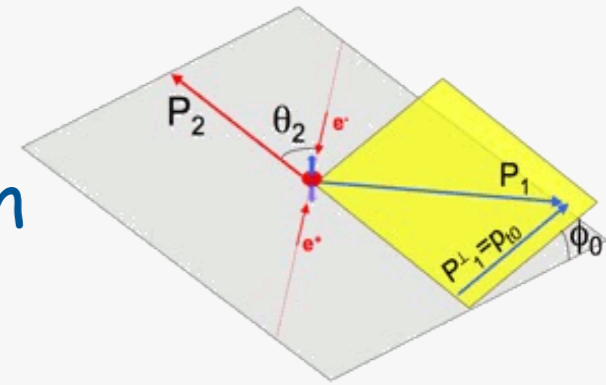
# Collins FF from $e^+e^-$

- analyzed in different frames:

- Collins-Soper



vs. Gottfried-Jackson



→ different convolutions over transverse momenta:

$$A_{12} \propto \cos(\phi_1 + \phi_2) \frac{H_1^{\perp,[1]} \bar{H}_1^{\perp,[1]}}{D_1^{[0]} \bar{D}_1^{[0]}}$$

$$A_0 \propto \cos(2\phi_0) \frac{\mathcal{F}[WH_1^{\perp} \bar{H}_1^{\perp}]}{\mathcal{F}[D_1 \bar{D}_1]}$$

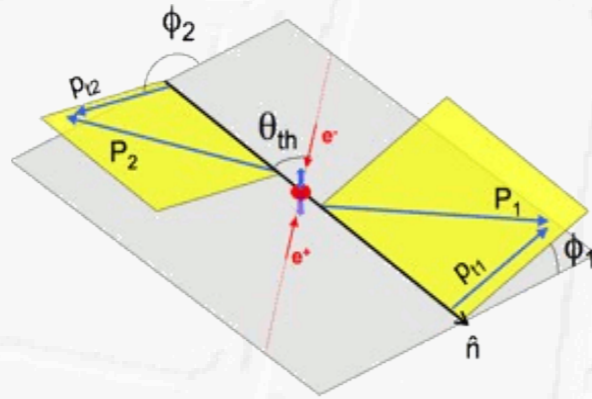
$$F^{[n]} = \int d|\mathbf{k}_T|^2 \left[ \frac{|\mathbf{k}_T|}{M_h} \right]^n F(z, \mathbf{k}_T^2)$$



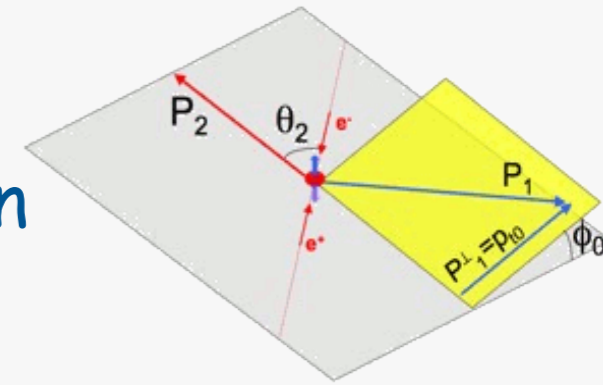
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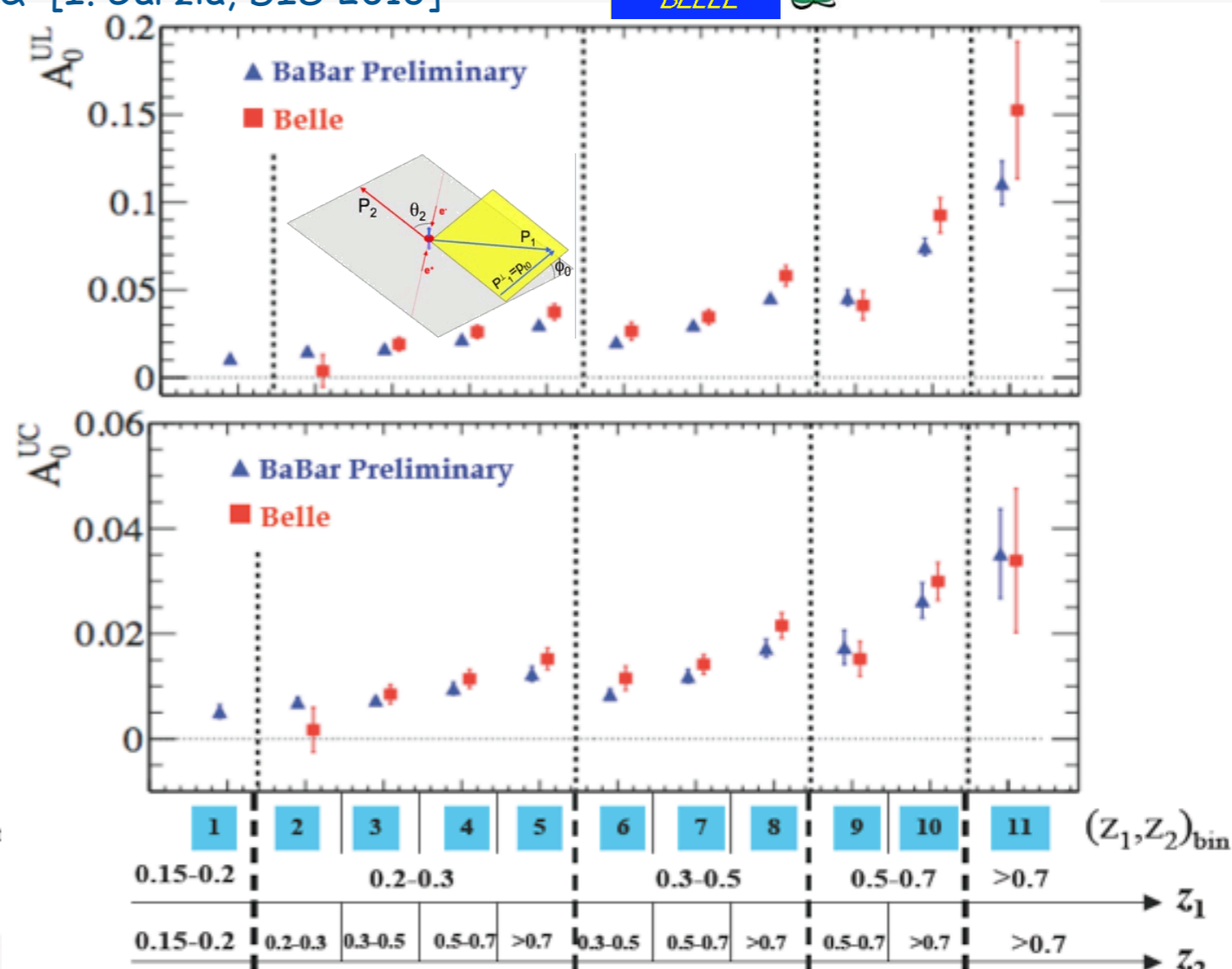
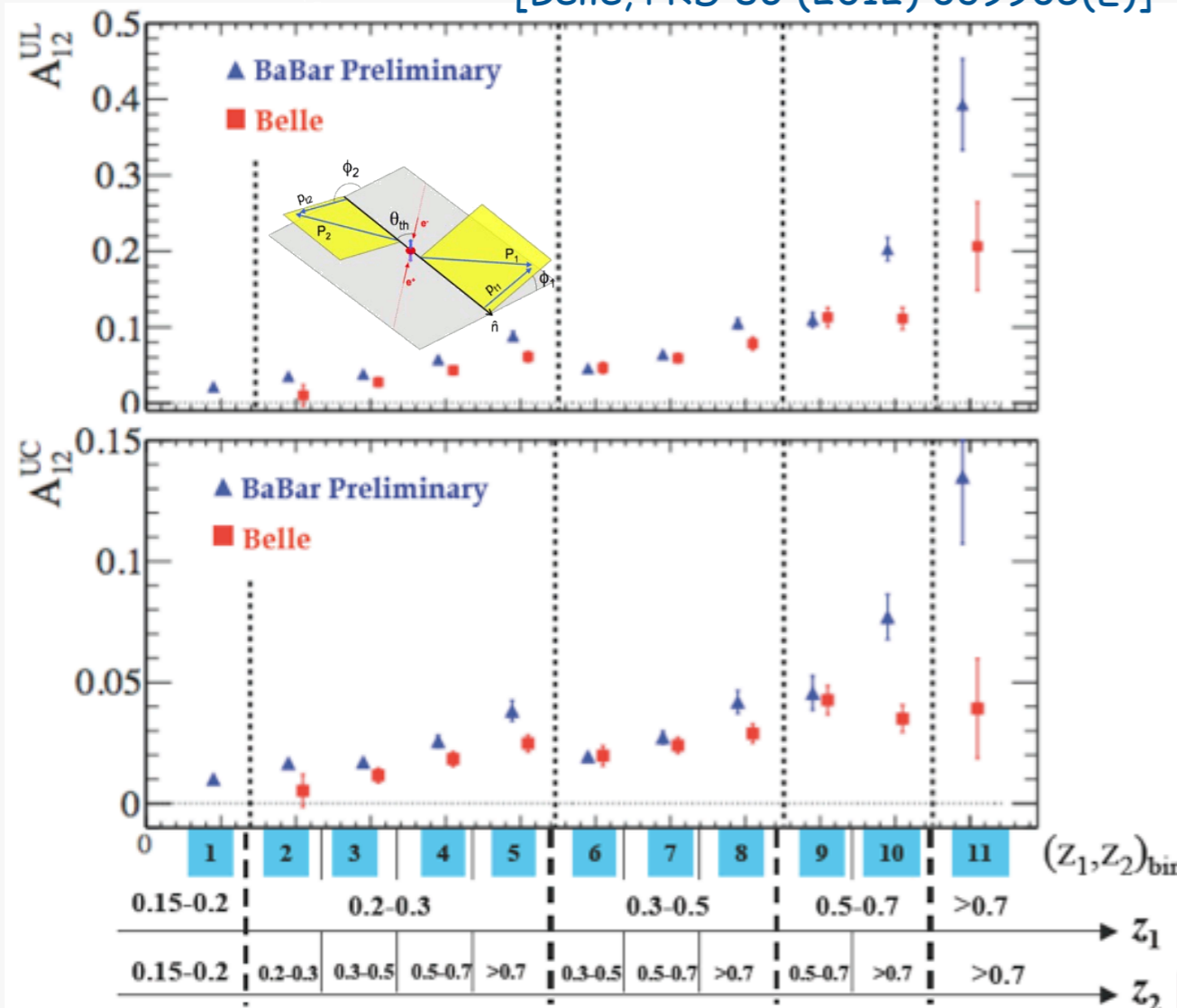


vs. Gottfried-Jackson



different convolutions over transverse momenta:

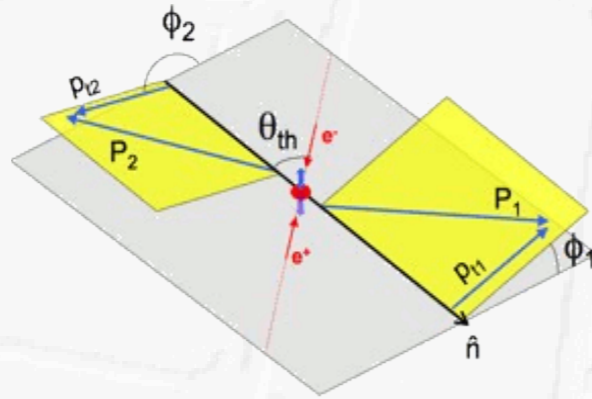
[Belle, PRD 86 (2012) 039905(E)] & [I. Garzia, DIS 2013]



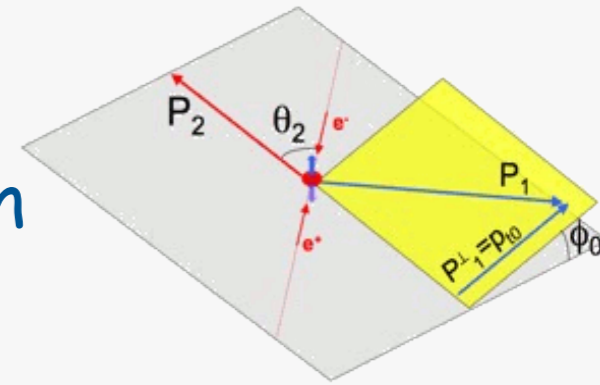
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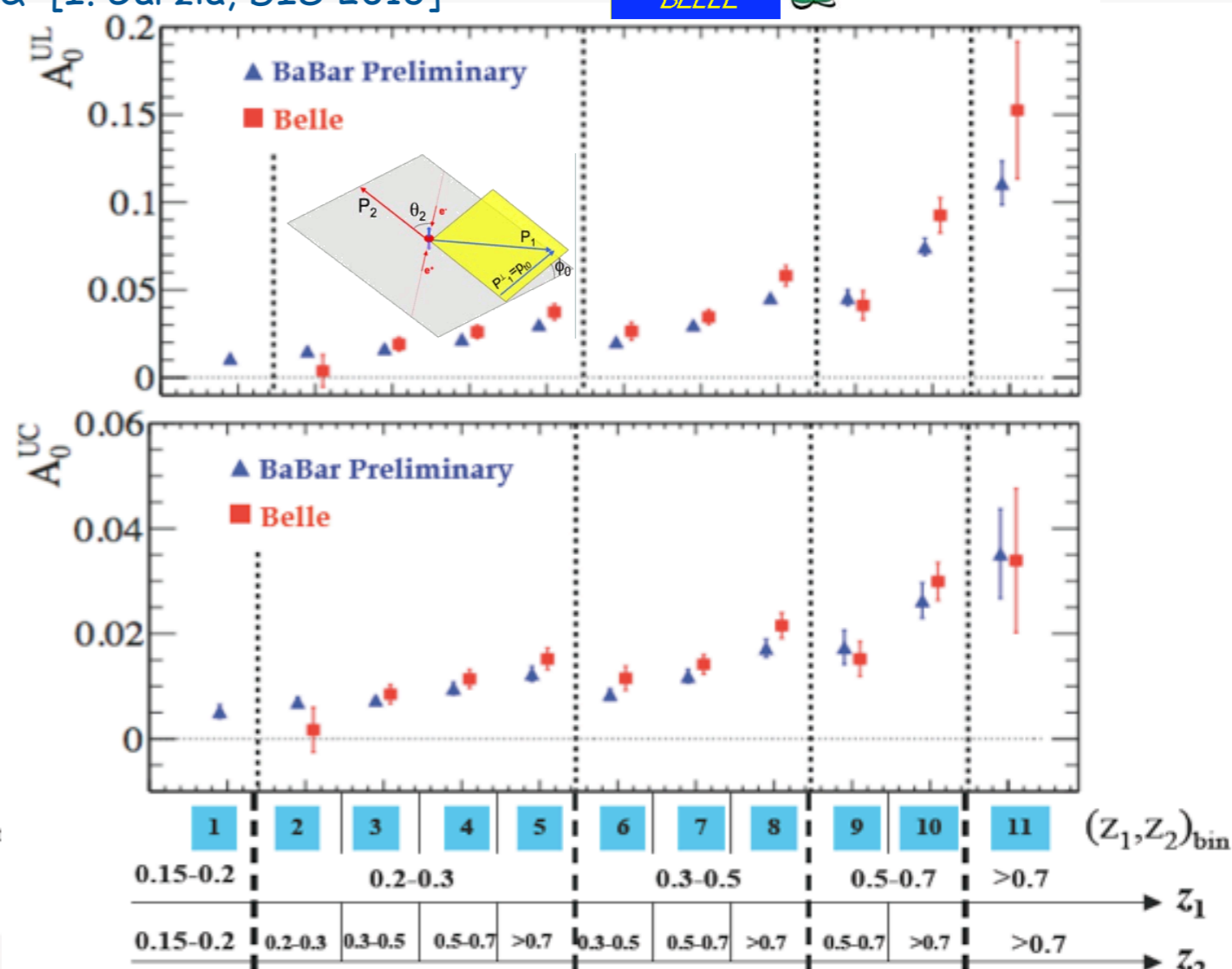
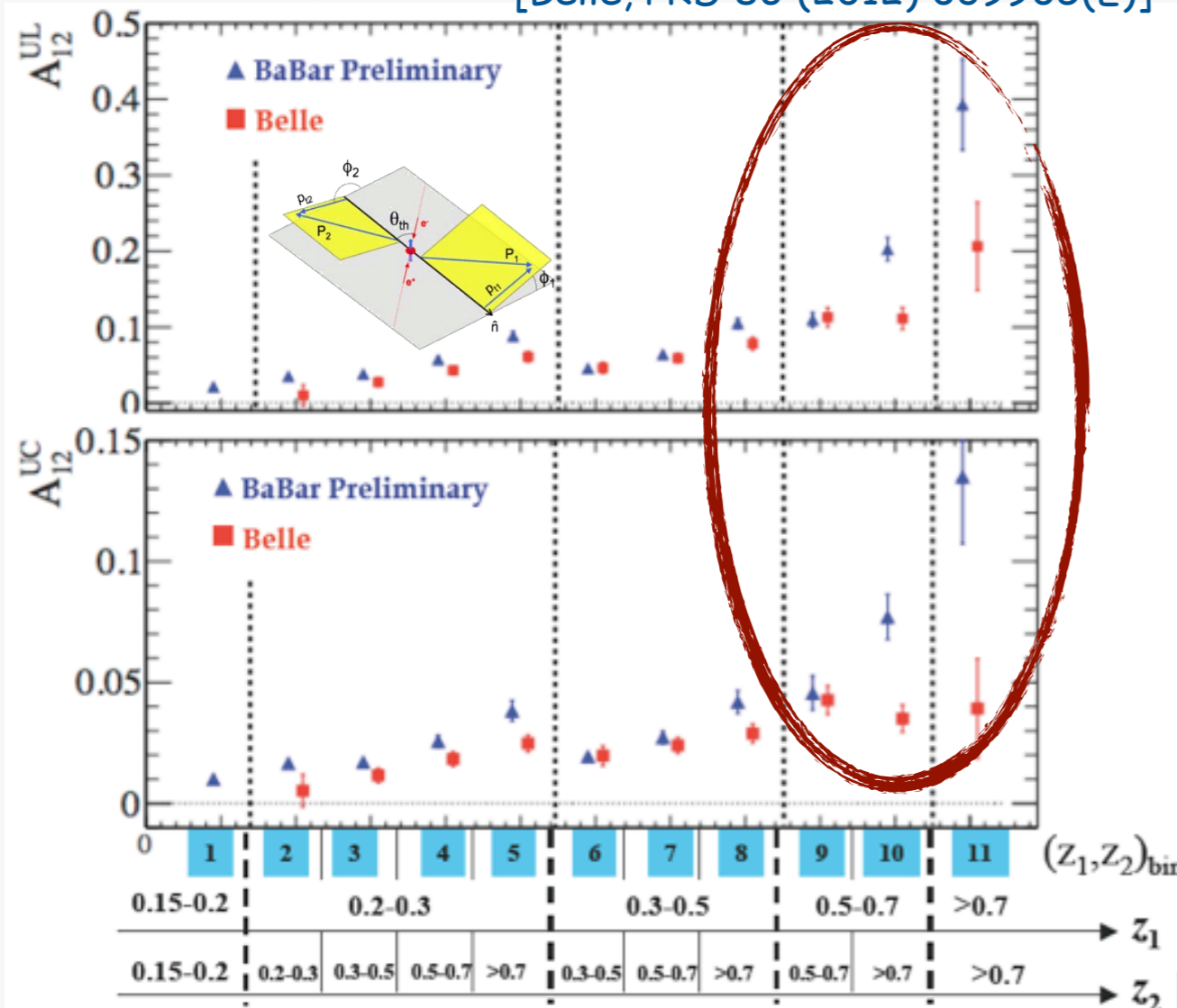


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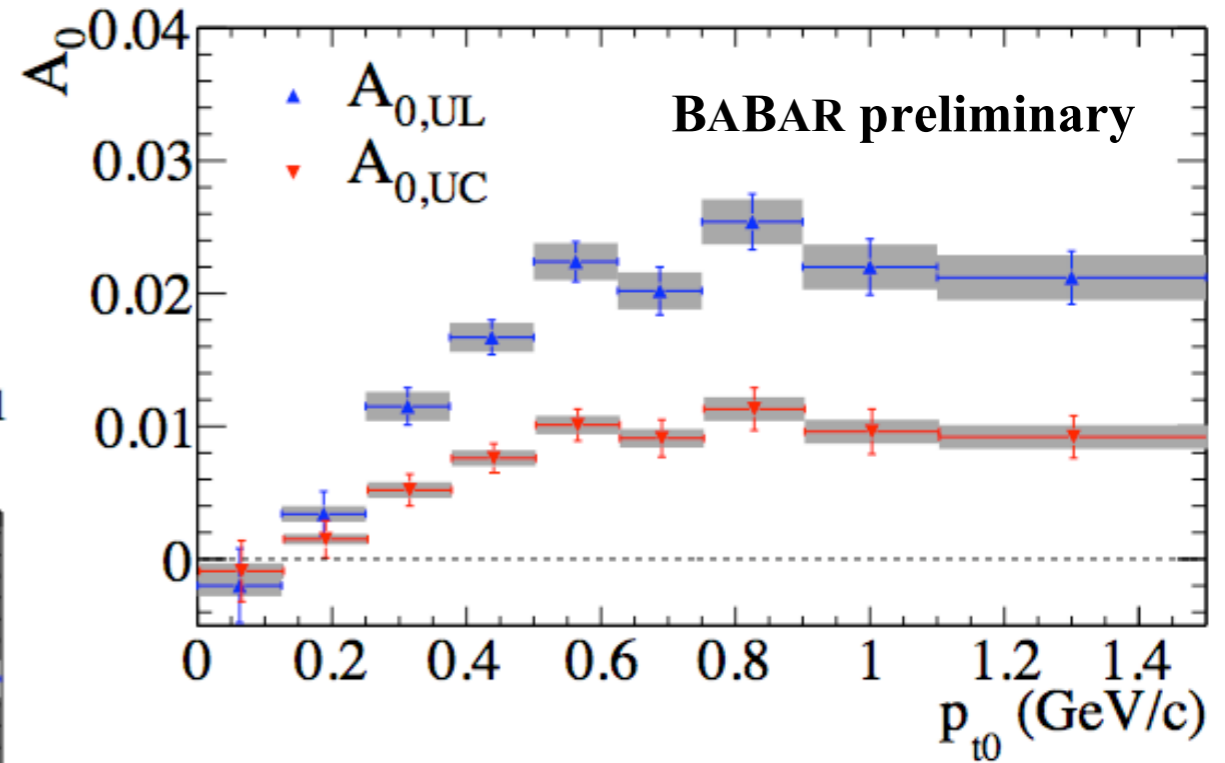
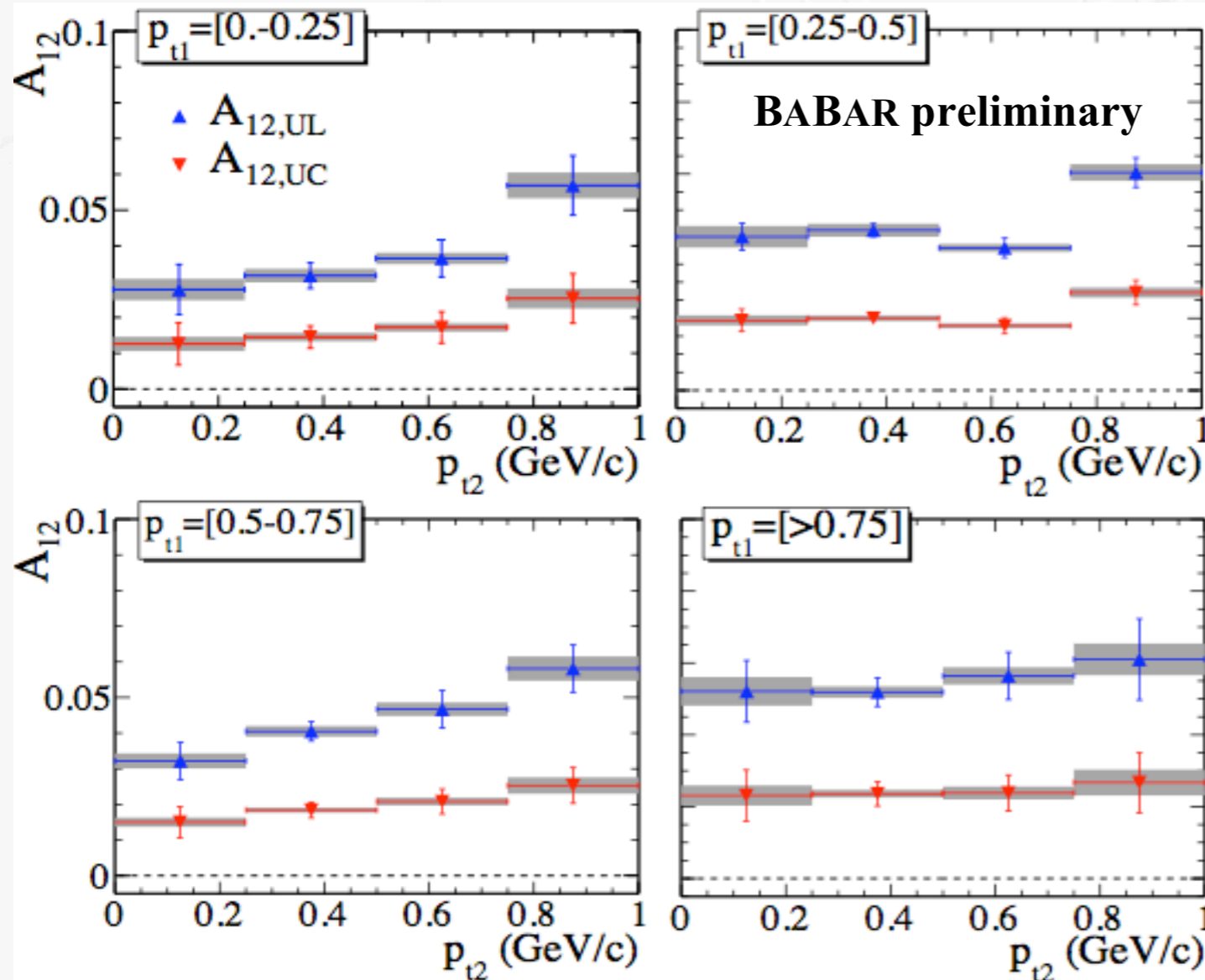


different convolutions over transverse momenta:

[Belle, PRD 86 (2012) 039905(E)] & [I. Garzia, DIS 2013]



# Collins FF from $e^+e^-$



**FIRST MEASUREMENT of Collins asymmetries vs.  $p_t$  in  $e^+e^-$  annihilation at  $Q^2 \sim 110$  (GeV/c) $^2$  (time-like region)**

- **nonzero  $A^{UL}$  and  $A^{UC}$**

- $\Rightarrow$  only modest dependence on  $(p_{t1}, p_{t2})$

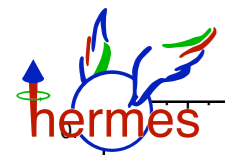
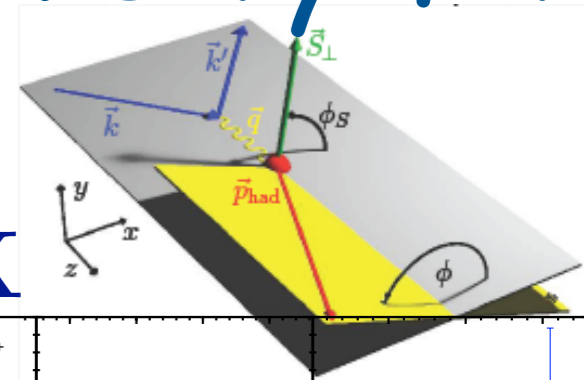
- $\Rightarrow A^{UC} < A^{UL}$ ; complementary information on  $H_1^{\perp, fav}$  and  $H_1^{\perp, dis}$

- $\Rightarrow A_0 < A_{12}$ , but interesting structure in  $p_t$

slide taken from [I. Garzia, DIS 2013]

# Collins FF and transversity fit

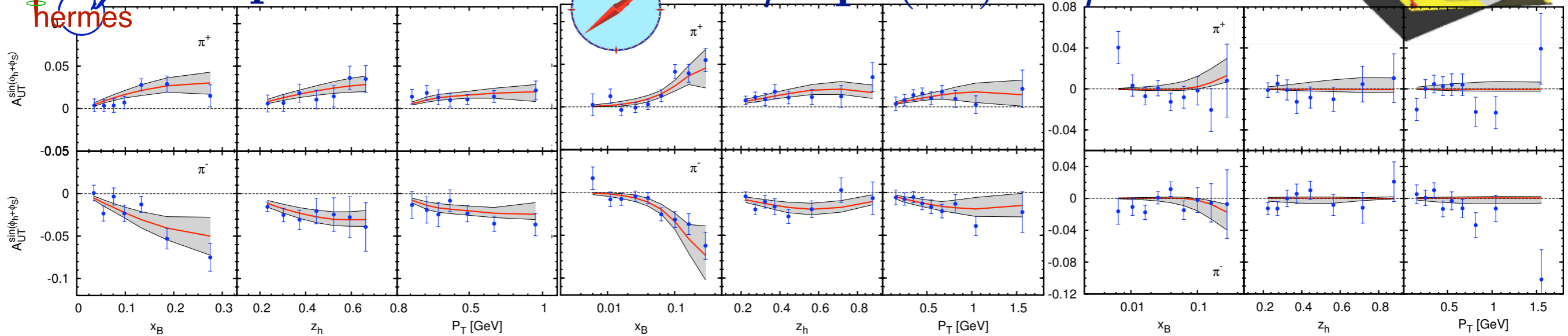
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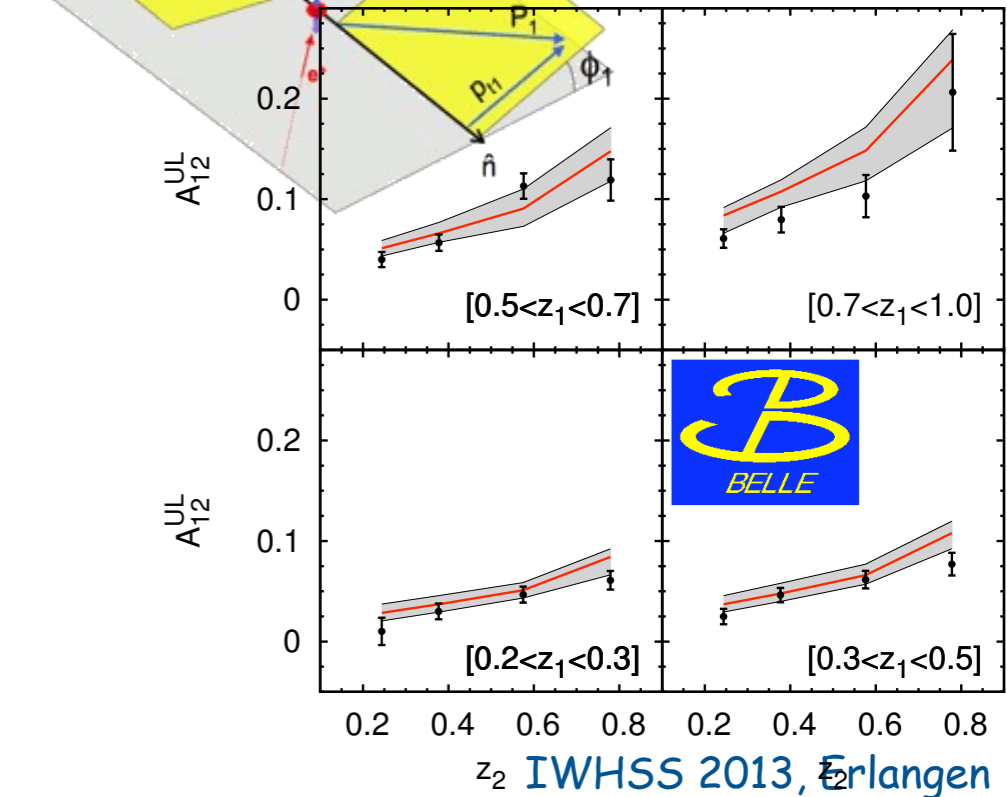
$$e^\pm p^\uparrow \rightarrow e^\pm \pi X$$



$$\mu^\pm p^\uparrow (d^\uparrow) \rightarrow \mu^\pm \pi X$$

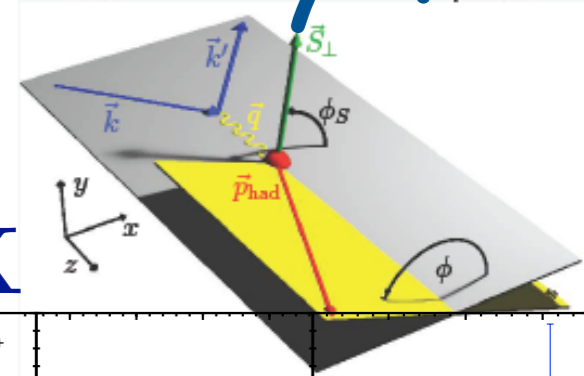


$$e^+e^- \rightarrow \pi\pi X$$



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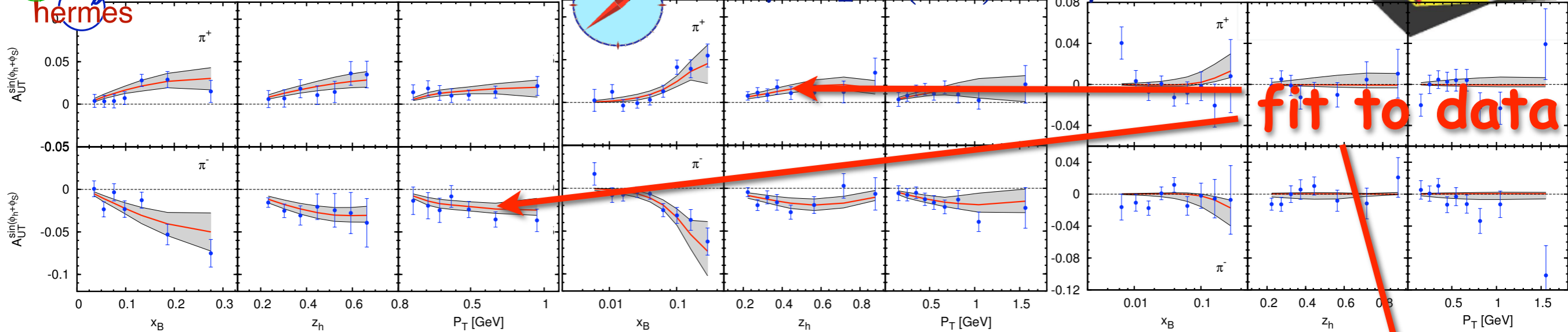
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**hermes**  $e^\pm p^\uparrow \rightarrow e^\pm \pi X$

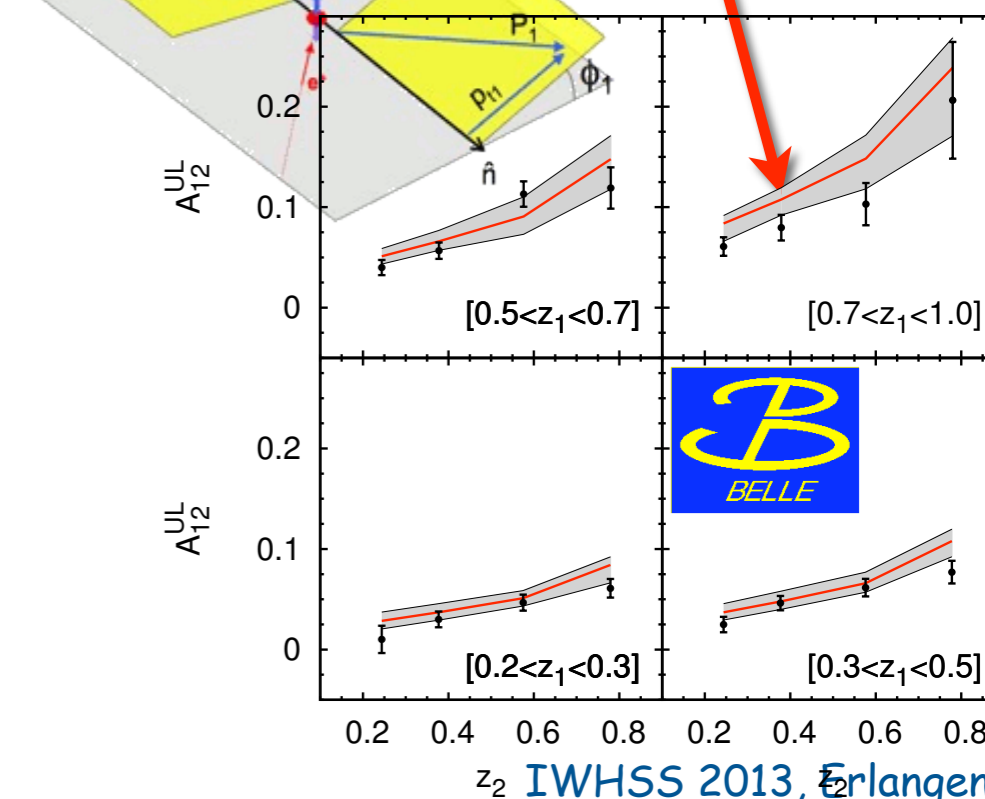


$\mu^\pm p^\uparrow (d^\uparrow) \rightarrow \mu^\pm \pi X$



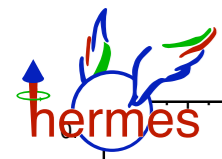
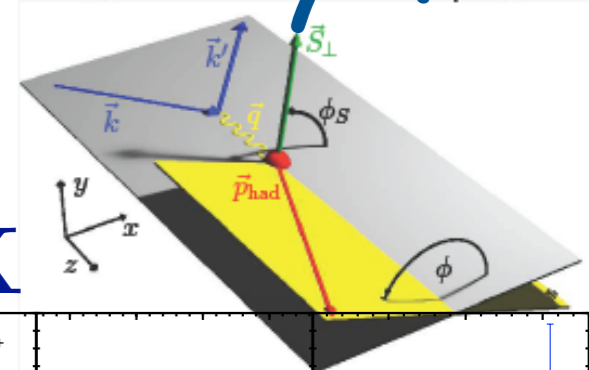
**fit to data**

$e^+e^- \rightarrow \pi\pi X$



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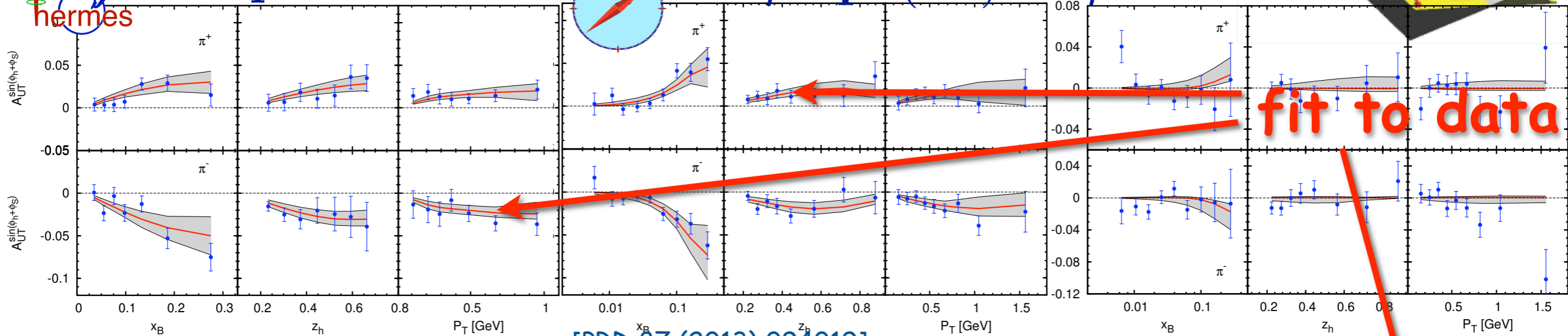
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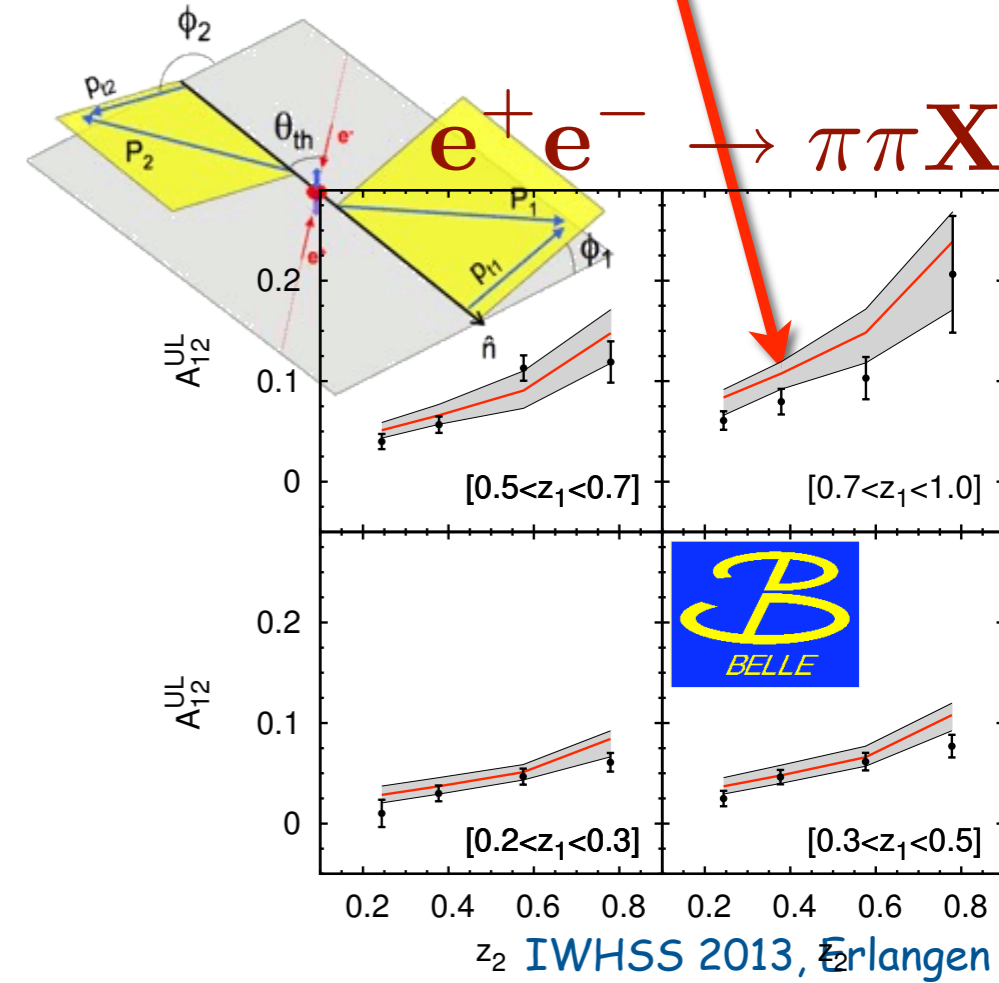
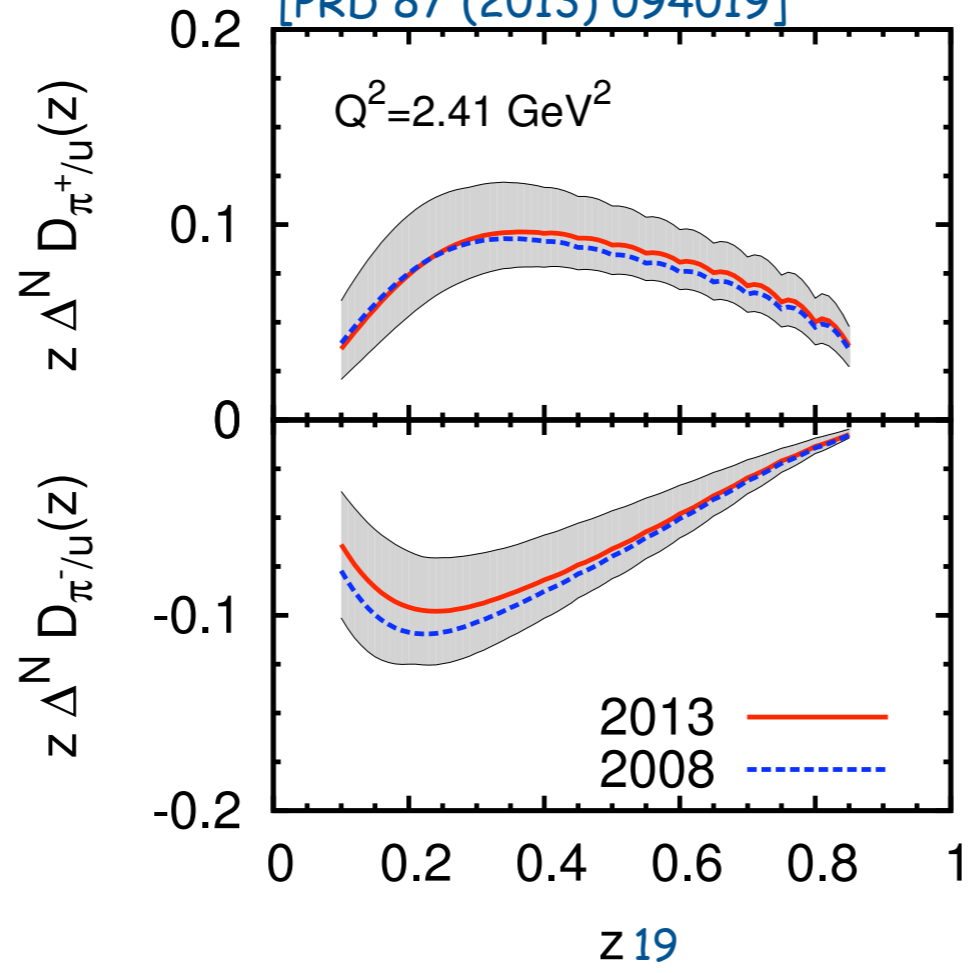


$$\mu^\pm p^\uparrow (d^\uparrow) \rightarrow \mu^\pm \pi X$$



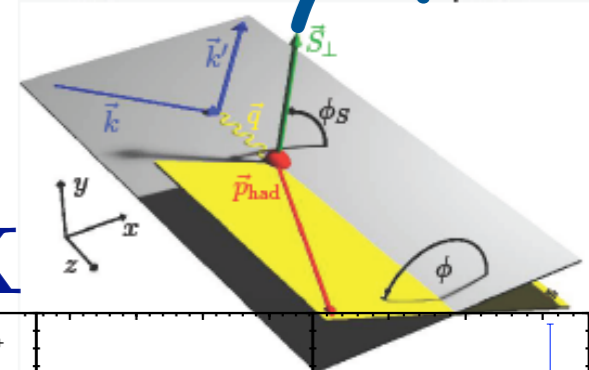
fit to data

[PRD 87 (2013) 094019]



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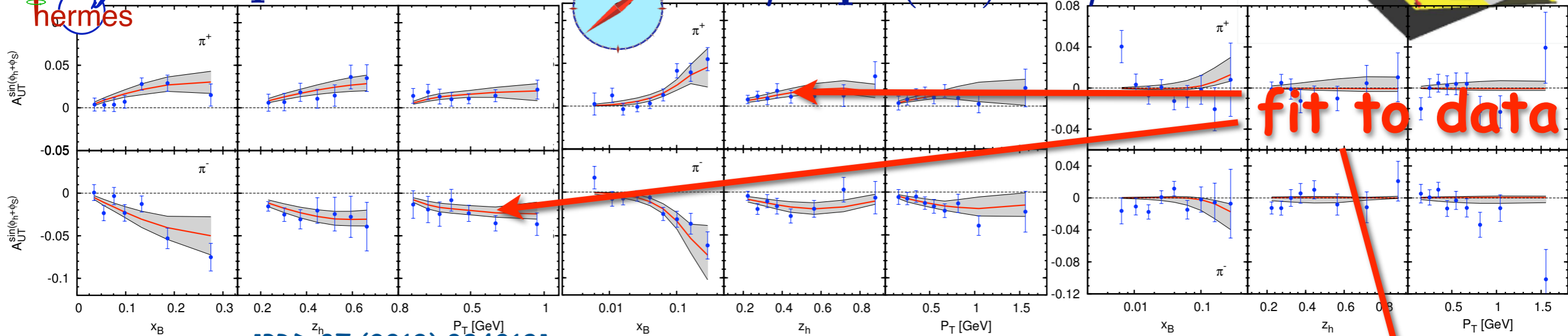
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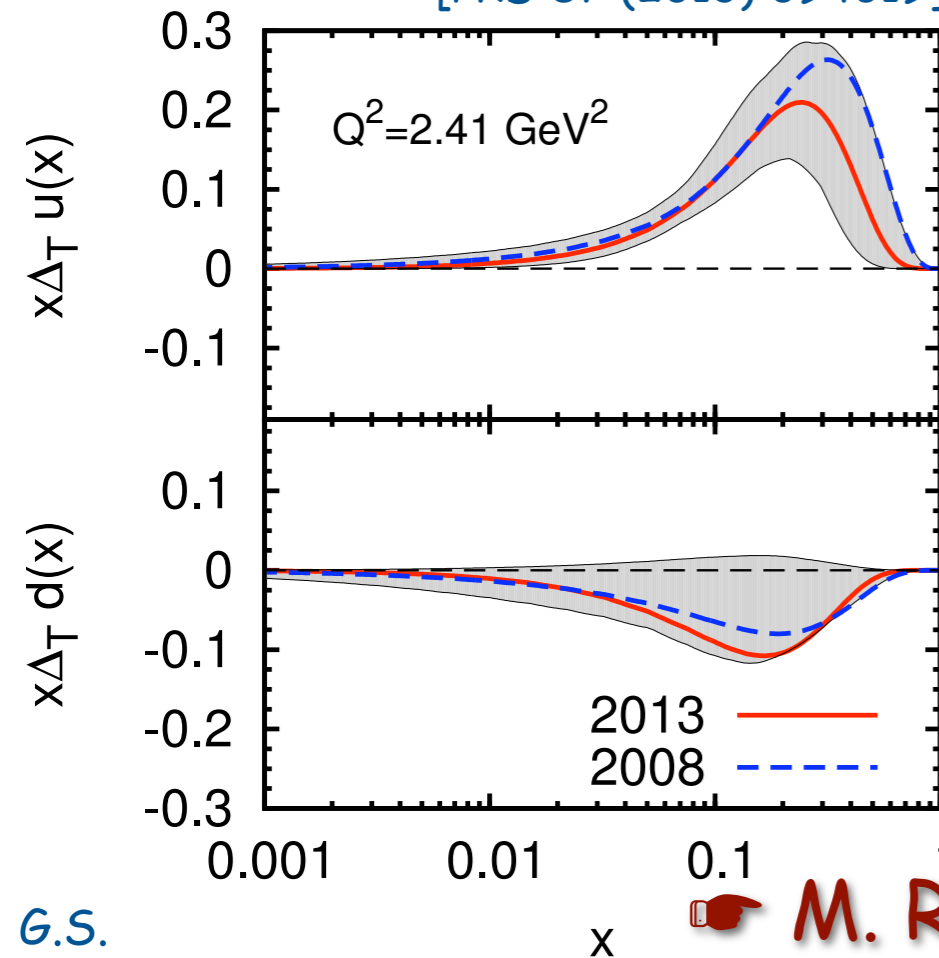
**hermes**  $e^\pm p^\uparrow \rightarrow e^\pm \pi X$



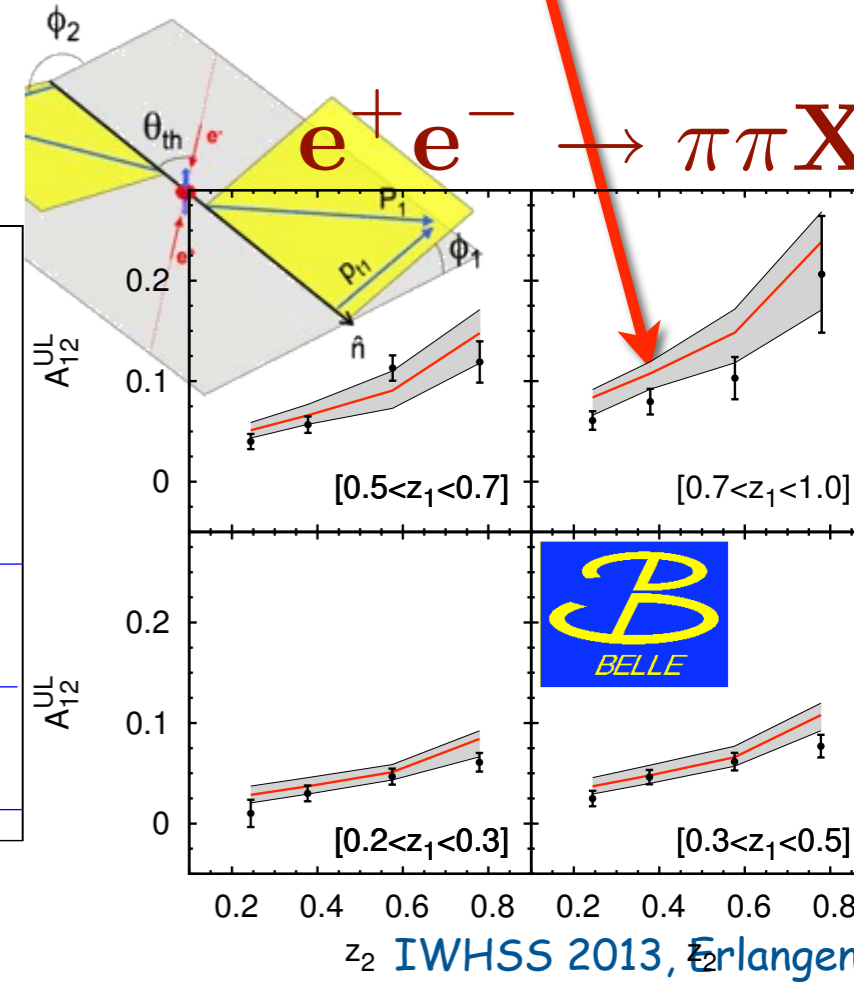
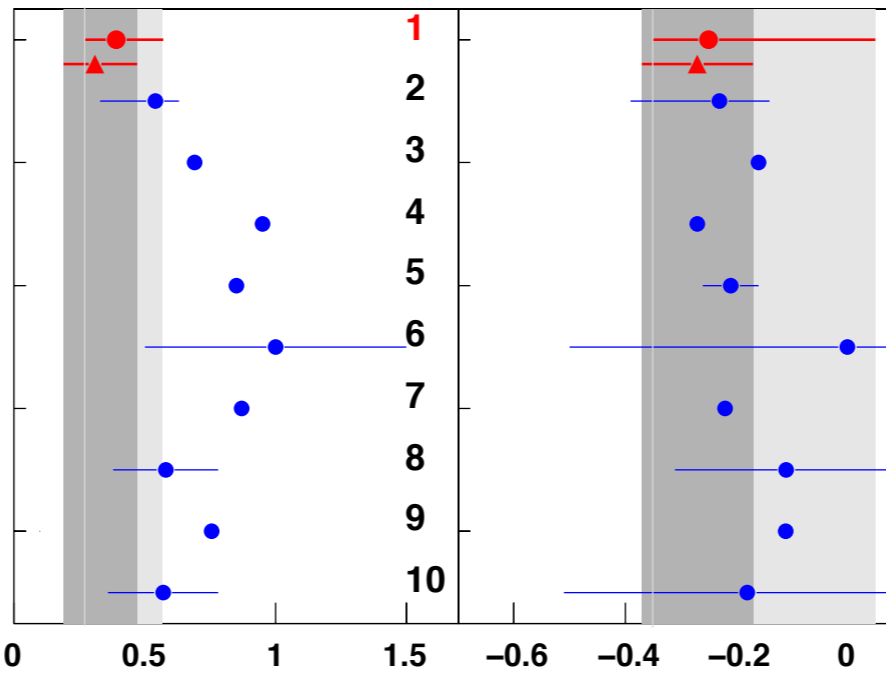
$\mu^\pm p^\uparrow (d^\uparrow) \rightarrow \mu^\pm \pi X$



[PRD 87 (2013) 094019]



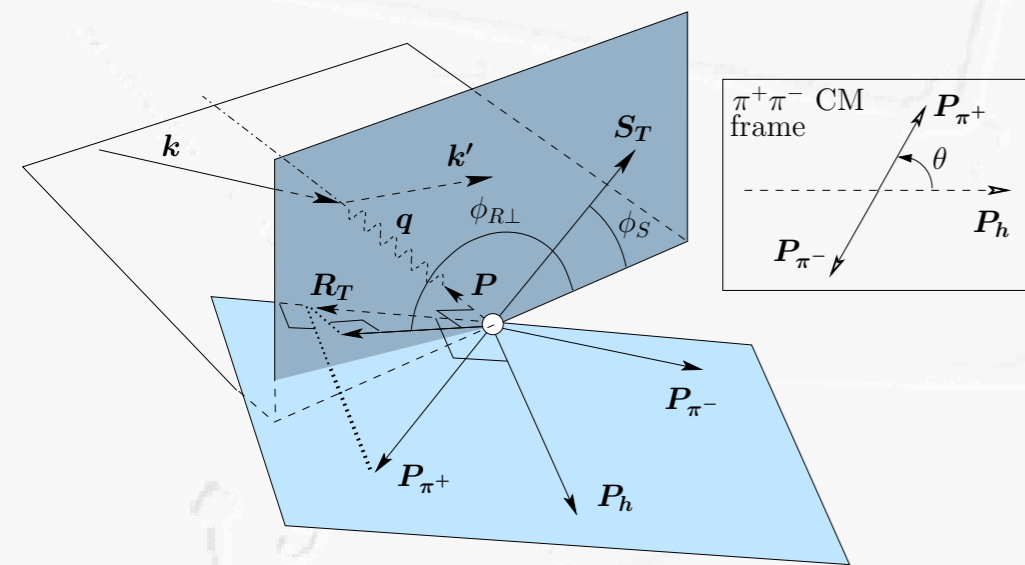
- $\delta u = 0.39^{+0.18}_{-0.12}$
- $\delta d = -0.25^{+0.30}_{-0.10}$
- ▲  $\delta u = 0.31^{+0.16}_{-0.12}$
- ▲  $\delta d = -0.27^{+0.10}_{-0.10}$



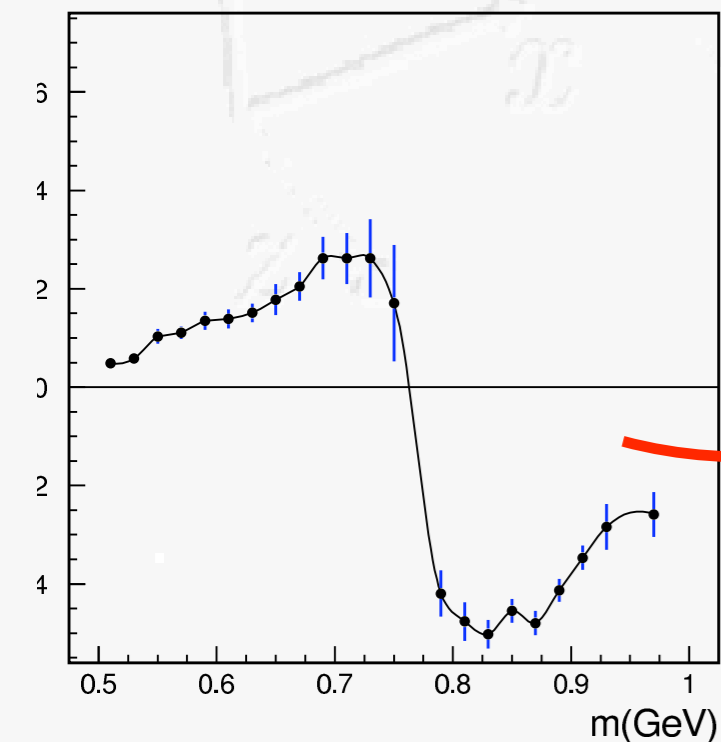
**M. Radici & M. Boglione**

# Transversity through 2-hadron fragmentation

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$



$$A_{UT} \sim \sin(\phi_{R\perp} + \phi_S) \sin\theta h_1 H_1^{\triangleleft}$$



Jaffe et al. [hep-ph/9709322]:

$$H_1^{\triangleleft, sp}(z, M_{\pi\pi}^2) = \frac{\sin\delta_0 \sin\delta_1 \sin(\delta_0 - \delta_1) H_1^{\triangleleft, sp'}(z)}{\delta_0 (\delta_1) \rightarrow \text{S(P)-wave phase shifts}}$$

$$= \mathcal{P}(M_{\pi\pi}^2) H_1^{\triangleleft, sp'}(z)$$

$\Rightarrow A_{UT}$  might depend strongly on  $M_{\pi\pi}$



# Transversity distribution (2-hadron fragmentation)

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

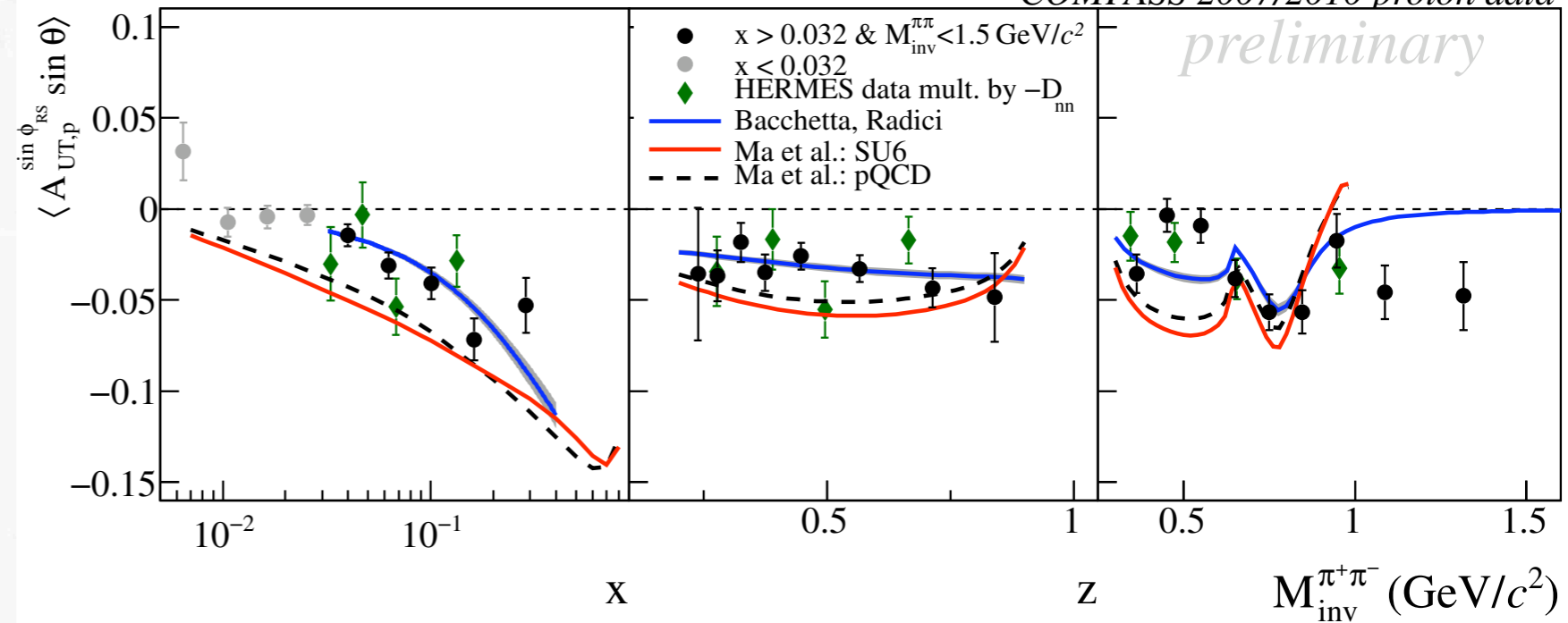
- HERMES, COMPASS:  
for comparison scaled  
HERMES data by  
depolarization factor and  
changed sign
- $^2\text{H}$  results consistent with  
zero

[A. Airapetian et al., JHEP 06 (2008) 017]

COMPASS 2007: [C. Adolph et al., Phys. Lett. B713 (2012) 10]

COMPASS 2010: [C. Braun et al., Nuovo Cimento C 035 (2012) 02]

COMPASS 2007/2010 proton data



# Transversity distribution (2-hadron fragmentation)

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

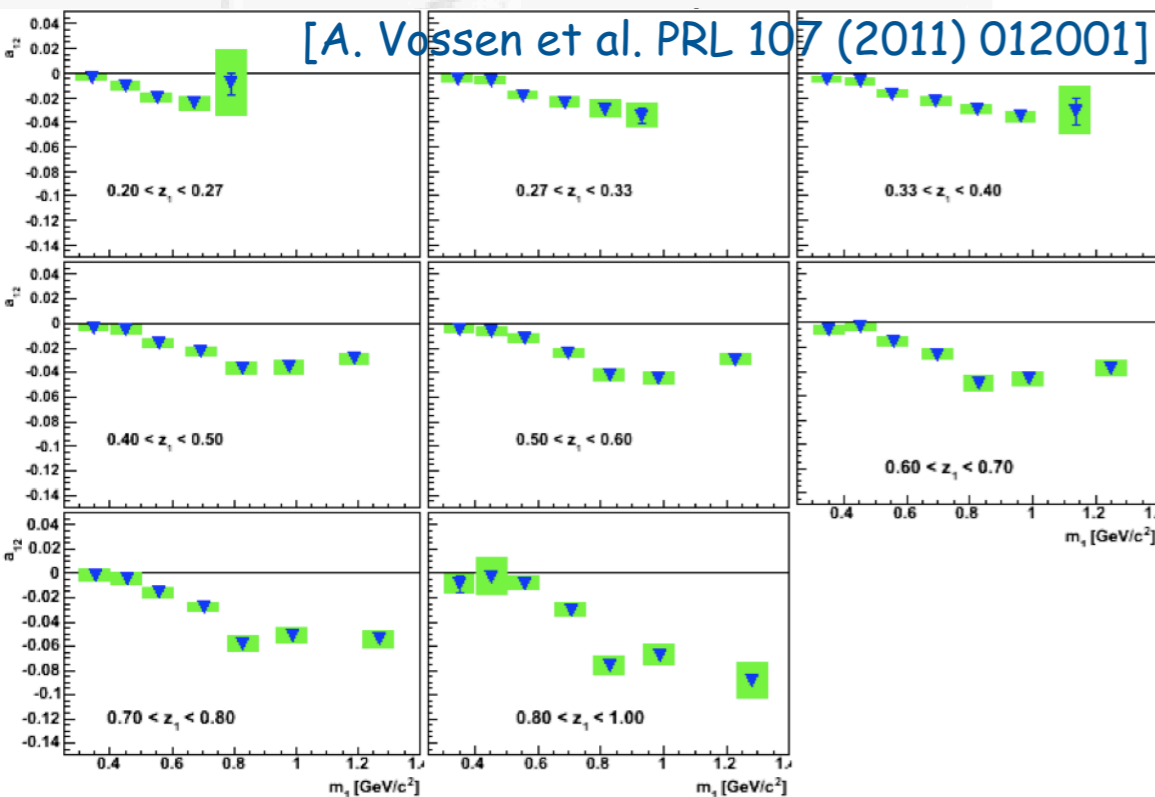
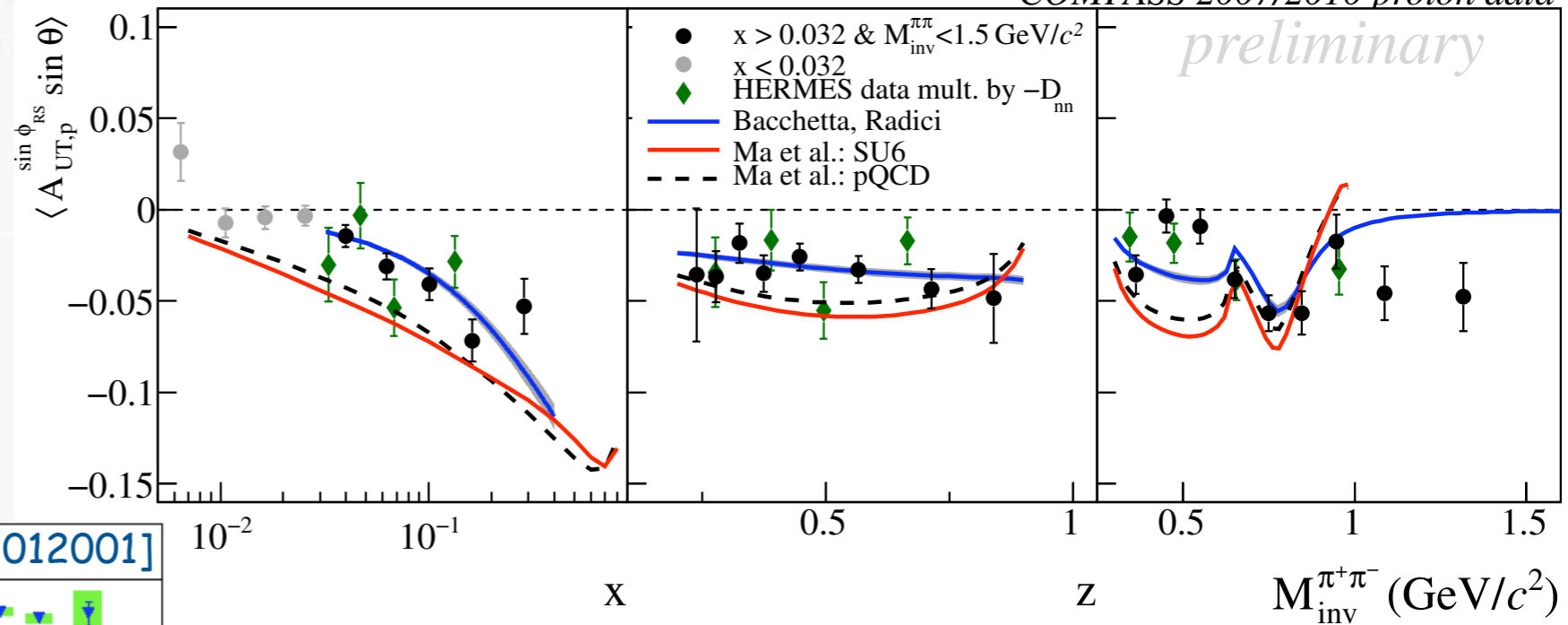
- HERMES, COMPASS: for comparison scaled HERMES data by depolarization factor and changed sign
- $^2\text{H}$  results consistent with zero

[A. Airapetian et al., JHEP 06 (2008) 017]

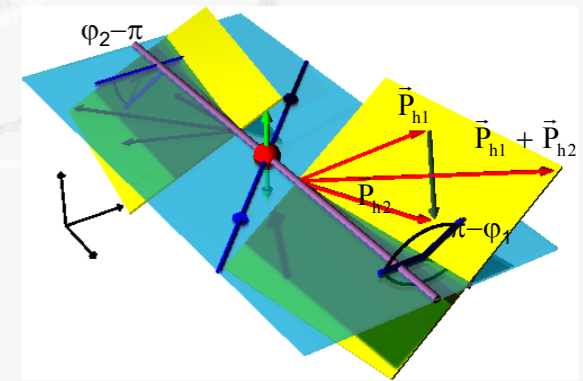
COMPASS 2007: [C. Adolph et al., Phys. Lett. B713 (2012) 10]

COMPASS 2010: [C. Braun et al., Nuovo Cimento C 035 (2012) 02]

COMPASS 2007/2010 proton data



- data from  $e^+e^-$  by BELLE



# Transversity distribution (2-hadron fragmentation)

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

[A. Airapetian et al., JHEP 06 (2008) 017]

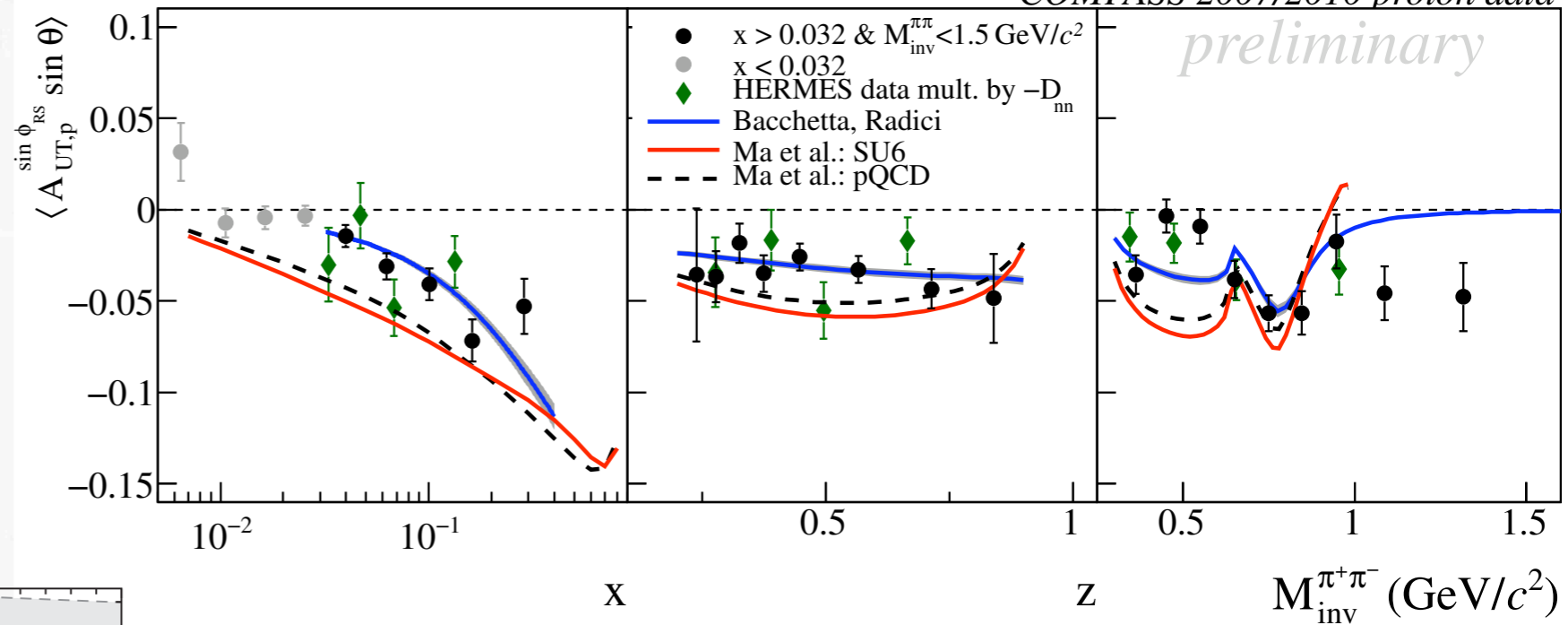
COMPASS 2007: [C. Adolph et al., Phys. Lett. B713 (2012) 10]

COMPASS 2010: [C. Braun et al., Nuovo Cimento C 035 (2012) 02]

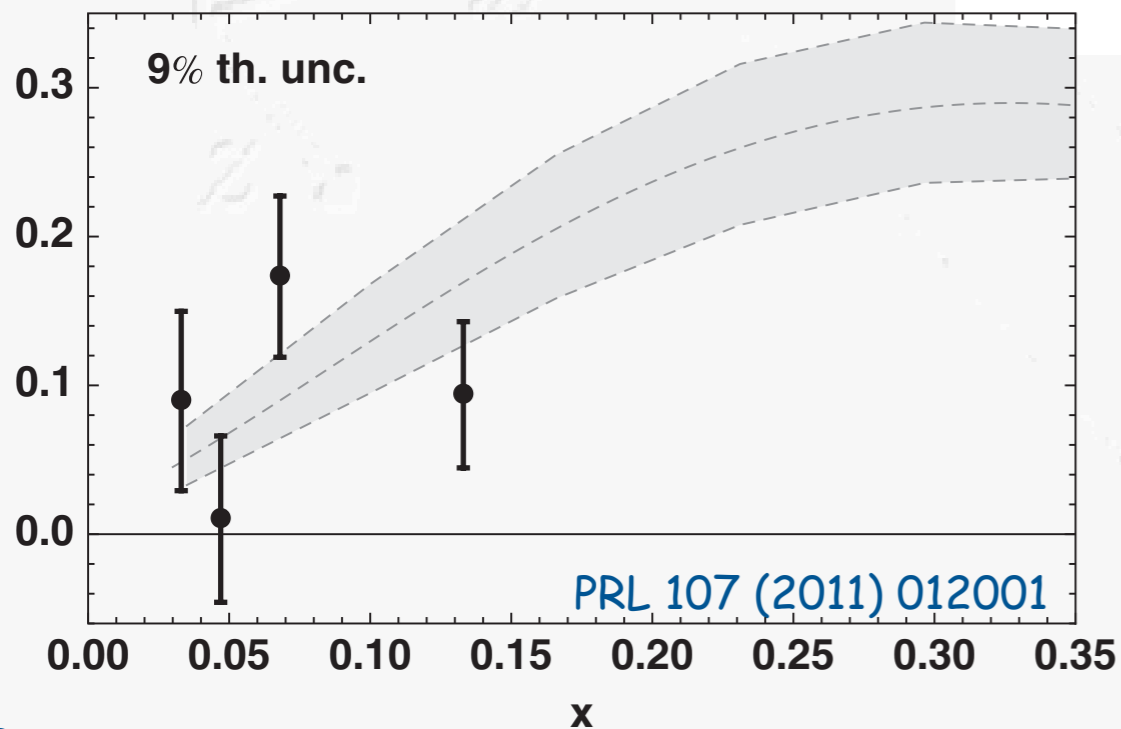
- HERMES, COMPASS: for comparison scaled HERMES data by depolarization factor and changed sign

- $^2\text{H}$  results consistent with zero

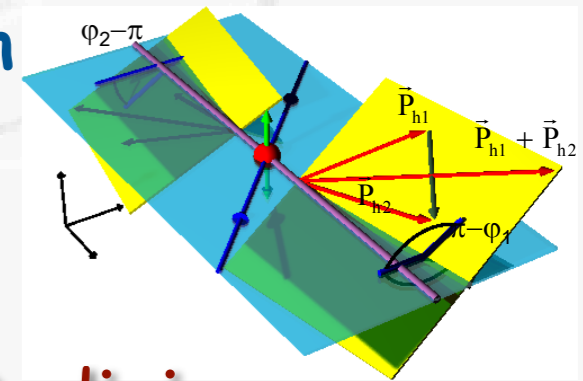
COMPASS 2007/2010 proton data



$$x h_1^{u_v}(x) - x h_1^{d_v}(x)/4$$



- data from  $e^+e^-$  by BELLE allow first (collinear) extraction of transversity (compared to Anselmino et al.)

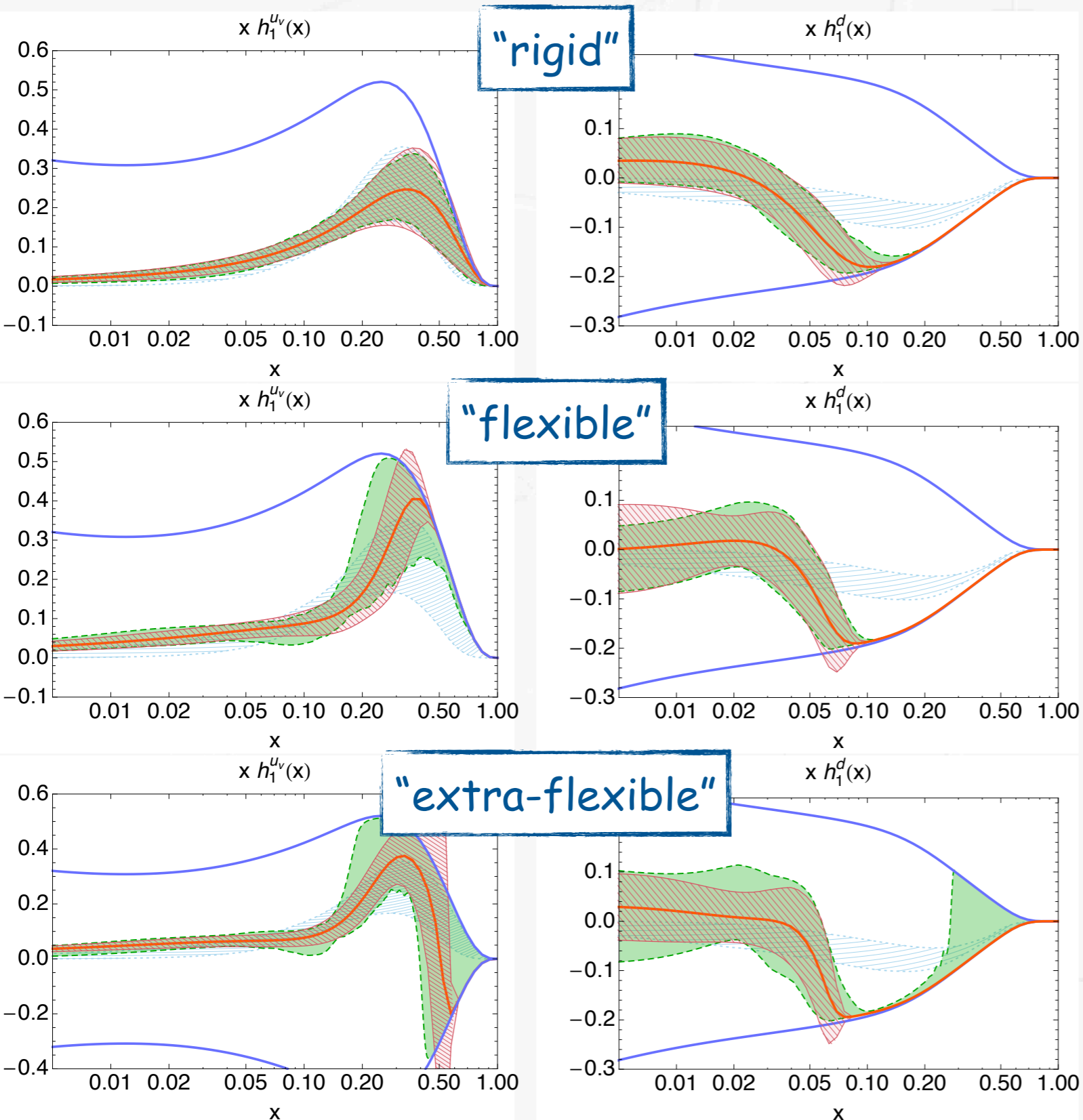


- updated analysis

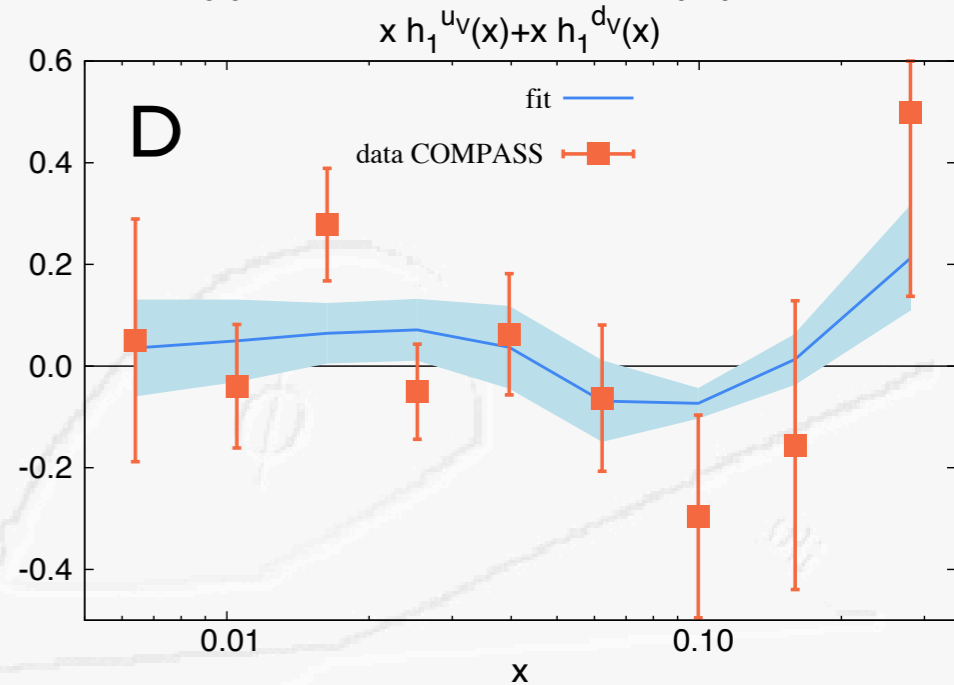
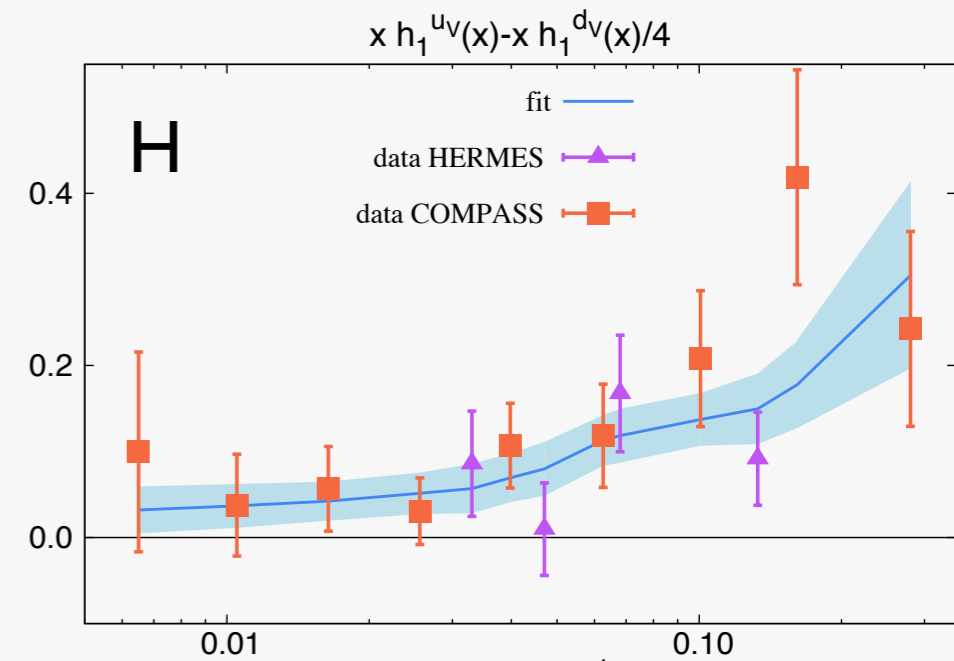
M. Radici

IWHSS 2013, Erlangen

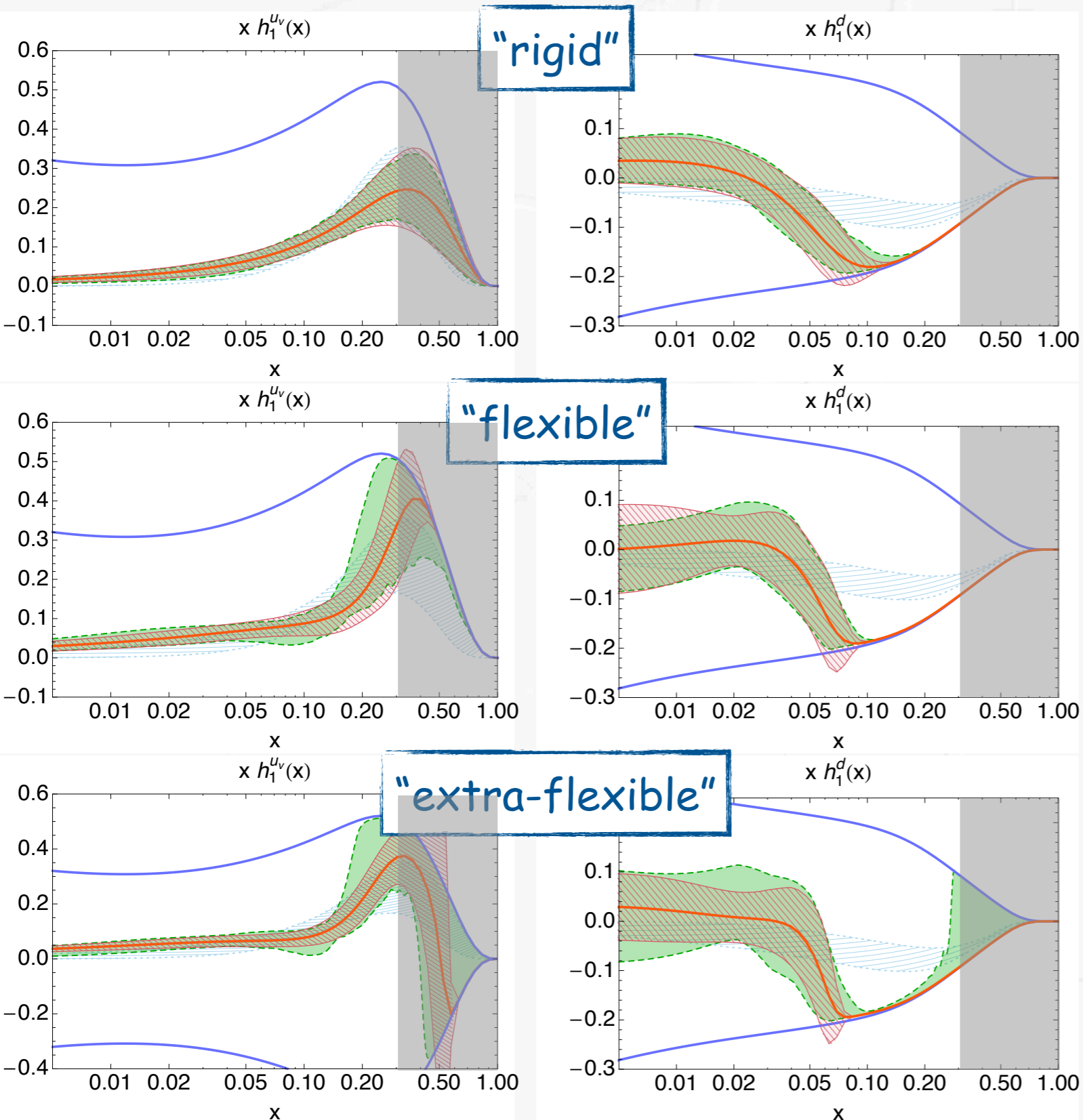
# collinear extraction of valence transversity



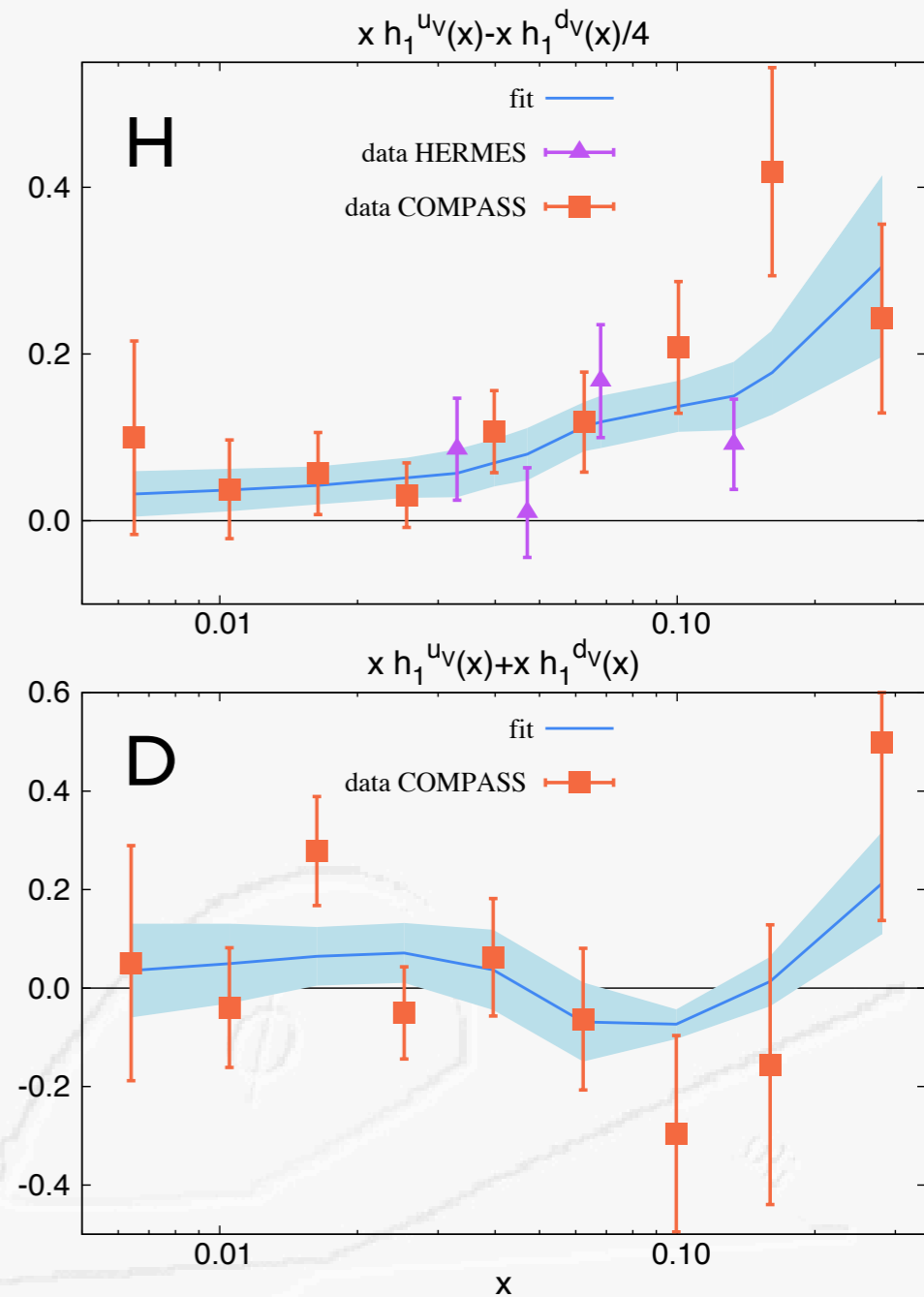
[A. Bacchetta et al. JHEP 03 (2013) 119]



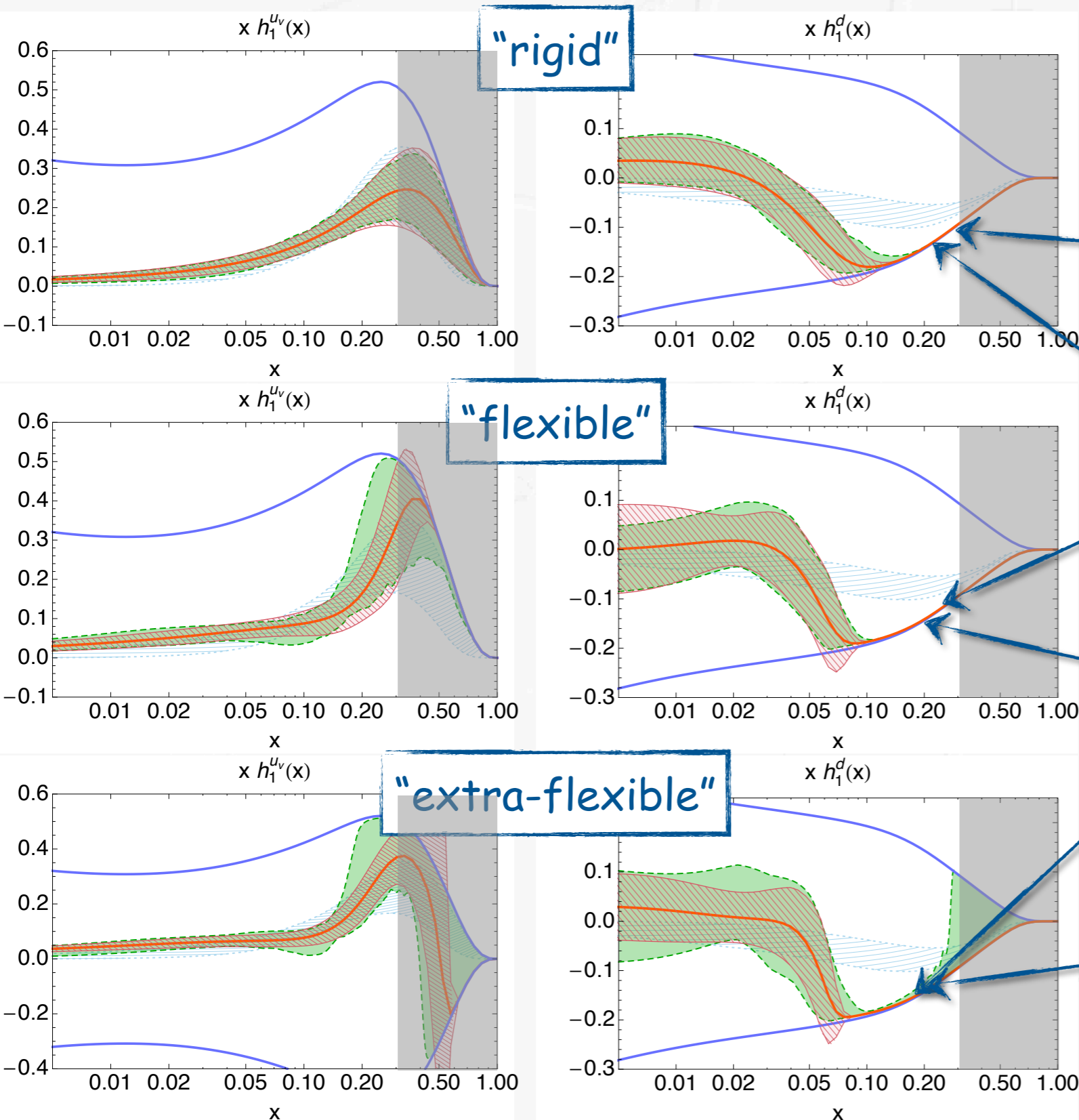
# collinear extraction of valence transversity



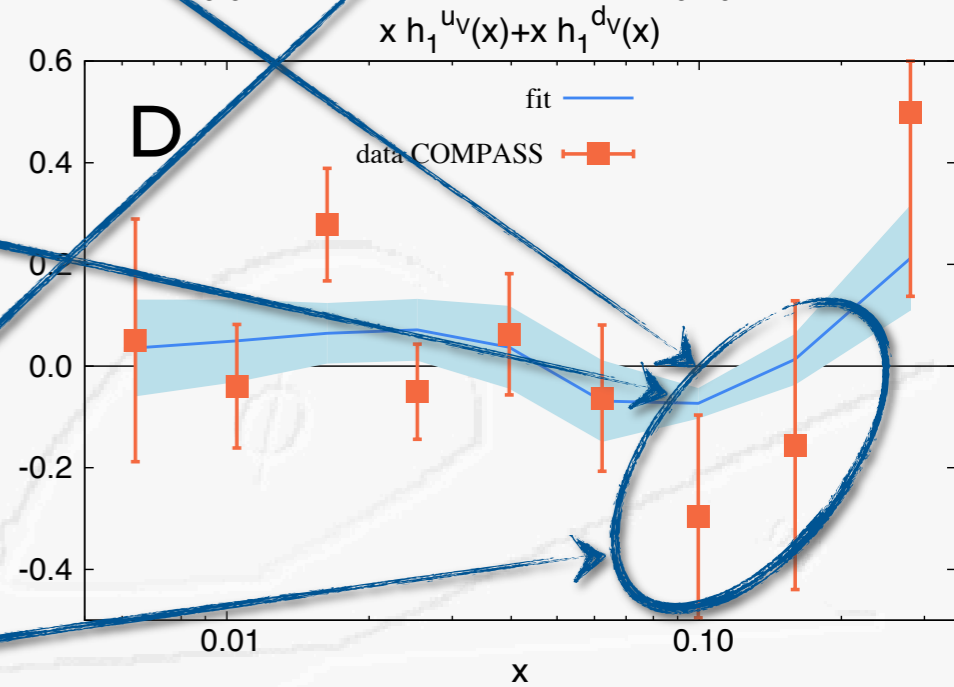
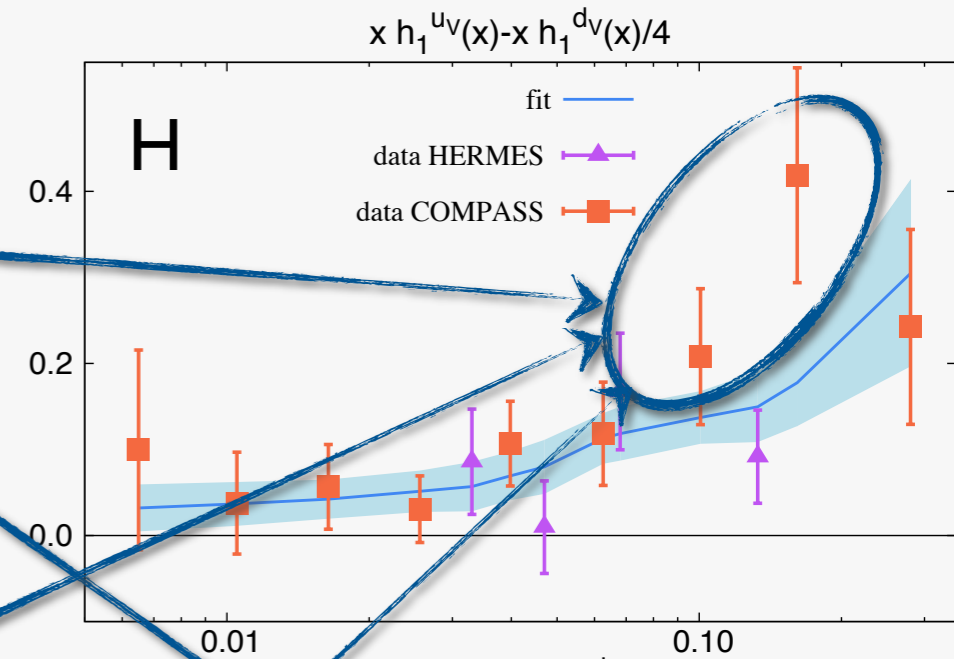
[A. Bacchetta et al. JHEP 03 (2013) 119]



# collinear extraction of valence transversity



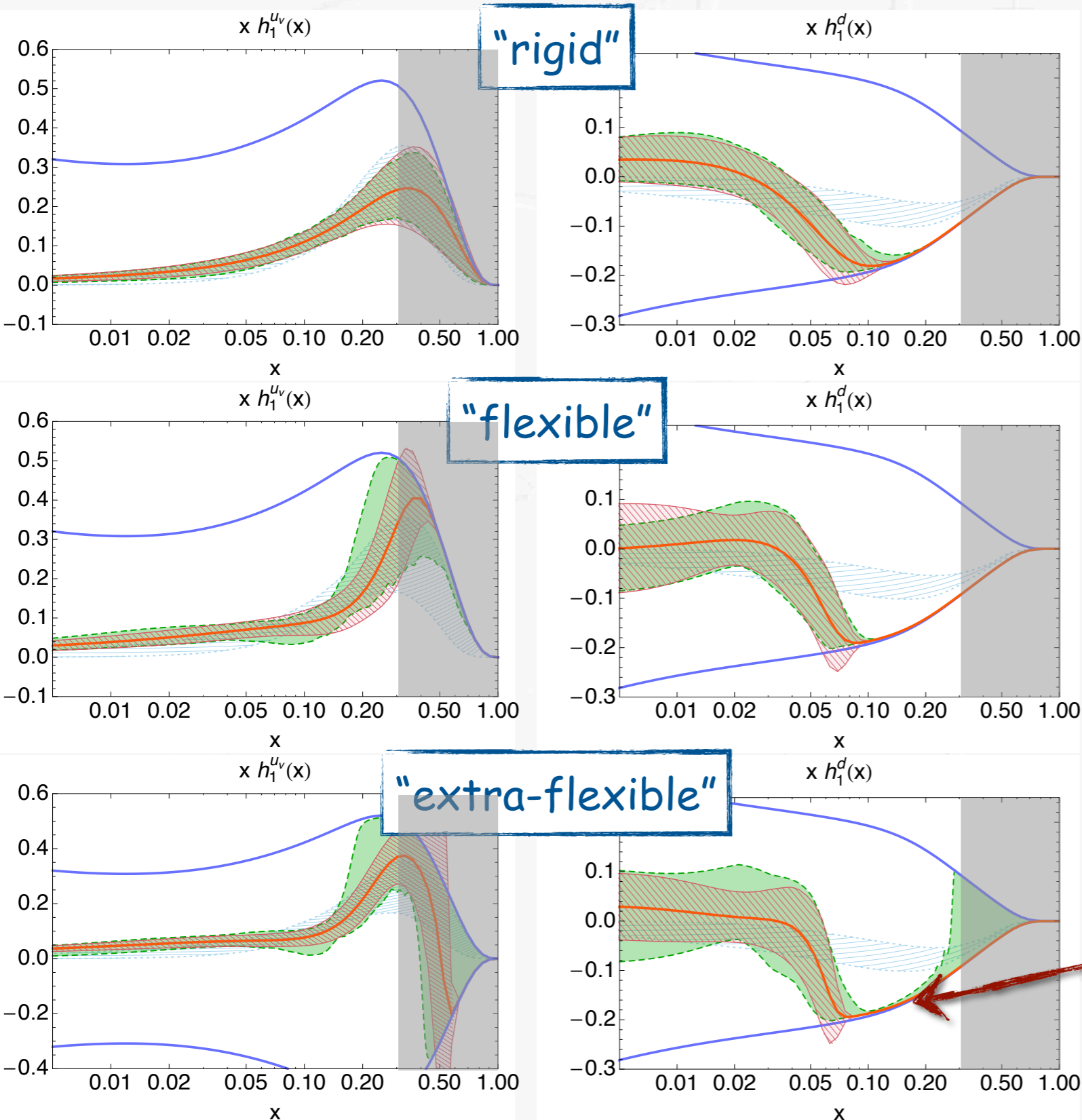
[A. Bacchetta et al. JHEP 03 (2013) 119]



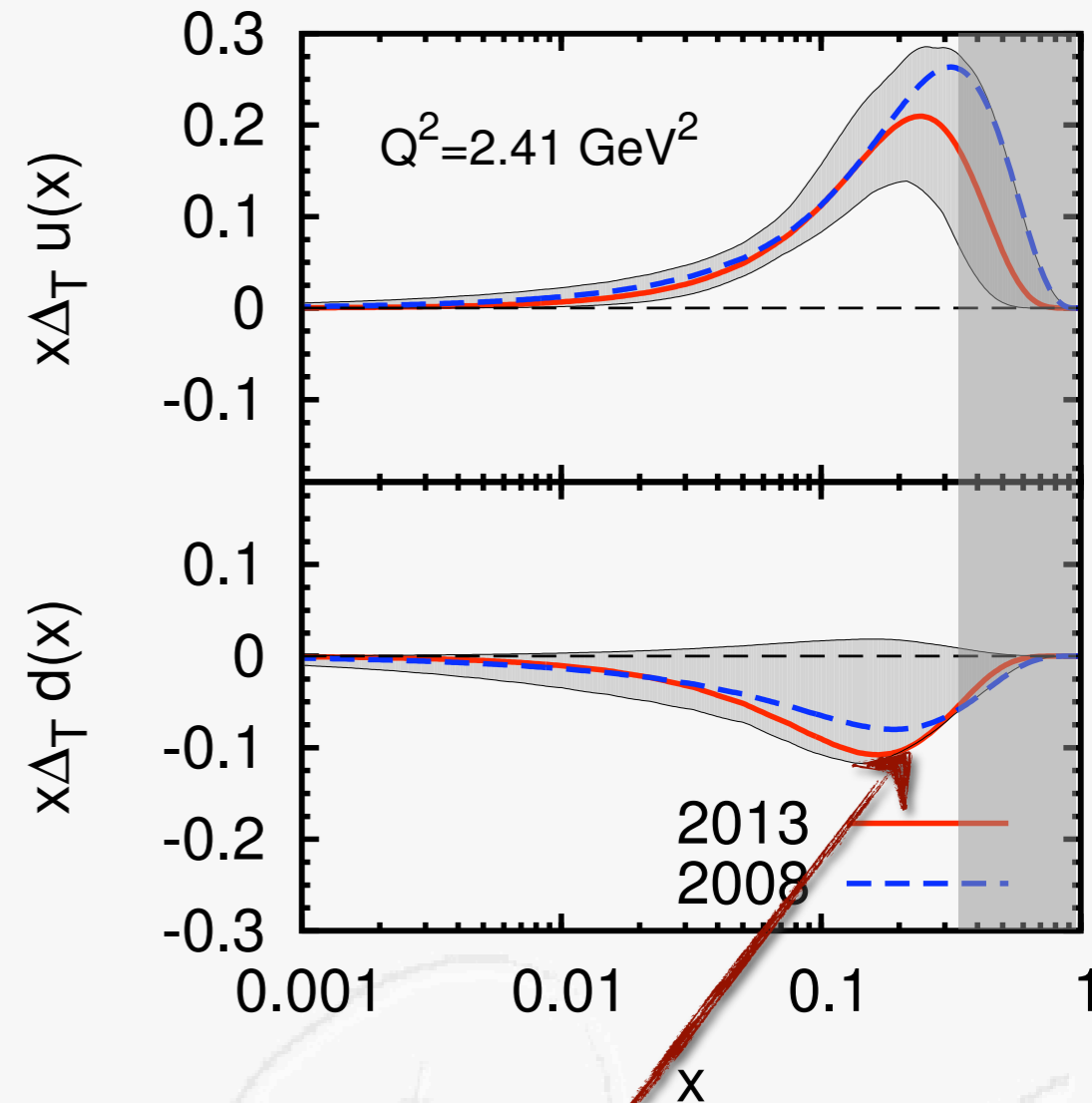
$$|h_1^q(x)| \leq \frac{1}{2} [f_1^q(x) + g_1^q(x)]$$

# $d_v$ -transversity Soffer bound

[A. Bacchetta et al. JHEP 03 (2013) 119]



[M. Anselmino et al., PRD 87 (2013) 094019]



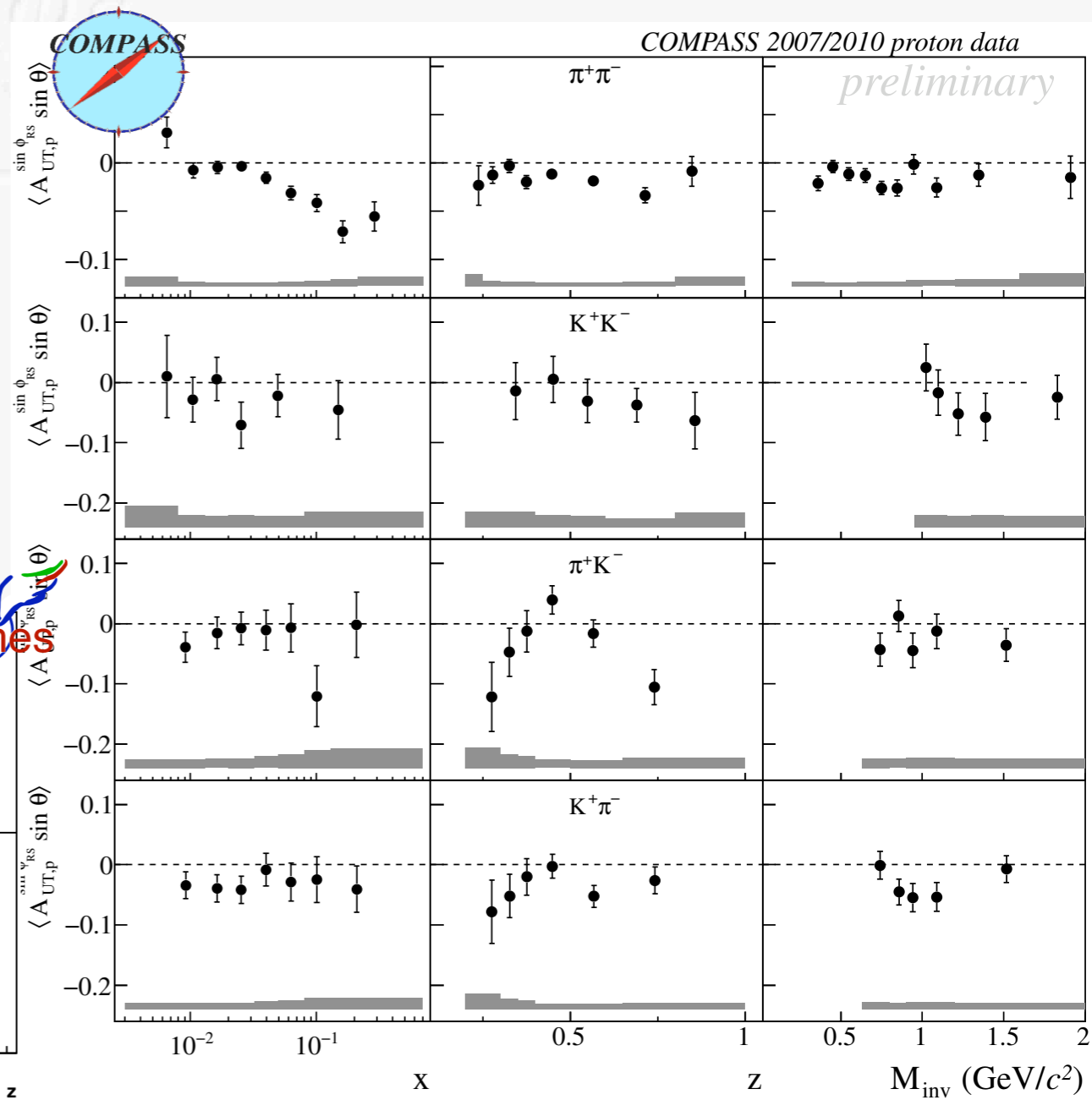
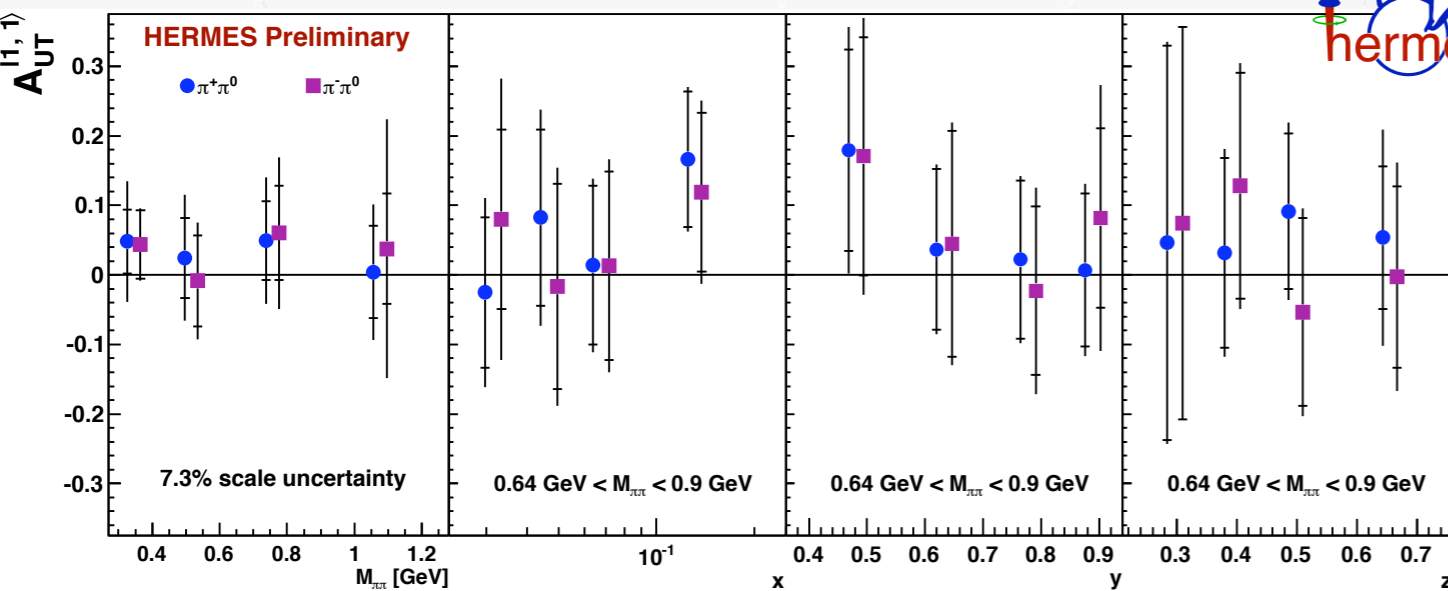
general trend towards violating d-Soffer bound?

$$|h_1^q(x)| \leq \frac{1}{2} [f_1^q(x) + g_1^q(x)]$$

# Transversity distribution (2-hadron fragmentation)

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

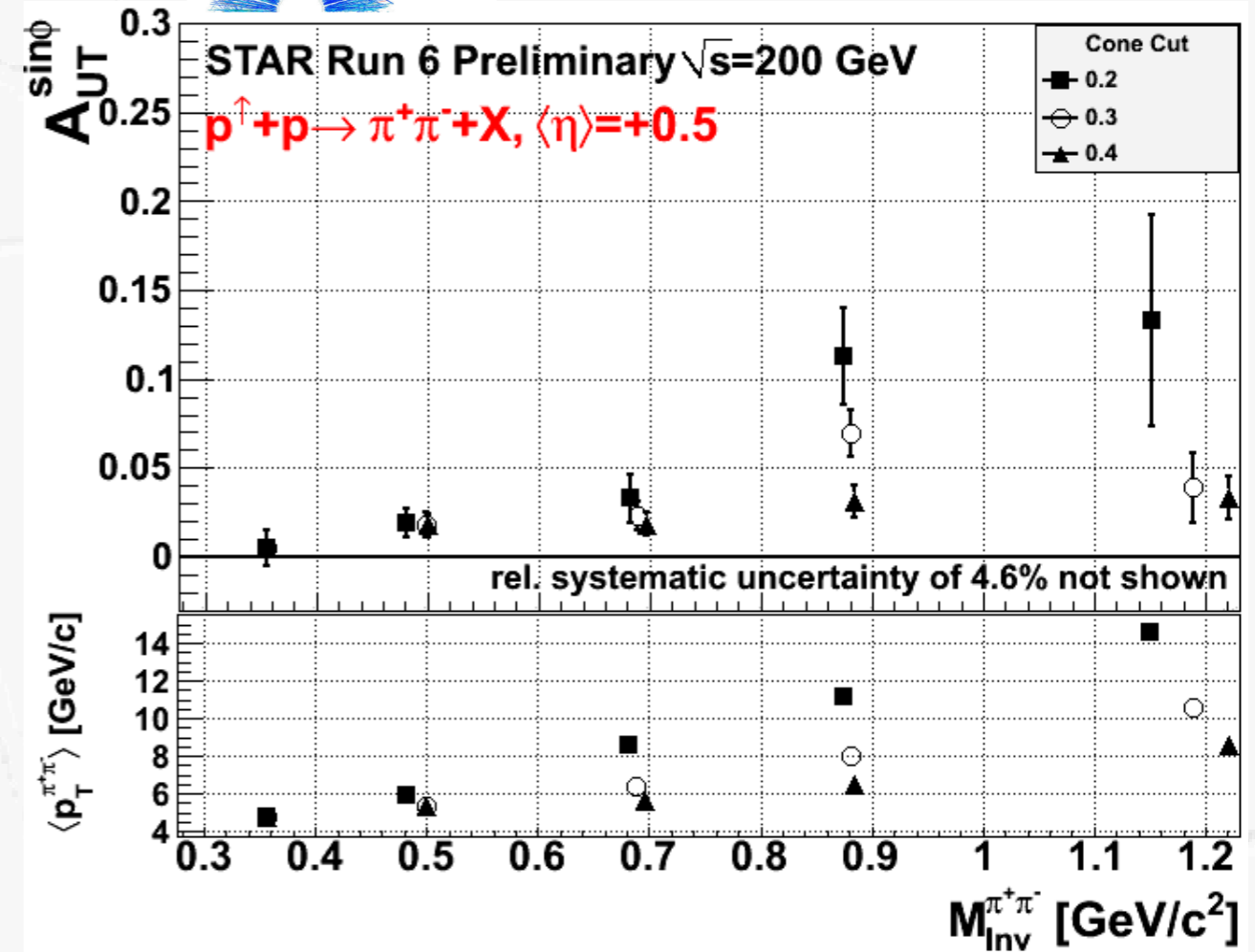
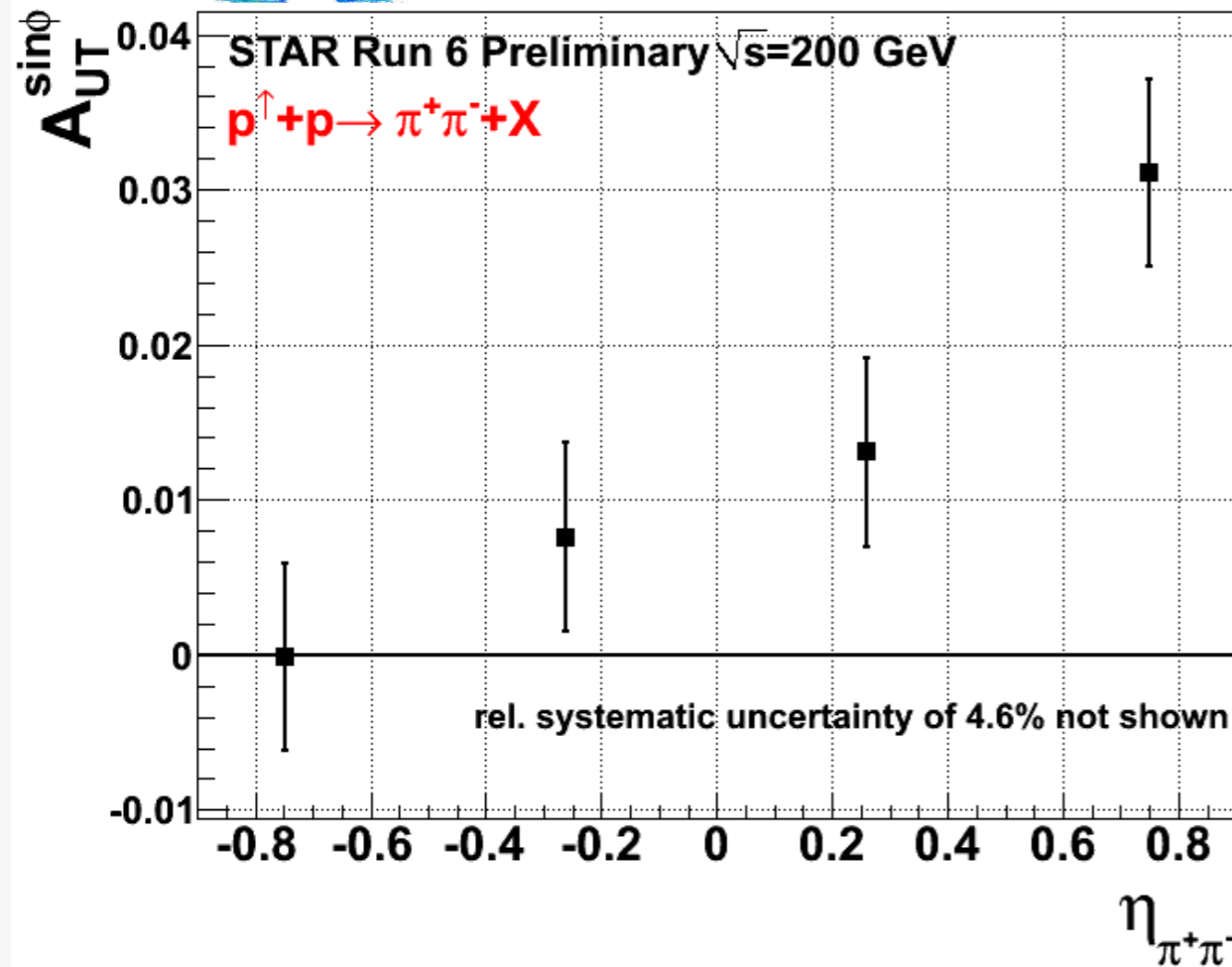
- new preliminary results on various other hadron combinations
- COMPASS: charged  $\pi^\pm K^\mp$
- HERMES:  $\pi^\pm \pi^0$





	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

# First signal of transversity from polarized $p^\uparrow p \rightarrow \pi^+ \pi^- X$



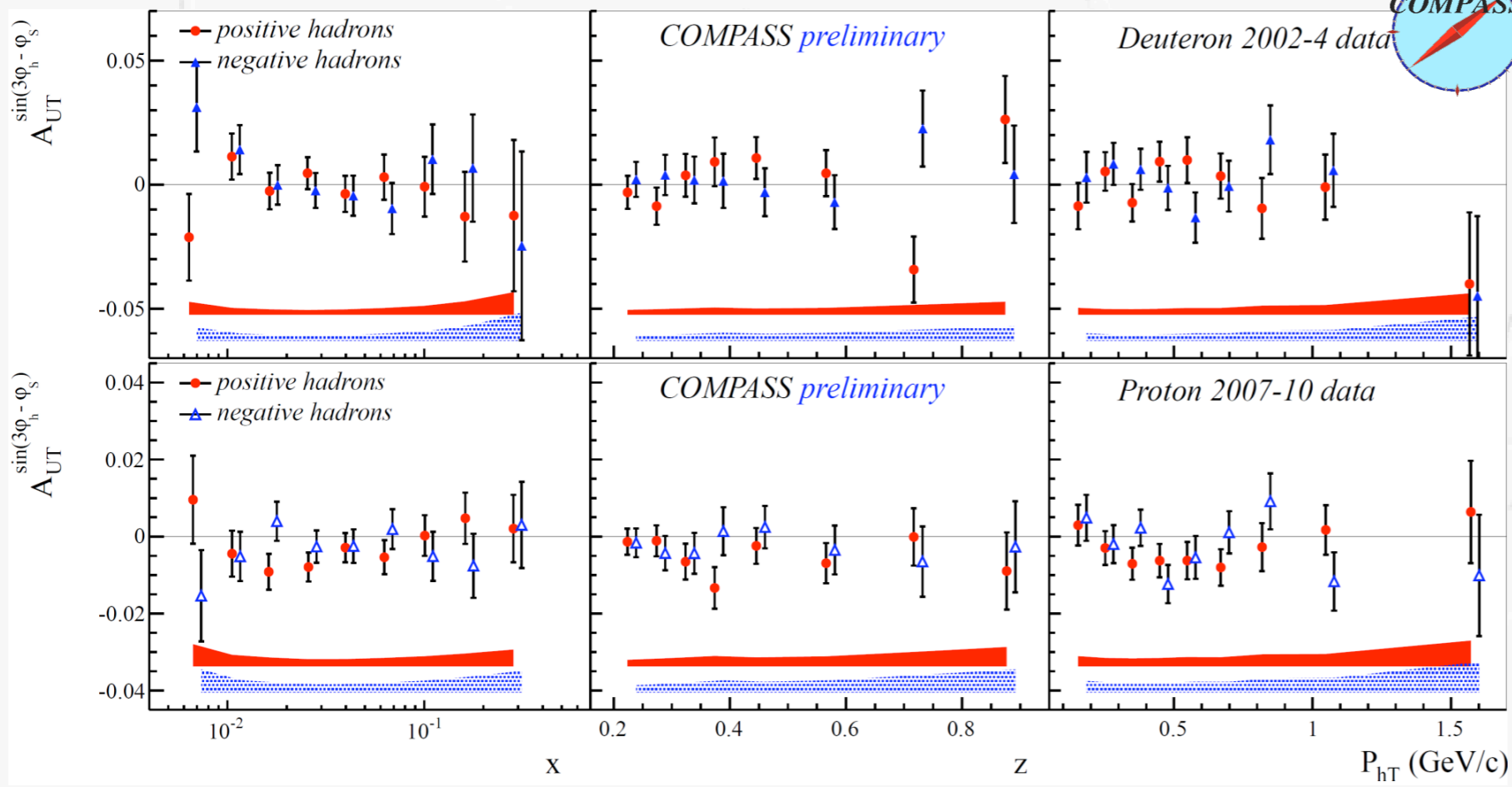
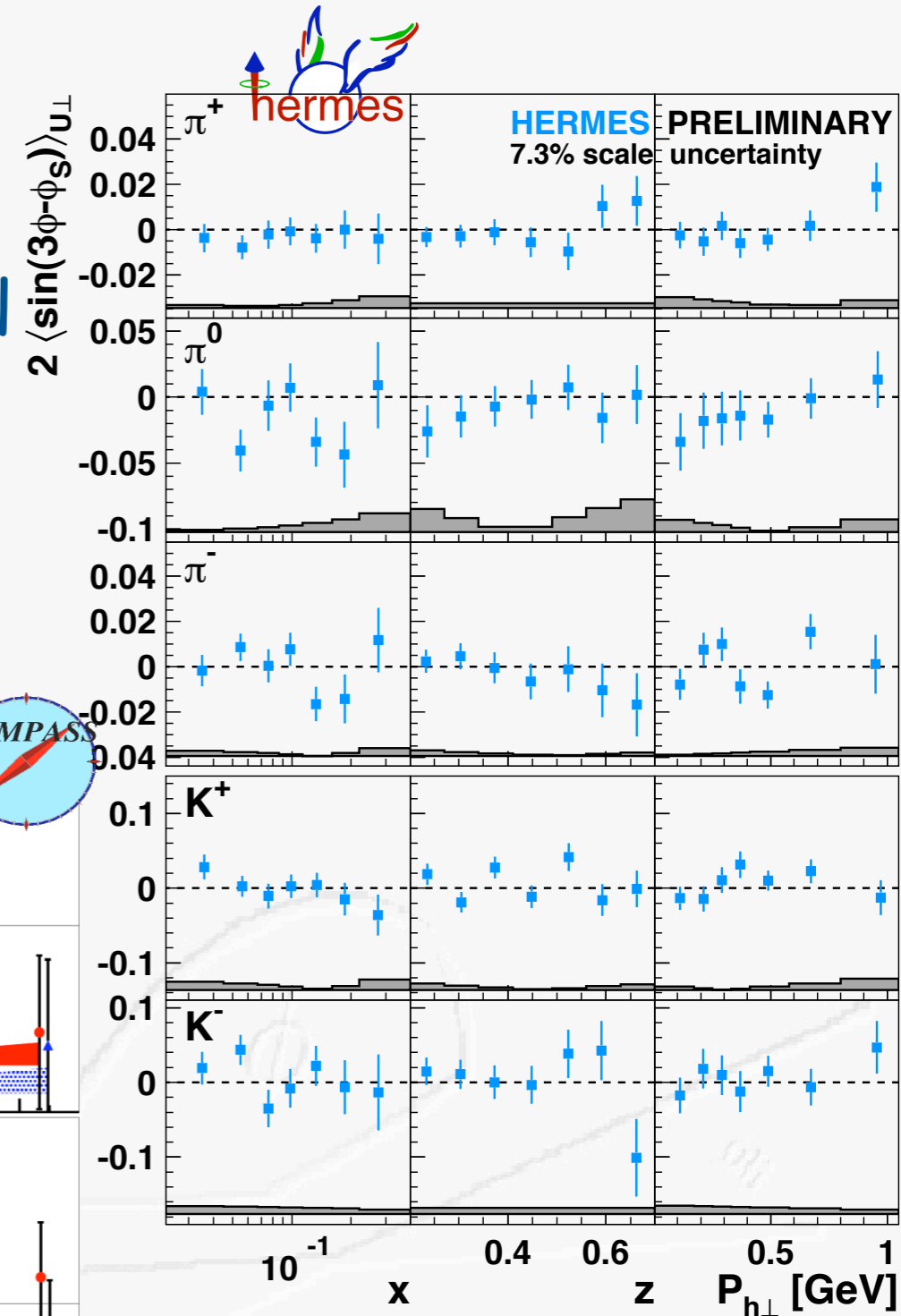
- forward region  $\rightarrow$  valence effect from polarized (beam) proton?
- previous mid-rapidity preliminary data from PHENIX consistent with zero
- dependence on cone cut; due to underlying  $p_T$  dependence?

Transversity's friends

# Pretzelosity

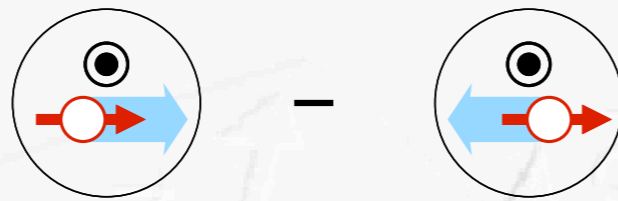
	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

- chiral-odd  $\Rightarrow$  needs Collins FF (or similar)
- proton & deuteron data consistently small
- cancelations? pretzelosity=zero?  
or just the additional suppression by two powers of  $P_{h\perp}$



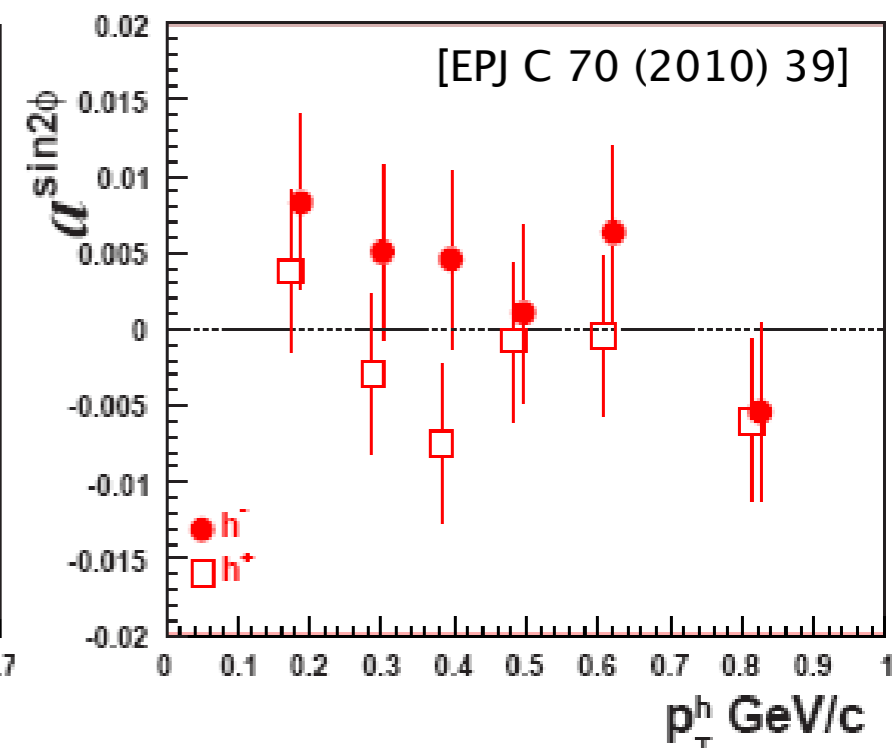
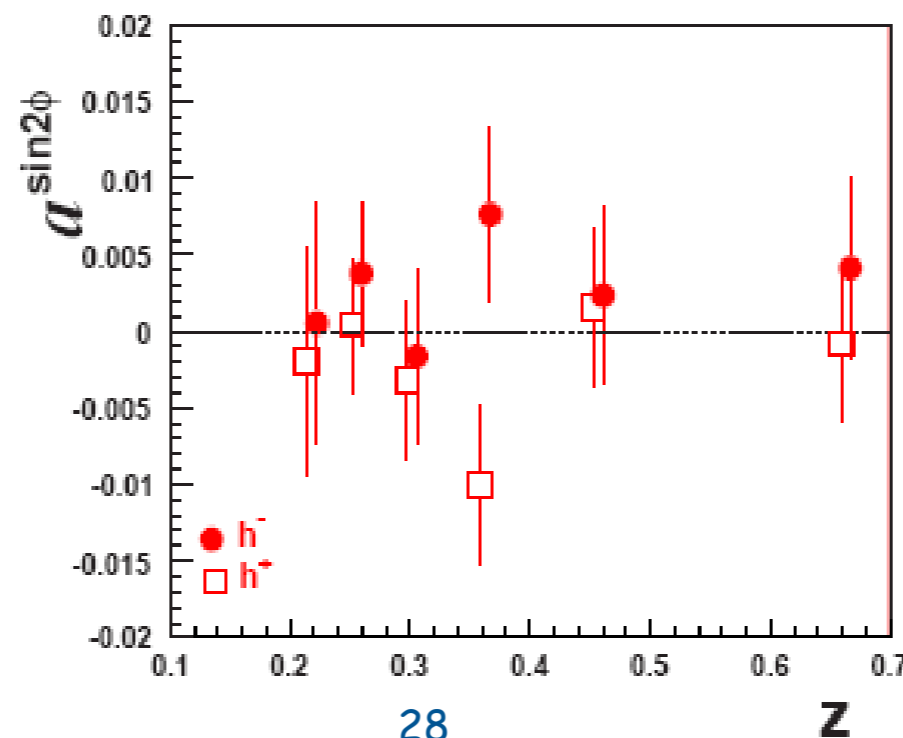
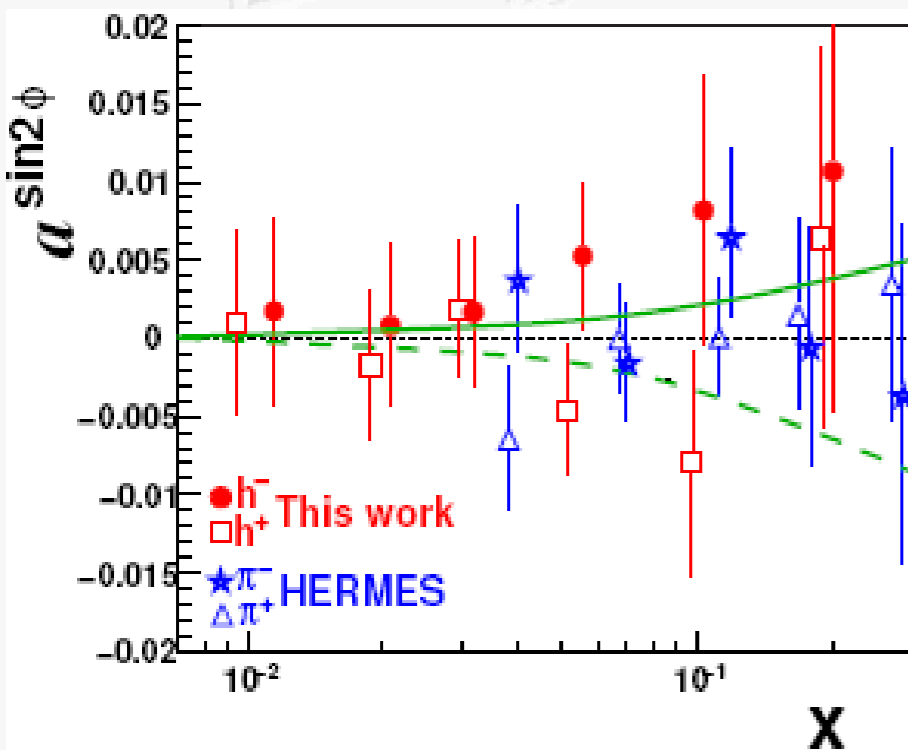
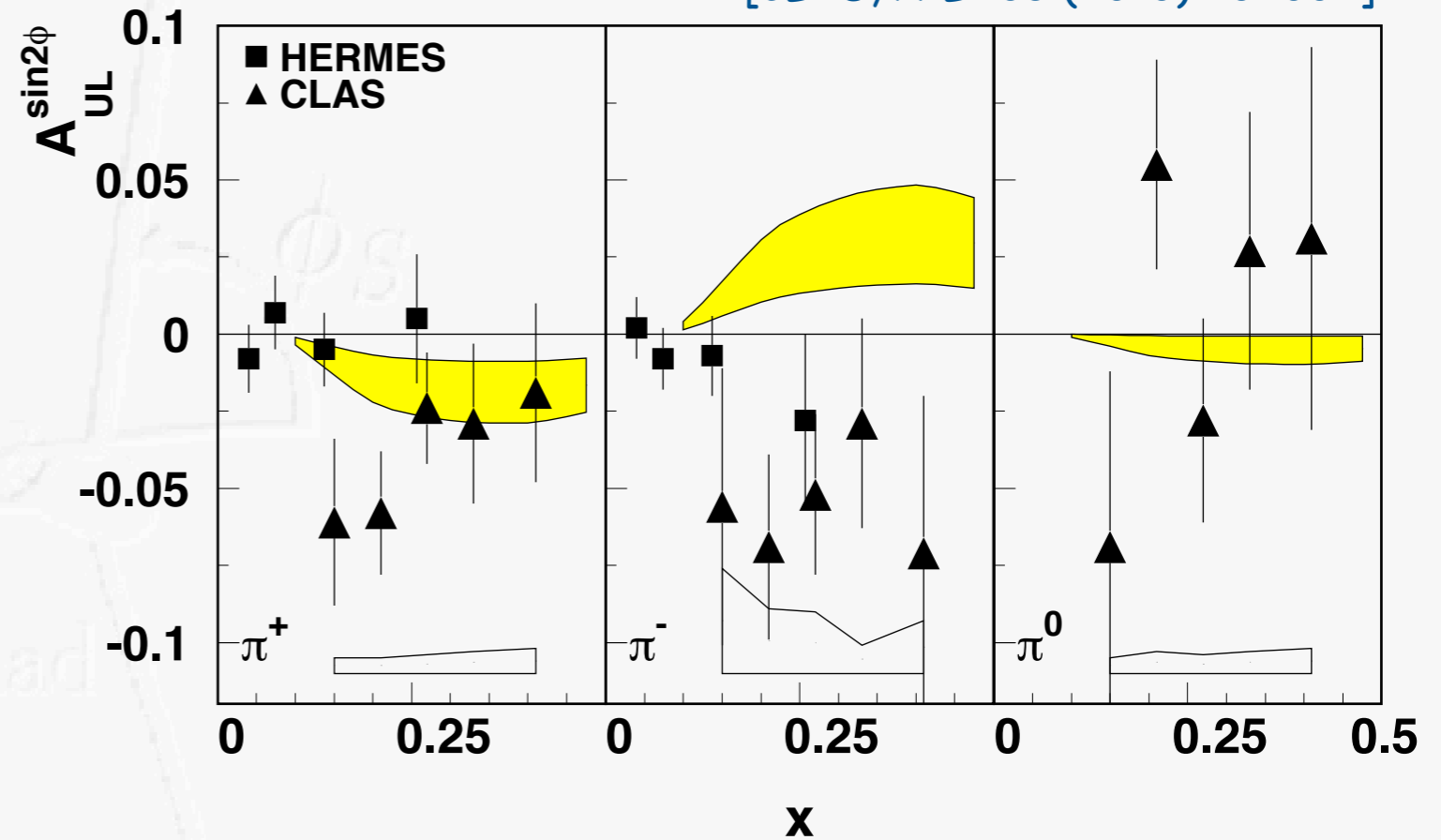
# Worm-Gear I

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$



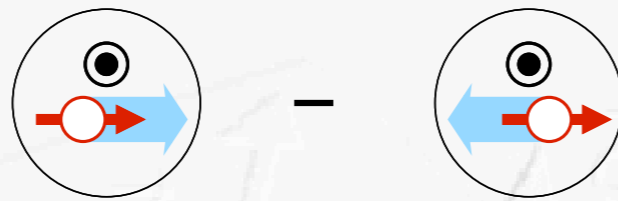
[CLAS, PRL 105 (2010) 262002]

- again: chiral-odd
- evidence from CLAS (violating isospin symmetry?)
- consistent with zero at COMPASS and HERMES

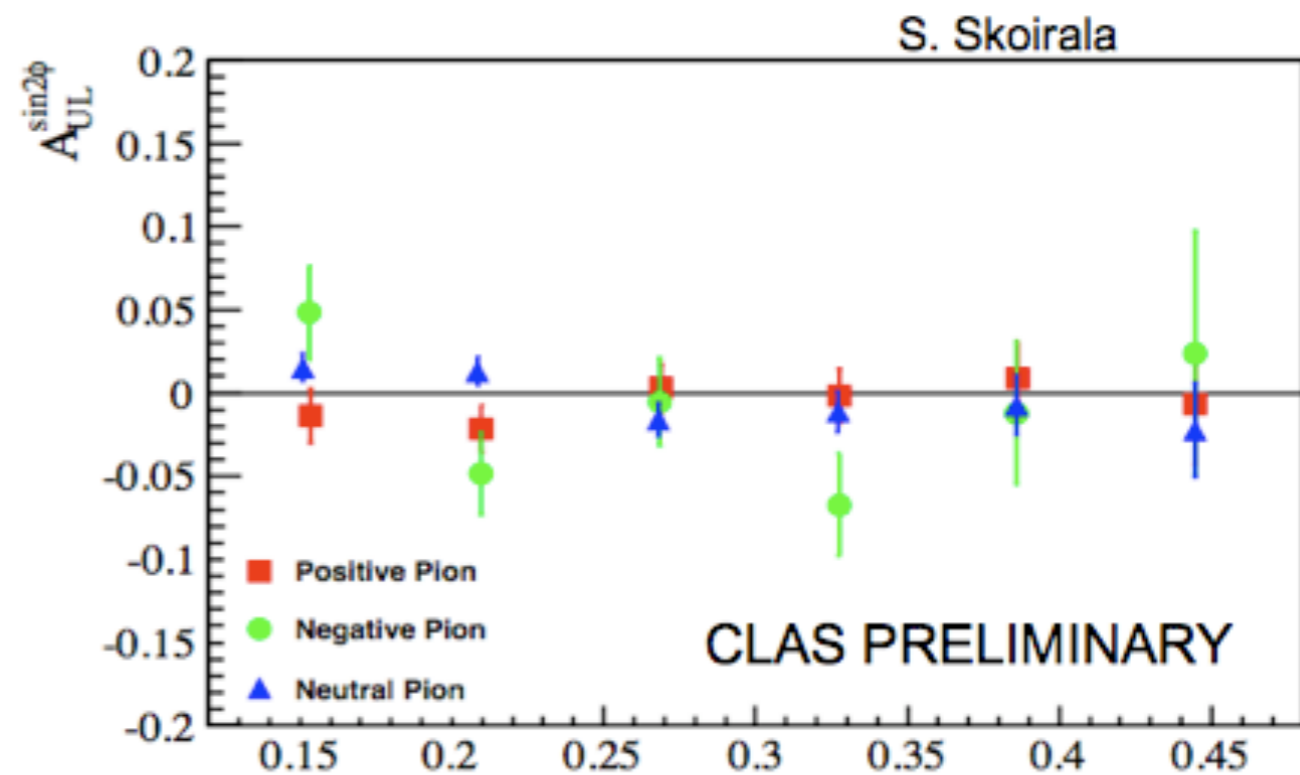
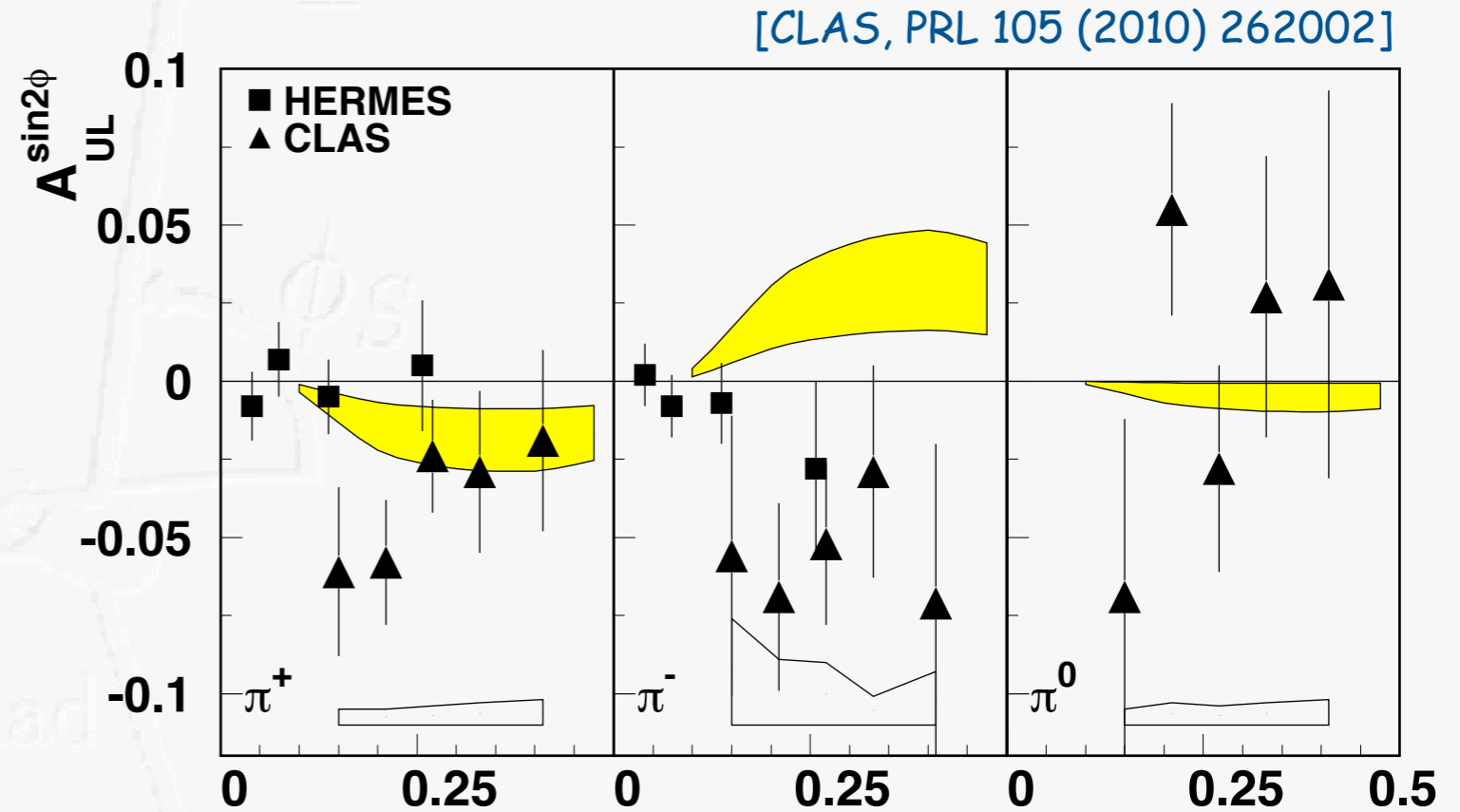


# Worm-Gear I

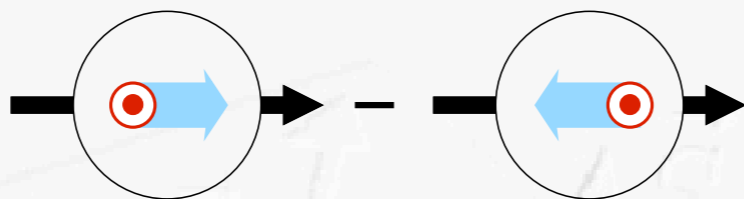
	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$



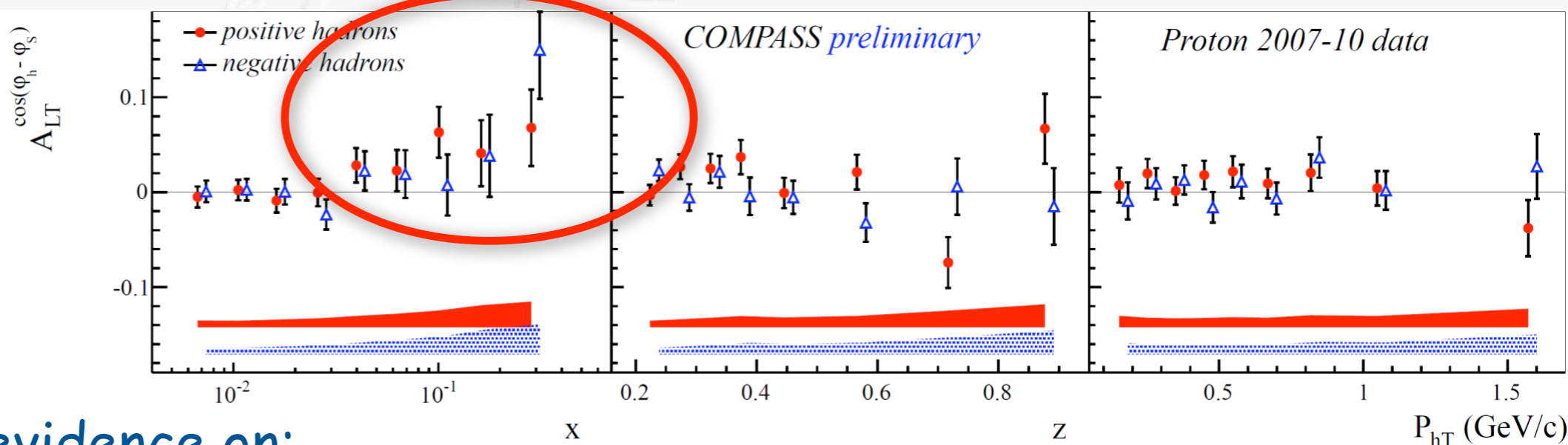
- again: chiral-odd
- evidence from CLAS (violating isospin symmetry?)
- consistent with zero at COMPASS and HERMES
- new preliminary data from CLAS closer to HERMES/COMPASS (and to zero)



	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$



# Worm-Gear II

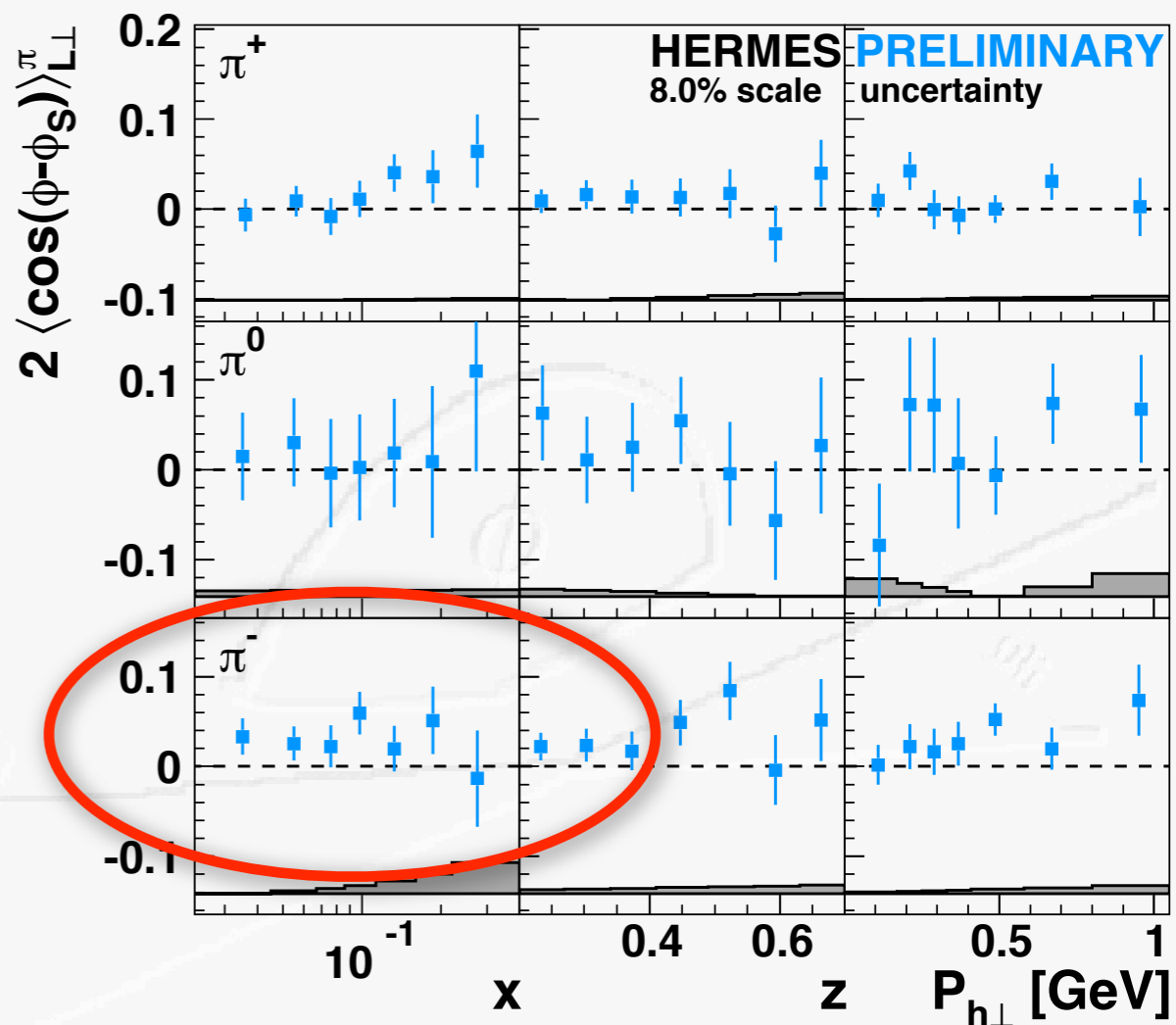
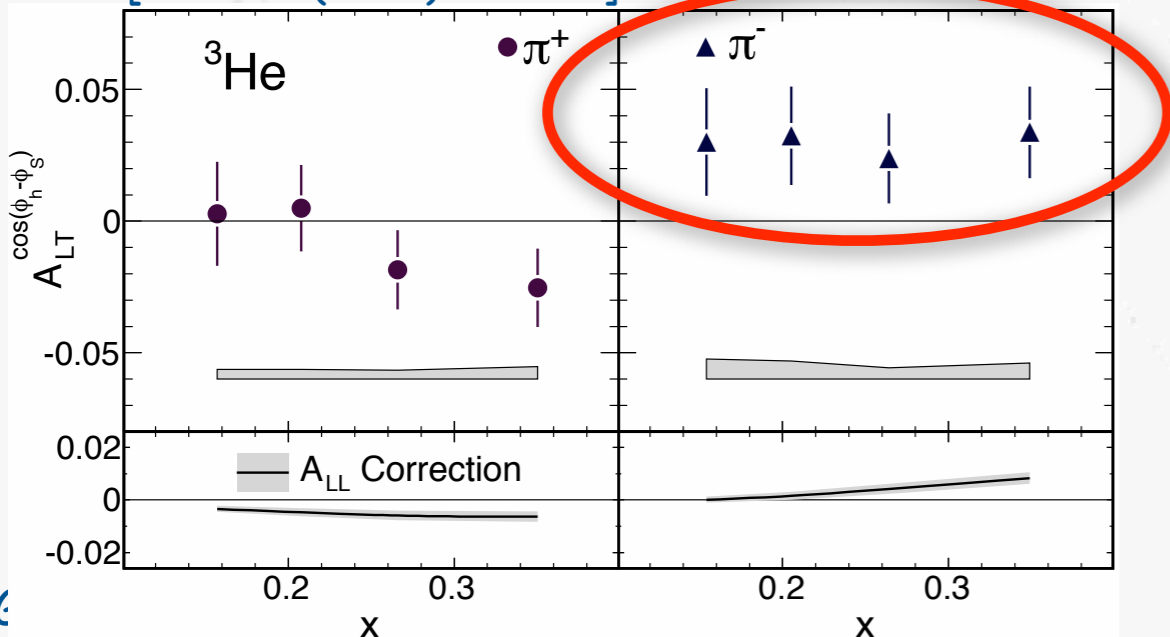


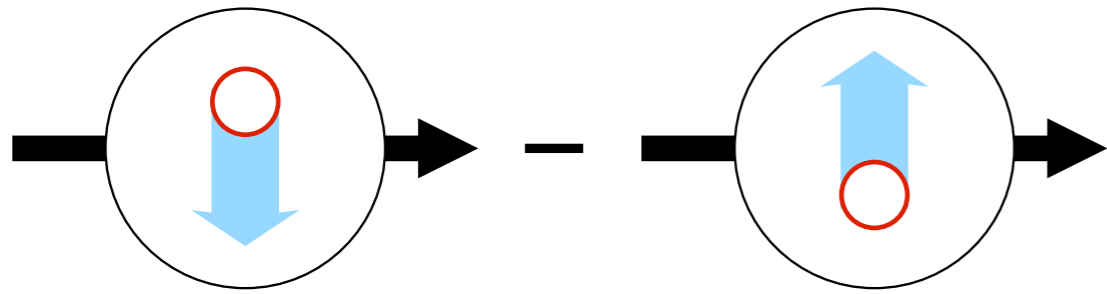
● first direct evidence on:

●  $^3\text{He}$  target at JLab

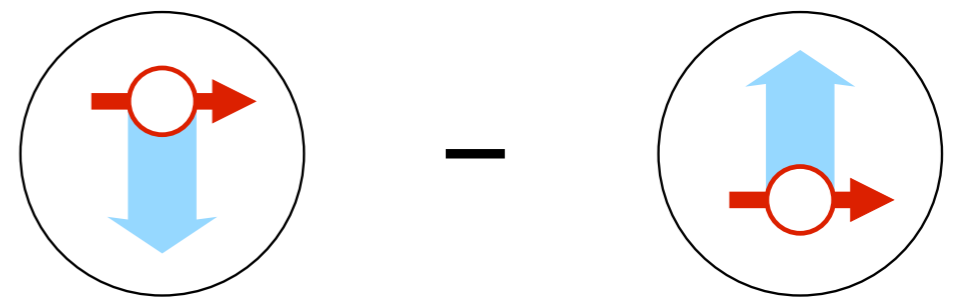
● H target at COMPASS & HERMES

[PRL 108 (2012) 052001]





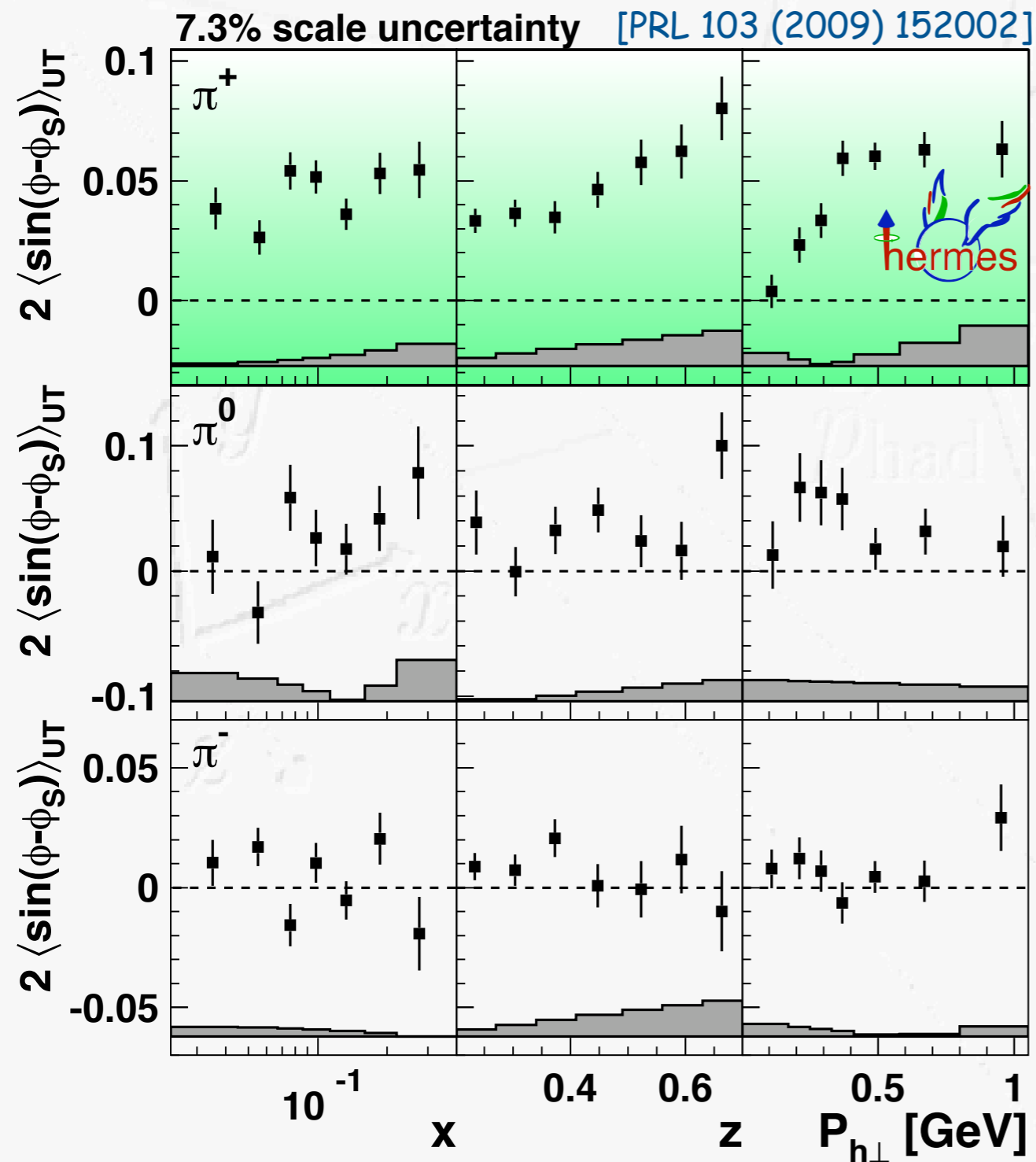
**“Wilson-line physics”**  
naively T-odd distributions



# Sivers amplitudes for pions

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

$$2\langle \sin(\phi - \phi_S) \rangle_{UT} = - \frac{\sum_q e_q^2 f_{1T}^{\perp,q}(x, p_T^2) \otimes_{\mathcal{W}} D_1^q(z, k_T^2)}{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)}$$

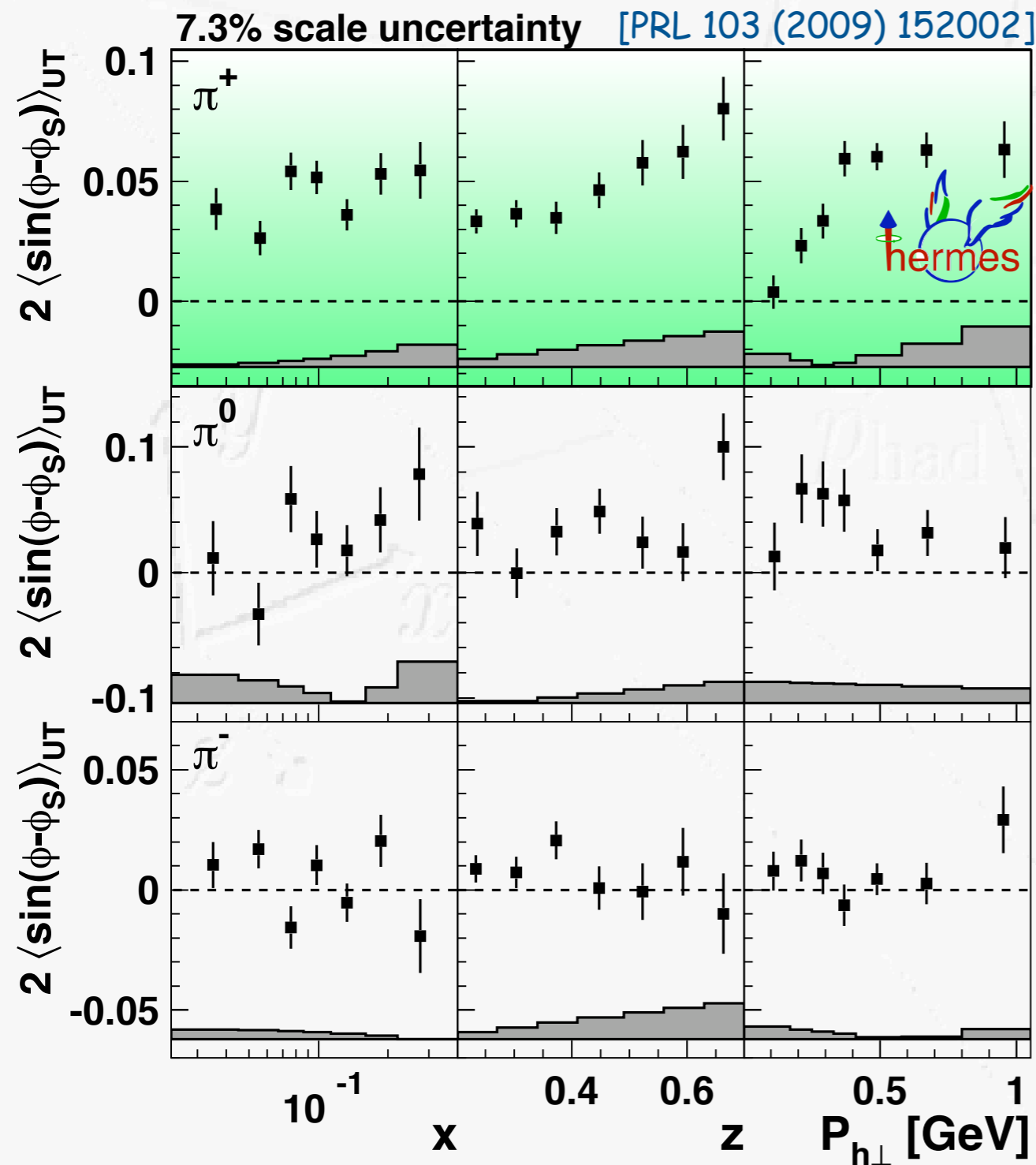




# Sivers amplitudes for pions

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

$$2\langle \sin(\phi - \phi_S) \rangle_{UT} = - \frac{\sum_q e_q^2 f_{1T}^{\perp,q}(x, p_T^2) \otimes_{\mathcal{W}} D_1^q(z, k_T^2)}{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)}$$



$\pi^+$  dominated by u-quark scattering:

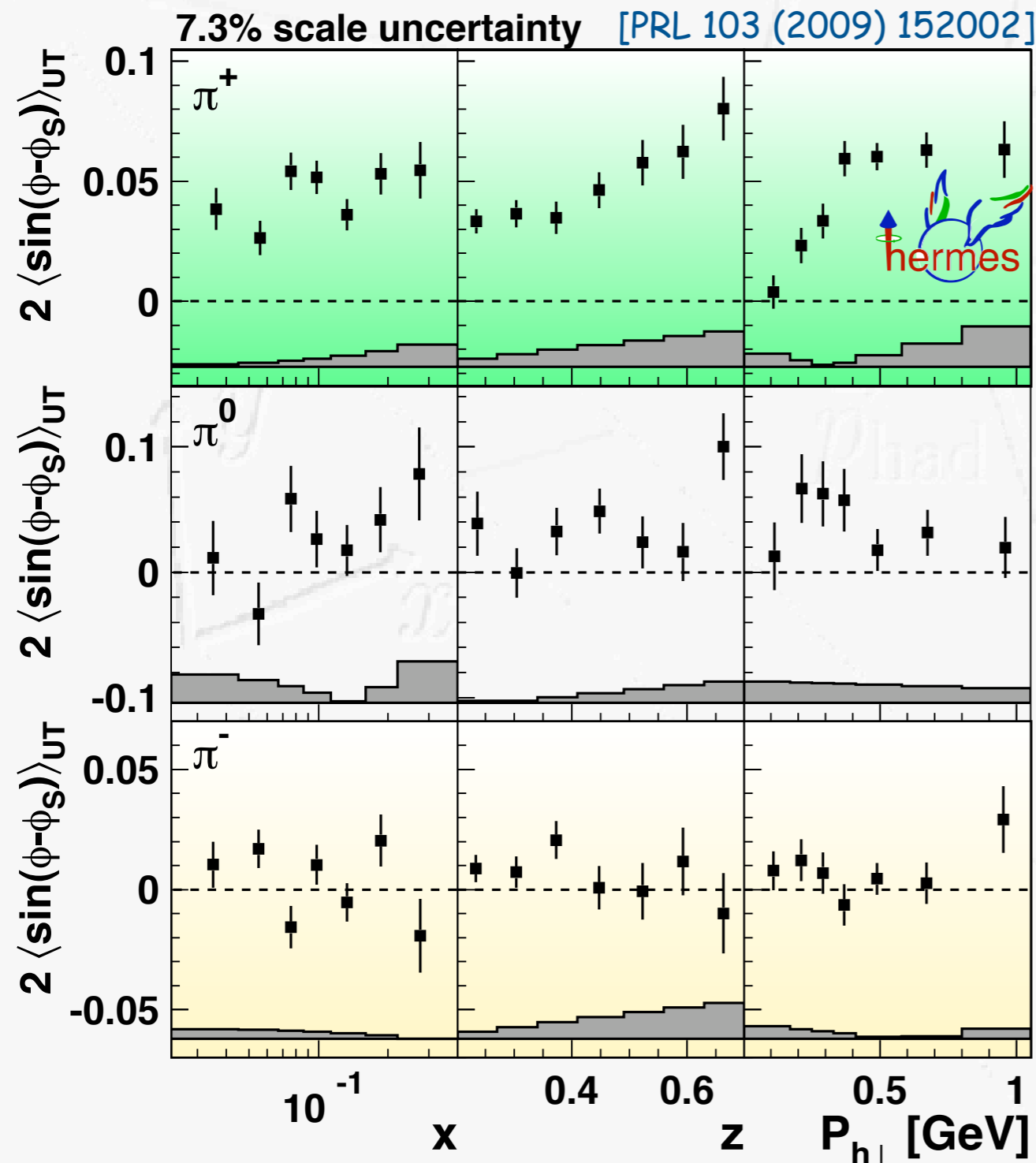
$$\simeq - \frac{f_{1T}^{\perp,u}(x, p_T^2) \otimes_{\mathcal{W}} D_1^{u \rightarrow \pi^+}(z, k_T^2)}{f_1^u(x, p_T^2) \otimes D_1^{u \rightarrow \pi^+}(z, k_T^2)}$$

u-quark Sivers DF < 0

# Sivers amplitudes for pions

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

$$2\langle \sin(\phi - \phi_S) \rangle_{UT} = - \frac{\sum_q e_q^2 f_{1T}^{\perp,q}(x, p_T^2) \otimes_{\mathcal{W}} D_1^q(z, k_T^2)}{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)}$$



$\pi^+$  dominated by u-quark scattering:

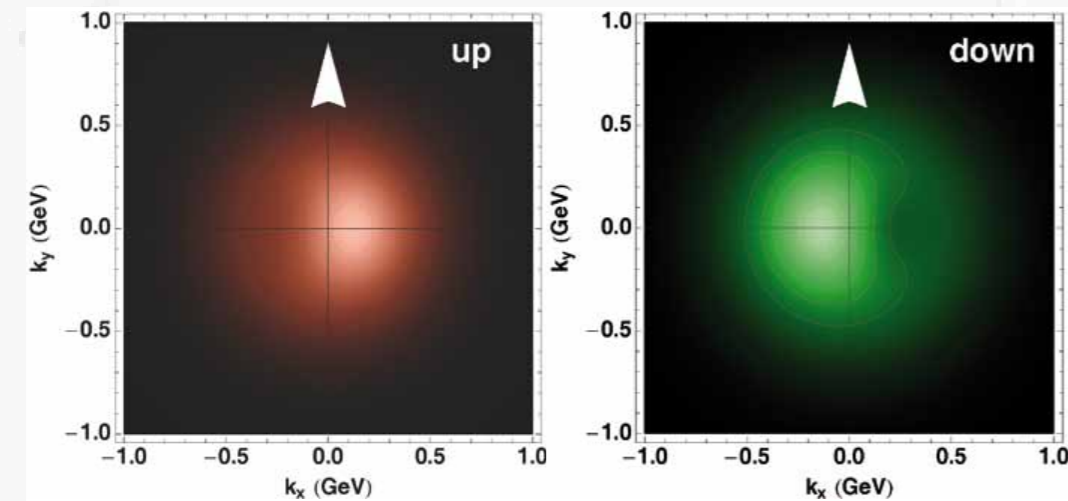
$$\simeq - \frac{f_{1T}^{\perp,u}(x, p_T^2) \otimes_{\mathcal{W}} D_1^{u \rightarrow \pi^+}(z, k_T^2)}{f_1^u(x, p_T^2) \otimes D_1^{u \rightarrow \pi^+}(z, k_T^2)}$$

👉 u-quark Sivers DF < 0

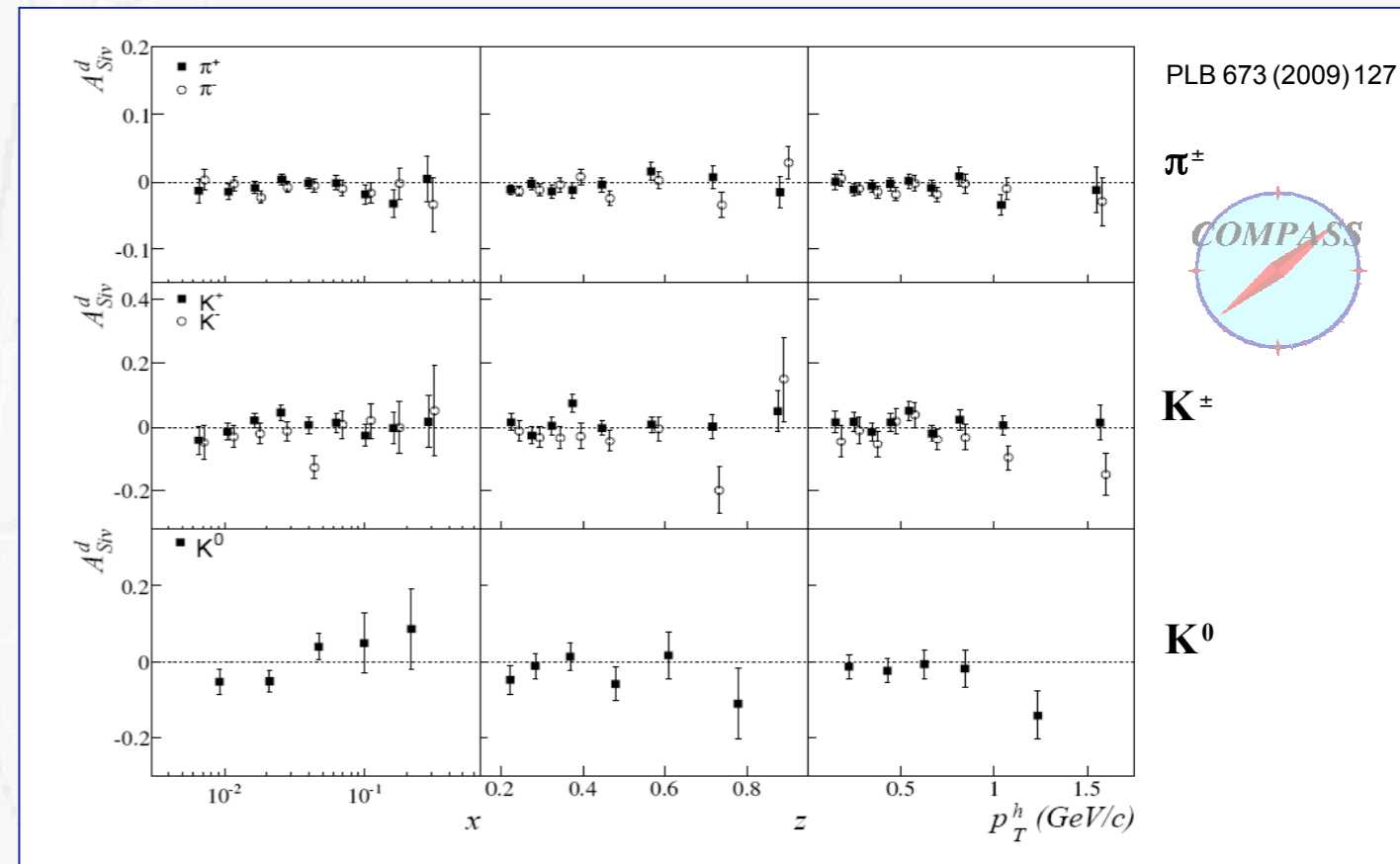
👉 d-quark Sivers DF > 0  
(cancellation for  $\pi^-$ )

# Sivers amplitudes

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$



[courtesy of A. Bacchetta]

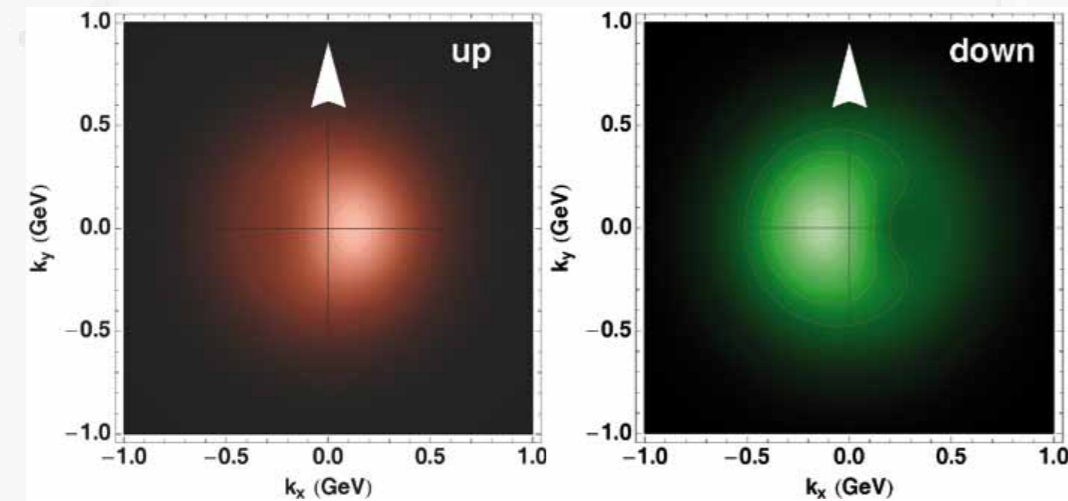


- cancelation for D target supports opposite signs of up and down Sivers

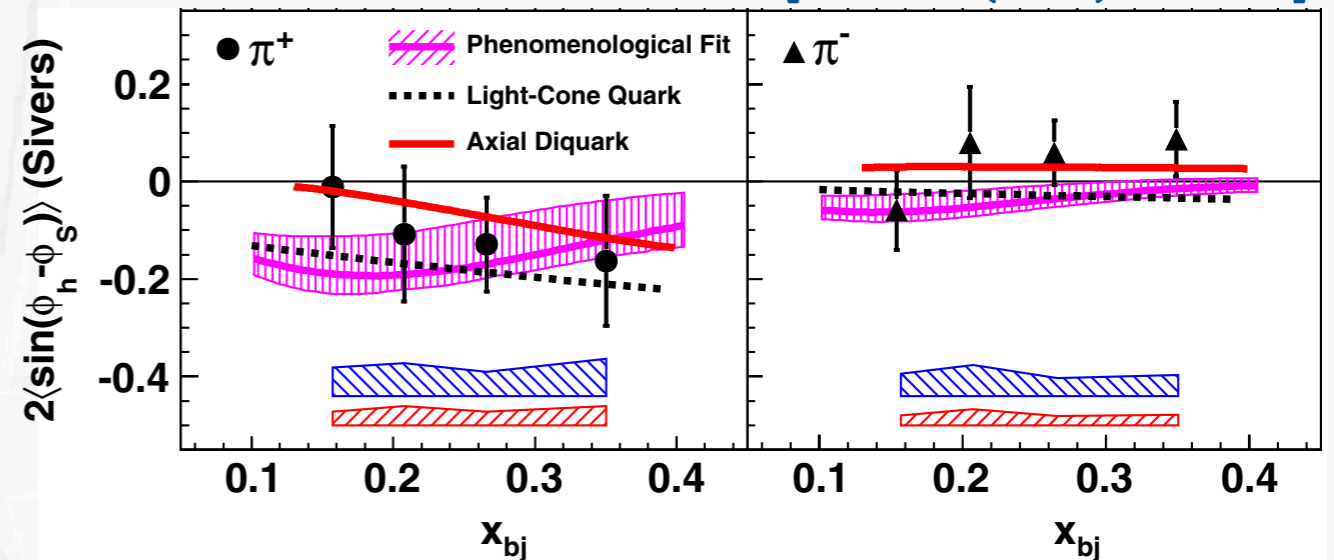
# Sivers amplitudes

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

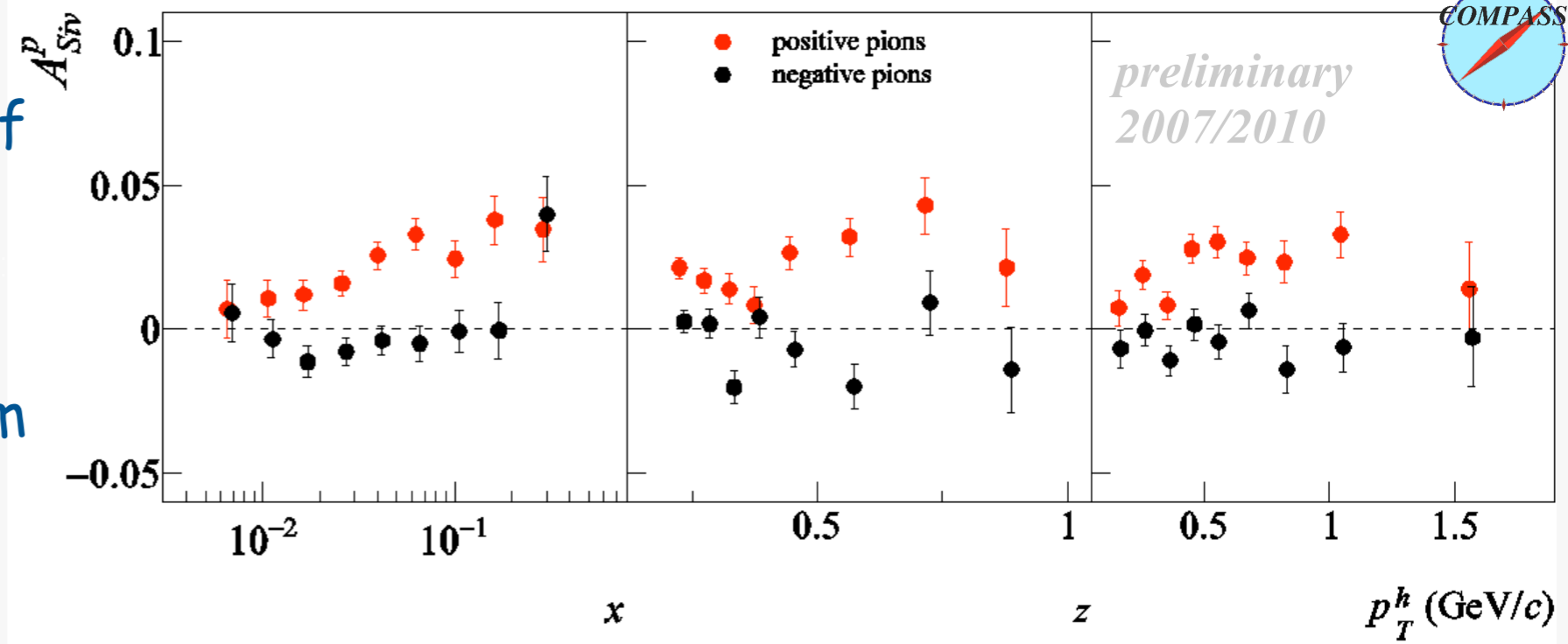
[PRL 107 (2011) 072003]



[courtesy of A. Bacchetta]



- cancelation for D target supports opposite signs of up and down Sivers
- new results from JLab using  $^3\text{He}$  target and from COMPASS for proton target

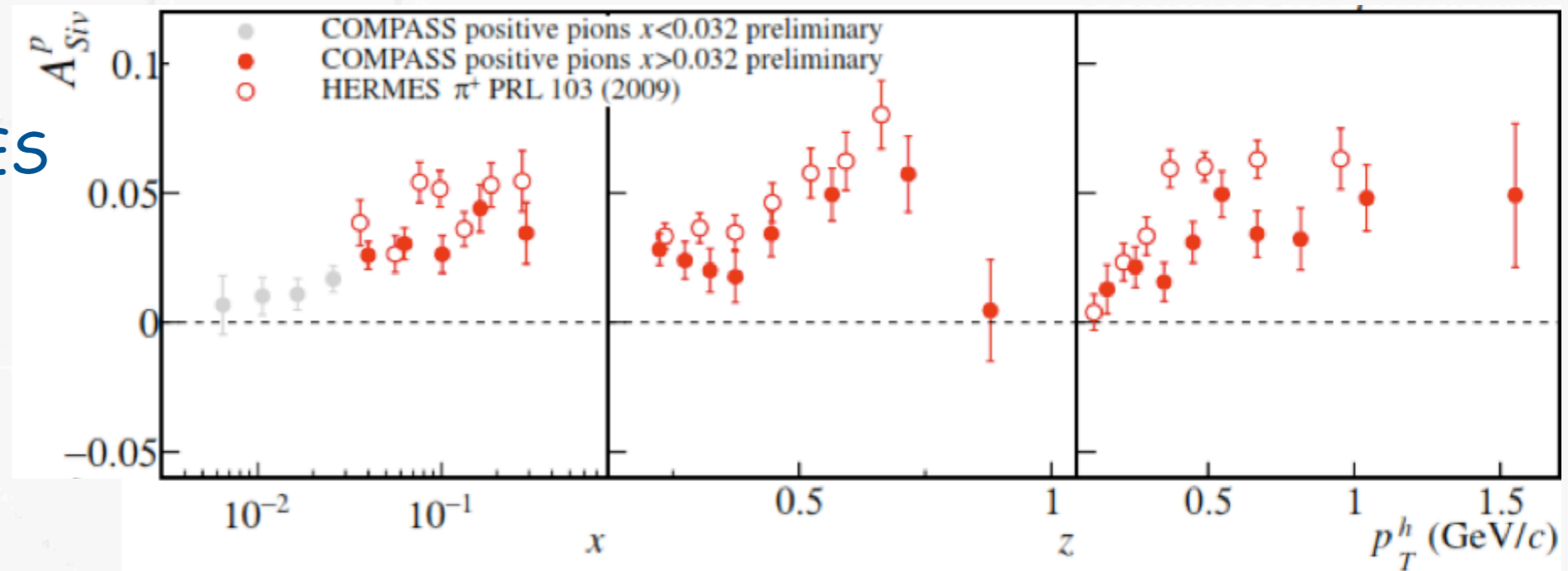


# Sivers amplitudes

## $Q^2$ dependence?

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

- slightly larger amplitudes at HERMES
- average  $Q^2$  about factor 3 larger at COMPASS

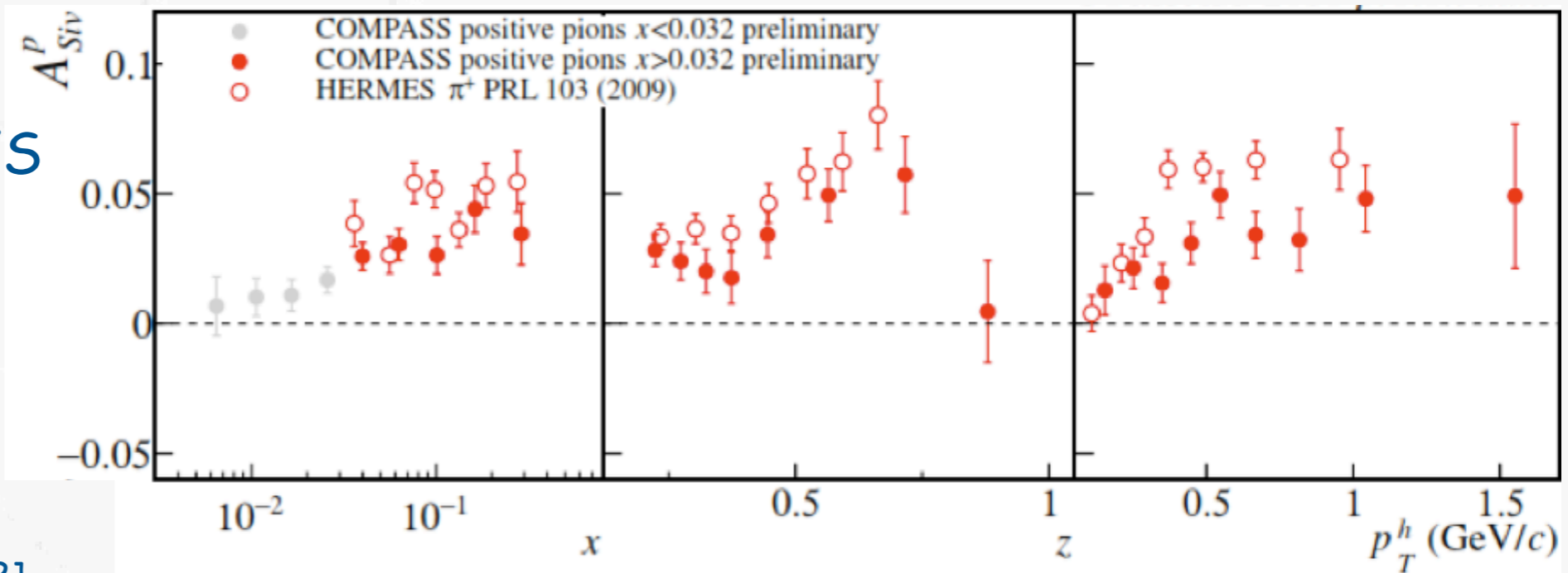


# Sivers amplitudes

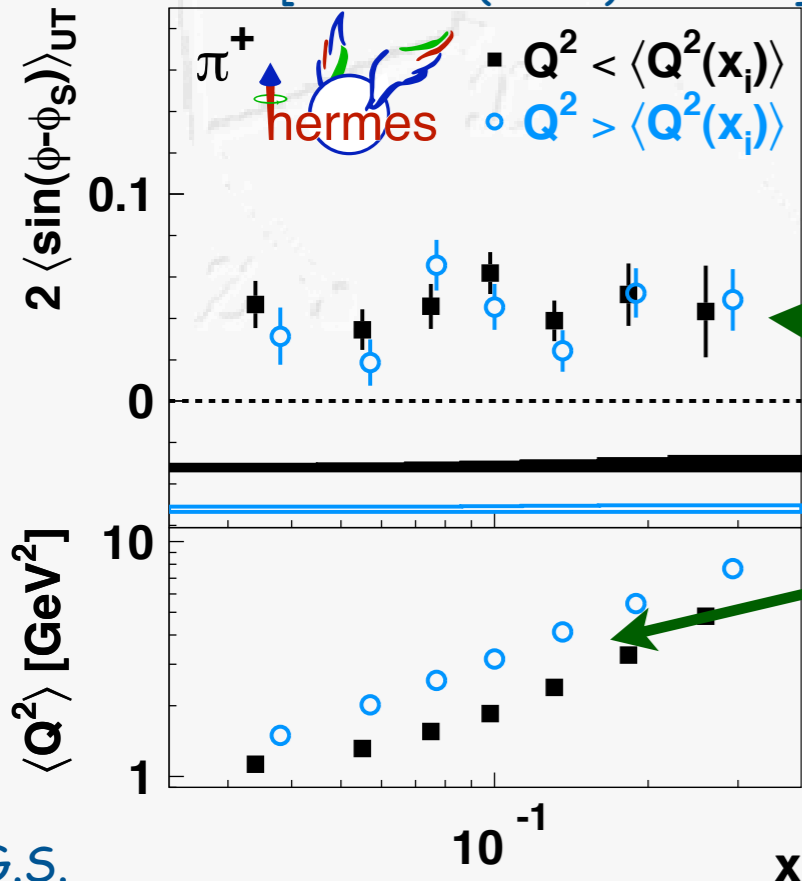
## $Q^2$ dependence?

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

- slightly larger amplitudes at HERMES
- average  $Q^2$  about factor 3 larger at COMPASS



[PRL 103 (2009) 152002]



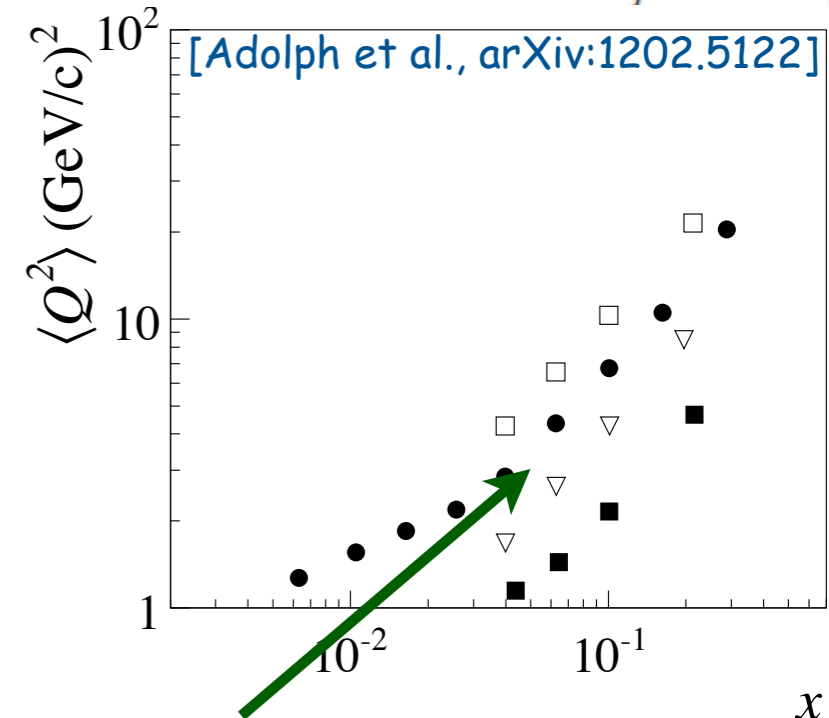
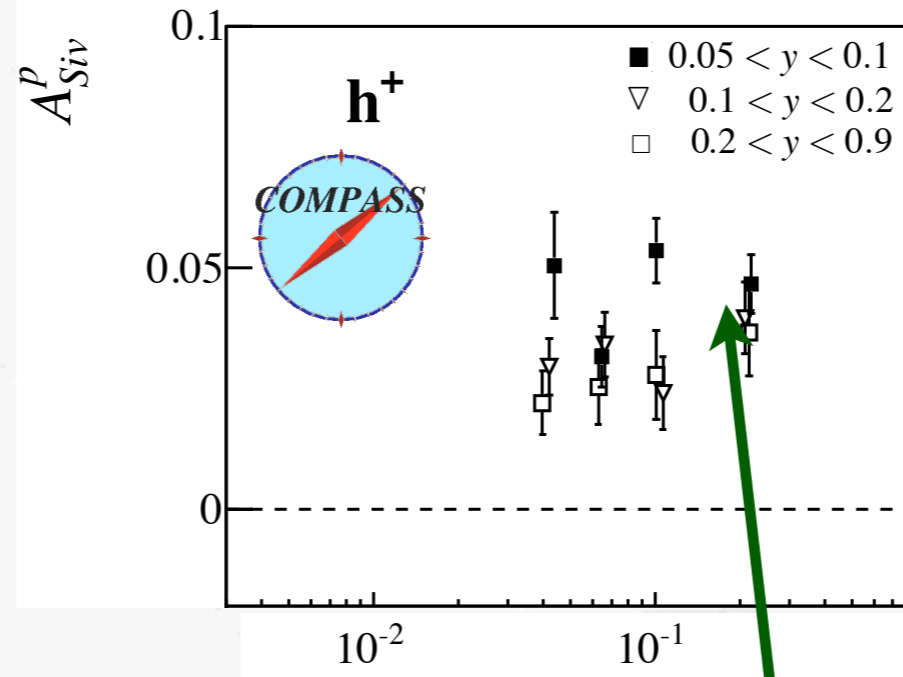
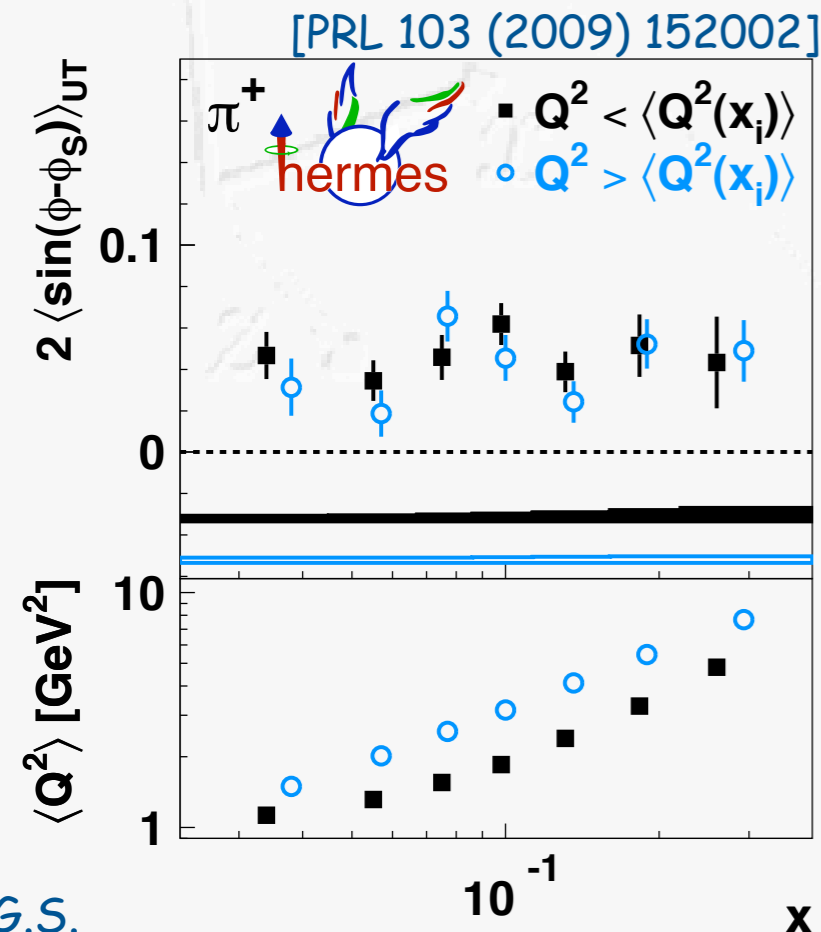
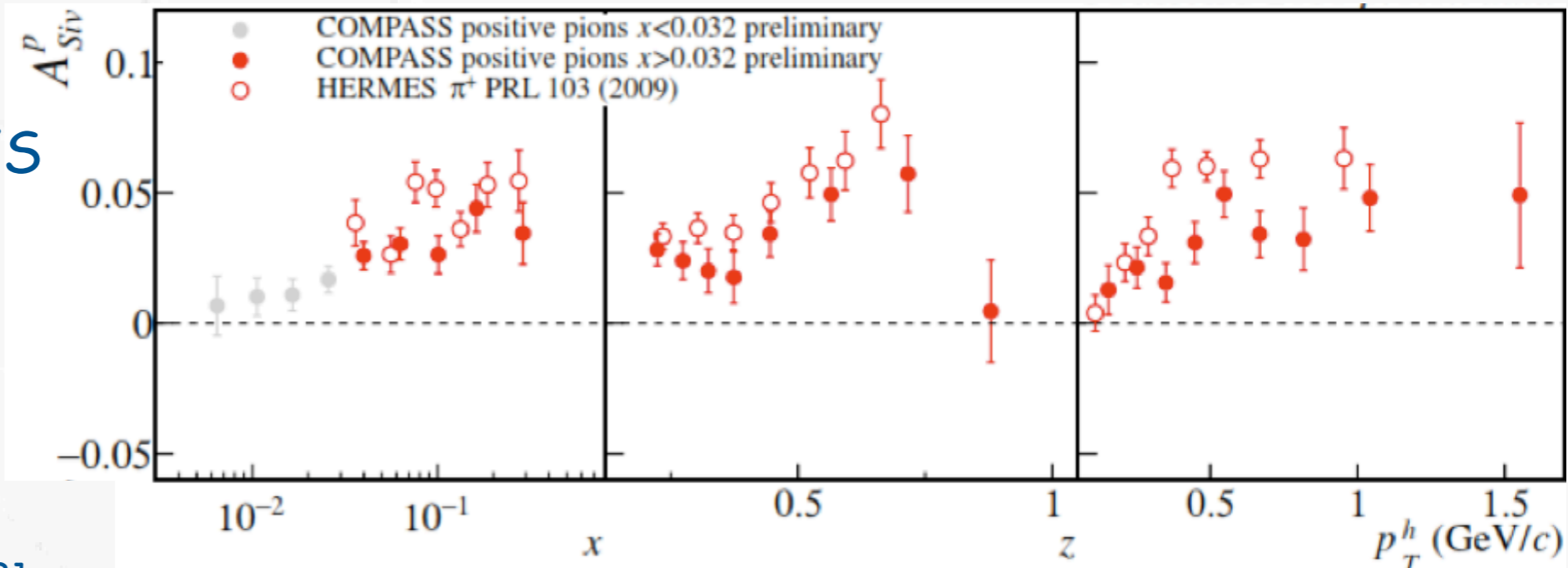
nothing seen at HERMES

# Sivers amplitudes

## $Q^2$ dependence?

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

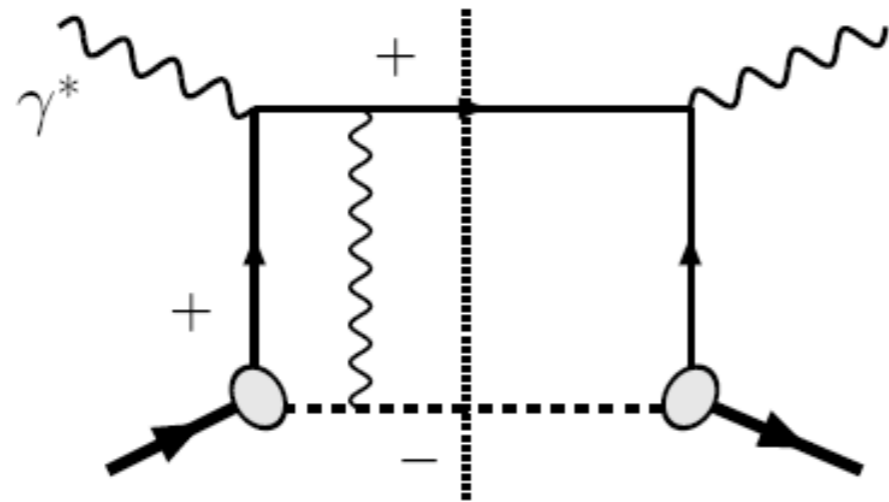
- slightly larger amplitudes at HERMES
- average  $Q^2$  about factor 3 larger at COMPASS



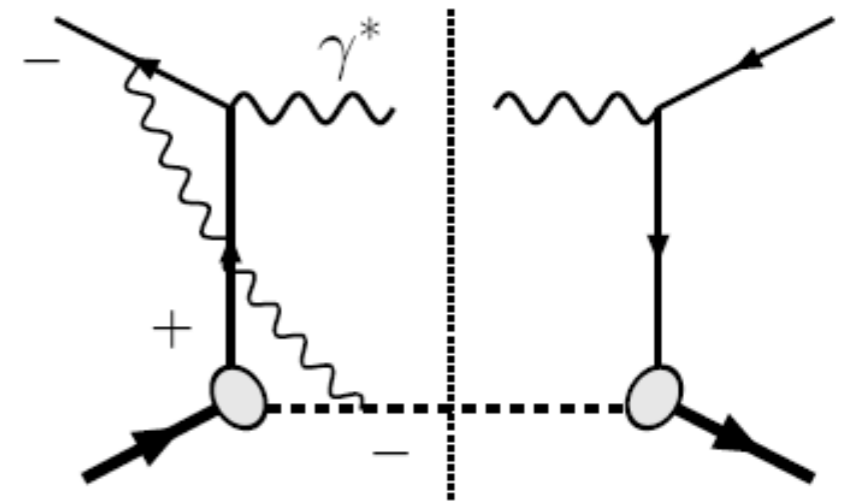
is  $y$ -dependence a  $Q^2$  dependence? Evolution?

# Process dependence

simple QED  
example



DIS: attractive

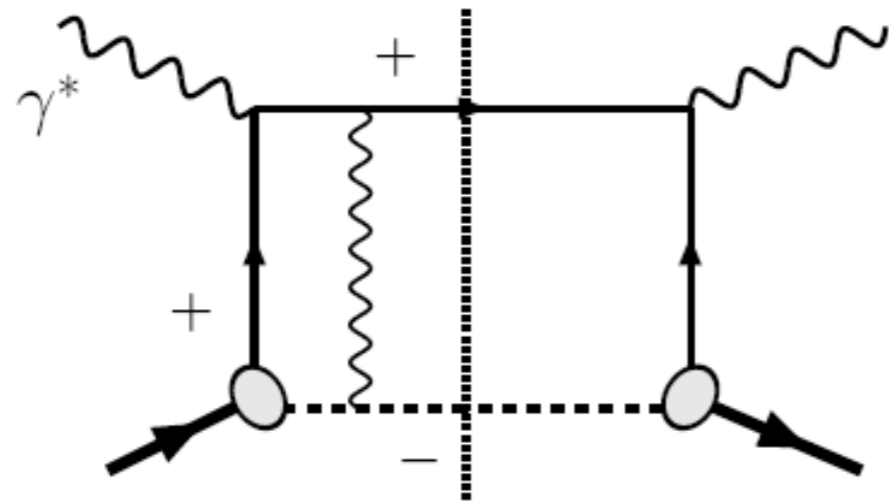


Drell-Yan: repulsive

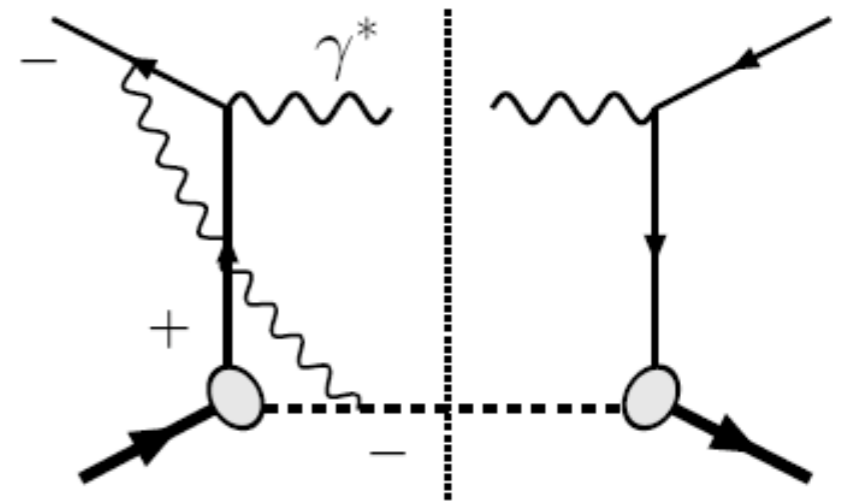


# Process dependence

simple QED  
example

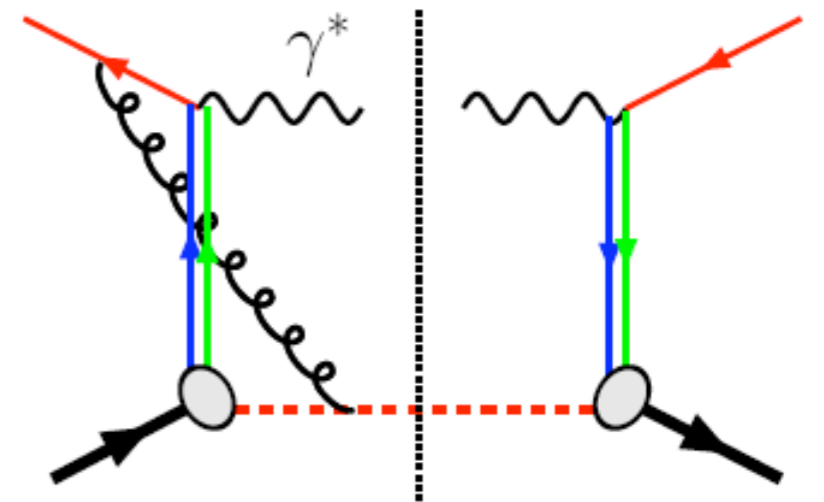
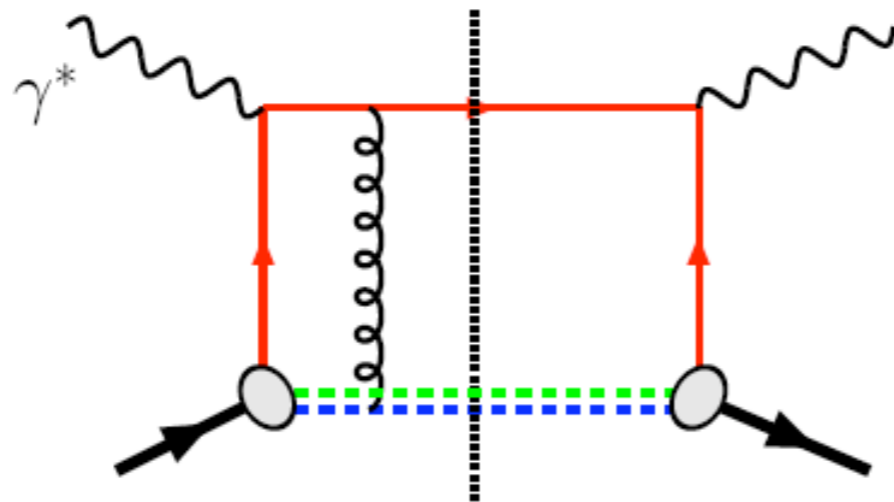


DIS: attractive



Drell-Yan: repulsive

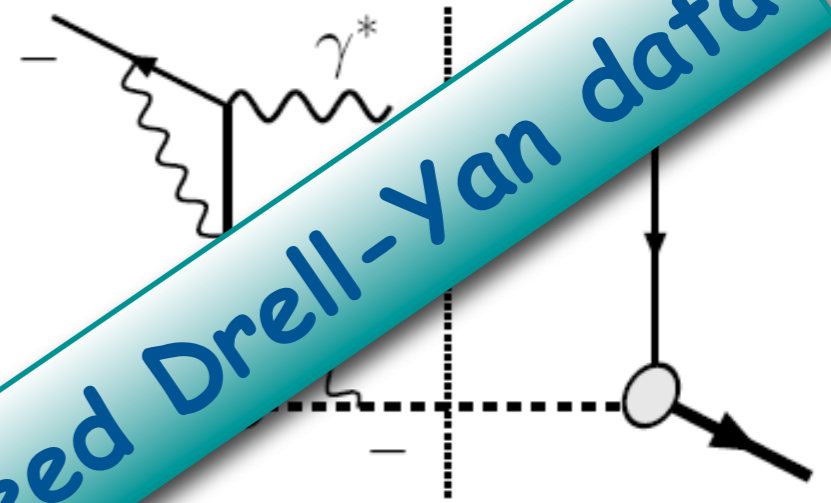
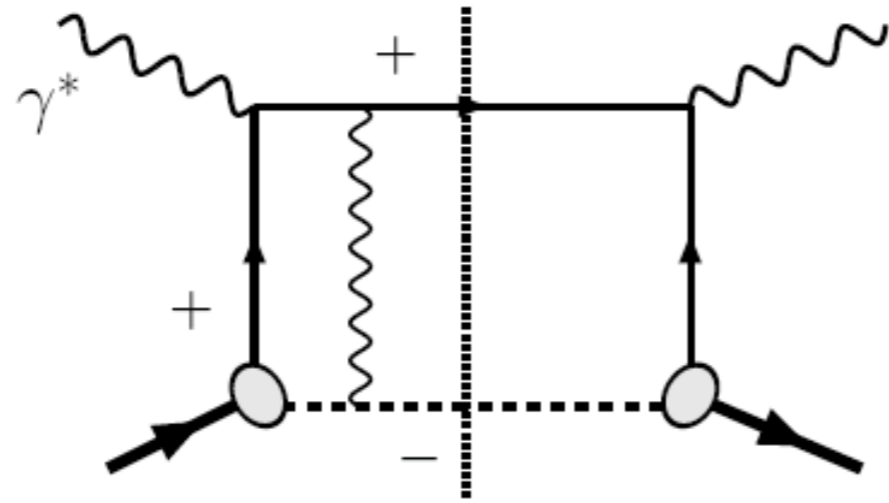
add color:  
QCD



result:  $Sivers|_{DIS} = - Sivers|_{DY}$

# Process dependence

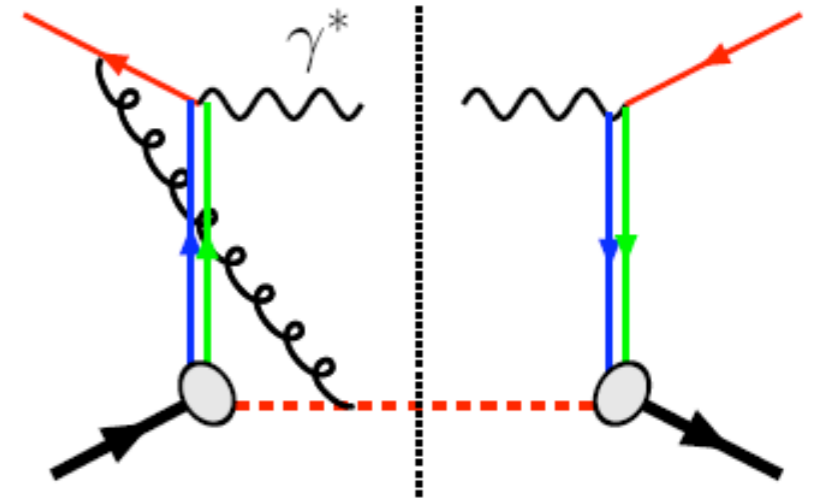
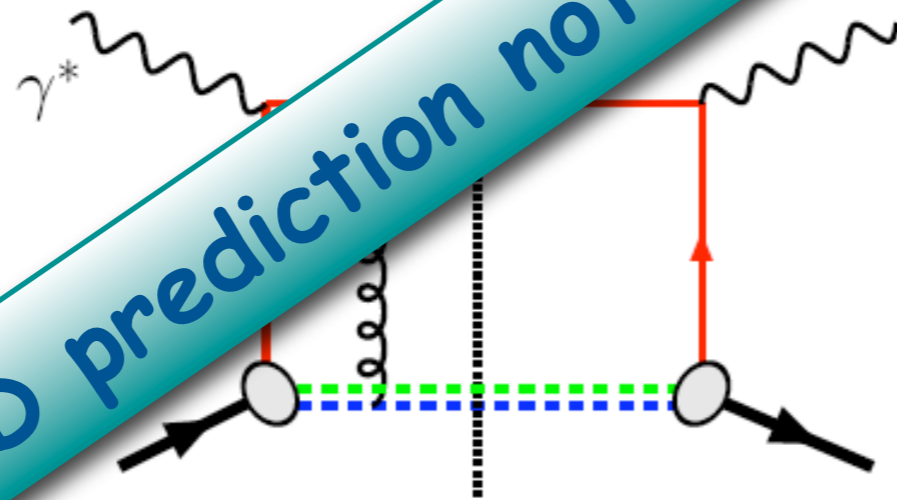
simple QED  
example



DIS: attractive

Drell-Yan: repulsive

add color:  
QCD



result:  $Sivers|_{DIS} = -Sivers|_{DY}$

rigorous QCD prediction not tested!! - need Drell-Yan data

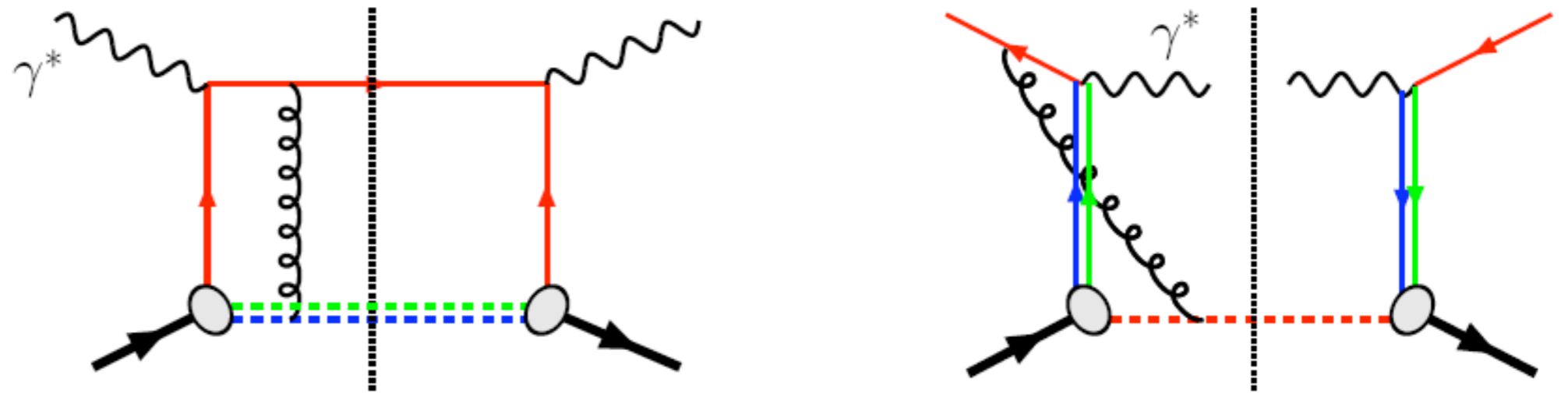
# Process dependence

need Drell-Yan experiments with transverse polarization:  
**COMPASS, transverse SeaQuest, RHIC, ...**

☛ C. Riedl

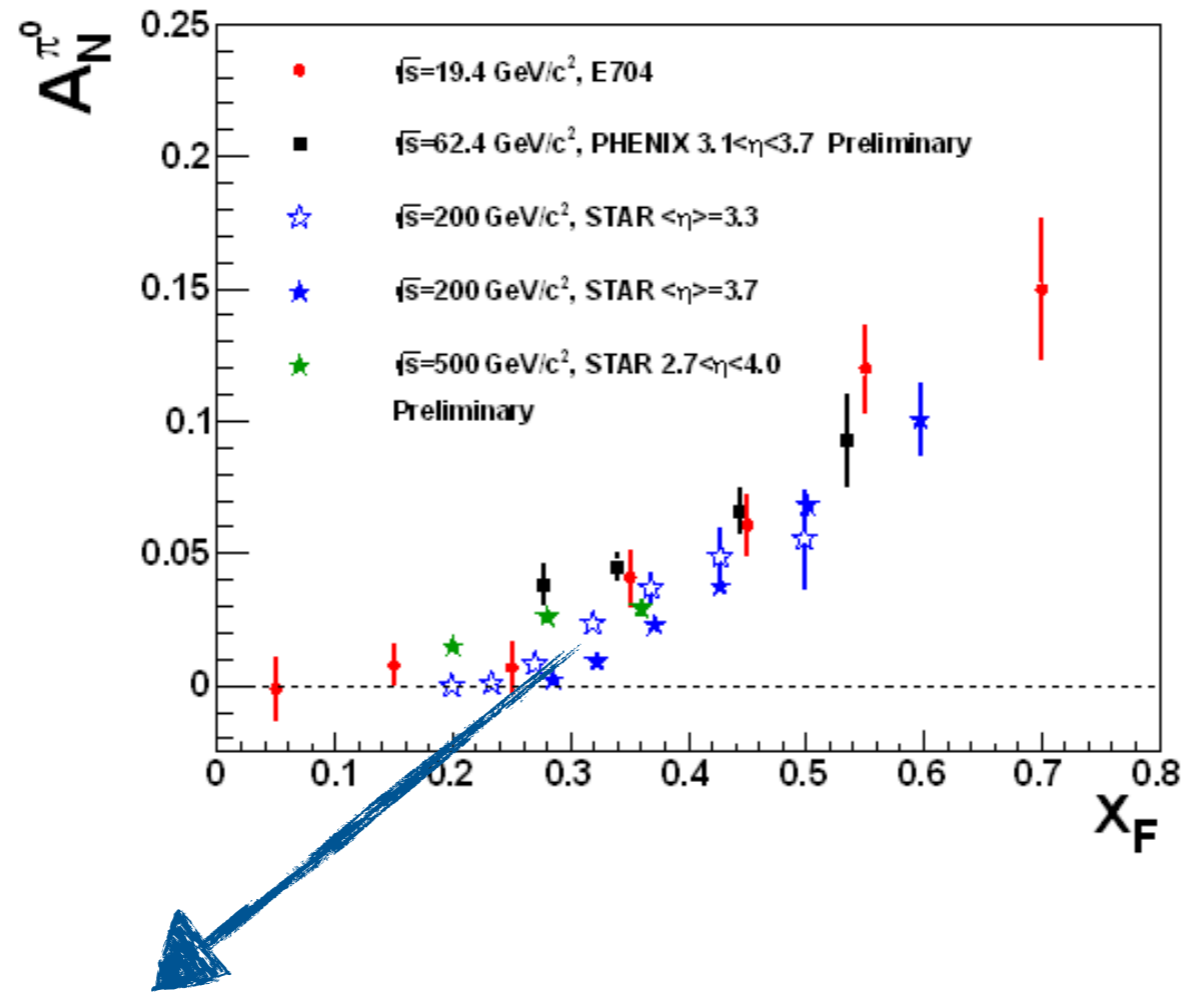
add color:

QCD



result:  $Sivers|_{DIS} = - Sivers|_{DY}$

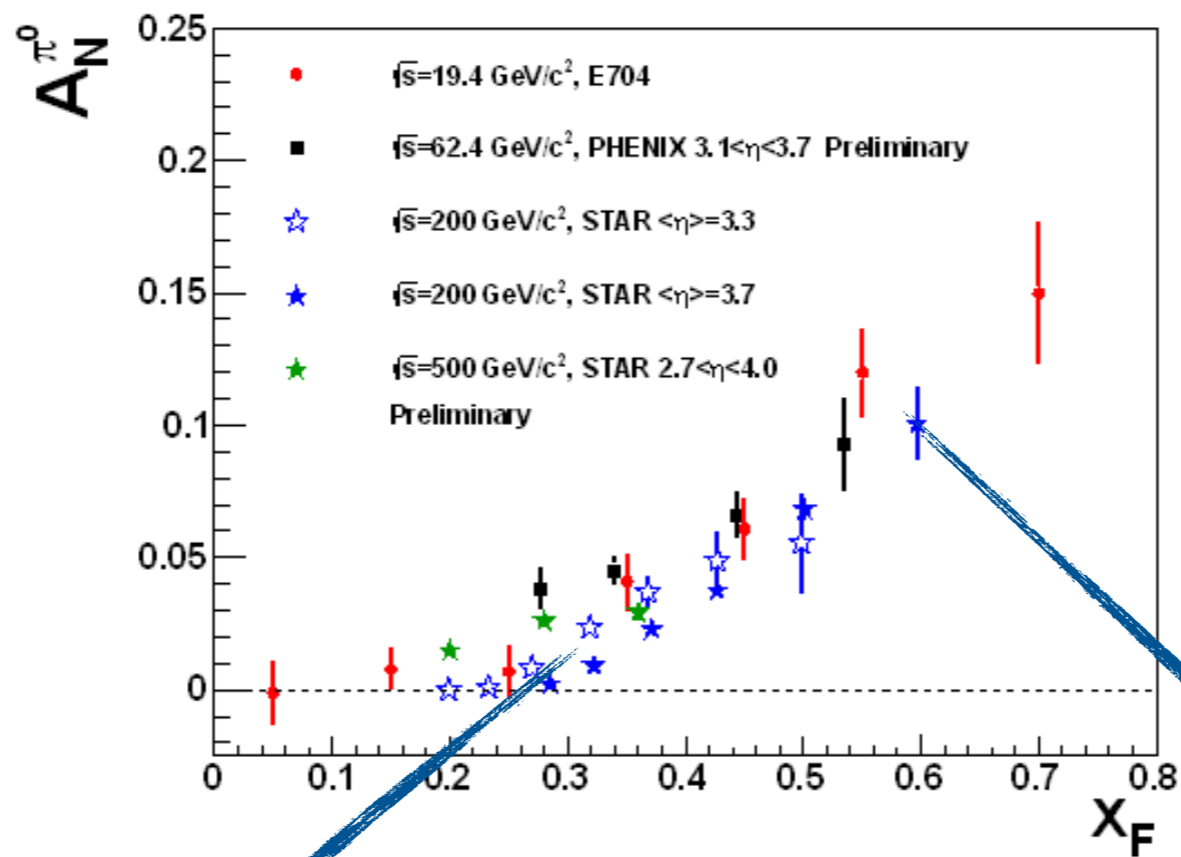
$$p \uparrow p \rightarrow \pi X$$



“generalized parton model”

no rigorous TMD factorization!

$$p \uparrow p \rightarrow \pi X$$



“generalized parton model”

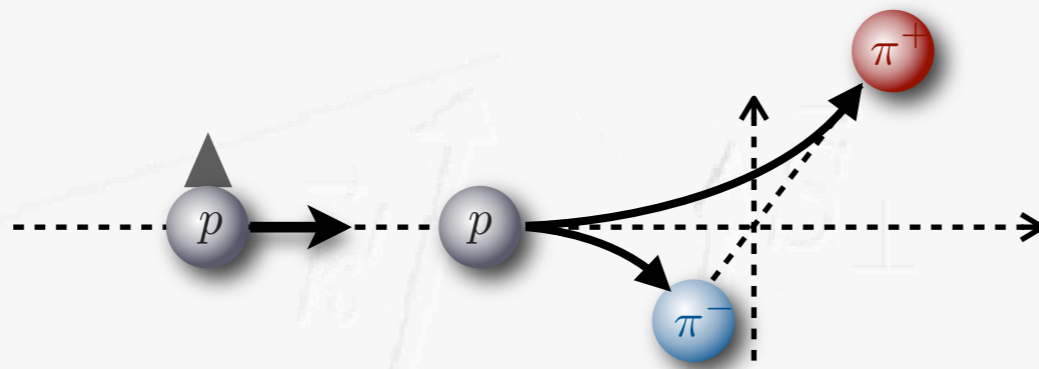
collinear twist-3

no rigorous TMD factorization!

$$gT_{q,F}(x, x) = - \int d^2 k_{\perp} \frac{|k_{\perp}|^2}{M} f_{1T}^{\perp q}(x, k_{\perp}^2) |_{\text{SIDIS}}$$

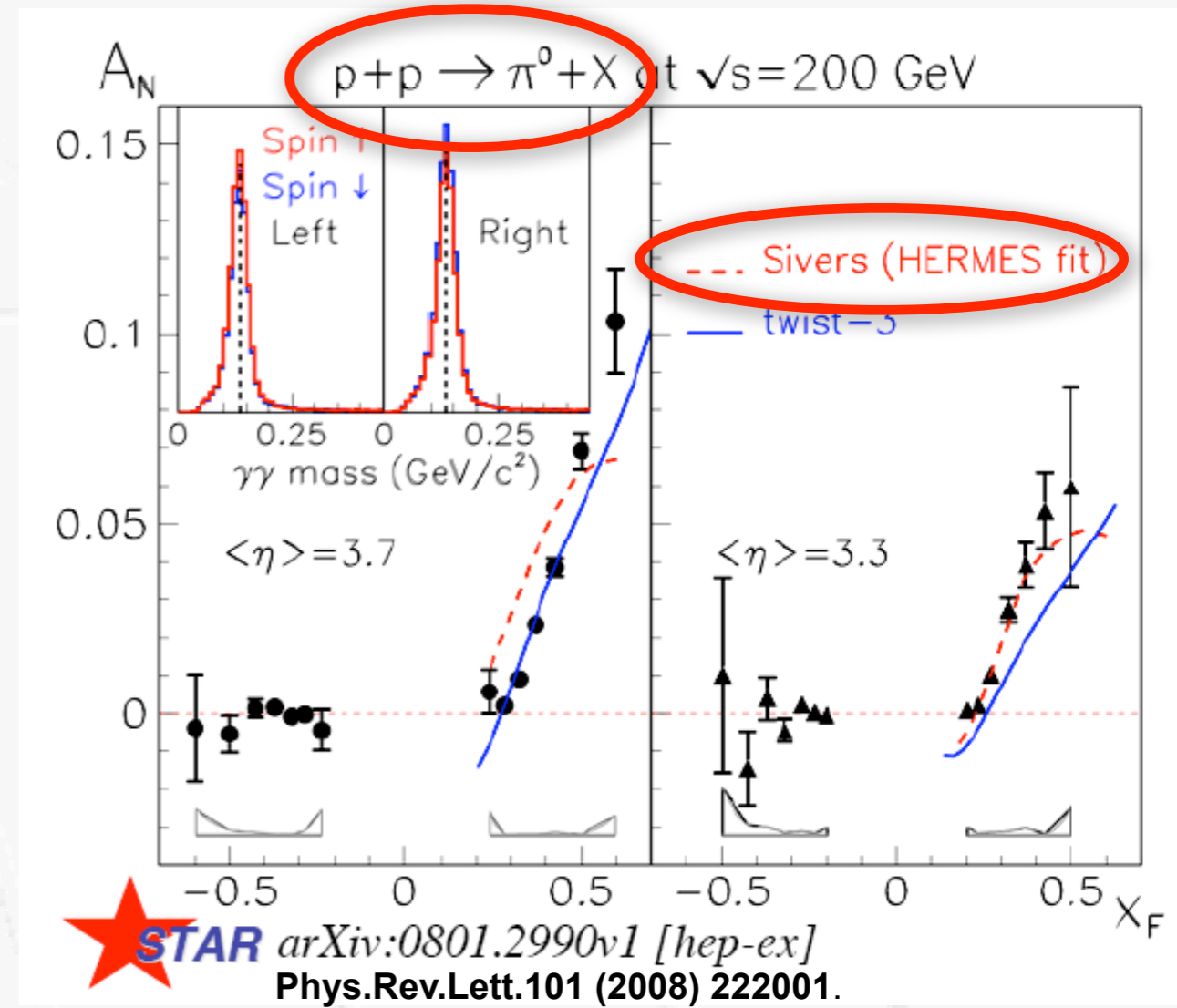
TMD factorization

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

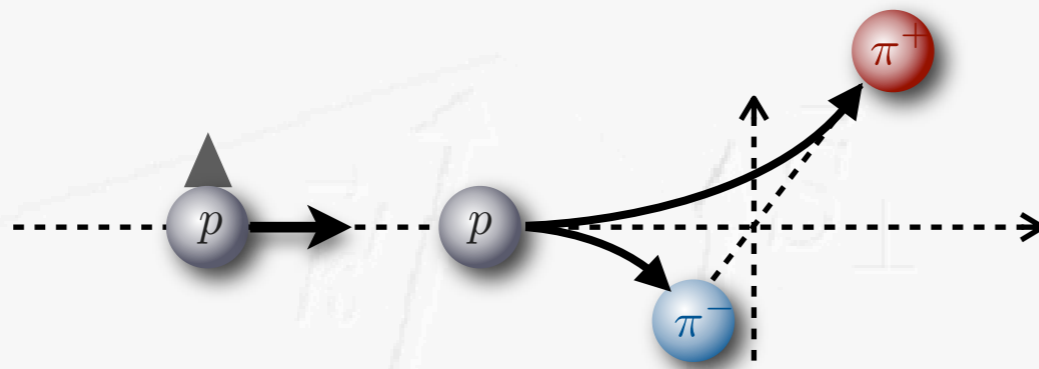


$$p^\uparrow p \rightarrow \pi X$$

- Sivers fit to HERMES data nicely described  $A_N$  in pp

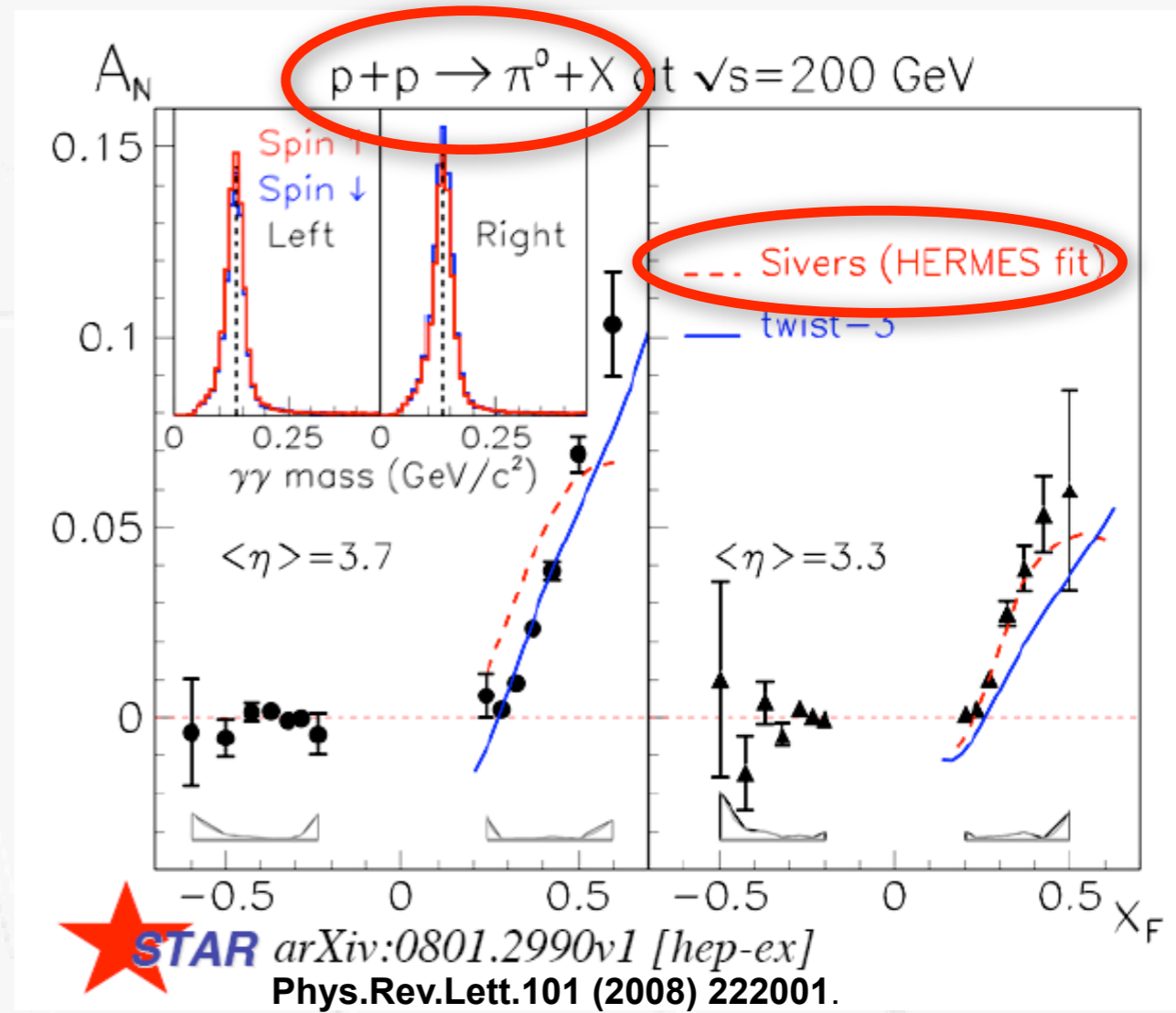


	U	L	T
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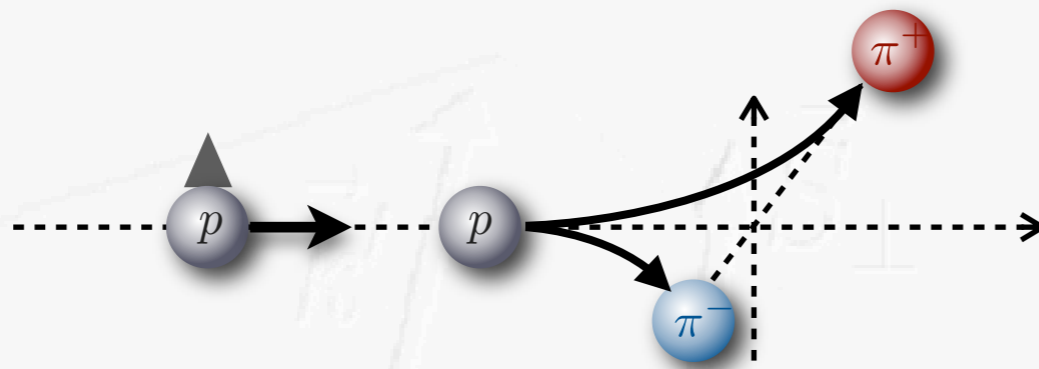


$$p^\uparrow p \rightarrow \pi X$$

- Sivers fit to HERMES data nicely described  $A_N$  in pp
- may also originate from Collins effect or twist-3 effects

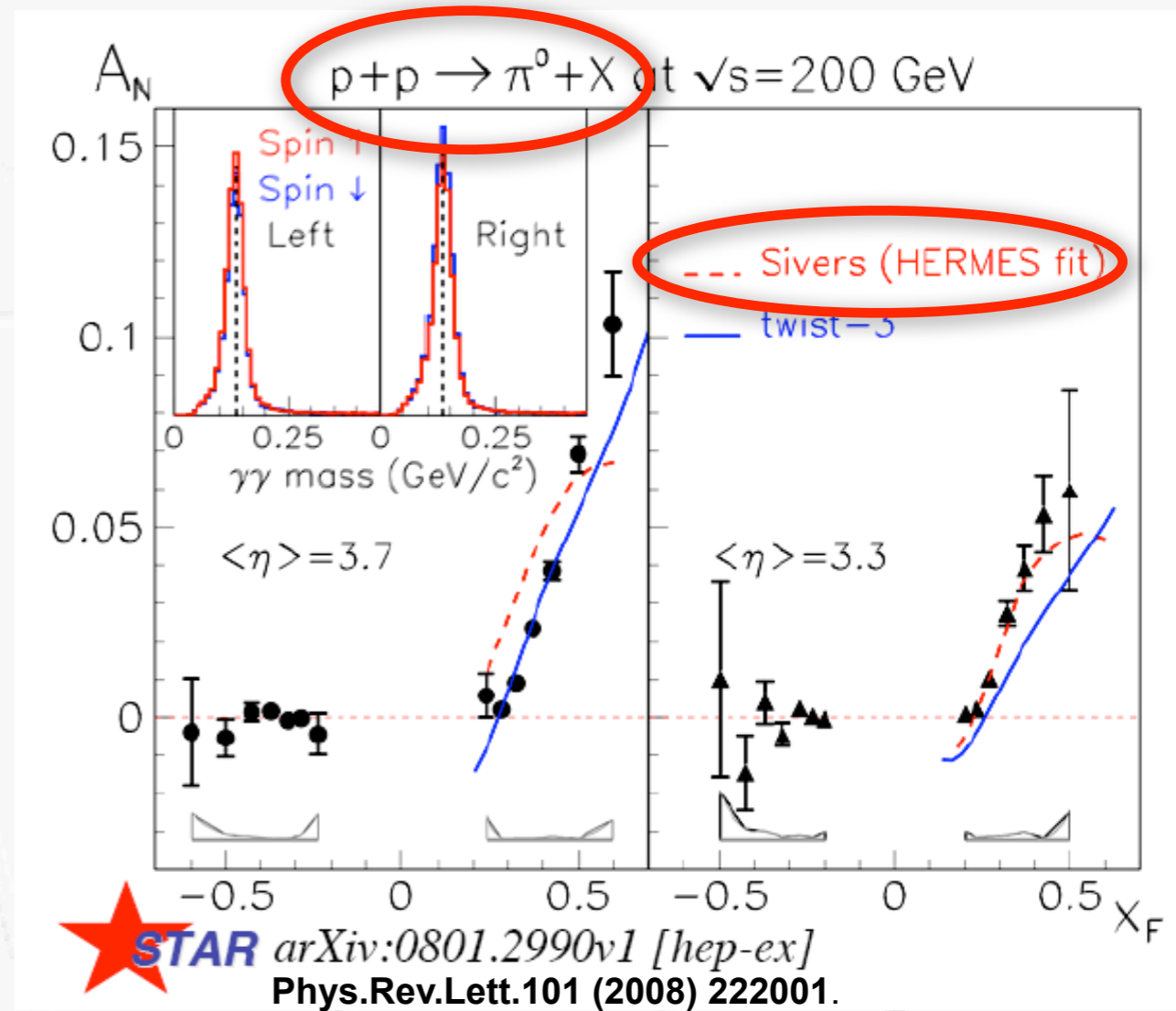


	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$



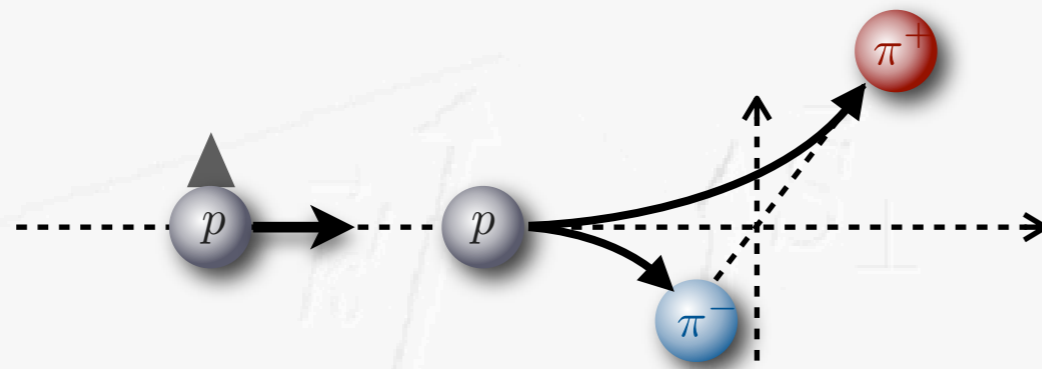
$$p^\uparrow p \rightarrow \pi X$$

- Sivers fit to HERMES data nicely described  $A_N$  in pp
- may also originate from Collins effect or twist-3 effects
- only sizable in forward direction



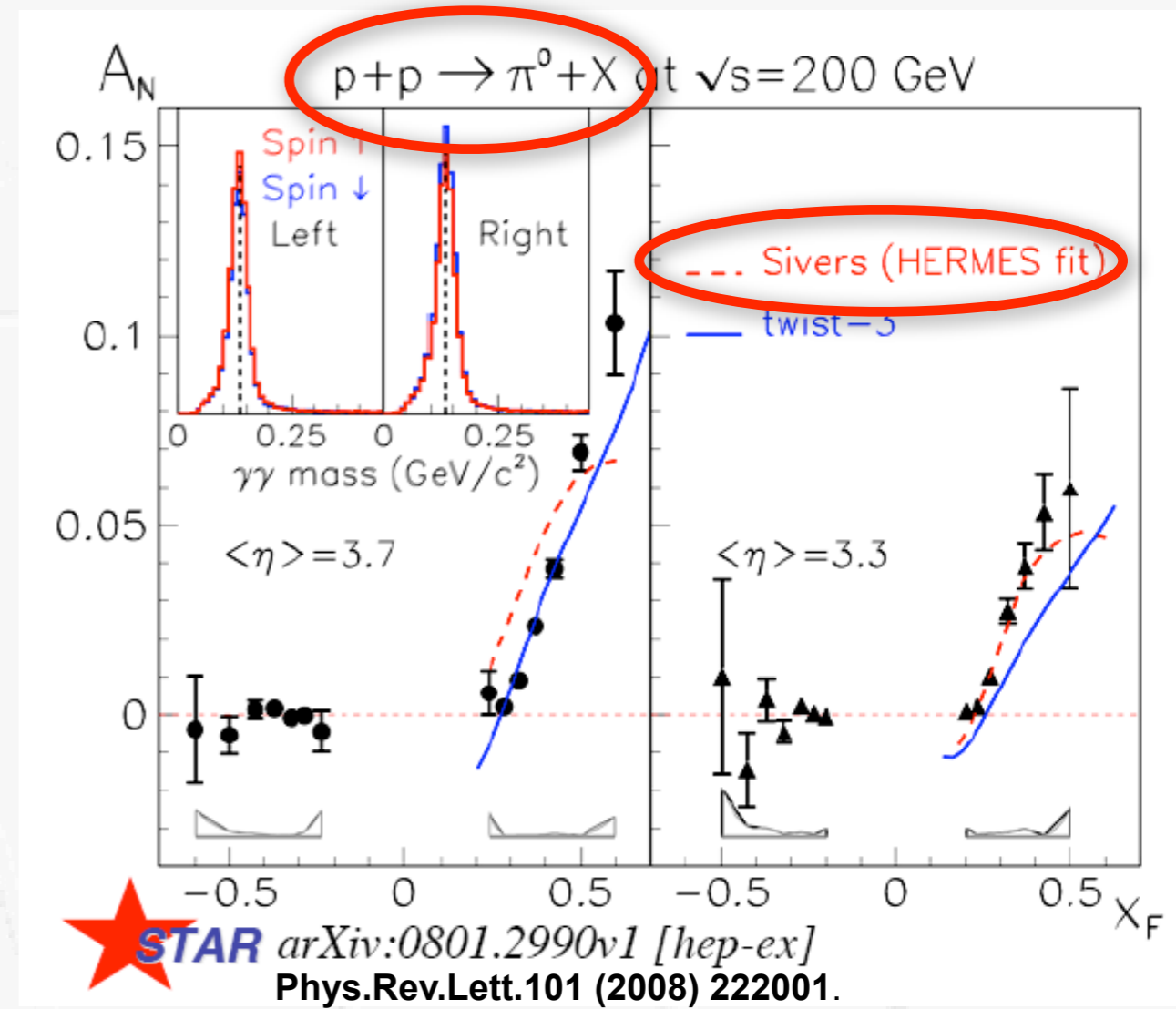


	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$



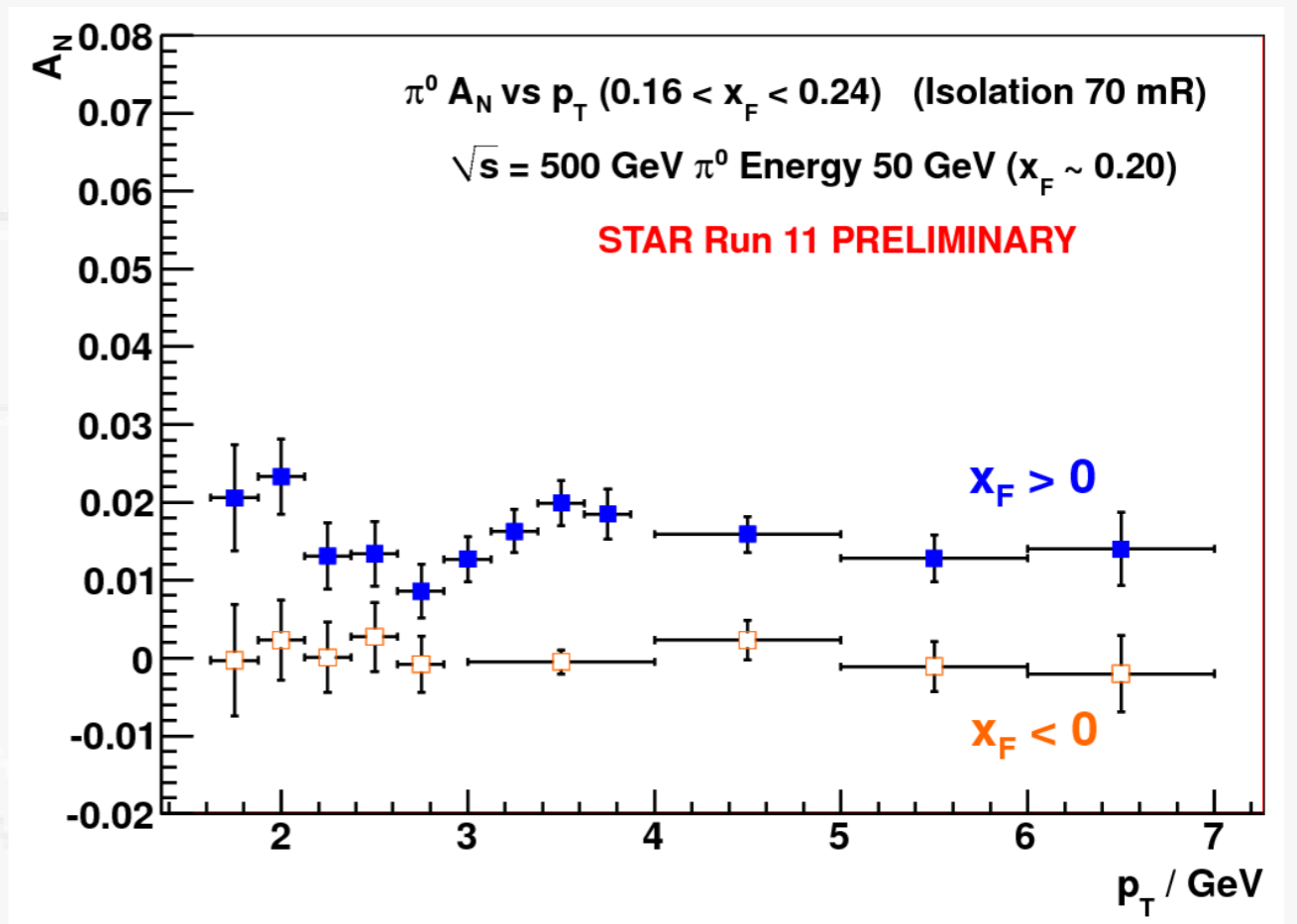
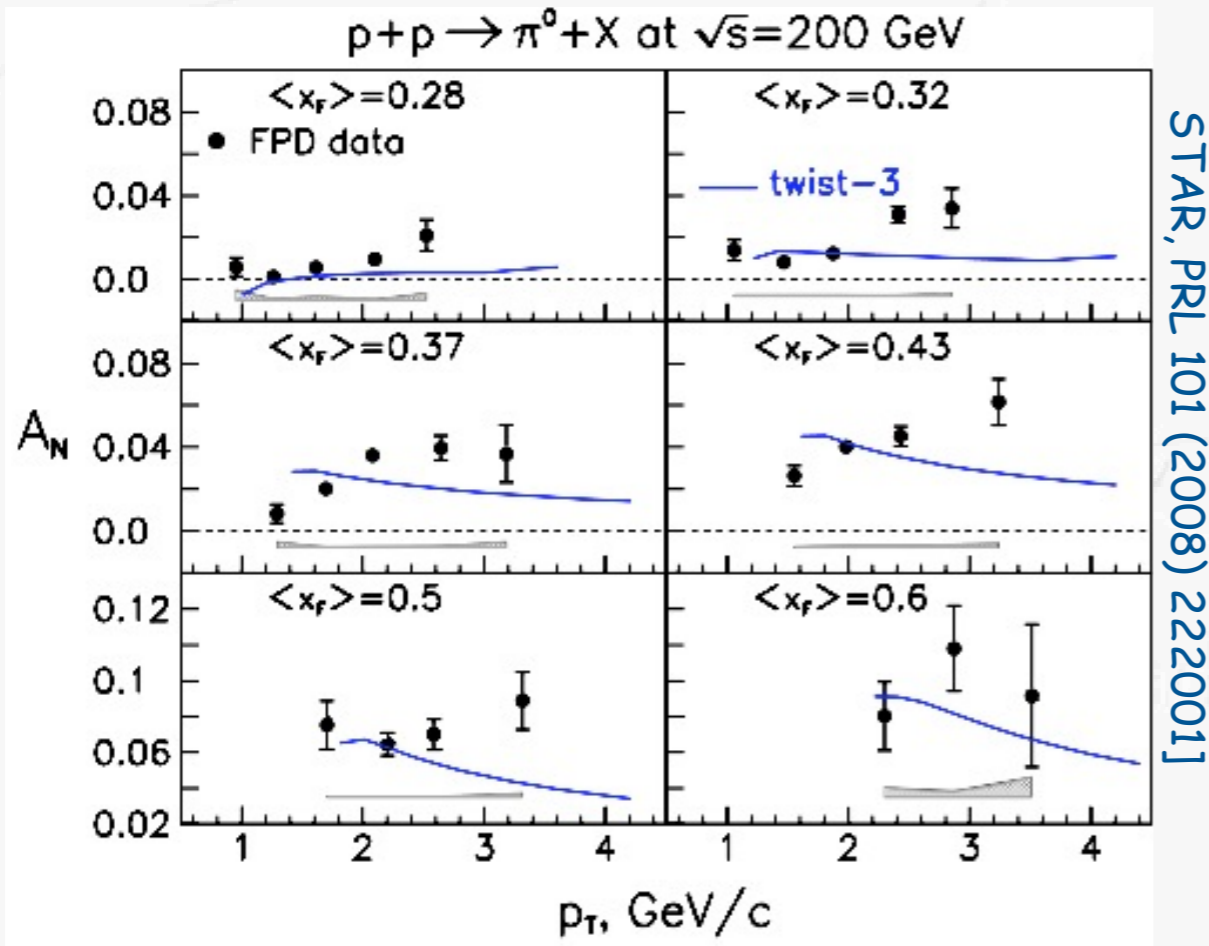
$$p^\uparrow p \rightarrow \pi X$$

- Sivers fit to HERMES data nicely described  $A_N$  in pp
- may also originate from Collins effect or twist-3 effects
- only sizable in forward direction
- after early success of linking twist-3 with Sivers, sign mismatch discovered:



$$gT_{q,F}(x, x) = - \int d^2 k_\perp \frac{|k_\perp|^2}{M} f_{1T}^{\perp q}(x, k_\perp^2) \Big|_{\text{SIDIS}}$$

# $p^\uparrow p \rightarrow \pi X$ - $p_T$ dependence

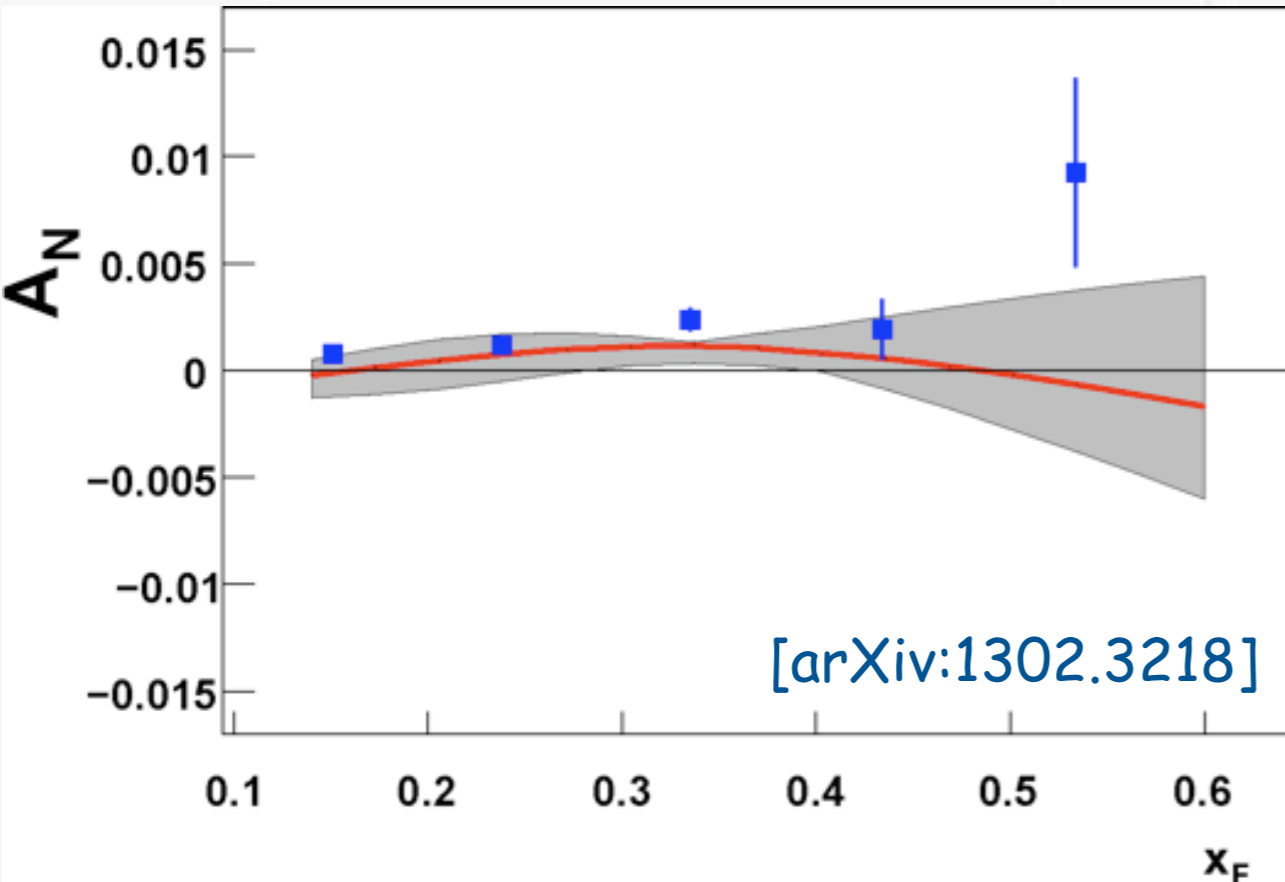


- clean approach: collinear twist-3
- but expected  $p_T$  fall-off not seen; or at least it's very slow

# ... not quite Drell-Yan yet: jet SSA

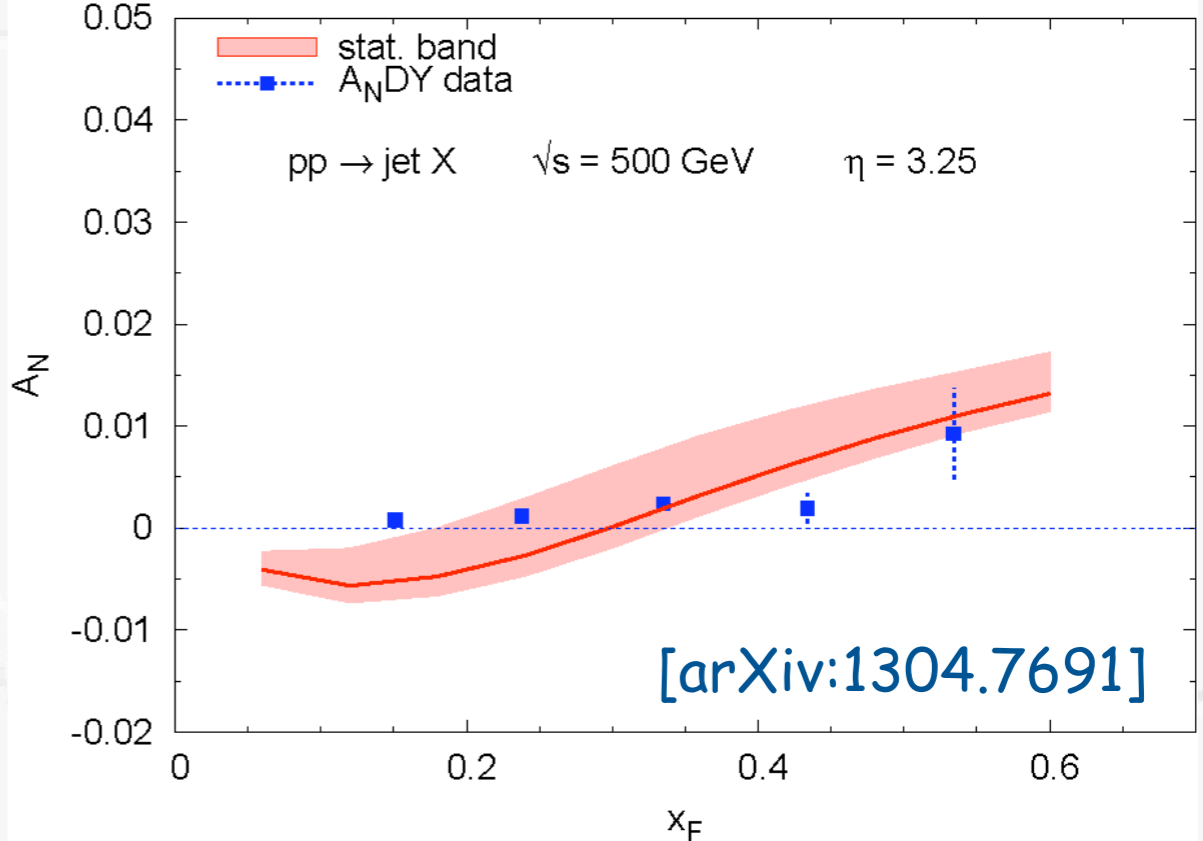
- no sensitivity to fragmentation details:  $p^\uparrow p \rightarrow \text{jet} + X$
- Sivers-type mechanism (-> use Sivers fctn from SIDIS fits)

data from [A<sub>N</sub>DY Collaboration, arXiv:1304.1454]



Includes initial- and final-state color-charge interactions

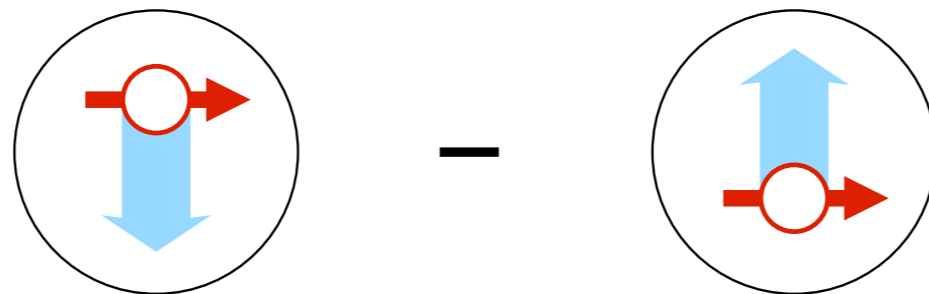
$$gT_{q,F}(x, x) = - \int d^2k_\perp \frac{|k_\perp|^2}{M} f_{1T}^{\perp q}(x, k_\perp^2)|_{\text{SIDIS}}$$



Excludes initial- and final-state color-charge interactions

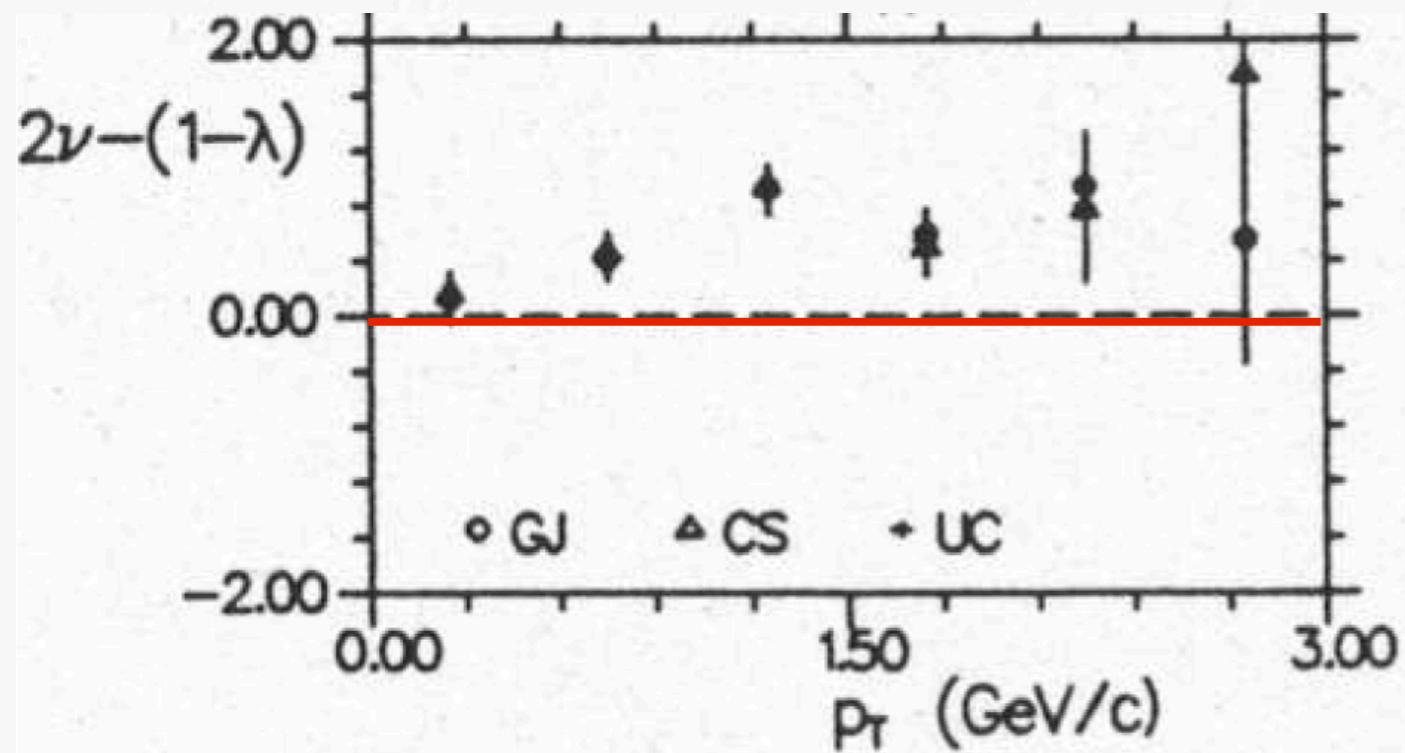
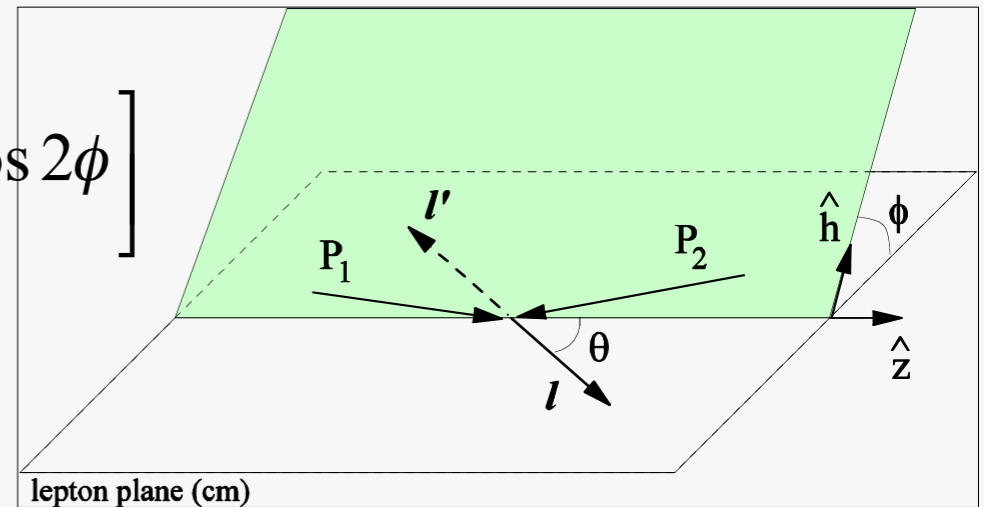
# Boer-Mulders

spin-effects in unpolarized reactions



# Unpolarized Drell-Yan

$$\left(\frac{1}{\sigma}\right)\left(\frac{d\sigma}{d\Omega}\right) = \left[\frac{3}{4\pi}\right] \left[ 1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi \right]$$



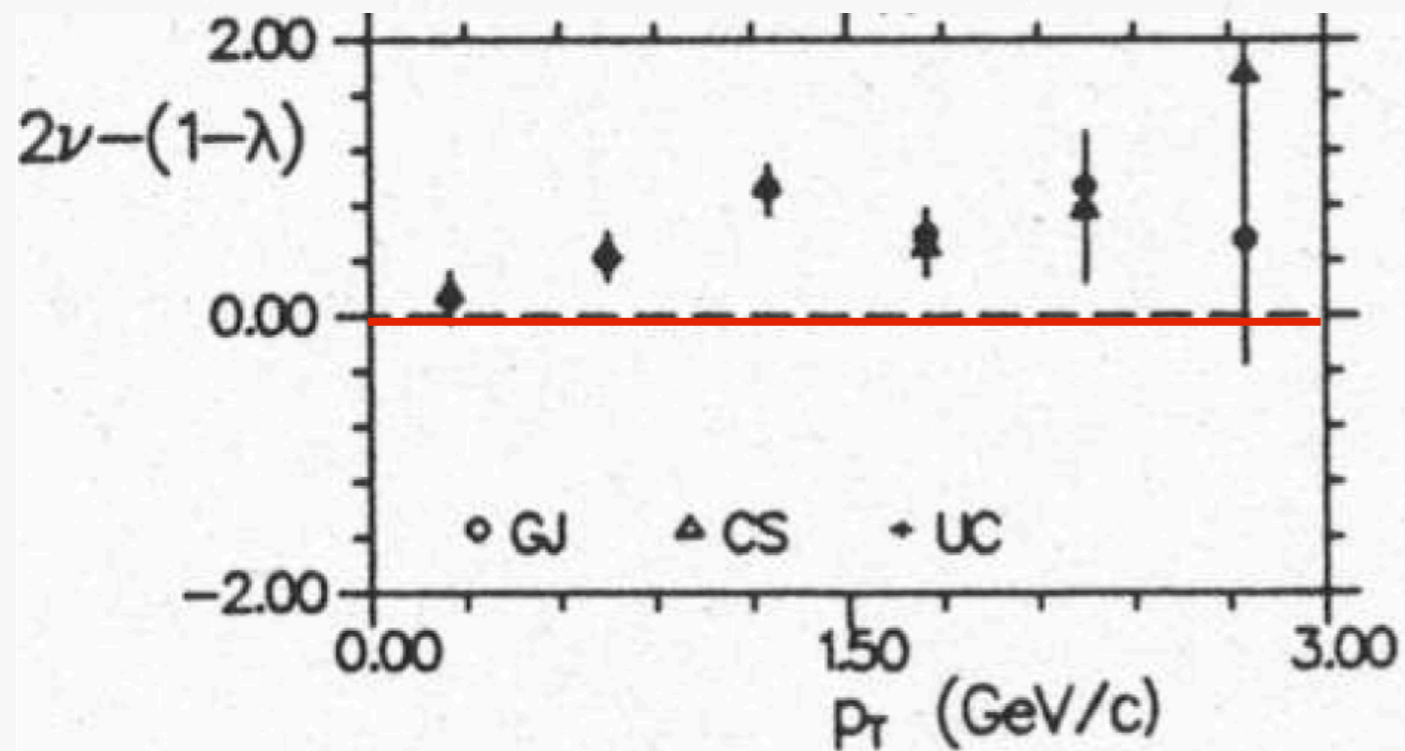
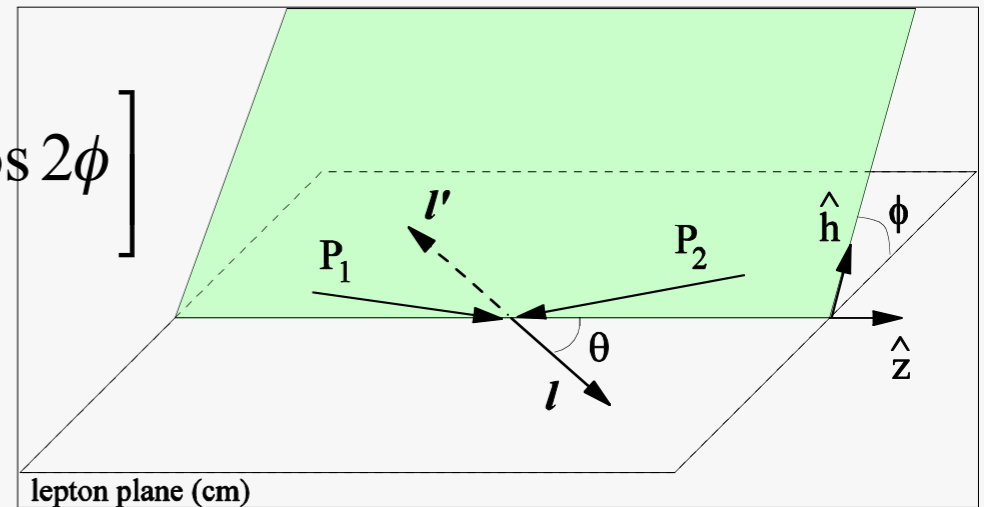
$$1 - \lambda - 2\nu = 0$$

Large deviations from Lam-Tung relation observed in DY  
[NA10 ('86/'88) & E615 ('89)]

C. Riedl

# Unpolarized Drell-Yan

$$\left(\frac{1}{\sigma}\right)\left(\frac{d\sigma}{d\Omega}\right) = \left[\frac{3}{4\pi}\right] \left[ 1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi \right]$$



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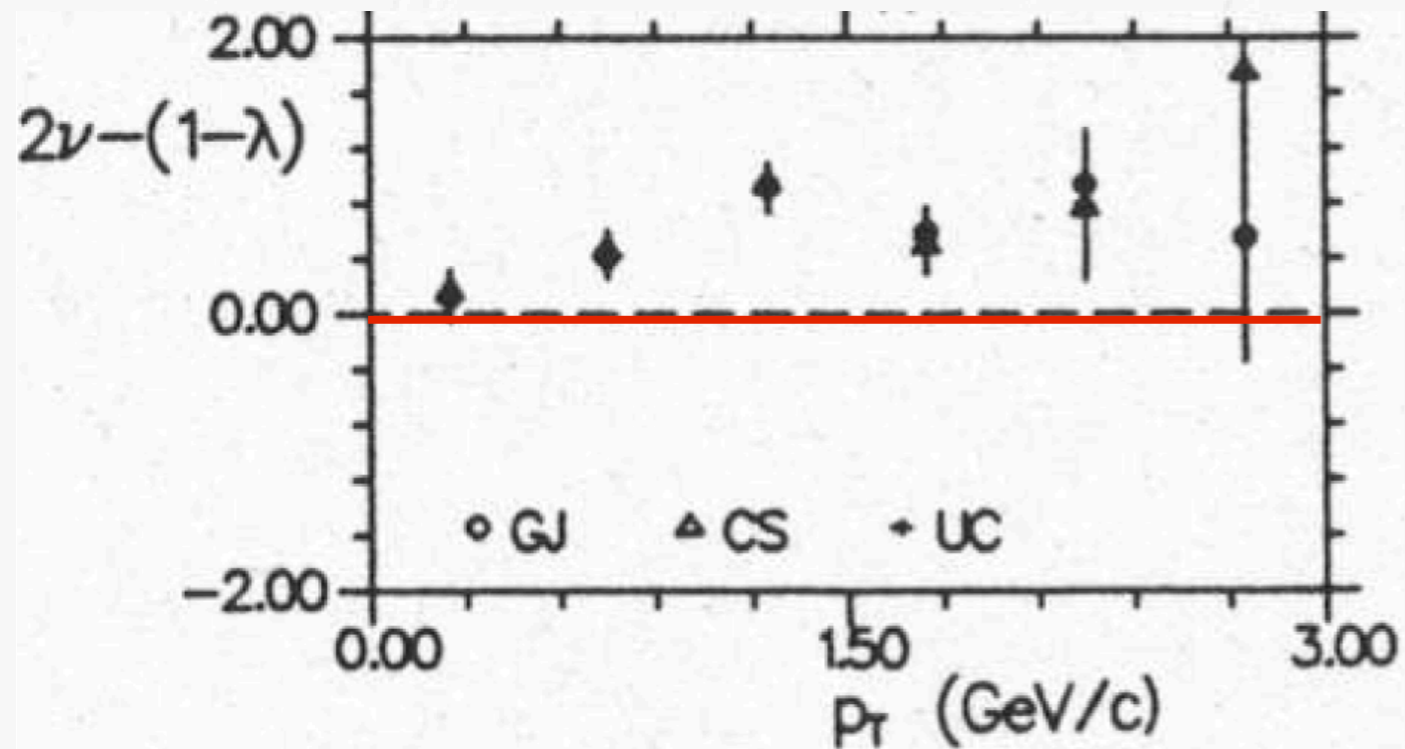
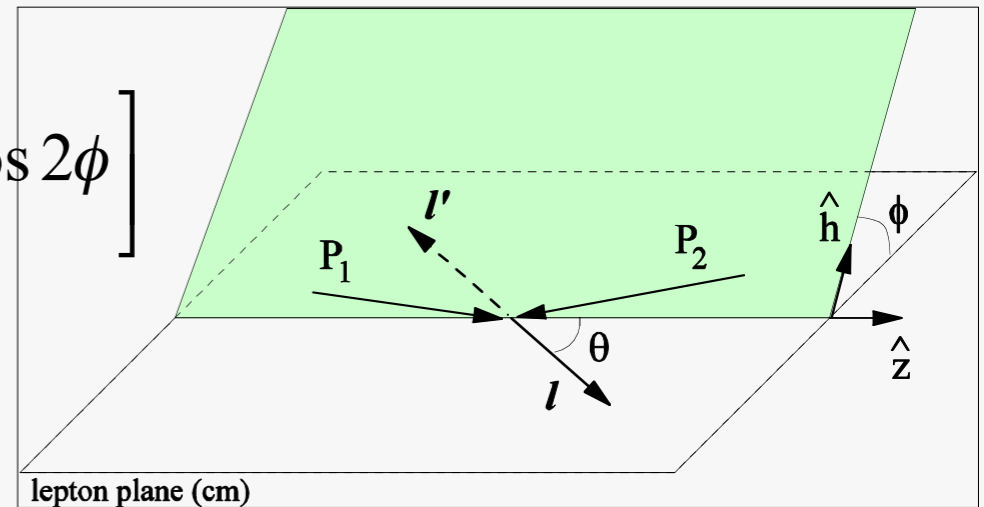
Large deviations from Lam-Tung relation observed in DY  
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- “failure” of collinear pQCD

➡ C. Riedl

# Unpolarized Drell-Yan

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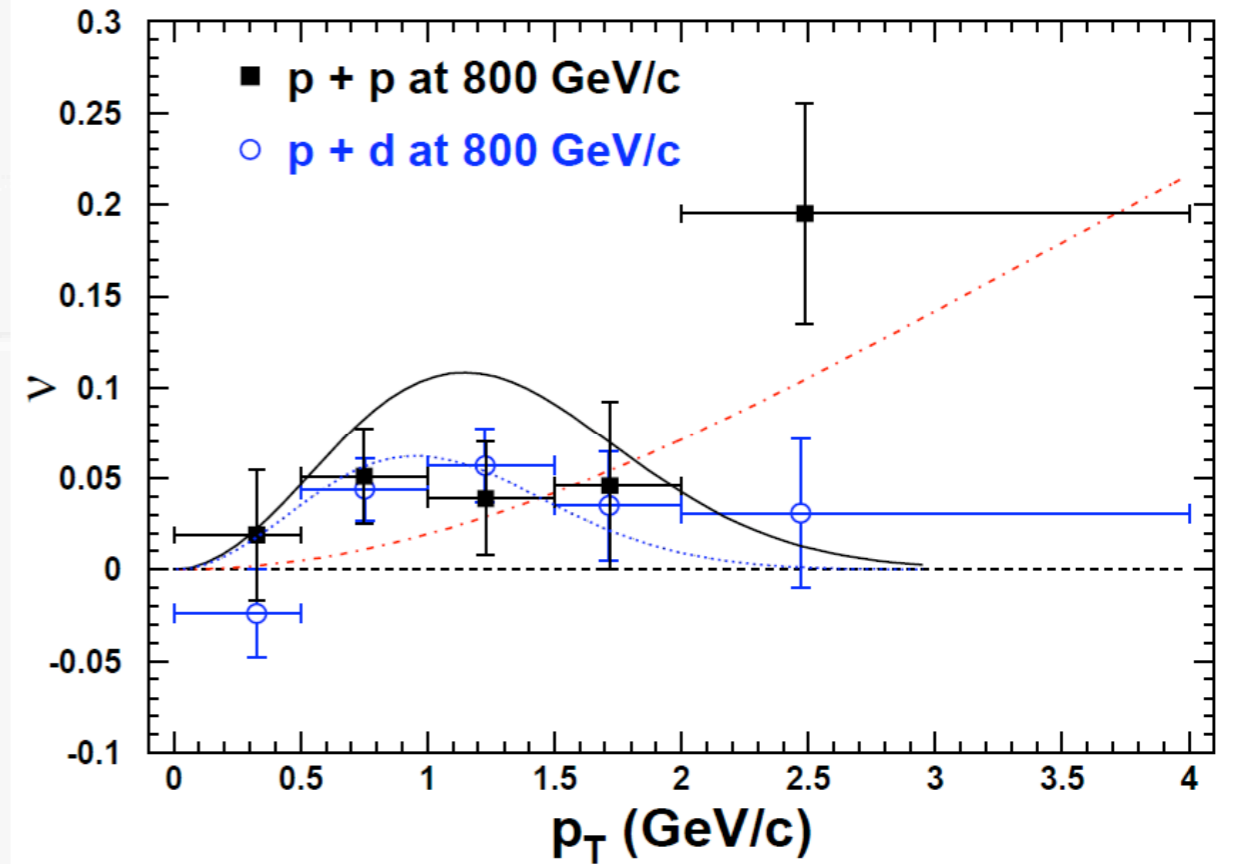
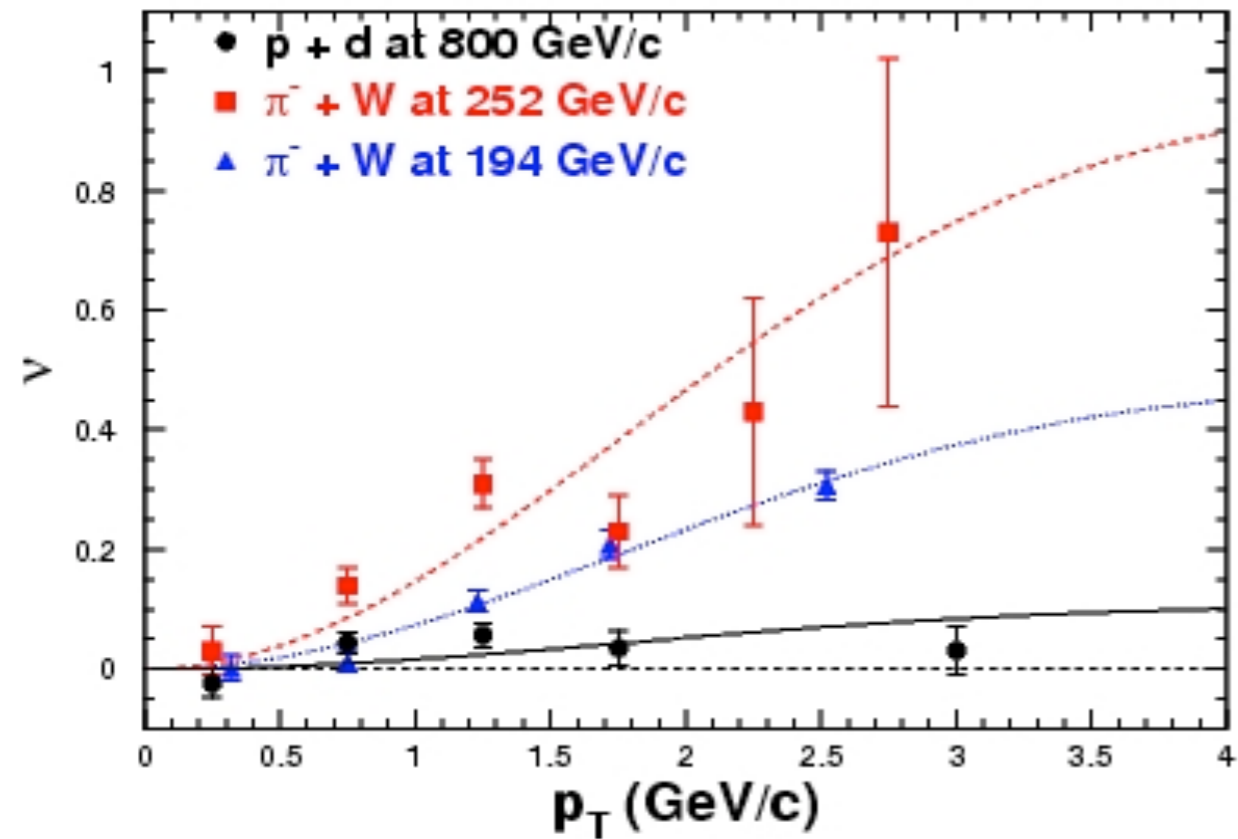
Large deviations from Lam-Tung relation observed in DY  
[NA10 ('86/'88) & E615 ('89)]

- “failure” of collinear pQCD
- possible source: Boer-Mulders effect

👉 C. Riedl

# Signs of Boer-Mulders

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

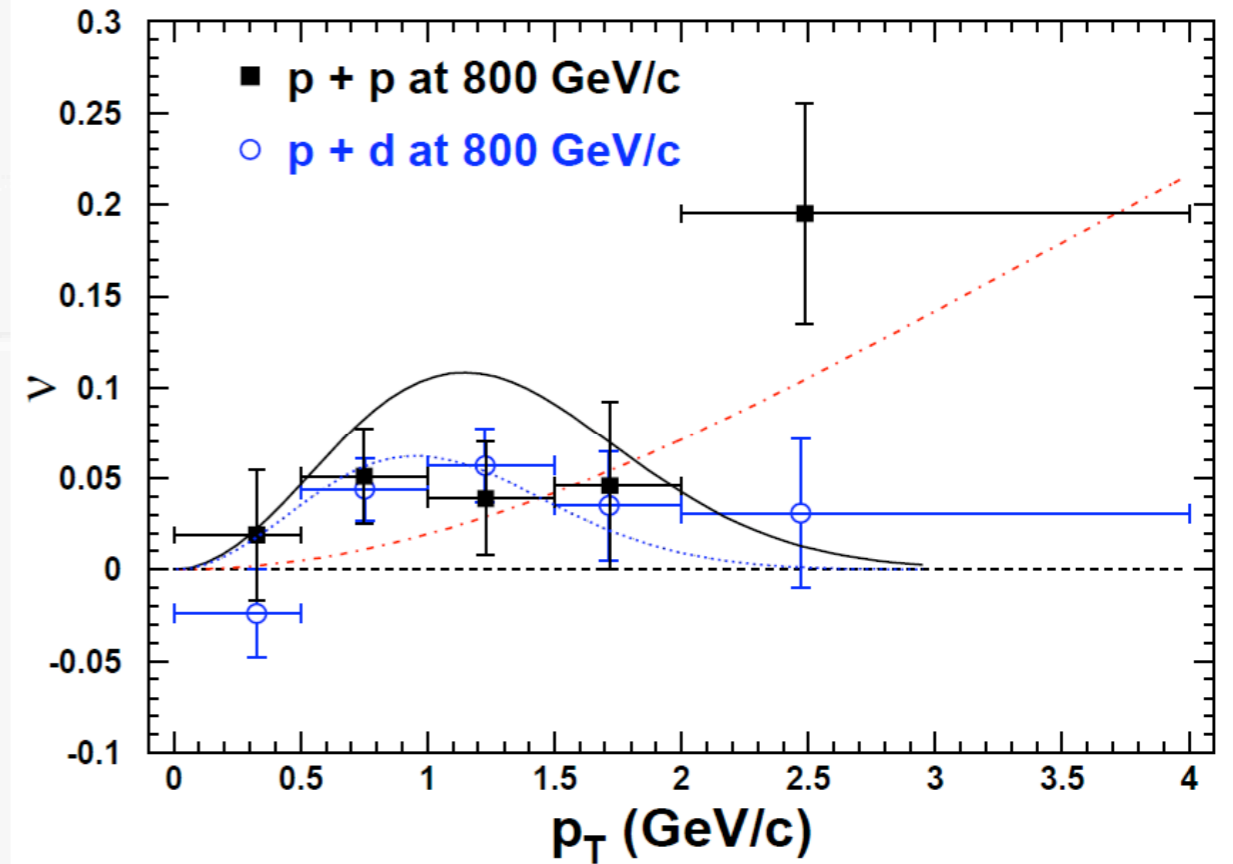
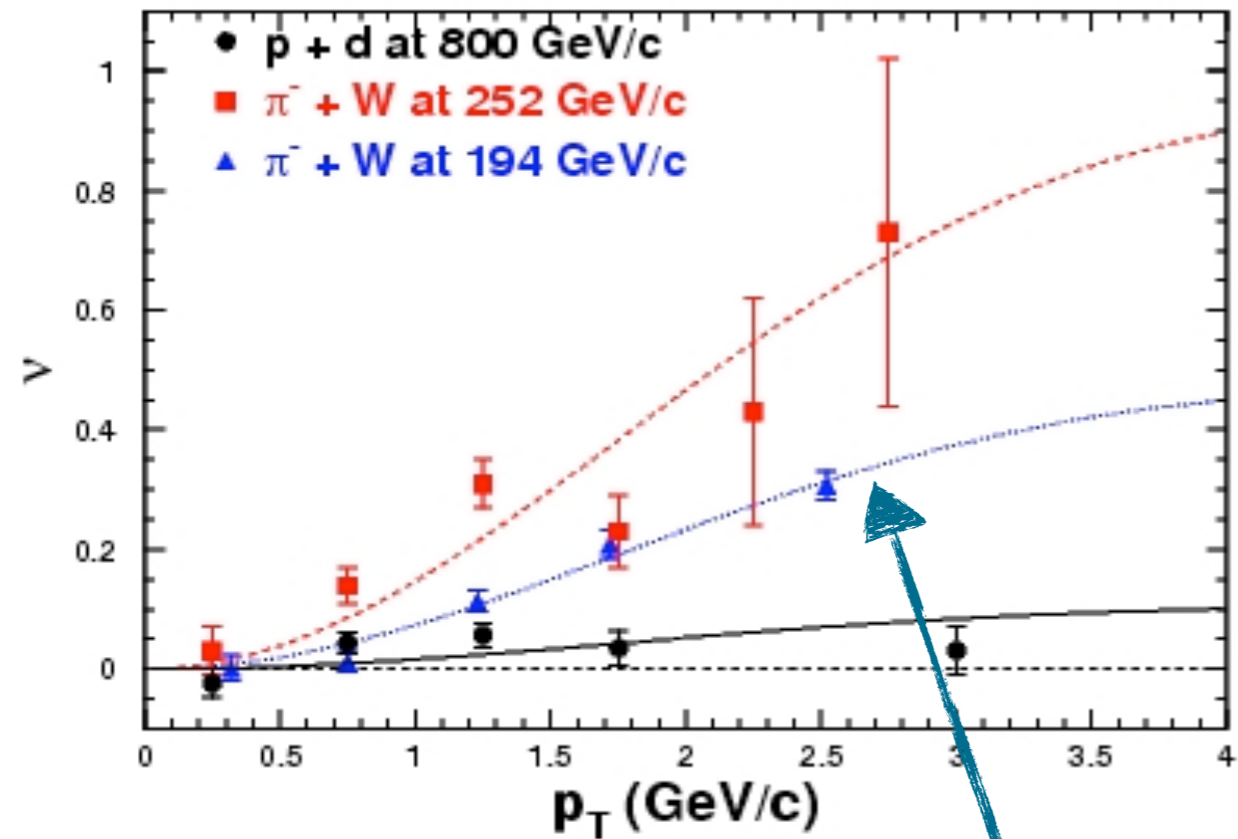


 C. Riedl



# Signs of Boer-Mulders

	U	L	T
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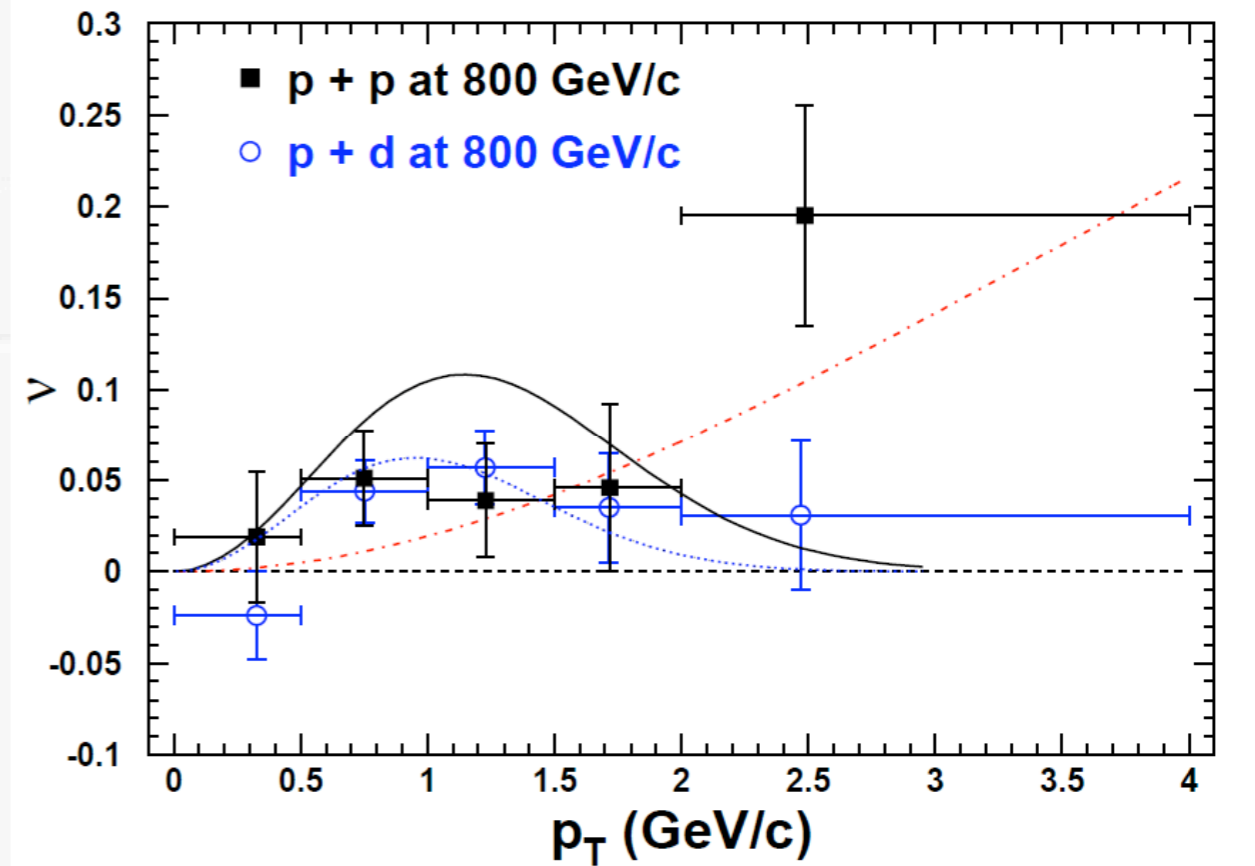
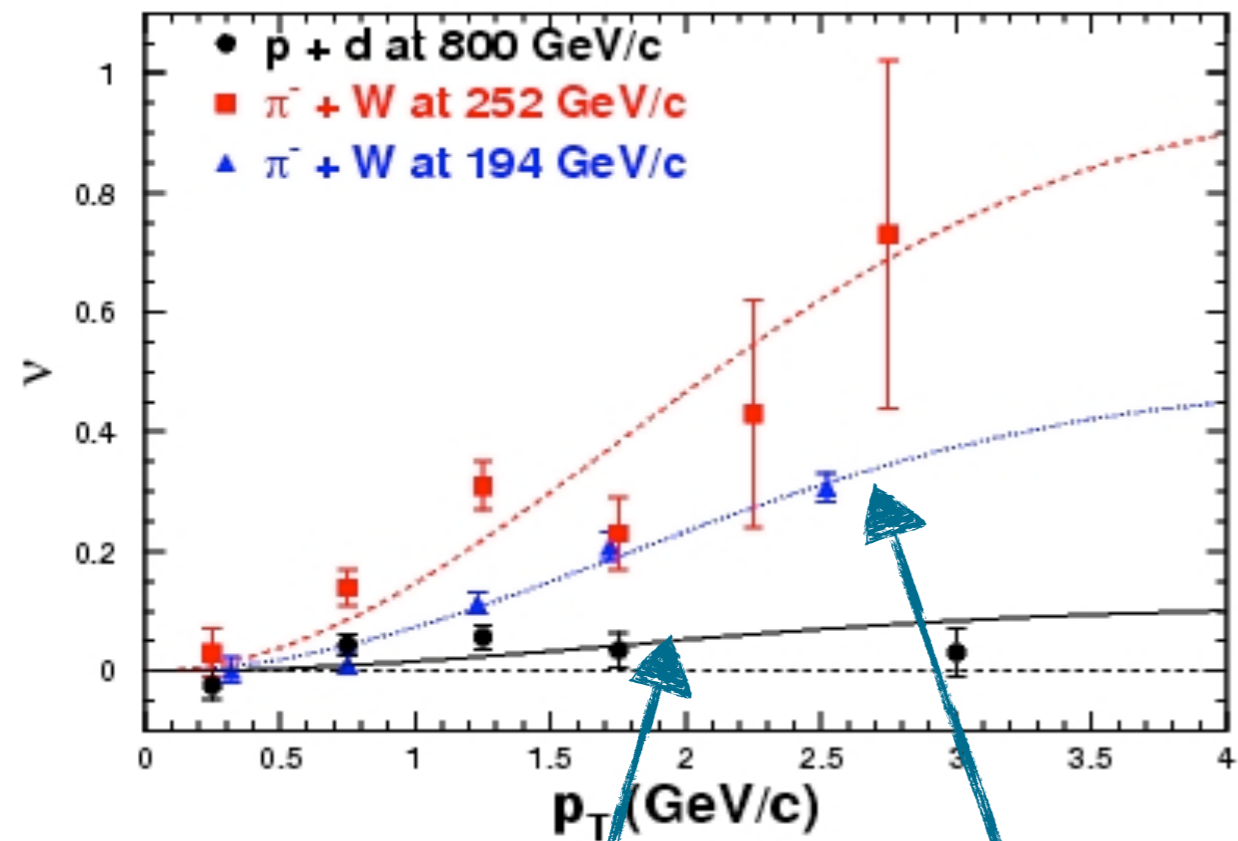


valence BM fctn

C. Riedl

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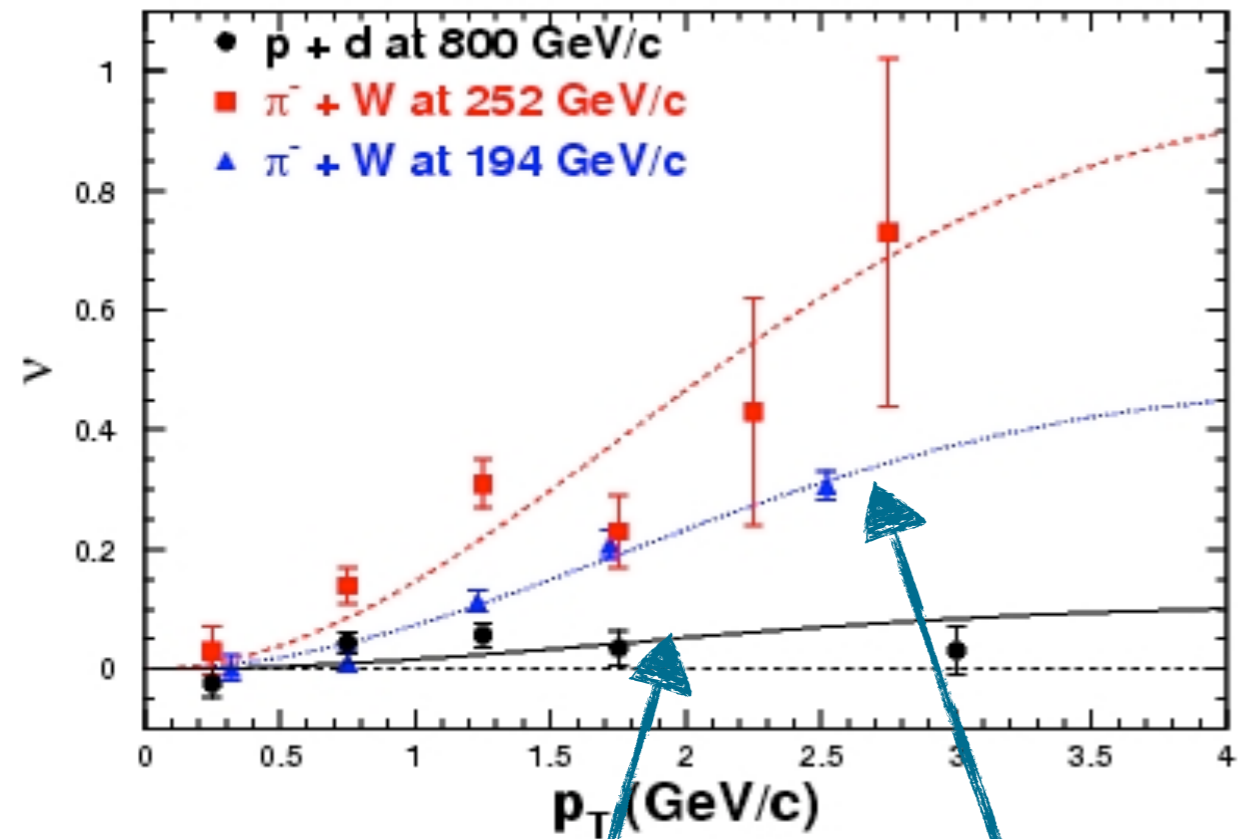
valence and sea BM fctn

valence BM fctn

👉 C. Riedl

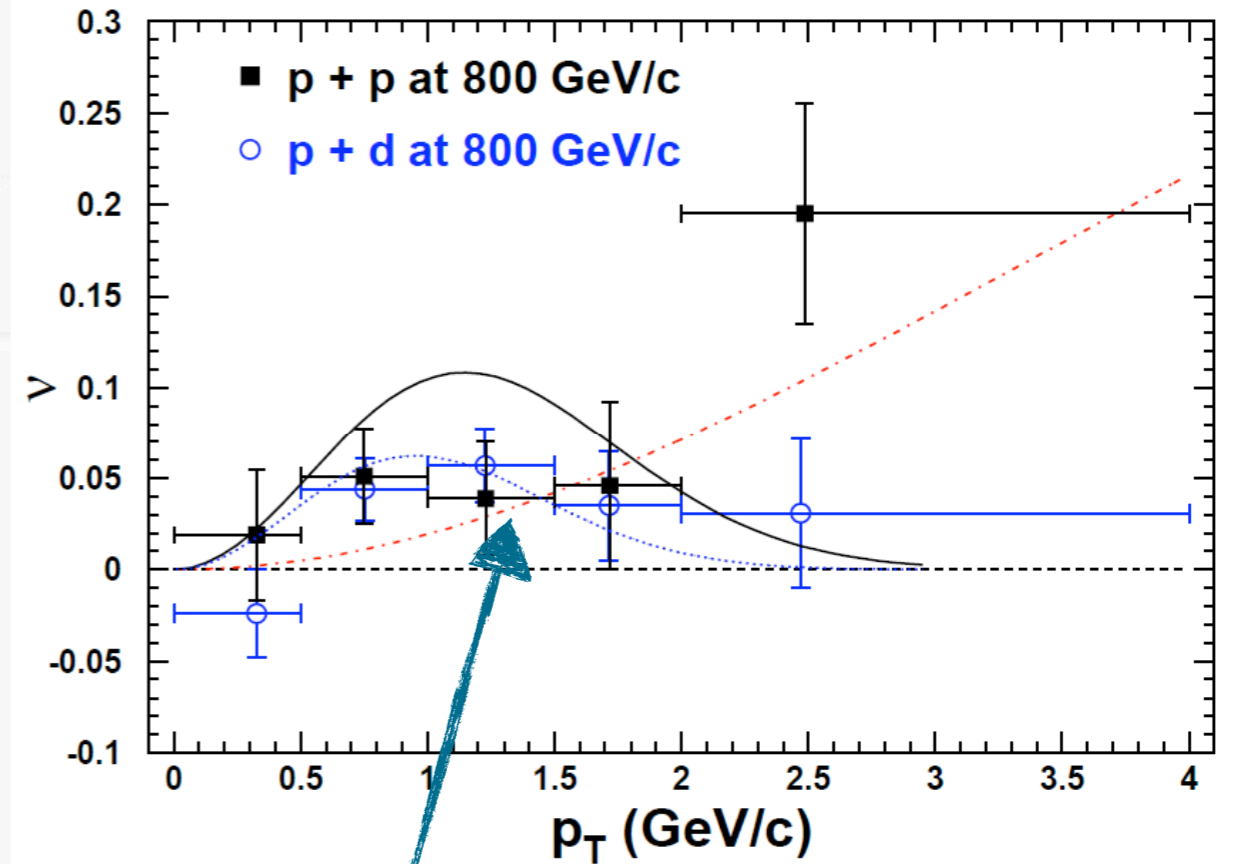
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valence and sea BM fctn

valence BM fctn

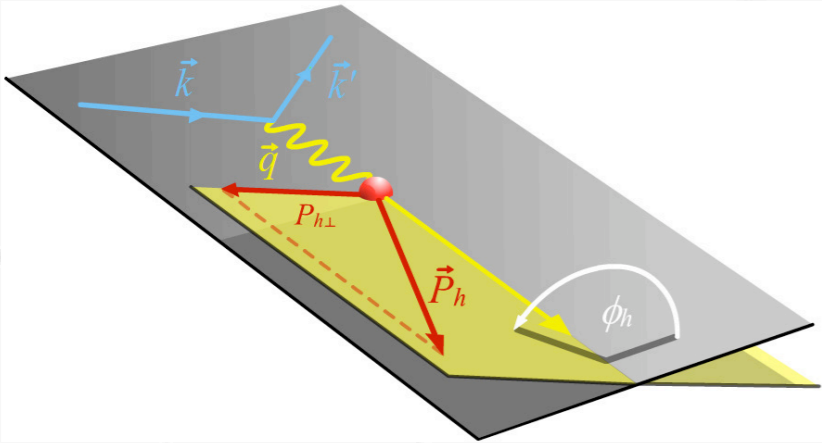


similar BM fctn for up  
and down quarks?

👉 C. Riedl

# Modulations in spin-independent SIDIS cross section

## SIDIS cross section



$$\frac{d^5 \sigma}{dx dy dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ A(y) F_{UU,T} + B(y) F_{UU,L} + C(y) \cos \phi_h F_{UU}^{\cos \phi_h} + B(y) \cos 2\phi_h F_{UU}^{\cos 2\phi_h} \right\}$$

**leading twist**  
 $F_{UU}^{\cos 2\phi_h} \propto C \left[ \frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{MM_h} h_1^\perp H_1^\perp \right]$  **BOER-MULDERS EFFECT**

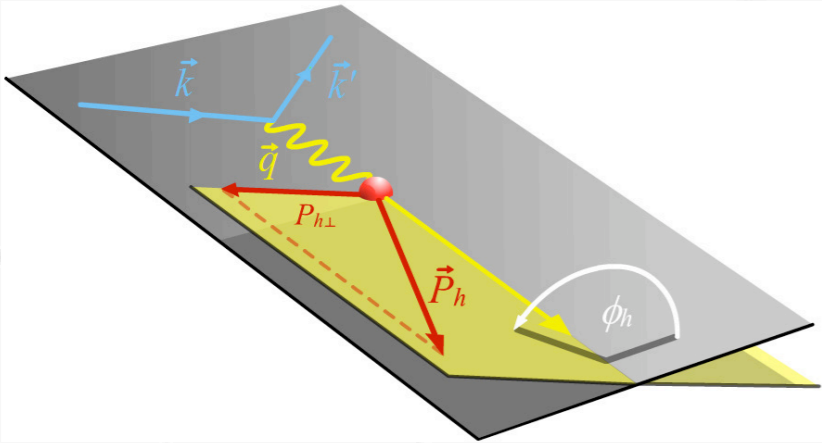
**next to leading twist**  
 $F_{UU}^{\cos \phi_h} \propto \frac{2M}{Q} C \left[ \frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M_h} x h_1^\perp H_1^\perp - \frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M} x f_1 D_1 + \dots \right]$  **CAHN EFFECT**

Interaction dependent terms neglected

(Implicit sum over quark flavours)

# Modulations in spin-independent SIDIS cross section

## SIDIS cross section



$$\frac{d^5 \sigma}{dx dy dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \left( 1 + \frac{\gamma^2}{2x} \right) \left\{ A(y) F_{UU,T} + B(y) F_{UU,L} + C(y) \cos \phi_h F_{UU}^{\cos \phi_h} + B(y) \cos 2\phi_h F_{UU}^{\cos 2\phi_h} \right\}$$

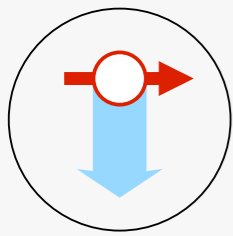
**leading twist**  
 $F_{UU}^{\cos 2\phi_h} \propto C \left[ \frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{MM_h} h_1^\perp H_1^\perp \right]$  **BOER-MULDERS EFFECT**

**next to leading twist**  
 $F_{UU}^{\cos \phi_h} \propto \frac{2M}{Q} C \left[ \frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M_h} x h_1^\perp H_1^\perp - \frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M} x f_1 D_1 + \dots \right]$  **CAHN EFFECT**

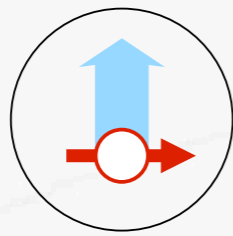
Interaction dependent terms neglected

(Implicit sum over quark flavours)

B. Parsamyan

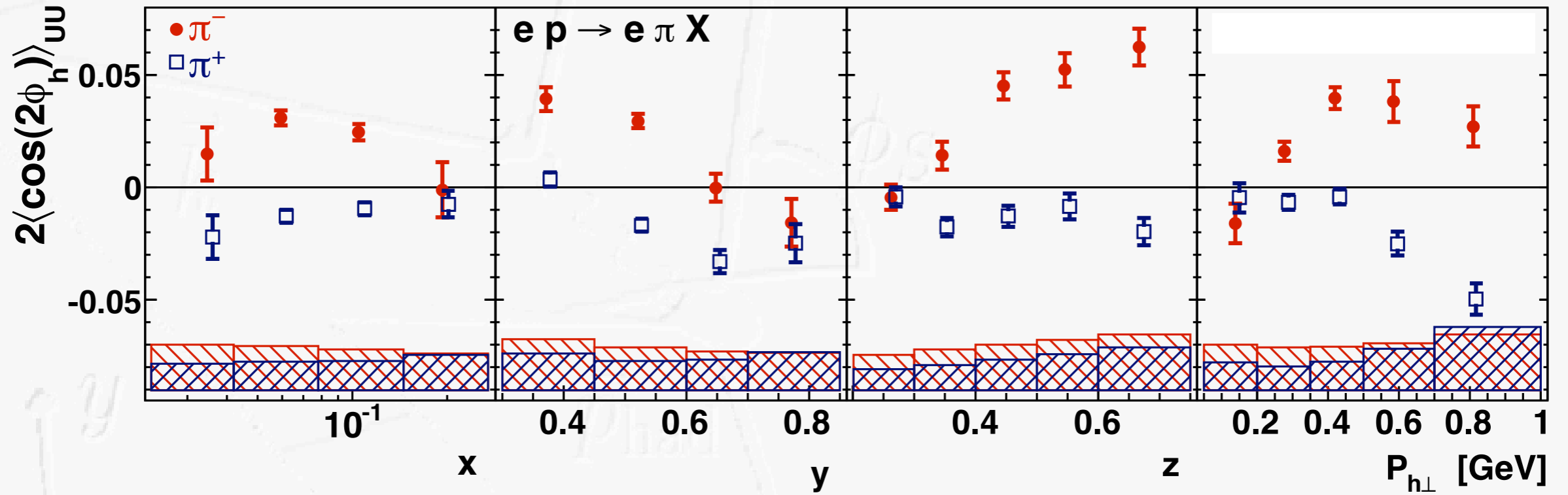


-



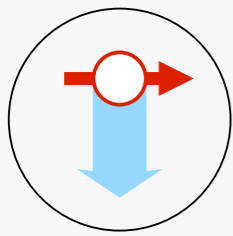
# signs of Boer-Mulders

[Airapetian et al., PRD 87 (2013) 012010]

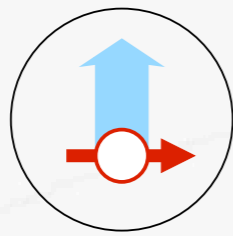


● not zero!

👉 B. Parsamyan

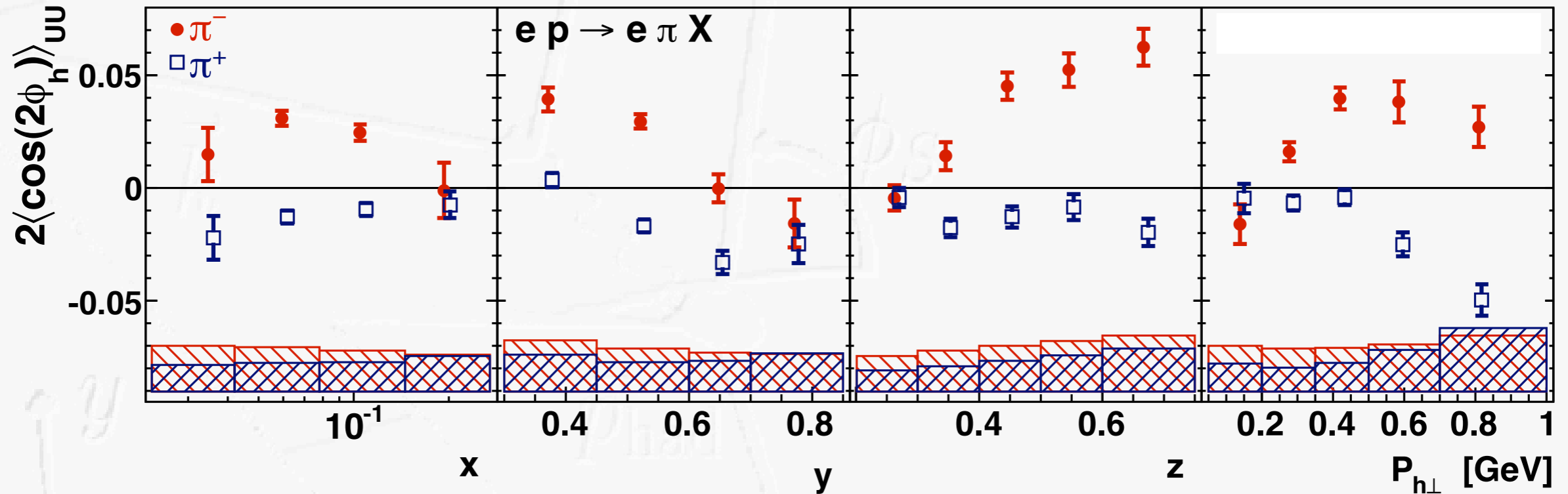


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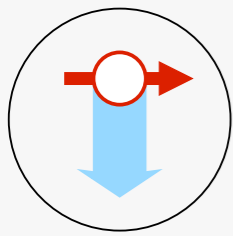


# signs of Boer-Mulders

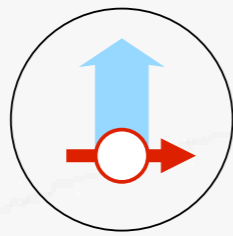
[Airapetian et al., PRD 87 (2013) 012010]



- not zero!
- opposite sign for charged pions with larger magnitude for  $\pi^-$   
→ same-sign BM-function for valence quarks?

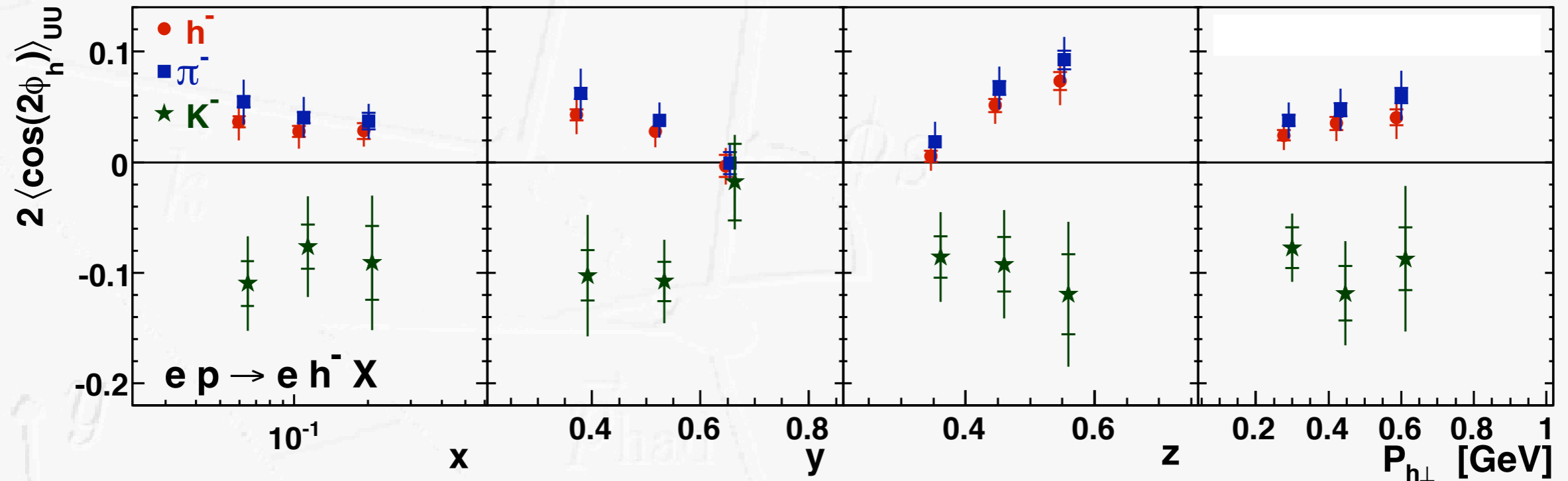


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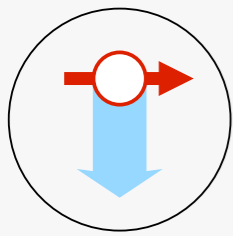
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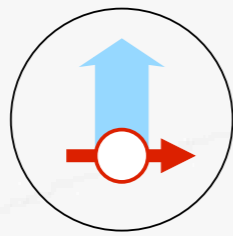


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- intriguing behavior for kaons



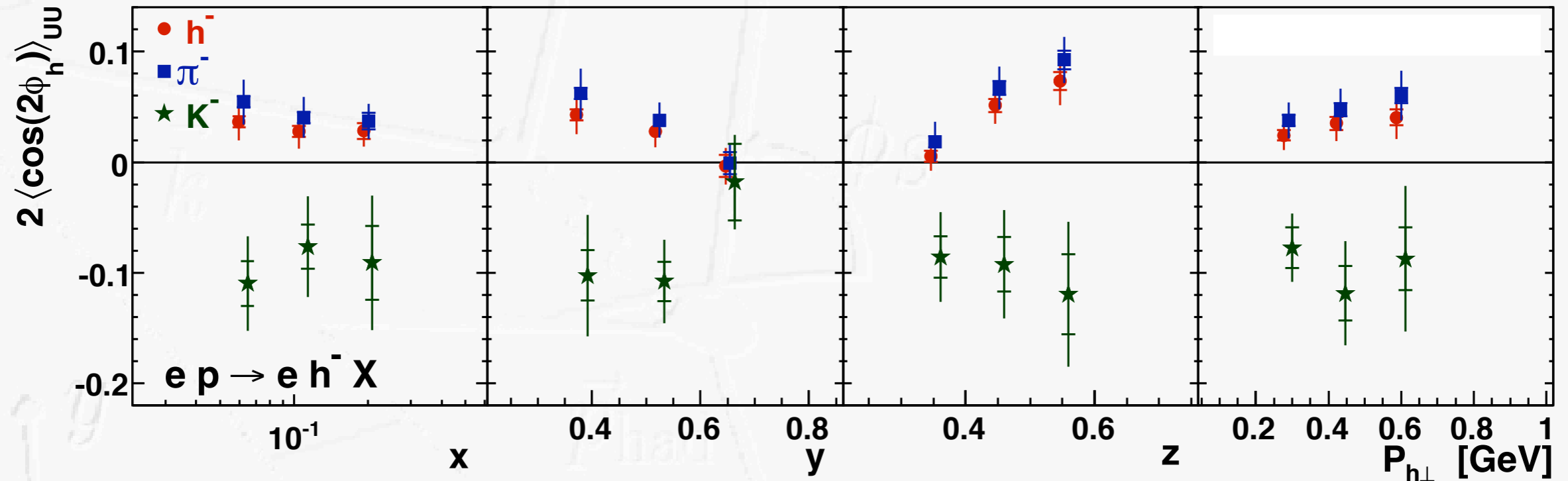


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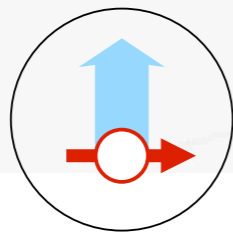
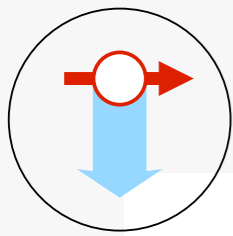
# signs of Boer-Mulders

[Airapetian et al., PRD 87 (2013) 012010]



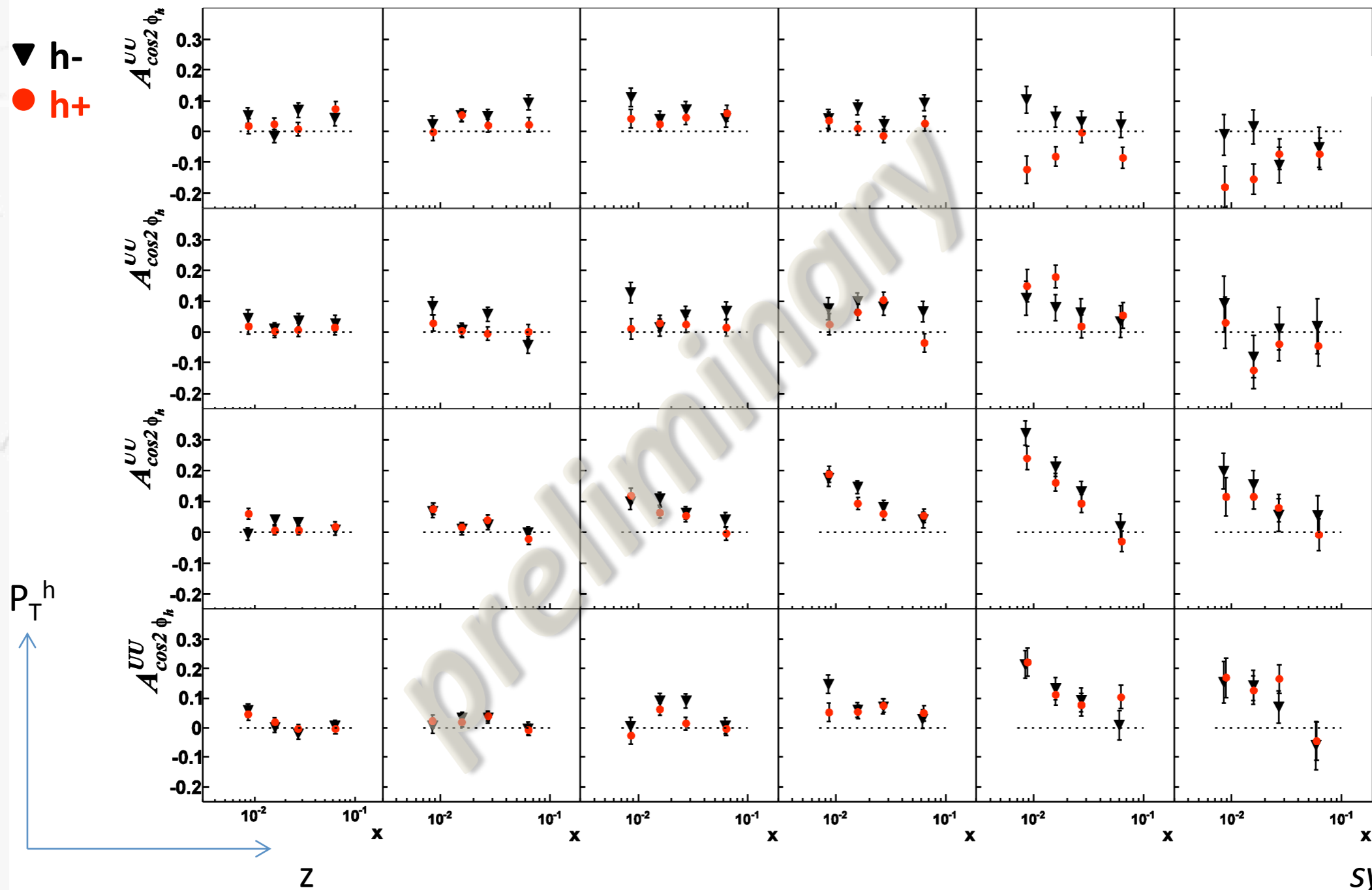
- not zero!
- opposite sign for charged pions with larger magnitude for  $\pi^-$   
→ same-sign BM-function for valence quarks?
- intriguing behavior for kaons
- available in multidimensional binning both from HERMES and soon from COMPASS

➡ B. Parsamyan

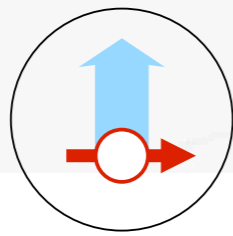
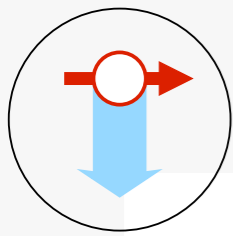


# signs of Boer-Mulders

COMPASS<sup>6</sup>LiD (25% of 2004 data)

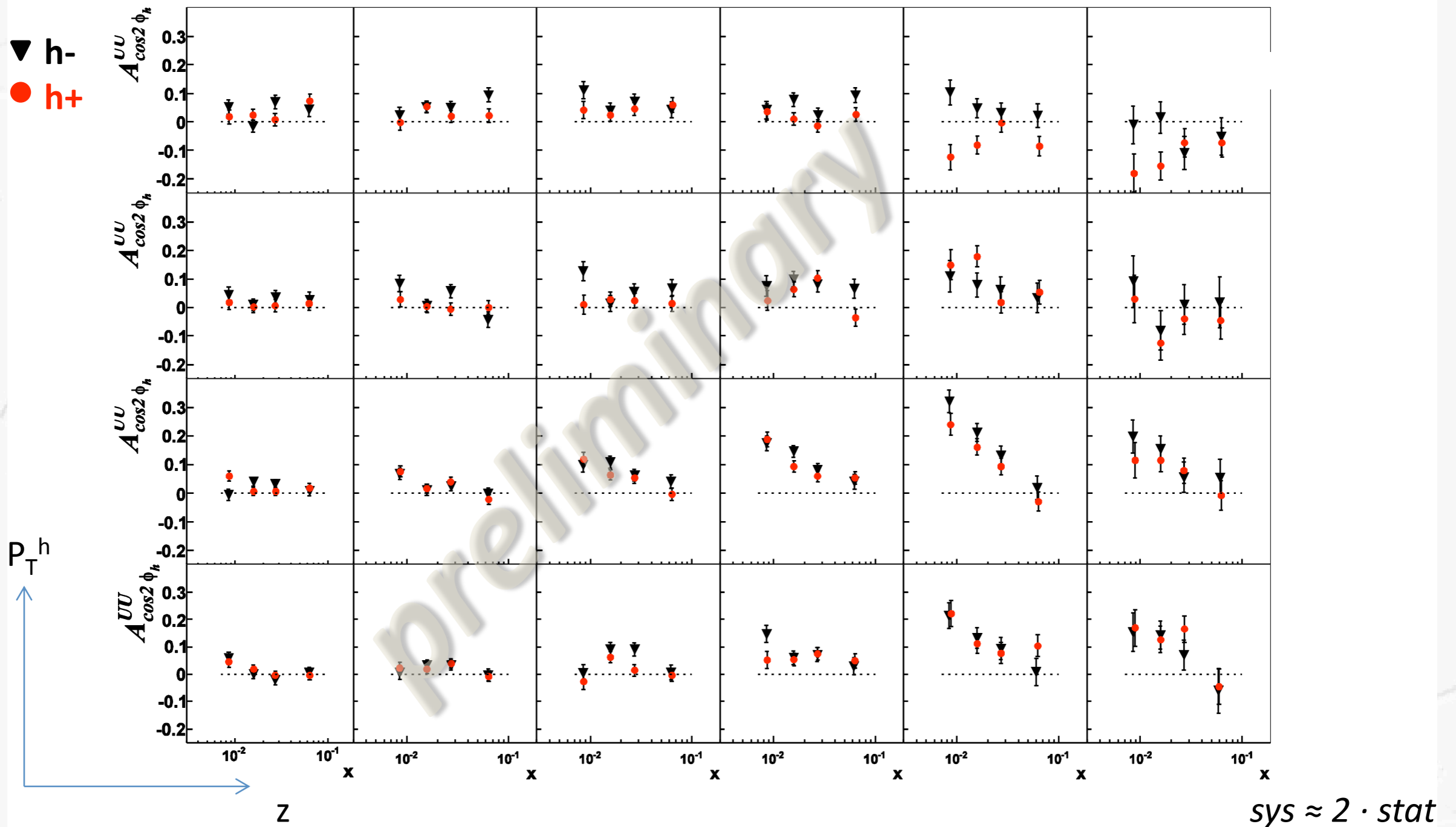


B. Parsamyan



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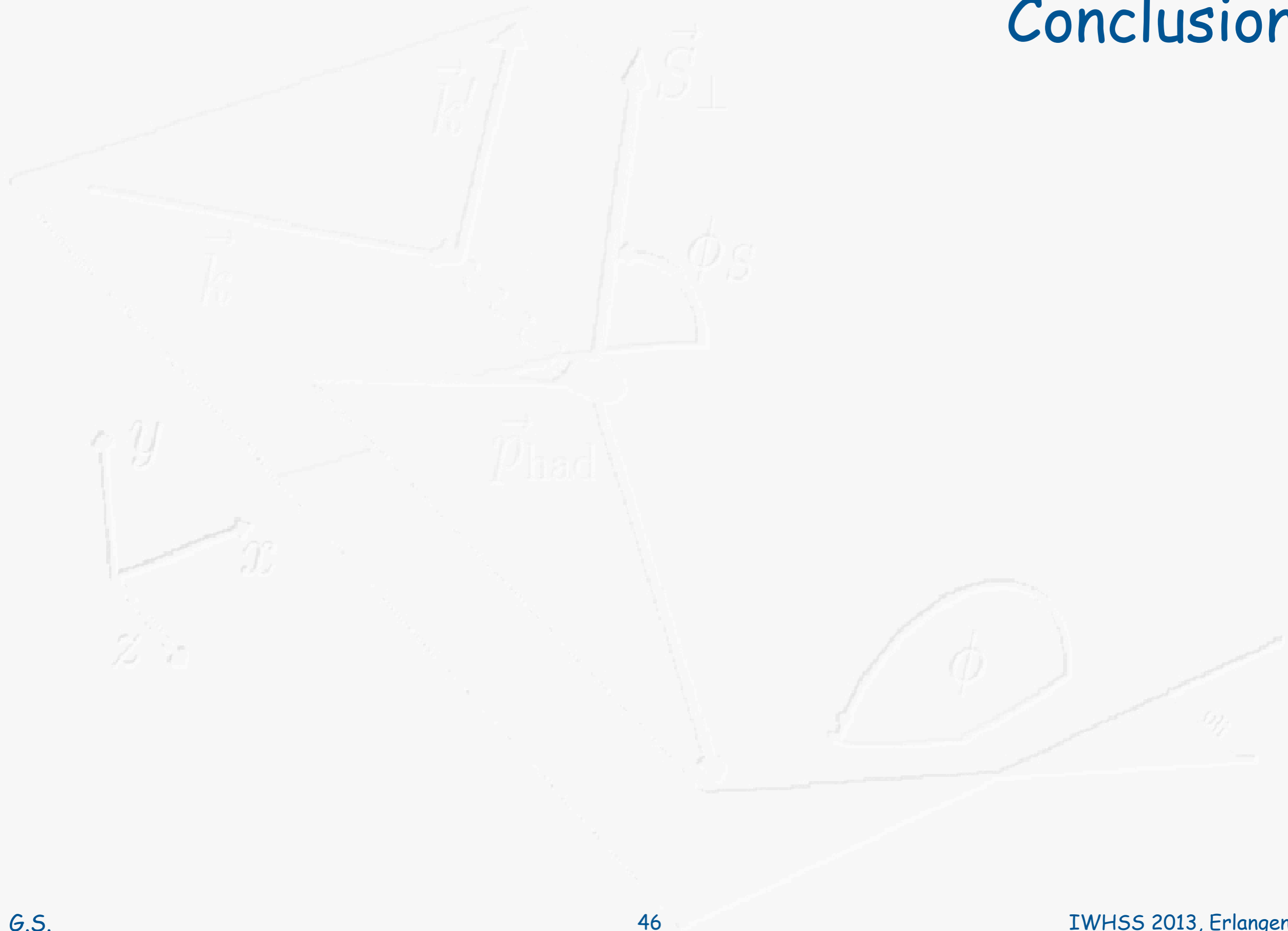
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B. Parsamyan

# Conclusion



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  - non-zero correlation between quark transverse momentum and nucleon transverse polarization (**Sivers effect**)
  - non-zero **transversity**, and correlation between transverse hadron momentum and transverse spin of fragm. quark (**Collins effect**)
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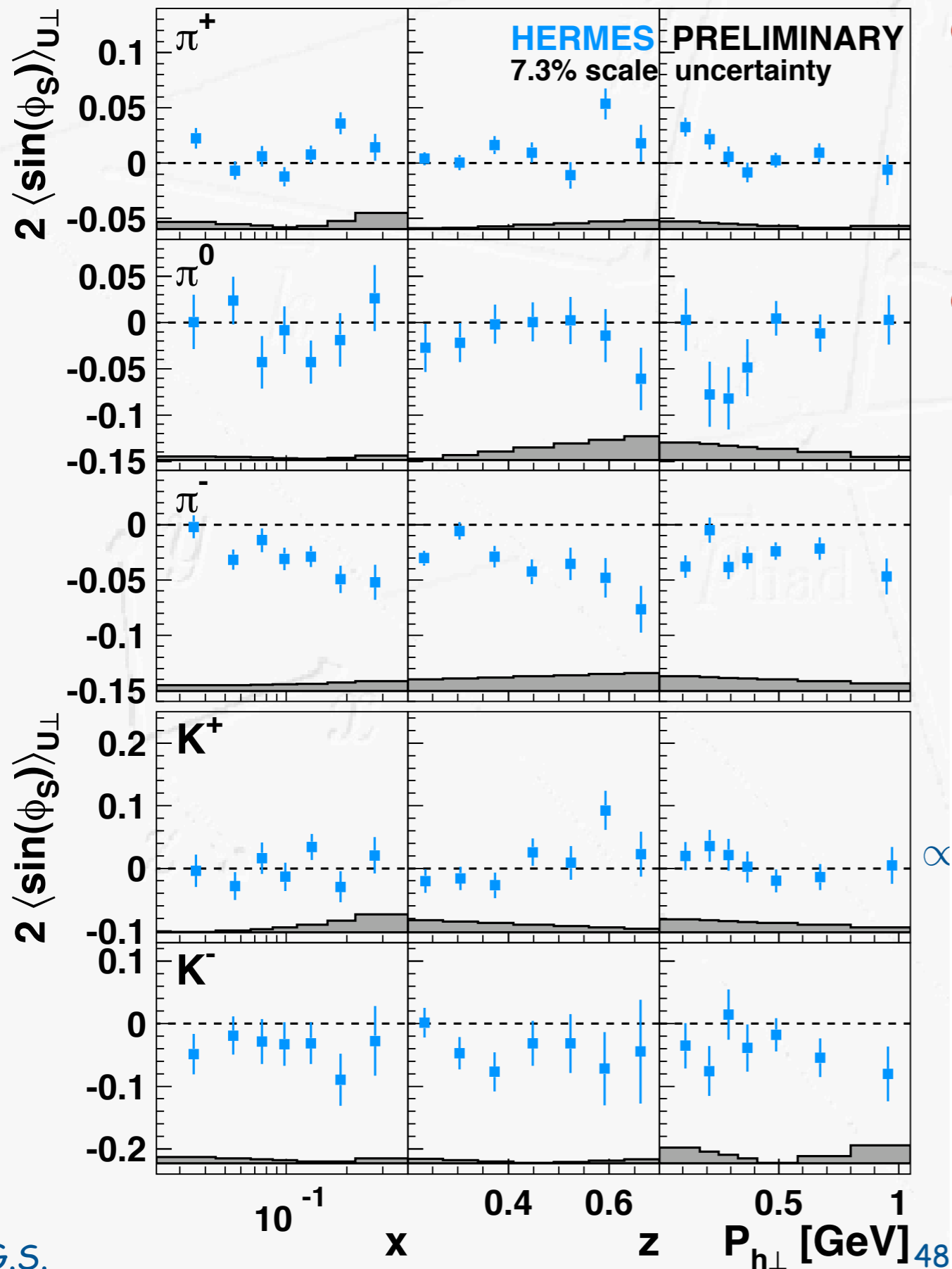
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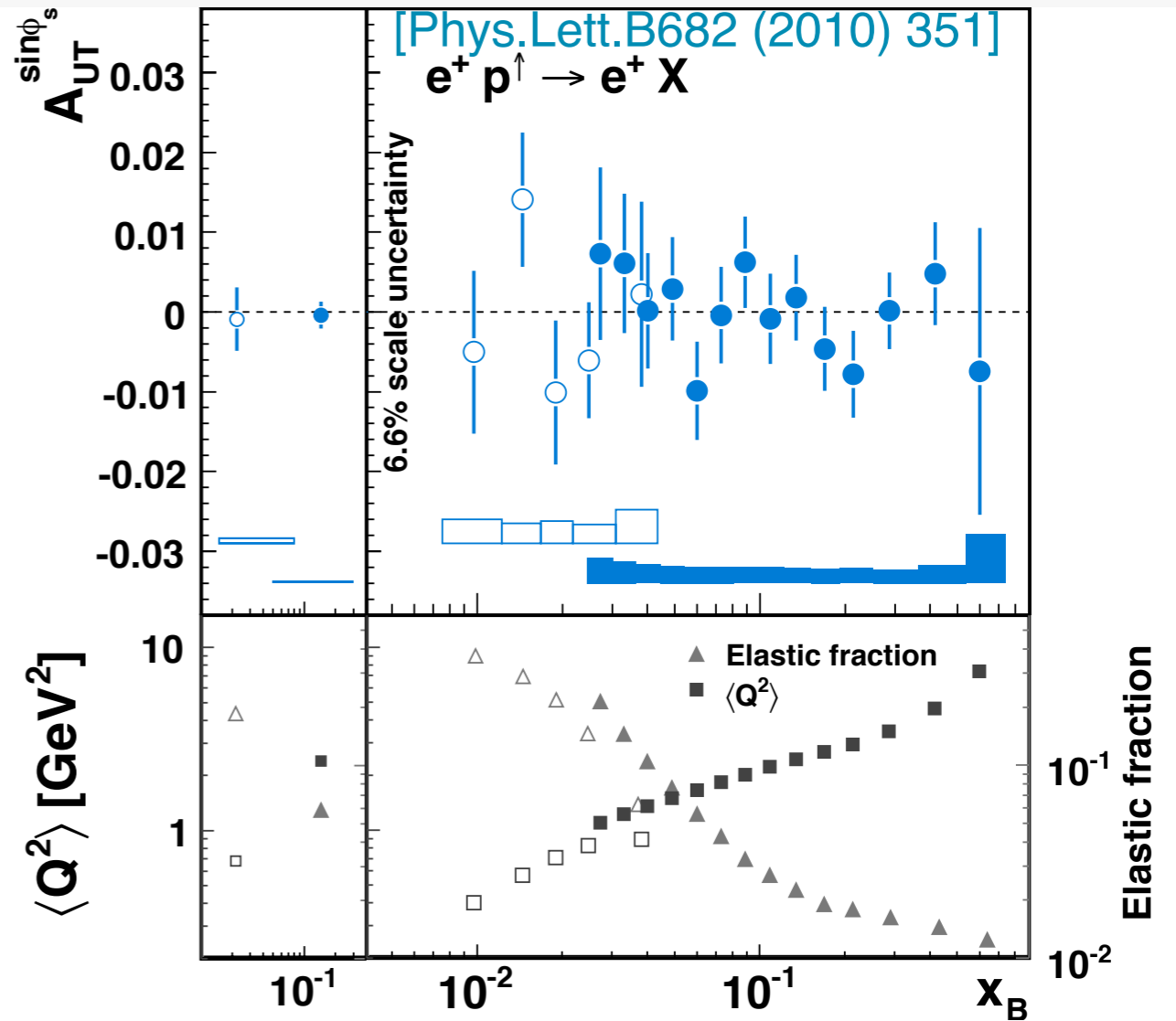
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- let's prepare for
  - precision measurements at ongoing and future facilities
  - fundamental QCD tests in Drell-Yan experiments

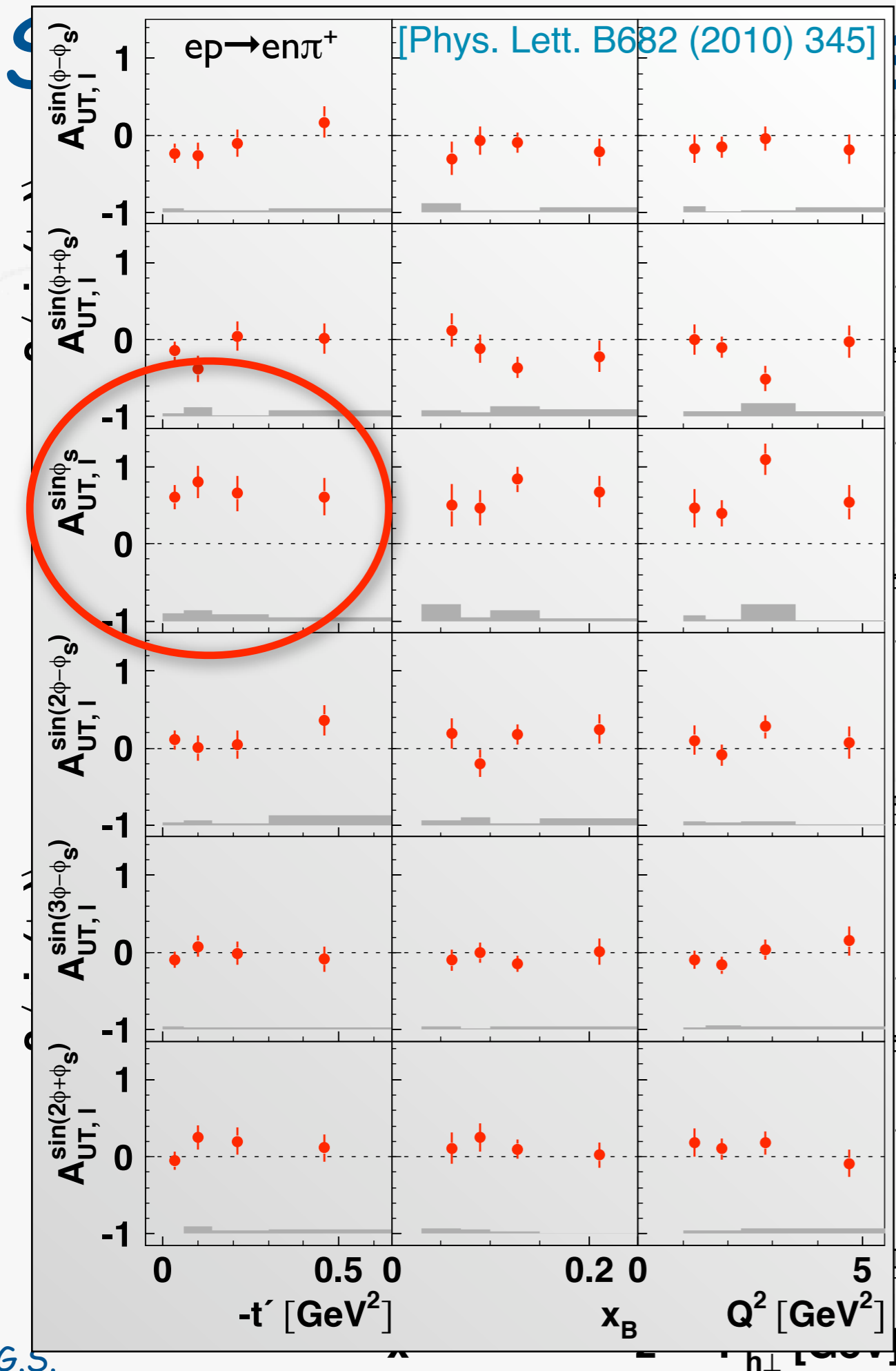
some backup slides

# Subleading twist - $\sin(\phi_s)$



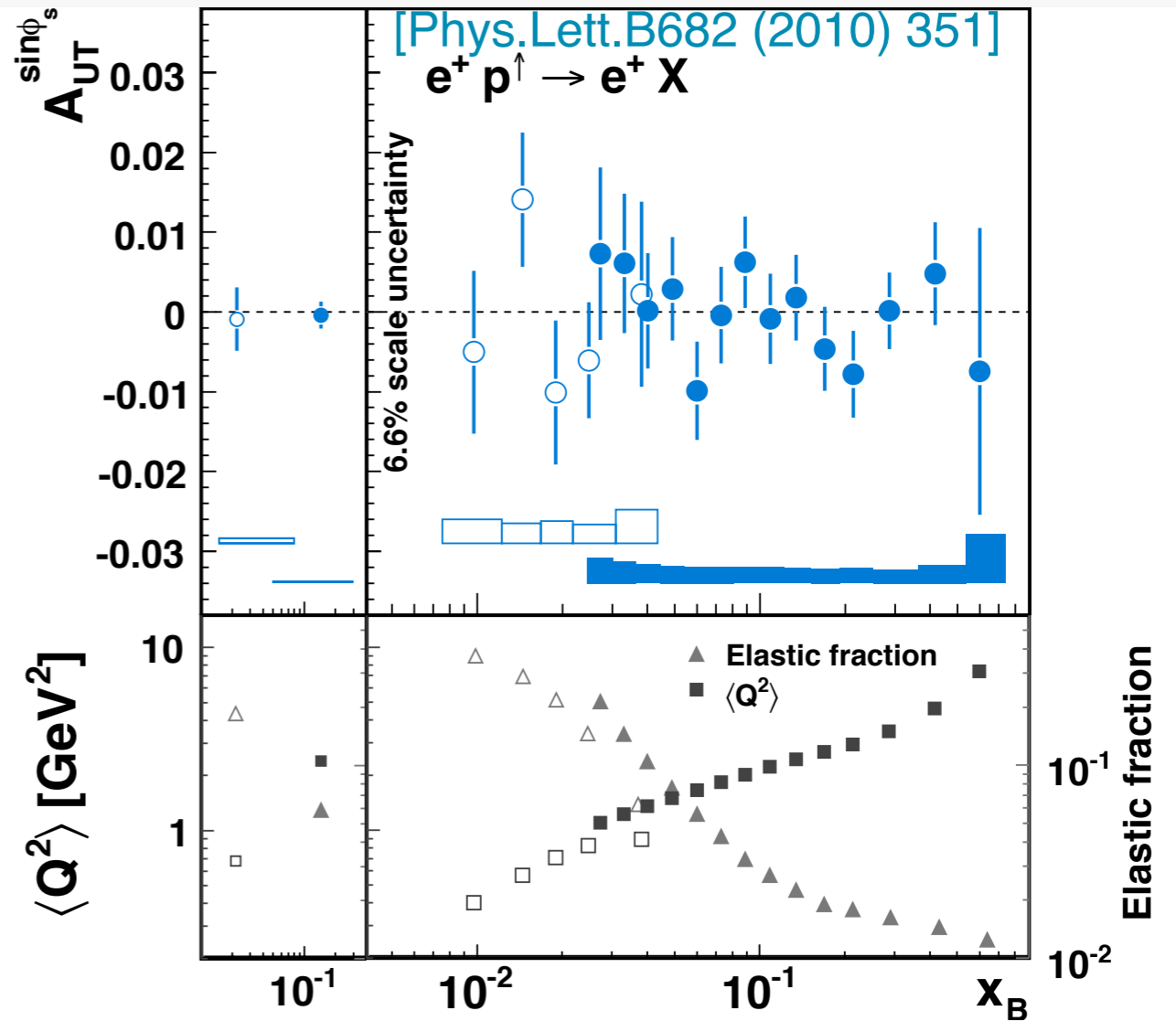
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- must vanish after integration over  $P_{h\perp}$  and  $z$ , and summation over all hadrons



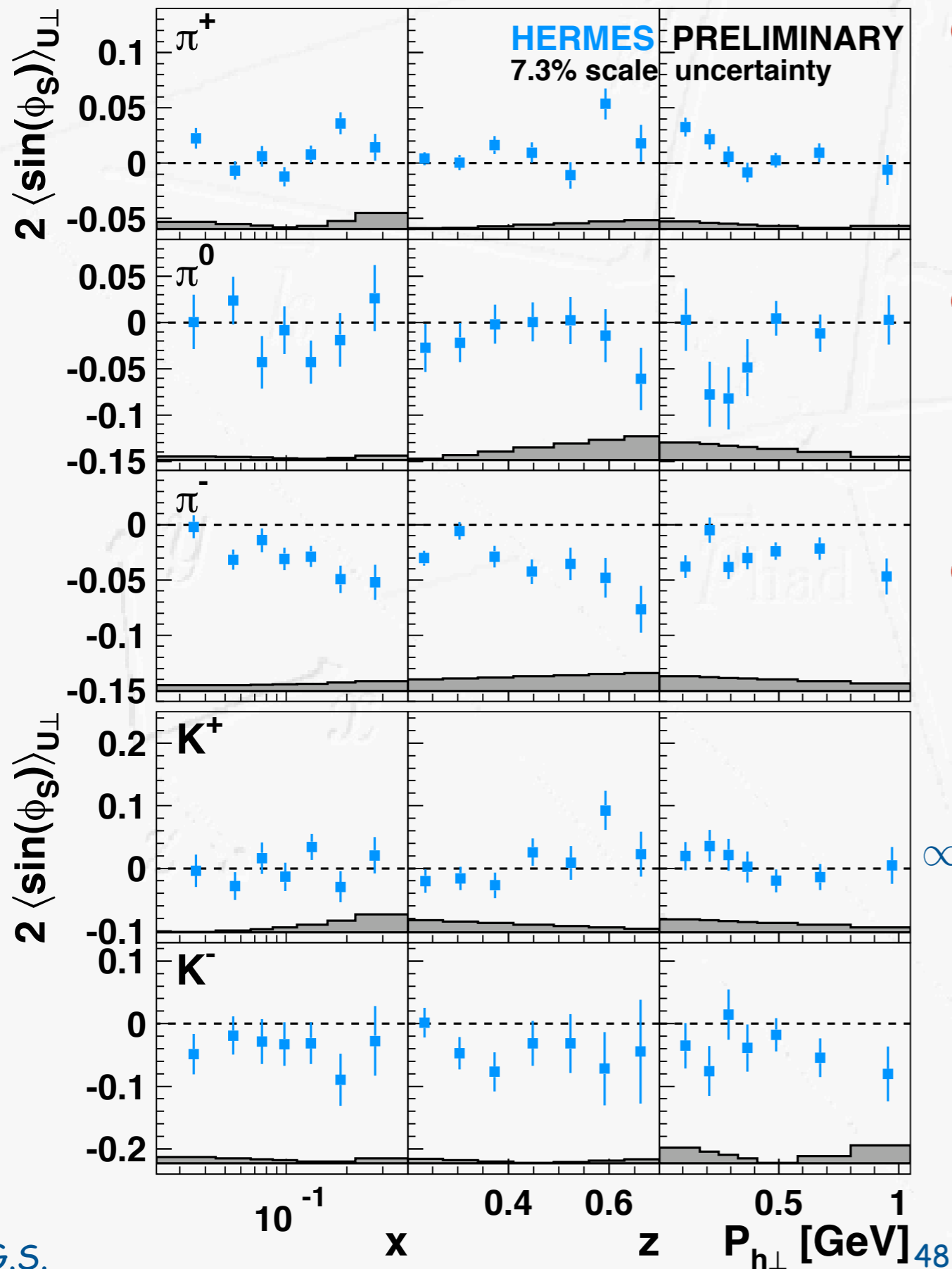


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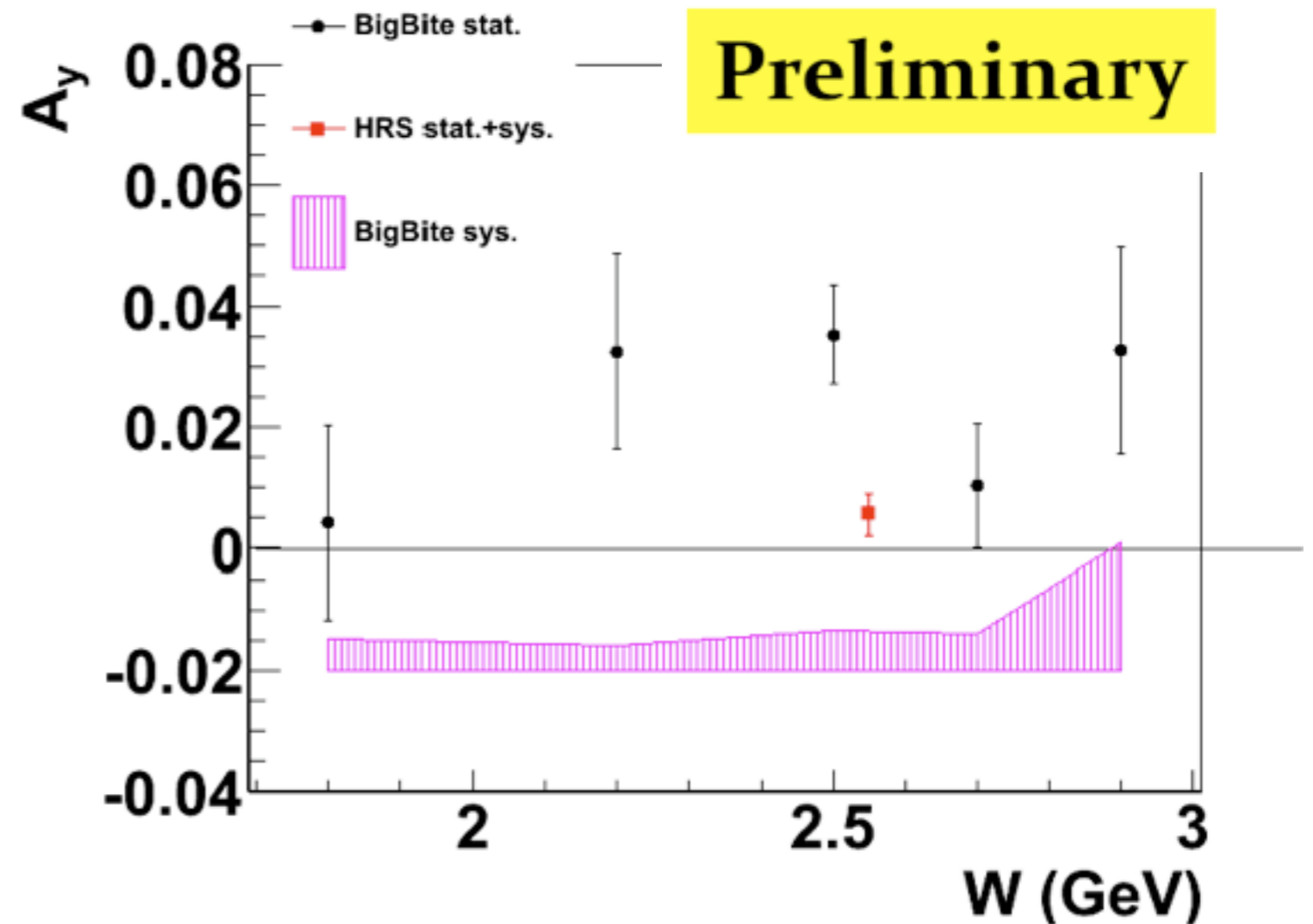


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- must vanish after integration over  $P_{h\perp}$  and  $z$ , and summation over all hadrons
- various terms related to transversity, worm-gear, Sivers etc.:

$$\propto \left( x f_{\text{T}}^{\perp} D_1 - \frac{M_h}{M} h_1 \frac{\tilde{H}}{z} \right) - \mathcal{W}(p_{\text{T}}, k_{\text{T}}, P_{h\perp}) \left[ \left( x h_{\text{T}} H_1^{\perp} + \frac{M_h}{M} g_{1\text{T}} \frac{\tilde{G}^{\perp}}{z} \right) - \left( x h_{\text{T}}^{\perp} H_1^{\perp} - \frac{M_h}{M} f_{1\text{T}}^{\perp} \frac{\tilde{D}^{\perp}}{z} \right) \right]$$

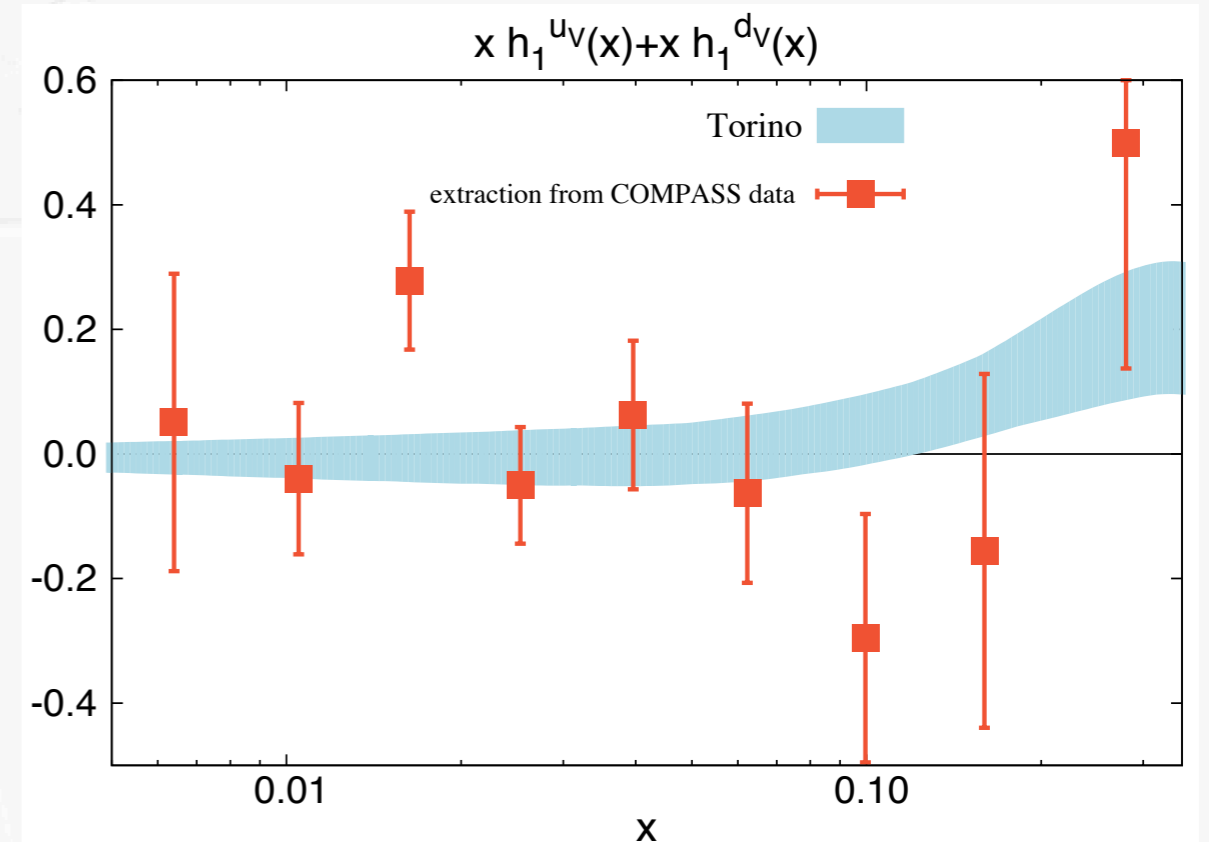
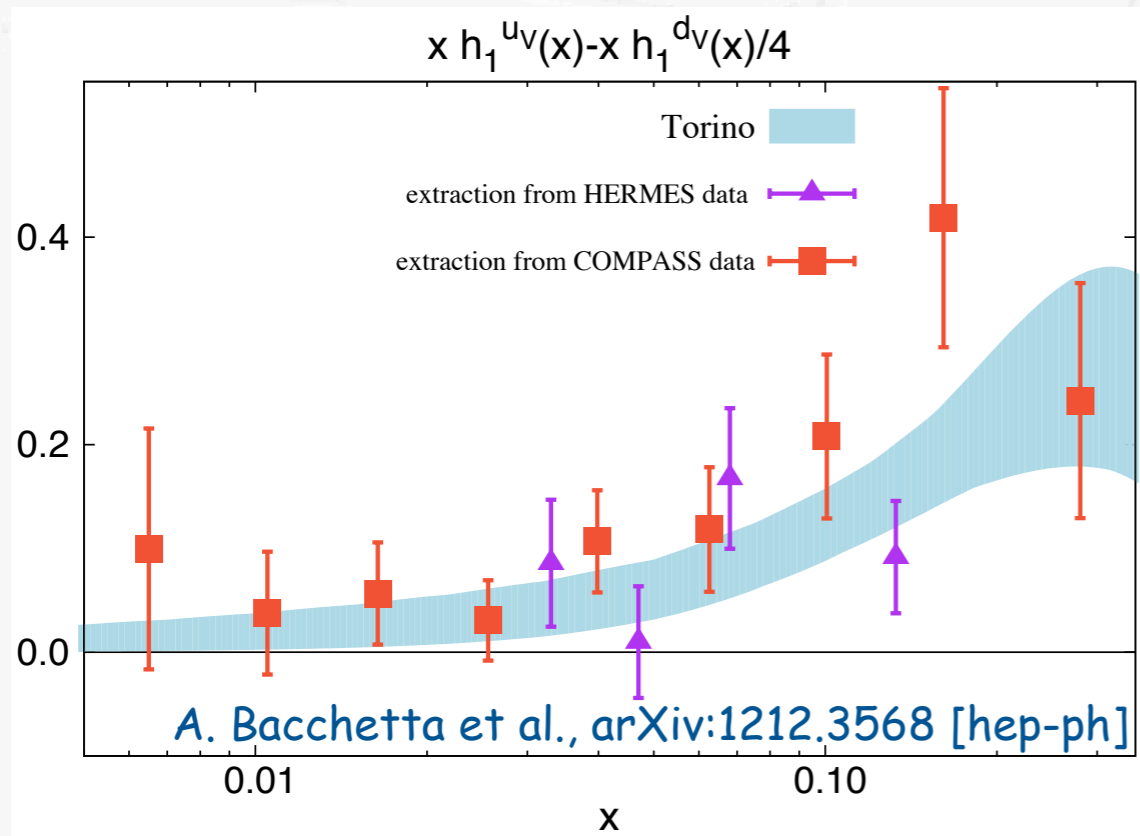
# 2-photon exchange signal from JLab

- non-zero inclusive LR asymmetry on neutron
- goes beyond single-photon exchange interpretation



# transversity extraction

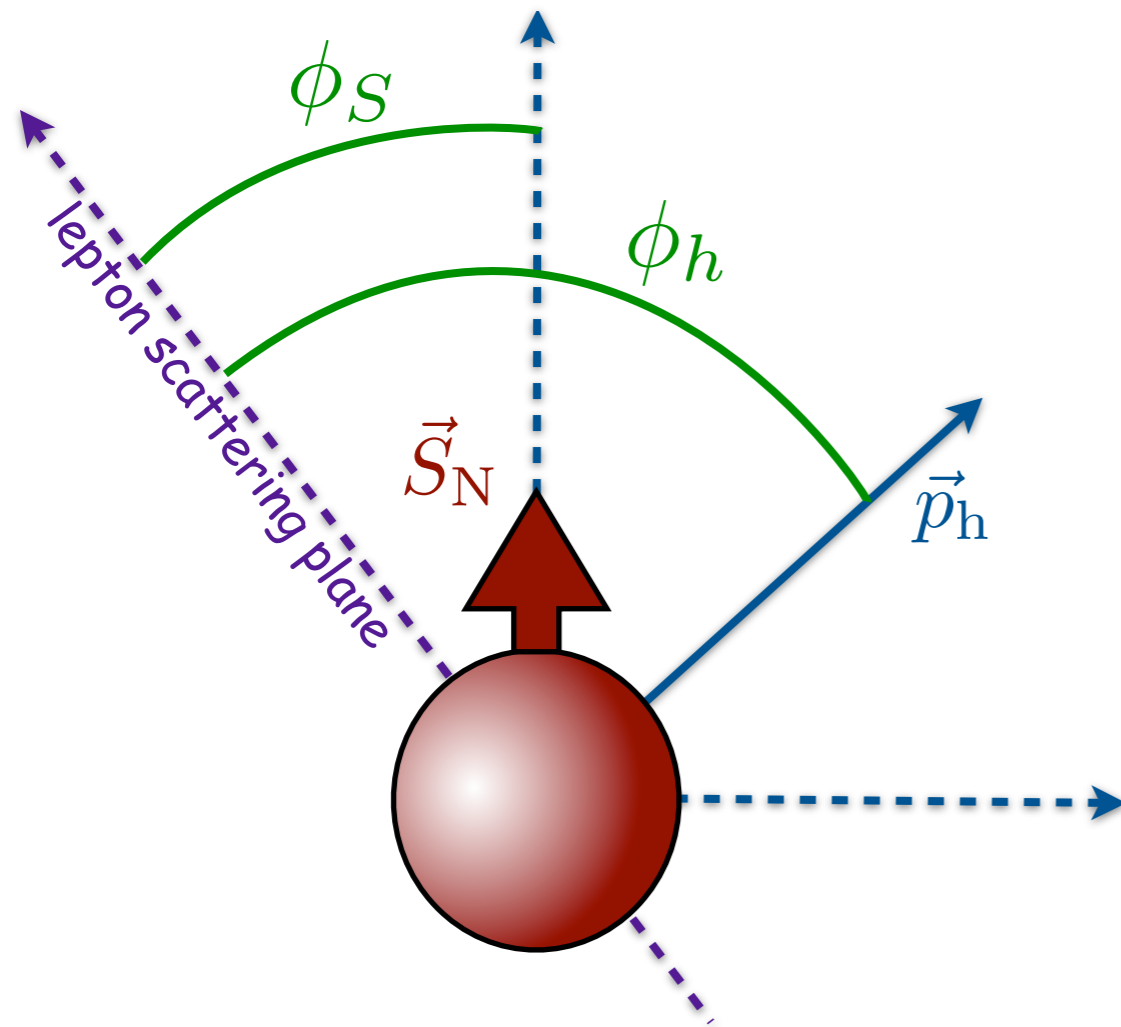
- combining SIDIS (COMPASS & HERMES) and  $e^+e^-$  data (BELLE):



- promising agreement between collinear and TMD extraction of transversity
- no obvious sign of difference in TMD (Collins) from collinear (dihadron)

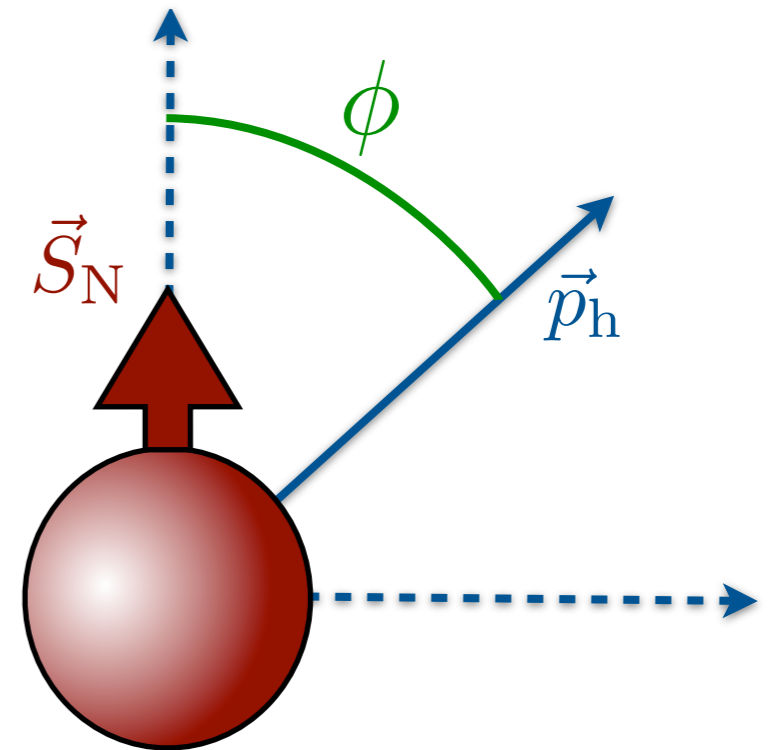
# Inclusive hadron electro-production

$$ep^{\uparrow} \rightarrow ehX$$



virtual photon going  
into the page

$$ep^{\uparrow} \rightarrow hX$$



lepton beam going  
into the page

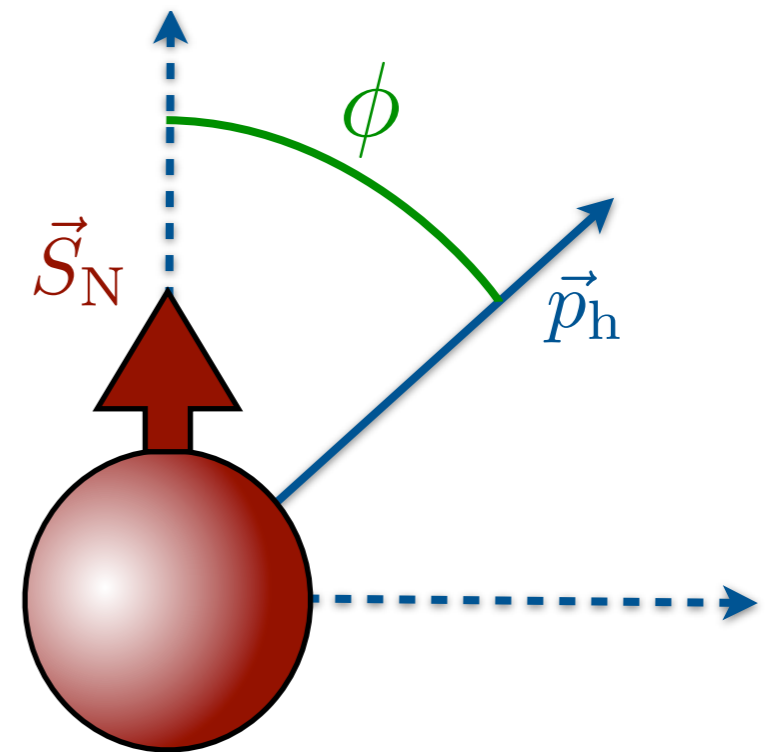
$$\phi \simeq \phi_h - \phi_S$$

→ "Sivers angle"



# Inclusive hadron electro-production

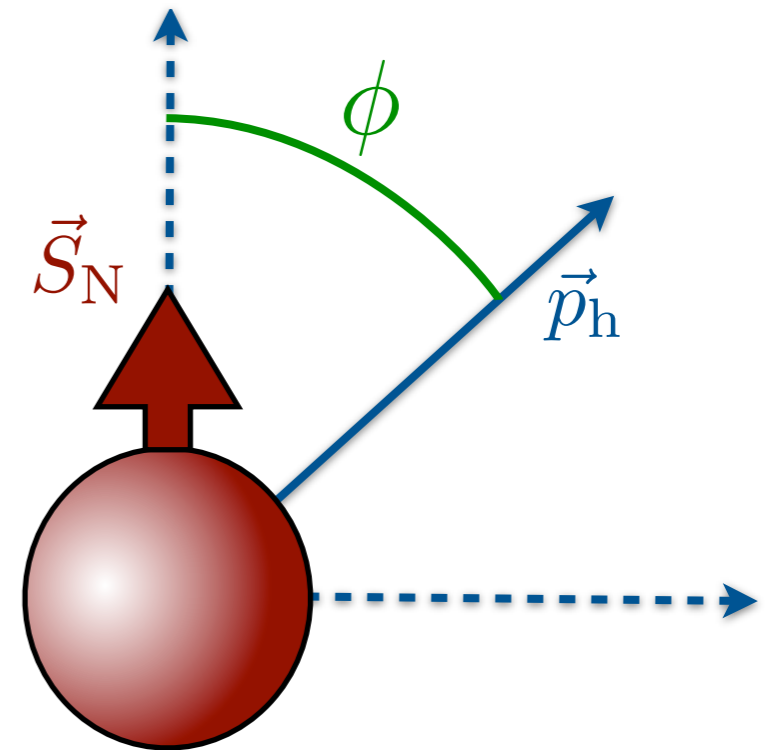
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# Inclusive hadron electro-production

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↳ lepton kinematics unknown

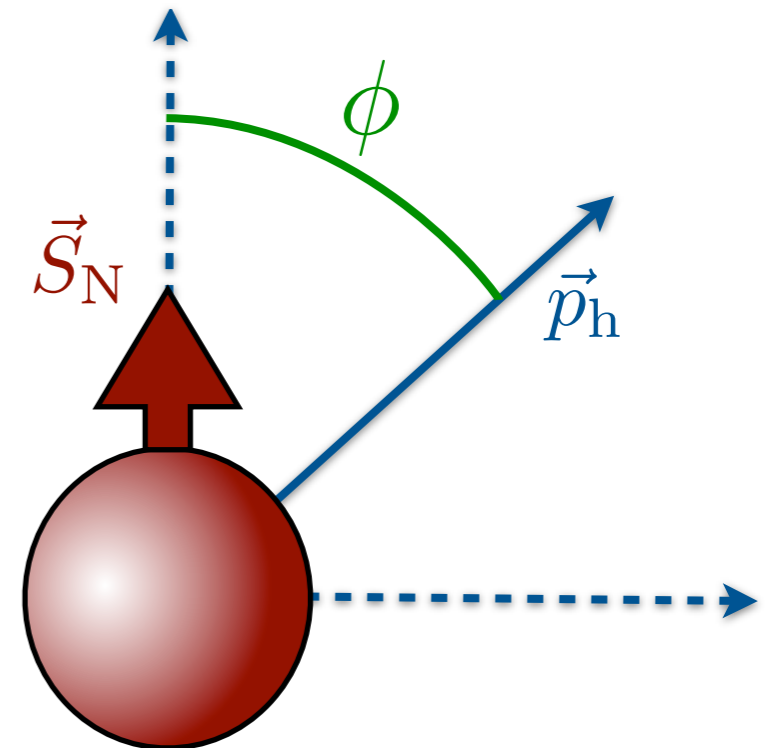
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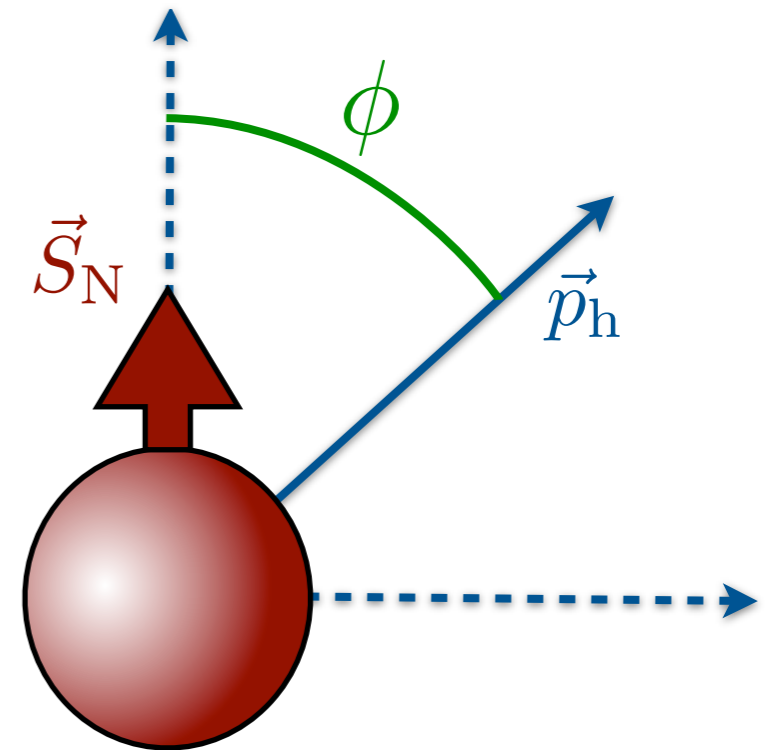
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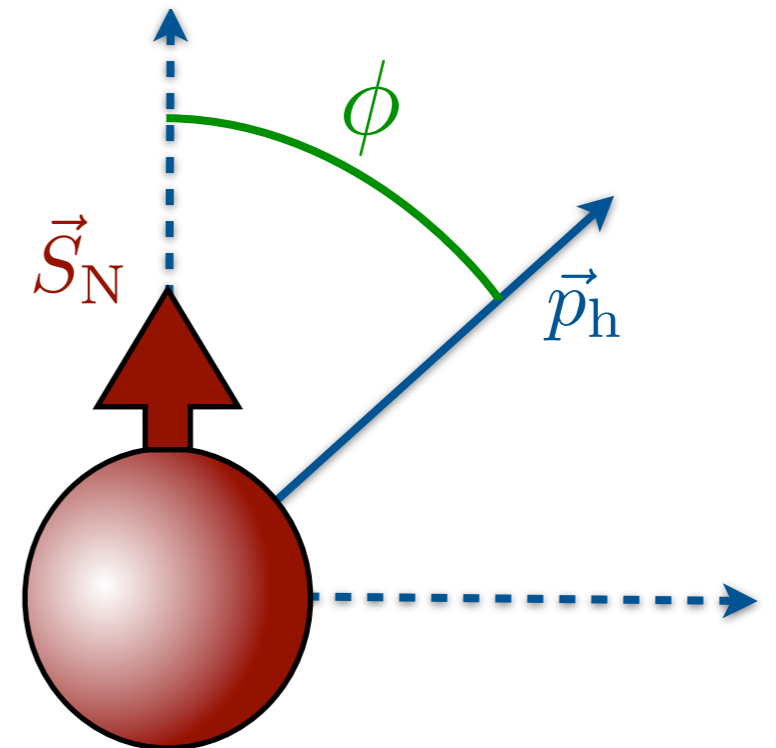
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$$A_{UT}(p_T, x_F, \phi) =$$

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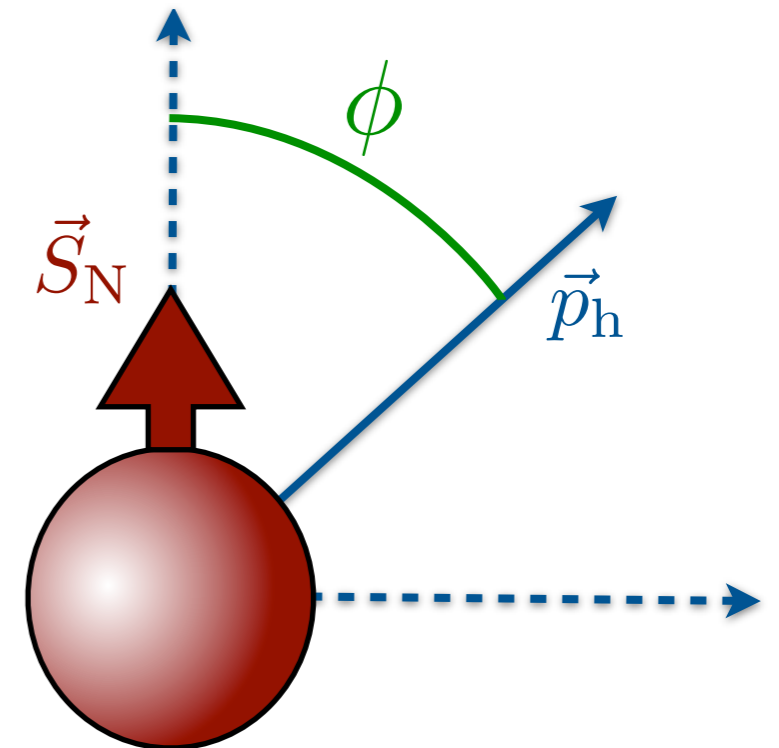
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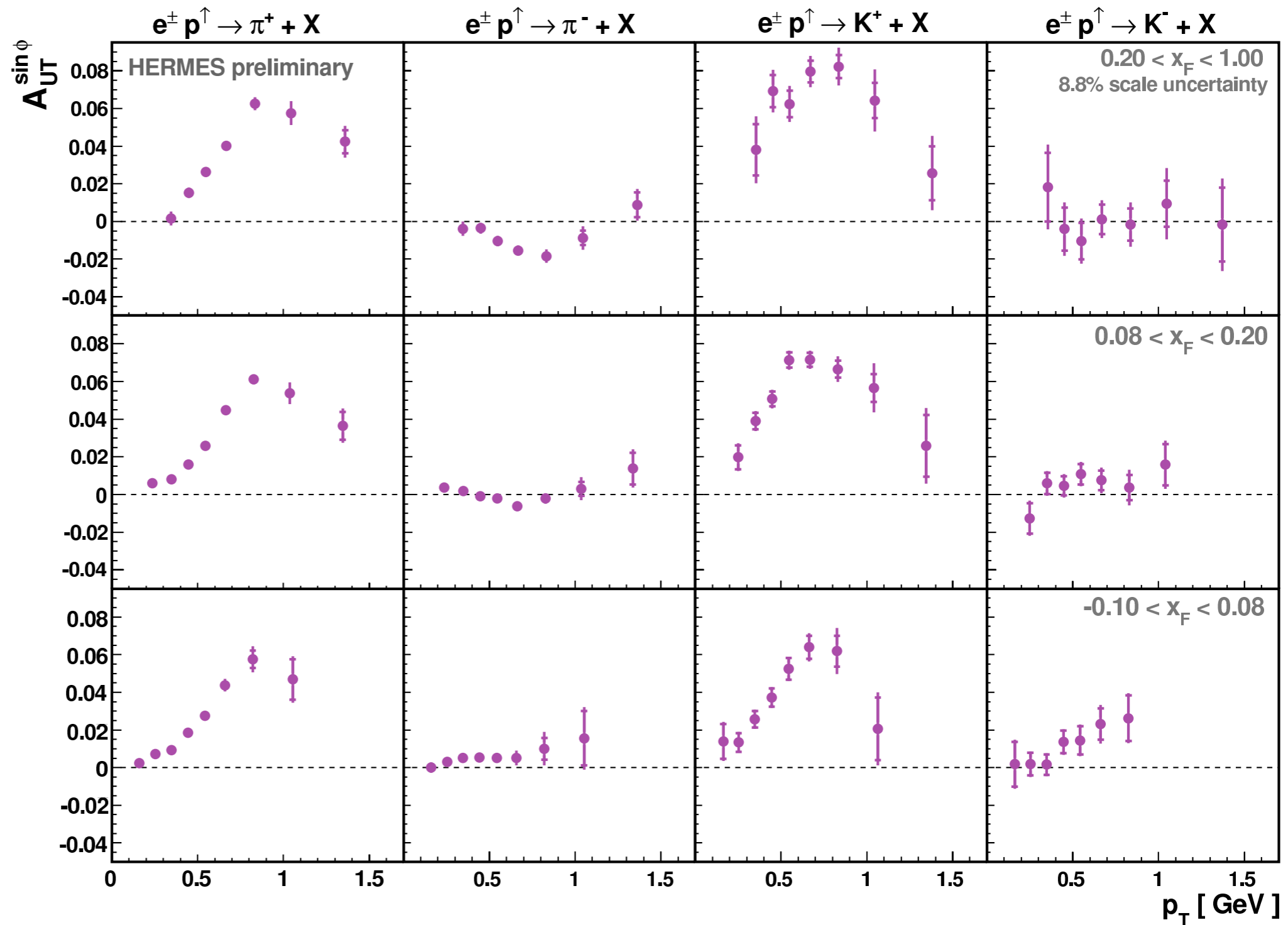
$$\frac{\int_{\pi}^{2\pi} d\phi \sigma_{UT} \sin \phi - \int_0^{\pi} d\phi \sigma_{UT} \sin \phi}{\int_0^{2\pi} d\phi \sigma_{UU}}$$

$$= -\frac{2}{\pi} A_{UT}^{\sin \phi}$$

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$



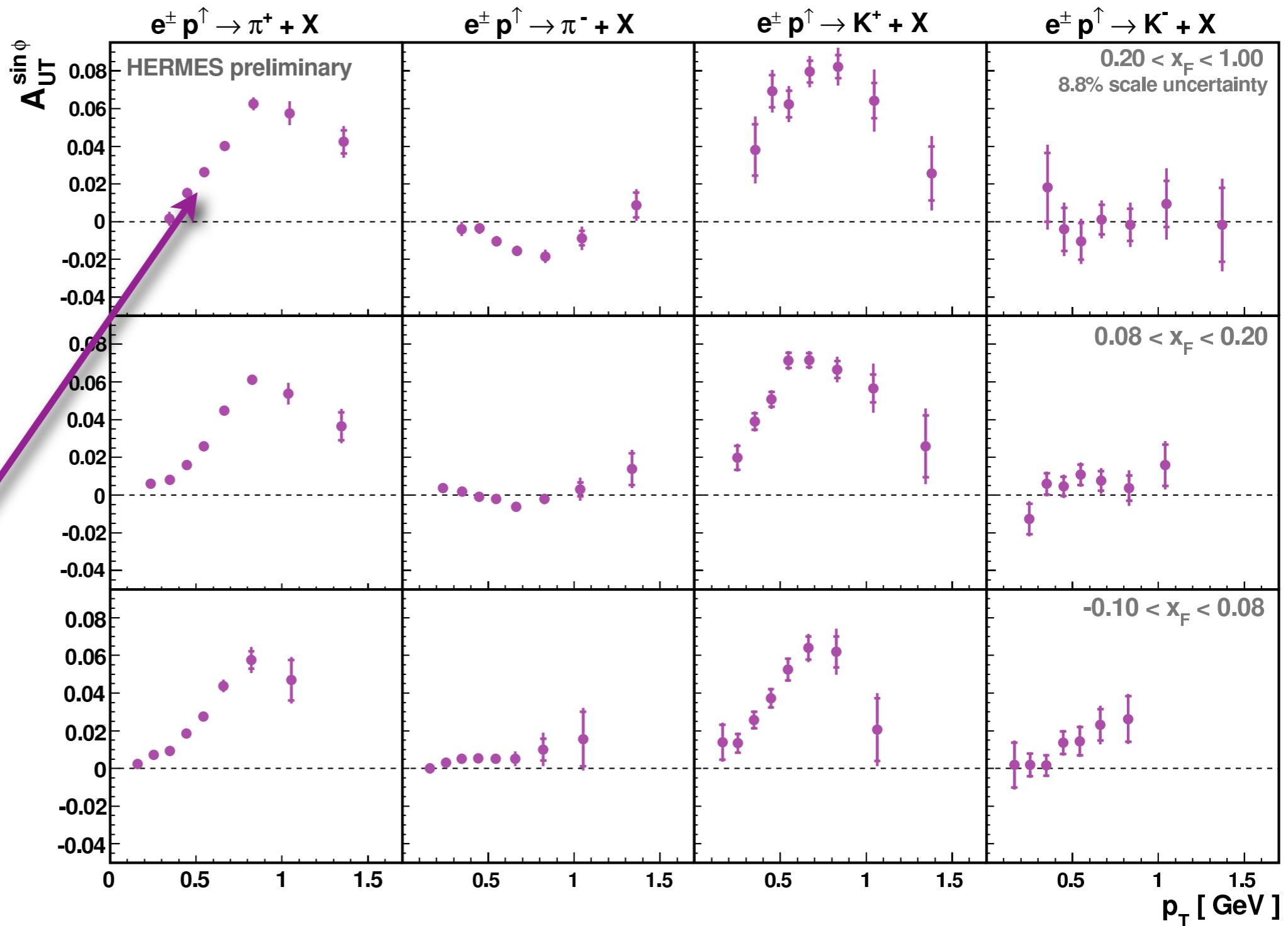
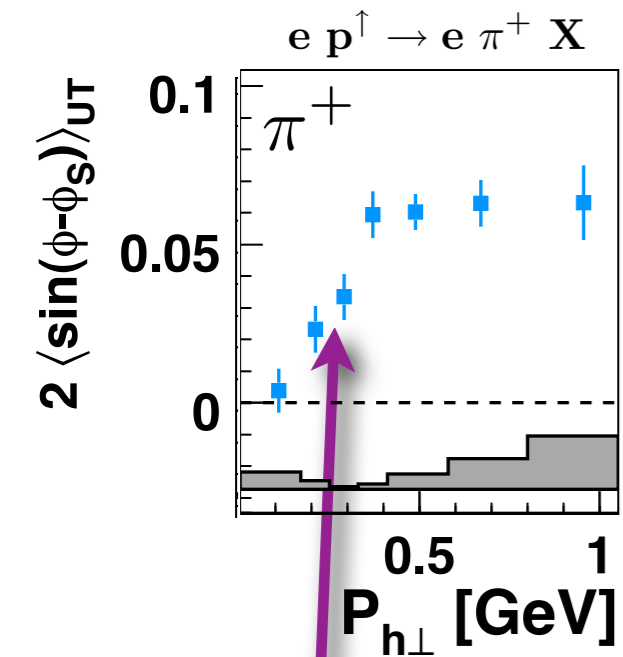
# Inclusive hadrons in ep





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	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$



behavior and size similar to SIDIS Sivers