



When Astrophysics starts to constrain the Supersymmetric parameter space:

what is left for the neutralino?

Trying to close the neutralino window with all available tools...

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Scanning over the SUSY parameter space

Why considering SUSY DM?

large framework; conclusions valid for other 'SM'-like model
Useful for SUSY searches (complement LHC) but also for
DM in general

Which SUSY Model?

pMSSM (17/19 parameters), NMSSM (11 parameters),...

Which constraints?

Particle physics (SUSY dependent but used for the scan) →
Relic density (only upper bound)
DM direct detection and indirect detection
(they are applied after the scans)

Which mass range/which candidate?

neutralinos as light as a few GeV and as heavy as a few TeV

| constraint | value/range | tolerance | applied |
|---------------------------------------|-------------------------------|---|---------------|
| S_{masses} | | none | both |
| $\Omega_{WMAP} h^2$ | 0.01131 - 0.1131 | 0.0034 | both |
| $(g-2)_\mu$ | $25.5 \cdot 10^{-10}$ | stat: $6.3 \cdot 10^{-10}$ sys: $4.9 \cdot 10^{-10}$ | both |
| $\Delta\rho$ | ≤ 0.002 | 0.0001 | MSSM |
| $b \rightarrow s\gamma$ | $3.52 \cdot 10^{-4}$ [38, 39] | th: $0.24 \cdot 10^{-4}$ exp: $0.23 \cdot 10^{-4}$ | both |
| $B_s \rightarrow \mu^+\mu^-$ | $\leq 4.7 \cdot 10^{-8}$ | $4.7 \cdot 10^{-10}$ | both |
| $R(B \rightarrow \tau\nu)$ | 1.28 [38] | 0.38 | both |
| m_H | ≥ 114.4 | 1% | MSSM |
| $Z \rightarrow \chi_1\chi_1$ | ≤ 1.7 MeV | 0.3 MeV none | MSSM NMSSM |
| $e^+e^- \rightarrow \chi_1\chi_{2,3}$ | ≤ 0.1 pb [40] | 0.001 pb none | MSSM NMSSM |
| ΔM_s | $117.0 \cdot 10^{-13}$ GeV | th: $21.1 \cdot 10^{-13}$ GeV exp: $0.8 \cdot 10^{-13}$ GeV | NMSSM |
| ΔM_d | $3.337 \cdot 10^{-13}$ GeV | th: $1.251 \cdot 10^{-13}$ GeV exp: $0.033 \cdot 10^{-13}$ GeV | NMSSM |

Scans are done with Particle Physics constraints
Only one 'astro/cosmo': **the relic density but we only care about the upper bound.**

Principle of the scans

MCMC (i.e. based on Likelihood)

Start at a given point of the parameter space;
Jumps to other point if they provide better likelihood [or random]
used micrOMEGAs, SoftSUSY, Higgsbounds

Constraints set as

neutralino must be the LSP

Parameters must be in agreement with Particle Physics measurements/limits

The rest is prediction ...

Likelihoods

We use a Gaussian distribution for all observables with a preferred value $\mu \pm \sigma$,

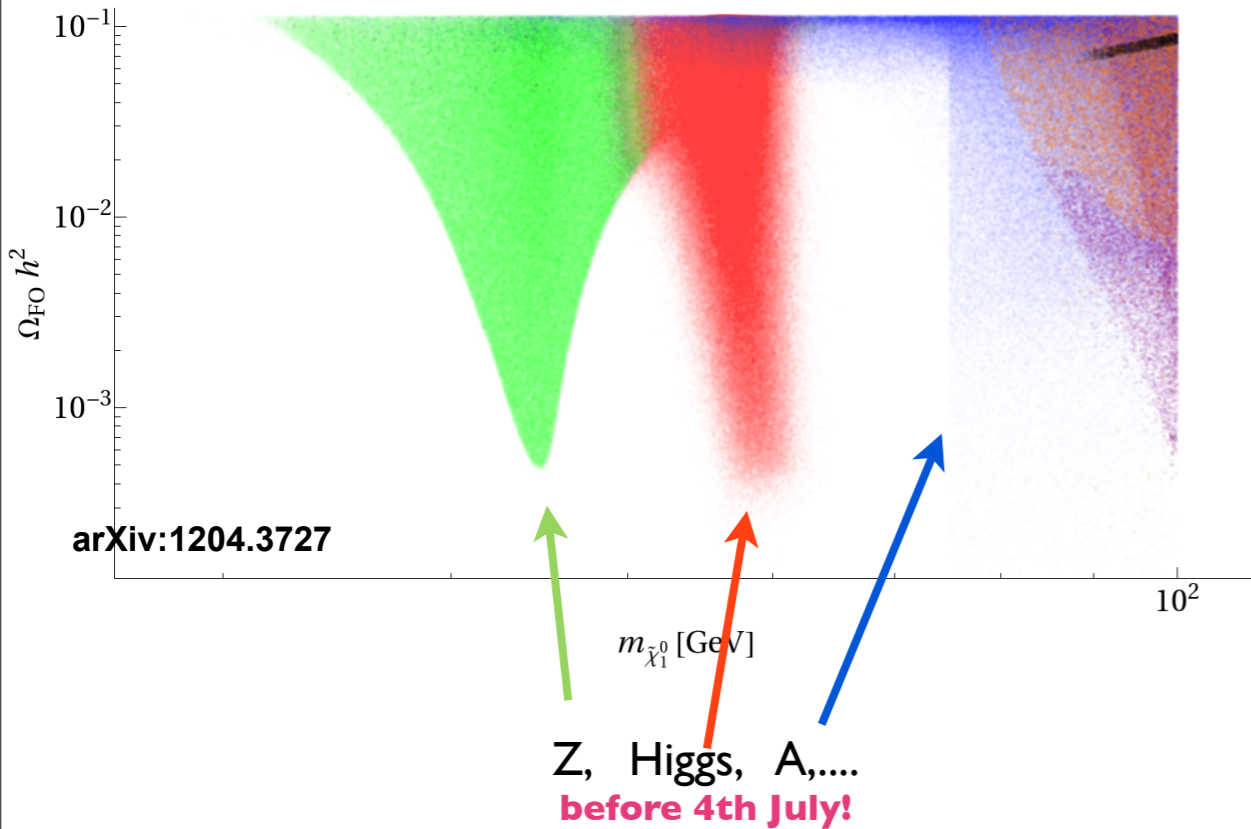
$$F_2(x, \mu, \sigma) = e^{-\frac{(x-\mu)^2}{2\sigma^2}} \quad (1)$$

$$F_3(x, \mu, \sigma) = \frac{1}{1 + e^{-\frac{x-\mu}{\sigma}}} \quad (2)$$

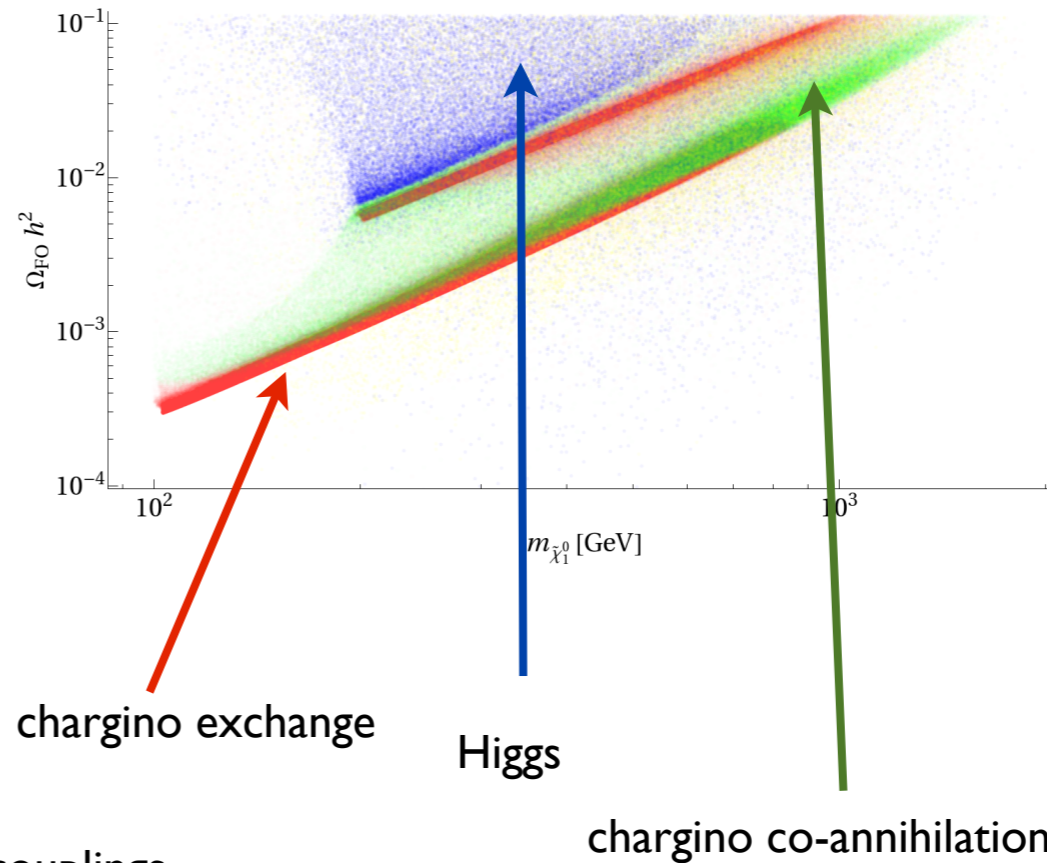
for observables which only have lower or upper bounds. The tolerance, σ , is negative (positive) when one deals with an upper (lower) bound.

**Relic density can still be a guide to scan the parameter space though:
Typical ‘annihilation’ channels to be expected:**

Low mass neutralino



High mass neutralino



To compensate resonance effects, one can decrease the couplings.

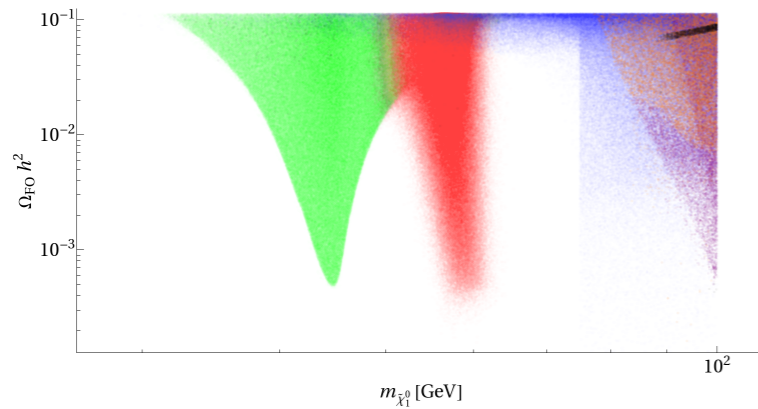
In the ‘SUSY’ language this translates into Bino/Wino/Higgsino fraction.
In a generic framework, this is related to the strength of the coupling...

Relic density can be extremely small if the DM mass corresponds to a value right on a Higgs or Z resonance

This is not necessarily a problem: neutralino could be a sub-dominant DM species or one could invoke regeneration mechanisms such as Freeze-In, ...

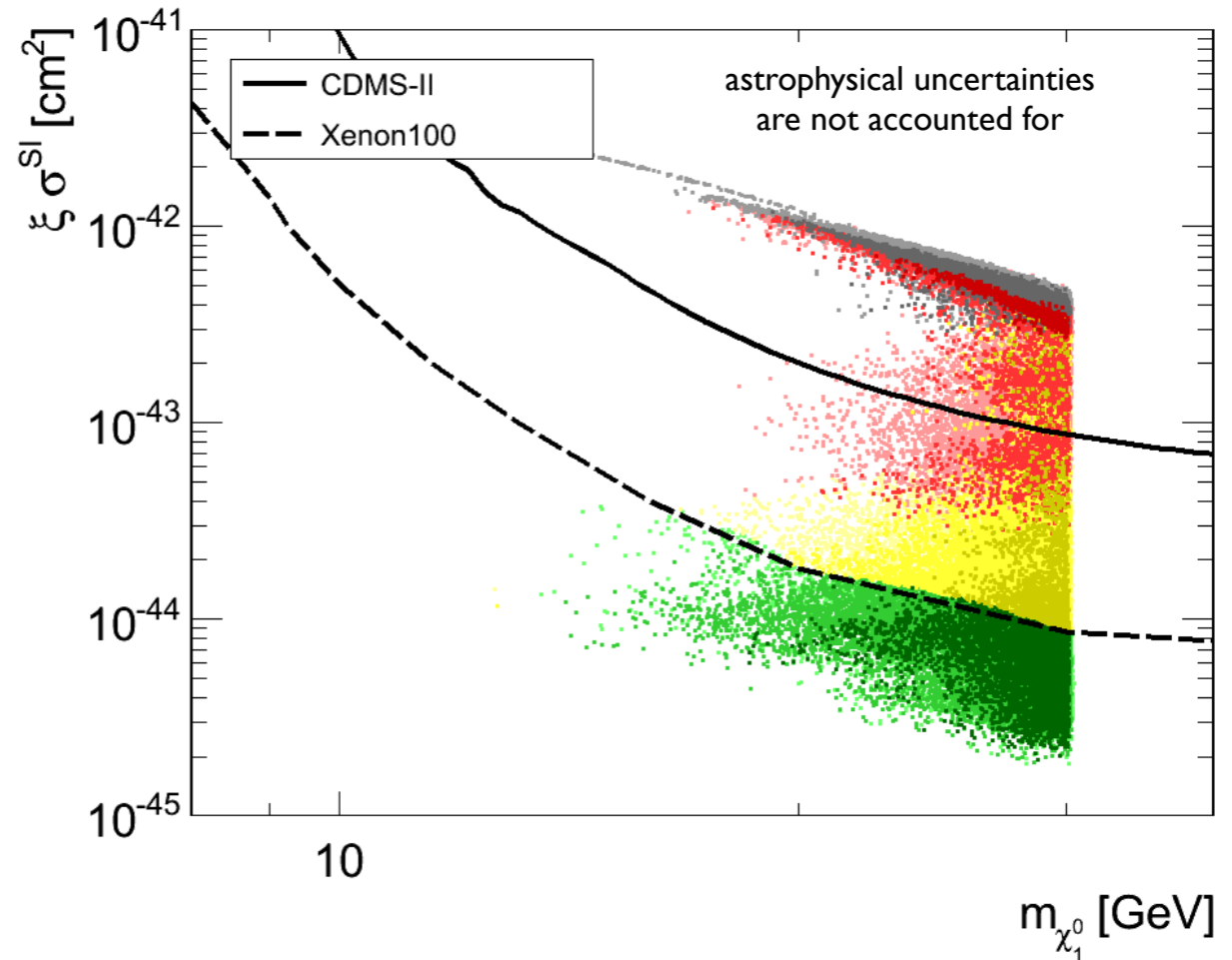
Small masses

Zoom in the small mass region (pMSSM)



| Parameter | Minimum | Maximum | Tolerance |
|-----------------------|---------|---------|-----------|
| M_1 | 1 | 1000 | 3 |
| M_2 | 100 | 2000 | 30 |
| M_3 | 500 | 6500 | 10 |
| μ | 0.5 | 1000 | 0.1 |
| $\tan\beta$ | 1 | 75 | 0.01 |
| M_A | 1 | 2000 | 4 |
| A_t | -3000 | 3000 | 100 |
| $M_{\tilde{t}_R}$ | 70 | 2000 | 15 |
| $M_{\tilde{t}_L}$ | 70 | 2000 | 15 |
| $M_{\tilde{q}_{1,2}}$ | 300 | 2000 | 14 |
| $M_{\tilde{q}_3}$ | 300 | 2000 | 14 |

TABLE I: Intervals for MSSM free parameters (GeV units).



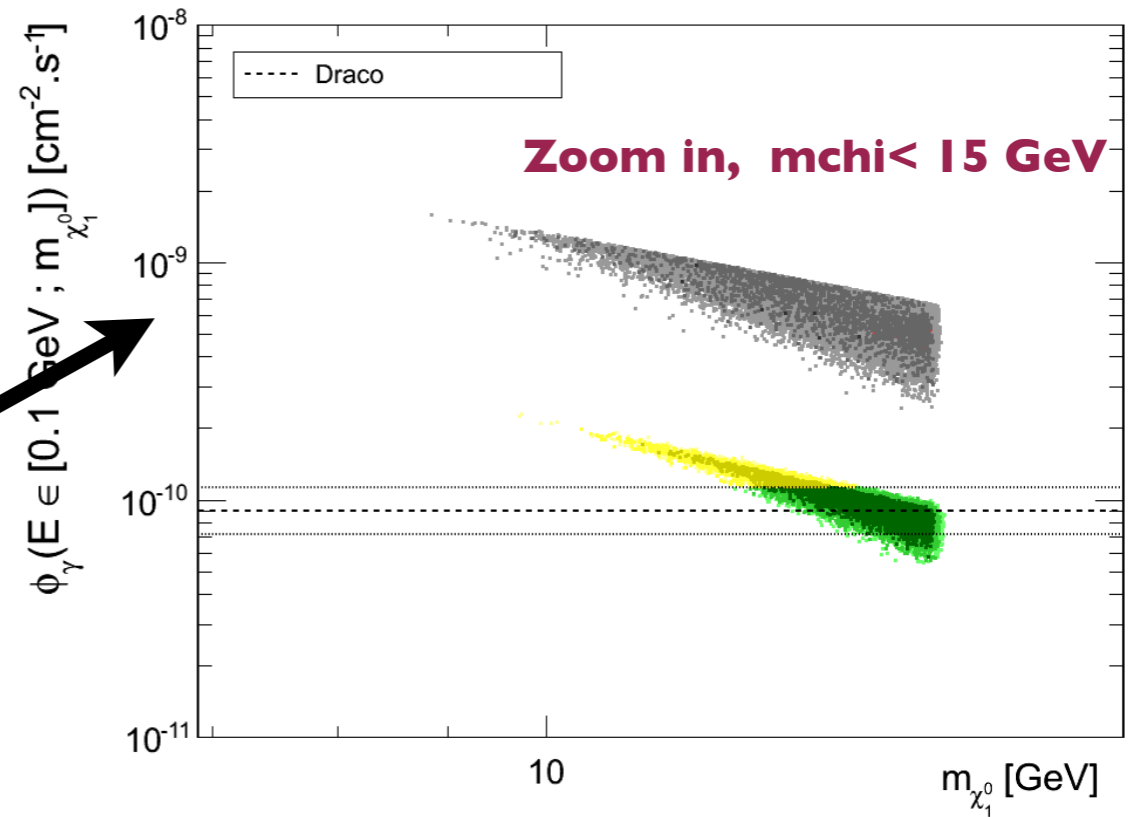
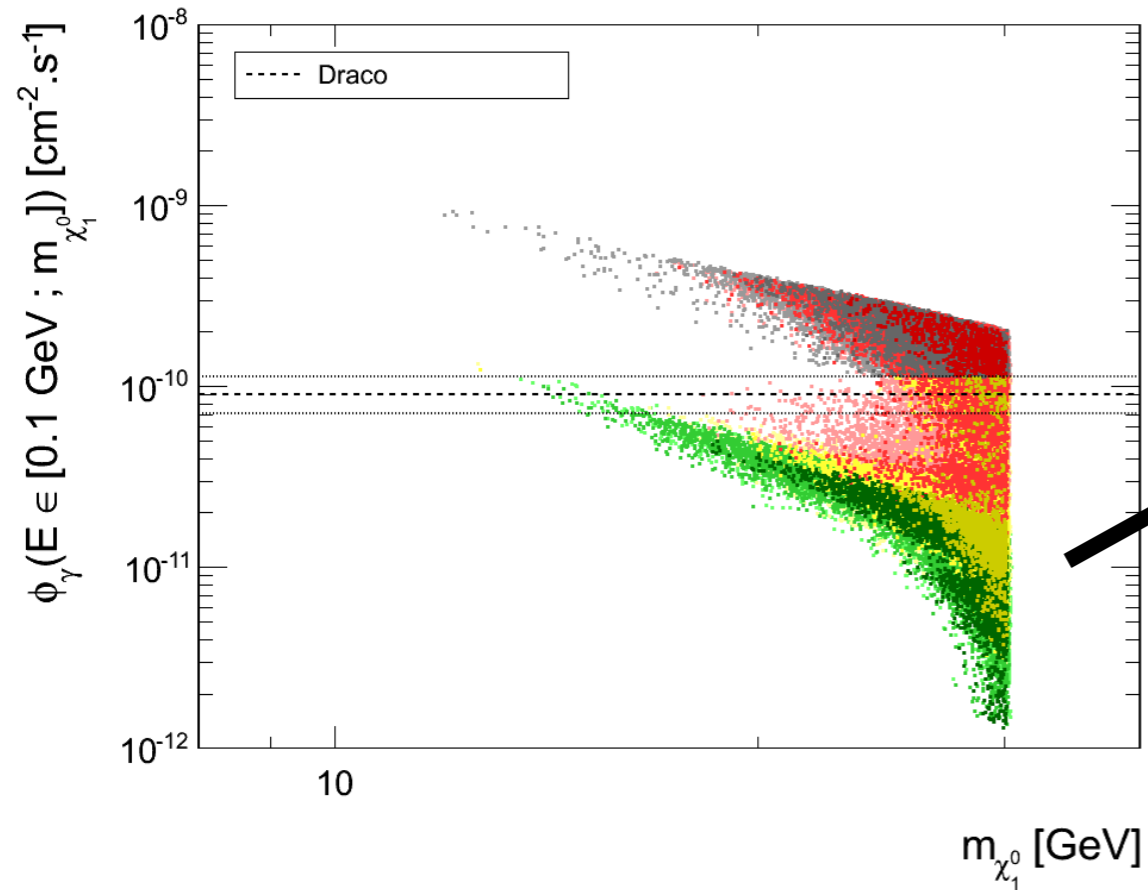
MSSM-EWSB; scans with $m_{dm} < 30$ GeV

black : excluded by LHC ($\tan\beta, m_A$) + FERMI/LAT+XENON100&CDMS
red : excluded by 2 of these 'experiments'
yellow : excluded by 1 of these 'experiments'
green : ok

- 1) **There are points below 30 GeV but not that much below 20 GeV**
(caveat: light neutralinos with very light sbottoms; may not be killed by monophoton searches, arXiv:1205.2557)
- 2) **most of the points are excluded by XENON100 (but...) and CDMS**
- 3) **An improvement of the XENON100 limit at low mass would be extremely useful to probe these scenarios**

Astrophysical constraints

low mass



In the exclusion region for FERMI/LAT
so this possibility should be ruled out/proved soon

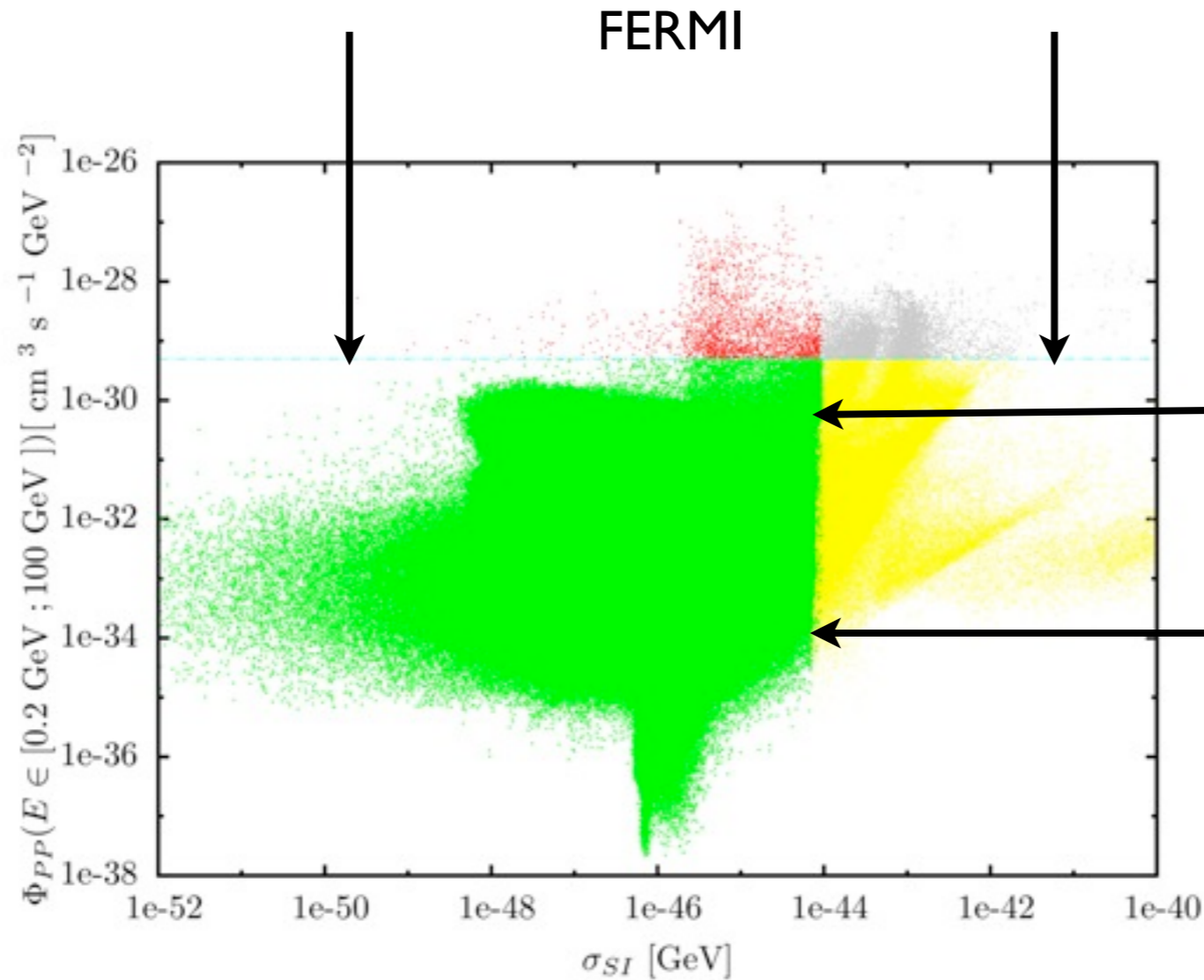
- black** : excluded by LHC (tan beta, mA) + FERMI/LAT+XENON100&CDMS
- red** : excluded by 2 of these 'experiments'
- yellow** : excluded by 1 of these 'experiments'
- green** : ok

**Increasing the mass range:
Cross-correlating Indirect and Direct Detection**

red/black: excluded

yellow: excluded by 1 experiment

green: ok



Model = pMSSM + relic density > 3% WMAP, $m_{dm} < 100$ GeV (no mass below 20 GeV)

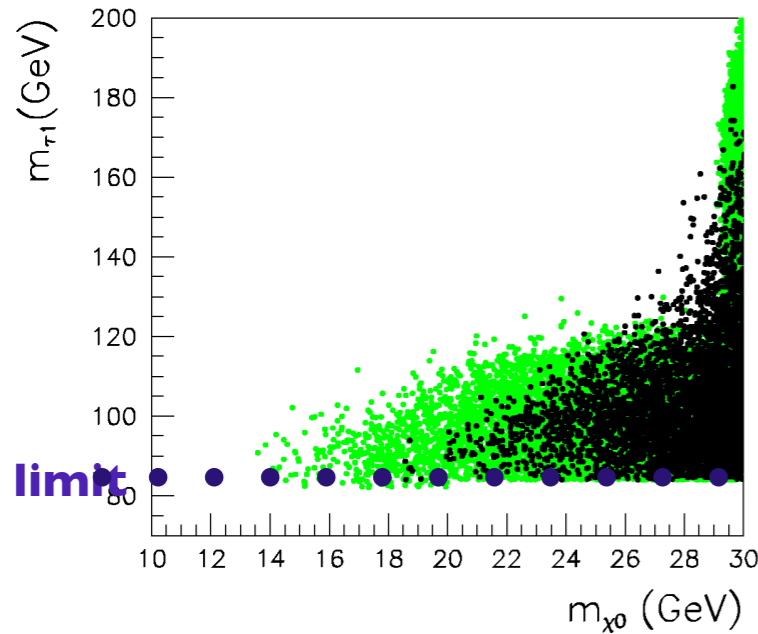
Combining both types of limits, one excludes a region that was not explored previously but there is still progress to do.

XENONIT (or experiments with similar potential) welcome!

Light staus are associated with light neutralinos (<28 GeV)

Are there signatures at LHC?

(Higgs coupling not efficient enough and no other sparticle to help the annihilations)



staus are produced by gluino and squark decays
They further decay into neutralino (not LSP) or chargino which decay into taus. This can give same sign di and tri-tau signatures.

these are the main channels to consider after cuts

arXiv:1206.5404

| Cuts | SSD τ_j | | | | | Trit τ_j | | | | |
|---|--------------|-----|-------|-----|-------|---------------|-----|-------|-----|------|
| | B | BP1 | Sig. | BP2 | Sig. | B | BP1 | Sig. | BP2 | Sig. |
| basic cuts | 2368 | 355 | 7.12 | 39 | 0.799 | 138 | 82 | 6.41 | 14 | 1.17 |
| $\cancel{E}_T > 150$ GeV | 376 | 259 | 12.15 | 22 | 1.12 | 19 | 60 | 10.25 | 8 | 1.72 |
| $\Sigma p_T > 1000$ GeV | 482 | 294 | 12.29 | 19 | 0.86 | 18 | 69 | 11.67 | 7 | 1.56 |
| $\Sigma p_T > 1100$ GeV | 319 | 280 | 13.96 | 19 | 1.05 | 12 | 67 | 12.79 | 7 | 1.86 |
| $M_{eff} > 1100$ GeV | 326 | 296 | 14.55 | 19 | 1.04 | 14 | 69 | 12.55 | 7 | 1.74 |
| $M_{eff} > 1200$ GeV | 257 | 287 | 15.5 | 19 | 1.17 | 10 | 68 | 13.58 | 7 | 2.01 |
| $\Sigma p_T > 1000$ GeV + $\cancel{E}_T > \max(150, 0.1\Sigma p_T)$ GeV | 106 | 208 | 16.31 | 15 | 1.42 | 8 | 52 | 11.74 | 7 | 2.20 |
| $M_{eff} > 1000$ GeV + $\cancel{E}_T > \max(150, 0.1M_{eff})$ GeV | 157 | 246 | 16.36 | 19 | 1.49 | 10 | 58 | 12.03 | 8 | 2.27 |

Table 2: Number of signal and background events for the $2\tau_j+3\text{-jets}+\cancel{E}_T$ and $3\tau_j+3\text{-jets}+\cancel{E}_T$ final states, considering all SUSY processes, with $E_{cm}=14$ TeV at an integrated luminosity of 10 fb^{-1} assuming tau identification efficiency of 50% and a jet rejection factor of 100. The series of cuts are applied independently.

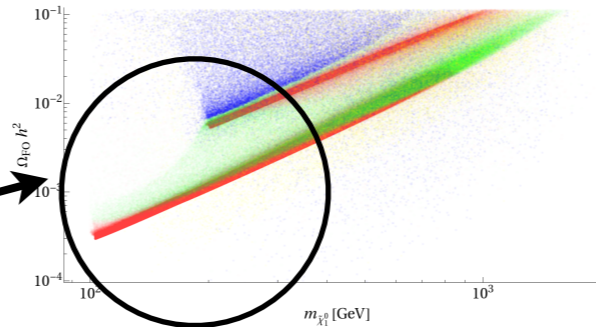
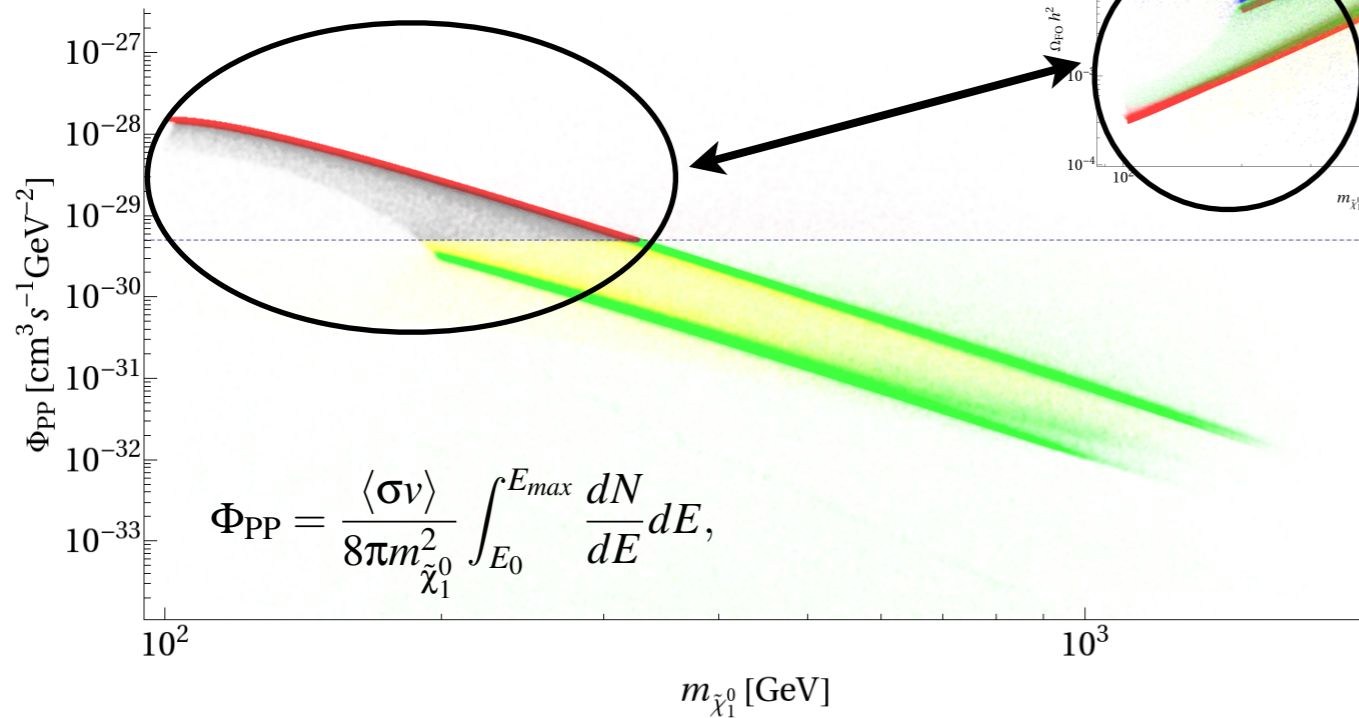
neutralinos with a mass below 28 GeV should be easy to rule out with LHC (if 14 TeV, 10 fb-1).

Higher masses

Astrophysical constraints

High mass

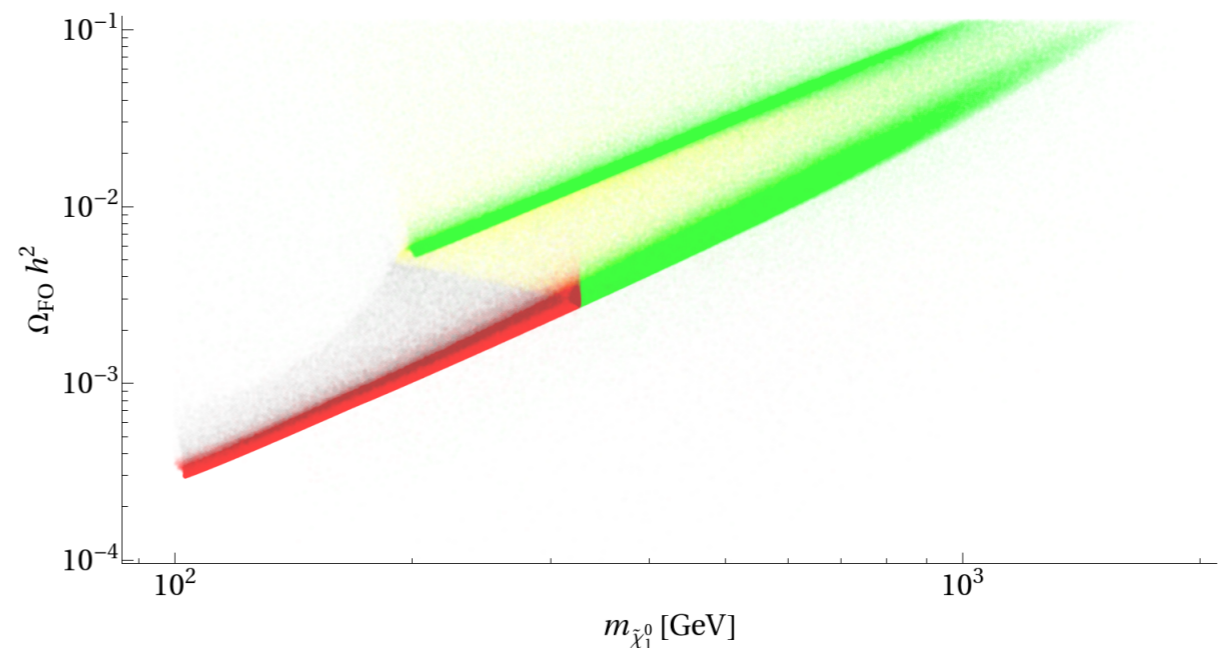
Gamma ray flux from dwarf galaxies



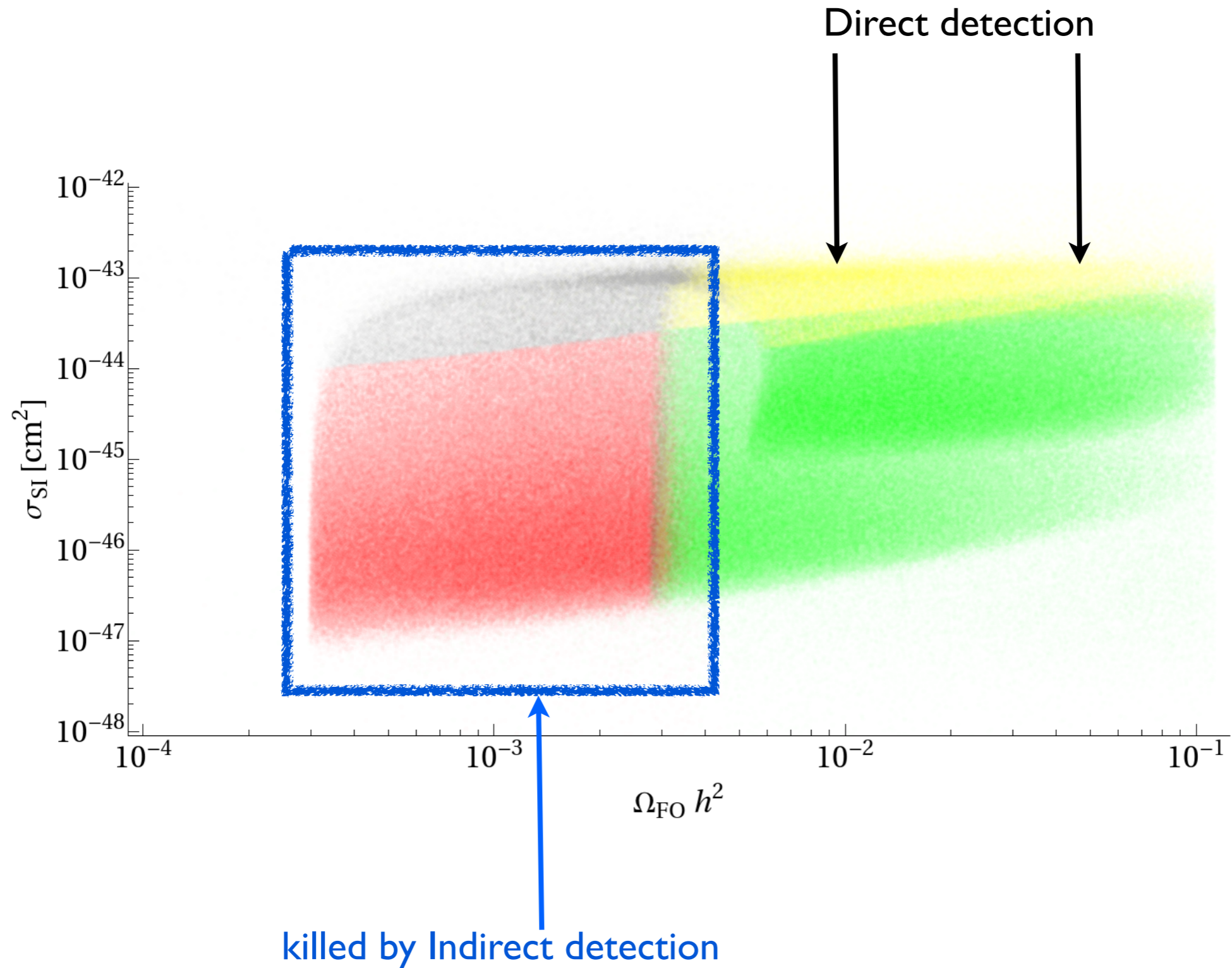
Red: excluded by Indirect detection
yellow: excluded by XENON100
black: excluded by both constraints
green: not excluded

FERMI/LAT do not kill all the points but they do kill many if we assume a regeneration mechanism!

As a result, scenarios with very large cross section at Freeze-Out cannot be regenerated!



$m_{dm} > 100 \text{ GeV}$



XENONIT (or similar) again welcome+LHC analysis

Change of Framework

Another example of complementarity between all experiments: NMSSM

extra singlet enable to have a very light Higgs
 enable to have light neutralinos with a FO relic density

1107.1614

fixed at the weak scale. The free parameters are taken to be the gaugino masses $M_1, M_2 = M_3/3$, the Higgs sector parameters $\mu, \tan\beta, \lambda, \kappa, A_\lambda, A_\kappa$, a common mass for the sleptons $m_{\tilde{l}}$ and the squarks $m_{\tilde{q}}$ as well as only one non-zero trilinear coupling, A_t , for more details see [4].

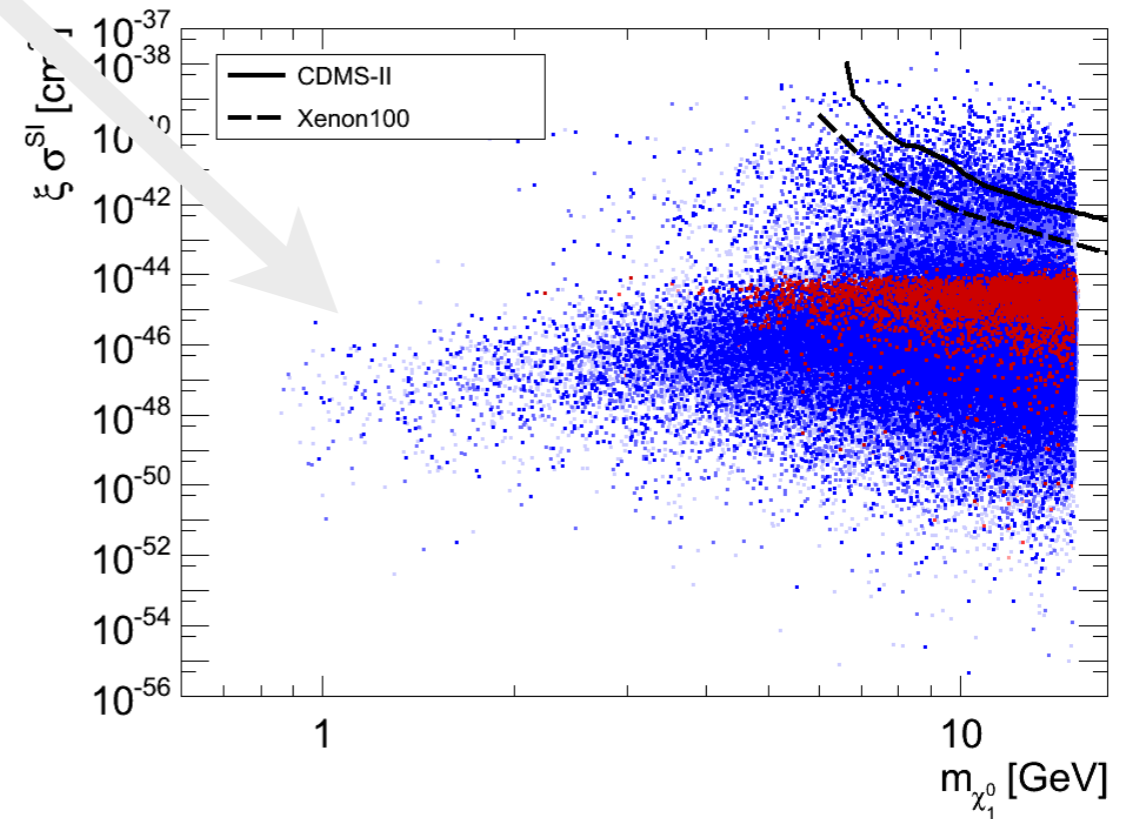
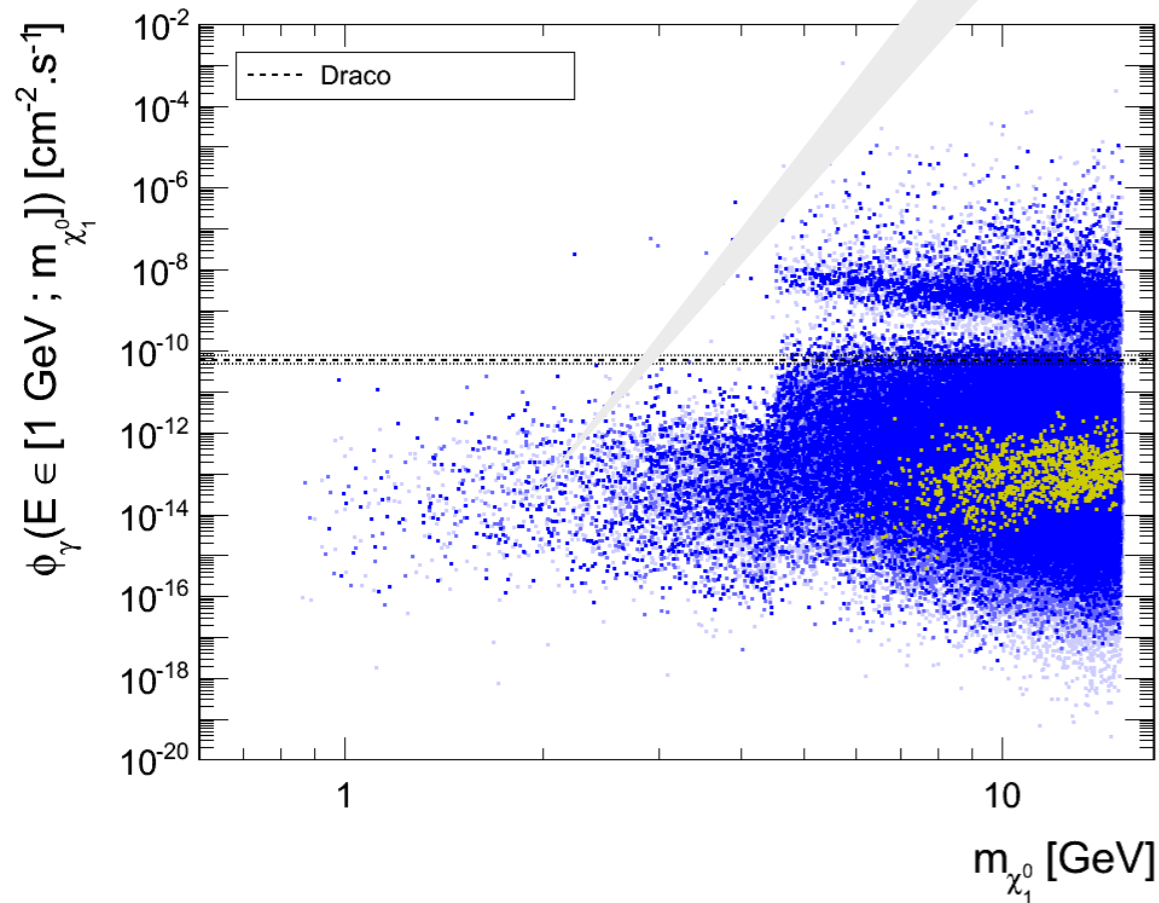
| | | | | | | | | | | |
|-------|-------|-----------------|-----------------|-------|-------------|-----------|----------|-------------|------------|-------|
| M_1 | M_2 | $M_{\tilde{l}}$ | $M_{\tilde{q}}$ | μ | $\tan\beta$ | λ | κ | A_λ | A_κ | A_t |
|-------|-------|-----------------|-----------------|-------|-------------|-----------|----------|-------------|------------|-------|

$$W = \lambda S H_u H_d + \frac{1}{3} \kappa S^3 \quad \mu = \lambda \langle S \rangle$$

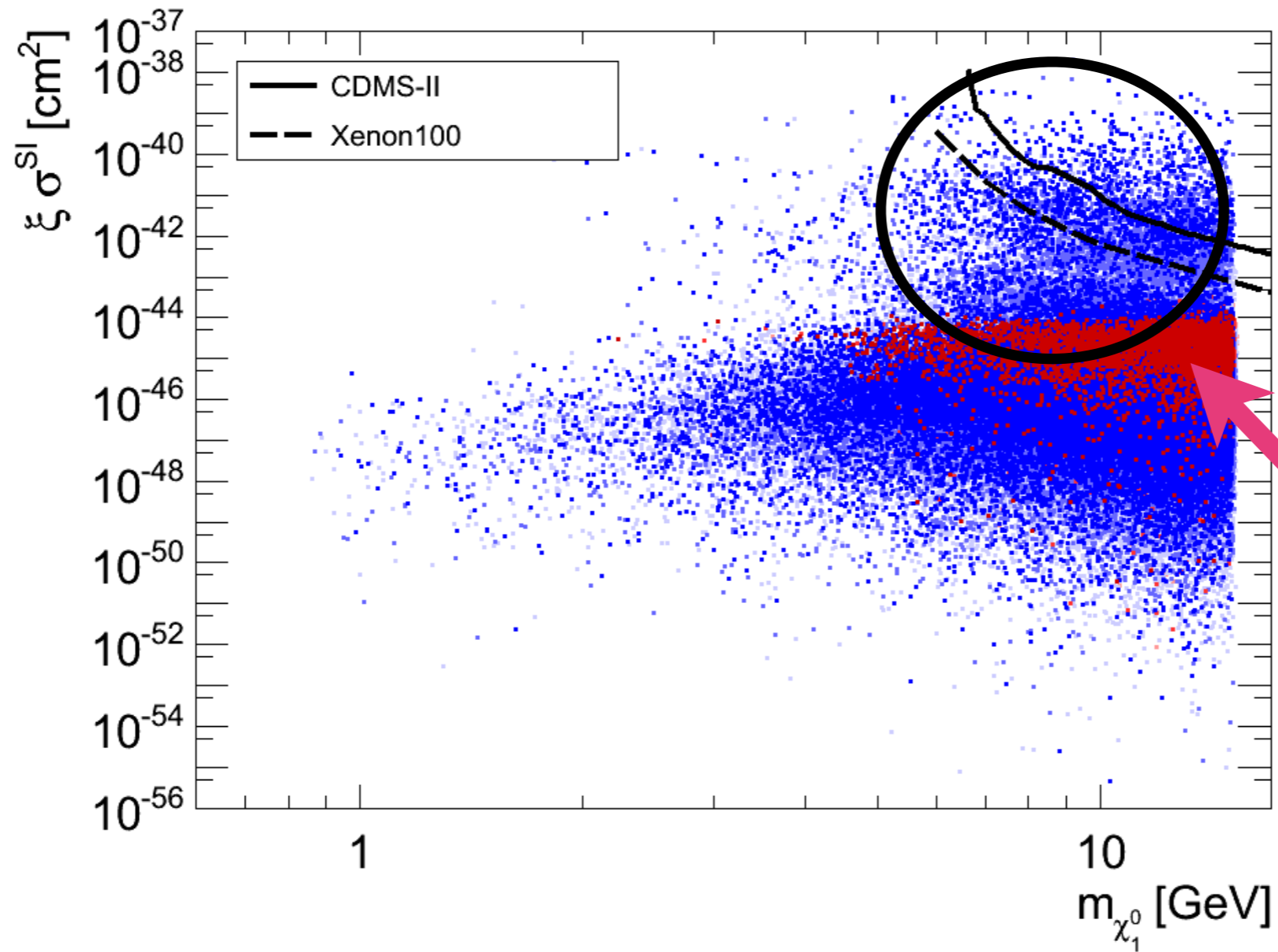
$$\mathcal{L}_{\text{soft}} = m_{H_u}^2 |H_u|^2 + m_{H_d}^2 |H_d|^2 + m_S^2 |S|^2 + (\lambda A_\lambda H_u H_d S + \frac{1}{3} \kappa A_\kappa S^3 + h.c.)$$

$\mu, \tan\beta$ as well as $\lambda, \kappa, A_\lambda, A_\kappa$.

light neutralinos...



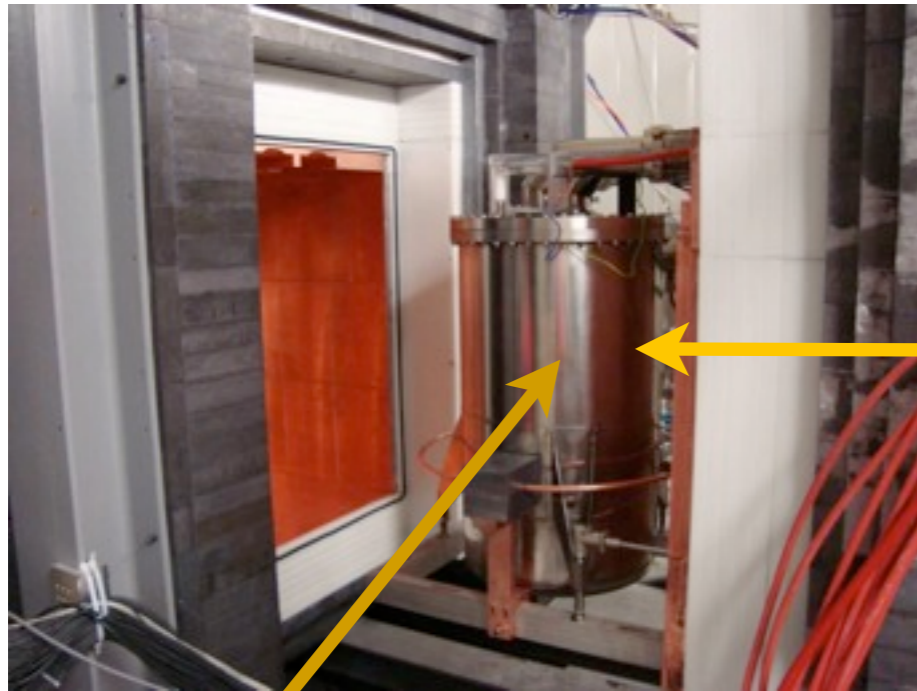
How far are the points close to the XENON100 limit close to be excluded?



What are the uncertainties?

already excluded by indirect detection

Re-investigating the XENON100 experiment

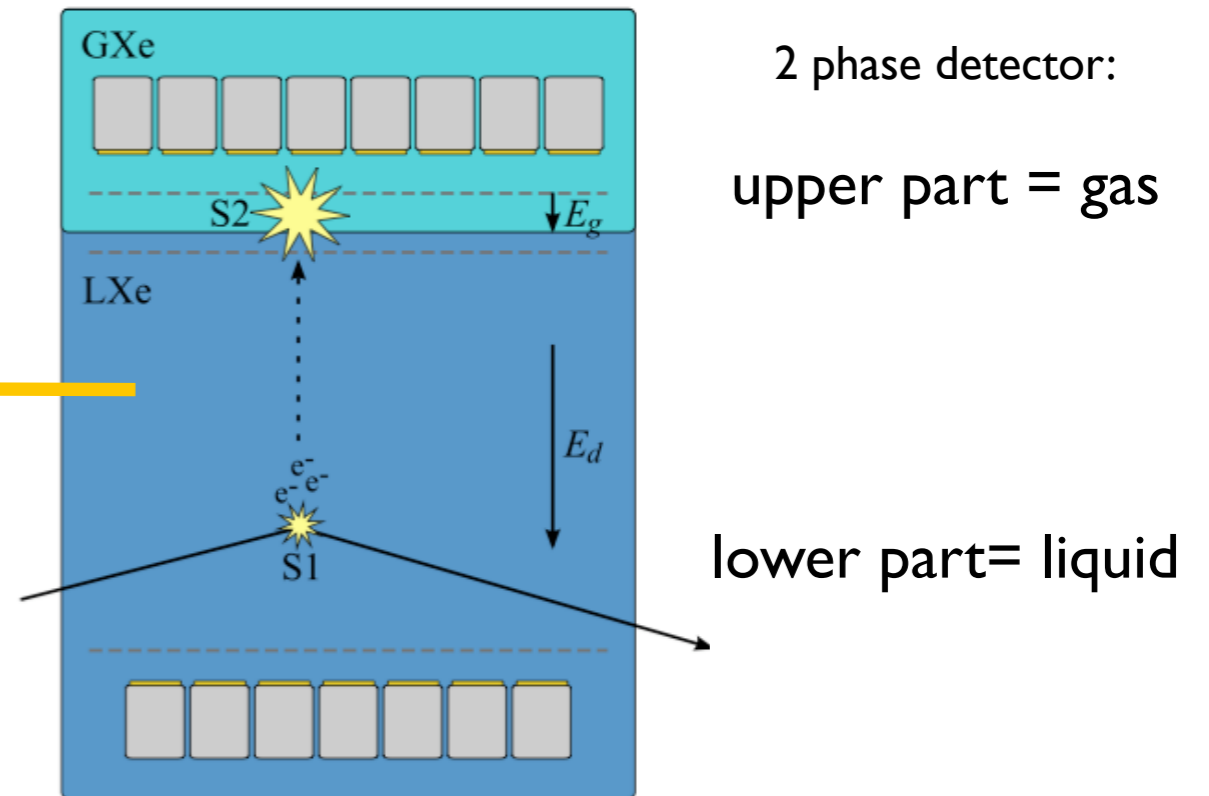


detector inside (shielded from radioactivity)

Exploiting S1 gives an information about the interaction of DM with Xenon nuclei but it depends on the scintillation efficiency of the Xenon nuclei.

Problem:

nobody has seen a DM particle so we do not know is the scintillation efficiency of a DM particle colliding with a Xenon nucleus. One needs to use calibration measurements
=> relative scintillation efficiency (Leff)



S1 = primary scintillation signal

S2 = secondary scintillation signal
(originates from the drift of electrons from ionised Xenon)

S1, S2 measured in photo-electrons

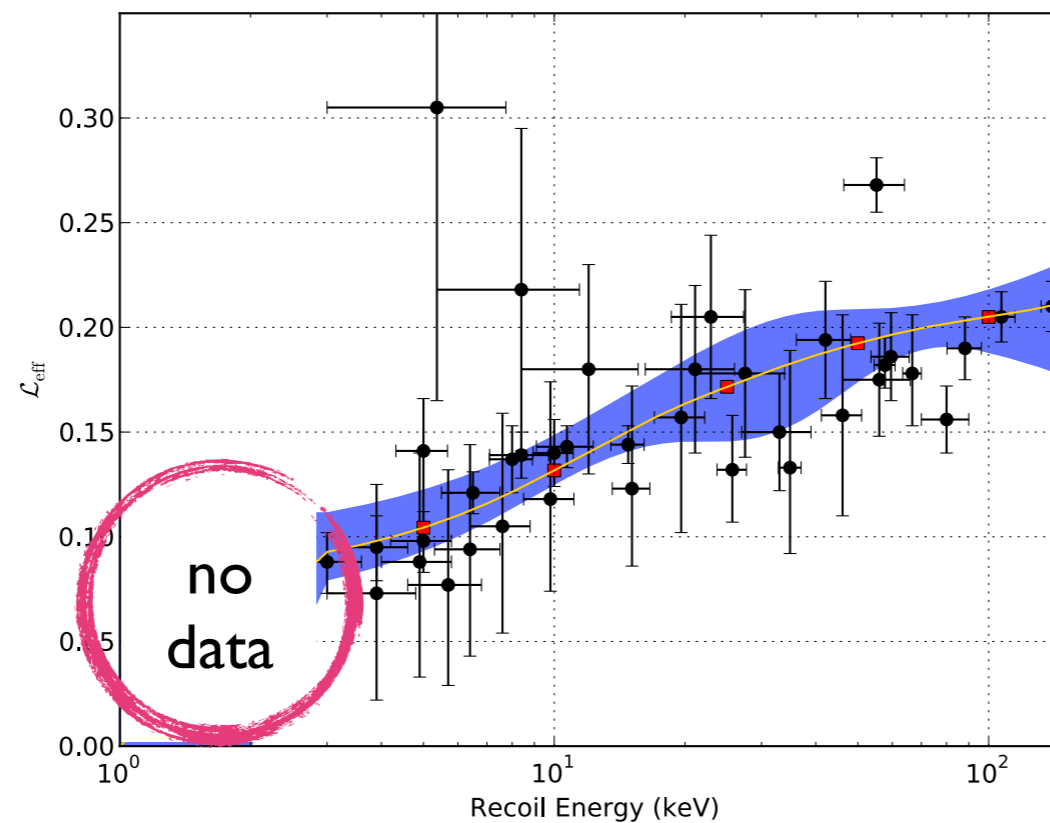
Sensitivity of XENON100 limit at low mass

Recoil energy $E_{nr} = \frac{S_1}{L_y} \frac{S_{er}}{L_{eff} S_{nr}}$ Recoil energy depends crucially on L_{eff}

Light yield for the calibration source emitting gammas

quenching factors, related to the electric field

One needs to measure L_{eff} but here are the data:

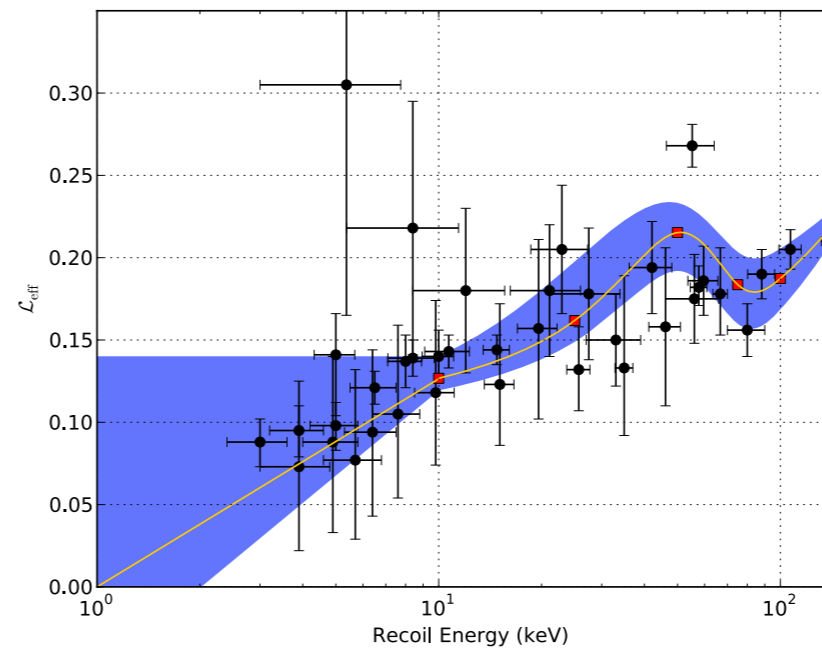
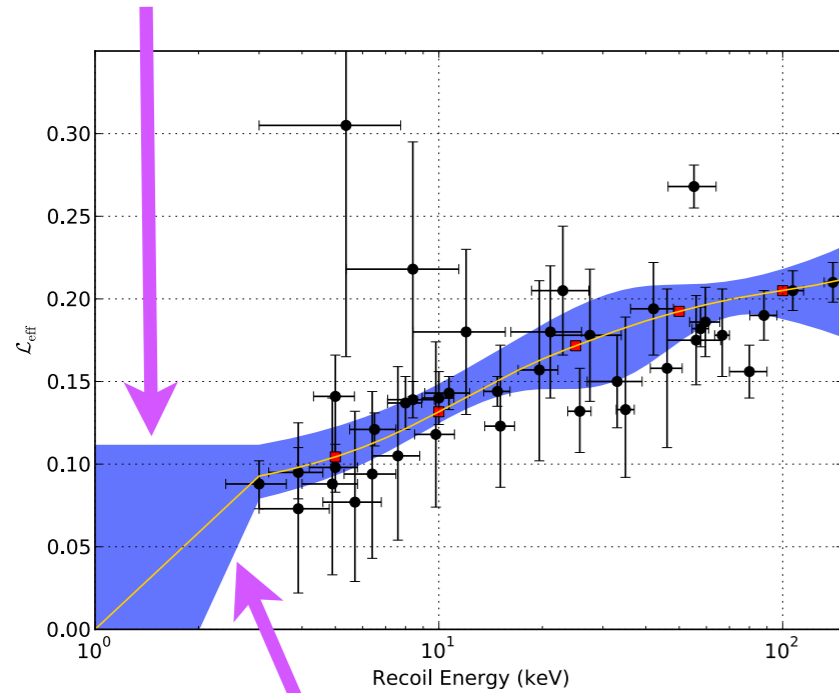


none of them are really consistent and there is no theoretical expression to use for L_{eff} to perform a best fit so the solution is to perform a cubic spline interpolation

Sensitivity of XENON100 limit at low mass

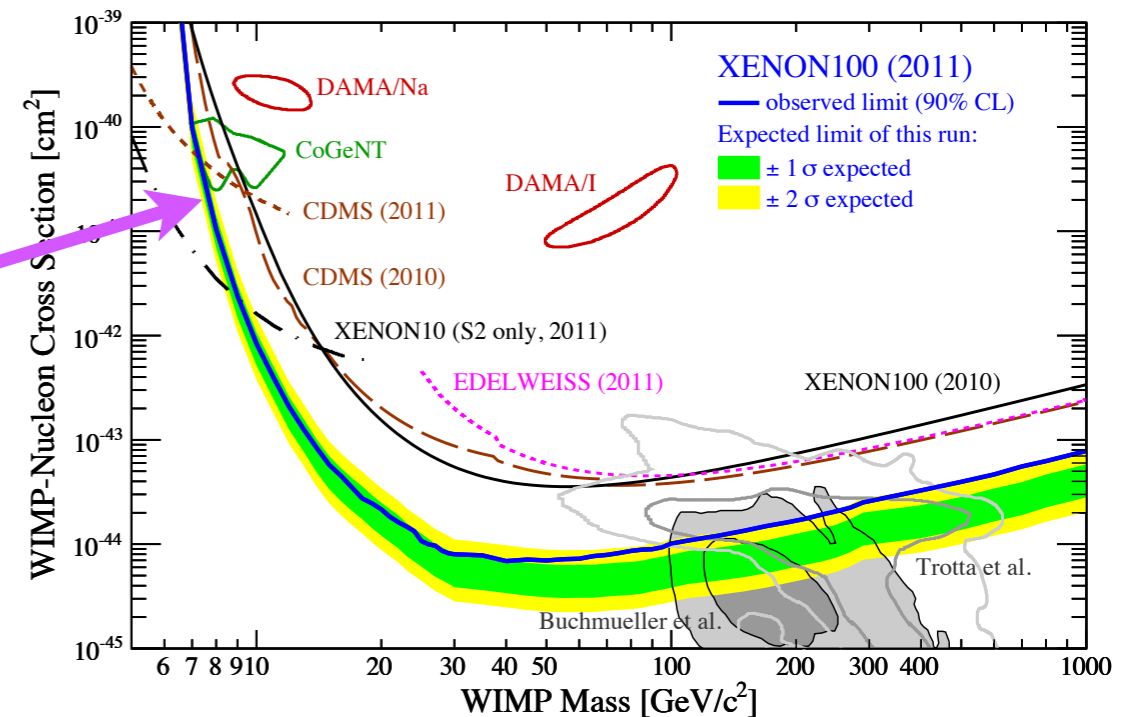
Recoil energy depends crucially on L_{eff} **but lack of data below 3keV**

One option is to extrapolate the fit of data below 3 keV...but there is some choice!



But how come such an uncertainty does **not** translate into the exclusion curve?

black curve = exclusion limit;
yellow/green colour band = what XENON100 expected



The importance of measuring L_{eff} at low E_{nr}

$$\mathcal{L} = \mathcal{L}_1(\sigma, N_b, \epsilon_s, \epsilon_b, L_{eff}, v_{esc}; m_\chi) \times \mathcal{L}_2(\epsilon_s) \times \mathcal{L}_3(\epsilon_b) \times \mathcal{L}_4(L_{eff}) \times \mathcal{L}_5(v_{esc})$$

Dark Matter likelihood

NR likelihood

ER likelihood

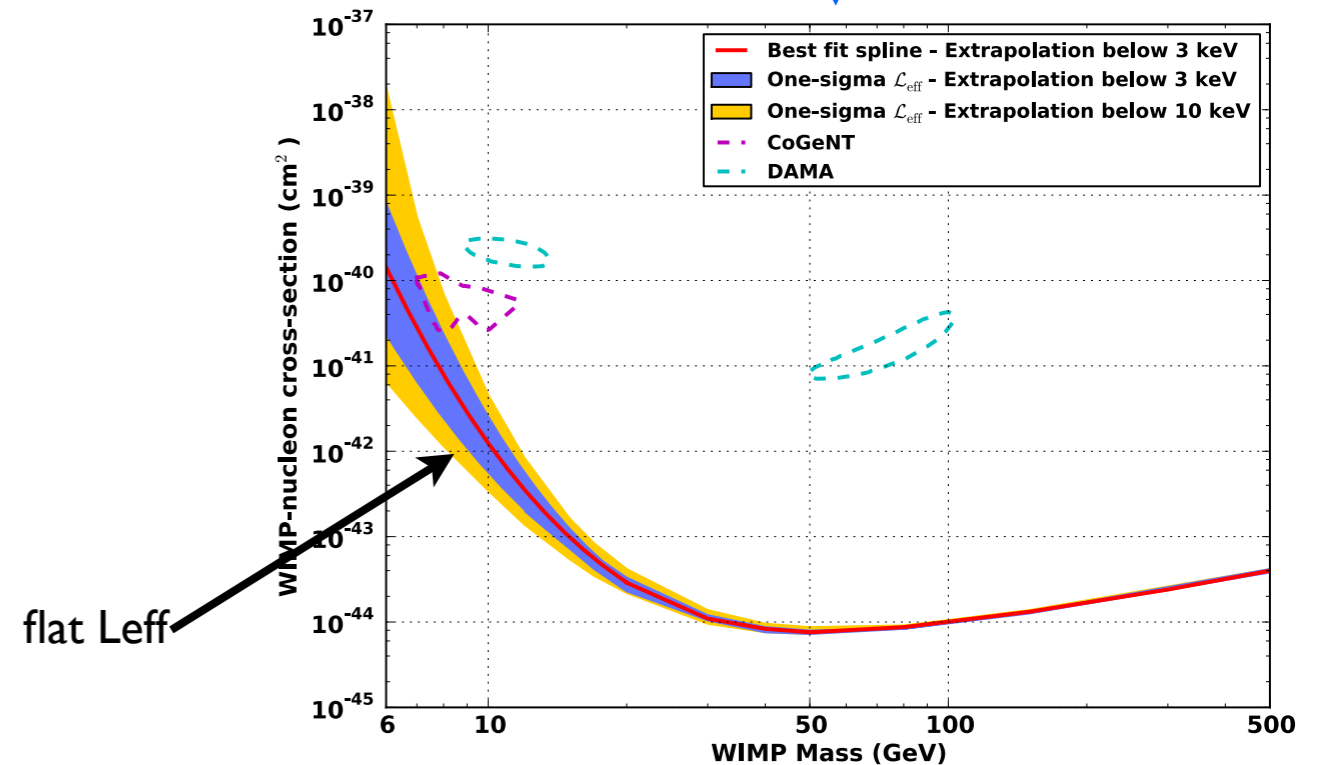
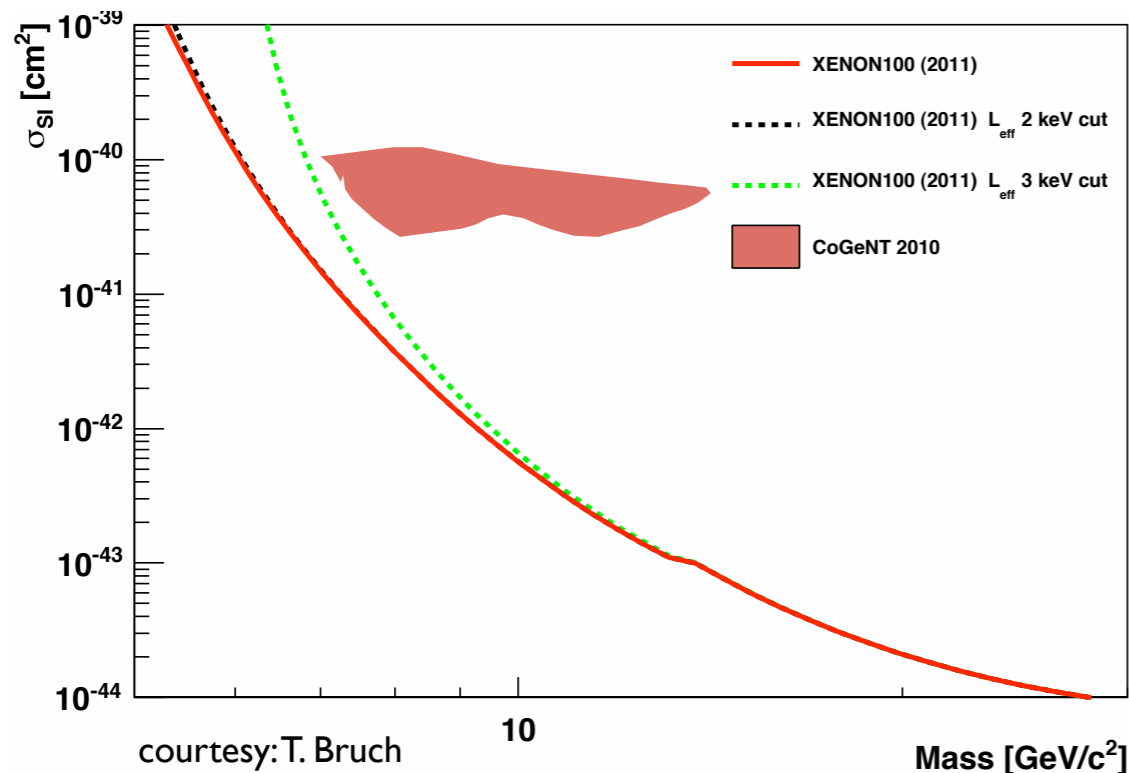
Uncertainties
on the energy
scale

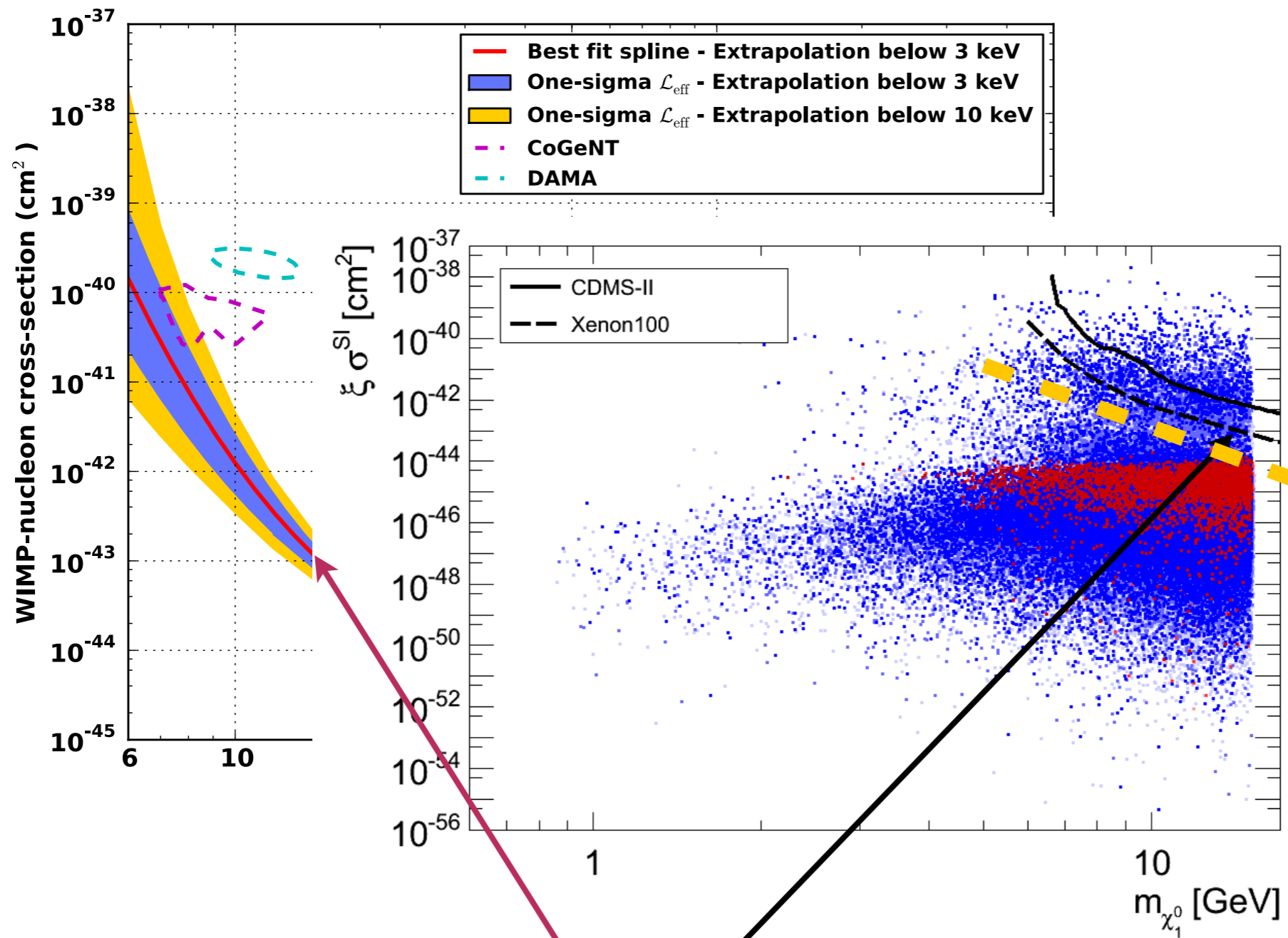
Uncertainties
on the escape
velocity

$$\begin{aligned} \mathcal{L} = & \prod_{j=1}^{\kappa} \text{Pois}(n^j | \epsilon_s^j N_s + \epsilon_b^j N_b) \\ & \times \prod_{i=1}^{n^j} \frac{\epsilon_s^j N_s f_s(S1) + \epsilon_b^j N_b f_b(S1)}{\epsilon_s^j N_s + \epsilon_b^j N_b} \\ & \times \text{Pois}(m_b^j | \epsilon_b^j M_b) \times \text{Pois}(m_s^j | \epsilon_s^j M_s) \\ & \times e^{-(t-t^{\text{obs}})^2/2} \times f_v(v_{\text{obs}} | v_{\text{esc}}). \end{aligned}$$

Same Likelihood but without
the parameterisation for L_{eff}

arXiv:1203.6823





XENON100 2011 data could dig even more into this region

mean value of \mathcal{L}_{eff} (with extrapolated fit but not necessarily physical \mathcal{L}_{eff})

Conclusion

Not so many very light neutralinos (hard to find below 15 GeV)

Combining direct, indirect detection is already reducing the parameter space

Even if we relax the lower bound on the relic density, one can set exclusion with INDIRECT detection but DIRECT detection is becoming complementary too!

SUSY searches at LHC will definitely help to reduce the parameter space
(di and tri-taus signatures)

Waiting for the XENON100 new data,
but please remove the parameterisation of L_{eff}

Waiting for LHC new results (including Higgs, arXiv:1203.3446)!

Astro-LHC

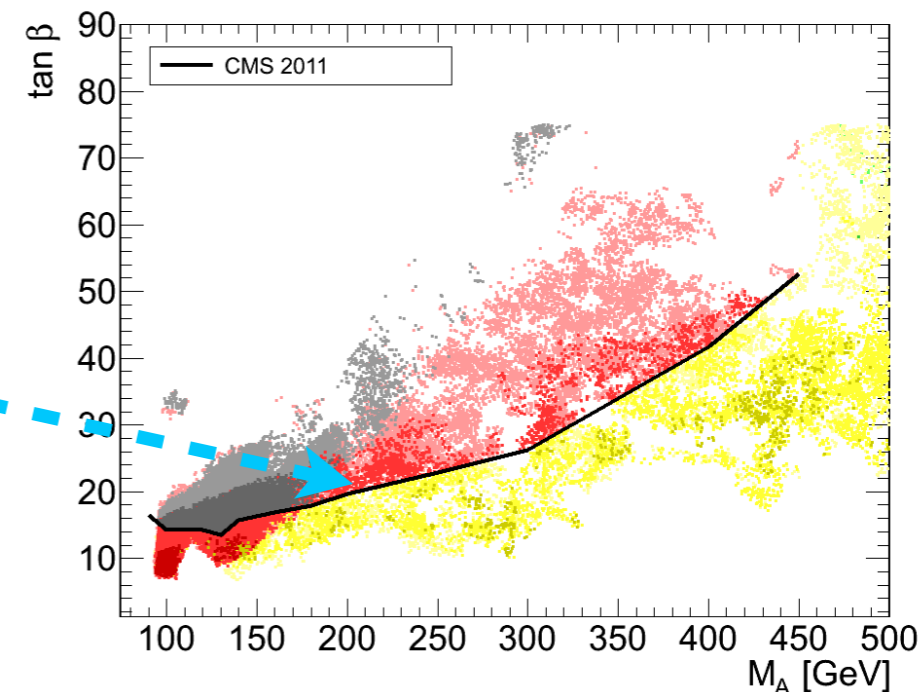
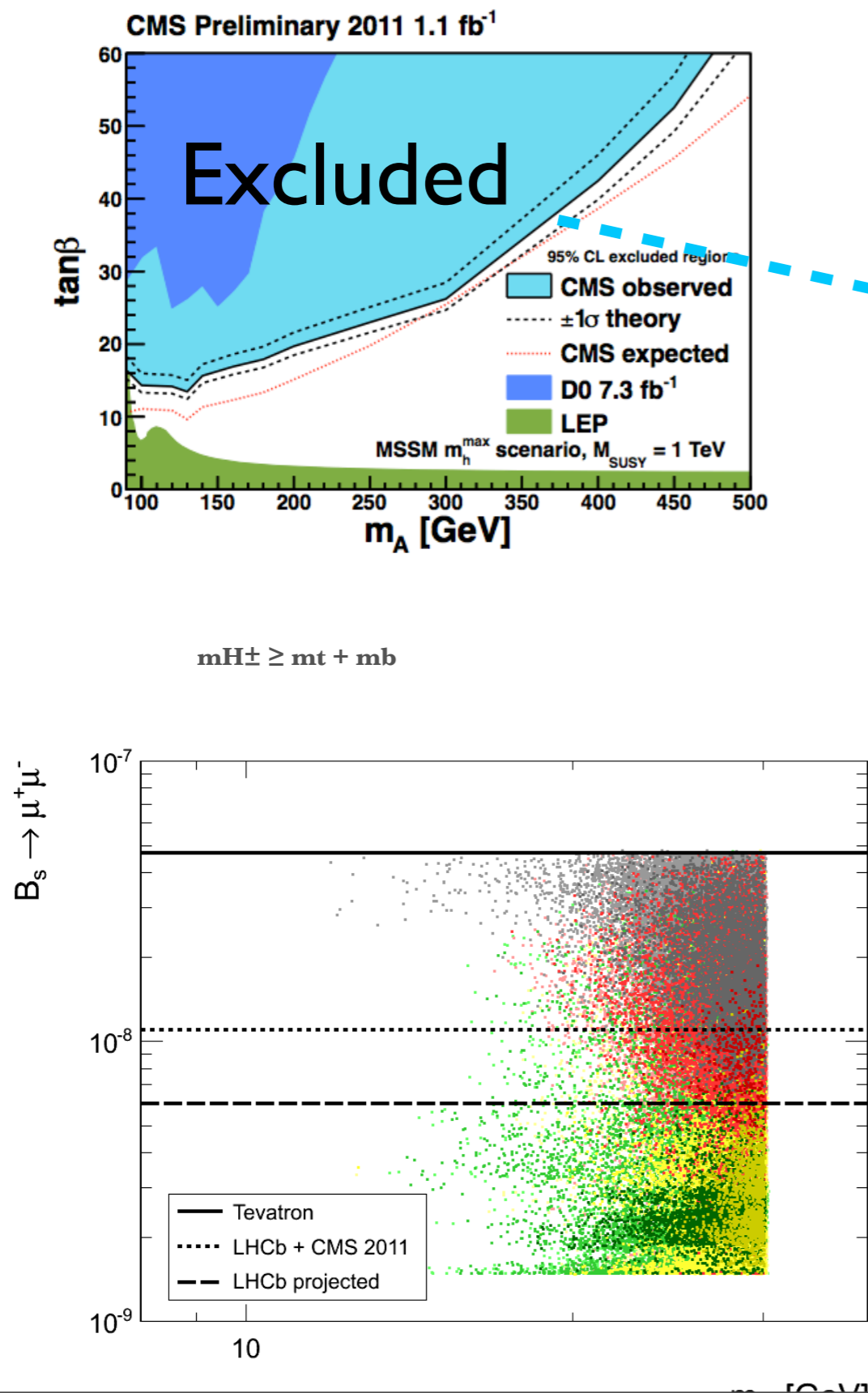


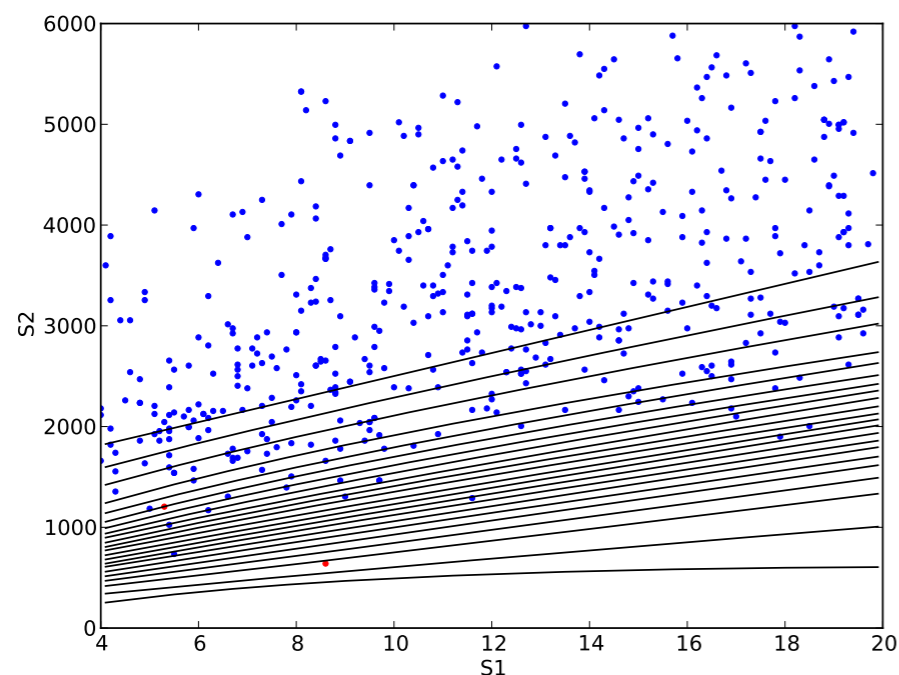
FIG. 2: Allowed points in the $\tan\beta$ vs. M_A plane in the $m_{\chi_1^0} < 30$ GeV search. We show only the region where $M_A < 500$ GeV. The exclusion limit from CMS is also displayed. In yellow (red), points excluded by one (two) constraint and in black those excluded by three constraints (CMS, XENON100 and dSph as described in section III A). The shading represents Q : weights of darker points are at most at 1σ from Q_{\max} while the lighter points are at most at 2σ and 3σ .

How to get the exclusion curve?

$\frac{dR}{dS_1}$: rate per number of photo-electrons detected

This rate is proportional to the rate per number of photo-electrons that are generated in the detector

$$\frac{dR}{dn} = \int dE \frac{dR}{dE} P(n, \nu(E)) \quad \text{with } P(n, \nu(E)) = \frac{\nu^n E^{-\nu}}{n!}$$



$$\nu(E) = E L_y \mathcal{L}_{eff} \frac{S_{nr}}{S_{er}}$$

number of photo-electrons expected for a given recoil energy

FIG. 5: An example of a simulated dataset, with two nuclear-recoil (signal) events, shown in red. The rest of the points are electronic-recoil (background), shown in blue. The black lines divide the S1-S2 plane into the bands used for the analysis.

To obtain the exclusion curve, XENON100 uses a profile Likelihood ratio

$$\lambda = \frac{\mathcal{L}_{max}(\sigma)}{\mathcal{L}_{max}(\hat{\sigma})}$$

Likelihood maximised with σ
←
Likelihood maximised without σ

$$\lambda(\sigma) = \frac{\max_{\sigma \text{ fixed}} \mathcal{L}(\sigma; \mathcal{L}_{\text{eff}}, v_{\text{esc}}, N_b, \epsilon_s, \epsilon_b)}{\max \mathcal{L}(\sigma, \mathcal{L}_{\text{eff}}, v_{\text{esc}}, N_b, \epsilon_s, \epsilon_b)}$$

$$\begin{aligned}
 q_\sigma &= -2 \ln \sigma \text{ if } \sigma > \hat{\sigma} \\
 q_\sigma &= 0 \text{ if } \sigma < \hat{\sigma}
 \end{aligned}
 \quad \longrightarrow \quad
 \lambda = 1 \text{ when } \sigma = \hat{\sigma}$$

For the present data, for a given mass and v_{esc}, one obtains $q_{\sigma_{obs}}$

But one experiment so not enough statistics...to compensate, XENON100 simulated Mock data giving rise to many values of q_σ

$$p_s = \int_{q_{\sigma_{obs}}}^{\infty} f(q_\sigma, H_\sigma) dq_\sigma \quad \mathbf{p\text{-value}} \quad p'_s = \frac{p_s}{1 - p_b} = 10\%$$

$$1 - p_b = \int_{q_{\sigma}^{obs}}^{\infty} f(q_\sigma | H_0) dq_\sigma$$