Fingerprinting dark energy: distinctive marks of viscosity

Elisabetta Majerotto



Work done in collaboration with *Domenico Sapone* accepted by PRD [arXiv:1203.2157]

"What is ν ?" workshop at GGI Florence, 15th of June 2012

"What is v?" workshop at GGI





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- 2 cosmological perturbations
- analytical solutions
 - observable effects?

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motivation

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- analytical solutions
- observable effects?

5 conclusions

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The accelerated expansion of the Universe is yet shrouded in mystery: what is its cause?

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In any (4D projection of) modified gravity model

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hence I can write it as an effective fluid with

$$G_{\mu\nu} = -8\pi G \left(T_{\mu\nu} + \frac{Y_{\mu\nu}}{8\pi G} \right)$$

viscous dark energy

Effective fluid description: all parameters are seen as effective functions describing an *effective dark energy fluid*.

Standard parameters describing dark energy:

- equation of state $w = p/\rho$. $w_{\Lambda} = -1$, $w_{\phi} = \frac{\dot{\phi}^2/2 V(\phi)}{\dot{\phi}^2/2 + V(\phi)}$
- speed of sound c_s^2 : $\delta p = c_s^2 \delta \rho + \frac{3aH(c_s^2 c_a^2)}{k^2} \rho V$. $c_{s,\Lambda}^2$ not defined (no perturbations), $c_{s,\phi}^2 = 1$

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We add one **extra parameter: the viscosity of the fluid** c_v^2 w. Hu, Astrophys. J. 506 (1998) 485-494. As an effective parameter, may describe more exotic models: extra dimensions, non minimally coupled scalar fields, modified 4D gravity...

Equation for the anisotropy σ :

$$\sigma' + \frac{3}{a}\sigma = \frac{8}{3}\frac{c_v^2}{(1+w)^2}\frac{V}{a^2H}$$

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- motivation: recovers the free streaming equations of motion for radiation (neutrinos + photons) up to the quadrupole
- for classic scalar fields $c_{v,\phi}^2 = 0$

first order perturbation equations for dark energy

 $\text{CMB} \rightarrow \text{homogeneous}$ and isotropic Universe at large scales.

At z = 1090, during radiation domination, the inhomogeneities are as small as 10^{-5} . Later, when matter becomes dominant, they grow: $\delta_m \gtrsim 1$.

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$$\begin{split} \delta' &= -\frac{V}{Ha^2} \left[1 + \frac{9a^2H^2\left(c_s^2 - w\right)}{k^2} \right] - \frac{3}{a} \left(c_s^2 - w\right) \delta + 3\left(1 + w\right) \phi' \\ V' &= -(1 - 3c_s^2) \frac{V}{a} + \frac{k^2 c_s^2 \delta}{a^2 H} + \frac{(1 + w)k^2}{a^2 H} \left[\psi - \sigma\right] \\ \sigma' &= -\frac{3}{a} \sigma + \frac{8}{3} \frac{c_v^2}{(1 + w)^2} \frac{V}{a^2 H} \end{split}$$

+ Einstein equations. perturbed metric: $ds^2 = a^2 \left[-(1+2\psi)d\tau^2 + (1-2\phi)dx_i dx^i \right]$

Past work was mainly numerical:

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- Forecasts on how well future CMB experiments will constrain an early, cold and stressed dark energy. E. Calabrese, R. de Putter, D. Huterer, E. V. Linder and A. Melchiorri, Phys. Rev. D 83 (2011) 023011 [arXiv:1010.5612
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- use them to understand general behaviours of viscous dark energy fluid
- and to predict observable effects: matter power spectrum, growth of matter perturbations, ISW (integrated Sachs-Wolfe) effect.

$$\begin{split} \delta &=& \frac{3(1+w)^2}{3c_s^2(1+w)+8\left(c_s^2-w\right)c_v^2}\frac{\phi_0}{k^2} \\ V &=& -3aH\left(c_s^2-w\right)\delta \\ \sigma &=& -\frac{8c_v^2\left(c_s^2-w\right)}{3c_s^2(1+w)+8(c_s^2-w)c_v^2}\frac{\phi_0}{k^2} \end{split}$$

Remind that

$$aH = H_0 \sqrt{\Omega_m} a^{-1/2}$$

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numerical solution computed with CAMB for a model with $c_v^2 = 10^{-4}$, $c_s^2 = 0$ and w = -0.8 for the mode $k = 200H_0$ approximated solution for $c_v^2 = 0$ approximated solution for $c_v^2 \neq 0$ *a* at which the mode enters the causal horizon

radiation omitted for visualisation purposes

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$$\begin{aligned} kc_v^2 \sim aH \\ \sigma' &= -\frac{3}{a}\sigma + \frac{8}{3}\frac{c_v^2}{(1+w)^2}\frac{V}{a^2H} \end{aligned}$$



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a at which the mode enters the *anisotropic horizon:*

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- once matter perturbations enter the anisotropic horizon, the solution tends to the unclustered dark energy solution.
- very small effect

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Growth function: $G(a) \equiv \frac{\delta_m(a)}{\delta_m(a_0)}$ can be written as $G(a) = \exp\left\{\int_{a_0}^a \frac{\Omega_m(a')^{\gamma}}{a'} da'\right\}$

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$$\begin{aligned} Q-1 &\equiv \frac{\delta\rho}{\delta\rho_m} = \frac{1-\Omega_{m_0}}{\Omega_{m_0}} (1+w) \frac{a^{-3w}}{1-3w + \frac{2k^2a}{3H_0^2\Omega_{m_0}}} c_{\text{eff}}^2 \\ \eta &\equiv \frac{\psi}{\phi} - 1 = -\frac{9}{2} H_0^2 (1-\Omega_{m_0}) (1+w) \frac{a^{-1-3w}}{k^2 Q} \left(1 - \frac{c_s^2}{c_{\text{eff}}^2}\right) \end{aligned}$$

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Express γ as a function of Q and η E.V. Linder and R.N. Cahn, Astropart. Phys. 28, 481 (2007)

$$\gamma = \frac{3(1 - w - A(Q, \eta))}{5 - 6w} \qquad A(Q, \eta) = \frac{(1 + \eta)Q - 1}{1 - \Omega_m(a)}$$

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- in some modified gravity model, e.g. DGP, $\gamma > \gamma_{LCDM}$
- in our model it can happen that $\gamma > \gamma_{LCDM}$, but even if we assume the viscosity term to be $c_v^2 = 1$ then $A(Q, \eta) \simeq -1.5 \times 10^{-5}$ for scales $k \simeq 200H_0$

observable effects: ISW

$$\zeta = \frac{\Delta T\left(\hat{n}\right)}{T_0} = \int \left(\frac{\partial\phi}{\partial\tau} + \frac{\partial\psi}{\partial\tau}\right) d\tau = \int_0^{\chi_H} d\chi W_{\zeta}\left(\chi\right) \Delta_{m,0}\left(k\right)$$
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 $C_{\ell} \equiv C_{\zeta\zeta} =$ ISW-auto correlation spectrum



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- work in progress: compute forecasts on how well it will be possible to measure c_s², c_v² from the Euclid galaxy survey.

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