

Quantum Physics with Massive Objects

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The Aspelmeyer Group



VCQ

Vienna Center for Quantum
Science and Technology

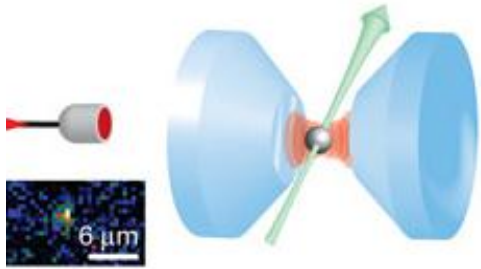


universität
wien

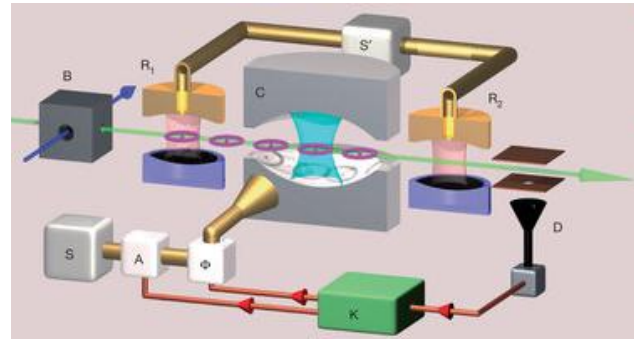
ICFP

14.06.2012

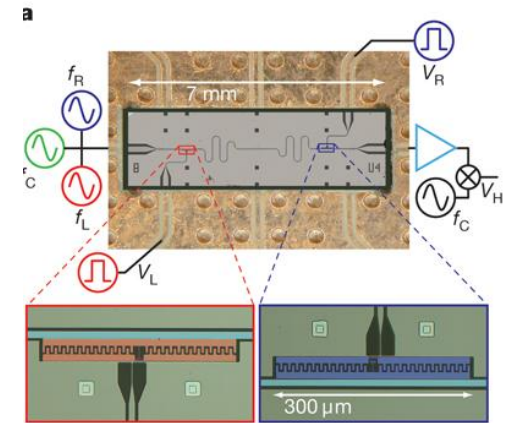
Well-controlled quantum systems an incomplete selection



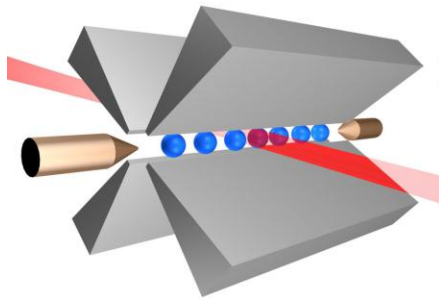
Nature 484, 195 (2012)



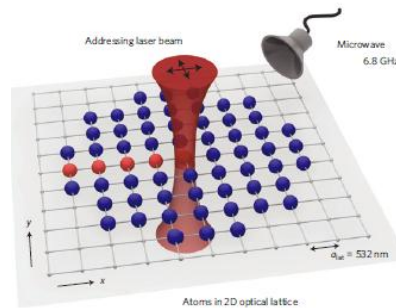
Nature 477, 73 (2011)



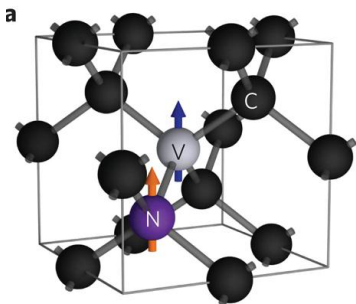
Nature 460, 240 (2009)



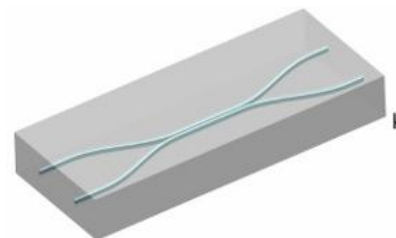
Science 334, 57 (2011)



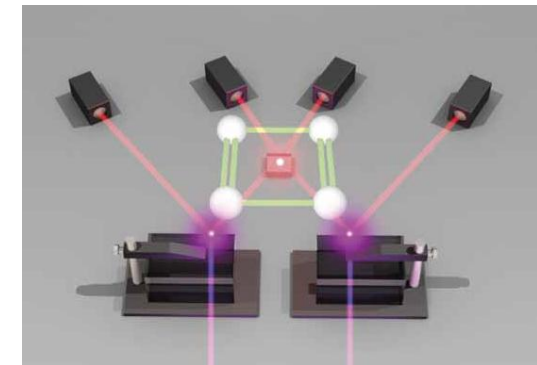
Nat Phys 8, 267 (2012)



Nanotec. 7, 105-108 (2012)

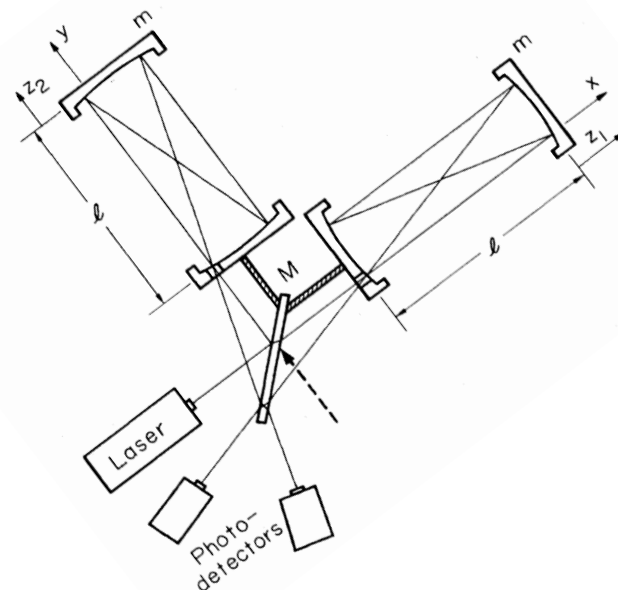
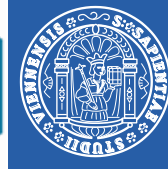


Science 320, 646



Nat. Phys. 8, 285 (2012)

Quantum physics with massive objects?



phase noise

$\langle \Delta \phi^2 \rangle$

Quantum-Mechanical Radiation-Pressure Fluctuations in an Interferometer

Carlton M. Caves

W. K. Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, California 91125

(Received 29 January 1980)

The interferometers now being developed to detect gravitational waves work by measuring small changes in the positions of free masses. There has been a controversy whether quantum-mechanical radiation-pressure fluctuations disturb this measurement. This Letter resolves the controversy: They do.

$\log P [W]$

Shot noise

SQL

back action noise

Controlling mechanical systems in the quantum regime



See also Teufel et al., arxiv 1103.2144 (2011)

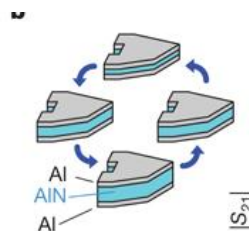
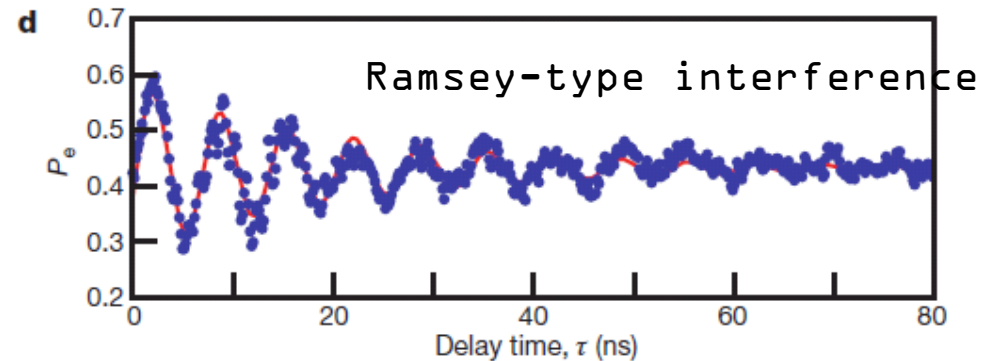
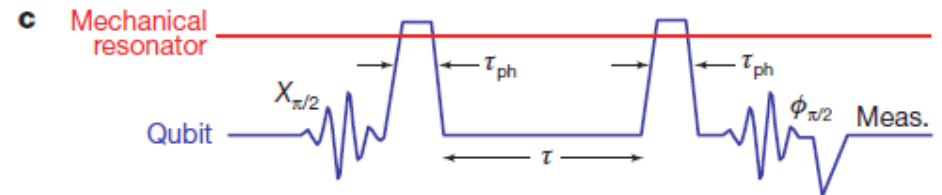
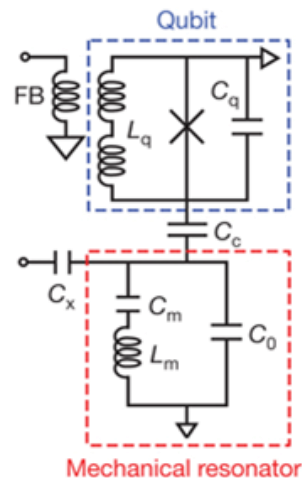
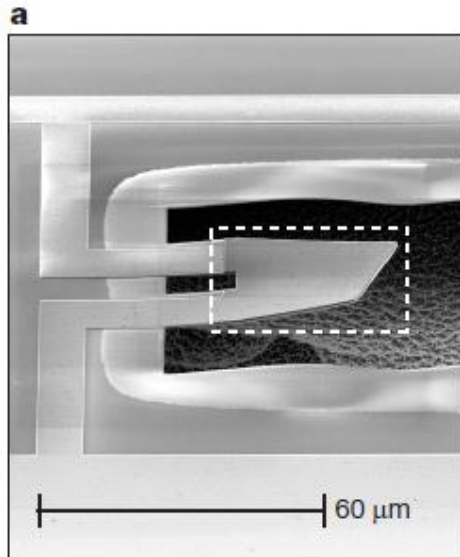
ARTICLES

Quantum ground state and single-phonon control of a mechanical resonator

6 GHz piezo vibration
→ $n \sim 0.07$ @ 20 mK

Cleland/Martinis groups (UCSB);
April 2010

A. D. O'Connell¹, M. Hofheinz¹, M. Ansmann¹, Radoslaw C. Bialczak¹, M. Lenander¹, Erik Lucero¹, M. Neeley¹, D. Sank¹, H. Wang¹, M. Weides¹, J. Wenner¹, John M. Martinis¹ & A. N. Cleland¹



Quantum regime of massive resonators



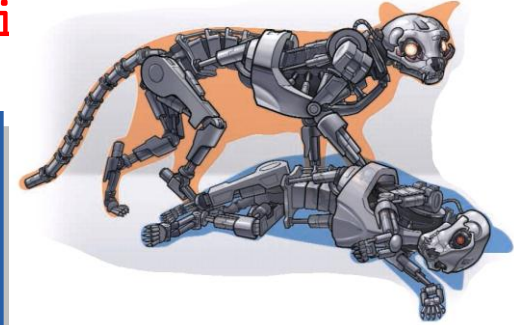
Cho, Science 327, 516 (2010)

Access a new realm of experimental physics

Quantum Foundations

macroscopic quantum superposition involving up to 10^{20} atoms

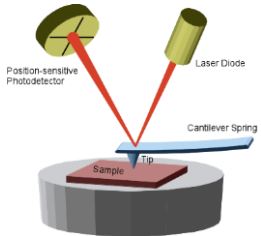
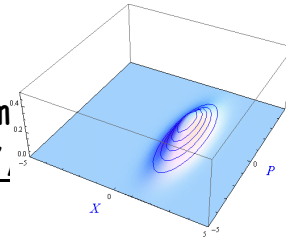
→ Is there a limit to the size/mass of Schrödinger cats?



Mechanical Sensing

present performance: zeptogram, zeptonewton, attom

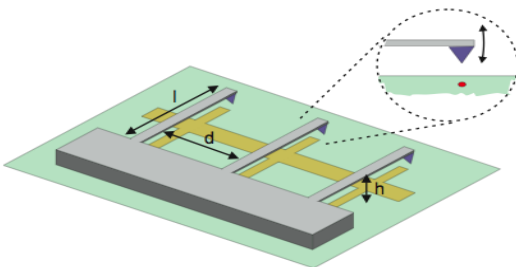
→ What are the quantum limits to mechanical sensing?



Quantum Information

e.g. potential for hybrid quantum information architectures on a chip

→ Can mechanical systems serve as universal quantum



Rabl et al.,

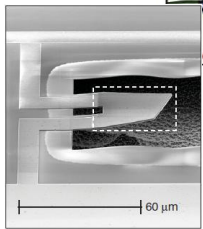
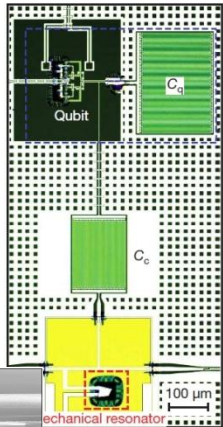
Nature Physics 6, 602 (2010).

Coupling to mechanics



charge

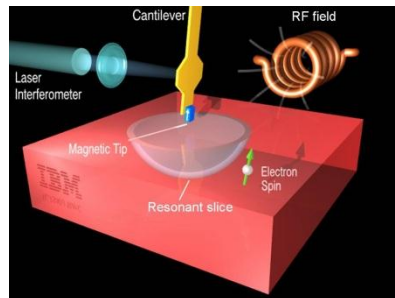
$$Q \quad U$$



O. Connell et al.,
Nature 464 (10)

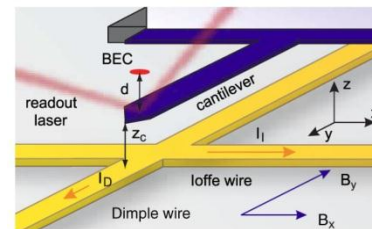
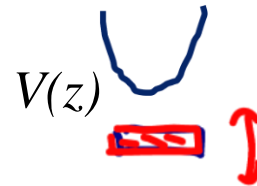
spin

$$\mu \quad B$$



D. Rugar et al.,
Nature 430 (04)

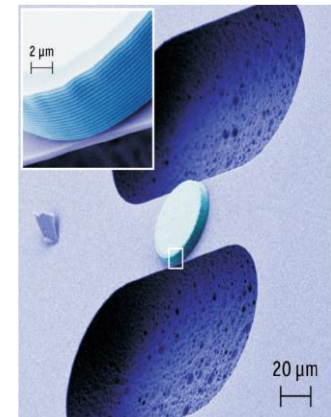
atoms



D. Hunger et al.,
PRL 104 (10)

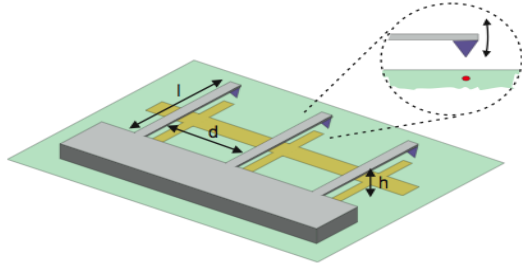
photon
momentum

$$\hbar k$$



S. Gröblacher et al.,
Nature Phys. 5 (09)

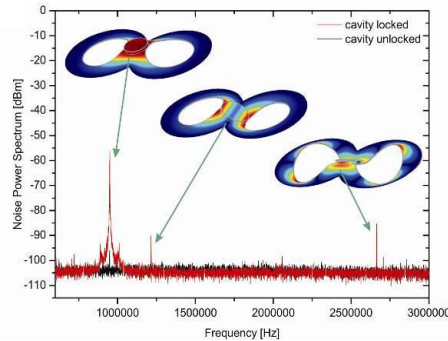
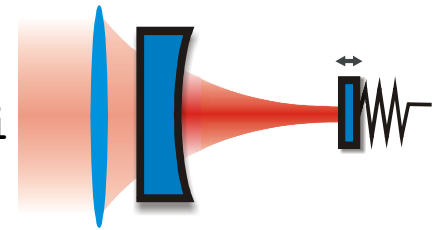
Cavity Optomechanics



Massive mechanical quantum systems?

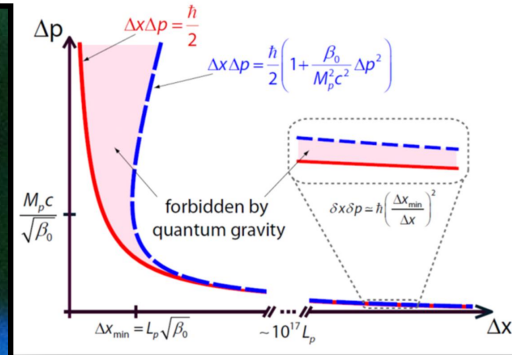
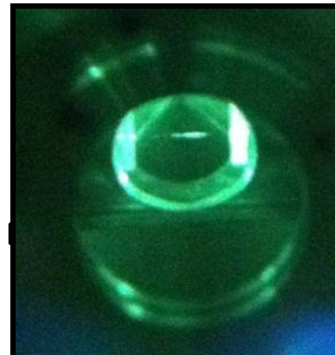
Optics and Light - a short history and basic principles

<http://vcq.quantum.at/fet11.5397.html>

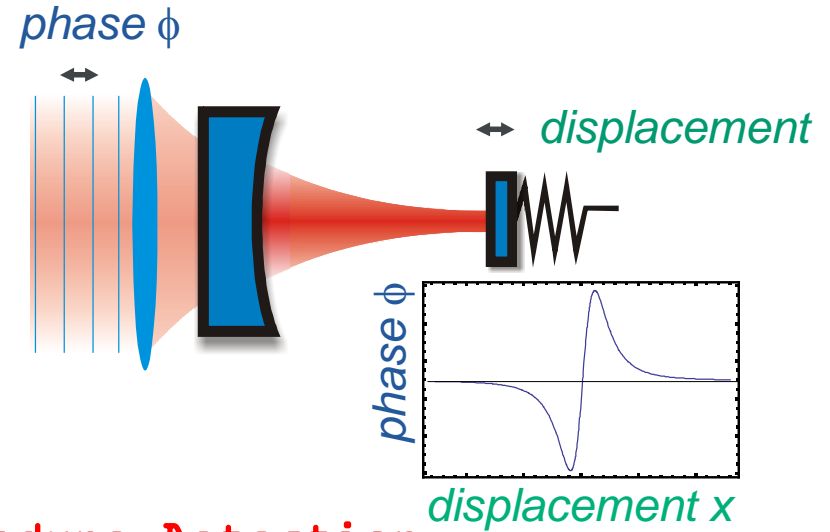
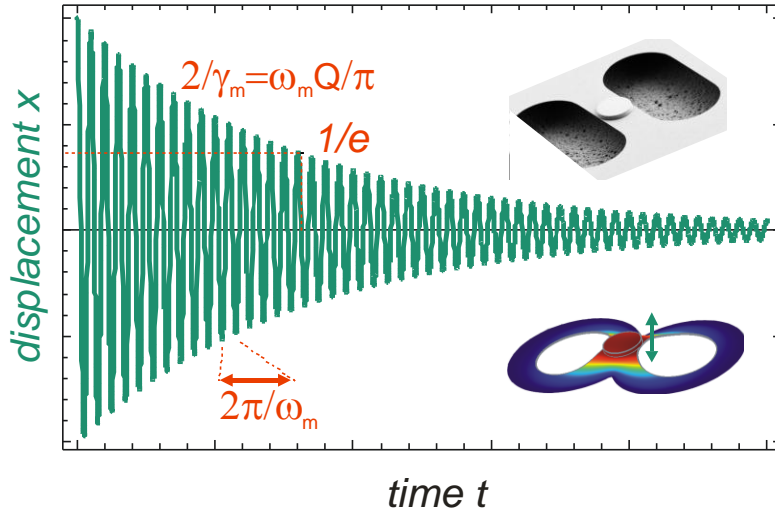


Towards Quantum Optomechanics - Experiments

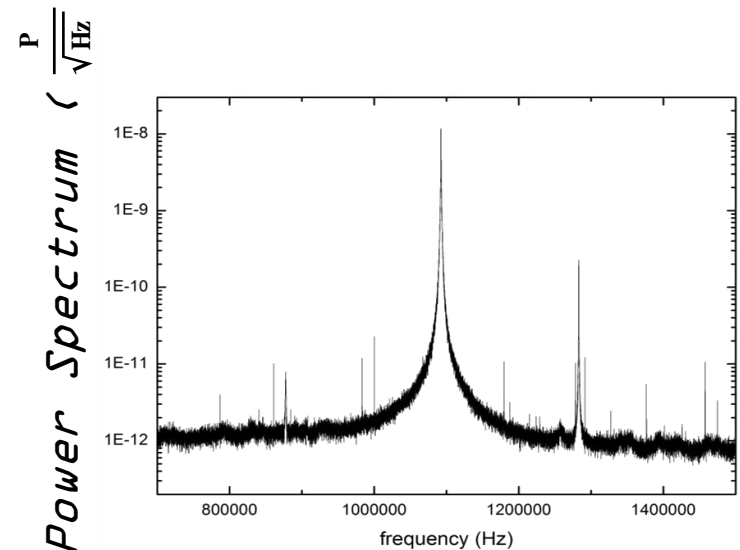
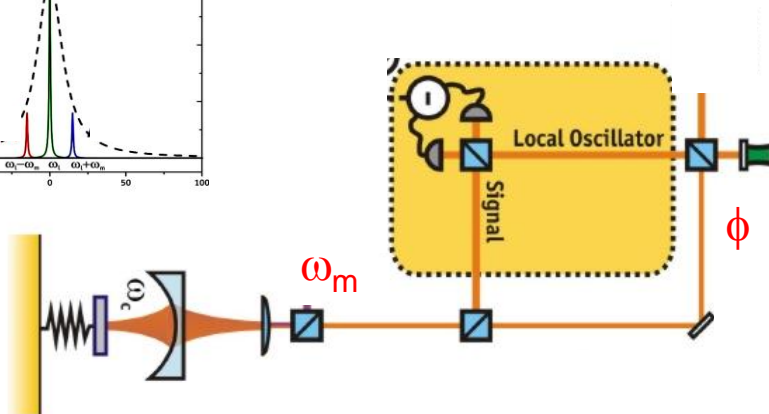
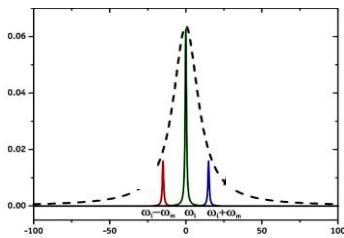
New ideas and future plans



Cavity Optomechanics - Readout

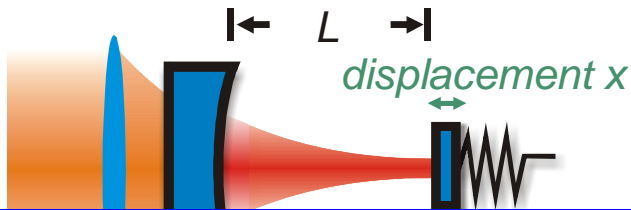
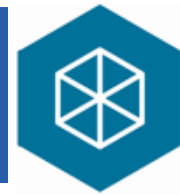


Readout by Homodyne Detection



Frequency (Hz)

Cavity Optomechanics



Idea: Added optical cavity allows to **manipulate**

A bit of history...

- Walther group: "Optical bistability and mirror confinement induced by radiation pressure" , Dorsel et al. PRL 51, 1550 (1983)
- 2003 Karrai group: "Optically tunable mechanics of microlevers"
Favero et al., APL 83, 1337 (2003)
- 2005 Vahala group: "Kerr-Nonlinearity Optical Parametric Oscillation in an

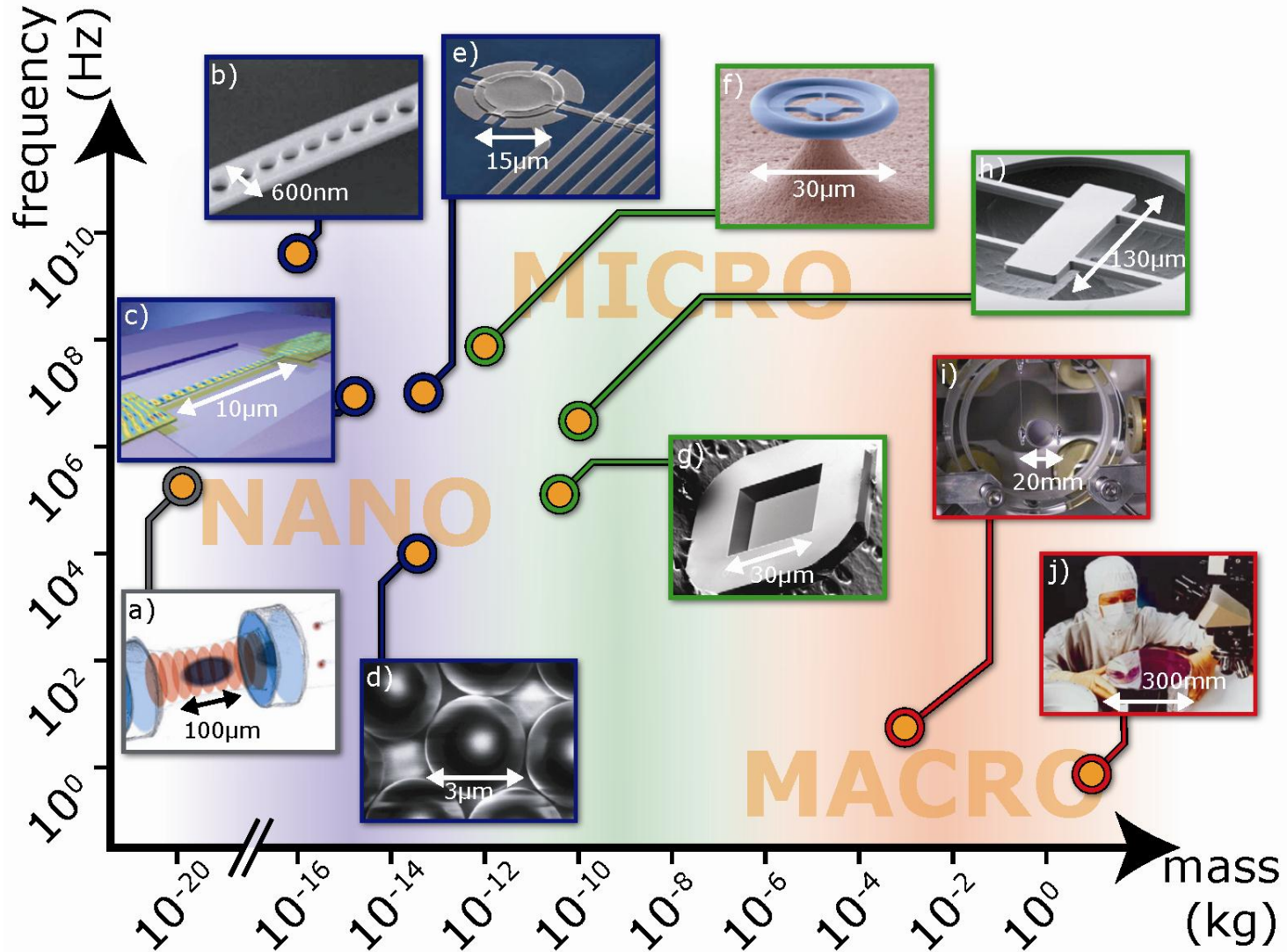
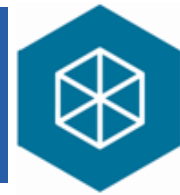
2004 Kippenberg et al., PRL 93, 033904 (2004) **Ultrahigh-Q Toroid Microcavity**

2006 Aspelmeyer and Kippenberg group, **Self-cooling by Radiation Pressure**

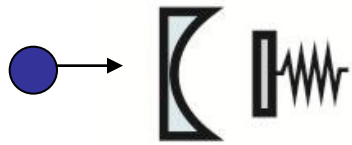
2006 Cogan et al., Nature 444, 476 (2006), **Change in spring constant of an optical spring**

2006 Arcizet et al., Nature 444, 71 (2006), **the mech. oscillator**

Optomechanical Systems



Cavity Optomechanics – The quantum version



$$H_{\text{int}} = -\hbar g_0 n_c X_m$$

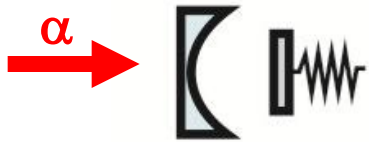
$$g_0 = \frac{\omega_c}{L} \sqrt{\frac{\hbar}{m \omega_m}}$$

0.1...100 Hz

single-phonon cavity frequency shift with most current systems (exception later)

(too small!!!)

Solution: strongly driven optomechanics



$$H_{\text{int}} = \hbar g_0 \alpha X_c X_m$$

$$\alpha = \sqrt{n_c} \approx \theta(10^5)$$

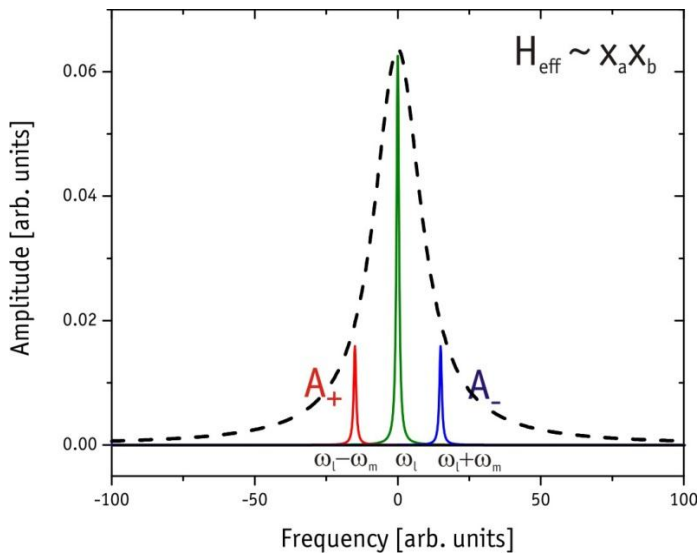
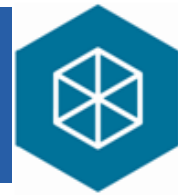
$$a \rightarrow \alpha + \bar{a}$$

enhancement by α

→ strong coupling

Trade-off: only linear coupling... BUT...

Linear coupling is sufficient



QND Measurement

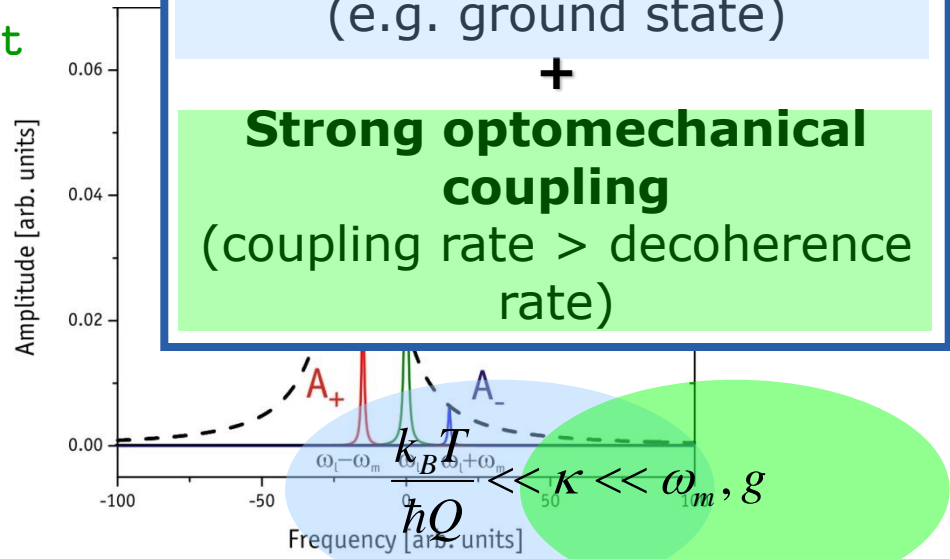
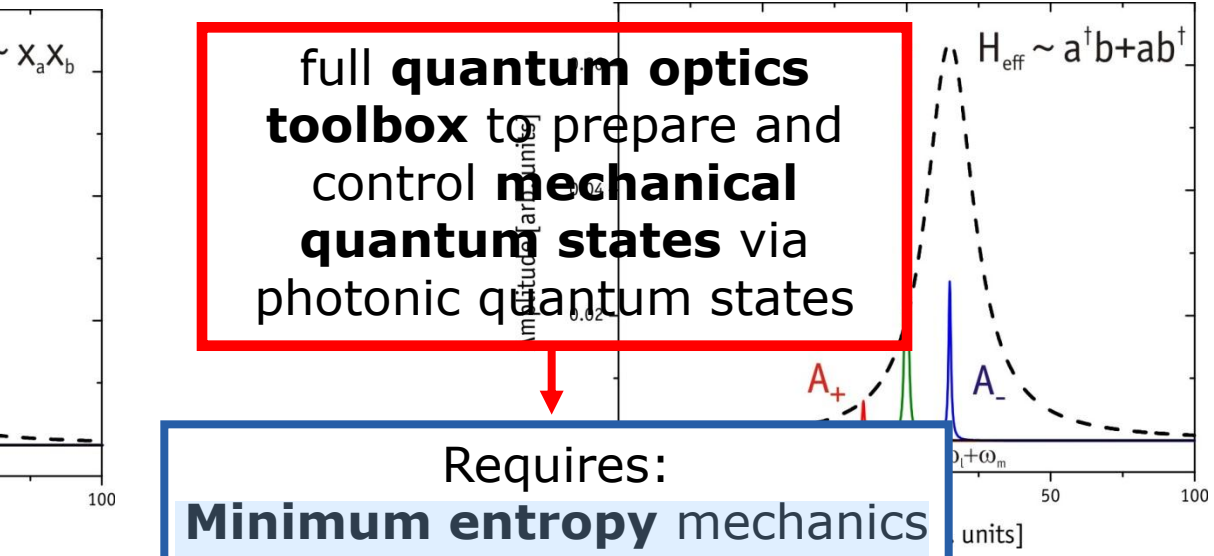
full **quantum optics toolbox** to prepare and control **mechanical quantum states** via photonic quantum states

Requires:

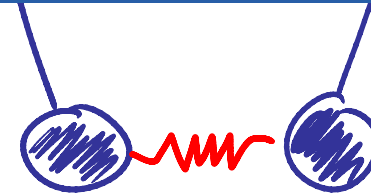
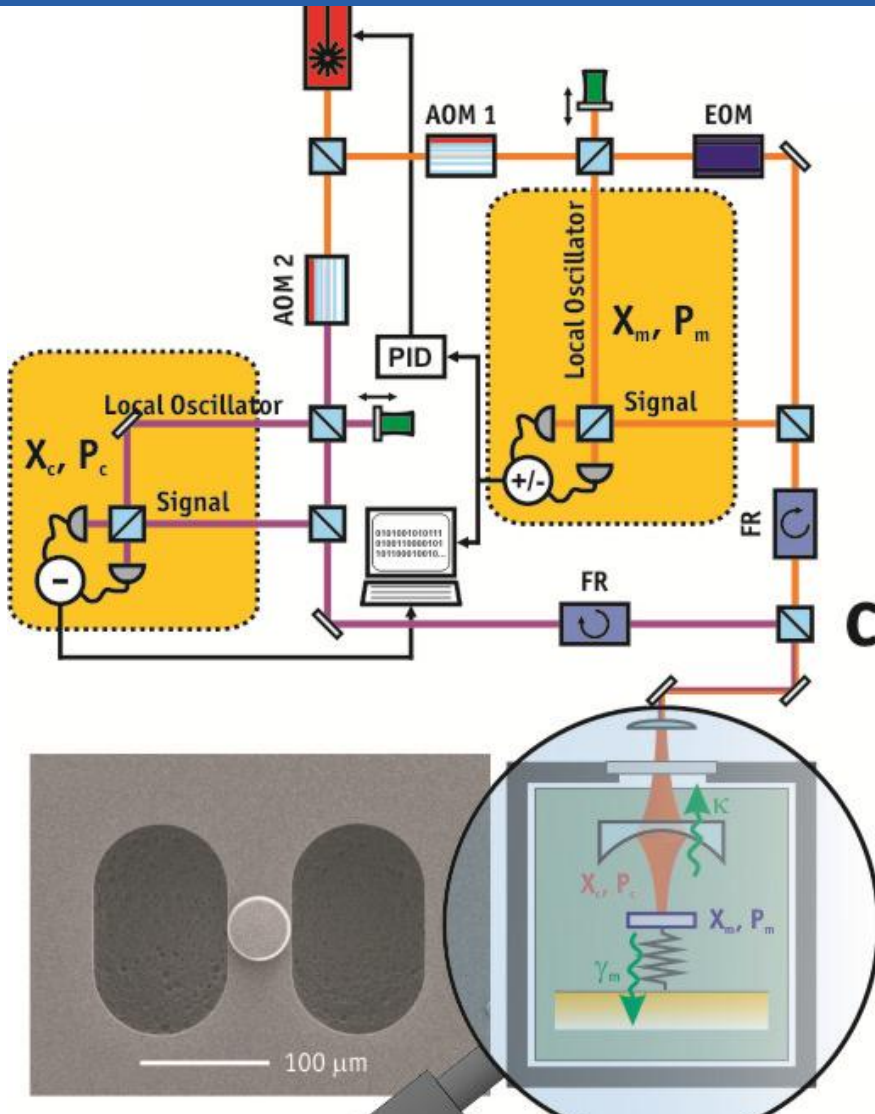
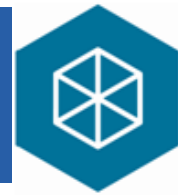
Minimum entropy mechanics (e.g. ground state)

+

Strong optomechanical coupling (coupling rate > decoherence rate)



Strong optomechanical coupling



„strong coupling“: hybrid „optomechanical“ system → new energy spectrum

$$X_{\pm} = \sqrt{\frac{\omega_m \pm g}{2\omega_m}} (X_c \pm X_m) \quad P_{\pm} = \sqrt{\frac{\omega_m}{2(\omega_m \pm g)}} (P_c \pm P_m)$$

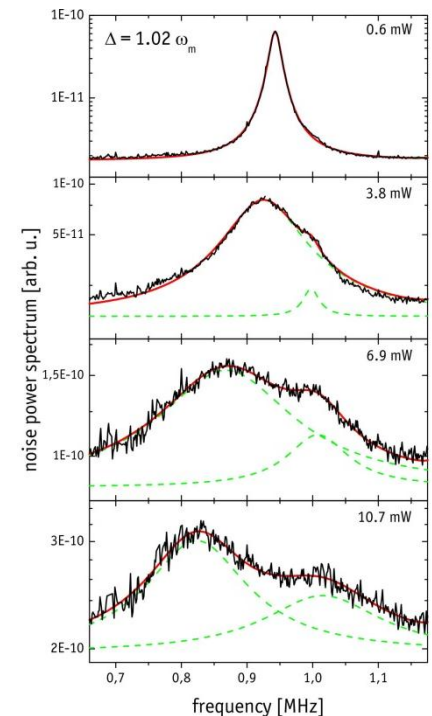
$$g \approx 2\pi \times 325 \text{ kHz}$$

$$\kappa = 2\pi \times 215 \text{ kHz}$$

$$\gamma_m = 2\pi \times 140 \text{ Hz}$$

$$g > \kappa, \gamma_m$$

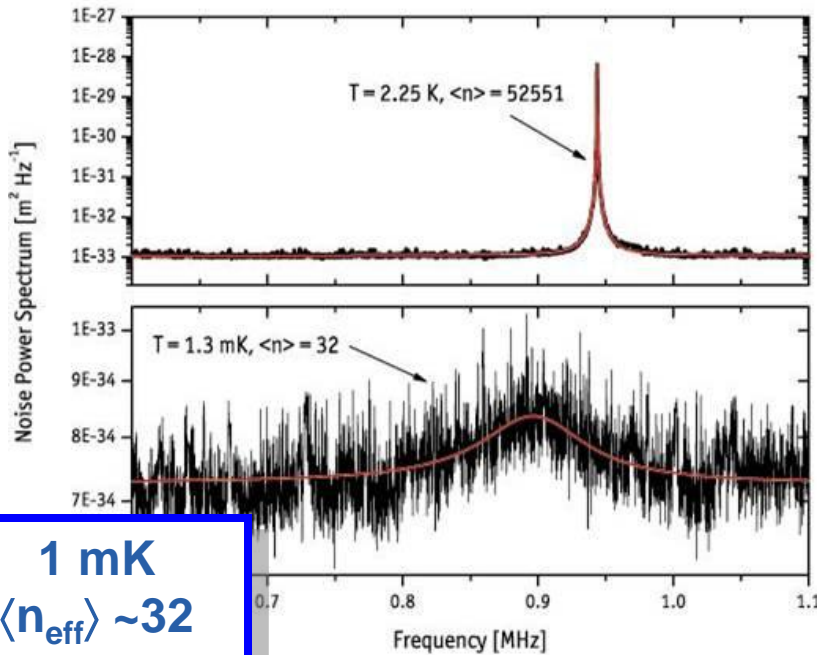
Important coupling condition for coherent quantum control!



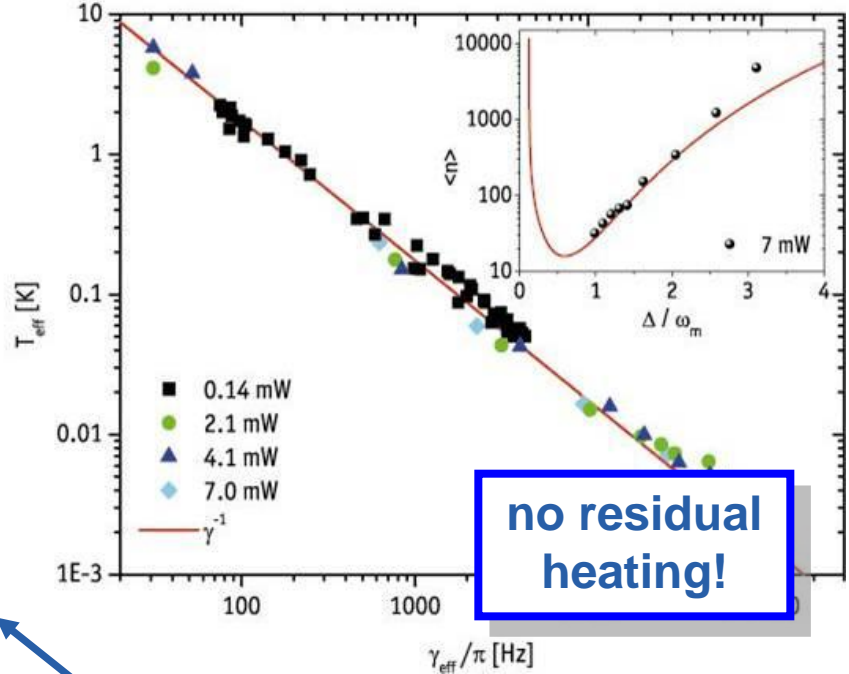
Gröblacher, Hammerer, Vanner, Aspelmeyer, **Nature 460, 724 (2009)**

See also Teufel et al., Nature 471, 204 (2011); Verhagen et al., Nature 482, 63 (2012)

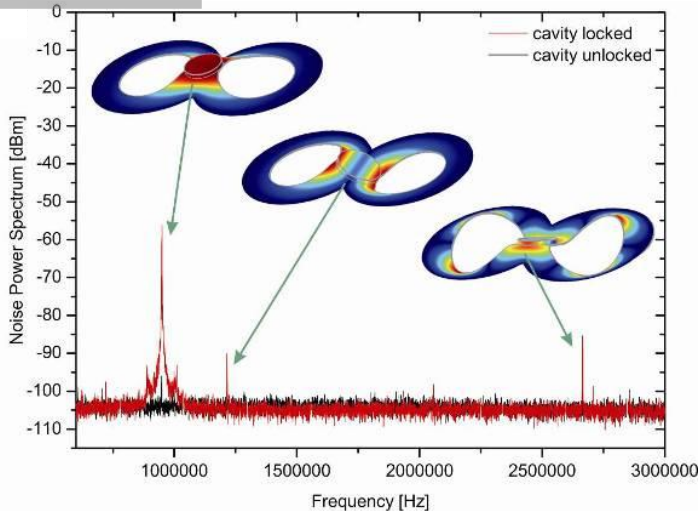
Optomechanical Cooling



1 mK
 $\langle n_{\text{eff}} \rangle \sim 32$



no residual heating!



noise floor $\sim 2.6 \times 10^{-17}$ mHz $^{-1/2}$

4x above the shot noise

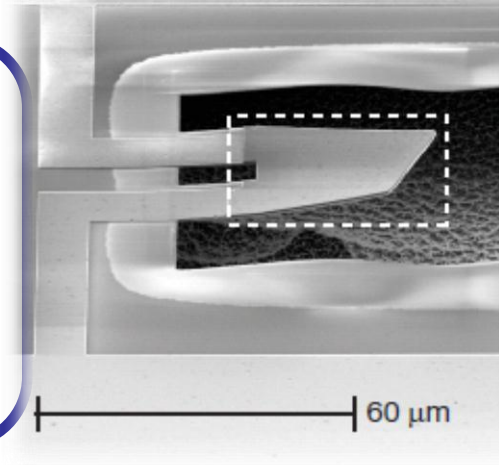
relevant modes identified via



Nature **464**, 697-703 (2010)

Quantum ground state and single-phonon control of a mechanical resonator

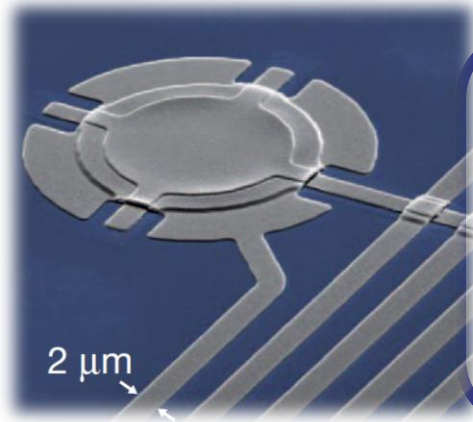
A. D. O'Connell¹, M. Hofheinz¹, M. Ansmann¹, Radoslaw C. Bialczak¹, M. Lenander¹, Erik Lucero¹, M. Neeley¹, D. Sank¹, H. Wang¹, M. Weides¹, J. Wenner¹, John M. Martinis¹ & A. N. Cleland¹



Nature **475**, 359-363 (2011)

Sideband cooling of micromechanical motion to the quantum ground state

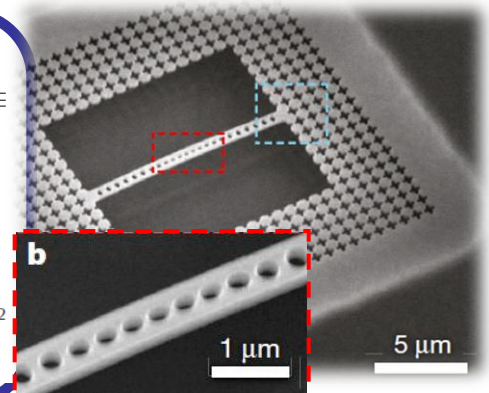
J. D. Teufel¹, T. Donner^{2,3}, Dale Li¹, J. W. Harlow^{2,3}, M. S. Allman^{1,3}, K. Cicak¹, A. J. Sirois^{1,3}, J. D. Whittaker^{1,3}, K. W. Lehnert^{2,3} & R. W. Simmonds¹



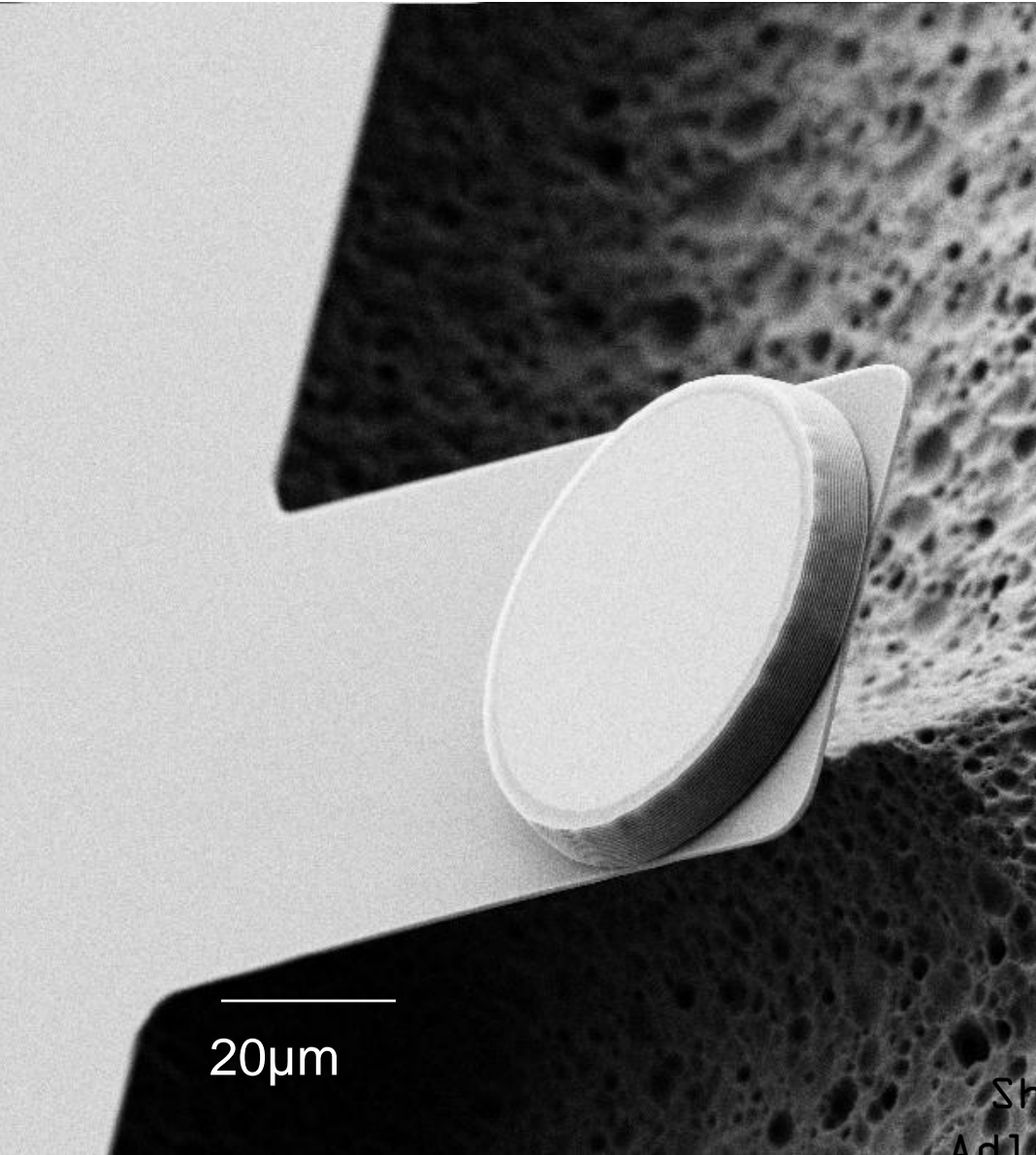
Nature **478**, 89-92 (2011)

Laser cooling of a nanomechanical oscillator into its quantum ground state

Jasper Chan¹, T. P. Mayer Alegre^{1†}, Amir H. Safavi-Naeini¹, Jeff T. Hill¹, Alex Krause¹, Simon Gröblacher^{1,2}, Markus Aspelmeyer² & Oskar Painter¹



A mechanical cat? Schrödinger's mirrors?



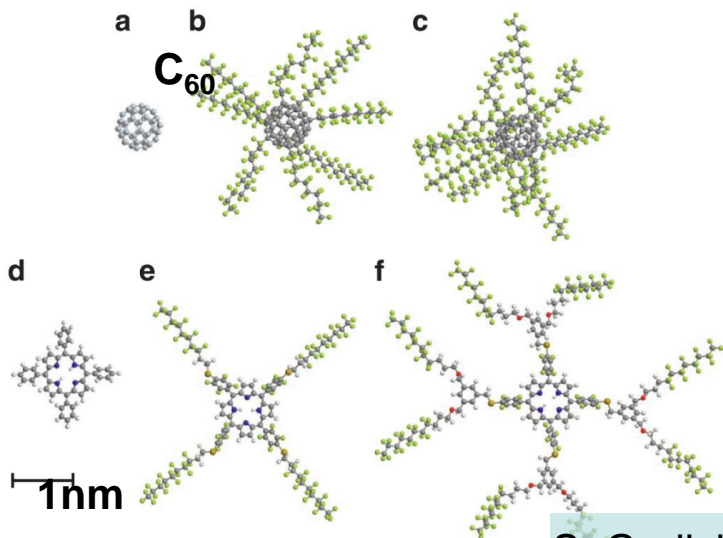
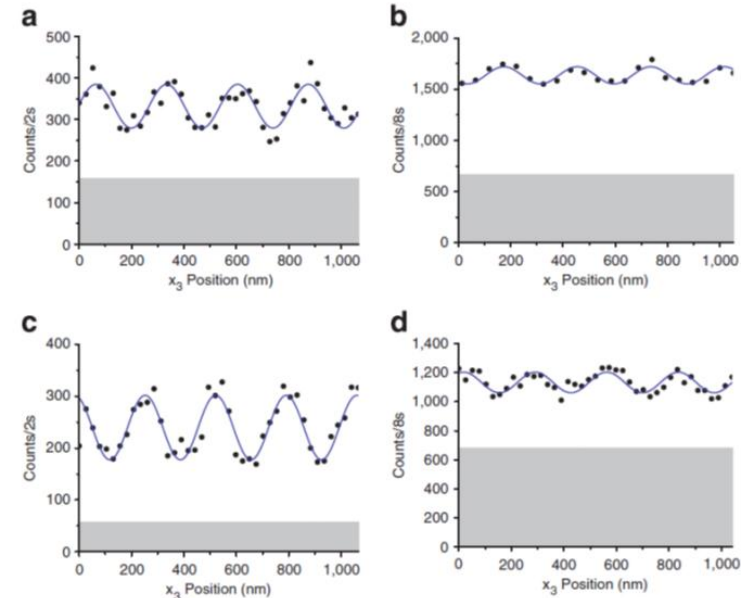
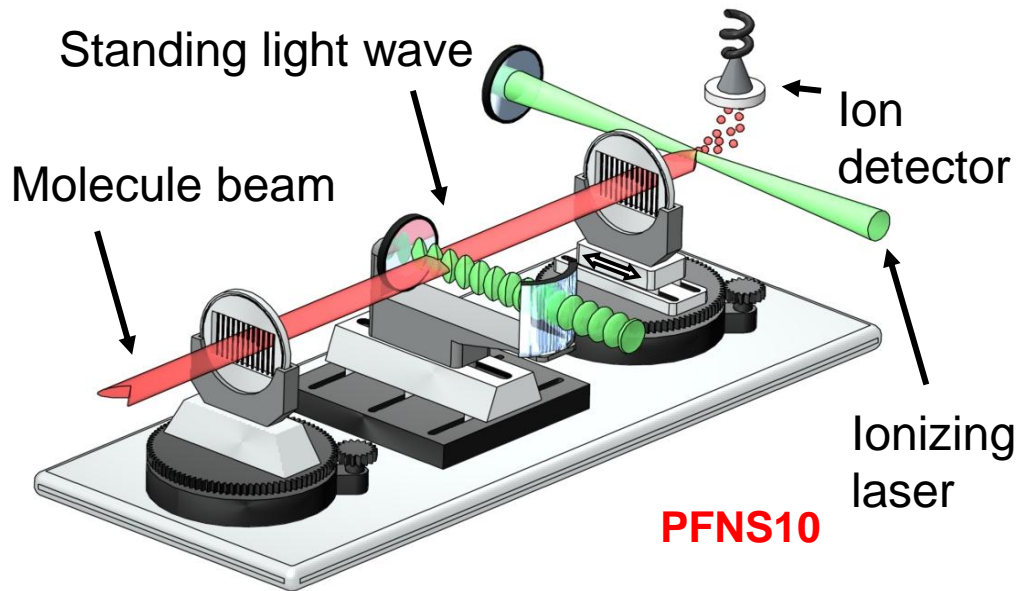
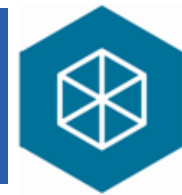
Superposition of macroscopically distinct states?

Tests of macrorealistic theories? (Collapse models, Leggett-Garg, ...)

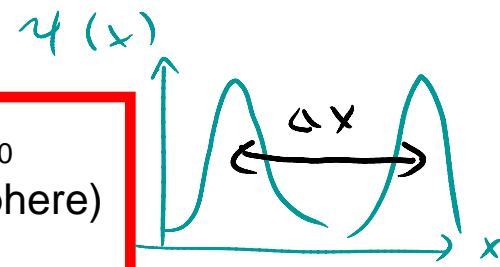
Tests of predictions of quantum gravity?

Short introduction to the subject
Adler, Bassi, Science 325, 275 (2007)

Talbot-Lau Interferometry with Macromolecules (Arndt group)



PFNS10: $C_{60}[C_{12}F_{25}]_{10}$
 (perfluoroalkylated nanosphere)
 430 atoms
 $m \sim 10^{-23} \text{ kg} = 6910 \text{ AMU}$
 $\Delta x \sim 100 \text{ nm}$ ($\sim 50x$ its diameter)



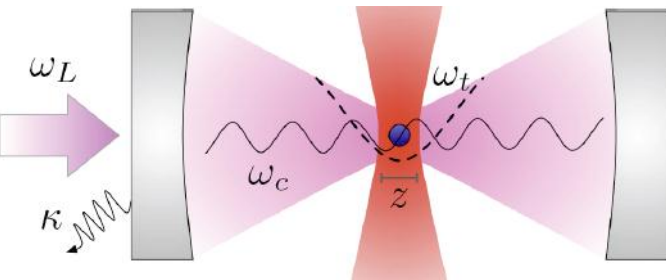
Towards state preparation of a free particle



Magnetically levitated spheres

Romero-Isart et al., 1112.5609, Cirio et al., 1112.5208

Optically levitated nanospheres



Romero-Isart et al. NJP 12, 33015, (2010)

Chang et al., PNAS 107, 1005 (2010)

P. F. Barker et al., PRA 81, 023826 (2010)

→ **Harmonic oscillator in optical potential**
(no support loss, high Q)

→ **Quantum control via cavity optomechanics**
(laser cooling, state transfer, etc.)

→ **Full Control of Spring Constant**
(parametric control, thermodynamic cycles, removing potential)

Generation of quantum superposition states of CM position/ momentum

- single-photon quantum state transfer
- quantum state teleportation
- ...

Akram, et al., NJP 12, 083030 (2010)

Khalili, Phys. Rev. Lett. 105, 070403 (2010)

Romero-Isart et al., PRA 83, 013803 (2011)

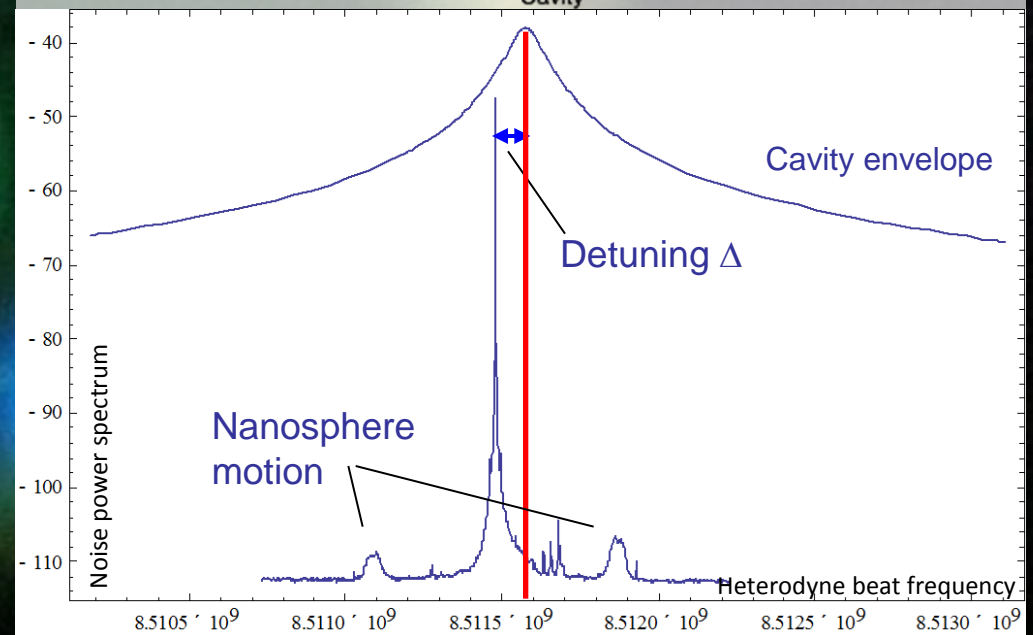
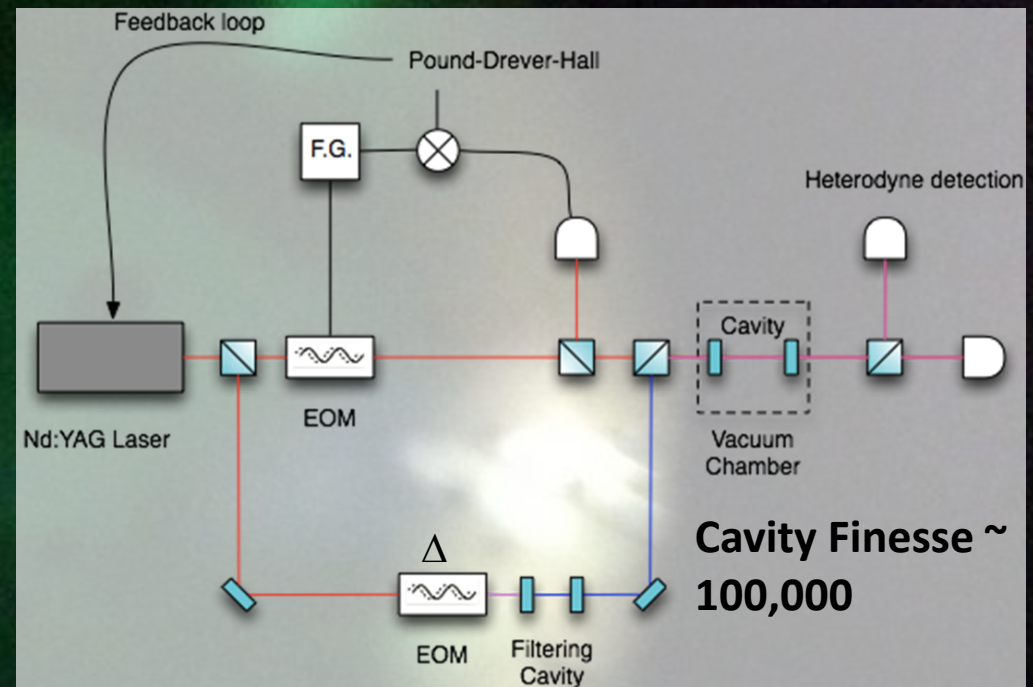
• **free fall experiments - interferometry** : is there intrinsic additional decoherence for massive objects (here 10^{10} amu)?

Optically trapped nanospheres as mechanical resonators

Ashkin since 1967

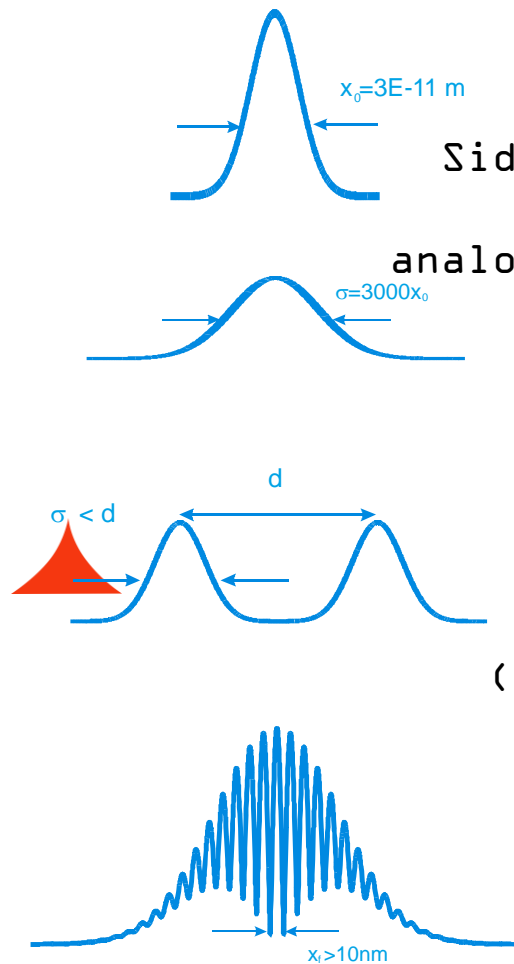
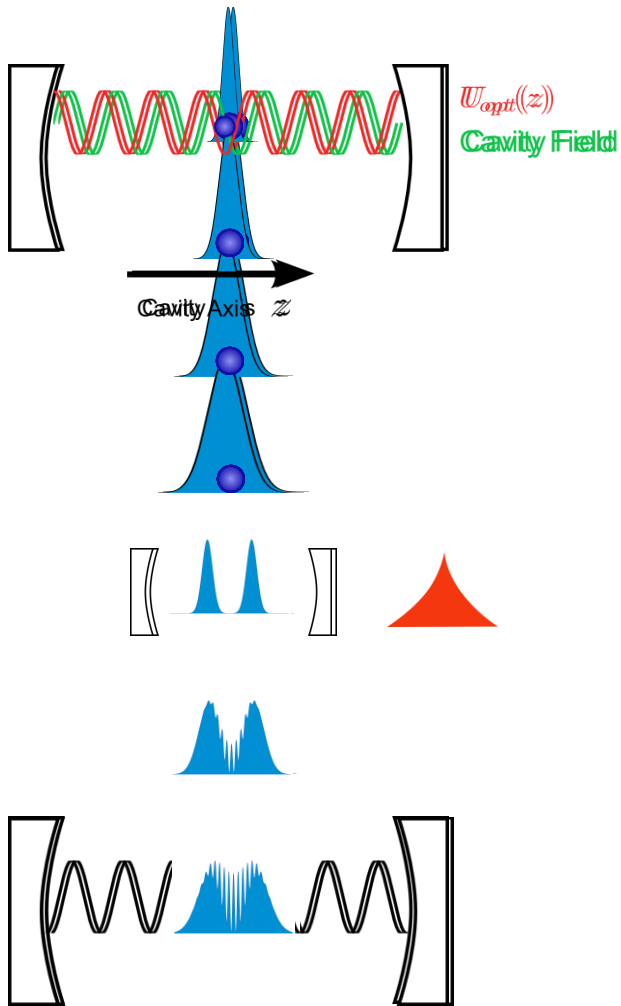
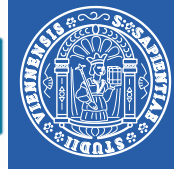
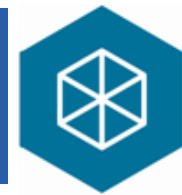
Raizen group, *Science* 2010

Novotny 2012



Optical trapping inside a cavity... ($R \sim 20\text{nm} - 2\mu\text{m}$)
Kiesel et al., work in progress

Potential Parameter Set



Object: $D=40\text{nm}$
Silica Sphere

Sideband Cooling of Nanosphere
to 0.1 phonons
analogous to cooling of micromi

3.3 ms

Short Pulse
 x^2 -readout Projection
on $\text{Cat-Stat}|x\rangle + |-x\rangle$
(Cavity: $L=2\mu\text{m}$, $F=130000$)

125 ms

Position Detection
Precision: 10nm

One possible application: test of alternative decoherence models



◊. Romero-Isart et al., PRL 107, 020405 (2011)

$\psi(x)$

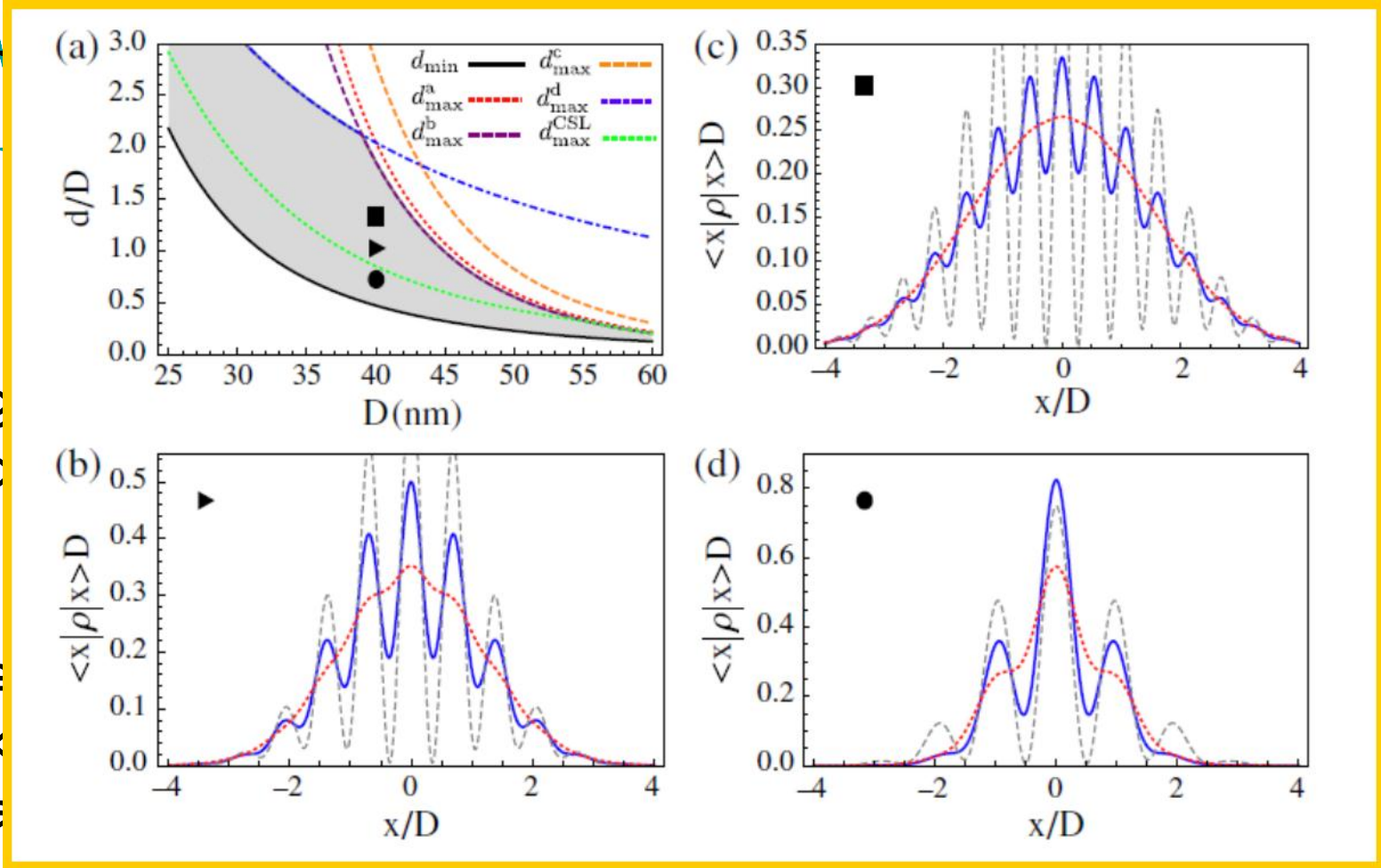
$\Delta x \sim$

Background
gas pressure
1 mbar

(here
black
radiation)

Károlyházy

Diosi (1985), Penrose (1980s), e.g. Gen. Rel. Grav. 34, 1141 (2002)

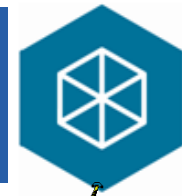


1 m

1 nm

In collaboration with ◊. Romero-Isart, A. Pf...
see also Romero-Isart, Phys. Rev. A 84, 0521

MAQRO: Macroscopic Quantum Resonators for Space



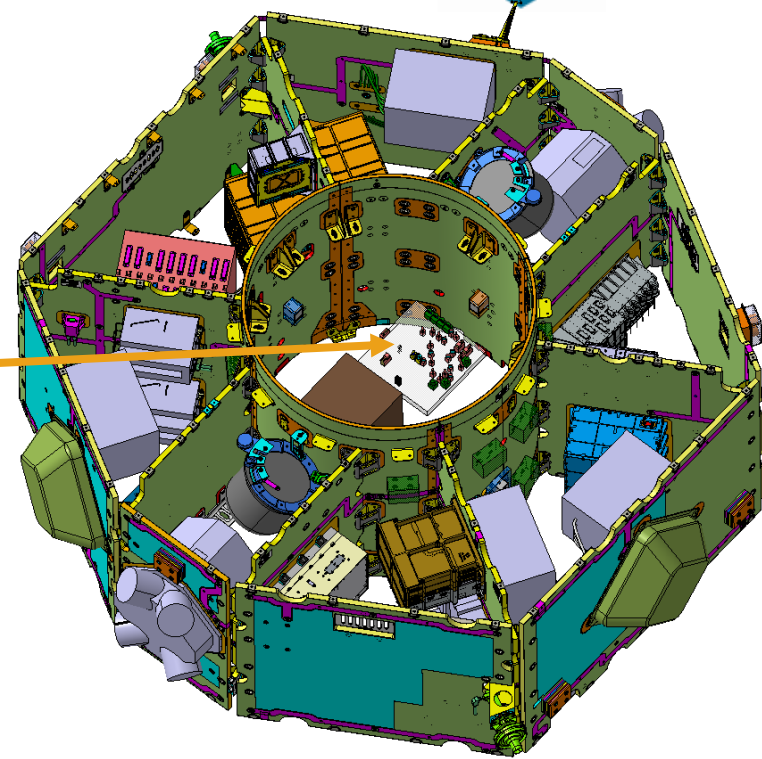
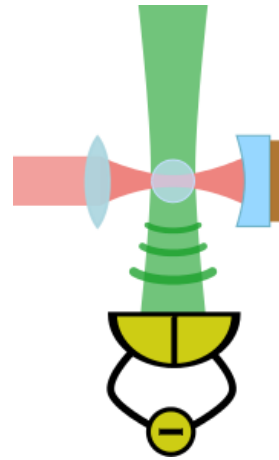
A possible space experiment under extreme conditions (vacuum, temperature)

$T_{env} \sim 10\text{ K}$

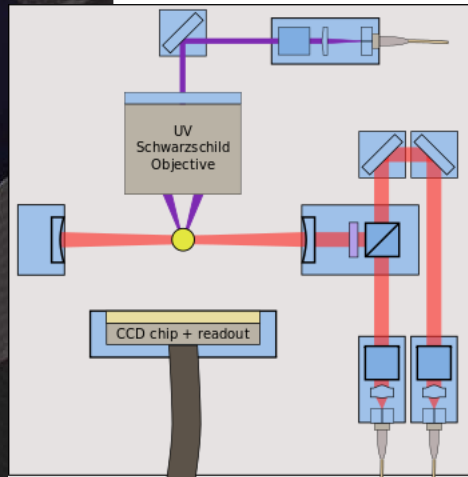
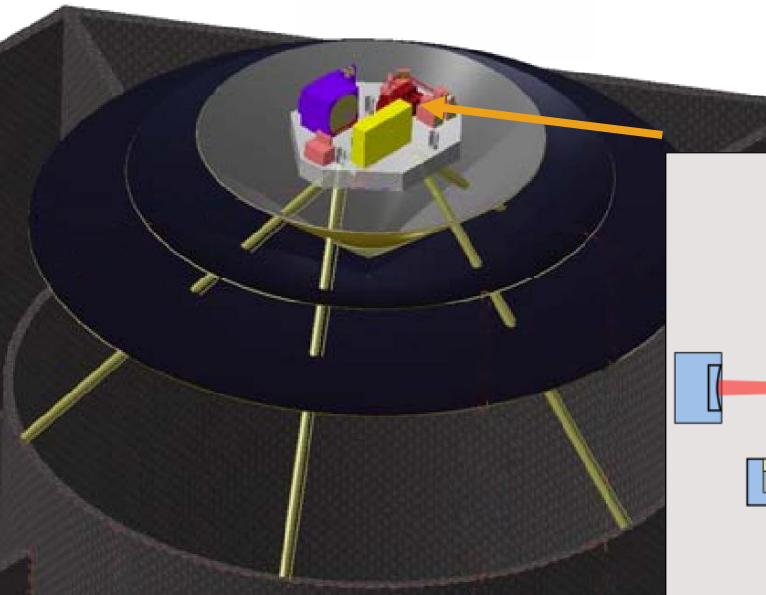
Background pressure $\ll 10^{-15}\text{ mbar}$

Micro-gravity environment

R. Kaltenbaek et al., arXiv:1201.4756
in collaboration with EADS ASTRIUM
Friedrichshafen



LTP Modul

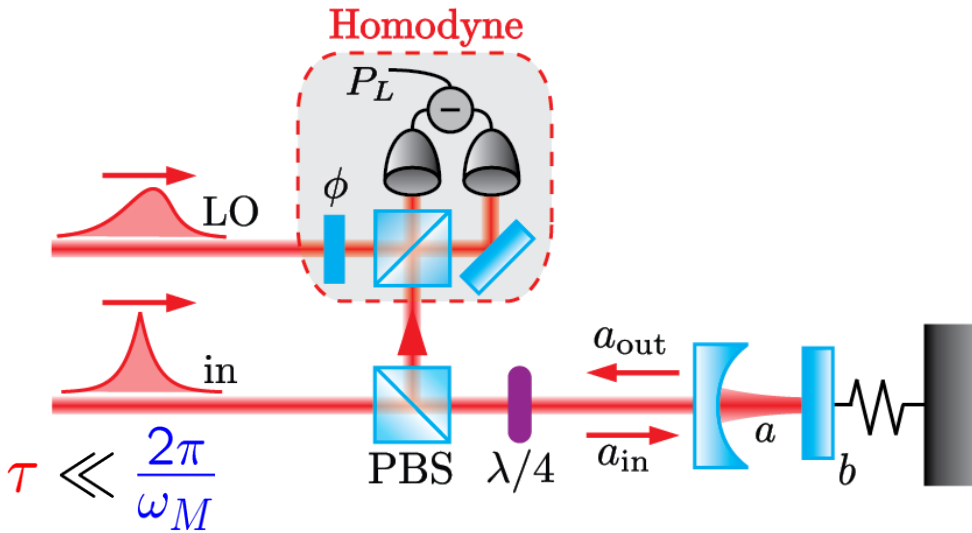
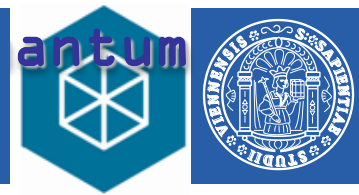


DECIDE

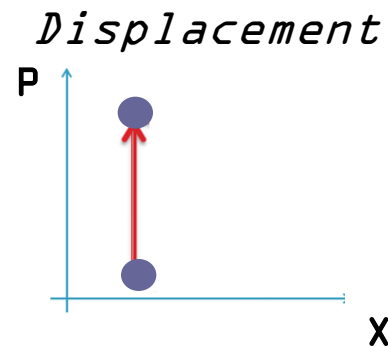
- macroscopic quantum state („Schrödinger Cat“)
- test quantum theory against macrorealistic models

R. Kaltenbaek et al.,
(MAQRO, Experimental
Astronomy (2012),

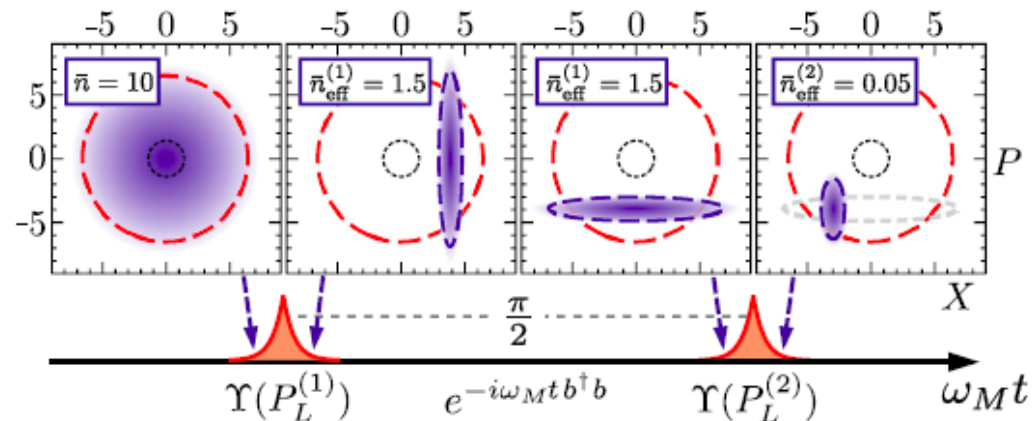
Pulsed Optomechanics



Short optical pulse „kicks“ mechanical resonator (displacement)
 Homodyne Phasereadout allows mechanical position measurement below mechanical shot noise (squeezing)



Squeezing



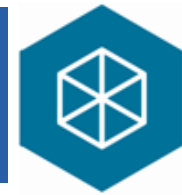
→ Squeezing and displacement of mechanical resonator

Vanner, Pikovski et al., PNAS 108, 16182 (2011)

→ Hamiltonian engineering by quantum interference

Machnes et al., arxiv 1104.5448; PRL (in press)

Towards tests of quantum gravity predictions?



Idea: **Closed loop** in (mechanical) phase space generates an (optical) **phase** related to the (mechanical) **commutator**

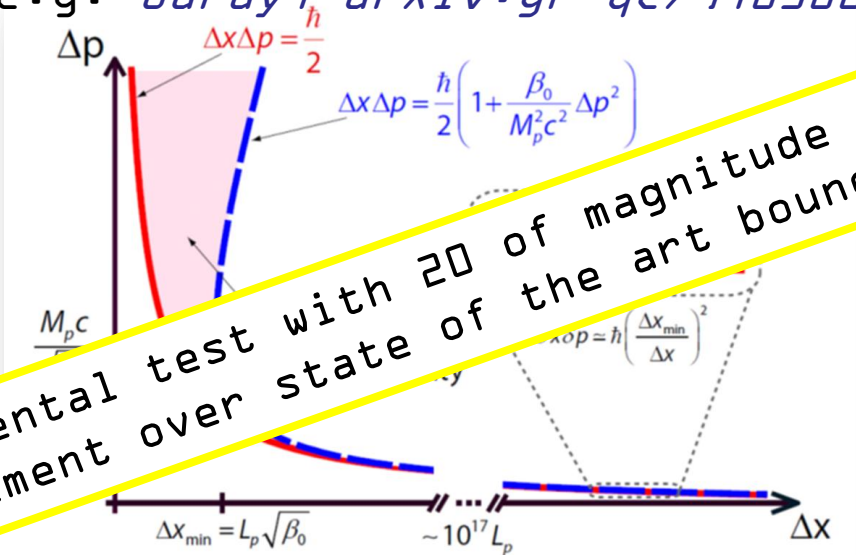
$$\hat{\xi} = e^{i\lambda\hat{n}_a\hat{P}} e^{-i\lambda\hat{n}_a\hat{X}} e^{-i\lambda\hat{n}_a\hat{P}} e^{i\lambda\hat{n}_a\hat{X}} = e^{-\lambda^2\hat{n}_a^2[\hat{X}, \hat{P}]}$$

$$\langle \hat{a}_a \rangle = \langle \alpha | \hat{\xi}^\dagger \hat{a}_a \hat{\xi} | \alpha \rangle \approx \alpha e^{-2|\alpha|^2\lambda^2[\hat{X}, \hat{P}]}$$

Test of uncertainty principle!

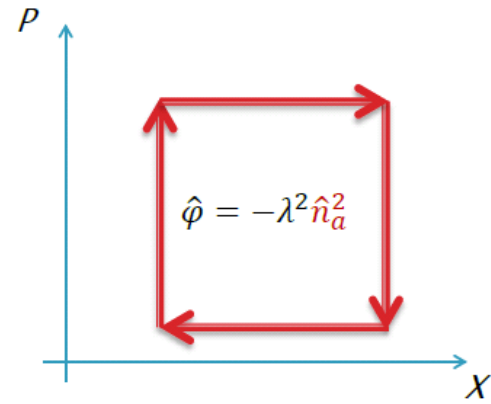
Revision due to minimal length scale?

(e.g. *Garay, arXiv:gr-qc/9403008*)

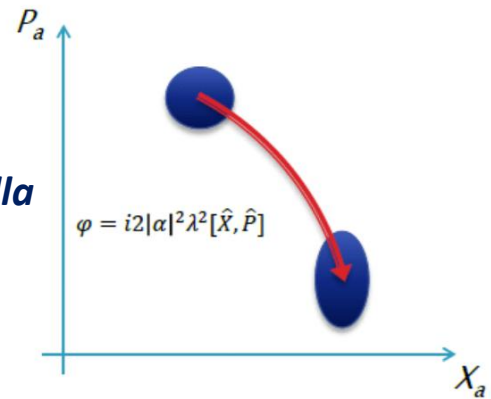


Experimental test with 20 orders of magnitude improvement over state of the art bounds seems feasible

mechanics

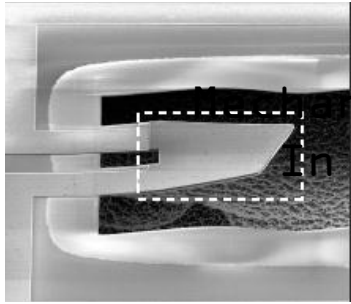
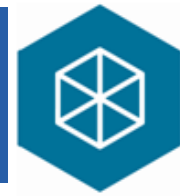


Optical ancilla

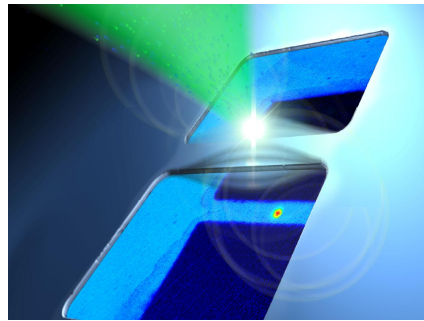


Without ancilla: see e.g. ion

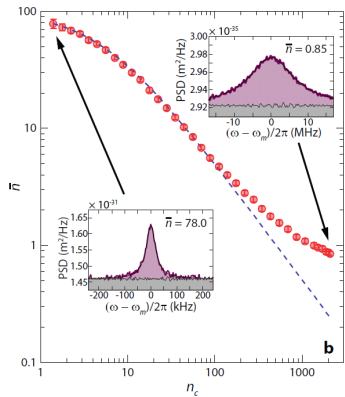
Summary



Mechanical Oscillators can serve as tailored quantum devices in a completely new parameter regime in mass and size

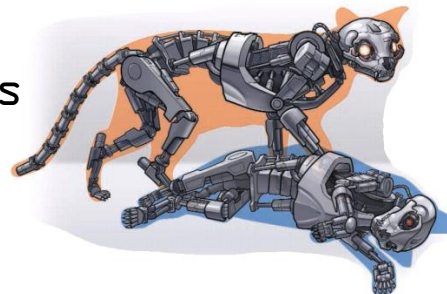


Light allows control of mechanical resonators at the quantum level. This requires careful design of optics and mechanics



Experiments already demonstrate cooling into the quantum ground state

Studies of (de)coherence and tests of alternative quantum theory with extremely massive systems can be



General Overview Articles on OM

- Kippenberg et al., Science 321, 1172 (2008).
- Favero, Nat. Photonics 3, 201 (2009).
- Marquardt, Phys. 2, 40 (2009).

Quantum-“Mechanics“ in Vienna: The Mirror Team 2012

Low-noise coatings & microfab

Garrett Cole
N.N. (cleanroom tech)

Towards testing quantum gravity & pulsed state preparation (with C. Brukner, M. Kim)

Michael Vanner
Joachim Hofer
Garrett Cole
Igor Pikovski
Philipp Köhler

Rainer Kaltenbaek
(APART / Marie Curie)

Quantum foundations and levitated resonators (with M. Arndt, R. Chiao)

Nikolai Kiesel
Rainer Kaltenbaek
Steve Minter
Florian Blaser
Uros Delic
David Grass
Nils Prigge

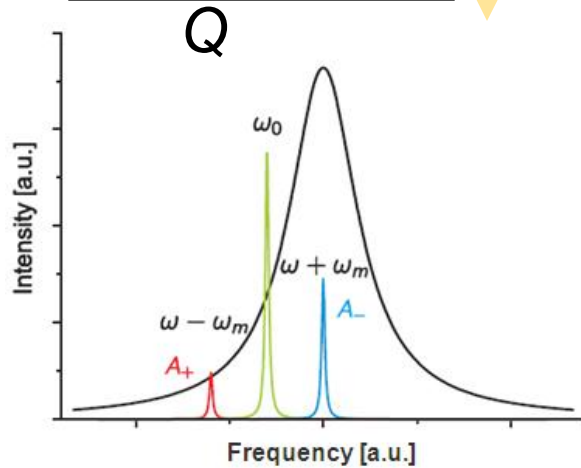
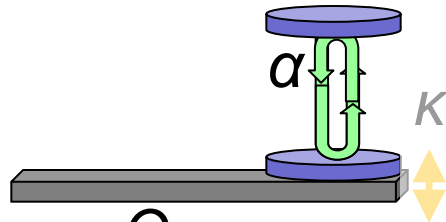
Quantum information interfaces (with K. Hammerer, P. Rabl, J. Eisert, O. Painter)

Witlef Wieczorek
Simon Gröblacher
Jason Hölscher-Obermayer
Jonas Schmöle
Sebastian Hofer
Jonas Hörschel

Hofer,
ver,
S,

Mechanical laser cooling by radiation pressure

Karrai (LMU) 2004: first proof-of-concept via photothermal forces
Nature 432, 1002 (2004)



Cooling rate $\Gamma = A_- - A_+ \approx \frac{(g_0\alpha)^2}{\kappa}$

Thermal coupling / decoherence rate $\Gamma_{thermal} = \frac{k_B T}{\hbar Q}$

Effective mode occupation $\langle n \rangle_{mech} = \frac{\Gamma_{thermal} + A_+}{\Gamma}$

$\langle n \rangle_{mech}^{min} \approx \left(\frac{\kappa}{4\omega_m} \right)^2$

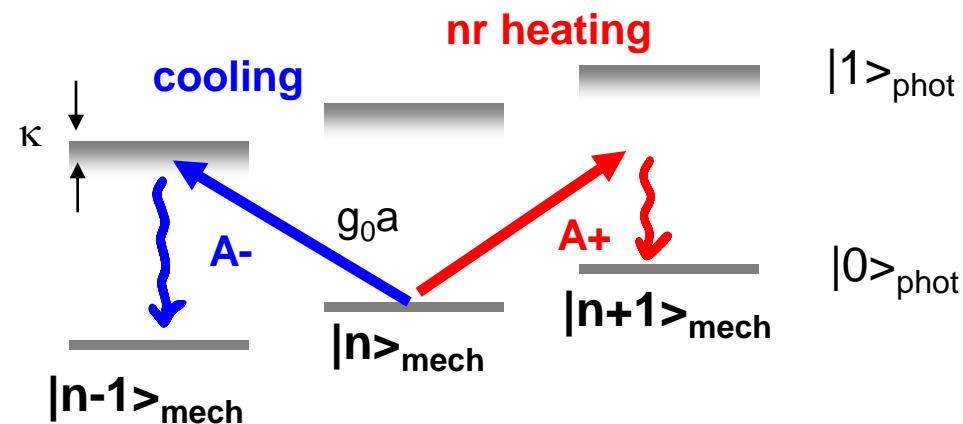
$H_{BS} \propto a_m^\dagger a_c + a_m a_c^\dagger$

Laser-cooling via radiation pressure...

- Vienna (Aspelmeyer): S. Gigan et al., Nature 444, 67 (2006)
- Paris (Heidmann): O. Arcizet et al., Nature 444, 71 (2006)
- Munich (Kippenberg): Schliesser et al, PRL 97, 243905 (2006)
- MIT (Mavalvala): Corbitt et al., PRL 98, 150892 (2007)
- Yale (Harris): Thompson et al., Nature 452, 72 (2008)
- JILA (Lehnert): Regal et al., Nature Physics 4, 555 (2008)

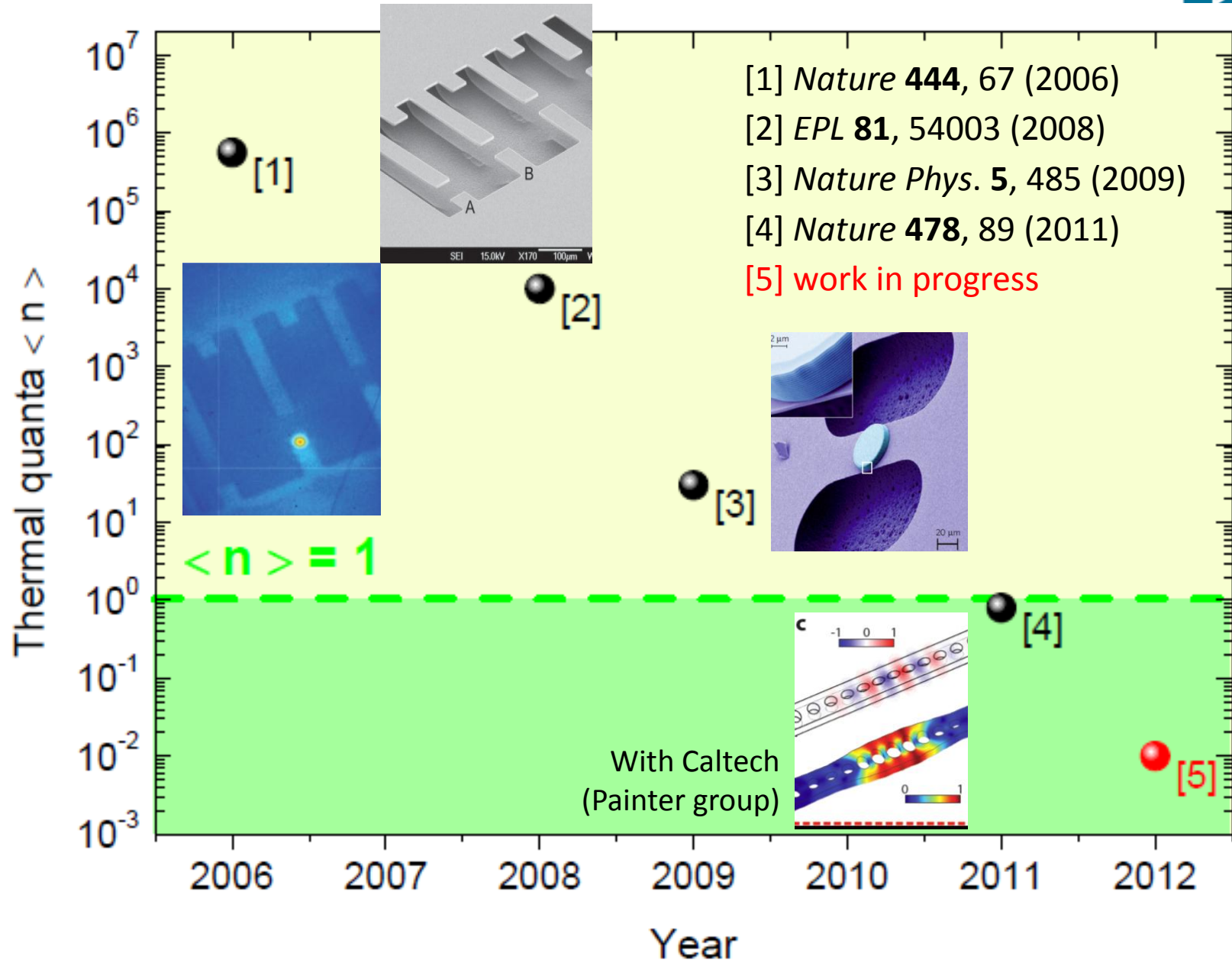
...allows cooling into the quantum ground state

- F. Marquardt et al. PRL 99, 093902 (2007)
- I. Wilson-Rae et al., PRL 99, 093901 (2007)
- C. Genes et al., PRA 77, 033804 (2008)

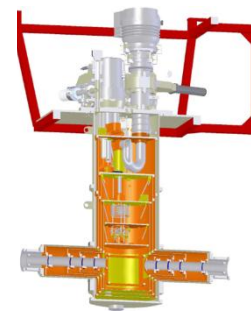


Analogue: sideband-resolved cooling of ions

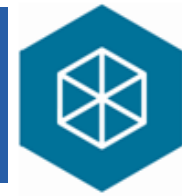
Vienna cooling...



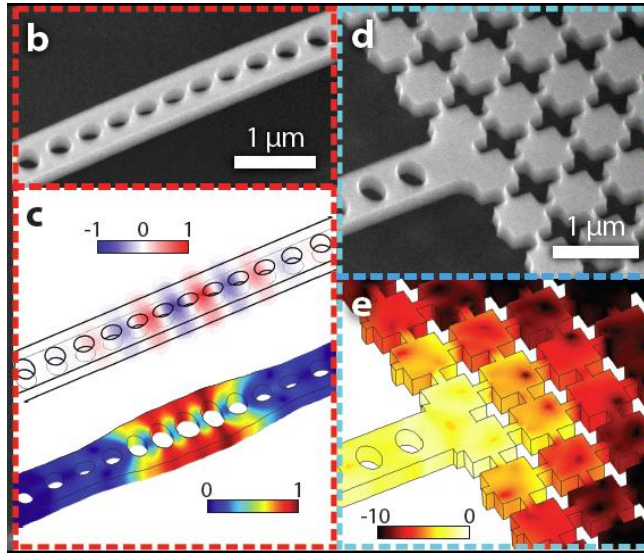
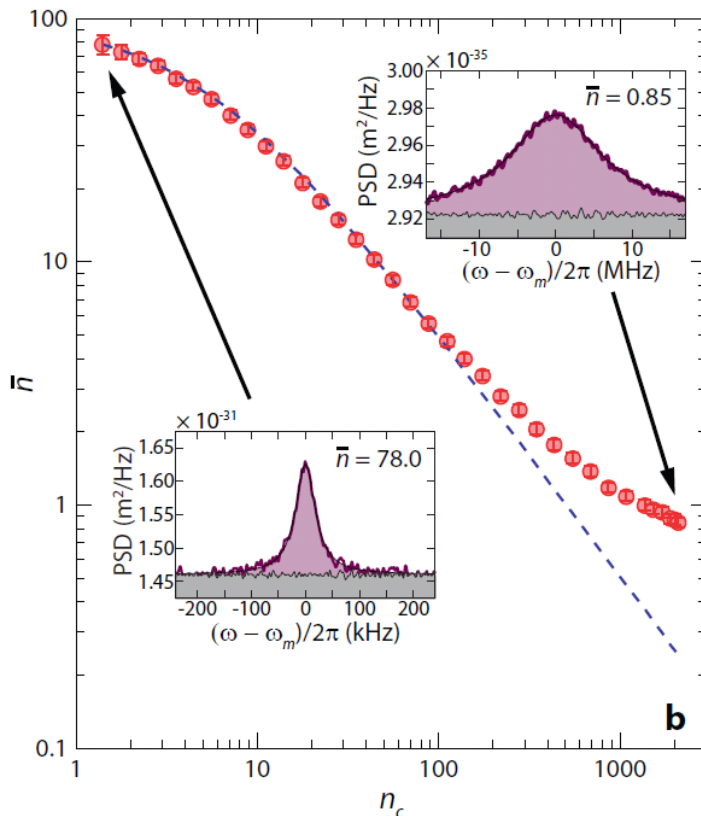
- [1] *Nature* **444**, 67 (2006)
- [2] *EPL* **81**, 54003 (2008)
- [3] *Nature Phys.* **5**, 485 (2009)
- [4] *Nature* **478**, 89 (2011)
- [5] work in progress



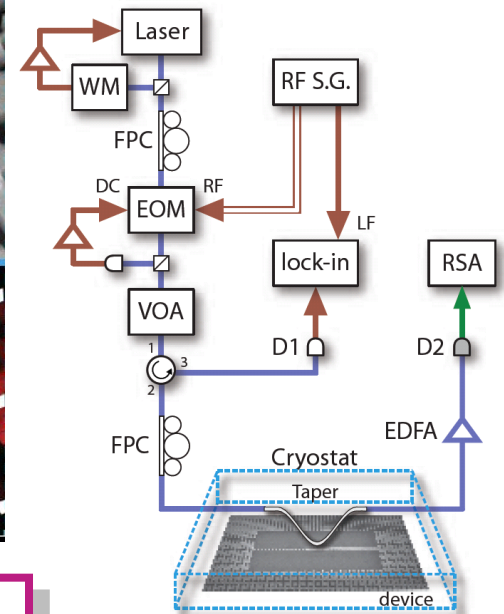
Ground-state laser cooling of a nanomechanical resonator



- **Optomechanical crystal** (photonic & phononic bandgap structure)
- **3.5 GHz mechanical mode** at 20 K ($\langle n \rangle \sim 100$)
- $m \sim \text{O}(\text{pg})$, $N \sim \text{O}(10^{10} \text{ atoms})$
- currently limited by absorption effects



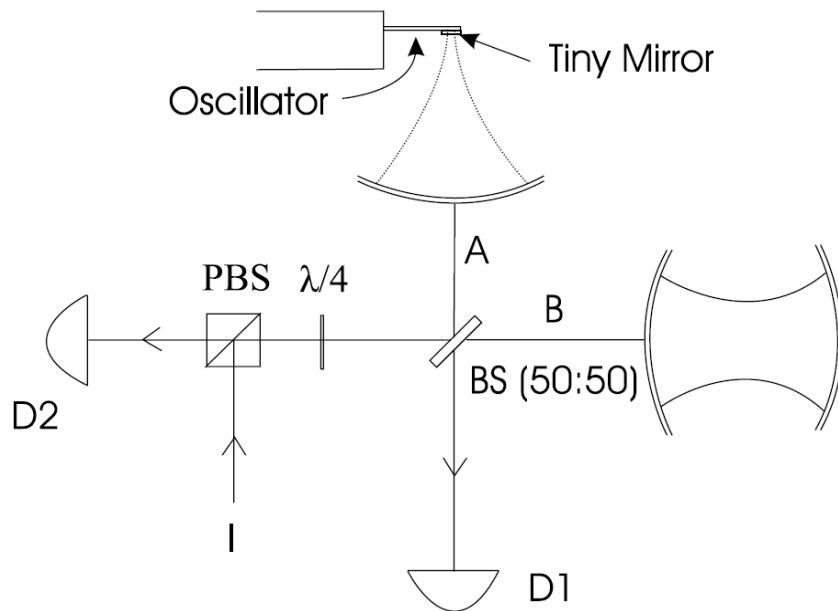
$\langle n \rangle \sim 0.8$
Caltech/Vienna May 2011



A mechanical cat? Schrödinger's mirrors?



Marshall, Simon, Penrose, Bouwmeester,
PRL 91, 130401 (2003)



also: A.D. Armour, M.P. Blencowe, and K. Schwab, PRL
88, 148301 (2002.)

A single photon - 2 paths

1. Path energy exchange with mechanical displacement
2. Path no interaction

Interference and project
Photon: $\frac{1}{2}$ excitation of

Challenging:

Single Photon Coupling
and

Low Frequencies
(for large displacement)

(high mechanical Q/T required)

Towards tests of quantum gravity predictions?

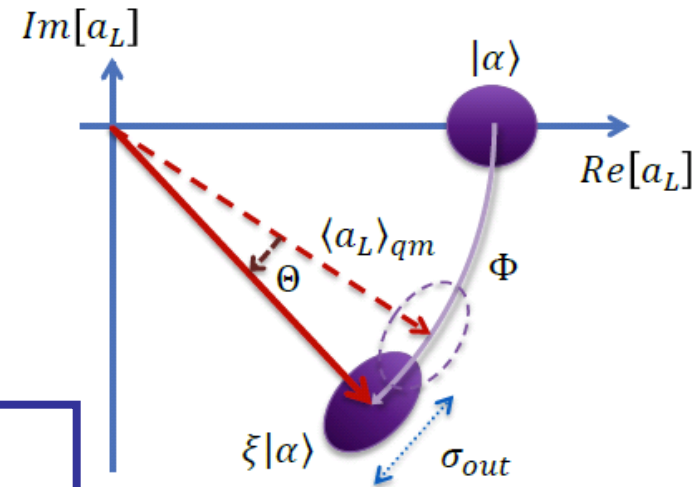


Current state of the art:

system/ experiment	$\beta_{0,max}$	$\gamma_{0,max}$
Position measurements	10^{24}	10^{24}
Lamb shift in Hydrogen	10^{36}	10^{10}
Electron tunneling	10^{33}	10^{11}

Estimates for optomechanics scheme:

$[X_m, P_m]$	Eq. 2	Eq. 3	Eq. 1
$ \Theta $	$\mu_0 \frac{32\hbar\mathcal{F}^2 m N_P}{M_P^2 \lambda_L^2 \omega_m}$	$\gamma_0 \frac{96\hbar^2 \mathcal{F}^3 N_P^2}{M_P c \lambda_L^3 m \omega_m}$	$\beta_0 \frac{1024\hbar^3 \mathcal{F}^4 N_P^3}{3M_P^2 c^2 \lambda_L^4 m \omega_m}$
\mathcal{F}	10^5	2×10^5	5×10^5
m	10^{-11} kg	10^{-11} kg	10^{-6} kg
$\omega_m/2\pi$	10^5 Hz	10^5 Hz	10^5 Hz
λ_L	1064 nm	1064 nm	532 nm
N_P	10^8	5×10^{10}	10^{14}
N_r	1	10^2	10^4
$\delta\langle\Phi\rangle$	10^{-4}	5×10^{-7}	10^{-8}



$$\langle a_L \rangle \simeq \langle a_L \rangle_{qm} e^{-i\Theta}$$

→ Improvement by more than 20 orders of magnitude compared to existing bounds !