Unitary Triangle, LHC and B factories

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Beyond The Standard Model of Particle Physics Quy Nhon, Vietnam July 15-21, 2012 Cabibbo-Kobayashi-Maskawa (CKM) matrix " $V\!\!\!\!\!V$

- Fundamental in Standard Model (SM)
- Four parameters $(\theta_{12}, \theta_{13}, \theta_{23}, \phi \leftrightarrow A, \lambda, \rho, \eta)$
- Source of ${\cal CP}$ violation in SM

Testing the SM – V is unitary 3×3 matrix in SM

- Additional generations can make non-unitary
- Can test unitarity relations with measurements of magnitudes and/or phases

New physics can show up in loops, often at same order as SM graphs

 Look for differences among quantities that should be the same in SM, or for deviations from SM predictions

CKM matrix and Unitarity Triangle

Wolfenstein parameterization:

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda + \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4(1 + 4A^2) & A\lambda^2 \\ A\lambda^3[1 - (1 - \frac{1}{2}\lambda^2)(\rho + i\eta)] & -A\lambda^2 + \frac{1}{2}A\lambda^4[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}A^2\lambda^4 \end{pmatrix} \begin{matrix} \textbf{C} \\ \textbf{T} \\ \textbf{C} \\ \textbf{$$

$$\begin{aligned} \alpha &\equiv \varphi_2 \equiv \arg\left(-\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*}\right), \\ \beta &\equiv \varphi_1 \equiv \arg\left(-\frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*}\right), \\ \gamma &\equiv \varphi_3 \equiv \arg\left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right), \end{aligned}$$

 $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0 \; . \label{eq:Vud}$



The "normalized" Unitarity Triangle

$$\lambda \approx 0.22$$
, $A \approx 0.8$, $\sqrt{\rho^2 + \eta^2} \approx 0.4$

$$\approx \frac{V_{ub}}{\lambda V_{cb}} * (\rho, \eta) \qquad V_{td} \\ \gamma (\phi_2) \qquad \lambda V_{cb} \\ \gamma (\phi_3) \qquad (\phi_1) \beta \\ (0,0) \qquad (1,0) \\ \gamma \approx \arg V_{ub} \\ \gamma \approx -\arg V_{td} \\ \alpha = \pi - \beta - \gamma$$

$$\begin{split} \frac{V_{ud}V_{ub}^{*}}{V_{cd}V_{cb}^{*}} + 1 + \frac{V_{td}V_{tb}^{*}}{V_{cd}V_{cb}^{*}} = 0\\ V_{cd} = \lambda , \quad V_{ud} \approx V_{tb} \approx 1 \end{split}$$

Tree vs Loop



- Tree measurements free from NP contributions (ϕ_3 and $|V_{ub}|$), Loop measurements may be affected by NP (ϕ_1 and $|V_{td}|$)
- Experimental precision: $\phi_1 \gg \phi_2 \gg \phi_3$, $|V_{cb}| \gg |V_{td}|$, $|V_{ub}|$ Theoretical cleanness: $\phi_3 > \phi_1 > \phi_2 \gg |V_{cb}| \gg |V_{ub}|$, $|V_{td}|$

Heavy Flavor Dataset



Belle+BaBar total 1240 M $B\overline{B}$ + (even more) **charm** + τ BaBar (1999–2008) > 500 fb⁻¹, **Belle (1999–2010)** > 1000 fb⁻¹

LHCb 1.0 fb⁻¹ (2011) + 0.6 fb⁻¹ (2012 June) + more to come already surpassing Belle/BaBar in all charged track final state modes

Other players: CLEO(-c), BESIII, CDF, D0, ATLAS, CMS, ..., and averaging / fitting groups: HFAG, CKMfitter, UTfit, ...

Angles and CPV

Time-dependent CPV measurements







Belle's final data sample (772 M BB) (BaBar's look very similar)
Golden mode (B → J/ψK⁰_S) (only good flavor-tag sample shown)

 ϕ_1/β from b \rightarrow ccs : status • More modes added: $\psi(2S)K_s^0$, $\chi_{c1}K_s^0$, $J/\psi K_L^0$, ... • $\sin 2\phi_1 = 0.68 \pm 0.02$, $\phi_1 = (21.4 \pm 0.8)^\circ$ (2-fold ambiguity resolved) $A_f = -0.005 \pm 0.017$ (consistent with 0 at <2%) Still statistics limited! ⇒ homework for Belle II/SuperB $\sin(2\beta) \equiv \sin(2\phi_1)$ $\beta \equiv \phi_1$ n BaBar $0.69 \pm 0.03 \pm 0.01$ 망망 PRD 79 (2009) 072009 BaBar χ_{ο0} K_S PRD 80 (2009) 112001 $0.69 \pm 0.52 \pm 0.04 \pm 0.07$ AVOURED 1 BaBar J/ψ (hadronic) K_S PRD 69 (2004) 052001 1,56 ± 0.42 ± 0.21 0.8 Belle $0.67 \pm 0.02 \pm 0.01$ ω PRL 108 (2012) 171802 ~ $0.84^{+0.82}_{-1.04} \pm 0.16$ ALEPH 0.6 PLB 492, 259 (2000) $\beta_{\equiv \phi_1} = (21.4 \pm 0.8)^\circ$ 3.20 +1.80 ± 0.50, OPAL EPJ C5, 379 (1998) 0.4 0.79 +0.41 CDF PRD 61, 072005 (2000) 0.2 $0.53 + 0.28 \pm 0.05$ LHCb LHCb-CONF-2011-004 Belle5S $0.57 \pm 0.58 \pm 0.06$ 0 PRL 108 (2012) 171801 Average 0.68 ± 0.02 HFAG 02 0.6 0.8 04 -2 -1 0 2 3 ρ



$$S_{\pi\pi} = \sqrt{1 - \mathcal{R}_{\pi\pi}^2} \sin 2\phi_2^{\text{eff}}$$
, where $\phi_2^{\text{eff}} = (\phi_2 + \kappa)$ is not ϕ_2

Isospin analysis [Gronau-London PRL65,3381(1990)] Relations with $B^+ \to \pi^+\pi^0$ and $B^0 \to \pi^0\pi^0$ (same for $B \to \rho\rho$ after resolving polarization) Isospin breaking effects are small (~ 2°) [EW penguins, $m_u \neq m_d$, $\pi - \eta^{(\prime)}$ mixing] $A(\pi^+\pi^0) = \overline{A}(\pi^-\pi^0)$

• Time-dependent Dalitz analysis [Snyder-Quinn PRD48,2139(1993)] $B^0 \rightarrow \pi^+ \pi^- \pi^0$ contains $\rho^+ \pi^-$, $\rho^- \pi^+$, $\rho^0 \pi^0$ and their interferences ϕ_2/α directly determined, $\rho^\pm \pi^0$ and $\rho^0 \pi^+$ for further improvement



Huge signal sample



[LHCb 0.7 fb⁻¹, LHCb-CONF-2012-007]

 $S_{\pi\pi} = A_{\pi\pi}^{\text{mix}} = 0.56 \pm 0.17 \pm 0.03$ $\mathcal{A}_{\pi\pi} = A_{\pi\pi}^{\rm dir} = 0.11 \pm 0.21 \pm 0.03$

First significant (3.2 σ) mixing-induced CPV measurement at a hadron collider

 ϕ_2/α from b \rightarrow uud : status



● Multifold ambiguity solved by combination of ππ, ρπ and ρρ⇒ Consistent solution exists, ρρ bound is most stringent

Many Belle's / some BaBar's results yet to be updated to the full statistics, LHCb will further improve $S_{\pi\pi}$ and $\mathcal{A}_{\pi\pi}$ Further ϕ_2/α related measurements are homework for Belle II/SuperB

Measurement of ϕ_3 / γ in B \rightarrow DK decays





If D^0 and \overline{D}^0 decay into the same final state: $|\tilde{D}\rangle = |D^0\rangle + re^{i\theta}|\overline{D}^0\rangle$ Relative phase in $B^+ \to DK^+$: $\theta = +\phi_3 + \delta_B$ $B^- \to DK^-$: $\theta = -\phi_3 + \delta_B$

Ratio of the two amplitudes:

$$r = \left| \frac{A(B^- \to \overline{D}{}^0 K^-)}{A(B^- \to D^0 K^-)} \right| = \left| \frac{V_{ub} V_{cs}^*}{V_{cb} V_{us}^*} \right| \times [\text{Color supp}] \sim 0.1$$

- Several choices of the D decays:
 - $D \rightarrow KK$, ππ, $K_s \pi^0$, $K_s \phi$, $K_s \omega$, ... (Gronau, London, and Wyler)
 - $D \rightarrow K\pi$, $K\pi\pi^0$, ... (Atwood, Dunietz, and Soni)
 - $D \rightarrow K_s \pi \pi$, $K_s KK$, ... (*Bondar*, Giri, Grossman, Soffer, and Zupan)



Dalitz analysis of D decays from $B \rightarrow DK$

Use $B^{\pm} \rightarrow DK^{\pm}$ modes with 3-body decay $D \rightarrow K_S^0 \pi^+ \pi^-$. Dalitz plot density: $d\sigma_{\pm}(m_+^2, m_-^2) \sim |M_{\pm}|^2 dm_+^2 dm_-^2$

 $|M_{\pm}(m_{+}^{2}, m_{-}^{2})|^{2} = |f_{D}(m_{+}^{2}, m_{-}^{2}) + re^{i\delta_{B}\pm i\phi_{3}}f_{D}(m_{-}^{2}, m_{+}^{2})|^{2}$ $= \left| \left| \left| \left| \left| \left| \right| \right| \right| + re^{i\delta_{B}\pm i\phi_{3}} \right| \left| \left| \left| \left| \left| \right| \right| \right| \right| \right|^{2}$

 $\overline{D}^0 \rightarrow K_S^0 \pi^+ \pi^-$ amplitude f_D is extracted from continuum $(D^{*\pm} \rightarrow D\pi^{\pm})$, parametrized as a set of two-body amplitudes. Only $|f_D|^2$ is observable \Rightarrow Model dependence as a result . Latest Belle result: $\phi_3 = [78^{+11}_{-12} \pm 4(\text{syst}) \pm 9(\text{model})]^\circ$ (605 fb⁻¹) $r_B = 0.16 \pm 0.04 \pm 0.01(\text{syst})^{+0.05}_{-0.01}(\text{model})$ Model error would dominate precise measurements at Super B factories.

Solution: use binned Dalitz plot and deal with numbers of events in bins



$$M_{i}^{\pm} = h\{K_{i} + r_{B}^{2}K_{-i} + 2\sqrt{K_{i}K_{-i}}(x_{\pm}c_{i} + y_{\pm}s_{i})\}$$
$$x_{\pm} = r_{B}\cos(\delta_{B} \pm \phi_{3}) \quad y_{\pm} = r_{B}\sin(\delta_{B} \pm \phi_{3})$$

$$\begin{split} M_i^{\pm}: \text{ numbers of events in } D &\to K_S^0 \pi^+ \pi^- \text{ bins from } B^{\pm} \to DK^{\pm} \\ K_i: \text{ numbers of events in bins of flavor } \overline{D}^0 \to K_S^0 \pi^+ \pi^- \text{ from } D^* \to D\pi. \\ c_i, s_i \text{ contain information about strong phase difference between symmetric } \\ \text{Dalitz plot points } (m_{K_S^0 \pi^+}^2, m_{K_S^0 \pi^-}^2) \text{ and } (m_{K_S^0 \pi^-}^2, m_{K_S^0 \pi^+}^2): \\ c_i &= \langle \cos \Delta \delta_D \rangle, \quad s_i = \langle \sin \Delta \delta_D \rangle \end{split}$$

Obtaining c_i, s_i

Coefficients c_i, s_i can be obtained in $\psi(3770) \rightarrow D^0 \overline{D}^0$ decays. Use quantum correlations between D^0 and \overline{D}^0 .

• If both D decay to $K_S^0 \pi^+ \pi^-$, the number of events in *i*-th bin of $D_1 \to K_S^0 \pi^+ \pi^-$ and *j*-th bin of $D_2 \to K_S^0 \pi^+ \pi^-$ is

$$M_{ij} = K_i K_{-j} + K_{-i} K_j - 2\sqrt{K_i K_{-i} K_j K_{-j}} (c_i c_j + s_i s_j).$$

 \Rightarrow constrain c_i and s_i .

• If one D decays to a CP eigenstate, the number of events in *i*-th bin of another $D \rightarrow K_S^0 \pi^+ \pi^-$ is

$$M_i = K_i + K_{-i} \pm 2\sqrt{K_i K_{-i}}c_i.$$

 \Rightarrow constrain c_i .

 c_i, s_i measurement has been done by CLEO and can be done in future at BES-III.

CLEO measurement of c_i, s_i

Binned analysis reduces stat. precision. Can improve this by choosing a binning inspired by $\overline{D}^0 \to K_S^0 \pi^+ \pi^-$ model. [CLEO collaboration, PRD 82, 112006 (2010)]



Optimized $\overline{D}{}^0 \rightarrow K_S^0 \pi^+ \pi^-$ binning using BaBar 2008 measurement.



Measured c_i, s_i values and predictions by Belle model

Optimal binning depends on model, but ϕ_3 does not. Bad model \Rightarrow worse precision, but no bias!

Results of ϕ_3/γ measurement

Simultaneous fit to signal selection variables in all bins $\begin{bmatrix} Accepted to Phys.Rev.D \\ [arXiv:1204.6561] \end{bmatrix}$ Free parameters: (x, y), normalization, background fractions in bins.



 $corr(x_+, y_+) = +0.059$ 1st error is statistical, 2nd — systematic, 3rd — c_i, s_i precision.

CPV Results



LHCb prospects for ϕ_3 : half statistics of Belle's sample with 2011 data of 1fb⁻¹, but less background









 ΔIncl.~6% (↓from 18% in 2004)
ΔExcl.~10%
Up to 2-3 σ difference between Excl.-Incl.

V_{ub} and $B \rightarrow \tau v$

- Purely leptonic decay, proportional to $f_B^2 |V_{ub}|^2$ (in SM) or sensitive to charged Higgs (in type-II 2HDM)
- However, f_B is not precisely known (only from Lattice)
- Instead, more reliable constraint from \(\Delta m_d\) and other CKM (and no more direct constraint to \(|V_{ub}|\))



status before ICHEP: **2.8** σ tension in direct vs indirect $B^+ \rightarrow \tau^+ \nu$

New Babar's results $B \rightarrow \tau v$



(BaBar average with semileptonic-tag: $\mathcal{B}(B^+ \rightarrow \tau^+ \nu) = (1.79 \pm 0.48) \times 10^{-4})$

New Belle's results $B \rightarrow \tau v$

- **> 72% more data: 449M \rightarrow 772M B\overline{B}**
- Improved (slow) track efficiency by reprocessing
- New hadronic-tag algorithm Neurobayes neural network
- Newly added K_L veto after understanding data/MC difference
- Output States and the state of the state
- Better understanding of peaking background
- Newly including missing-mass in the fit
- Signal peak at 0 in the remnant calorimeter energy E_{ECL}





 $\mathcal{B}(B^+ \to \tau^+ \nu) = (0.72 \, {}^{+0.27}_{-0.25} \pm 0.11) \times 10^{-4}$ (62 ${}^{+23}_{-22}$ events, 3.0 σ)

First 57% of data (same as previous sample) gives $\mathcal{B} = (1.08^{+0.37}_{-0.35}) \times 10^{-4}$, consistent with previous result < 1.9σ even if fully overlapped Additional 43% data gives low branching fraction $\mathcal{B} = (0.24^{+0.34}_{-0.39}) \times 10^{-4}$ Sub-decays of τ (*evv*, $\mu\nu\nu$, $\pi\nu$, $\rho\nu$) give consistent results New K_L^0 veto is not killing the true signal, and more checks were made...



400

350

300

250

200

150

100

50

Balle

25

E_{ECL} (GeV)

0.5

Peaking Backgrounds

Since $e^+e^- \rightarrow B^+B^-$, analysis uses reconstruction

120

80

60

40

20

ີຂີ່ 100

ent

Belle

new

of B⁺, detection of $\tau^- \rightarrow$ one track & small extra E Belle Belle Redfonic-tag Peaking background ma

 E_{ECL} (GeV)

Peaking background may look more significant in the hadronic-tag?

> Backgrond level of semileptonic-tag is higher

New hadronic-tag includes missing mass in the fit, some of the peaking background are included in the projection instead of cut

$B \rightarrow \tau \nu$ comparison with 2006 result

	PRL 97 (2006)	ICHEP 2012 hadronic tag(new) 2D fit to (E _{ECL} , M _{miss} ²) 771		1. 2.
Analysis	hadronic tag 1D fit to E_{ECL}			
N(BB) (x 10 ⁶)	(set A) 449			
		(set A) 449	(set B) 332	I
Efficiency (x 10 ⁻⁴)	3.0	11.2		
N(signal yield)	24.1+7.6	54.1 ^{+18.8}	8.6+14.0	
Br(B ⁺ \rightarrow τ ⁺ ν) (x 10 ⁺)	1.79 ^{+0.56}	1.08+0.37	0.24+0.39	
			1	
		0.72+0.27		
1.			2.5σ	

conservative comparison

- 1. Only with statistical error.
 - Assuming all the signal candidates in the old analysis become signal candidates in the new analysis.

SET A: the data-set used in 2006

SET B: corresponds to the data-set not used in 2006

SET A': corresponds to the data-set used in 2006, but reproduced

All events used for the New Analysis

Old (set A) vs. New (set B) : 2.5σ difference New results. set A' vs. set B : 1.6σ difference Old (set A) vs. New (set A') : 1.2σ difference

*Old result (set A) vs. New (only for non-overlapping events in the set A) BF(non-overlapping events) = $(0.6 + 0.4) \times 10^{-4} \rightarrow 1.9 \sigma$ difference







 $|V_{ud}|, |V_{us}|$ $|V_{cb}|, |V_{ub}|_{SL}$ $B \rightarrow \tau \nu$ $\Delta m_d, \Delta m_s$ ϵK $\sin 2\beta$ α γ $A = 0.812^{+0.015}_{-0.022}$ $\lambda = 0.2254^{+0.006}_{-0.0010}$ $\bar{\rho} = 0.145^{+0.027}_{-0.027}$ $\bar{\eta} = 0.343^{+0.015}_{-0.015}$ (68% CL)

Summary

•Still good agreement with Standard Model (CKM) prediction based on a global fit of the Unitarity Triangle

•Need to verify with a better precision (LHCb and BelleII/SuperB in near future)

•CP violation in the B meson decays is well established at the B factories

•Further search for Beyond Standard Model physics in CP violation. Two main motivations:

- The strength of CP violation in the SM is not sufficient to generate the observed Baryon Asymmetry in the Universe

- Almost all extensions of the SM have new sources of CP violation which can in principle be detected

Thank you for your attention!



1.2

 $B^+ \to \tau^+ \nu_{\tau}$

Using these variables for 2D histogram PDF fitting.

Improves the signal significance by about 20%

Use of 2-D fitting will reduce the sensitivity to peaking backgrounds in E_{ECL} .





B⁰-tagged total without reconstructed KL with reconstructed KL

Background rejection using the K_L is introduced \rightarrow Effective to reduce the peaking background

Improves the signal significance by about 5%

Belle full data + improvement of analysis

Expected signal significance : 6.3σ for Br($B \rightarrow \tau \nu$)=1.65 × 10⁻⁴





Interference between mixing and decay to a CP eigenstate f_{CP} $\Rightarrow \Gamma(B^0_{phys}(t) \rightarrow f_{CP}) \neq \Gamma(\overline{B}^0_{phys}(t) \rightarrow f_{CP})$

Flavor-tagged time-dependent decay rates are different! they are governed by the "CP parameter":



Observables: "direct" CP asymmetry



Time-integrated "direct" CP asymmetry requires two amplitudes and $\delta \neq 0$:



B->DK, D-> $K_s \pi^+\pi^-$ signal selection

Use 711 fb⁻¹ sample (772M $B\overline{B}$ pairs). Belle preliminary Data reprocessed with new tracking \Rightarrow improved efficiency (12% \rightarrow 16%)



Signal selection variables: $M_{\rm bc}$, ΔE , event shape (cos $\theta_{\rm thr}$, "virtual calorimeter" Fisher discriminant). 4D unbinned fit to get signal yield. Signal yield: 1176 + 43 events ($\sim 55\%$ more data than in prev. analysis).



Dalitz plots



Dalitz plots for signal-enriched region: $(M_{\rm bc} > 5.27 \text{ GeV}/c^2, |\Delta E| < 30 \text{ MeV}, \cos \theta_{\rm thr} < 0.8).$



New Belle's V_{ub} results

- Full $\Upsilon(4S)$ data used ($N(B\overline{B}) = 772M / 711 \text{fb}^{-1}$)
- Signal yield extracted from maximum-likelihood fit to M²_{miss}

