

Quy Nhon, Vietnam July 15 - 21, 2012

TOP QUARK POLARIZATION AND THE SEARCH FOR NEW PHYSICS

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Based on work in collaboration with:

Qing-Hong Cao, Chuan-Ren Chen, Jianghao Yu, and Hao Zhang

arXiv: 1101.5625 Phys. Rev. Lett. 106, 201801 (2011);

arXiv: 1111.3641, Phys. Rev. Lett. 108, 072002 (2012);

arXiv: 1207.1101 (July 2012)

OUTLINE

☒ **Semi-leptonic top quark decay.** Methods to measure the top quark polarization

☒ **New physics interpretations of the top quark rapidity asymmetry** at the Tevatron -- what, in addition, do we learn from the decay lepton asymmetry

$$\mathcal{A}_{\text{FB}}^{\ell} = \frac{N(q\ell y_{\ell} > 0) - N(q\ell y_{\ell} < 0)}{N(q\ell y_{\ell} > 0) + N(q\ell y_{\ell} < 0)}$$

☒ **Models** (axigluon model and right-handed W' model) and the decay lepton asymmetry

☒ **Implications for the LHC:** same sign top pairs; rapidity asymmetry

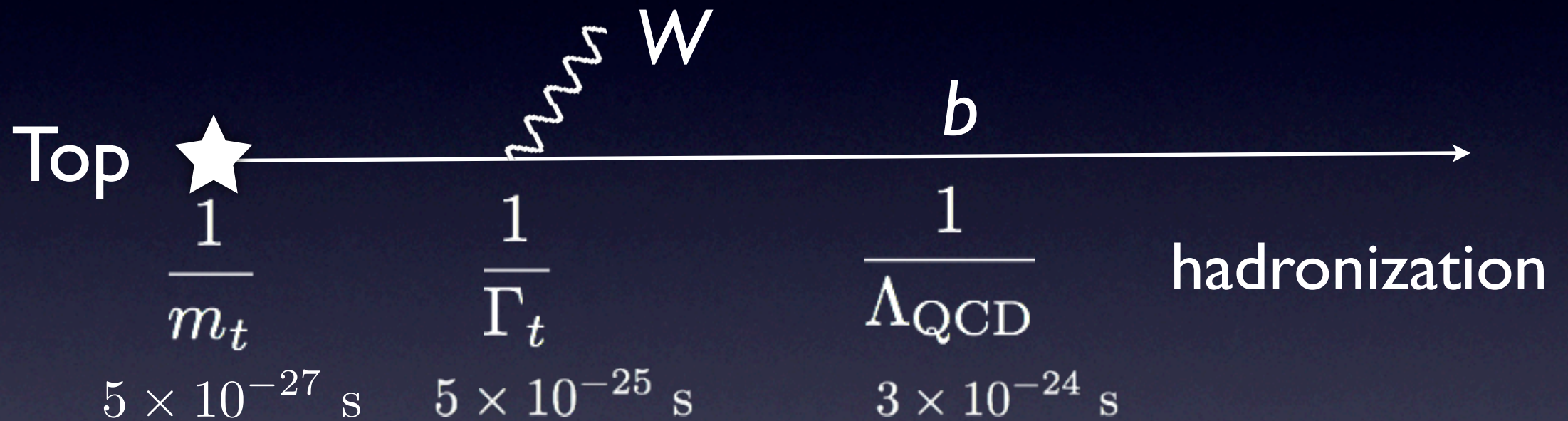
☒ **Models with dark matter candidates** -- added information from top quark polarization

Top quark: most massive of the SM

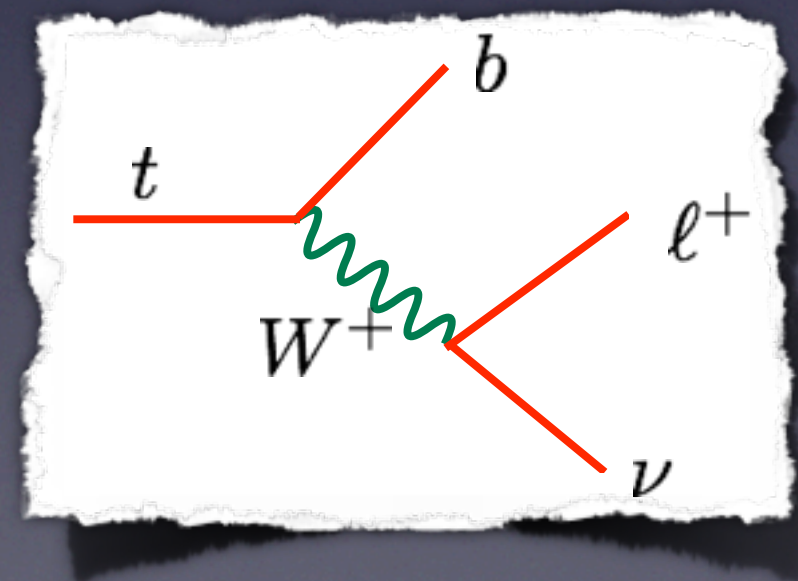
- Large mass : $173 \text{ GeV} \sim \text{VEV} (246 \text{ GeV})$ $Y_t \sim \mathcal{O}(1)$
- Large mass suggests sensitivity to symmetry breaking and BSM effects
- Experiment -- Tevatron deviation from SM expectations of the F/B rapidity asymmetry for top
- Various models of new physics proposed to interpret the asymmetry data (e.g, W' , Z' , ...) invoke right-handed couplings of the top quark
- Other new physics schemes -- unrelated to the asymmetry -- also favor right-handed couplings; valuable to **measure polarization of top quarks**

Top quark

- Large mass : 173 GeV \sim VEV (246 GeV) $Y_t \sim O(1)$
- Short lifetime:

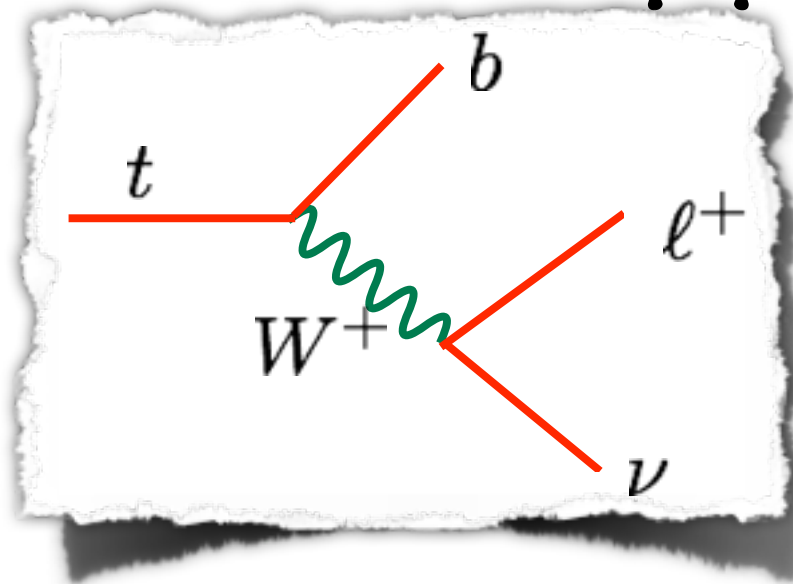


- “bare” quark : spin info retained among decay products in (V-A) interaction




TWO METHODS TO MEASURE TOP POLARIZATION

-  A. Lepton angular distribution in top quark rest frame -- maximally correlated with the top quark spin orientation.



-  Method requires full reconstruction of the top quark kinematics, e.g., with MT2 method

-  B. Lepton momentum distribution -- useful for more complex final states, e.g., when missing energy from dark matter candidates is present ([arXiv:1207.1101](https://arxiv.org/abs/1207.1101))

Angular distribution of decay lepton is a top quark spin analyzer

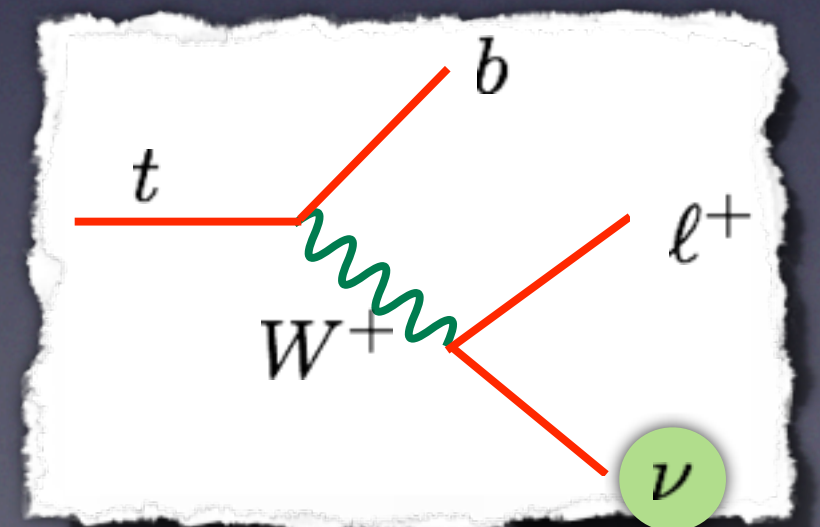
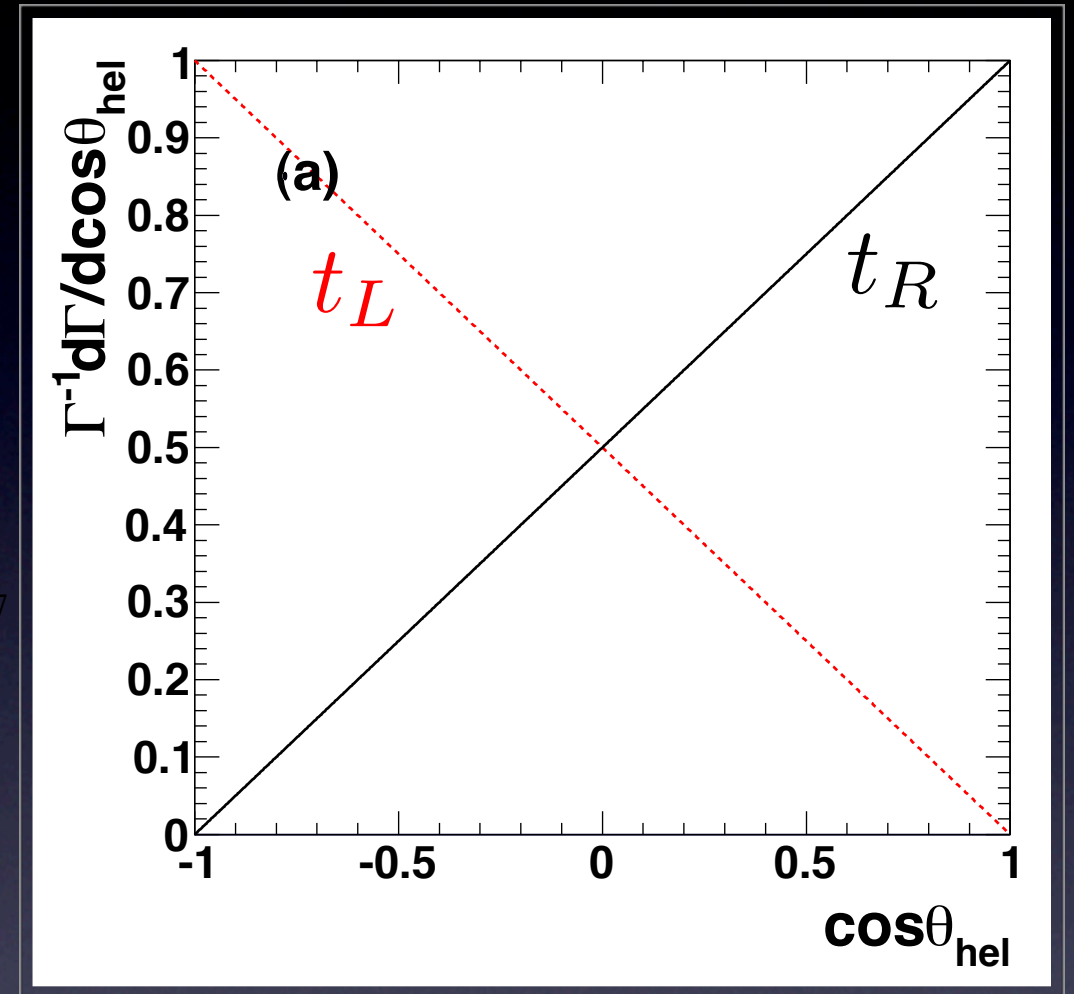
- In the top-quark rest frame

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta_{\text{hel}}} = \frac{1 + \lambda_t \cos\theta_{\text{hel}}}{2}$$

$\lambda_t = +$ right-handed

$\lambda_t = -$ left-handed

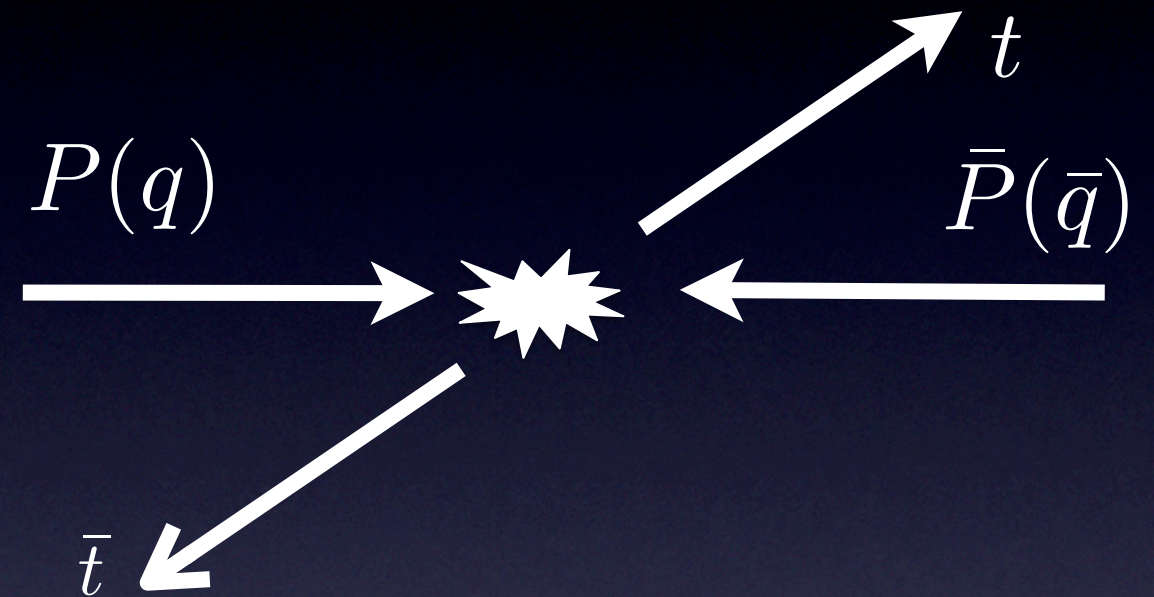
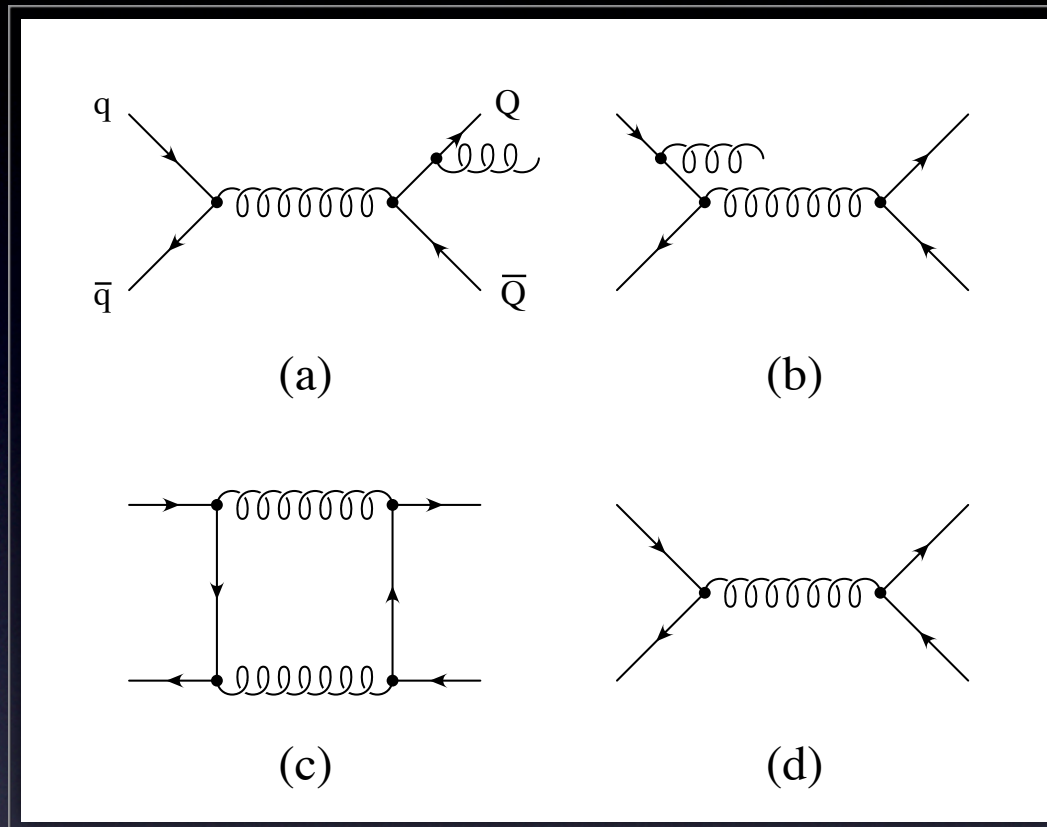
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II. Top quark forward- backward asymmetry

Top-quark F-B asymmetry in the SM

- A charge asymmetry arises at NLO



Top quarks are produced along the direction of the incoming quark

$$A^{p\bar{p}} = \frac{N_t(y > 0) - N_{\bar{t}}(y > 0)}{N_t(y > 0) + N_{\bar{t}}(y > 0)} = 0.051(6)$$

$$A^{t\bar{t}} = \frac{N(\Delta y > 0) - N(\Delta y < 0)}{N(\Delta y > 0) + N(\Delta y < 0)} = 0.078(9) \quad \Delta y = y_t - y_{\bar{t}}$$

TOP AFB FROM TEVATRON

CDF collaboration (CDF Note 10807)

CDF Run II Preliminary L = 8.7 fb⁻¹

Parton Level	NLO (QCD+EW)	$t\bar{t}$	5.3 fb ⁻¹	8.7 fb ⁻¹
$ \Delta y $	A_{FB}		$A_{\text{FB}} (\pm[\text{stat.}+\text{syst.}])$	$A_{\text{FB}} (\pm[\text{stat.}+\text{syst.}])$
Inclusive	0.066		0.158 ± 0.074	0.162 ± 0.047
< 1.0	0.043		0.026 ± 0.118	0.088 ± 0.047
≥ 1.0	0.139		0.611 ± 0.256	0.433 ± 0.109
Parton Level	NLO (QCD+EW)	$t\bar{t}$	5.3 fb ⁻¹	8.7 fb ⁻¹
$M_{t\bar{t}}$	A_{FB}		$A_{\text{FB}} (\pm[\text{stat.}+\text{syst.}])$	$A_{\text{FB}} (\pm[\text{stat.}+\text{syst.}])$
< 450 GeV/c ²	0.047		-0.116 ± 0.153	0.078 ± 0.054
≥ 450 GeV/c ²	0.100		0.475 ± 0.112	0.296 ± 0.067

 After the increase in luminosity, the discrepancy from the SM prediction is still nearly 3σ

A_{FB}^t and Some NP models

s-channel

EFT

Ferrario, Rodrigo
Axigluon
0809.3353

Frampton, Shu, Wang
Axigluon
0911.2955

Q-H.Cao et al
Effective coupling
(G', Z', W', H^0, H^+)
1003.3461

Ferrario, Rodrigo
chiral G'
0906.5541

Antunan, Kuhn, Rodrigo
Axigluon
0709.1652

Djouadi, Moreau, Richard, Singh
KK Gluon
0906.0604

Jung, Ko, Lee, Nam
EFT
0912.1105

2007, 2008

2009

2010, 2011

Jung, Murayama, Pierce, Wells
FCNC Z-prime
0907.4112

Shu, Tait, Wang
Color Sextet/triplet scalar
0911.3237

Xiao, Wang, Zhu,
NLO QCD to Z-prime
1006.2510

Cheung, Keung, Yuan
FC W-prime
0908.2589

Arhrib, Benbrik, Chen
Color Sextet/triplet scalar
0911.4875

Yan, Wang, Shao, Li
NLO QCD to W-prime
1110.6684

J. Cao, Heng, Wu, Yang
 \mathcal{R} -SUSY and TC2
0912.1447

Shao, Li, et al
NLO QCD to EFT
1107.4012

t-channel

NLO QCD

MORE INSIGHT (INTO THESE MODELS) FROM TEVATRON?

 **D0** collaboration measured the lepton charge asymmetry

SM: $A_{FB}^t = 0.051 \pm 0.001$


D0: $A_{FB}^t = 0.196 \pm 0.065$

$$A_{FB}^\ell = 0.021 \pm 0.001$$

$$A_{FB}^\ell = 0.152 \pm 0.040$$

$$\frac{A_{FB}^\ell}{A_{FB}^t} \sim 40\%$$

$$\frac{A_{FB}^\ell}{A_{FB}^t} \sim 75\%$$

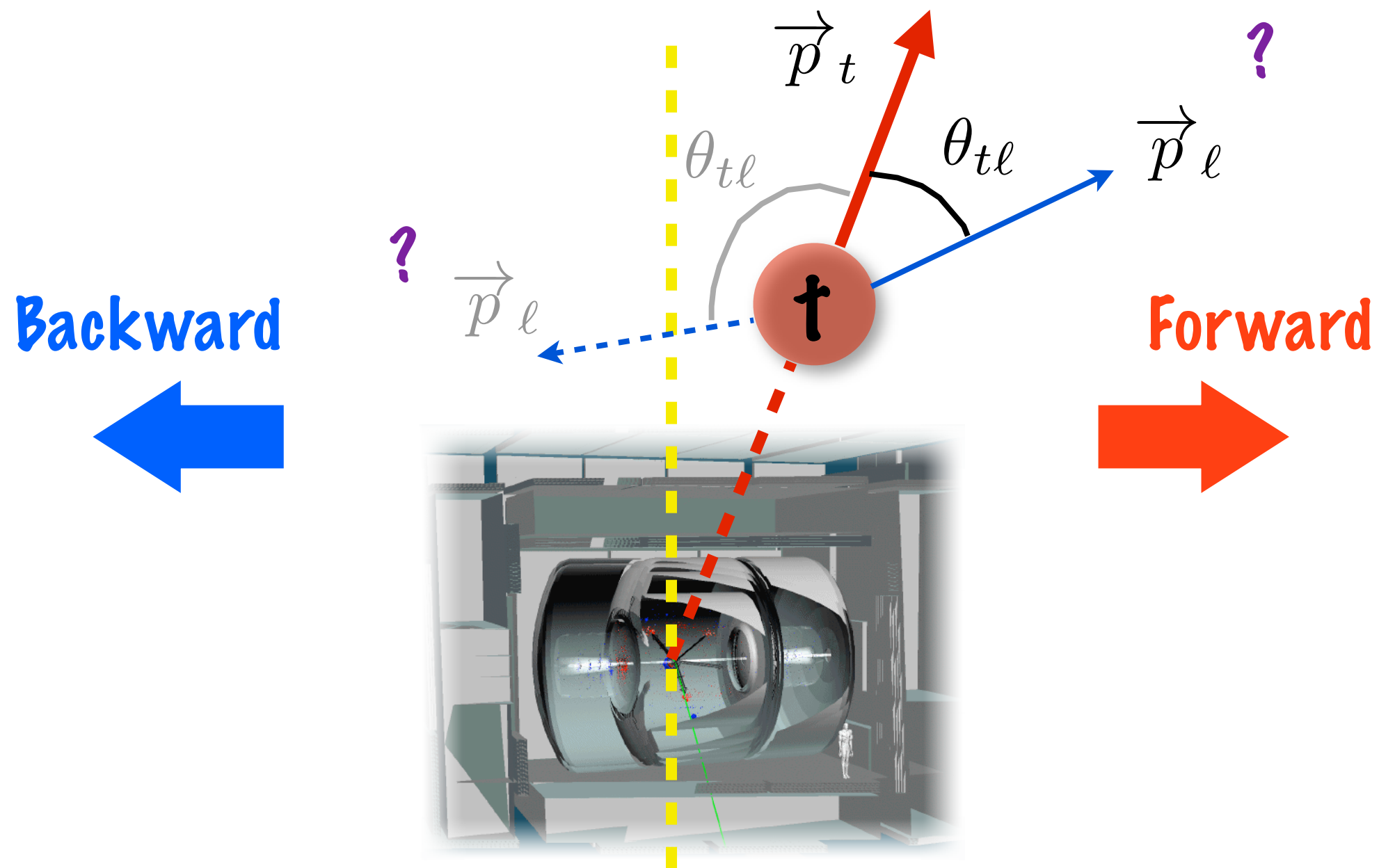
 **Theoretically - for the same top quark momentum distribution, a left-handed top quark and a right-handed top quark leads to a different lepton charge asymmetry**

 **How can we relate AFB(lepton) and AFB(top)? Show here that AFB(lepton) provides independent insight into new physics models**

From top AFB to lepton AFB

TOP LEPTONIC DECAY

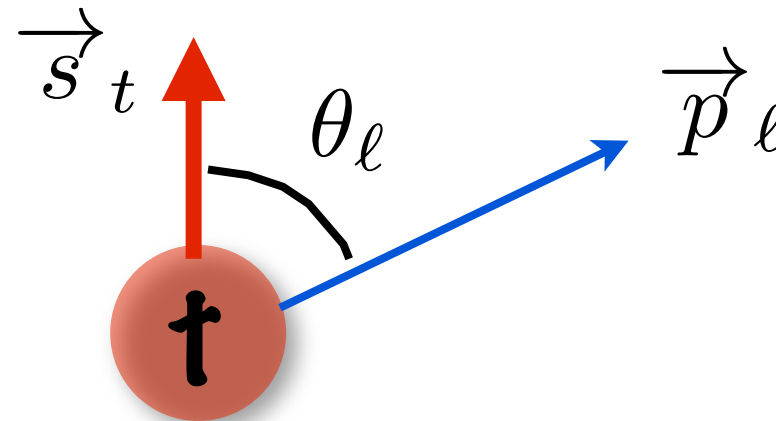
❏ If we know the momentum and spin direction of the top quark, what is the probability that the decay lepton is in the forward (backward) region in the laboratory frame?



TOP LEPTONIC DECAY

Recall - in the top quark rest frame

$$\frac{d\Gamma}{\Gamma d\cos\theta_\ell} = \frac{1 + \cos\theta_\ell}{2}$$

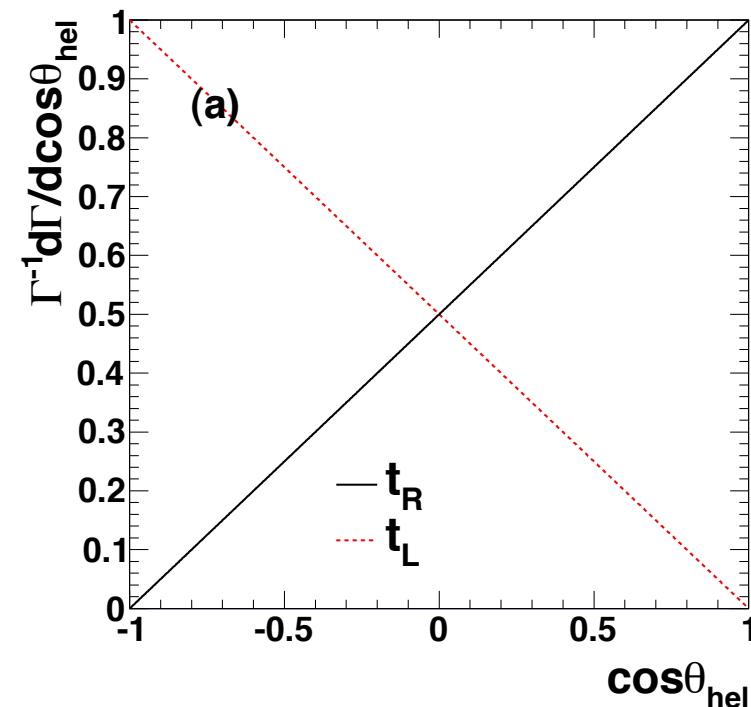


In the helicity basis, the momentum direction of the lepton from a left(right)-handed top quark is opposite (same) as the top quark spin direction

$$\frac{d\Gamma}{\Gamma d\cos\theta_{\text{hel}}} = \frac{1 + \lambda_t \cos\theta_{\text{hel}}}{2}$$

$\lambda_t = +1$ — positive helicity, right-handed

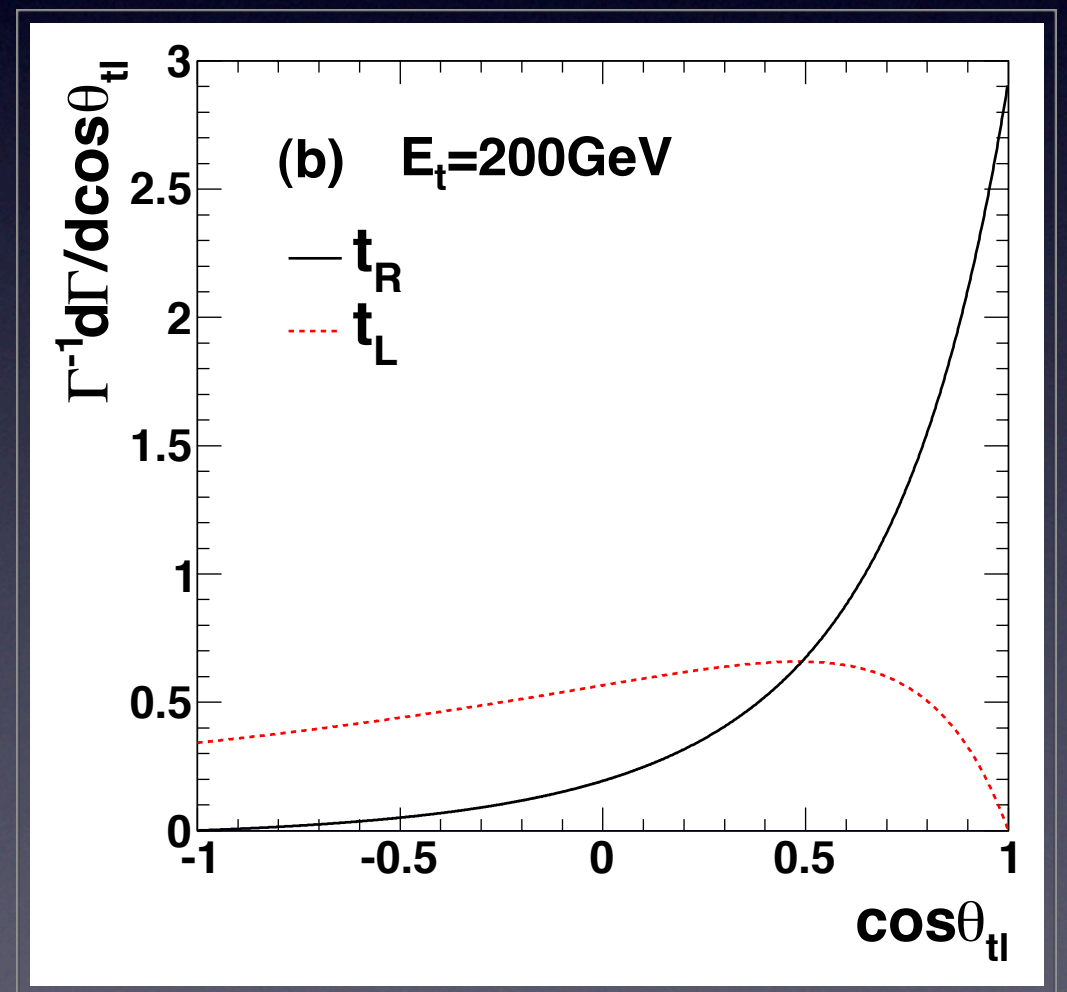
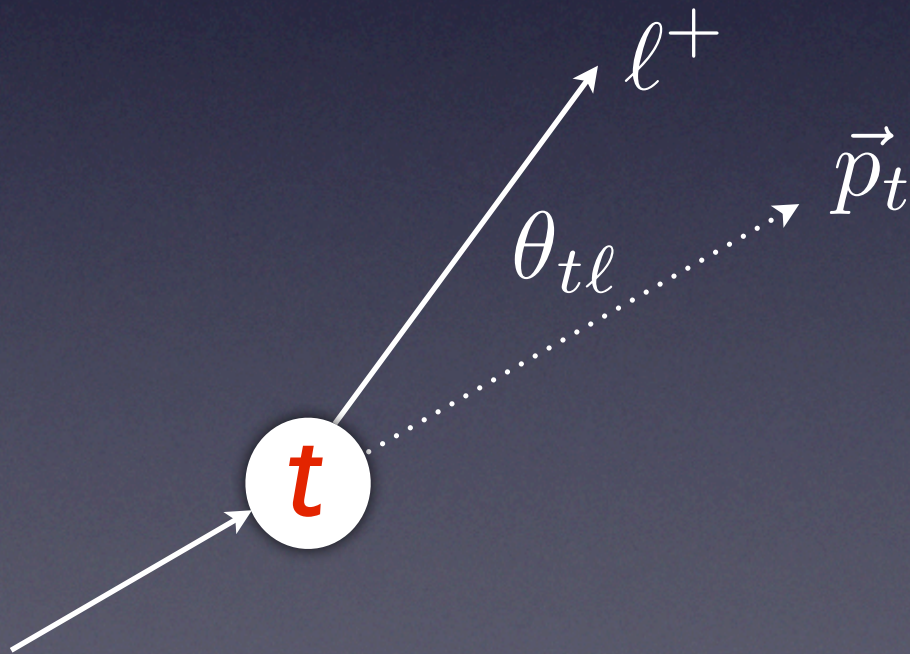
$\lambda_t = -1$ — negative helicity, left-handed



Charged lepton distribution

- When the top quark is boosted along the spin direction, the angular distribution becomes

$$\frac{d\Gamma}{\Gamma d\cos\theta_{t\ell}} = \frac{1 - \beta \cos\theta_{t\ell} + \lambda_t (\cos\theta_{t\ell} - \beta)}{2\gamma^2 (1 - \beta \cos\theta_{t\ell})^3}$$



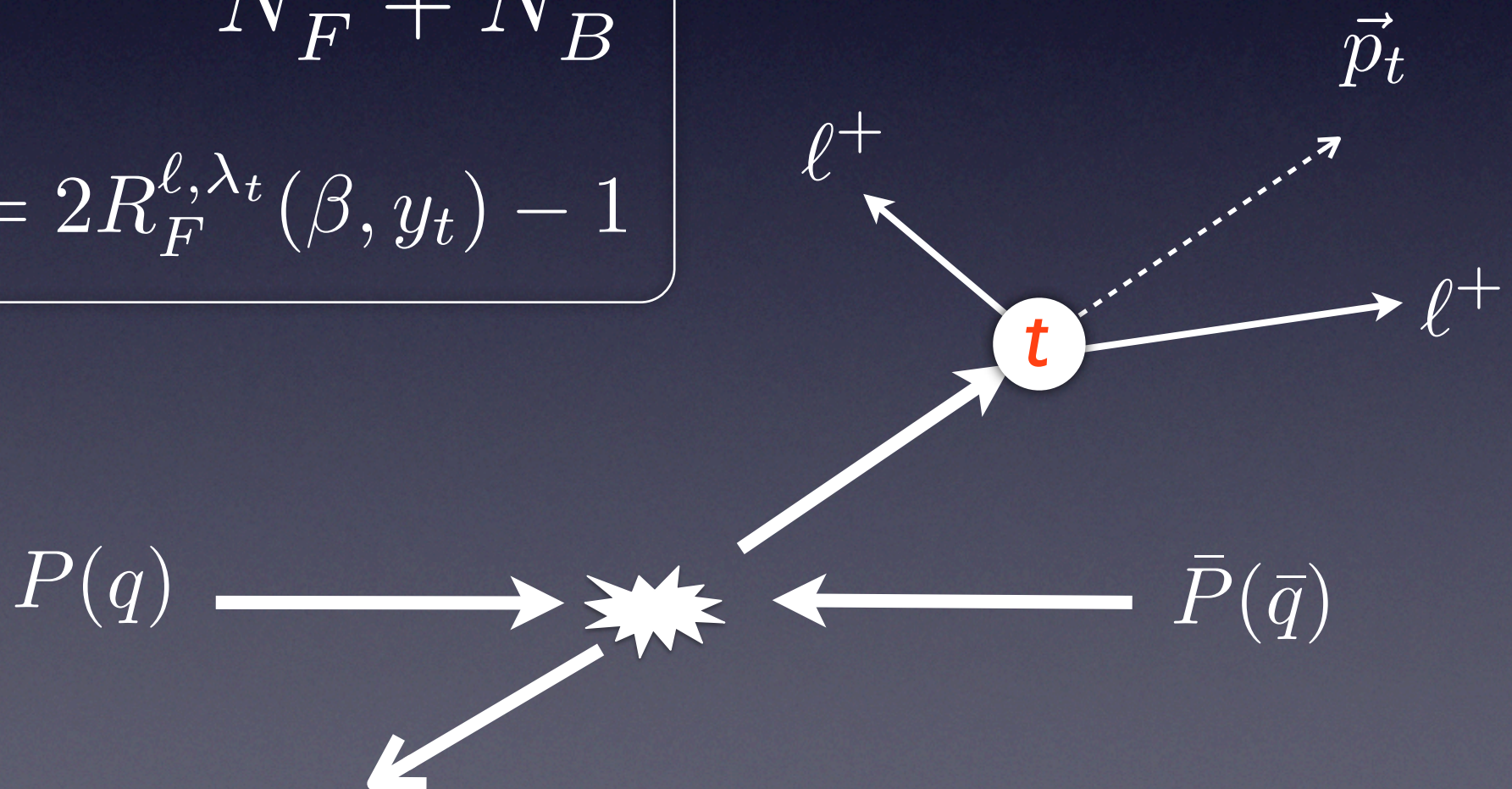
Next: rotate to the laboratory frame

A_{FB}^ℓ dependence on top kinematics

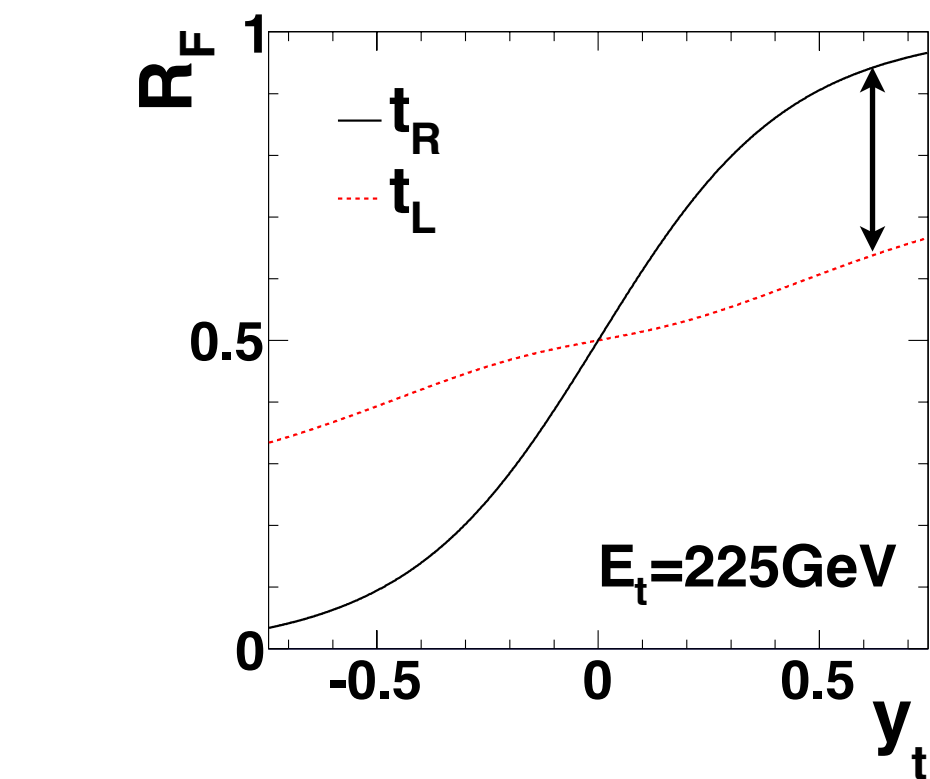
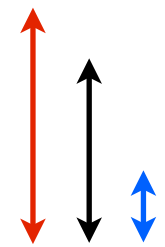
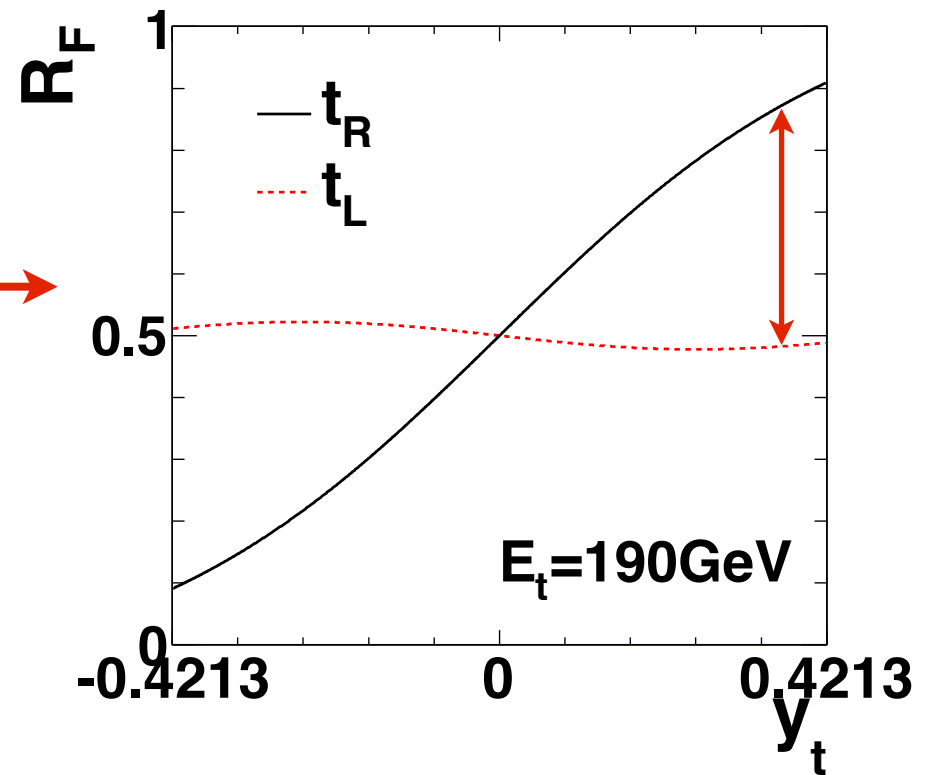
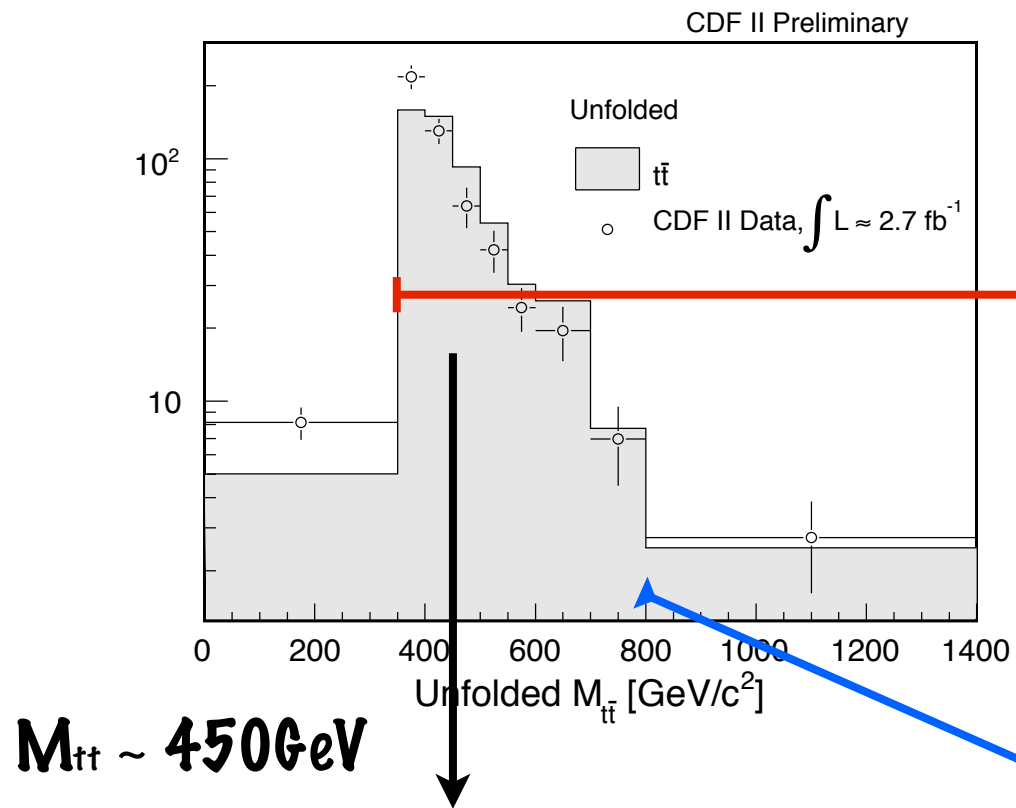
- Probability that the decay lepton is in the forward region of detector for a top-quark (β, y_t, λ_t) is encoded in an analytic expression [arXiv:1201.1790](https://arxiv.org/abs/1201.1790)

$$R_F^{\ell, \lambda_t}(\beta, y_t) = \frac{N_F^\ell}{N_F^\ell + N_B^\ell}$$

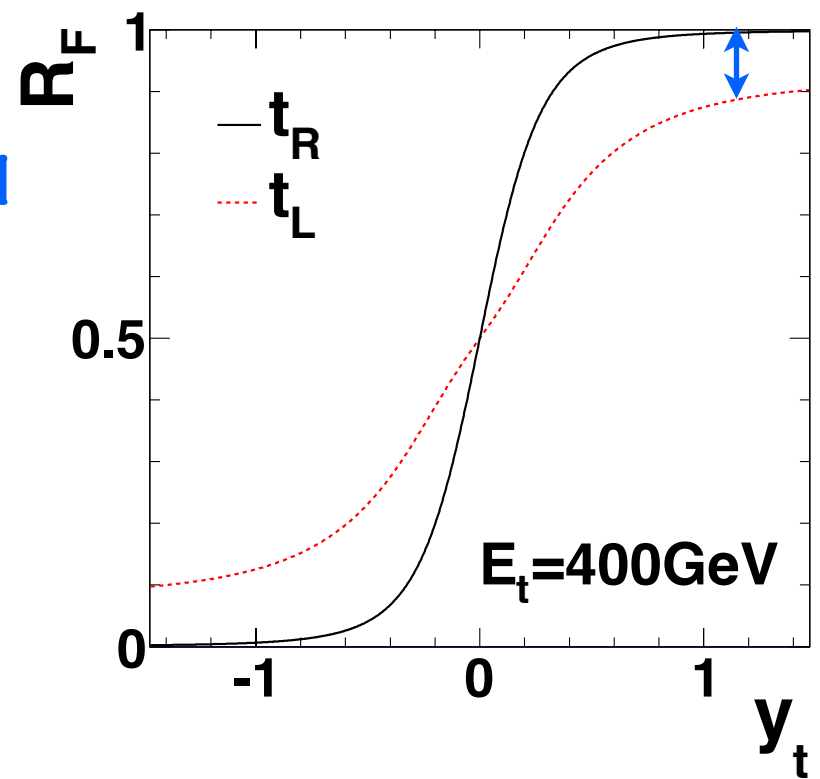
$$A_{FB}^{\ell, \lambda_t}(\beta, y_t) = 2R_F^{\ell, \lambda_t}(\beta, y_t) - 1$$




TOP LEPTONIC DECAY



Highly boosted



FROM TOP AFB TO LEPTON AFB

 When we know the top quark AFB and the final state $t\bar{t}$ distribution, how to estimate the lepton AFB? Convolution of the function R with the top quark momentum spectrum is required

$$n_{\ell}^F = \frac{1}{\sigma} \sum_{\lambda=+,-} \int R_F^{\lambda}(\beta, y_t) \frac{d^2\sigma|_{\lambda_t=\lambda}}{d\beta dy_t} d\beta \wedge dy_t$$

$$n_{\ell}^B = \frac{1}{\sigma} \sum_{\lambda=+,-} \int [1 - R_F^{\lambda}(\beta, y_t)] \frac{d^2\sigma|_{\lambda_t=\lambda}}{d\beta dy_t} d\beta \wedge dy_t$$

$$\begin{aligned} A_{FB}^{\ell} &= n_{\ell}^F - n_{\ell}^B \\ &= \frac{1}{\sigma} \sum_{\lambda=+,-} \int [2R_F^{\lambda}(\beta, y_t) - 1] \frac{d^2\sigma|_{\lambda_t=\lambda}}{d\beta dy_t} d\beta \wedge dy_t \end{aligned}$$

FROM TOP AFB TO LEPTON AFB

- For the SM, we have equal number of left-handed and right-handed top quarks in the final state.
- The dominant contribution is from the top quarks with energy around 200GeV,
 - left-handed: $2R_{F-1} \approx 0$
 - right-handed: $2R_{F-1} \approx 0.8$

$$\frac{A_{FB}^{\ell}}{A_{FB}^t} \approx \frac{0 + 0.8}{2} = 40\%$$

WHAT DO WE LEARN FROM D0 LEPTON AFB DATA?

The D0 result

$$\text{D0: } A_{FB}^t = 0.196 \pm 0.065$$

$$A_{FB}^\ell = 0.152 \pm 0.040$$

$$\frac{A_{FB}^\ell}{A_{FB}^t} \sim 75\%$$

Data require larger $2R_F-1$ than the SM

Two possibilities:

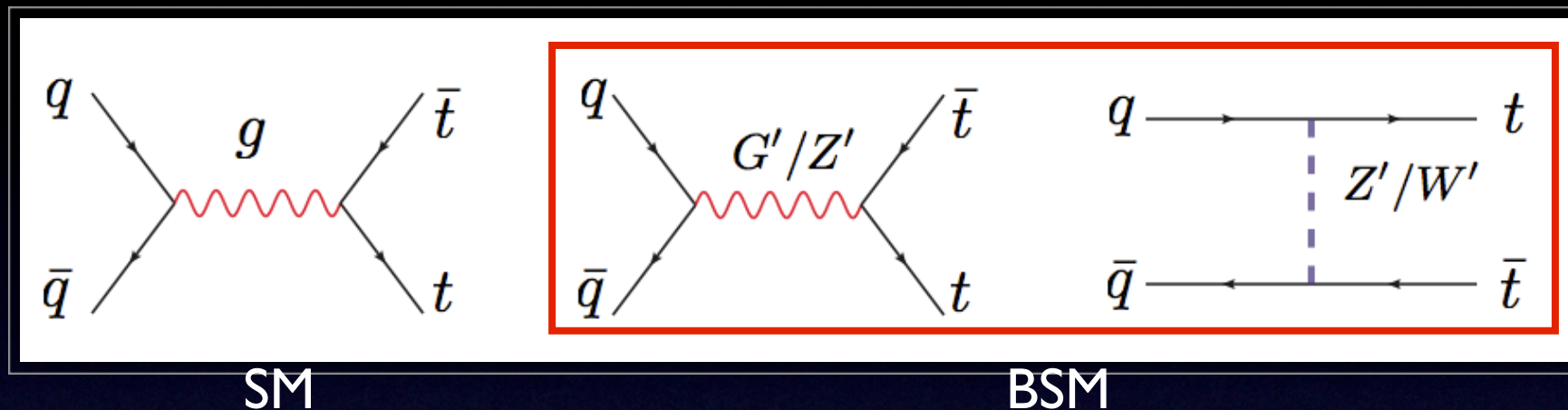
(1) If the contribution to AFB is dominated by the threshold region, the new physics must produce **more right-handed top quarks**

(2) Or the contribution to AFB must be from highly boosted region. But...

III. Two examples of New Physics Models

New physics models

NP models are divided into two classes



- **s-channel: extra octet vector gluon (axigluon is an example)**

Small couplings to the first two generations: dijet constraints at 7 TeV

Large couplings to third generation: to generate large A_{FB}

Heavy resonances: $t\bar{t}$ invariant mass spectrum

Very broad width: to interfere with the SM channel

- **t-channel: flavor changing interaction**

color singlet: Z' -u-t (ϕ -u-t)

W'^+ -d-t (ϕ^+ -d-t)

color sextet or triplet

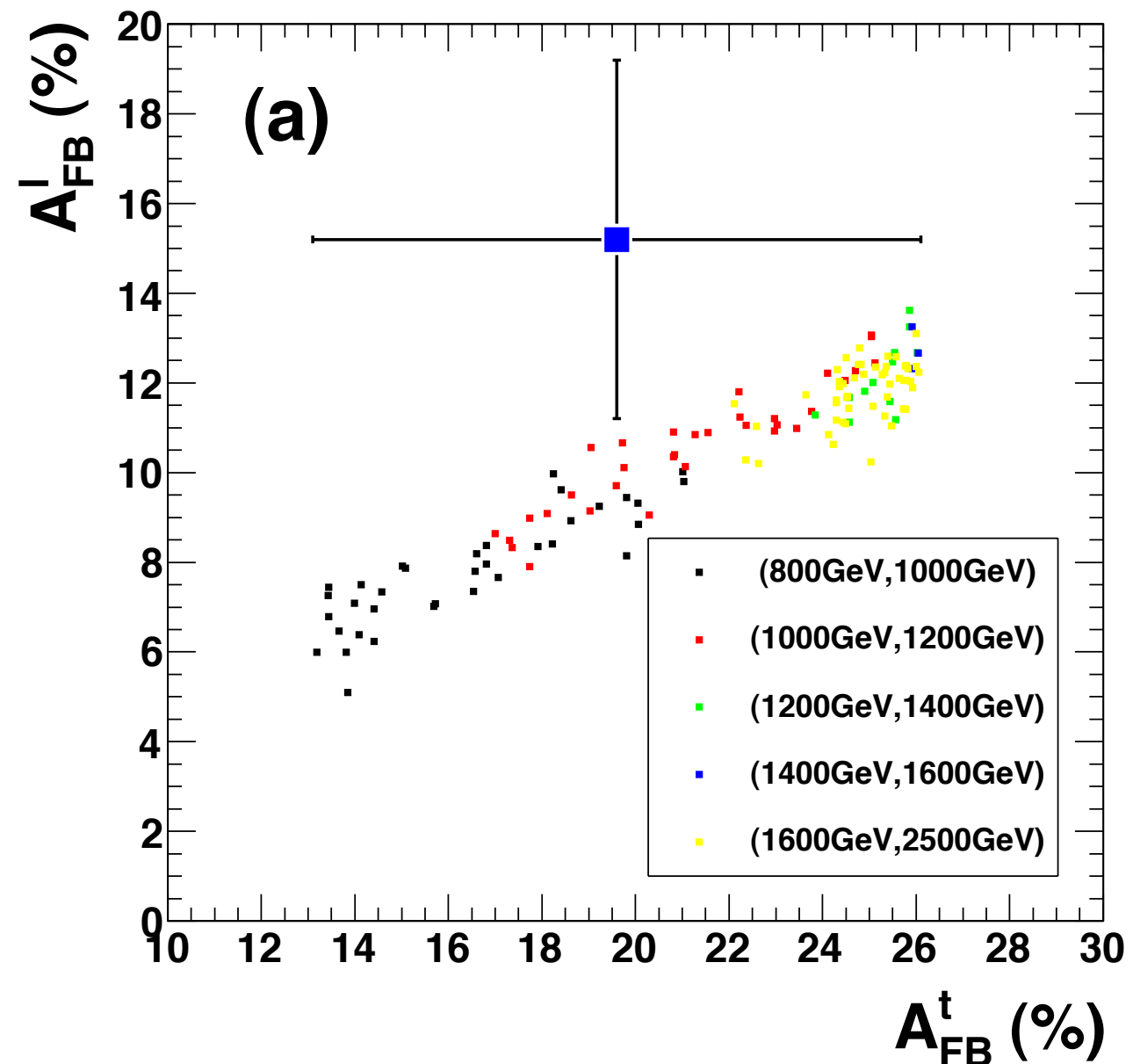
(I). AXIGLUON

☞ To determine parameters, require top AFB and the total cross section to fit within 1σ . Compute the correlation between top and lepton AFB:

☞ Pure pseudo-vector interaction (equal left and right tops)

☞ An axigluon produces a small increase in the

$$A_{FB}^{\ell} \simeq 0.47 \times A_{FB}^t + 0.25$$



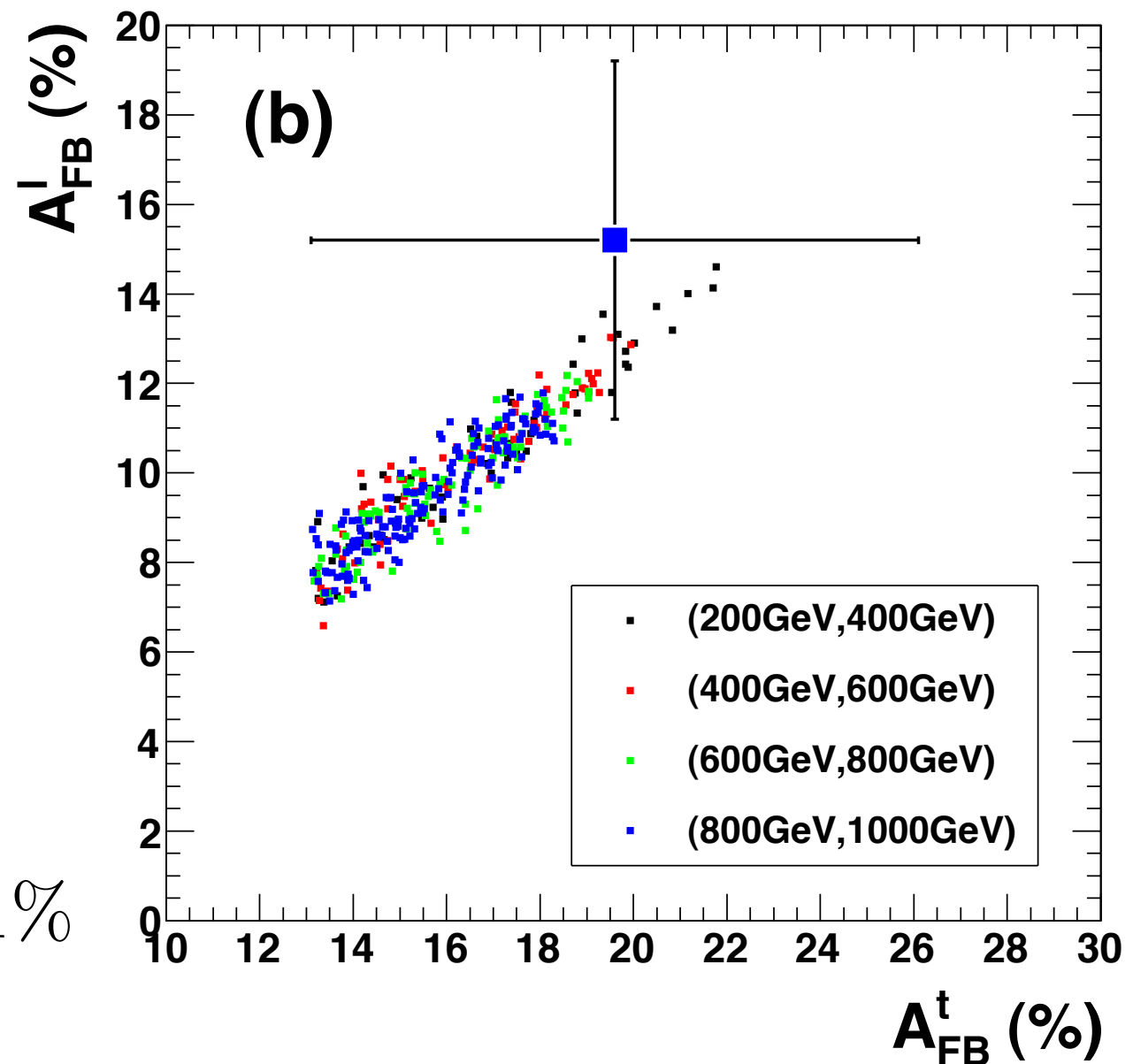
(II). W'

☞ To determine parameters, require top AFB and the total cross section to fit within 1σ . Compute the correlation between top and lepton AFB:

☞ Purely right-handed FC interaction

☞ W' model produces a large increase in the lepton AFB.

$$A_{FB}^{\ell} \simeq 0.75 \times A_{FB}^t - 2.1\%$$



SUMMARY ON top AFB and lepton AFB

- ☒ Owing to the spin correlation in top quark decay, the top AFB and lepton AFB are strongly positively correlated for **right-handed** top quarks.
- ☒ For **left-handed** top quarks, the correlation depends on the energy of the top quark.
- ☒ Data from the D0 collaboration show a relatively large positive correlation.
- ☒ **A model of new physics that predicts more right-handed top quarks is favored**
- ☒ *** Important to measure both top and lepton AFB ***

Phys. Rev. Lett. 108, 072002 (2012)

OUTLOOK

 The $D0$ experimental uncertainty is large

$$\frac{A_{FB}^{\ell}}{A_{FB}^t} \Big|_{D0} = 78 \pm 33\%$$

 Analysis of more data from the Tevatron could reduce this uncertainty

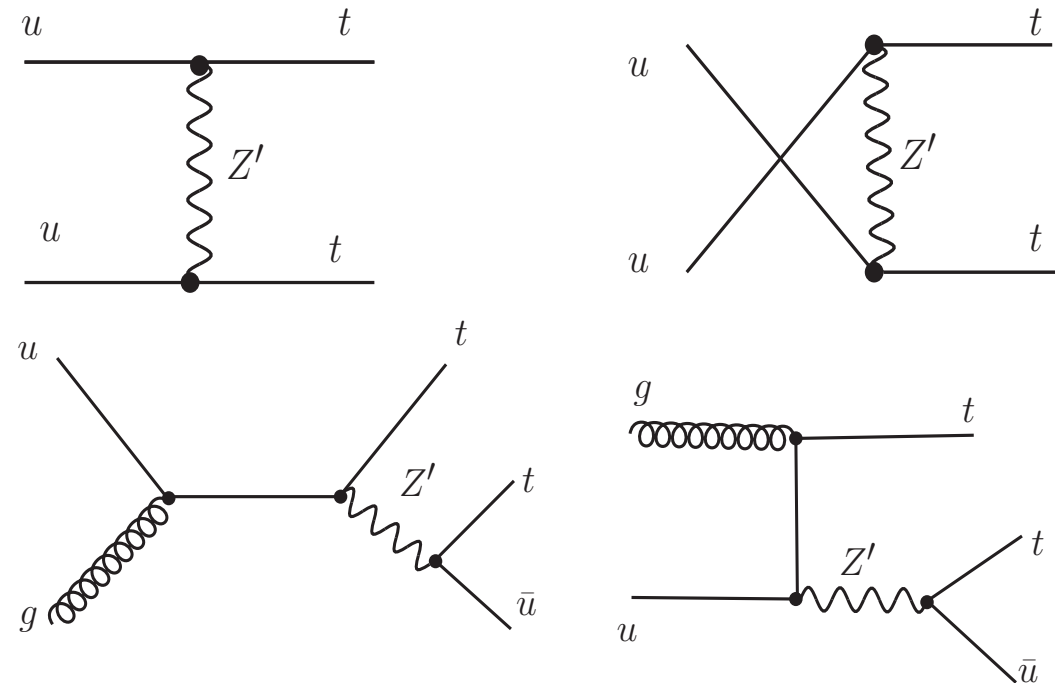
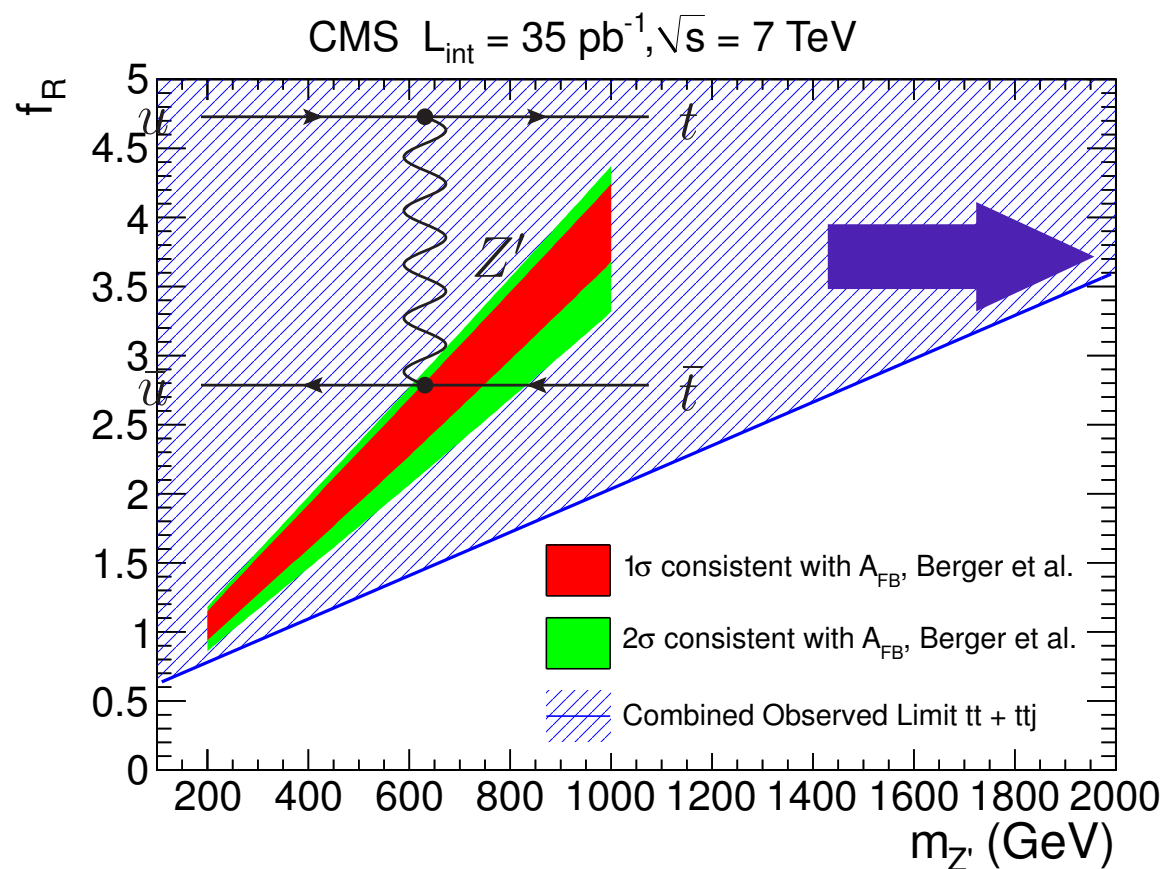
What about the LHC?



IV. LHC Implications

IMPLICATIONS OF MODELS AT THE LHC?

- ☑ Same sign top pair production
- ☑ Prediction based on Tevatron analysis; checked by CMS
- ☑ Minimal FCNC Z' model is disfavored (PRL 106, 201801, E Berger, Q-H Cao, C-R Chen, CS Li and Hao Zhang; JHEP08(2011)005, CMS collaboration)



LHC RAPIDITY ASYMMETRIES

It is more difficult to measure AFB at the LHC

(1) pp collider

(2) gg initial state dominant -- yields no asymmetry

(3) for the qqbar initial state process, an asymmetry persists, but its effect is diluted by the large gg contribution

Define LHC asymmetries:

$$A_C^{t\bar{t}} \equiv \frac{N(|y_t| - |y_{\bar{t}}| > 0) - N(|y_t| - |y_{\bar{t}}| < 0)}{N(|y_t| - |y_{\bar{t}}| > 0) + N(|y_t| - |y_{\bar{t}}| < 0)}$$

$$A_C^{e\bar{e}} \equiv \frac{N(|y_{e^+}| - |y_{e^-}| > 0) - N(|y_{e^+}| - |y_{e^-}| < 0)}{N(|y_{e^+}| - |y_{e^-}| > 0) + N(|y_{e^+}| - |y_{e^-}| < 0)}$$

LHC RAPIDITY ASYMMETRY DATA

The results from the two collaborations are different, even if they are consistent within the quoted uncertainties

$$A_C^{t\bar{t}} = 0.029 \pm 0.018(\text{stat.}) \pm 0.014(\text{syst.})$$




$$A_C^{\ell\ell} = 0.023 \pm 0.012(\text{stat.}) \pm 0.008(\text{syst.})$$

ATLAS-CONF-2012-057

$$A_C^{t\bar{t}} = 0.004 \pm 0.010(\text{stat.}) \pm 0.011(\text{syst.})$$

CMS Collaboration, arXiv: 1207.0065

$$A_C^{t\bar{t}}^{\text{SM}} = 0.006, \quad A_C^{\ell\ell}^{\text{SM}} = 0.004 \quad \text{MC@NLO}$$

-  We can obtain an estimate of AFB (ttbar) at the LHC by extrapolating from the Tevatron and applying the gg dilution
-  The LHC value should be about 10% of the Tevatron
-  ATLAS value agrees with the Tevatron asymmetry

LHC RAPIDITY ASYMMETRY DATA

**CMS result on AFB ($t\bar{t}$ bar) agrees with SM; no need for NP.
ATLAS data exceed SM**

$$A_C^{t\bar{t}} = 0.029 \pm 0.018(\text{stat.}) \pm 0.014(\text{syst.})$$




$$A_C^{\ell\ell} = 0.023 \pm 0.012(\text{stat.}) \pm 0.008(\text{syst.})$$

ATLAS-CONF-2012-057

$$A_C^{t\bar{t}} = 0.004 \pm 0.010(\text{stat.}) \pm 0.011(\text{syst.})$$

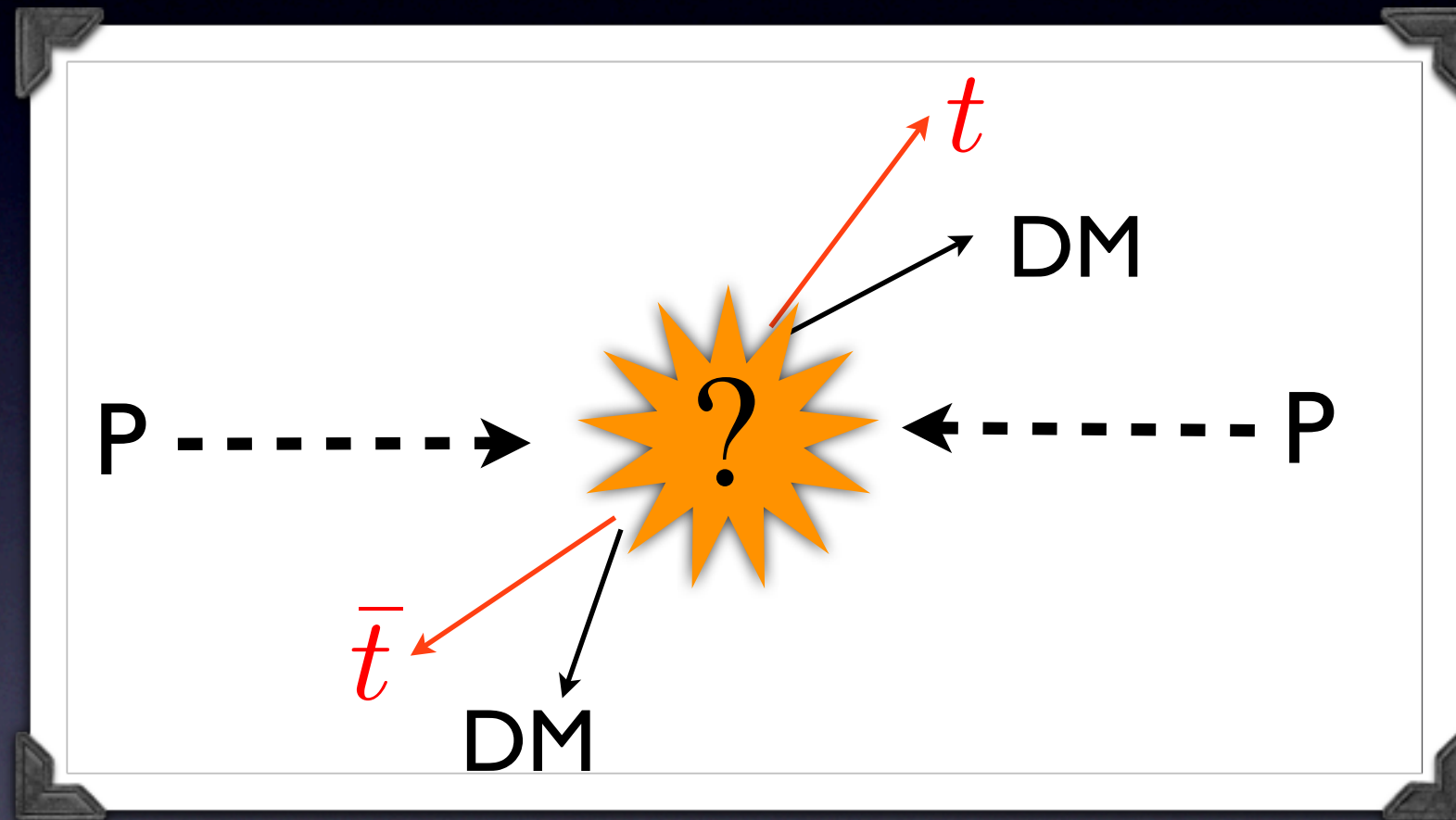
CMS Collaboration, arXiv: 1207.0065

$$A_C^{t\bar{t}}^{\text{SM}} = 0.006, \quad A_C^{\ell\ell}^{\text{SM}} = 0.004 \quad \text{MC@NLO}$$

-  We can obtain an estimate of AFB ($t\bar{t}$ bar) at the LHC by extrapolating from the Tevatron and applying the gg dilution
-  The LHC value should be about 10% of the Tevatron
-  ATLAS value agrees with the Tevatron asymmetry

V. New Physics Models with DM candidates

Berger, Qing-Hong Cao, Jianghao Yu, and Hao Zhang,
arXiv:1207.1101

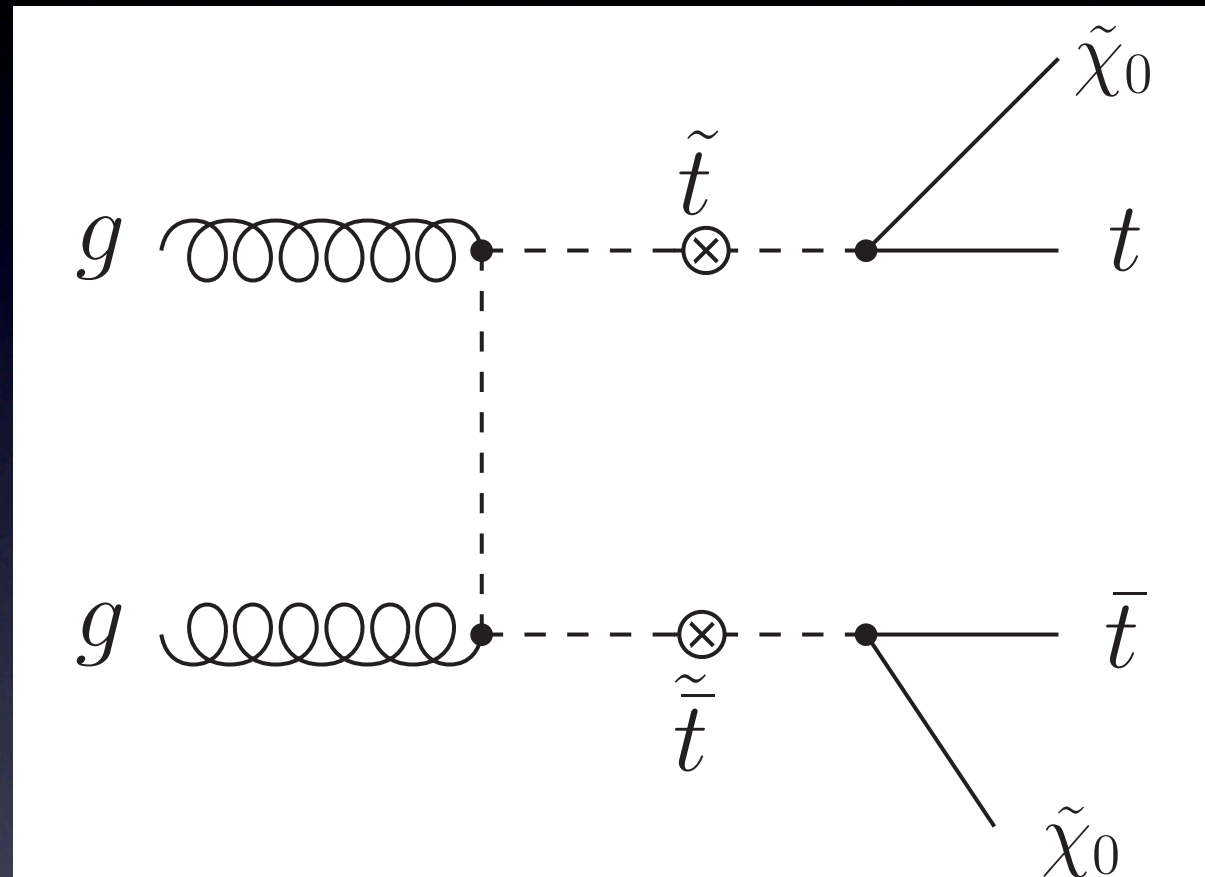


Measuring top-quark polarization *without*
reconstructing top-quark kinematics

NP signature: Top antitop pair plus MET

- top squark pair production in the MSSM

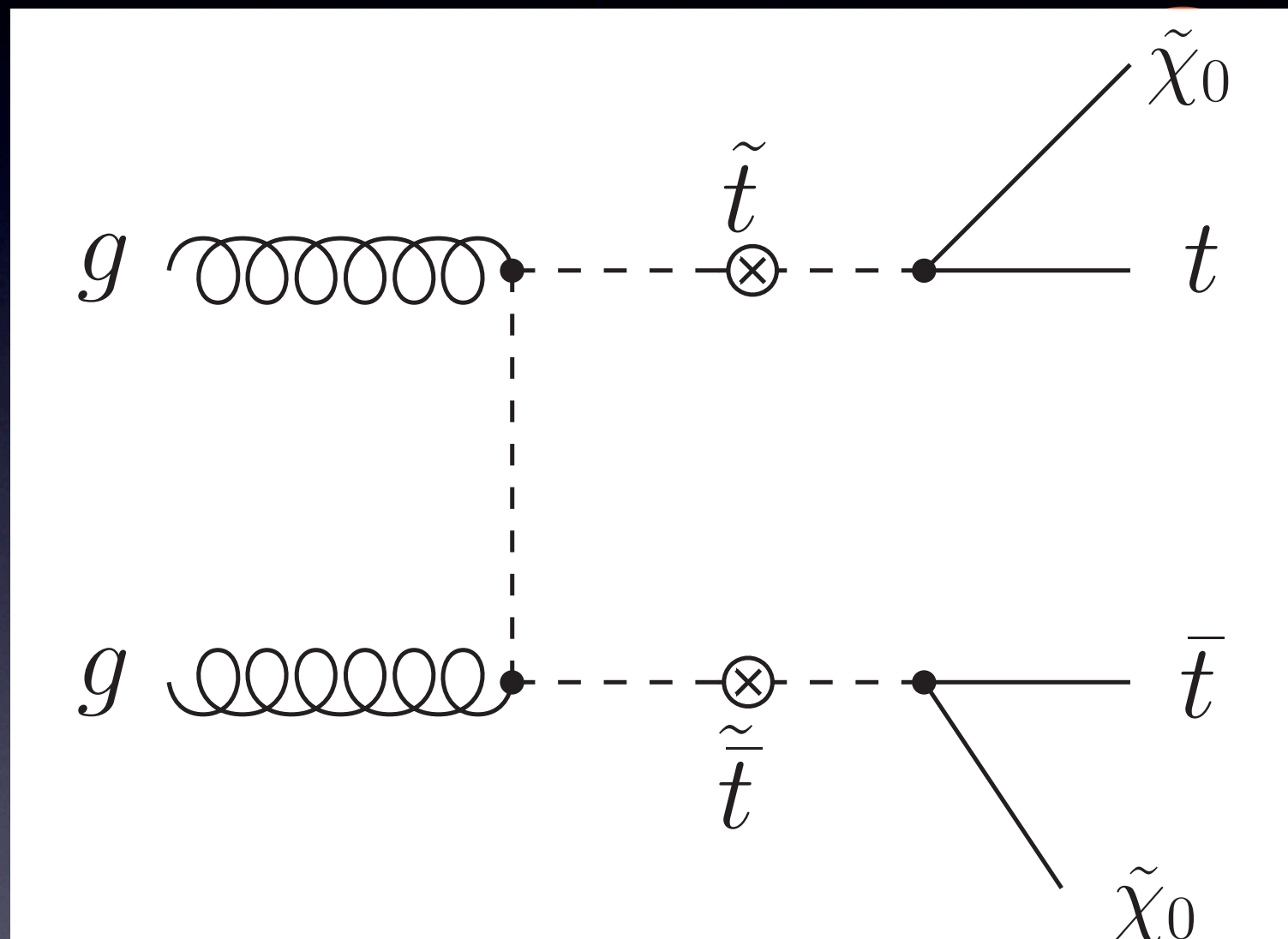
Hall, Pinner and Ruderman, 1112.2703



- ▶ Light top squark is “preferred” to raise m_h to 125 GeV in the maximal mixing scenario.
- ▶ Top quark polarization could shed light on the top squark mixing matrix.

Difficulty in NP signature of $t\bar{t}$ plus MET

- Not possible to reconstruct top quark in the leptonic-decay mode.
Angular distribution of the charged-lepton cannot be used.



assume $p_{\bar{t}}$
is known

10 unknowns
(neutrino from
top decay, 2 DM)
-2 from MET

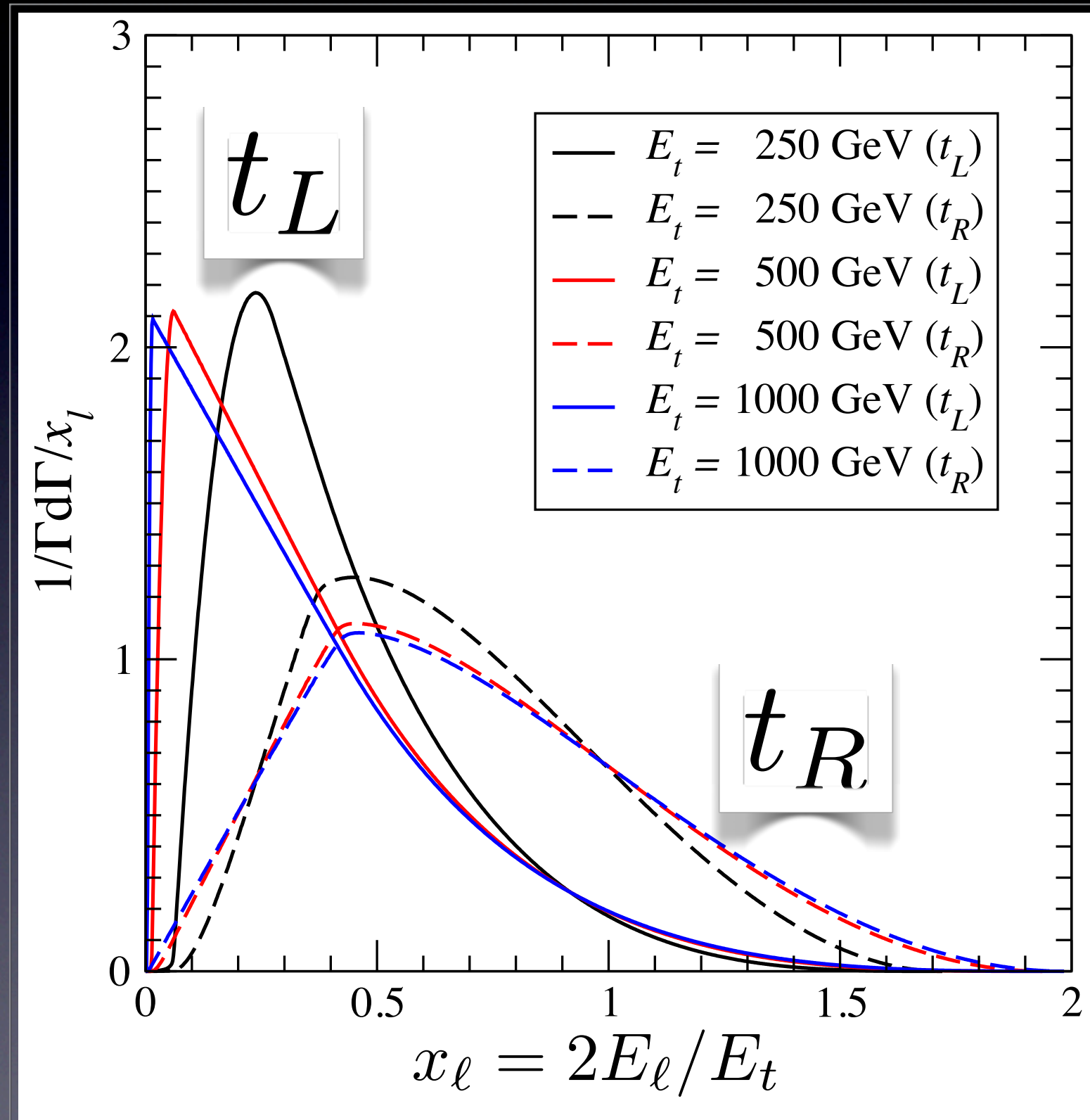


Not enough
constraints

Still possible to measure the top quark polarization

Lepton energy and top quark polarization

★ Lepton energy distribution is sensitive to top quark polarization.

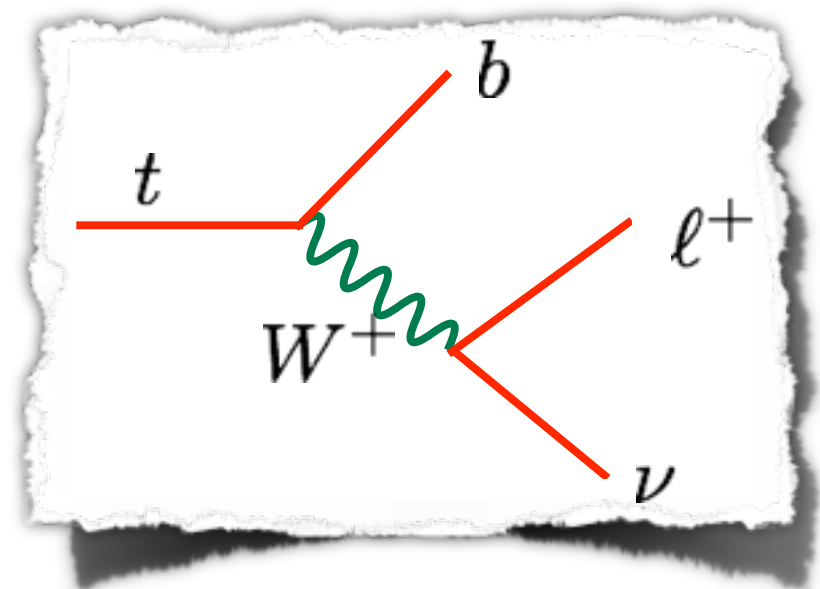


Conclusion

Summary

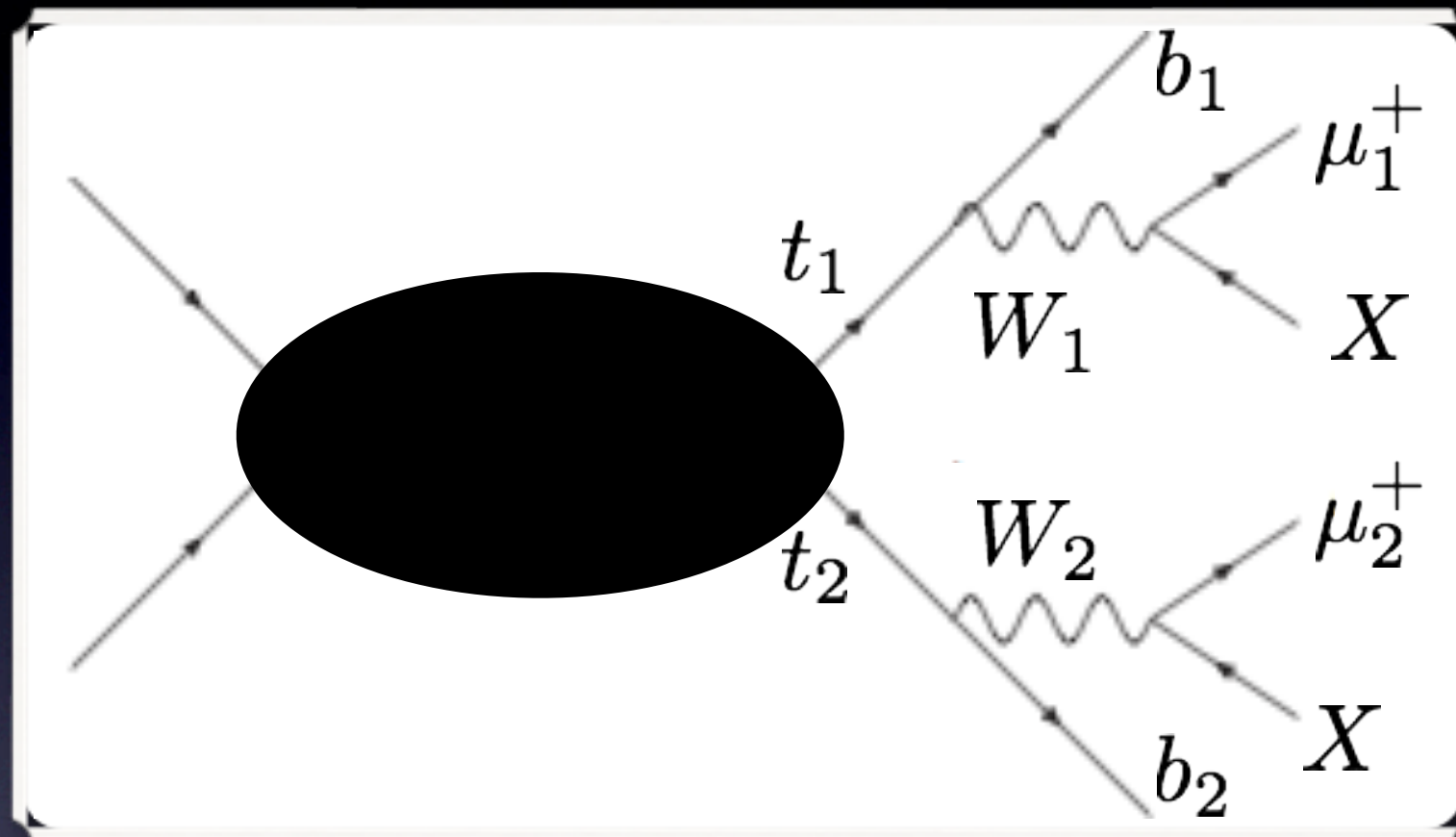
- Top-quark polarization provides richer insight into BSM physics
- Lepton AFB and top AFB are connected by the top quark and charged lepton spin correlation; D0 data suggest BSM with right-handed couplings. Data need confirmation
- LHC CMS data on the asymmetry show evidence of tension with the Tevatron, independent of models, but ATLAS data are consistent with the Tevatron
- Lepton energy distribution can be exploited to measure top quark polarization, especially in new physics models with dark matter candidates

Back up



Full kinematic reconstruction

★ Four unknowns and four on-shell conditions



6 unknowns
-2 from MET

$$\begin{aligned}
 m_{W_1}^2 &= (p_{\mu_1} + p_{\nu_1})^2 \\
 m_{W_2}^2 &= (p_{\mu_2} + p_{\nu_2})^2 \\
 m_{t_1}^2 &= (p_{W_1} + p_{b_1})^2 \\
 m_{t_2}^2 &= (p_{W_2} + p_{b_2})^2
 \end{aligned}$$

Quartic equation

(correct l - b pairing is necessary)

$$p_x^4(\nu_1) + a p_x^3(\nu_1) + b p_x^2(\nu_1) + c p_x(\nu_1) + d = 0$$

~~Two complex~~, two real solutions

It is “easy” to show ...

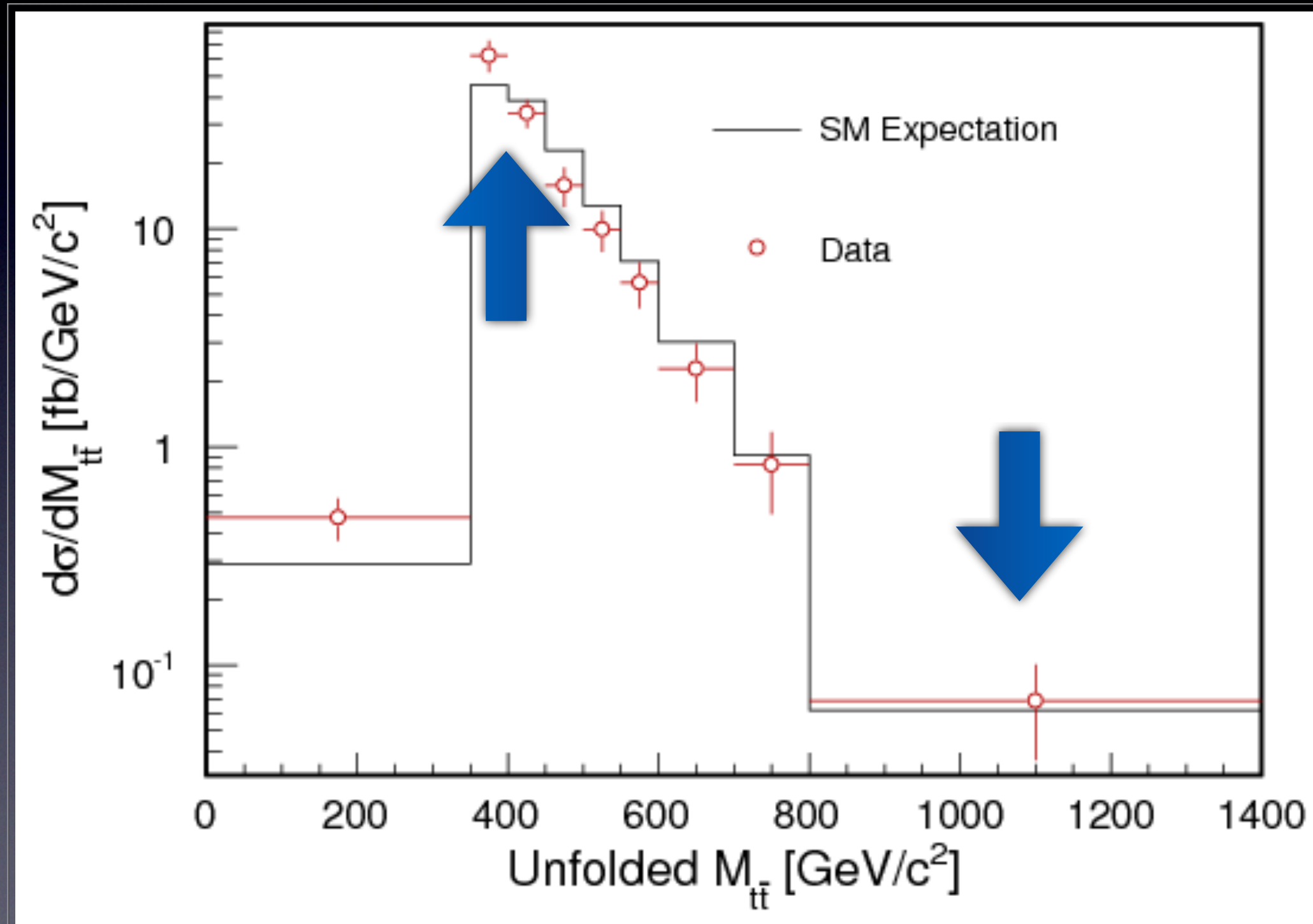
- After rotation of frames, derive the probability that lepton is in the forward region of the detector for a top quark top quark with (β, y_t, λ_t) is

$$R_F^{\ell, \lambda_t}(\beta, y_t)$$

$$= \begin{cases} \frac{1}{2} + \frac{1}{2(1 + \gamma^{-2} \coth^2 y_t)^{1/2}} + \frac{\lambda_t \coth^2 y_t}{4\beta\gamma^2 (1 + \gamma^{-2} \coth^2 y_t)^{3/2}}, & (y_t > 0) \\ \frac{1}{2} - \frac{1}{2(1 + \gamma^{-2} \coth^2 y_t)^{1/2}} - \frac{\lambda_t \coth^2 y_t}{4\beta\gamma^2 (1 + \gamma^{-2} \coth^2 y_t)^{3/2}}, & (y_t < 0) \end{cases}$$

Invariant mass spectrum of top quark pair

CDF, Phys.Rev.Lett. 102 (2009) 222003



A_{FB}^{ℓ} versus A_{FB}^t

D0: $A_{FB}^t = 0.196 \pm 0.065$

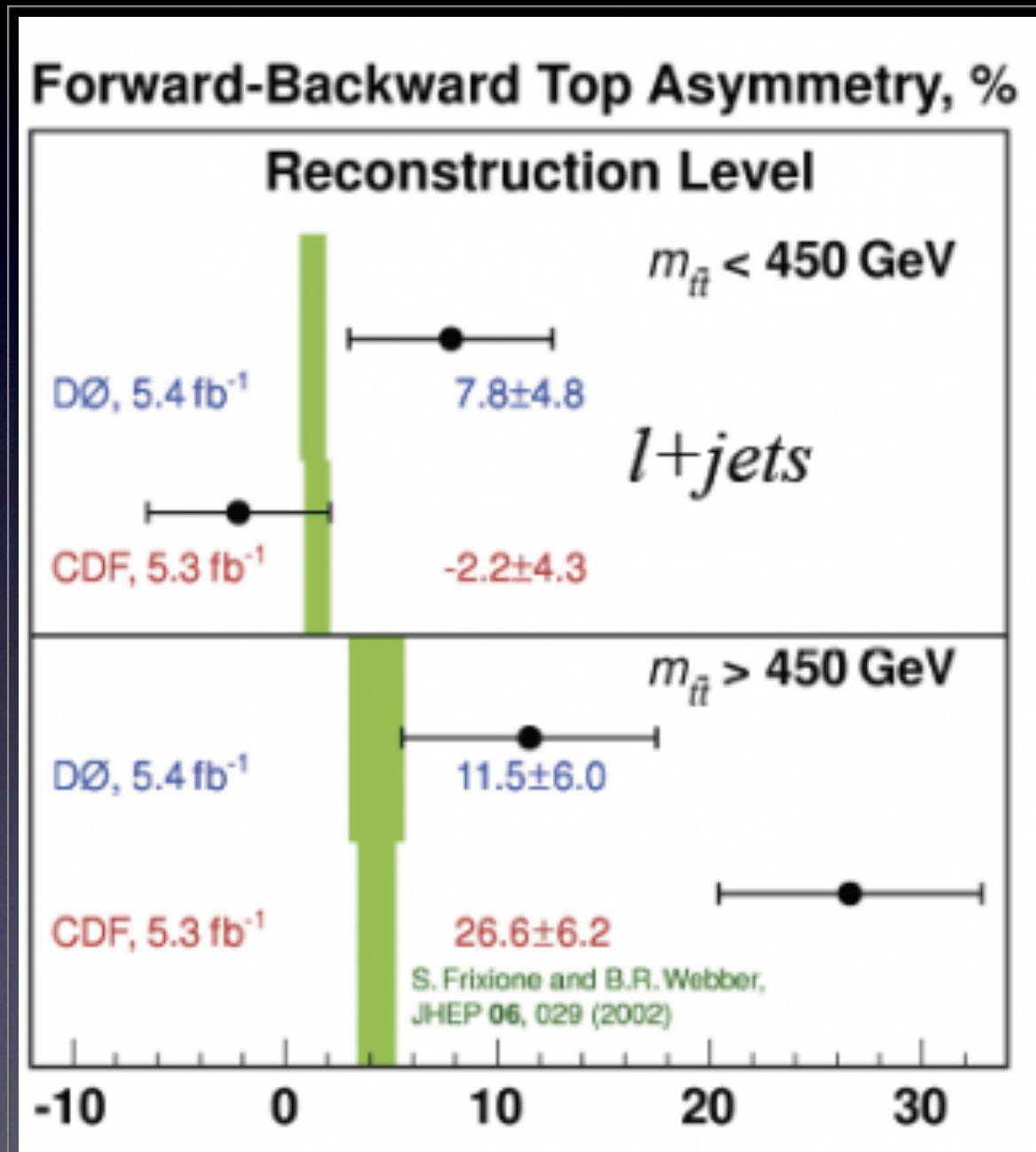
$A_{FB}^{\ell} = 0.152 \pm 0.040$

$$\left. \frac{A_{FB}^{\ell}}{A_{FB}^t} \right|_{D0} \sim \frac{3}{4}$$

SM: $A_{FB}^t = 0.051 \pm 0.001$

$A_{FB}^{\ell} = 0.021 \pm 0.001$

$$\left. \frac{A_{FB}^{\ell}}{A_{FB}^t} \right|_{SM} \sim \frac{1}{2}$$



TWO EXAMPLES (I). AXIGLUON

❏ The interaction of the axigluon is chosen to be

$$\mathcal{L} = g_s (g_l \bar{q} \gamma^\mu \gamma_5 q + g_h \bar{Q} \gamma^\mu \gamma_5 Q) G'_\mu$$

❏ Some properties of axigluon model

(1) Interference term (INT) gives top AFB $\propto -g_l g_h$, does not change the total xsec

(2) Should be heavy to satisfy the $t\bar{t}$ invariant mass spectrum and total cross section

(3) Pure new physics contribution (NP) is suppressed by the propagator

(4) Equal number of left-handed and right-handed top quarks in final state from this new physics

TWO EXAMPLES (II). W'

-  The interaction of the pure right-handed W' is chosen to be

$$\mathcal{L} = g_2 g_R \bar{d} \gamma^\mu P_R t W'_\mu + h.c.$$

-  Some properties of W' model

(1) Both interference term and pure new physics term contribute to the AFB

(2) There is a cancellation between the contribution to the $t\bar{t}$ total cross section from interference term and pure new physics term

(3) More right-handed top quarks in final state

Axigluon: s-channel

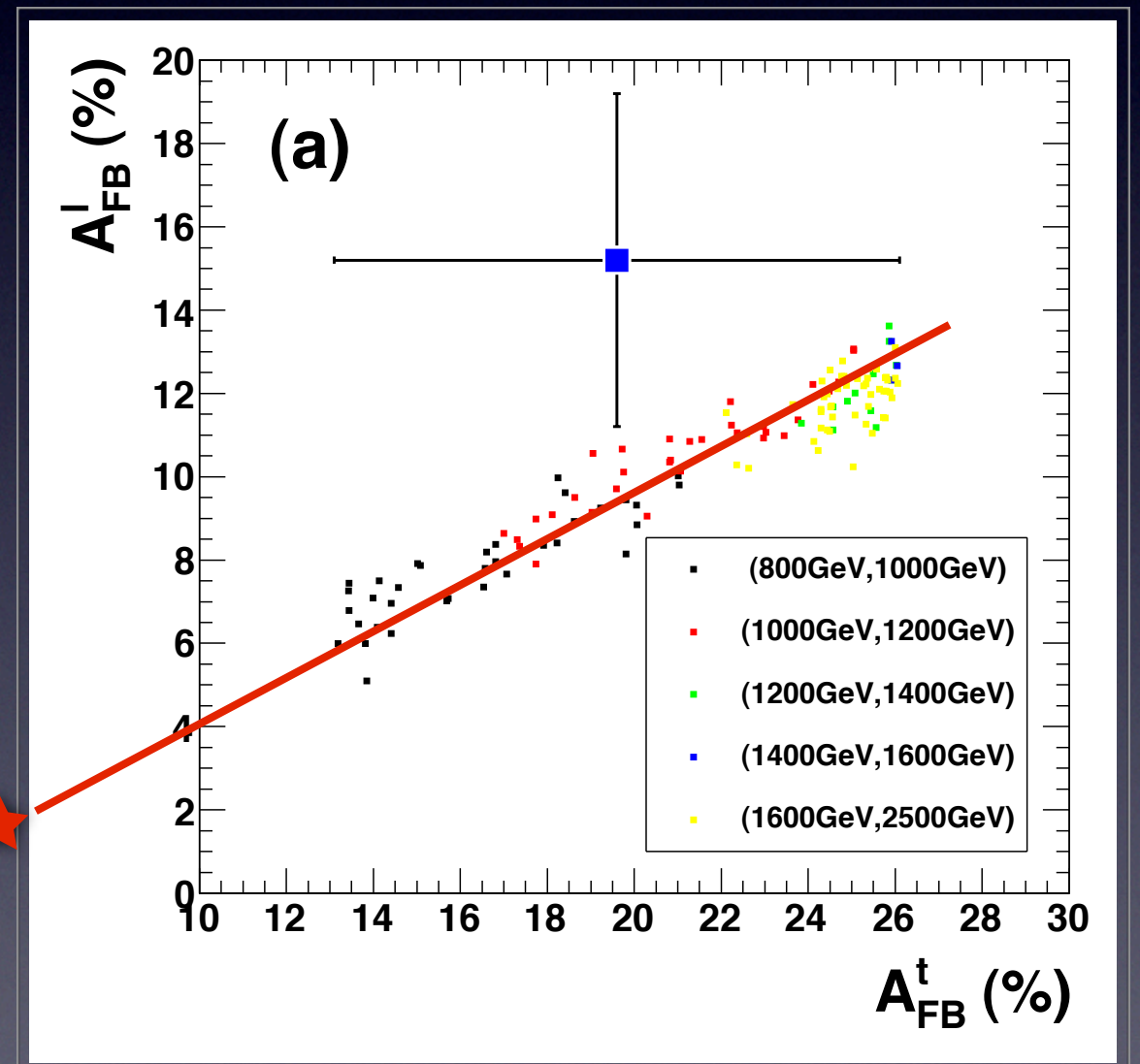
- Purely pseudo-vector coupling

$$\mathcal{L} = g_s (g_l \bar{q} \gamma^\mu \gamma_5 q + g_h \bar{Q} \gamma^\mu \gamma_5 Q) G'_\mu$$

- Best-fit

$$A_{FB}^l \simeq 0.47 \times A_{FB}^t + 0.25\%$$

SM ★



FC W -prime: t -channel

- Purely right-handed flavor changing interaction

$$\mathcal{L} = g_2 g_R \bar{d} \gamma^\mu P_R t W'_\mu + h.c.$$

$$\rho_{t_R} > \rho_{t_L}$$

- Best-fit

$$A_{FB}^\ell \simeq 0.75 \times A_{FB}^t - 2.1\%$$

SM ★

